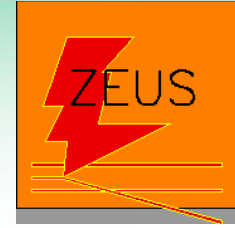




# Inclusive Diffraction at HERA



RINGBERG WORKSHOP: New Trends in HERA Physics 2011,  
September 25 - 28, 2011

M.Kapishin, JINR

on behalf of the H1 and ZEUS Collaborations

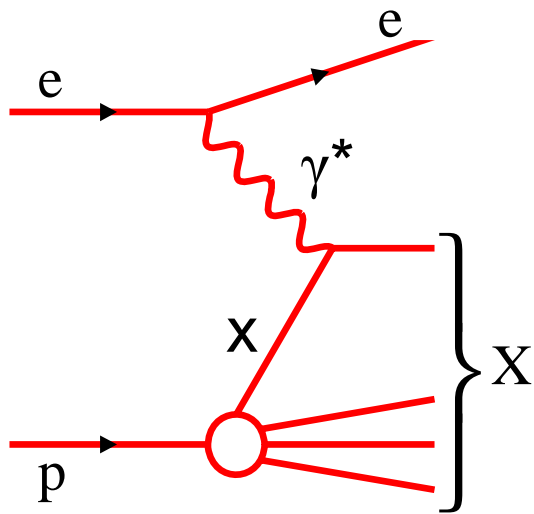
- Selection of Diffraction at HERA
- H1 and ZEUS leading proton data
- LRG cross sections and DPDF fits
- $F_L^D$  measurement
- Factorisation tests

# Diffraction DIS at HERA

**HERA:** ~10% of low-x DIS events are diffractive with no color flow between hadron systems Y(p) and X

→ Probe structure of color singlet exchange with virtual photon

## Standard DIS



$F_2 \rightarrow$  probe structure of proton

M.Kapishin

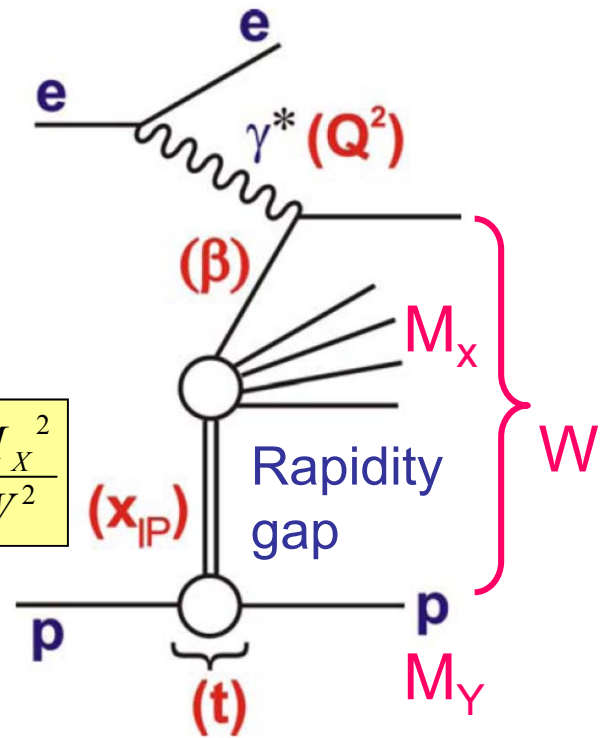
## Diffraction DIS

Momentum fraction of color singlet carried by struck quark

$$\beta = \frac{x}{x_{IP}} \approx \frac{Q^2}{Q^2 + M_X^2}$$

$$x_{IP} = \frac{q \cdot (p - p')}{q \cdot p} \approx \frac{Q^2 + M_X^2}{Q^2 + W^2}$$

Momentum fraction of proton carried by color singlet exchange

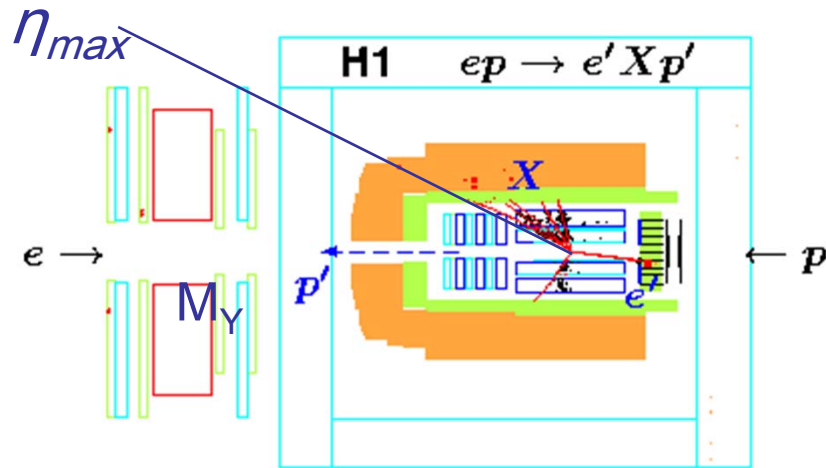


Squared 4-momentum transfer

Inclusive Diffraction at HERA

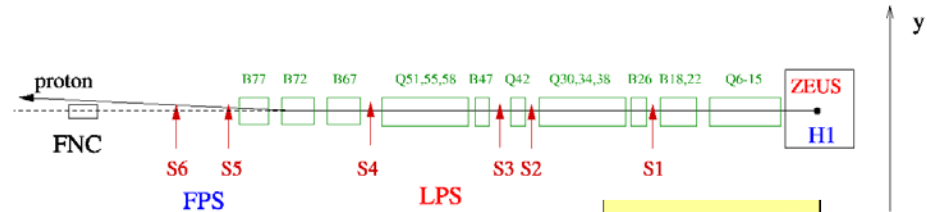
# Selection of diffraction at HERA

Large rapidity gap (LRG) between leading proton  $p$  and  $X$



- ❑ high statistics, data integrated over  $|t| < 1 \text{ GeV}^2$
- ❑ p-dissociation contribution
- ❑ limited by systematic uncertainties related to missing proton
- ➔ LRG and FPS methods have different systematic uncertainties

Proton Spectrometers (PS)



