MAX-PLANCK-INSTITUT
FÜR PHYSIK

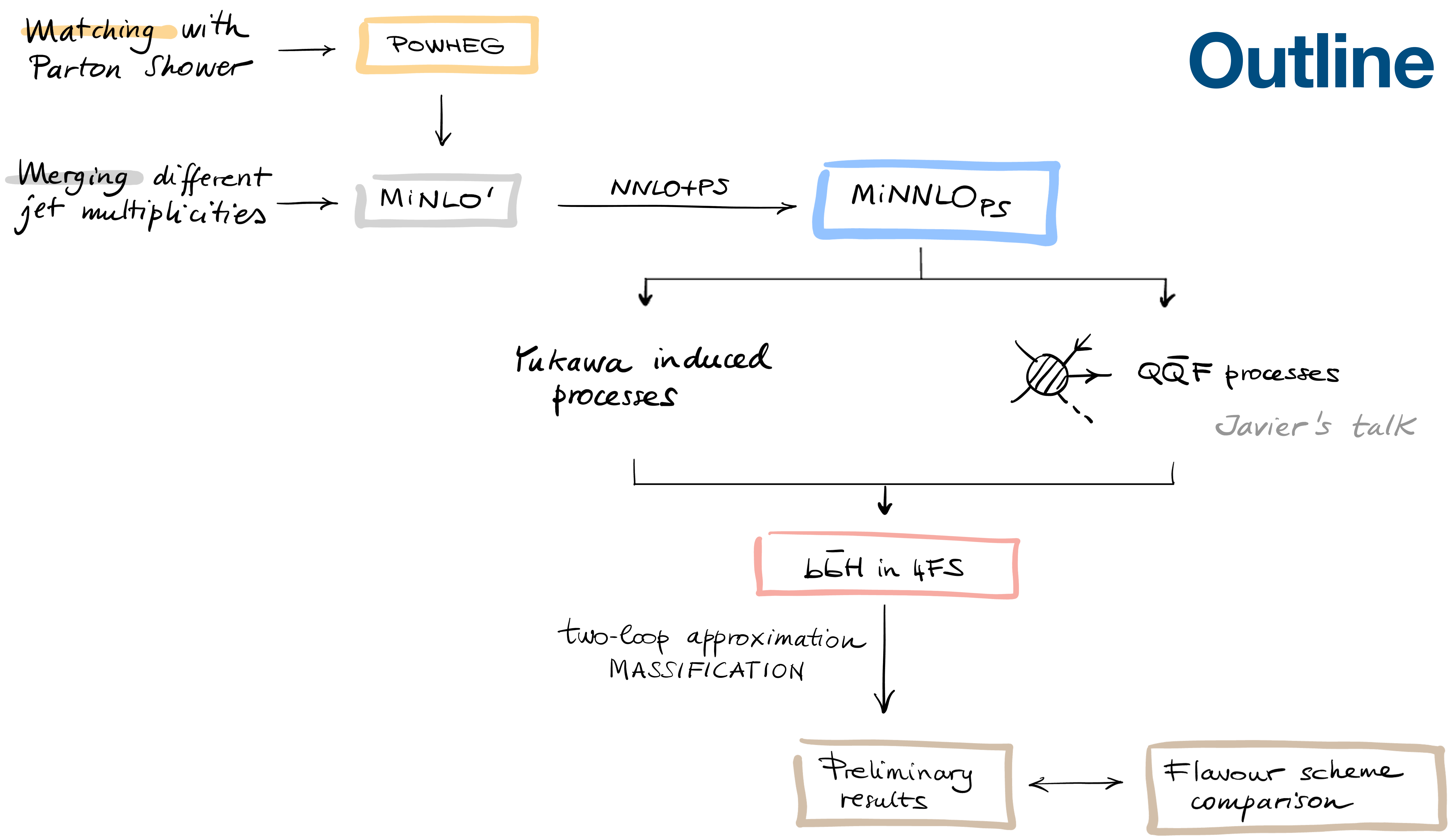
NNLO+PS predictions for bbH production in the four-flavour scheme

Christian Biello

in collaboration with
Javier Mazzitelli, Aparna Sankar, Marius Wiesemann, Giulia Zanderighi

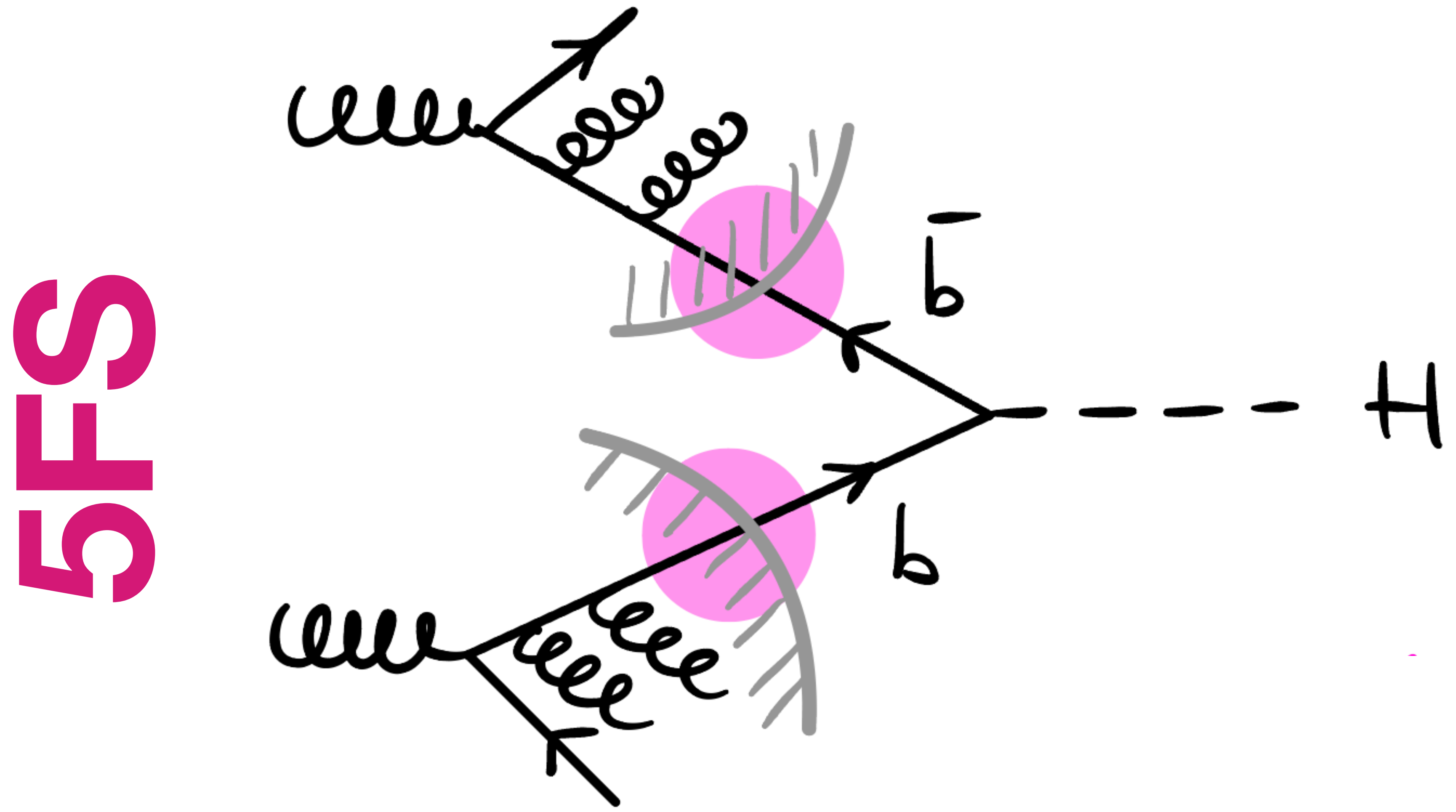
2nd Workshop on Tools for High Precision LHC Simulations
Ringberg Castle
May 9th, 2024

Outline



Matching with Parton Shower
POWHEG
Merging different jet multiplicities
MiNLO'
NNLO+PS
MiNNLOPS
Yukawa induced processes
QQ̄F processes
Javier's talk
bb̄H in 4FS
two-loop approximation
MASSIFICATION
Preliminary results
Flavour scheme comparison

Matching with PS in bbH: current state of the art



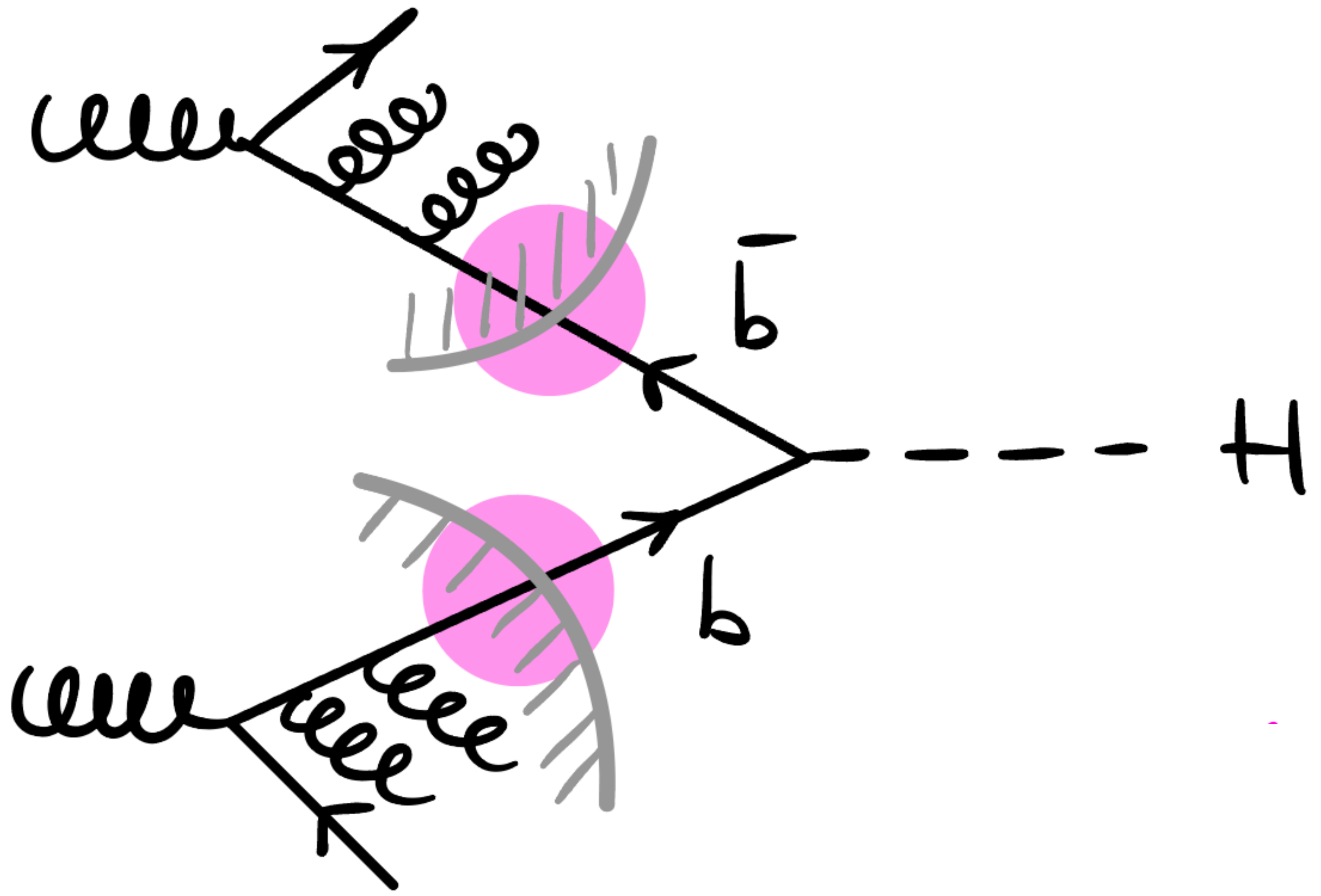
- Cross-section FO @N^3LO

  Duhr, Dulat, Mistlberger [1904.09990]

- $NNLO_{QCD} + PS$ Aparna's talk

Matching with PS in bbH: current state of the art

5FS



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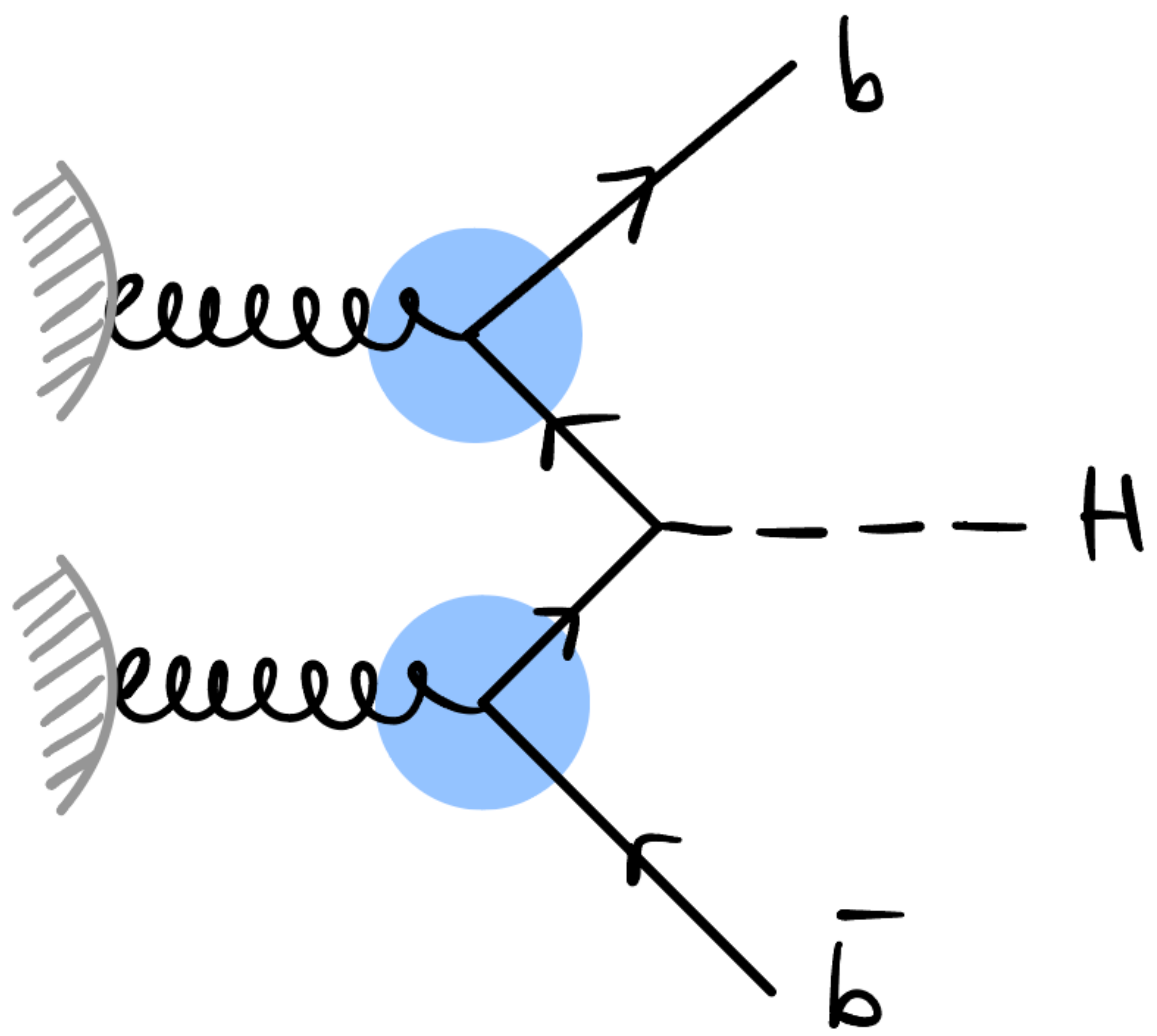
4FS



- Cross-section FO @NLO

  Dittmaier, Krämer, Spira [hep-ph/0309204]

- NLO$_{QCD}$ + PS

  Wiesemann, Frederix, Frixione, Hirschi, Maltoni, Torrielli [1409.5301]
  Jäger, Reina, Wackeroth [1509.05843]

- NLO$_{QCD}$ + PS combined with NLO$_{EW}$

  Pagani, Shao, Zaro [2005.10277]

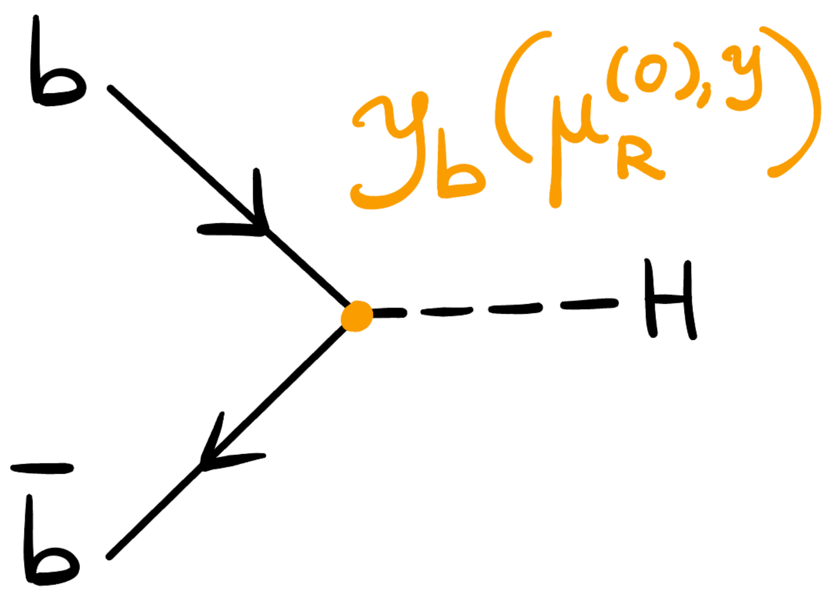
- NNLO$_{QCD}$ + PS   This talk

Yukawa in MiNNLOPS

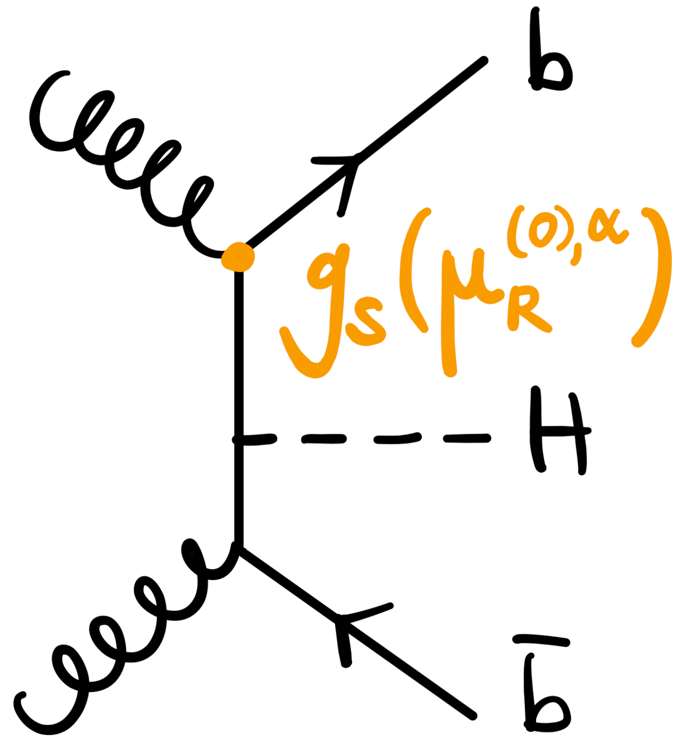
The $\overline{\text{MS}}$ running of this Born couplings

$$\sigma_{LO} \sim \alpha_s^{n_B}(\mu_R^{(0),\alpha})\, y^{m_B}(\mu_R^{(0),y})$$

requires some adaptations.



$(n_B = 0, m_B = 2)$



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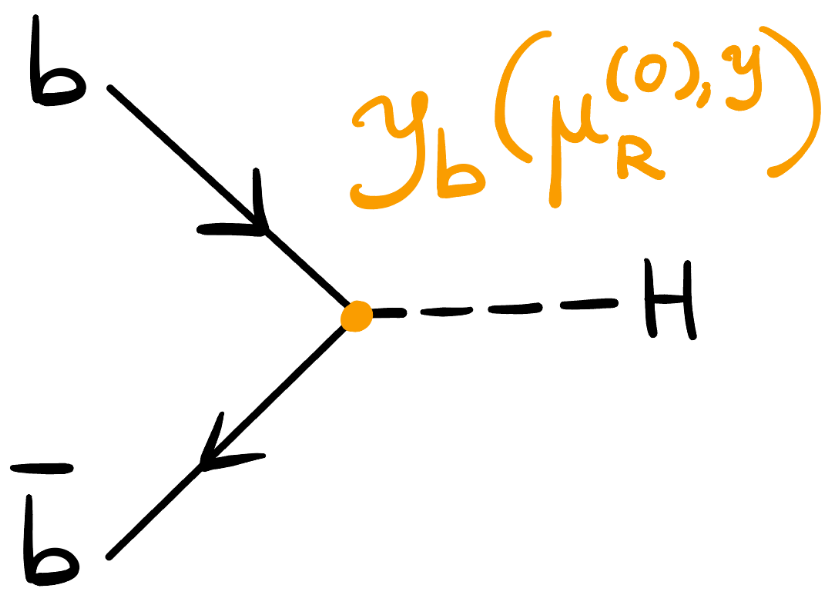

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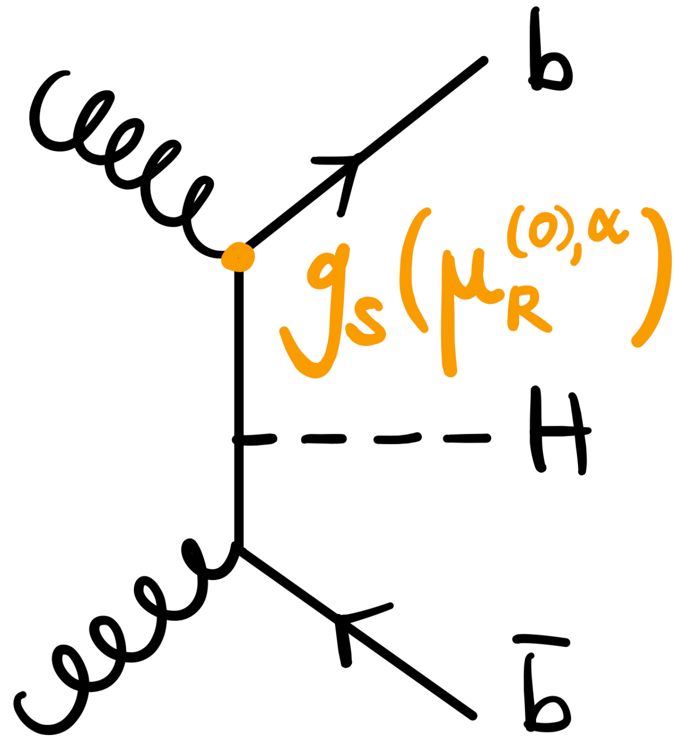

$(n_B = 2, m_B = 2)$

$H^{(1)} \supset$ single $\log(\mu_R^{(0),y})$

$H^{(2)} \supset$ single and double $\log(\mu_R^{(0),y})$ and mixed terms $\sim n_B m_B \log \mu_R^{(0),\alpha} \log \mu_R^{(0),y}$

$\tilde{B}^{(2)} \supset H^{(1)} \supset$ single $\log(\mu_R^{(0),y})$

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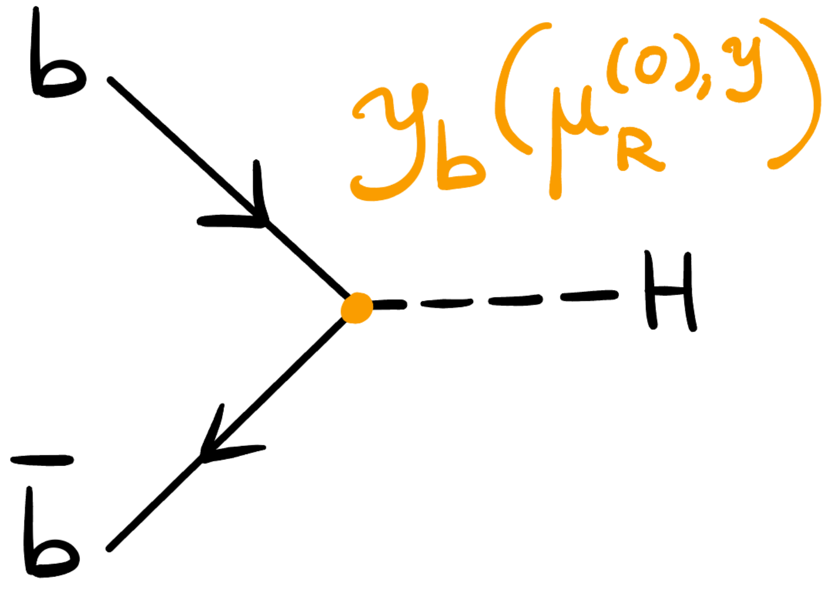

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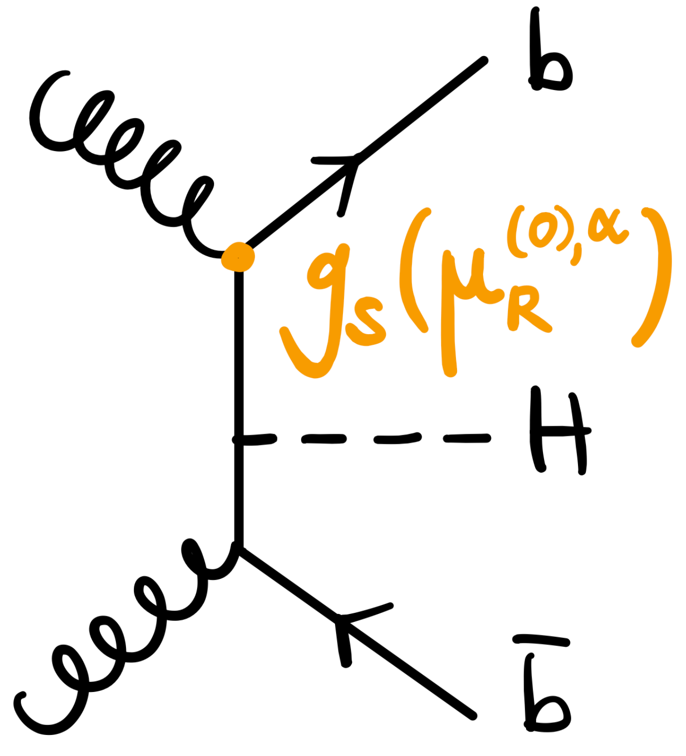

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$\tilde{B}^{(2)} \supset H^{(1)} \supset$ single $\log(\mu_R^{(0),y})$

The Yukawa scale has an interplay with the renormalisation and resummation scale factors

$$\alpha_s(p_T) \to \alpha_s\left(\frac{K_R}{K_Q} p_T\right) \rightsquigarrow H^{(2)} \supset \log K_R \log \mu_R^{(0),y} \text{ and } \log K_Q \log \mu_R^{(0),y}$$

POWHEG implementation

NLOPS Hbb

For future studies, we provided NLO+PS predictions for the y_b^2 contribution in Hbb.

We checked our code against the public one.

Jäger, Reina, Wackeroth [1509.05843]

We can perform predictions with new settings since we disentangled the Born scales.

	$(\mu_R^{(0),\alpha}, \mu_R^{(0),y})$	NLO_{PS}
default	$(\frac{H_T}{4}, m_H)$	$0.381(2)^{+20.2\%}_{-15.9\%}$ pb
	$(\frac{H_T}{4}, \frac{H_T}{4})$	$0.406(4)^{+16.6\%}_{-14.3\%}$ pb

$$H_T = \sum_{b,\bar{b},H} \sqrt{m_i^2 + p_{T,i}^2}$$

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$$H_T = \sum_{b,\bar{b},H} \sqrt{m_i^2 + p_{T,i}^2}$$

NLOps Hbbj

The starting point of our calculation is the

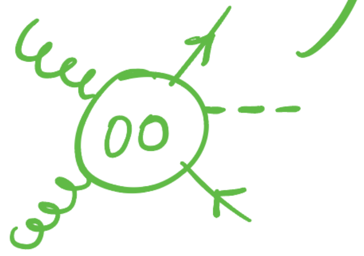
$$\text{POWHEG} + 1j$$

generator.

We used `OpenLoops` as amplitude provider (setting $y_t = 0$) and inserted a transverse momentum cut for the Born jet.

