

# RooFit : Fitting of the $\Delta t$ Resolution Function

Vladimir Chekelian for discussion 19.12.2018

→ **Time dependent analyses:** *unbinned maximum likelihood fit to  $\Delta t = t_{B_{sig}} - t_{B_{tag}}$*   
maximum  $L = \prod_i P(\Delta t_i, \text{physics \& event reco parameters})$ , where

$$P_{sig, bkg}(\Delta t) = \int_{-\infty}^{+\infty} d(\Delta t') \mathcal{P}_{sig, bkg}(\Delta t') R_{sig, bkg}(\Delta t - \Delta t')$$

→ **Fitting of the Resolution Function  $R_{sig, bkg}(\Delta t - \Delta t')$ :**

- using RooFit package in Root and MC of  $B^0 B^0_{bar}$  ( $B_{sig} \rightarrow J/\Psi K^0_s$ )
- make fits of  $\Delta t$ -pulls corresponding to  $(\Delta t_{rec} - \Delta t_{true}) / \delta_{ev}(\Delta t)$  (errors per event)
- $\Delta t$ -pull distribution is equivalent to  $\Delta t$  resolution function with transformation:  
parameters ( $\Delta t$ -pull model)  $\rightarrow$  parameter  $\cdot \delta_{ev}(\Delta t)$  ( $\Delta t$  resolution function)  
e.g.  $Gauss(dtPull, \mu, \sigma) \rightarrow Gauss(dt, \mu \cdot \delta_{ev}(\Delta t), \sigma \cdot \delta_{ev}(\Delta t))$
- $\Delta t$ -pulls are fitted by three gaussian functions:

$$f_1 \cdot G_1(dtPull, \mu_1, \sigma_1) + f_2 \cdot G_2(dtPull, \mu_2, \sigma_2) + (1 - f_1 - f_2) \cdot G_3(dtPull, \mu_3, \sigma_3)$$

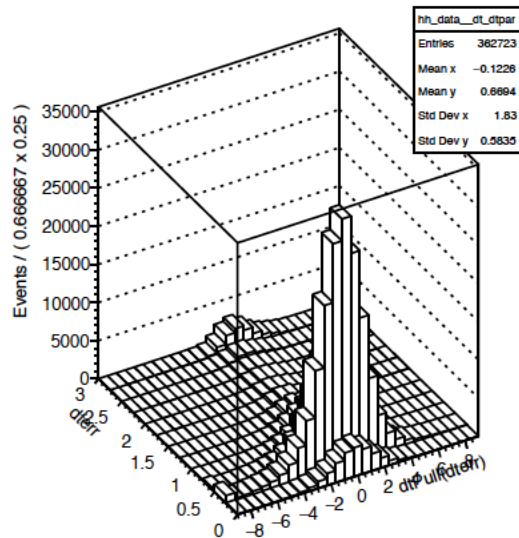
$G_1$ :  $\mu_1 = c_0 + c_1 \cdot evpar$ ,  $\sigma_1 = s_0 + s_1 \cdot evpar$ , where  $c_0, c_1, s_0, s_1$  are free  
and  $evpar = \delta_{ev}(\Delta t), \Delta t(true), Pvalue, zB_{tag}(true, rec)$

$G_2$ :  $\mu_2, \sigma_2$  are two free parameters independent of  $\delta_{ev}(\Delta t)$

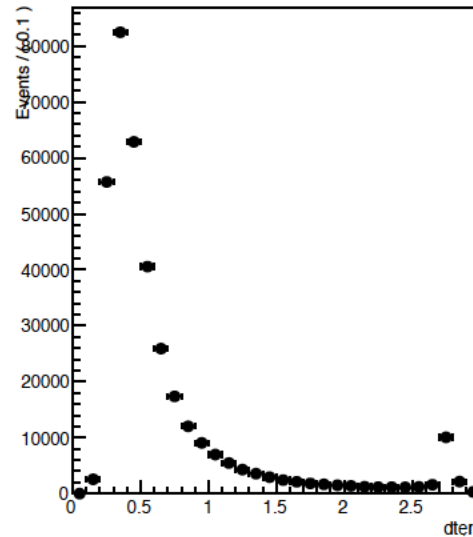
$G_3$ :  $\mu_3 = 0., \sigma_3 = 8.$  are fixed and fractions  $f_1$  and  $f_2$  are free

