

Probing and Controlling Ultracold Quantum Matter under Extreme Conditions

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Ludwig-Maximilians Universität***

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€ MPG, European Union, DFG
\$ DARPA (OLE)



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Outline

Introduction

Single Atom Imaging

Three Applications

SF-Mott Insulator Transition/Thermometry/
Quantum Fluctuations

Controlling Single Spins

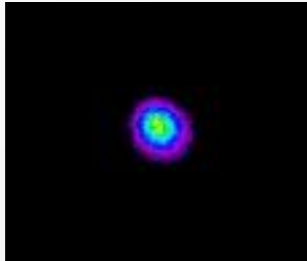
'Higgs'-Amplitude Mode in 2D

Artificial Gauge Fields - Extreme Magnetic Fields

Quantum Matter at Negative Absolute Temperature

Outlook

Control of single particles



Single Atoms and Ions



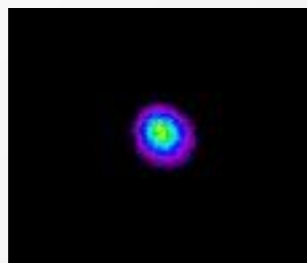
Photons



D. Wineland

S. Haroche

Control of single particles



Single Atoms and Ions



Photons



D. Wineland

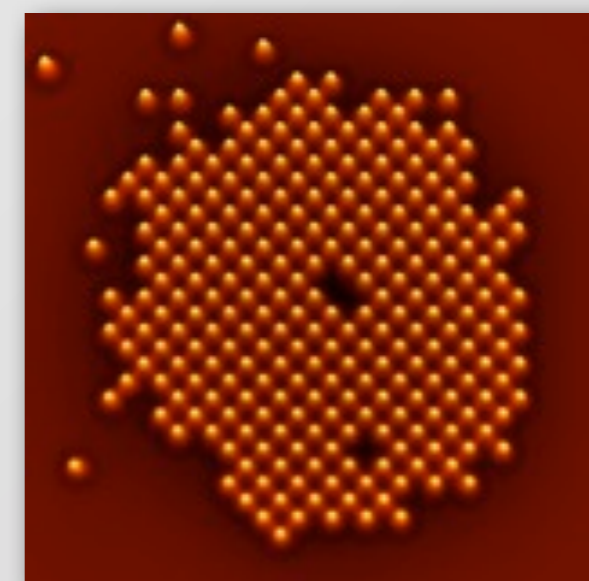
S. Haroche

Challenge: ... towards ultimate control of many-body quantum systems



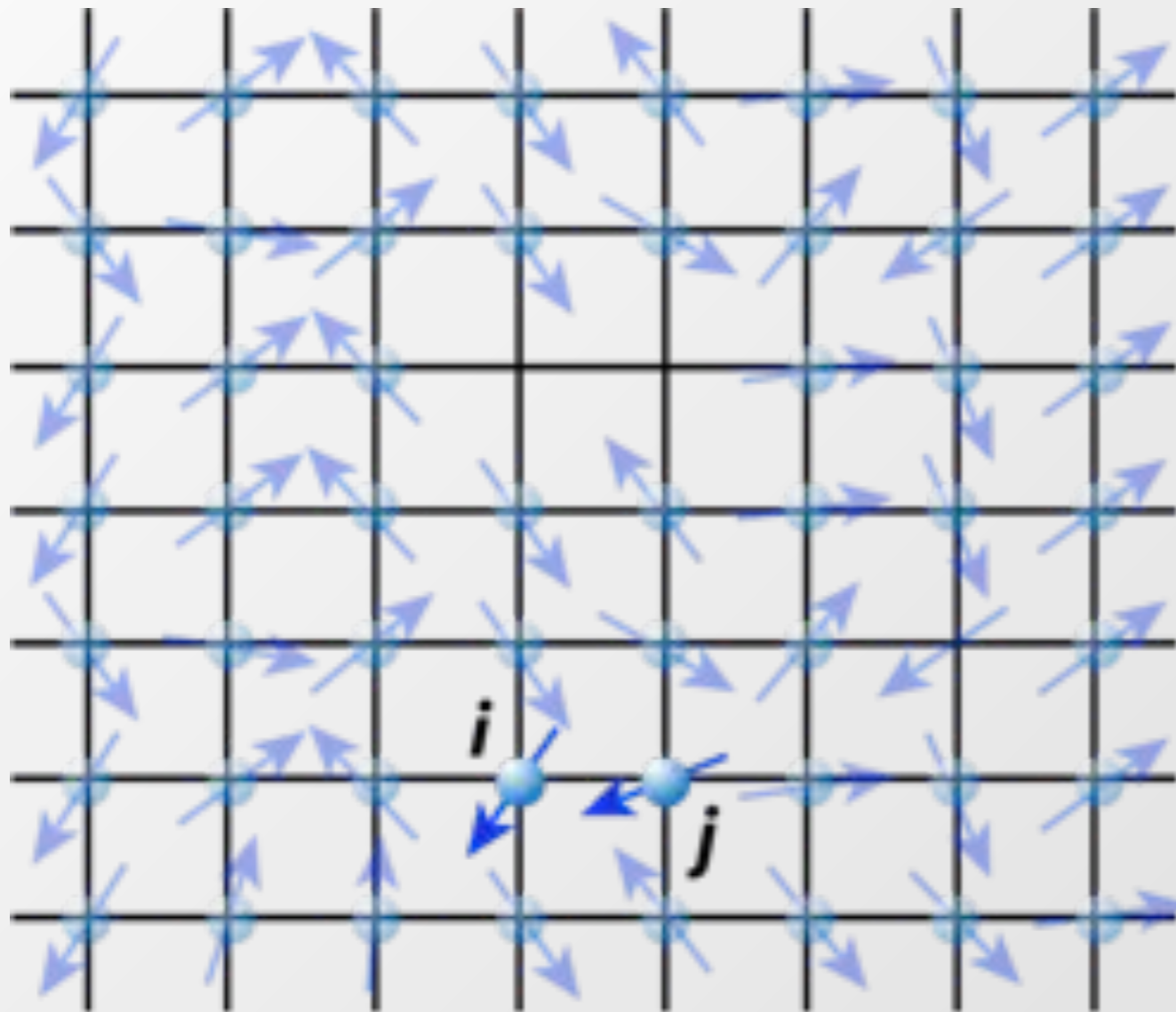
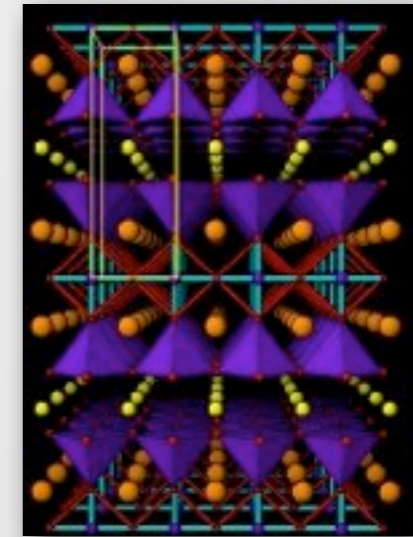
R. P. Feynman's Vision

A *Quantum Simulator* to study the dynamics of another quantum system.



Crystal of Atoms Bound by Light

$$H = -J \sum_{\langle i,j \rangle, \sigma} \hat{c}_{i,\sigma}^\dagger \hat{c}_{j,\sigma} + U \sum_i \hat{n}_{i,\uparrow} \hat{n}_{i,\downarrow} + V_0 \sum_{i,\sigma} R_i^2 \hat{n}_{i,\sigma}$$



In strongly correlated electron system **spin-spin interactions** exist.

$$-J_{ex} \vec{S}_i \cdot \vec{S}_j$$

Underlying many solid state & material science problems:
Magnets, High-Tc Superconductors, Spintronics



Parameters:Densities: 10^{15} cm^{-3}

Temperatures: Nano Kelvin

Atom Numbers 10^6 Ground States at $T=0$ 

**Bose-Einstein
Condensates e.g. ^{87}Rb**



**Degenerate Fermi Gases
e.g. ^{40}K**

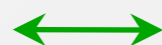
*Centennial Nobel Prize in Physics for BEC
E. Cornell, C. Wieman & W. Ketterle*



Laser



Laser



$$\lambda/2 = 425 \text{ nm}$$

optical standing wave

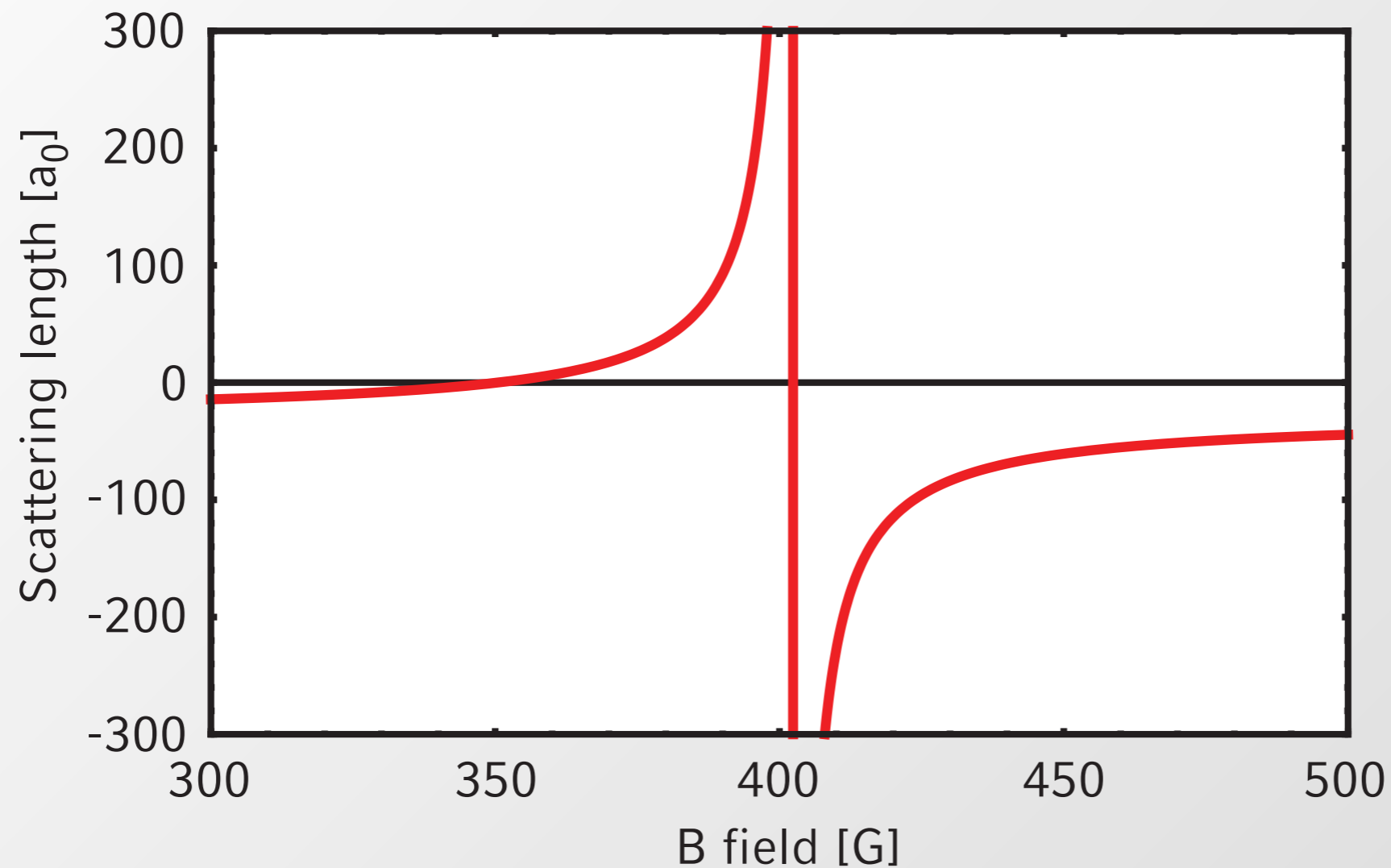


*Perfect model systems for a
fundamental understanding of
quantum many-body systems*

Periodic intensity pattern creates 1D, 2D or 3D light crystals for atoms (Here shown for small polystyrol particles).



^{39}K - ^{39}K Feshbach resonance

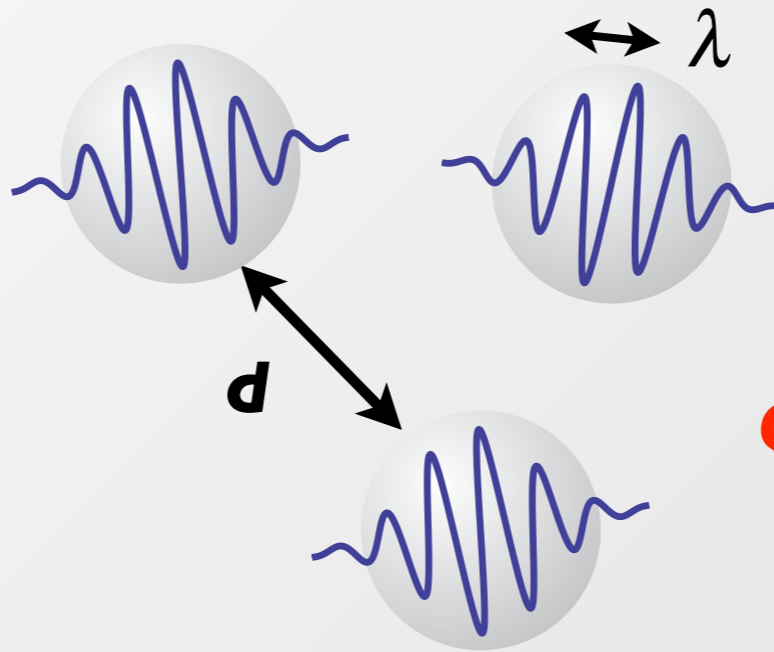


Feshbach resonance allow us to control interactions!



Quantum Regime

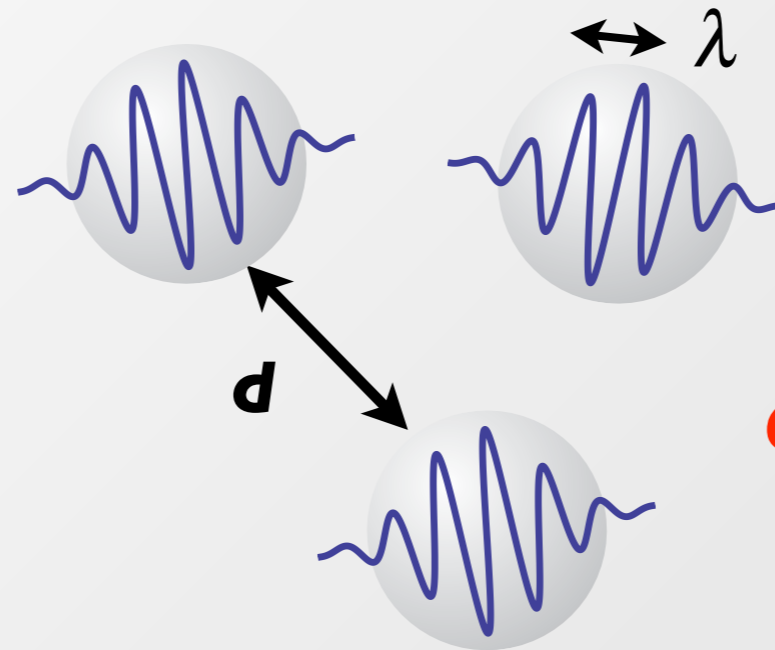
$$\lambda/d \gtrsim 1$$



de Broglie Wavepackets

**Universality of
Quantum Mechanics!**

Quantum Regime
 $\lambda/d \gtrsim 1$

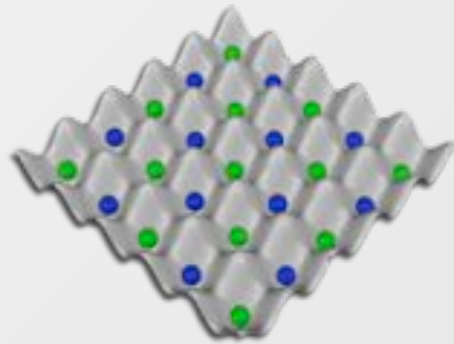


de Broglie Wavepackets

Universality of Quantum Mechanics!

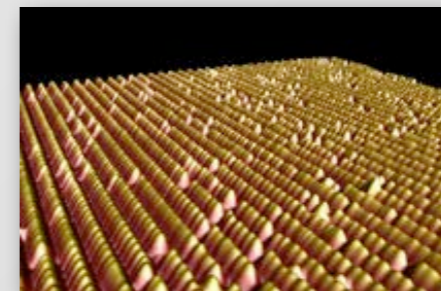
Ultracold Quantum Matter

- **Densities:** $10^{14}/\text{cm}^3$
 (100000 times thinner than air)
- **Temperatures:** **few nK**
 (100 million times lower than outer space)



Real Materials

- **Densities:** $10^{24}-10^{25}/\text{cm}^3$
- **Temperatures:** **mK – several hundred K**



(Neuchatel)

Same λ/d !

Expanding the field operator in the **Wannier basis** of localized wave functions on each lattice site, yields :

$$\hat{\psi}(\mathbf{x}) = \sum_i \hat{a}_i w(\mathbf{x} - \mathbf{x}_i)$$

Bose-Hubbard Hamiltonian

$$H = -J \sum_{\langle i,j \rangle} \hat{a}_i^\dagger \hat{a}_j + \sum_i \varepsilon_i \hat{n}_i + \frac{1}{2} U \sum_i \hat{n}_i (\hat{n}_i - 1)$$

Tunnelmatrix element/Hopping element

$$J = -\int d^3x w(\mathbf{x} - \mathbf{x}_i) \left(-\frac{\hbar^2}{2m} \nabla^2 + V_{lat}(\mathbf{x}) \right) w(\mathbf{x} - \mathbf{x}_j)$$

Onsite interaction matrix element

$$U = \frac{4\pi \hbar^2 a}{m} \int d^3x |w(\mathbf{x})|^4$$

M.P.A. Fisher et al., PRB 40, 546 (1989); D. Jaksch et al., PRL 81, 3108 (1998)

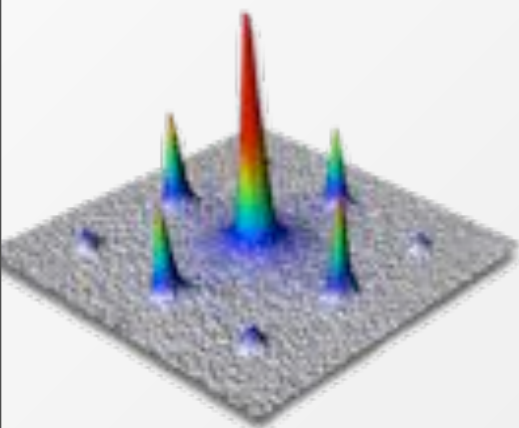
Mott Insulators now at: Munich, Mainz, NIST, ETHZ, Texas, Innsbruck, MIT, Chicago, Florence, ...
see also work on JJ arrays H. Mooij et al., E. Cornell, ...



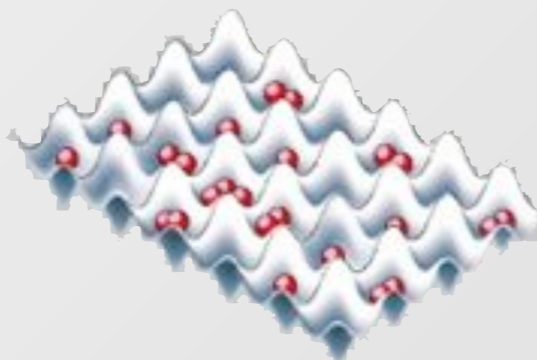
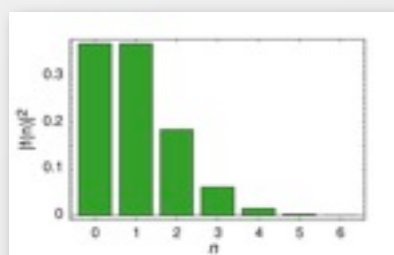
$$\gamma = \frac{\text{Interaction Energy}}{\text{Kinetic Energy}} \gg 1$$




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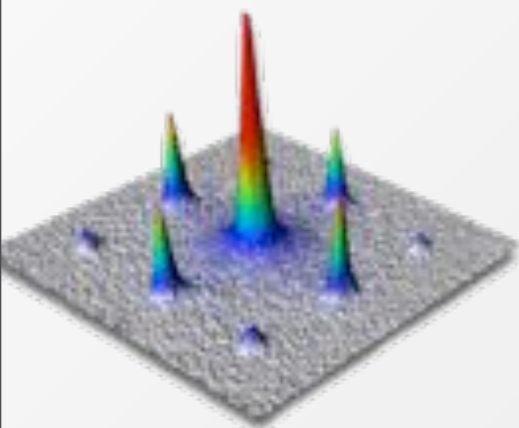



Weak Interactions

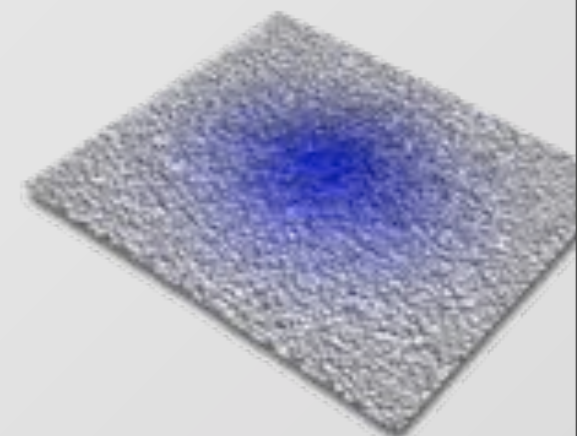


$$\gamma = \frac{\text{Interaction Energy}}{\text{Kinetic Energy}} \gg 1$$

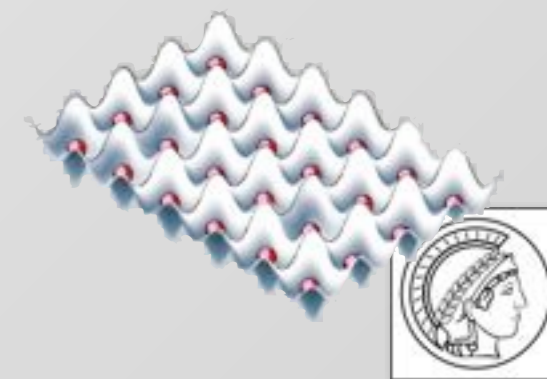
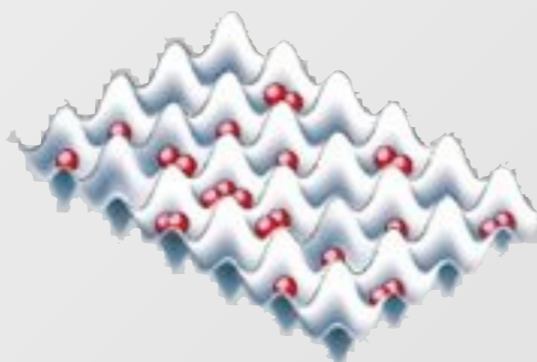
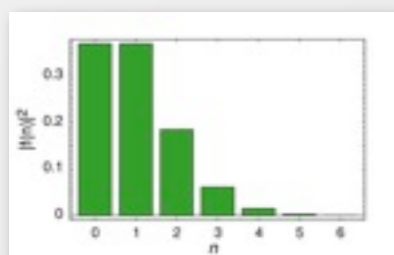




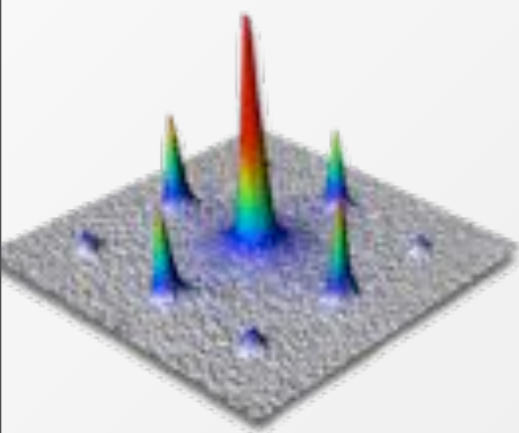
Weak Interactions



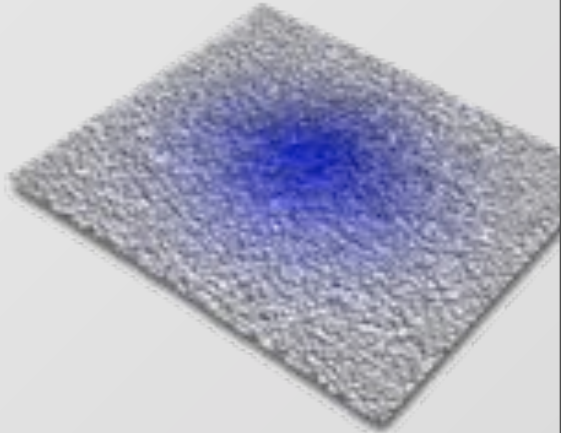
Strong Interactions



$$\gamma = \frac{\text{Interaction Energy}}{\text{Kinetic Energy}} \gg 1$$

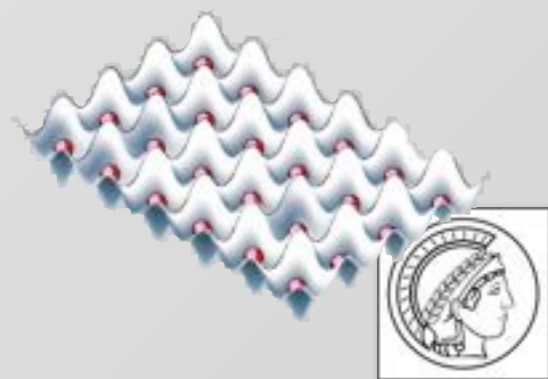
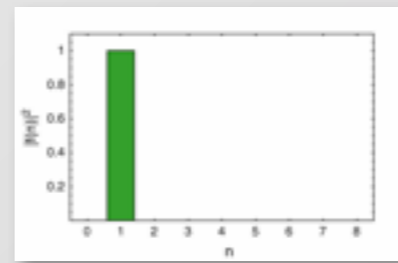
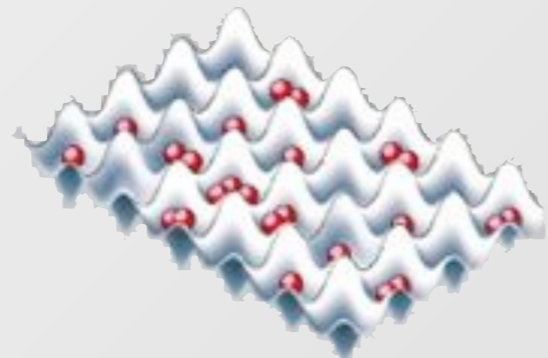


Weak Interactions

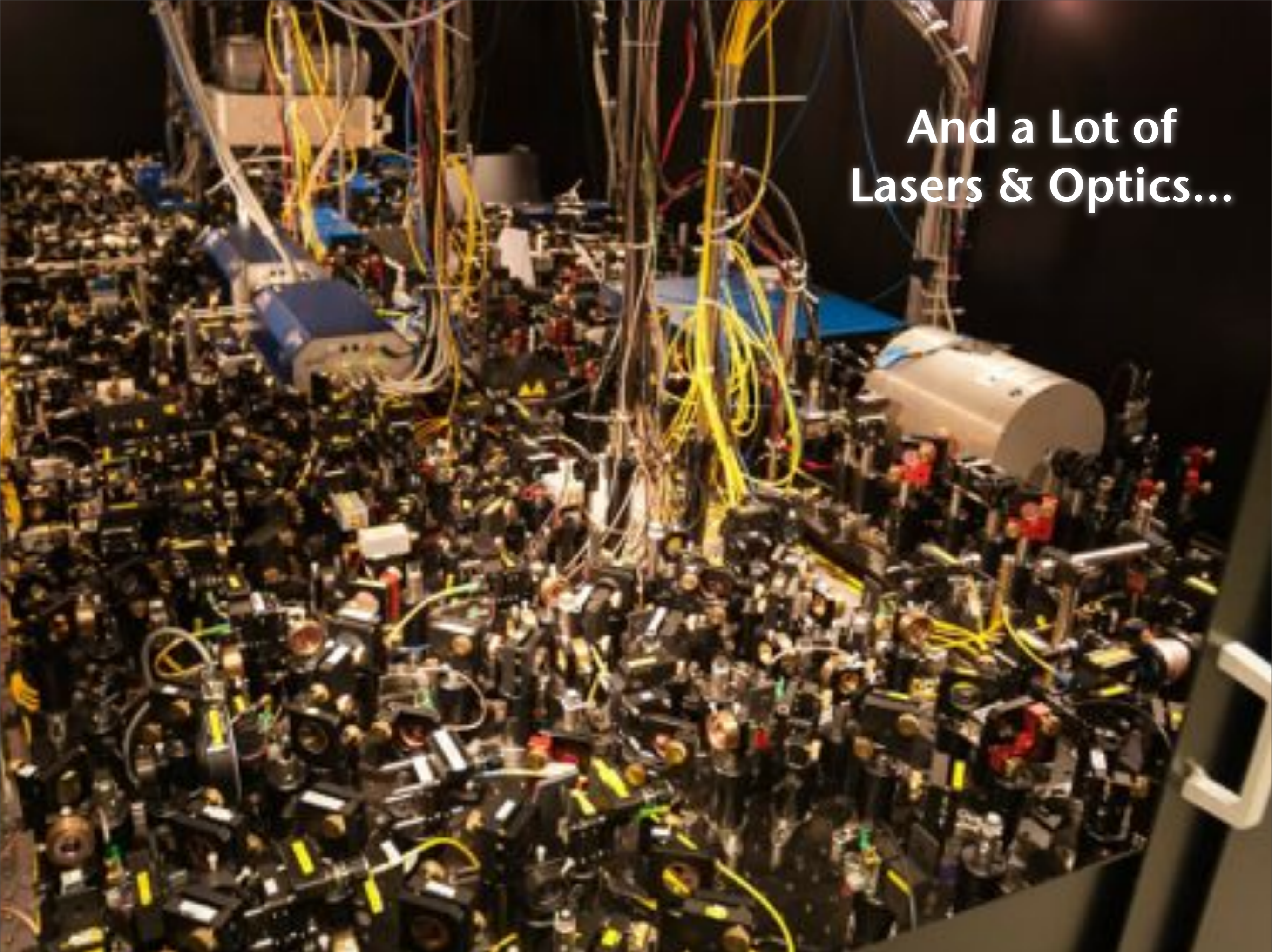


Strong Interactions

Quantum Phase Transition
See S. Sachdev & B. Keimer Phys. Today 2011



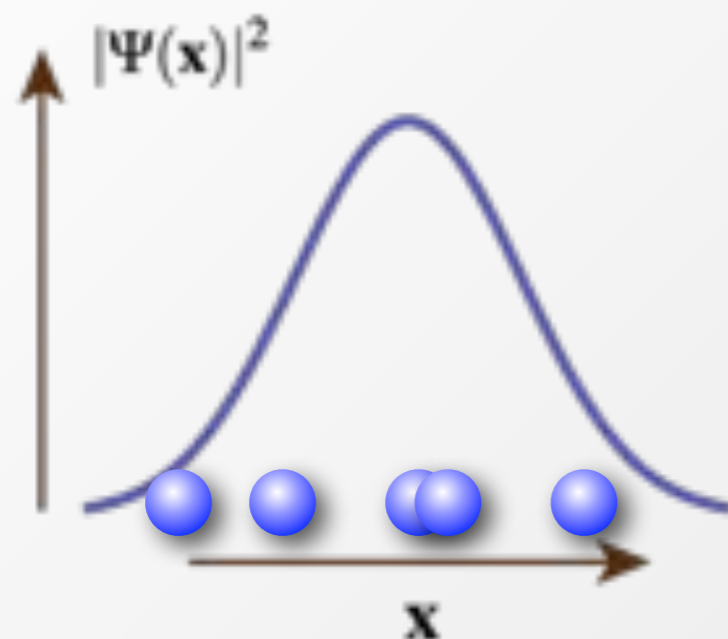
**And a Lot of
Lasers & Optics...**



Single Atom Detection in a Lattice

Sherson et al. Nature 467, 68 (2010),
see also Bakr et al. Nature (2009) & Bakr et al. Science (2010)

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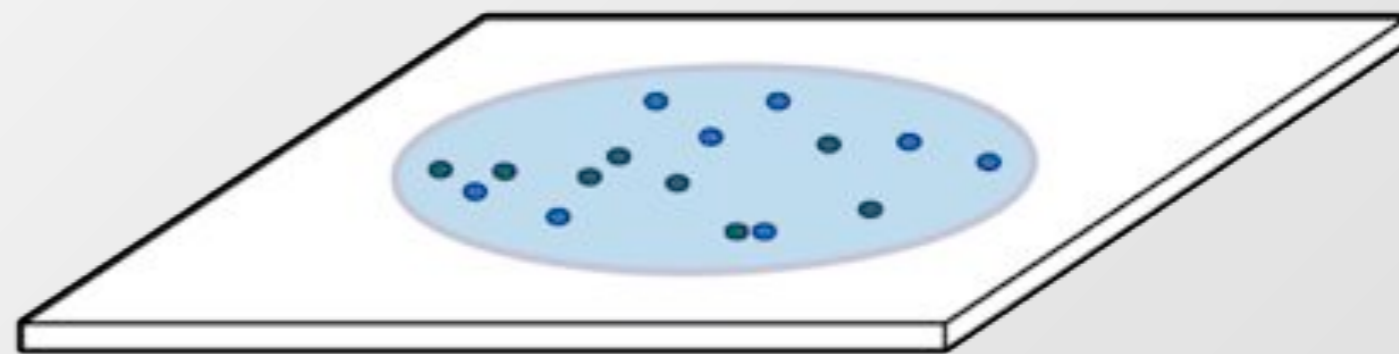


Single Particle

$\Psi(\mathbf{x})$ wave function

$|\Psi(\mathbf{x})|^2$ probability distribution

averaging over *single-particle measurements*, we obtain $|\Psi(\mathbf{x})|^2$



Correlated 2D Quantum Liquid

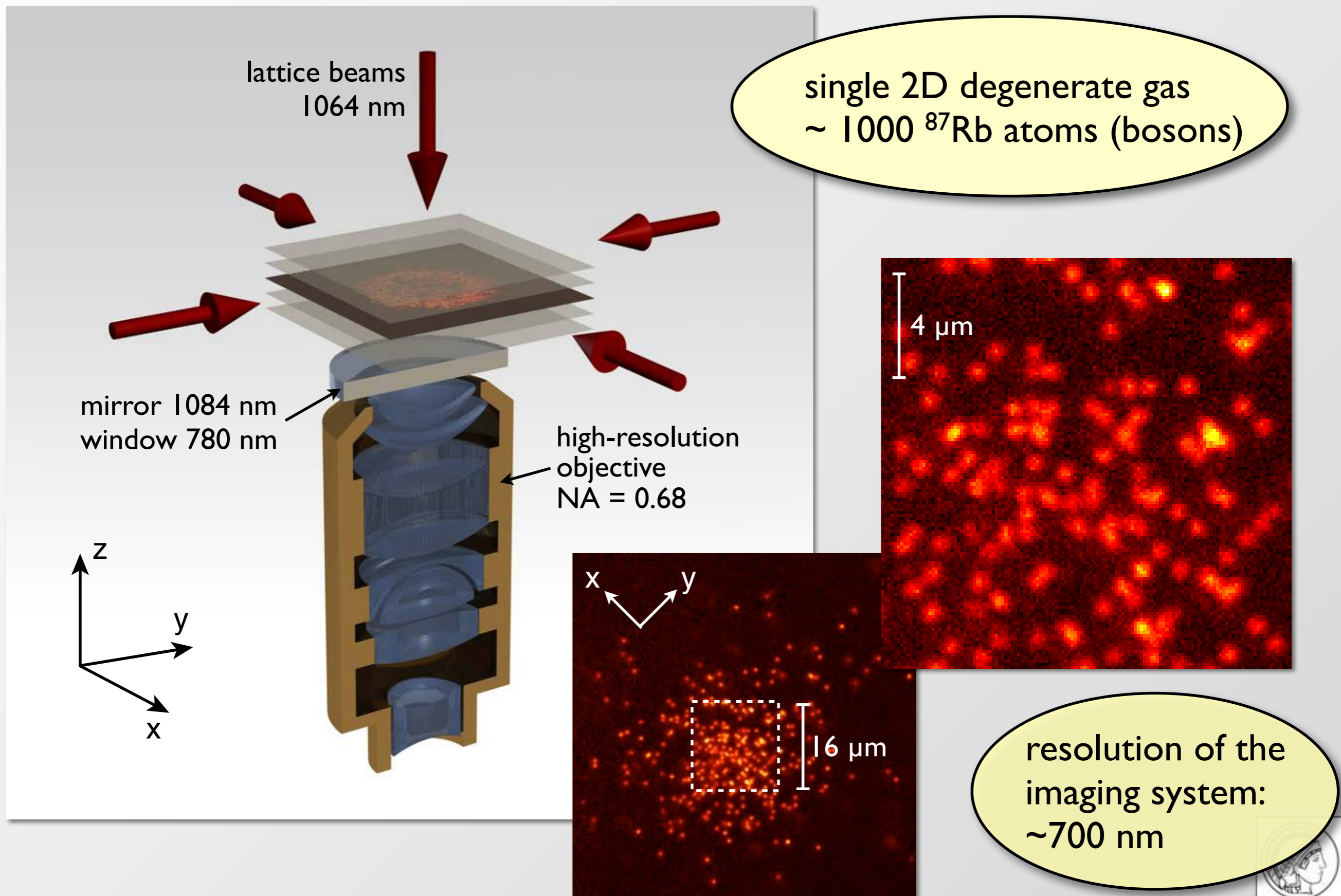
$\Psi(\mathbf{x}_1, \mathbf{x}_2, \mathbf{x}_3, \dots, \mathbf{x}_N)$

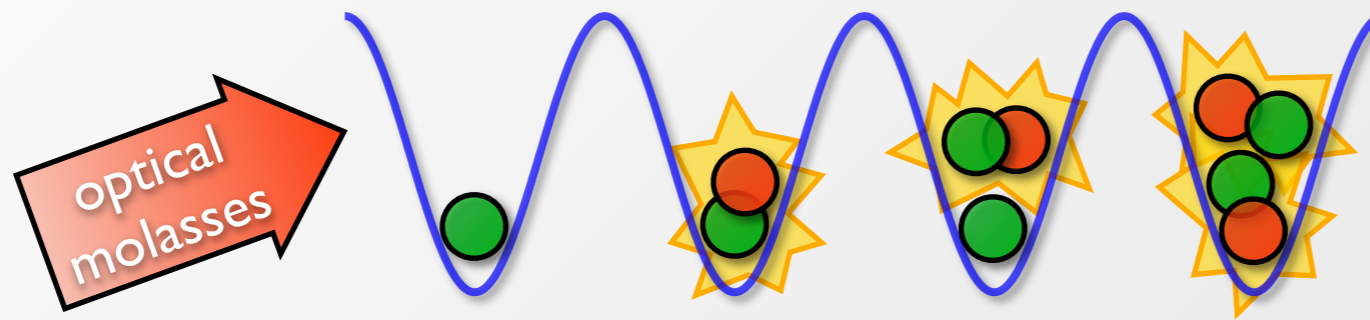
$|\Psi(\mathbf{x}_1, \mathbf{x}_2, \mathbf{x}_3, \dots, \mathbf{x}_N)|^2$

For many-body system: need access to *single snapshots of the many-particle system!*

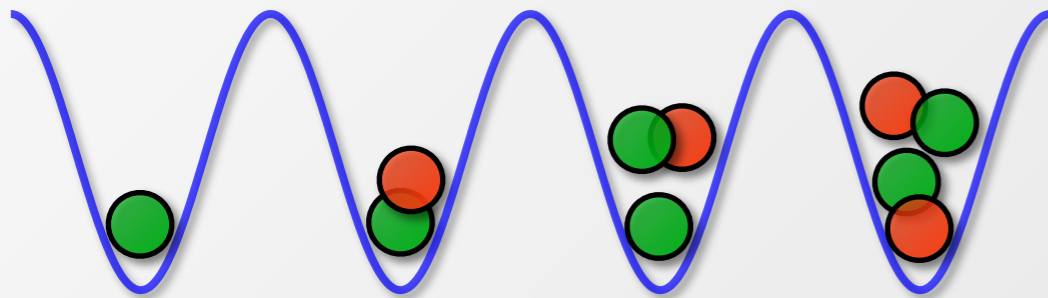
Enables Measurement of
Non-local Correlations



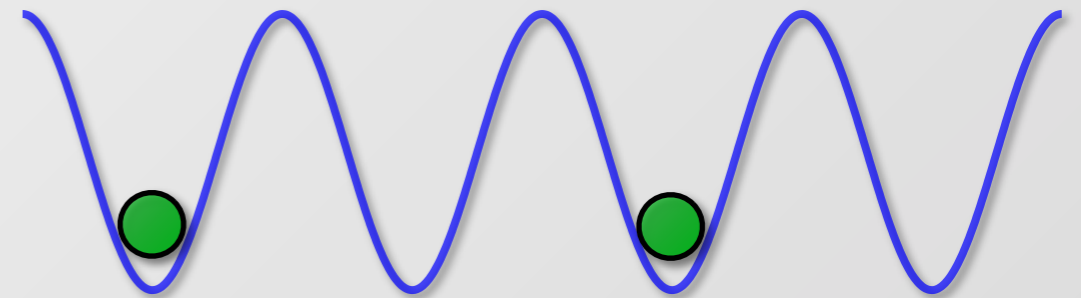


dePue et al., PRL **82**, 2262 (1999)Light-induced
collisions

initial density distribution



measured density distribution

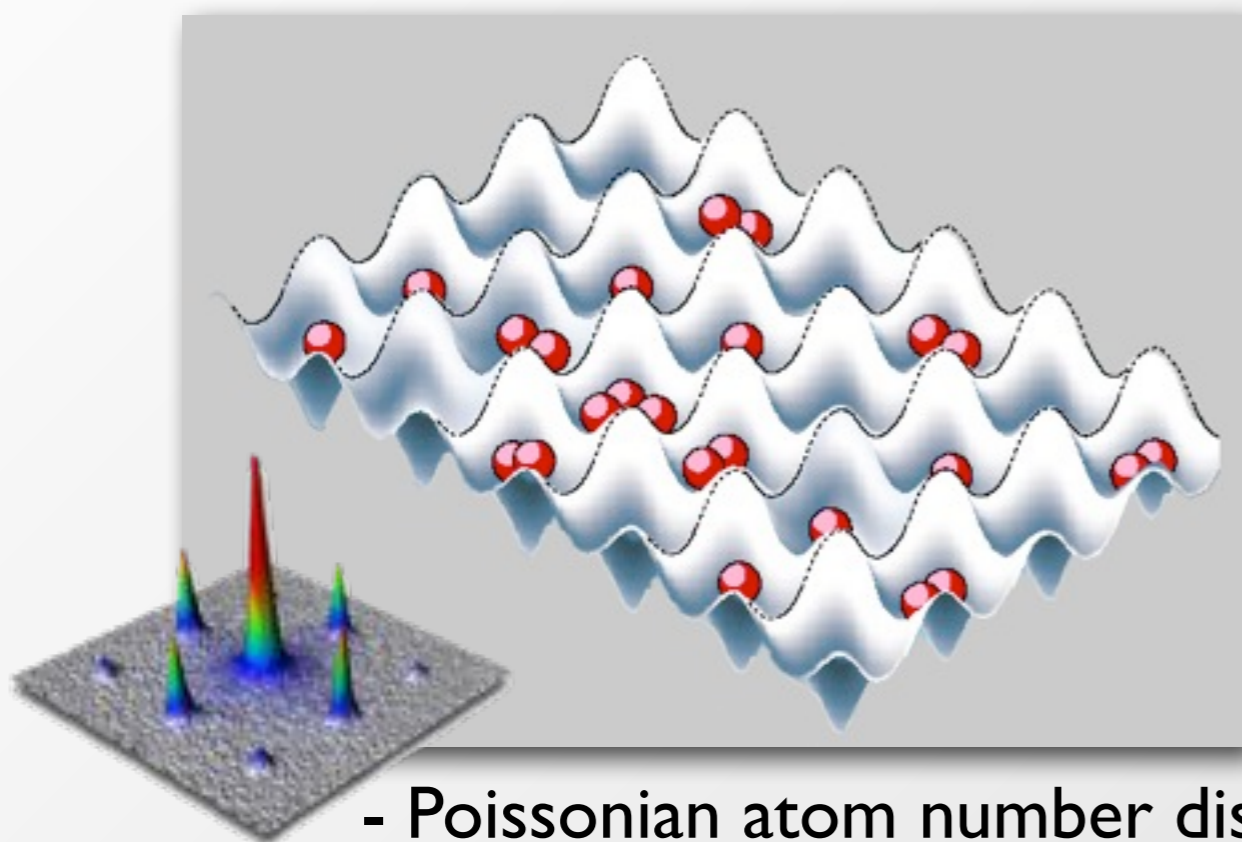
measured occupation: $n_{\text{det}} = \text{mod}_2 n$ measured variance: $\sigma_{\text{det}}^2 = \langle n_{\text{det}}^2 \rangle - \langle n_{\text{det}} \rangle^2$ parity projection $\Rightarrow \langle n_{\text{det}}^2 \rangle = \langle n_{\text{det}} \rangle$ see also E. Kapit & E. Mueller, Phys. Rev. A **82**, 013644 (2010)

In-Situ Imaging of a Mott Insulator

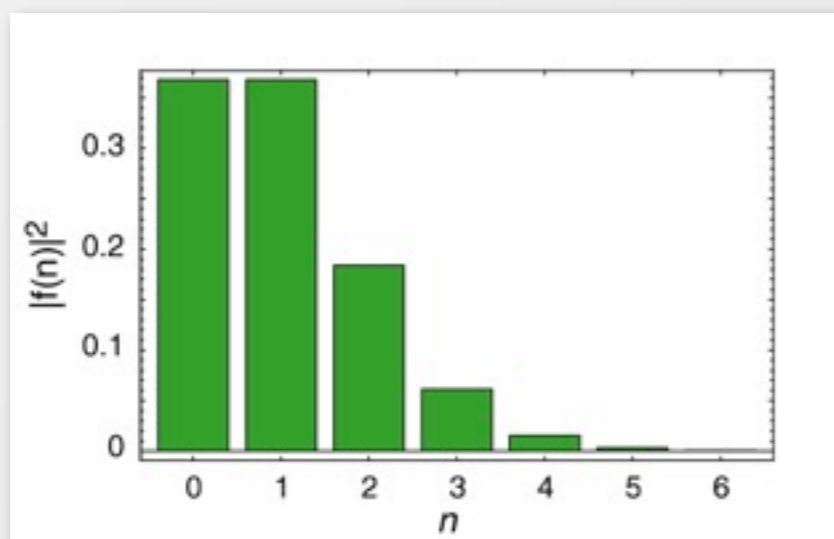
J. Sherson et al. Nature **467**, 68 (2010),
see also S. Fölling et al. Phys. Rev. Lett (2006), G.K. Campbell et al. Science (2006)
N. Gemelke et al. Nature (2009), W. Bakr et al. Science (2010)

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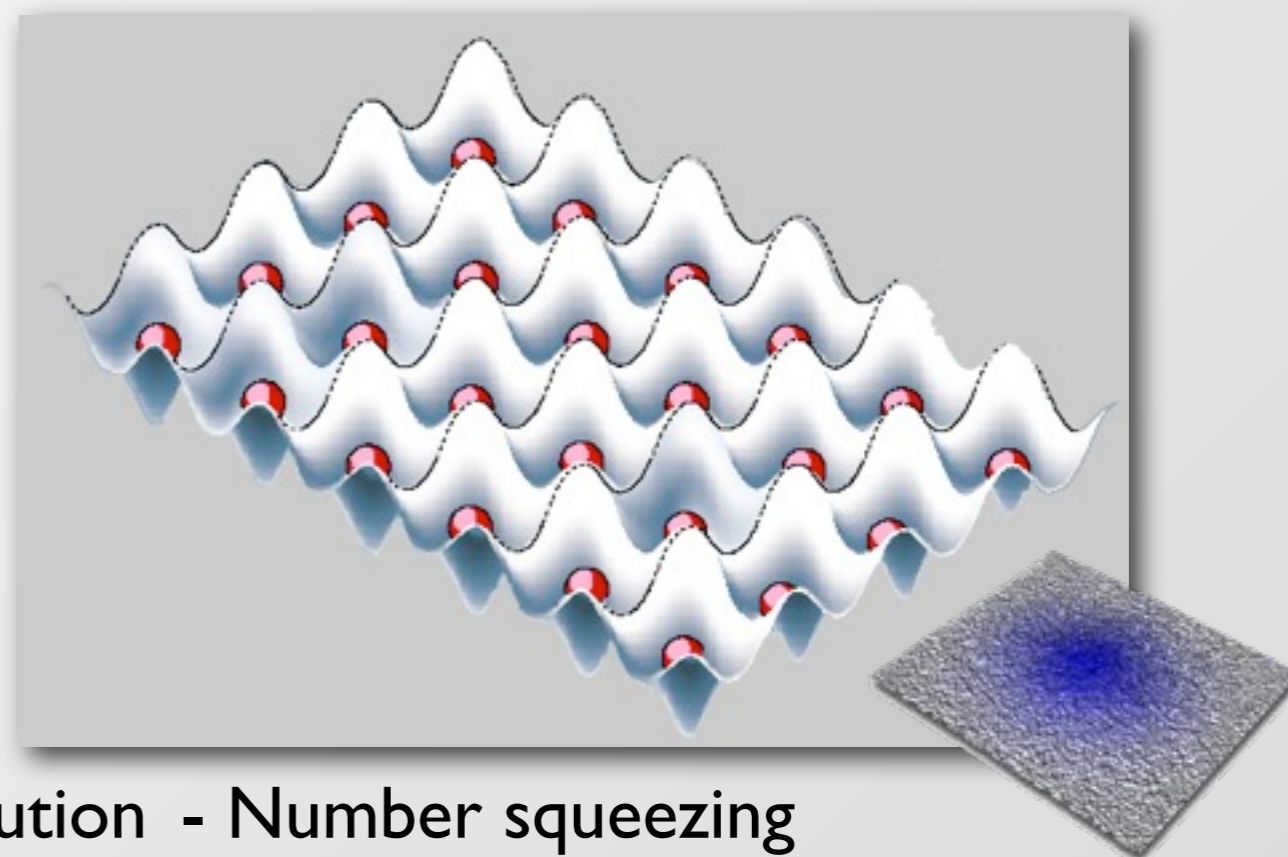
Superfluid



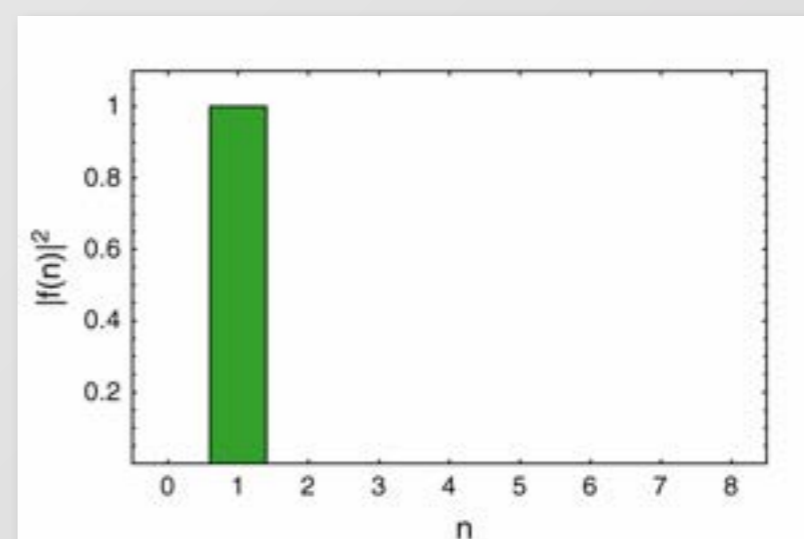
- Poissonian atom number distribution
- Long range phase coherence

