

New Models and Methods for Particle Physics

From Neutrinos to Quantum Computing

Lena Funcke



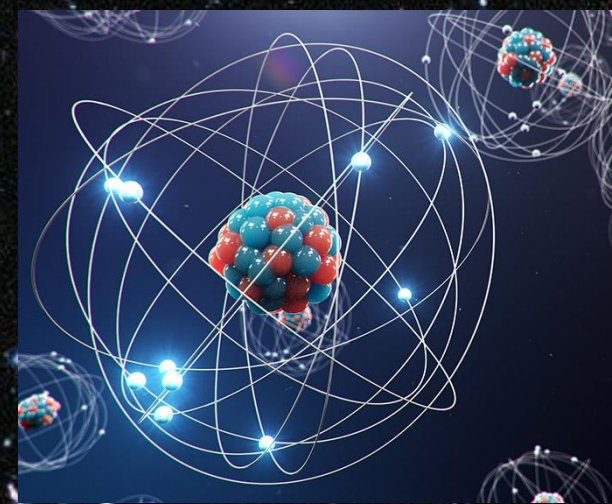
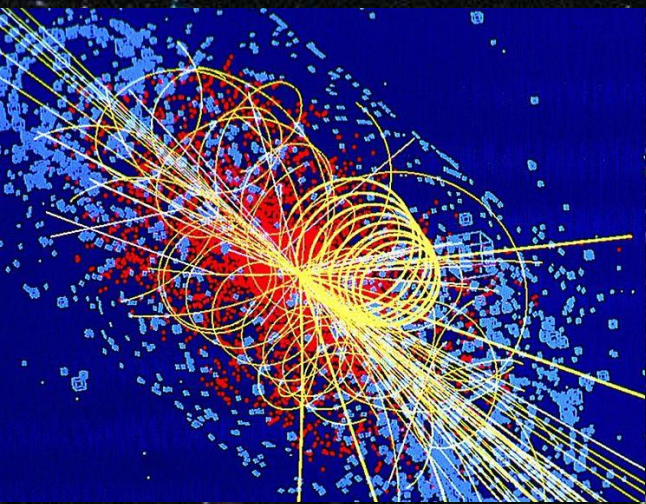
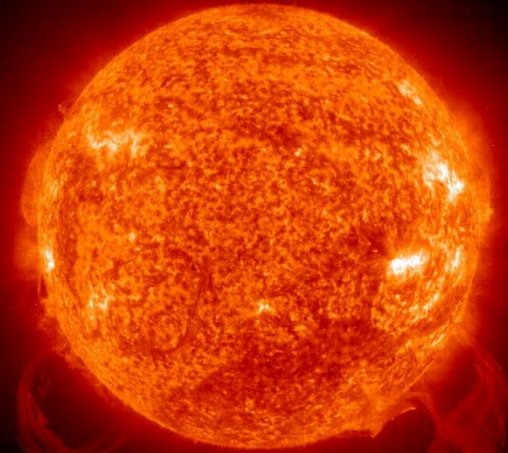
MPP Colloquium, 26 November 2024

Cosmology

Astrophysics

Particle Physics

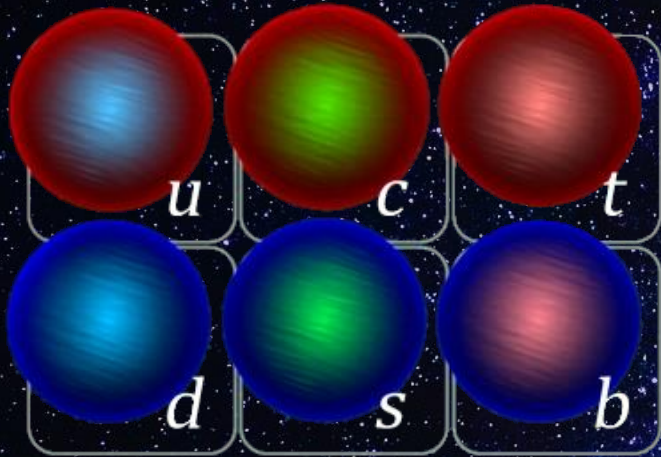
Nuclear Physics



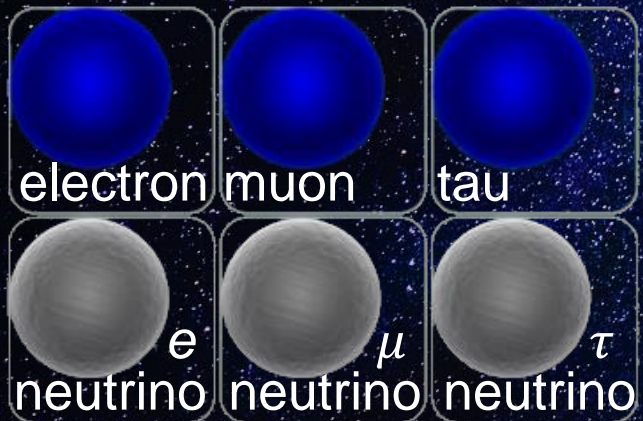
“Standard Model” of Particle Physics

Matter (+ Antimatter)

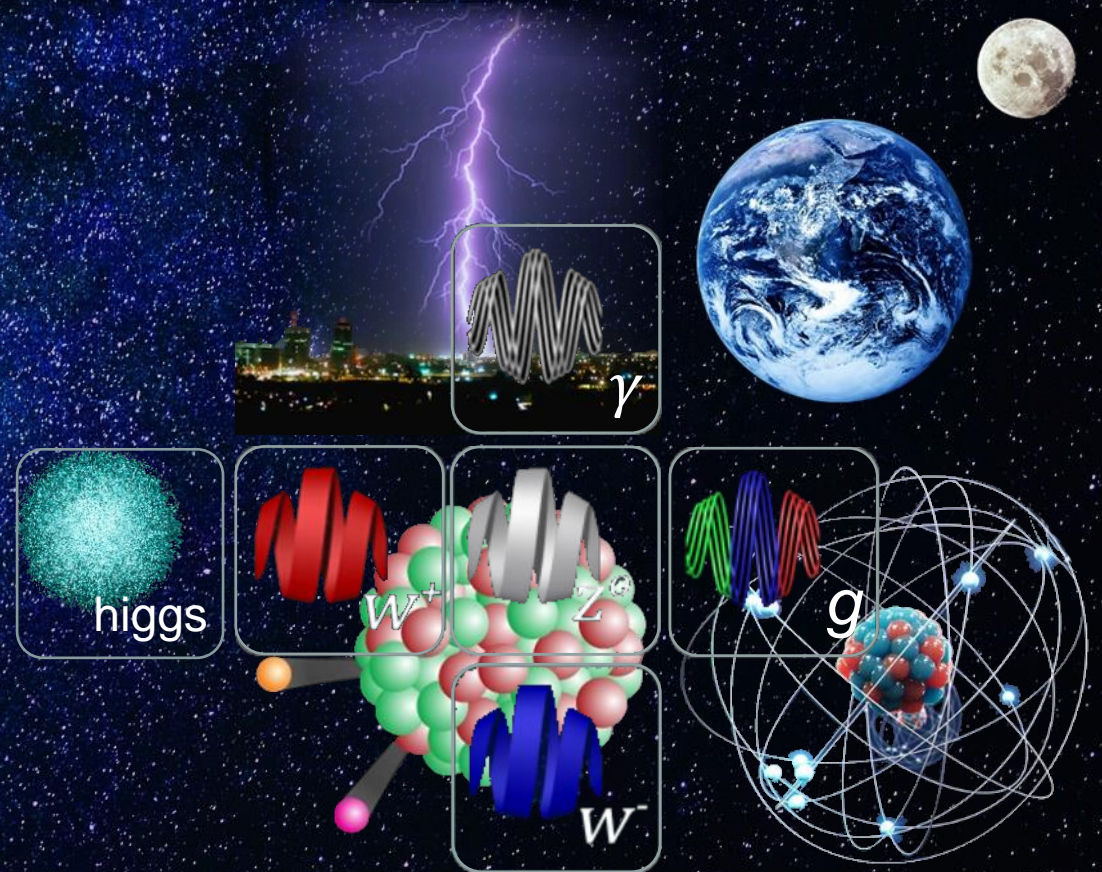
Quarks



Leptons

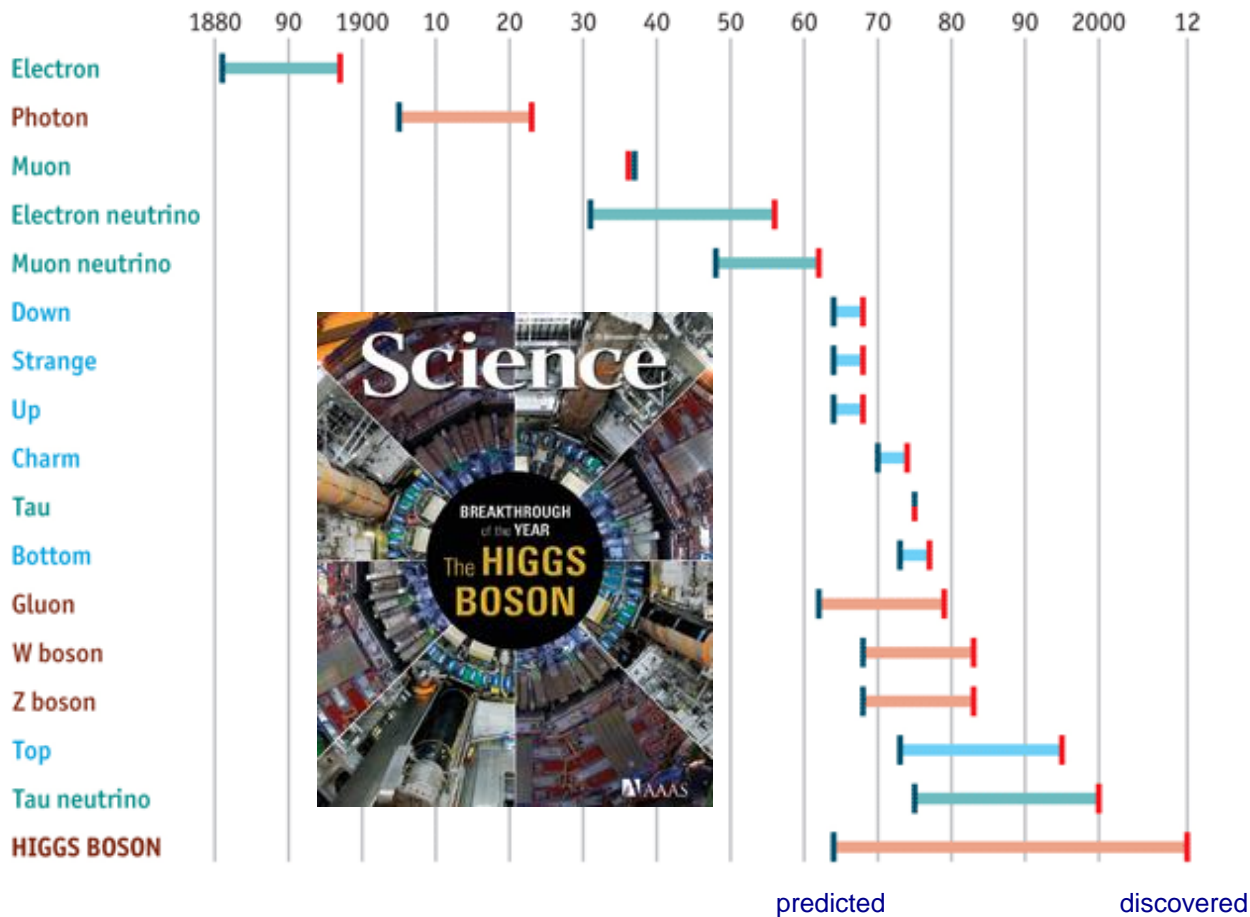


Forces



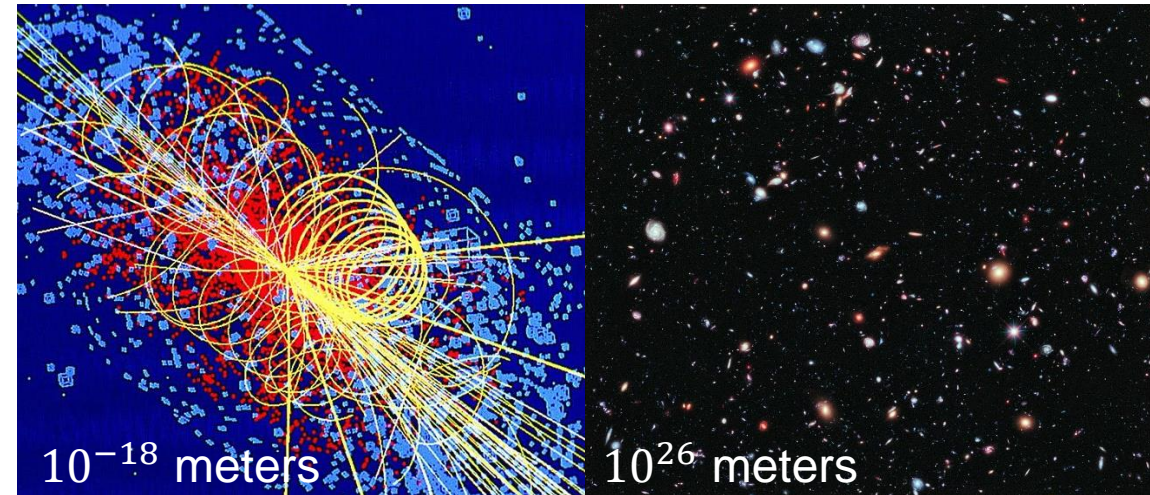
The success of the “Standard Model”

Every predicted particle was eventually discovered:



Content: all particles & forces (except for gravity)

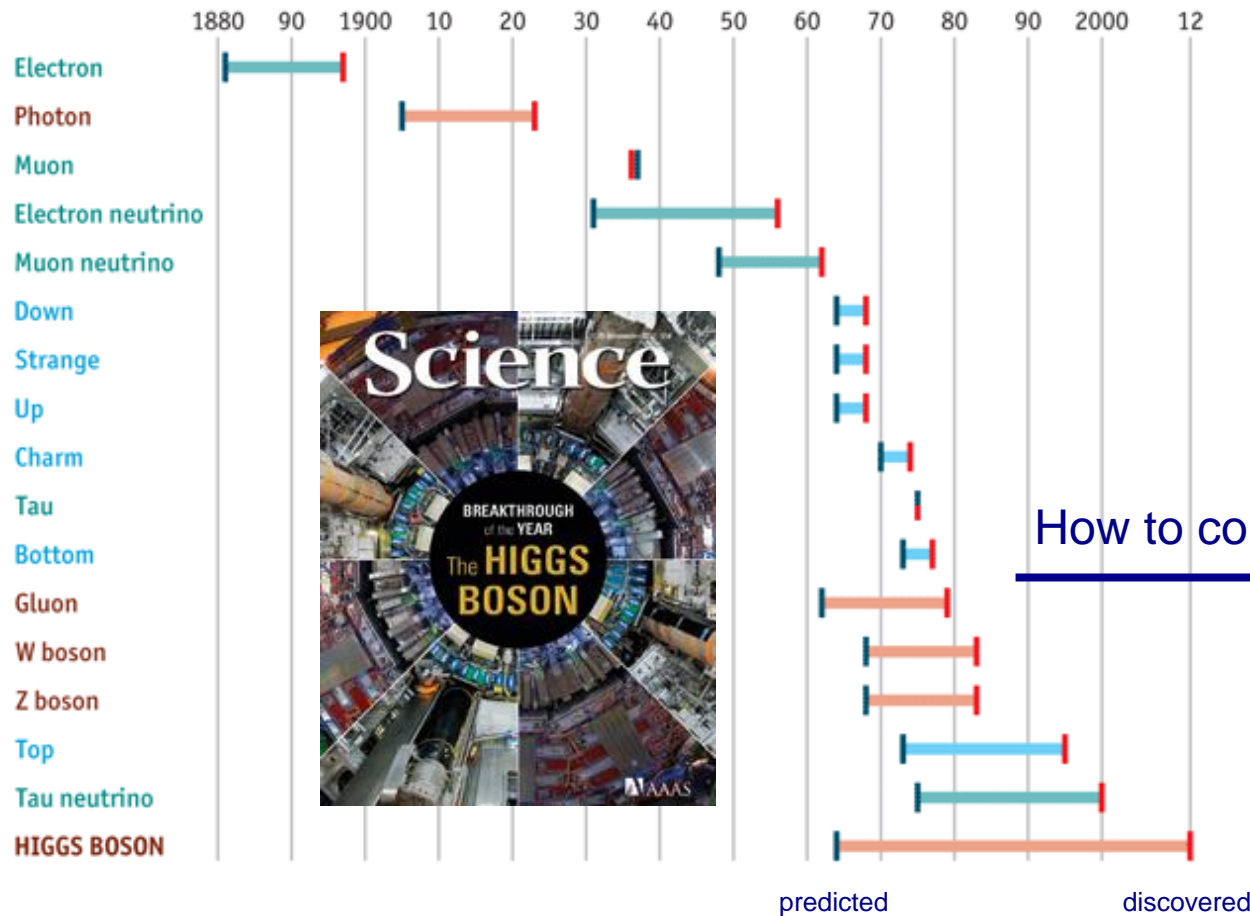
Range:



Precision: up to 0.0000000001 (electron g -factor)

Open questions of the “Standard Model”

Every predicted particle was eventually discovered:



Why do neutrinos have masses?

