

Indirect Constraints on Third Generation Baryon Number Violation

Gael Finauri

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MAX-PLANCK-INSTITUT
FÜR PHYSIK

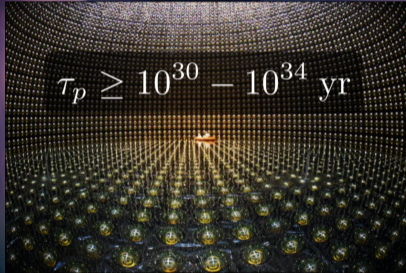
based on M. Beneke, GF, A. A. Petrov 2404.09642



Matter-antimatter asymmetry of the Universe requires Baryon Number Violation (BNV)

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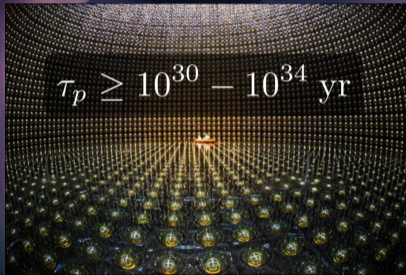
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Super-Kamiokande, Japan

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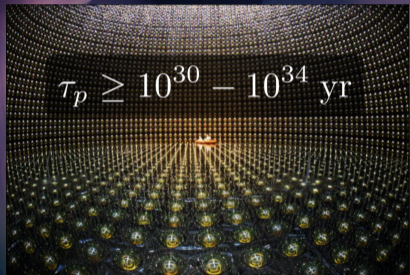
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suggesting New Physics from very high scales

$$\Lambda_{\text{BNV}} \sim 10^{15} - 10^{16} \text{ GeV}$$

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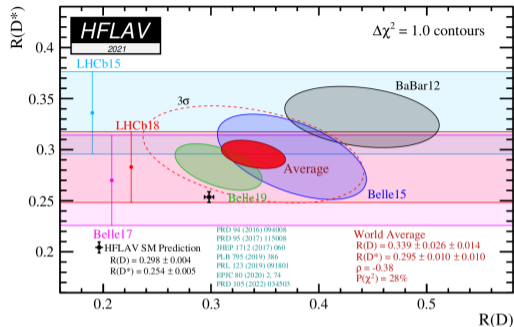
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But what if BNV needs third generation quarks?

Why?

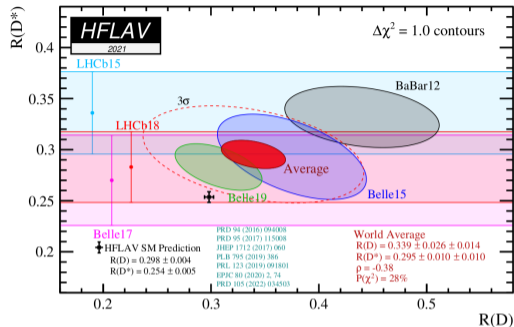
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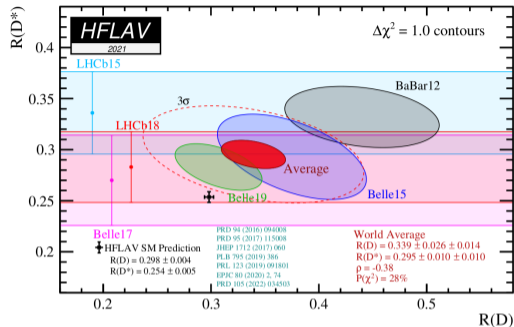
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 $\Lambda_{\text{fl}} \sim 1 - 10 \text{ TeV}$



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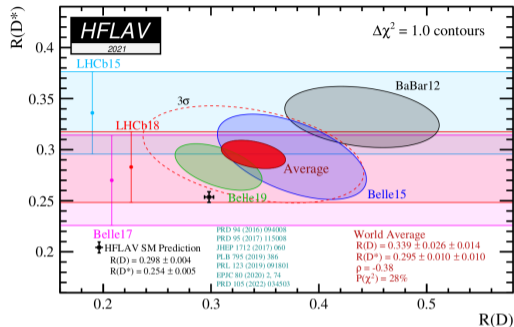
Natural questions:

- If BNV comes only from b quarks, can $\Lambda_{\text{BNV}} \sim \Lambda_{\text{fl}} \ll 10^{15} \text{ GeV}$ be possible?