MiNLO’

$$\bar{B}(\Phi_{XJ}) = e^{-\tilde{S}(p_T)}\left\{B\left(1-\alpha_s(p_T)\,\tilde{S}^{(1)}\right)+V+\int \mathrm{d}\phi_{rad}\,R + \cancel{\left[D^{(3)}(p_T)\right]\times F^{corr}}\right\}$$



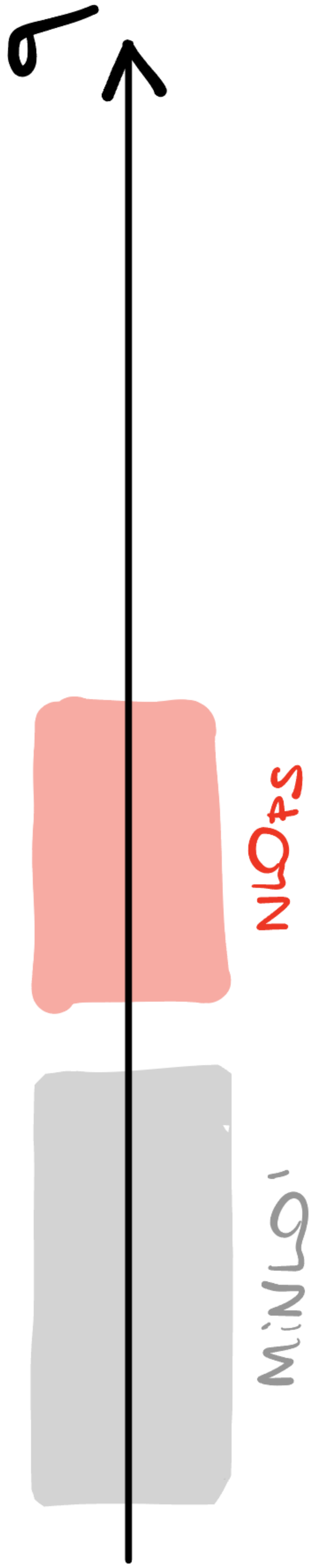
included in the Luminosity for MiNNLO$_{PS}$

In MiNLO’ there are no cancellations of the large $\log(m_b)$ in the real (RV, RR) contributions.

We need the VV contribution to cancel the quasi-collinear divergences.

Same behaviour observed in $b\bar{b}\ell^+\ell^-$.

Mazzitelli, Sotnikov, Wiesemann [2404.08598]



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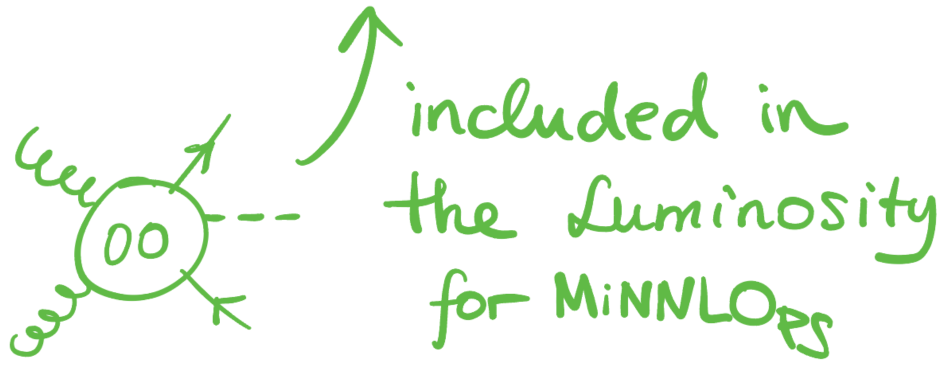

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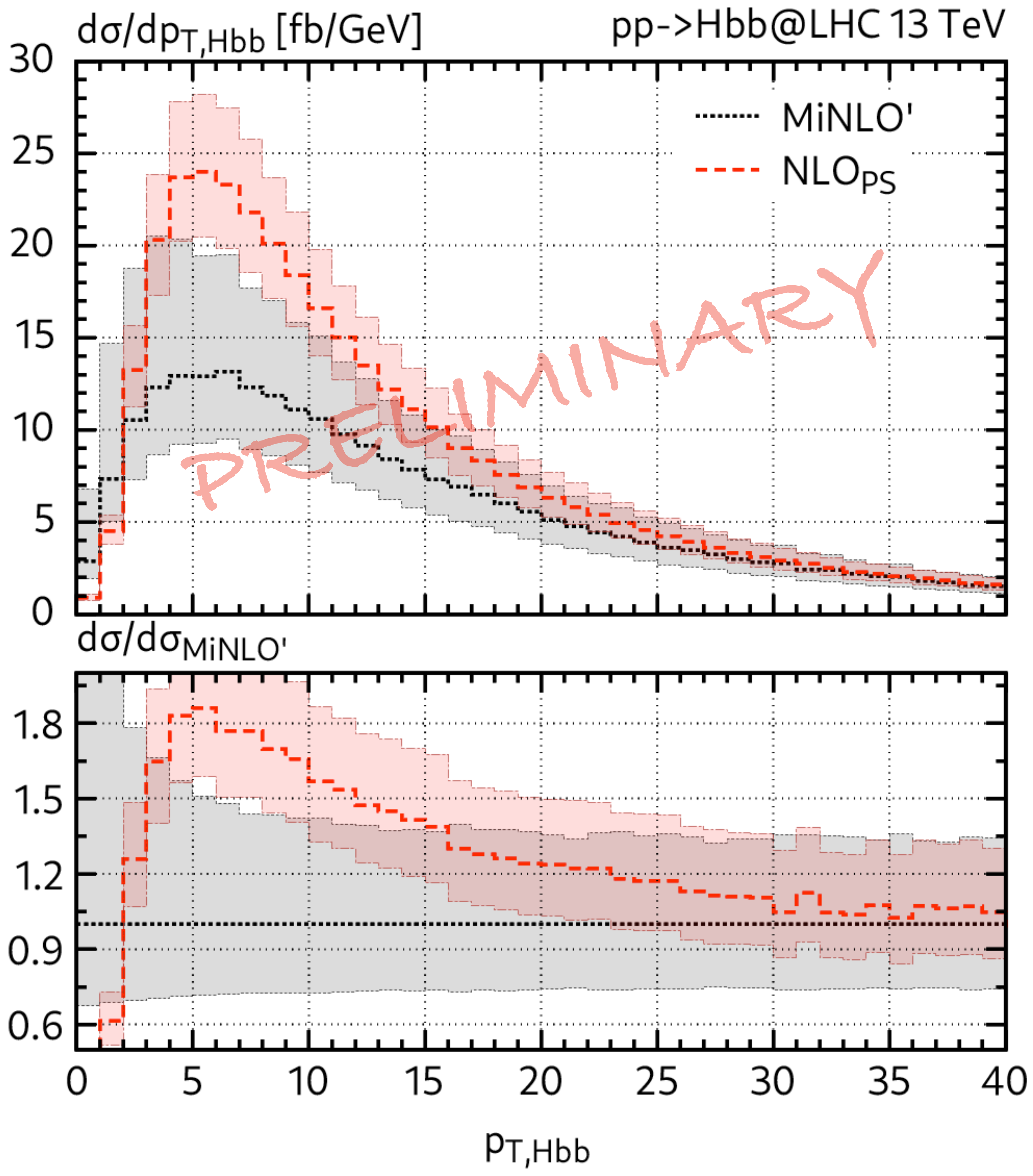

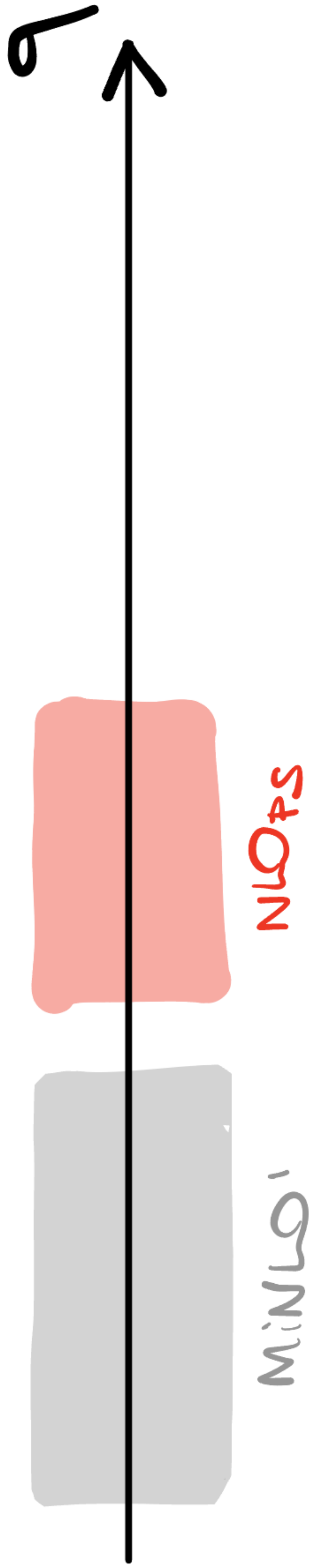

Two-loop approximation

The double virtual correction for massive bottoms is not known.

Approximation by retaining all the log-enhanced contributions through the massification procedure.

$$|\mathscr{A}^{(2)}\rangle = \log(m_b)\text{-terms} + \text{const.} + \mathcal{O}\left(\frac{m_b}{Q}\right)$$

$$\mathscr{F}^{(2)}|\mathscr{A}^{(0)}_{m_b=0}\rangle + \mathscr{F}^{(1)}|\mathscr{A}^{(1)}_{m_b=0}\rangle + \mathscr{F}^{(0)}|\mathscr{A}^{(2)}_{m_b=0}\rangle$$

MiNNLOPS with only logarithmic contributions in the VV predicts a total cross-section bigger than the NLO+PS one.

$(\mu_R^{(0),\alpha}, \mu_R^{(0),y})$	NLOPS	MiNLO'	MiNNLOPS ($\mathcal{F}^{(0)}=0$)
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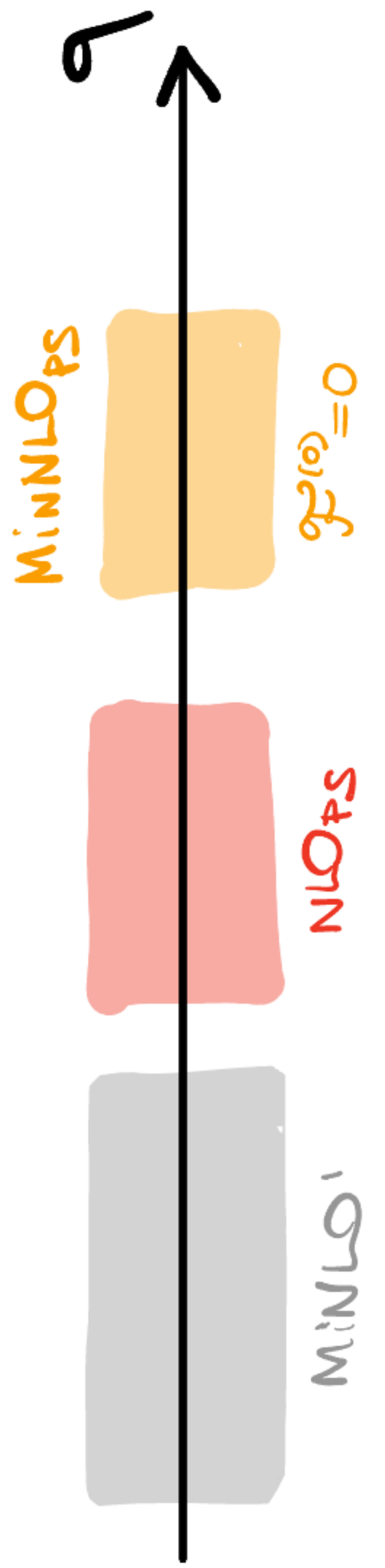
$(\frac{H_T}{4}, \frac{H_T}{4})$	$0.406(4)^{+16.6\%}_{-14.3\%}$ pb	$0.315(3)^{+30.6\%}_{-27.5\%}$ pb	$0.443(9)^{+4.0\%}_{-8.7\%}$ pb



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How to evaluate the massless two-loop?

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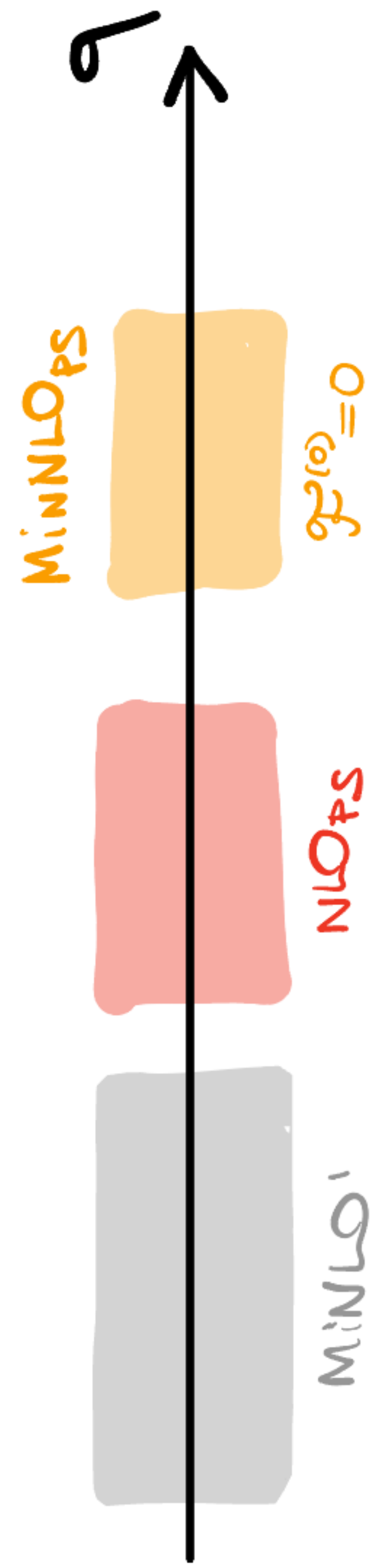
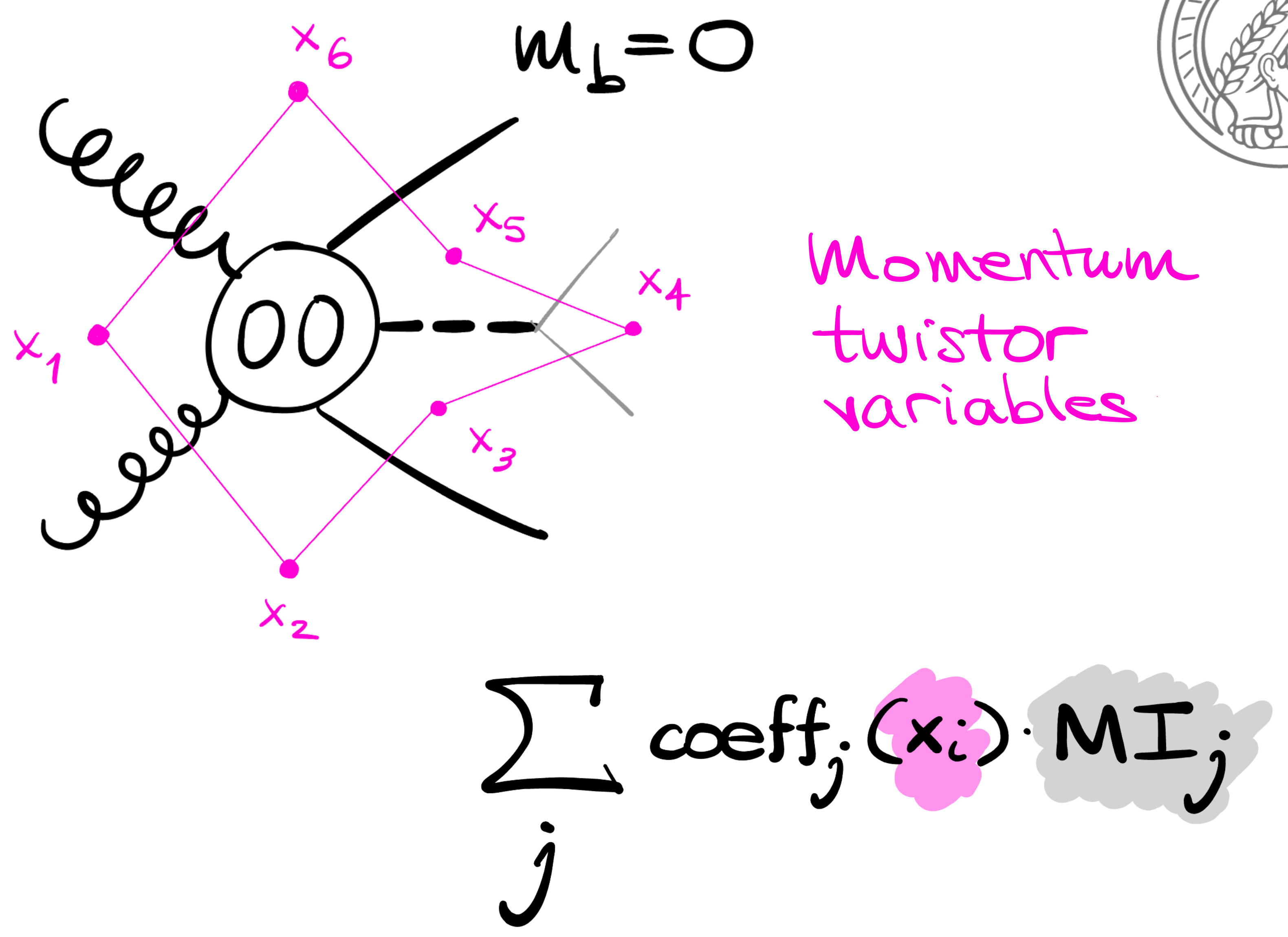


Massless two-loop library

We used analytic two-loop amplitudes for massless bottoms computed in the leading color approximation.

Badger, Hartanto, Kryś, Zoia [2107.14733]



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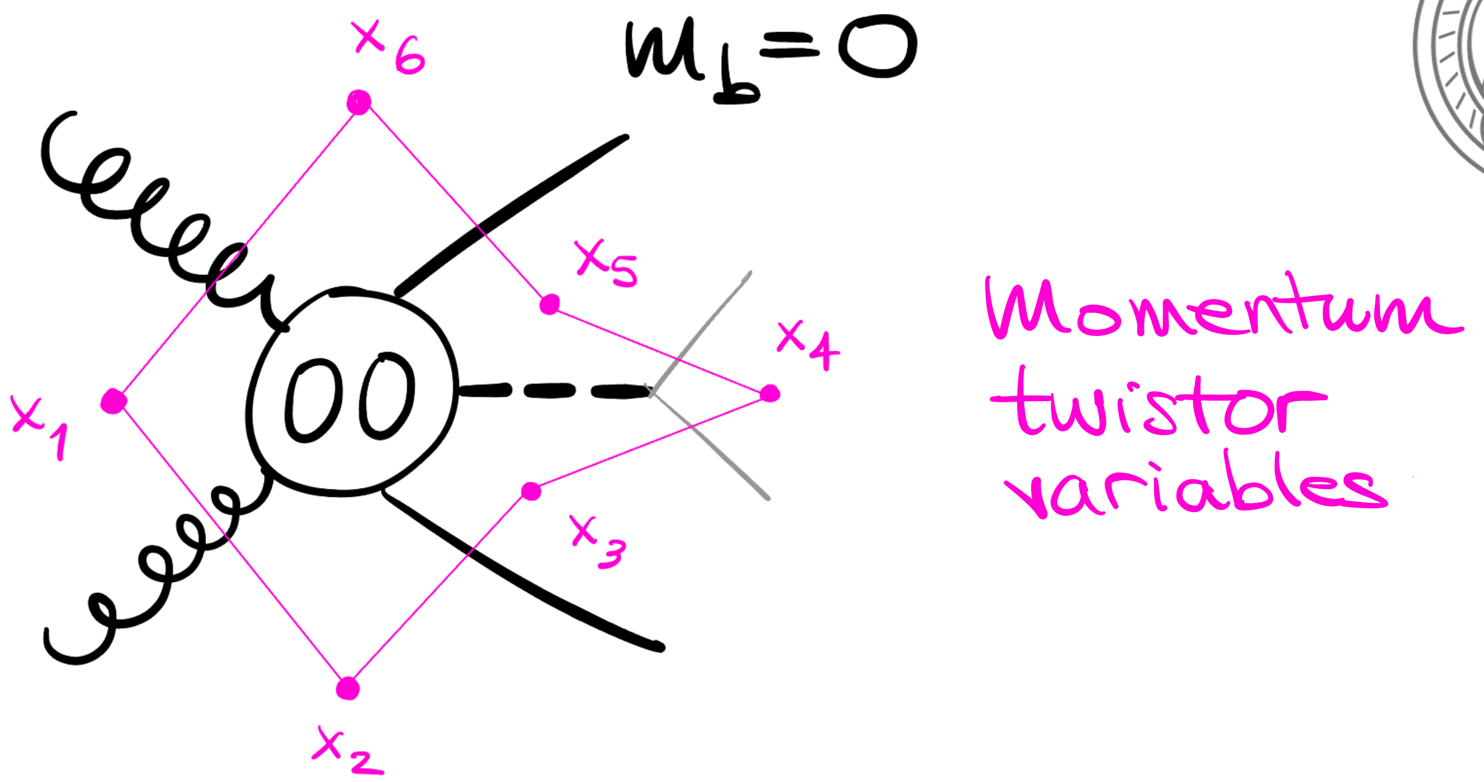
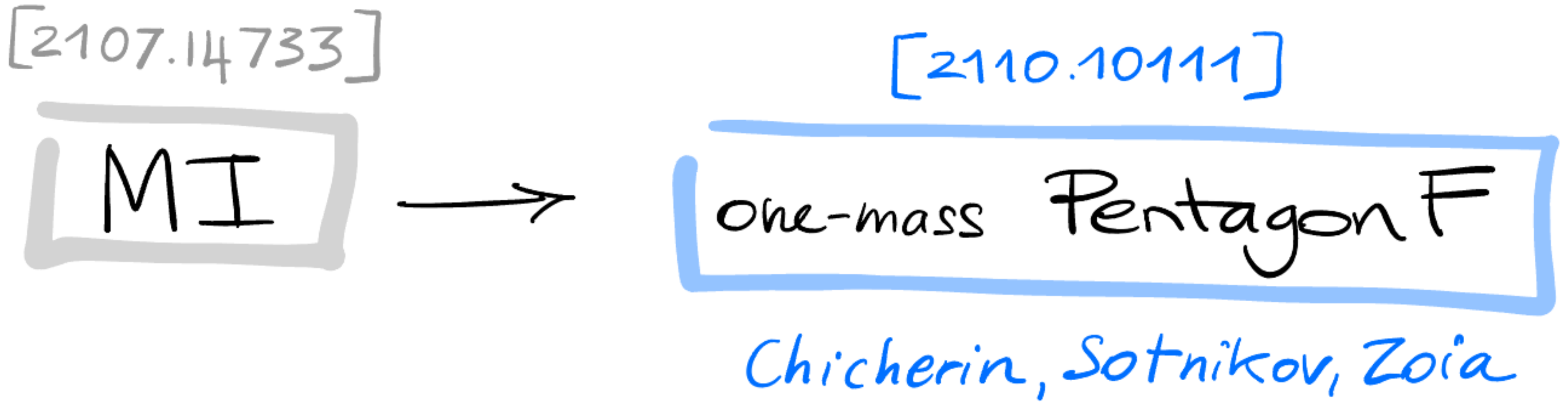


$$\sum_j \mathrm{coeff}_j(x_i)\cdot \mathrm{MI}_j$$

For fast numerical evaluation, we derived a mapping for the MIs in order to use the `PentagonFunctions` library [2009.07803, 2110.10111]



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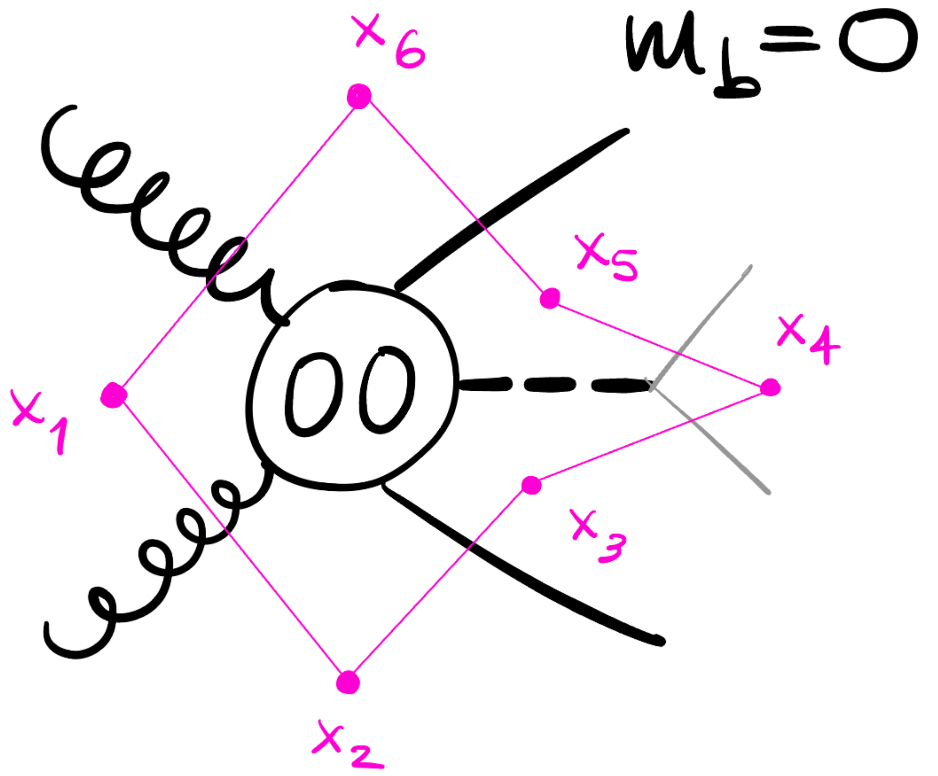
[2107.14733] MI → [2110.10111] One-mass PentagonF

Chicherin, Sotnikov, Zoia



Momentum twistor variables

$$\sum_j \text{coeff}_j(x_i) \cdot \text{MI}_j$$

IR SCHEME in the library

$$\mathcal{A}^{\text{Catani}} = (\mathbb{1} - \mathbb{I})\, \mathcal{A}^{\text{UV-ren}} \quad \text{[hep-ph/9802439]}$$

$$\mathcal{A}^{\text{SCET}} = \mathcal{Z}^{-1}\, \mathcal{A}^{\text{UV-ren}} \quad \text{[0901.0722]}$$

$$\rightsquigarrow \mathcal{A}^{\text{SCET}} = \mathcal{Z}^{-1} (\mathbb{1} - \mathbb{I})^{-1} \mathcal{A}^{\text{Catani}}$$

output of the library (for $\mathcal{A}^{\text{SCET}}$); Badger et al. (for $\mathcal{A}^{\text{Catani}}$)

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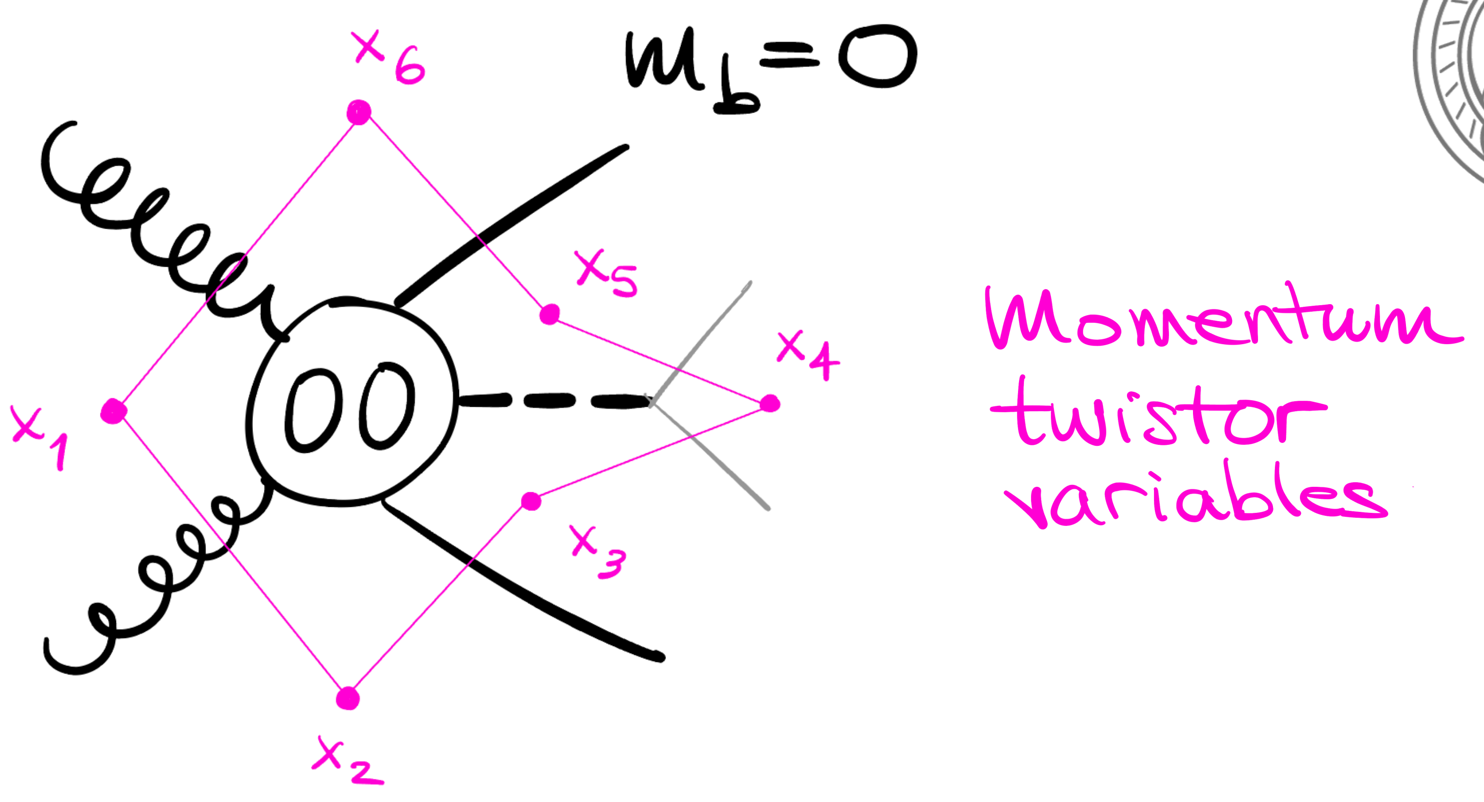

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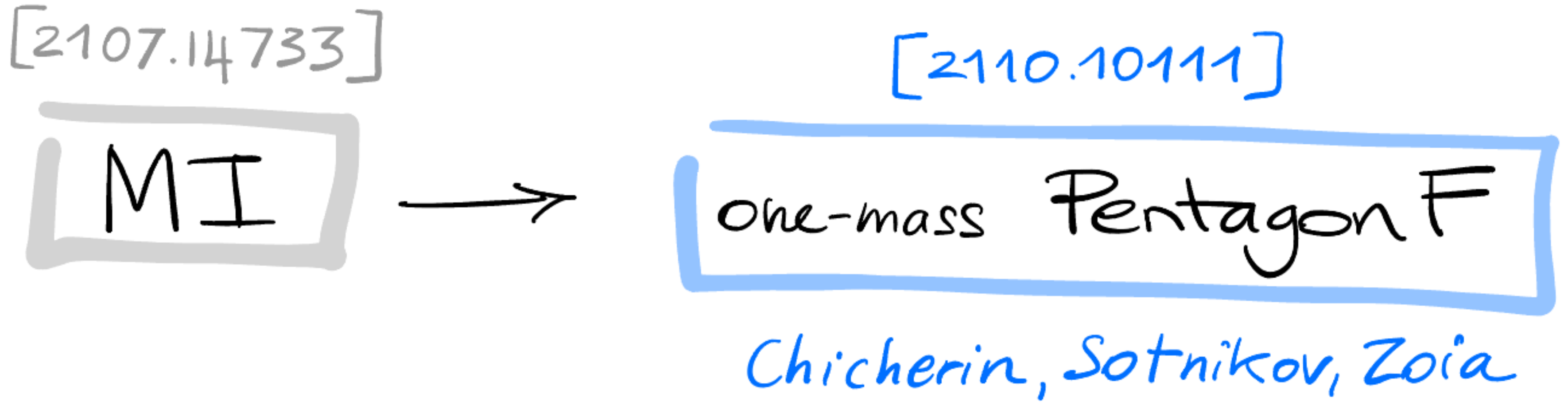

C++ code interfaced with POWHEG:

~ 3 sec for each PS point in double precision

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output of the library — Badger et al.