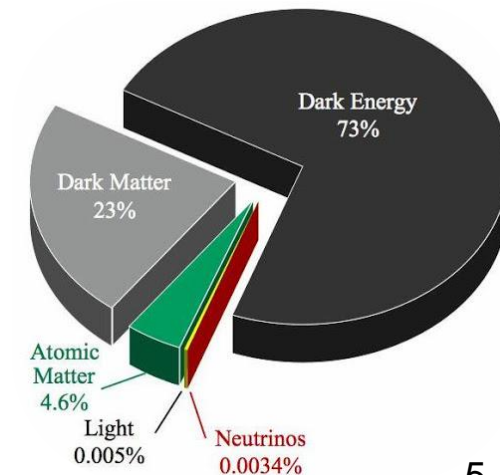
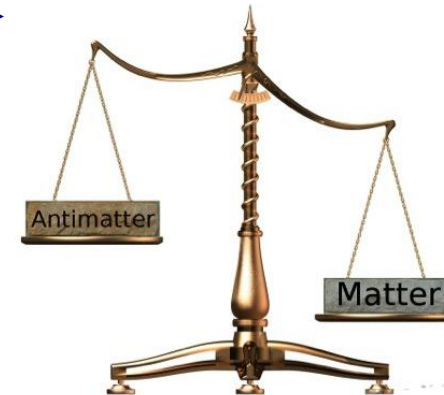
Why is there more matter than antimatter in the universe?

Why has no strong CP violation been observed?

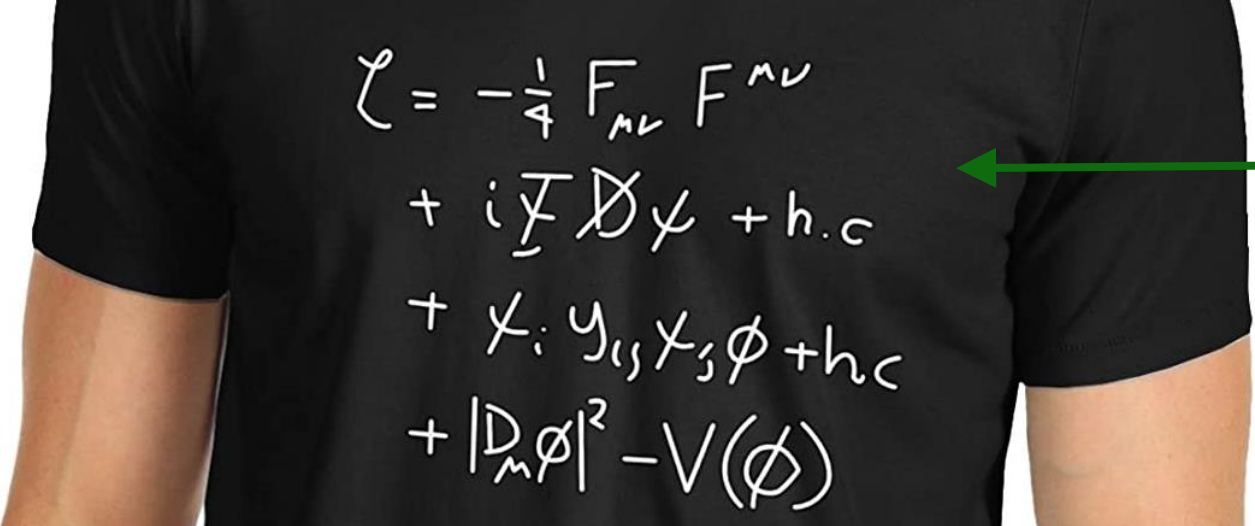
What are dark matter and dark energy?

...

How to continue?



How can we answer these open questions?


$$\begin{aligned}\mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i\bar{\psi} \not{D} \psi + h.c \\ & + \chi_i y_{ij} \chi_j \phi + h.c \\ & + |D_\mu \phi|^2 - V(\phi)\end{aligned}$$

Simple equation

Beautiful but incomplete!

Need new equations → *new models*



Complex phenomena

Emergent structures!

Need numerical simulations → *new methods*

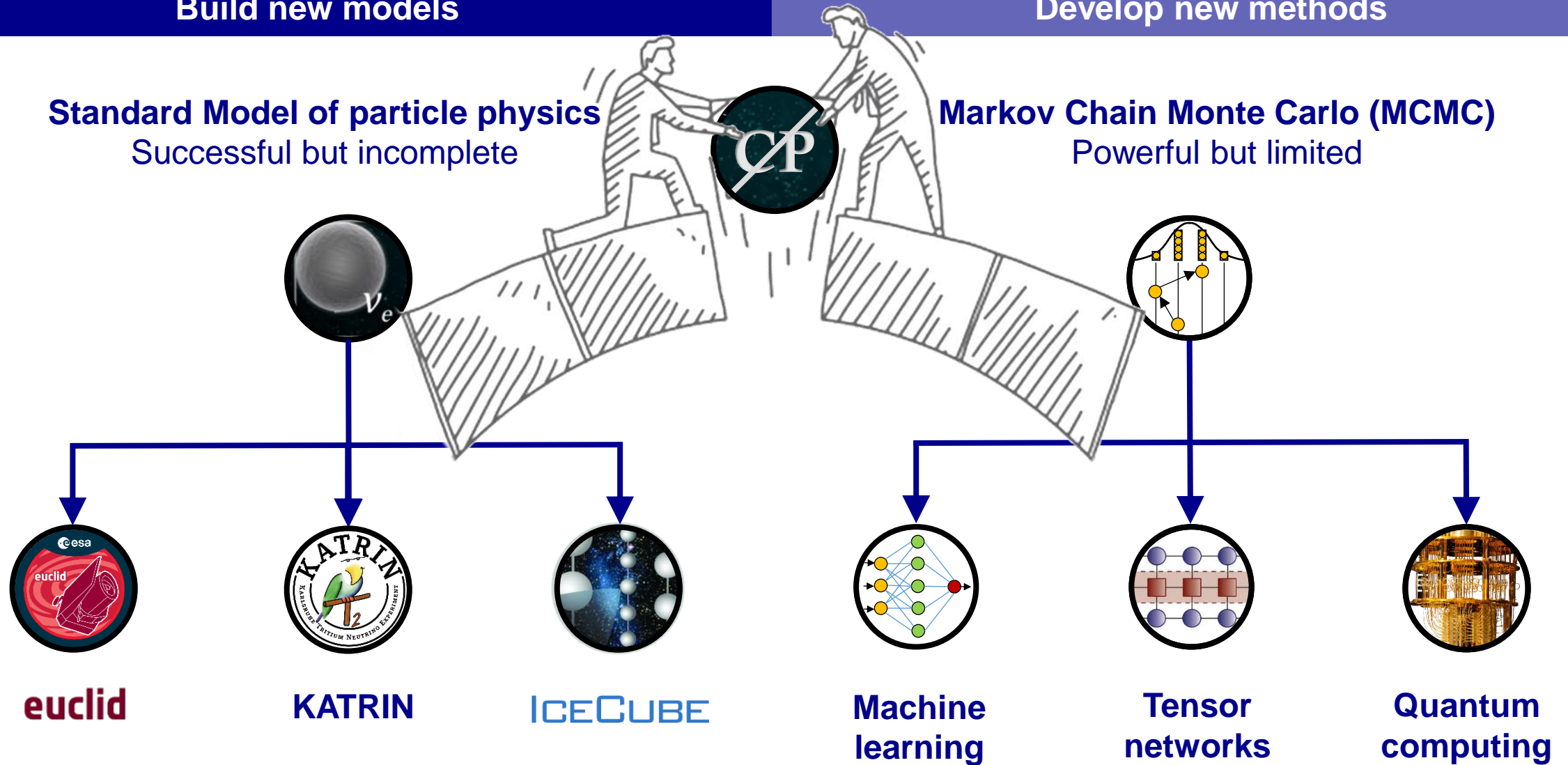
New models and methods for particle physics

Build new models

Develop new methods

Standard Model of particle physics
Successful but incomplete

Markov Chain Monte Carlo (MCMC)
Powerful but limited



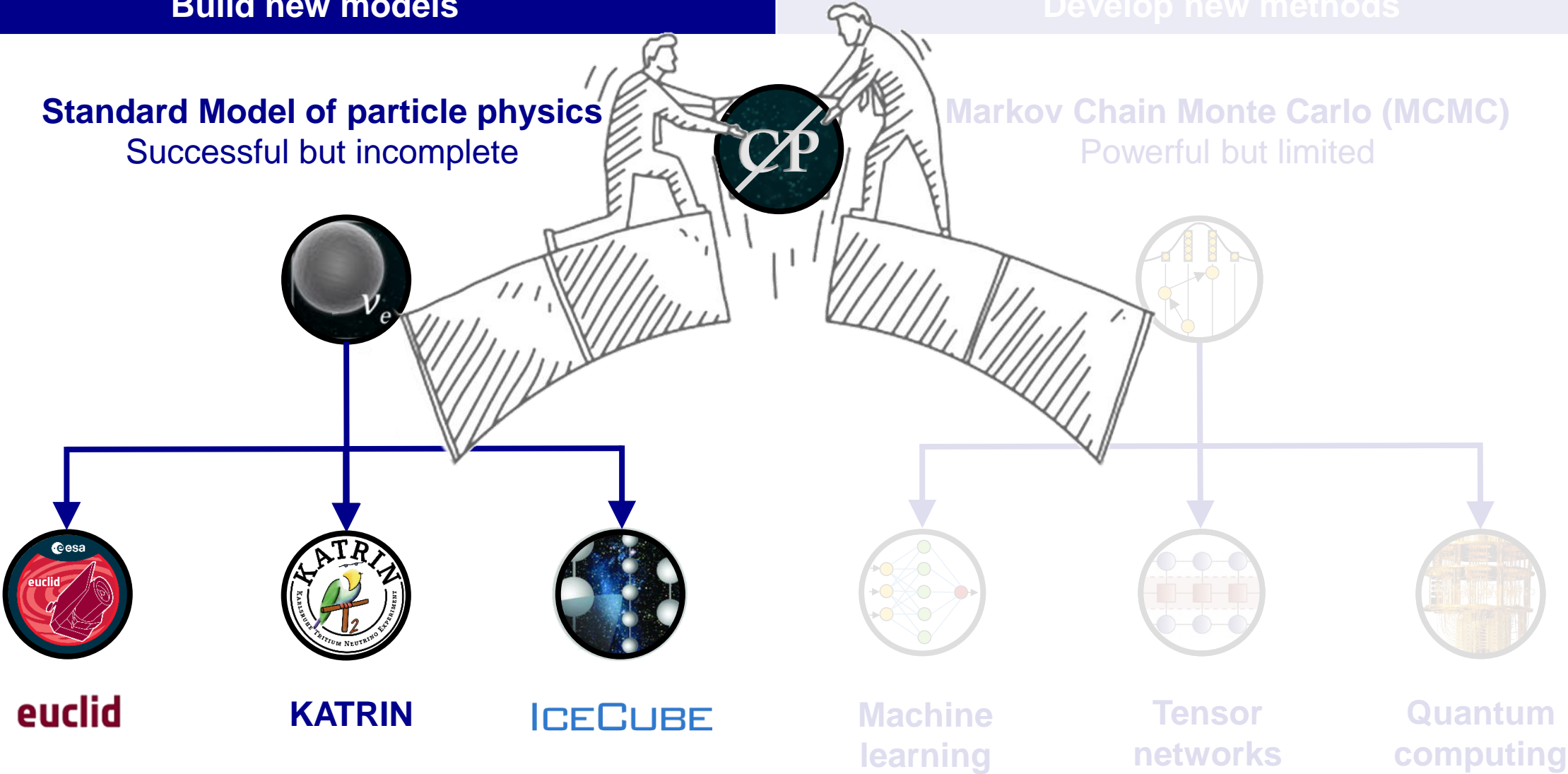
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How to build new models?

Neutrino mass model

Standard Model

Masses of particles are generated in the early universe

Problem

Neutrino masses: predicted = 0 but measured $\neq 0$

Our model ¹

Neutrinos can become massive in the late Universe

Key prediction

Neutrino condensation \rightarrow flavor symmetry breaking

History of Universe



¹ Dvali, LF, *PRD* (2016a)

New neutrino physics hiding at low energies

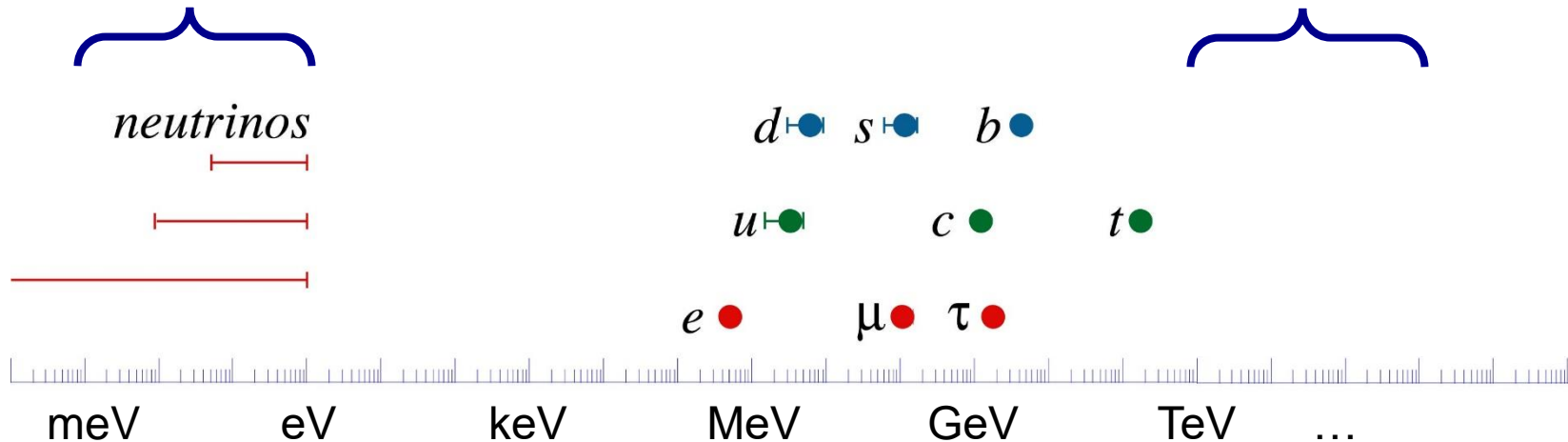
New low-energy model ¹

Idea

Small neutrino masses from gravitational anomaly
 → Standard Model + gravity

New concept

Neutrino condensate and effective masses
 → at new low-energy gravitational scale



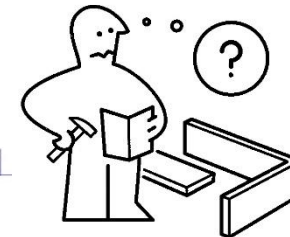
Common high-energy models

Ideas

“Seesaw” mechanisms, large extra dimensions, ...
 → Standard Model + new particles, symmetries, ...