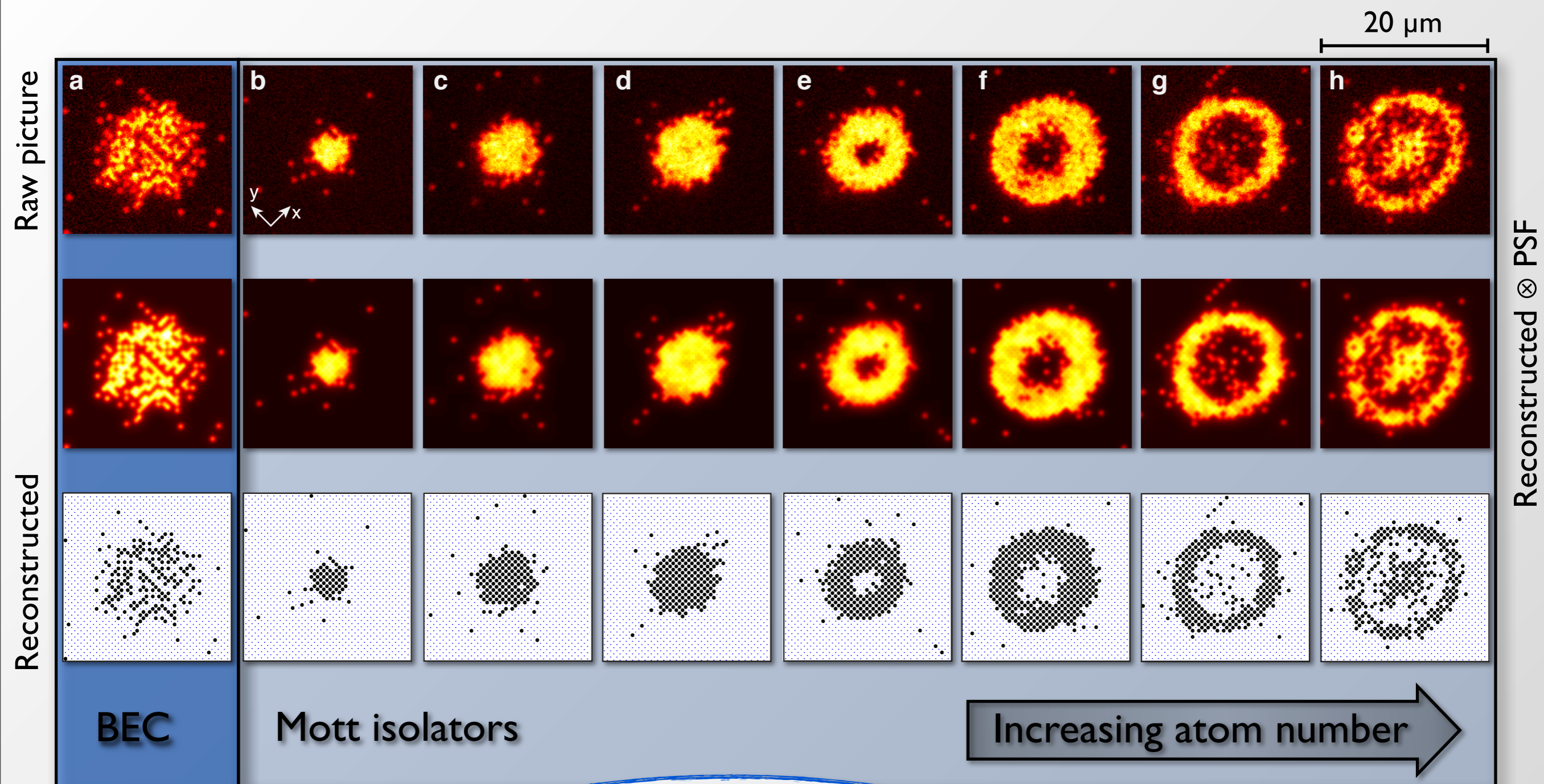


Mott-Insulator



- Number squeezing
- No phase coherence



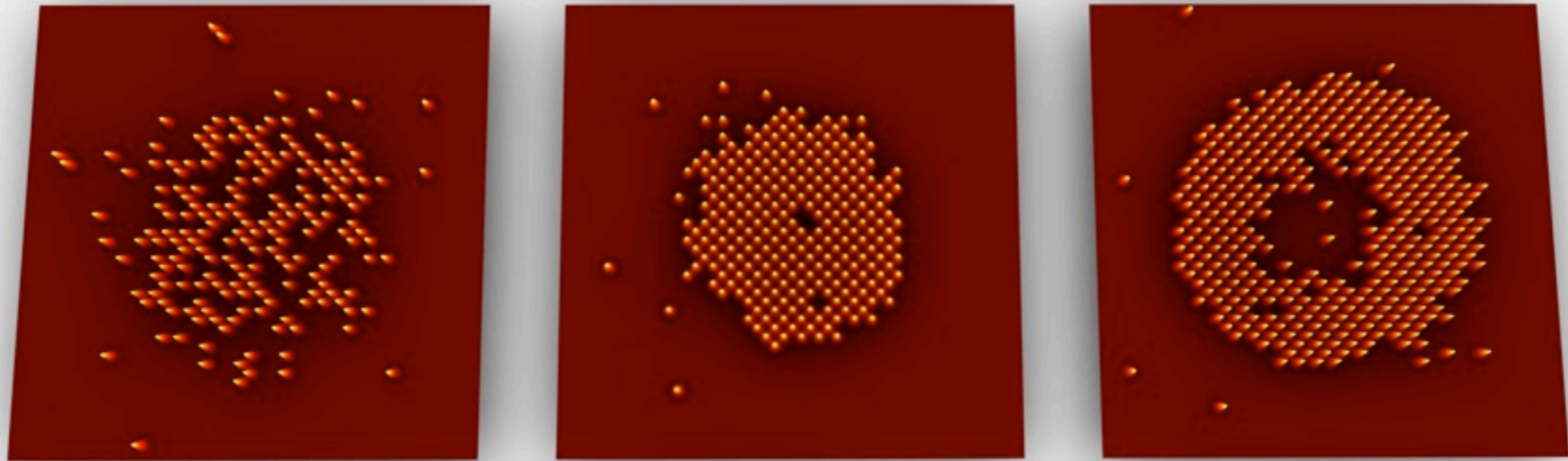


for the Mott insulators: $U/J \sim 300$
 \Rightarrow only thermal fluctuations

(critical $U/J \sim 16$)



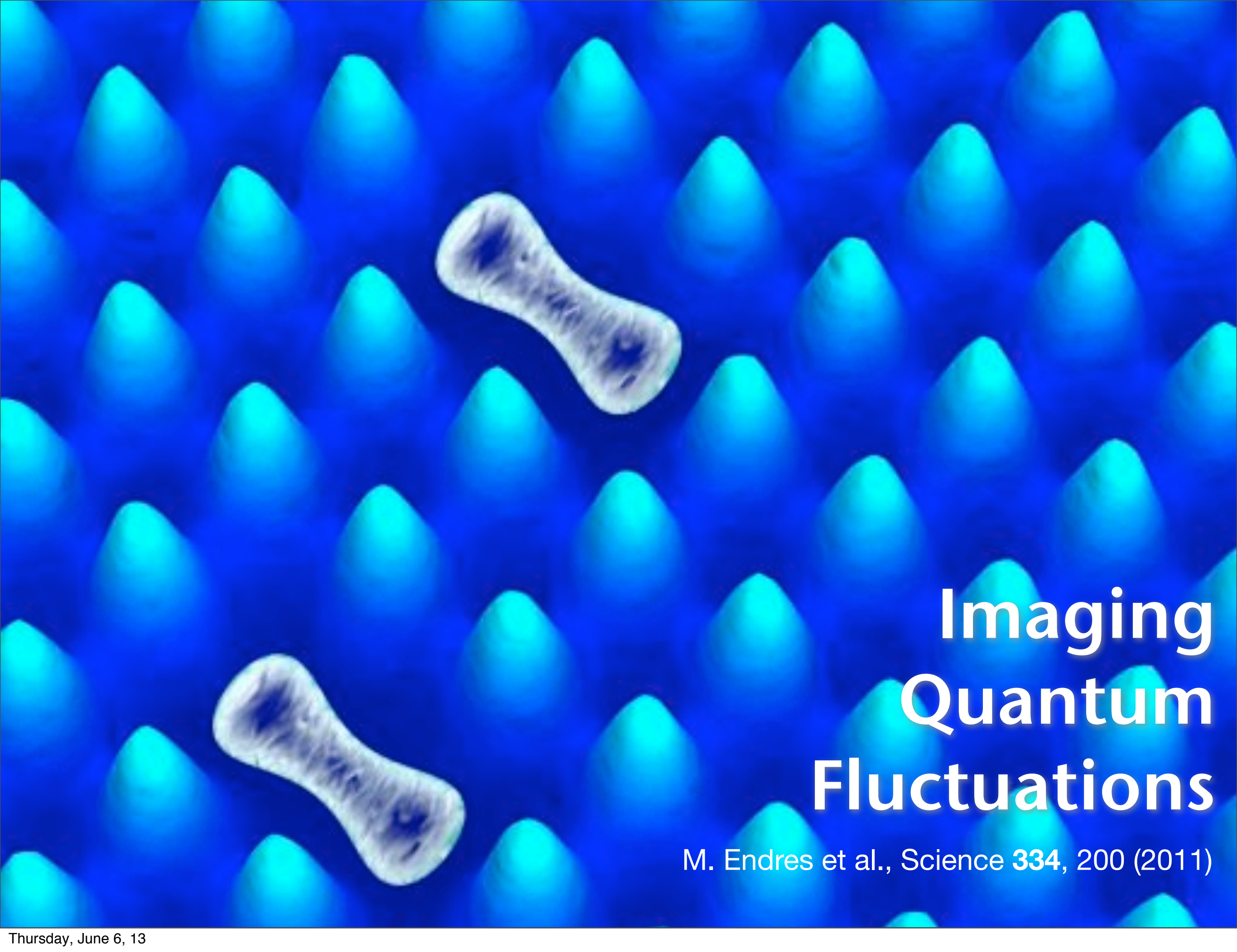
Snapshot of an Atomic Density Distribution



BEC

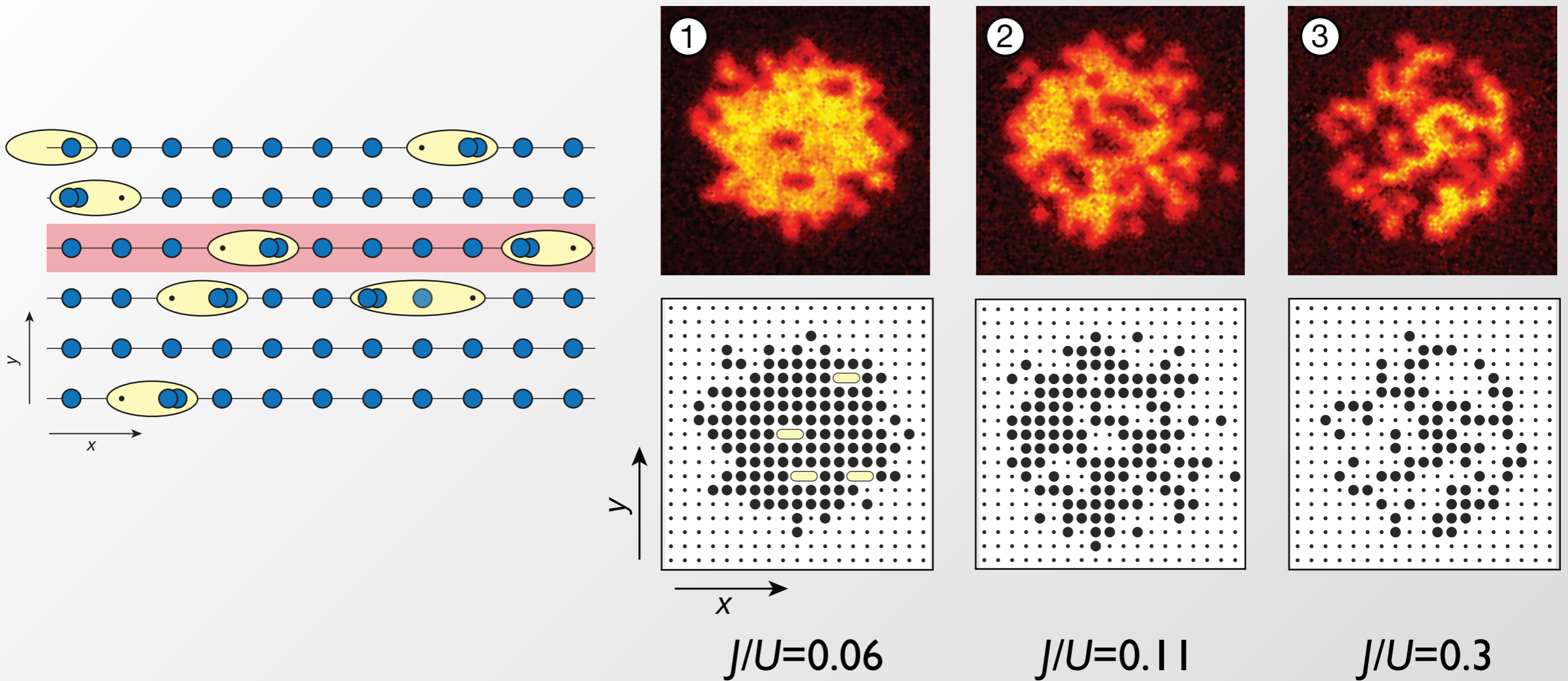
$n=1$
Mott Insulator

$n=1$ & $n=2$
Mott Insulator

The background of the slide is a vibrant blue with a repeating pattern of pointed, scale-like shapes. Two rod-shaped bacteria, likely Bacillus subtilis, are shown in grayscale. They have a characteristic dumbbell shape with a narrower central region and wider, rounded ends. One bacterium is positioned in the upper-middle section, and the other is in the lower-left section.

Imaging Quantum Fluctuations

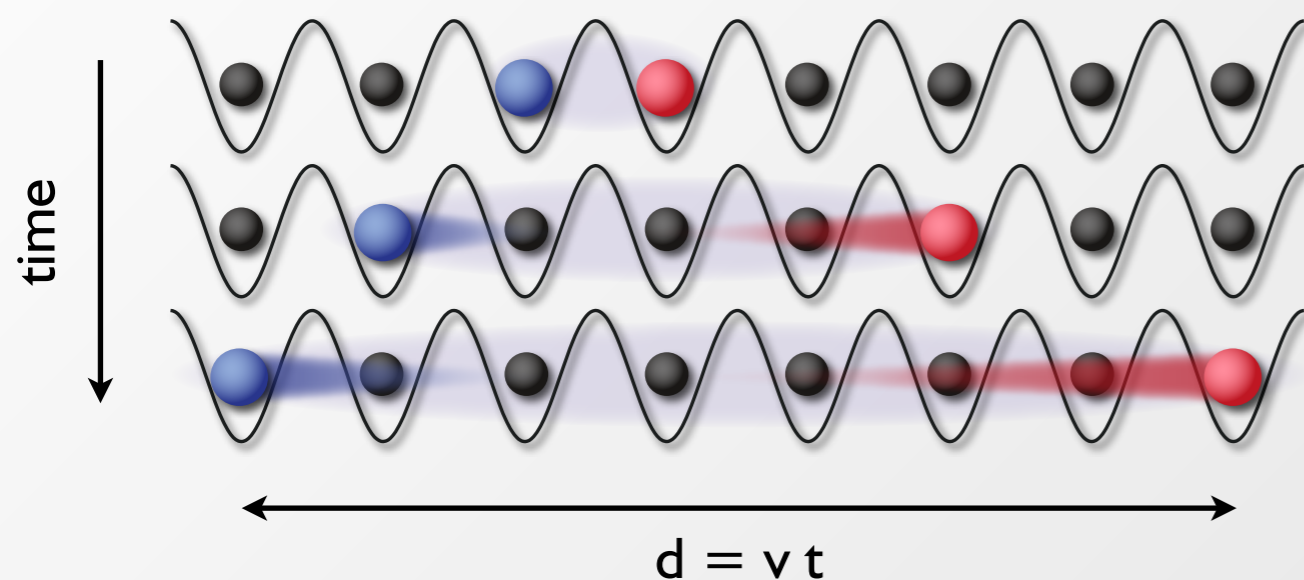
M. Endres et al., Science **334**, 200 (2011)



$$C(d) = \langle \hat{S}_k \hat{S}_{k+d} \rangle - \langle \hat{S}_k \rangle \langle \hat{S}_{k+d} \rangle$$

Two point correlator

- Quasiparticle dynamics



E. Lieb & D.W. Robinson (1972)

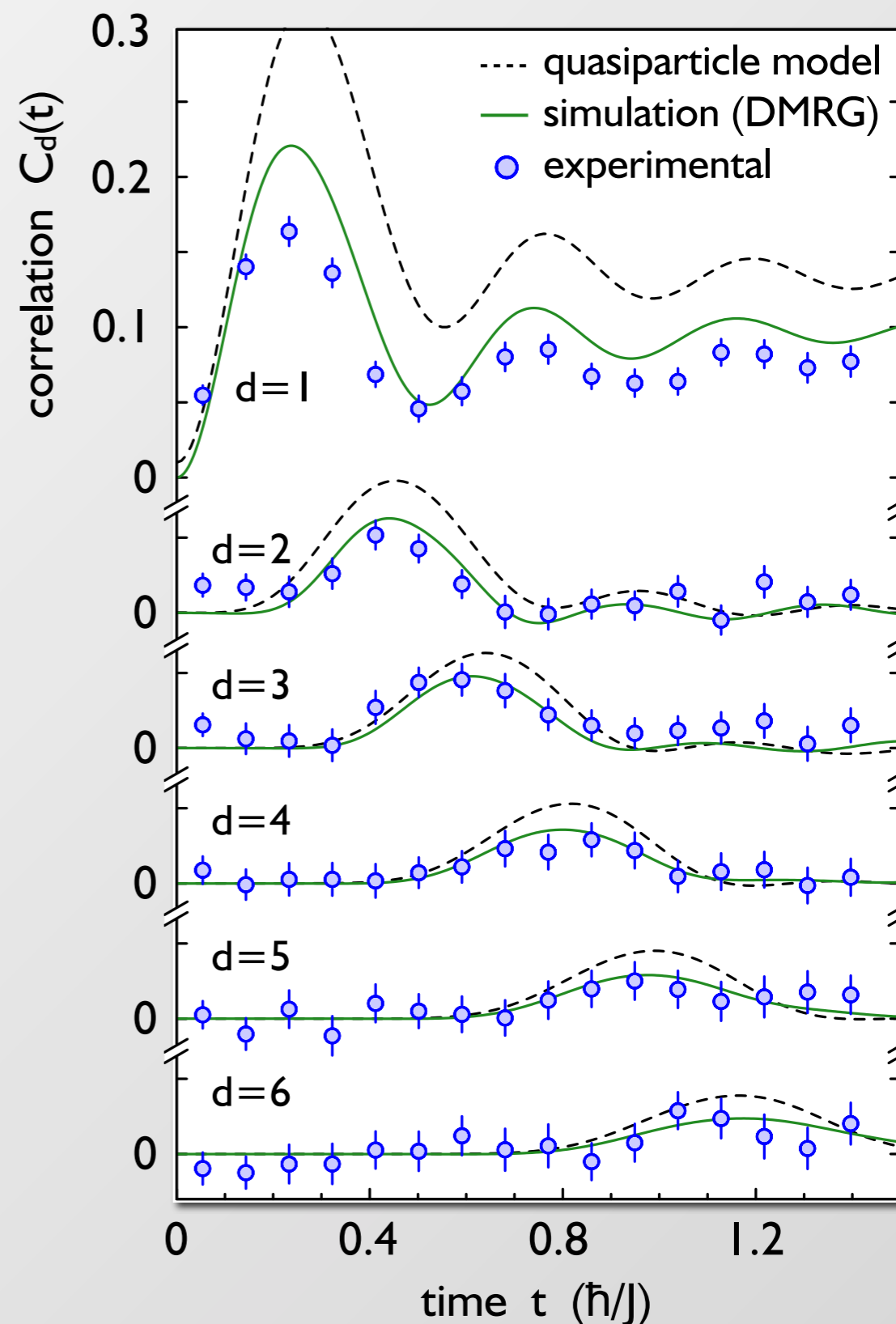
Bravyi, Hastings and Verstraete (2006)

Calabrese and Cardy (2006)

Eisert and Osborne (2006)

Nachtergaele, Ogata and Sims (2006)

... *and many others since then*



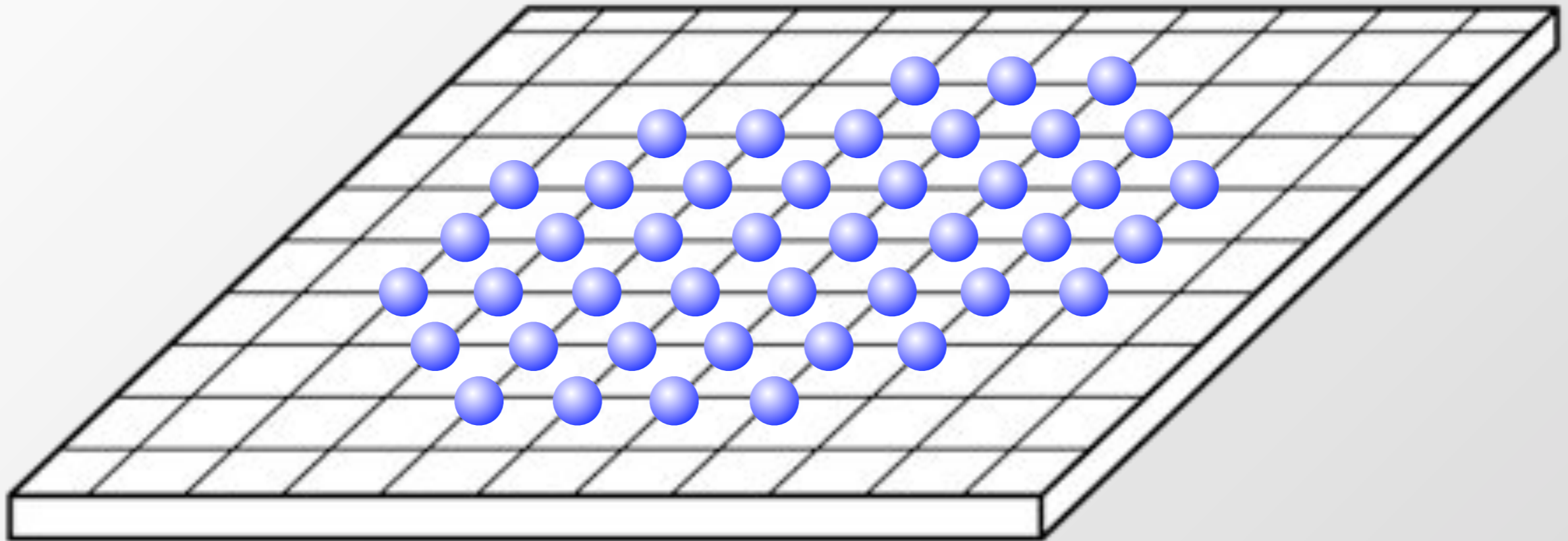
M. Cheneau et al. Nature (2012)

Single Site Addressing

A scanning electron microscope (SEM) image of a quantum dot array. The dots are arranged in a regular grid. Some dots are highlighted in red, indicating they are being addressed individually. The background is dark, and the dots are bright green and red.

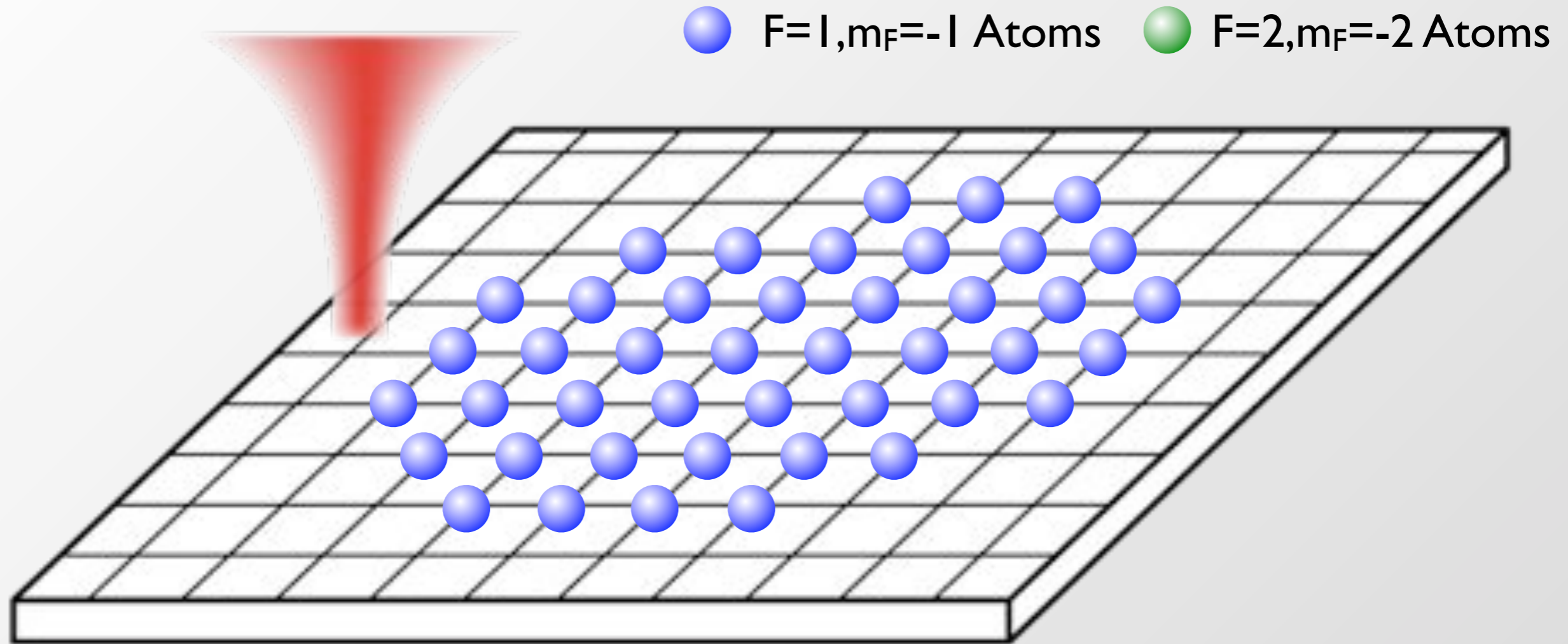
Ch. Weitenberg et al., Nature 471, 319-324 (2011)

● $F=1, m_F=-1$ Atoms ● $F=2, m_F=-2$ Atoms



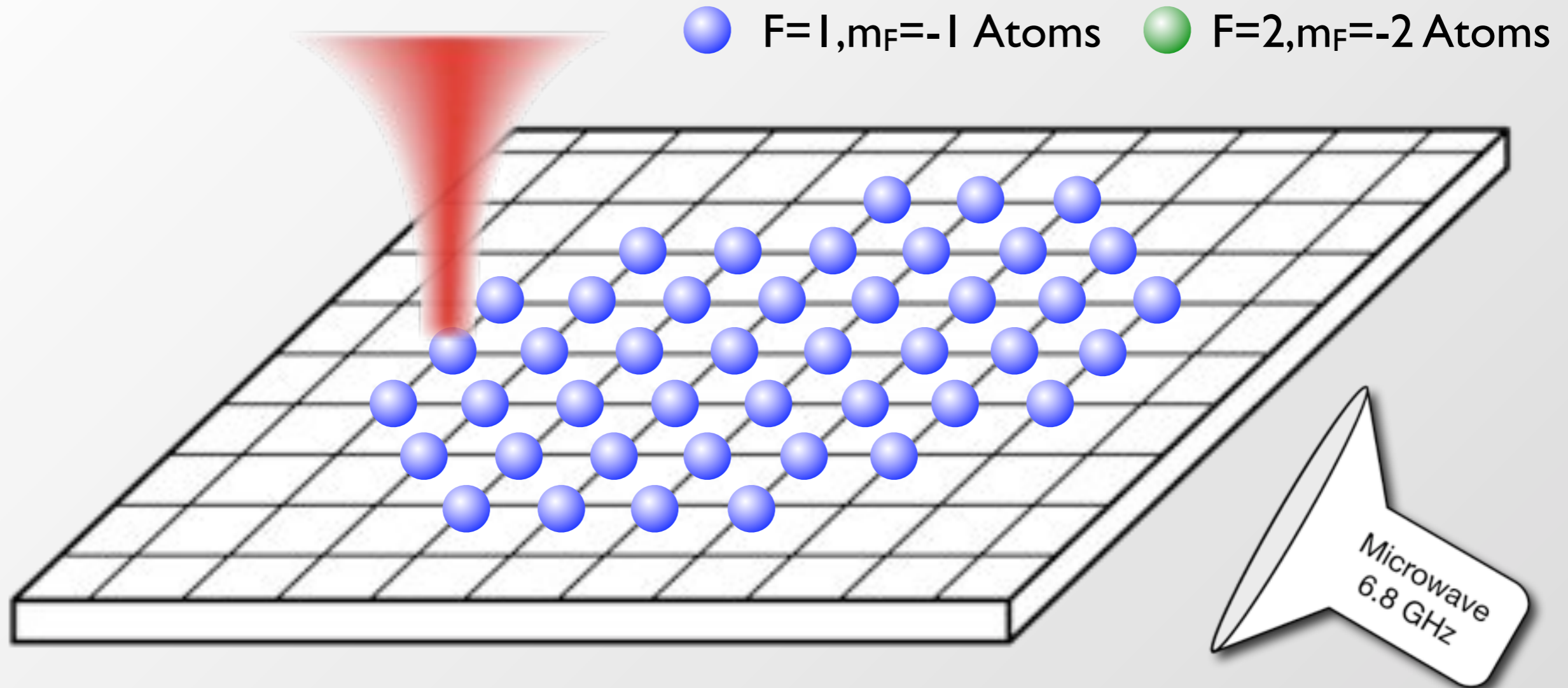
Differential light shift allows to coherently address single atoms!
Landau-Zener Microwave sweep to coherently convert atoms between spin-states.



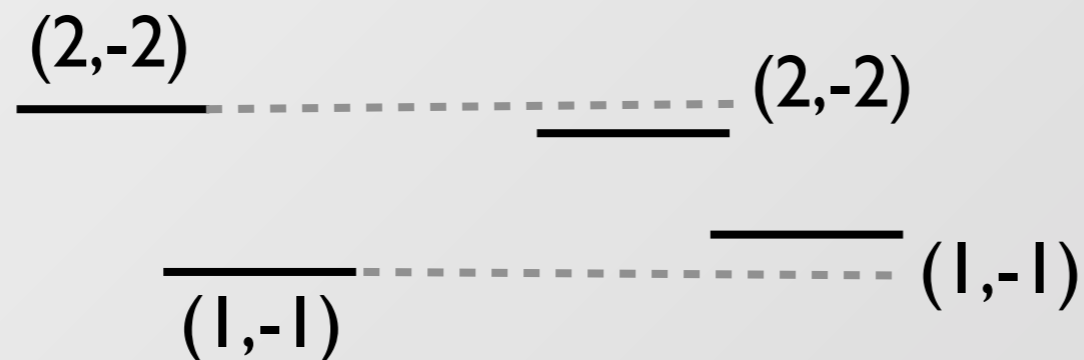


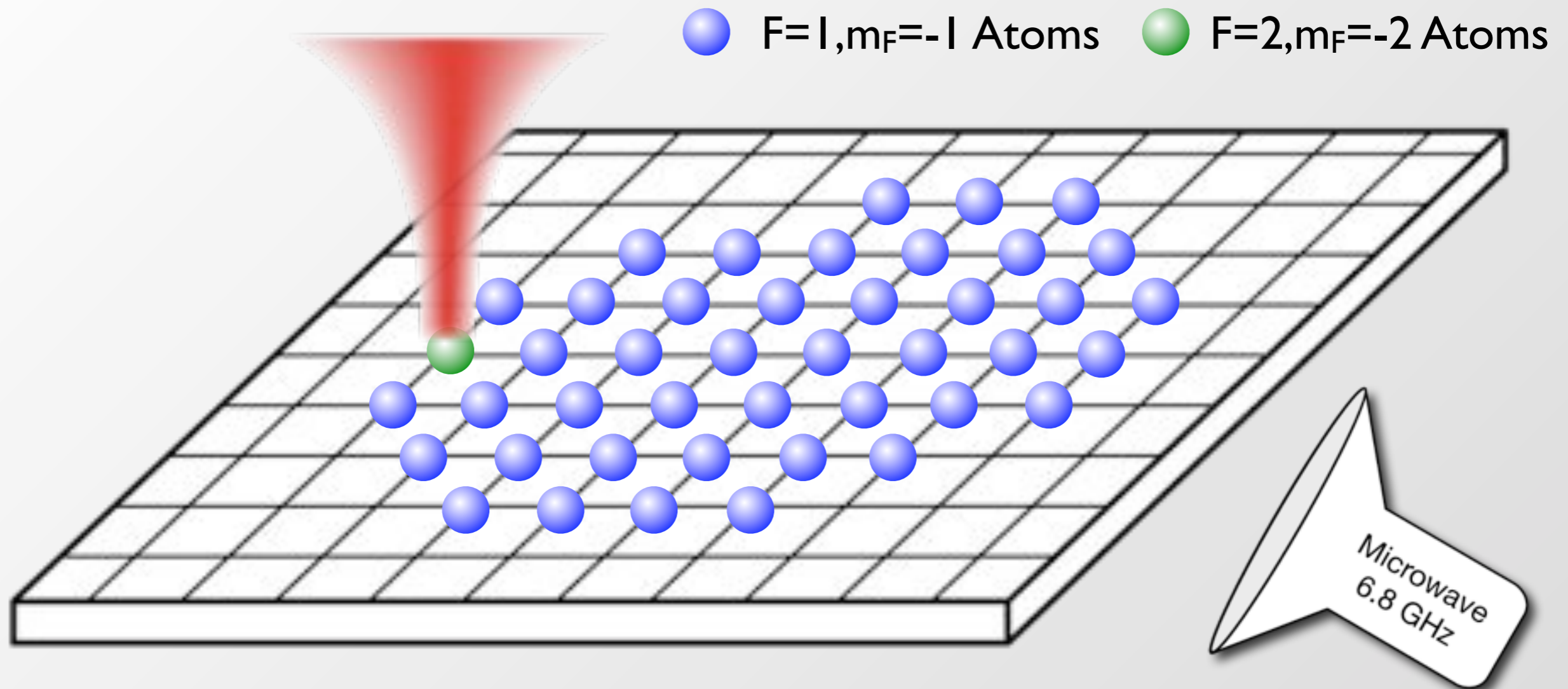
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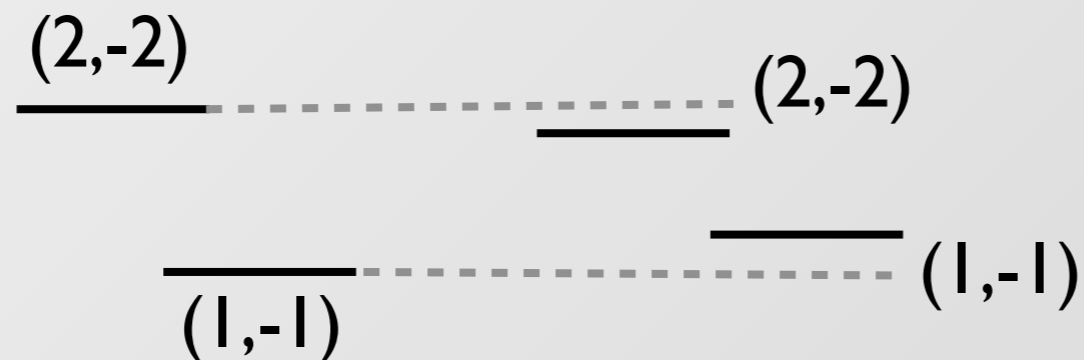


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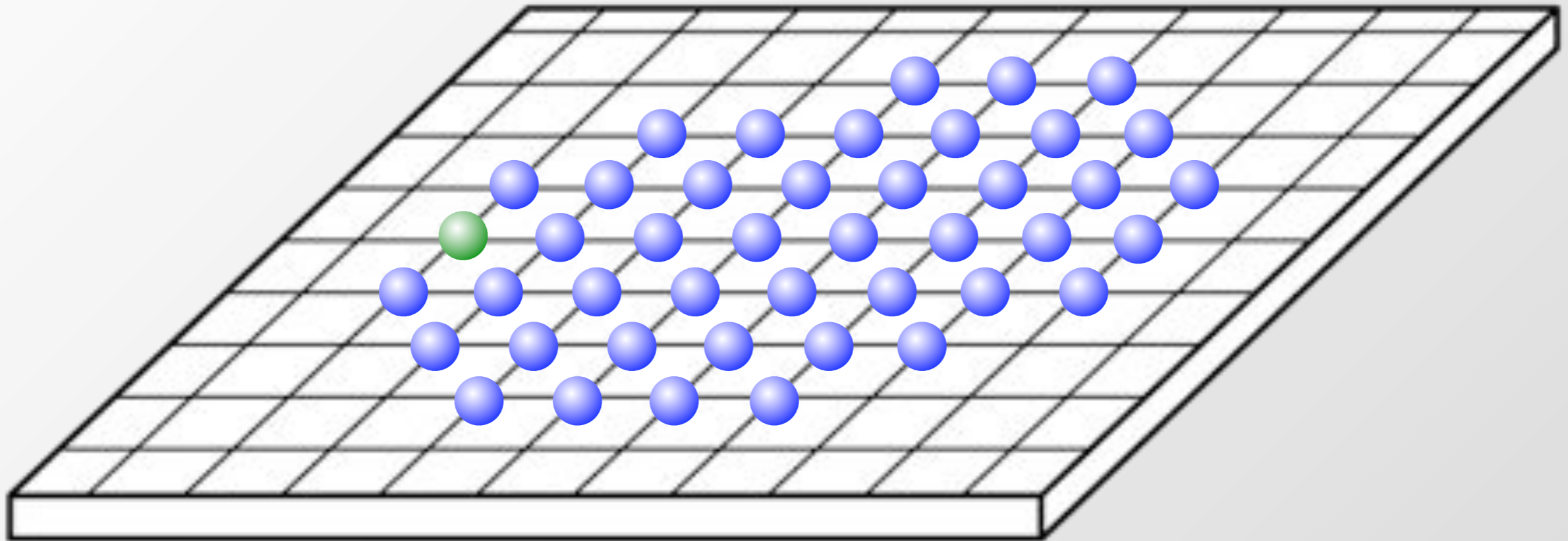




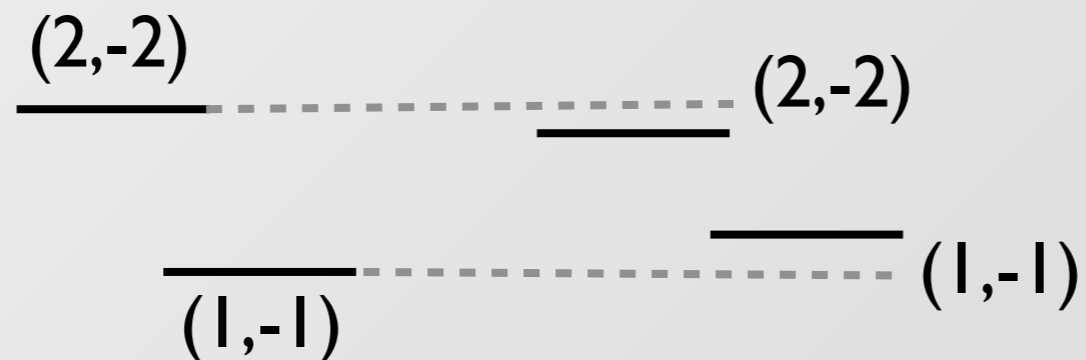
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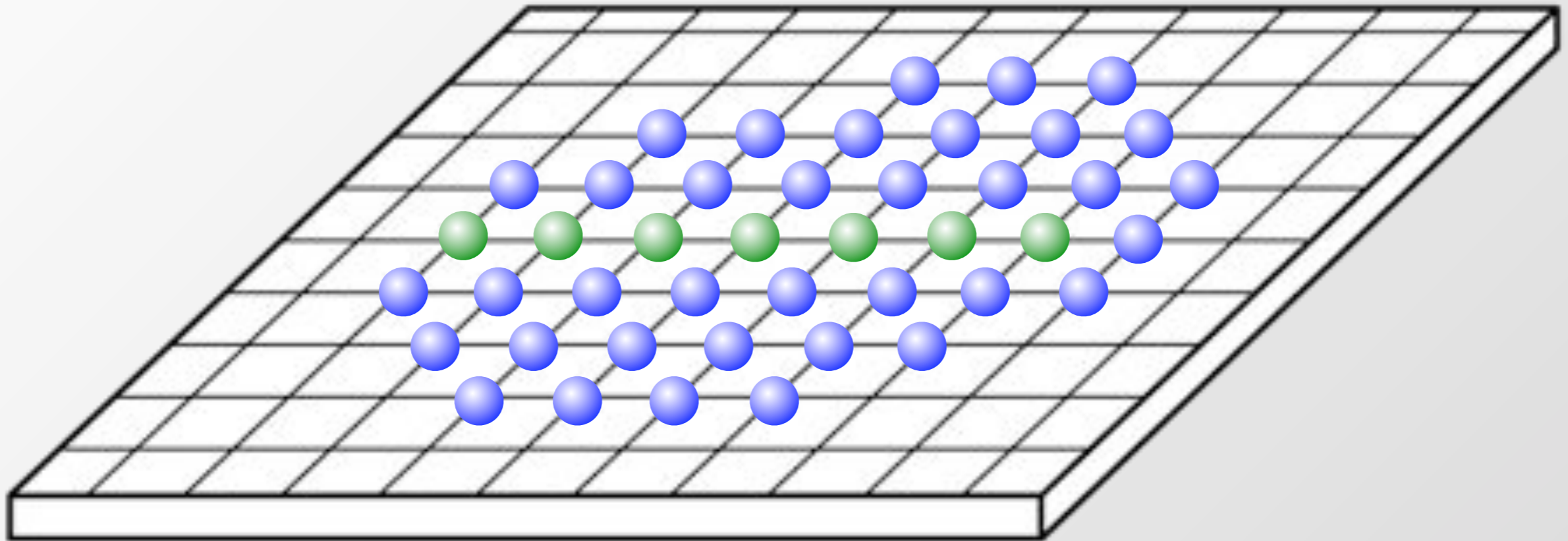
● $F=1, m_F=-1$ Atoms
 ● $F=2, m_F=-2$ Atoms



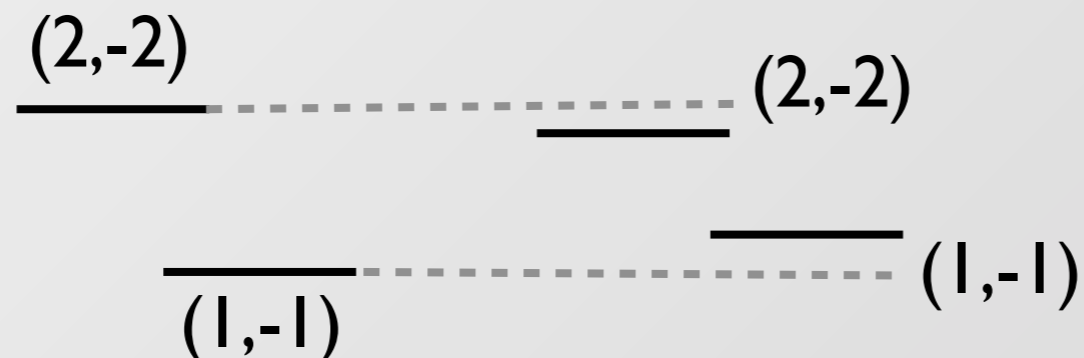
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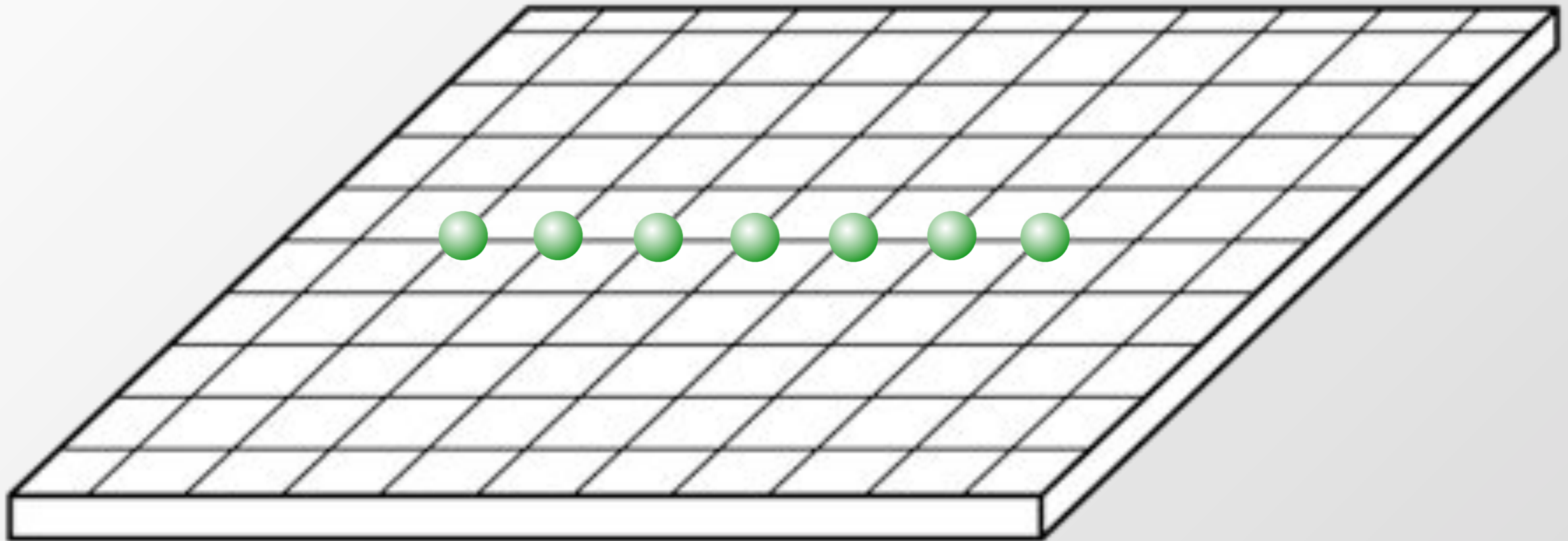
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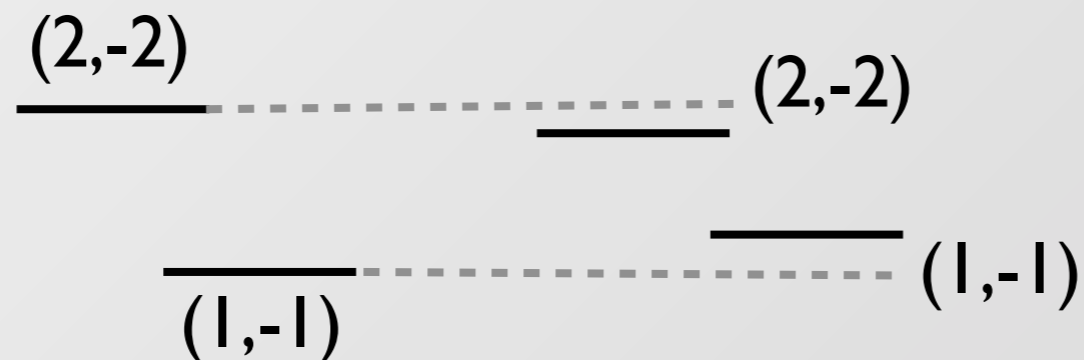
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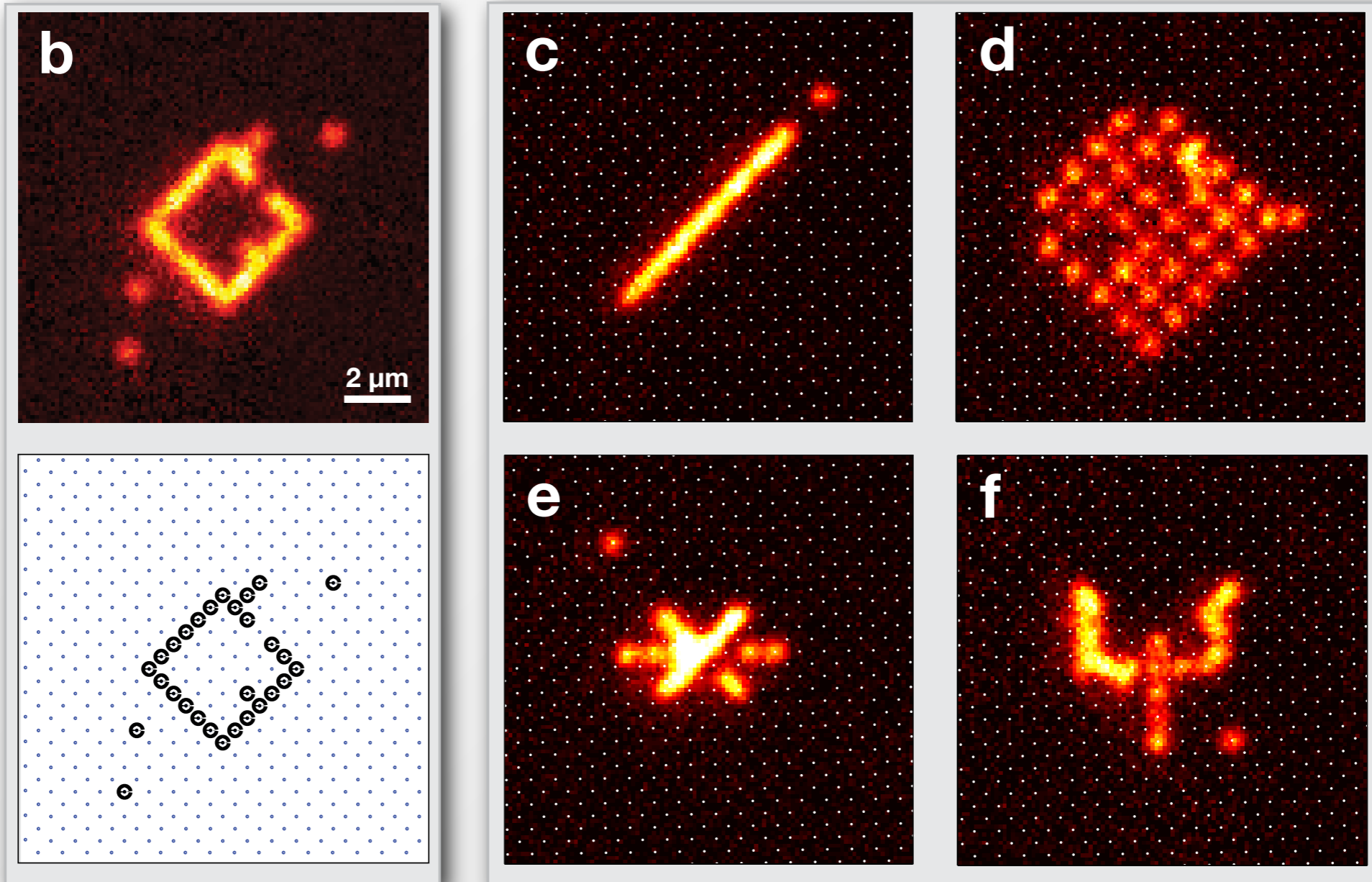


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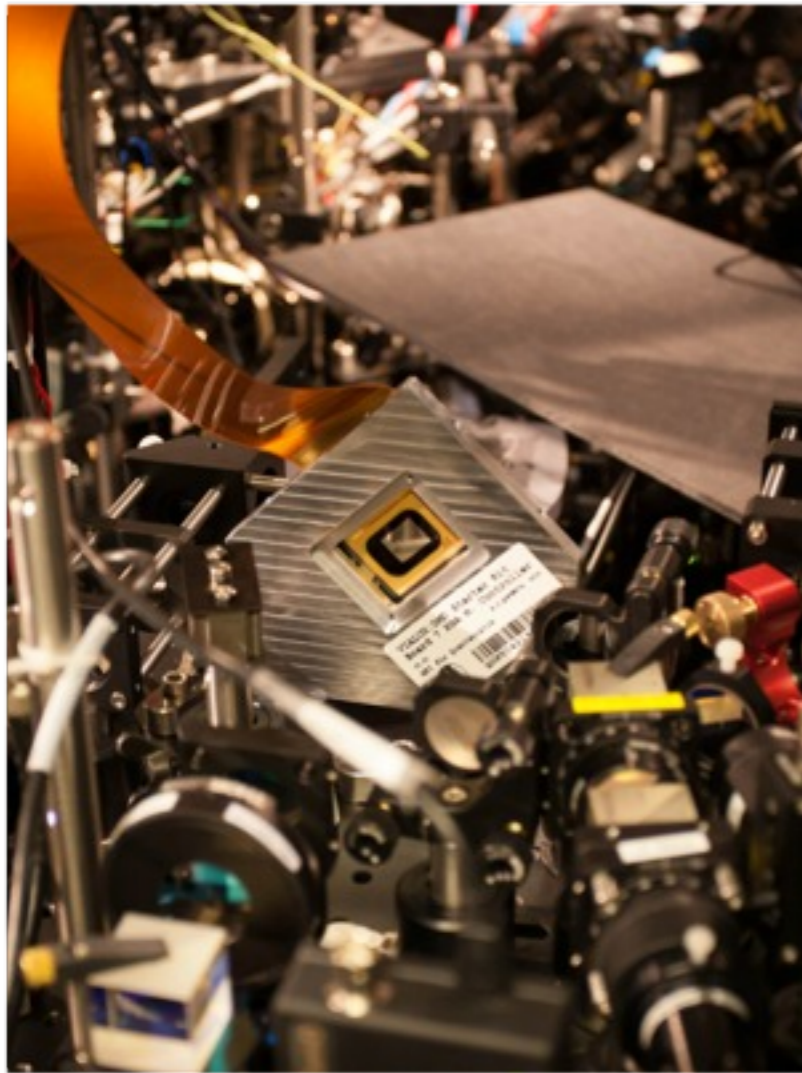
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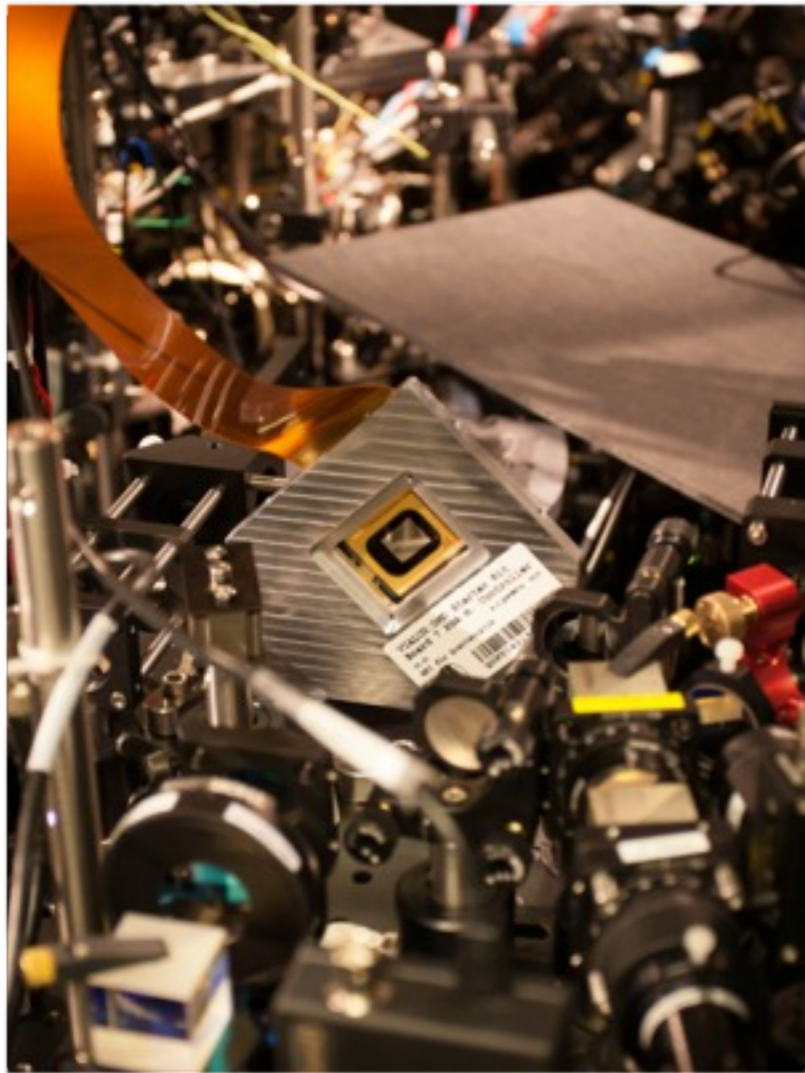
Subwavelength spatial resolution: 50 nm