# RooFit : dependence of $\Delta t$ -pull on $\Delta t$ error

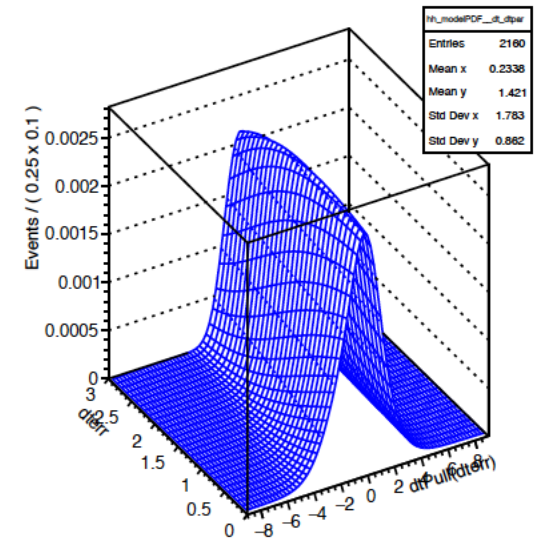
Histogram of hh\_data\_dt\_dtpar



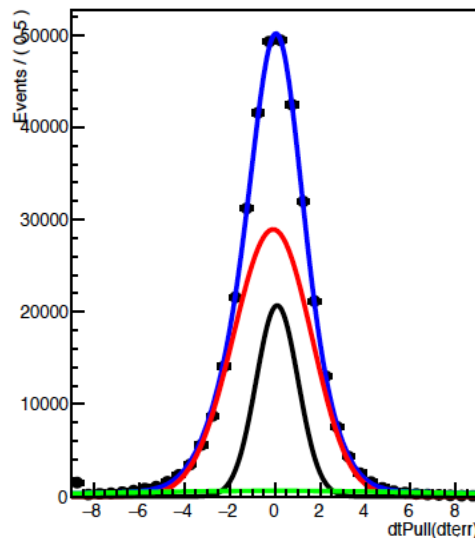
Projection of (dtPull/dtpar) on dtpar



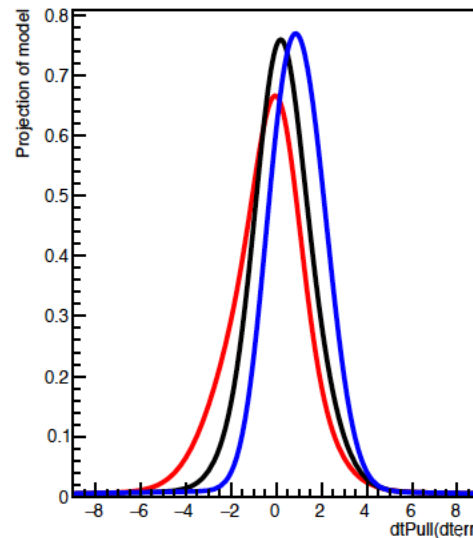
Histogram of hh\_modelPDF\_dt\_dtpar



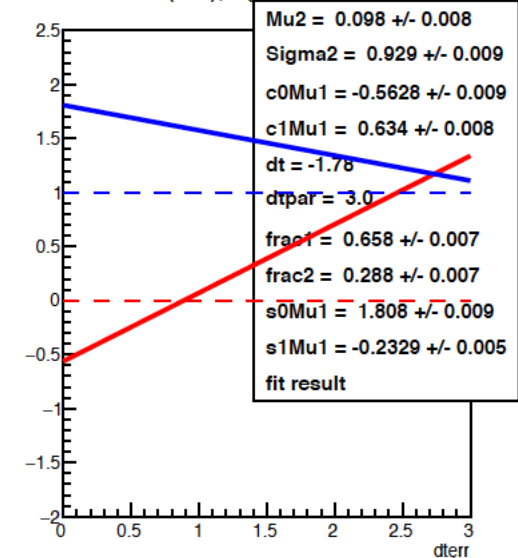
Projection of (dtPull/dtpar) on dtPull



modelPDF: dtpar=min,middle,max

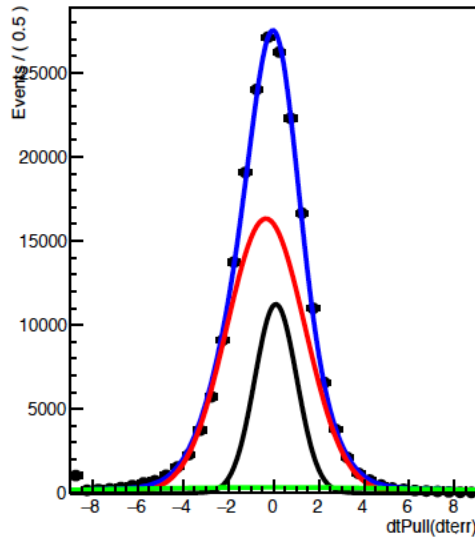


Mu1(red),Sigma1=a+b\*x

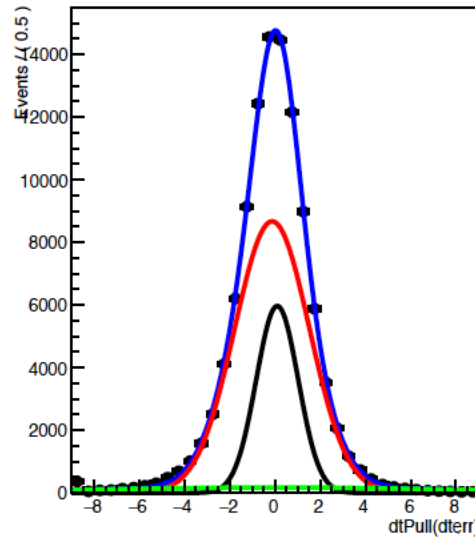


# RooFit : dependence of $\Delta t$ -pull on $\Delta t$ error

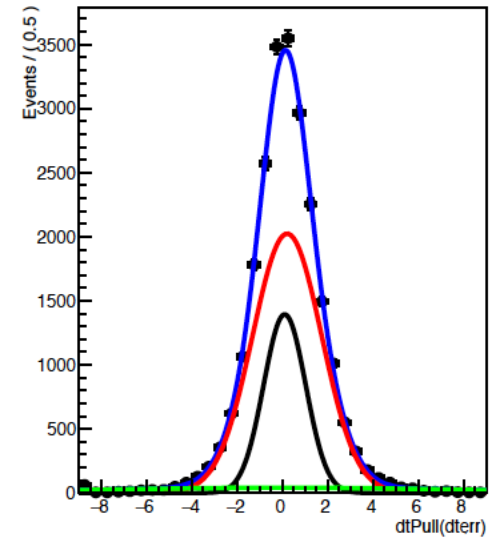
dtPull: 1st slice (of 6) in dtpar



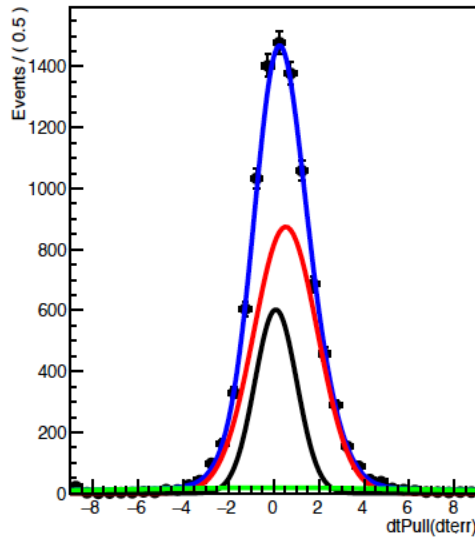
dtPull: 2nd slice (of 6) in dtpar



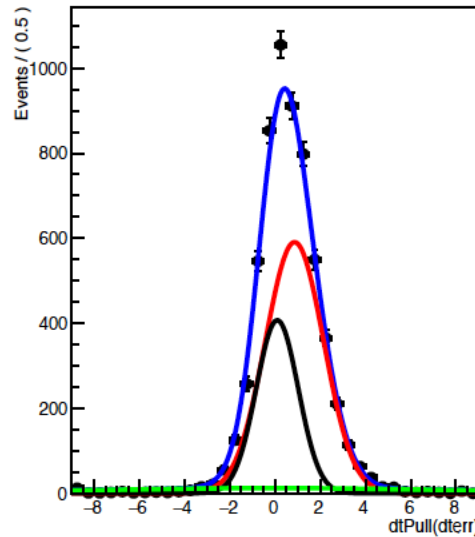
dtPull: 3rd slice (of 6) in dtpar



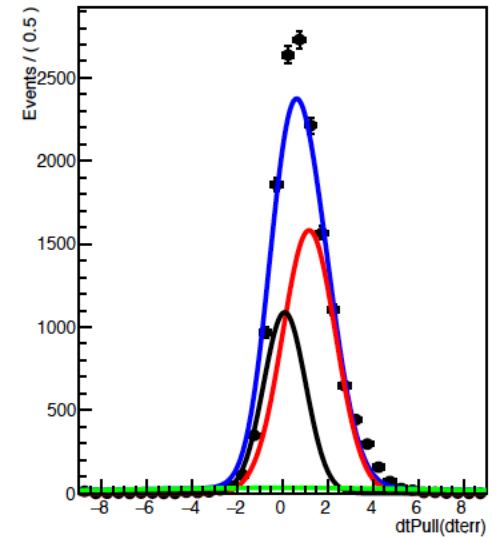
dtPull: 4th slice (of 6) in dtpar



dtPull: 5th slice (of 6) in dtpar

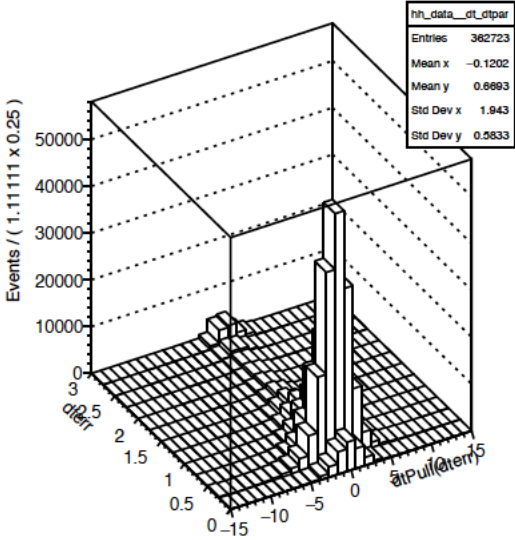


dtPull: 6th slice (of 6) in dtpar

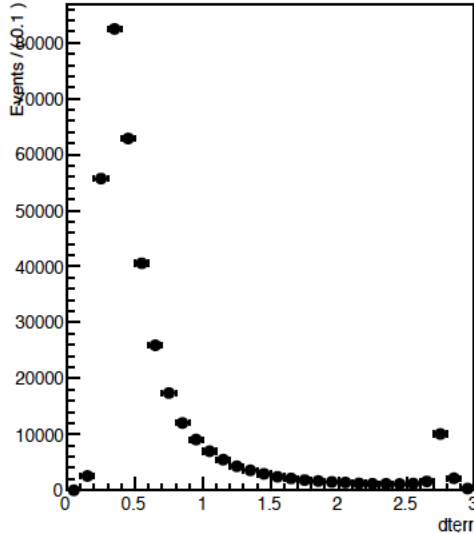


# RooFit : dependence of $\Delta t$ -pull on $\Delta t$ err (log)

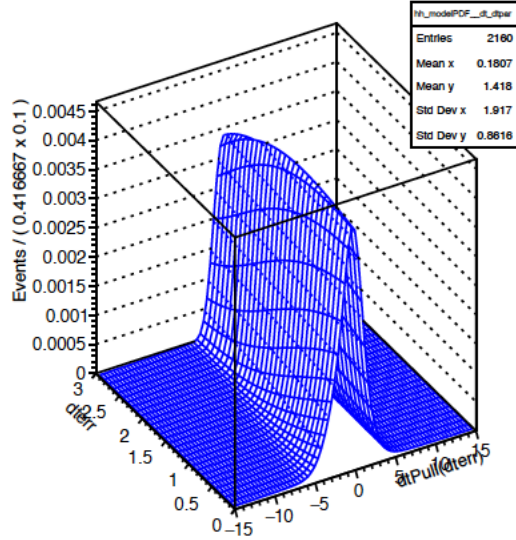
Histogram of hh\_data\_dt\_dtpar



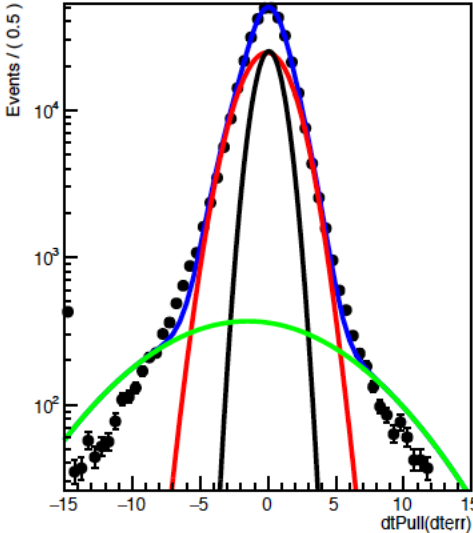
Projection of (dtPull/dtpar) on dtpar



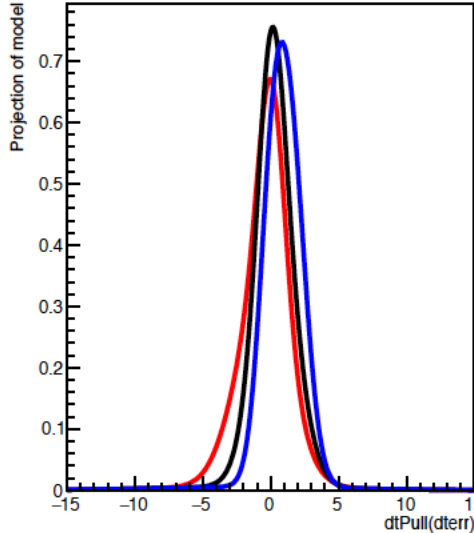
Histogram of hh\_modelPDF\_dt\_dtpar



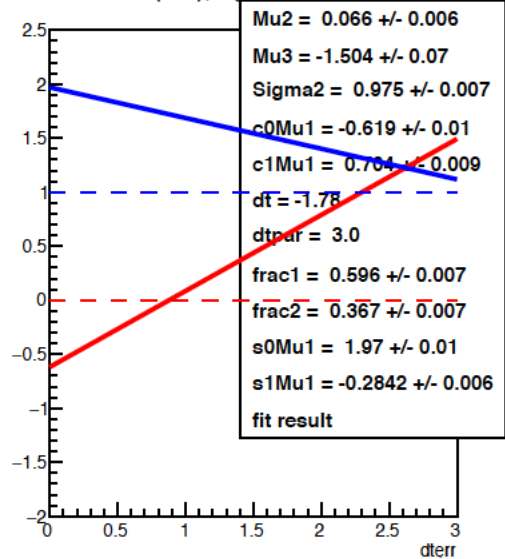
Projection of (dtPull/dtpar) on dtPull



modelPDF: dtpar=min,middle,max

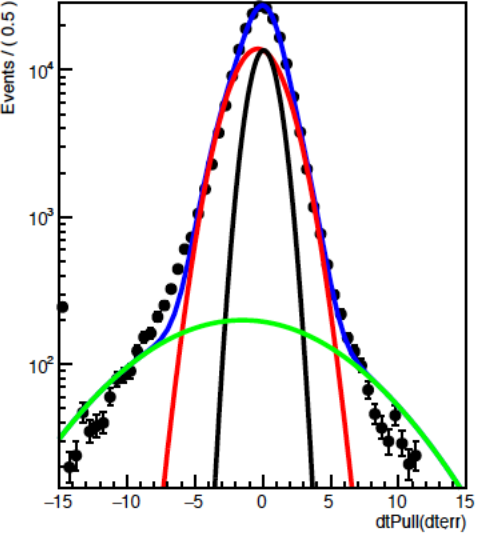


Mu1(red),Sigma1=a+b\*x

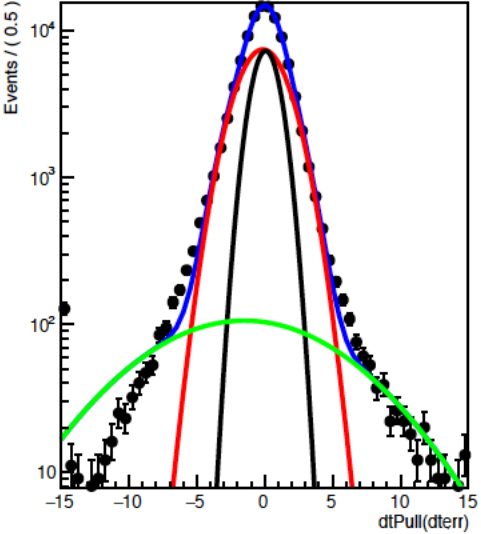


# RooFit : dependence of $\Delta t$ -pull on $\Delta t$ err (log)

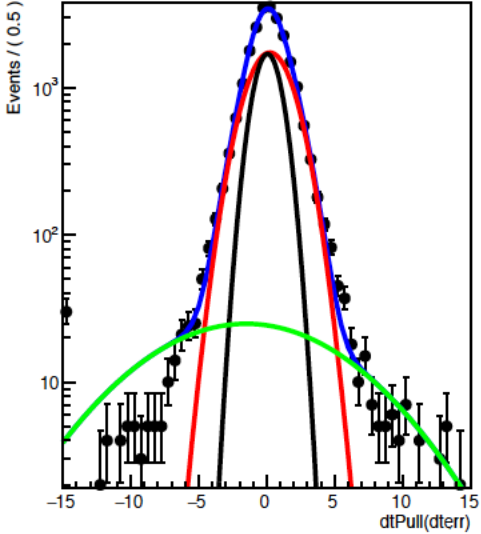
dtPull: 1st slice (of 6) in dtpar



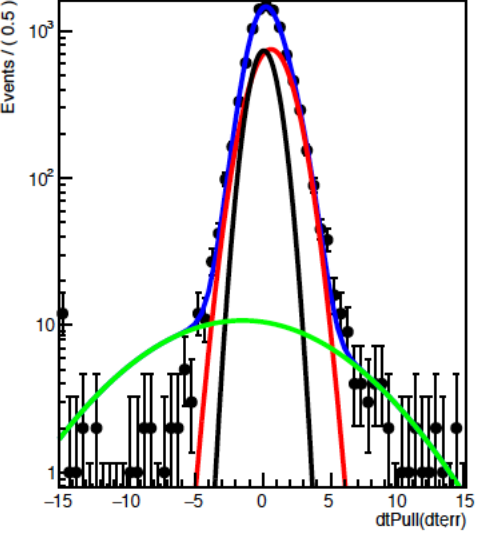
dtPull: 2nd slice (of 6) in dtpar



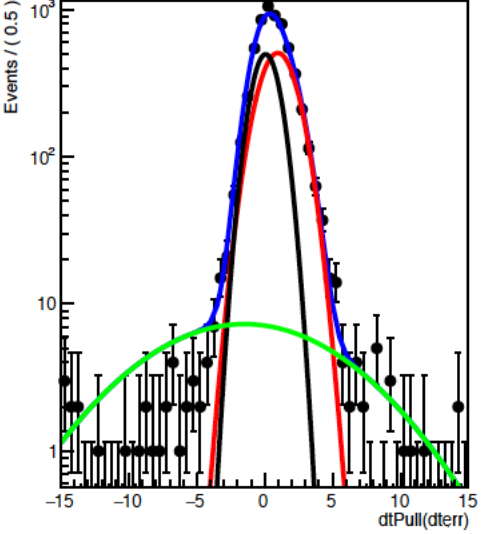
dtPull: 3rd slice (of 6) in dtpar



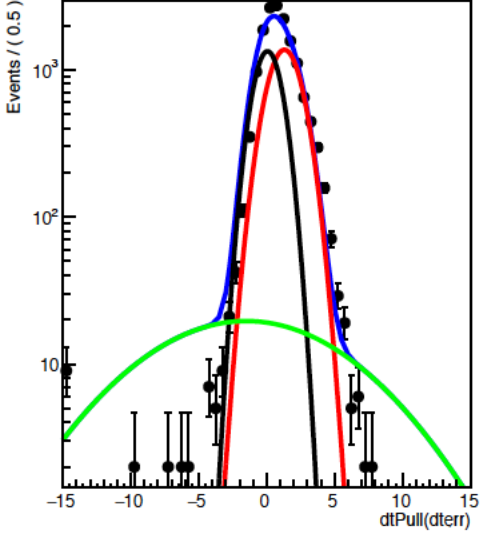
dtPull: 4th slice (of 6) in dtpar



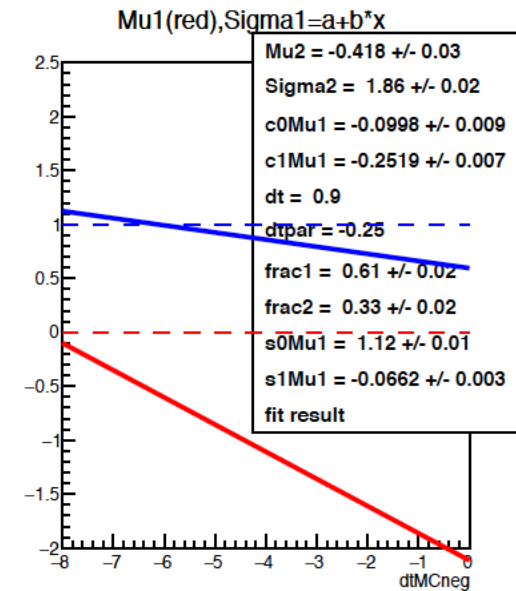
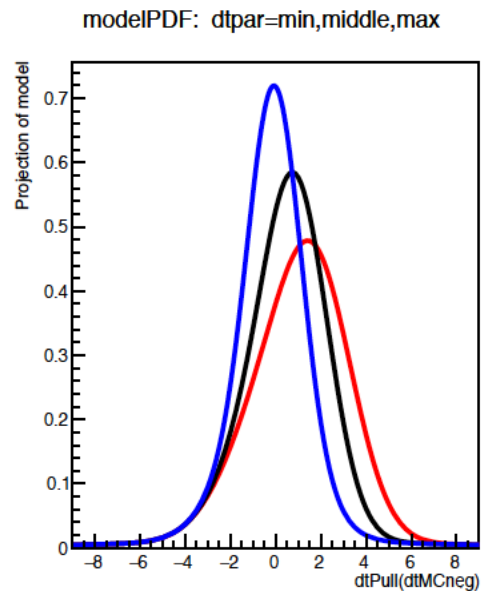
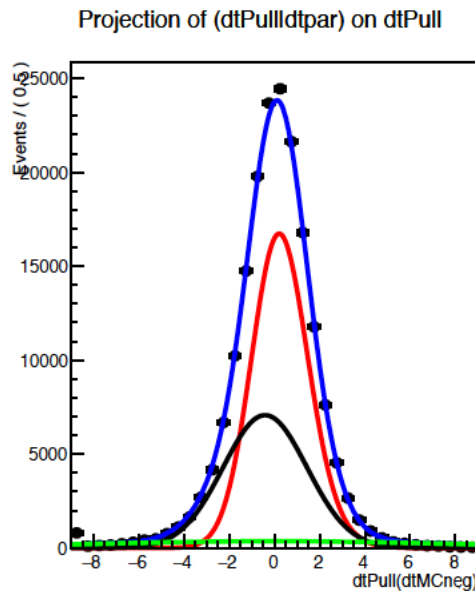
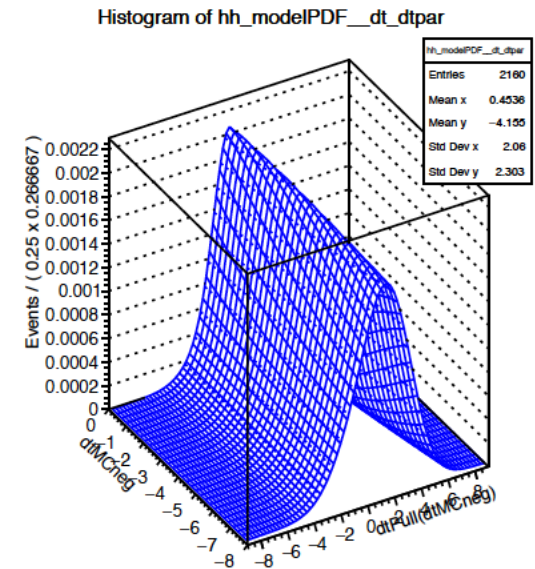
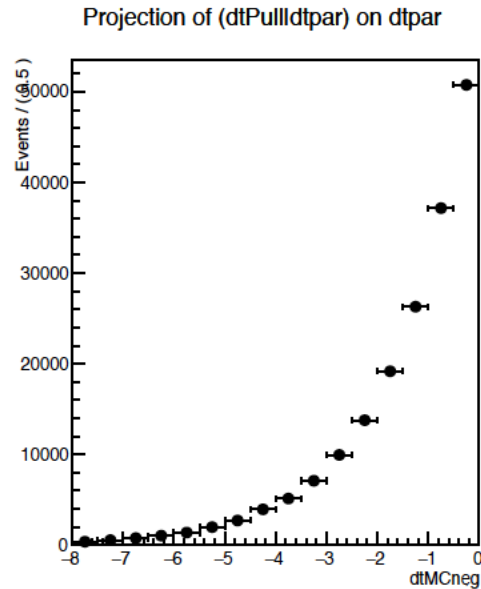
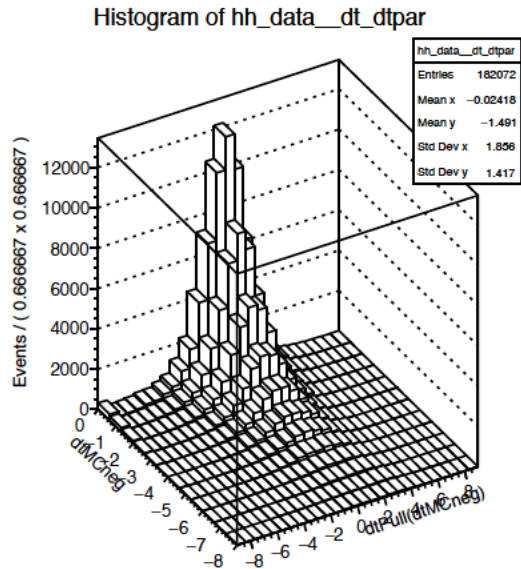
dtPull: 5th slice (of 6) in dtpar



dtPull: 6th slice (of 6) in dtpar



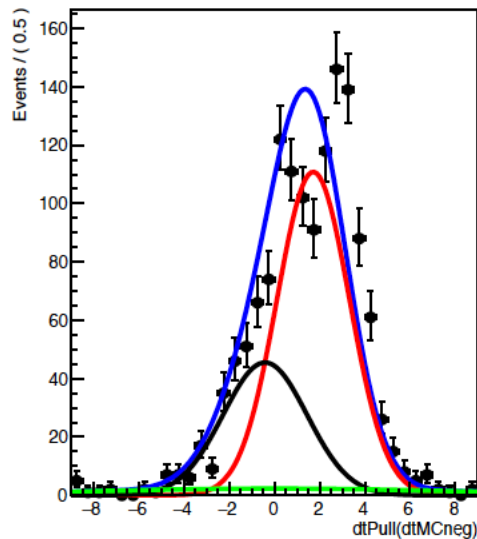
# Roofit: dependence of $\Delta t$ -pull on $\Delta t$ -true ( $< 0$ )



