Standard Model physics with ATLAS A selection of results with major MPP contributions



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ATLAS experiment makes precision measurement of top-quark mass

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The top quark is SATLAS copionity produced at the LHC, allowing measurements of its properties. The mass of the top quark, man plays a special role in the Standard Model (SM) of particle physics. It is a key part of the mechanism of electroweak symmetry breaking and one of the parameters governing the stability of the universe in the SM. Following years of meticalous work

ATLAS presented a new measurement of m... at the 10th International Workshop on Too Oaark Physics held in Brasa, Portnaal, in late Sectember. The measurement was performed using around 100,000 protonproton collision events at an energy of 8 TeV, each containing a top-quark pair reconstructed in the sinale-lepton final state. In this chaunel, each top quark immediately decays to a W boson and a bottom made, and one W boson deems to an electron or moon and a neutrino, while the second W boson decays to two light quarks. A simultaneous measurement of mtogether with a global jet energy scale factor in the tingle-lepton channel at 7 TeV and a relative bottom-to-light jet-energy

scale factor was performed. The inclusion of these scale factors strongly reduces systematic uncertainties. The precision of the measurement is further improved by differentiating between correctly reconstructed top-court correct and events



(Left) The reconstructed top-mark mass recorded at 8 TeV together with the best-\$t townlote (Riald) the new ATLAS combined result compared to those from other experiments

where the final-state objects are incorrectly thereby reducing the correlation among the measurements. The combined result thus has assigned to the two top quarks. While only retaining 40% of the events, the total a 41% smaller uncertainty than the single uncertainty is improved by 19%, leading to a most precise measurement. The current combined value is 172 51+0 50 GeV with a The newer of this measurement, which relative precision of 0.29%, which is reainly is the second most precise individual Smited by the calibration of the ist emeral ton, mark mass measurement made by scales and is similar to that of the leading ATLAS to date, is revealed when combined sinale-experiment combined measurements with onevious ATLAS measurements The current precision on m ... represents a significant achievement that demonstrates and the dilepton channel at 8 TeV. This the precise understanding of all the relevant combination relies on a careful evaluation aspects of the ATLAS detector. The of the correlation between measurements measurement will allow further and deeper tests of the consistency of the SM. In both channels at 8 TeV, the analysis optimisation trades reduced systematic Further reading

Further reading ATLAS Collaboration 2017 ATLAS, CONF, 2017, 071

against increased statistical uncertainty. MPP Project Review 2017 18-19 December 2017 || Munich, Germany



Outline

- Dataset used
 - ▶ 20.2 fb⁻¹ of pp collision data recorded by ATLAS
 - ► Collisions provided by the LHC at a centre-of-mass energy of $\sqrt{s} = 8 \text{ TeV}$
- Measurements made
 - WW/WZ (WV or diboson) production in semi-leptonic decays ¹
 - ★ Fiducial cross-section measurement
 - Search for anomalous triple gauge-boson couplings (aTGCs)
 - Top quark mass (m_{top}) measurements
 - $\star\,$ In the $t\overline{t} \rightarrow$ all-jets channel 2
 - \star In the $t\overline{t} \rightarrow$ lepton+jets channel ³
 - ★ New ATLAS combination ³
- Conclusions

¹Eur. Phys. J. C 77 (2017) 563 \parallel ²JHEP 09 (2017) 118 \parallel ³ATLAS-CONF-2017-071



Torold Magnets Solenoid Magnet SCT Tracker Pixel Detector TRT Tracker



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SM physics with ATLAS

WV cross-section and search for aTGCs

- Motivation
 - Measurements of diboson production are powerful probes of the electroweak part of the Standard Model (SM)
 - ★ Especially the structure of the TGC
 - Cannot separate WW from WZ, so combine as WV
- Goals
 - Measure the semi-leptonic $WV
 ightarrow \ell
 u qq$ cross-section
 - Search for beyond-the SM (BSM) enhancements of diboson production in the form of aTGCs
- Analysis channels
 - Resolved topology
 - * Hadronic W/Z reconstructed as two separate jets (jj)
 - Boosted topology
 - * Hadronic W/Z reconstructed as one large-R jet (J)