Unifying concept

Neutrino masses from Higgs condensate
 → suppressed by new high-energy physics



¹ Dvali, LF, *PRD* (2016a)

Analogy: Non-perturbative QCD vacuum

Quantity

QCD with 3 quarks

Gravity with 3 neutrinos

Fermion flavor symmetry

$$U(3)_L \times U(3)_R \rightarrow U(3)_V$$

$$U(3)_L \times U(3)_R \text{ exact if } m_\nu = 0$$

(Pseudo) Goldstone bosons

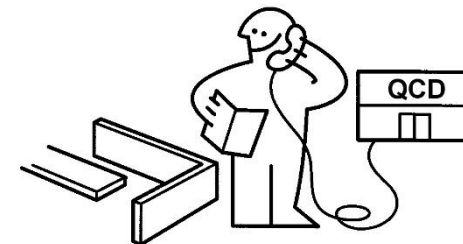
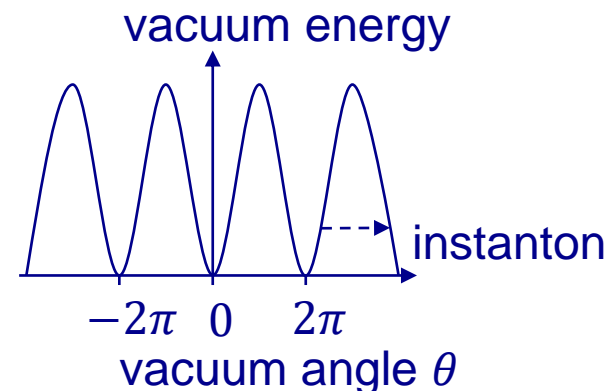
$$1(\eta') + 8(\pi, K, \eta)$$

Axial anomaly

$$\partial_\mu j_5^\mu = G\tilde{G} + m_q \bar{q}\gamma_5 q$$

Topological susceptibility

$$\langle G\tilde{G}, G\tilde{G} \rangle_{p \rightarrow 0} \neq 0 \rightarrow \langle \bar{q}q \rangle \neq 0$$



Analogy: Non-perturbative QCD vacuum

Quantity

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$$U(3)_L \times U(3)_R \rightarrow U(3)_V$$

$$U(3)_L \times U(3)_R \rightarrow U(1)^3 ?^1$$

(Pseudo) Goldstone bosons

$$1(\eta') + 8(\pi, K, \eta)$$

$$1(\eta_\nu) + 14(\phi_k)^1$$

Axial anomaly

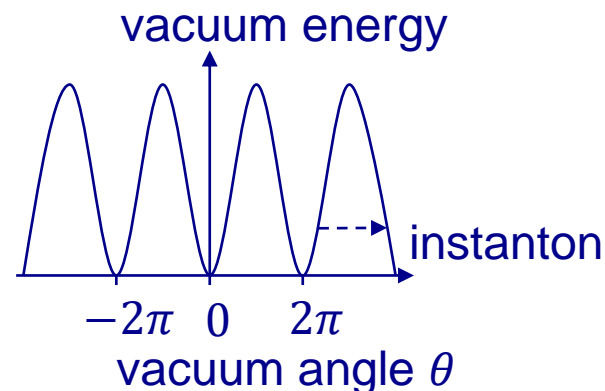
$$\partial_\mu j_5^\mu = G\tilde{G} + m_q \bar{q}\gamma_5 q$$

$$\partial_\mu j_5^\mu = R\tilde{R} + m_\nu \bar{\nu}\gamma_5 \nu$$

Topological susceptibility

$$\langle G\tilde{G}, G\tilde{G} \rangle_{p \rightarrow 0} \neq 0 \rightarrow \langle \bar{q}q \rangle \neq 0$$

$$\langle R\tilde{R}, R\tilde{R} \rangle_{p \rightarrow 0} \neq 0 ? \rightarrow \langle \bar{\nu}\nu \rangle \neq 0^1$$



¹ Dvali, LF, PRD (2016a)

The model: Neutrino condensation

Pure gravity

Starting point

Non-perturbative topological effects in pure gravity

Assumption

Non-zero topological vacuum susceptibility $\rightarrow \theta$ -term

Consequence ¹

New low-energy gravitational scale Λ_G

Gravity coupled to neutrinos

Anomaly

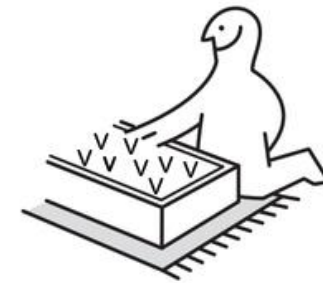
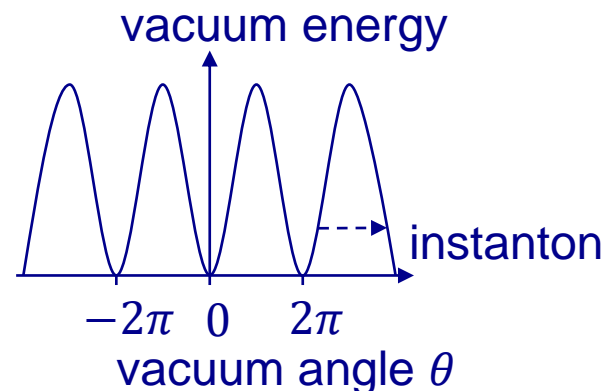
Neutrino flavor symmetry breaking via chiral anomaly

Condensation ¹

Neutrino condensation below scale Λ_G : $\langle \bar{\nu}\nu \rangle \neq 0$

New particles ¹

Emergence of η_ν and 14 massless Goldstones ϕ_k



¹ Dvali, LF, *PRD* (2016a)

The model: Neutrino masses

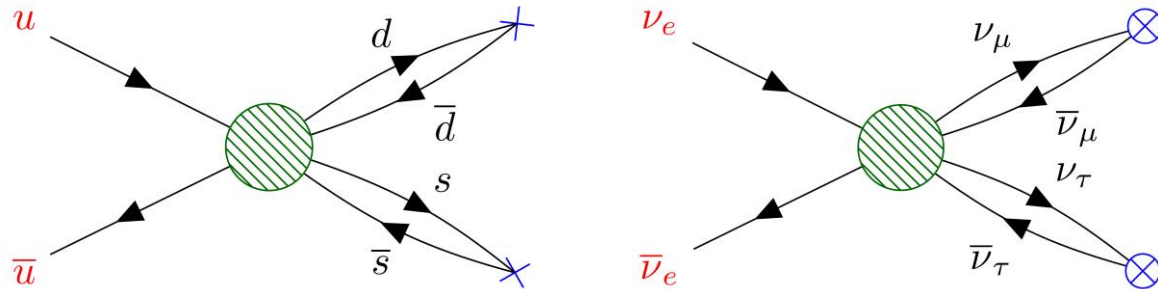
Non-perturbative origin

Effective masses ¹

Generated via non-perturbative coupling to condensate

QCD analogy

Coupling analogous to 't Hooft vertex in QCD ²



Properties

Effective potential ¹

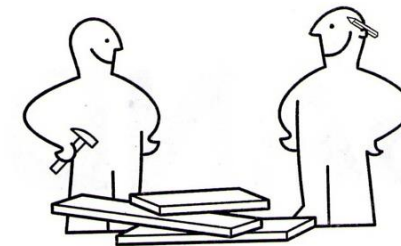
$$V(\hat{X}) = \sum_n \frac{1}{n} c_n \text{Tr} \left[(\hat{X} + \hat{X})^n \right] \text{ with } \hat{X}_{\alpha_L}^{\alpha_R} \equiv \langle \bar{\nu}_{\alpha_L} \nu_{\alpha_R} \rangle$$

Mass hierarchy ¹

$$\hat{X} = \text{diag}(m_1, m_2, m_3) \text{ determined by minimum } \frac{\partial V}{\partial m_i} = 0$$

Dirac vs. Majorana ¹

Model works for both natures: $\langle \bar{\nu}_L \nu_R \rangle$ or $\langle \nu_L^T C \nu_L \rangle$



¹ Dvali, LF, *PRD* (2016a), ² Computation of topological up-quark mass contribution with Lattice QCD: Alexandrou, Finkenrath, LF, et al., *PRL* (2020)

The model: Theory summary

Neutrino mass model

Standard Model

Masses of particles are generated in the early universe

Problem

Neutrino masses: predicted = 0 but measured > 0

Our model ¹

Neutrinos can become massive in the late universe

Key prediction

Neutrino condensation \rightarrow flavor symmetry breaking

¹ Dvali, LF, *PRD* (2016a)

How to constrain this model?

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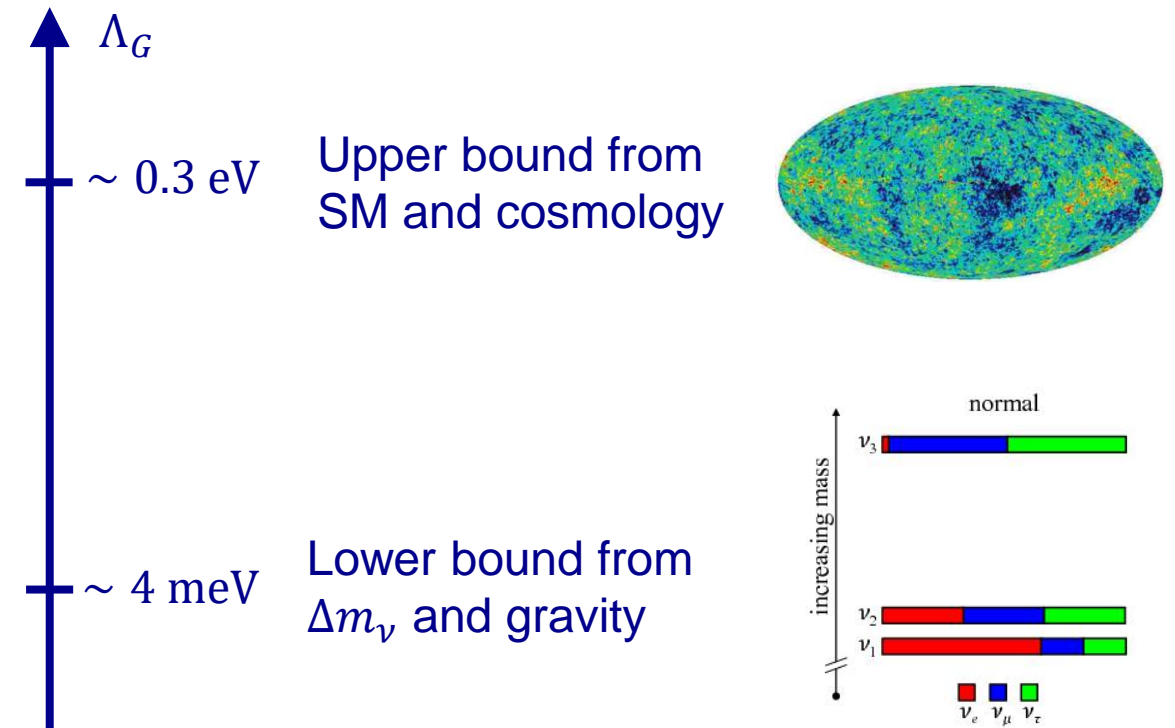
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Constraints

Condensate $|\langle \bar{\nu}\nu \rangle| \sim \text{scale } \Lambda_G^3 \sim \text{temperature } T_{\text{SSB}}^3$



¹ Dvali, LF, *PRD* (2016a)

How to test this model?

Neutrino mass model

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Implications for dark energy

Numerical coincidence ¹

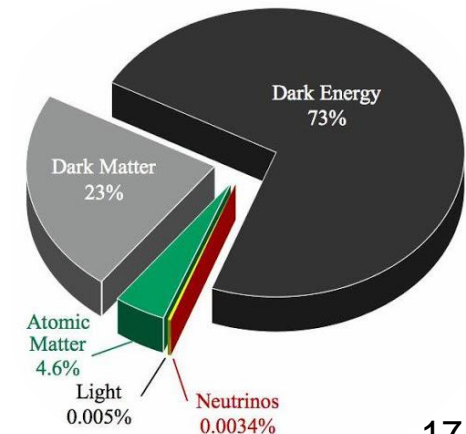
Condensate $\langle \bar{\nu}\nu \rangle$ on dark energy scale, $\rho_{\text{DE}} \sim (\text{meV})^4$
 \rightarrow connected to fundamental new energy scale Λ_G

Cosmological constant? ²

Excluded by S-matrix formulation of quantum gravity

Dynamical dark energy? ³

Predicted time dependence, e.o.s. parameter $w \neq -1$



¹ Dvali, LF, *PRD* (2016a);

² Dvali, Gomez, *JCAP* (2014); ³ Dvali, Freche, LF, *manuscript in preparation*

How to test this model?

Neutrino mass model

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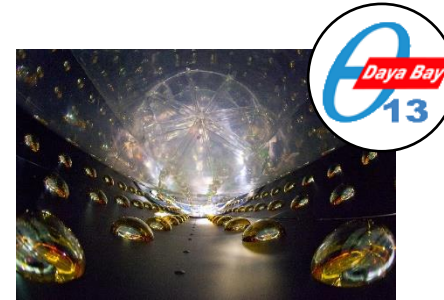
Neutrinos can become massive in the late universe

Key prediction

Neutrino condensation \rightarrow flavor symmetry breaking

Predictions for cosmic neutrinos

Topological defects emerge from phase transition ²



Cosmic neutrinos disappear after phase transition ^{1,3}

\rightarrow no mass detection at

only at



¹ Dvali, LF, *PRD* (2016a);

² Dvali, LF, Vachaspati, *PRL* (2023); ³ Lorenz, LF, et al., *PRD* (2019), (2021); ongoing work with Brinckmann (Euclid Collaboration)

How to test this model?