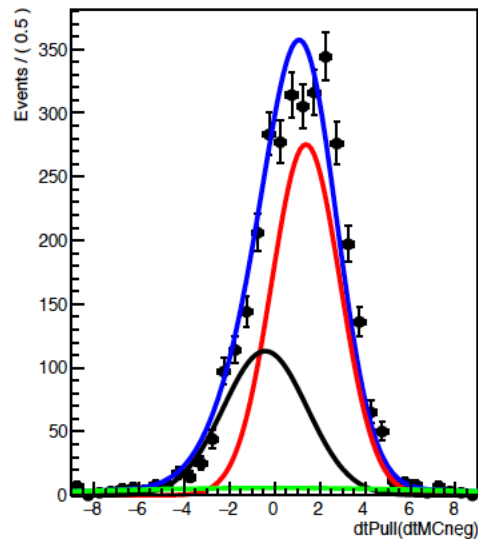


# RooFit: dependence of $\Delta t$ -pull on $\Delta t$ -true ( $<0$ )

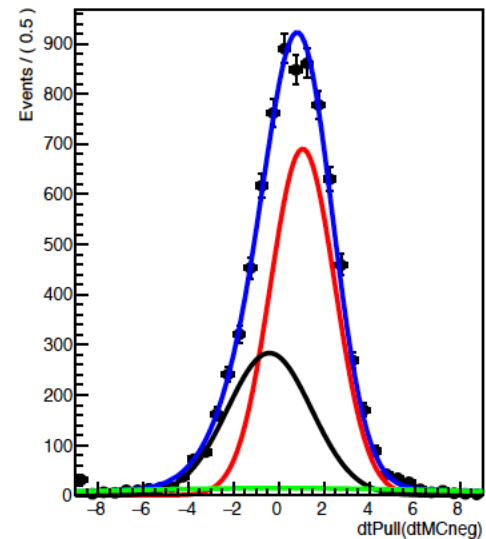
dtPull: 1st slice (of 6) in dtpar



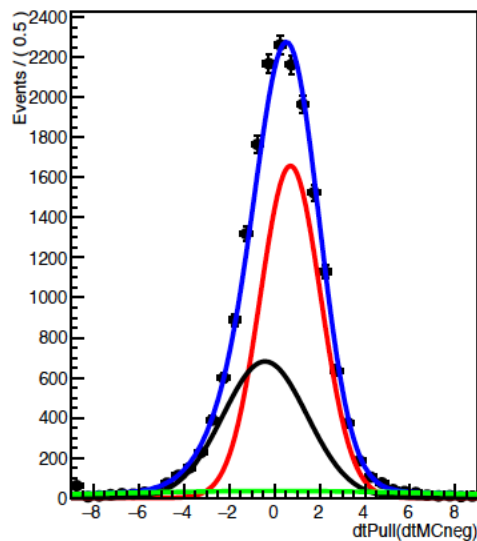
dtPull: 2nd slice (of 6) in dtpar



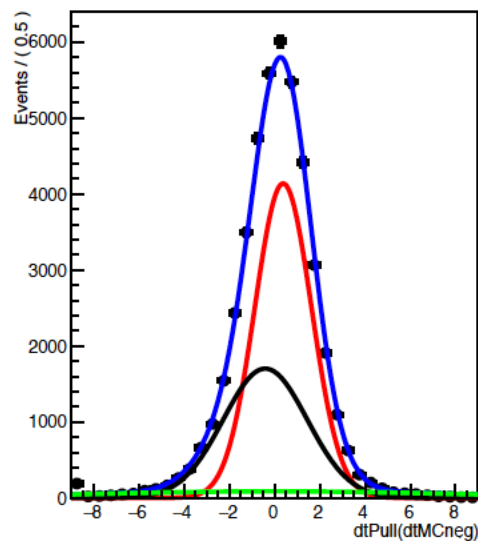
dtPull: 3rd slice (of 6) in dtpar



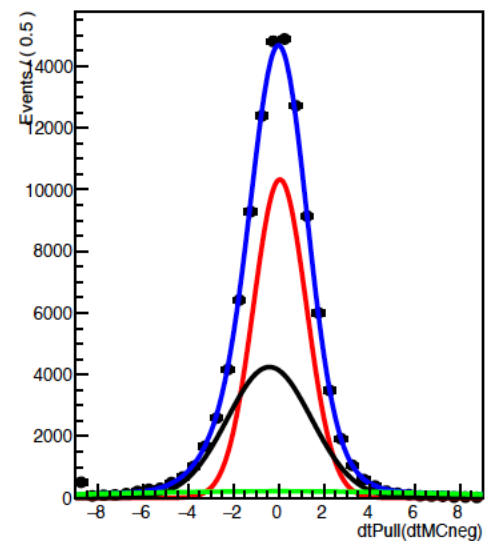
dtPull: 4th slice (of 6) in dtpar



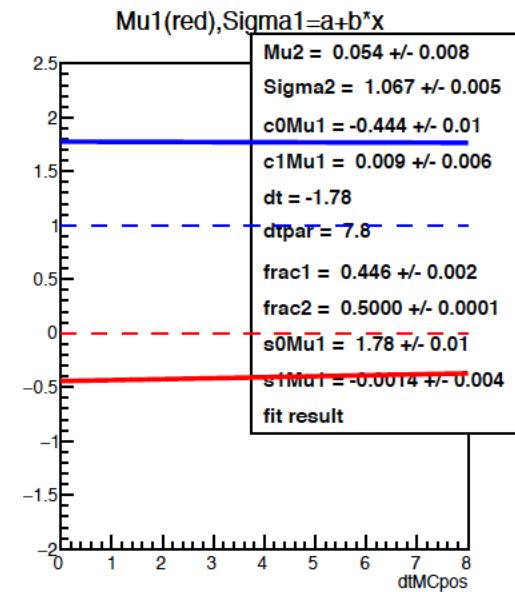
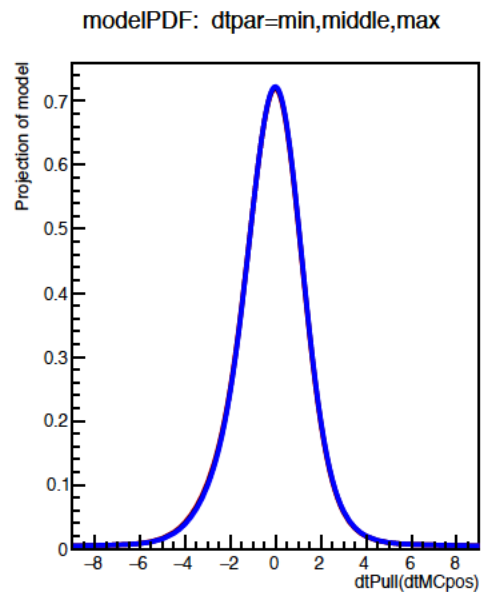
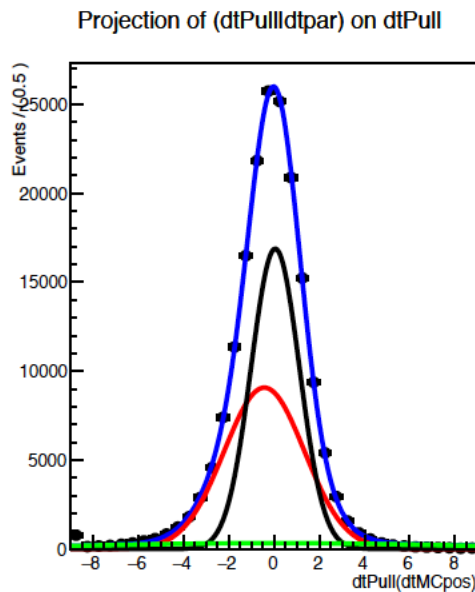
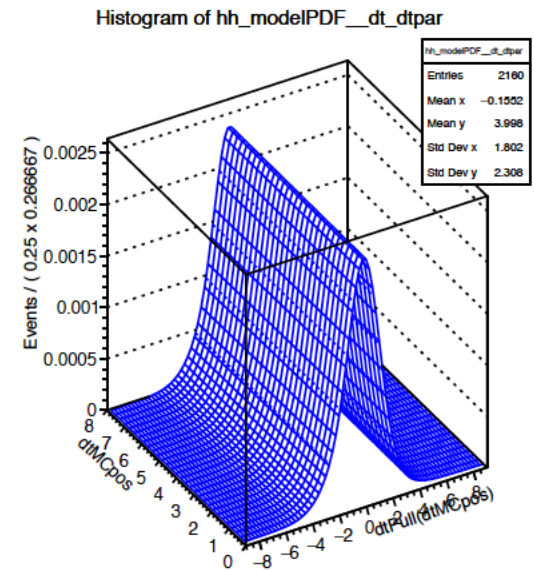
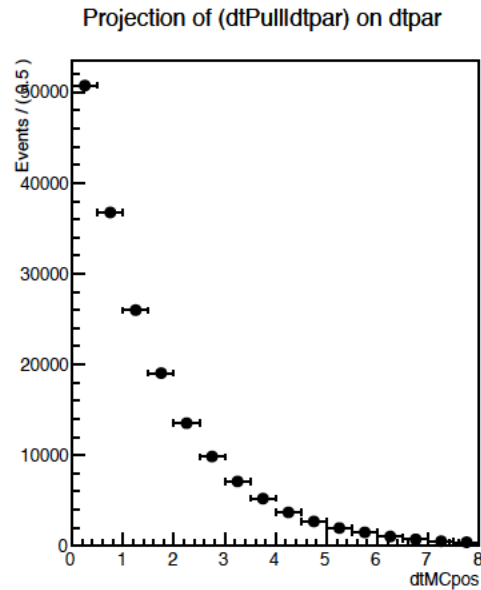
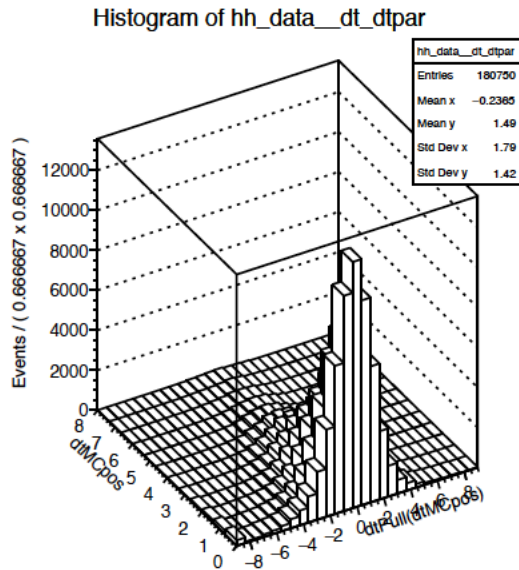
dtPull: 5th slice (of 6) in dtpar



dtPull: 6th slice (of 6) in dtpar



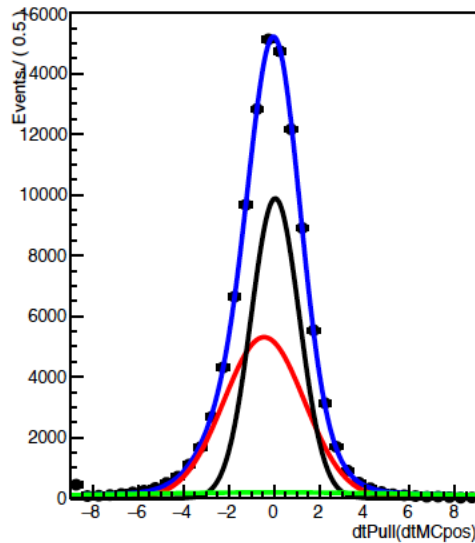
# Roofit: dependence of $\Delta t$ -pull on $\Delta t$ -true( $>0$ )