Measurement strategy



Cross-section measurement:

t

- Signal-to-background ratio (S/B)
 - $\blacktriangleright~\sim 5\%~(\sim 10\%)$ for resolved (boosted)
 - Dominant background: W+jets
- Signal extracted by Maximum-Likelihood (ML) fit to the dijet mass (m_{jj}) or the mass of the large-R jet (m_J)



Search for aTGCs:

- aTGCs enhance the event rate of bosons with high transverse momentum (p_T)
 - Search for deviations from the SM in the p_T(jj) and p_T(J) distributions
- \bullet Added event requirement to increase S/B
 - 65 GeV $< m_{jj}/m_J <$ 95 GeV

Results

Extracted fiducial cross-section results:

- Resolved channel: $\sigma_{\rm fid}$ = 209 \pm 28 (stat) \pm 45 (syst) fb \rightarrow 4.5 σ significance
- Boosted channel: $\sigma_{\rm fid} = 30 \pm 11 \; ({\rm stat}) \pm 22 \; ({\rm syst}) \; {\rm fb} \; \rightarrow \; 1.3\sigma$ significance
- Dominant systematic uncertainties from MC modelling



Search results for aTGCs:

- No significant deviation from the SM prediction is observed
- Constraints computed for aTGC parameters
- Boosted channel significantly more sensitive to the new-physics parameters
- Constraints are comparable to previous most-stringent constraints from other diboson analyses

$m_{\rm top}$ measurements: Motivation

The top quark

- Heaviest elementary particle discovered
 - Decays before it can hadronise
 - \star t \rightarrow Wb nearly 100% of the time
- $m_{\rm top}$ is a fundamental parameter of the SM important for:
 - Precision tests of the SM
 - Tests of new physics scenarios
- The LHC is a top quark factory
 - Primarily produced is pairs $(t\bar{t})$
 - $t\bar{t}$ decay channels defined by W decays
 - all-jets: highest rate, but largest background
 - lepton+jets: medium rate, but better purity
 - dilepton: lowest rate and incomplete kinematics, but best purity



$m_{\rm top}$ measurements: Strategies

- \bullet Direct measurements of $m_{\rm top}$ in ATLAS use the template method
 - Reconstructed variable distributions sensitive to *m*_{top} are fit to analytical functions parameterised as functions of the input top quark mass
- However, reconstruction of the $t\bar{t}$ decay requires the use of jets
 - Large sensitivity to uncertainties in the jet energy scale (JES) and b-to-light jet energy scale (bJES)
- Two primary strategies to reduce the uncertainty in m_{top} induced by variations in the JES
 - ► I. Find an m_{top}-sensitive variable with some built-in protection (e.g. all-jets measurement)
 - II. Make an in-situ calibration of global jet energy scale factors (e.g. lepton+jets measurement)



$m_{ m top}$ in the $t \overline{t} ightarrow$ all-jets channel: Strategy I

- Use a 1-Dimensional (1-D) template method
- Use the $R_{3/2}$ distribution as the estimator for $m_{\rm top}$: $R_{3/2} = \frac{m_{qqb}}{m_{qq}} \propto "\frac{{\sf JES} + {\sf bJES}}{{\sf JES}}$ "
 - Protected from variations in the JES (see comparison to m_{jjj} below left \rightarrow middle)
 - Retains good sensitivity to $m_{
 m top}$ (see below right)



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Event topology

- Require at least 6 high-p_T central jets and a veto on leptons
 - At least two jets must be b-tagged

Background fraction is large: > 60%

- Made up of QCD multi-jet events
- Three control regions are used to determine the shape of the background from the data
 - ► The final background normalisation in the signal region is a free parameter in the m_{top}-extraction fit to the data



• A binned minimum χ^2 fit to the observed data results in

$m_{ m top} = 173.72 \pm 0.55(m stat) \pm 1.01(m syst)\, m GeV$ with a total uncertainty of 1.15~ m GeV

- Dominant systematic uncertainties (Δm_{top})
 - hadronisation modelling (0.64 GeV)
 - ► JES (0.60 GeV)
- 0.66% precision in $m_{\rm top}$
- 36% improvement over the 7 TeV all-jets measurement



$m_{ m top}$ in the $t \bar{t} ightarrow$ lepton+jets channel: Strategy II

- Make a simultaneous measurement of m_{top} with a jet energy scale factor (JSF) and a relative *b*-to-light-jet energy scale factor (bJSF)
- Use a multi-variate template method (developed in the 7 TeV lepton+jets analysis)
 - Templates constructed from simulated distributions of m_{top}^{reco} , m_{W}^{reco} , and R_{ba}^{reco}