Neutrino mass model

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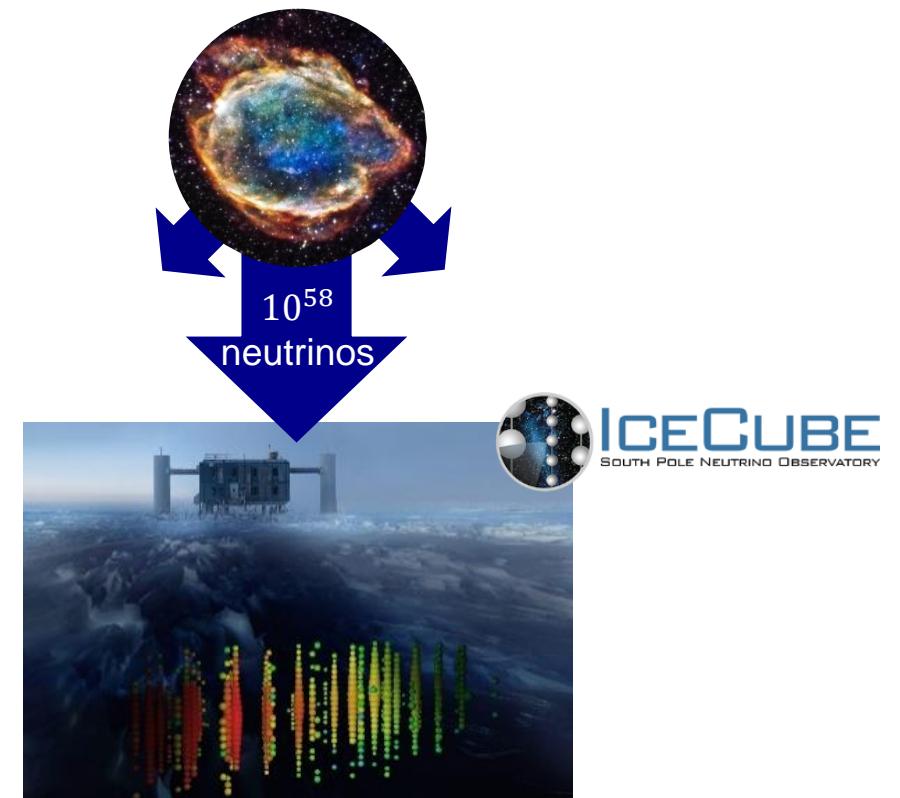
Key prediction

Neutrino condensation \rightarrow flavor symmetry breaking

Predictions for astrophysical neutrinos

Heavier neutrinos decay into lightest: ¹ $\nu_i \rightarrow \phi_k + \nu_j$ or $\bar{\nu}_j$

Discover: neutrino = or \neq antineutrino? ²



¹ Dvali, LF, *PRD* (2016a);

² LF, Raffelt, Vitagliano, *PRD* (2020)

How to test this model?

Neutrino mass model

Standard Model

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Problem

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Our model ¹

Neutrinos can become massive in the late universe

Key prediction

Neutrino condensation \rightarrow flavor symmetry breaking

Predictions for axion-search experiments

Standard Model

Weak force distinguishes matter from antimatter

Problem

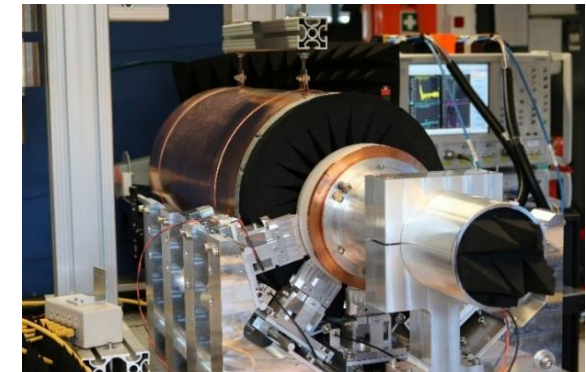
Strong force doesn't! Need new particle: axion?

Our model ¹

New axion-like particles η_ν and $\phi_k \rightarrow$ testable at ...



... ALPS II experiment ²



... MADMAX experiment? ³

¹ Dvali, LF, *PRD* (2016a);

² Dvali, LF (2016b); ³ ongoing discussions with Dvali, Zhang, et al.

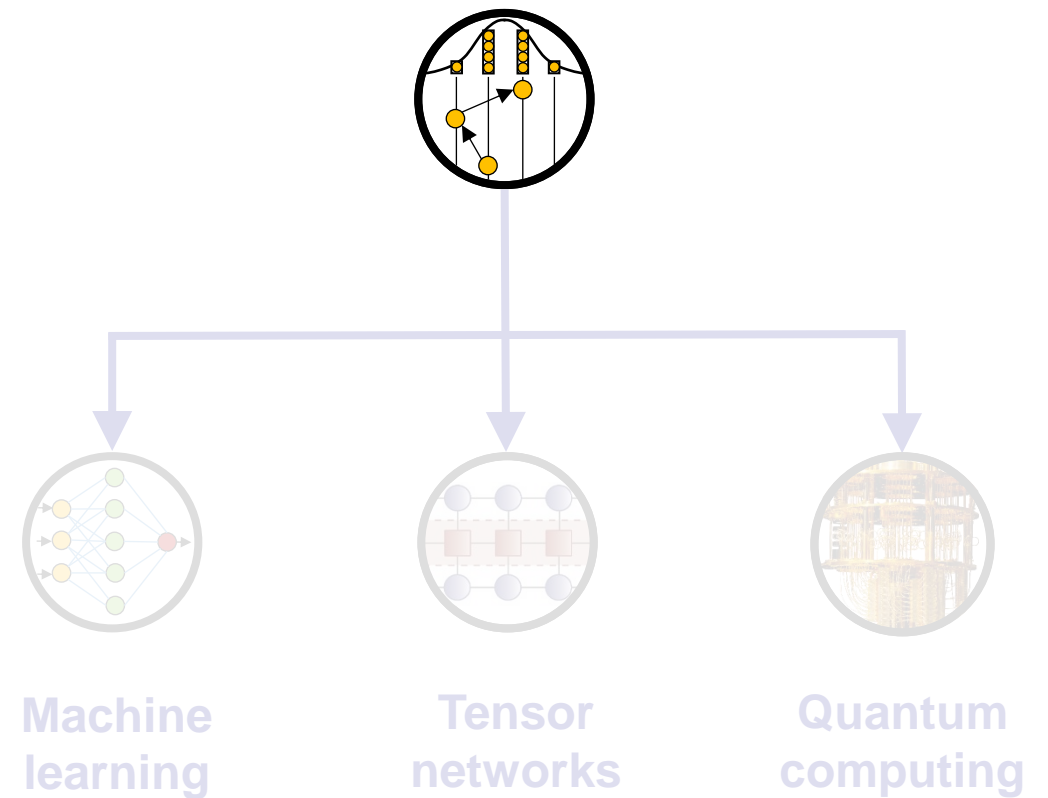
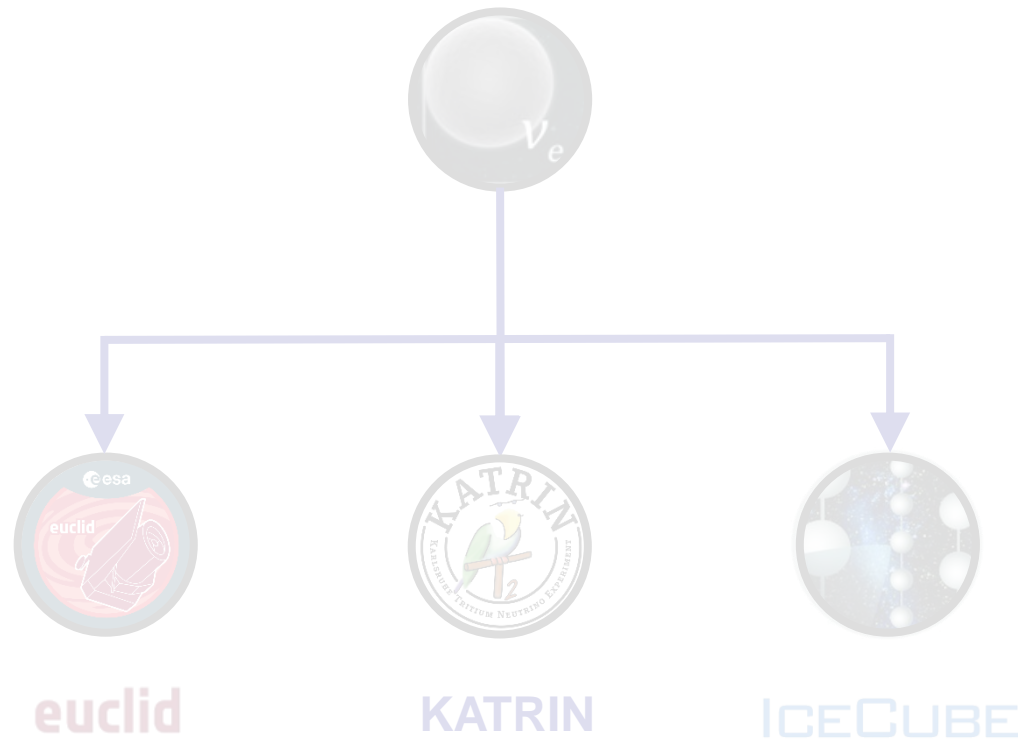
New models and methods for particle physics

Build new models

Develop new methods

Standard Model of particle physics
Successful but incomplete

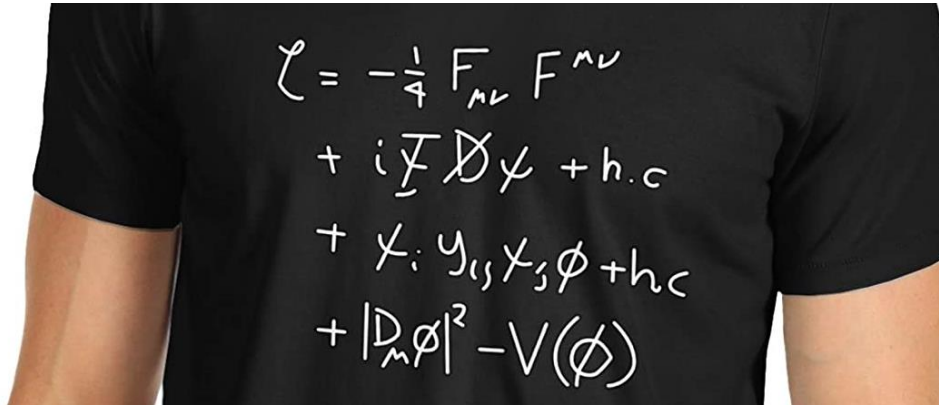
Markov Chain Monte Carlo (MCMC)
Powerful but limited



Why do we need numerical methods?

\int

Integrate



$dF d\psi d\phi$

over forces (F), matter (ψ), Higgs field (ϕ)

Too complex:
no exact computation!



Way out:
approximation!



Which methods do we currently use?

Particle physics

Markov Chain Monte Carlo (MCMC) method

“Lattice” QCD: quarks and gluons on spacetime grid

Our work¹

Falsified $m_u = 0$ solution to strong CP problem → axion

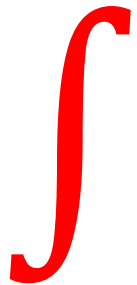
Cosmology

MCMC method

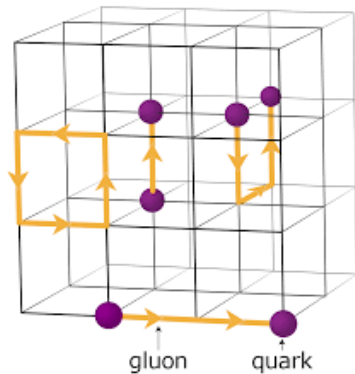
Cosmological parameter estimation: age of Universe, ...

Our work²

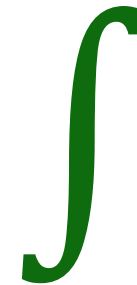
Studied time-dependent cosmological neutrino masses



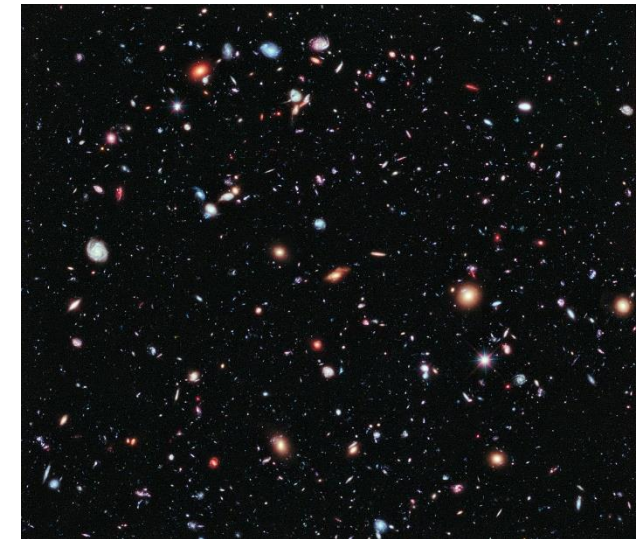
Integrate



common methods for
particle physics, cosmology,
condensed matter physics,
chemistry, biology, ...



Integrate



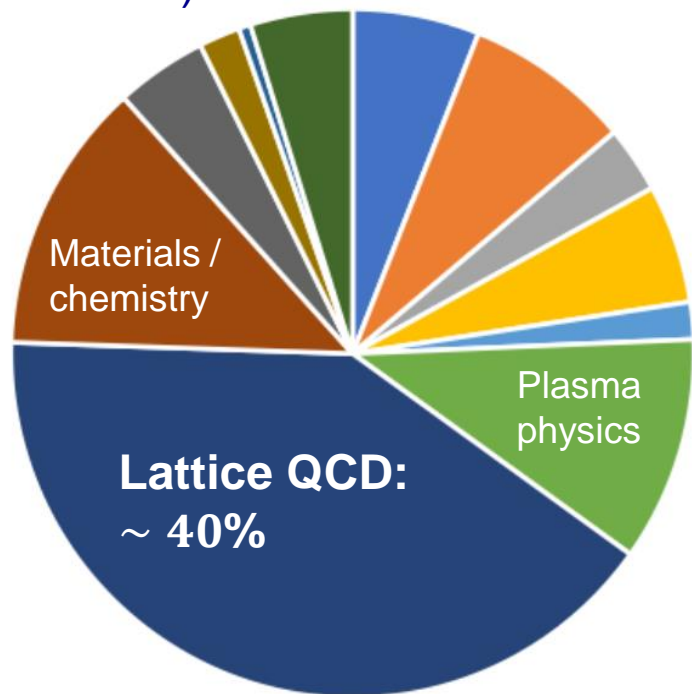
¹ Alexandrou, Finkenrath, LF, et al., *PRL* (2020); ² Lorenz, LF, et al., *PRD* (2019), (2021), ongoing work with Brinckmann (Euclid Collaboration)

Why do we need new methods?