Moriond QCD 2024

Checked against the independent Zurich implementation

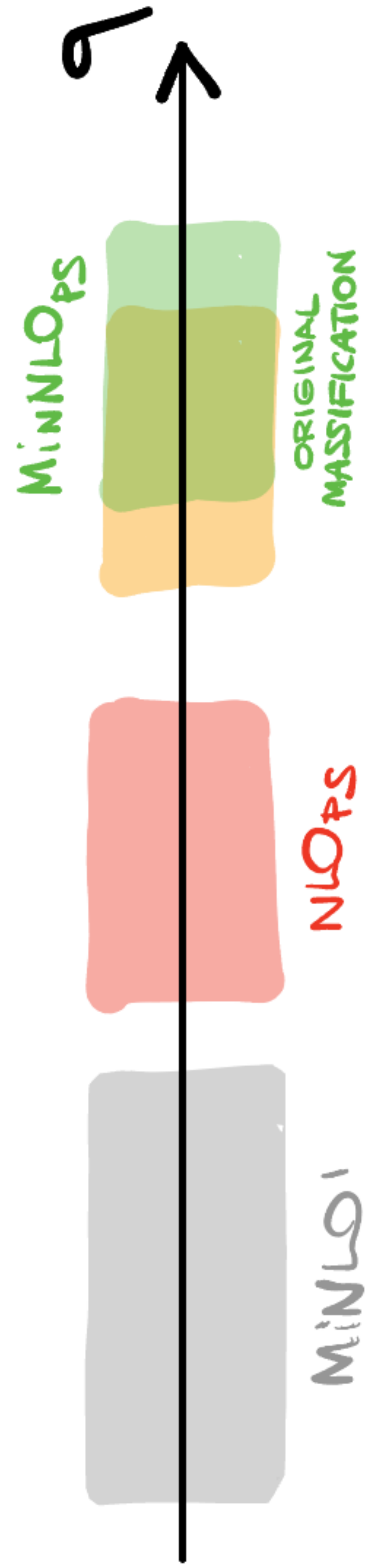
Original massification

First two-loop massification in Bhabha scattering — Penin [hep-ph/0508127]

Extension for non-abelian theories from factorisation principles — Mitov, Moch [hep-ph/0612149]

$$|\mathcal{A}(m_i,\epsilon)\rangle = \prod_{i\,=\,\text{massive external legs}} \overbrace{\left(Z_i\left(\frac{m^2}{\mu^2},\alpha_s(\mu^2),\epsilon\right)\right)}^{\text{Universal factors}}{}^{1/2}\; |\mathcal{A}(m_i=0,\epsilon)\rangle$$

First check in $q\bar{q} \to Q\bar{Q}$
Czakon, Mitov, Moch [0705.1975]



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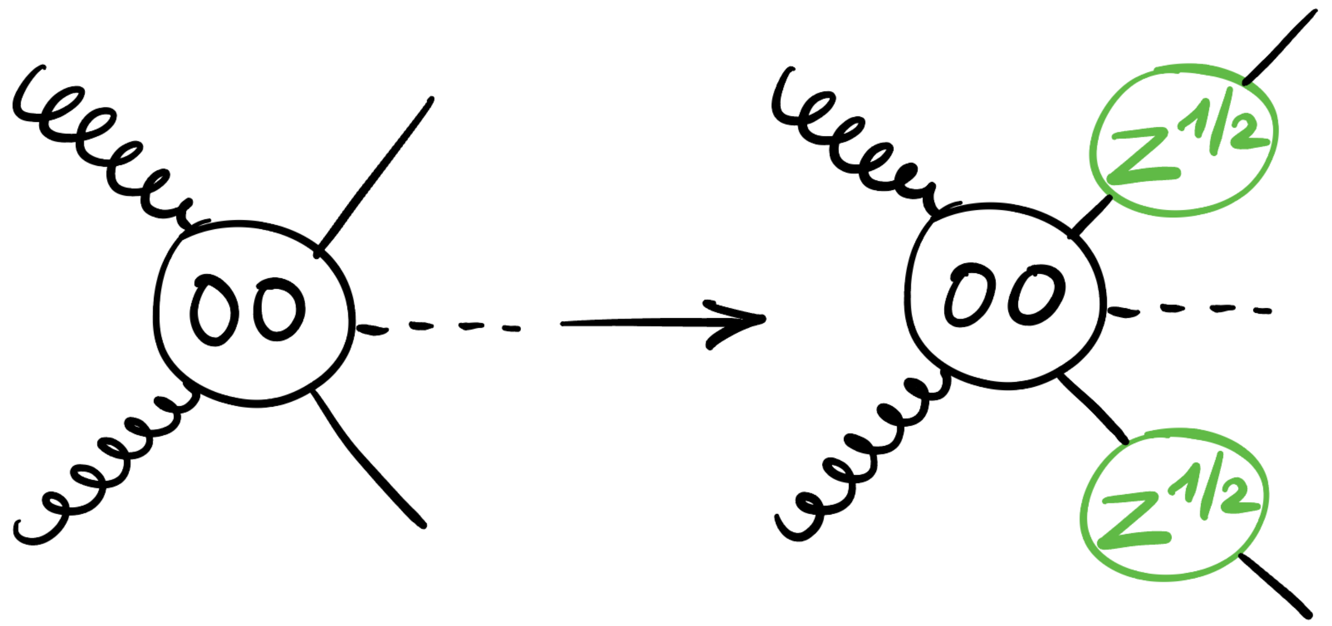
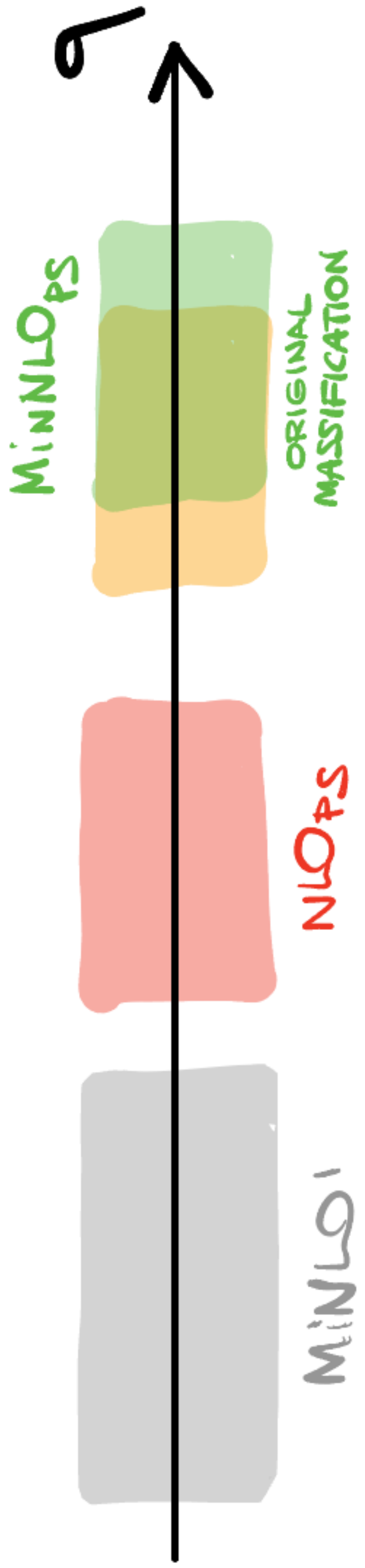


First check in $q\bar{q} \to Q\bar{Q}$
Czakon, Mitov, Moch [0705.1975]

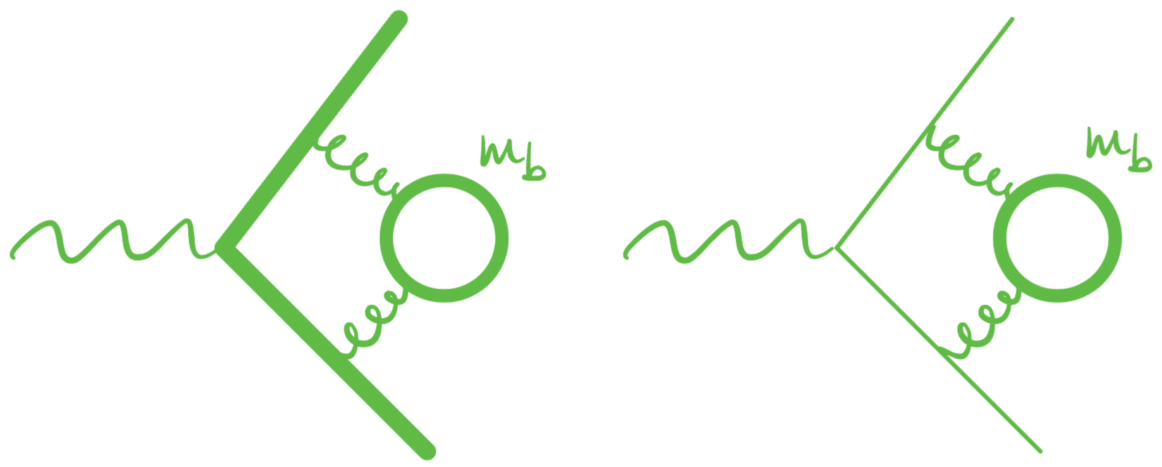
Mapping $\eta : \mathrm{PS}_{m_b} \mapsto \mathrm{PS}_{m=0}$

$\eta_{q\bar{q}}$ preserves the total momentum of $b\bar{b}$

η_{gg} avoids a collinear singularity



Generalised massification



First massification of internal loops in Bhabha using the SCET formalism

Becher, Melnikov [0704.3582]

Recent application for QCD amplitudes

Wang, Xia, Yang, Ye [2312.12242]

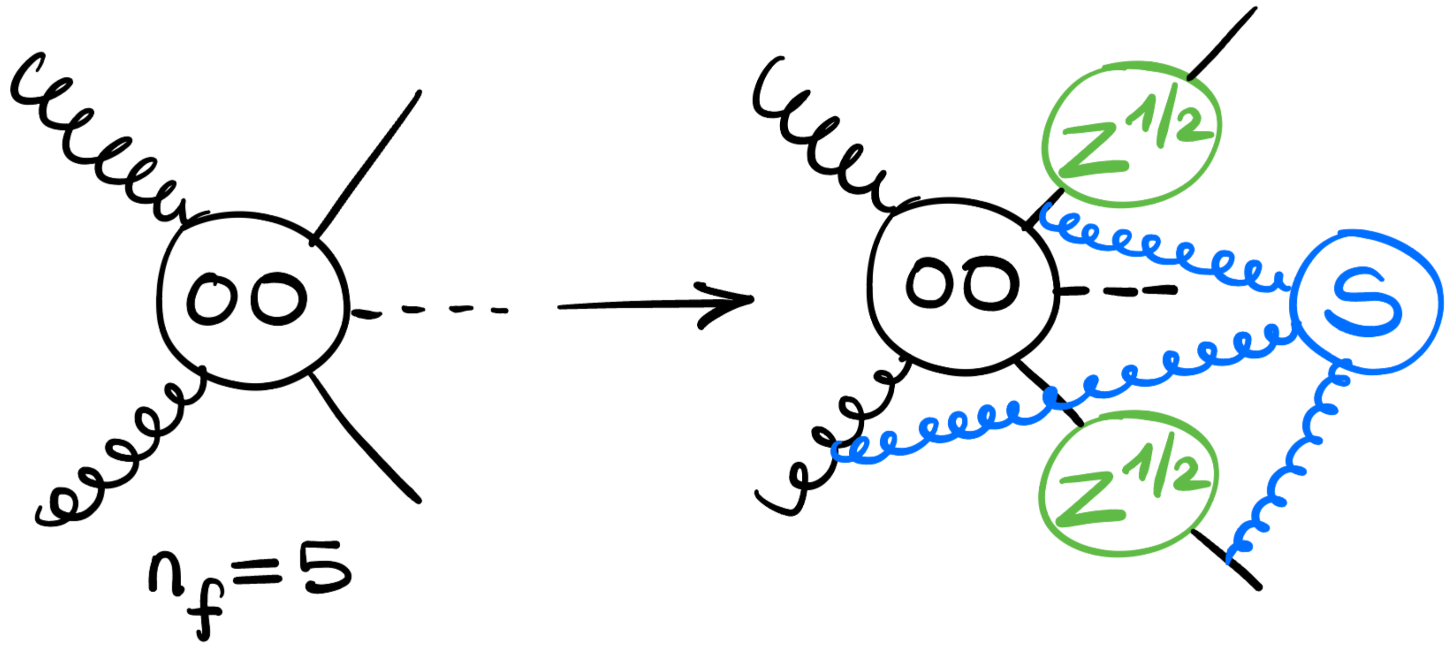
$$|\mathcal{M}_{massive}\rangle = \prod_i \left(Z_i(\{m\})\right)^{1/2} S(\{m\}) \, |\mathcal{M}_{massless}\rangle$$

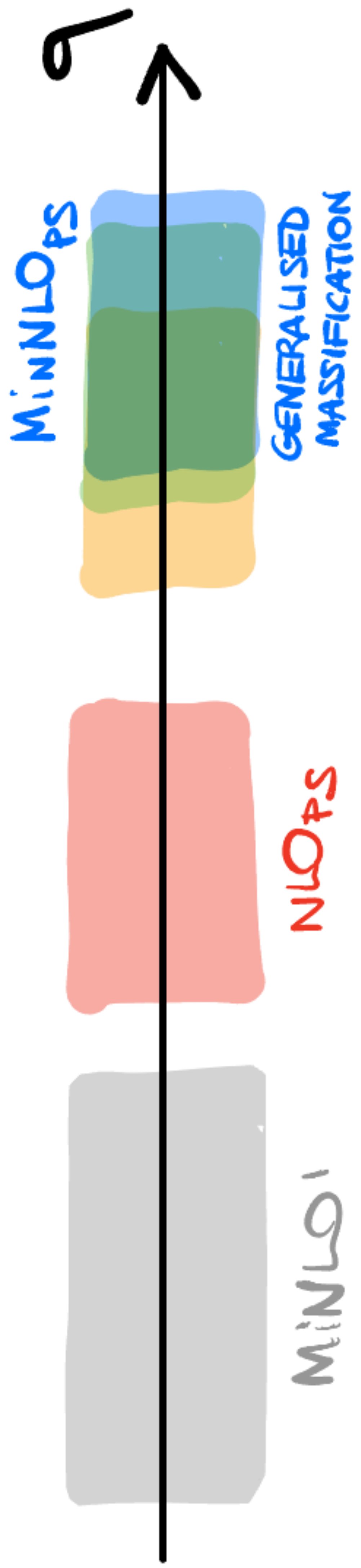
SOFT FUNCTION

with massive loop effects

$\mathcal{O}(\alpha_s^2)$ effects

$T_i \cdot T_j$





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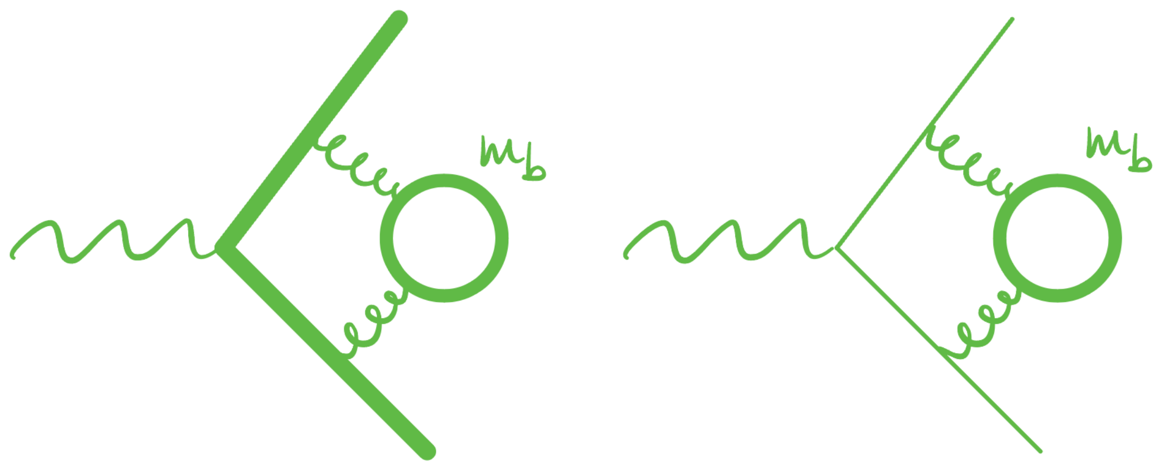

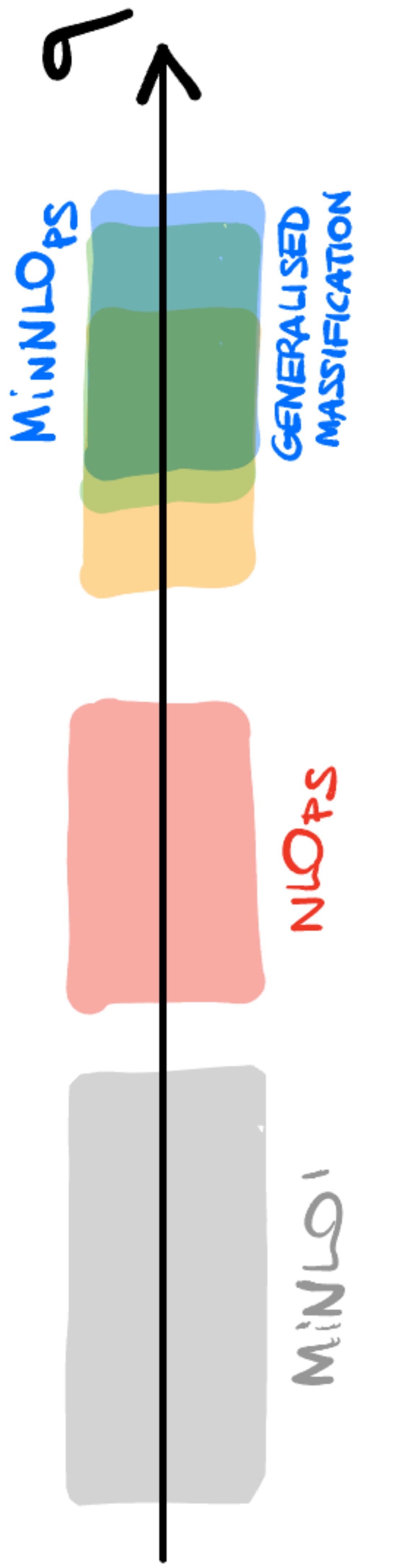

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$$|\mathcal{A}_{\text{massive}}\rangle = \prod_i \left(Z_i(\{m\})\right)^{1/2} S(\{m\})\,|\mathcal{A}_{\text{massless}}\rangle$$

with massive loop effects

$\mathcal{O}(\alpha_s^2)$ effects

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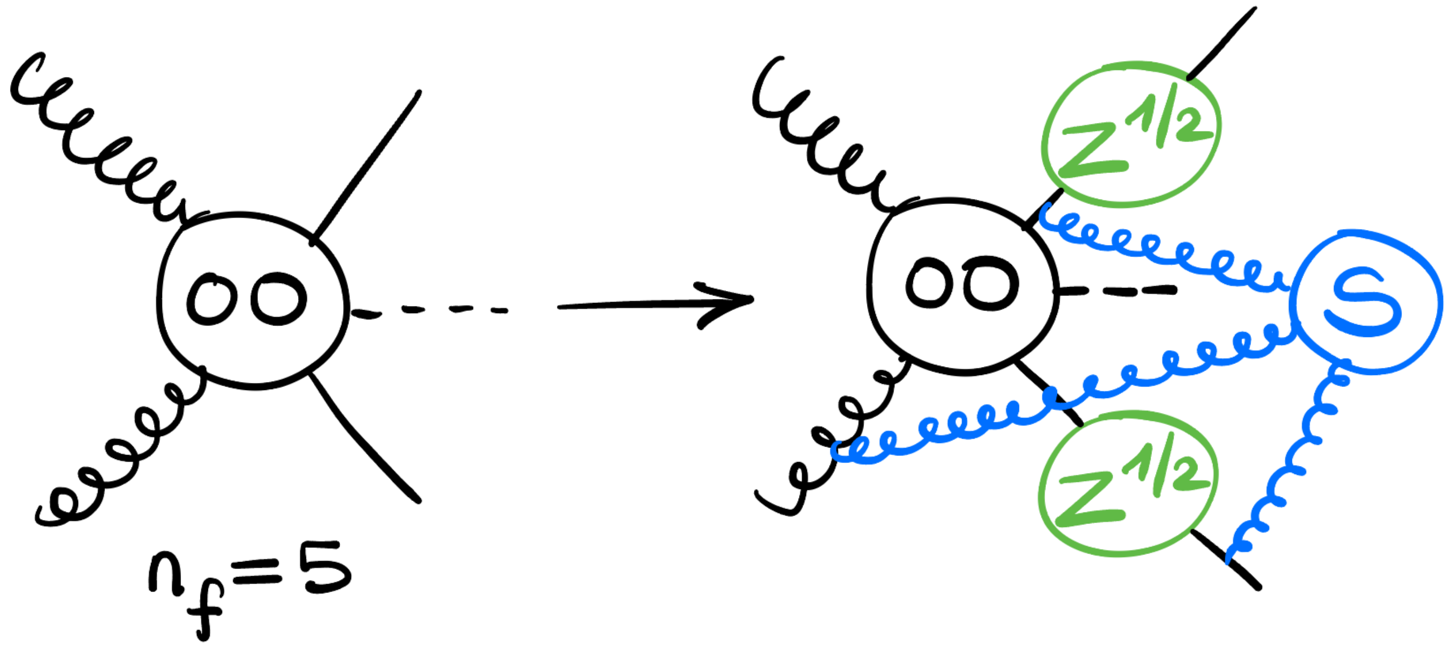
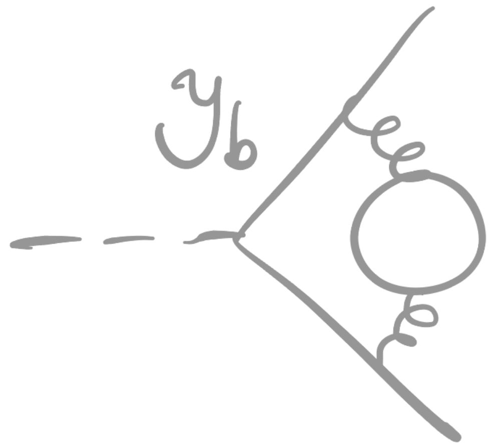


We applied decoupling relations for α_s and $\overline{\text{MS}}$ Yukawa

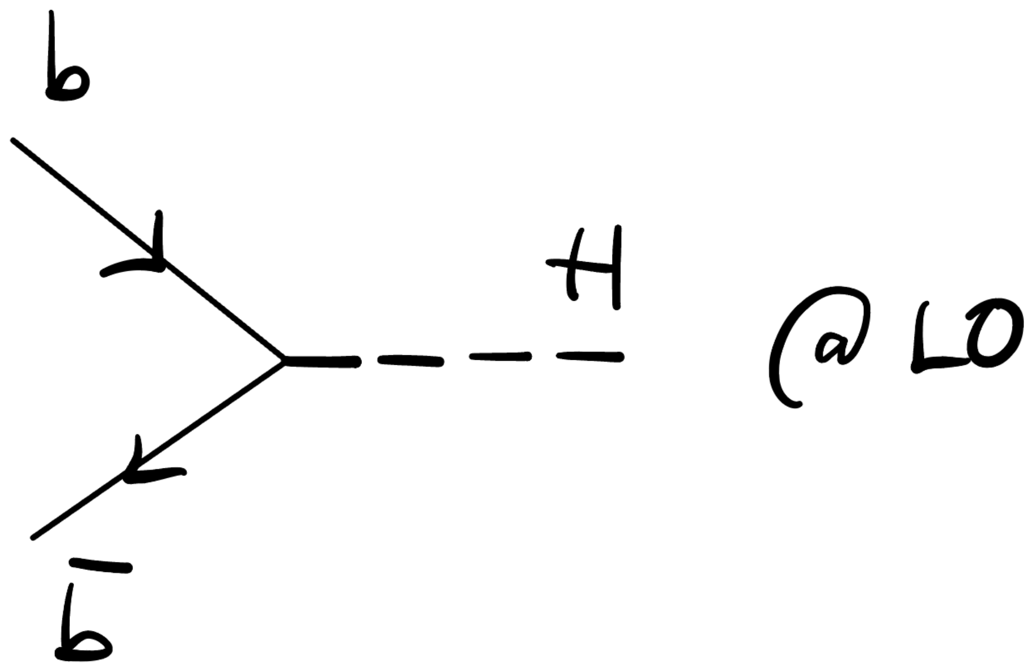


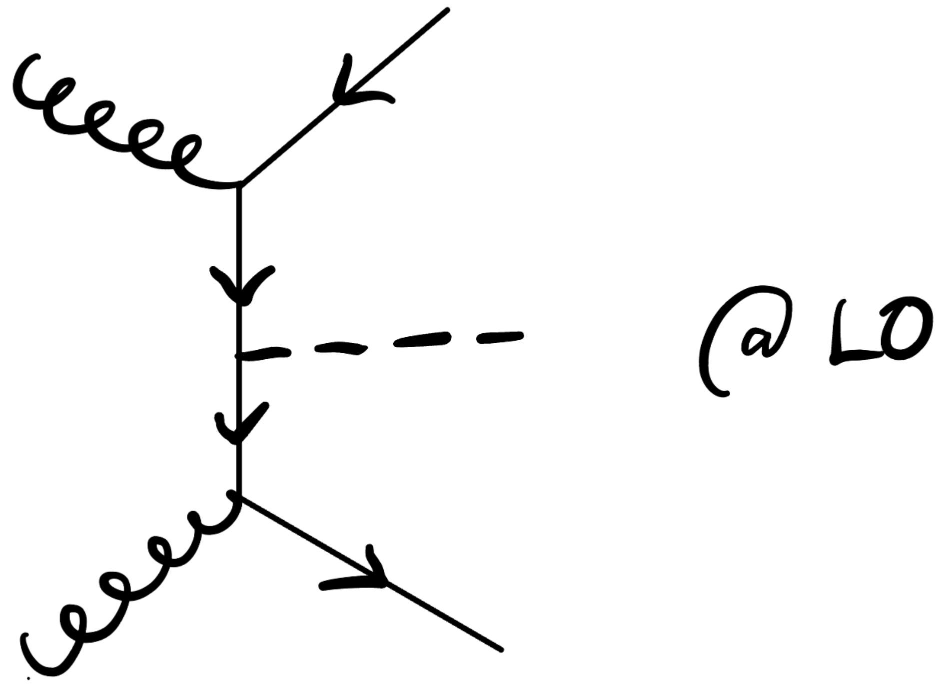
$$y_b^{(n+1)}(\mu) = y_b^{(n)}(\mu)\left(1 + \alpha_s^2(\mu)\cdot \text{logs}\right)$$