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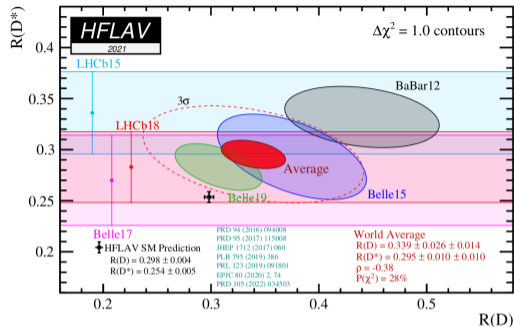
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- Would it lead to observable BNV B decays?

Answer: Don't know!

Proton would still decay through virtual b quarks, constraining Λ_{BNV}

Dominant Decay Channels

Assumption: BNV happens only if at least a b quark is involved.

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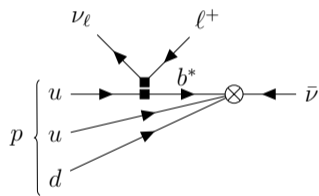
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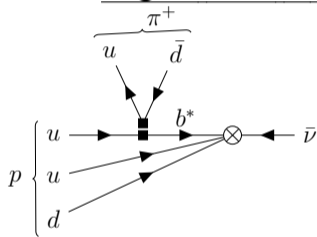
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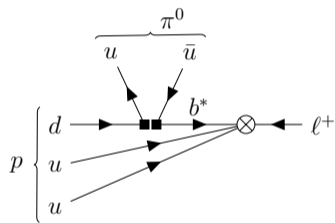
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• $p \rightarrow \pi^+ \bar{\nu}$



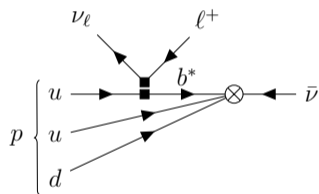
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mediated by weak interaction and four-fermion BNV operators (\otimes) from SMEFT:

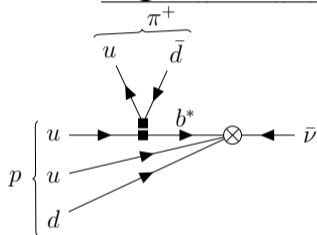
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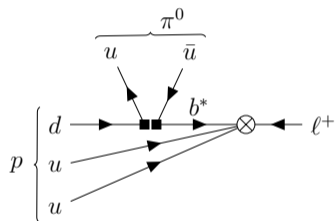
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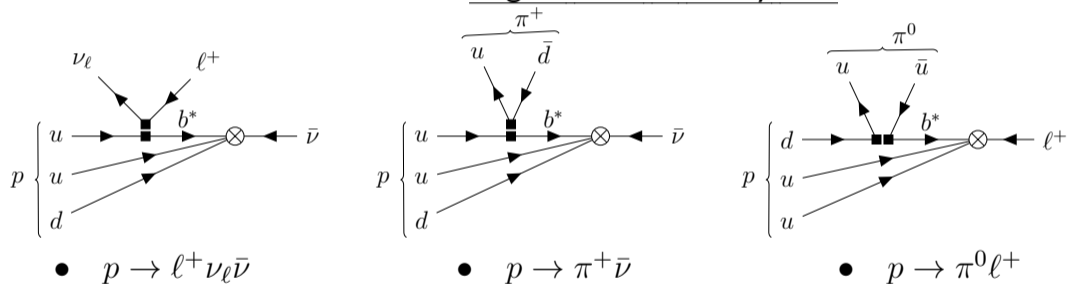
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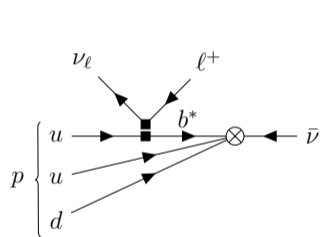