 $R_{bq}^{\rm reco} = \frac{p_{\rm T}^{b_{\rm had}} + p_{\rm T}^{b_{\rm lep}}}{p_{\rm T}^{q_1} + p_{\rm T}^{q_2}} \propto "\frac{{\sf JSF}*{\sf bJSF}}{{\sf JSF}}", \text{ where } q_1 \text{ and } q_2 \text{ are light jets from the } W \text{ boson}$



Results

• Simultaneous unbinned maximum likelihood fit to the distributions in data results in

 $m_{
m top} = 172.08 \pm 0.39(
m stat) \pm 0.82(
m syst)$ GeV with a total uncertainty of 0.91~
m GeV~(0.53%)

- Dominant sources of uncertainty
 - ► JES (0.54 GeV) and *b*-tagging (0.38 GeV)
- 29% improvement over the 7 TeV $m_{
 m top}^{
 m l+jets}$
- Traded large sample size for smaller total uncertainty using a sample reduction via a multivariate analysis (BDT)
 - Reduces the total uncertainty by 19%!!
 - Resolution improves considerably
 - ★ Removes 60% of events with very little increase in statistical uncertainty



- Yellow filled area is best fit to data
- Blue band is $\pm 1\sigma$ uncertainty on the fit

$m_{\rm top}$ combination: example with the two most precise ATLAS results

- Example combination of the two most precise measurements
- The **red** and **gray** lines indicate the precision of the input measurements
- The **blue curve** shows the uncertainty in the example combination as a function of the total correlation of the input measurements
 - ► Correlation is of utmost importance
- Careful **evaluation** of the estimator correlation for each source of uncertainty reveals small correlations
 - Much smaller than what is usually assigned



New preliminary ATLAS combination of $m_{ m top}$

- Evolution of the combination when adding one measurement at a time
 - all-jets measurements not yet included
- No significant improvement is observed below the line in red
- New preliminary ATLAS combination:

 $m_{
m top}^{
m comb}=172.51\pm0.50\,\,{
m GeV}$

• Compare to the previous ATLAS combination:

```
m_{
m top}^{
m comb} = 172.84 \pm 0.70 GeV
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- \bullet a 29% improvement w.r.t. the previous ATLAS combination
- \bullet a 41% improvement w.r.t. the most precise input measurement

- LHC combinations have smaller systematic uncertainties than Tevatron ones
- ATLAS and CMS combinations nearly coincide and have comparable precision
 - CMS has more precise individual measurements
 - ATLAS has smaller correlations



Conclusions and remarks

- WV production measurements
 - Resolved channel observed significance of 4.5σ
 - Boosted channel observed significance of 1.3σ
 - \blacktriangleright No deviation from the SM \rightarrow constraints on aTGCs
- ATLAS has measured $m_{
 m top}$ in all three $t ar{t}$ decay channels at two collision energies
 - Individual results since last MPP Project Review (all at $\sqrt{s} = 8 \text{ TeV}$)
 - * $m_{
 m top}^{
 m dil} = 172.99 \pm 0.84$ GeV
 - $\star~m_{
 m top}^{
 m all-jets} = 173.72 \pm 1.15$ GeV
 - $\star~m_{
 m top}^{
 m l+jets} = 172.08 \pm 0.91~{
 m GeV}$
 - New ATLAS combination
 - * $m_{
 m top}^{
 m comb} = 172.51 \pm 0.50 \,\, {
 m GeV}$
- Outlook
 - Include all-jets measurements in combination
 - Move to 13 TeV $m_{
 m top}$ analyses

| | $m_{ m top}^{ m all-jets}$ [GeV] | | $m_{ m top}^{ m l+jets}$ [GeV] | | $m_{ m top}^{ m dil}$ [GeV] | |
|-----------------------------------|----------------------------------|-----------------|--------------------------------|---------------------|-----------------------------|-----------------|
| | 7 TeV | 8 TeV | 7 TeV | 8 TeV | 7 TeV | 8 TeV |
| $m_{ m top}$ | 175.06 | 173.72 | 172.33 | 172.08 | 173.79 | 172.99 |
| Statistical unc. | 1.35 | 0.55 | 0.75 | 0.39 | 0.54 | 0.41 |
| Dominant syst uns | JES: 0.60 | JES: 0.60 | JES: 0.58 | JES: 0.54 | JES: 0.76 | JES: 0.54 |
| Dominant syst. unc. | bJES: 0.62 | Had: 0.64 | <i>b</i> -tag: 0.50 | <i>b</i> -tag: 0.38 | bJES: 0.68 | bJES: 0.30 |
| Total systematic unc. | 1.21 ± 0.16 | 1.01 ± 0.12 | $1.04~\pm~0.08$ | 0.82 ± 0.06 | 1.31 ± 0.07 | $0.74~\pm~0.05$ |
| Total uncertainty | $1.81~\pm~0.16$ | $1.15~\pm~0.12$ | 1.28 ± 0.08 | 0.91 ± 0.06 | 1.42 ± 0.07 | $0.84~\pm~0.05$ |
| $7 \rightarrow 8$ TeV improvement | 36% | | 29% | | 40% | |

$m_{\rm top}$ combination: example correlations of pairs of estimators

- Combination is performed using the Best Linear Unbiased Estimate (BLUE) method
- Correlations of each pair of measurements are evaluated for each uncertainty component
 - Example figure below for the two most precise measurements



- Pairwise Δm_{top} when simultaneously varying the pair of measurements for each systematic uncertainty
- Sizes of crosses indicate statistical precision of the systematic uncertainty components
- \bullet Correlated cases \rightarrow red full points
- \bullet Anti-correlated cases \rightarrow blue open points
- This pair of measurements has many significant anti-correlated components

$m_{\rm top}$ combination correlations: 7 and 8 TeV dilepton

- Combination is performed using the Best Linear Unbiased Estimate (BLUE) method
- Correlations of each pair of measurements are evaluated for each uncertainty component



- Pairwise $\Delta m_{\rm top}$ when simultaneously varying the pair of measurements for each systematic uncertainty
- Sizes of crosses indicate statistical precision of the systematic uncertainty components
- \bullet Correlated cases \rightarrow blue open points
- \bullet Anti-correlated cases \rightarrow red full points
- This pair of measurements is strongly correlated

$m_{\rm top}$ combination results: 7 and 8 TeV dilepton



- Combined value (left) and uncertainty (right) in the combination of the 7 and 8 TeV dilepton measurements as a function of their total correlation (blue line)
- The red and gray lines indicate the pair of input values (left) and uncertainties (right)