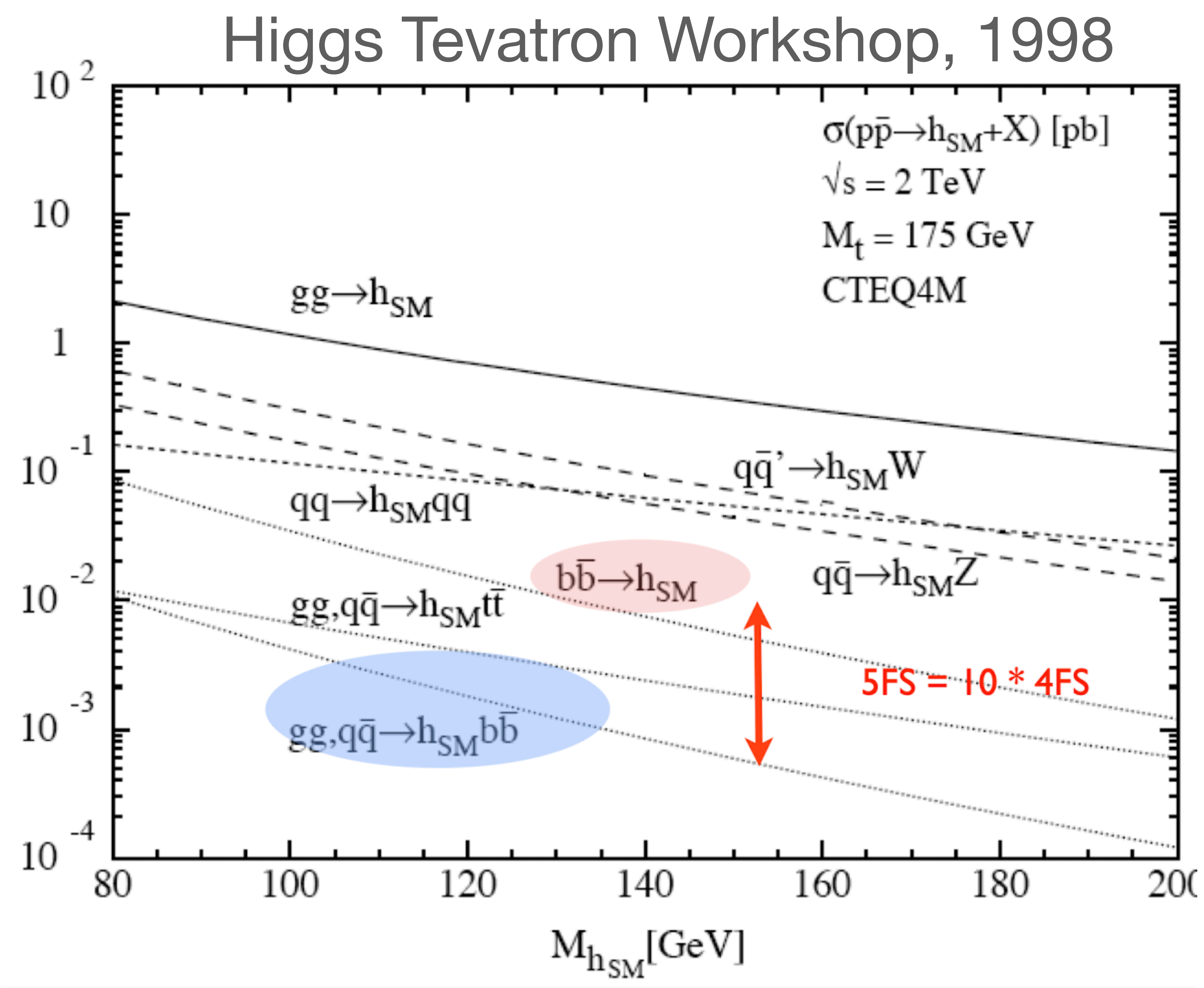
$$\bar{\mathcal{F}}^{(2)} \to \bar{\mathcal{F}}^{(2)} + \text{logs}$$

Comparison between the flavour schemes

FS comparison: LO



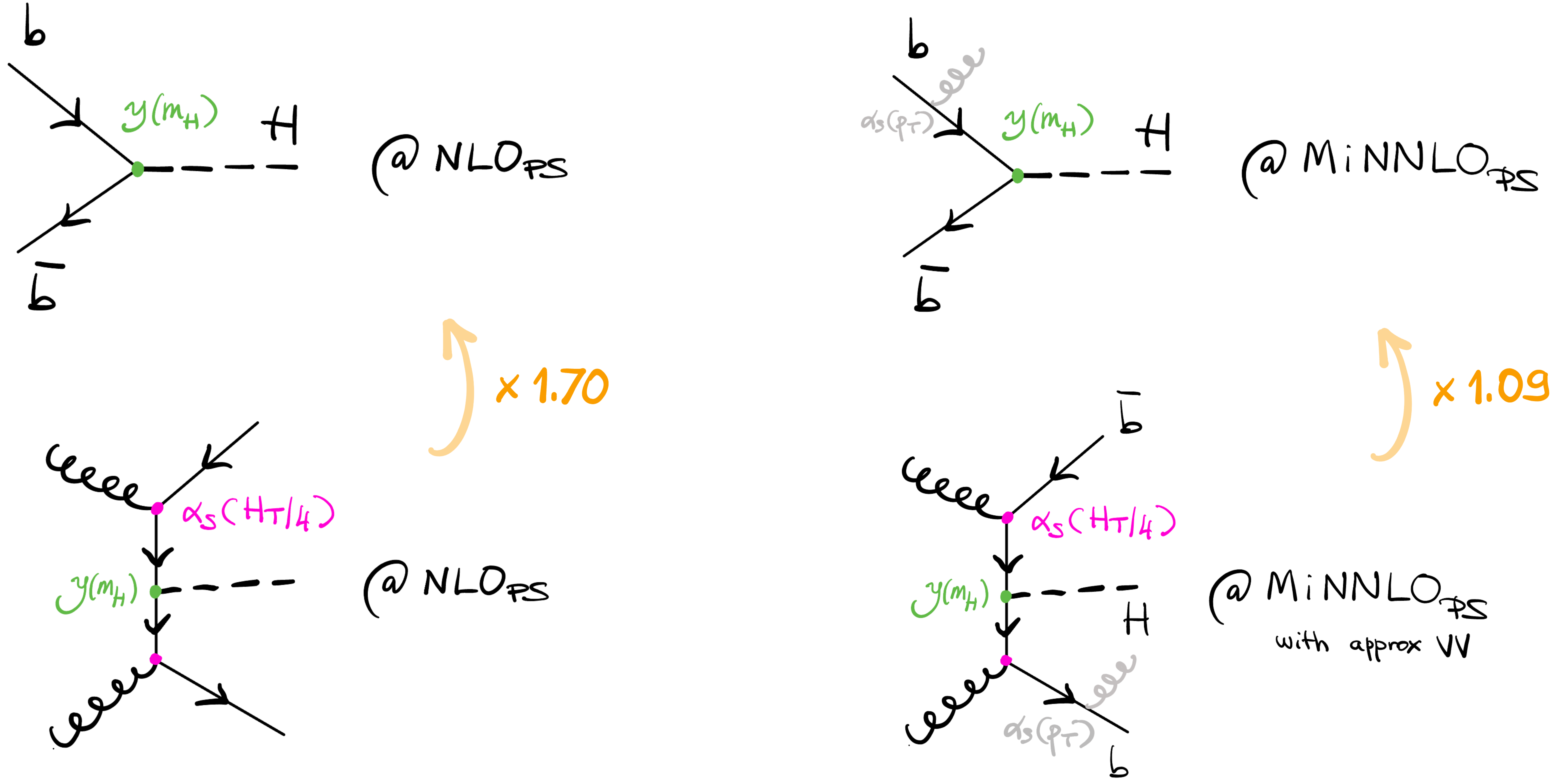




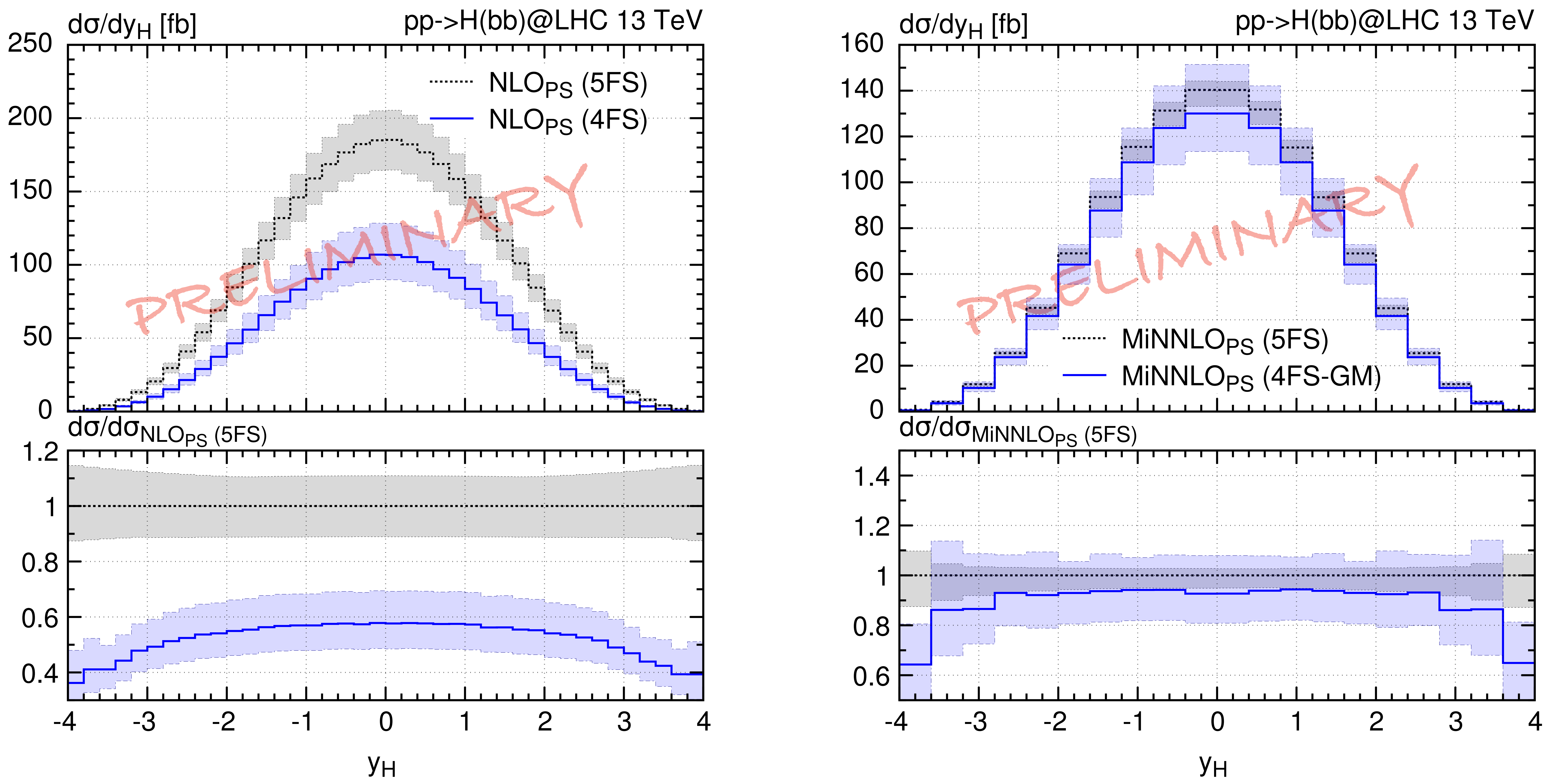
Large differences in the predictions were first observed at leading order: the effect of collinear resummation is extremely large.

Factorisation scales were tuned in order to improve the agreement $\left(\mu_F^{5FS} = \mu_F^{4FS}/4\right)$.

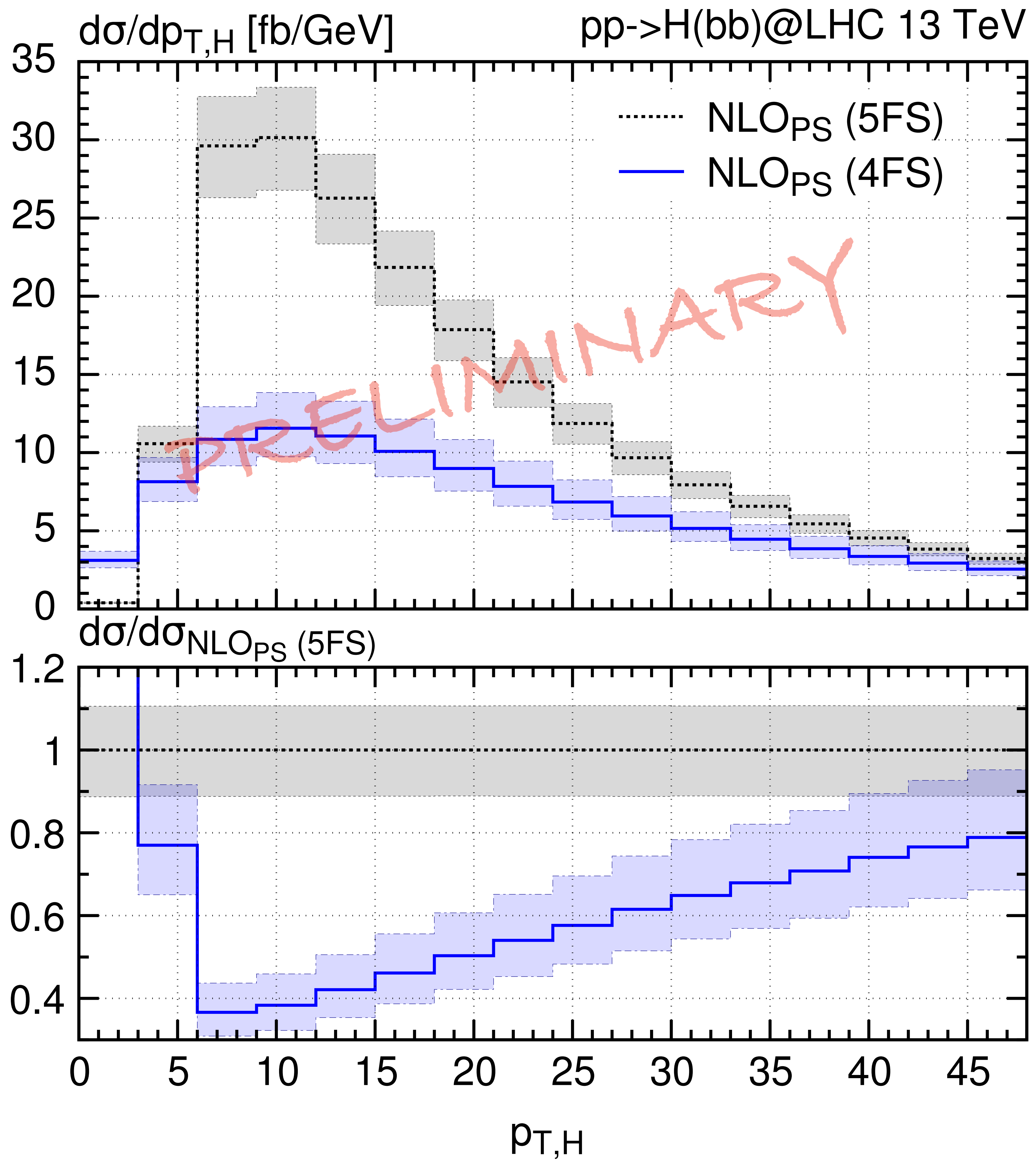
FS comparison: NLO and NNLO

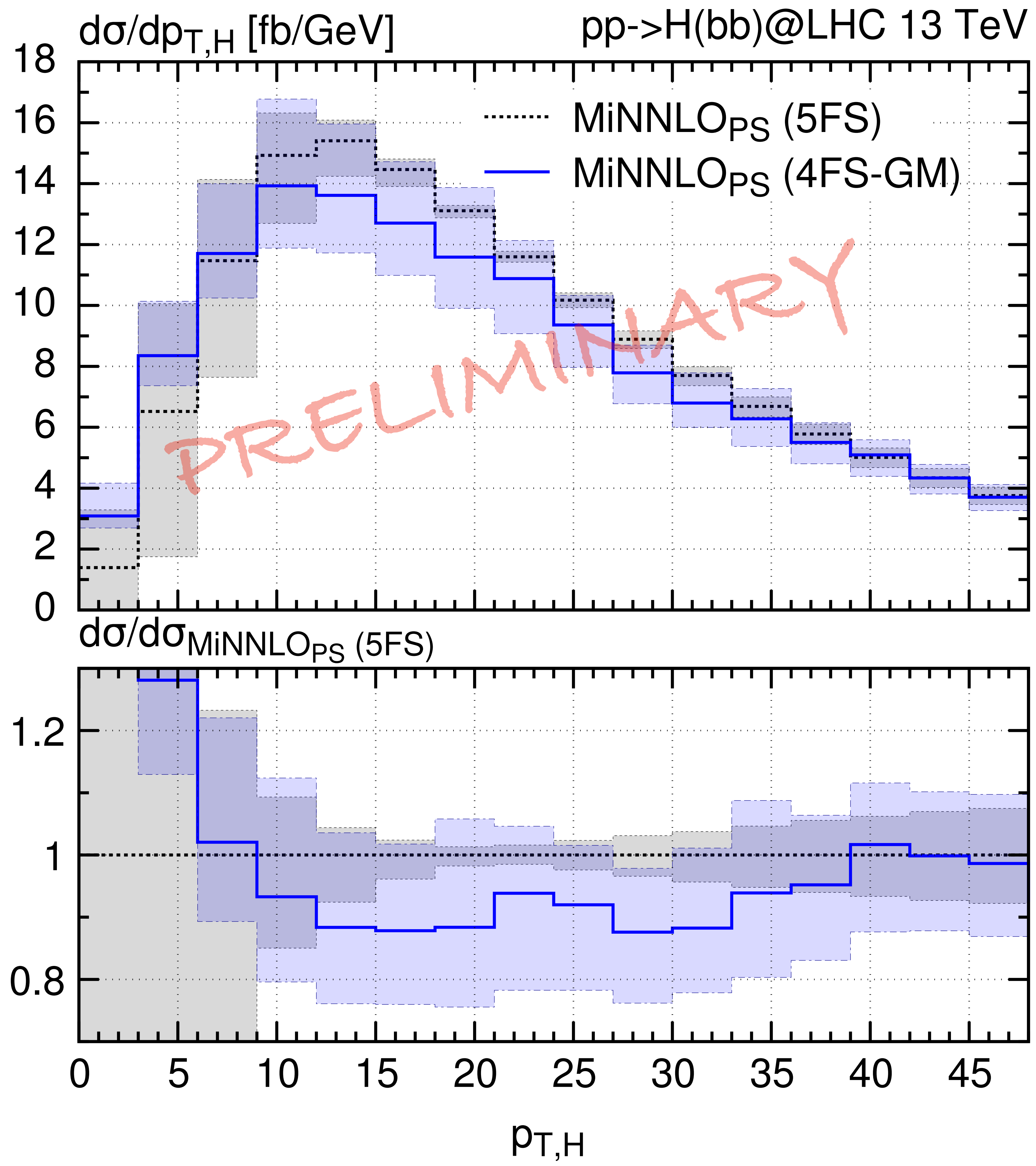


FS comparison: Higgs rapidity



FS comparison: Higgs spectrum





Summary and outlook

- Implementation of the MiNNLOPS method for bbH in 4FS with $\overline{\text{MS}}$ Yukawa
- Approximation of the VV correction using the massification procedure
  - For external bottoms
  - For internal bottom loops

- The theoretical tension between the 4FS and 5FS predictions significantly decreases at NNLO: they agree within the scale uncertainty

- ○ We can perform a b-tagging of the MiNNLOPS events
- ○ A combination of 4FS and 5FS results can improve the description of the process in the whole phase space at differential level

Thank you for the attention!

Backup slides

Cross-section details

K_R	K_F	MiNLO′	MiNNLO$_{PS}$ (Orig. Mass.)	MiNNLO$_{PS}$ (Gen. Mass.)
1	1	0.277(0)	0.460(7)	0.464(9)
1	2	0.268(8)	0.465(2)	0.470(7)
2	1	0.192(5)	0.403(0)	0.408(1)
2	2	0.195(5)	0.407(0)	0.412(1)
1	$\frac{1}{2}$	0.258(9)	0.457(8)	0.466(0)
$\frac{1}{2}$	1	0.382(7)	0.520(7)	0.527(4)
$\frac{1}{2}$	$\frac{1}{2}$	0.375(3)	0.519(3)	0.525(1)
		$0.277(0)^{+34\%}_{-27\%}$ pb	$0.460(7)^{+13\%}_{-13\%}$ pb	$0.464(9)^{+14\%}_{-13\%}$ pb

NLO+PS (5FS)	NLO+PS (4FS)	MiNNLO$_{PS}$ (5FS)	MiNNLO$_{PS}$ (4FS-GM)
$0.677(2)^{+11\%}_{-11\%}$ pb	$0.381(0)^{+20\%}_{-16\%}$ pb	$0.509(8)^{+3.0\%}_{-5.0\%}$ pb	$0.469(2)^{+14\%}_{-13\%}$ pb

Massive-massless mapping

We fix the 4-momenta of the incoming partons and the Higgs state k_5. We want to maintain the invariant mass of the pair

$$m_{QQ} = (k_3 + k_4)^2 = (\tilde{k}_3 + \tilde{k}_4)^2.$$

We introduce the factors

$$\rho_\pm = \frac{1 \pm \rho}{2\rho},\ \rho = \sqrt{1 - \frac{4m_Q^2}{m_{QQ}^2}} \tag{3}$$

and we define the new momenta as a linear combination of the old ones as follows in the quark-channel,

$$\tilde{k}_3^\mu = \rho_+ k_3^\mu - \rho_- k_4^\mu, \tag{4}$$

$$\tilde{k}_4^\mu = \rho_+ k_4^\mu - \rho_- k_3^\mu. \tag{5}$$

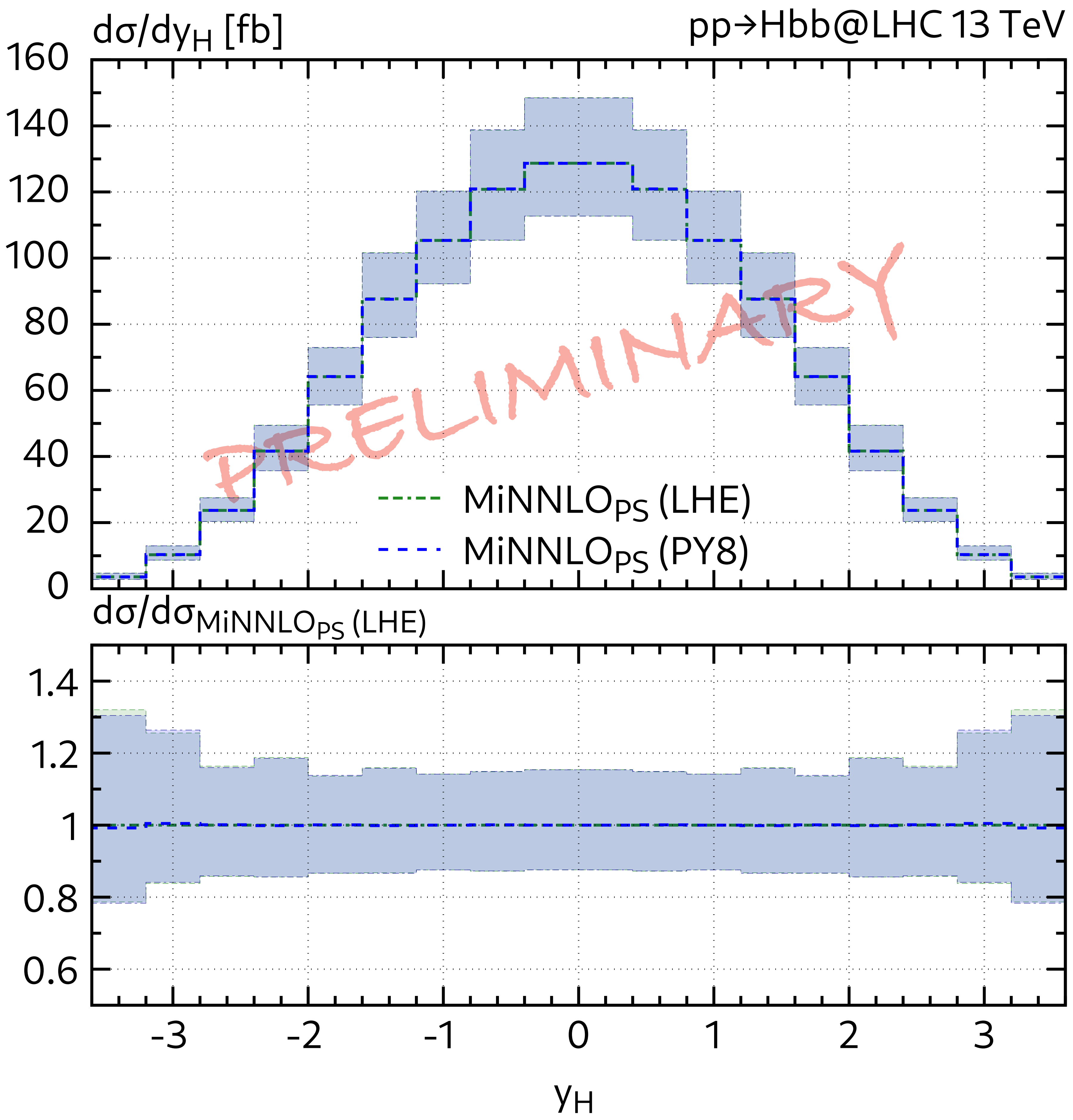
For the gluon channel, we have to avoid the collinear divergence,

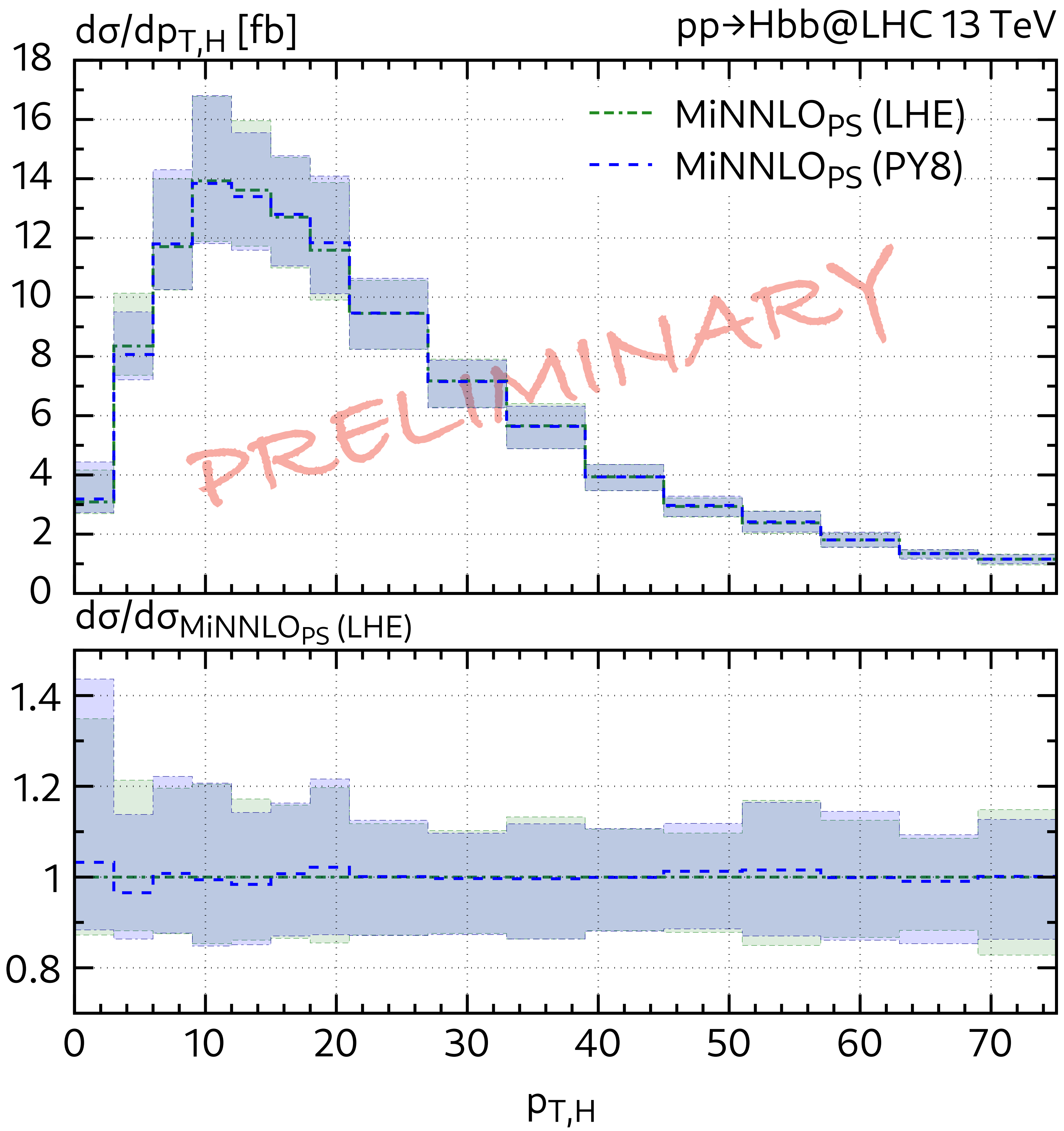
$$\tilde{k}_i^\mu = k_i^\mu + \left(\sqrt{1 - \frac{m_Q^2 n_x^2}{(p_i \cdot n_i)^2}} - 1\right) \frac{p_i \cdot n_i}{n_i}, \quad \text{for i=3,4}, \tag{6}$$

where n_i is the transverse component to both k_1 and k_2. The momentum conservation is restored by performing a Boost such that