smallest Λ_{BNV} from τ_p constraints

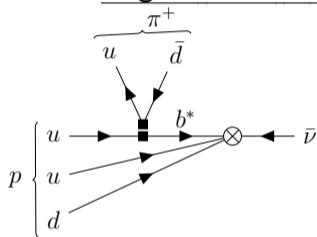
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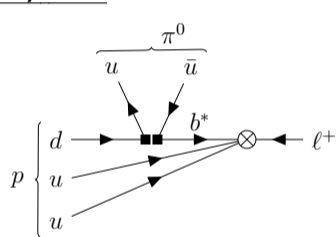
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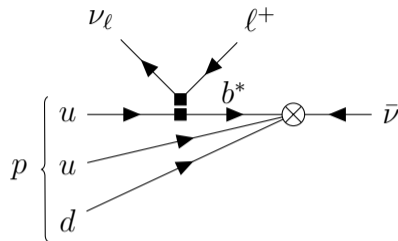


highest $\Gamma(\bar{B} \rightarrow X \ell)$

Results for $p \rightarrow \ell^+ \nu_\ell \bar{\nu}$

Experimental bounds [Super-Kamiokande 2014]

- $\Gamma(p \rightarrow e^+ \nu \nu) < 1.23 \cdot 10^{-64} \text{ GeV}$
- $\Gamma(p \rightarrow \mu^+ \nu \nu) < 0.95 \cdot 10^{-64} \text{ GeV}$

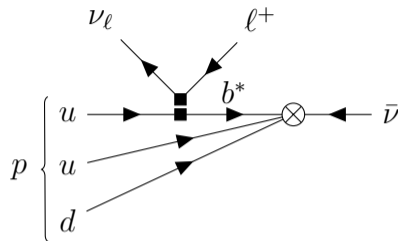


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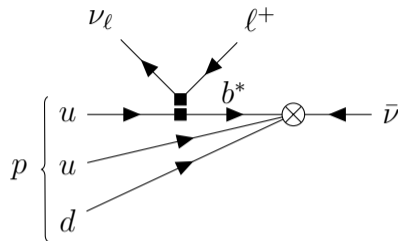
$$\Gamma(p \rightarrow \ell^+ \nu_\ell \bar{\nu}) = \frac{|C_\nu|^2}{\Lambda_{\text{BNV}}^4} \frac{|V_{ub}|^2 G_F^2 m_p^7}{7680 \pi^3 m_b^2} 10^{-3} \text{GeV}^4 \times \begin{cases} 1.028, & \text{for } p \rightarrow e^+ \nu_e \bar{\nu} \\ 0.933, & \text{for } p \rightarrow \mu^+ \nu_\mu \bar{\nu} \end{cases}$$

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Using the experimental constraints

$$\frac{\Lambda_{\text{BNV}}}{\sqrt{|C_\nu|}} \Big|_{p \rightarrow e^+ \nu_e \bar{\nu}} > 6.59 \cdot 10^9 \text{ GeV}$$

$$\frac{\Lambda_{\text{BNV}}}{\sqrt{|C_\nu|}} \Big|_{p \rightarrow \mu^+ \nu_\mu \bar{\nu}} > 6.86 \cdot 10^9 \text{ GeV}$$

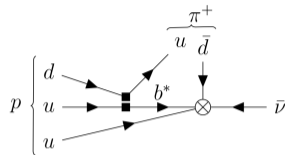
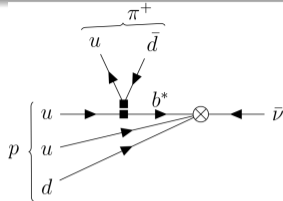
rather **high**! Already showing that $\Lambda_{\text{BNV}} \sim \Lambda_{\text{fl}}$ is ruled out!