H1 FPS + ZEUS LPS  
+ H1 VFPS

$$x_{\text{IP}} = 1 - \frac{E'_p}{E_p}$$

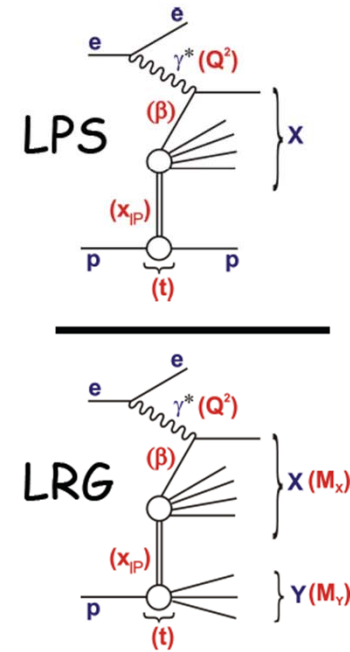
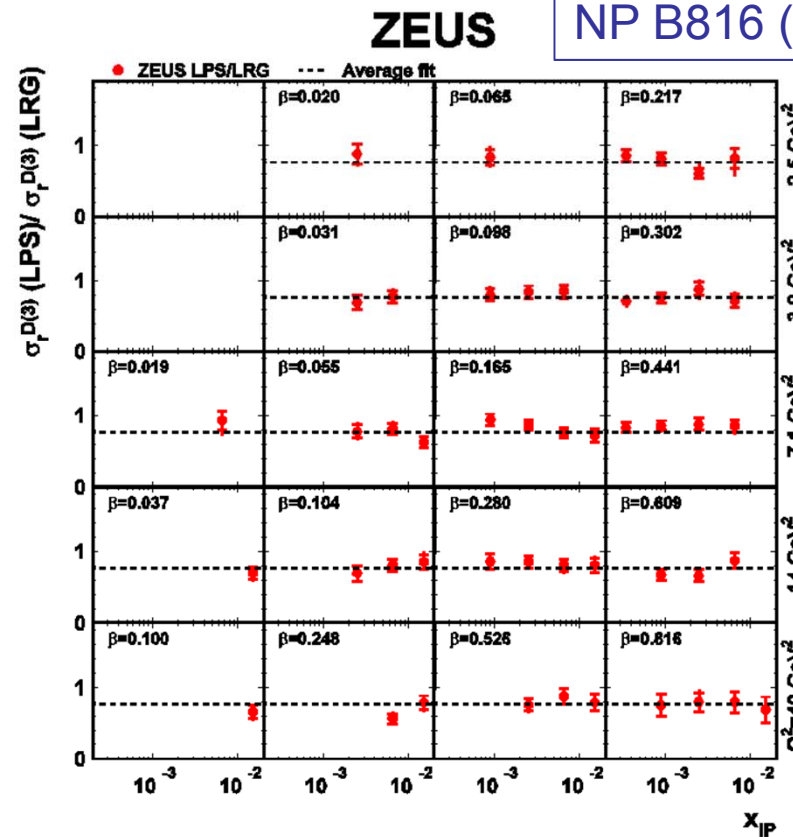
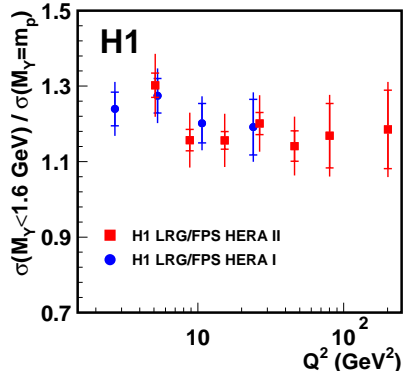
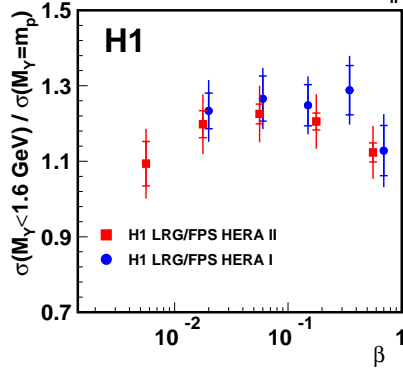
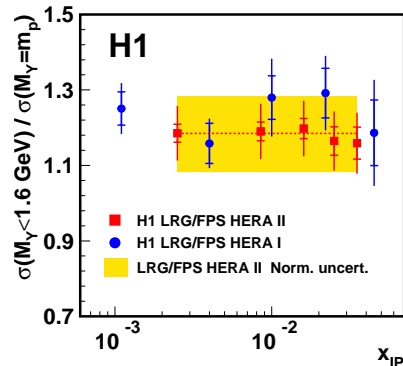
- ❑ free of p-dissociation background
- ❑  $x_{\text{IP}}$  and t-measurements
- ❑ access to high  $x_{\text{IP}}$  range (IP+IR)
- ❑ low geometrical acceptance

HERA-2:

- H1 FPS detector upgrade
- ➔ 20 times higher statistics than collected at HERA-1
- H1 VFPS has high acceptance



# Comparisons between Methods



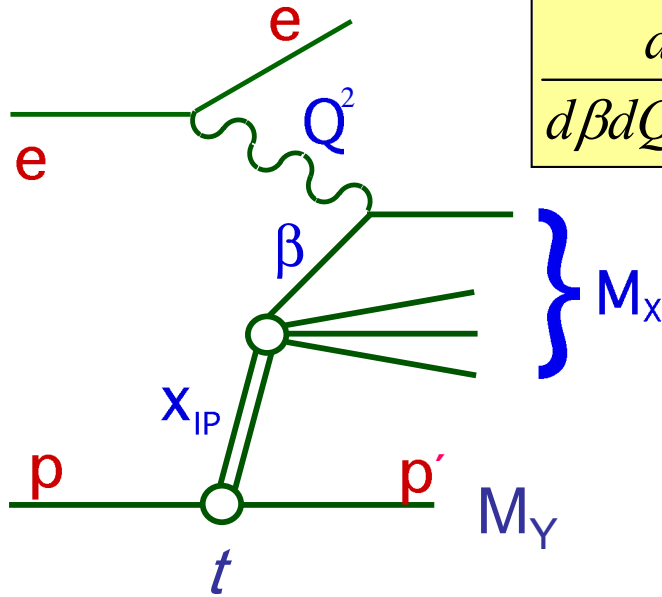
H1:  $\sigma(M_Y < 1.6 \text{ GeV}) / \sigma(M_Y = M_p) = 1.20 \pm 0.11(\text{exp.})$

- ➔ LRG data contain ~20% of p-diss contribution
- ➔ no significant dependence on  $Q^2$ ,  $\beta$ ,  $x_{IP}$

EPJ C71 (2011) 1578

Inclusive Diffraction at HERA

# Diffractive Reduced Cross Section



$$\frac{d^4\sigma}{d\beta dQ^2 dx_{IP} dt} = \frac{4\pi\alpha^2}{\beta Q^4} \left(1 - y + \frac{y^2}{2}\right) \sigma_r^{D(4)}(\beta, Q^2, x_{IP}, t)$$

Relation to  $F_2^D$  and  $F_L^D$ :

$$\sigma_r^{D(4)} = F_2^{D(4)} - \frac{y^2}{2(1 - y + y^2/2)} F_L^{D(4)}$$

$$\sigma_r^D \approx F_2^D \text{ at low and medium } y$$

$$\sigma_r^{D(3)} = \int \sigma_r^{D(4)} dt$$

→ integrate over  $|t| < 1 \text{ GeV}^2$  to compare PS results with LRG and diffractive PDF predictions

- $F_2$  directly related to quark density in proton
- $dF_2/d\ln Q^2$  (scaling violations) sensitive to gluon density
- $F_L$  only non-zero in higher order QCD – independent access to gluon density

# Factorisation in Diffractive DIS

QCD hard scattering collinear factorisation:

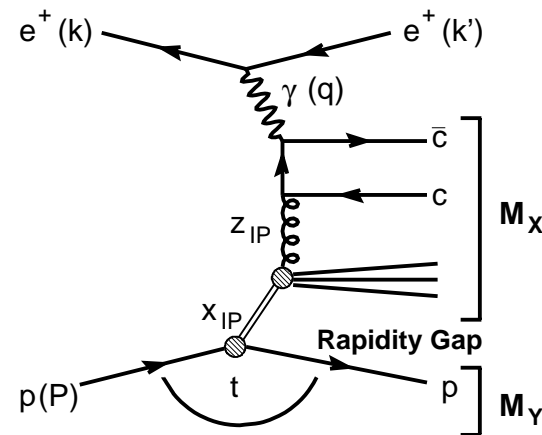
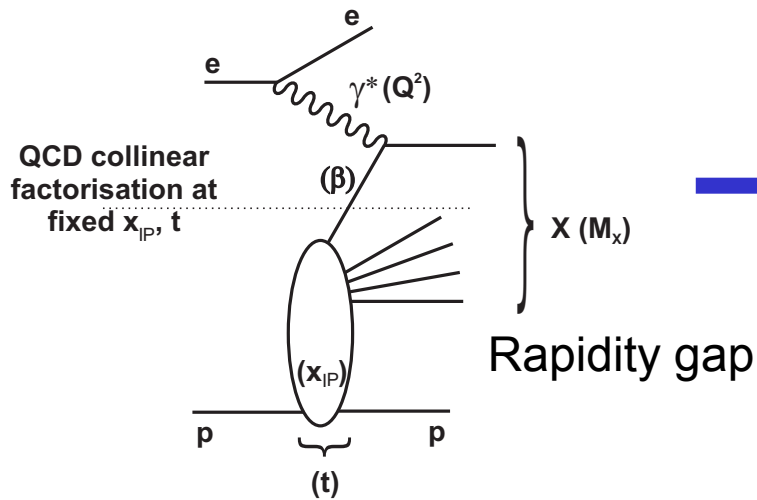
$$\sigma^D(\gamma^* p \rightarrow Xp) = \sum_{parton\_i} f_i^D(x, Q^2, x_{IP}, t) \cdot \sigma^{\gamma^*i}(x, Q^2)$$

$\sigma^{\gamma^*i}$  - universal hard scattering cross section (same as in inclusive DIS)

$f_i^D$  - Diffractive Parton Distribution Function  $\rightarrow$  obey DGLAP,  
universal for diffractive  $ep$  DIS (inclusive, Dijets, Charm)

□ Extract DPDFs from QCD fit to inclusive diffractive DIS

□ Test DPDFs in diffractive Final States (Boson Gluon Fusion)



# Factorisation in Diffractive DIS

Assumption of **proton vertex factorisation** for leading  $IP$  and sub-leading  $IR$  exchanges  $\rightarrow$  hard scattering is independent of  $x_{IP}$  and  $t$

$$F_2^{D(4)}(\beta, Q^2, x_{IP}, t) = f_{IP}(x_{IP}, t) \cdot F_2^{IP}(\beta, Q^2) + n_{IR} \cdot f_{IR}(x_{IP}, t) \cdot F_2^{IR}(\beta, Q^2)$$

- $x_{IP}$  and  $t$  dependences are described by Regge motivated  $IP$  and  $IR$  fluxes:

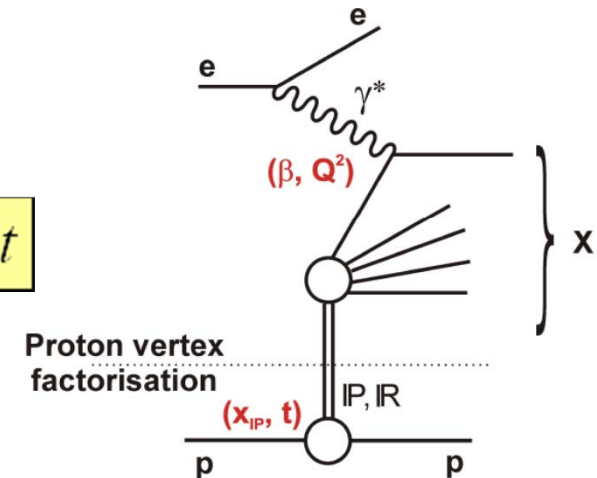
$$f_{IP}(x_{IP}, t) = \frac{e^{B_{IP}t}}{x_{IP}^{2\alpha_{IP}(t)-1}}$$

$$\alpha_{IP}(t) = \alpha_{IP}(0) + \alpha'_{IP} t$$

- Dominance of  $IP$  trajectory with  $\alpha_{IP} > 1$  at  $x_{IP} < 0.01$  and contribution of sub-leading  $IR$  trajectory with  $\alpha_{IR} < 1$  at higher  $x_{IP}$

- Shrinkage of  $\exp t$ -slope with  $\ln(1/x_{IP}) \rightarrow$

$\rightarrow$  Perform 'Regge' fits to diffractive data to extract parameters of  $IP$  flux