Computational costs of MCMC

E.g. “Lattice QCD”:
dominant supercomputer
usage (INCITE 2019)

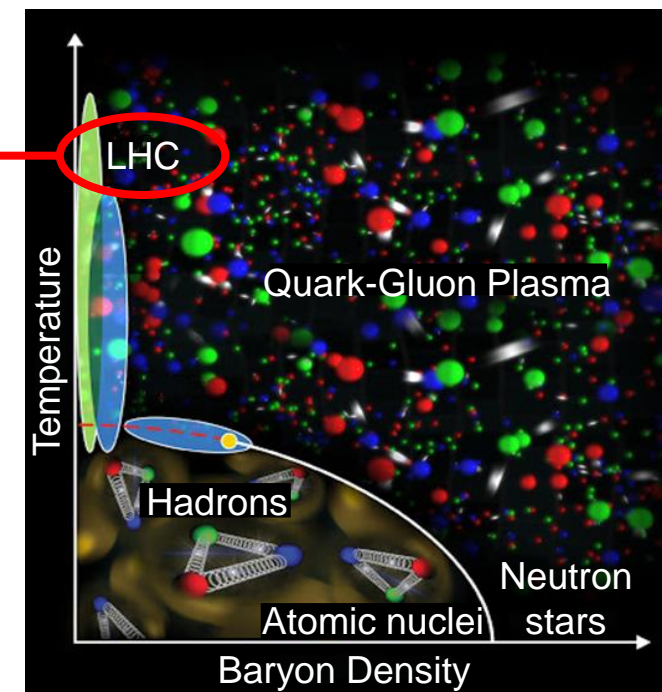
→ *machine learning*¹



Computational challenges of MCMC

Cannot directly compute
free energy, entropy, ...

→ *machine learning*¹



¹ White Paper: Boyda, Cali, Foreman, LF, et al. (2022); Nicoli, Anders, LF, et al., *PRL* (2021); ...

² LF, et al., *PRD* (2023); LF et al., *PRD* (2020); Nakayama, LF, et al., *PRD* (2022); ...

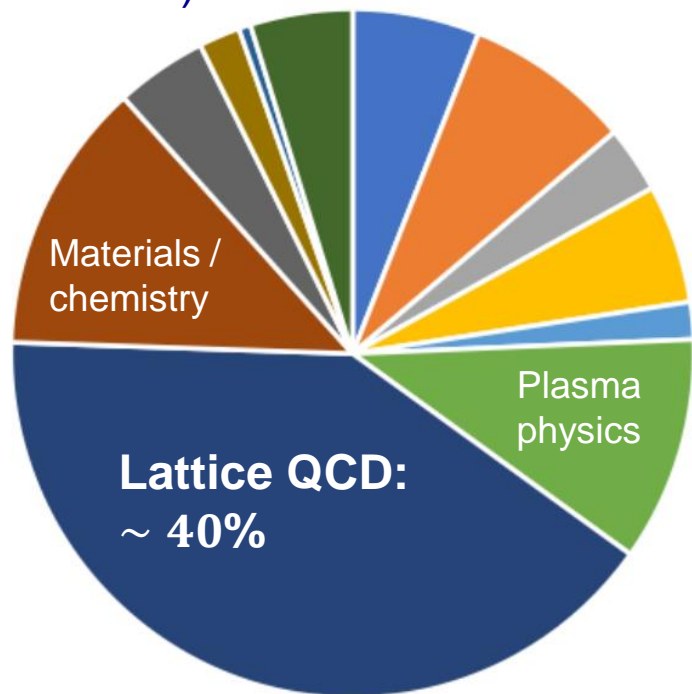
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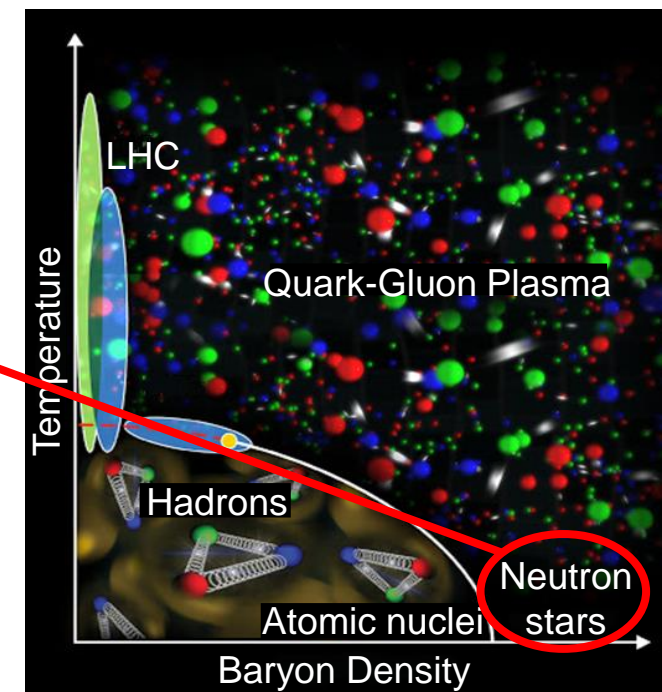
Computational challenges of MCMC

Cannot directly compute
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→ *machine learning*¹

Cannot simulate large θ -
term, chemical potential, ...

→ *tensor networks*²



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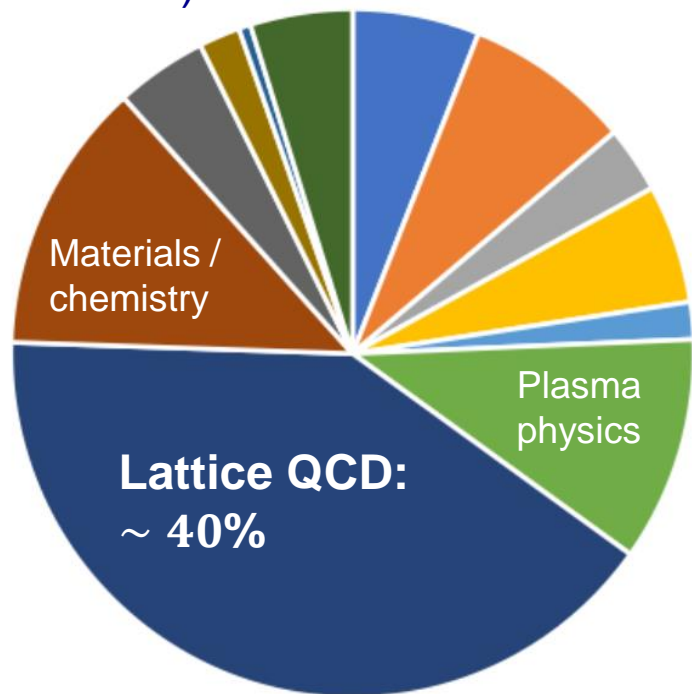
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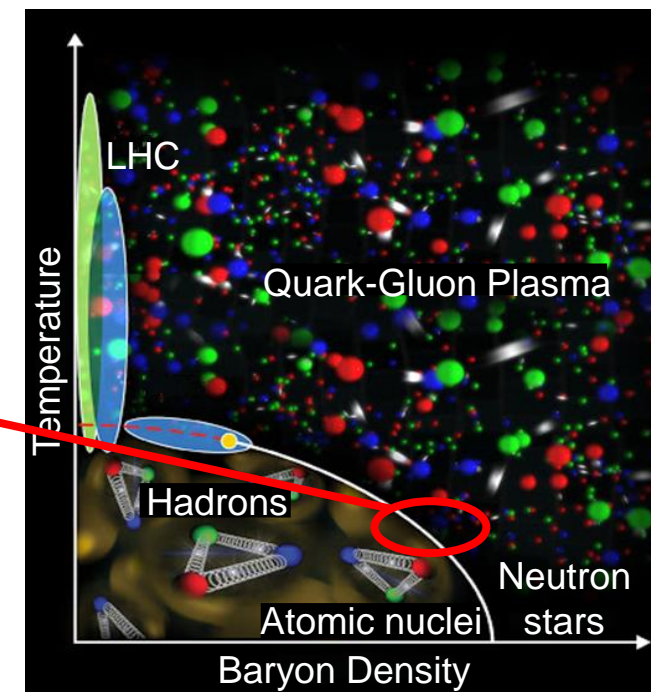
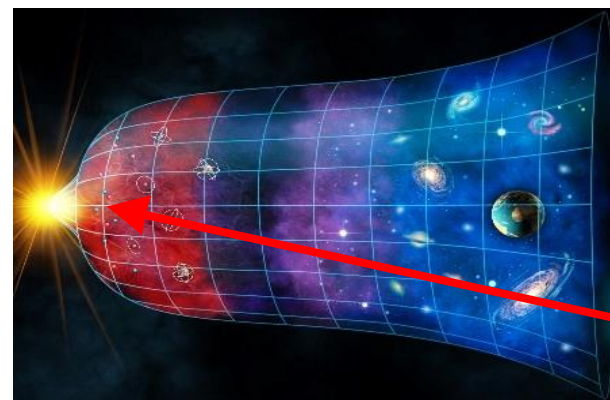
→ *machine learning*¹

Cannot simulate large θ -
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→ *tensor networks*²

Cannot simulate out-of-
equilibrium dynamics, ...

→ *quantum computing*³



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² LF, et al., *PRD* (2023); LF et al., *PRD* (2020); Nakayama, LF, et al., *PRD* (2022); ...

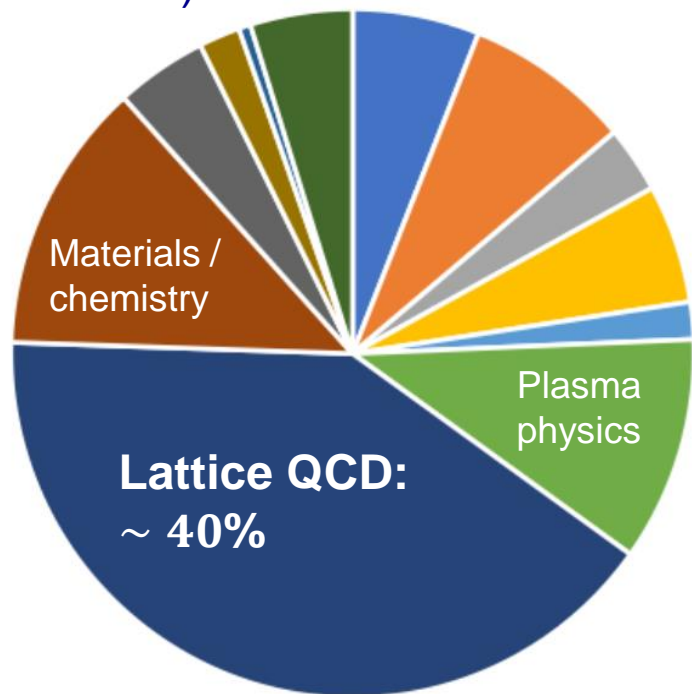
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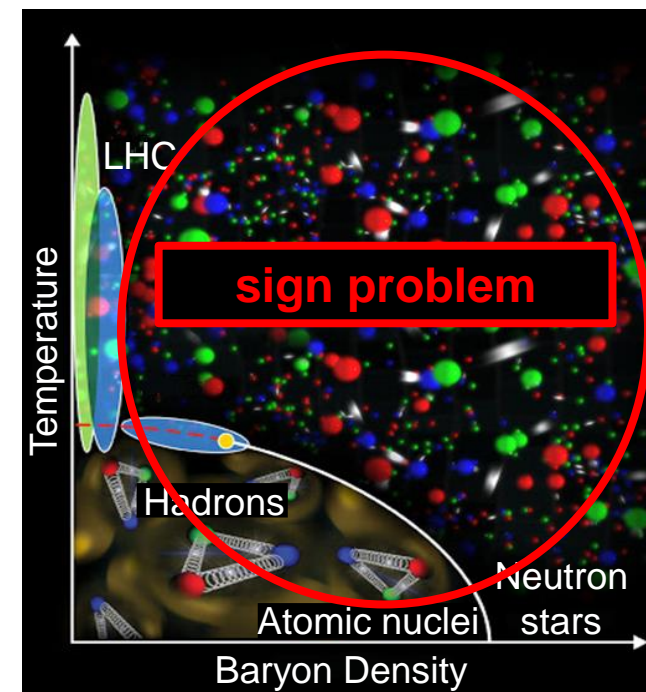
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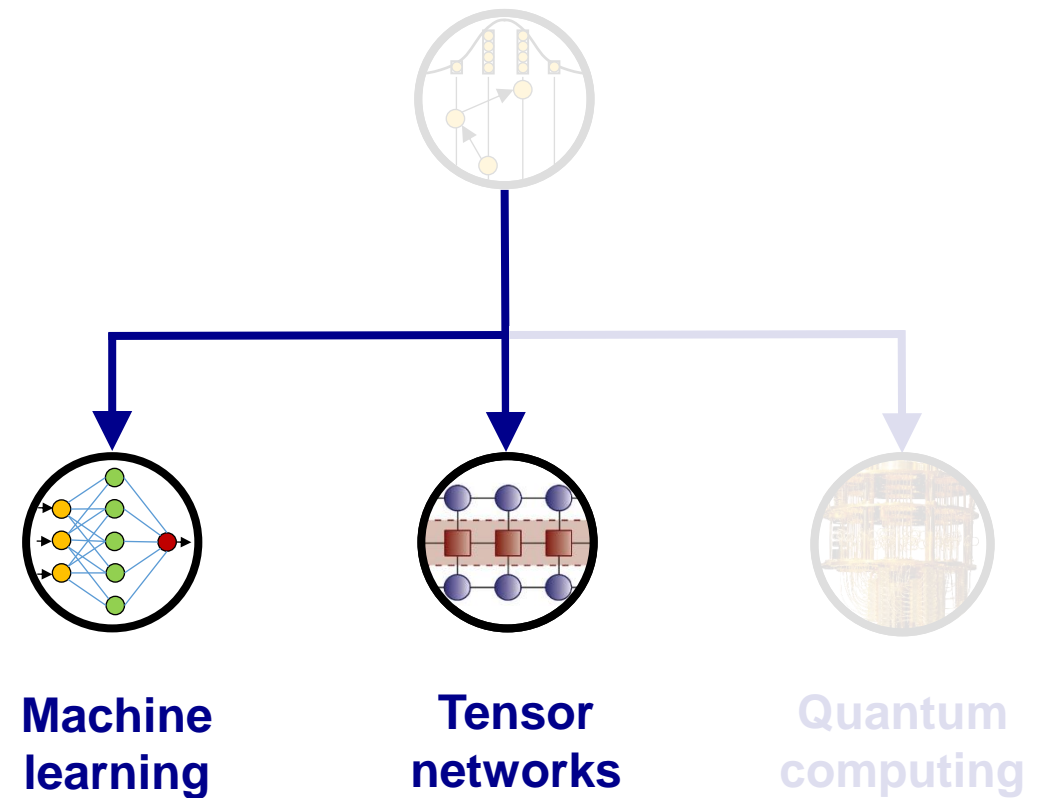
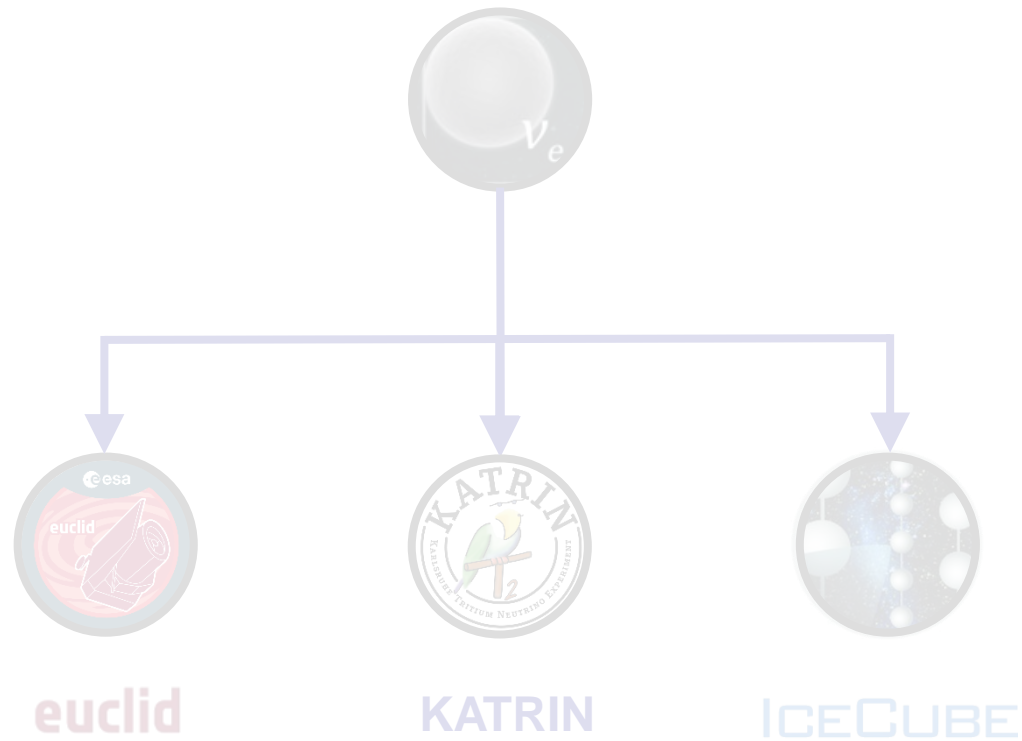
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How to tackle MCMC challenges with new methods?