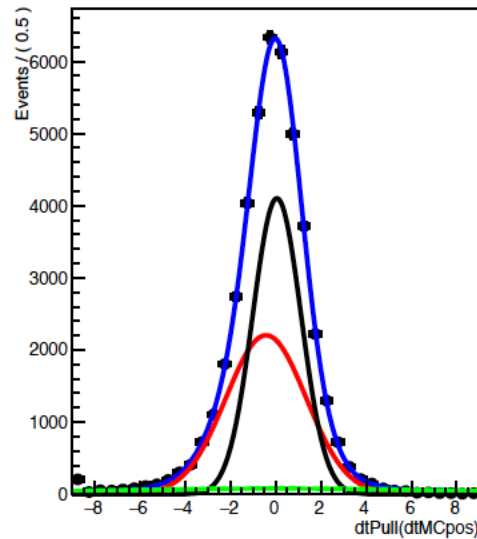


# Roofit: dependence of $\Delta t$ -pull on $\Delta t$ -true( $>0$ )

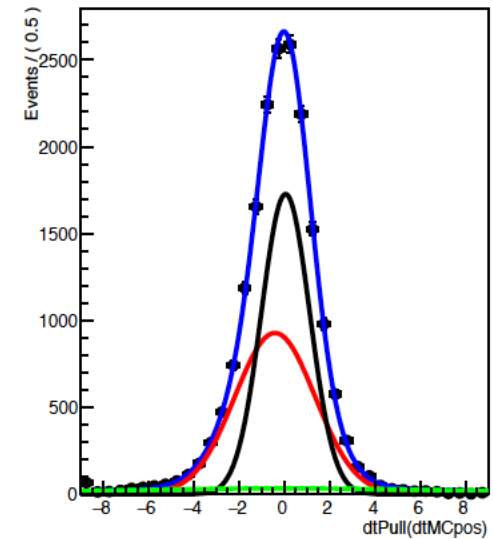
dtPull: 1st slice (of 6) in dtpar



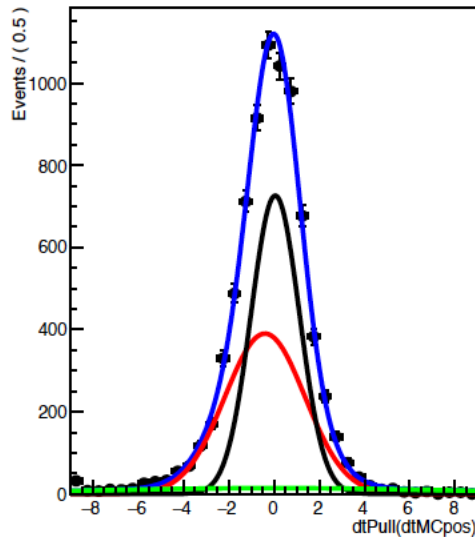
dtPull: 2nd slice (of 6) in dtpar



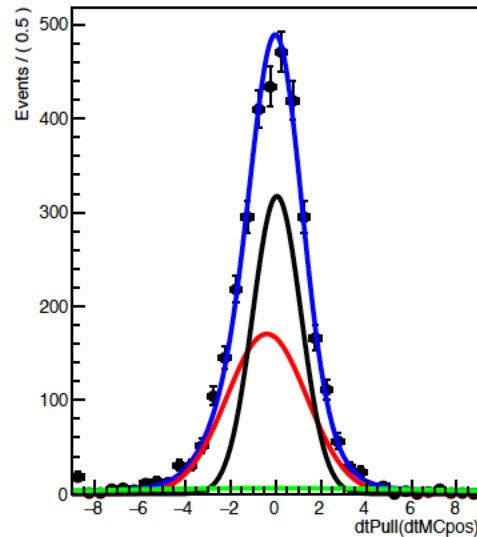
dtPull: 3rd slice (of 6) in dtpar



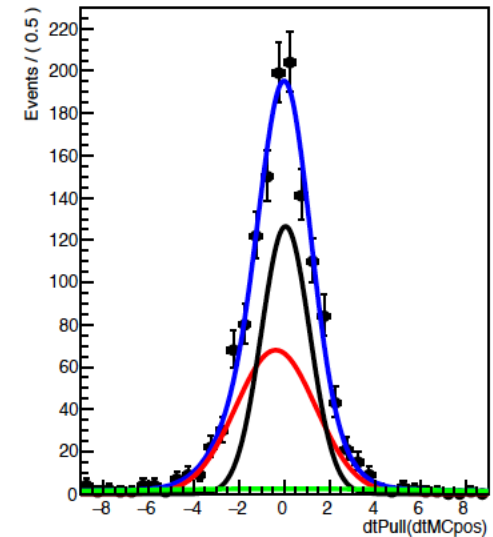
dtPull: 4th slice (of 6) in dtpar



dtPull: 5th slice (of 6) in dtpar

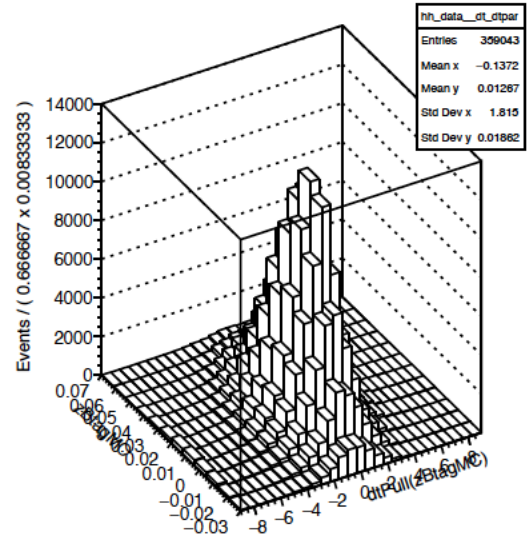


dtPull: 6th slice (of 6) in dtpar

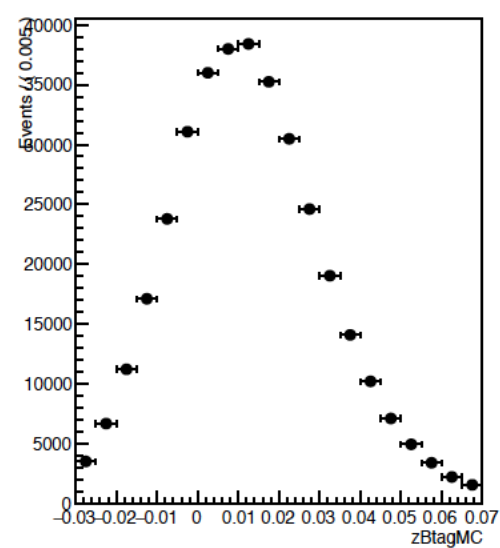


# RooFit : dependence of $\Delta t$ -pull on $z_{Btag}(true)$

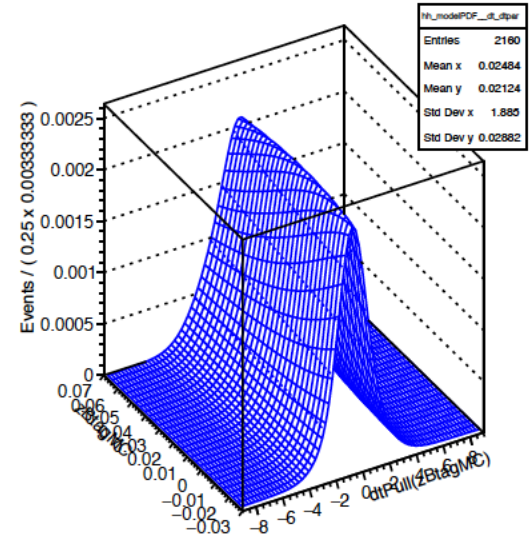
Histogram of hh\_data\_dt\_dtpar



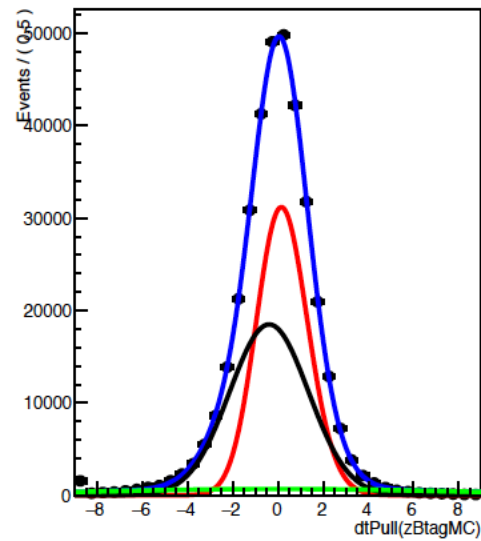
Projection of (dtPull|dtpar) on dtpar



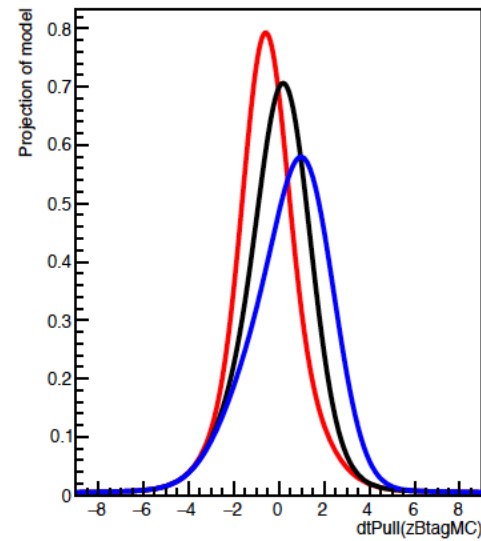
Histogram of hh\_modelPDF\_dt\_dtpar



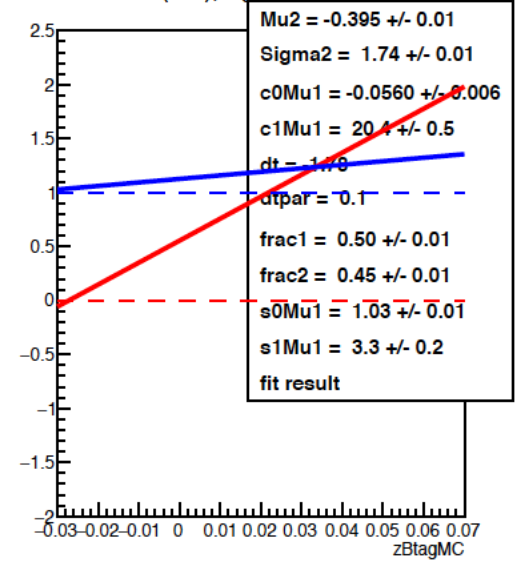
Projection of (dtPull|dtpar) on dtPull



modelPDF: dtpar=min,middle,max

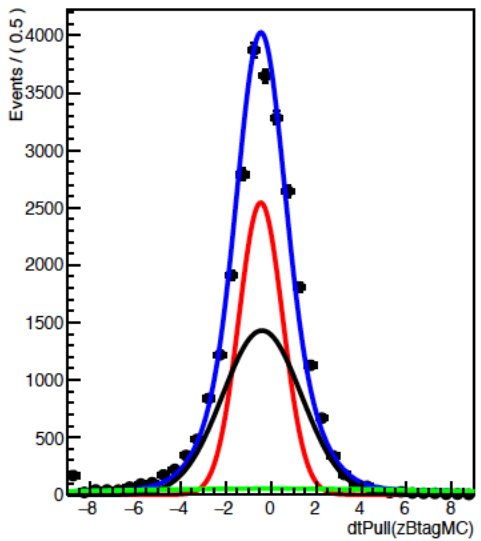


Mu1(red),Sigma1=a+b\*x

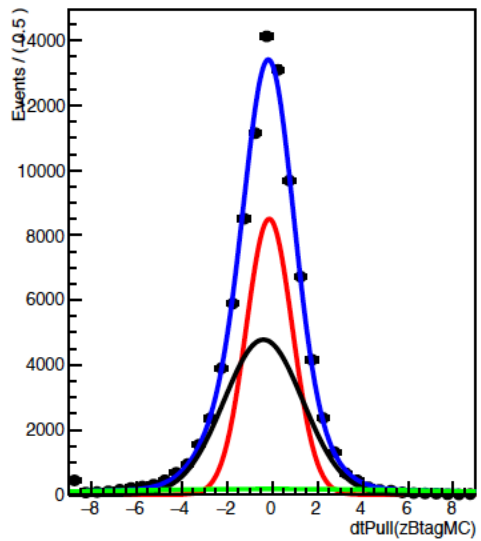


# RooFit : dependence of $\Delta t$ -pull on $z_{Btag}(true)$

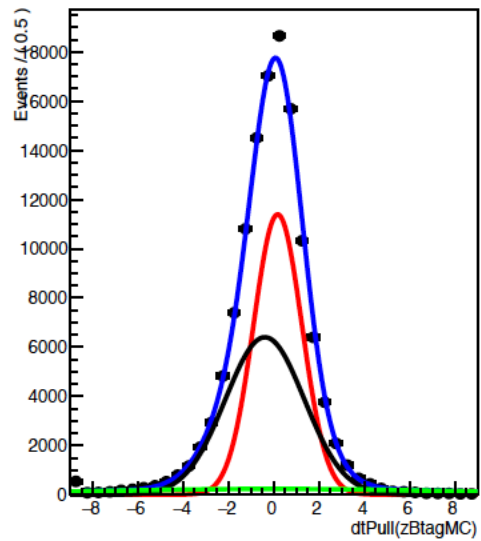
dtPull: 1st slice (of 6) in dtpar



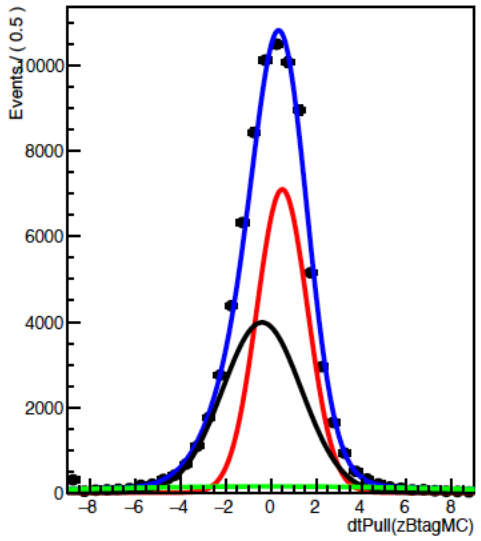
dtPull: 2nd slice (of 6) in dtpar



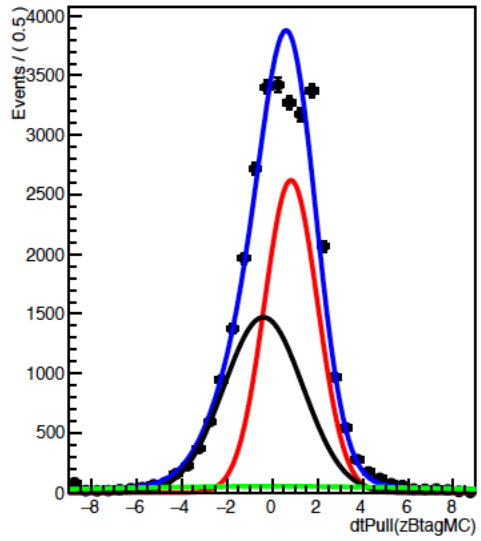
dtPull: 3rd slice (of 6) in dtpar



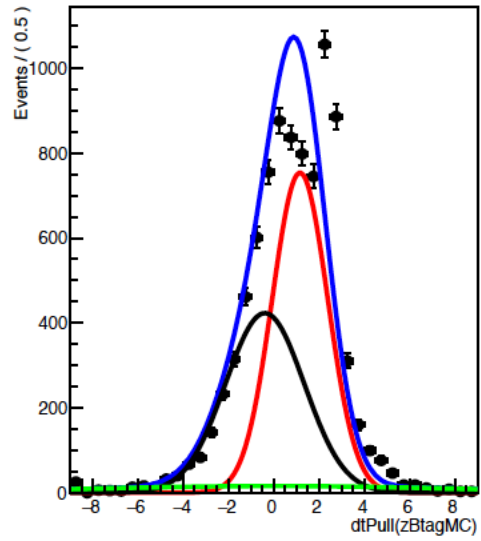
dtPull: 4th slice (of 6) in dtpar



dtPull: 5th slice (of 6) in dtpar

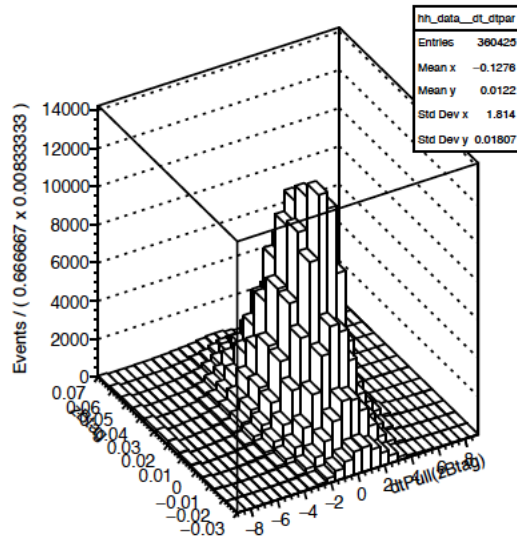


dtPull: 6th slice (of 6) in dtpar

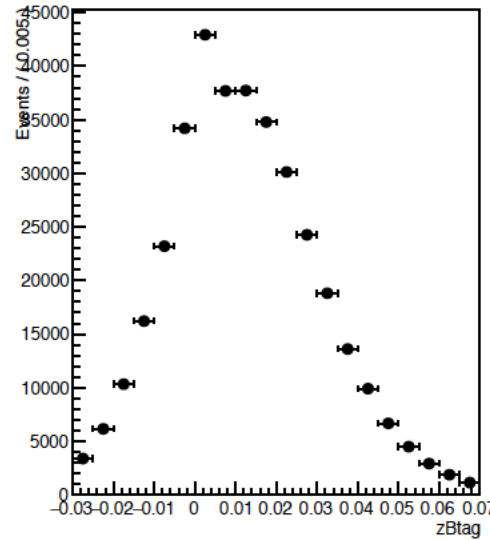


# Roofit : dependence of $\Delta t$ -pull on $z_{Btag}(rec)$

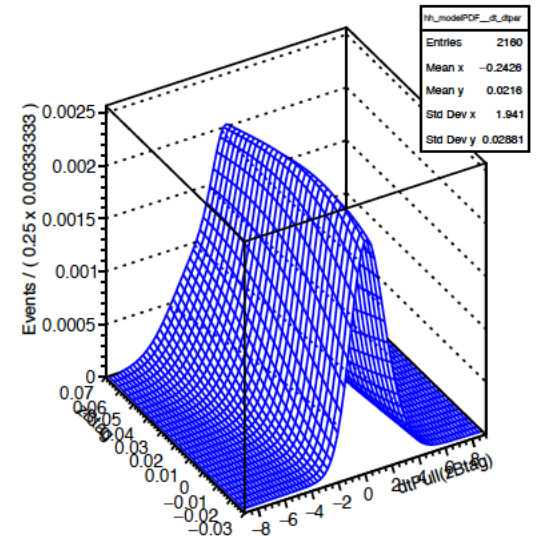
Histogram of hh\_data\_dt\_dtpar



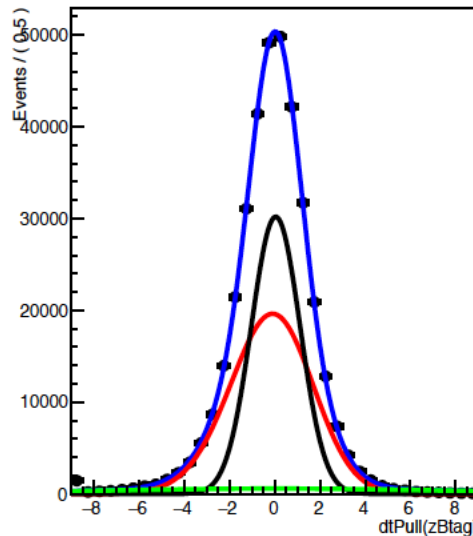
Projection of (dtPull/dtpar) on dtpar



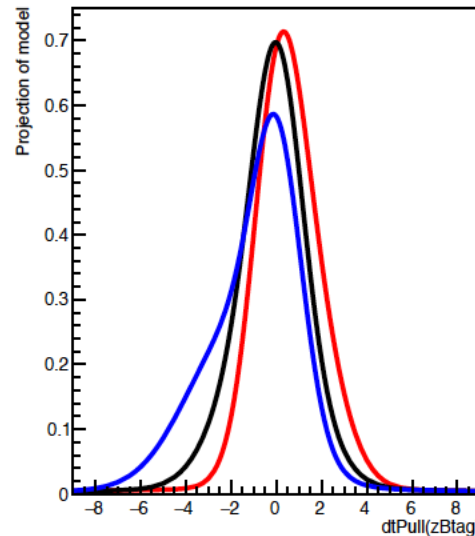
Histogram of hh\_modelPDF\_dt\_dtpar