$$\frac{d\sigma}{dt} \sim \exp B|t|$$

$$B = B_{IP} + 2\alpha'_{IP} \ln(1/x_{IP})$$

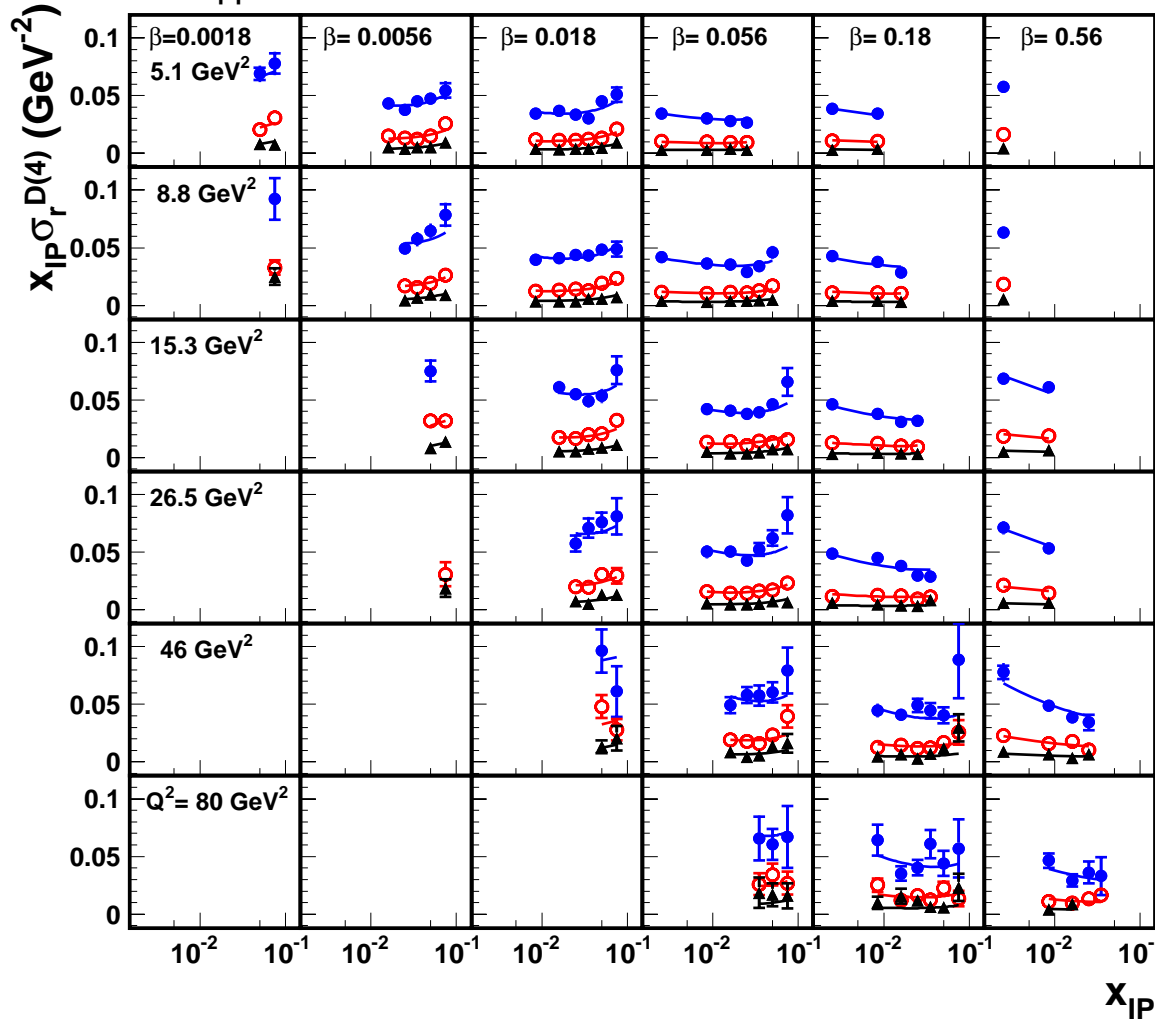


$$x_{IP} \sigma_r^{D(4)}(\beta, Q^2, x_{IP}, t)$$

# H1 FPS

- $|t|=0.2 \text{ GeV}^2$
- $|t|=0.4 \text{ GeV}^2$
- ▲  $|t|=0.6 \text{ GeV}^2$

— Regge fit IP+IR



$Q^2$  New H1 FPS HERA-2

5  $\sigma_r^{D(4)}$  data:

- $5 < Q^2 < 80 \text{ GeV}^2$

- 9 • luminosity  $156 \text{ pb}^{-1}$

- 15 • 20 times higher statistics than in HERA-1 data

- 26 • norm. uncertainty  $\sim 4.3\%$   
→ smaller than in HERA-1

46  $x_{IP}$ -dependence in  $(Q^2, \beta, t)$  bins

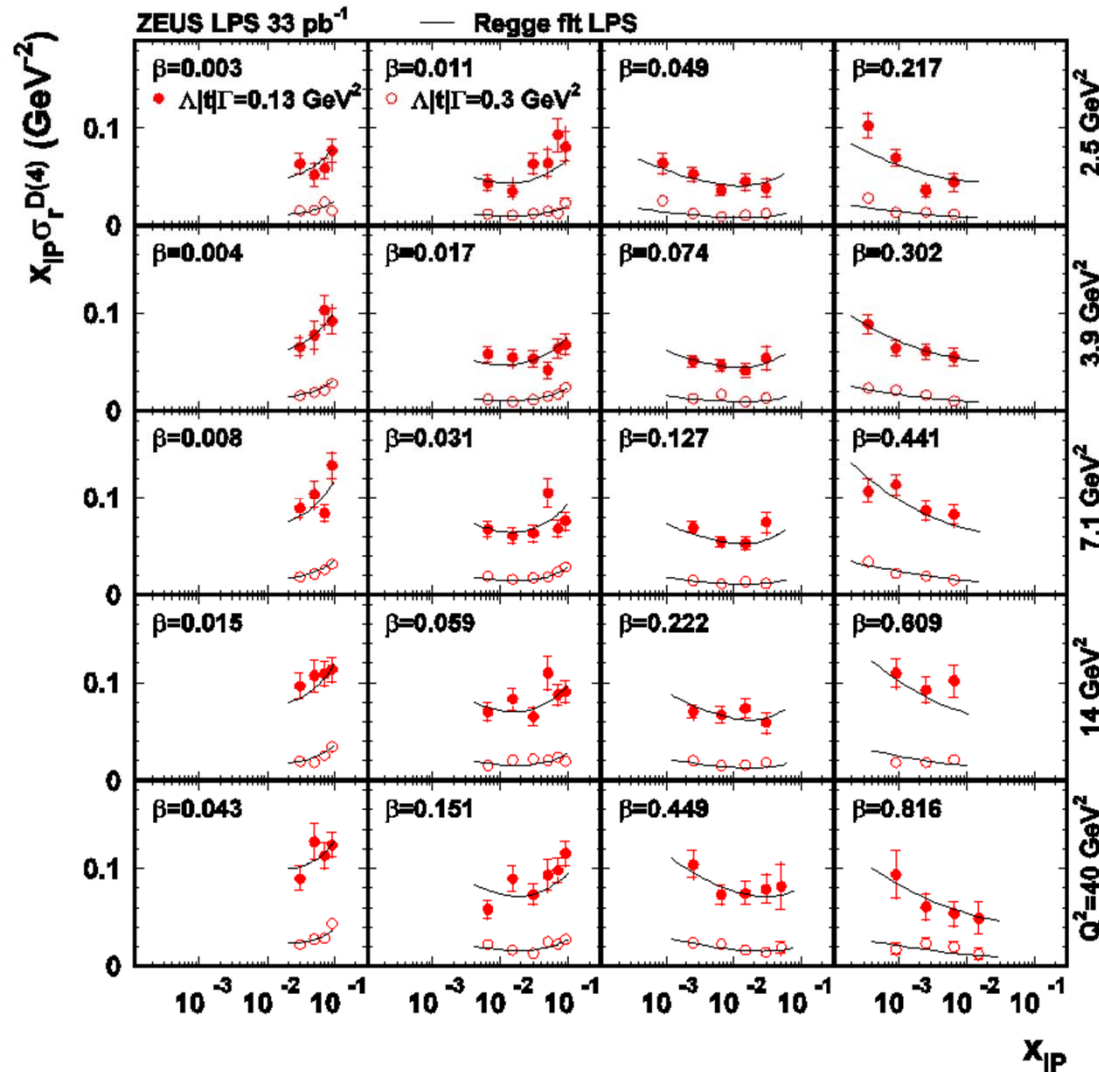
80  $\rightarrow$  IP and IR contributions



# ZEUS LPS: $x_{IP}\sigma_r^{D(4)}$



## ZEUS



ZEUS LPS  $|t|=0.13$  GeV<sup>2</sup>

ZEUS LPS  $|t|=0.3$  GeV<sup>2</sup>

— Regge fit IP+IR

• luminosity 32.6 pb<sup>-1</sup>

• norm. uncertainty of ZEUS LPS  $\sigma_r^{D(4)}$  data is 7%

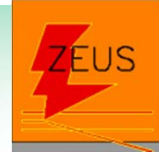
$x_{IP}$ -dependence in  $(\beta, Q^2, t)$  bins