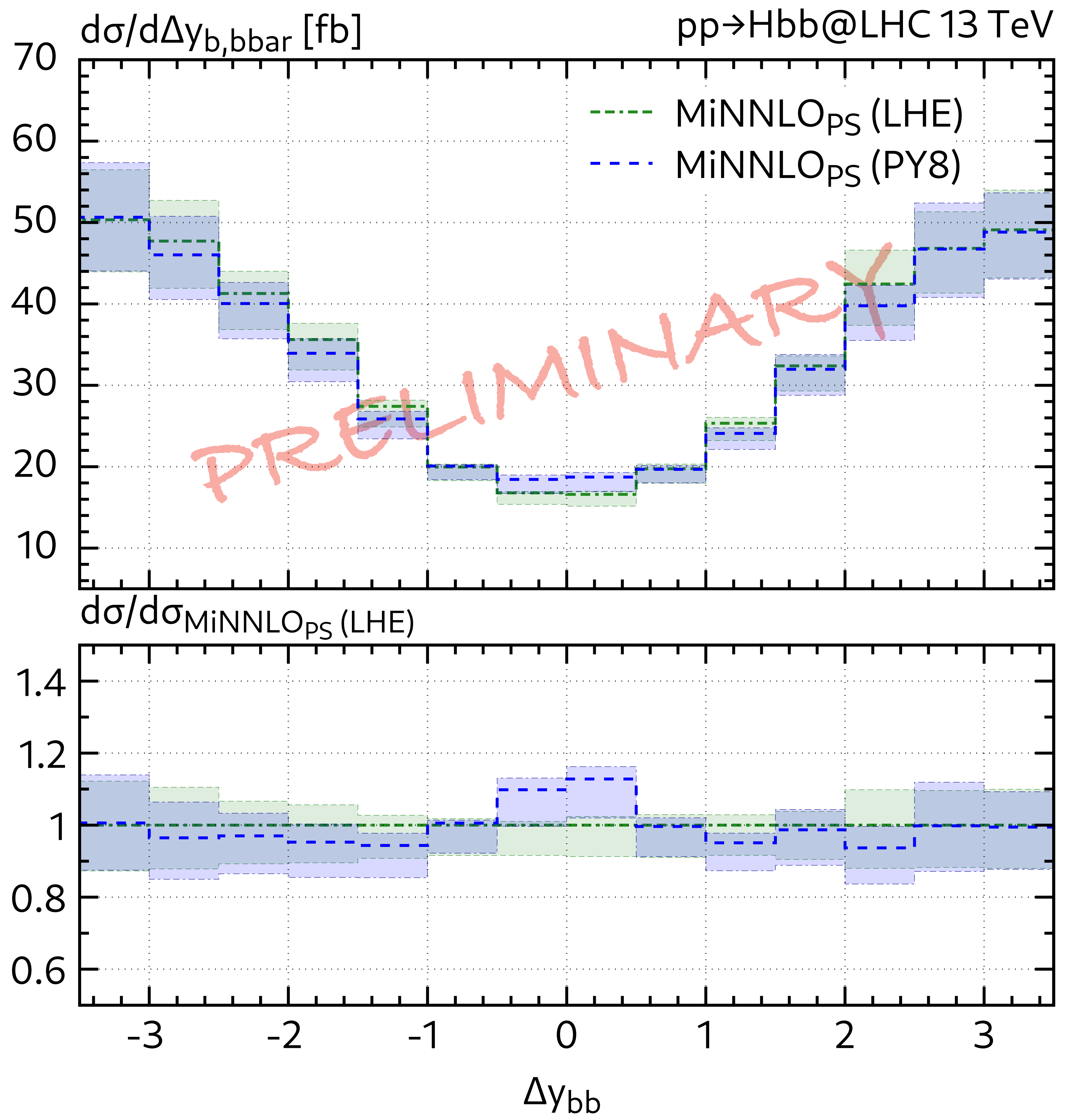
$$\tilde{k}_1 + \tilde{k}_2 = k_1 + k_2 - (k_3 + k_4 - \tilde{k}_3 - \tilde{k}_4). \tag{7}$$

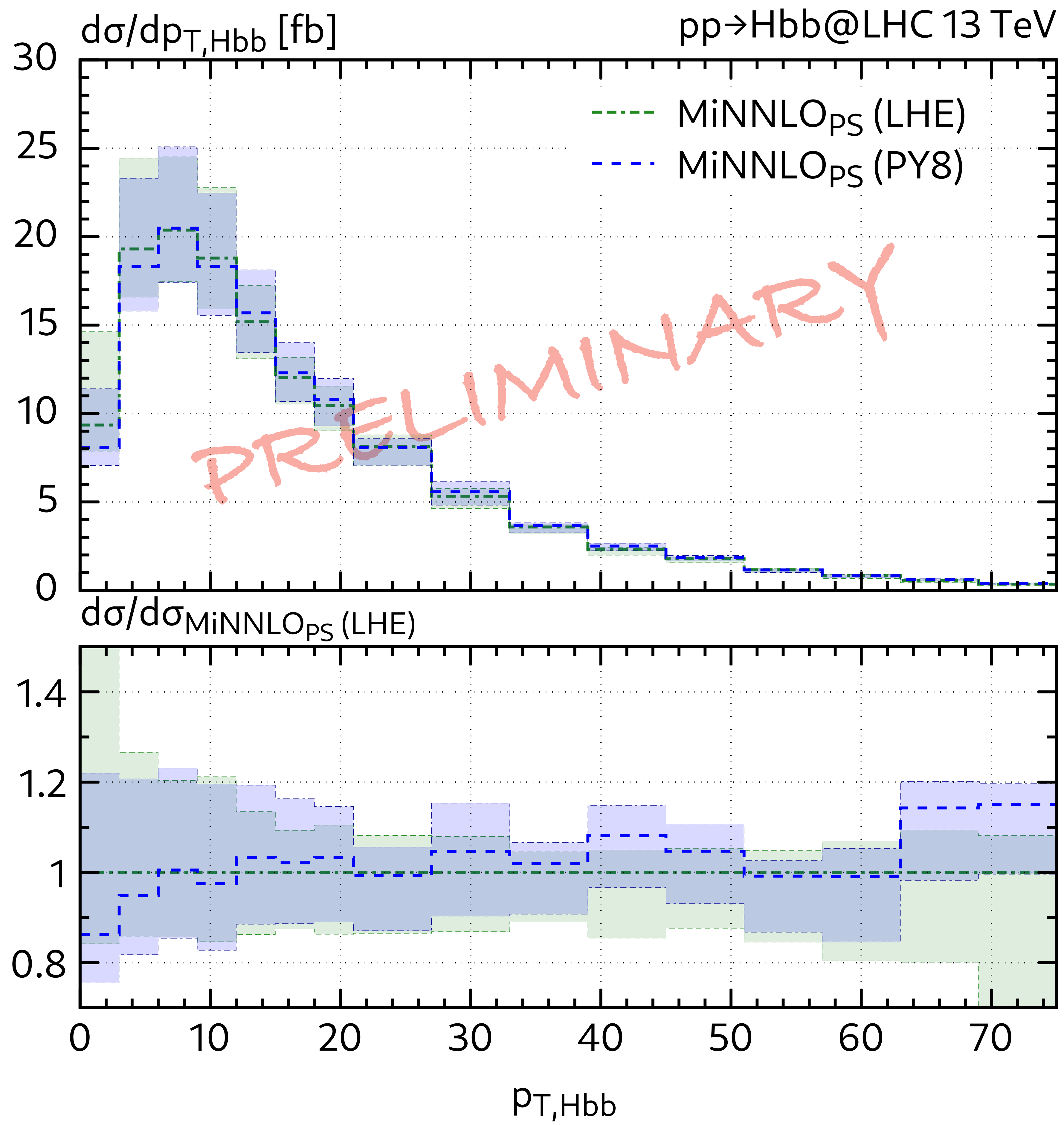
Shower effects in 4FS



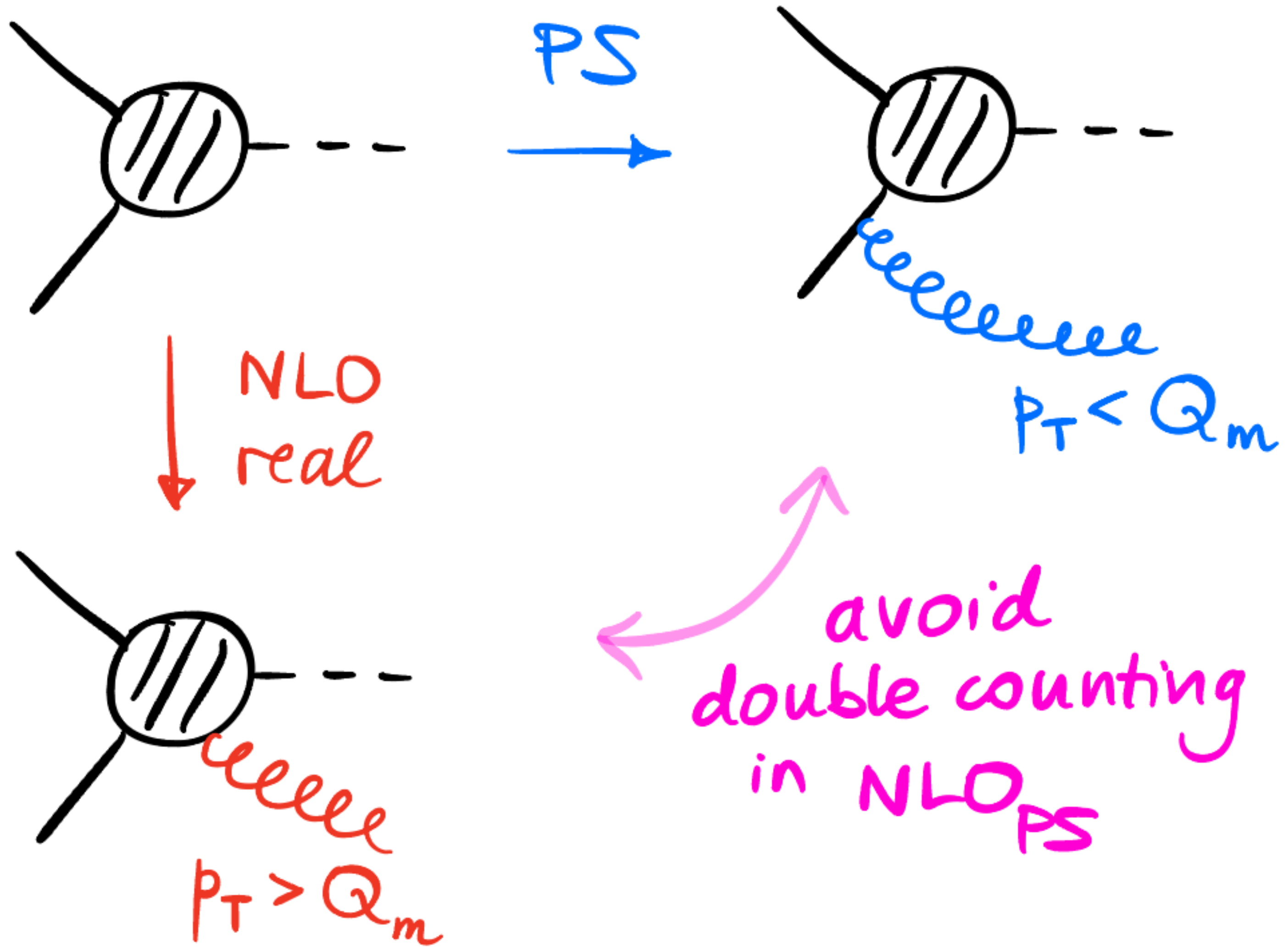


Shower effects in 4FS





Matching



Problem: Match fixed-order predictions with Parton Shower avoiding an unphysical matching scale.

POWHEG idea: implement a Monte Carlo generator that produces just one emission (the hardest one) which alone gives the correct NLO result.

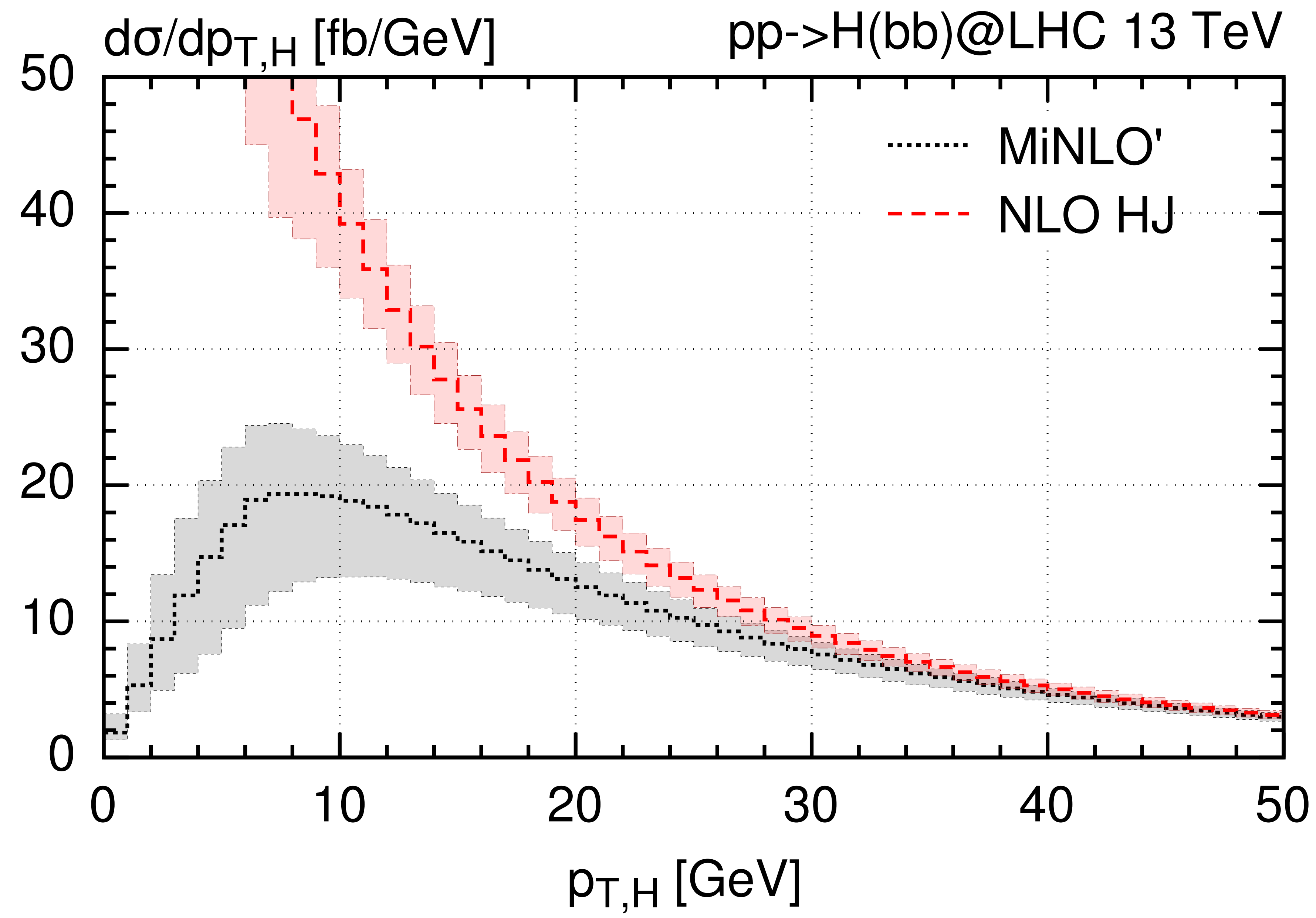
Nason [hep-ph/0409146]

Merging

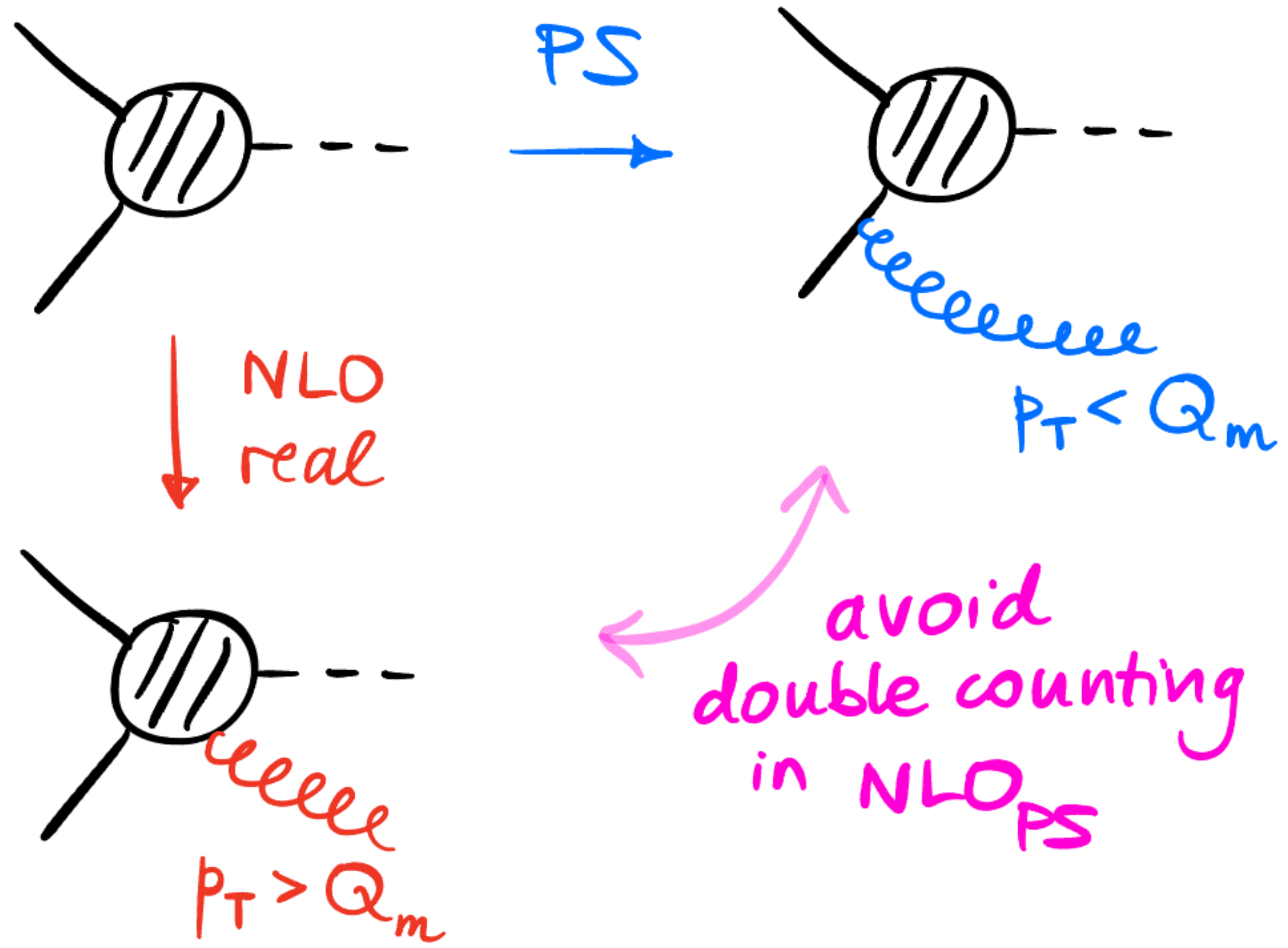
Problem: Merge different multijet calculations without any unphysical merging scale.

MiNLO' idea: Start from a FO X+1jet prediction matched with PS and obtain inclusive predictions through particular scale choices and inclusion of a Sudakov form factor.

Hamilton, Nason, Zanderighi [1206.3572]
Hamilton, Nason, Oleari, Zanderighi [1212.4504]



Matching problem



Double counting can be easily solved by applying a cut in phase space:

- **Reject hard jets** produced by PS with $p_T > Q_m$

But how can we obtain smooth distributions without a critical dependence on the matching scale Q_m?

MC@NLO [Frixione, Webber, 2002] and POWHEG [Nason, 2004] are two fully tested solutions.

POWHEG Idea

Write a simplified Monte Carlo that generates just one emission (the hardest one) which alone gives the correct NLO result.

$$\Delta^{pwg} = \exp\left[-\int \text{exact real-radiation probability above } p_T\right]$$

POWHEG in a nutshell

$$\bar{B} = B + V + \int d\phi_{rad} R$$

The exact NLO prediction is

$$\langle \mathcal{O} \rangle = \int d\Phi_n \, \mathcal{O}(\Phi_n) \bar{B}(\Phi_n) + \int d\Phi_n \, d\phi_{rad} \big(\mathcal{O}(\Phi_n, \phi_{rad}) - \mathcal{O}(\Phi_n) \big) R(\Phi_n, \phi_{rad})$$

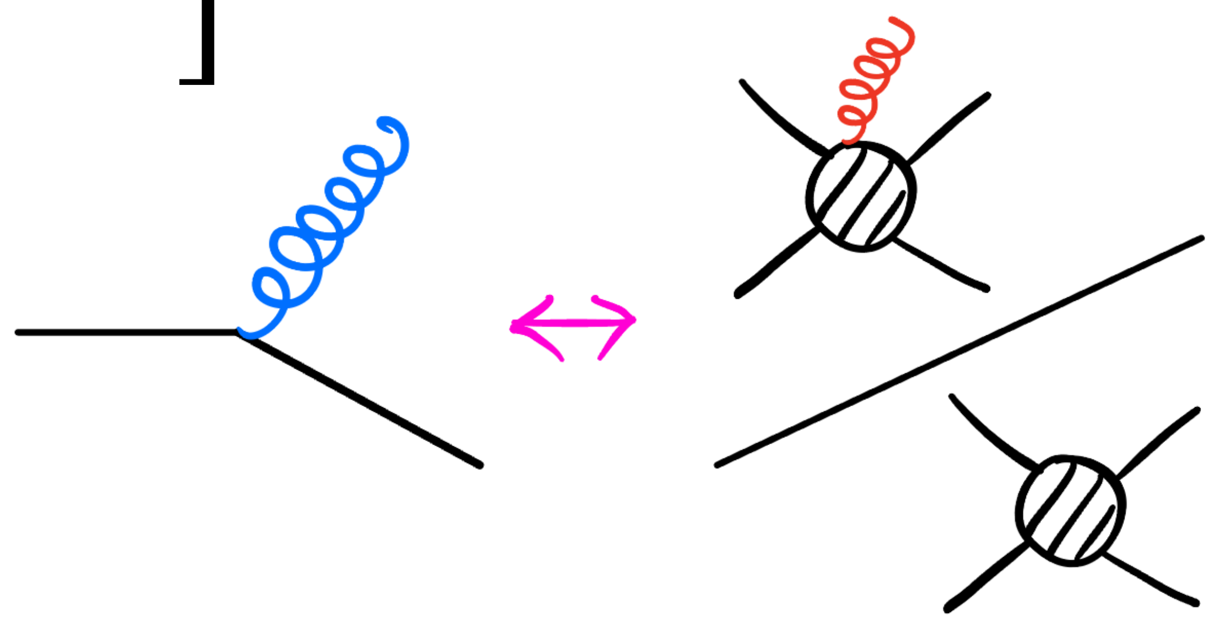
Comparing with the SMC

$$\langle \mathcal{O} \rangle_{SMC} \simeq \int d\Phi_n \left[\mathcal{O}(\Phi_n) B(\Phi_n) + B(\Phi_n) \int_{t_0} \frac{dt}{t} dz d\varphi \left(\mathcal{O}(\Phi_n, \phi_r) - \mathcal{O}(\Phi_n) \right) \frac{\alpha_s}{2\pi} P(z) \right],$$

we deduce the Sudakov form factor and the shower formula in POWHEG

$$\langle \mathcal{O} \rangle = \int d\Phi_n \bar{B}(\Phi_n) \left[\mathcal{O}(\Phi_n) \, \Delta_{t_0}^{pwg} + \int d\phi_{rad} \, \mathcal{O}(\Phi_n, \phi_{rad}) \, \Delta_t^{pwg} \frac{R(\Phi_n, \phi_{rad})}{B(\Phi_n)}) \right]$$

with $\Delta_t^{pwg} = \exp \left[- \int d\phi'_{rad} \frac{R(\Phi_n, \phi'_{rad})}{B(\Phi_n)} \Theta(t' - t) \right]$



MiNNLOPS in a nutshell

NLO Xj ⟶ NNLO X

MiNNLOPS is an extension of MiNLO' to achieve NNLO+PS accuracy for inclusive observables.

Monni, Nason, Re, Wiesemann, Zanderighi [1908.06987]

The modified POWHEG function is

$$\bar{B}(\Phi_{XJ}) = e^{-\tilde{S}(p_T)} \left\{ B\left(1 - \alpha_s(p_T)\,\tilde{S}^{(1)}\right) + V + \int \mathrm{d}\phi_{rad}\, R + \left[D^{(3)}(p_T)\right] \times F^{corr} \right\}$$

Sudakov form factor

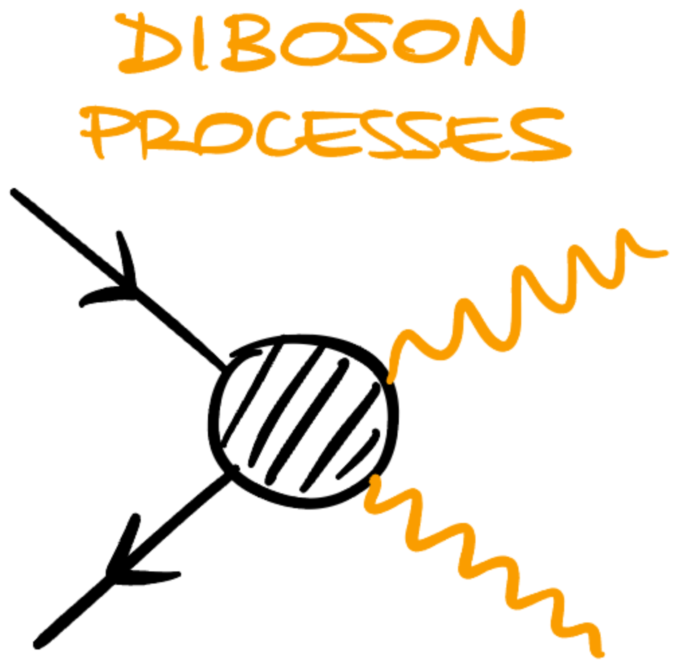
MiNLO' structure

Extra term:
it ensures NNLO accuracy.

F^{corr} encodes the spreading upon the full Φ_{XJ}.

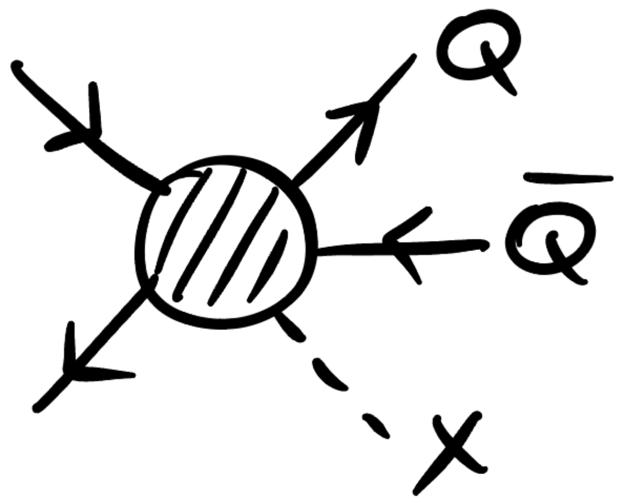
The QCD scales must be $\mu_F \sim \mu_R \sim p_T$ in the singular region.