- $\bullet\,$ The uncertainty in the combined $\mathit{m}_{\mathrm{top}}$ strongly depends on the total correlation

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$m_{ m top}$ combination correlations: 7 TeV lepton+jets and 8 TeV dilepton

- Combination is performed using the Best Linear Unbiased Estimate (BLUE) method
- Correlations of each pair of measurements are evaluated for each uncertainty component



- Pairwise Δm_{top} when simultaneously varying the pair of measurements for each systematic uncertainty
- Sizes of crosses indicate statistical precision of the systematic uncertainty components
- \bullet Correlated cases \rightarrow blue open points
- \bullet Anti-correlated cases \rightarrow red full points
- This pair of measurements has roughly equal correlated and anti-correlated components

$m_{\rm top}$ combination results: 7 TeV lepton+jets and 8 TeV dilepton



- Combined value (left) and uncertainty (right) in the combination of the 7 TeV lepton+jets and 8 TeV dilepton measurements as a function of their total correlation (blue line)
- The red and gray lines indicate the pair of input values (left) and uncertainties (right)
- $\bullet\,$ The uncertainty in the combined ${\it m}_{\rm top}$ strongly depends on the total correlation

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$m_{ m top}$ in the $t\bar{t} ightarrow$ lepton+jets channel: Optimisation

Event topology

- Require one high-p_T electron or muon and at least four high-p_T central jets
 - Exactly two jets must be b-tagged

Multi-Variate Analysis (MVA) technique

- Train a Boosted Decision Tree (BDT) algorithm on $t\bar{t}$ signal to distinguish wrongly/unmatched events from correctly matched events
 - Wrongly/unmatched events expected to have larger systematic uncertainties
- Chose a cut on the BDT output that minimises the total uncertainty in $m_{\rm top}$

Background fraction is only $\sim 1\%$



- 19% improvement over no BDT (Standard)
- Reduces theory modelling uncertainties
- Also improves resolution in m_{top} as seen by flatness of the stat. unc. with the loss of > 60% of events

SM physics with ATLAS

$m_{\rm top}$ in the $t\bar{t} \rightarrow$ lepton+jets channel: data/MC agreement

- \bullet After applying the $r_{\rm BDT}$ cut, the background fraction is only 1%
- Single-top-quark production is included in signal
 - resulting in a background independent of $m_{
 m top}$
- Distributions of fit variables agree well with data within uncertainties
 - MC simulation is normalised to the data and only shape uncertainties remain in the band



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$m_{\rm top}$ in the $t\bar{t} ightarrow$ lepton+jets channel: results in data

• The simultaneous unbinned maximum likelihood fit to the three distributions in data results in:

 $m_{\rm top} = 172.08 \pm 0.39 ({\rm stat}) {
m GeV}$ $JSF = 1.005 \pm 0.001$ (stat) $bJSF = 1.008 \pm 0.005(stat)$ Events / GeV data I+iets Events / 0.05 data. I+iets data, I+iets ATLAS Preliminary ATLAS Preliminary TLAS Preliminary 1200 /s=8 TeV, 20.2 fb s=8 TeV. 20.2 fb Best fit backgroun Best fit background s=8 TeV. 20.2 fb⁻¹ Best fit background 1600E Events 160 **Best fit** Rost fit 1000 Uncertainty 1400 Uncertainty 1400 Uncertainty 1200 1200 80 1000 1000 600 800 800 600 400 600 400 200 200 130 140 150 160 190 70 80 15 m^{reco} [GeV] m^{reco} [GeV] $R_{ba}^{
m reco}$ $m_{\rm top}^{
m reco}$ $m_W^{
m reco}$

• Including systematic uncertainties, the result is:

 $m_{
m top} = 172.08 \pm 0.39 ({
m stat}) \pm 0.82 ({
m syst}) ~{
m GeV} = 172.08 \pm 0.91 ~{
m GeV}$

SM physics with ATLAS

$m_{ m top}$ in the $tar{t} ightarrow$ lepton+jets channel: uncertainties in $m_{ m top}$

- Dominant sources of uncertainty
 - ► JES (0.54 GeV) and *b*-tagging (0.38 GeV)
- Total uncertainty reduced with BDT sel.
 - 19% improvement over no BDT at 8 TeV
 - Reduces theory modelling uncertainties
 - Also improves resolution in m_{top} as seen by the scaling of the stat. unc.