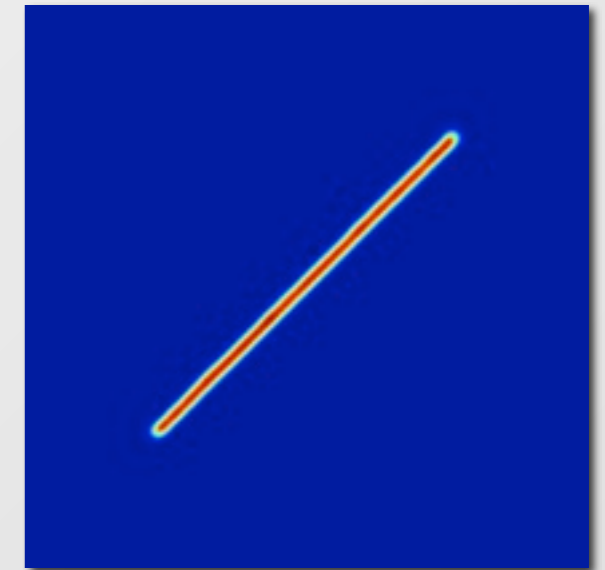
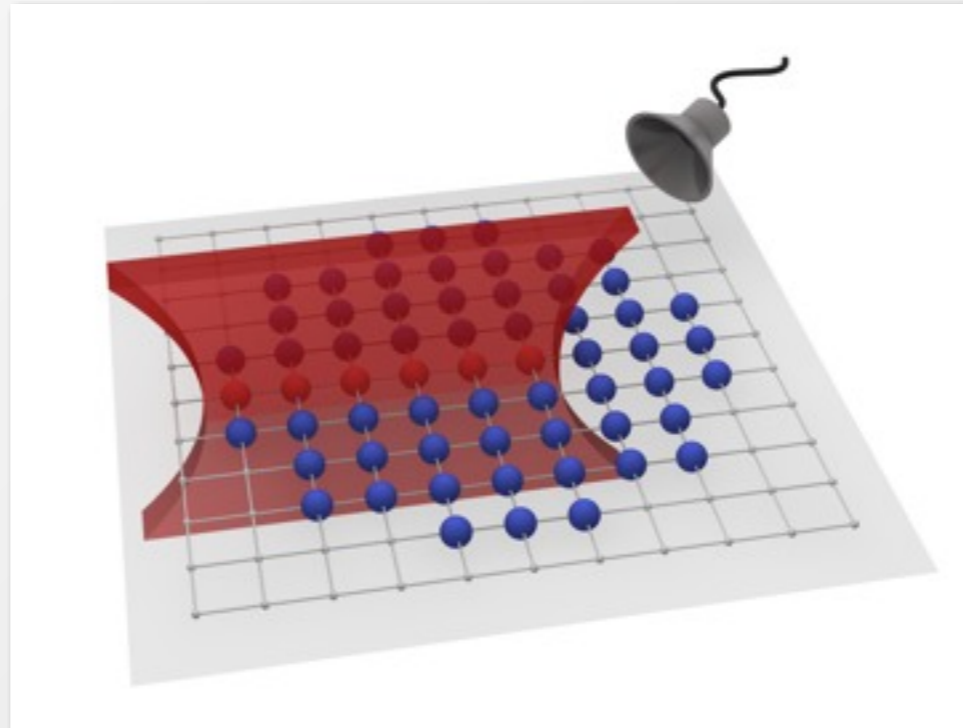


Digital Mirror Device
(DMD)





Digital Mirror Device
(DMD)

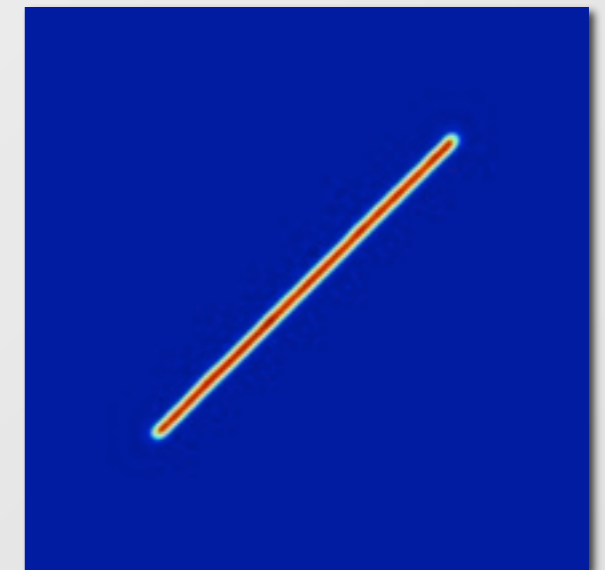
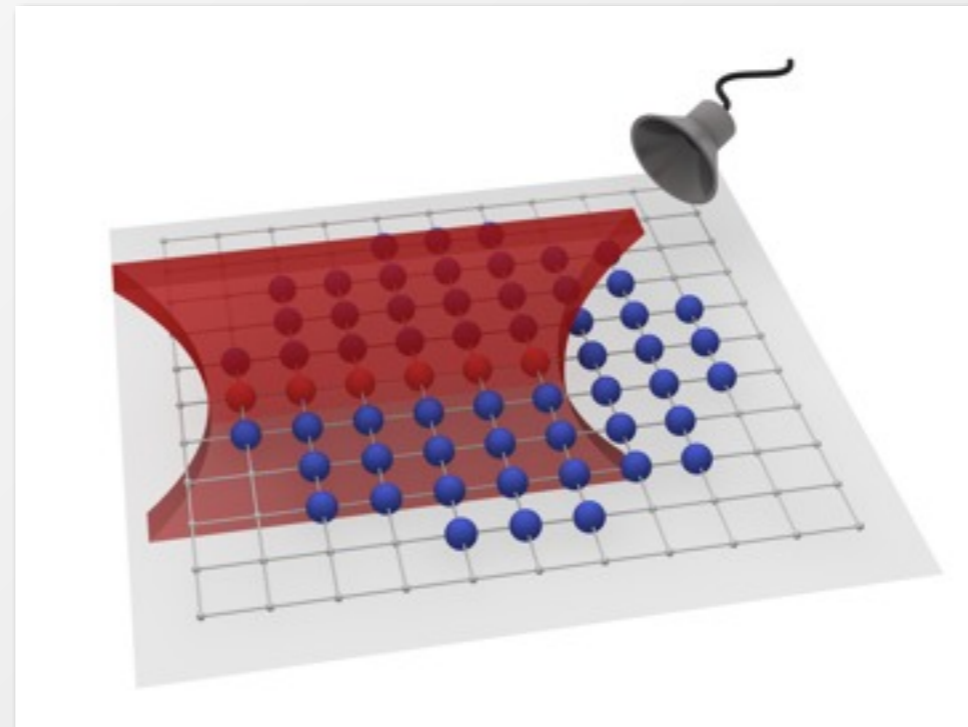


Measured Light Pattern

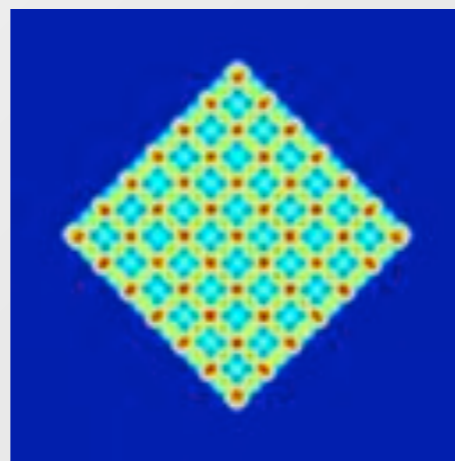




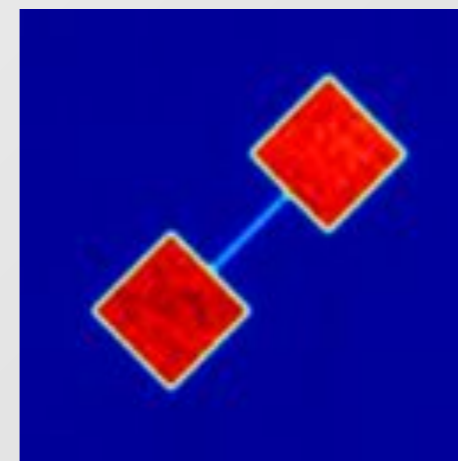
Digital Mirror Device
(DMD)



Measured Light Pattern



Exotic Lattices



Quantum Wires

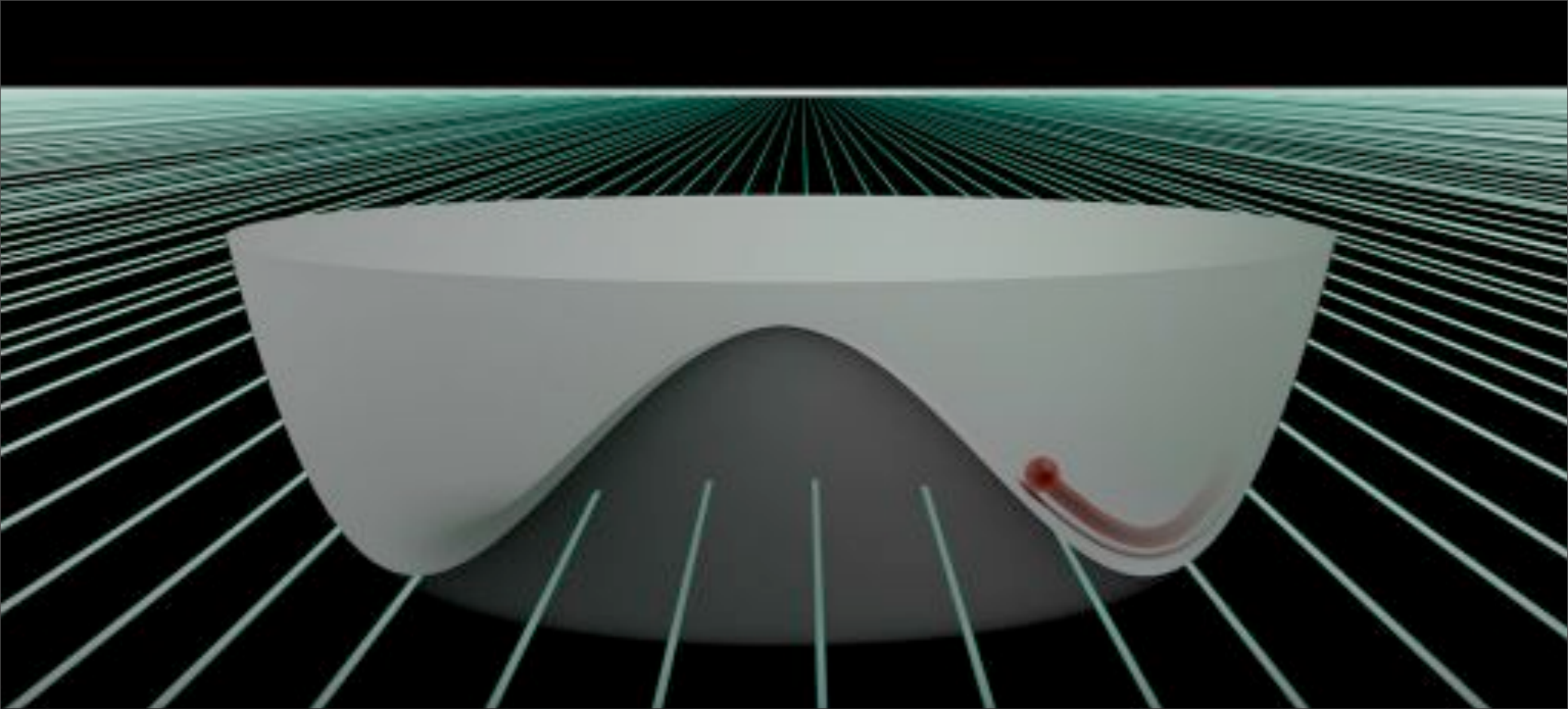


Box Potentials

Almost Arbitrary Light Patterns Possible!

Single Spin Impurity Dynamics, Domain Walls, Quantum Wires, Novel Exotic Lattice Geometries, ...





'Higgs' Amplitude Mode in Flatland

M. Endres, T. Fukuhara, M. Cheneau, P. Schauss, D. Pekkar, E. Demler, S. Kuhr & I.B.

M. Endres et al. Nature (2012)

Chubukov & Sachdev, PRB 1993; Sachdev, PRB 1999; Zwerger, PRL 2004; Altman, Blatter, Huber, PRB 2007, PRL 2008; U. Bissbort et al. Phys. Rev. Lett. (2011); D. Podolsky, A. Auerbach, D. Arovas, PRB 2011

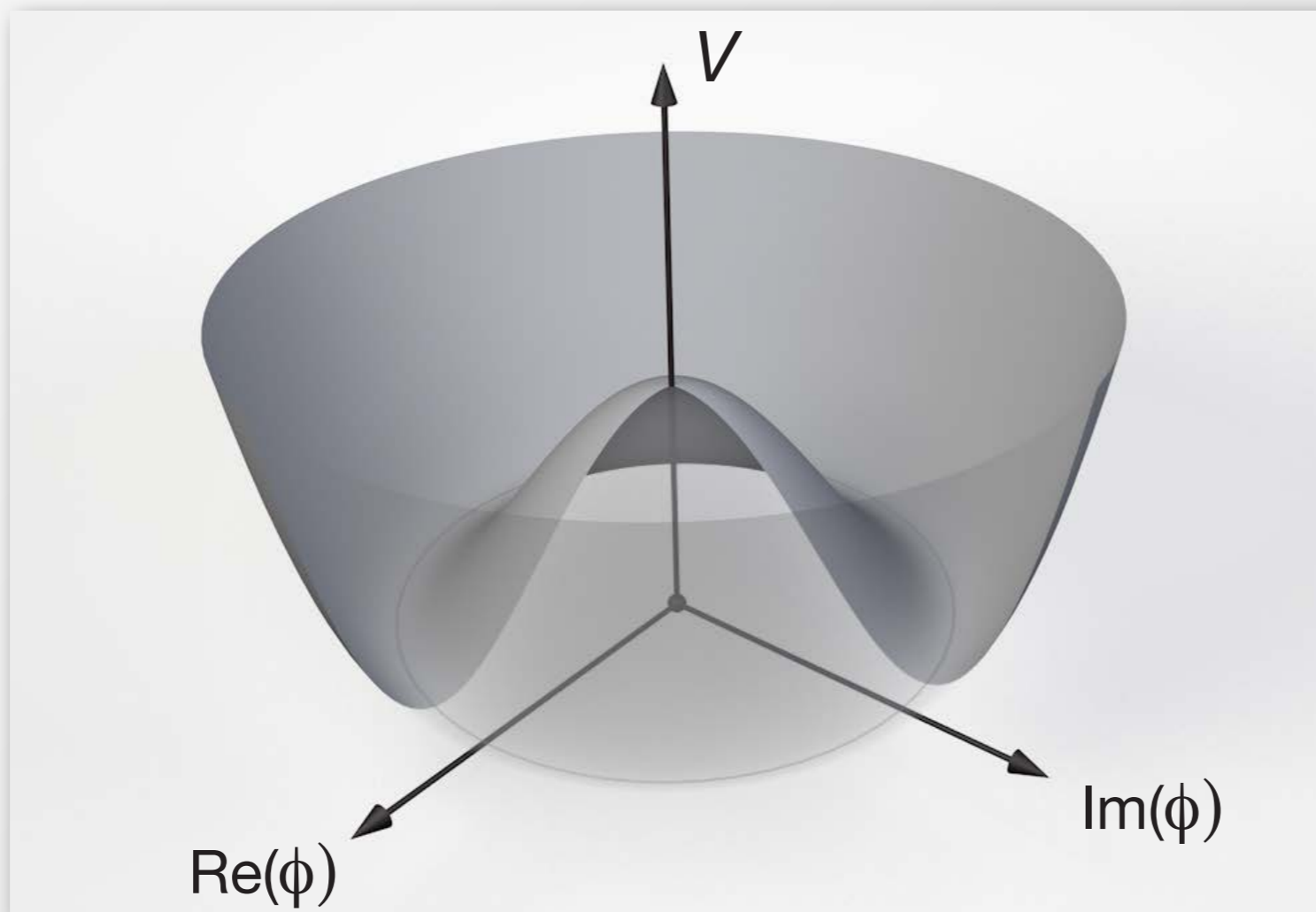
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$$L = \partial_\mu \phi^* \partial^\mu \phi - m^2 \phi^* \phi - \frac{1}{2} \lambda (\phi^* \phi)^2$$

Relativistic Quantum Field-Theory
of complex field ϕ with mass m .

$$L = \partial_\mu \phi^* \partial^\mu \phi + m^2 \phi^* \phi - \frac{1}{2} \lambda (\phi^* \phi)^2$$

Imagine **negative mass term**.



$$L = \partial_\mu \phi^* \partial^\mu \phi - V(\phi)$$

$$\phi(x) \rightarrow \phi(x) e^{i\theta}$$

Lagrangian is U(1)
symmetric



$$V(\phi) = -\frac{1}{2}\lambda v^2 \phi^* \phi + \frac{1}{2}\lambda (\phi^* \phi)^2 \quad v^2 = -2m^2 / \lambda$$

Minimum of Mexican Hat at: $|\phi|^2 = \frac{v^2}{2}$

Pick one vacuum state! Expand field around:

$$\phi = \frac{1}{\sqrt{2}}(v + \varphi_1 + i\varphi_2)$$

$$L = \frac{1}{2} [(\partial_\mu \varphi_1)^2 + (\partial_\mu \varphi_2)^2] - \frac{1}{2}\lambda v^2 \varphi_1^2 + \dots$$

φ_1, φ_2 real scalar fields



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Massless Nambu-Goldstone mode

φ_1, φ_2 real scalar fields



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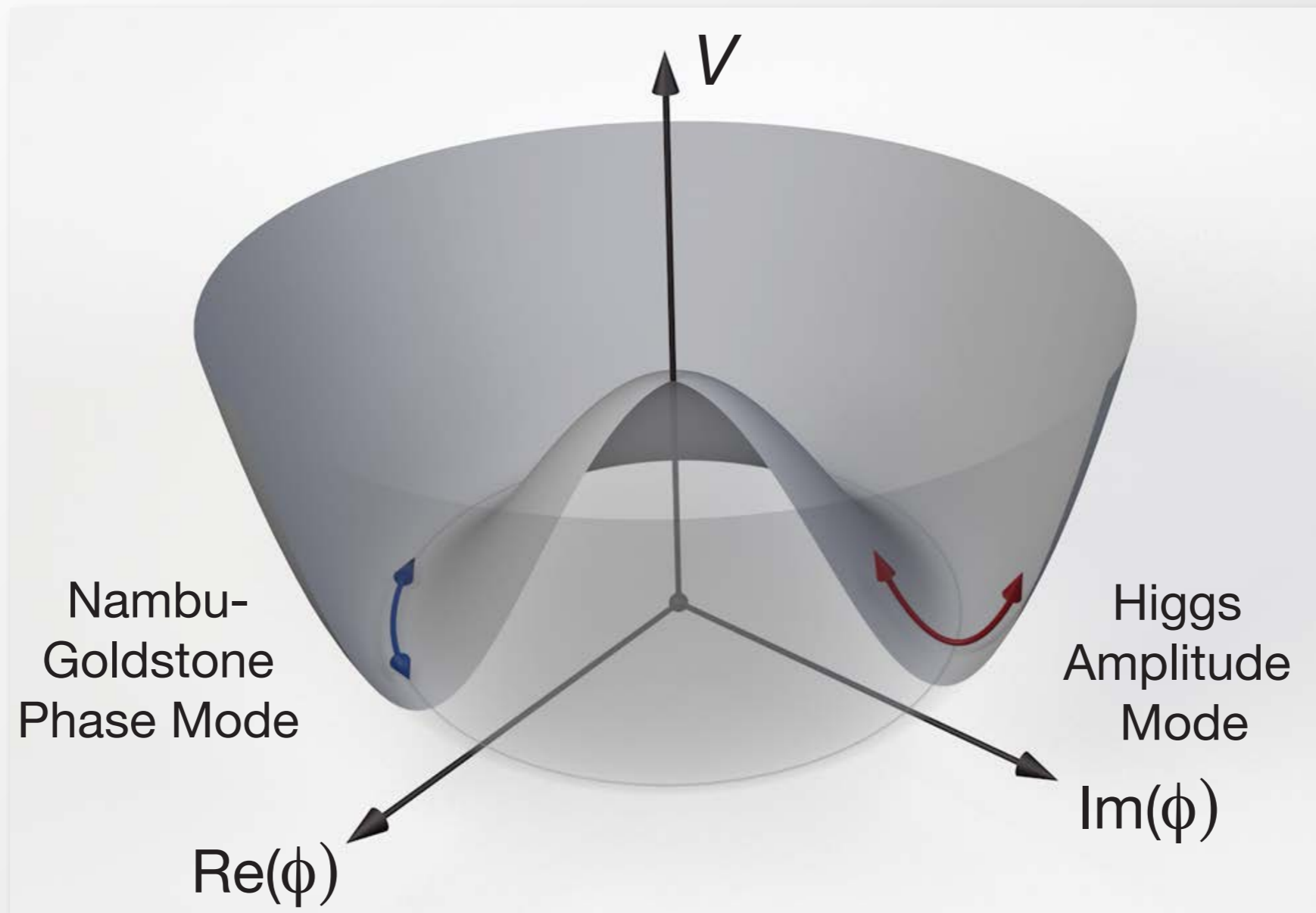
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Massless Nambu-Goldstone mode

Massive Higgs mode

φ_1, φ_2 real scalar fields





Excitations in **radial direction are gapped** due to 'Higgs mass'!



$\theta \rightarrow \theta(x)$ Extend to local U(1) gauge symmetry.

$A_\mu \rightarrow A_\mu(x) - \frac{1}{e} \partial_\mu \theta(x)$ introduces vector potential

$D_\mu \phi = \partial_\mu \phi + ieA_\mu \phi$ minimal coupling

$$L = D_\mu \phi^* D^\mu \phi - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - V(\phi)$$

Breaking symmetry leads to:

$$L = \frac{1}{2} (\partial \varphi_1)^2 + \frac{1}{2} (\partial_\mu \varphi_2 + e\nu A_\mu)^2 - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{2} \lambda \nu^2 \varphi_1^2 + \dots$$

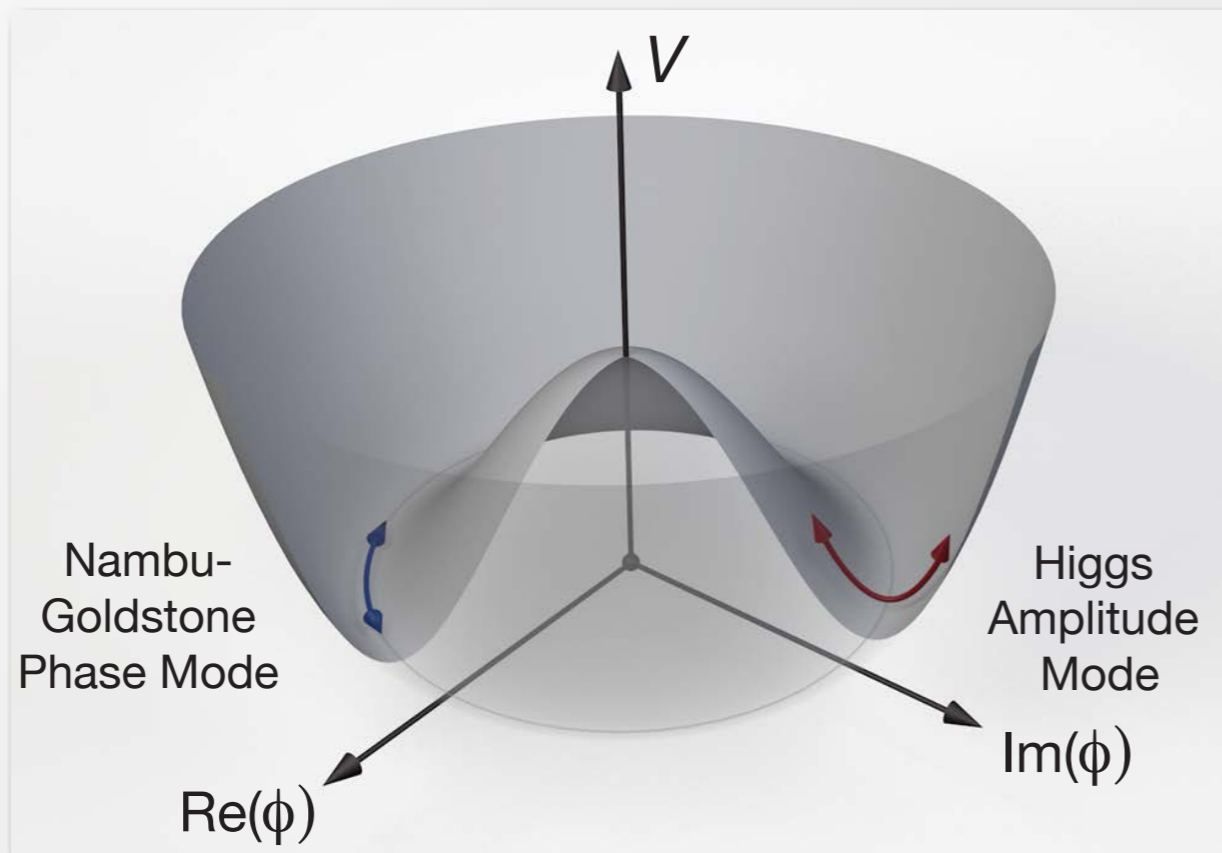
Photons have become massive ($m^2=e\nu$)! \longrightarrow Meissner effect Anderson 1963

Similar for non-Abelian gauge theory U(1) \times SU(2) \longrightarrow W,Z bosons acquire mass
Englert, Brout, Higgs, Guralnik, Hagen, Kibble, Weinberg ~1964



Close to a quantum critical point, **effectively relativistic field theory!**
see e.g.: Subir Sachdev, Quantum Phase Transitions

Here: **SF-MI transition for $n=1$, $O(2)$ field theory in $2+1$ dimension**



**Fundamental question
in 2D:**

**is mode observable or
overdamped?**

Chubukov & Sachdev, PRB 1993
Sachdev, PRB 1999; Zwerger, PRL 2004;
Altman, Blatter, Huber, PRB 2007, PRL 2008;
Menotti & Trivedi, PRB 2008; Podolsky,
Auerbach, Arovas, PRB 2011; Pollet &
Prokof'ev PRL 2012; Sachdev & Podolsky, PRB
2012; ...

Other systems: Quantum spin systems $O(3)$ in $3+1$ dimensions

Ch. Rüegg et al. Physical Review Letters (2008)

in superconductors coupled to CDW:

C.Varma & P. Littlewood PRL, PRB (1981,1982)



Far from the Mott lobe, SF described by Gross-Pitaevskii action:

$$S = \int d^3 r dt \left(-i\psi^* \partial_t \psi - \frac{1}{2m^*} |\nabla \psi|^2 + \mu |\psi|^2 - g |\psi|^4 \right)$$

GPE: Phase and amplitude mode are c.c. variables! Therefore only one mode!

Close to QCP: Phase and amplitude of order parameter commute: two

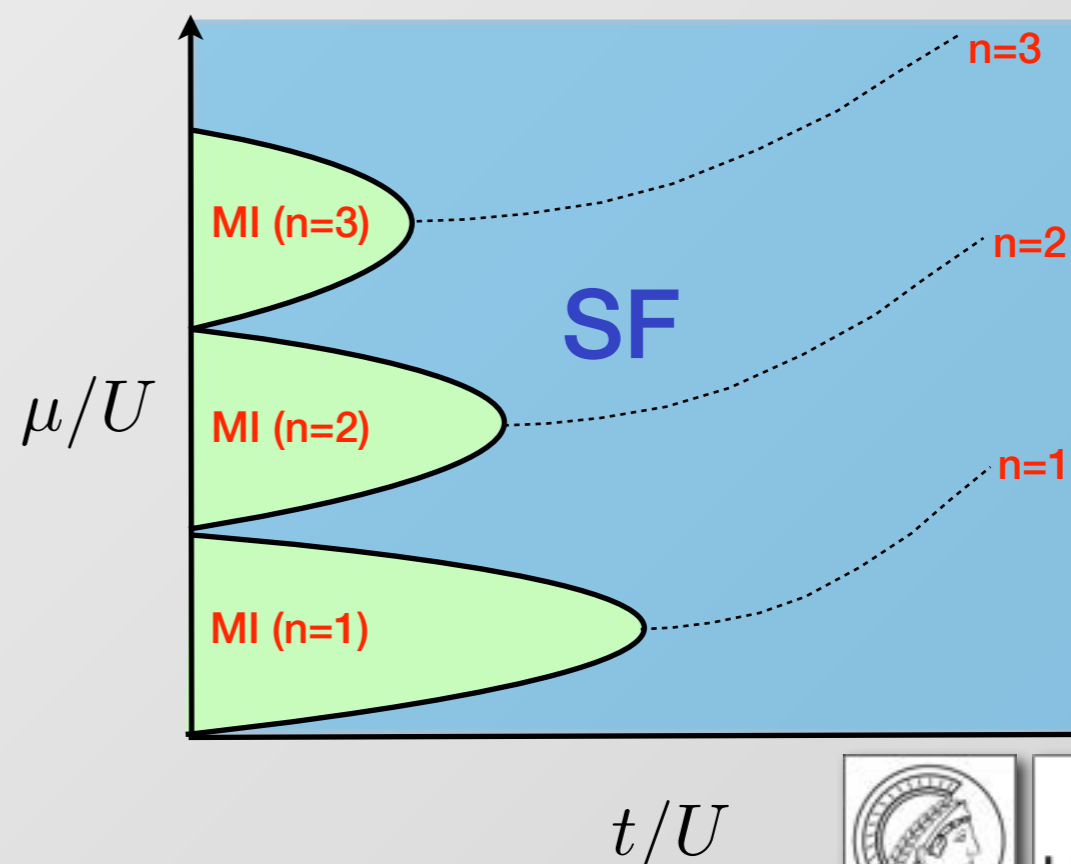
Galilean invariant. Predicts massless Goldstone mode, but not

Near the Mott lobe at integer filling, particle-hole symmetry leads to relativistic dynamics:

$$S = \int d^3 r dt \left(|\partial_t \psi|^2 - c^2 |\nabla \psi|^2 + r |\psi|^2 - u |\psi|^4 \right)$$

Lorentz invariant. Predicts Goldstone mode **and** Higgs mode.

Courtesy: Danny Podolsky (Technion)



From Euler-Lagrange equation, we obtain:

Lorentz invariant action

$$\ddot{\phi}_1 = c_s^2 \nabla^2 \phi_1 - \Delta_0^2 \phi_1$$

$$\ddot{\phi}_2 = c_s^2 \nabla^2 \phi_2$$

$$\omega_1(k) = \sqrt{\Delta_0^2 + c_s^2 k^2}$$

$$\omega_2(k) = c_s k$$

Relativistic Mode

Amplitude!

Sound Mode

Density!

Galilean invariant action

$$-\dot{\phi}_1 = \frac{\hbar^2}{2m} \nabla^2 \phi_2$$

$$\dot{\phi}_2 = \frac{\hbar^2}{2m} \nabla^2 \phi_1 - 2\mu \phi_1$$

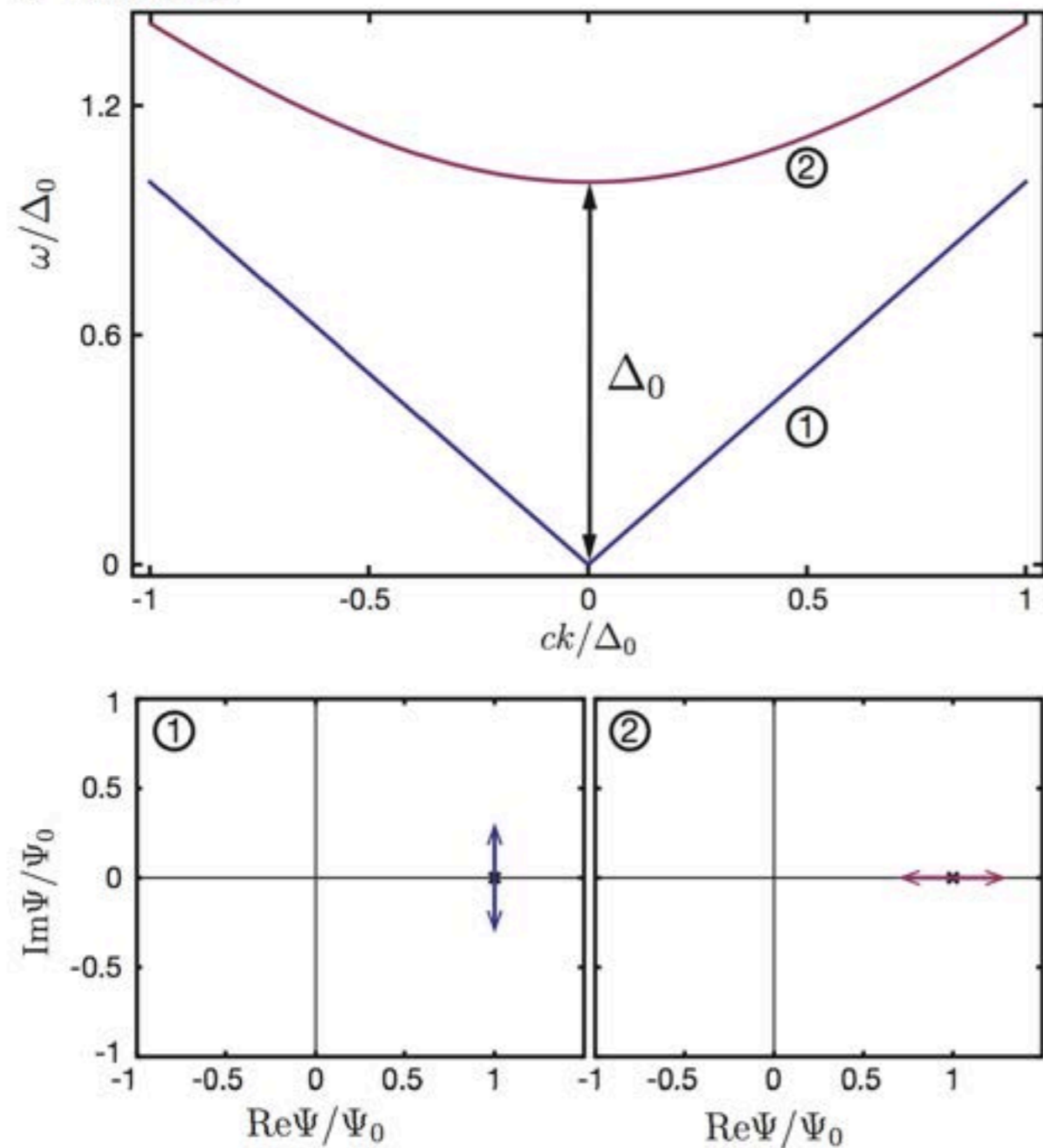
$$\omega(\tilde{k}) = \sqrt{\mu^2 \tilde{k}^2 (\tilde{k}^2 + 2)}$$

Bogoliubov Mode

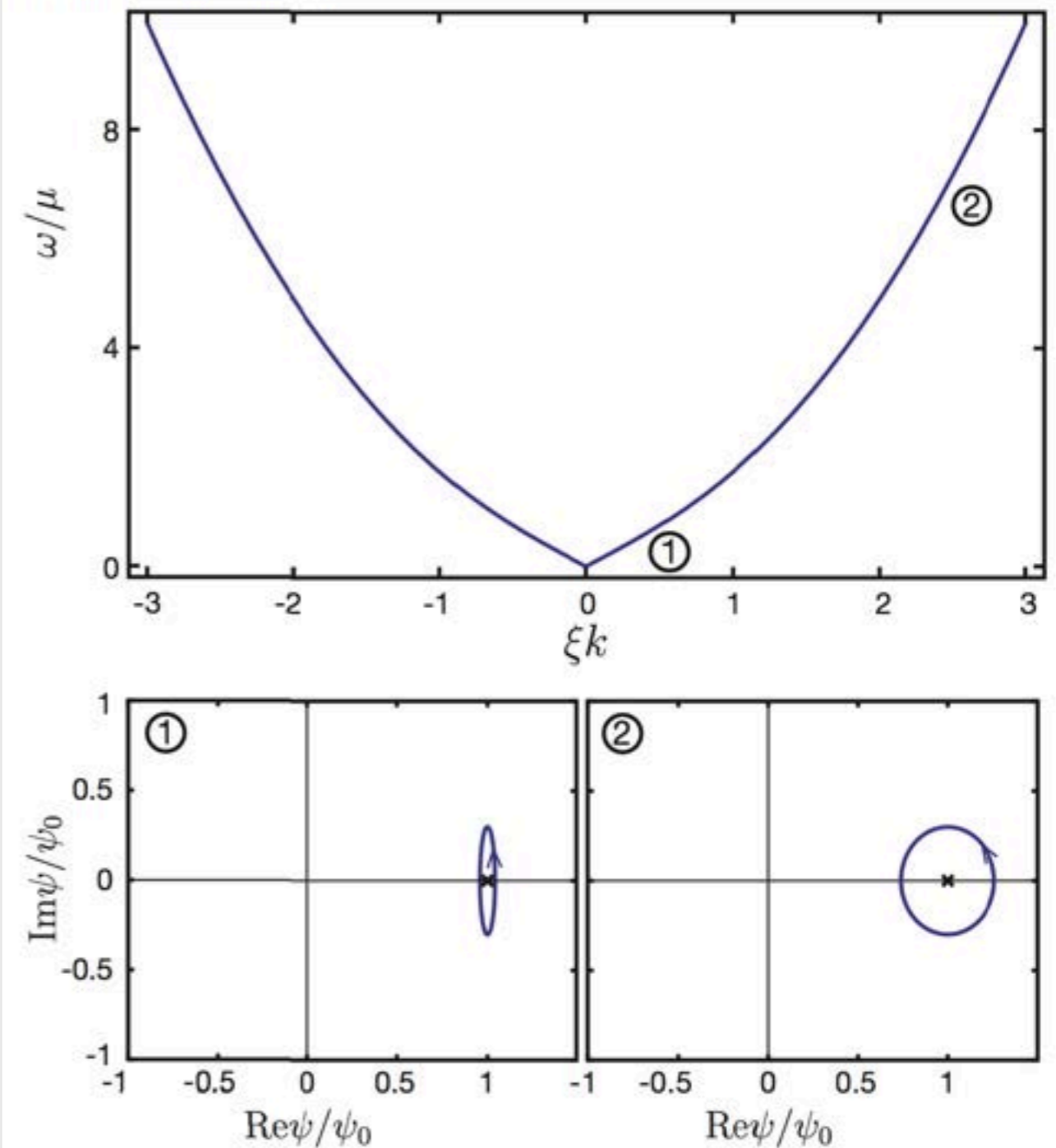
Amplitude-Density Coupled!



a 'relativistic'



b Gross-Pitaevskii



'Relativistic'
Lorentz Invariant

'Classical'
Galilean Invariant



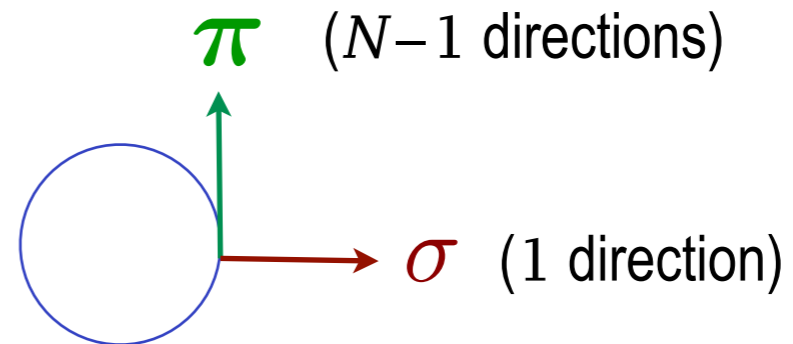
Courtesy: Danny Podolsky (Technion)



Two ways to parameterize deviations from the ordered state :

I) Cartesian : $\phi = (\sqrt{N} + \sigma, \pi)$

$$\mathcal{L}_0 = \frac{1}{2g} \left[(\partial_\mu \sigma)^2 - m^2 \sigma^2 + (\partial_\mu \pi)^2 \right]$$

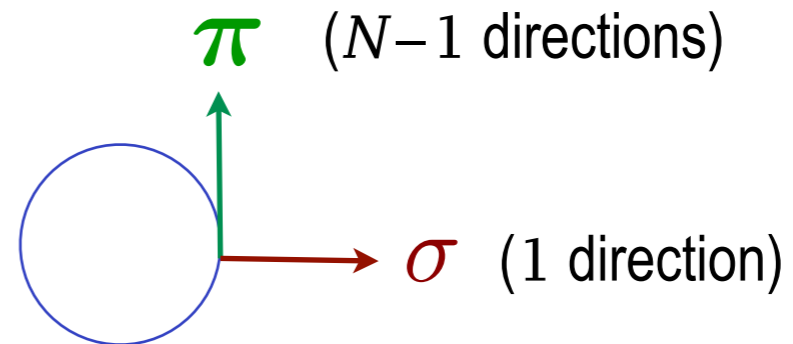


Courtesy: Danny Podolsky (Technion)

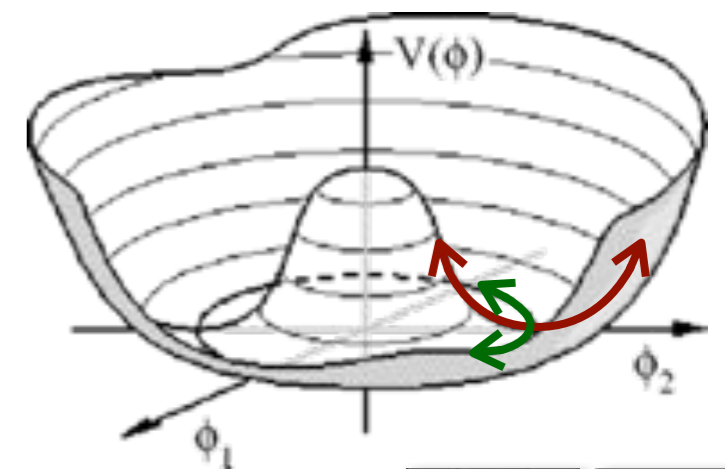
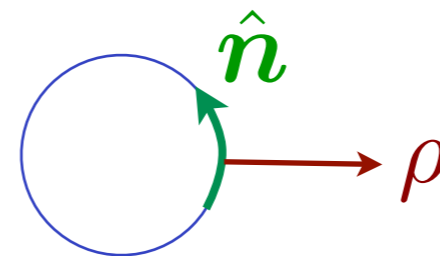
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2) Polar : $\phi = \sqrt{N} (1 + \rho)^{1/2} \hat{n}$

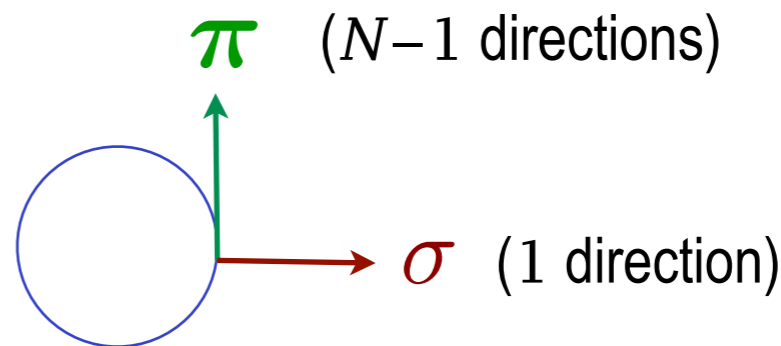


Courtesy: Danny Podolsky (Technion)

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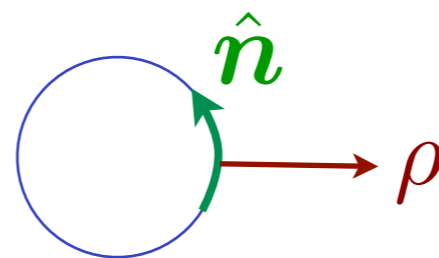
1) Cartesian : $\phi = (\sqrt{N} + \sigma, \boldsymbol{\pi})$

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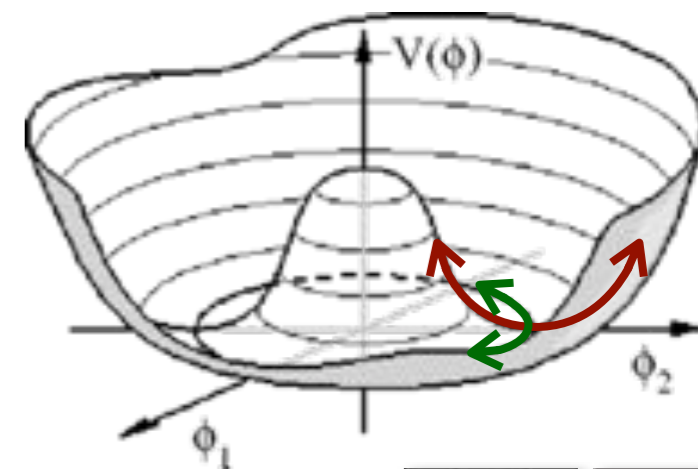


$$\mathcal{L}_1 = \frac{m^2}{2g} \left[\frac{1}{\sqrt{N}} \sigma \boldsymbol{\pi}^2 + \frac{1}{\sqrt{N}} \sigma^3 + \frac{1}{4N} \sigma^4 + \frac{2}{N} \sigma^2 \boldsymbol{\pi}^2 + \frac{1}{4N} (\boldsymbol{\pi}^2)^2 \right]$$

2) Polar : $\phi = \sqrt{N} (1 + \rho)^{1/2} \hat{n}$



$$\mathcal{L} = \frac{1}{2g} \left[N(1 + \rho)(\partial_\mu \hat{n})^2 + \frac{(\partial_\mu \rho)^2}{4(N + \rho)} + \frac{m^2 \rho^2}{4N} \right]$$

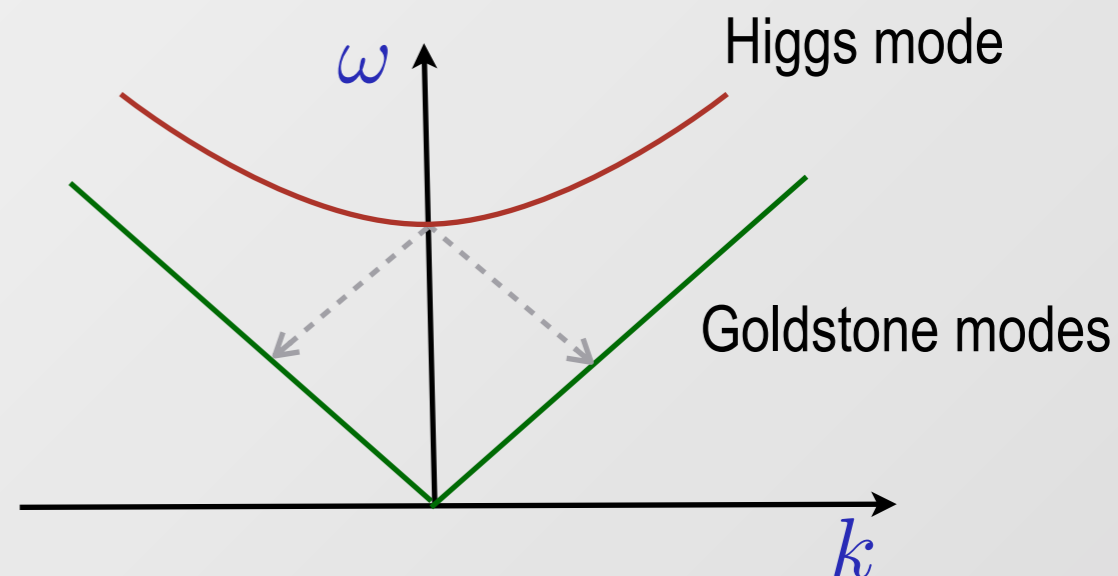


Courtesy: Danny Podolsky (Technion)



It can decay into a pair of Goldstone bosons :

$$\mathcal{L}_{\text{int}} \propto \begin{cases} \sigma \pi^2 & \text{(Cartesian)} \\ \rho (\partial_\mu \hat{n})^2 & \text{(polar)} \end{cases}$$

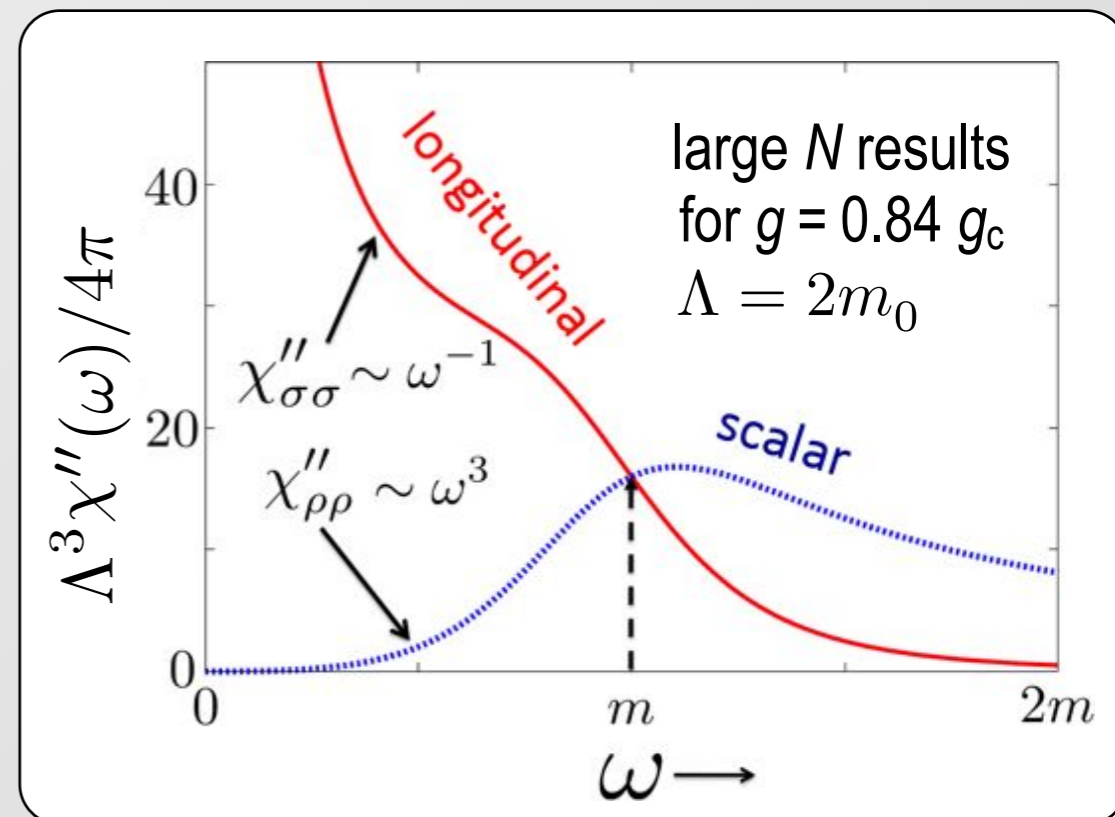


Cartesian and polar calculations correspond to *different correlation functions*.

Depends on the type of experiment performed.



Courtesy: Danny Podolsky (Technion)



The **longitudinal** response function is measured by an experiment where the probe couples directly to the order parameter field:

$$S_{\text{probe}} = \int d^d x \int dt \mathbf{h}(\mathbf{x}, t) \cdot \phi(\mathbf{x}, t)$$

Example : neutron scattering in an antiferromagnet.

Courtesy: Danny Podolsky (Technion)



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Example : neutron scattering in an antiferromagnet.