→ IP and IR contributions

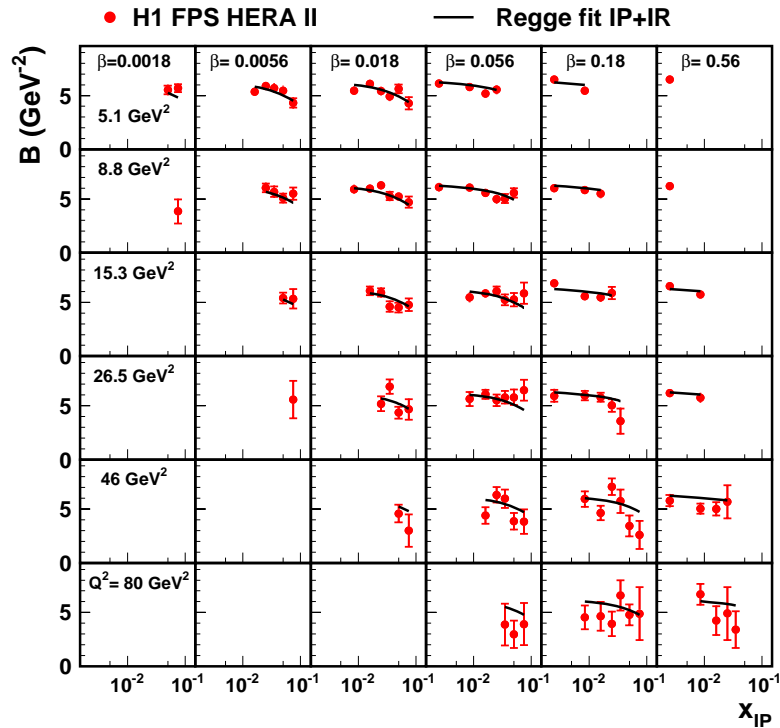
NP B816 (2009) 1



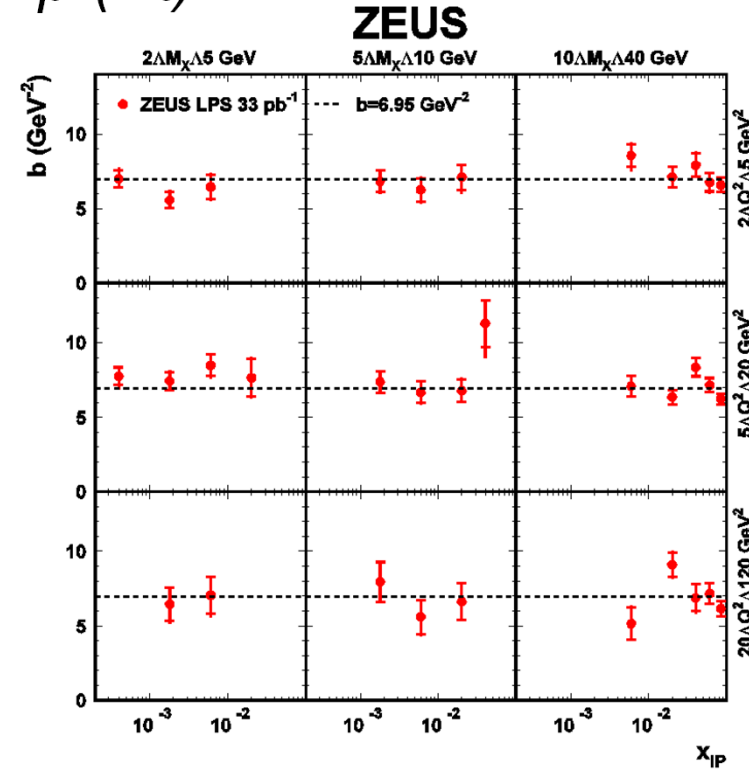
# t-slope as a function of $Q^2, \beta, M_x, x_{IP}$



$$d\sigma/dt \sim \exp(Bt)$$



H1 FPS: IR contribution at large  $x_{IP}$

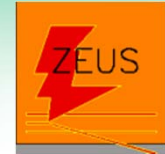


ZEUS LPS: no strong effect from IR contribution

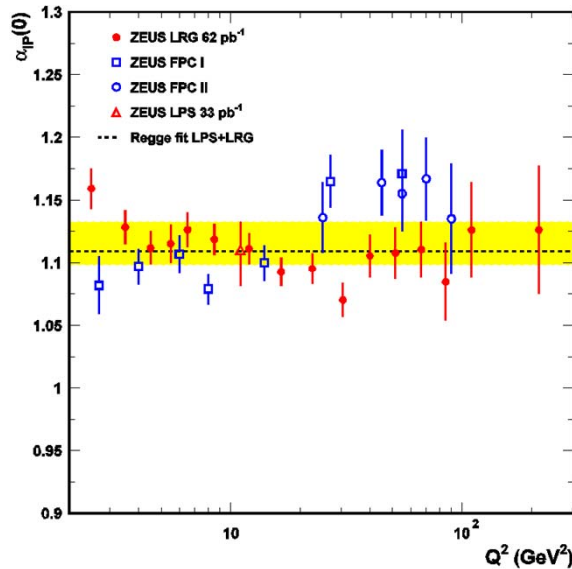
H1 and ZEUS:  $t$ -slope does not change with  $\beta$ ,  $M_x$  or  $Q^2$  at fixed  $x_{IP}$   
 → data consistent with **proton vertex factorisation**



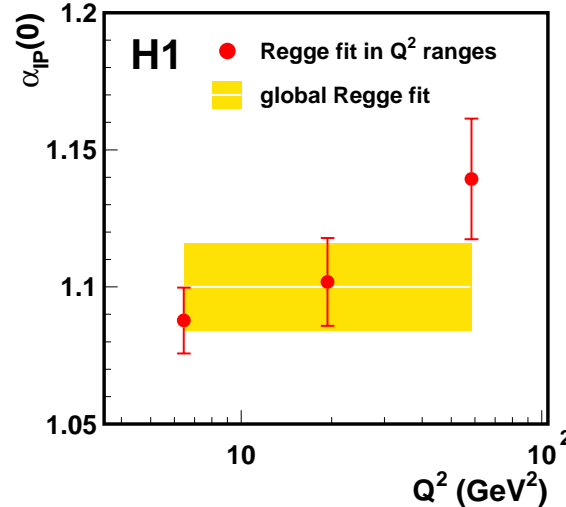
# Proton Vertex Factorisation



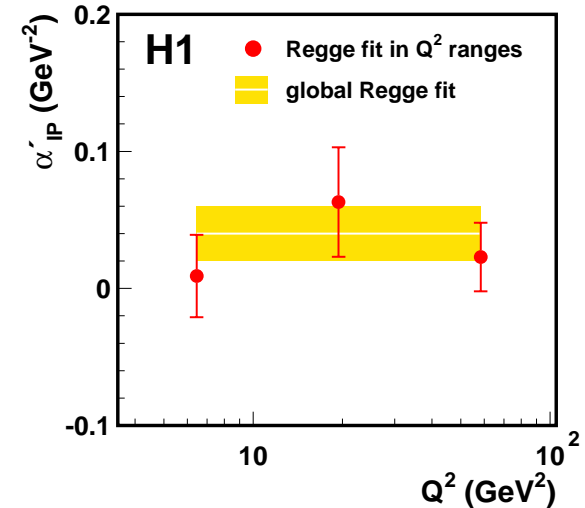
ZEUS



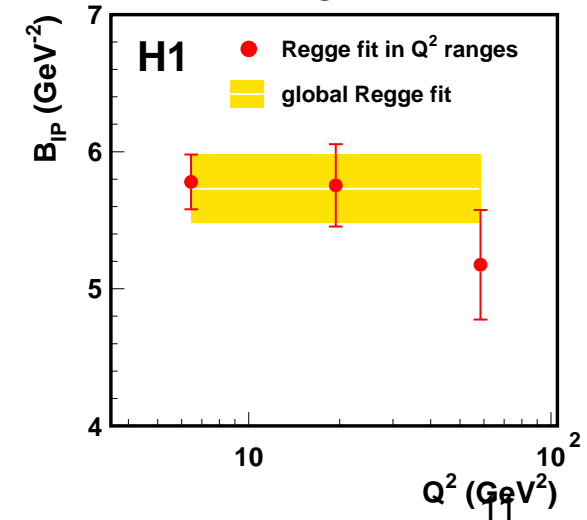
H1 FPS HERA II



H1 FPS HERA II



H1 FPS HERA II



- $\alpha_{IP}(0) \approx 1.10$  in agreement with  $\alpha_{IP}(\text{soft}) \sim 1.08$
- $\alpha'_{IP} \approx 0 \rightarrow$  no “shrinkage”  $< \alpha'_{IP}(\text{soft}) \sim 0.25 \text{ GeV}^{-2}$
- $B_{IP}$  consistent with hard process
- no strong dependence of  $\alpha_{IP}(0)$ ,  $\alpha'_{IP}$ ,  $B_{IP}$  on  $Q^2$
- H1 and ZEUS results are consistent with **proton vertex factorisation** within uncertainties