 - * With no improvement in resolution: $\sigma_{\text{BDT}}^{\text{stat}} = \sigma_{\text{std}}^{\text{stat}} \sqrt{N_{\text{std}}/N_{\text{BDT}}} = 0.60$ as compared to 0.39
 - Altogether, a 29% improvement over the 7 TeV lepton+jets measurement

| | m_{top} [GeV] | | |
|--|----------------------------|-----------------|-----------------|
| | $\sqrt{s} = 7 \text{ TeV}$ | $\sqrt{s} =$ | 8 TeV |
| Event selection | Standard | Standard | BDT |
| Result | 172.33 | 171.90 | 172.08 |
| Statistics | 0.75 | 0.38 | 0.39 |
| $-Stat. comp. (m_{top})$ | 0.23 | 0.12 | 0.11 |
| – Stat. comp. (JSF) | 0.25 | 0.11 | 0.11 |
| - Stat. comp. (bJSF) | 0.67 | 0.34 | 0.35 |
| Method | 0.11 ± 0.10 | 0.04 ± 0.11 | 0.13 ± 0.11 |
| Signal Monte Carlo generator | 0.22 ± 0.21 | 0.50 ± 0.17 | 0.16 ± 0.17 |
| Hadronisation | 0.18 ± 0.12 | 0.05 ± 0.10 | 0.15 ± 0.10 |
| Initial- and final-state QCD radiation | 0.32 ± 0.06 | 0.28 ± 0.11 | 0.08 ± 0.11 |
| Underlying event | 0.15 ± 0.07 | 0.08 ± 0.15 | 0.08 ± 0.15 |
| Colour reconnection | 0.11 ± 0.07 | 0.37 ± 0.15 | 0.19 ± 0.15 |
| Parton distribution function | 0.25 ± 0.00 | 0.08 ± 0.00 | 0.09 ± 0.01 |
| Background normalisation | 0.10 ± 0.00 | 0.04 ± 0.00 | 0.08 ± 0.00 |
| W+jets shape | 0.29 ± 0.00 | 0.05 ± 0.00 | 0.11 ± 0.00 |
| Fake leptons shape | 0.05 ± 0.00 | 0 | 0 |
| Jet energy scale | 0.58 ± 0.11 | 0.63 ± 0.02 | 0.54 ± 0.02 |
| Relative b-to-light-jet energy scale | 0.06 ± 0.03 | 0.05 ± 0.01 | 0.03 ± 0.01 |
| Jet energy resolution | 0.22 ± 0.11 | 0.23 ± 0.03 | 0.20 ± 0.04 |
| Jet reconstruction efficiency | 0.12 ± 0.00 | 0.04 ± 0.01 | 0.02 ± 0.01 |
| Jet vertex fraction | 0.01 ± 0.00 | 0.13 ± 0.01 | 0.09 ± 0.01 |
| <i>b</i> -tagging | 0.50 ± 0.00 | 0.37 ± 0.00 | 0.38 ± 0.00 |
| Leptons | 0.04 ± 0.00 | 0.16 ± 0.01 | 0.16 ± 0.01 |
| $E_{\rm T}^{\rm miss}$ | 0.15 ± 0.04 | 0.08 ± 0.01 | 0.05 ± 0.01 |
| Pile-up | 0.02 ± 0.01 | 0.14 ± 0.01 | 0.15 ± 0.01 |
| Total systematic uncertainty | 1.03 ± 0.08 | 1.07 ± 0.10 | 0.82 ± 0.06 |
| Total | 1.27 ± 0.08 | 1.13 ± 0.10 | 0.91 ± 0.06 |

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SM physics with ATLAS

Munich, Germany || 19 December 2017

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$m_{ m top}$ in the $t \bar{t} ightarrow$ all-jets channel: Extras

| Sources of uncertainty in m_{tc} | • | Sources | of | uncertainty | in | $m_{ m top}$ | |
|--|---|---------|----|-------------|----|--------------|--|
|--|---|---------|----|-------------|----|--------------|--|

 $\blacktriangleright \ {\rm See \ table} \rightarrow$

• Functional form for fit

- Signal: sum of a Novosibirsk function and a Landau function
- Background: sum of a Gaussian function and a Landau function

| Source of uncertainty | $\Delta m_{\rm top} \ [{\rm GeV}]$ |
|--|------------------------------------|
| Monte Carlo generator | 0.18 ± 0.21 |
| Hadronisation modelling | 0.64 ± 0.15 |
| Parton distribution functions | 0.04 ± 0.00 |
| Initial/final-state radiation | 0.10 ± 0.28 |
| Underlying event | 0.13 ± 0.16 |
| Colour reconnection | 0.12 ± 0.16 |
| Bias in template method | 0.06 |
| Signal and bkgd parameterisation | 0.09 |
| Non all-hadronic $t\bar{t}$ contribution | 0.06 |
| ABCD method vs. ABCDEF method | 0.16 |
| Trigger efficiency | 0.08 ± 0.01 |
| $Lepton/E_T^{miss}$ calibration | 0.02 ± 0.01 |
| Overall flavour-tagging | 0.10 ± 0.00 |
| Jet energy scale (JES) | 0.60 ± 0.05 |
| b-jet energy scale (bJES) | 0.34 ± 0.02 |
| Jet energy resolution | 0.10 ± 0.04 |
| Jet vertex fraction | 0.03 ± 0.01 |
| Total systematic uncertainty | 1.01 |
| Total statistical uncertainty | 0.55 |
| Total uncertainty | 1.15 |

WV analysis: Confidence intervals for aTGC in EFT

- The constraints computed for aTGC parameters can be re-interpreted as constraints on parameters in an effective field theory (EFT)
 - Assuming the "LEP constraint" only three free parameters remain
 - > The resulting confidence intervals are shown in the figures below
 - ▶ Each parameter is constrained while the other two are fixed to 0 (their SM expectation)