The **scalar** response function is measured by an experiment where the probe couples directly to the magnitude of the order parameter field:

$$S_{\text{probe}} = \int d^d x \int dt u(\mathbf{x}, t) |\boldsymbol{\phi}(\mathbf{x}, t)|^2 \quad |\boldsymbol{\phi}|^2 = N(1 + \rho)$$

Examples : lattice modulation spectroscopy

Courtesy: Danny Podolsky (Technion)



V

Modulate coupling strength
close to Quantum Phase
Transition!

$$j = j + \delta j \sin(\omega t)$$

 ϕ

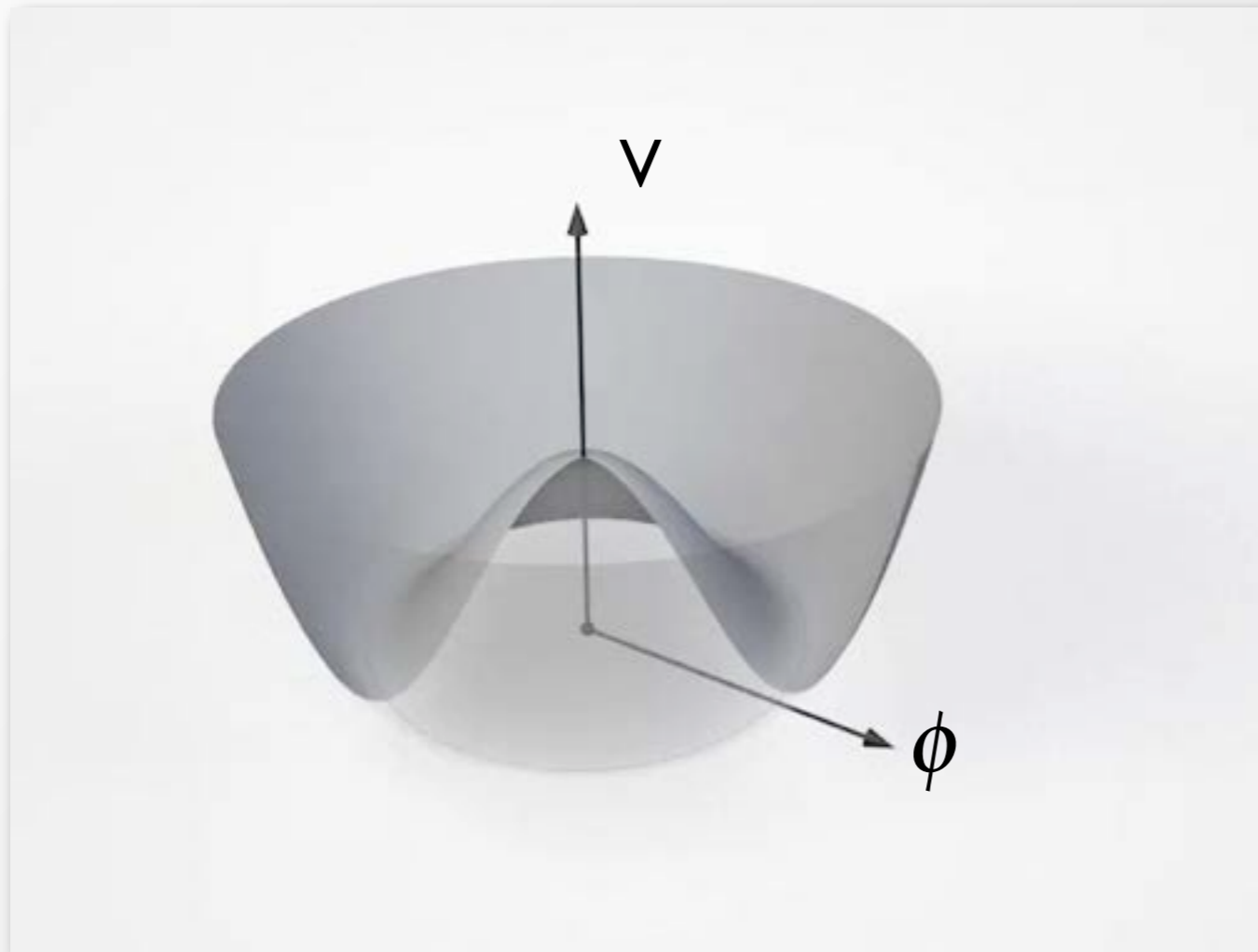
$$j = J/U$$

Amplitude Modulation of Lattice

Bragg spectroscopy: couples mainly to phonons

Exp.: Ch. Schori et al. Phys. Rev. Lett. (2004) (ETHZ), Theory: C. Kollath et al., Phys. Rev. Lett (2006)
U. Bissbort et al. Phys. Rev. Lett. (2011) (Frankfurt, Hamburg)





Modulate coupling strength
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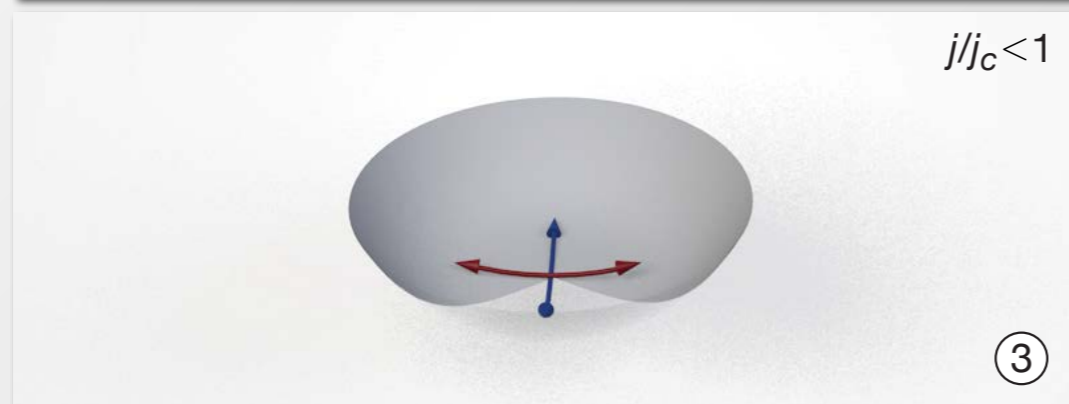
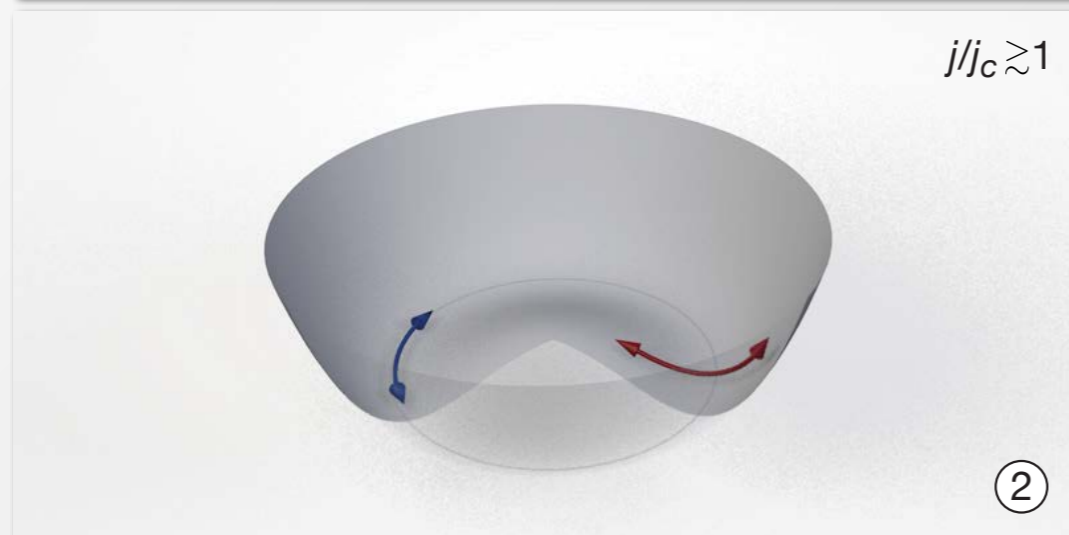
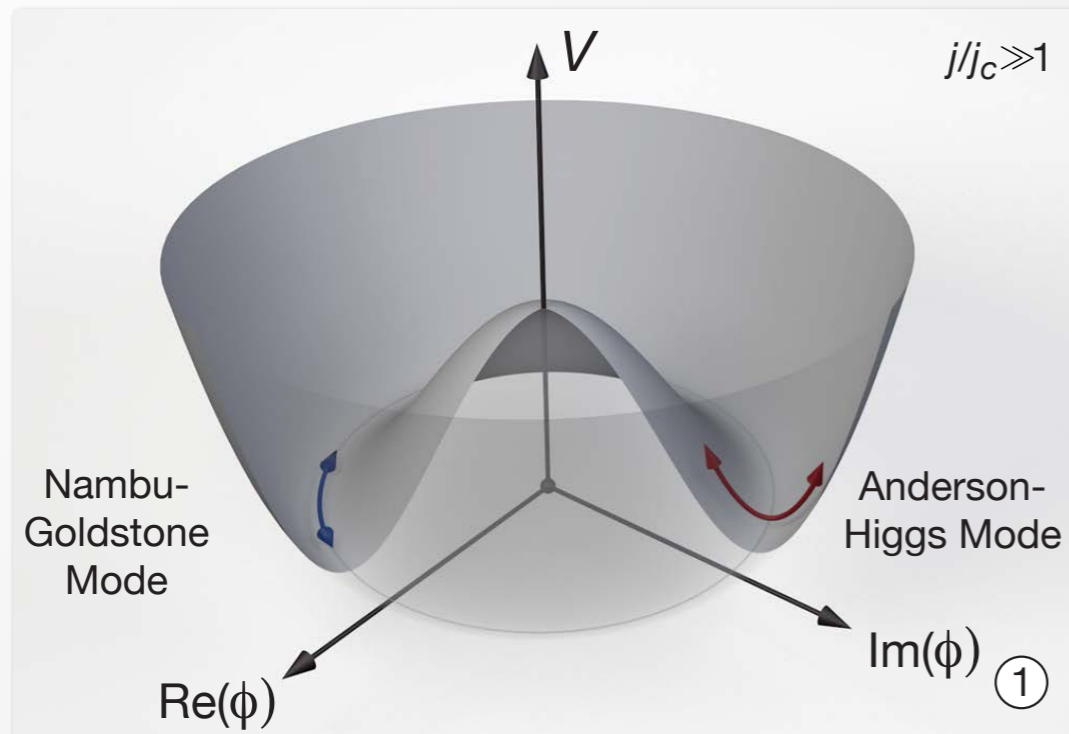
Amplitude Modulation of Lattice

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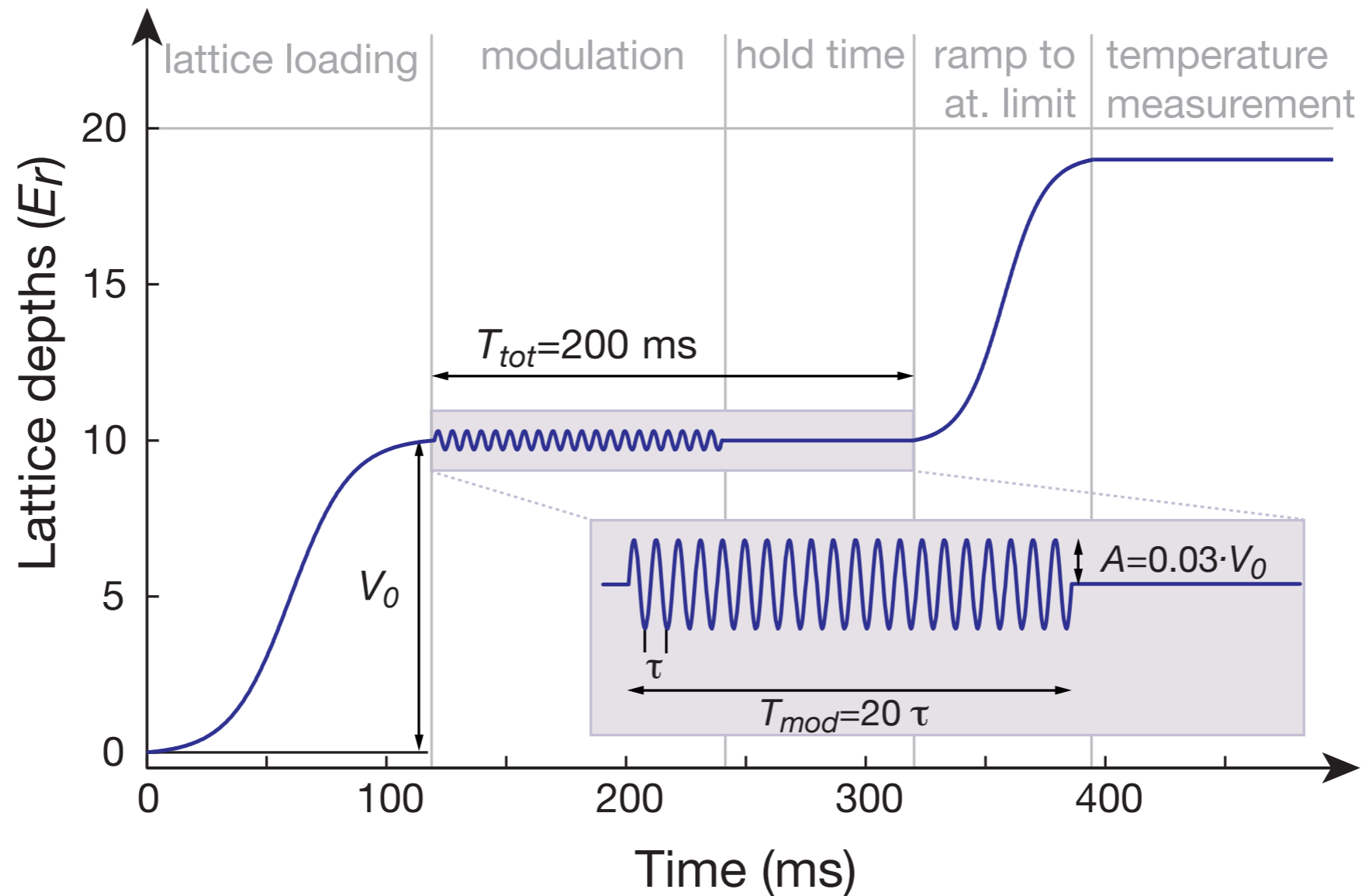
U. Bissbort et al. Phys. Rev. Lett. (2011) (Frankfurt, Hamburg)





Higgs mode softens towards critical point!



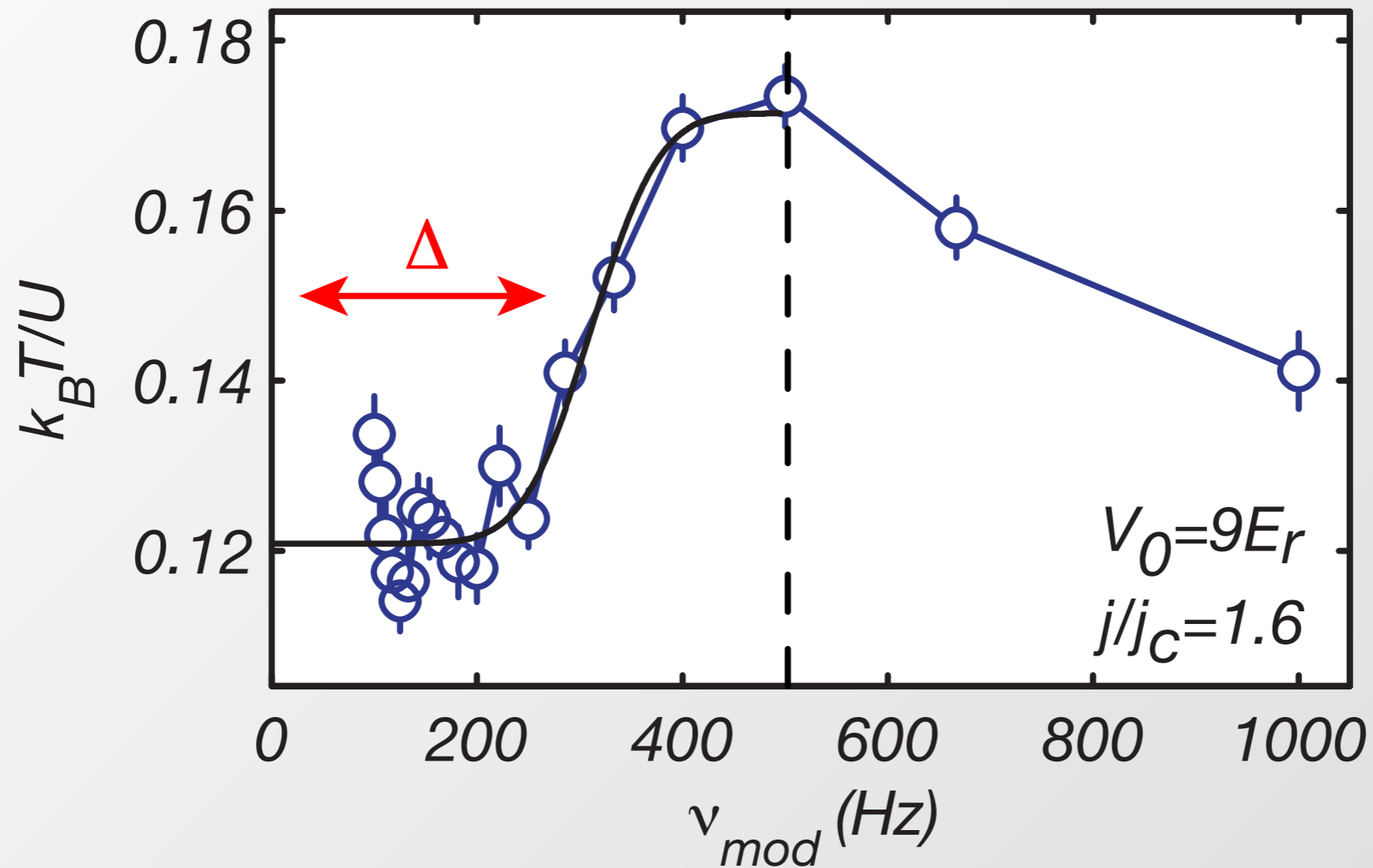


Absorbed energy

$$E = 2\pi(\delta J)^2 S(\omega) \omega T_{mod}$$

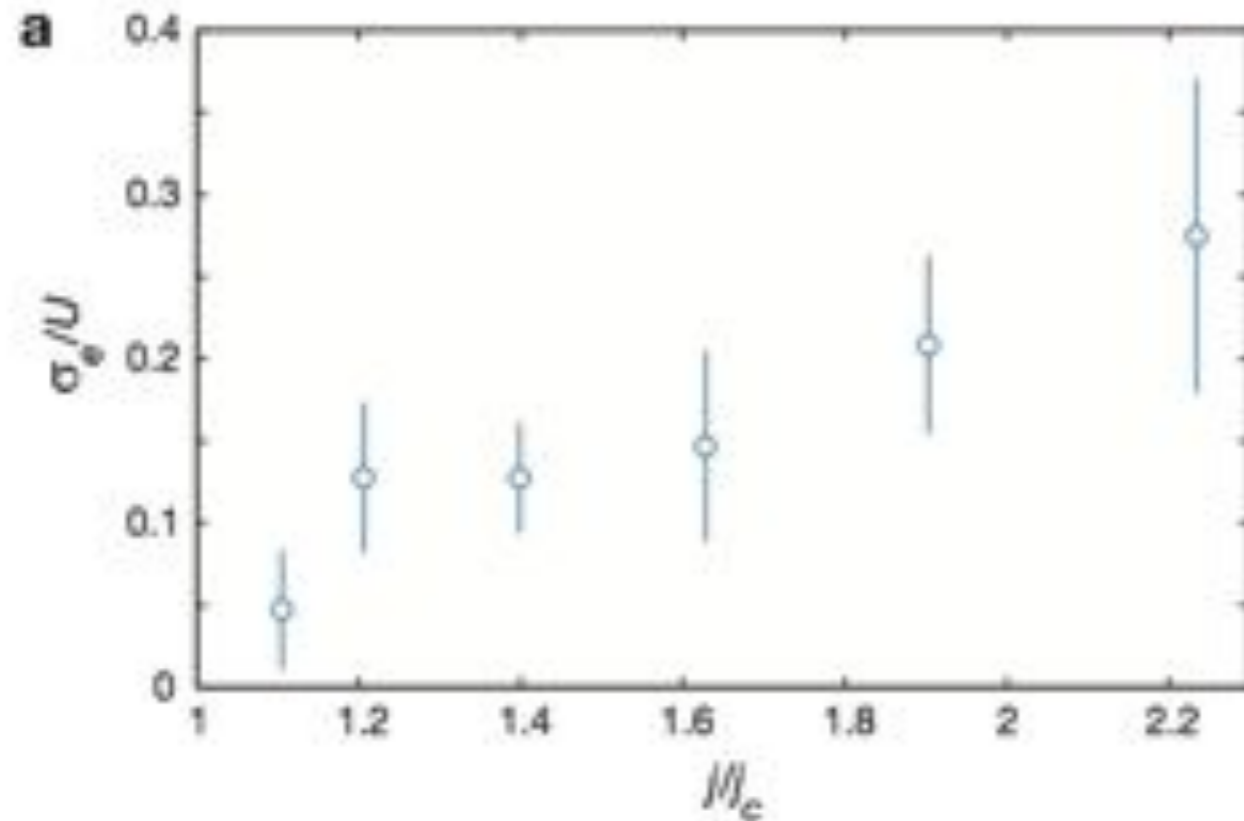
Very low modulation amplitude!

Very sensitive temperature measurement!

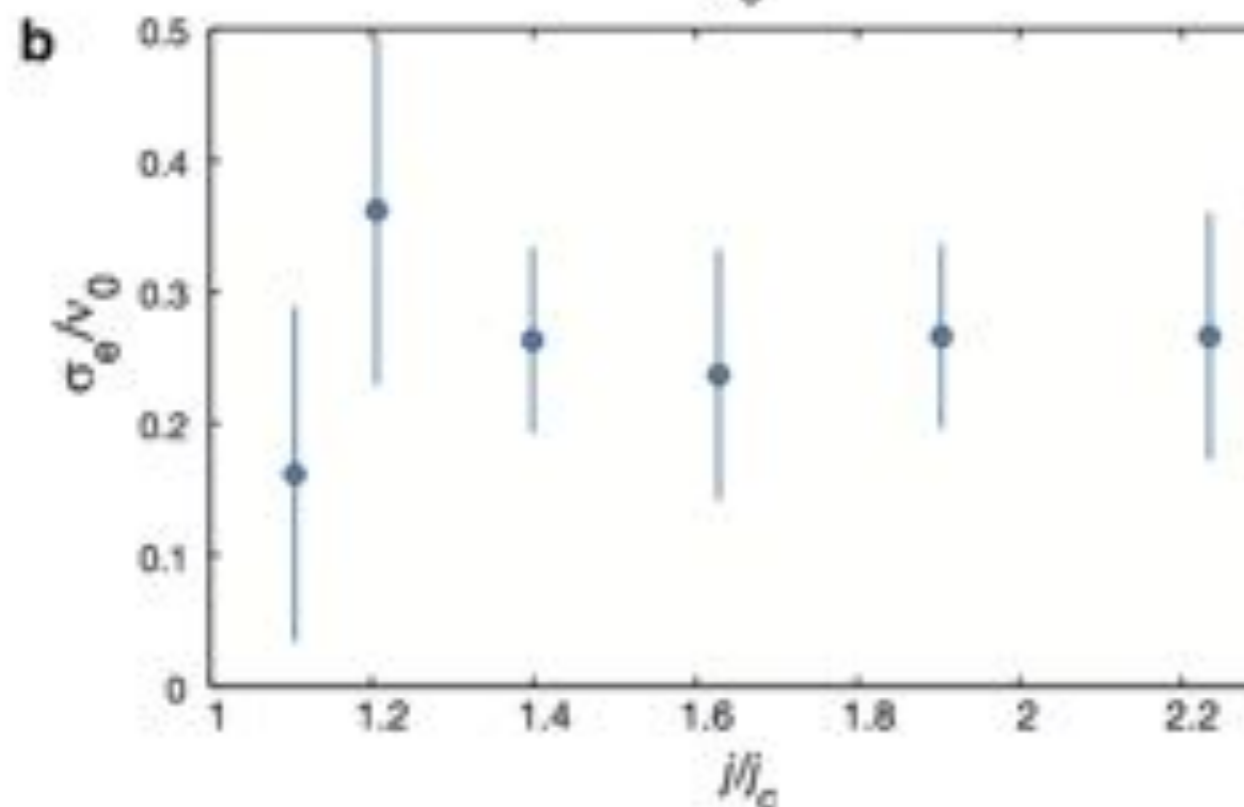


Use fit with error function to find **minimum excitation frequency!**
(also avoids inhomogeneous trap effects)





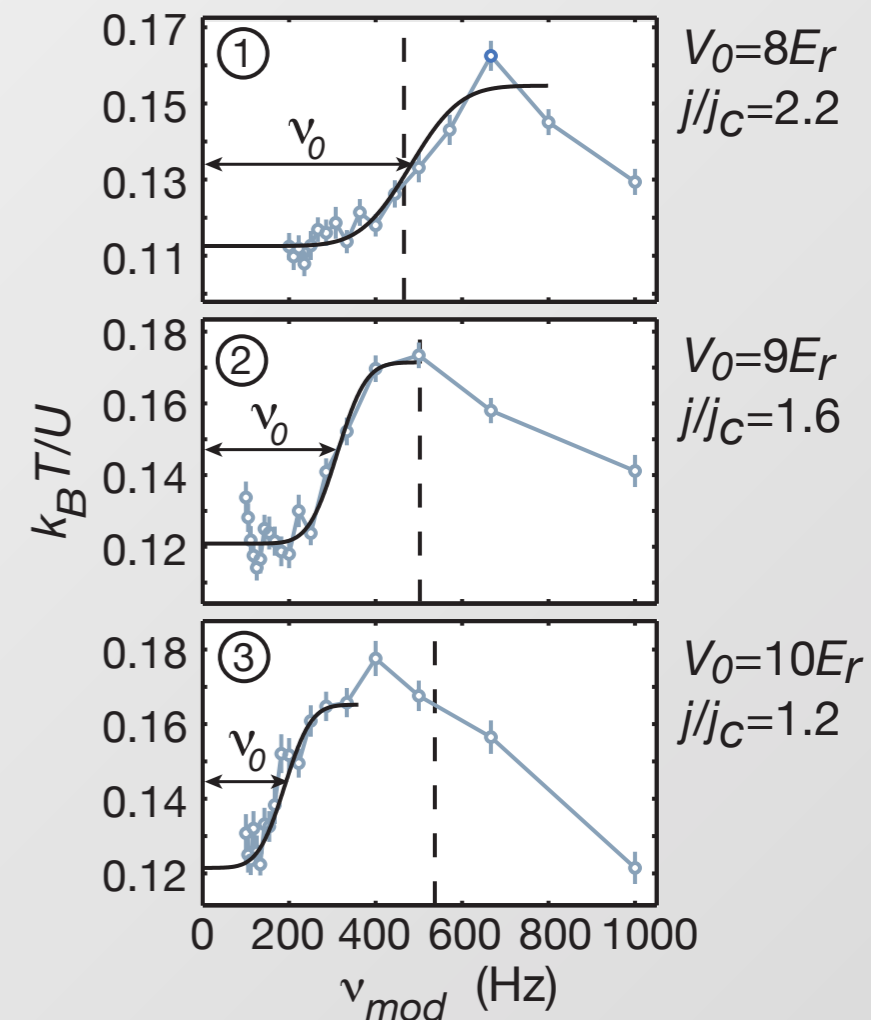
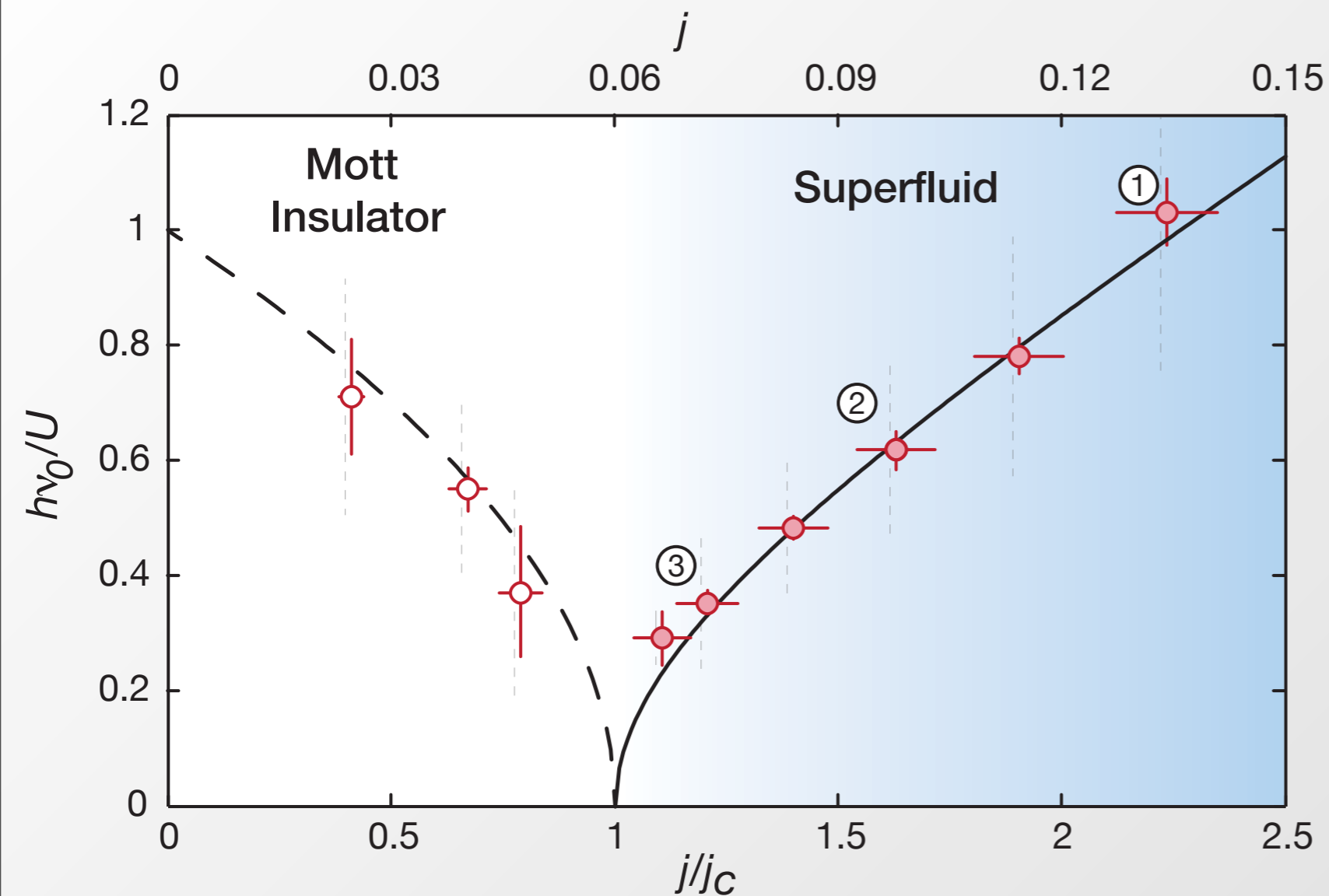
Width of model 'error' function



Ratio width vs resonance frequency

Mode remains well defined upon approaching the critical point!

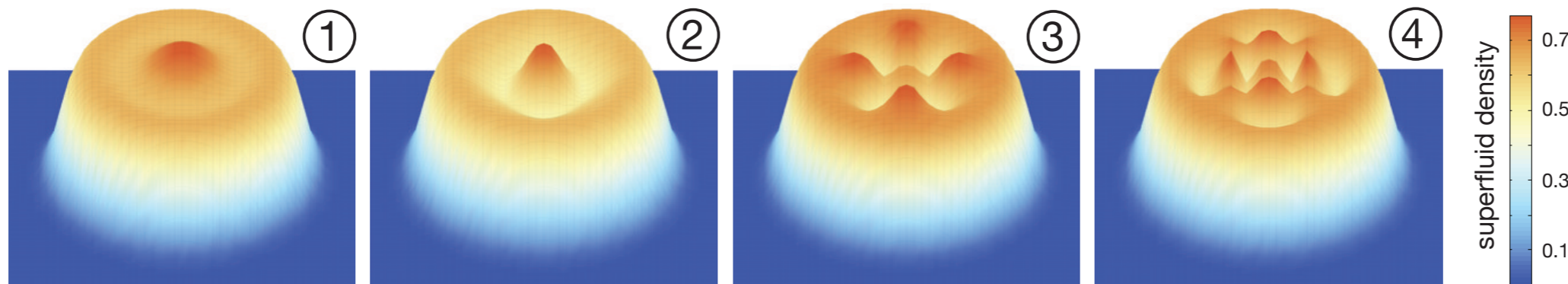
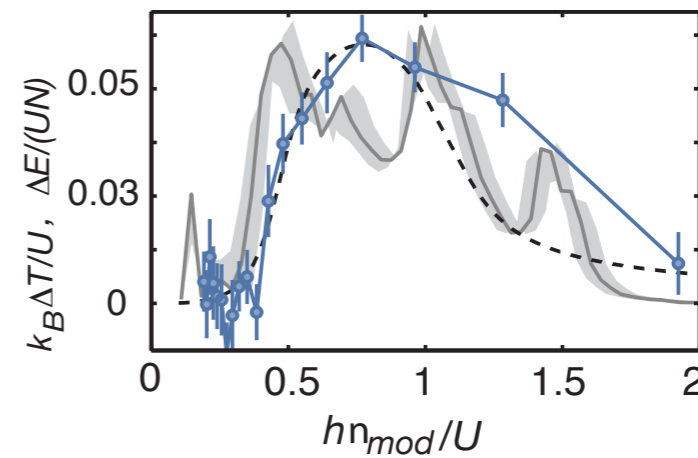
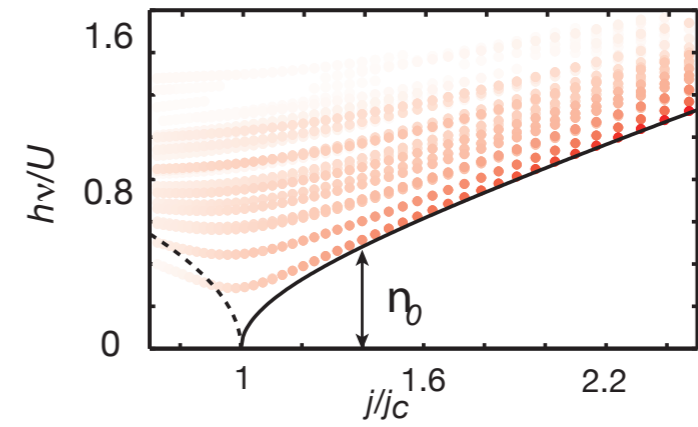
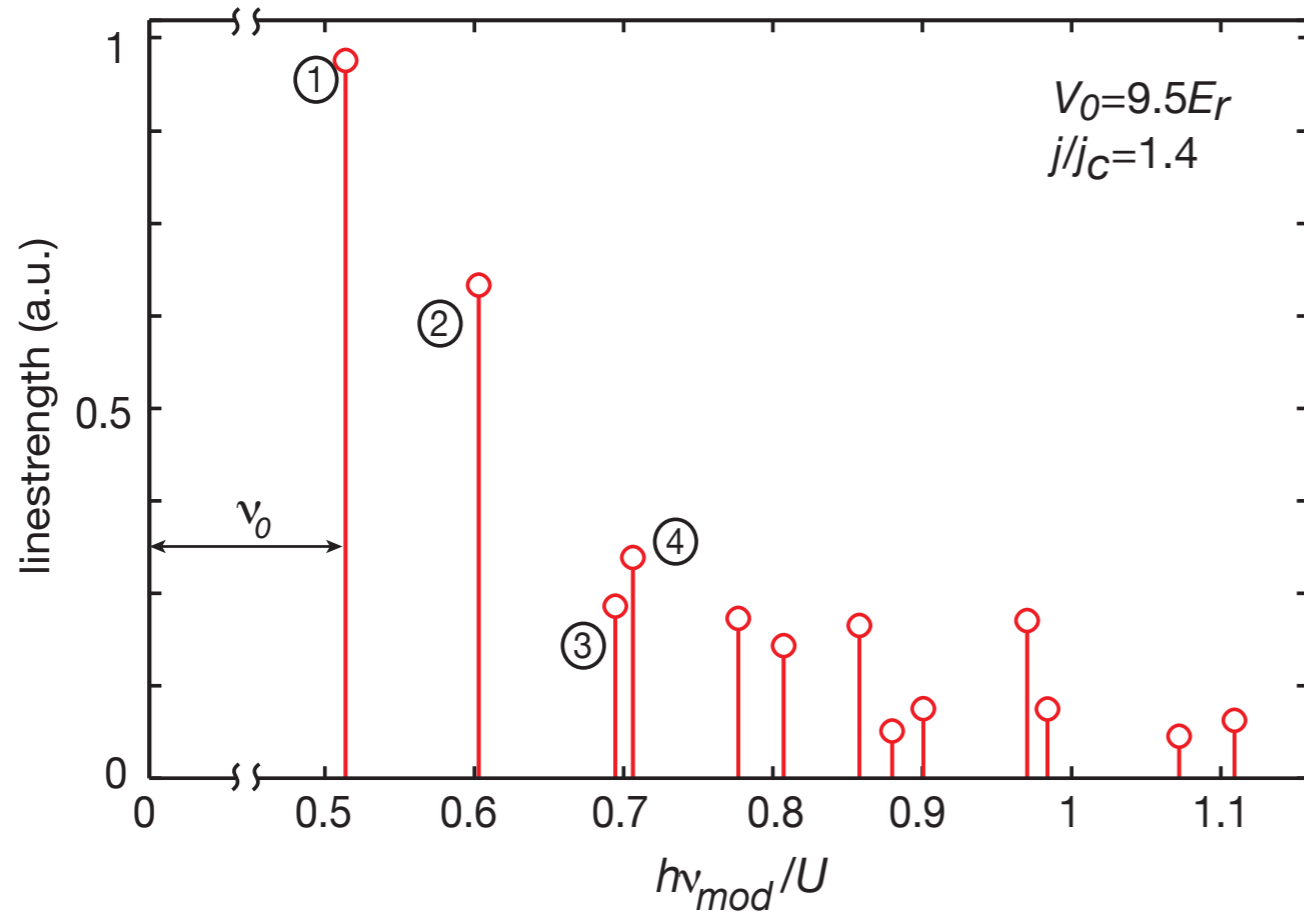




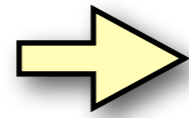
Anderson-Higgs mode softens towards critical point and turns into opening gap of Mott Insulator!

Theory in SF (S. Huber et al. PRB 2007) $\Delta_m = \sqrt{3\sqrt{2} - 4\sqrt{(j/j_c)^2 - 1}}$

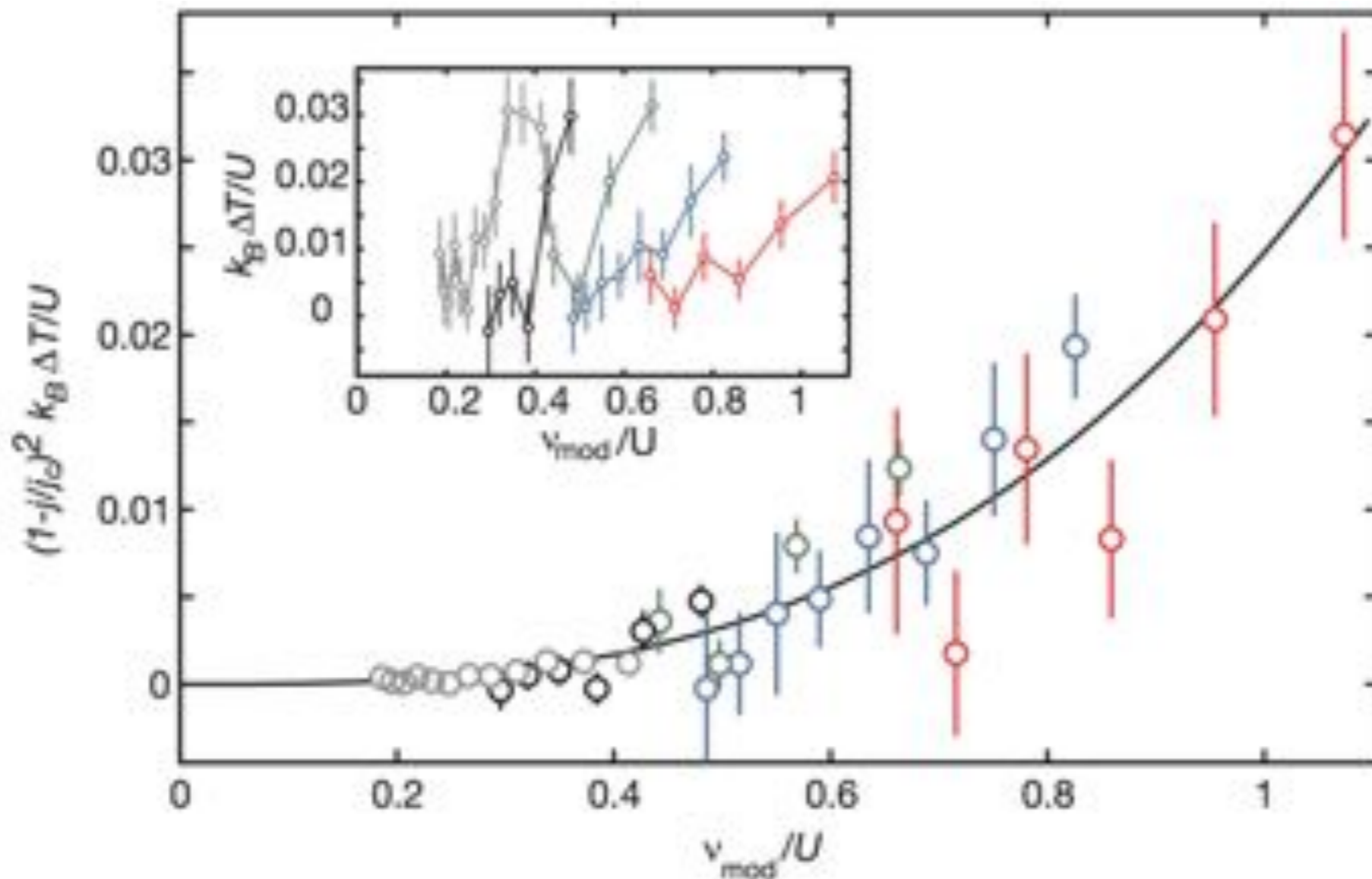




$$F\left(\nu, \frac{j}{j_c}\right)_u = A\Delta^{3-2/\nu_c}\Phi\left(\frac{\nu}{\Delta}\right)$$



$$F\left(\nu, \frac{j}{j_c}\right)_u = A\left(1 - \frac{j}{j_c}\right)^{-2}\nu^3$$



Fit Function

$$a\nu^b$$

we obtain

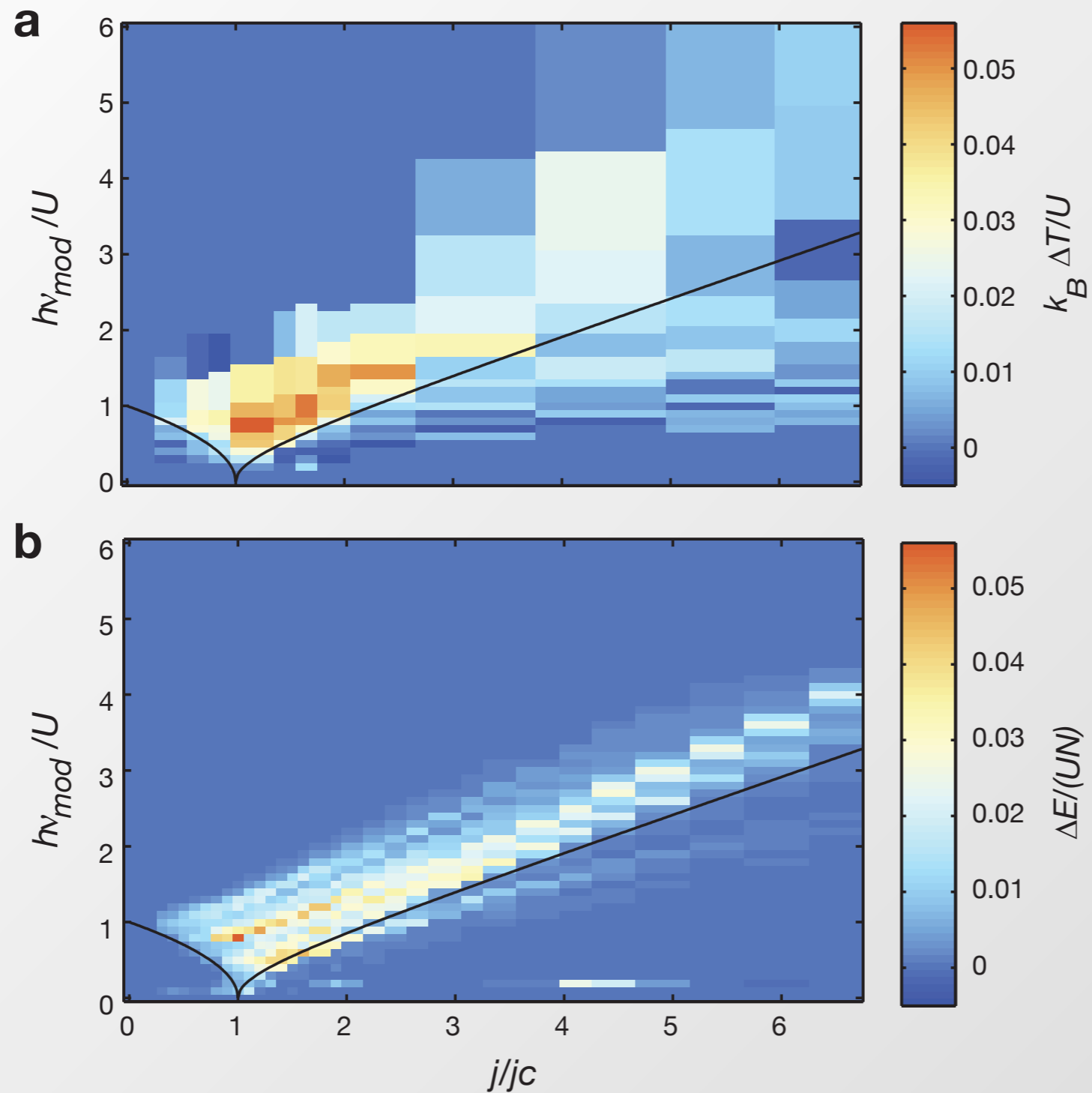
$$b = 2.9(5)$$

S. Sachdev. *Quantum Phase Transitions*. Cambridge University Press, Cambridge, (2011)

D. Podolsky, A. Auerbach, and D. P. Arovas. *Phys. Rev. B* **84**, 174522 (2011)

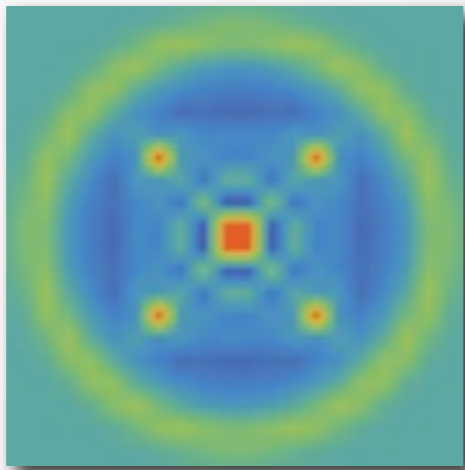
D. Podolsky and S. Sachdev, *Phys. Rev. B* **86**, 054508 (2012)





Open theory question: what is the fate of Higgs mode towards weaker interactions?

- ✓ Selectively excite Higgs eigenmodes (larger system, spatial modulation)
- ✓ Probe Quantum Critical behaviour via Dynamical critical scaling



Higgs drum, spatial eigenmodes!

- ✓ Fate of mode at weaker interactions (towards GPE)
- ✓ Ratio of 'Higgs' mass to Mott gap
- ✓ Well defined mode down to critical point?
- ✓ Anderson-Higgs Mechanism via Coupling to (Dynamical) Gauge Field

Generation of Large Effective Magnetic Fields

M. Aidelsburger, M. Atala, S. Nascimbène, Yu-Ao Chen & I. Bloch

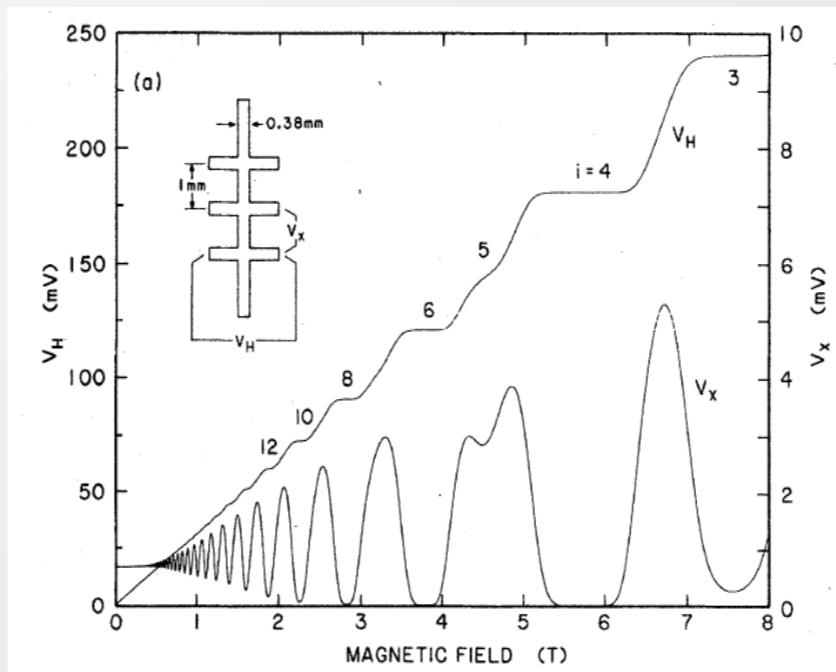
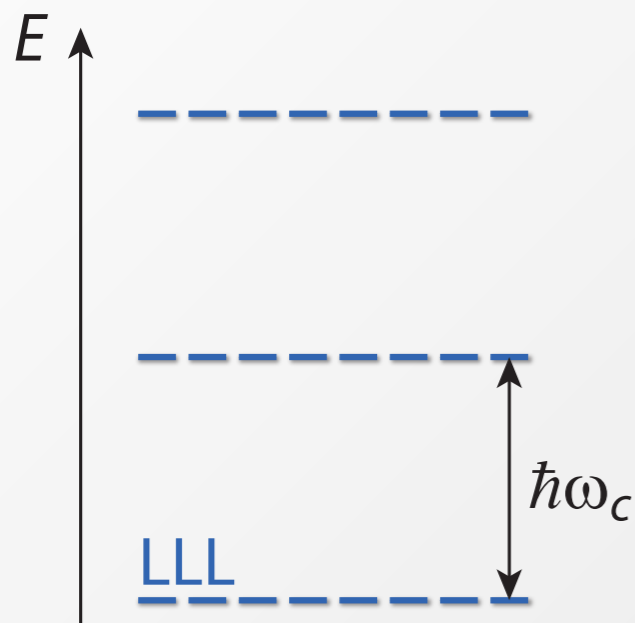
M. Aidelsburger et al. PRL 107, 255301 (2011)

D. Jaksch & P. Zoller NJP (2003), F. Gerbier & J. Dalibard NJP (2010)



www.quantum-munich.de

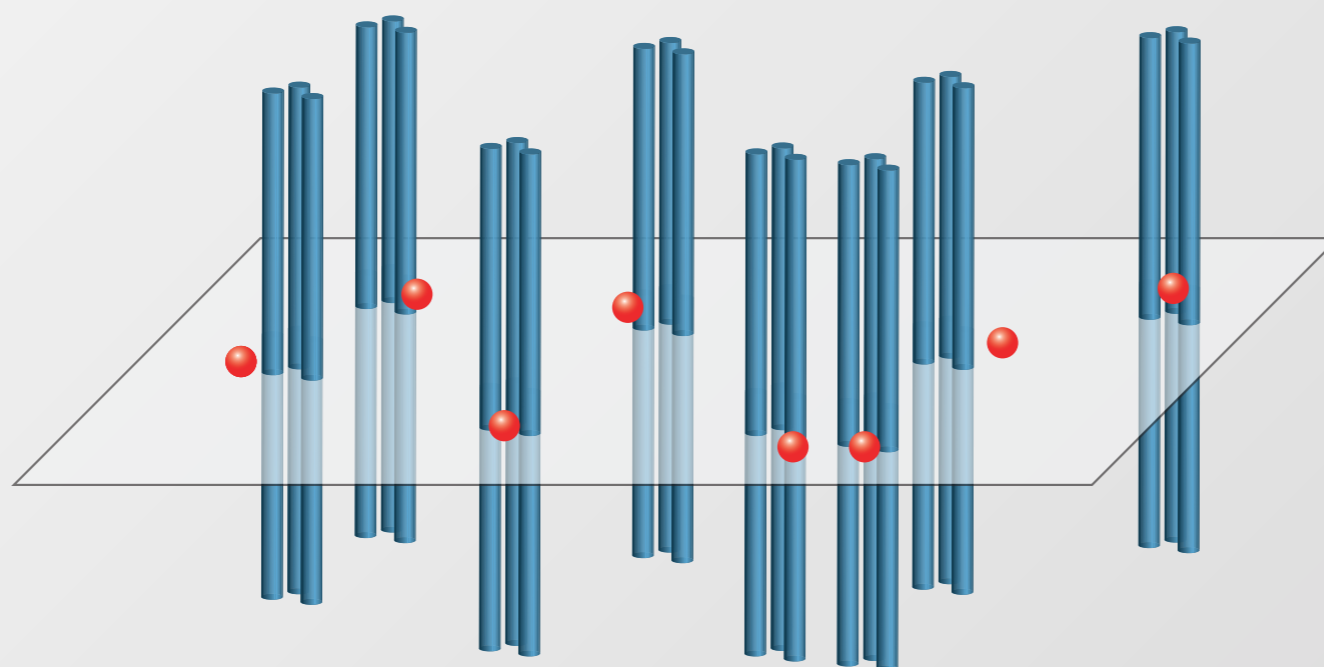
Integer Quantum Hall Effect



$$\sigma_{xy} = \nu e^2 / h$$

ν Integer

Fractional Quantum Hall Effect



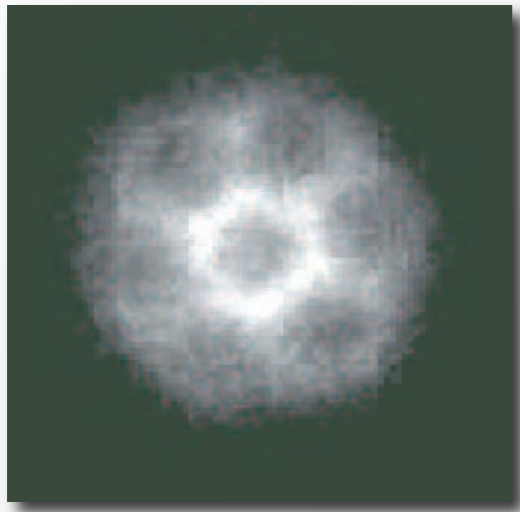
Laughlin state at $\nu = 1/3$

flux quantum $\phi_0 = h/ec$

electron



1) Rotation



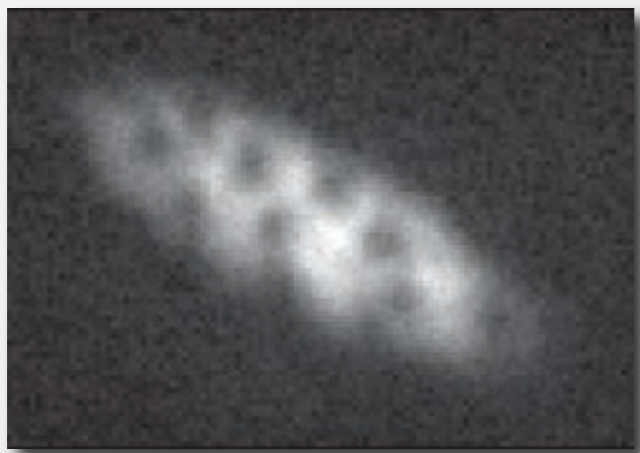
In rapidly rotating gases, **Coriolis force** is equivalent to **Lorentz force**.

$$\mathbf{F}_L = q \mathbf{v} \times \mathbf{B} \longleftrightarrow \mathbf{F}_C = 2m \mathbf{v} \times \boldsymbol{\Omega}_{\text{rot}}$$

K. Madison *et al.*, PRL (2000)

J.R. Abo-Shaeer *et al.* Science (2001)

2) Raman Induced Gauge Fields

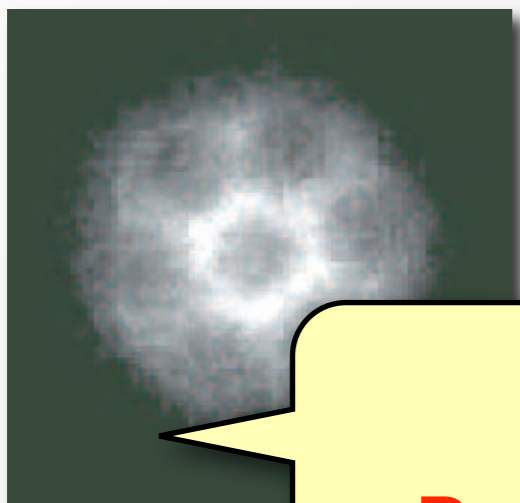


Spatially dependent optical couplings lead to a **Berry phase** analogous to the **Aharonov-Bohm phase**

Y. Lin *et al.*, Nature (2009)



1) Rotation



In rapidly rotating gases, **Coriolis force** is equivalent to **Lorentz force**.

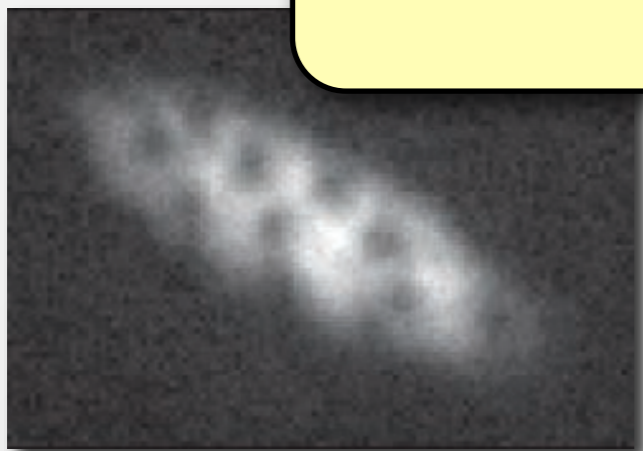
$$\mathbf{v} \times \boldsymbol{\Omega}_{\text{rot}}$$

t al., PRL (2000)

. Science (2001)

Problem in both cases: small B-fields
(large $v > 1000$ for now), heating...