Results for $p \rightarrow \pi^+ \bar{\nu}$

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$$\Gamma(p \rightarrow \pi^+ \nu) < 5.35 \cdot 10^{-65} \text{ GeV}$$

Assume factorization, true up to $\mathcal{O}(1)$ corrections

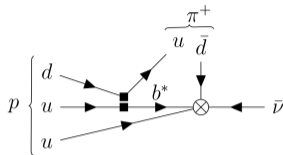
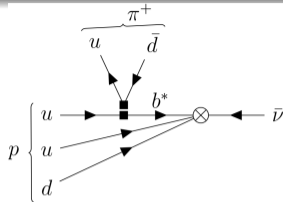


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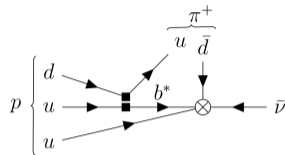
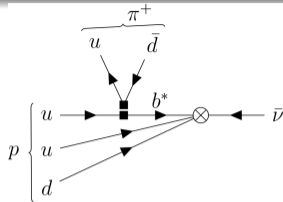
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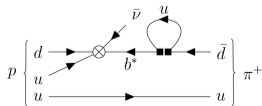
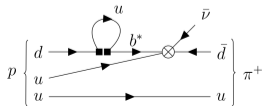
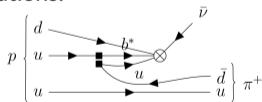
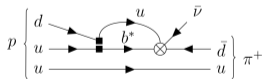
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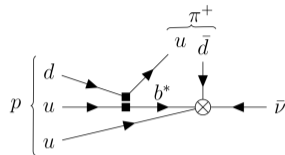
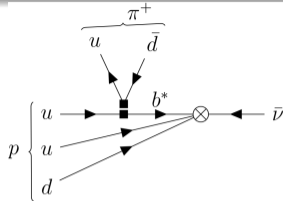


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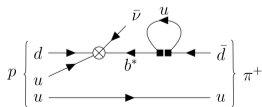
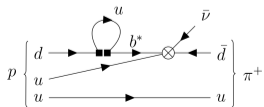
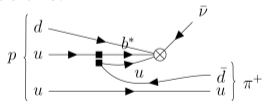
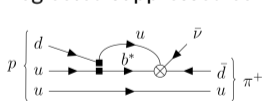
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less effective than leptonic decay



Strongest experimental bounds [Super-Kamiokande 2020]

- $\Gamma(p \rightarrow \pi^0 e^+) < 0.87 \cdot 10^{-66} \text{ GeV}$
- $\Gamma(p \rightarrow \pi^0 \mu^+) < 1.30 \cdot 10^{-66} \text{ GeV}$

two independent operators contributing
➡ 2D constraints!

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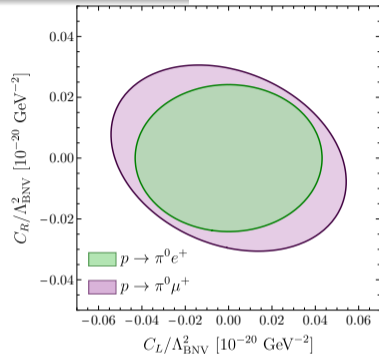
$$\Lambda_{\text{BNV}} \Big|_{p \rightarrow \pi^0 e^+} > 6.23 \cdot 10^{10} \text{ GeV} \left(|C_R^e|^2 + 0.0014 \text{Re}[C_L^{e*} C_R^e] + 0.304 |C_L^e|^2 \right)^{1/4},$$
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these coefficients are 10 times more constrained with respect to C_ν