Standard method: MCMC for Lattice QCD

Concept

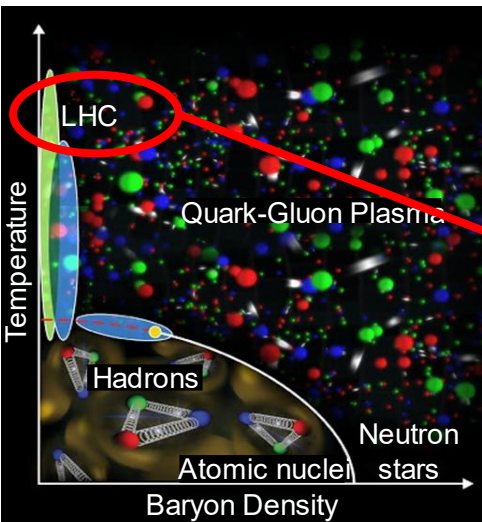
Compute observables: $\langle O \rangle = \frac{1}{Z} \int D\phi e^{-S(\phi)} O(\phi)$

Sample: $\langle O \rangle \approx \frac{1}{N} \sum O(\phi_i)$, where $\phi_i \sim p(\phi) = \frac{1}{Z} e^{-S(\phi)}$

Problem

Sequential, correlated sampling of $\phi_i \rightarrow$ slow and costly

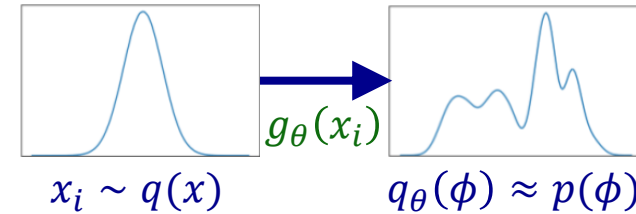
No *direct* computation of free energy \rightarrow large errors



New method: machine learning

Concept

Train **deep neural network**:



Results

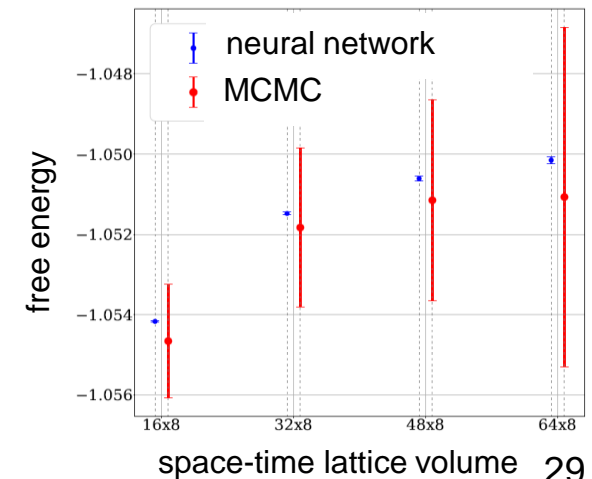
Parallel, uncorrelated sampling of $x_i \rightarrow$ get $\phi_i = g_\theta(x_i)$

Direct computation of free energy in 1+1D Higgs model ¹

Future

Observables in
2+1D ² & 3+1D ³

¹ Nicoli, Anders, LF, et al., *PRL* (2021), *PoS Lattice* (2022), *PoS Lattice* (2024);
² Ongoing work with Nicoli, Schuh, et al.; development of software package NeuLat;
³ White Paper: Boyda, Cali, Foreman, LF, et al. (2022)



How to tackle MCMC challenges with new methods?

Standard method: MCMC for Lattice QCD

Concept

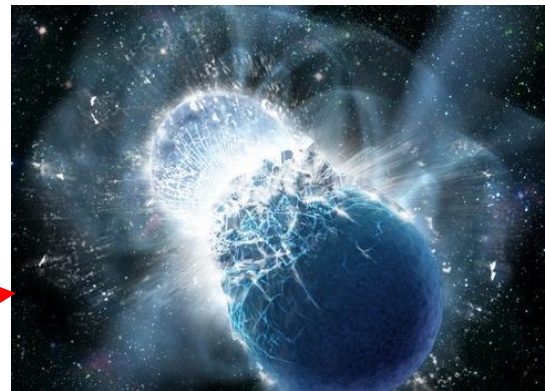
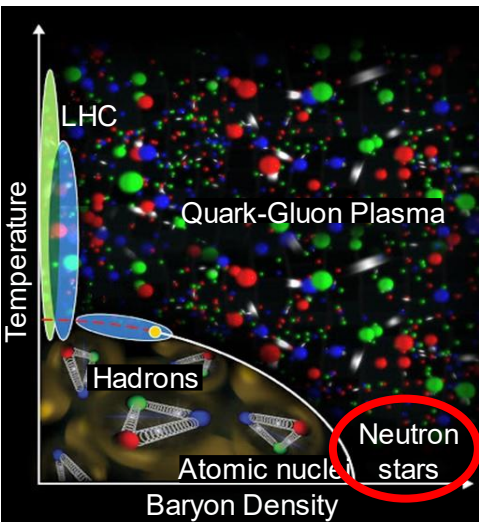
Compute observables: $\langle O \rangle = \frac{1}{Z} \int D\phi e^{-S(\phi)} O(\phi)$

Sample: $\langle O \rangle \approx \frac{1}{N} \sum O(\phi_i)$, where $\phi_i \sim p(\phi) = \frac{1}{Z} e^{-S(\phi)}$

Problem

Complex action for θ -term and chemical potential μ

→ “sign problem” → no simulations for large θ or μ



New method: tensor networks

Concept

Compute observables: $\langle O \rangle = \langle \psi | O | \psi \rangle$, approximate $|\psi\rangle$

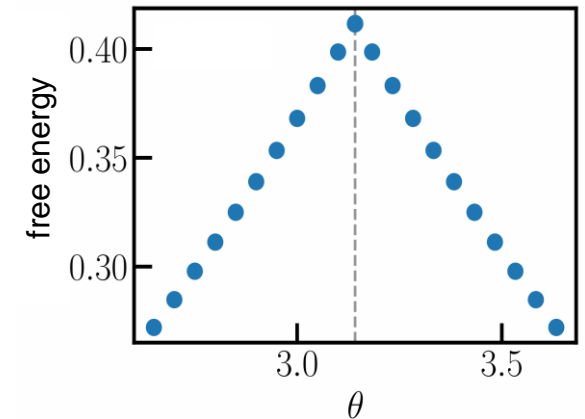
E.g.: $|\psi\rangle = \sum c_{i_1 \dots i_n} |i_1\rangle \dots |i_n\rangle \approx \sum A_{i_1}^1 \dots A_{i_n}^n |i_1\rangle \dots |i_n\rangle$

Results

Simulations of phase transitions for large θ or μ in 1+1D¹

Future

Phase transitions in 2+1D and 3+1D²



¹ LF, et al., *PRD* (2020); Nakayama, LF, et al., *PRD* (2022); LF, et al., *PRD* (2023);

² Kühn, Gerken, LF, et al., *PRB* (2023); Crippa, Romiti, LF, et al. (2024);

Crane, et int., LF, et al. (2024); ongoing work with Diamantini, et al.

What are the prospects and challenges of new methods?

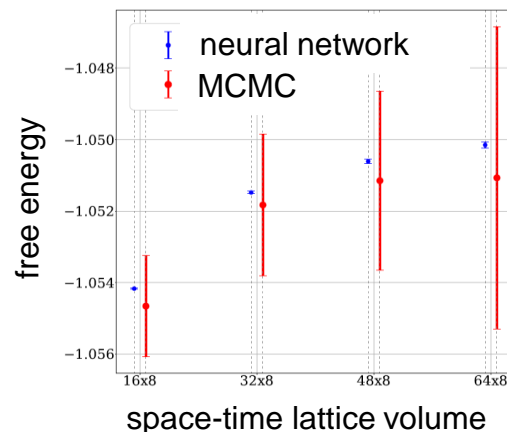
New method: machine learning

Prospects

- ✓ Direct computation of free energy, entropy, ... ¹
- ✗ Mitigate sign problem ²

Challenges

- ✗ Mode collapse ³
- ✗ Focus on 1+1D, first ansatzes in 2+1D & 3+1D
→ roadmap to QCD ⁴



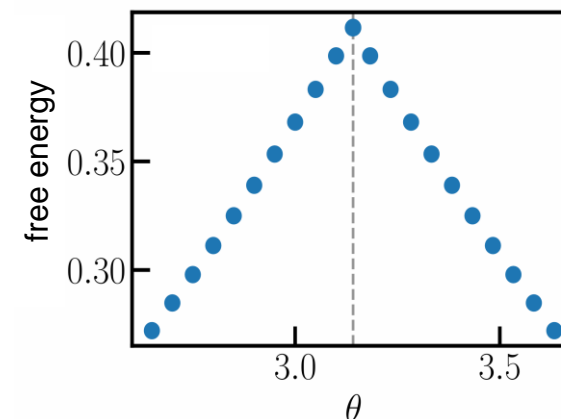
New method: tensor networks

Prospects

- ✓ Direct computation of free energy, entropy, ... ⁵
- ✓ Evade sign problem ⁵

Challenges

- ✗ Approximation inefficient for highly entangled states
- ✗ Focus on 1+1D, first ansatzes in 2+1D & 3+1D ⁶
→ competition with quantum computing ⁷



¹ Nicoli, Anders, LF, et al., *PRL* (2021), *PoS Lattice* (2024); ² Ongoing work with Nicoli, Schuh, et al., ³ Nicoli, Anders, LF, et al., *PoS Lattice* (2022); ⁴ Boyda, Cali, Foreman, LF, et al. (2022); ⁵ LF, et al., *PRD* (2020); Nakayama, LF, et al., *PRD* (2022); LF, et al., *PRD* (2023); ⁶ Crippa, Romiti, LF, et al. (2024); Avkhadiev, LF, et al. (2024); ⁷ review: LF, et al., *PoS Lattice* (2023)

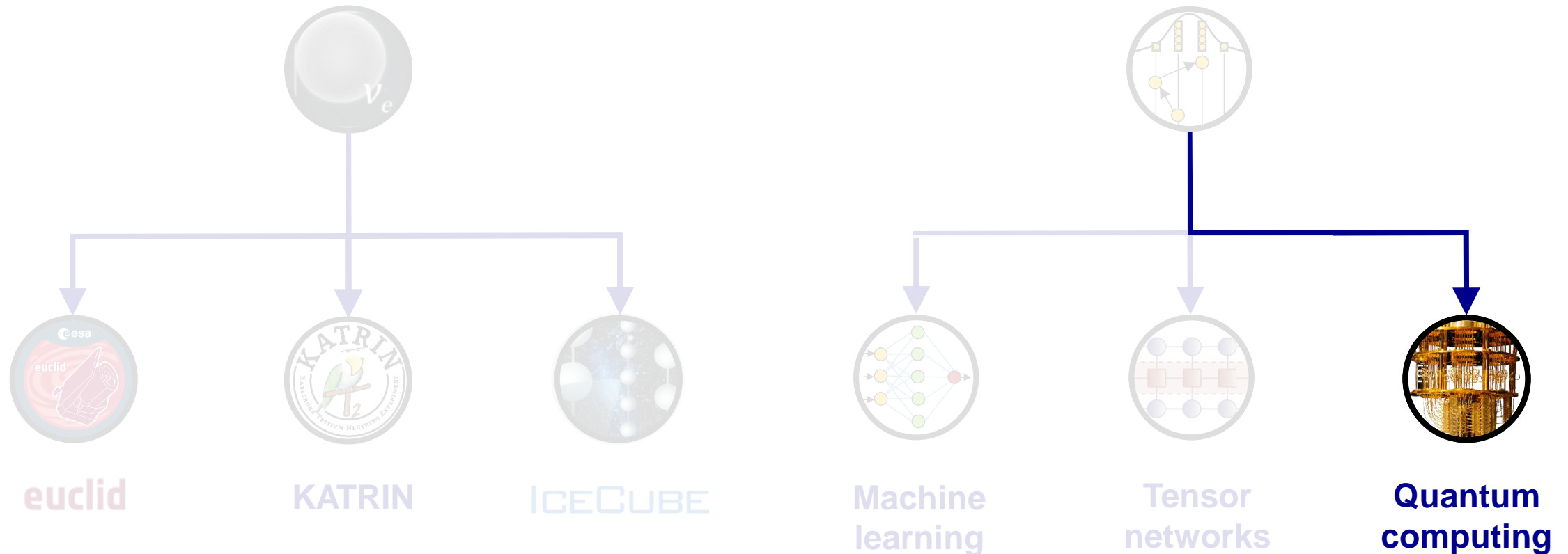
New models and methods for particle physics

Build new models

Develop new methods

Standard Model of particle physics
Successful but incomplete

Markov Chain Monte Carlo (MCMC)
Powerful but limited



How to tackle MCMC challenges with new methods?