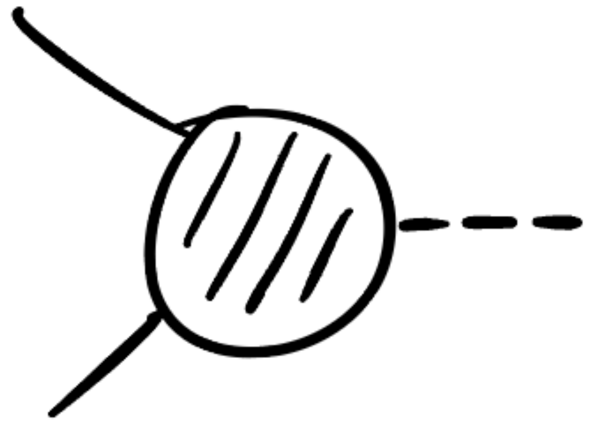
Phenomenology with MiNNLOPS



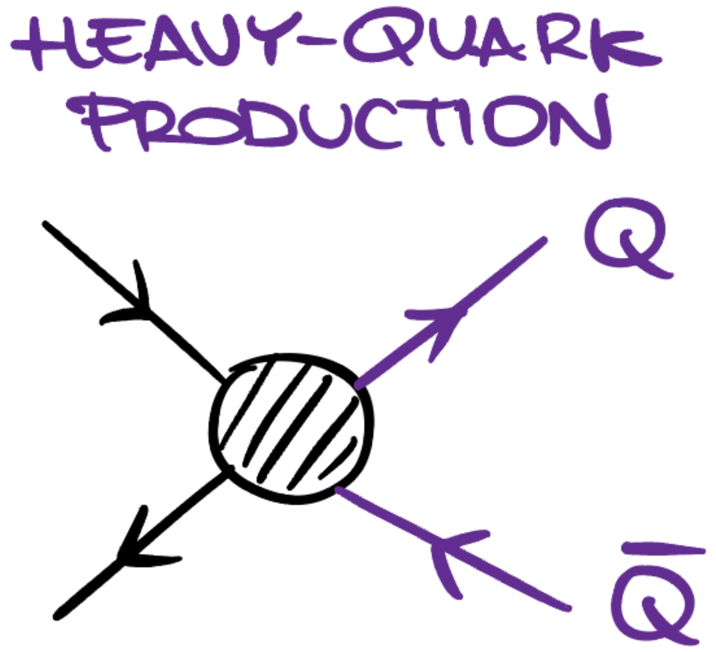
$Z\gamma$ [2010.10478, 2108.11315]
WW [2103.12077]
ZZ [2108.05337]
$WH/ZH(H \to b\bar{b})$ [2112.04168]
$\gamma\gamma$ [2204.12602]
WZ [2208.12660]
SMEFT studies [2204.00663, 2311.06107]

$b\bar{b}H$ **4FS**





$gg \to H, W/Z$ [1908.06987, 2006.04133, 2402.00596]
5FS $b\bar{b} \to H$ [2402.04025]

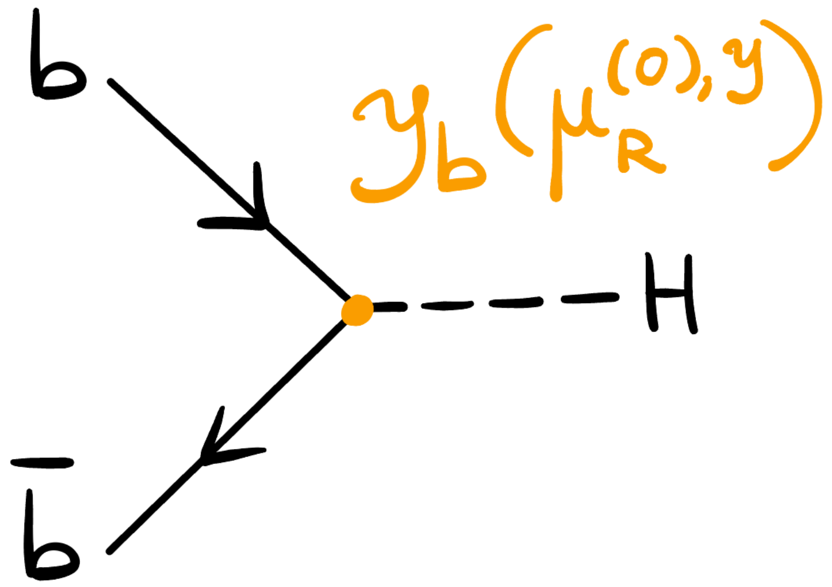


$t\bar{t}$ [2012.14267,2112.12135]
$b\bar{b}$ [2302.01645]

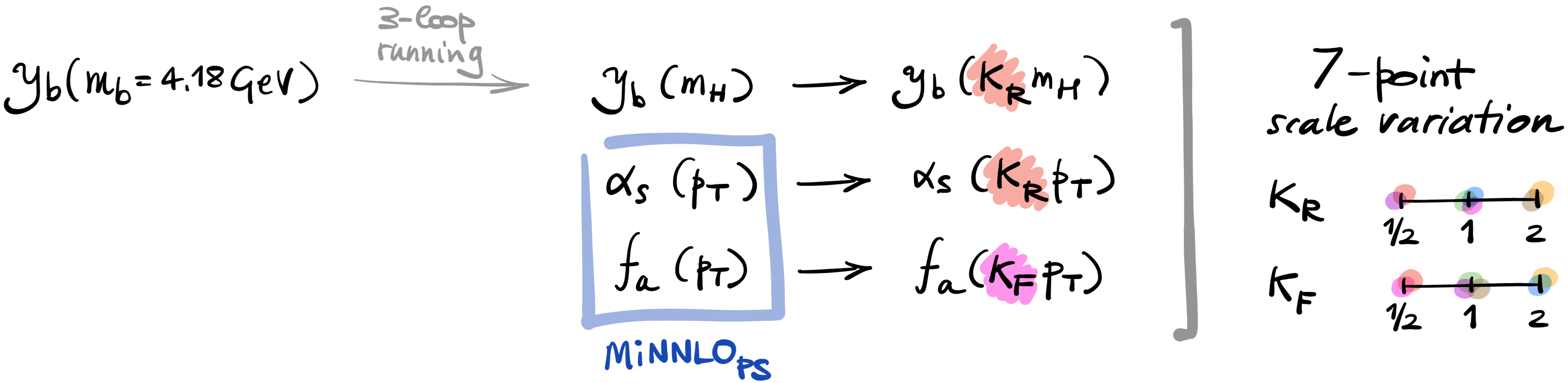
MiNNLOPS for Yukawa induced processes

The Yukawa coupling is renormalised in $\overline{\text{MS}}$ scheme.

The running of this Born coupling requires some adaptations of the MiNNLOPS method to take account the extra scale dependence.

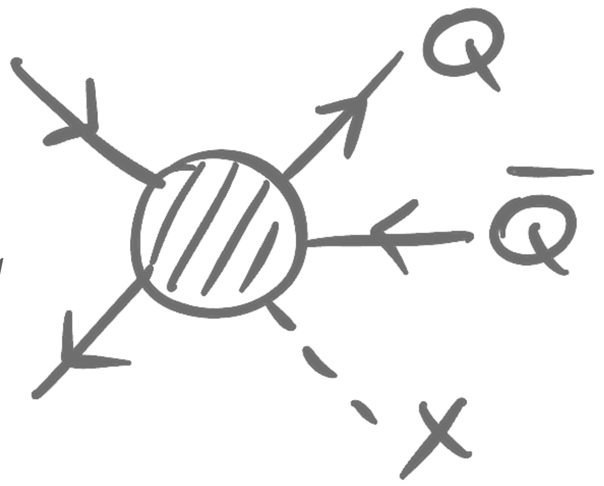


$$H^{(1,2)} \to H^{(1,2)}\left(\log \frac{\mu_R^{(0),y}}{m_H}\right)$$



MiNNLOPS in 4FS

- Start from the POWHEG $Hb\bar{b}j$ generator
- Produce the NNLO+PS predictions using the framework of MiNNLO$_{PS}$



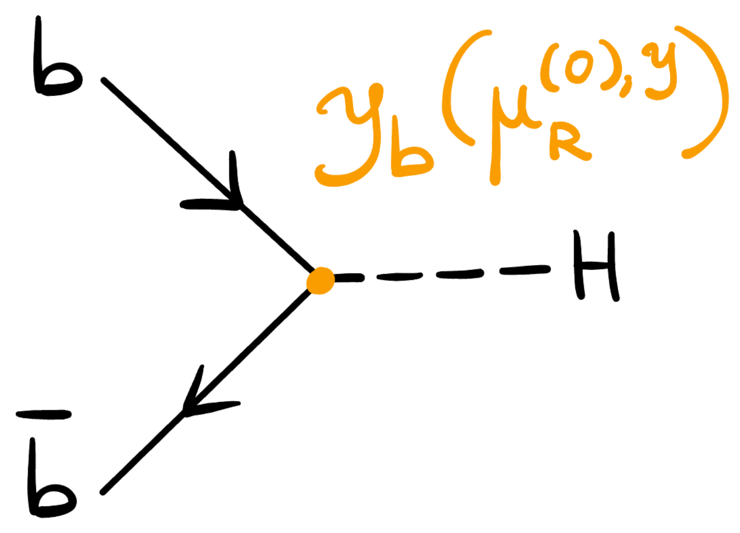
Mazzitelli, Wiesemann

The **double virtual** correction for a massive bottom pair and Higgs production is not known: approximate it with the **massification procedure**

$$\mathscr{A}^{(2)} = \mathscr{F}^{(2)}\mathscr{A}^{(0)}_{m_b=0} + \mathscr{F}^{(1)}\mathscr{A}^{(1)}_{m_b=0} + \mathscr{F}^{(0)}\mathscr{A}^{(2)}_{m_b=0} + \mathcal{O}\left(\frac{m_b}{Q}\right)$$

Mitov, Moch [0612149]

Badger, Hartanto, Kryś, Zoia [2107.14733]

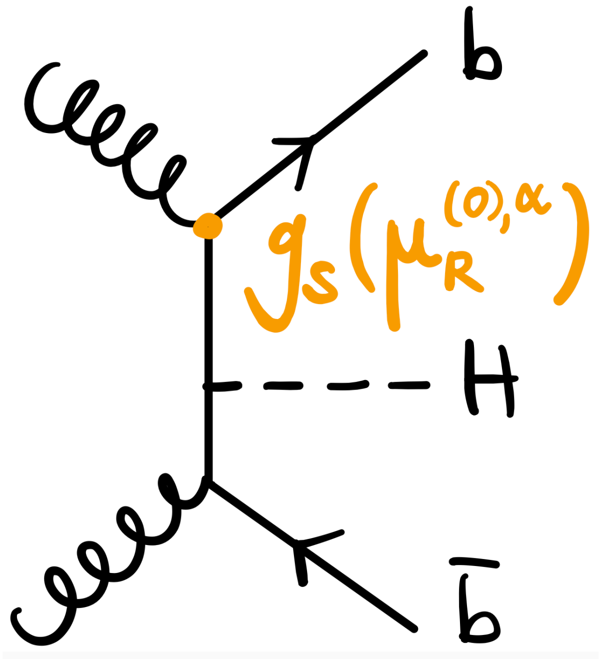


$(\mu_R^{(0),\alpha}, \mu_R^{(0),y})$	NLOPS (5FS)	NLOPS (4FS)	MiNNLOPS (5FS)	MiNNLOPS (4FS, $\mathscr{F}^{(0)}=0$)
$(\frac{1}{4}H_T, m_H)$	$0.646(0)^{+10.4\%}_{-10.9\%}$ pb	$0.381(2)^{+20.2\%}_{-15.9\%}$ pb	$0.509(8)^{+2.9\%}_{-5.3\%}$ pb	$0.434(1)^{+6.4\%}_{-10.0\%}$ pb

$$H_T = \sum_{b,\bar{b},H} \sqrt{m_i^2 + p_{T,i}^2}$$

1.70x

1.17x



MiNNLOPS in a nutshell

NLO Xj → NNLO X

MiNNLOPS is an extension of MiNLO' to achieve NNLO+PS accuracy for inclusive observables.

Monni, Nason, Re, Wiesemann, Zanderighi [1206.3572]

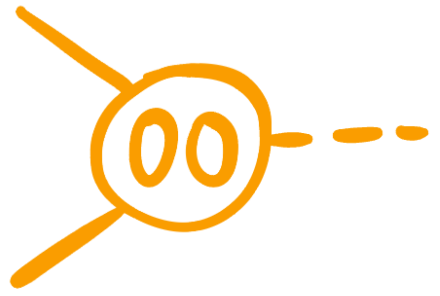
Split the differential inclusive cross-section into the singular and regular part in the small transverse momentum limit: $\mathrm{d}\sigma = \mathrm{d}\sigma^{sing} + \mathrm{d}\sigma^{reg}$.

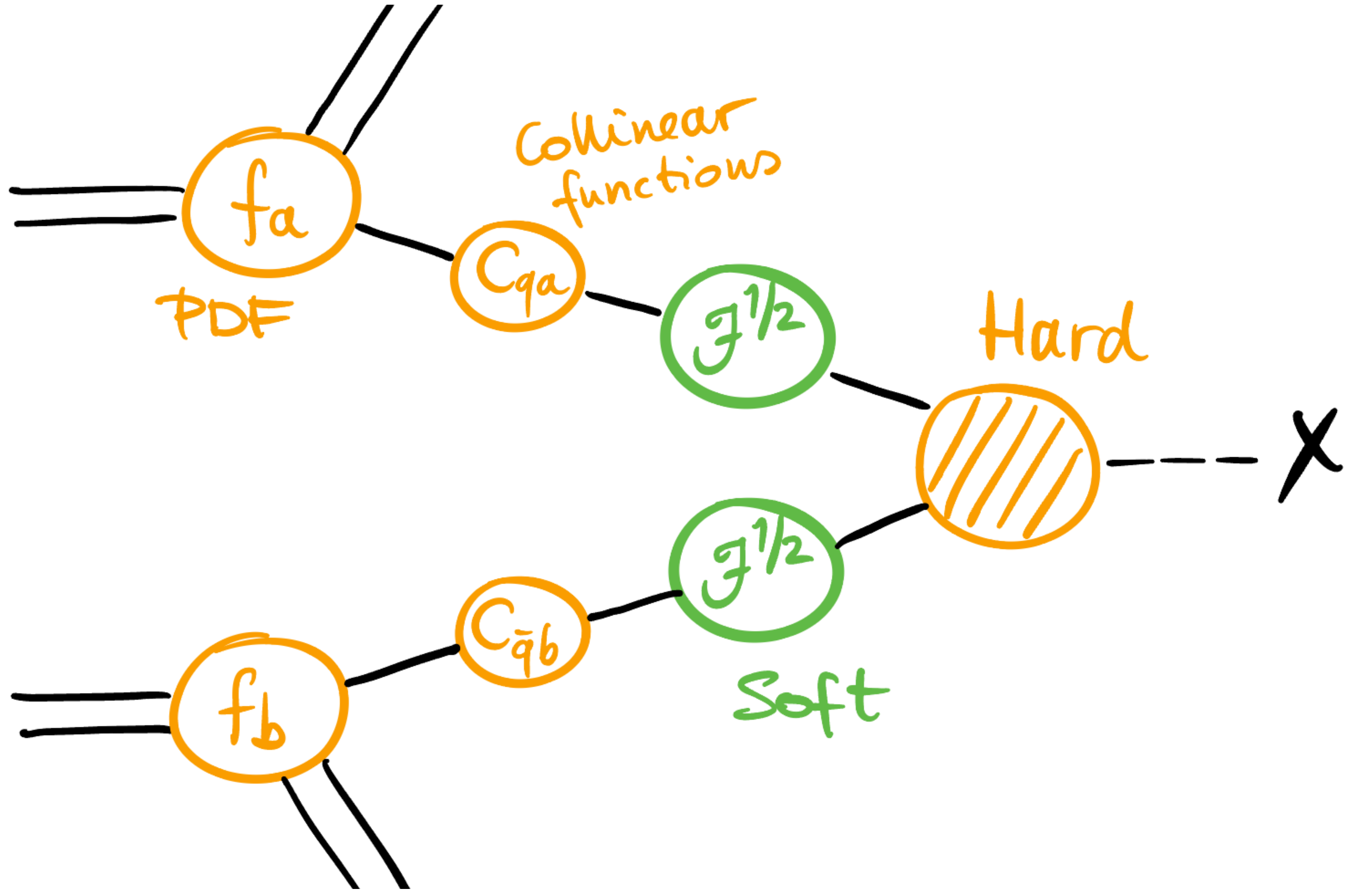
$$\frac{\mathrm{d}\sigma^{sing}}{\mathrm{d}p_T\,\mathrm{d}\Phi_X} = \frac{\mathrm{d}}{\mathrm{d}p_T}\left\{\mathscr{F}(p_T)\,\mathscr{L}(p_T)\right\} =: \exp\left[-\tilde{S}(p_T)\right] D(p_T)$$

Sudakov form factor

$$\mathscr{F}(p_T) = \exp\left[-\tilde{S}(p_T)\right]$$

Luminosity: it also contains





MiNNLOPS in a nutshell

$$\mathrm{d}\sigma = \mathrm{d}\sigma^{sing} + \mathrm{d}\sigma^{reg}$$

The modified POWHEG function is

$$\bar{B}(\Phi_{XJ}) = e^{-\tilde{S}(p_T)} \left\{ B\left(1 - \alpha_s(p_T)\,\tilde{S}^{(1)}\right) + V + \int \mathrm{d}\phi_{rad}\, R + \left[D(p_T) - D^{(1)} - D^{(2)}\right] \times F^{corr} \right\}$$

MiNLO' structure

Extra term: it ensures NNLO accuracy.

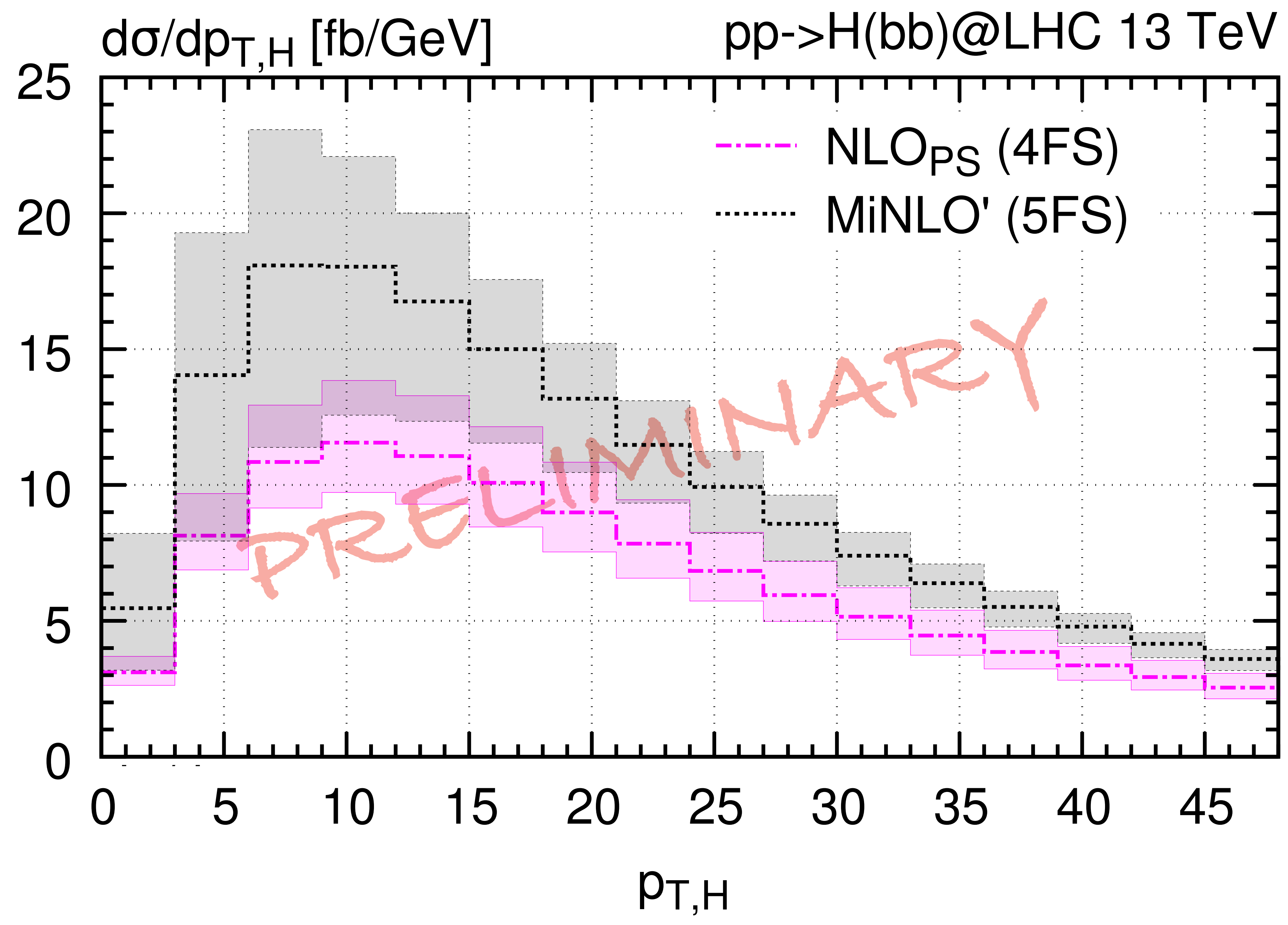
F^{corr} encodes the spreading of the D-terms upon the full Φ_{XJ}.

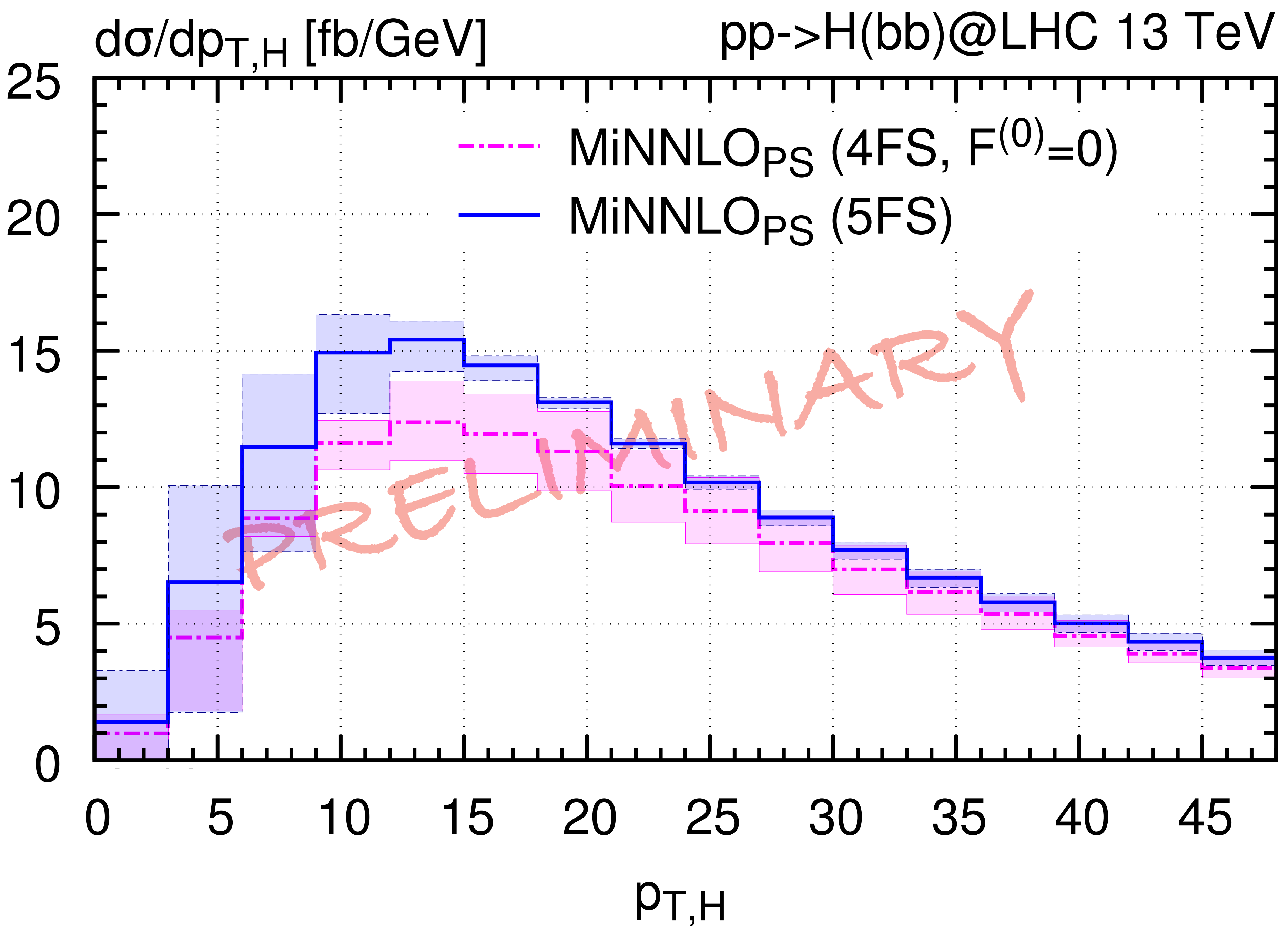
- In the singular part, the QCD scales must be $\mu_F \sim \mu_R \sim p_T$.
- For the regular part, different scale choices can be performed:
  - the transverse momentum p_T (original choice)
  - the hard scale Q (`FOatQ=1`)

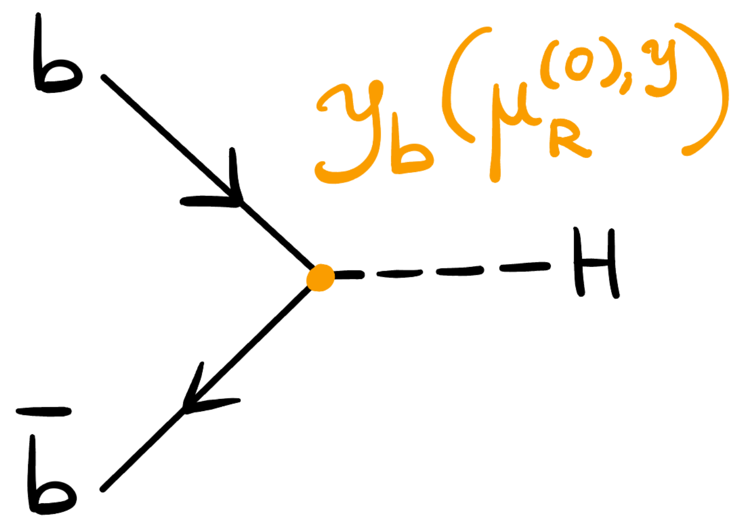
Gavardi, Oleari, Re [2204.12602]

Before the two-loop…

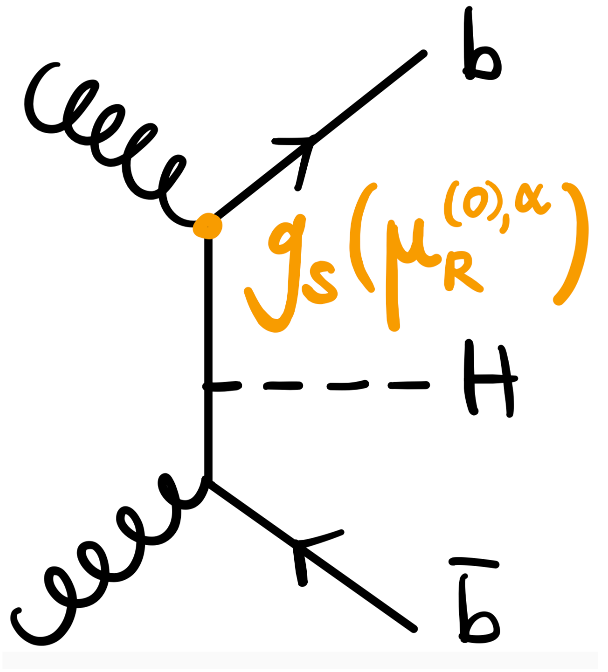
NNPDF40_nnlo_as_01180
with different active flavours



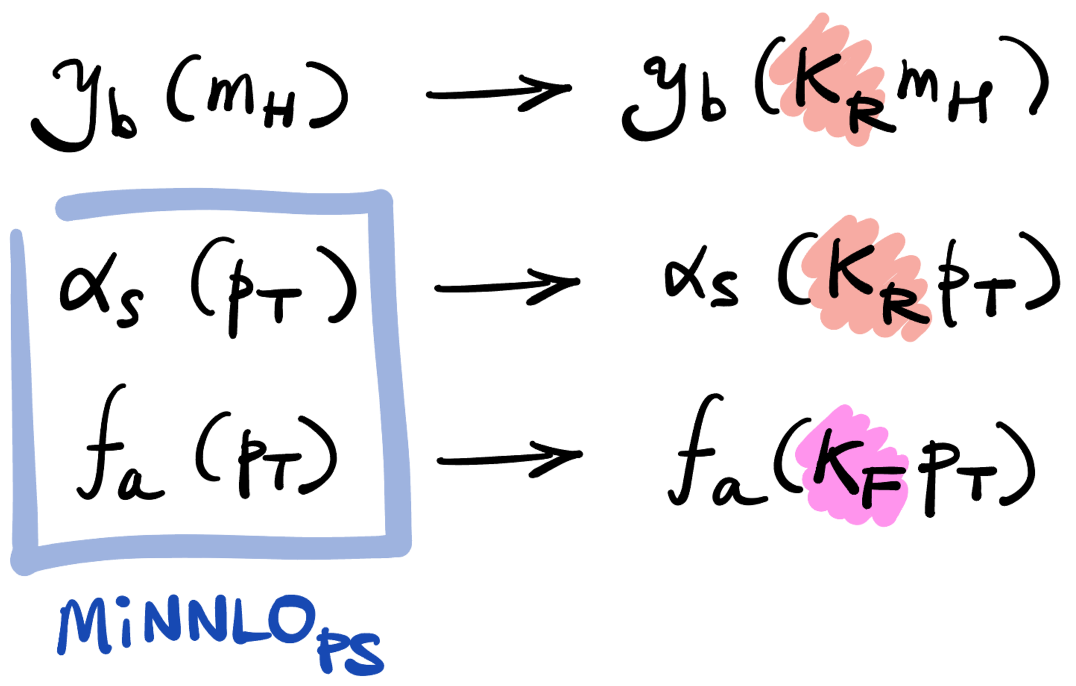




$(\mu_R^{(0),\alpha}, \mu_R^{(0),y})$	NLO$_{PS}$ (5FS)	NLO$_{PS}$ (4FS)	MiNNLO$_{PS}$ (5FS)	MiNNLO$_{PS}$ (4FS, $\mathscr{F}^{(0)} = 0$)
$(\frac{1}{4}H_T, m_H)$	$0.646(0)^{+10.4\%}_{-10.9\%}$ pb	$0.381(2)^{+20.2\%}_{-15.9\%}$ pb	$0.509(8)^{+2.9\%}_{-5.3\%}$ pb	$0.434(1)^{+6.4\%}_{-10.0\%}$ pb