2) Raman



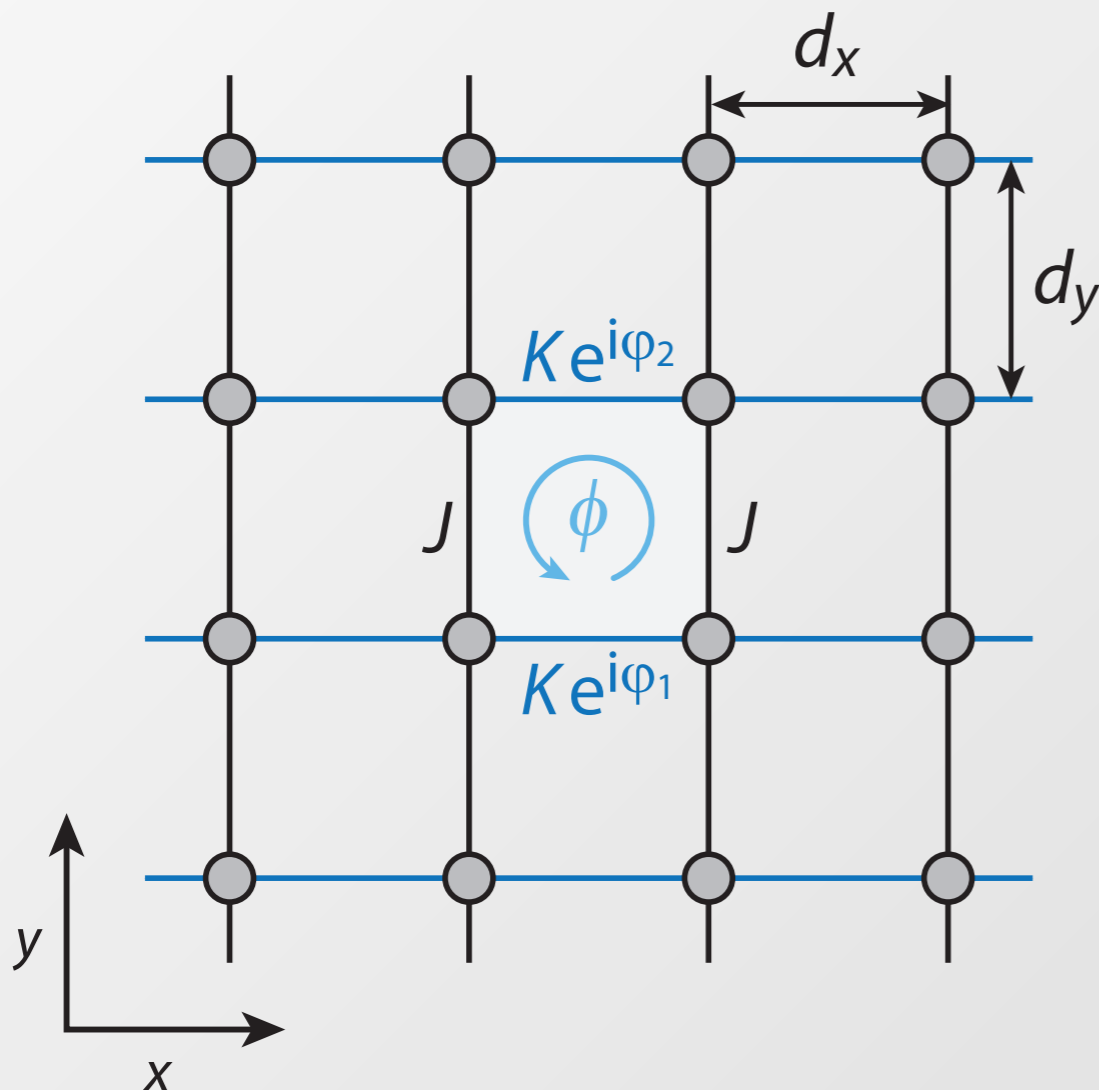
Spatially dependent optical couplings lead to a **Berry phase** analogous to the **Aharonov-Bohm phase**

Y. Lin *et al.*, Nature (2009)



Controlling atom tunneling along x with Raman lasers leads to **effective tunnel coupling** with **spatially-dependent Peierls phase** $\varphi(\mathbf{R})$

$$\hat{H} = - \sum_{\mathbf{R}} \left(K e^{i\varphi(\mathbf{R})} \hat{a}_{\mathbf{R}}^\dagger \hat{a}_{\mathbf{R}+\mathbf{d}_x} + J \hat{a}_{\mathbf{R}}^\dagger \hat{a}_{\mathbf{R}+\mathbf{d}_y} \right) + \text{h.c.}$$



Magnetic flux through a plaquette:

$$\phi = \int_{\square} B dS = \varphi_1 - \varphi_2$$

D. Jaksch & P. Zoller, *New J. Phys.* (2003)

F. Gerbier & J. Dalibard, *New J. Phys.* (2010)

E. Mueller, *Phys. Rev. A* (2004)

L.-K. Lim et al. *Phys. Rev. A* (2010)

A. Kolovsky, *Europhys. Lett.* (2011)

see also: lattice shaking

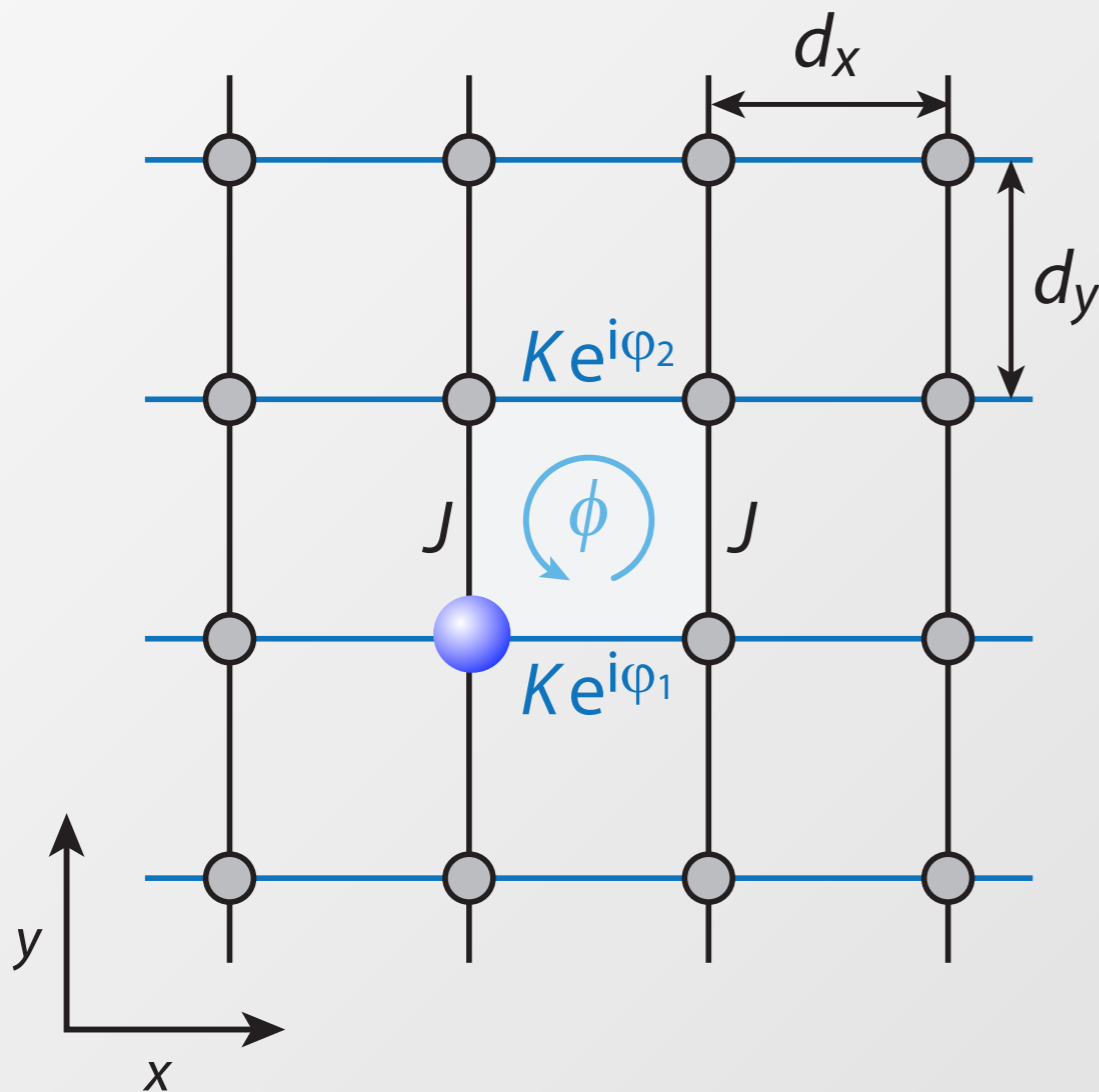
E. Arimondo, *Phys. Rev. Lett.* (2007)

K. Sengstock, *Science* (2011)



Controlling atom tunneling along x with Raman lasers leads to **effective tunnel coupling** with **spatially-dependent Peierls phase** $\varphi(\mathbf{R})$

$$\hat{H} = - \sum_{\mathbf{R}} \left(K e^{i\varphi(\mathbf{R})} \hat{a}_{\mathbf{R}}^\dagger \hat{a}_{\mathbf{R}+\mathbf{d}_x} + J \hat{a}_{\mathbf{R}}^\dagger \hat{a}_{\mathbf{R}+\mathbf{d}_y} \right) + \text{h.c.}$$



Magnetic flux through a plaquette:

$$\phi = \int_{\square} B dS = \varphi_1 - \varphi_2$$

D. Jaksch & P. Zoller, *New J. Phys.* (2003)

F. Gerbier & J. Dalibard, *New J. Phys.* (2010)

E. Mueller, *Phys. Rev. A* (2004)

L.-K. Lim et al. *Phys. Rev. A* (2010)

A. Kolovsky, *Europhys. Lett.* (2011)

see also: lattice shaking

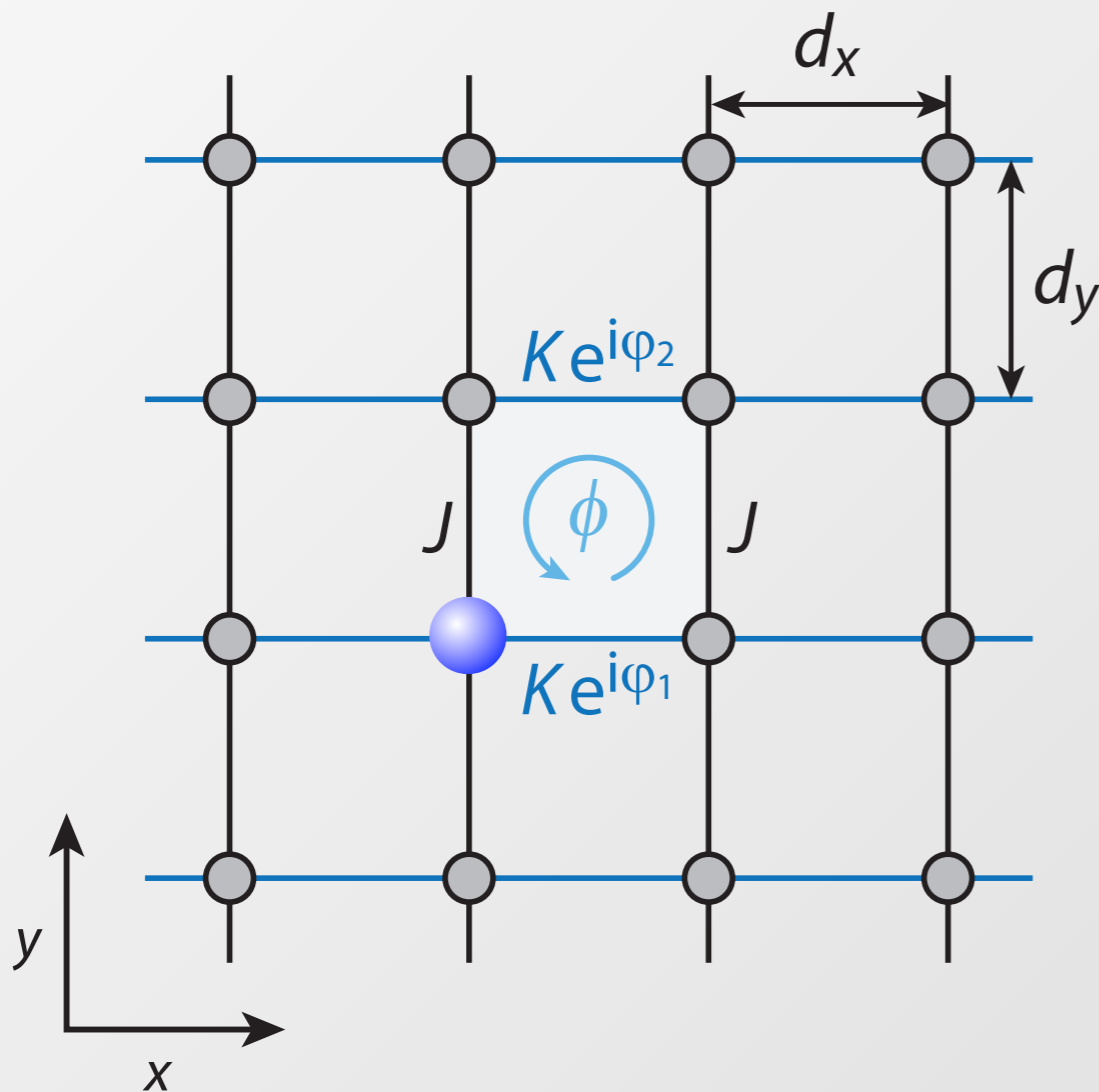
E. Arimondo, *Phys. Rev. Lett.* (2007)

K. Sengstock, *Science* (2011)



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A. Kolovsky, *Europhys. Lett.* (2011)

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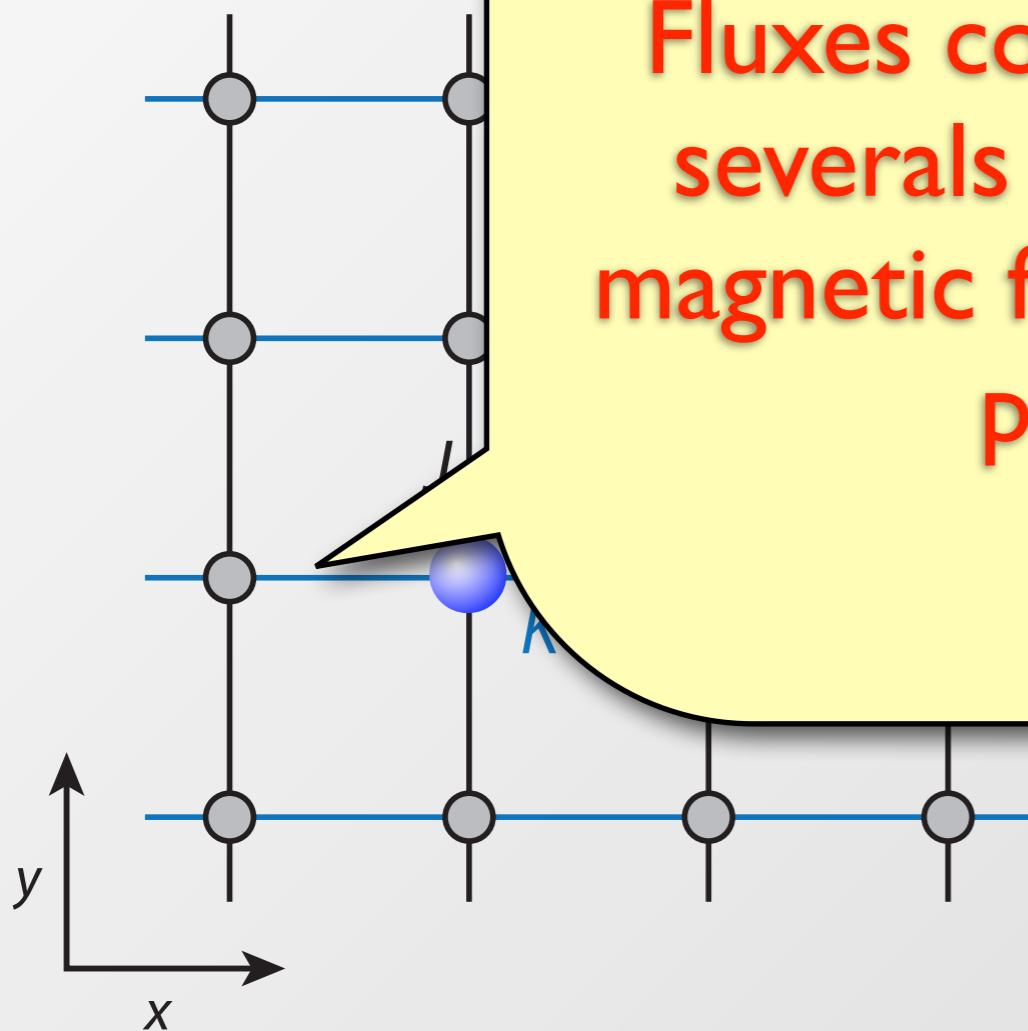
E. Arimondo, *Phys. Rev. Lett.* (2007)

K. Sengstock, *Science* (2011)



Controlling atom tunneling along x with Raman lasers leads to **effective tunnel coupling** with **spatially-dependent Peierls phase** $\varphi(\mathbf{R})$

$$\hat{H} = - \sum_{\mathbf{R}} (\dots) \text{h.c.}$$



Fluxes corresponding to several thousand Tesla magnetic field strength are possible!

through a plaquette:

$$S = \varphi_1 - \varphi_2$$

W. Ketterle & P. Zoller, New J. Phys. (2003)

J. Dalibard & J. Dalibard, New J. Phys. (2010)

E. Mueller, Phys. Rev. A (2004)

L.-K. Lim et al. Phys. Rev. A (2010)

A. Kolovsky, Europhys. Lett. (2011)

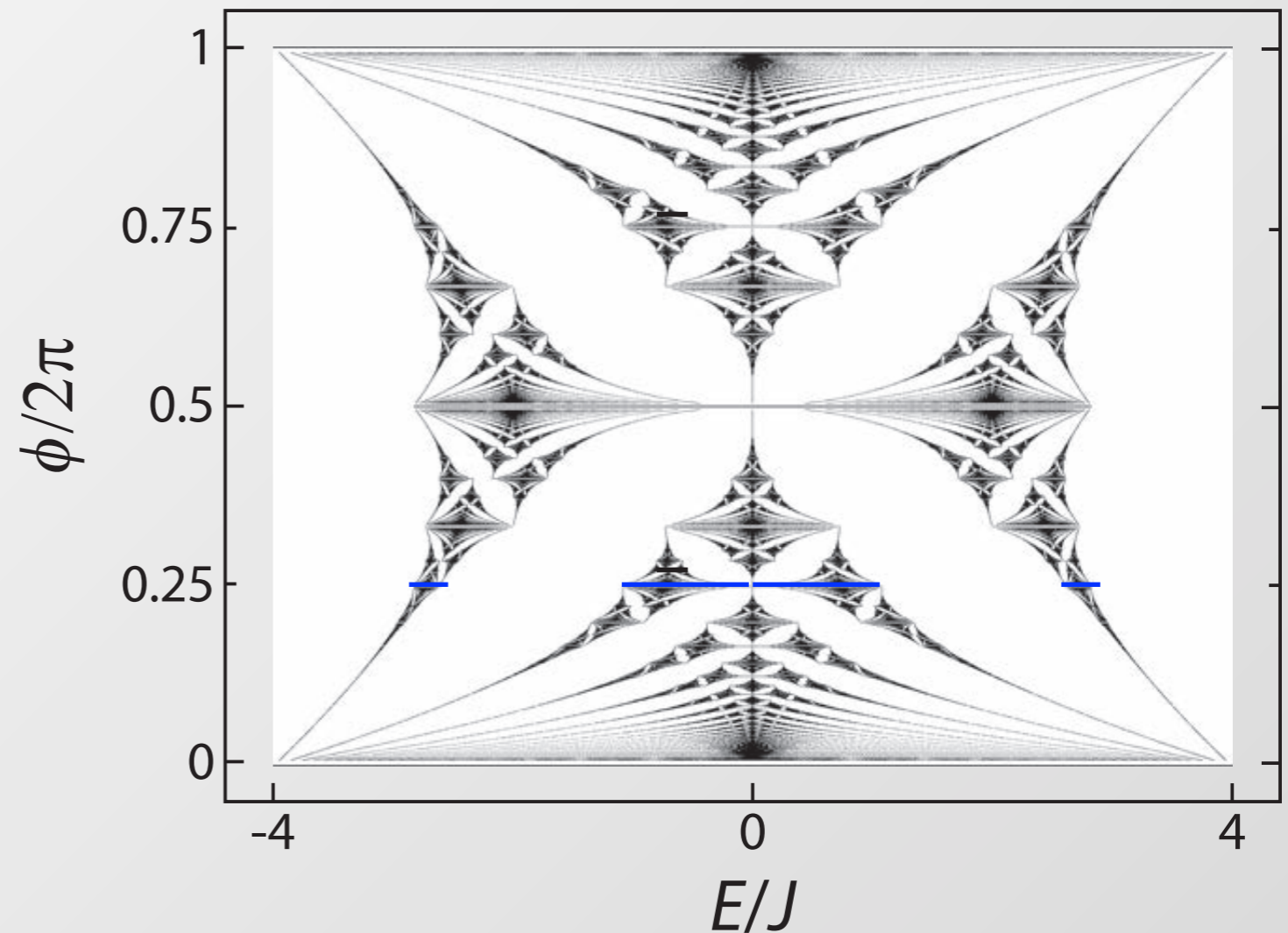
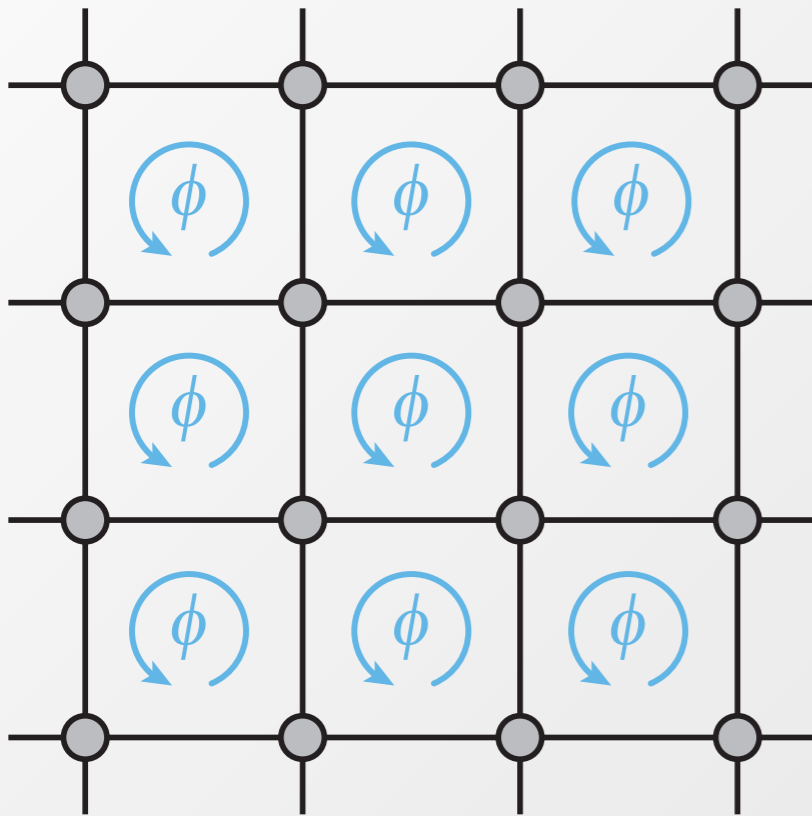
see also: lattice shaking

E. Arimondo, Phys. Rev. Lett (2007)

K. Sengstock, Science (2011)



Harper Hamiltonian: $J=K$ and ϕ uniform.



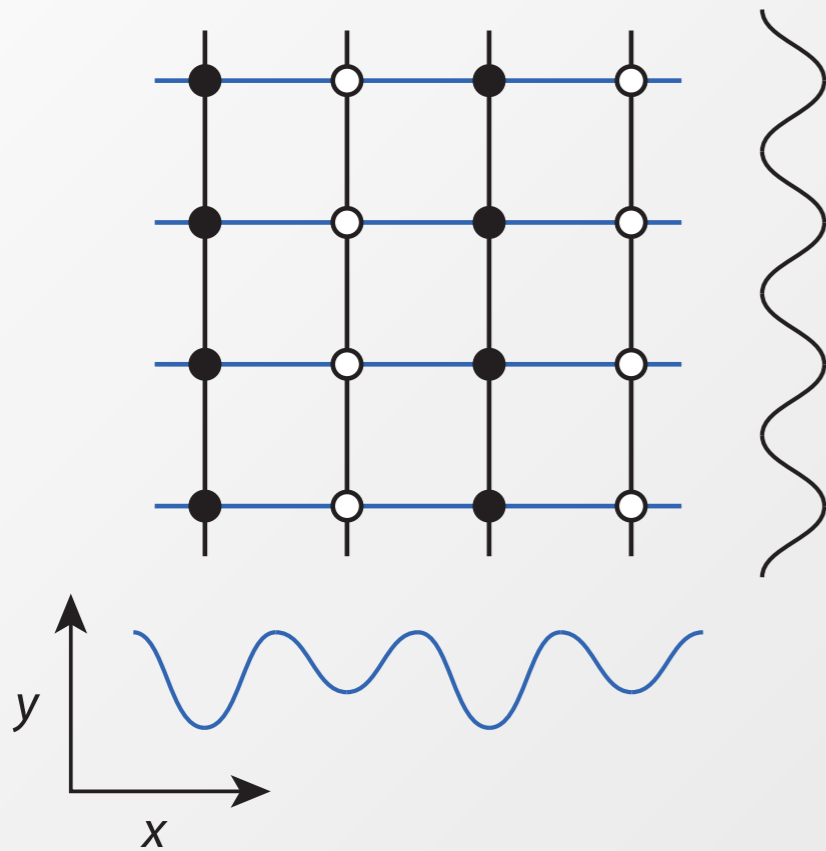
The lowest band is topologically equivalent to the lowest Landau level.

D.R. Hofstadter, Phys. Rev. B **14**, 2239 (1976)

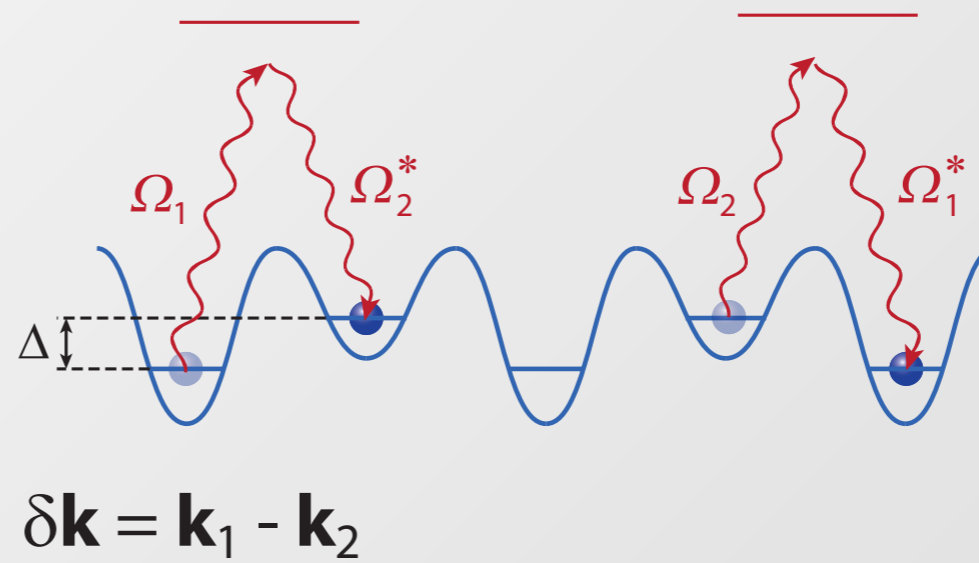
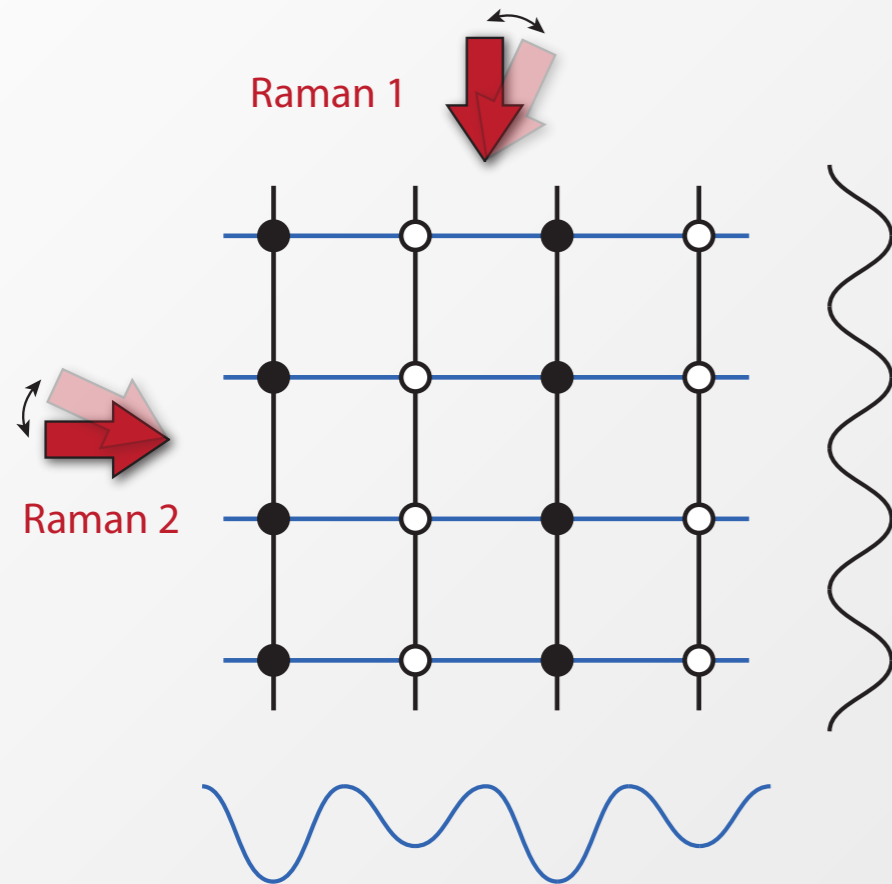
see also Y. Avron, D. Osadchy, R. Seiler, Physics Today **38**, 2003



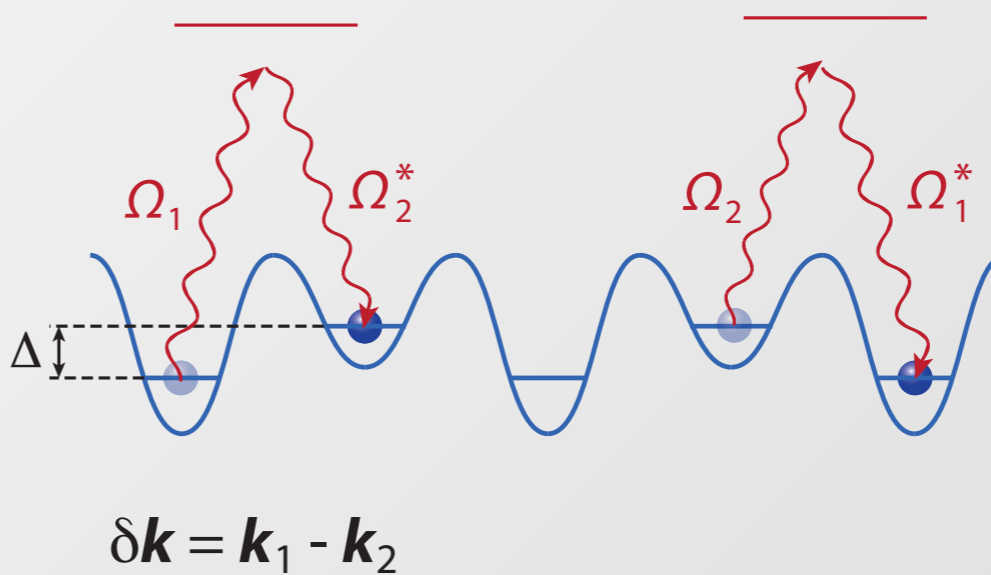
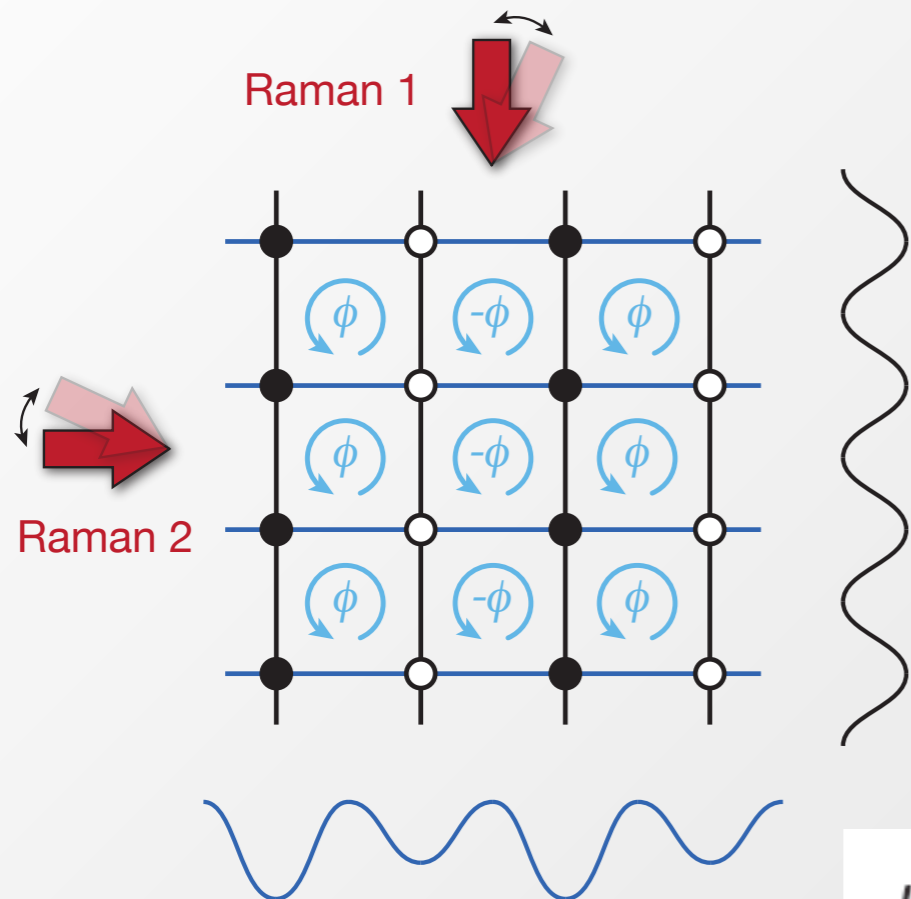
2D lattices - tunneling inhibited along the x-direction



Tunneling is restored with Raman beams

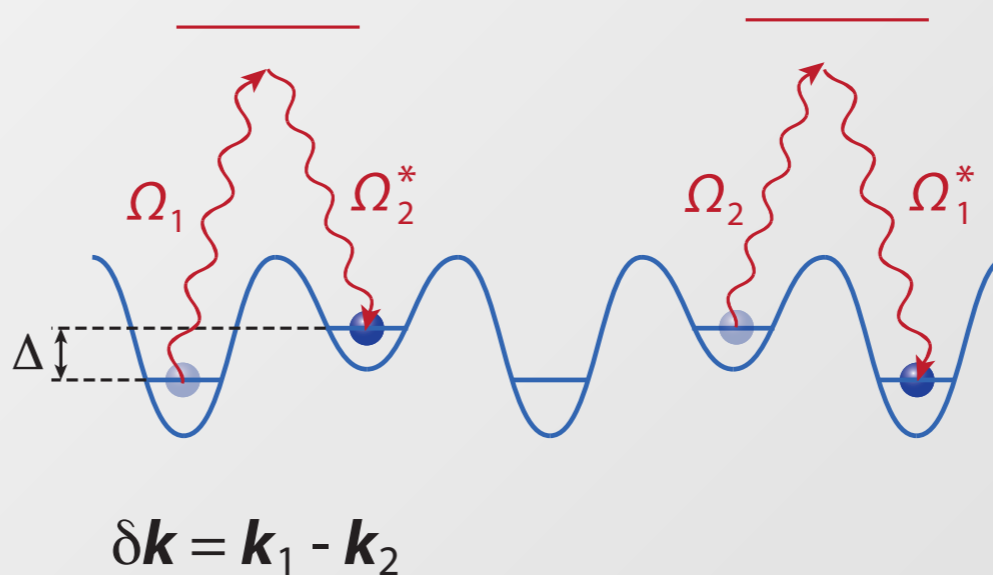
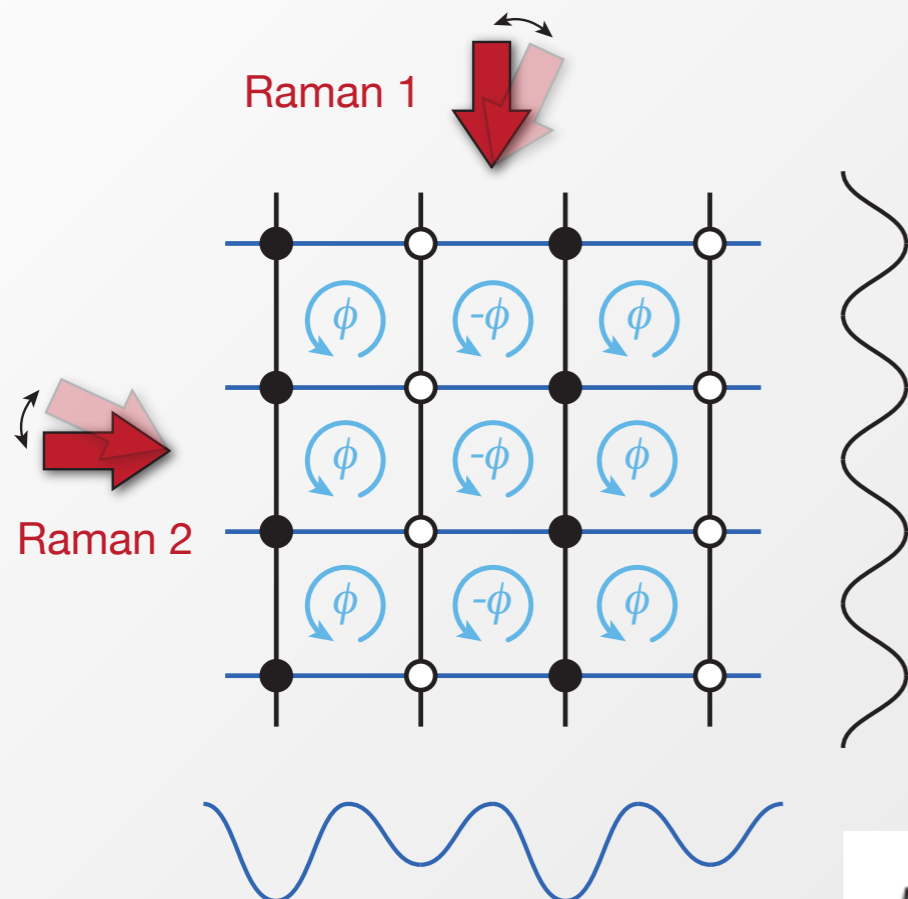


Staggered flux with zero mean



$$K_{|\bullet\rangle \rightarrow |o\rangle}(\mathbf{R}) = K e^{i\delta\mathbf{k} \cdot \mathbf{R}}, \quad K_{|o\rangle \rightarrow |\bullet\rangle}(\mathbf{R}') = K e^{-i\delta\mathbf{k} \cdot \mathbf{R}'}$$

Staggered flux with zero mean



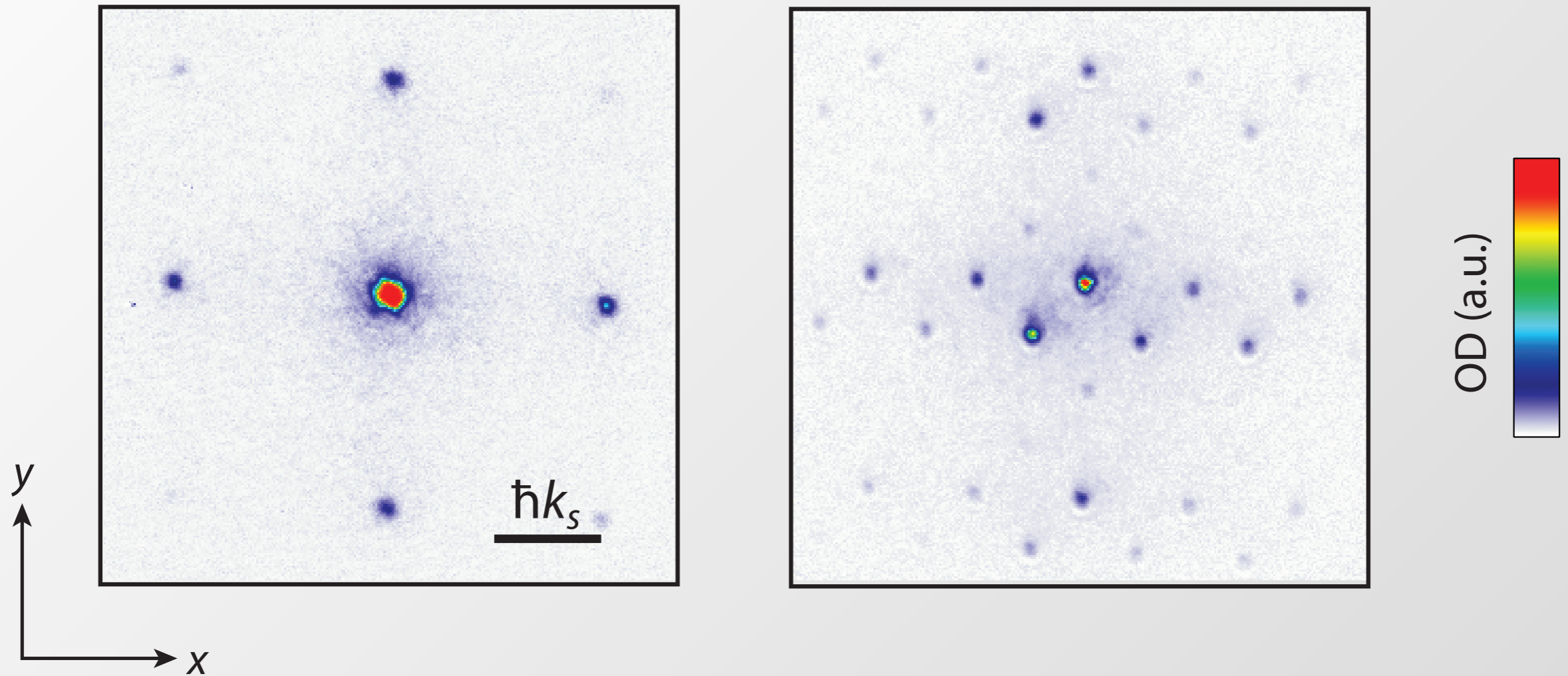
$$K_{|\bullet\rangle \rightarrow |o\rangle}(\mathbf{R}) = K e^{i\delta\mathbf{k} \cdot \mathbf{R}}, \quad K_{|o\rangle \rightarrow |\bullet\rangle}(\mathbf{R}') = K e^{-i\delta\mathbf{k} \cdot \mathbf{R}'}$$

From the geometry of the Raman lasers (angle 90° , wavelength $\lambda = 4d_x = 1534$ nm), we obtain:

$$\phi = \frac{\pi}{2}$$

Reference: cubic lattice
(no Raman drive)

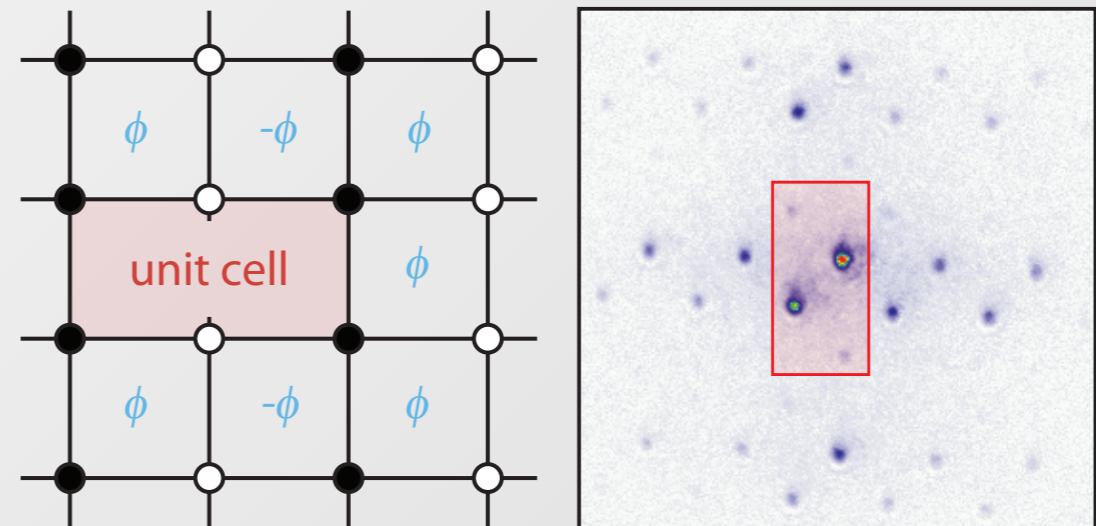
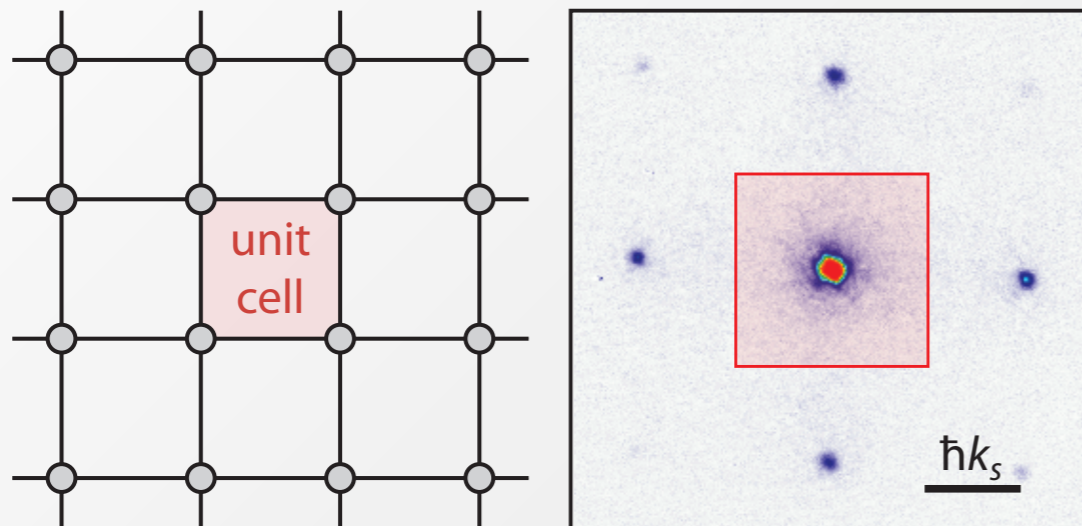
$J/K=1.0(1)$



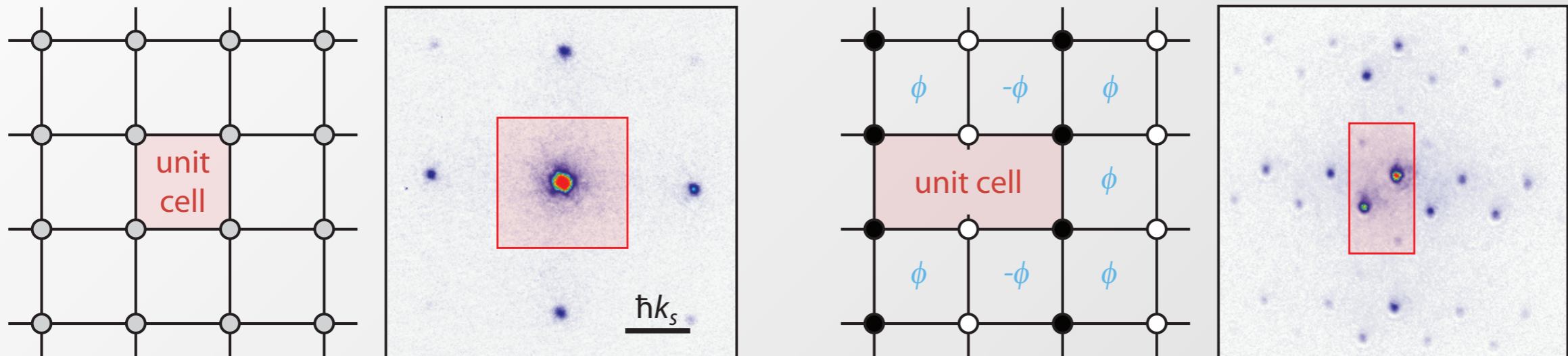
Due to the frustration introduced by the phase factors in $K(\mathbf{R})$, the condensation occurs at **non-zero momenta**.



Magnetic unit cell and Brillouin zone.



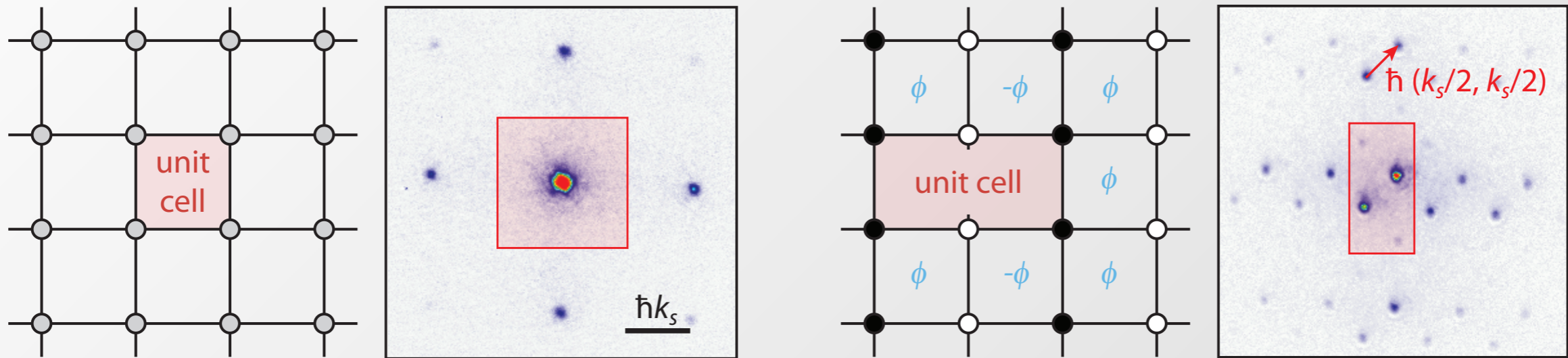
Magnetic unit cell and Brillouin zone.



Single-particle spectrum in the tight-binding approximation.
From the magnetic translation symmetries:

$$\psi_{|k_x, k_y\rangle}(\mathbf{R} = m\mathbf{d}_x + n\mathbf{d}_y) = e^{i(m \cdot k_x d_x + n \cdot k_y d_y)} \times \begin{cases} \psi_e & m \text{ even} \\ \psi_o e^{i\frac{\pi}{2}(m+n)} & m \text{ odd} \end{cases} ,$$

Magnetic unit cell and Brillouin zone.