Standard method: MCMC for Lattice QCD

Concept

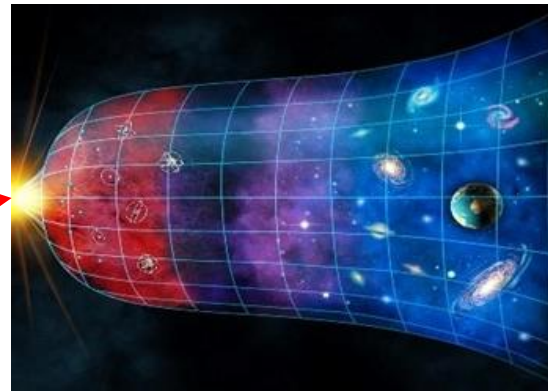
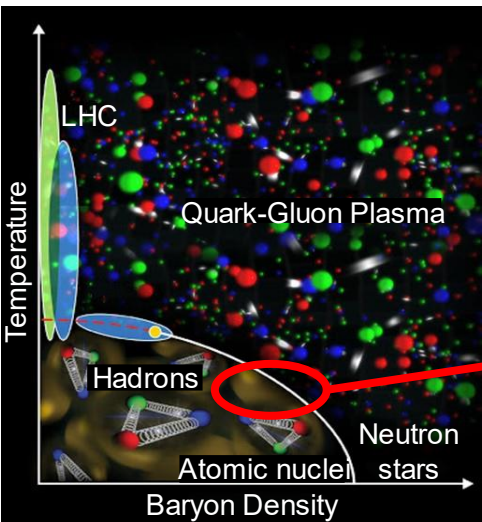
Compute observables: $\langle O \rangle = \frac{1}{Z} \int D\phi e^{-S(\phi)} O(\phi)$

Sample: $\langle O \rangle \approx \frac{1}{N} \sum O(\phi_i)$, where $\phi_i \sim p(\phi) = \frac{1}{Z} e^{-S(\phi)}$

Problem

Euclidean action $S(\tau = it) \rightarrow$ no real-time evolution

\rightarrow can be exponentially hard for tensor networks



New method: quantum algorithms

Concept

Compute $|\psi(t)\rangle = e^{-iHt} |\psi(0)\rangle$, encode 2^n basis states

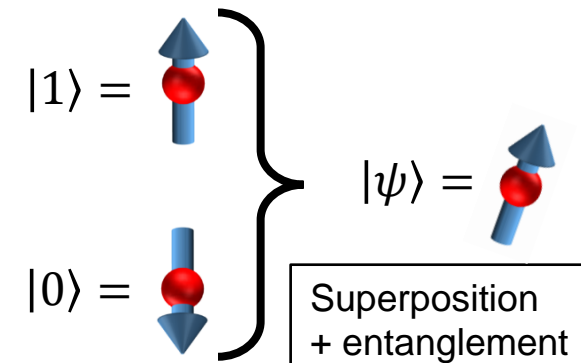
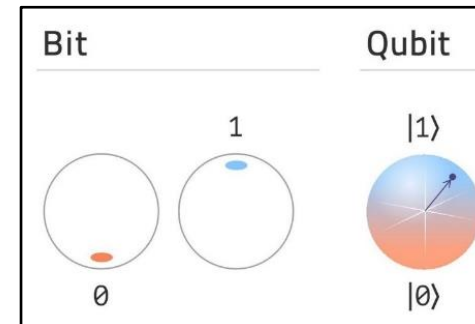
First step

Focus on ground-state preparation: $\min_{\alpha} E_{\alpha} = \langle \psi_{\alpha} | \mathcal{H} | \psi_{\alpha} \rangle$

Hybrid quantum-classical algorithms

Classical optimization of quantum gate parameters α

\rightarrow use machine learning ¹



¹ Nicoli, Anders, LF, et al., *NeurIPS* (2023), Anders, et int., LF, et al., *ICML* (2024)

Quantum Computing for High-Energy Physics

State of the Art and Challenges

Summary of the QC4HEP Working Group

Alberto Di Meglio,^{1, *} Karl Jansen,^{2, 3, †} Ivano Tavernelli,^{4, ‡} Constantia Alexandrou,^{5, 3} Srinivasan Arunachalam,⁶ Christian W. Bauer,⁷ Kerstin Borrás,^{8, 9} Stefano Carrazza,^{10, 1} Arianna Crippa,^{2, 11} Vincent Croft,¹² Roland de Putter,⁶ Andrea Delgado,¹³ Vedran Dunjko,¹² Daniel J. Egger,⁴ Elias Fernández-Combarro,¹⁴ Elina Fuchs,^{1, 15, 16} Lena Funcke,¹⁷ Daniel González-Cuadra,^{18, 19} Michele Grossi,¹ Jad C. Halimeh,^{20, 21} Zoë Holmes,²² Stefan Kühn,² Denis Lacroix,²³ Randy Lewis,²⁴ Donatella Lucchesi,^{25, 26, 1} Miriam Lucio Martinez,^{27, 28} Federico Meloni,⁸ Antonio Mezzacapo,⁶ Simone Montangero,^{25, 26} Lento Nagano,²⁹ Voica Radescu,³⁰ Enrique Rico Ortega,^{31, 32, 33, 34} Alessandro Roggero,^{35, 36} Julian Schuhmacher,⁴ Joao Seixas,^{37, 38, 39} Pietro Silvi,^{25, 26} Panagiotis Spentzouris,⁴⁰ Francesco Tacchino,⁴ Kristan Temme,⁶ Koji Terashi,²⁹ Jordi Tura,^{12, 41} Cenk Tüysüz,^{2, 11} Sofia Vallecorsa,¹ Uwe-Jens Wiese,⁴² Shinjae Yoo,⁴³ and Jinglei Zhang^{44, 45}

Quantum computers offer an intriguing path for a paradigmatic change of computing in the natural sciences and beyond, with the potential for achieving a so-called quantum advantage—namely, a significant (in some cases exponential) speedup of numerical simulations. The rapid development of hardware devices with various realizations of qubits enables the execution of small-scale but representative applications on quantum computers. In particular, the high-energy physics community plays a pivotal role in accessing the power of quantum computing, since the field is a driving source for challenging computational problems. This concerns, on the theoretical side, the exploration of models that are very hard or even impossible to address with classical techniques and, on the experimental side, the enormous data challenge of newly emerging experiments, such as the upgrade of the Large Hadron Collider. In this Roadmap paper, led by CERN, DESY, and IBM, we provide the status of high-energy physics quantum computations and give examples of theoretical and experimental target benchmark applications, which can be addressed in the near future. Having in mind hardware with about 100 qubits capable of executing several thousand two-qubit gates, where possible, we also provide resource estimates for the examples given using error-mitigated quantum computing. The ultimate declared goal of this task force is therefore to trigger further research in the high-energy physics community to develop interesting use cases for demonstrations on near-term quantum computers.

How can we quantum simulate* lattice field theories?

Overview

Current technology

$\mathcal{O}(100 - 1000)$ noisy qubits with error mitigation

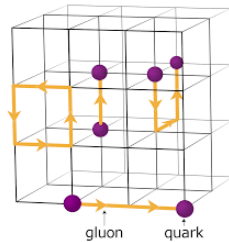
State of the art

First quantum simulations of 1+1D gauge theories ¹

Next steps

Efficient lattice fermion implementations ²

Hybrid MCMC-quantum simulations of gauge theories ³



* Note: quantum simulate or tensor-network-approximate

¹ Reviews: LF, et al., *PoS Lattice* (2023); Di Meglio, et int., LF, et al. (QC4HEP Working Group), *PRX Quantum* (2023); ² Angelides, LF, et al., *PRD* (2023); ³ Crippa, Romiti, LF, et al. (2024); Avkhadiyev, LF, et al. (2024); ⁴ Crane, et int., LF, et al. (2024); ⁵ ongoing work with Halimeh et al.; ⁶ Peng, Diamantini, LF, et al., (2024); ⁷ Schuster, Kühn, LF, et al., *PRD* (2024); ...

Sign-problem-afflicted regimes

Topological terms

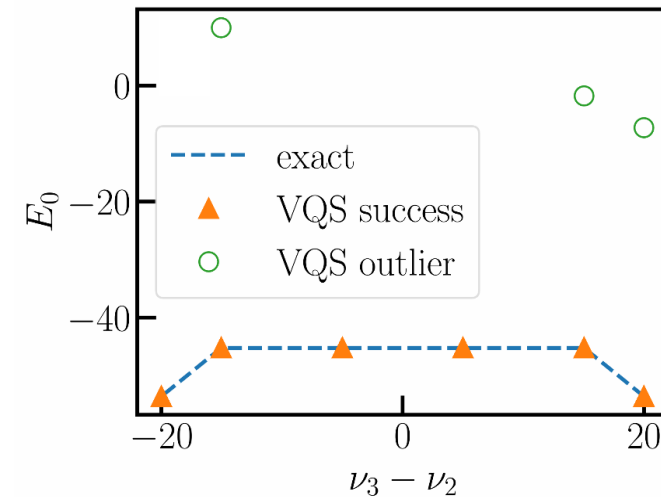
1+1D gauge theories with θ -term ⁴ and dynamical axion ⁵

2+1D gauge theories with Chern-Simons term ⁶



Chemical potentials

1+1D gauge theories with chemical potentials ν_f ⁷



Outlook: how can we address the sign problem in 3+1D?

Example: U(1) lattice gauge theory with θ -term

First classical results for a single cube

Goal

Study phase transition at $\theta = \pi$ and large $g = \beta^{-1/2}$

Theoretical requirements

Derive 3+1D θ -term in Hamiltonian lattice formulation ¹

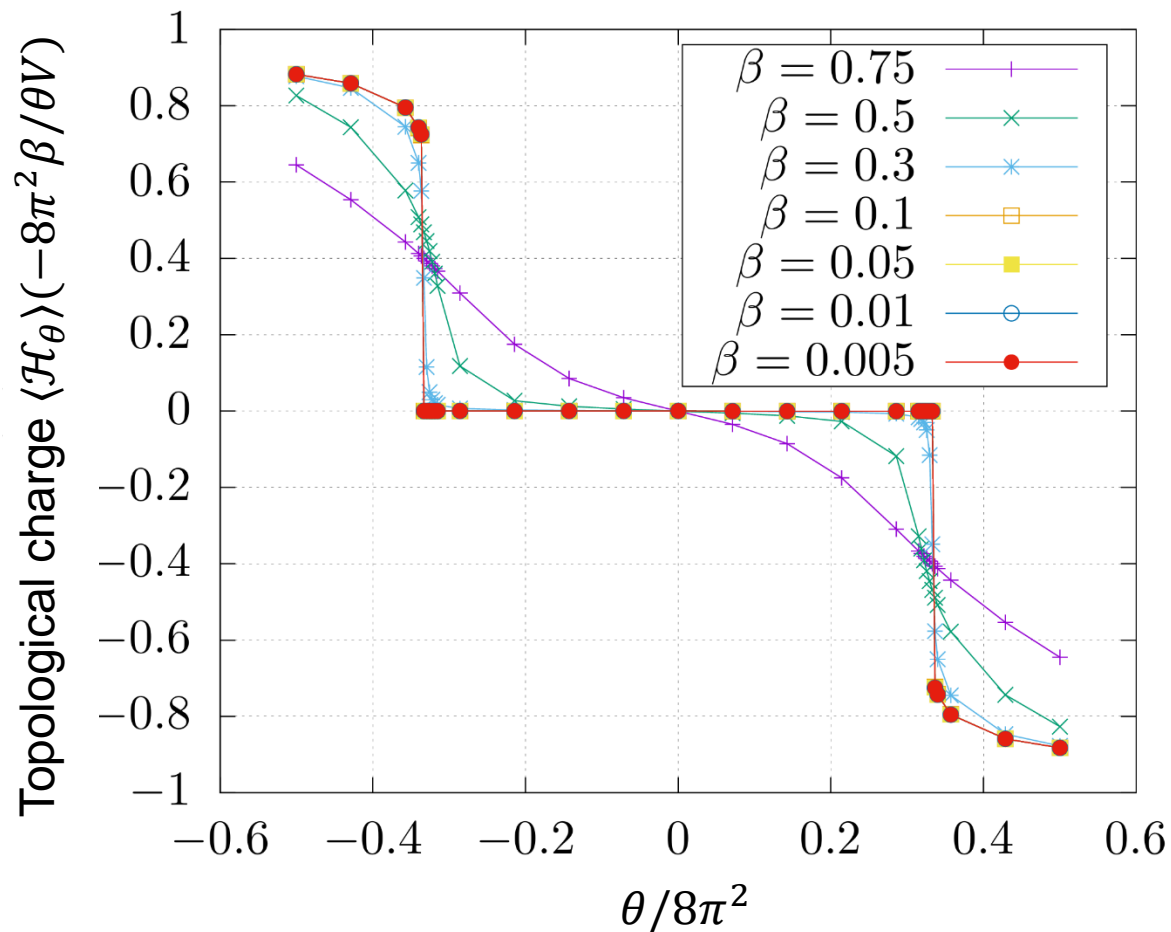
Develop quantum algorithms for 1+1D,² 2+1D,³ and 3+1D

First classical computations

Study phase transition with exact diagonalization ¹ 

Future work

Larger volumes: tensor-network & quantum computations



¹ Kan, LF, et al., *PRD* (2021);

² LF, et al., *PoS Lattice* (2023); Angelides, LF, et al., *PRD* (2023); Schuster, Kühn, LF, et al., *PRD* (2023); Avkhadiev, LF, et al. (2024);

³ Crippa, Romiti, LF, et al. (2024); Crane, et int., LF, et al. (2024); ...

Outlook: the future of quantum computing

The path to go...

State of the art *

First quantum simulations of 1+1D lattice theories ¹

Noise mitigation, ² circuit optimization, ³ new algorithms ⁴

Future goals *

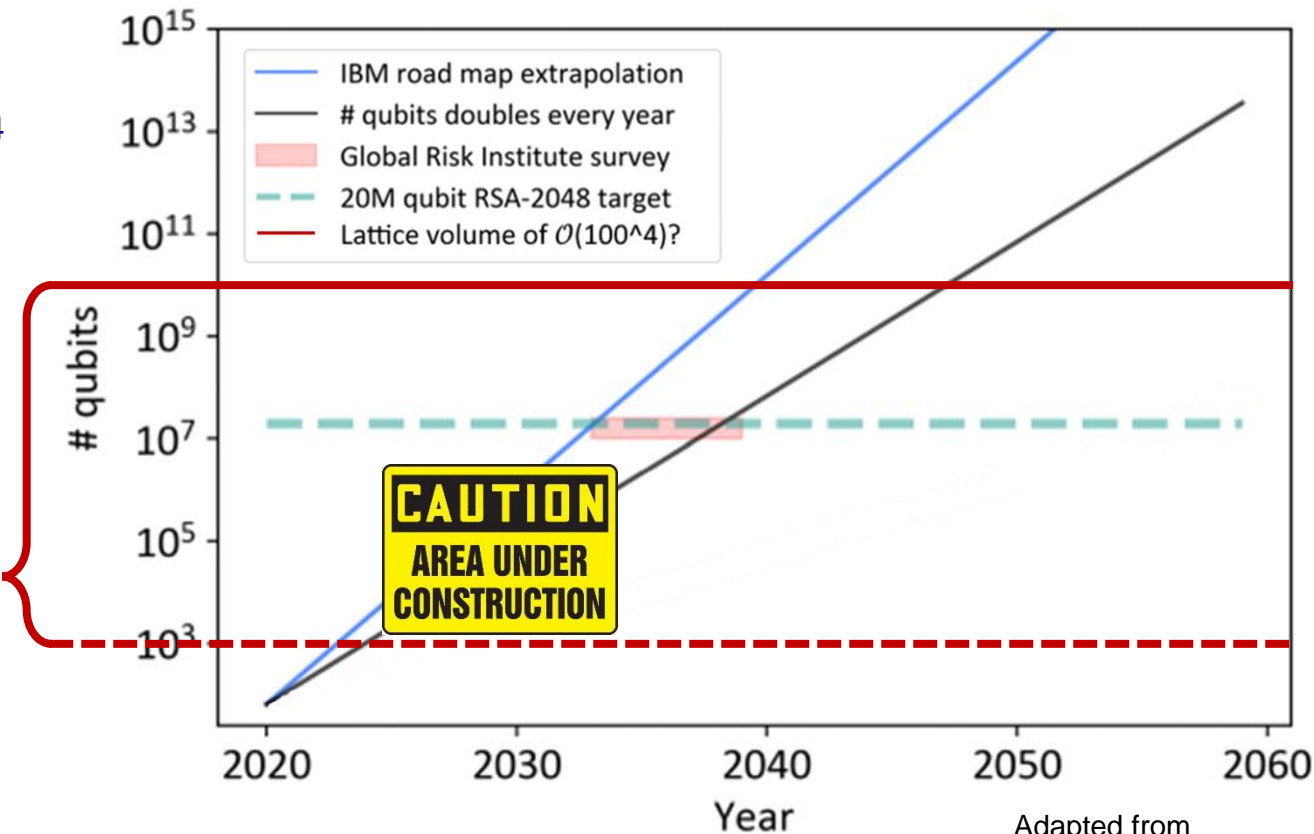
Quantum simulations for 2+1D & 3+1D theories

To evade sign problem, ... of Lattice QCD and beyond

Analogous to
Lattice QCD from
1980s to 2020s?