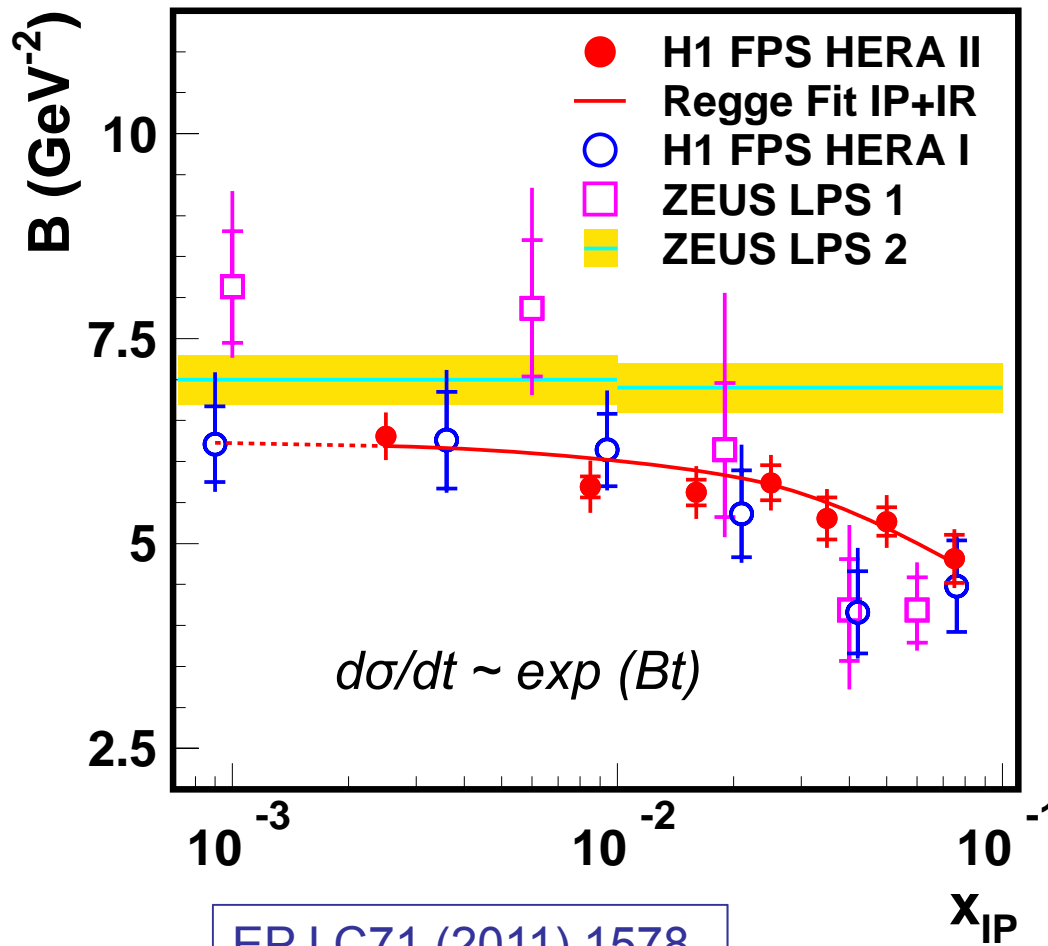


# t-slope as a function of $x_{IP}$



H1 Regge fit result:

$$B(x_{IP}) = f_{IP}(x_{IP}) \cdot B_{IP}(x_{IP}) + f_{IR}(x_{IP}) \cdot B_{IR}(x_{IP})$$



EPJ C71 (2011) 1578

•  $x_{IP}$ -dependence of t-slope, data averaged over  $Q^2$  and  $\beta$

→ H1 FPS HERA-1 and HERA-2 data are consistent,  $B \sim 5-6 \text{ GeV}^{-2}$

→ IR contribution at high  $x_{IP}$

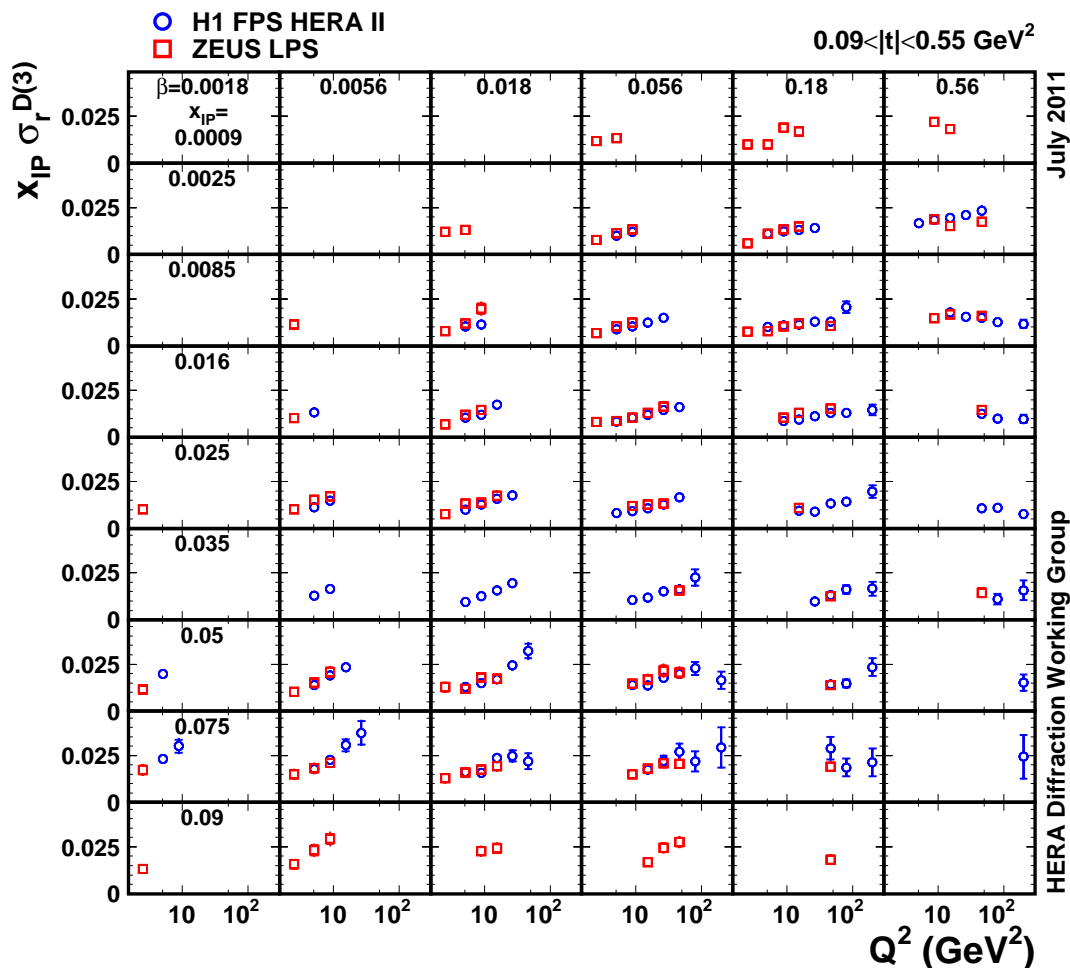
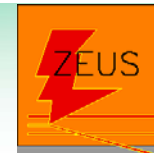
→ ZEUS LPS2 measures higher t-slope:  $B \sim 7 \text{ GeV}^{-2}$

→ are H1 / ZEUS uncertainties underestimated ?