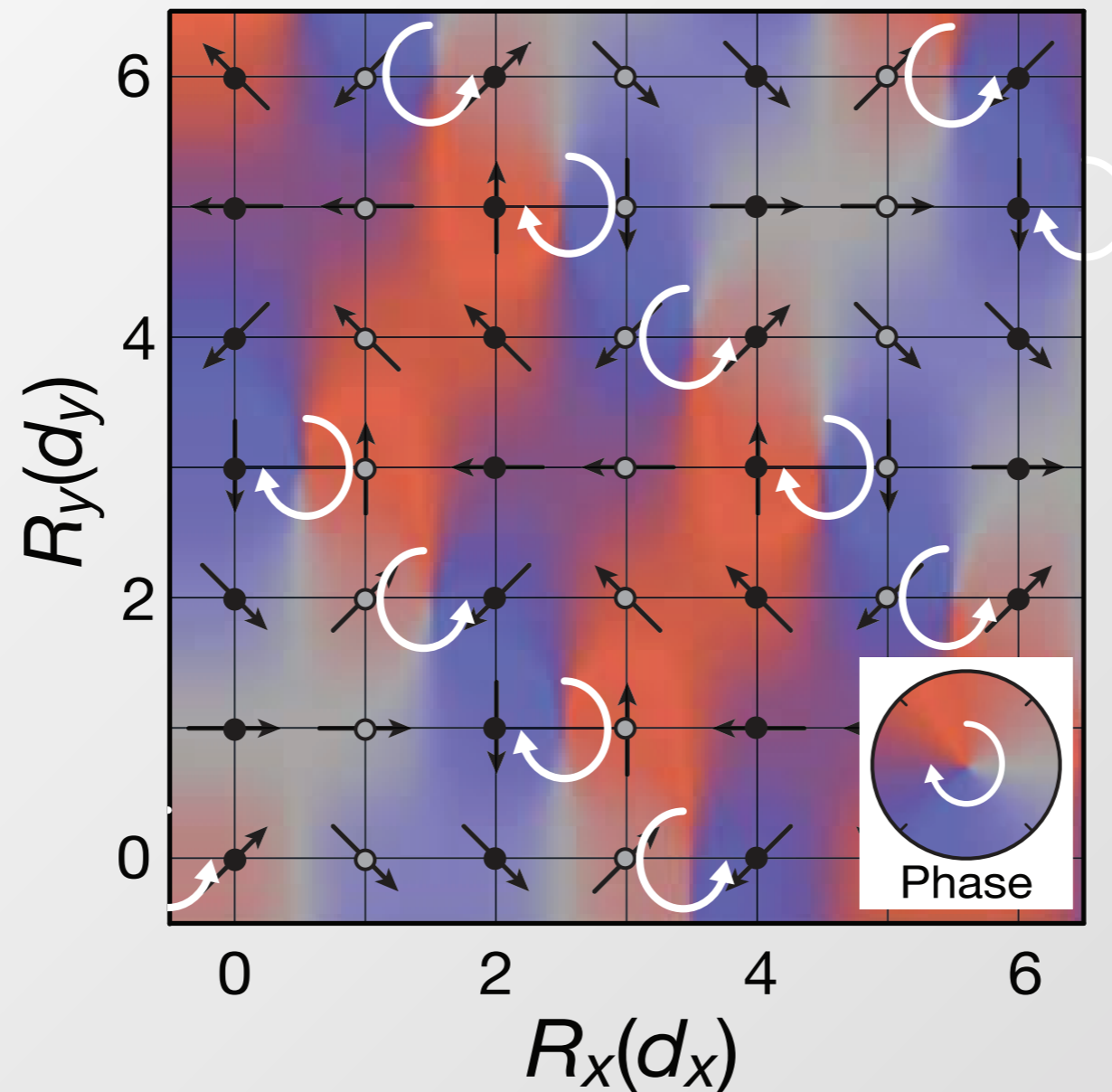


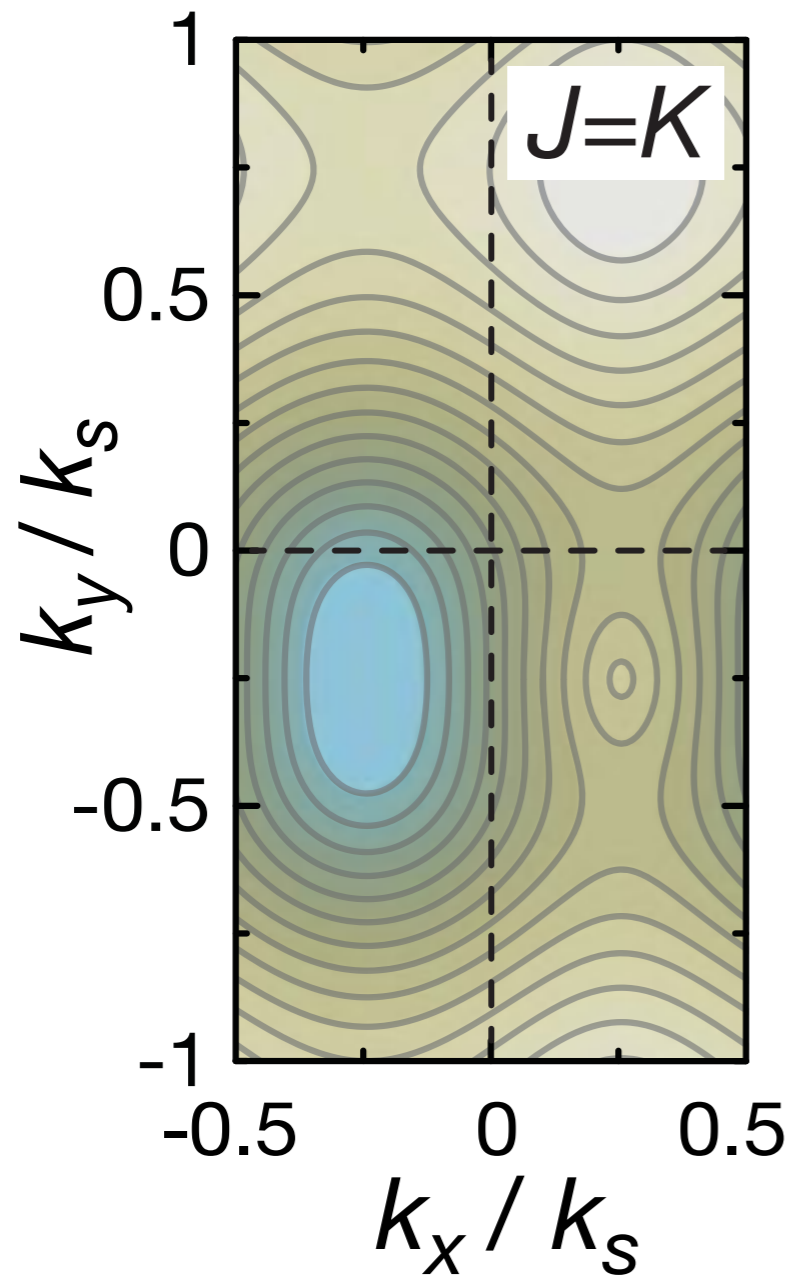
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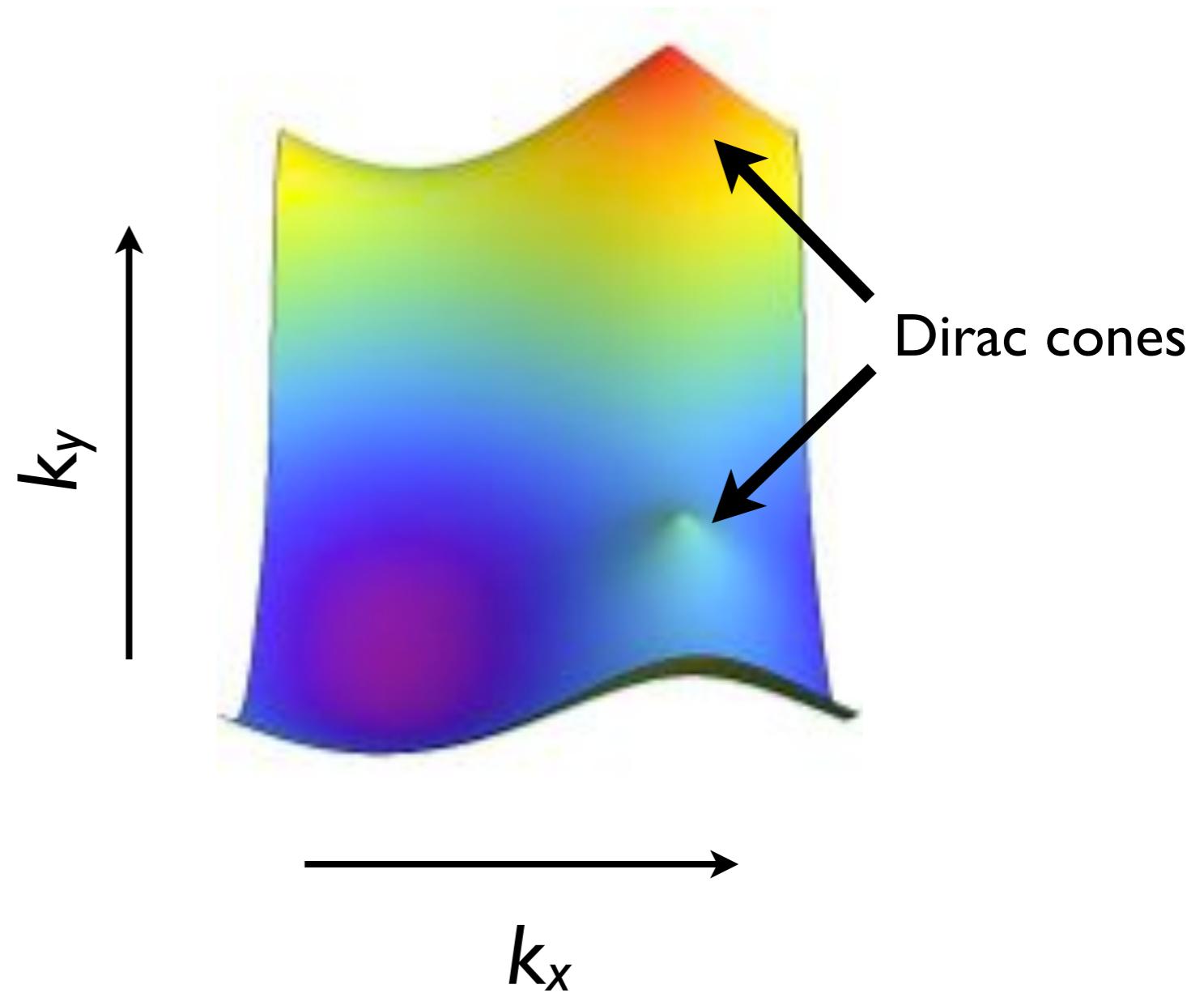
An eigenstate $|k_x, k_y\rangle$ has two momentum components

We consider again $J=K$.





Magnetic Brillouin Zone

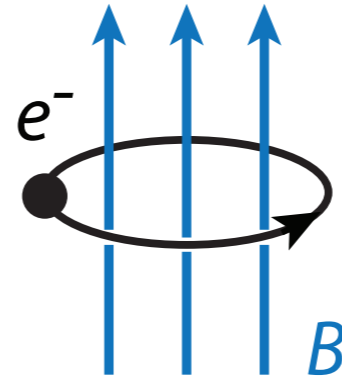


see hexagonal lattices: L.Tarruell et al. Nature (2012)



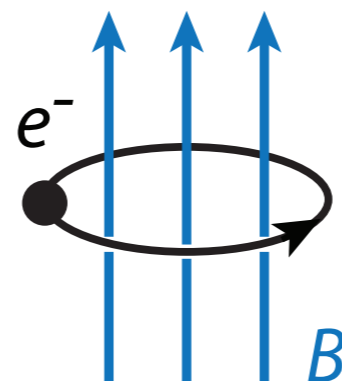
Classical:

Charged particle in magnetic field

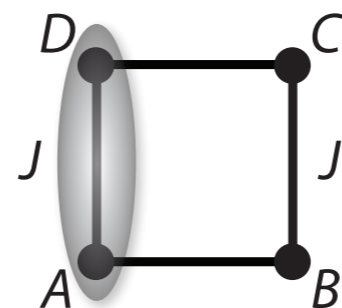


Classical:

Charged particle in magnetic field

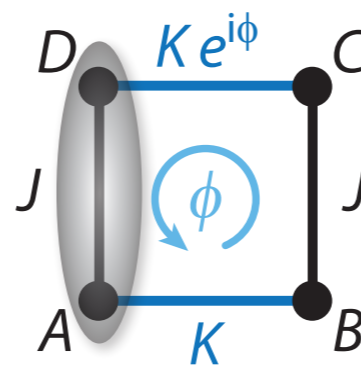
Quantum Analogue:*Initial State:*

Single Atom in the ground state of a tilted plaquette.

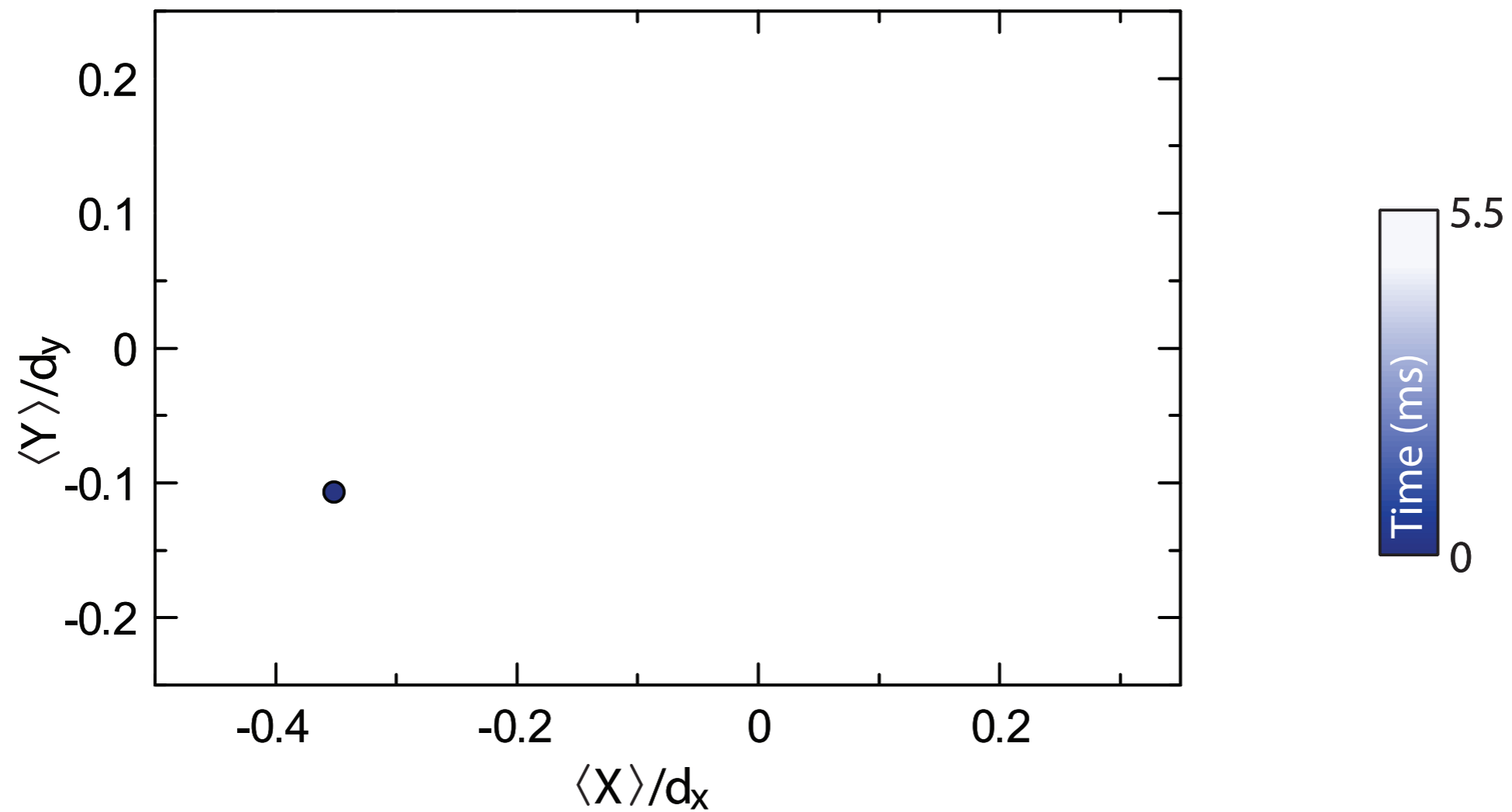


$$|\psi_0\rangle = \frac{|A\rangle + |D\rangle}{\sqrt{2}}$$

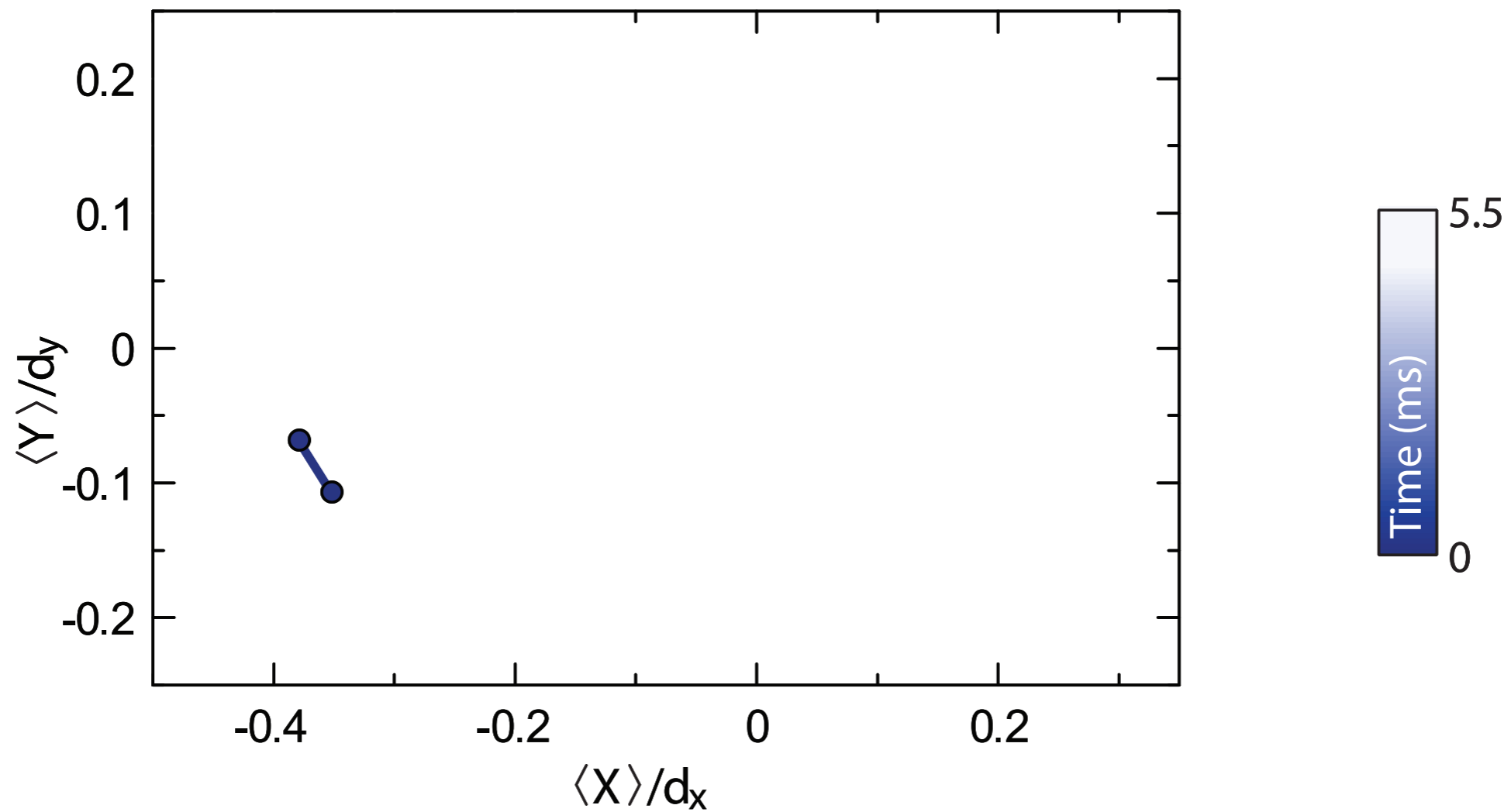
Switch on Raman coupling to induce tunneling



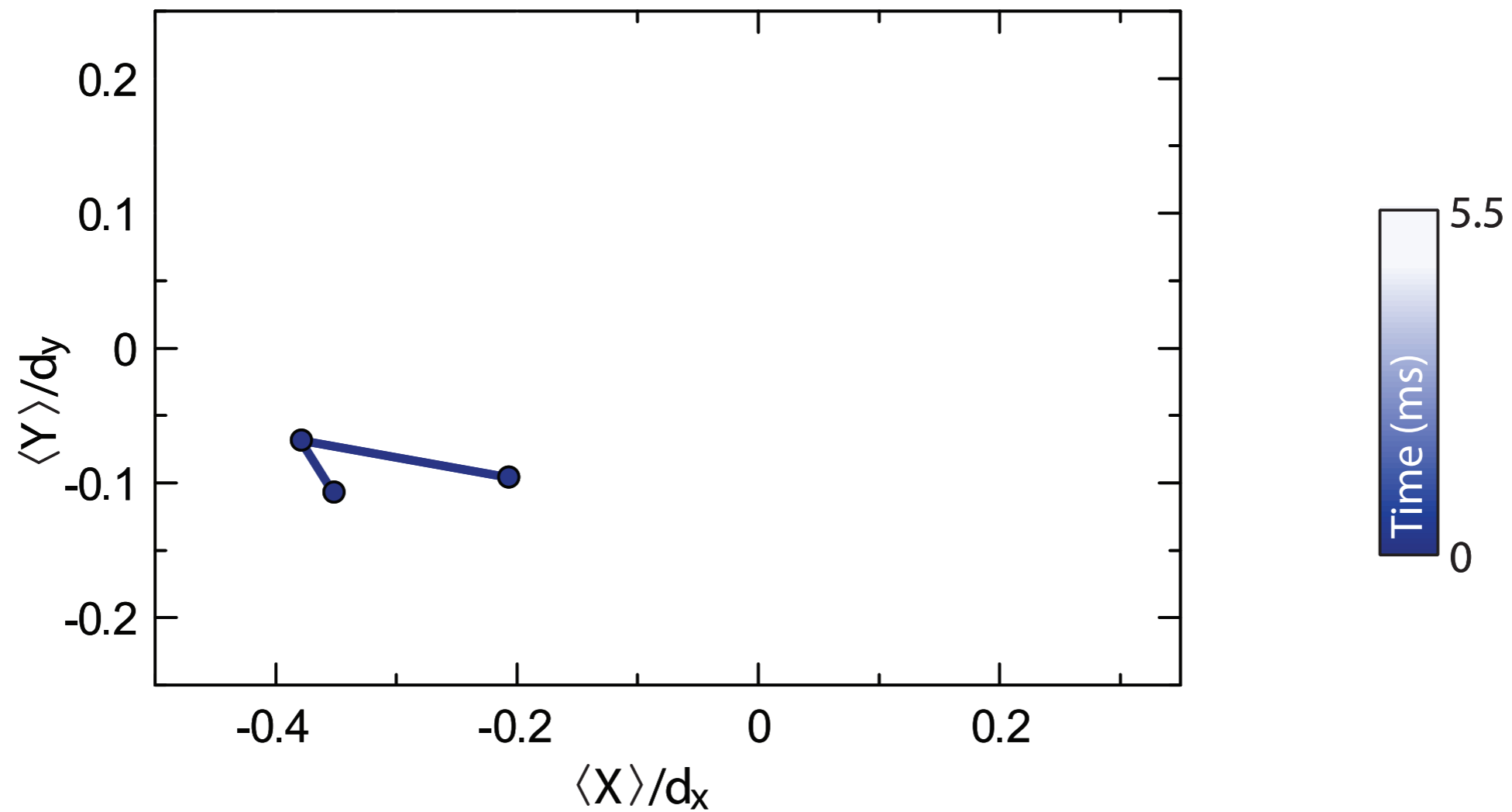
We plot the mean atom position during the evolution.



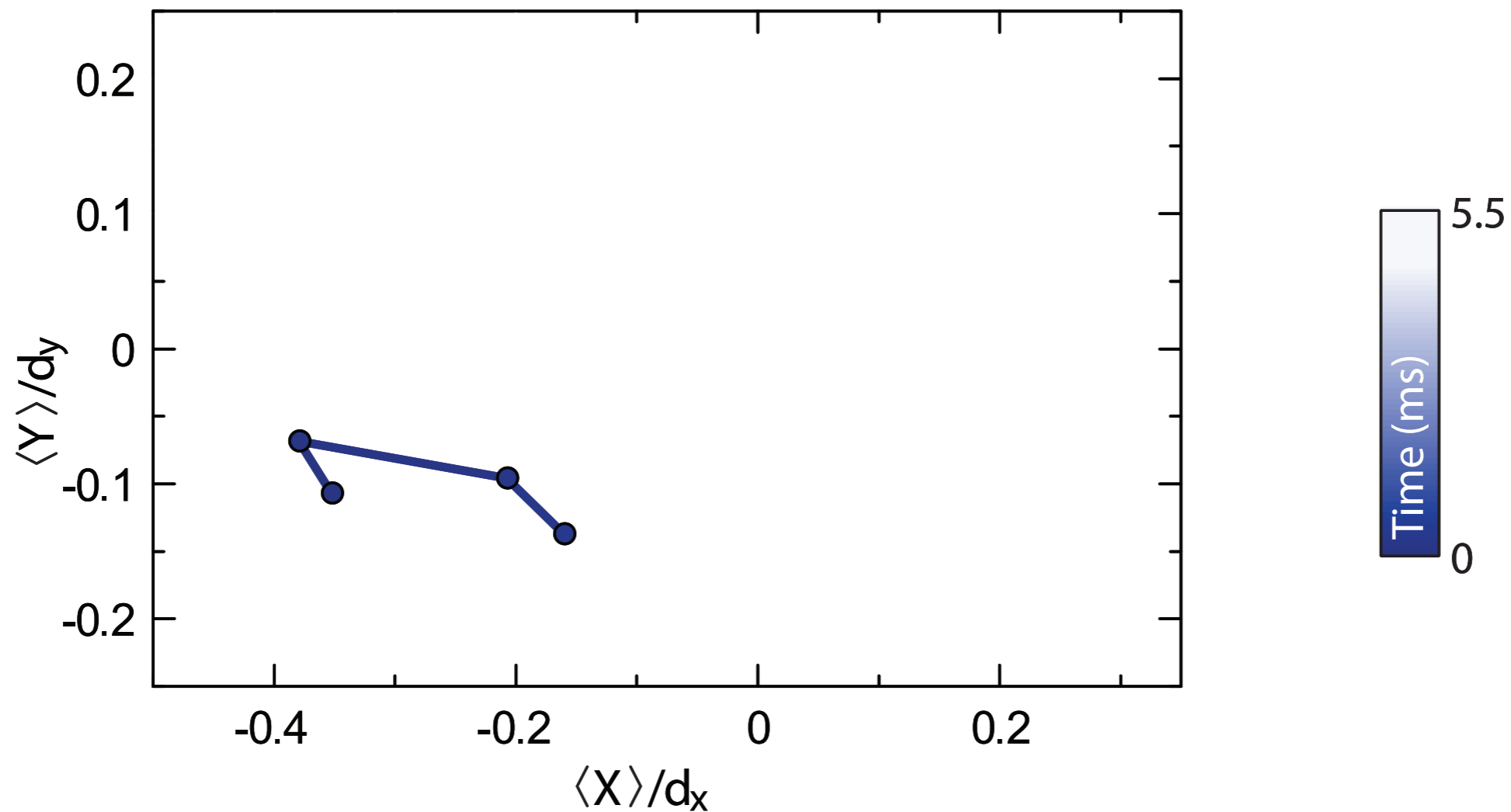
We plot the mean atom position during the evolution.



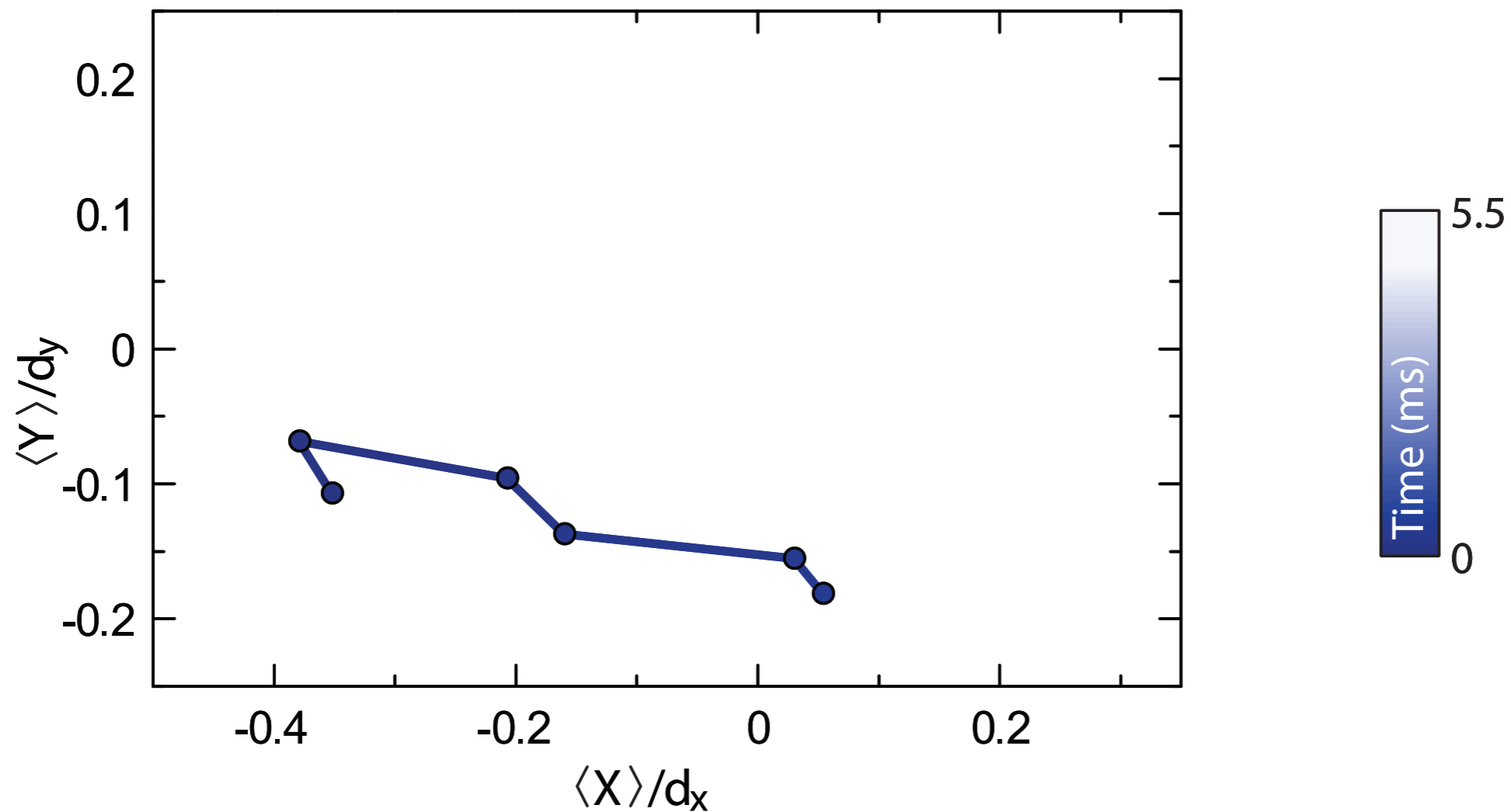
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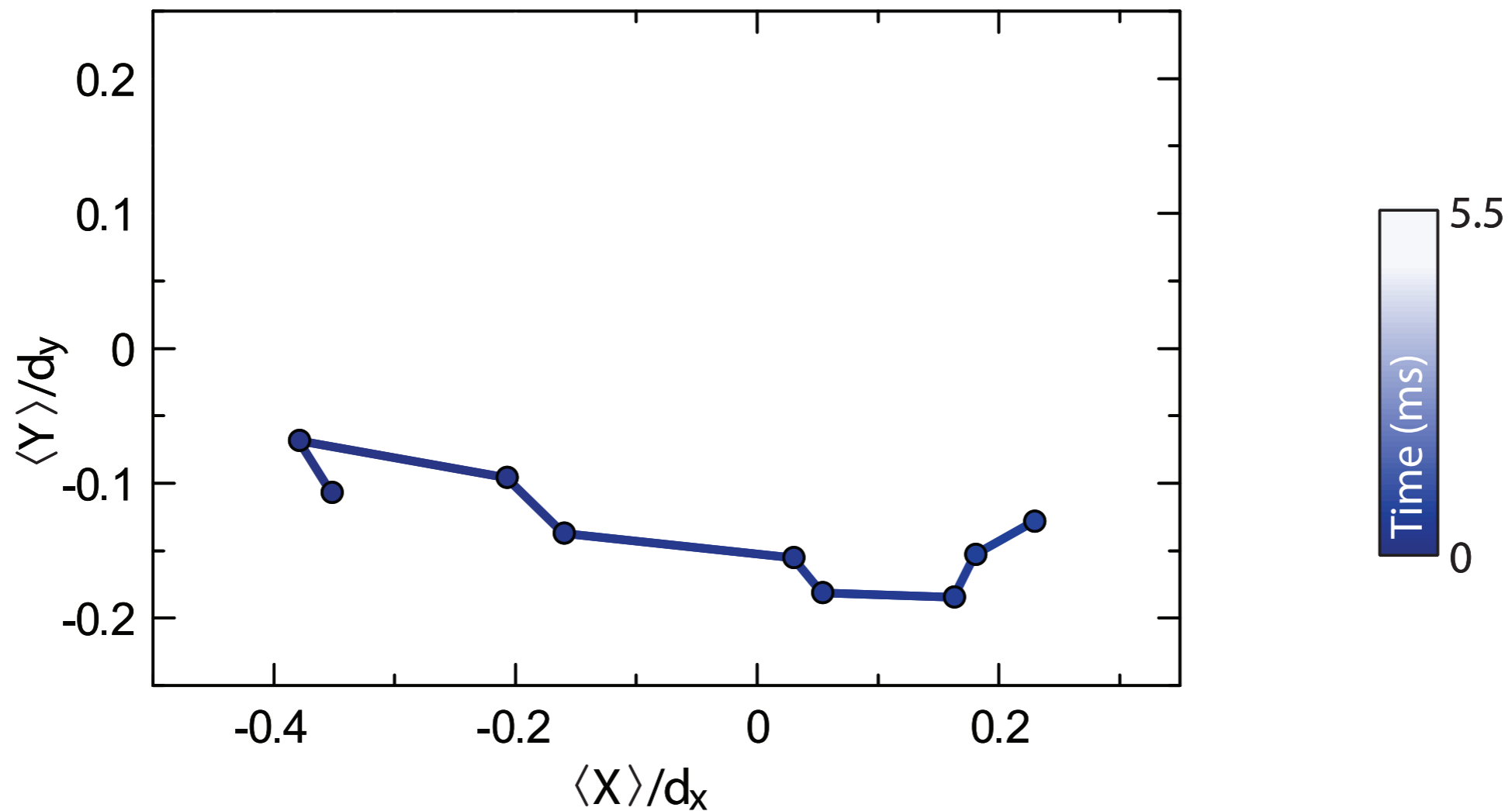
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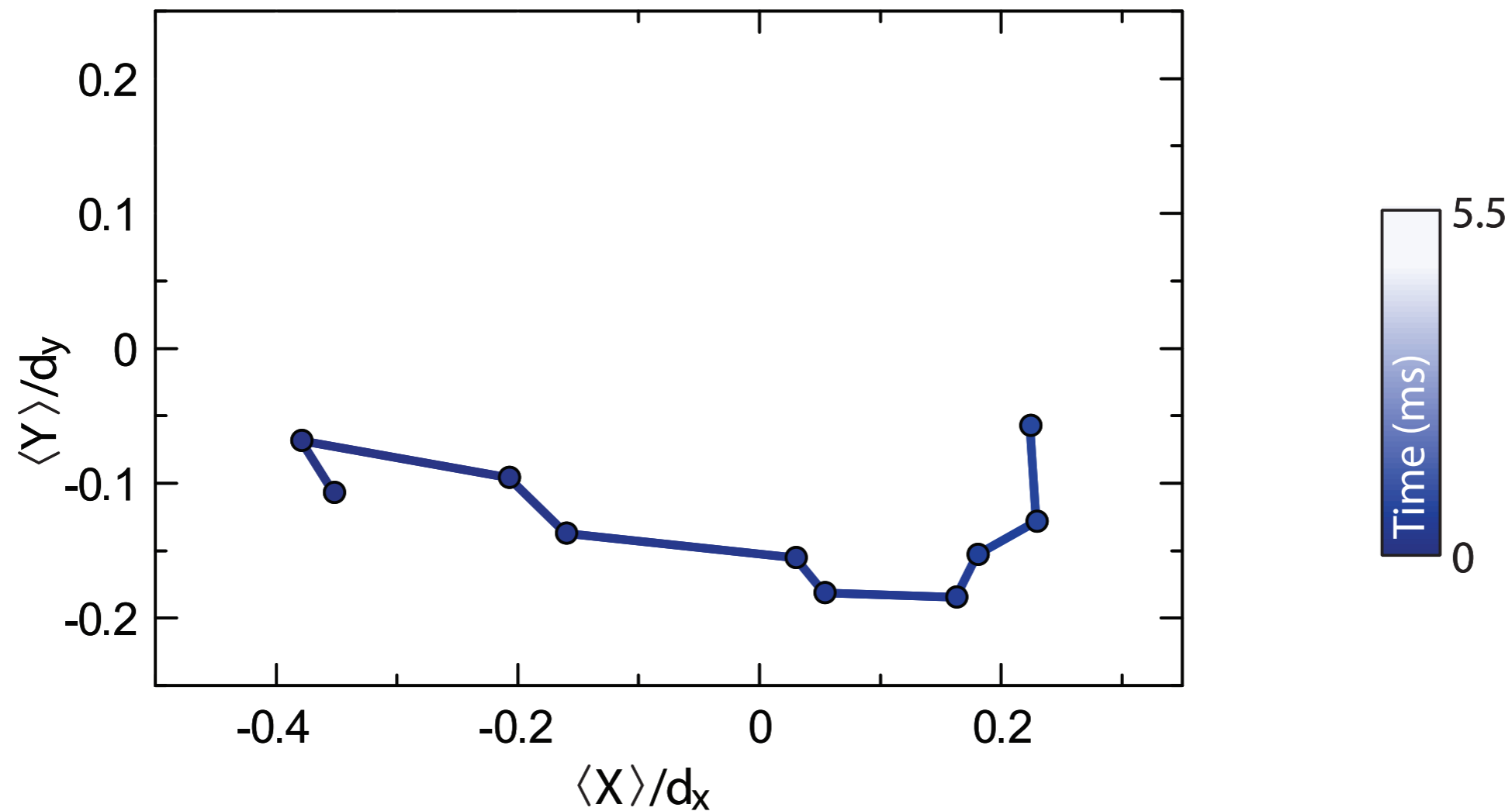
We plot the mean atom position during the evolution.



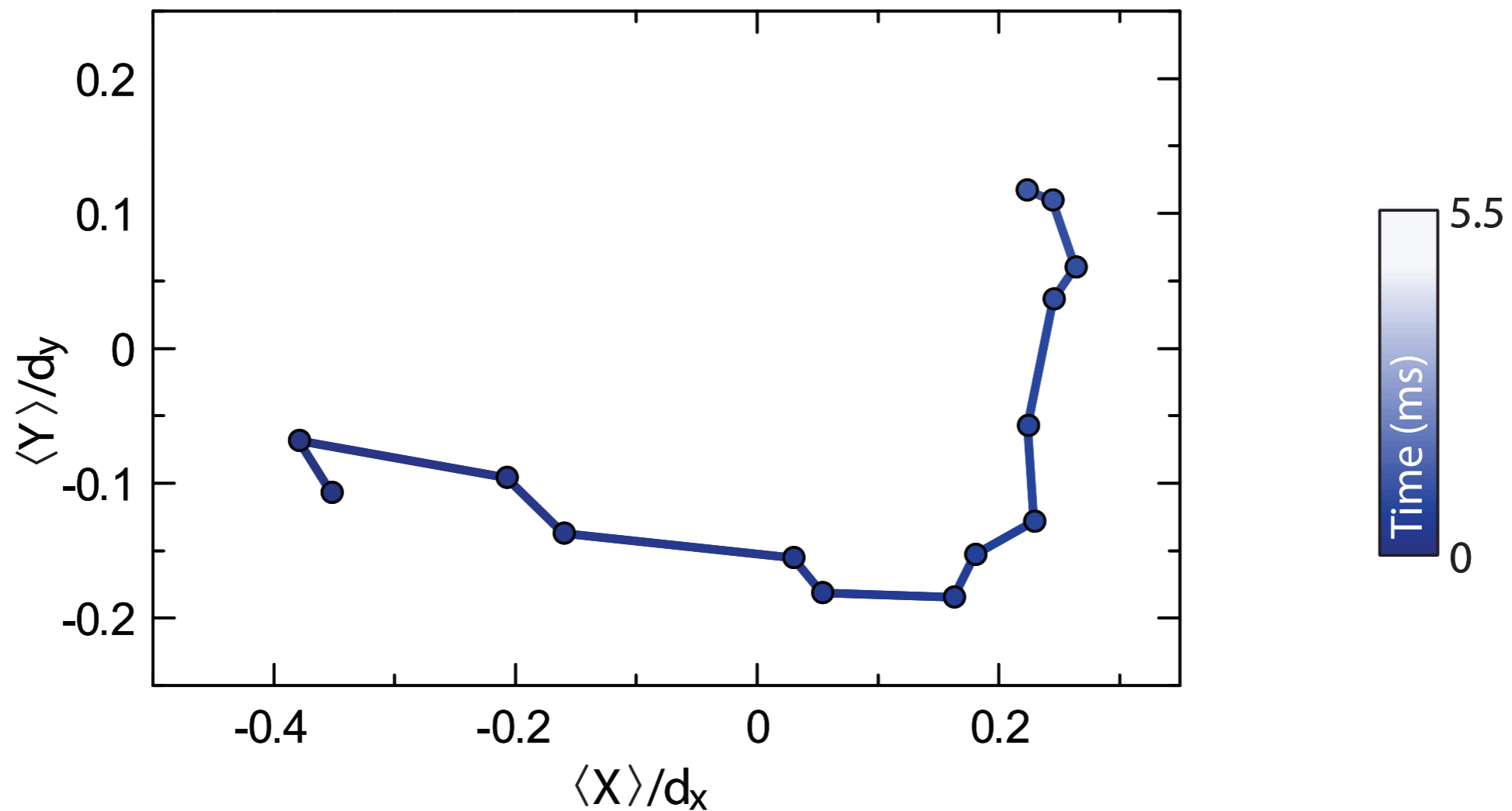
We plot the mean atom position during the evolution.



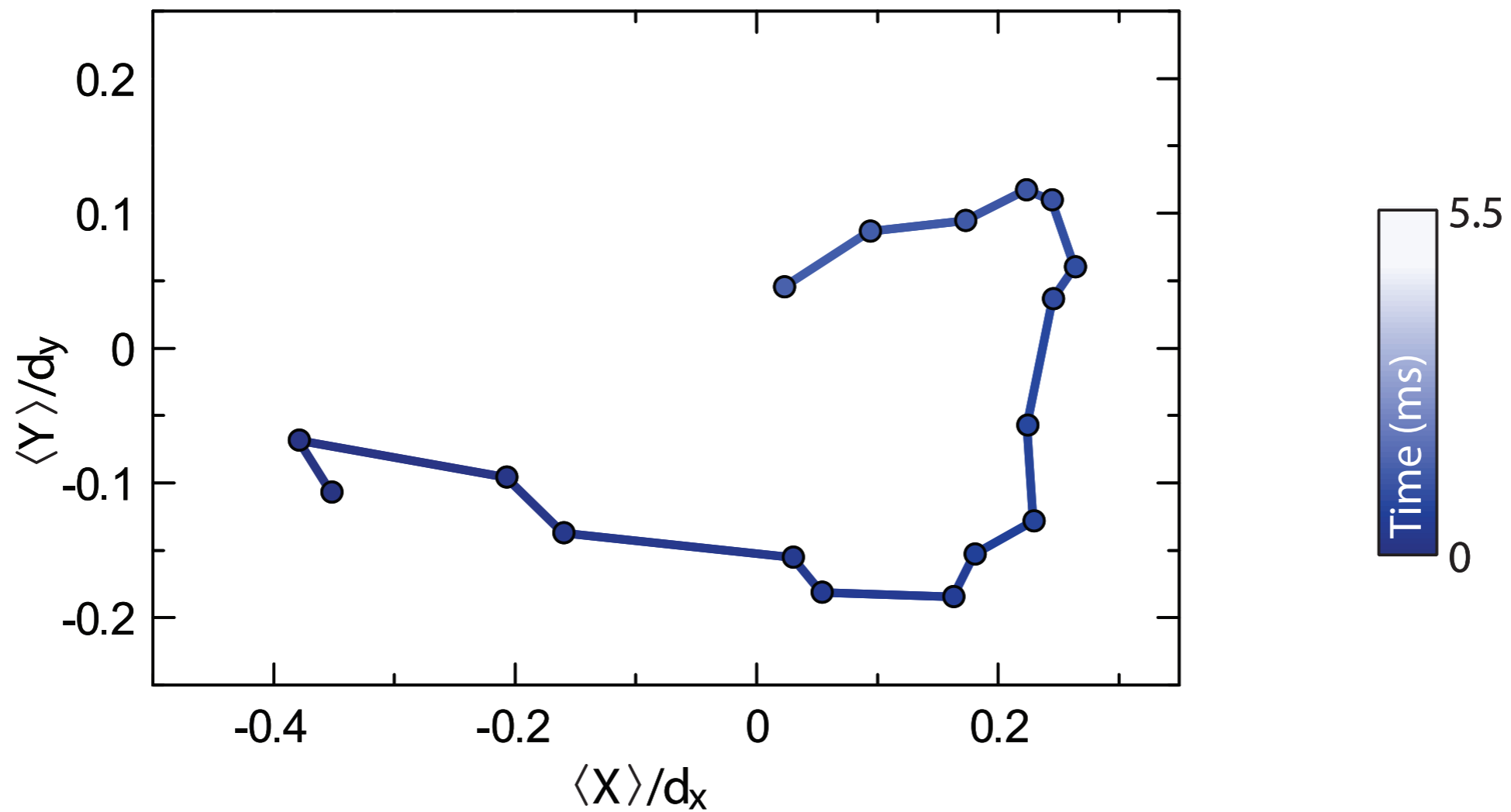
We plot the mean atom position during the evolution.