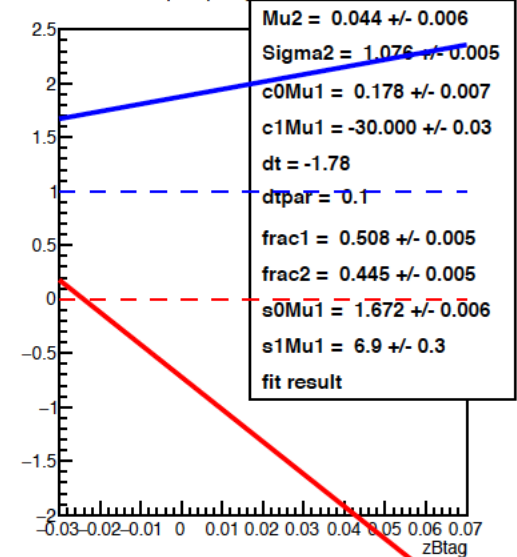
Projection of (dtPull/dtpar) on dtPull



modelPDF: dtpar=min,middle,max

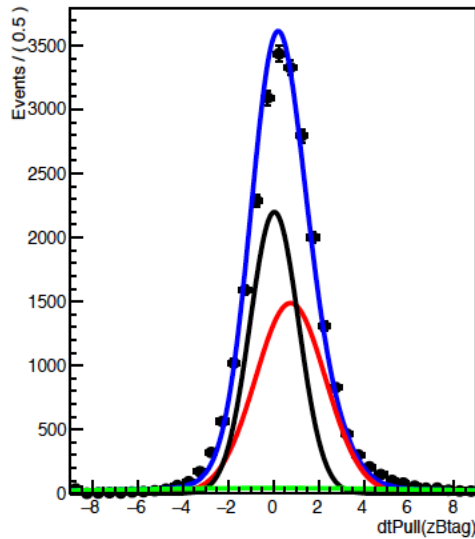


Mu1(red),Sigma1=a+b\*x

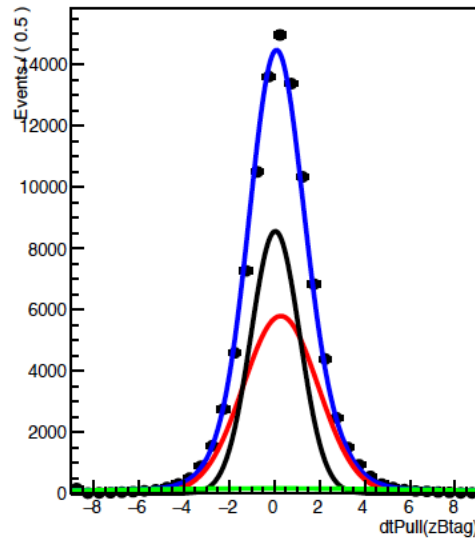


# Roofit : dependence of $\Delta t$ -pull on $z_{Btag}(rec)$

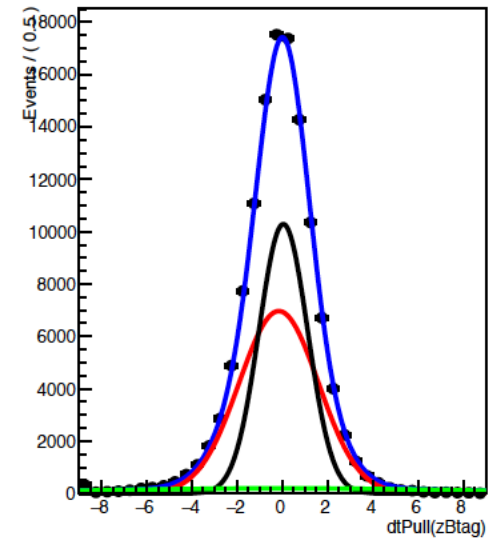
dtPull: 1st slice (of 6) in dtpar



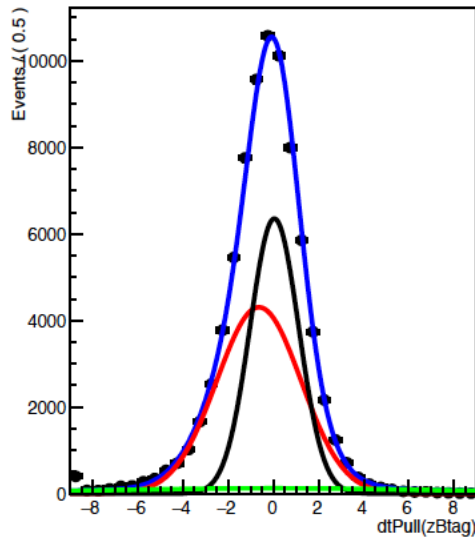
dtPull: 2nd slice (of 6) in dtpar



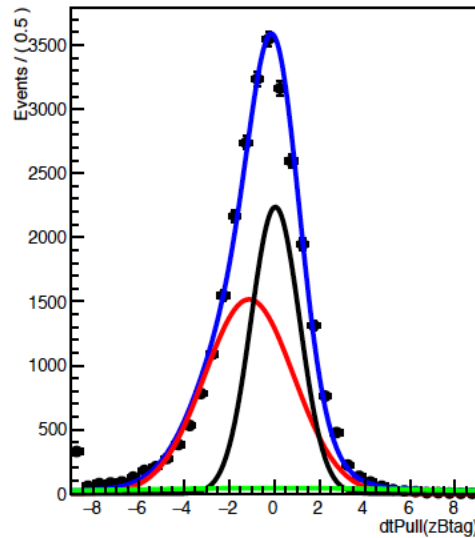
dtPull: 3rd slice (of 6) in dtpar



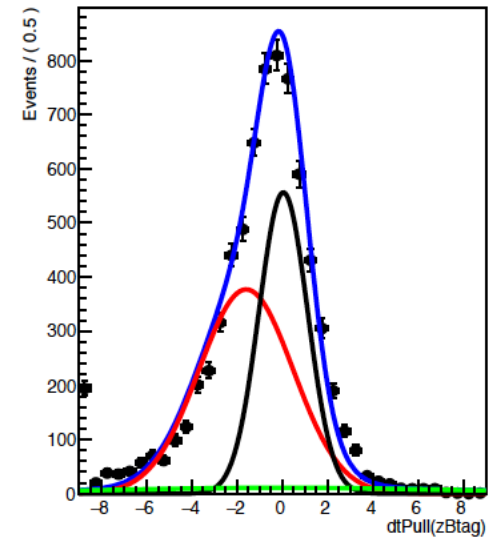
dtPull: 4th slice (of 6) in dtpar



dtPull: 5th slice (of 6) in dtpar

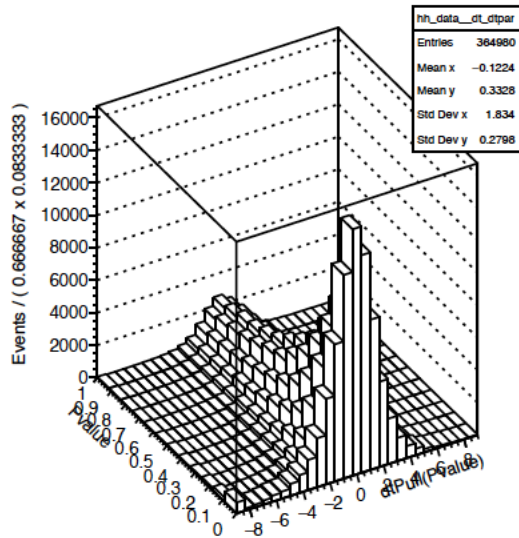


dtPull: 6th slice (of 6) in dtpar

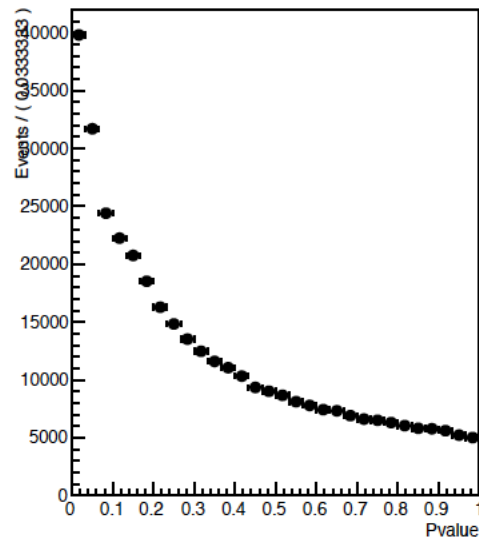


# RooFit: dependence of $\Delta t$ -pull on Pvalue( $zBtag$ )

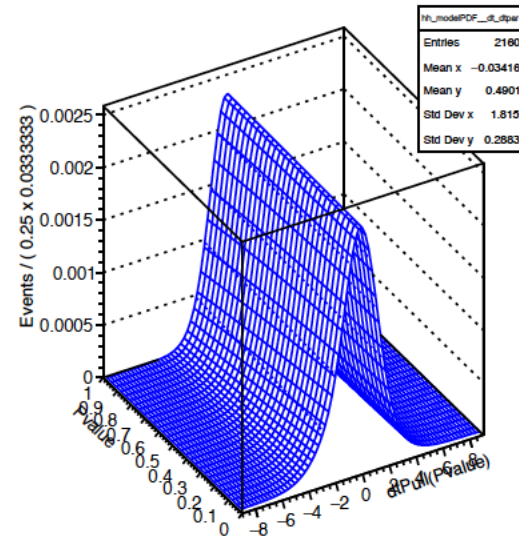
Histogram of hh\_data\_dt\_dtpar



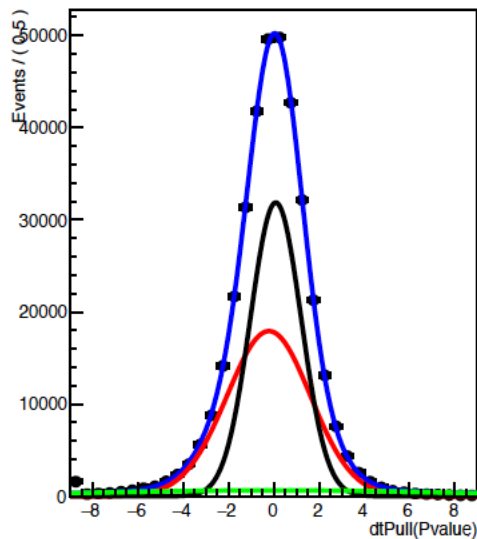
Projection of (dtPull|dtpar) on dtpar



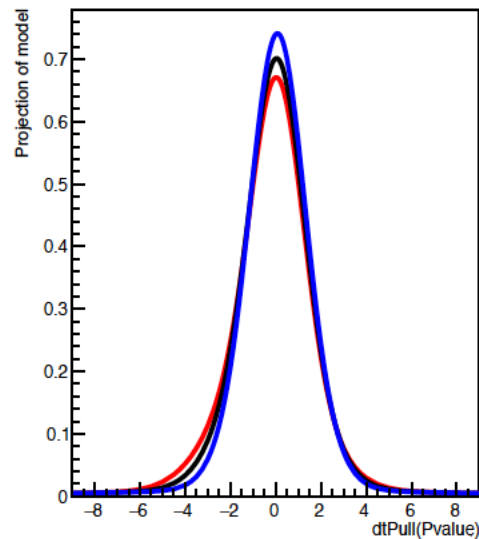
Histogram of hh\_modelPDF\_dt\_dtpar



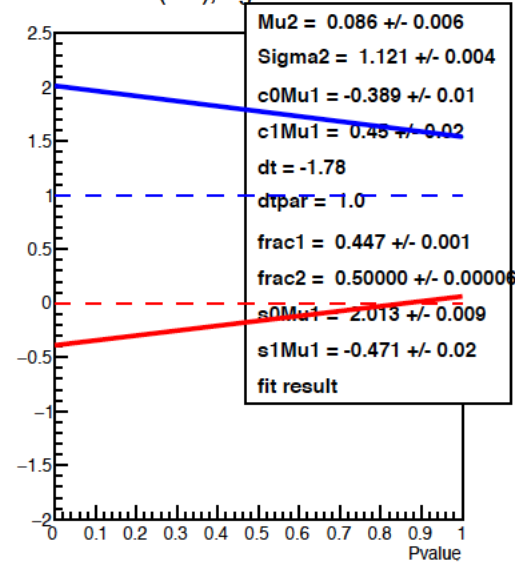
Projection of (dtPull|dtpar) on dtPull



modelPDF: dtpar=min,middle,max



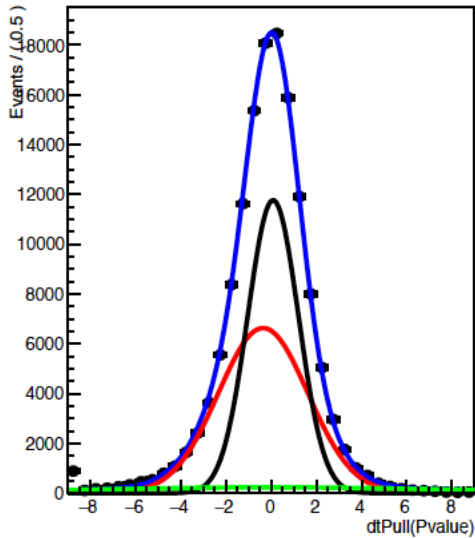
Mu1(red),Sigma1=a+b\*x



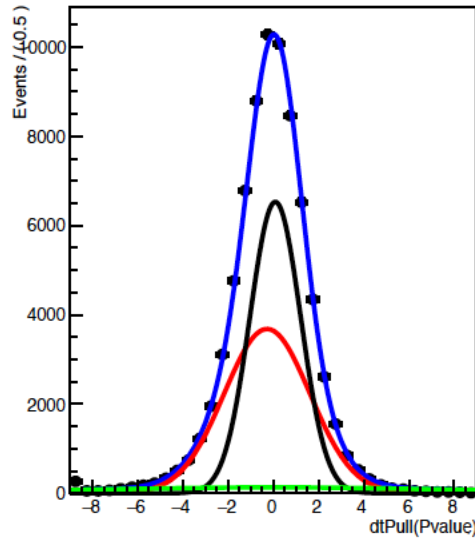


# RooFit: dependence of $\Delta t$ -pull on $P_{\text{value}}(z_{\text{Btag}})$

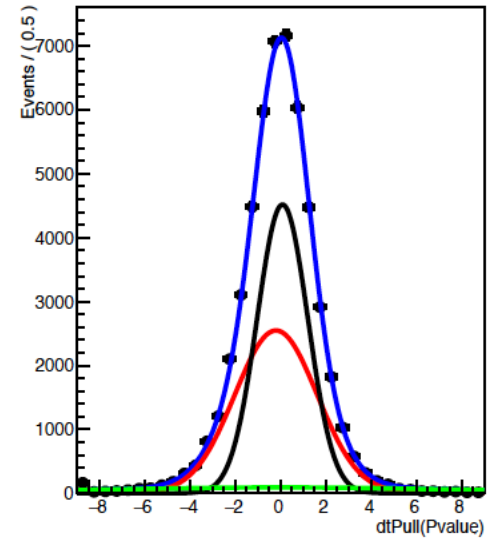
dtPull: 1st slice (of 6) in dtpar



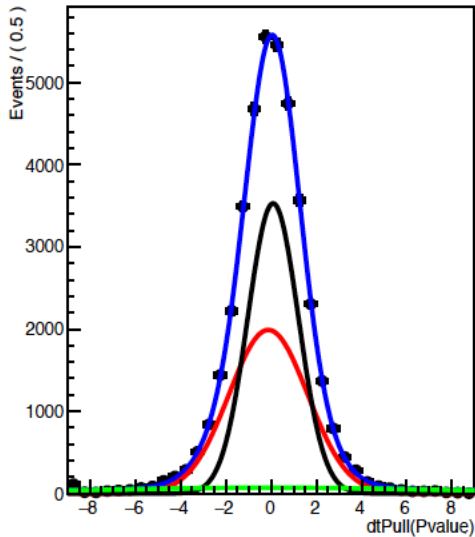
dtPull: 2nd slice (of 6) in dtpar



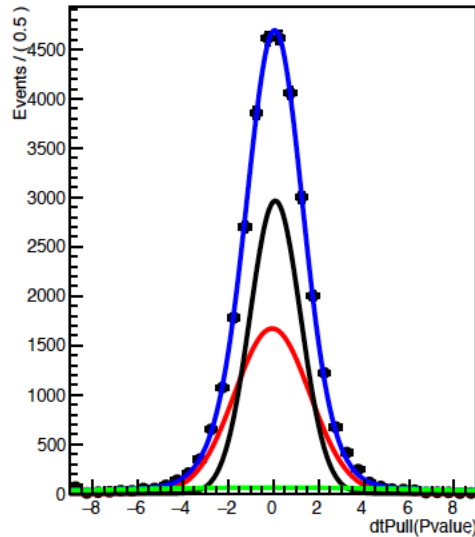
dtPull: 3rd slice (of 6) in dtpar



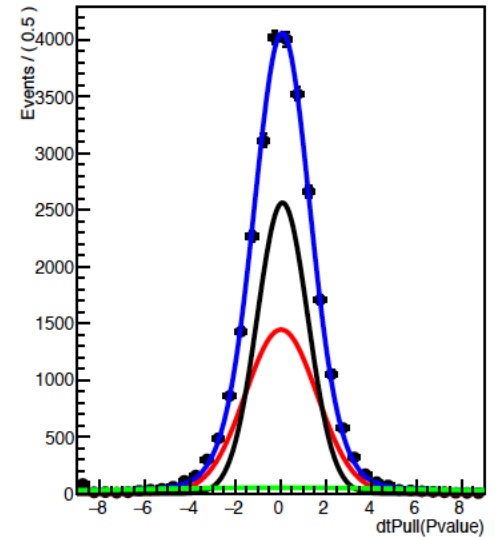
dtPull: 4th slice (of 6) in dtpar



dtPull: 5th slice (of 6) in dtpar



dtPull: 6th slice (of 6) in dtpar



# RooFit for Time Dependent Analyses

## → Platform for the Time dependent analyses:

*RooFit package in Root*

- *is developed to make this kind of analyses*
- *looks as a right choice for us*