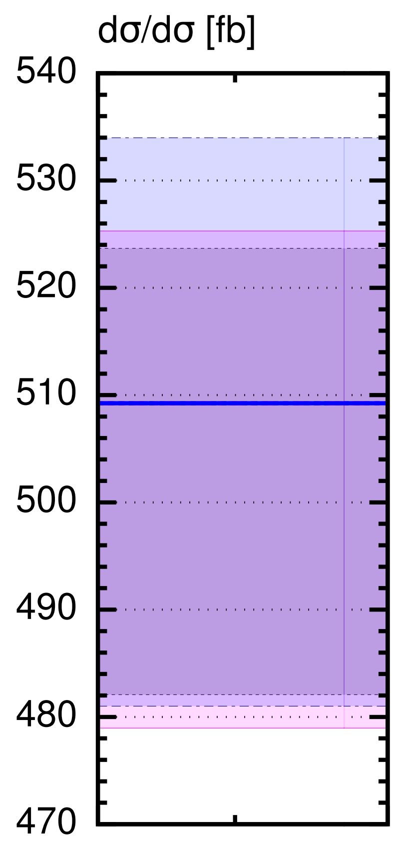
5FS scale variation

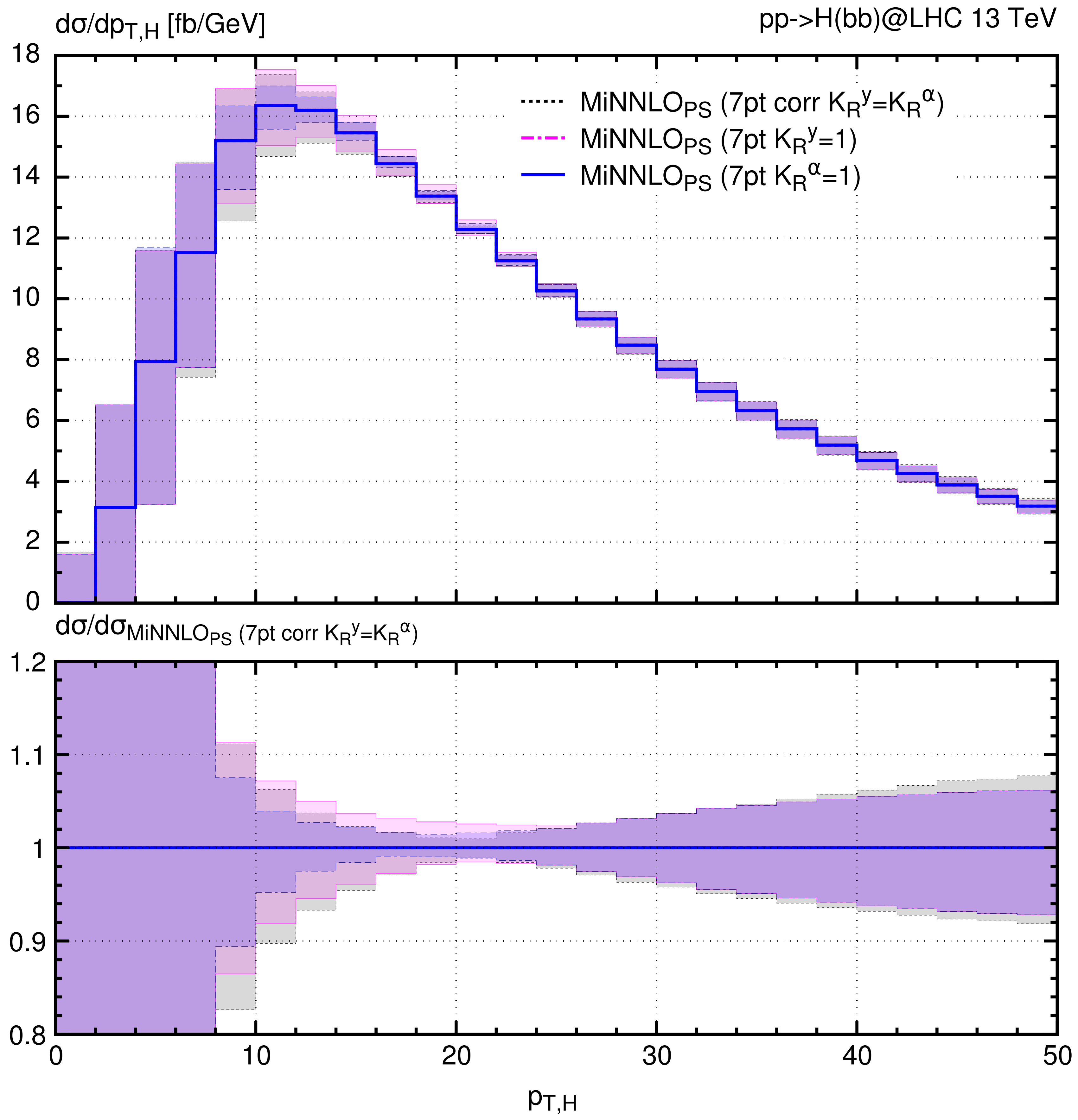


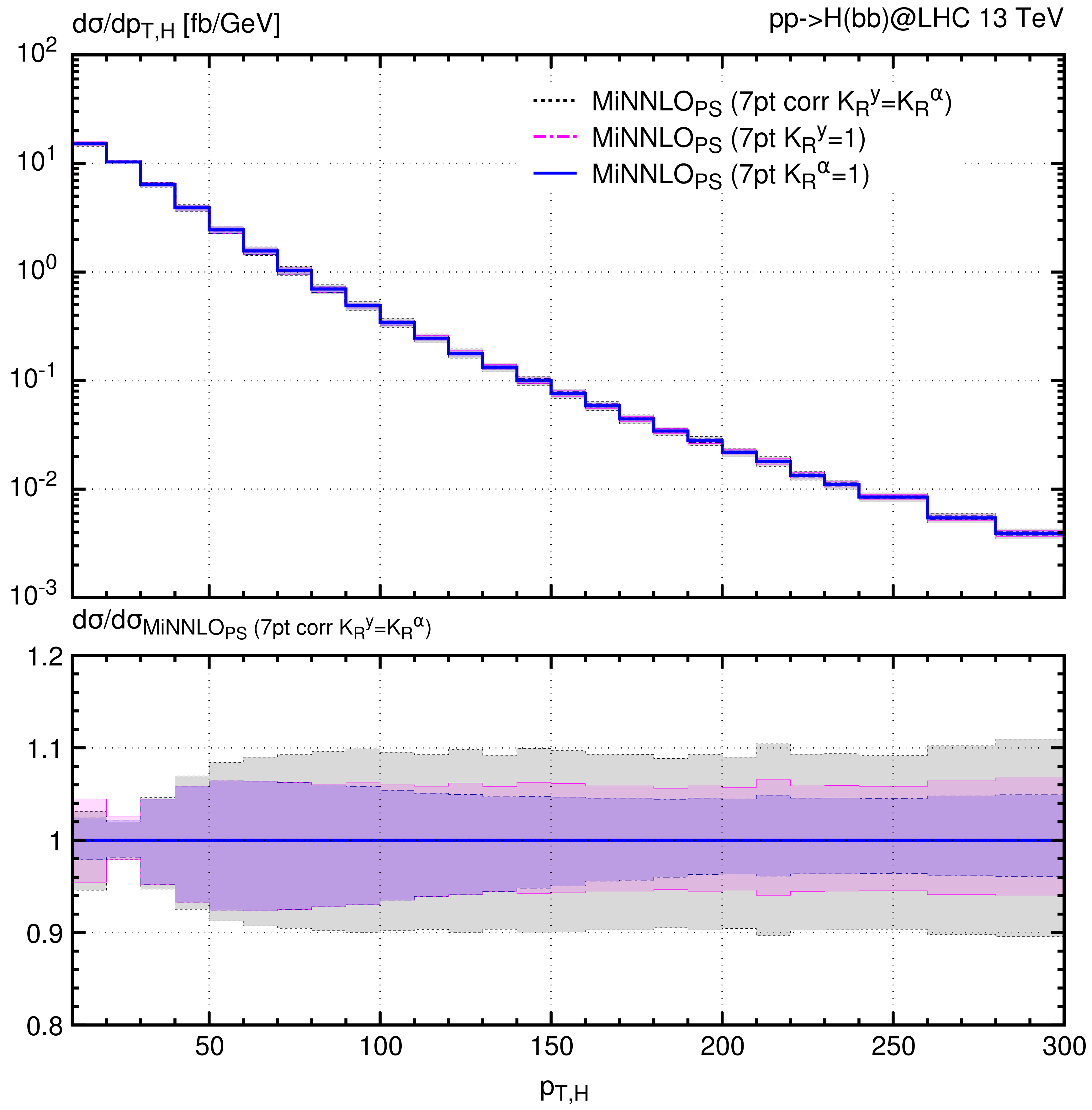
We studied the effects of the correlation between the renormalisation scale factors.

We compare:

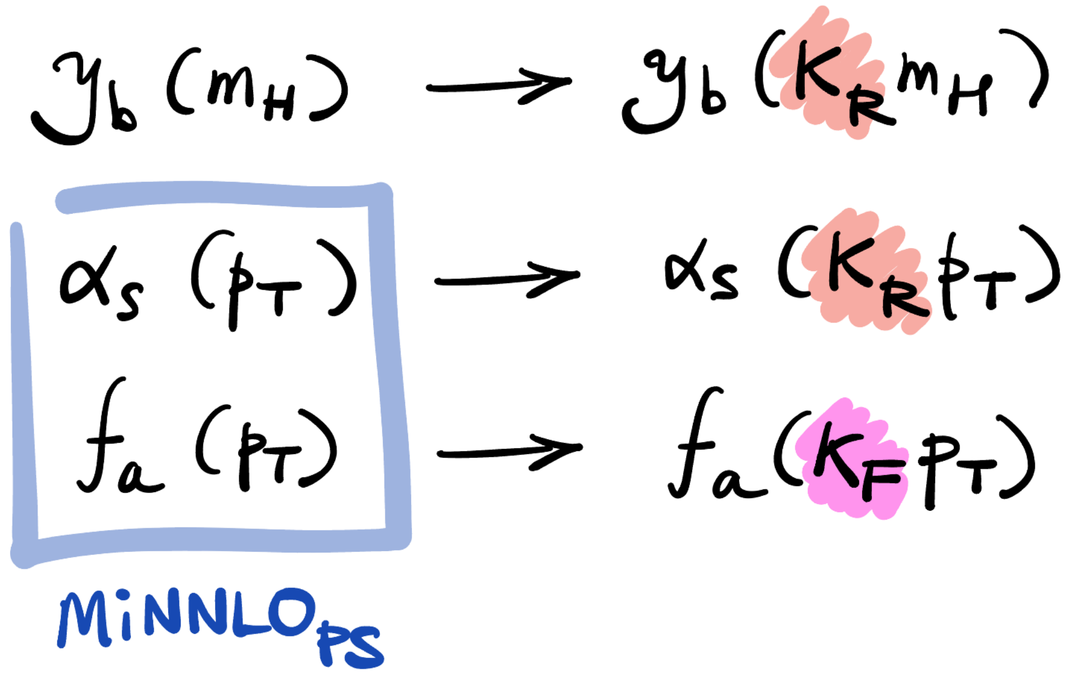
- The standard prediction
- 7pt s.v. for (K_R^α, K_F)
- 7pt s.v. for (K_R^y, K_F)







5FS scale variation



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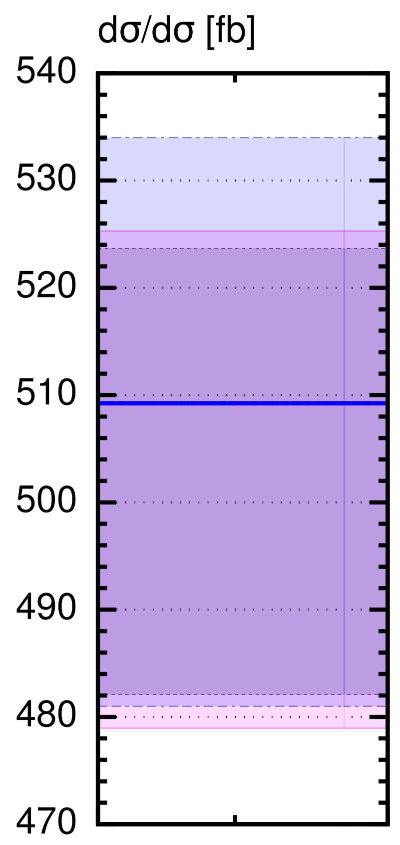
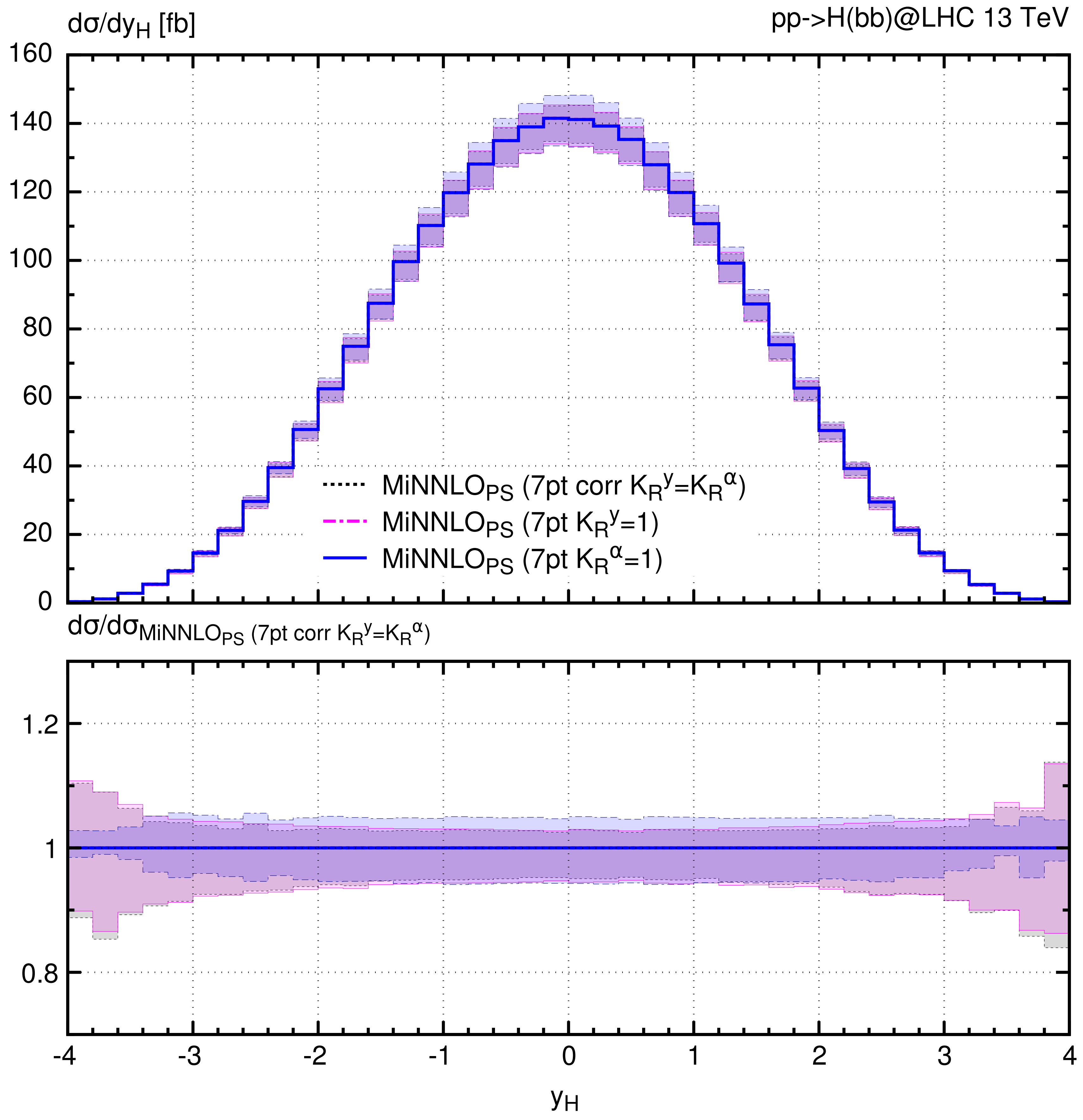
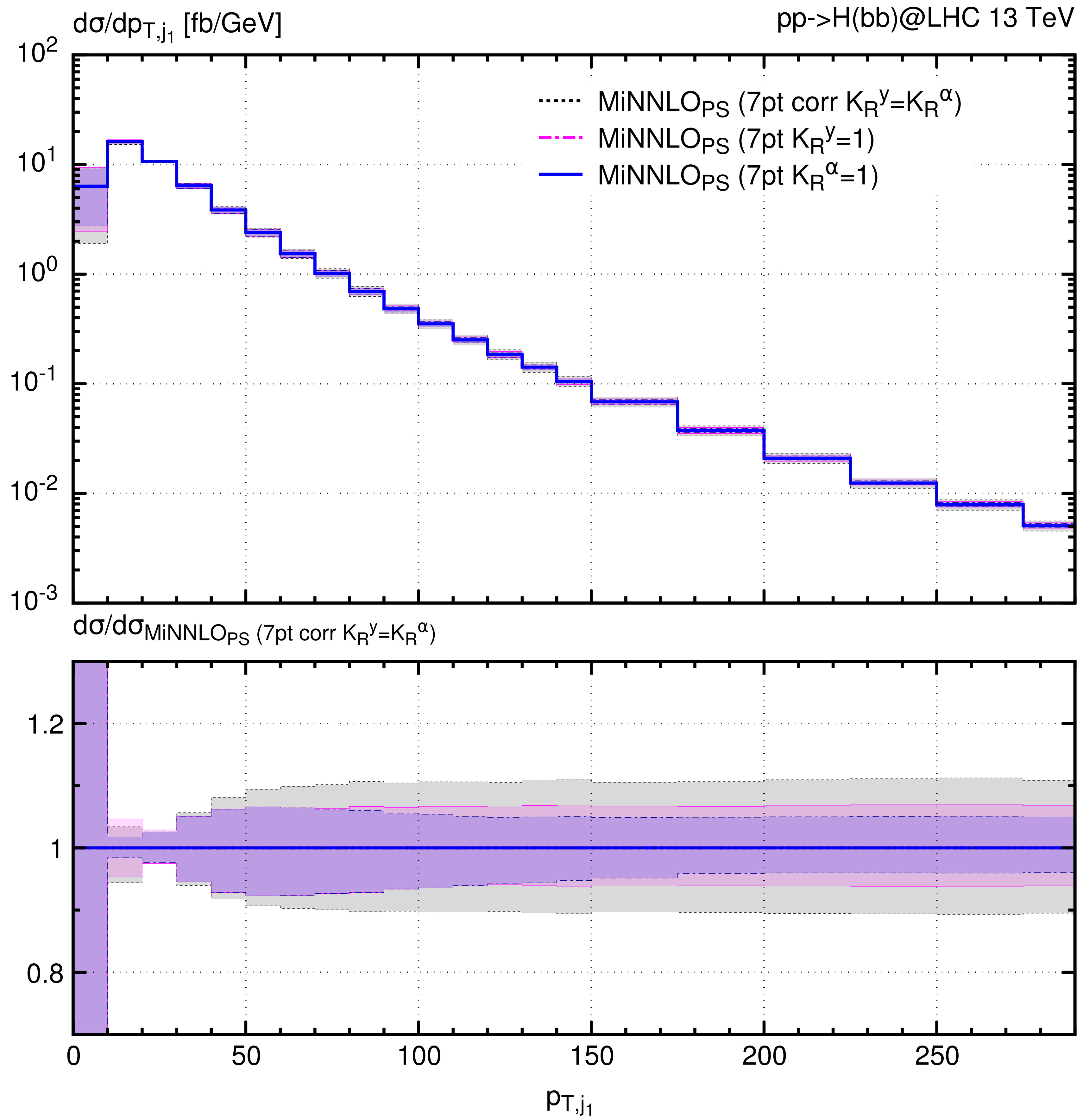
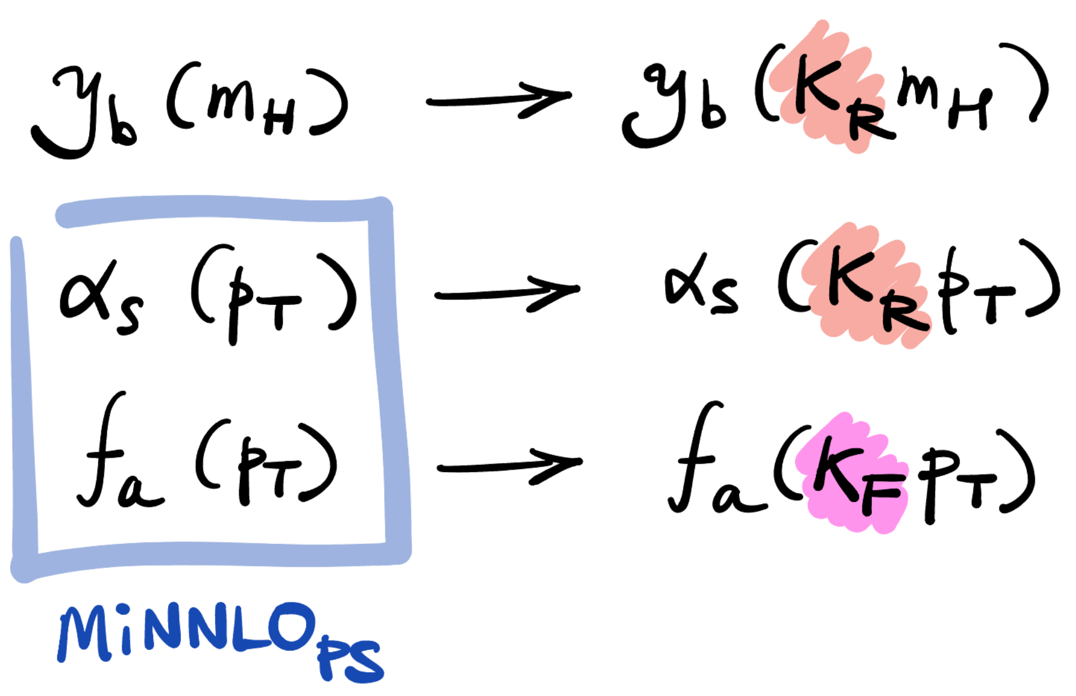




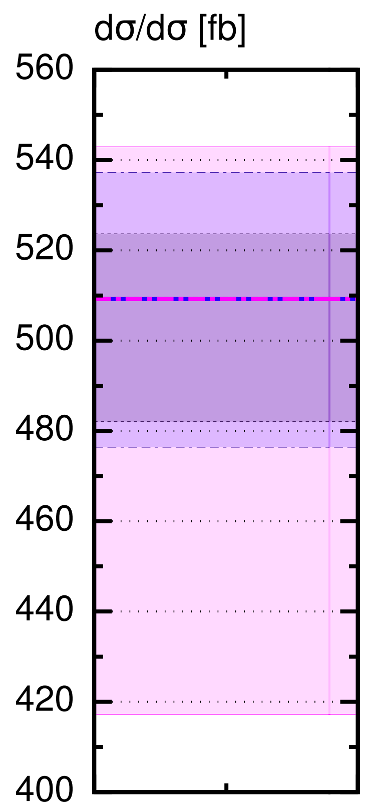


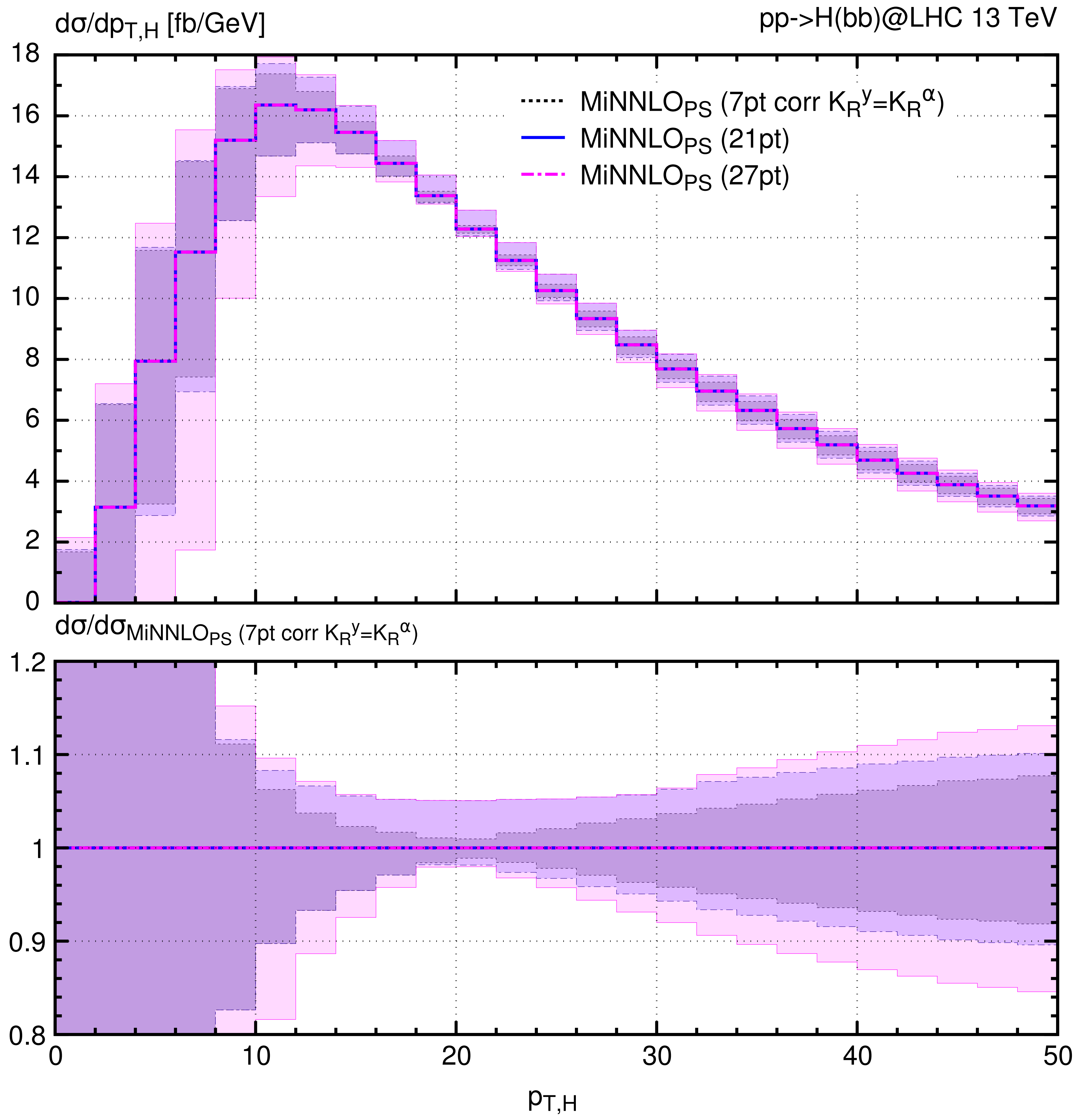
5FS scale variation

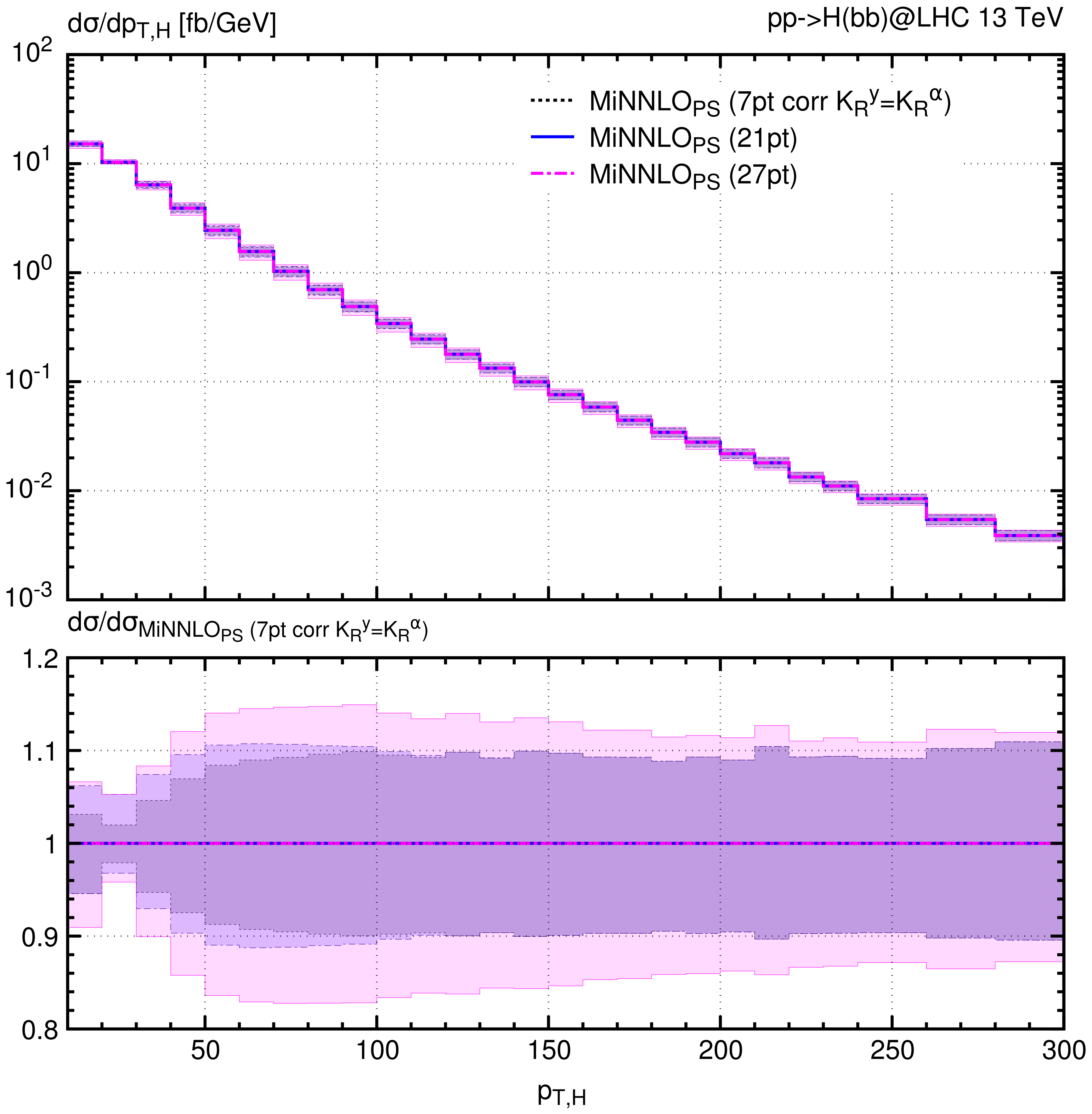


We compare:

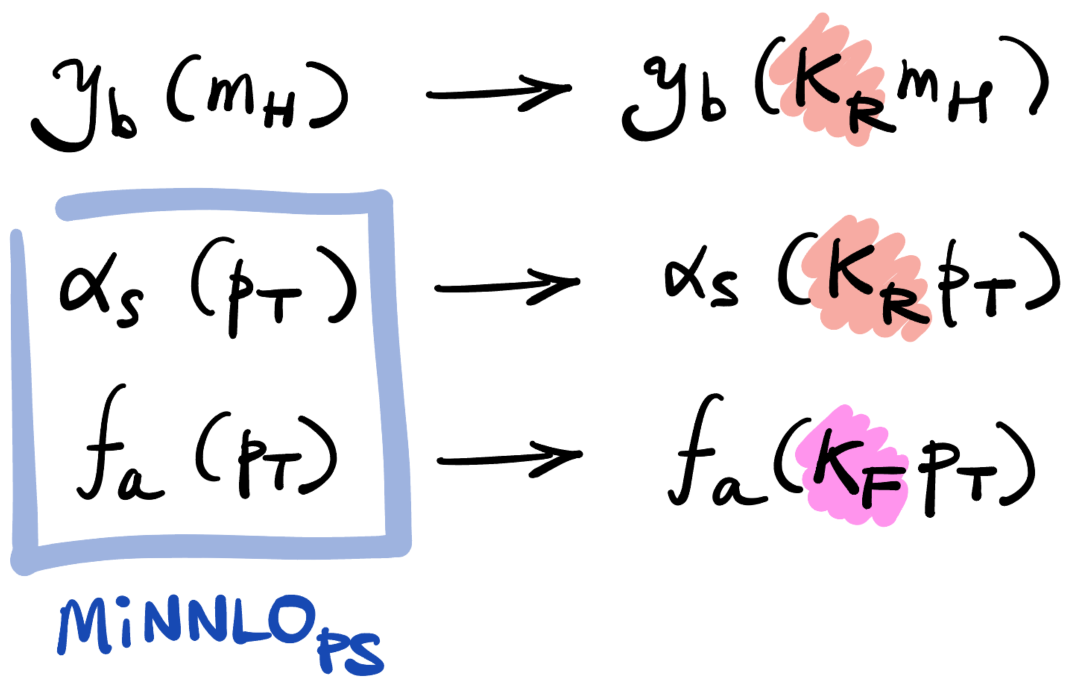
- The standard prediction
- 21pt s.v.: for any value of $K_F = \frac{1}{2}, 1, 2$, we perform a 7pt s.v. for (K_R^y, K_R^α)
- 27pt s.v. (K_R^α, K_R^y, K_F) including $K_i/K_y = 4$.