Estimates for inclusive BNV B decays

We can estimate the branching ratio using $\Lambda_{\text{BNV}} > 6 \cdot 10^9 \text{ GeV}$

$$\mathcal{B}(\bar{B} \rightarrow X\ell) \approx \frac{m_b^5}{2^{10} 3 \pi^3 \Gamma_{\text{tot}}^B \Lambda_{\text{BNV}}^4}$$

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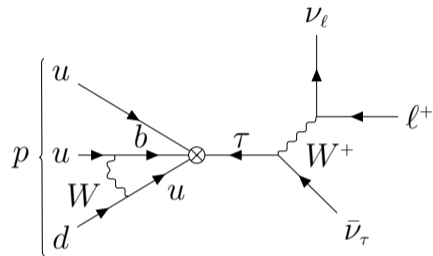
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However...

what about operators with τ lepton? Not directly constrained by p decay!

BNV Operators with b and τ

Both b and τ have to be virtual!
Efficiently constrained by loop induced effects



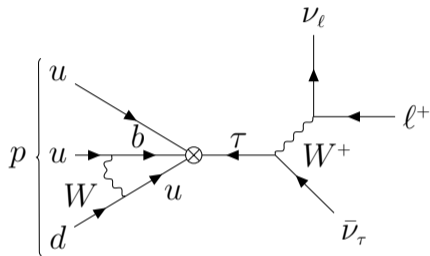
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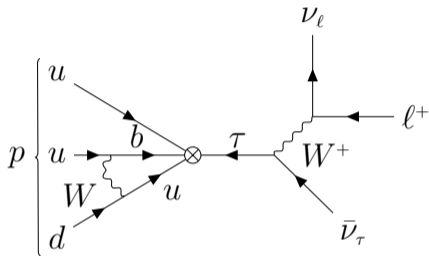
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$$\mathcal{B}(\bar{B} \rightarrow X\tau) \lesssim (10^{-13} \div 10^{-15})$$

closer to detectability, but experimental efficiency in reconstructing τ is much smaller...



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Under the assumption that BNV occurs only if b quark is involved:

- Scanned for the less constrained SMEFT operators
- Derived bounds for Λ_{BNV} from proton decay in three decay channels
- Showed $\mathcal{B}(\bar{B} \rightarrow X\ell) \lesssim \mathcal{O}(5 \cdot 10^{-29}) \Rightarrow$ undetectable!
- For τ less restrictive $\mathcal{B}(\bar{B} \rightarrow X\tau) \lesssim 10^{-13} \div 10^{-15}$

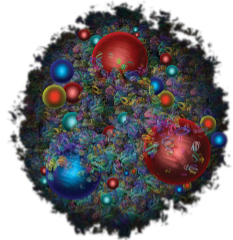
Under the assumption that BNV occurs only if b quark is involved:

- Scanned for the less constrained SMEFT operators
- Derived bounds for Λ_{BNV} from proton decay in three decay channels
- Showed $\mathcal{B}(\bar{B} \rightarrow X\ell) \lesssim \mathcal{O}(5 \cdot 10^{-29}) \Rightarrow$ undetectable!
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Thank You!

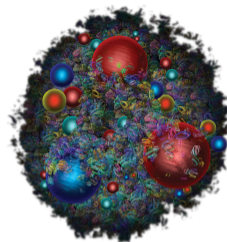
Backup Slides

Theoretical predictions are affected by the **non-perturbative** nature of hadronic QCD



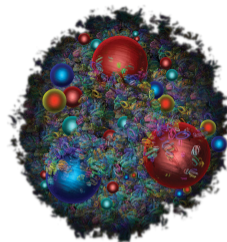
Theoretical predictions are affected by the **non-perturbative** nature of hadronic QCD

However nature provided an intrinsic **perturbative** scale $m_b \sim 5 \text{ GeV}$



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\Rightarrow B decays employing **Effective Field Theories** (HQET, SCET, ...) to separate **perturbative physics** from universal **non-perturbative inputs**