## → All that can be done in RooFit:

*unbinned maximum likelihood fit to the observed  $\Delta t = t(B_{\text{sig}}) - t(B_{\text{tag}})$  distribution to define physics parameters of interest*

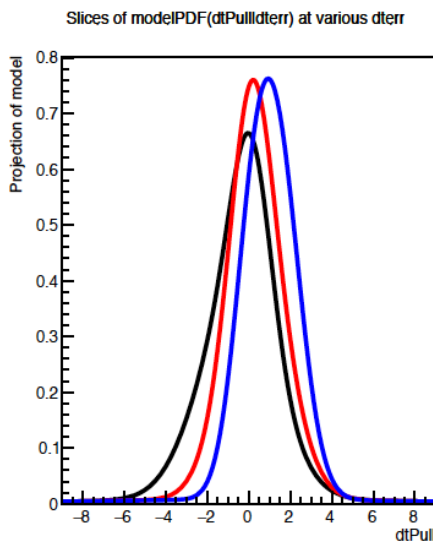
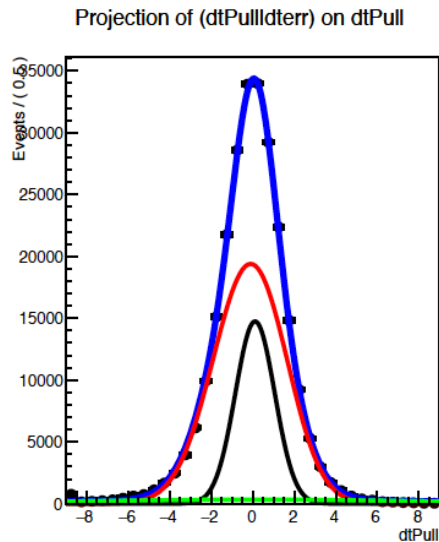
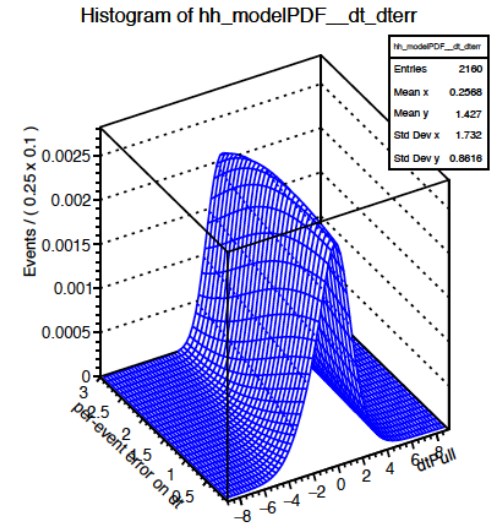
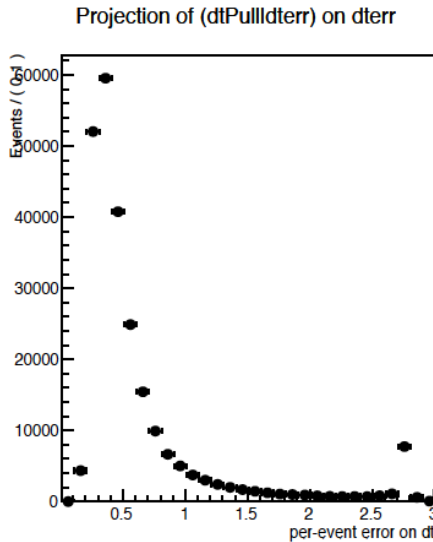
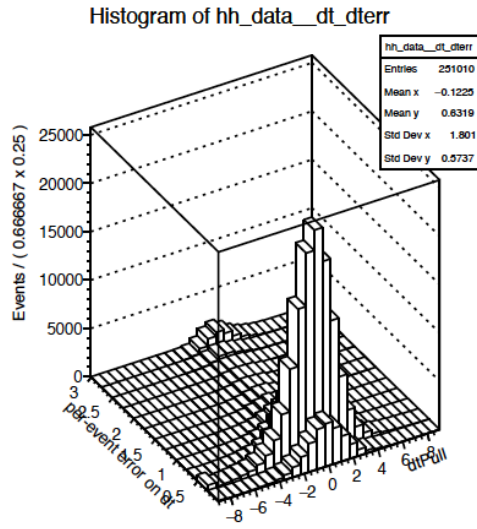
maximum  $L = \prod_i P(\Delta t_i, \text{physics \& event reco parameters})$

*The event probability density function (PDF) is a convolution of a true physics PDF and a resolution function  $R_{\text{sig, bkg}}(\Delta t - \Delta t')$ :*

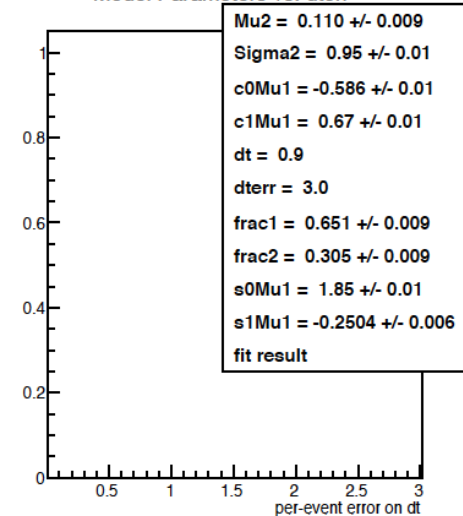
$$P_{\text{sig, bkg}}(\Delta t) = \int_{-\infty}^{+\infty} d(\Delta t') \wp_{\text{sig, bkg}}(\Delta t') R_{\text{sig, bkg}}(\Delta t - \Delta t')$$

*Strictly speaking (as it has been assumed in Belle and BABAR),  $R_{\text{sig, bkg}}(\Delta t - \Delta t')$  should be fully factorized from  $\wp_{\text{sig, bkg}}(\Delta t')$  and does not depend on true  $\Delta t'$  or any other “true” variable.*

# $\Delta t$ -pulls with $\Delta t$ error as a input parameter

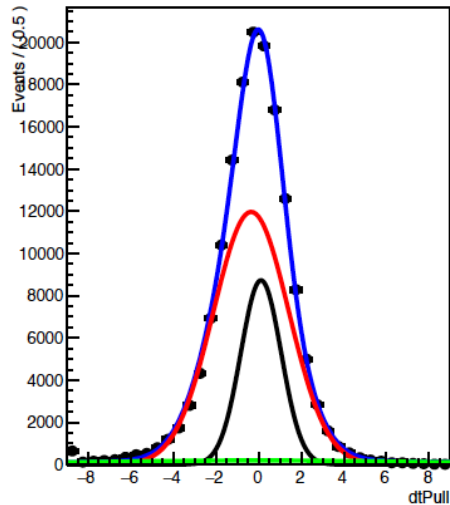


Model Parameters vs. dt\_err

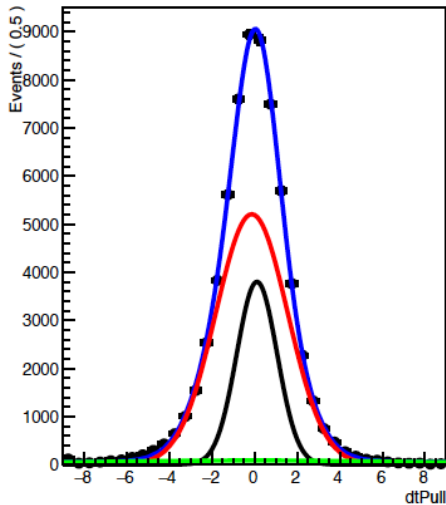


# $\Delta t$ -pulls for slices in $\Delta t$ errors from 0 to 3 ps

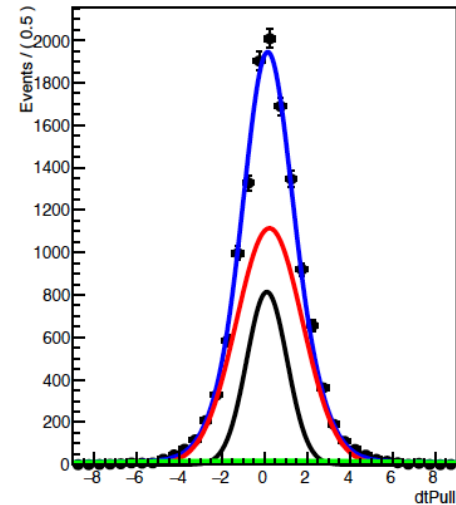
Projection of (dtPull|dterr): dterr[0,0.5]



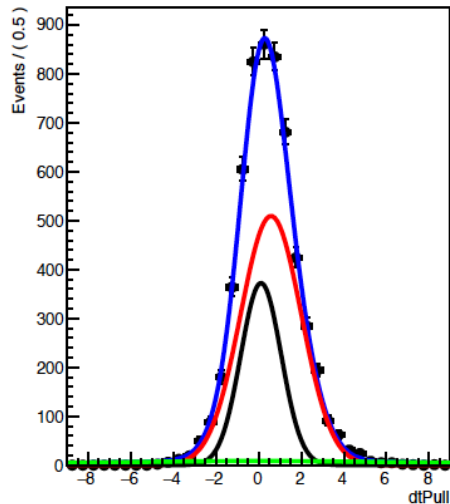
Projection of (dtPull|dterr): dterr[0.5,1]



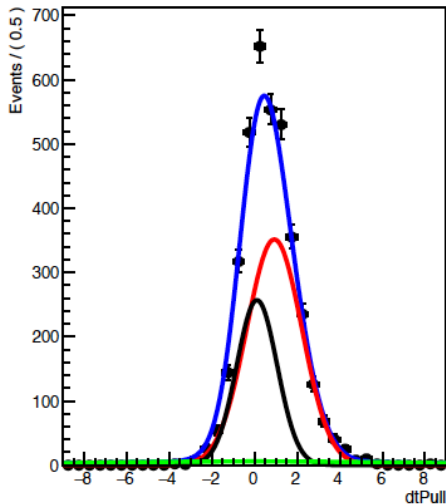
Projection of (dtPull|dterr): dterr[1,1.5]



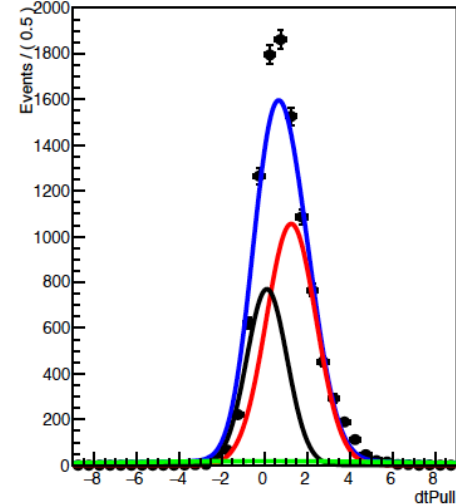
Projection of (dtPull|dterr): dterr[1.5,2]



Projection of (dtPull|dterr): dterr[2,2.5]



Projection of (dtPull|dterr): dterr[2.5,3]



# $\Delta t$ Resolution Function

## → Time dependent analyses:

- *B meson lifetime*
- *mixing and  $B^0\bar{B}^0$  oscillations*
- *time-dependent CP asymmetry*

## → Method:

*unbinned maximum likelihood fit to the observed  $\Delta t = t(B_{\text{sig}}) - t(B_{\text{tag}})$  distribution to define physics parameters of interest*

$$\text{maximum } L = \prod_i P(\Delta t_i, \text{physics \& event reco parameters})$$

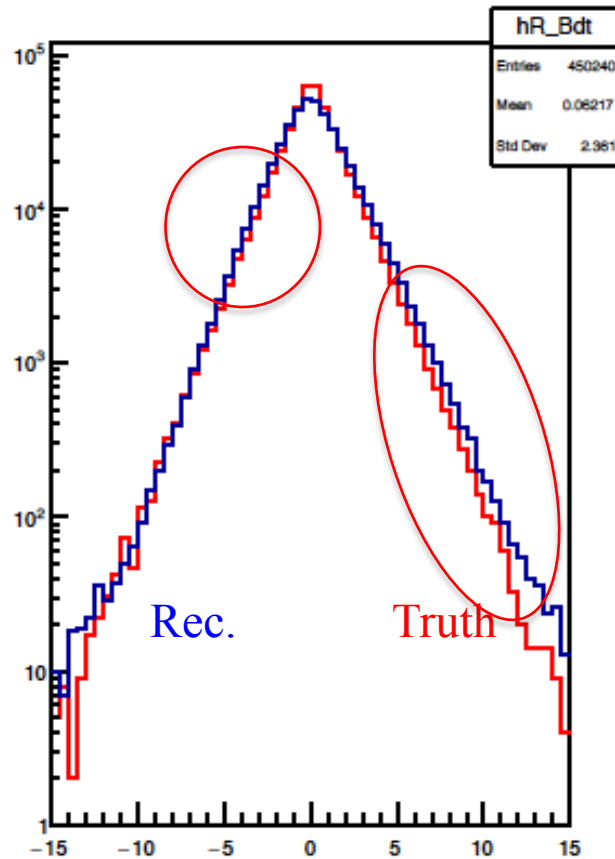
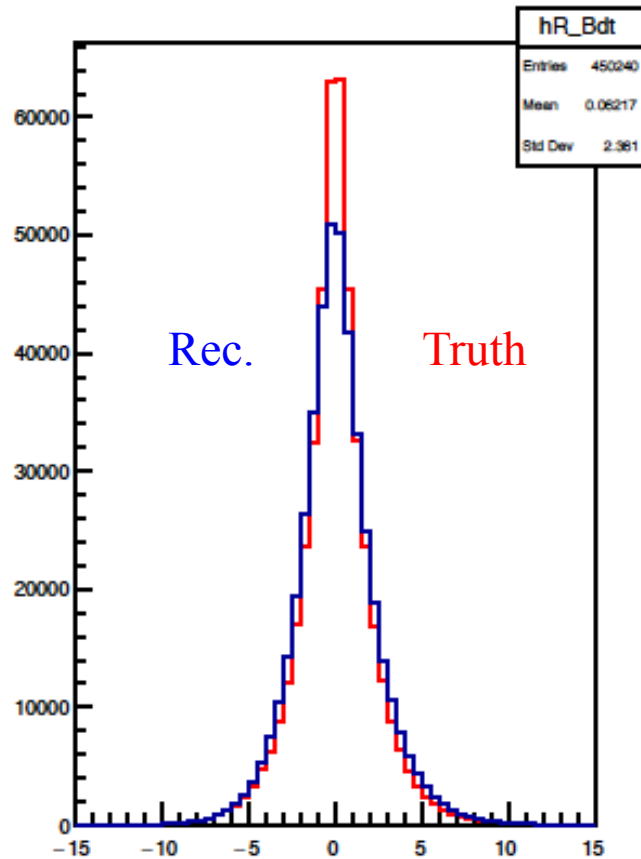
*The event probability density function (PDF) is a convolution of a true physics PDF and a resolution function  $R_{\text{sig, bkg}}(\Delta t - \Delta t')$ :*

$$P_{\text{sig, bkg}}(\Delta t) = \int_{-\infty}^{+\infty} d(\Delta t') \wp_{\text{sig, bkg}}(\Delta t') R_{\text{sig, bkg}}(\Delta t - \Delta t')$$