* Focus on algorithms: usable also for tensor networks

A rough sketch...



Adapted from
Groenland (2024)

¹ Reviews: LF, et al., *PoS Lattice* (2023); Di Meglio, et int., LF, et al. (QC4HEP Working Group), *PRX Quantum* (2023);

² LF, et al., *PRA* (2022), ..., ³ LF, et al., *Quantum* (2021), LF, et al., *IEEE ICWS* (2021), ..., ⁴ Angelides, LF, et al., *PRD* (2023); Crippa, Romiti, LF, et al. (2024); ...

Summary: new models and methods for particle physics

New models

State of the art

Low-energy avenue of model building: ¹ $m_\nu, \rho_{DE}, \phi_k, \dots$

Future goals

Further developing and testing new low-energy models

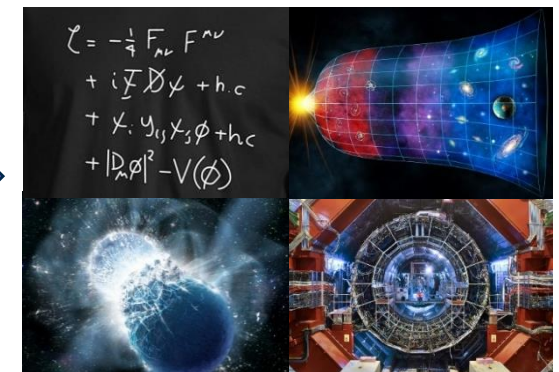
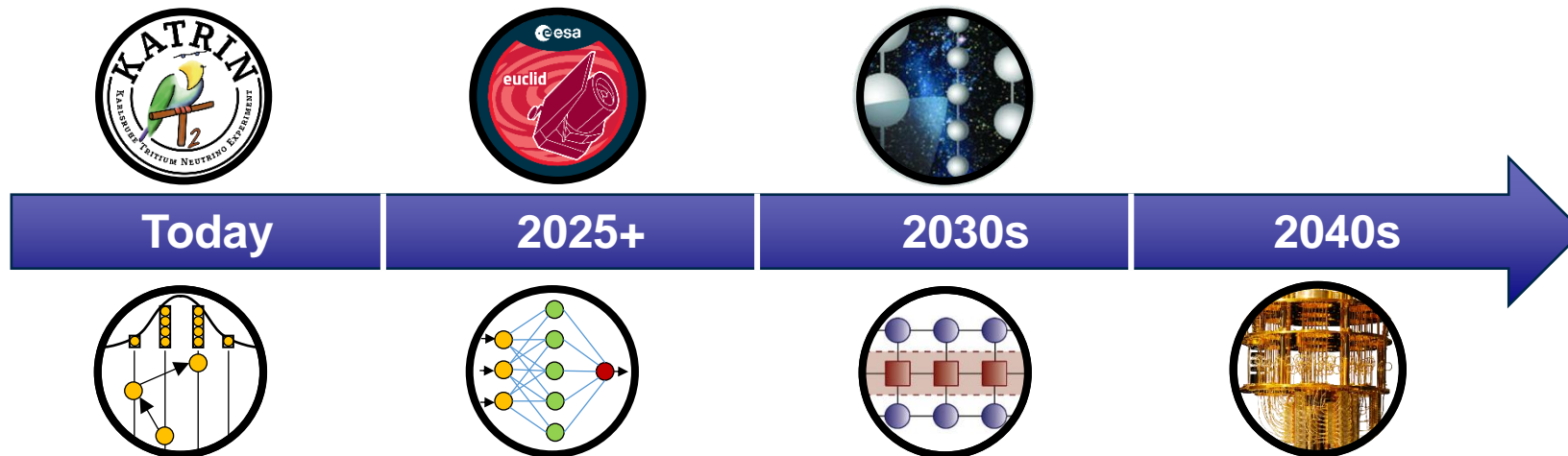
New methods

State of the art

Testing (B)SM physics with MCMC, ² new methods ³

Future goals

Application of new methods to (B)SM phenomena



¹ Dvali, LF, *PRD* (2016a); (2016b); Lorenz, LF, et al., *PRD* (2019); LF, Raffelt, Vitagliano, *PRD* (2020); Dvali, LF, Vachaspati, *PRL* (2023); Dvali, Freche, LF, *manuscript in prep.*;

² Lorenz, LF, et al., *PRD* (2021); Alexandrou, Finkenrath, LF, et al., *PRL* (2020); ³ LF, et al., *Quantum* (2021), LF, et al., *PRA* (2022), LF, et al., *PRD* (2023); Avkhadiev, LF, et al. (2024); ... 38

Thanks to my collaborators



Gia Dvali
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(MPP)



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(DESY)



Phiala Shanahan
(MIT)



Jesse Thaler
(MIT)



Christine Muschik
(Perimeter Inst.)



Tanmay Vachaspati
(Arizona State U.)



Philipp Stratmann
(Intel Munich)



Ivano Tavernelli
(IBM Zurich)



Stefan Kühn
(DESY)



Carsten Urbach
(Bonn U.)



Sofia Vallecorsa
(CERN)



Erminia Calabrese
(Cardiff U.)



Steven Girvin
(Yale U.)

and many more...

Special thanks

... to my research group:



... for support and funding:



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MATTER AND LIGHT FOR
QUANTUM COMPUTING



Bethe Center for
Theoretical Physics



... for computing time:



Thanks to you for listening! Any questions on ... ?

New models

New methods

Standard Model of particle physics
Successful but incomplete

Markov chain Monte Carlo (MCMC)
Powerful but limited

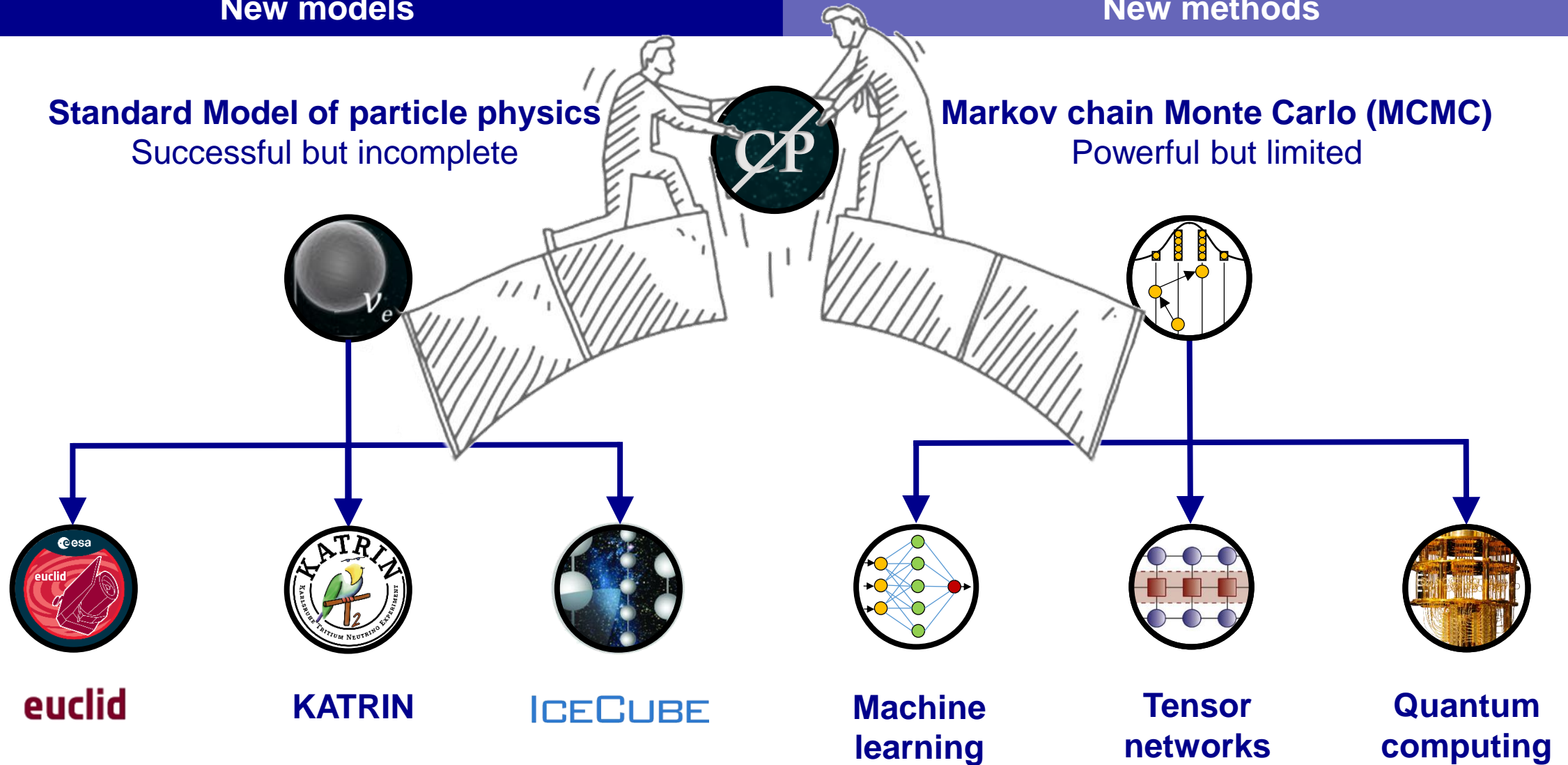


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US Department of Energy, <https://phys.org/news/2017-10-supercomputers-delve-blocks.html> (also s. 25, 26, 27, 28, 30, 31, 34)

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Credit: NASA, ESA, H. Teplitz and M. Rafelski (IPAC/Caltech), A. Koekemoer (STScI), R. Windhorst (Arizona State University), and Z. Levay (STScI), <https://hubblesite.org/contents/articles/hubble-deep-fields> (also s. 4, 6, 24)
CERN, Lucas Taylor, <https://cms.cern/physics/higgs-boson> (also s. 4)
ESO, <https://www.eso.org/public/outreach/eduoff/vt-2004/Background/Inf01/BIS-C2.html> (also s. 6)
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Felix Mittermeier, <https://pixabay.com/de/photos/sternenklarer-himmel-nachthimmel-2675322/>
Thundercrest, <https://bronsheimmusic.com/thundercrest-fanfare-band>
NASA, <https://explorer1.jpl.nasa.gov/galleries/earth-from-space/#gallery-10>
Kailogical, https://commons.wikimedia.org/wiki/File:Alpha-beta-gamma_decay.png

Slide 5:

The Economist, <https://www.economist.com/graphic-detail/2012/07/04/worth-the-wait>
Science, <https://www.science.org/content/article/sciences-breakthrough-2012>
Oleg Ruchayskiy, https://www.epfl.ch/schools/sb/research/ipphys/wp-content/uploads/2018/10/cosmology_lecture_BSM2014.pdf
Henning Bahl, https://www.desy.de/~bahl/assets/talks/2022_06_02_CERN_BSM_forum.pdf

Slide 6:

DESY, https://www.desy.de/news/news/archive_before_2010/2004/partphys_0710/index_eng.html (also s. 24)
Redbubble, <https://www.redbubble.com/shop/standard+model> (also s. 23, 39)

Slide 7:

Euclid, <https://euclid2023.org/> (also s. 8, 18, 21, 22, 29, 33, 39, 42)
KATRIN, <https://github.com/KATRIN-Experiment> (also s. 8, 18, 21, 22, 29, 33, 39, 42)
IceCube Neutrino Observatory, <https://github.com/icecube> (also s. 8, 19, 21, 22, 29, 33, 39, 42)
IBM, <http://ibm.com> (also s. 8, 21, 22, 29, 33, 39, 42)
Banuls et al., JHEP 11 (2013) 158, [https://link.springer.com/article/10.1007/JHEP11\(2013\)158](https://link.springer.com/article/10.1007/JHEP11(2013)158) (also s. 8, 21, 22, 29, 33, 39, 42)
Enisaksoy, <https://www.istockphoto.com/de/vektor/verhandlungsf%C3%BChrung-gm465033431-33117412> (also s. 8, 42)

Slide 9:

Astronomy Magazine, <https://eduvigyan.com/a-complete-history-of-the-universe/> (also s. 27, 34, 39)

Slide 10:

Hitoshi Murayama, <http://hitoshi.berkeley.edu/>
IKEA (also s. 11, 12, 13, 14)

Slide 16:

NASA / WMAP Science Team, <http://map.gsfc.nasa.gov/>
Patterson, Ann. Rev. of Nucl. and Part. Sci. 65, 177 (2015), <https://www.annualreviews.org/content/journals/10.1146/annurev-nucl-102014-021916>

Slide 18:

Roy Kaltschmidt, Lawrence Berkeley National Laboratory, <https://www.nature.com/articles/nature.2012.10202>
KIT, <https://www.sfb1258.de/news-items/official-inauguration-katrin-starts-measurements>

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IceCube Collaboration, <https://icecube.wisc.edu/gallery/published-in-prl-evidence-for-astrophysical-muon-neutrinos-from-the-northern-sky/>
NASA/CXC/U.Texas, <https://www.nasa.gov/image-article/exploded-star-blooms-like-cosmic-flower/>

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DESY, Marta Mayer, https://www.desy.de/news/news_search/index_eng.html?openDirectAnchor=2758
A. Hambarzumjan/MPP, <https://www.mpp.mpg.de/forschung/madmax>

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JICFuS, Tsukuba, https://www.jicfus.jp/en/promotion/pr/mj/brian_colquhoun/ (also s. 36)

Slide 25:

Jack Wells, Kate Clark, <https://indico.mitp.uni-mainz.de/event/231/contributions/3417/attachments/2631/2885/MLT-Clark.pdf>
(also s. 26, 27, 28)

J Ordan/CERN-PHOTO-201903-053-1, <https://cerncourier.com/a/alice-probes-extreme-electromagnetic-fields/> (also s. 30, 39)

Slide 26:

Dana Berry, Swift/NASA, <https://www.sciencenews.org/article/neutron-star-collision-fast-radio-burst> (also s. 31, 39)

Slide 30:

Nicoli et al., Phys. Rev. Lett. 126, 032001 (2021), <https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.126.032001> (also s. 32)

Slide 31:

Nakayama et al., Phys. Rev. D 105, 054507 (2022), <https://journals.aps.org/prd/abstract/10.1103/PhysRevD.105.054507> (also s. 32)

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Astibuag, <https://stock.adobe.com/de/images/qubit-vs-bit-states-of-classical-bit-compare-to-quantum-bit-superposition-vector-eps10/239139717>

Tavora, <https://towardsdatascience.com/neural-quantum-states-4793fdf67b13>

Slide 35:

Di Meglio et al., PRX Quantum 5, 037001 (2024), <https://journals.aps.org/prxquantum/abstract/10.1103/PRXQuantum.5.037001>

Slide 36:

Schuster et al., Phys. Rev. D 109, 114508 (2024), <https://journals.aps.org/prd/abstract/10.1103/PhysRevD.109.114508>

Slide 37:

Kan et al., Phys. Rev. D 104, 034504 (2021), <https://journals.aps.org/prd/abstract/10.1103/PhysRevD.104.034504>

Slide 38:

Susrut, <https://vectordad.com/printables/caution-hazardous-materials-sign/>