→ H1 VFPS will provide an independent measurement of t-slope in  $x_{IP}$  range 0.009-0.026



# $\sigma_r^{D(3)}$ : H1 FPS vs ZEUS LPS



H1 prel-11-111, ZEUS prel-11-011

Proton Spectrometer data in  $0.09 < |t| < 0.55 \text{ GeV}^2$

$Q^2$ -dependence in  $(\beta, x_{IP})$  bins

- H1 FPS norm. uncertainty 4.5%, ZEUS LPS norm. uncertainty 7%

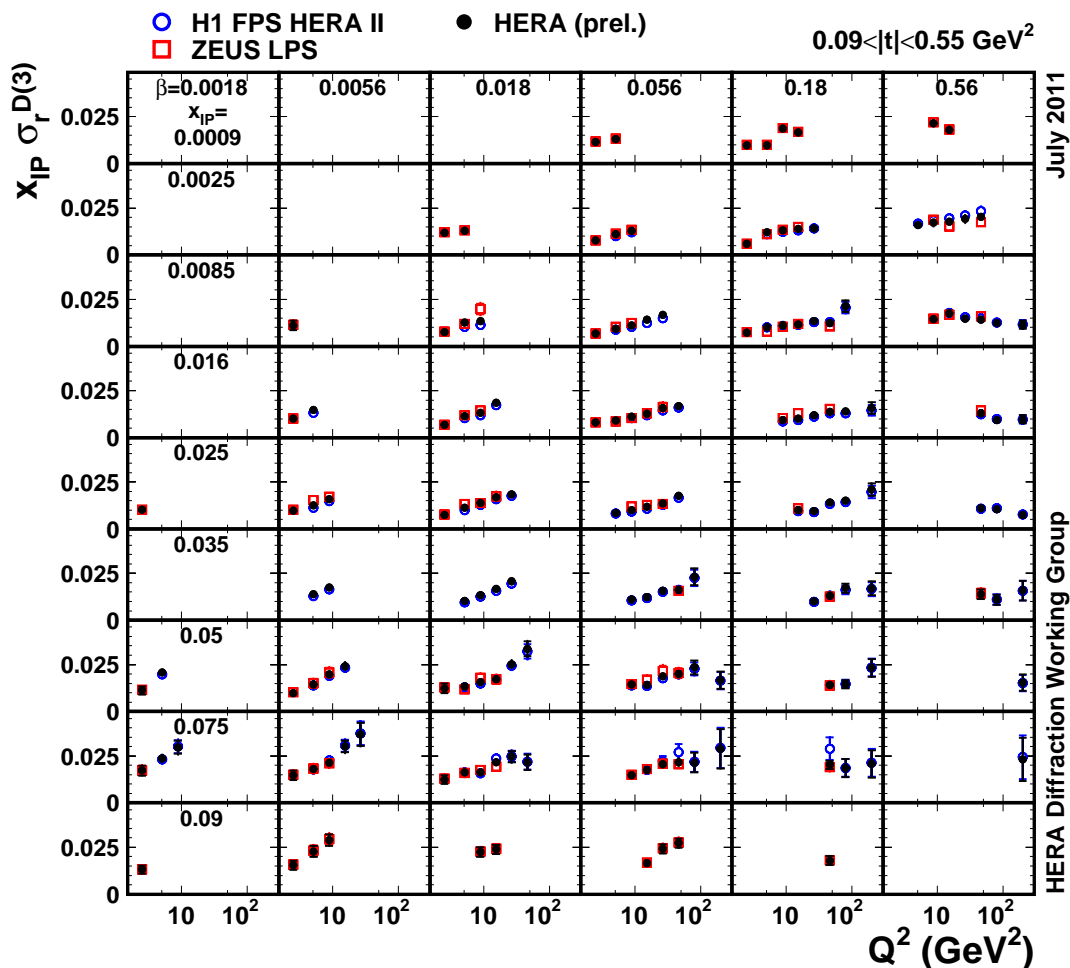
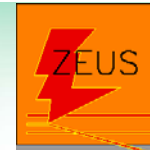
H1 / ZEUS: = 0.91 +/- 0.01(stat.) +/- 0.03(syst.) +/- 0.08(norm.)

➔ Reasonable agreement of H1 FPS HERA-2 and ZEUS LPS data in shape & normalisation

➔ Combine H1 and ZEUS cross sections to extend phase space and reduce uncertainties



# $\sigma_r^{D(3)}$ : H1 FPS vs ZEUS LPS



First combination of H1 and ZEUS diffractive data

→ Combined results from proton spectrometers

→ Consistency between data sets

→ Combination method uses iterative  $\chi^2$  minimization and include full error correlations [A.Glazov]