*Strictly speaking (as it has been assumed in Belle and BABAR),  $R_{\text{sig, bkg}}(\Delta t - \Delta t')$  should be fully factorized from  $\wp_{\text{sig, bkg}}(\Delta t')$  and does not depend on true  $\Delta t'$  or any other “true” variable.*

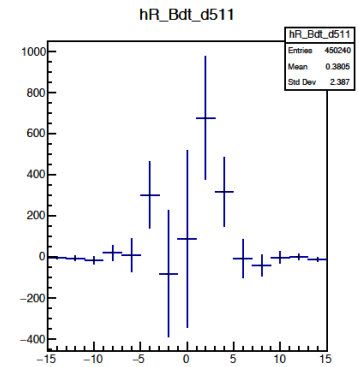
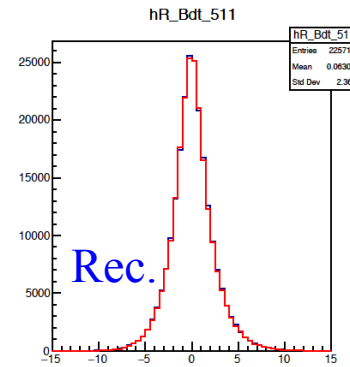
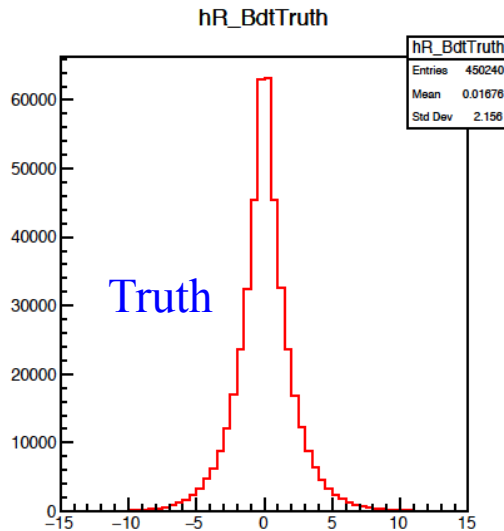
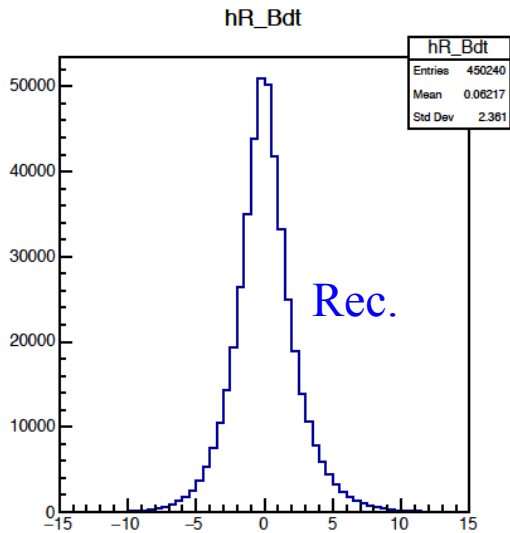
# True and reconstructed $\Delta t$ distributions

B0B0bar MC, Signal:  $B^0 \rightarrow J/\Psi K^0_S$   
hR\_BdtTruth

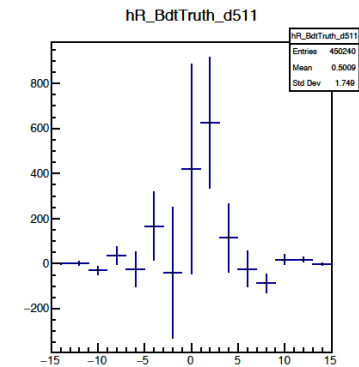
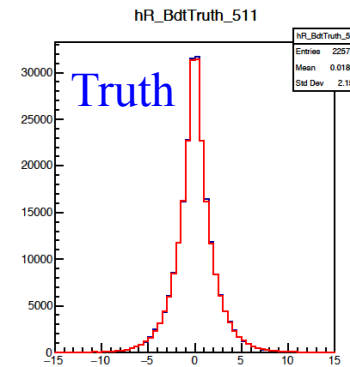
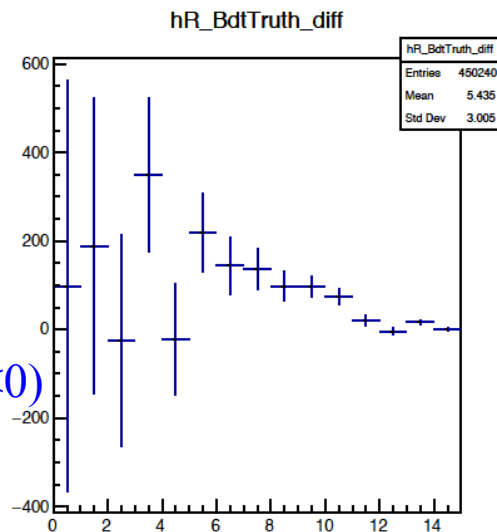
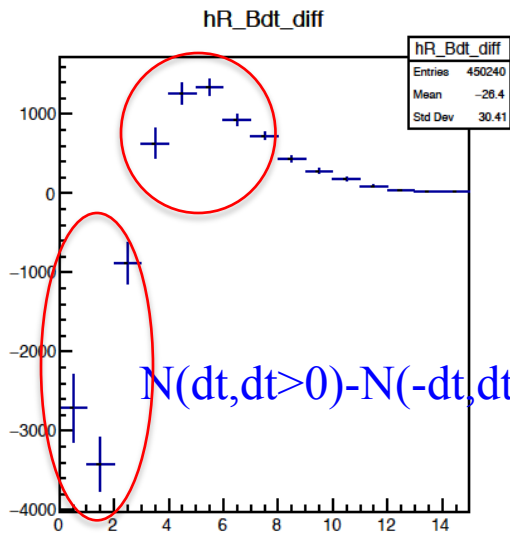




# Comparison of true and reconstructed $\Delta t$

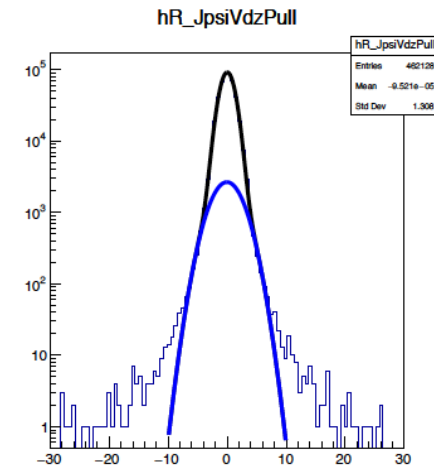
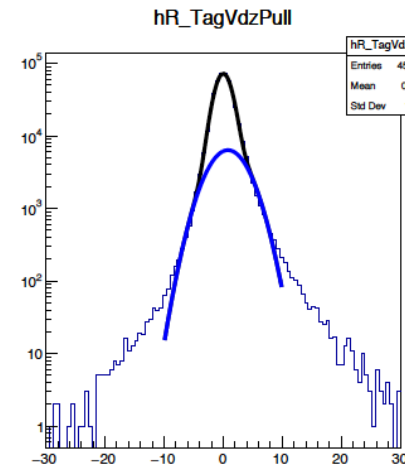
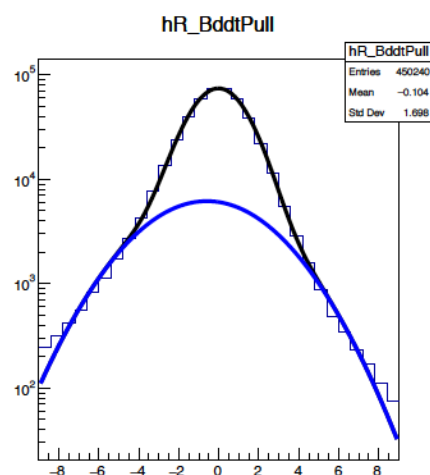
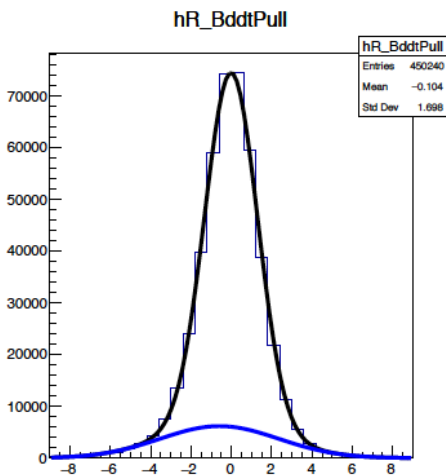
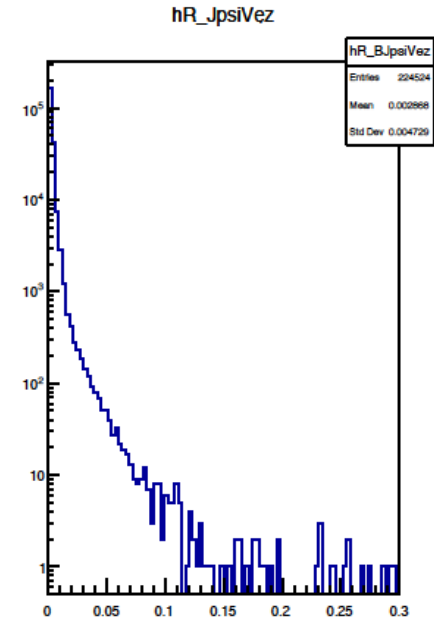
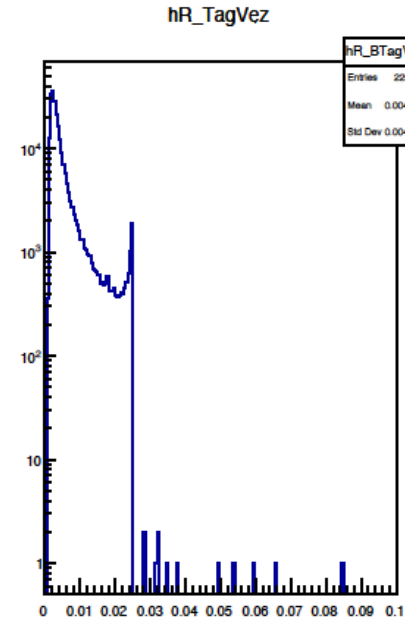
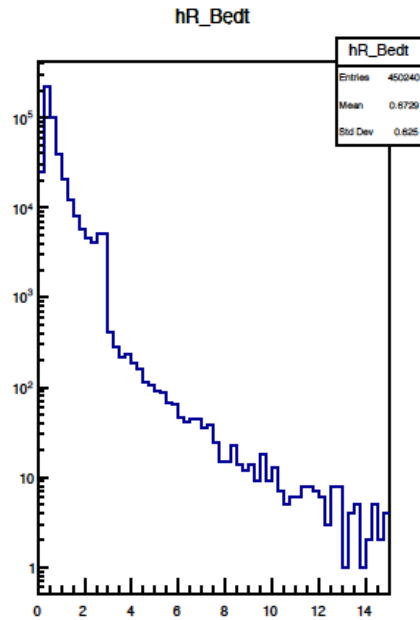
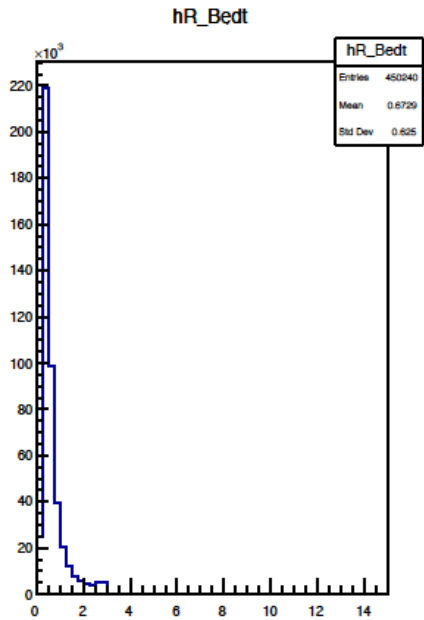


$N(dt, B0) - N(dt, B0bar)$

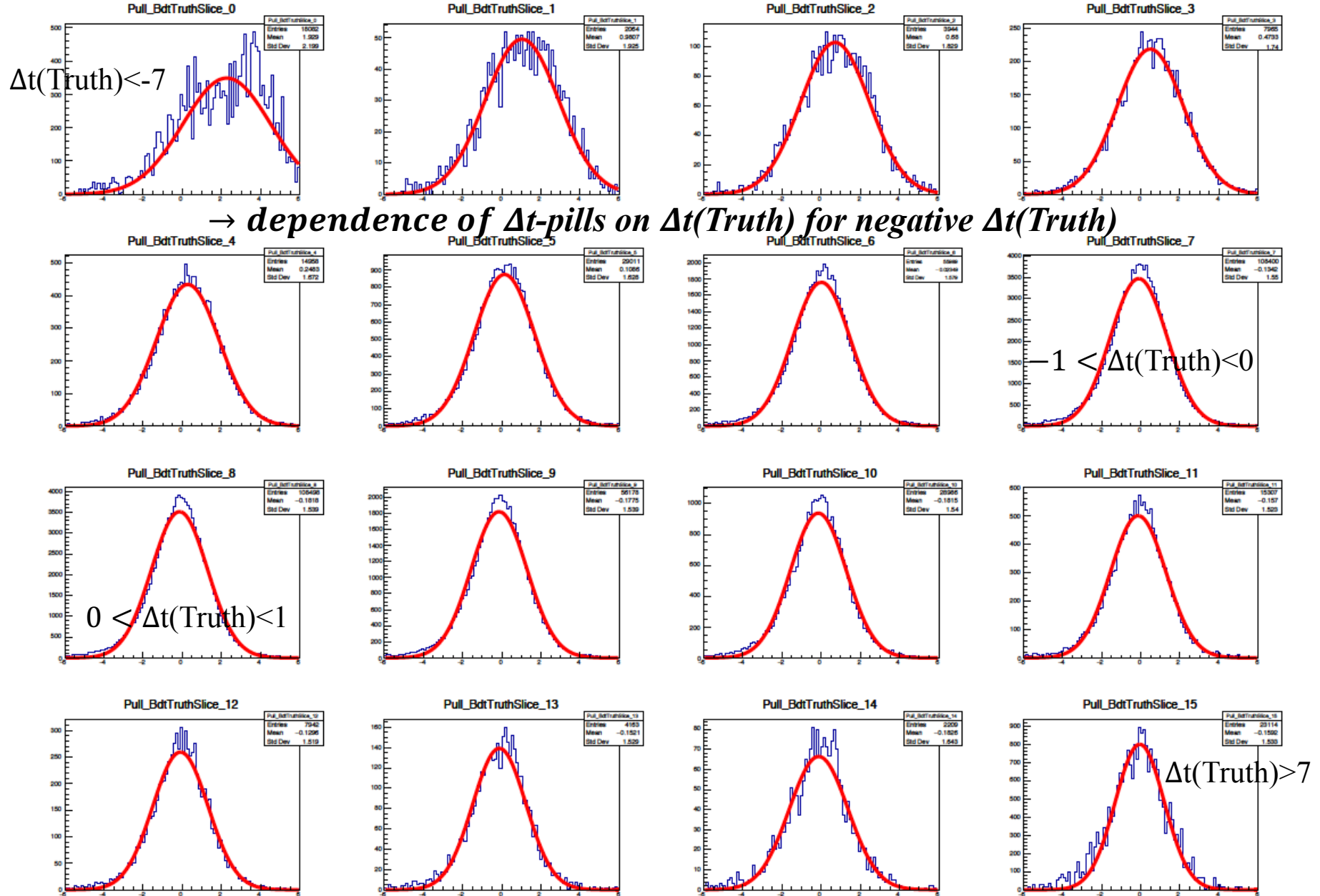


- strong differences in reco for positive and negative  $\Delta t$  (D-mesons, Beam spot)
- CPV asymmetry is less sensitive but much smaller than  $\Delta t$  biases in reco

# Uncertainties and pulls: $\Delta t$ , $z(\text{Btag})$ , $z(\text{J/Psi})$



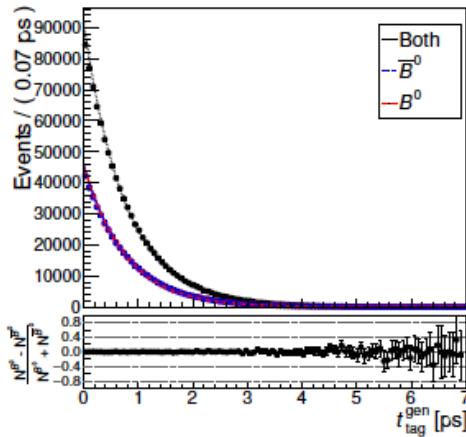
# $\Delta t$ -pulls for $\Delta t(\text{Truth})$ -slices from -8. to 8.