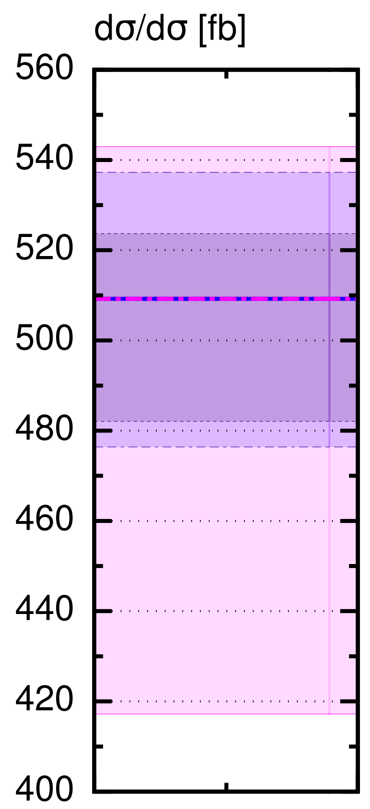


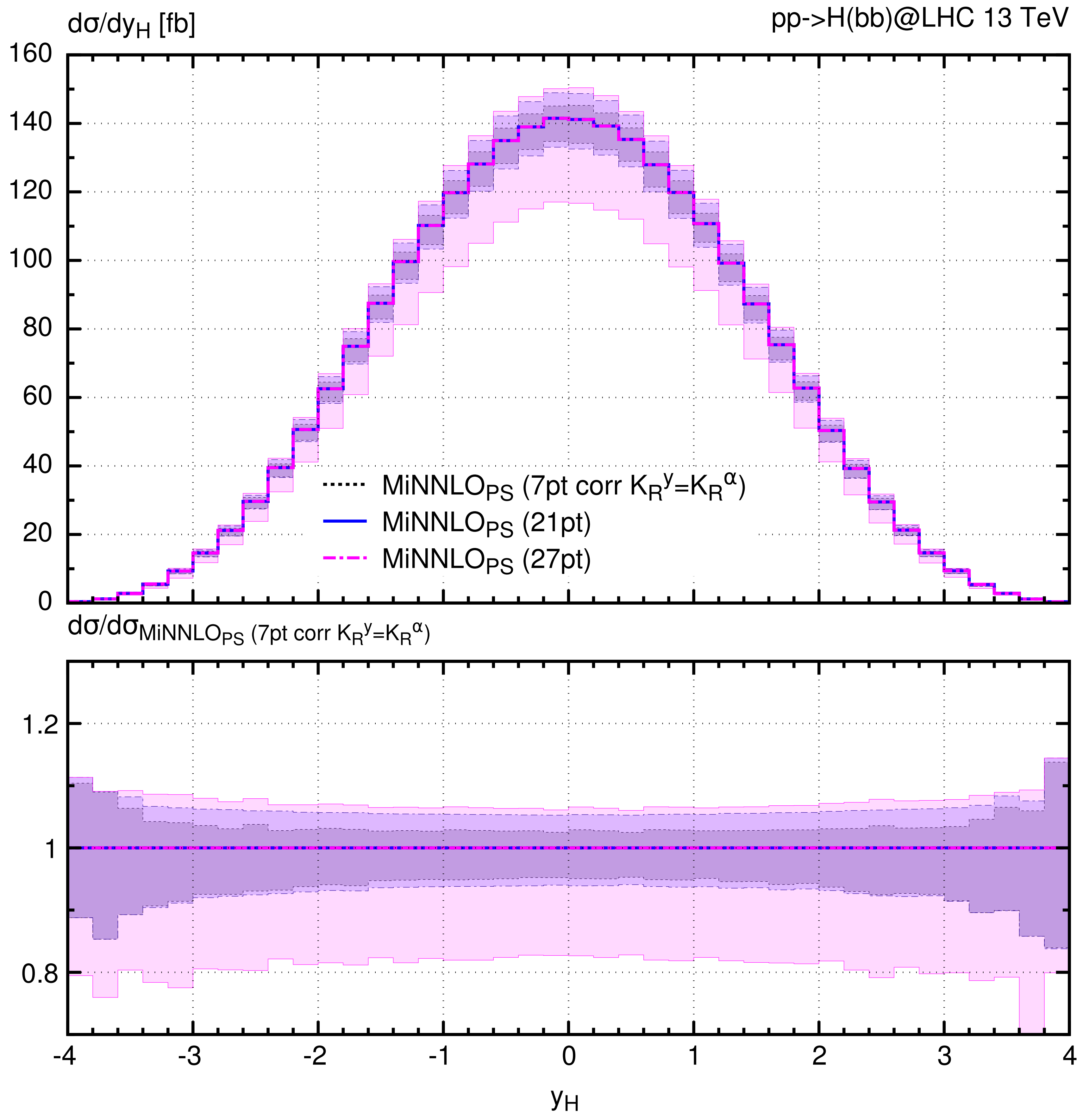
5FS scale variation

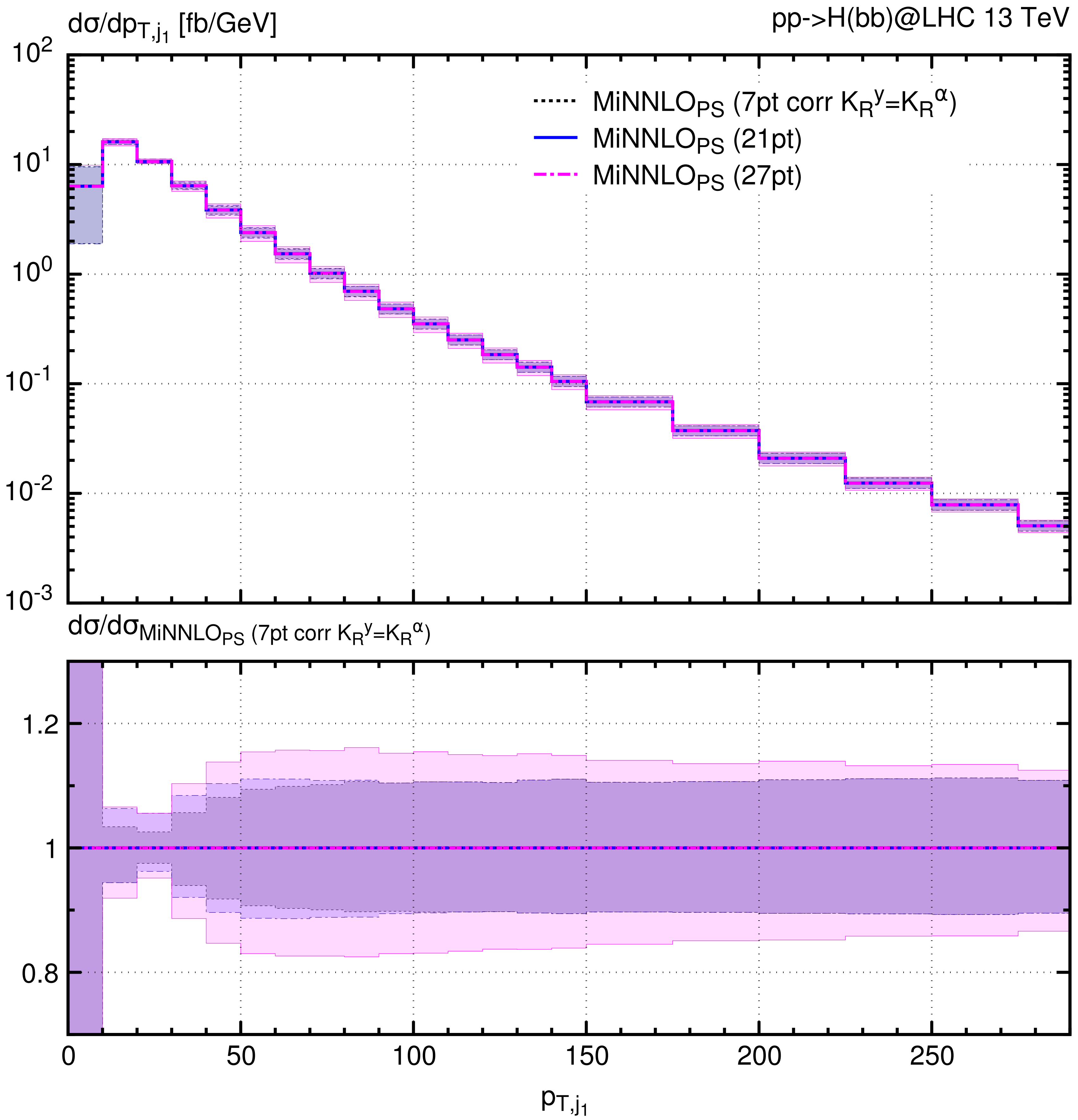


We compare:

- The standard prediction
- 21pt s.v.: for any value of $K_F = \frac{1}{2}, 1, 2$, we perform a 7pt s.v. for (K_R^y, K_R^α)
- 27pt s.v. (K_R^α, K_R^y, K_F) including $K_i/K_y = 4$.

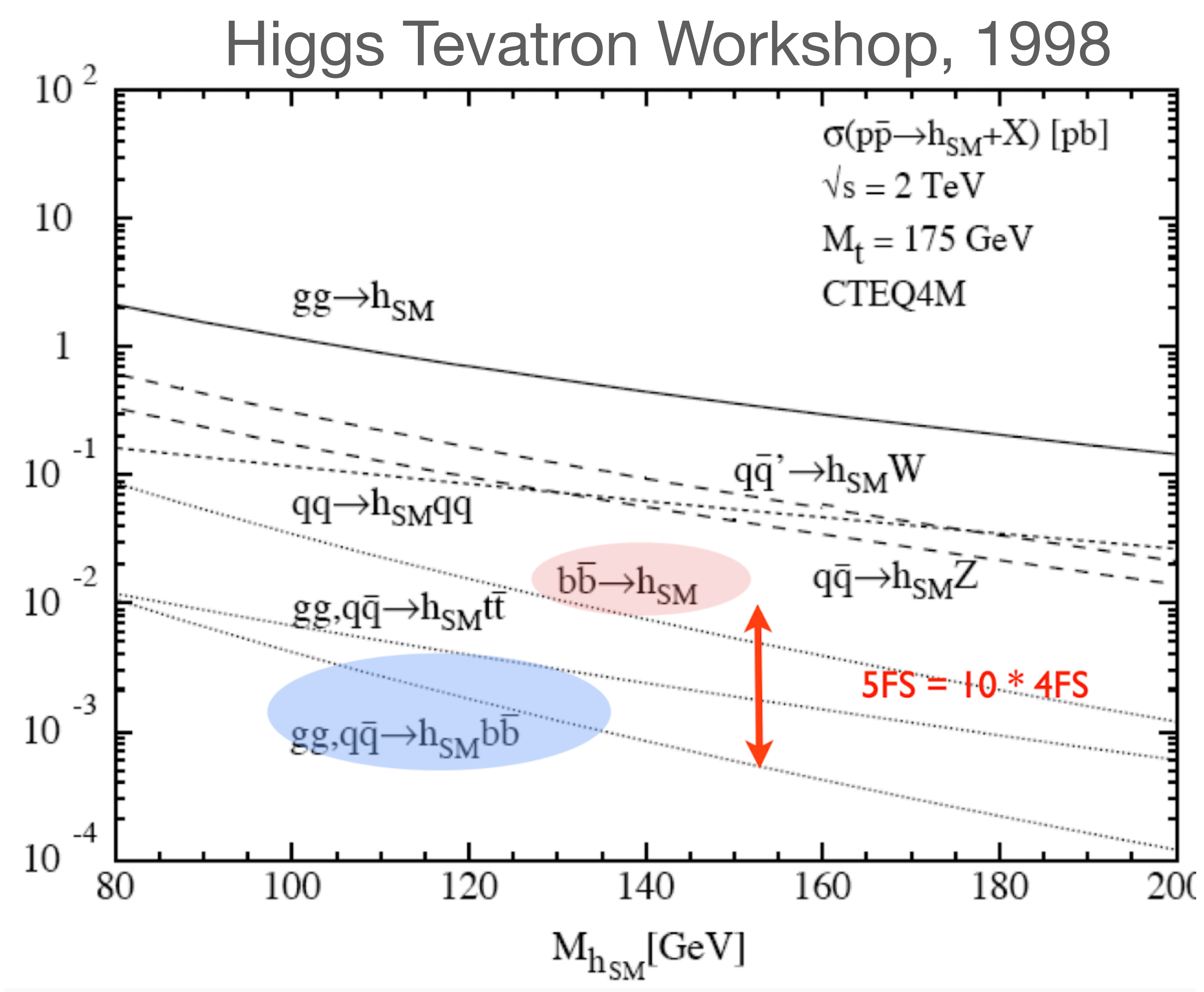


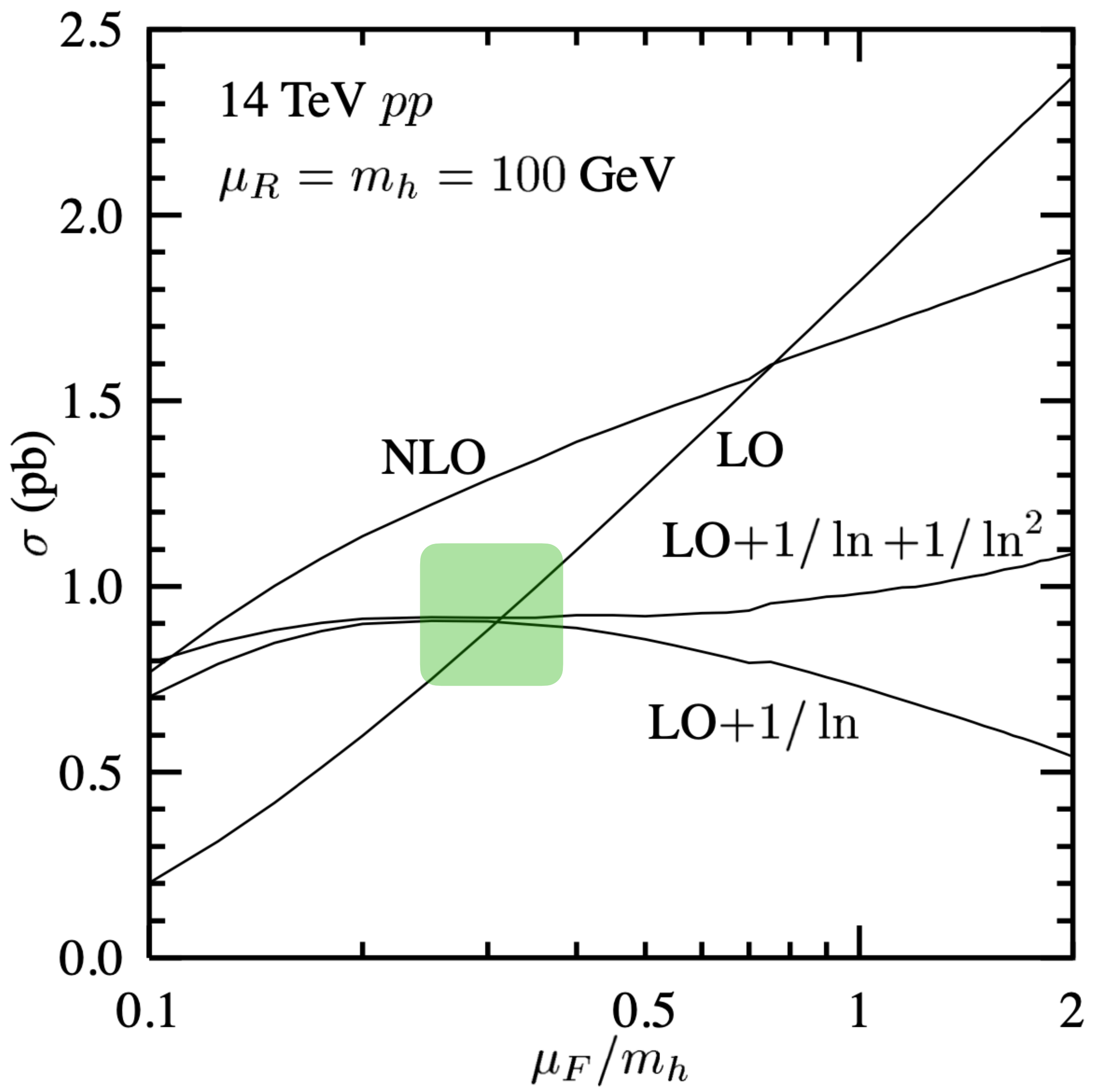




Historical LO comparisons

Large differences in the predictions were first observed at the leading order: the effect of collinear resummation is extremely large.





Maltoni, Sullivan, Willenbrock [hep-ph/0301033]

For $\mu_F = m_H/4$, FO computations in the different schemes become compatible, indeed the collinear logs have a small effect. This also improved the convergence of the perturbation series.

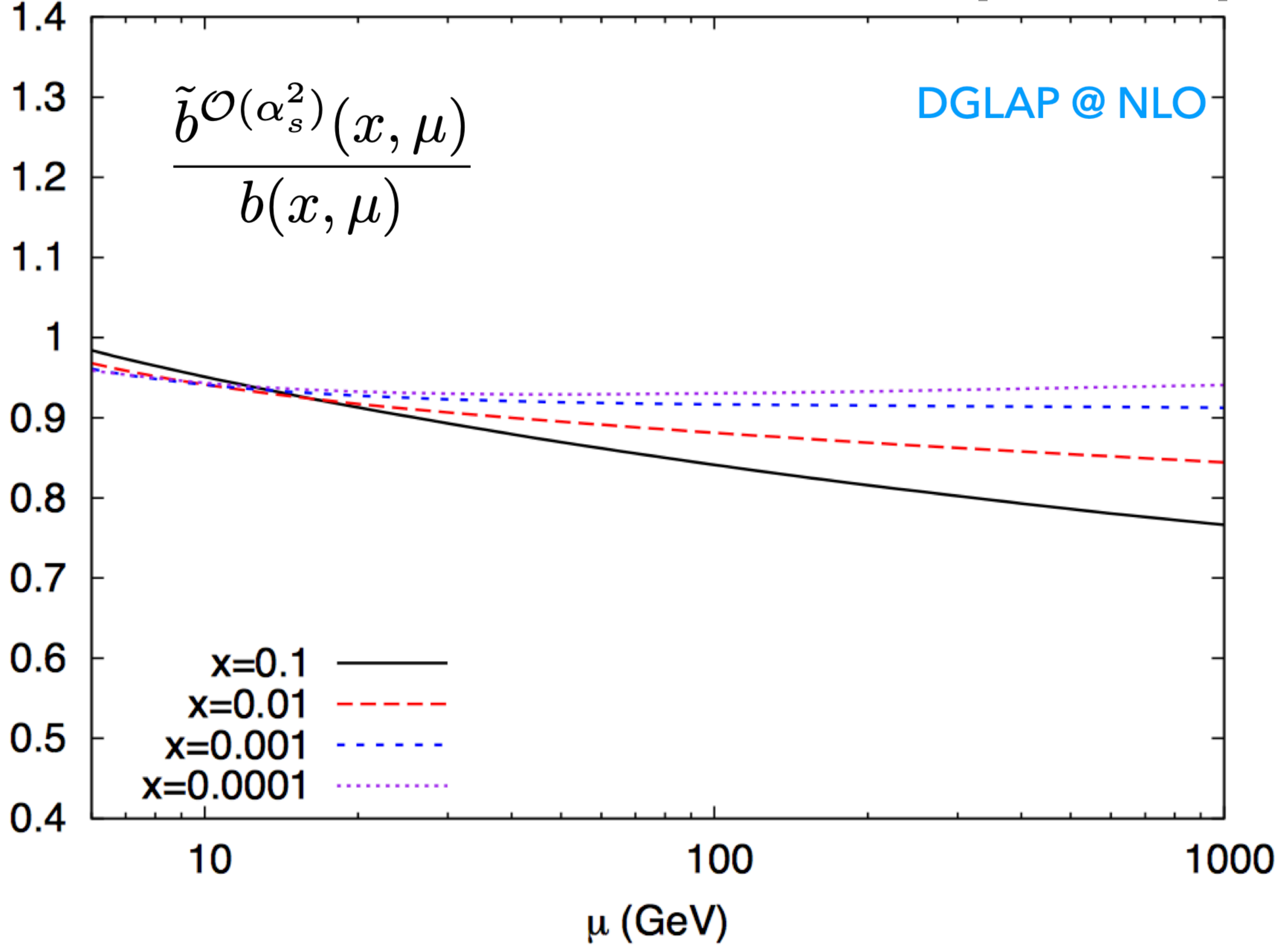
The improvement of the compatibility opens the possibility to match together the predictions at least at the inclusive level (Santander matching, FONLL…)

Differences between schemes

Maltoni, Ridolfi, Ubiali [1203.6393]
Thorne [1402.3536]
Olness, Schienbein [0812.3371]

Lot of progress in understanding the origin of the differences. The predictions can be merged into a consistent picture by taking into account two main results.

[1203.6393]



1. At NLO, the resummation effects of collinear logs are important only at high Bjorken-x
2. The possibly large ratios m_H^2/m_b^2 are always accompanied by universal phase space factors f

$$\ln^2 \frac{m_H^2 f}{m_b^2} = \ln^2 \frac{\tilde{\mu}^2}{m_b^2}, \quad \tilde{\mu} < m_H$$

FONLL

Forte, Napoletano, Ubiali [1508.01529]
Forte, Napoletano, Ubiali [1607.00389]

- FONLL matches the flavour schemes

  $\sigma^{FONNL} = \sigma^{4FS} + \sigma^{5FS}$ – double couting.

  For a consistent subtraction, we have to express the two cross-sections in terms of the same α_s and PDFs.

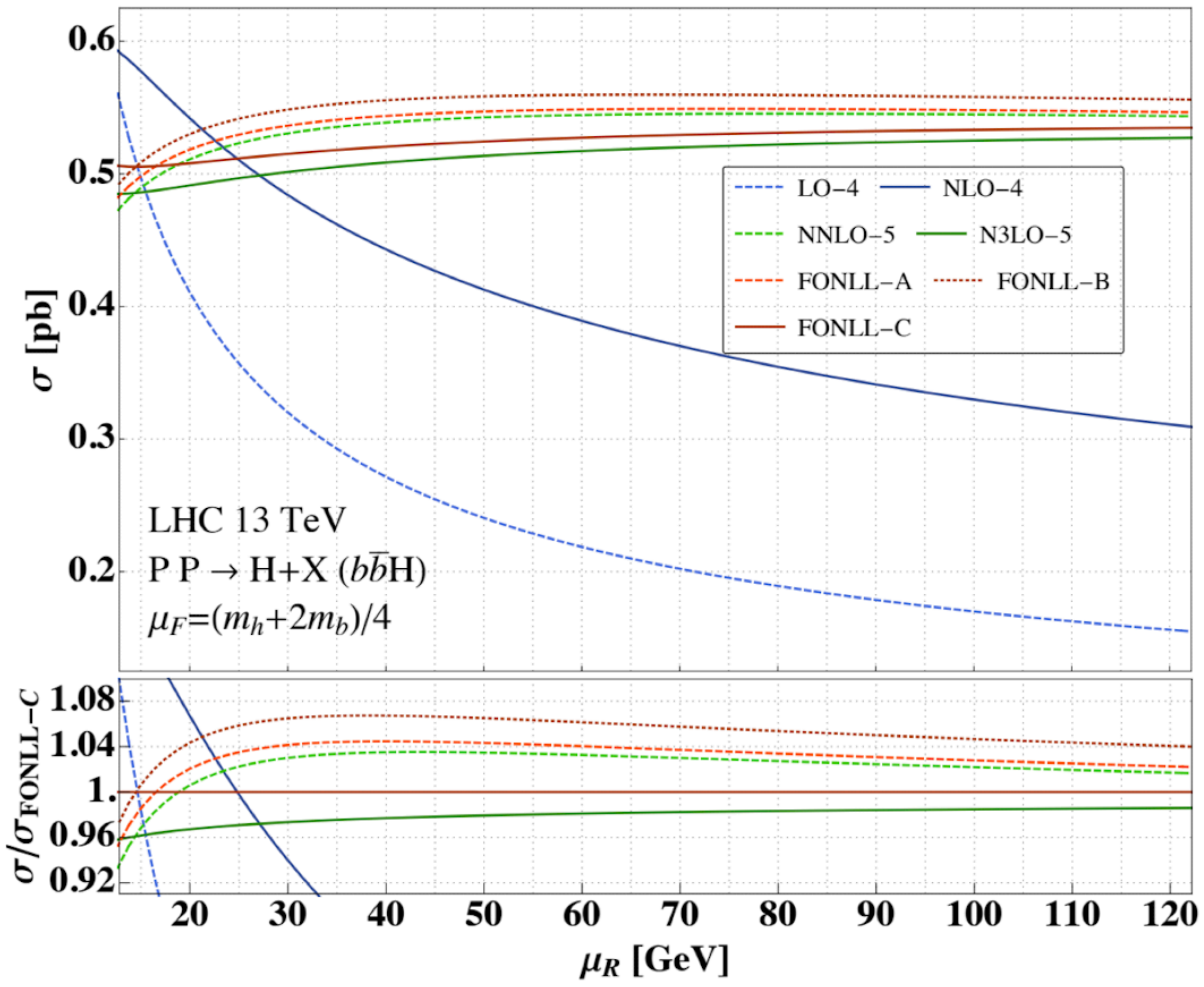
- Currently, the flavour matching for bbH is performed at

  $$\text{FONNL}_C := \text{N}^3\text{LO}_{5FS} \oplus \text{NLO}_{4FS}.$$

- Differential FONLL applied for Z+b-jet

  $$d\sigma^{FONLL} = d\sigma^{5FS} + \left(d\sigma^{4FS}_{m_b} - d\sigma^{4FS}_{m_b \to 0}\right)$$

Duhr, Dulat, Hirschi, Mistlberger [2004.04752]



[Gauld, Gehrmann-De Ridder, Glover, Huss, Majer, 2005.03016]

Exclusive observables

Recent developments in fully differential calculations, for example:

1. Introduce an unphysical scale μ_b in order to switch from 4FS to 5FS in a region where mass effects and collinear logs are not crucial [Bertone, Glazov, Mitov, Papanastasiou, Ubiali, 1711.03355]
2. Massive 5FS at NLO [Krauss, Napoletano, 1712.06832]
3. Differential FONLL applied for Z+b-jet [Gauld, Gehrmann-De Ridder, Glover, Huss, Majer, 2005.03016]

$$d\sigma^{FONLL} = d\sigma^{5FS} + \left(d\sigma^{4FS}_{m_b} - d\sigma^{4FS}_{m_b \to 0}\right)$$