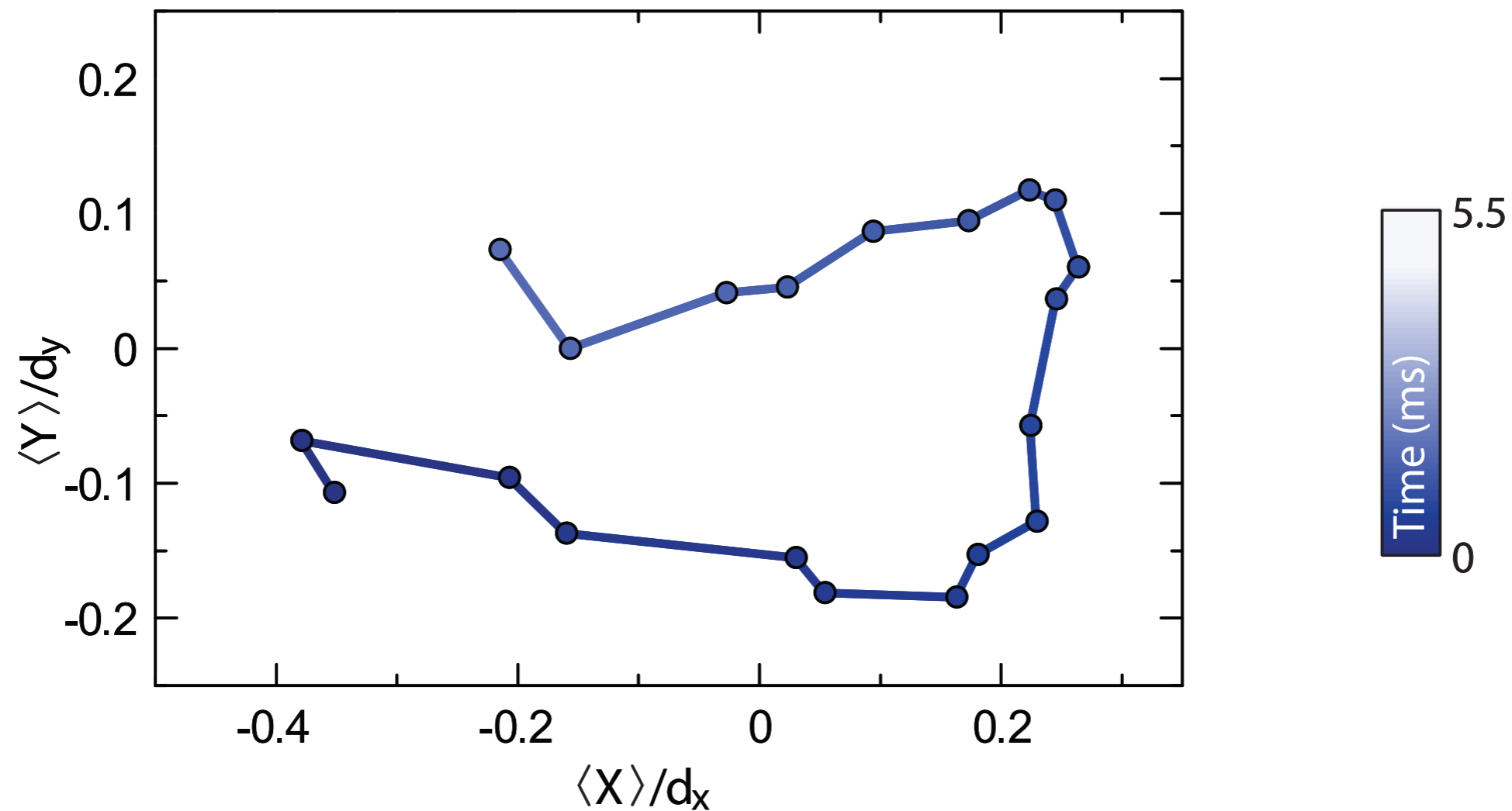
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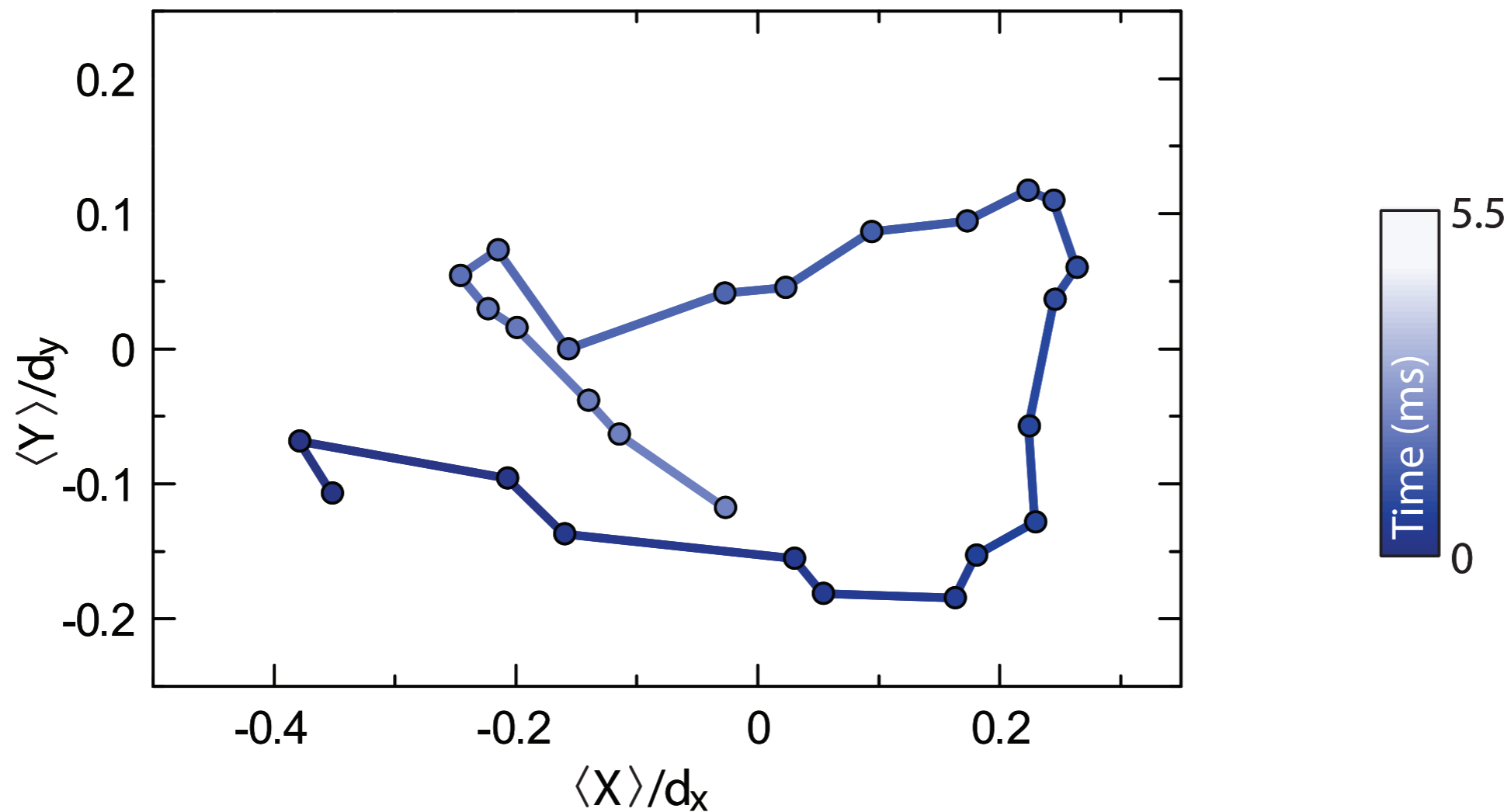
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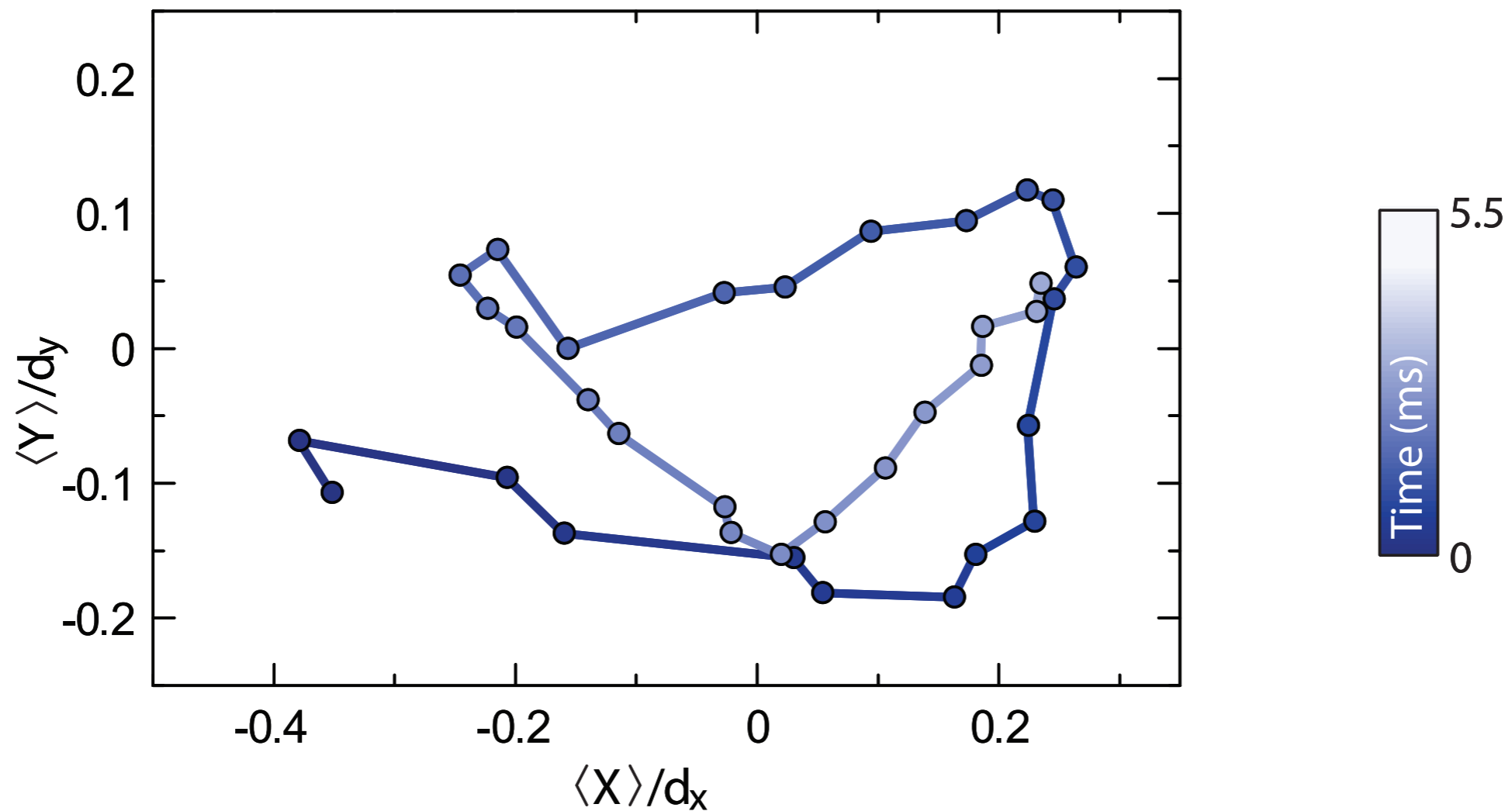
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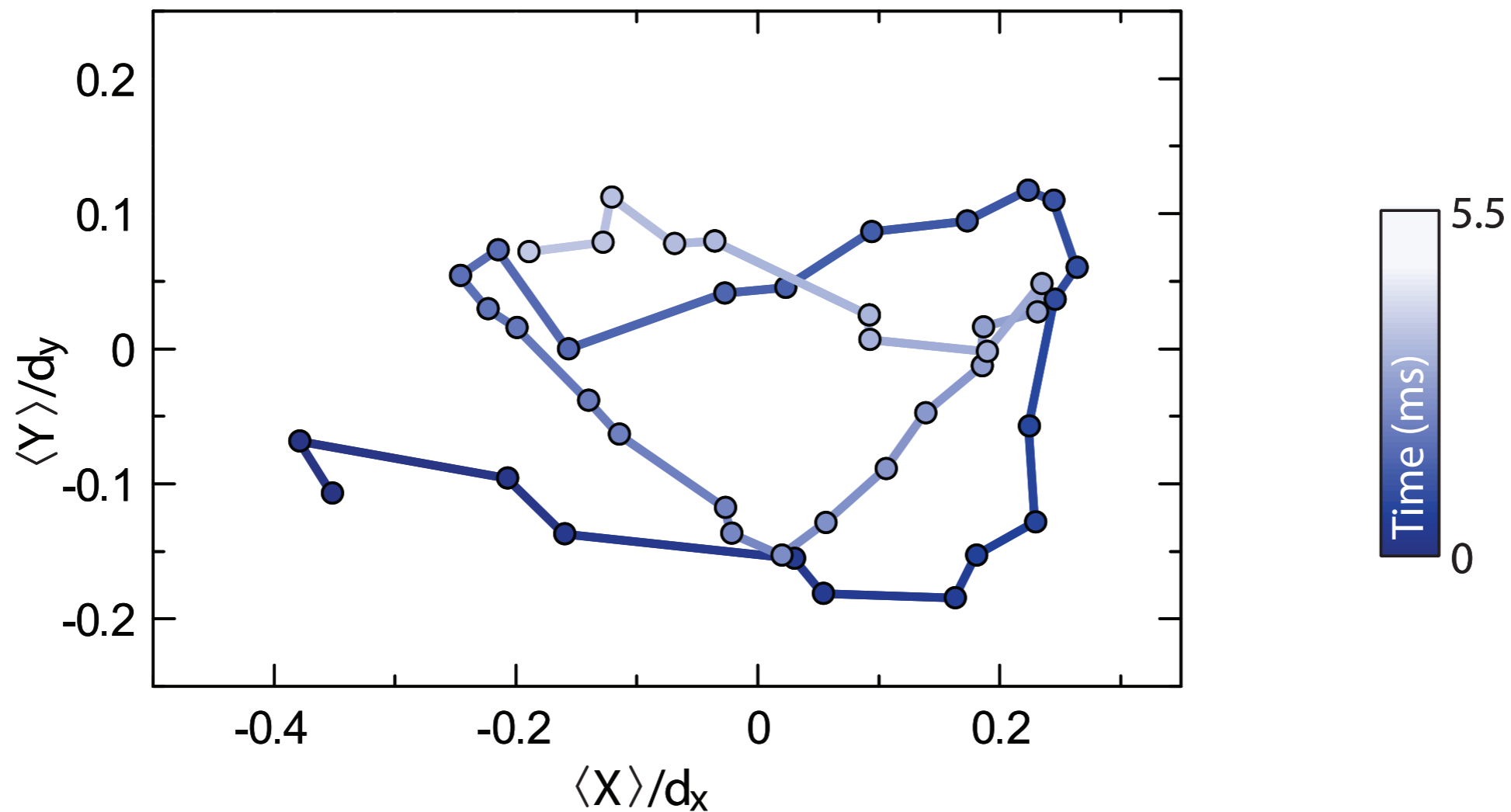
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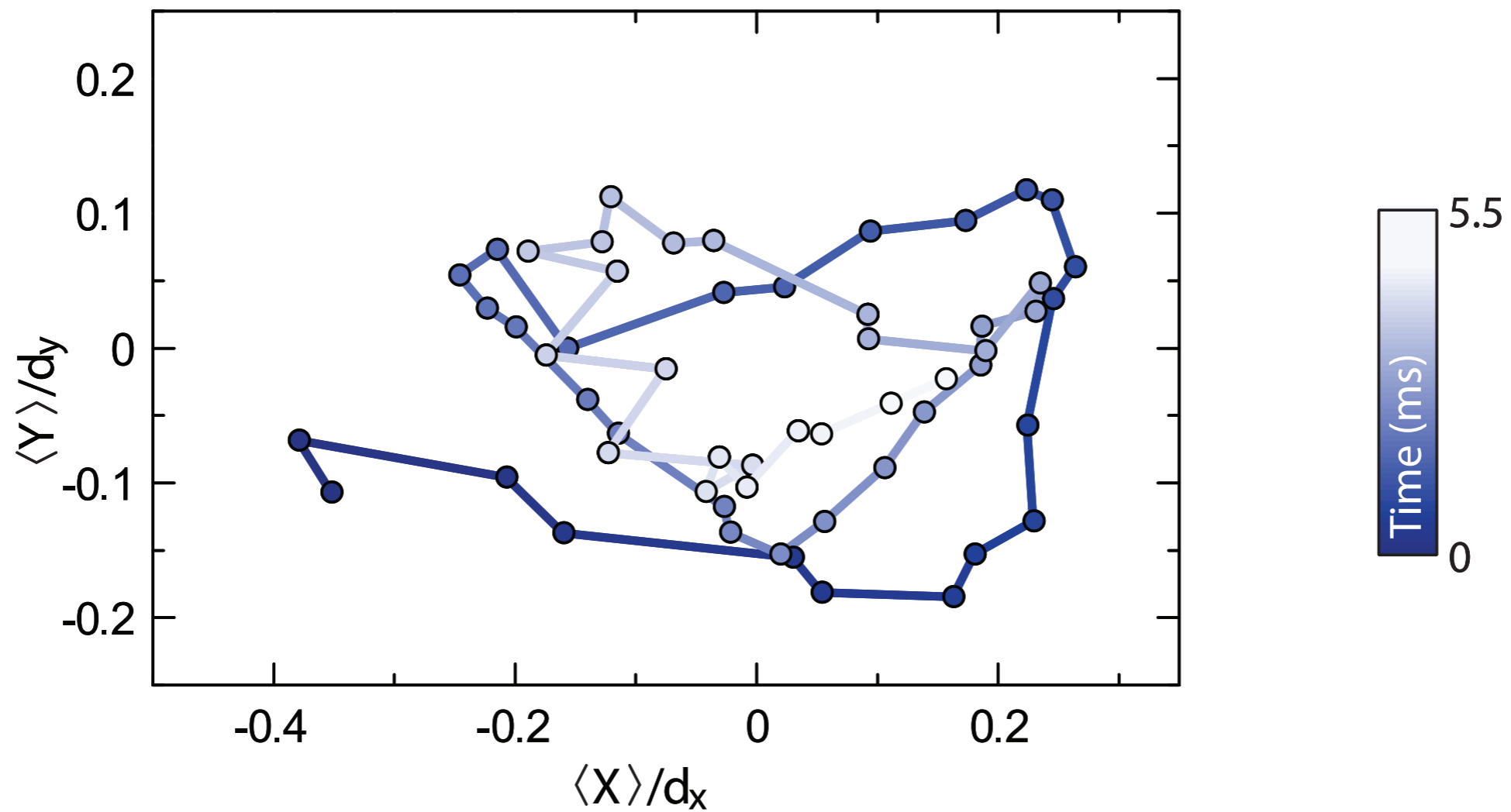
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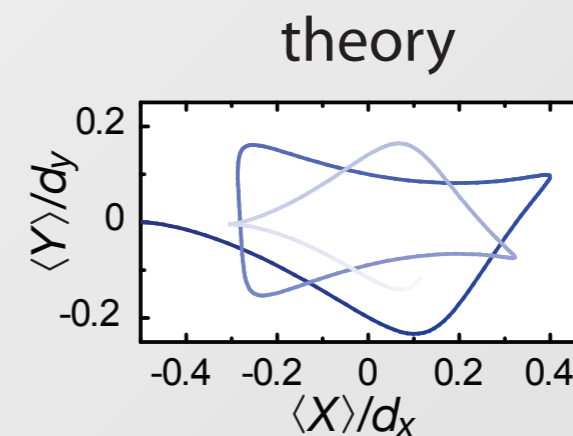
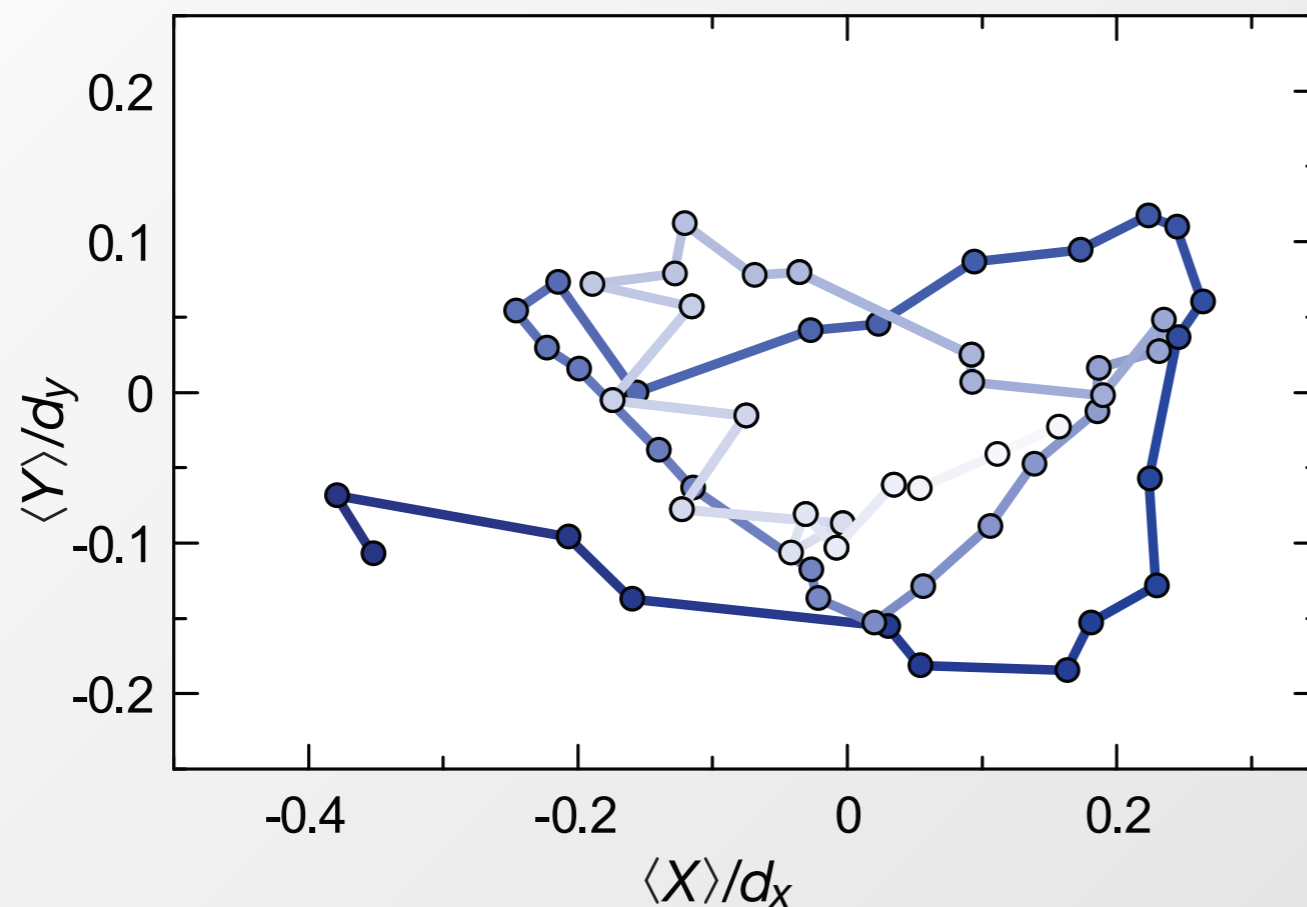
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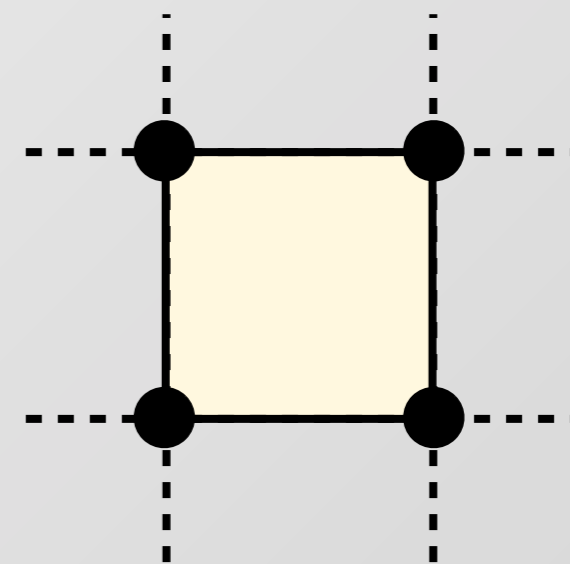
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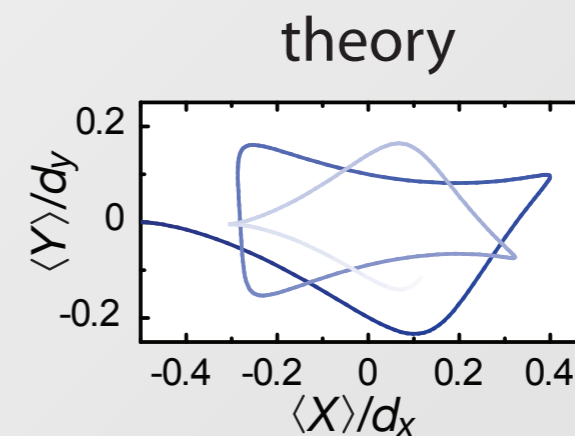
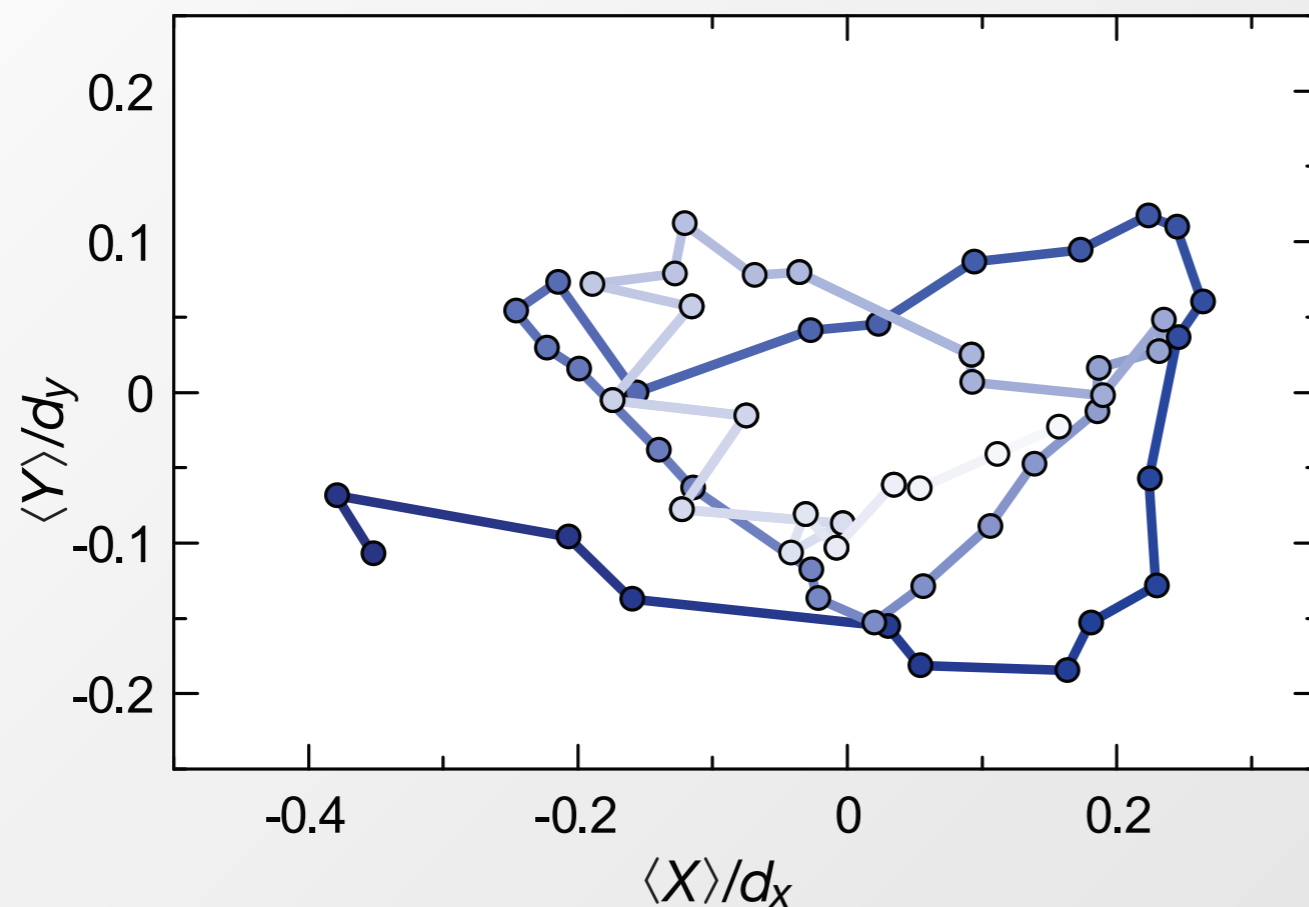
Quantum cyclotron orbit allows us to measure the applied flux!

$$\phi = 0.73(5) \frac{\pi}{2}$$

Deviation from $\pi/2$ due to geometric reasons.



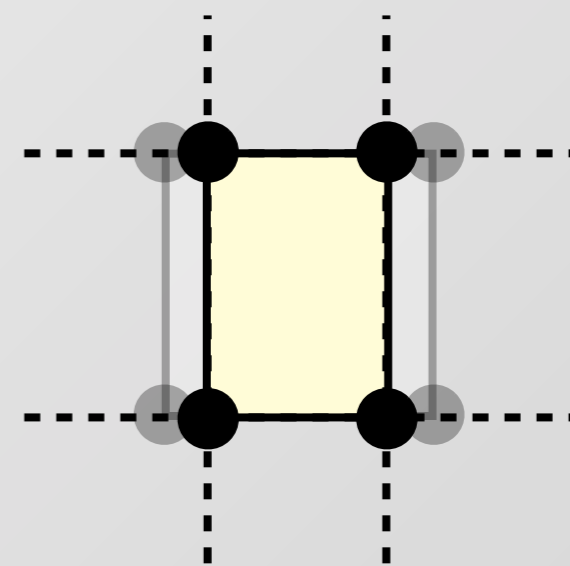
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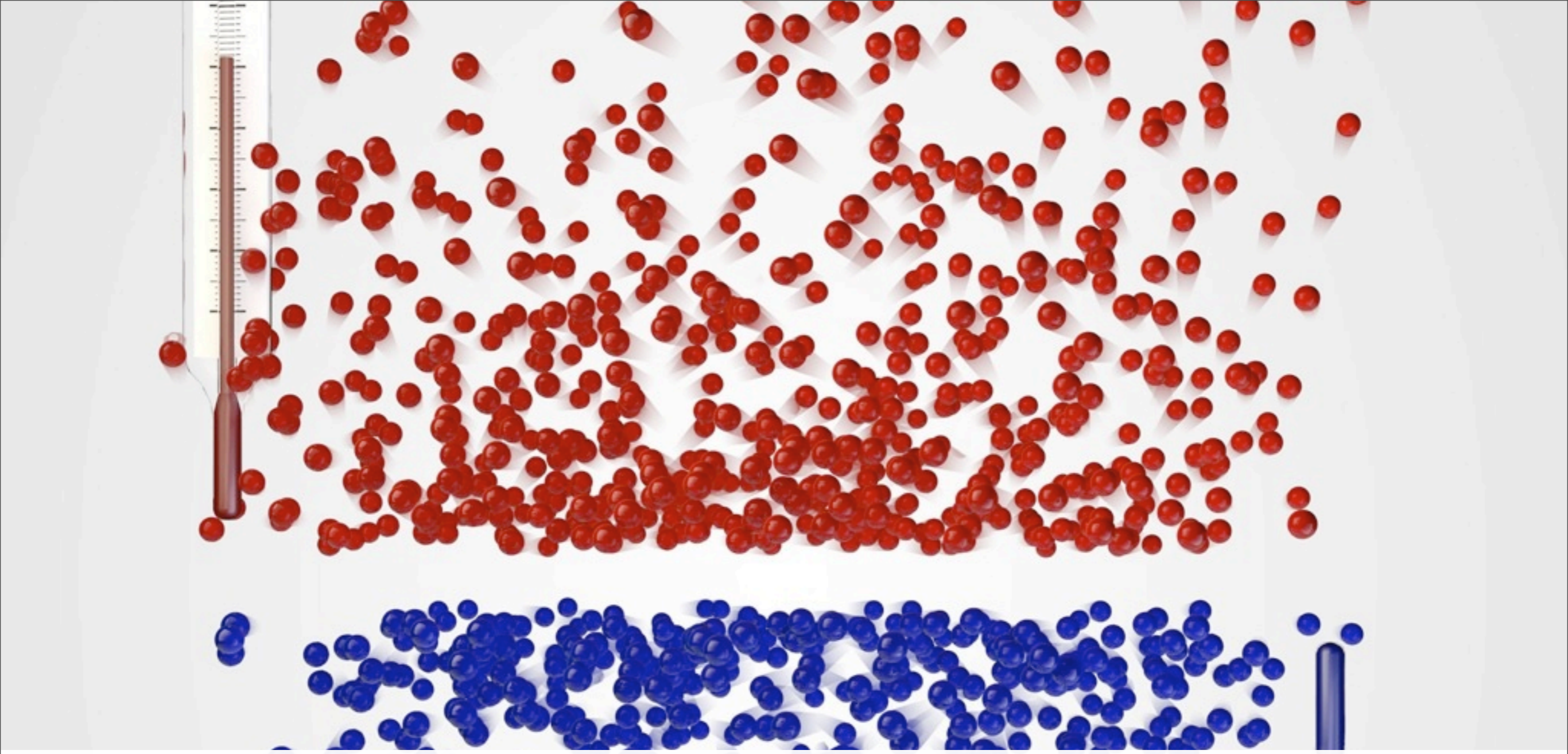


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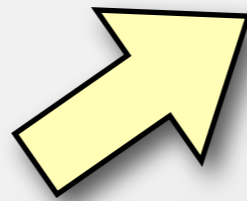
Quantum Matter at Negative Absolute Temperature

S. Braun, J.-P. Ronzheimer, M. Schreiber, S. Hodgman, T. Rom, D. Garbe, IB, U. Schneider

S. Braun et al. Science **339**, 52 (2013)

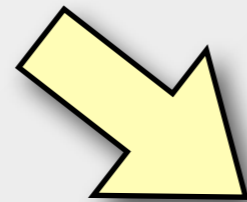
A. Mosk, PRL **95**, 040403 (2005) ,A. Rapp, S. Mandt & A. Rosch, PRL **105**, 220405 (2010)

$$\frac{1}{T} = \left(\frac{\partial S}{\partial E} \right)_V$$



Positive Temperature

Entropy increases with Energy

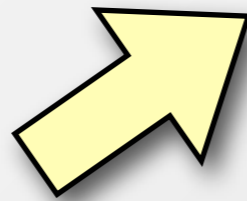


Negative Temperature

Entropy decreases with Energy

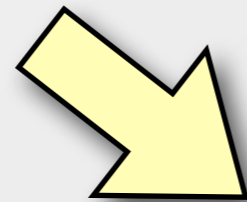


$$\frac{1}{T} = \left(\frac{\partial S}{\partial E} \right)_V$$



Positive Temperature

Entropy increases with Energy



Negative Temperature

Entropy decreases with Energy

Thermodynamic theorems apply in negative as well as positive temperature regime!

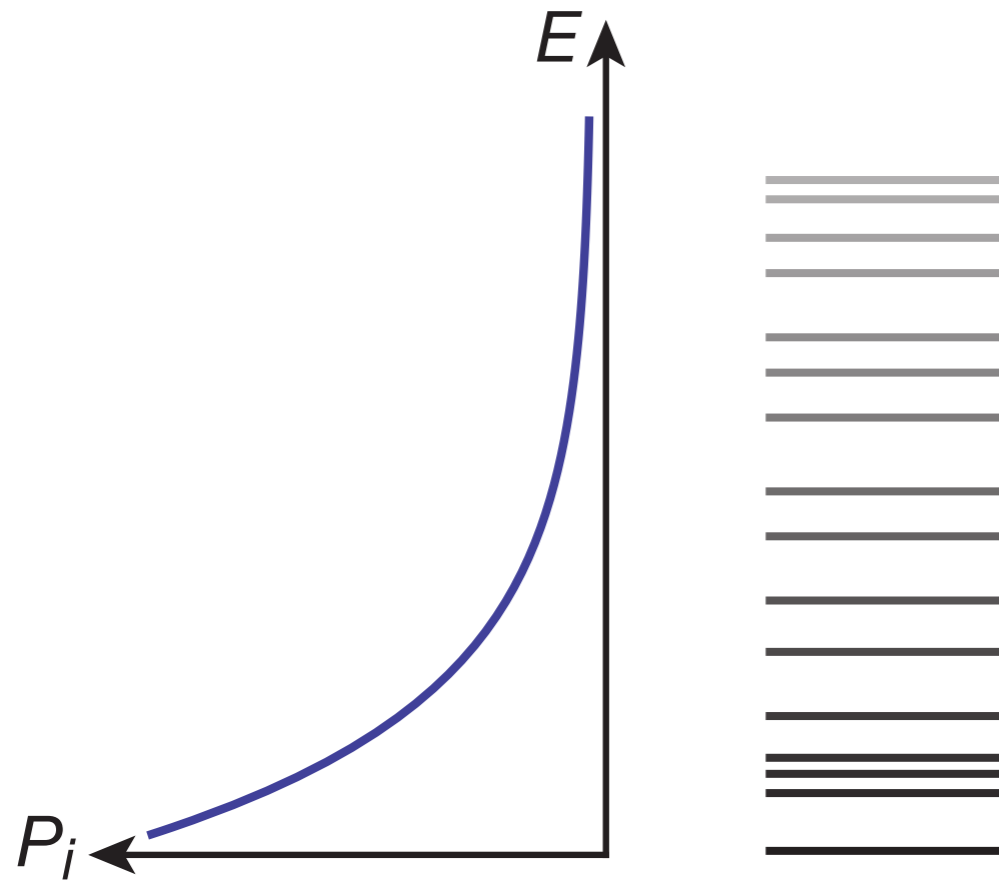


$$\frac{1}{T} = \left(\frac{\partial S}{\partial E} \right)$$

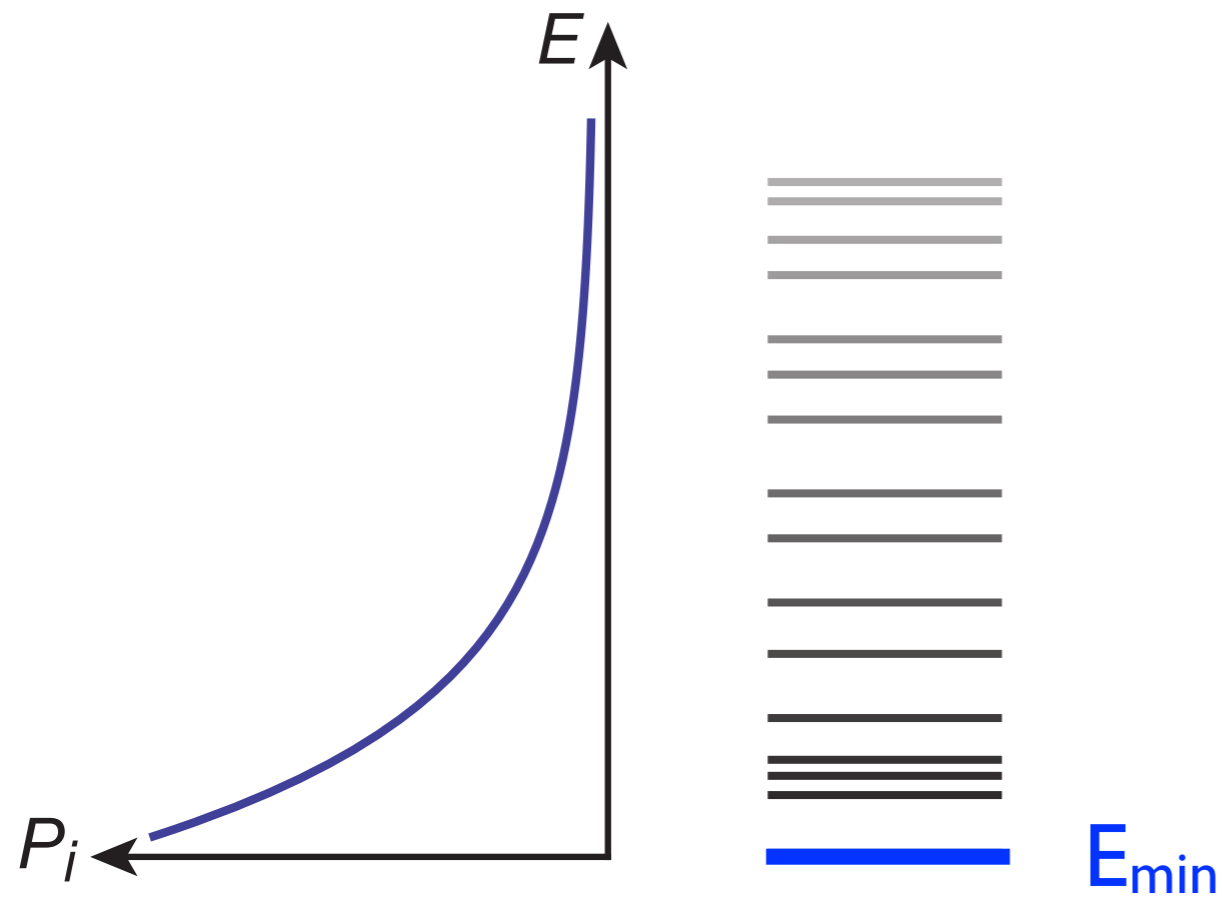
Warning:
Temperature
does not measure
energy content!!!

Thermodynamic theorems apply in negative as well
as positive temperature regime!



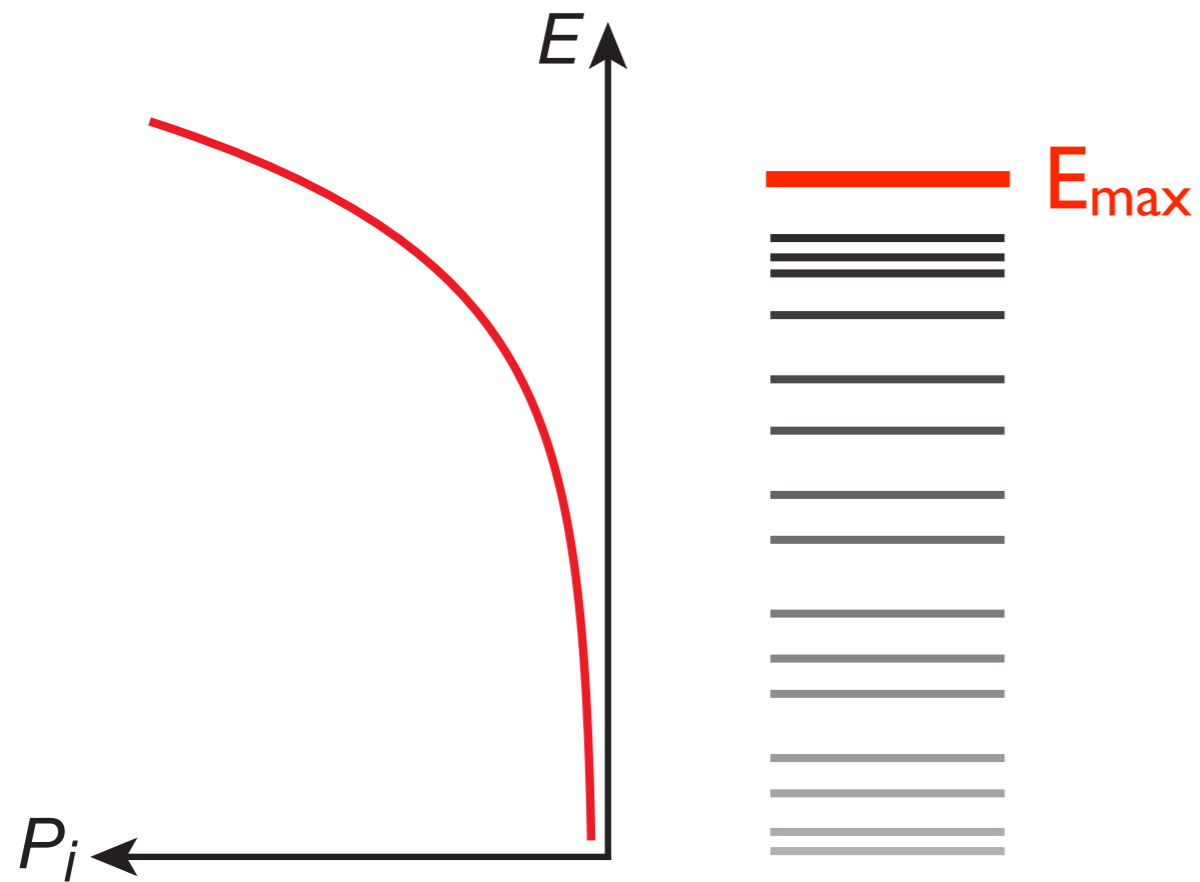


$$P_i \propto e^{-\frac{E_i}{k_B T}}$$



$$P_i \propto e^{-\frac{E_i}{k_B T}}$$

For positive temperatures, we require **lower energy bound** E_{\min} !



$$P_i \propto e^{-\frac{E_i}{k_B(-T)}}$$

For negative temperatures, we require **upper energy bound E_{\max}** !



Norman Ramsey
(1915-2011)

PHYSICAL REVIEW

VOLUME 103, NUMBER 1

JULY 1, 1956

Thermodynamics and Statistical Mechanics at Negative Absolute Temperatures

NORMAN F. RAMSEY*

Harvard University, Cambridge, Massachusetts, and Clarendon Laboratory, Oxford, England

(Received March 26, 1956)

As discussed in Sec. III below, the conditions for the existence of a system at negative temperatures are so restrictive that they are rarely met in practice except with some mutually interacting nuclear spin systems.

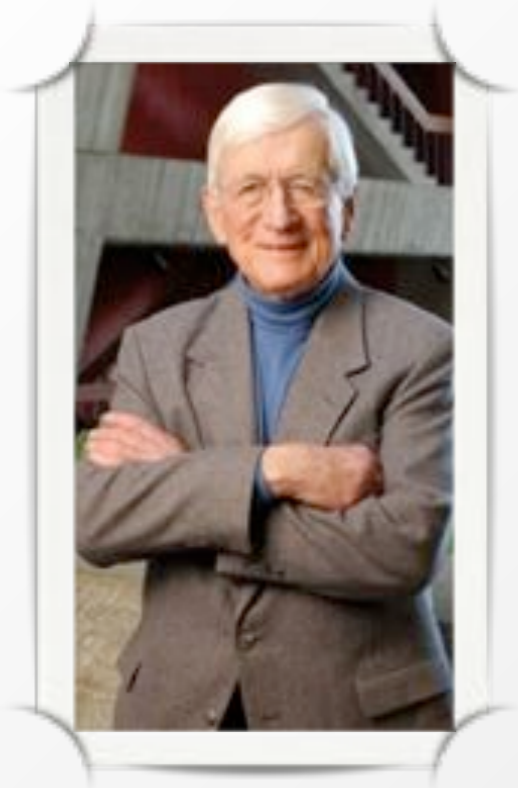
E.M. Purcell & R.V. Pound, Phys. Rev. **81**, 279 (1951)

N. Ramsey, Phys. Rev. **103**, 20 (1956)

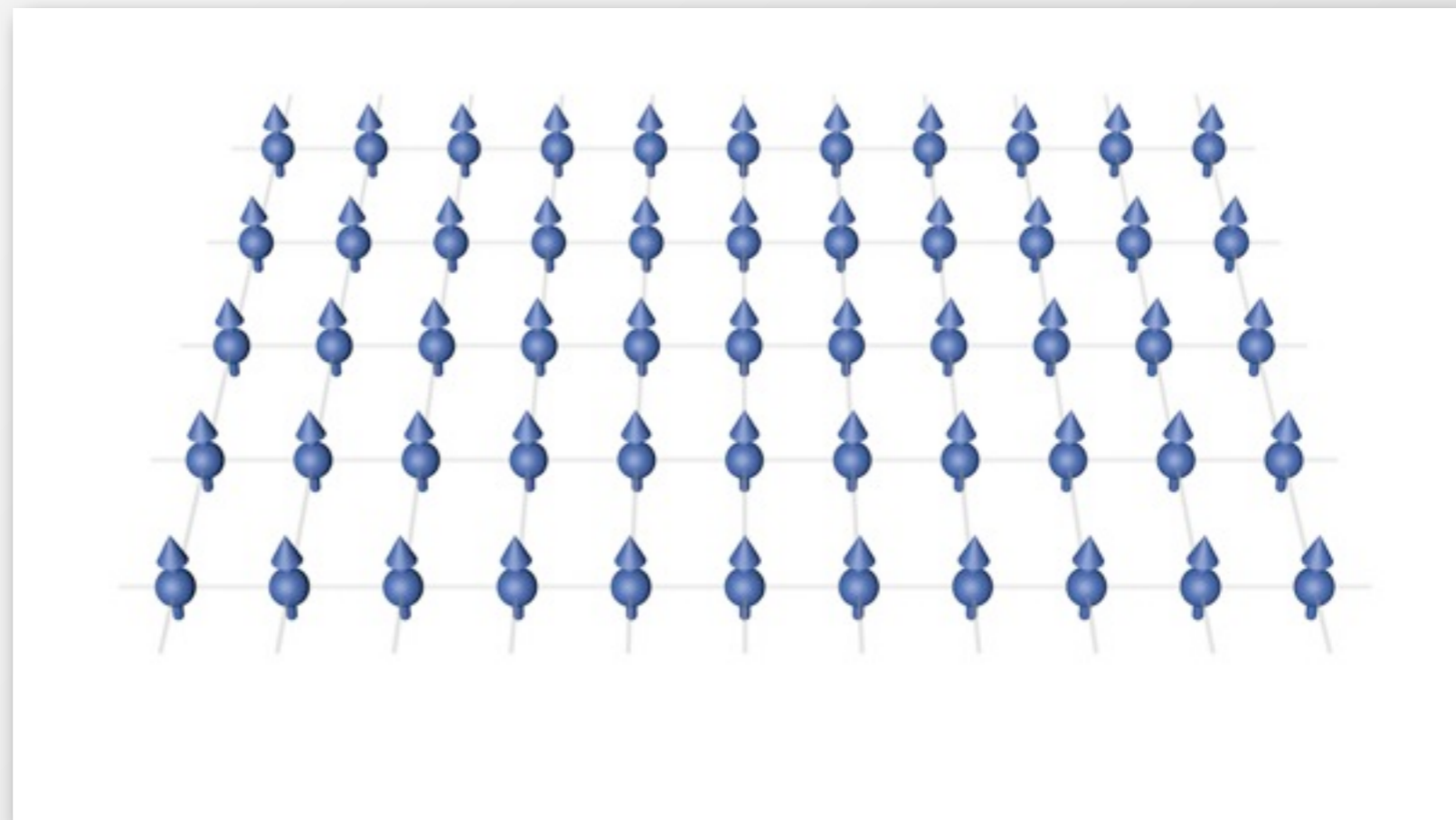
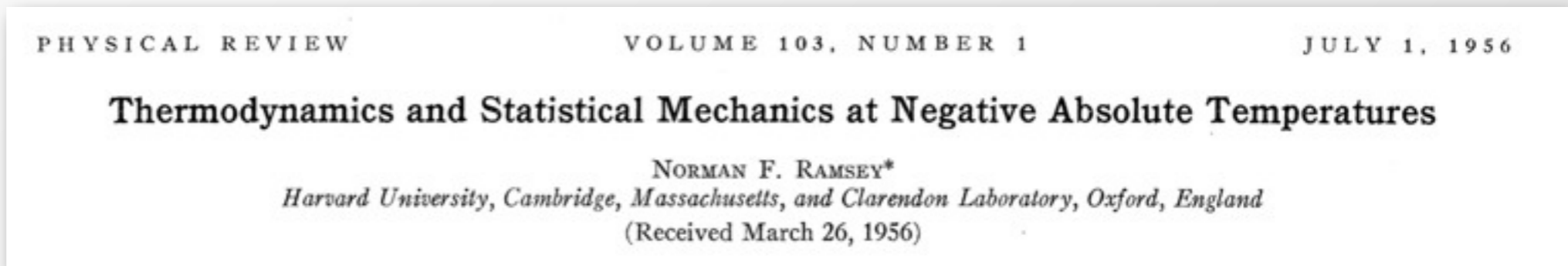
M.J. Klein, Phys. Rev. **104**, 589 (1956)

P. Hakonen & O.V. Lounasmaa, Science, **265**, 1821 (1994)





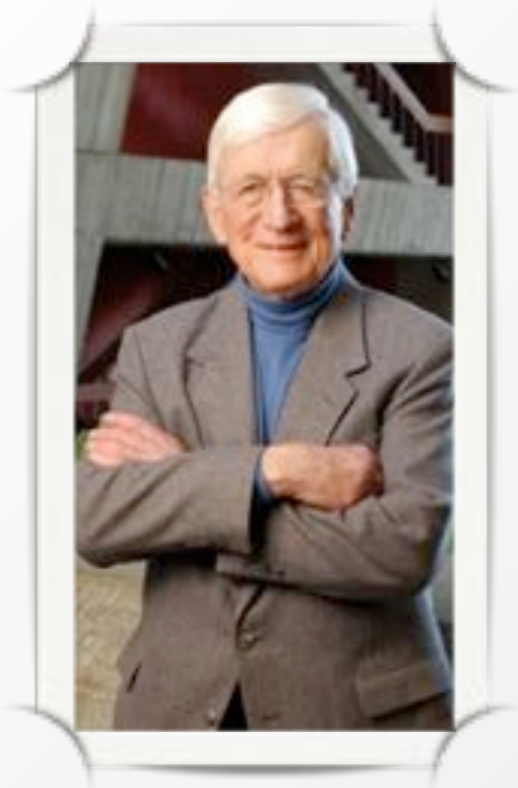
Norman Ramsey
(1915-2011)



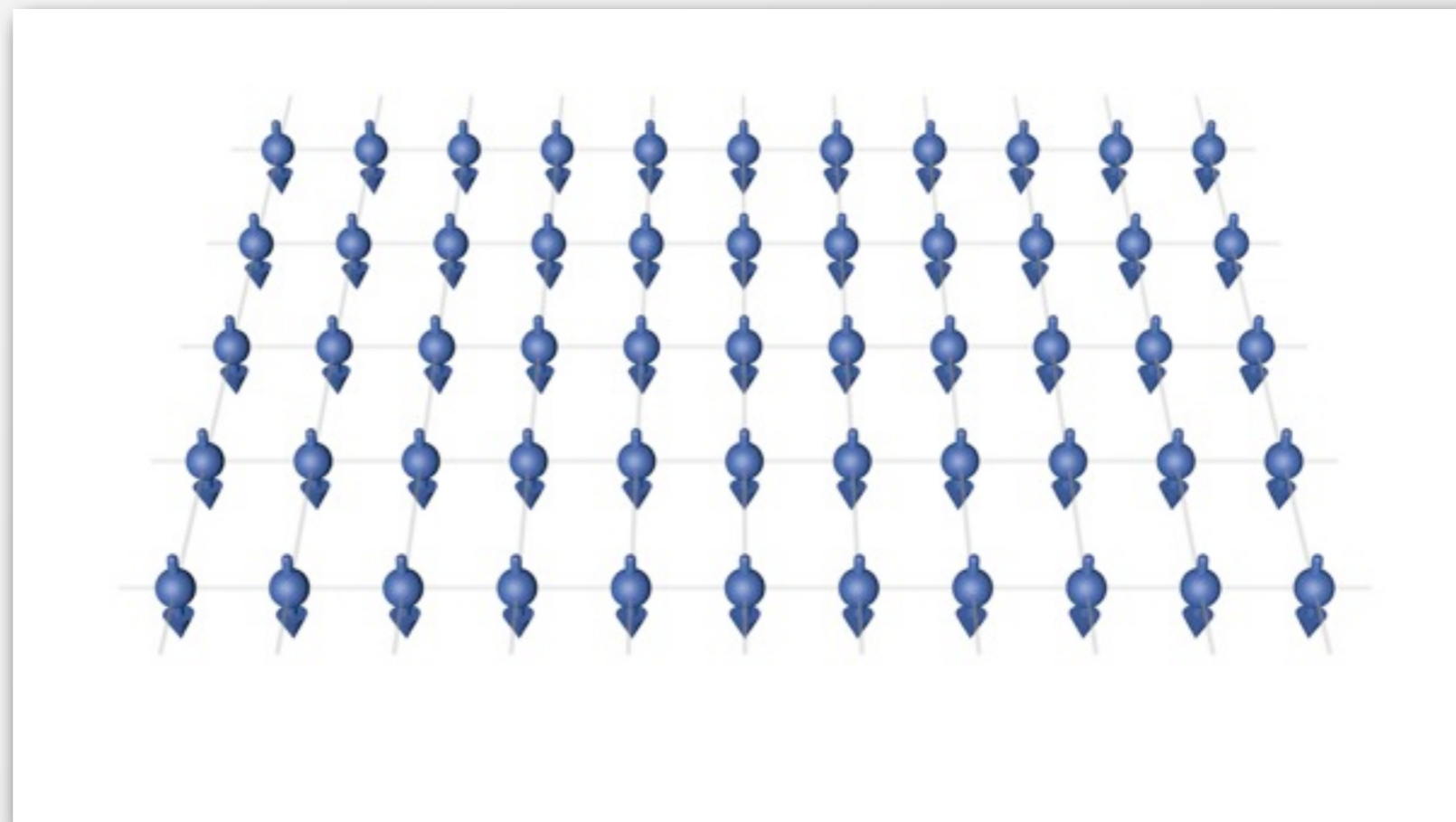
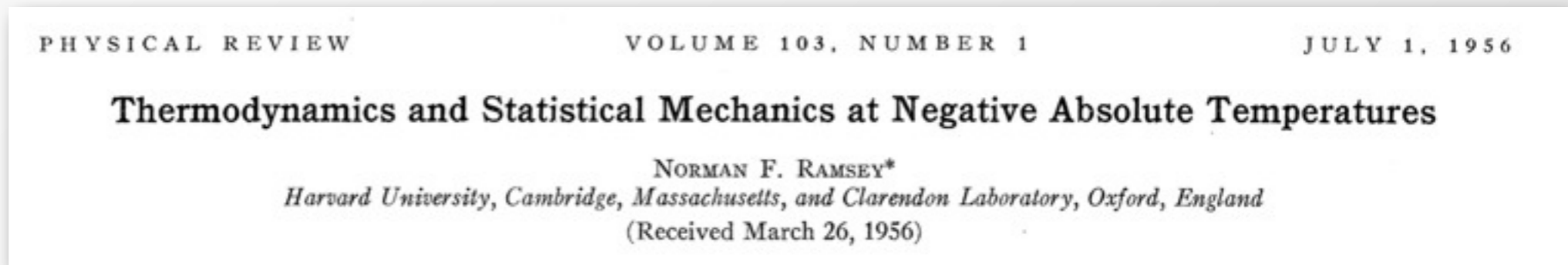
Lowest Energy State E_{min}

E.M. Purcell & R.V. Pound, Phys. Rev. **81**, 279 (1951)
 N. Ramsey, Phys. Rev. **103**, 20 (1956)
 M.J. Klein, Phys. Rev. **104**, 589 (1956)
 P. Hakonen & O.V. Lounasmaa, Science, **265**, 1821 (1994)





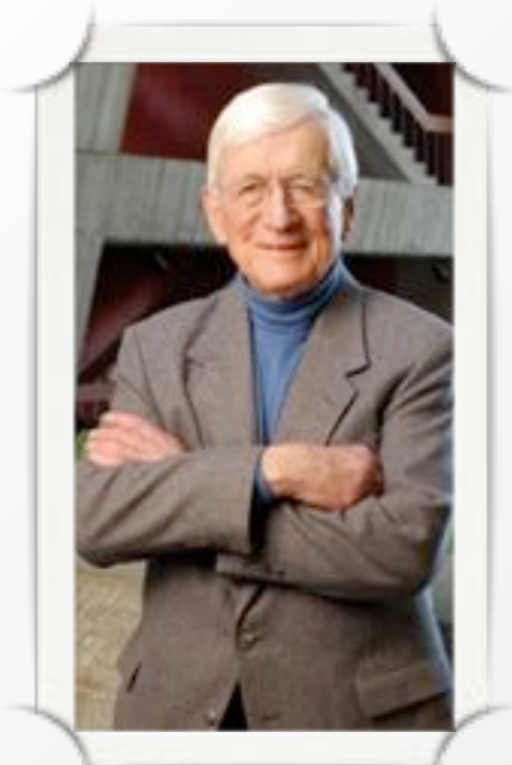
Norman Ramsey
(1915-2011)



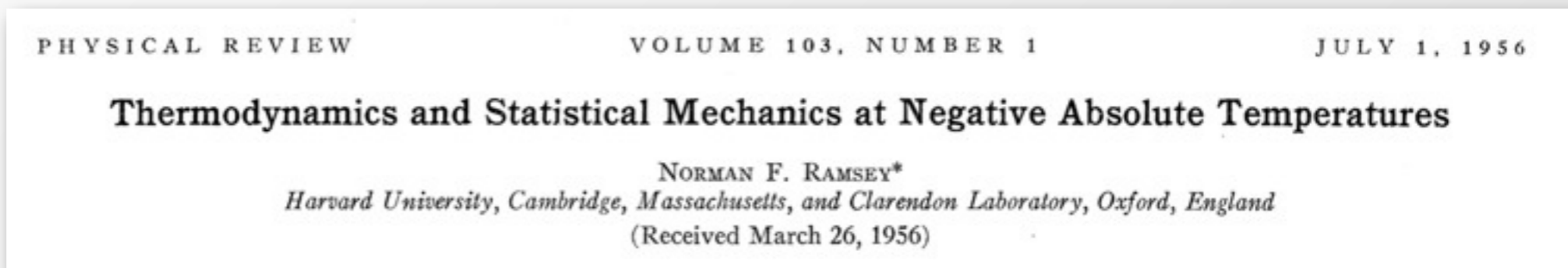
Highest Energy State E_{max}

E.M. Purcell & R.V. Pound, Phys. Rev. **81**, 279 (1951)
N. Ramsey, Phys. Rev. **103**, 20 (1956)
M.J. Klein, Phys. Rev. **104**, 589 (1956)
P. Hakonen & O.V. Lounasmaa, Science, **265**, 1821 (1994)

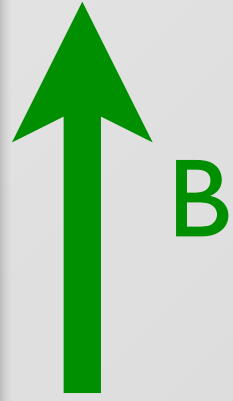




Norman Ramsey
(1915-2011)



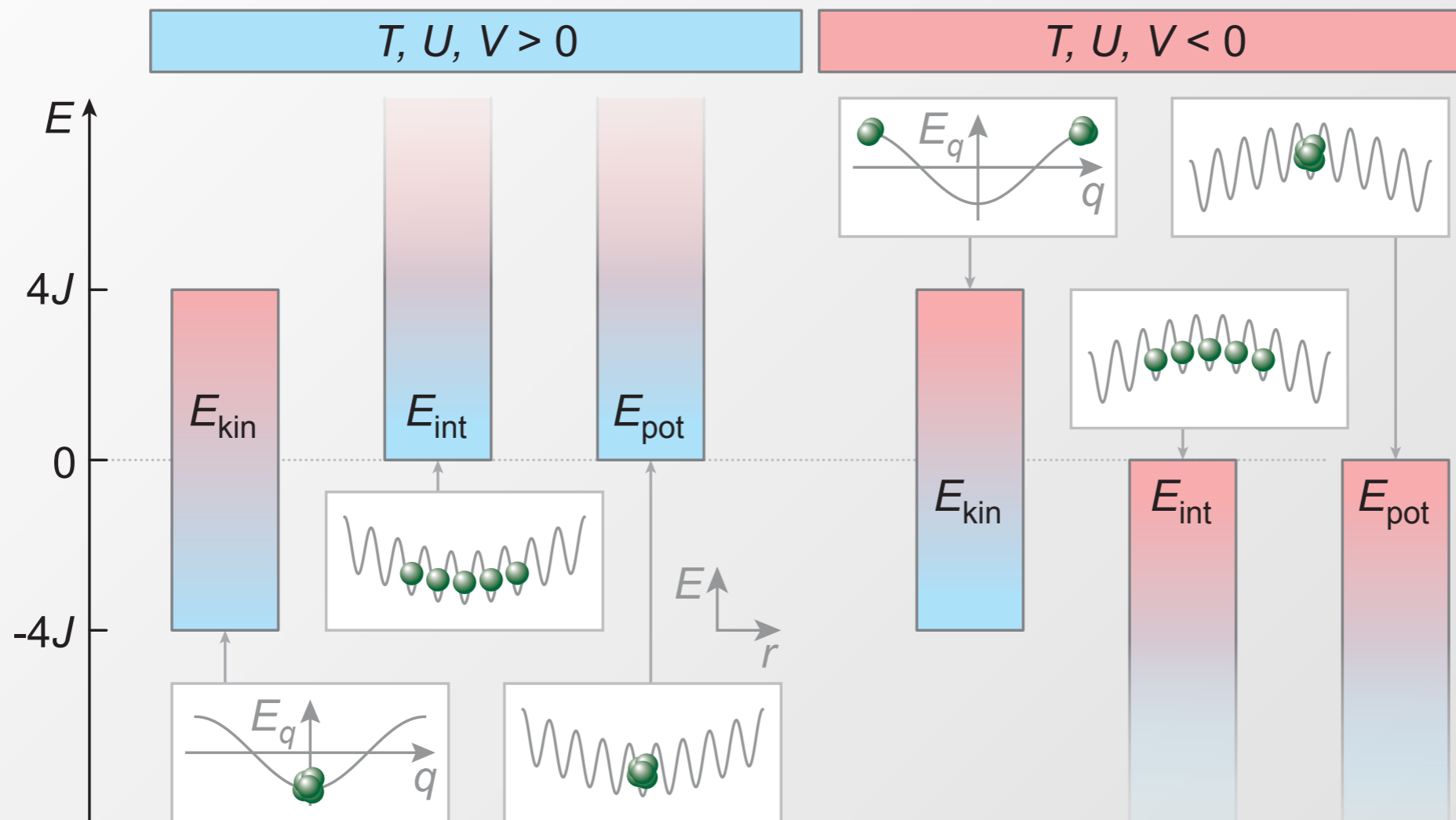
Can we achieve negative temperatures for motional degrees of freedom?