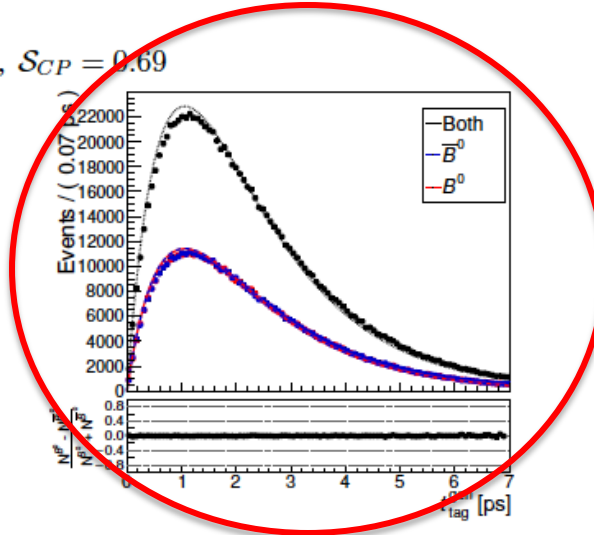
# Explanation of the dependence on $\Delta t(\text{Truth})$

Phd Fernando Abudinen

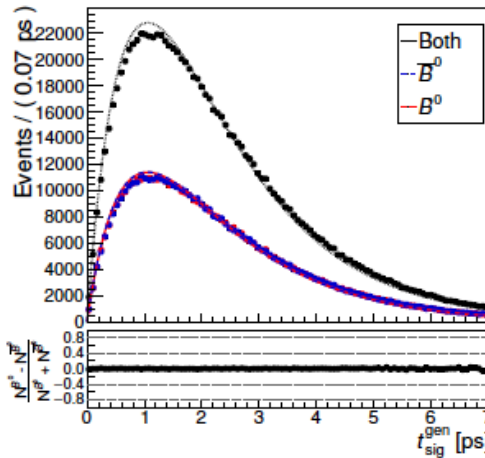
$$\mathcal{A}_{CP} = 0, \mathcal{S}_{CP} = 0.69$$



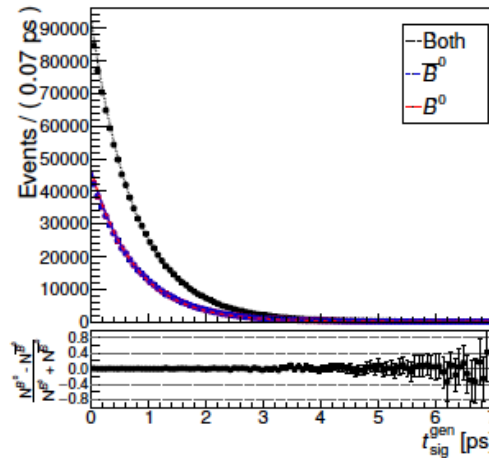
(a)  $t_{\text{tag}}$  for  $\Delta t > 0$ .



(b)  $t_{\text{tag}}$  for  $\Delta t < 0$ .



(c)  $t_{\text{sig}}$  for  $\Delta t > 0$ .

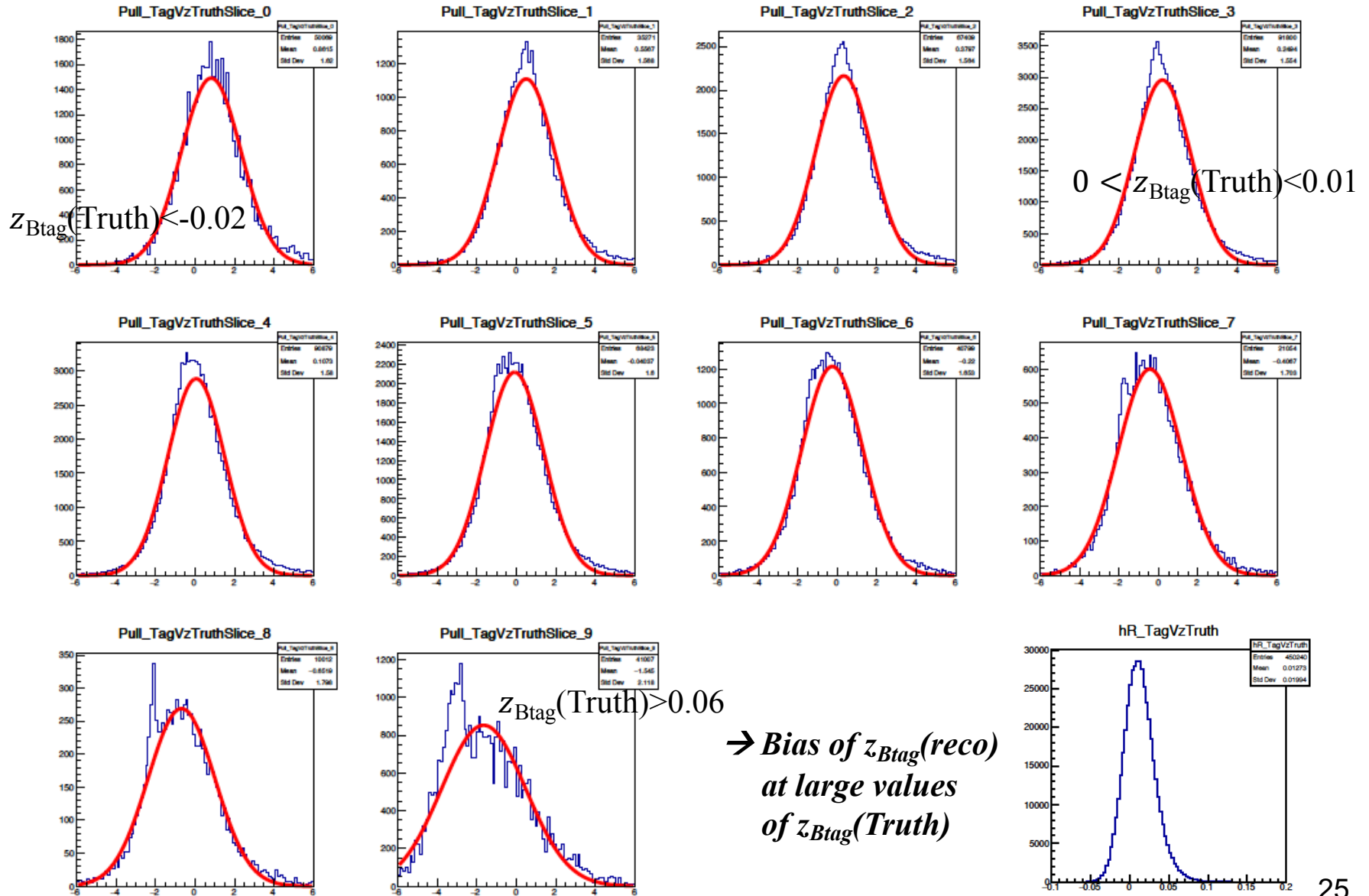


(d)  $t_{\text{sig}}$  for  $\Delta t < 0$ .

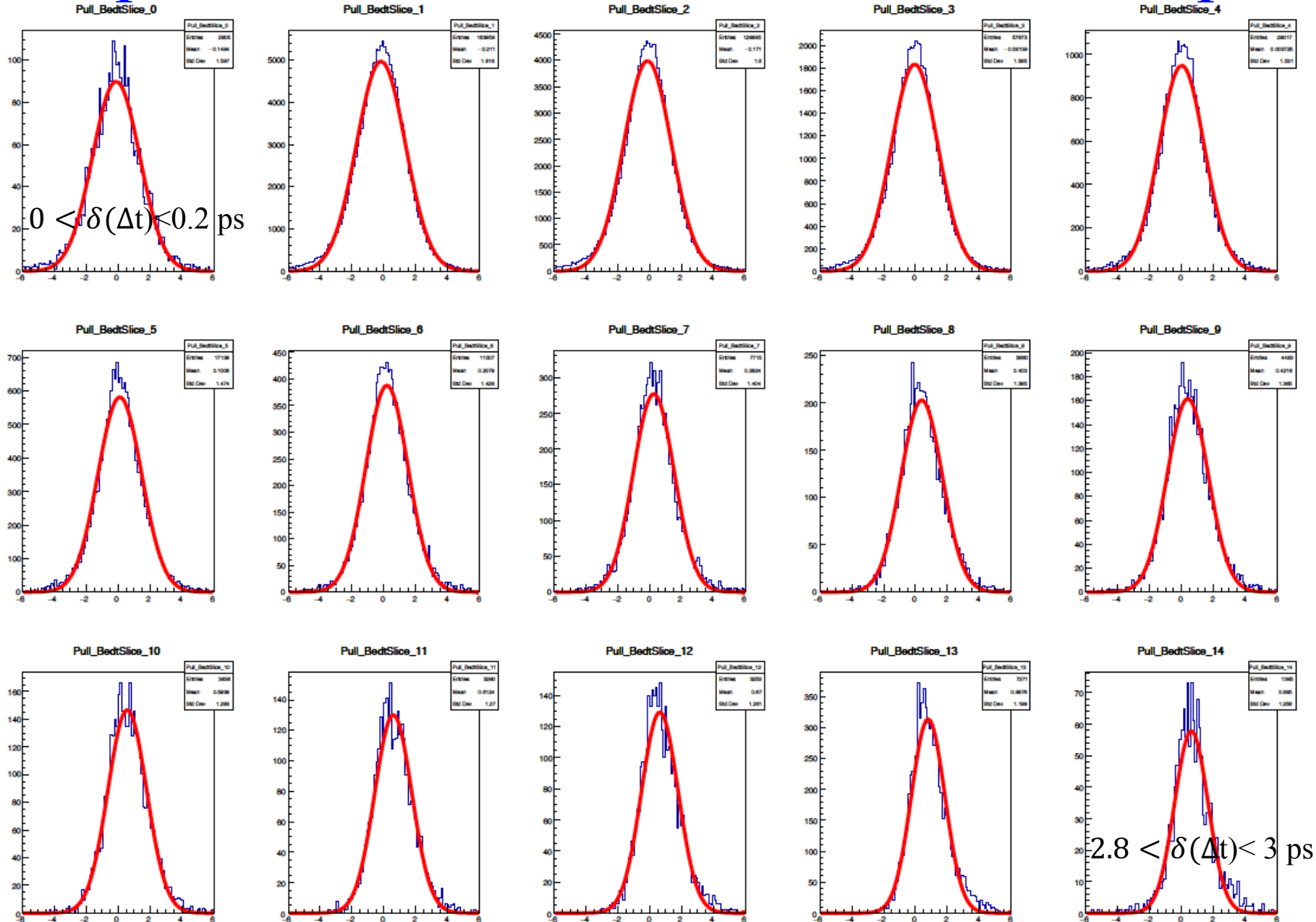
→ Possible explanation for  $\Delta t(\text{Truth})$ -dependence of  $\Delta t$ -pulls for negative  $\Delta t(\text{Truth})$ :

if  $t_{\text{Btag}}$  is positive and large the reconstructed Btag vertex position is biased towards the beam spot which is used as constraint in the vertex fit

# $z_{Btag}$ -pulls for slices in $z_{Btag}(\text{Truth})$

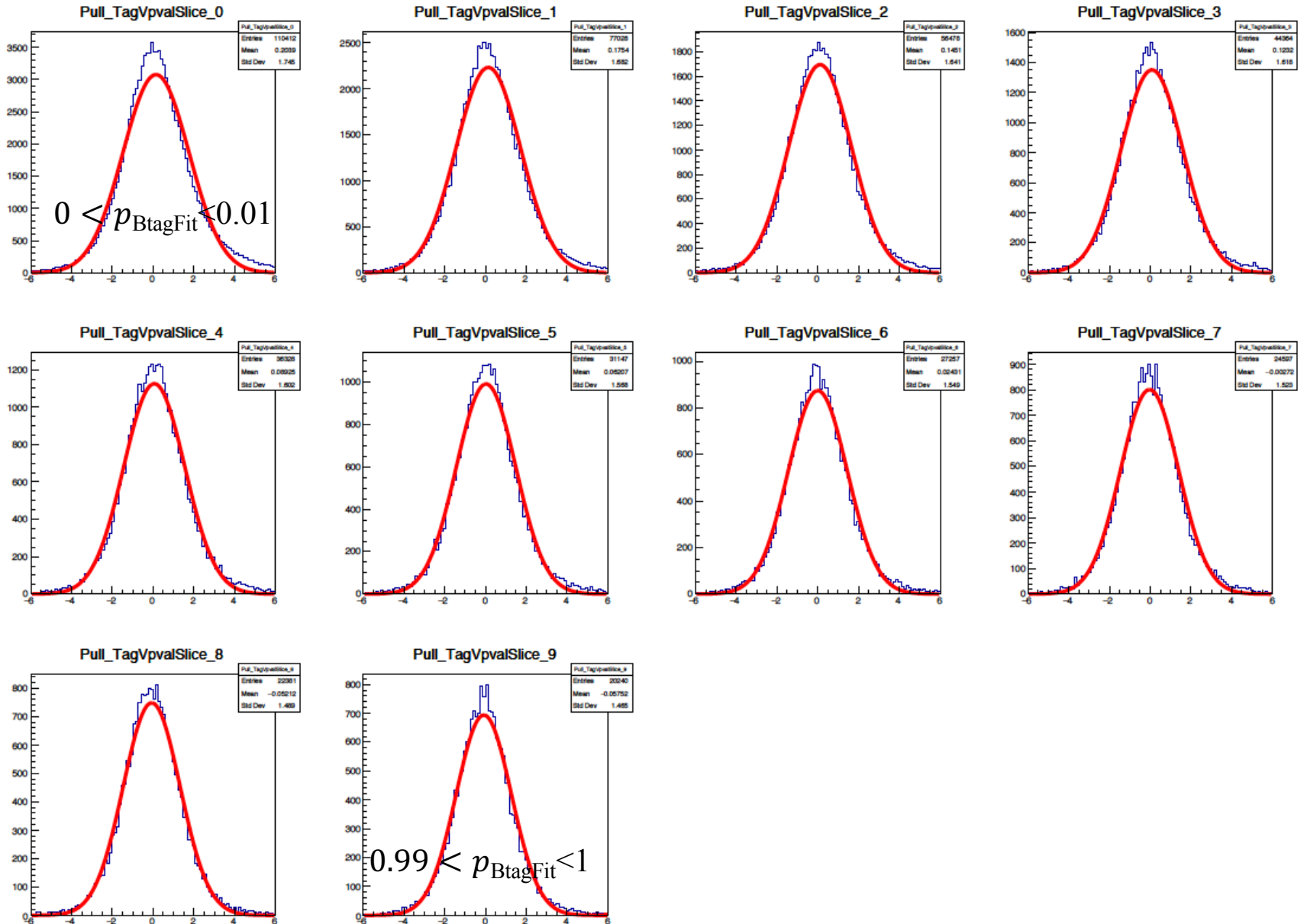


# $\Delta t$ -pulls for slices in $\Delta t$ errors from 0 to 3 ps





# $Z_{Btag}$ -pulls for slices in p-value of Btag fit



# Summary

*Biases of the  $\Delta t$  distribution due to reconstruction are considerably stronger than the effect caused by CPV asymmetry (although measurement of CPV asymmetry is less sensitive to these biases).*

*Biases in the  $\Delta t$  distribution are due to decays of D-mesons and the beam spot constraint in the Btag vertex fit.*

*The  $\Delta t$  resolution function ( $\Delta t$ -pulls) depends on*

- $\Delta t(\text{Truth}); t_{\text{Btag}}(\text{Truth}) \rightarrow$  **strictly forbidden ! It is open what to do.**
- $\delta(\Delta t)$  – error of  $\Delta t$
- $p$ -value of the Btag-fit.  $\rightarrow$  more fancy variables (“ $\xi^2$ ”, “ $t$ ”) are used in Belle but they are not (will not be ?) available in Belle2