A green arrow pointing upwards, with the letter 'B' to its right.

Highest Energy State E_{max}

E.M. Purcell & R.V. Pound, Phys. Rev. **81**, 279 (1951)
N. Ramsey, Phys. Rev. **103**, 20 (1956)
M.J. Klein, Phys. Rev. **104**, 589 (1956)
P. Hakonen & O.V. Lounasmaa, Science, **265**, 1821 (1994)

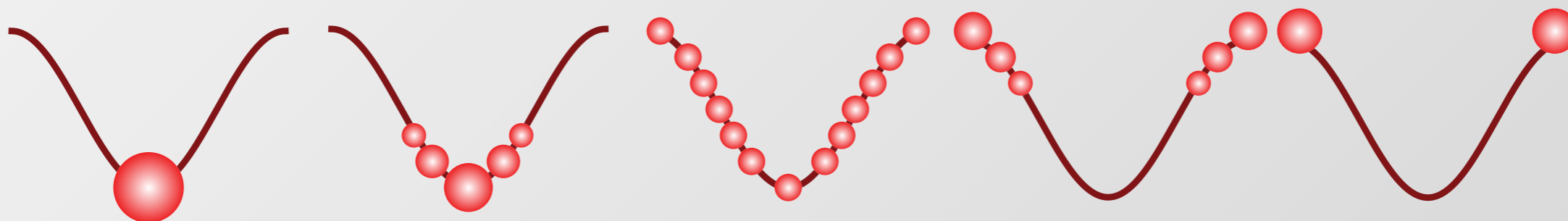
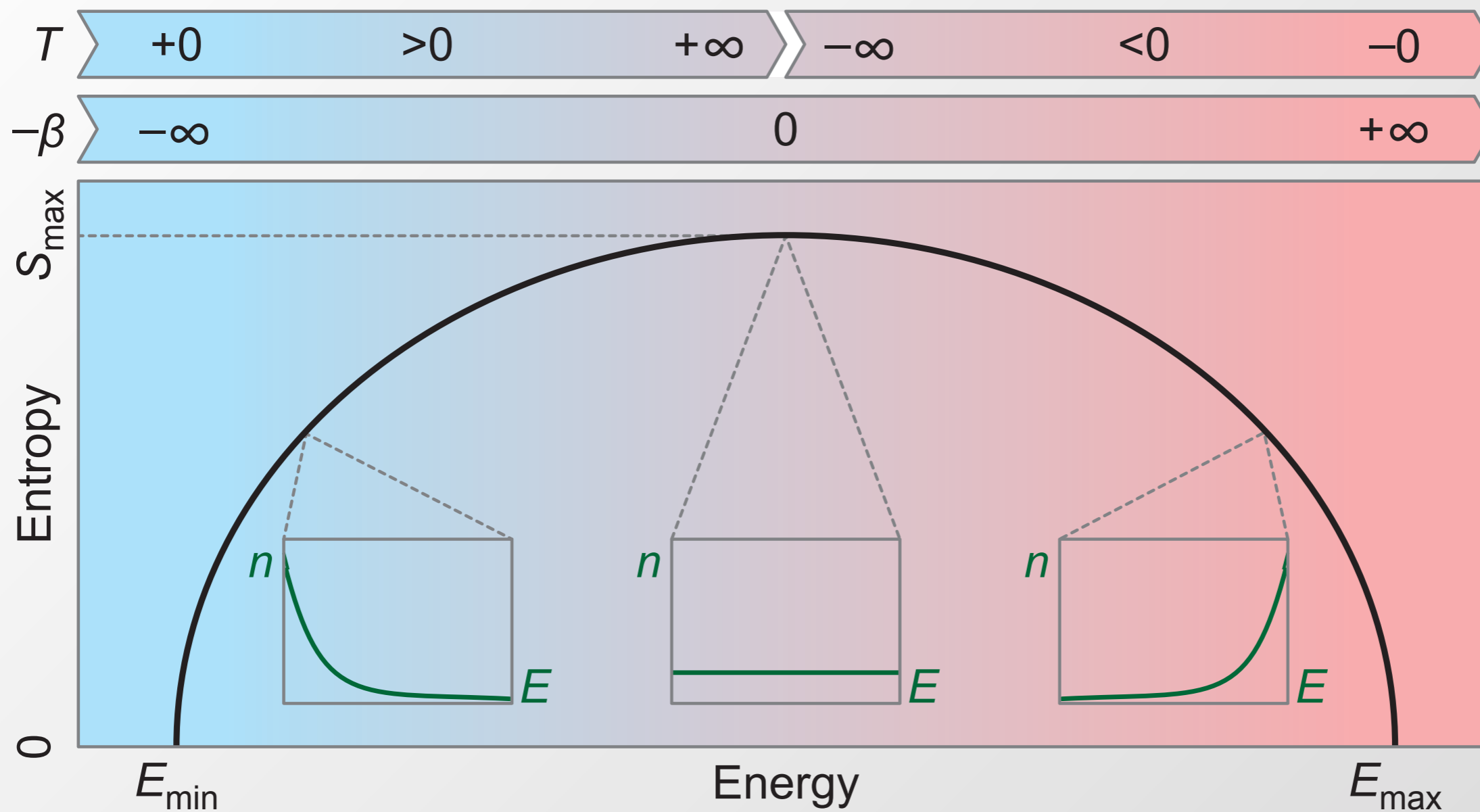


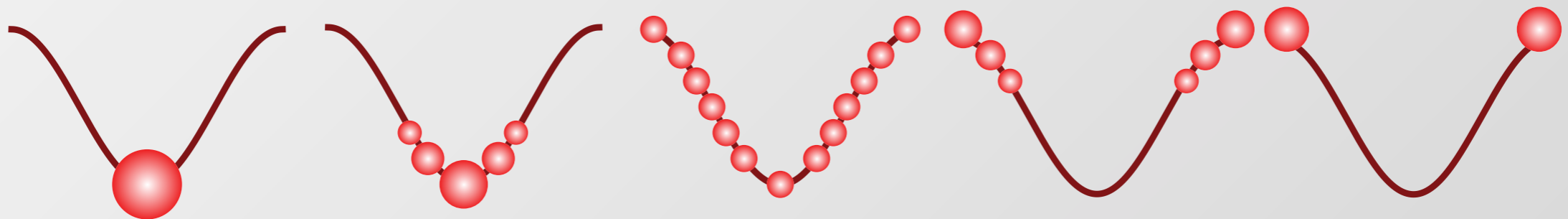
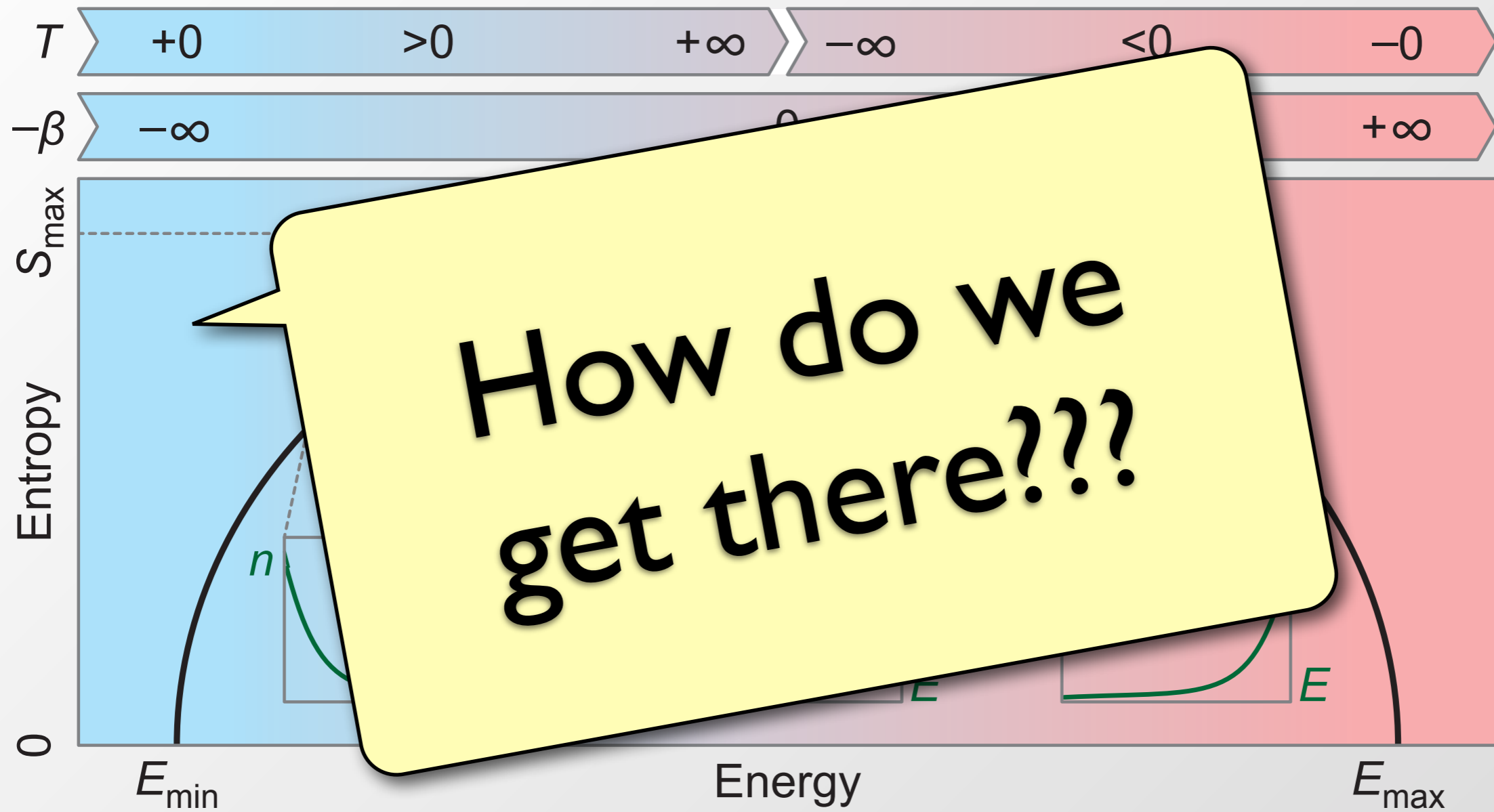


$$\hat{H} = -J \sum_{\langle i,j \rangle} \hat{a}_i^\dagger \hat{a}_j + \frac{U}{2} \sum_i \hat{n}_i (\hat{n}_i - 1) + V \sum_i \mathbf{R}_i^2 \hat{n}_i$$

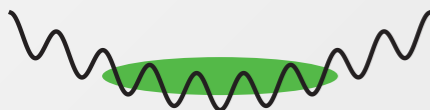
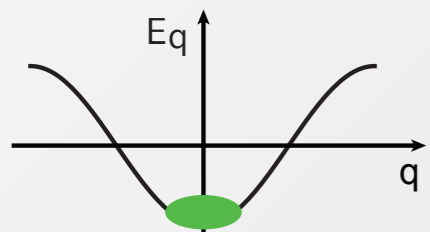
$U, V < 0$ required for upper energy bound!







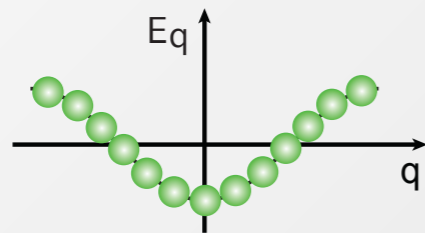
Superfluid



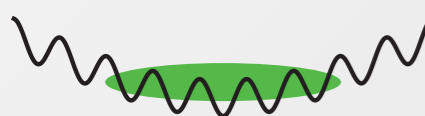
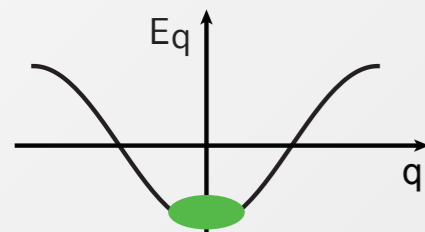
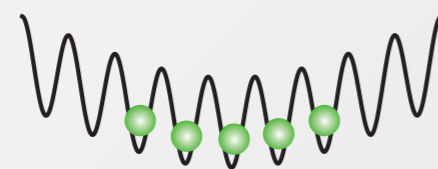
$$T, U, V > 0$$

Sequence: A. Rapp, S. Mandt & A. Rosch, PRL (2010)

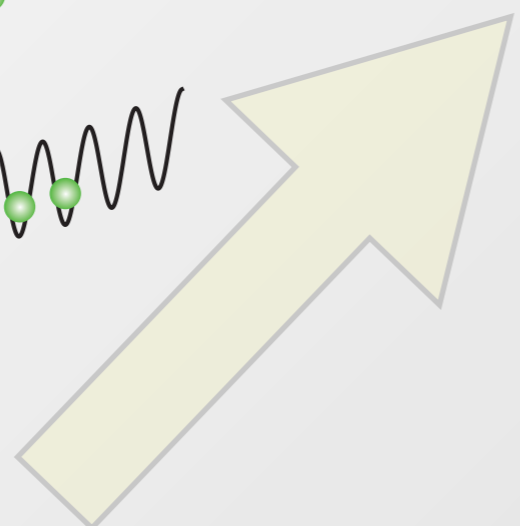
Mott Insulator



Superfluid

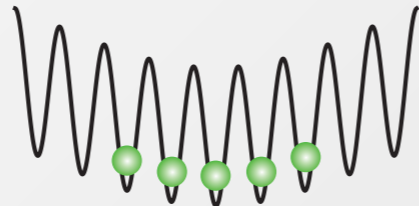
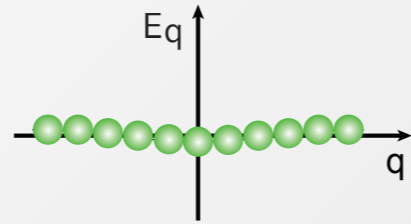


$T, U, V > 0$

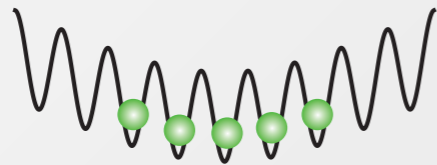
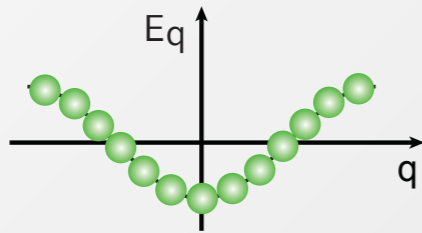


Sequence: A. Rapp, S. Mandt & A. Rosch, PRL (2010)

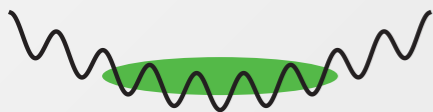
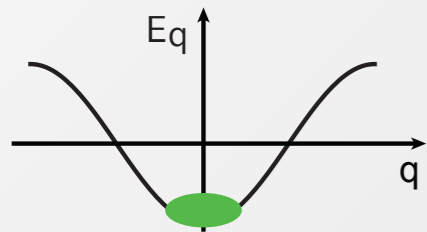
*Atomic Limit
Mott Insulator*



Mott Insulator



Superfluid

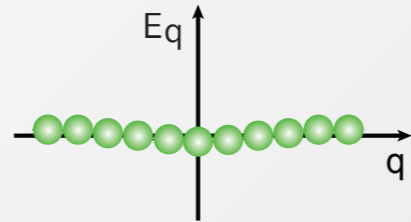


$T, U, V > 0$

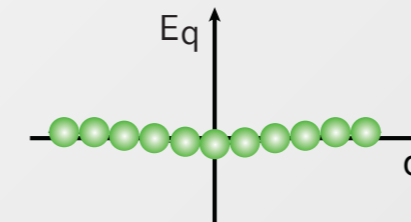
Sequence: A. Rapp, S. Mandt & A. Rosch, PRL (2010)

$U \rightsquigarrow -U \quad V \rightsquigarrow -V$

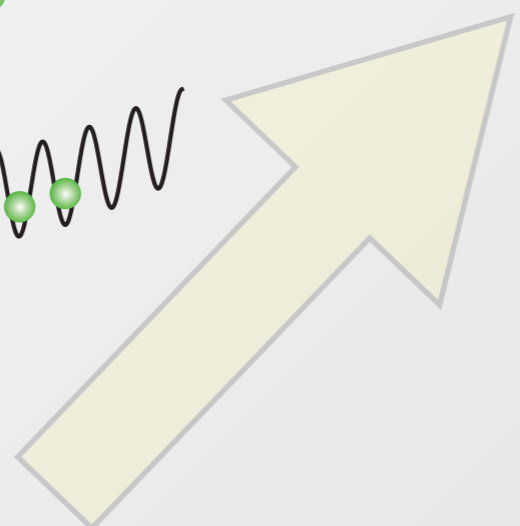
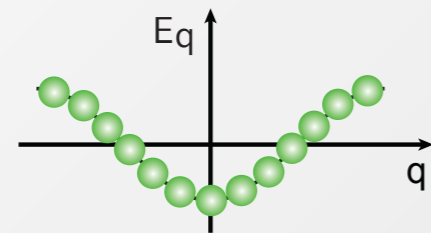
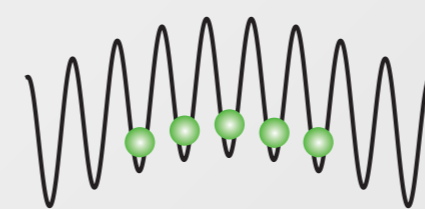
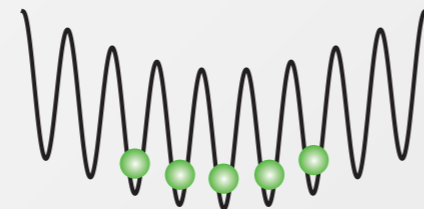
*Atomic Limit
Mott Insulator*



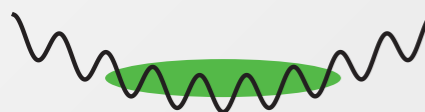
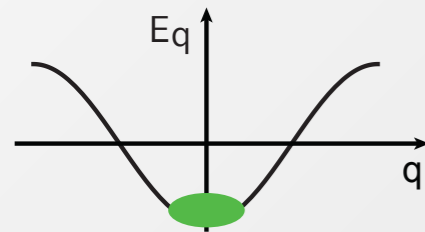
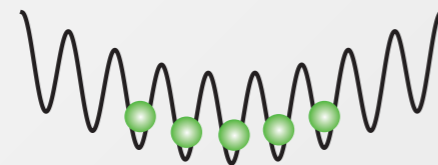
*Atomic Limit
Mott Insulator*



Mott Insulator



Superfluid

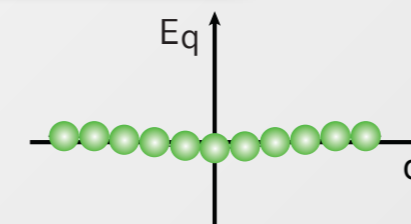
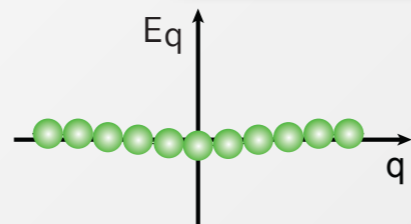


$T, U, V > 0$

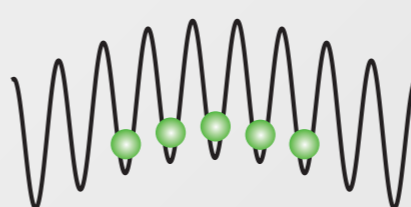
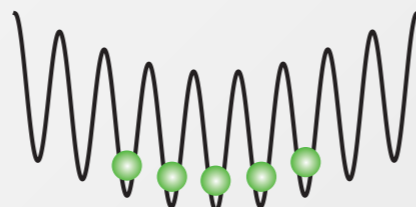
Sequence: A. Rapp, S. Mandt & A. Rosch, PRL (2010)

$U \rightarrow -U \quad V \rightarrow -V$

Atomic Limit
Mott Insulator

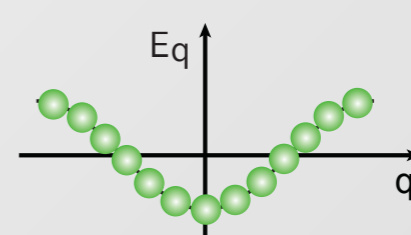
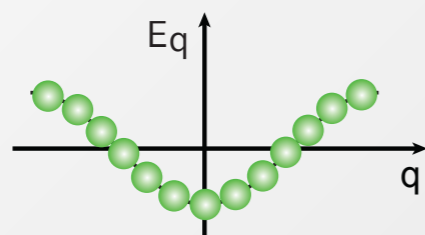


Atomic Limit
Mott Insulator



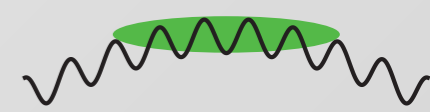
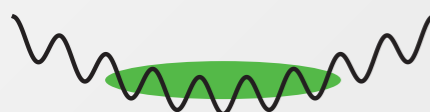
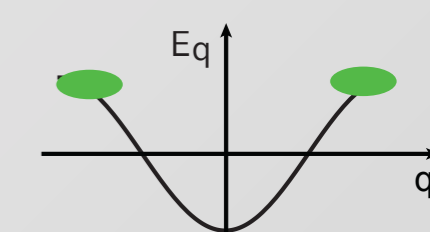
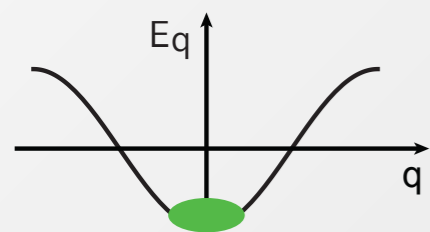
Mott Insulator

Mott Insulator



Superfluid

Superfluid

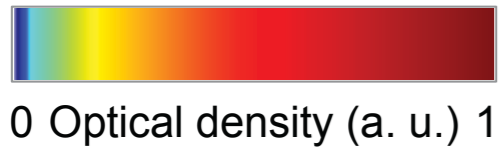
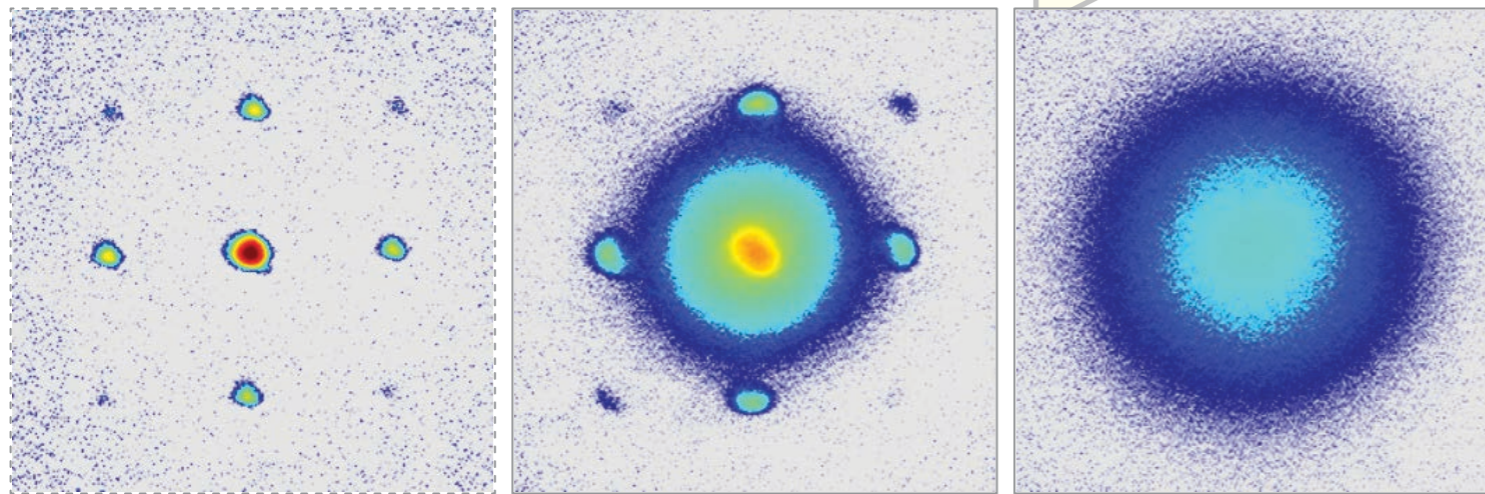


$T, U, V > 0$

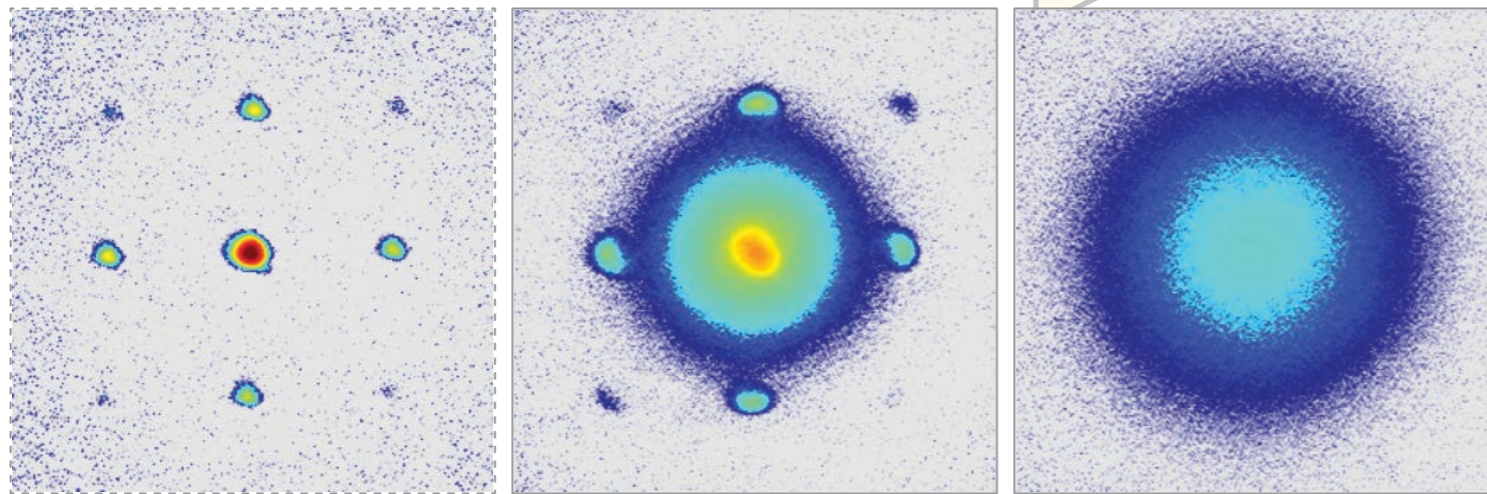
$T, U, V < 0$

Sequence: A. Rapp, S. Mandt & A. Rosch, PRL (2010)

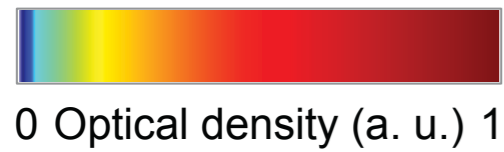
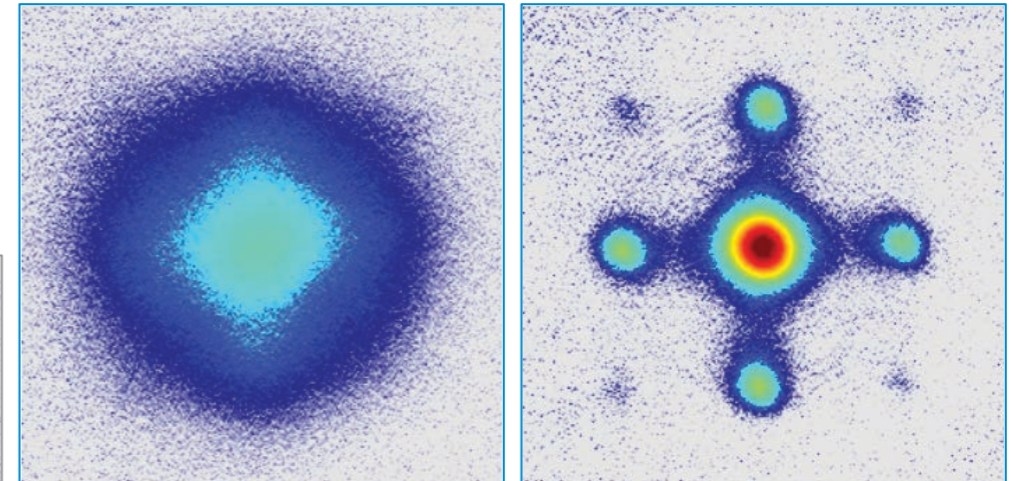
SF to MI

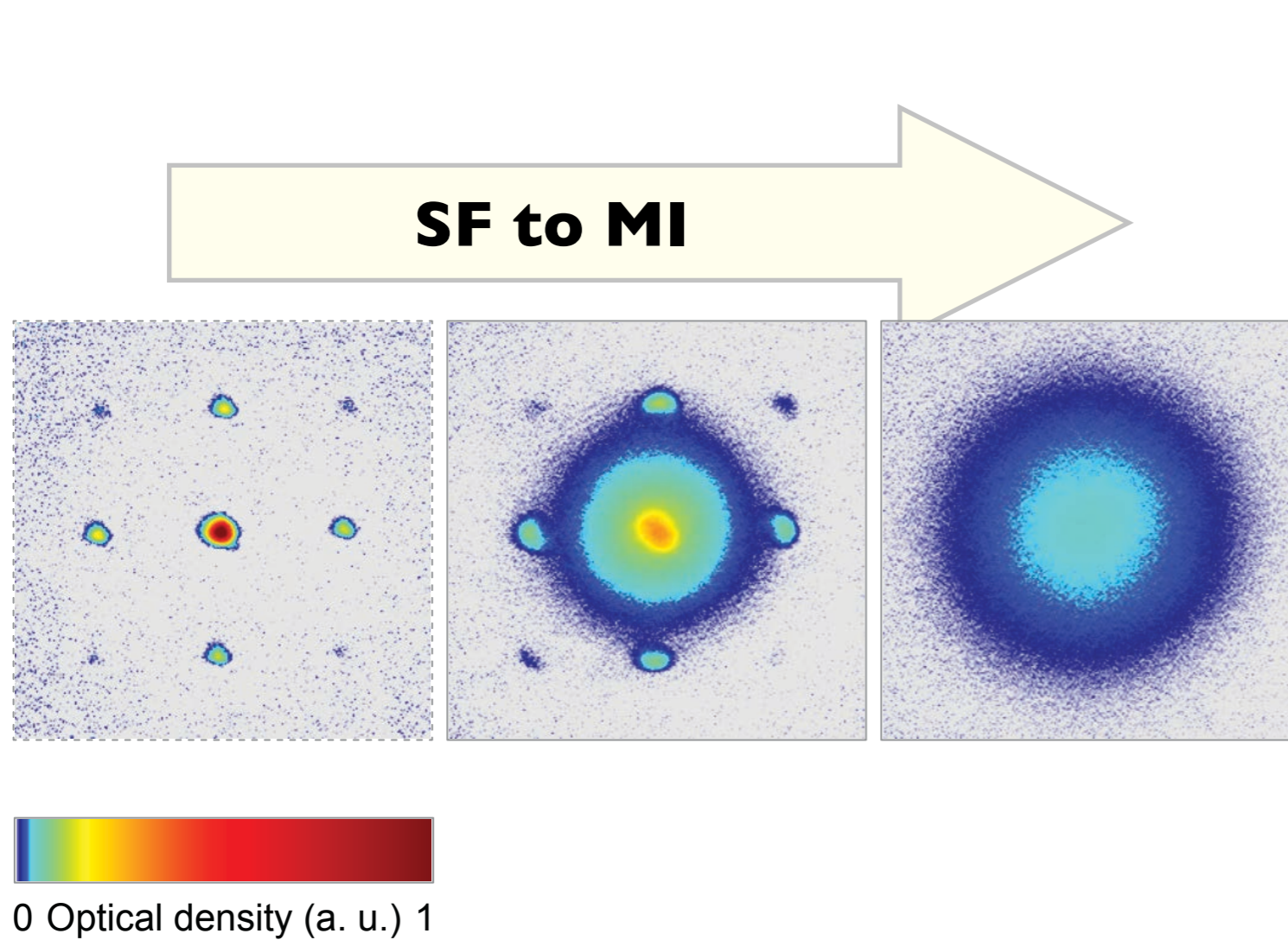


SF to MI

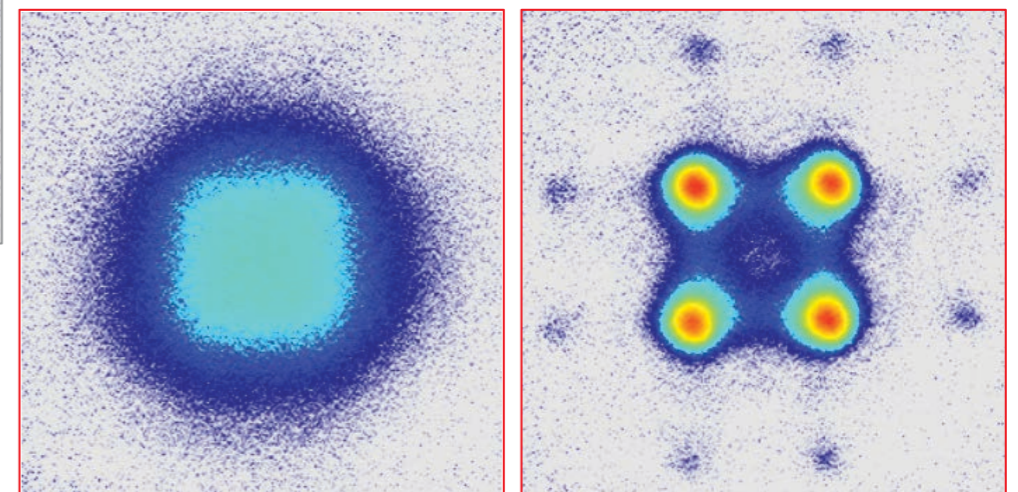
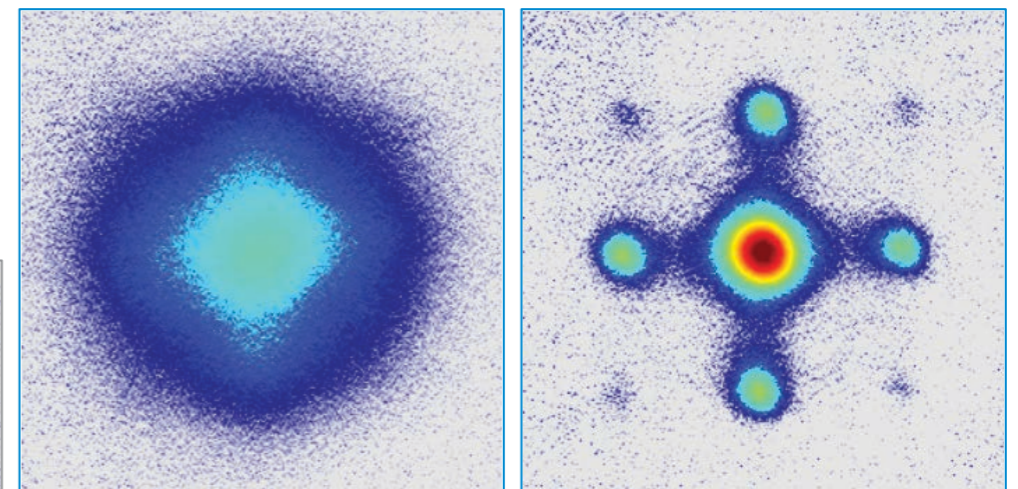


Positive Temperature w/o switching



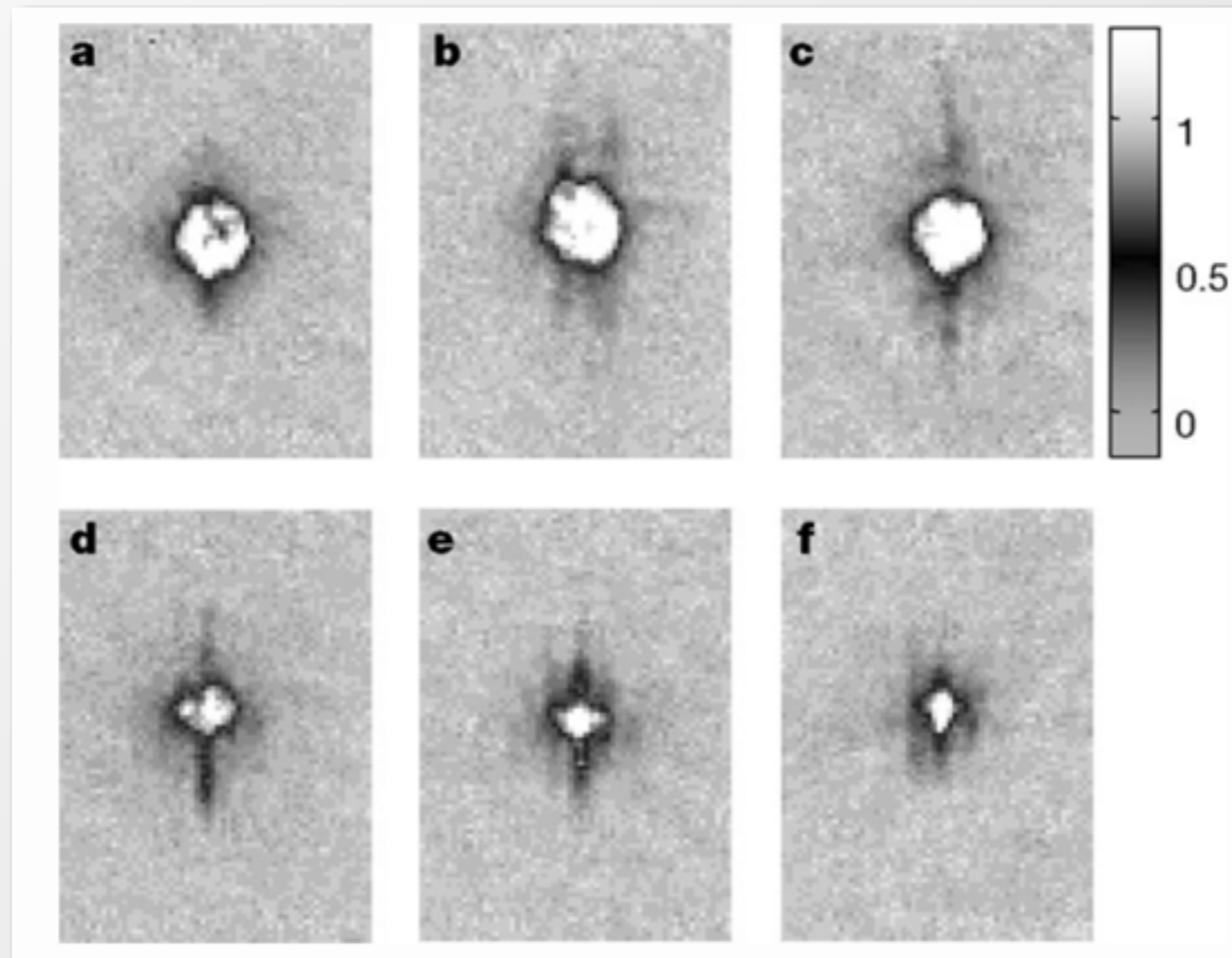


Positive Temperature w/o switching



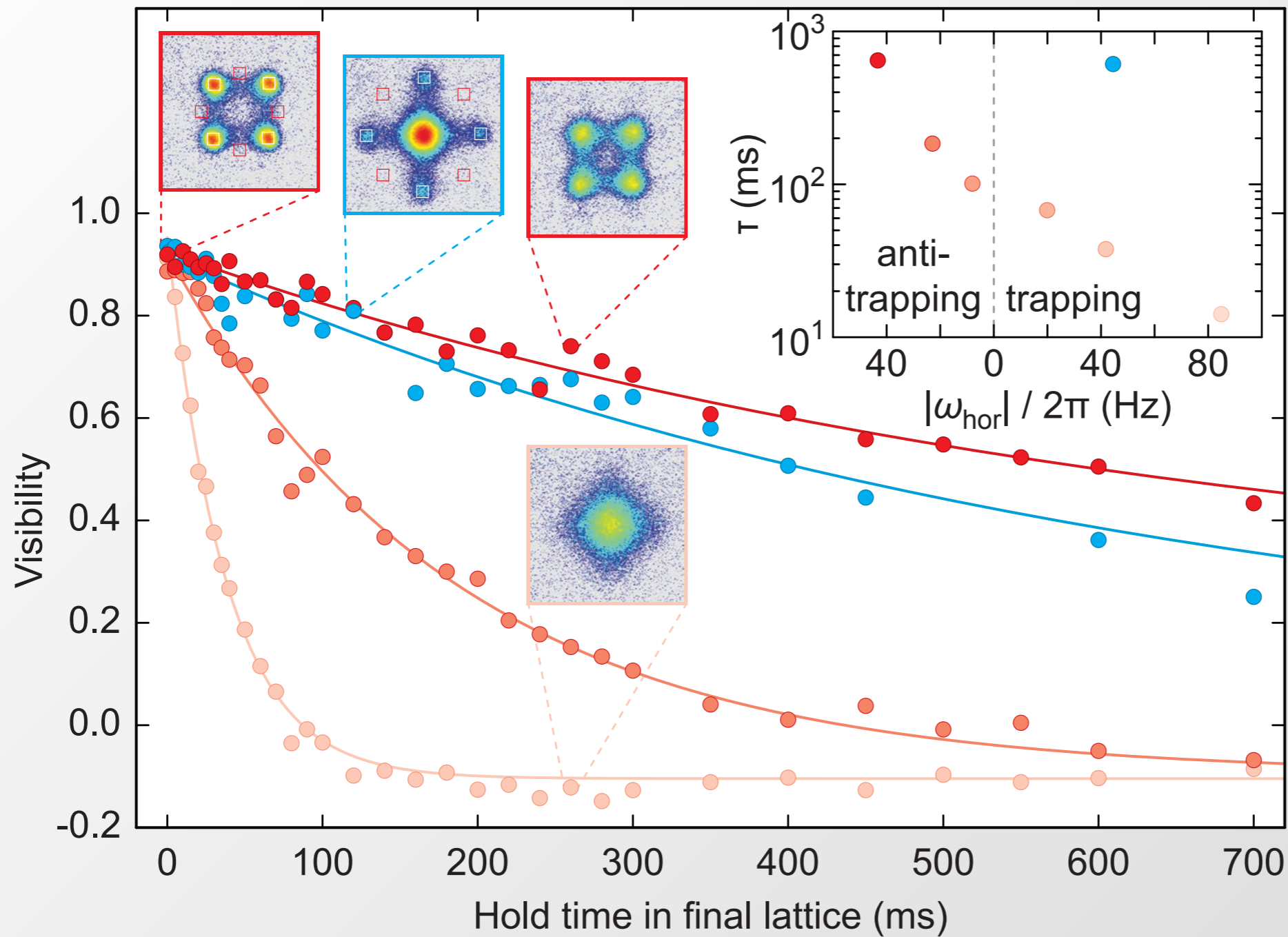
Negative Temperature w switching

For attractive interactions ($a < 0$), **condensate collapses!**



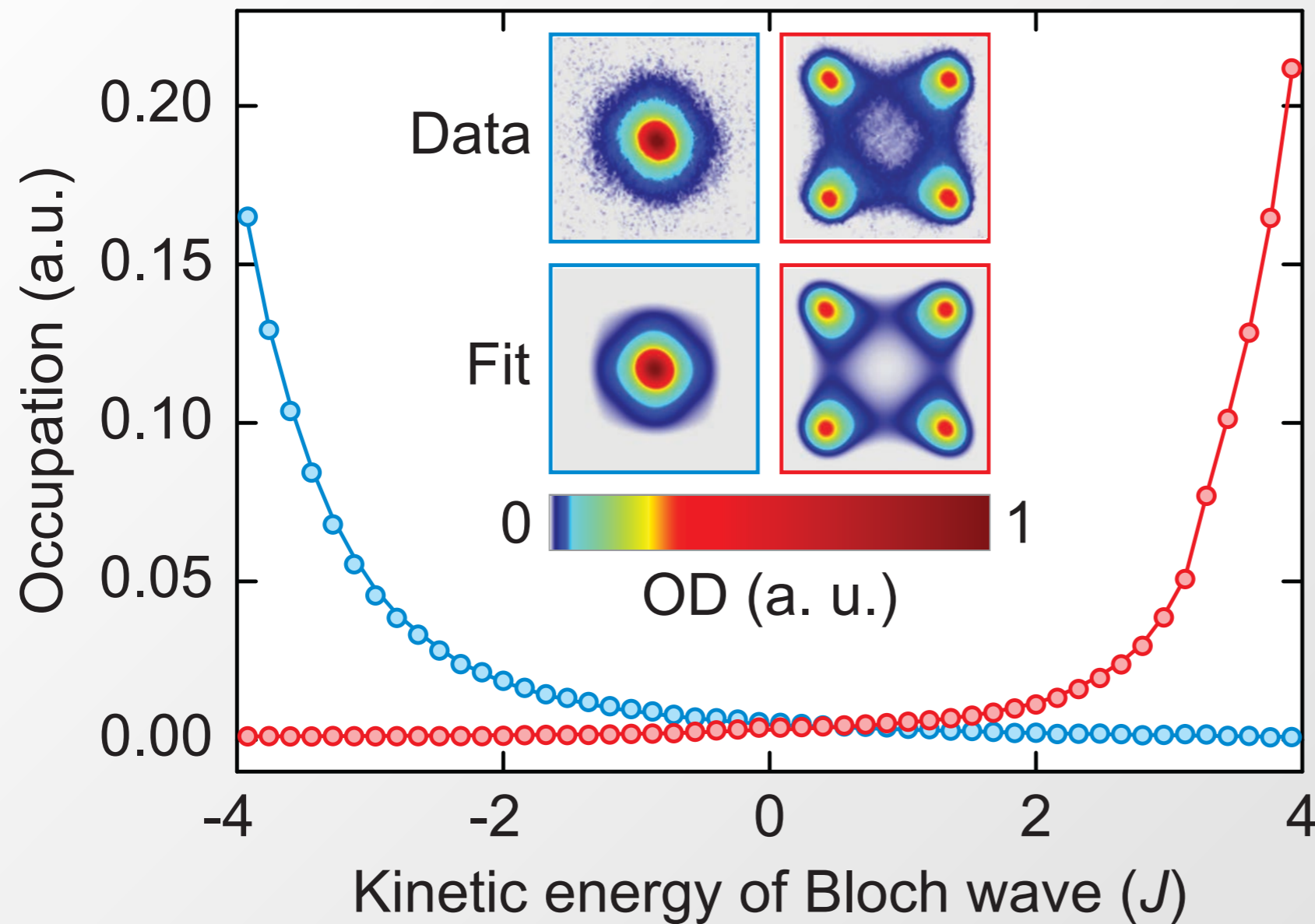
E.A. Donley et al. *Nature* **412**, 295-299 (2001)

J. M. Gerton et al. *Nature* **408**, 692 (2000)



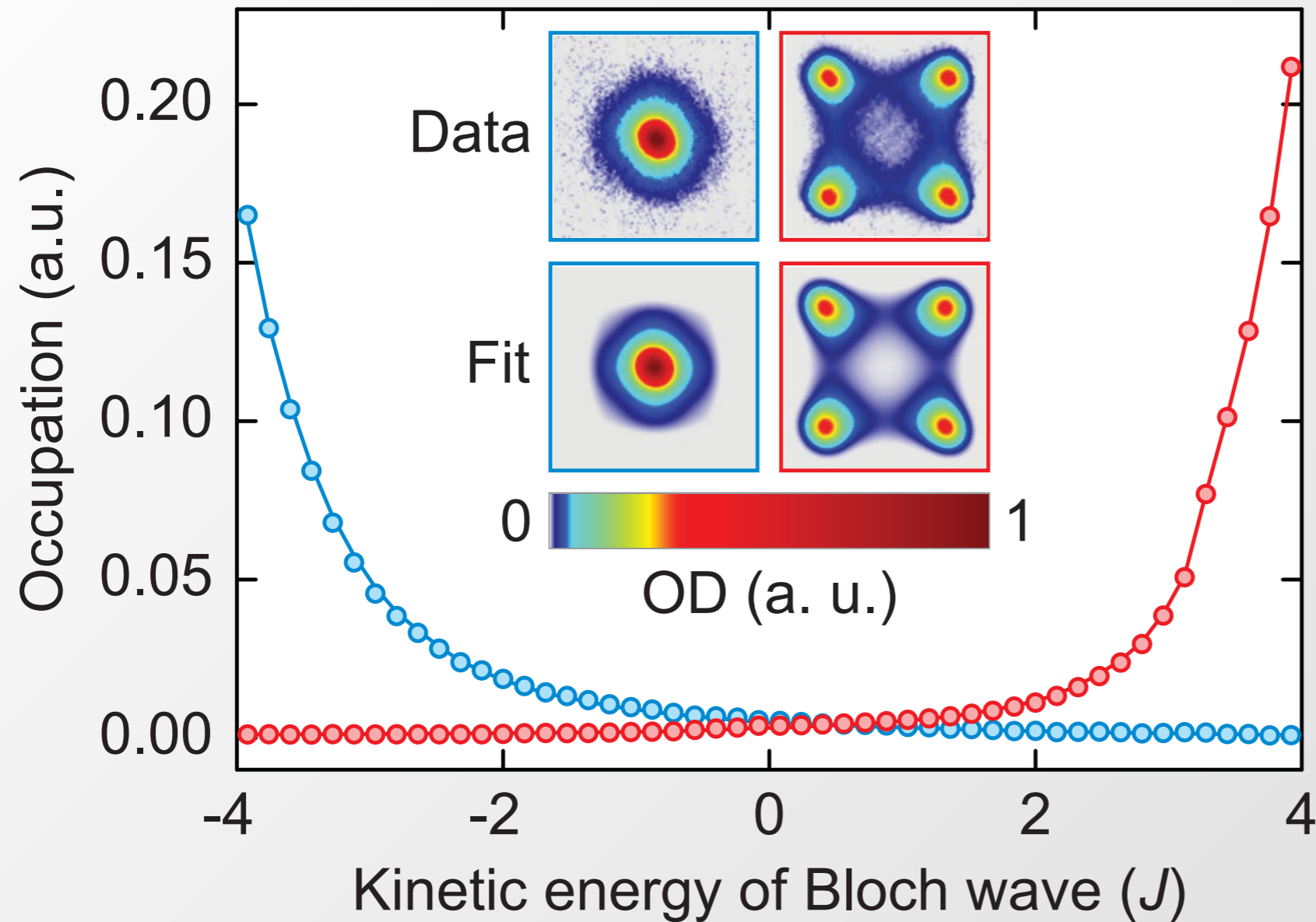
Negative Temperature State as Stable as Positive Temperature State!





$$n(q_x, q_y) = \frac{1}{e^{(E_{kin}(q_x, q_y) - \mu) / k_B T} - 1}$$

$$E_{kin}(q_x, q_y) = -2J [\cos(q_x d) + \cos(q_y d)]$$



$$T = -2.2J/k_B$$

$$n(q_x, q_y) = \frac{1}{e^{(E_{kin}(q_x, q_y) - \mu)/k_B T} - 1}$$

$$E_{kin}(q_x, q_y) = -2J [\cos(q_x d) + \cos(q_y d)]$$



Gases with **negative temperature** possess **negative pressure**!

$$\left. \frac{\partial S}{\partial V} \right|_E \geq 0 \quad \text{and} \quad dE = TdS - PdV$$

$$\Rightarrow \left. \frac{\partial S}{\partial V} \right|_E = \frac{P}{T} \geq 0$$



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Carnot engines **above unit efficiency!**

$$\eta = \frac{W}{Q_1} = 1 - \frac{T_2}{T_1}$$

Gases with **negative temperature** possess **negative pressure!**

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Carnot engines **above unit efficiency!**

$$\eta = \frac{W}{Q_1} = 1 - \frac{T_2}{T_1}$$

Some statements for the second law of thermodynamics become invalid!



Negative Temperature Team



Simon Braun



Sean Hodgman



Philipp Ronzheimer



Ulrich Schneider



Michael Schreiber





Takeshi
Fukuhara



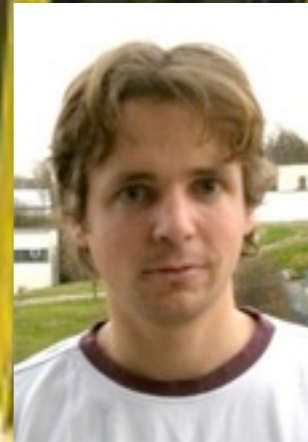
Peter
Schauß



Ahmed
Omran



David Bellem



Manuel
Endres



Christof
Weitenberg

Single Atom Team



Jacob
Sherson



Christian
Groß



Marc
Cheneau



Stefan
Kuhr



Immanuel
Bloch



Sebastian
Hild

Rosa Glöckner
& Ralf Labouvie



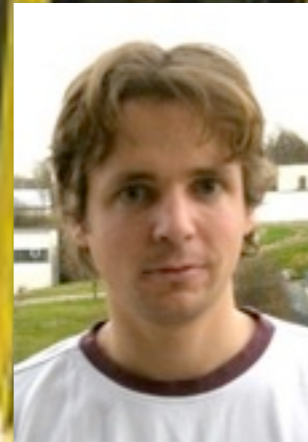
Peter Schauß



Ahmed Omran



David Bellem



Manuel Endres



Christof Weitenberg



Takeshi Fukuhara

Single Atom Team



Wolfgang Ketterle



Jacob Sherson



Immanuel Bloch



Christian Groß



Marc Cheneau



Stefan Kuhr



Sebastian Hild



Christophe Salomon

Rosa Glöckner & Ralf Labouvie

Thank you for your attention!

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