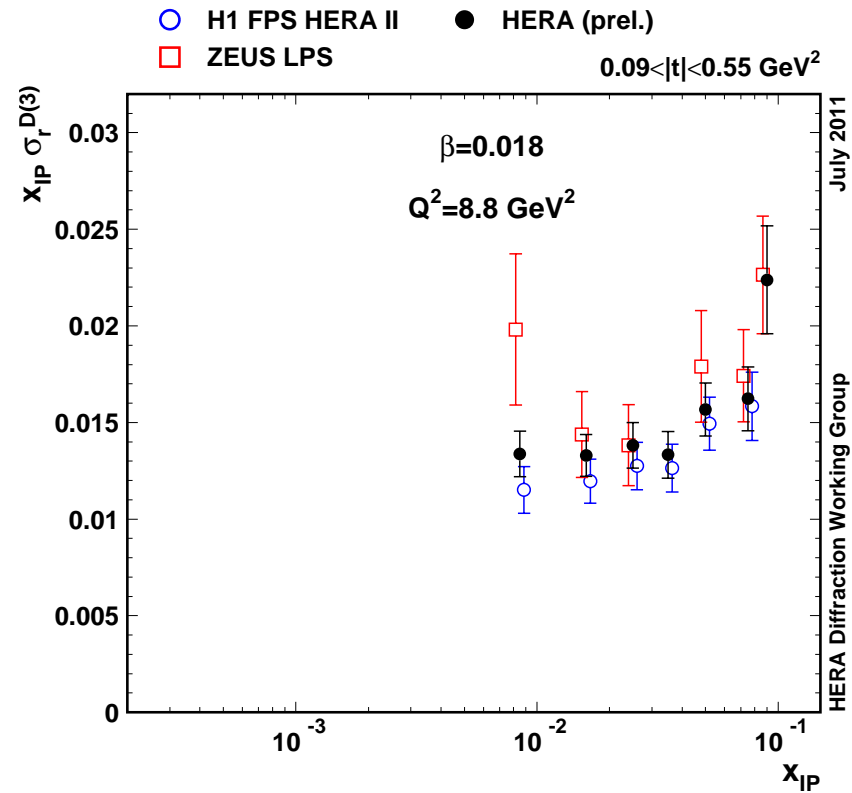
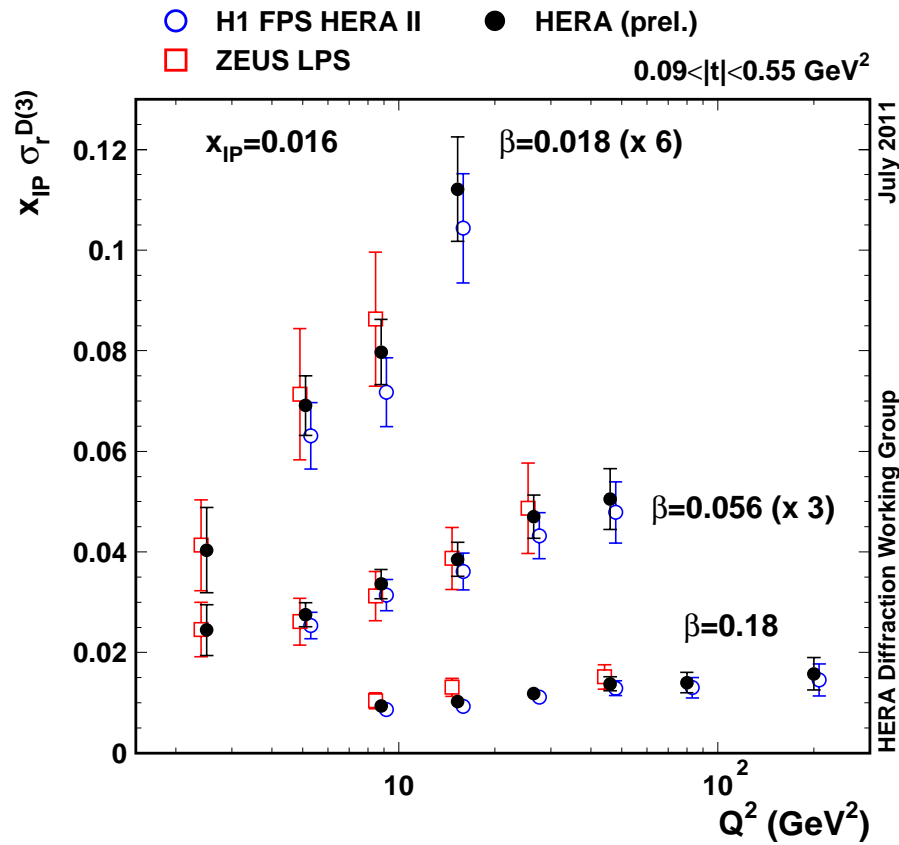
→ Two experiments calibrate each other resulting in reduction of systematic uncertainties



# $\sigma_r^{D(3)}$ : H1 FPS vs ZEUS LPS



- A detailed look to the combined data



→ combined data have ~20% smaller uncertainties with respect to H1 data

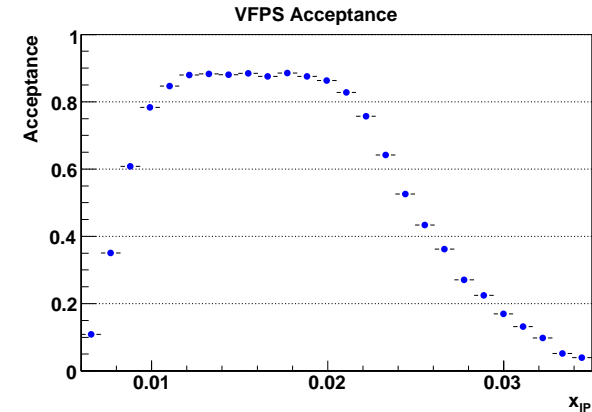


# $\sigma_r^{D(3)}$ : VFPS vs FPS vs LRG

H1 VFPS has high acceptance in range  $0.009 < x_{IP} < 0.026$ ,  $|t| < 0.5 \text{ GeV}^2$

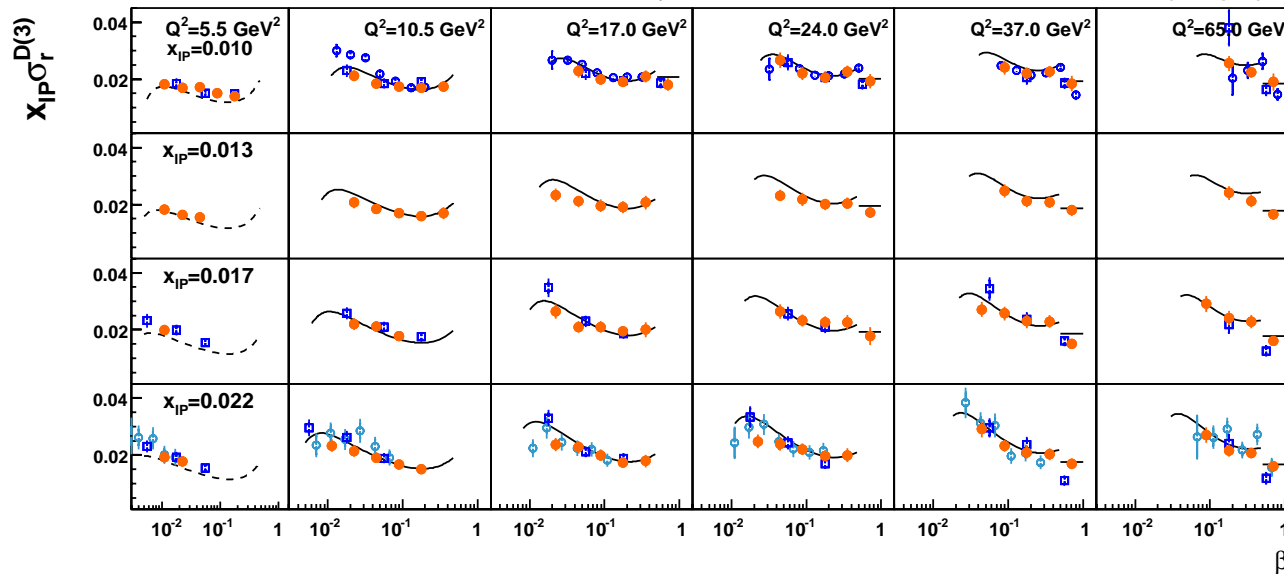
→ allows a high precision measurement over this  $x_{IP}$  range

→ VFPS t-slope and  $\sigma_r^{D(4)}$  measurements are on the way



## H1 PRELIMINARY

- H1 VFPS Preliminary
- H1 FPS Preliminary
- H1 LRG Preliminary x 0.81
- H1 LRG Published x 0.81
- H1 2006 DPDF Fit B x 0.81
- - - H1 2006 DPDF Fit B x 0.81 (extrapol.)



$\sigma_r^{D(3)}$  for  $|t| < 1 \text{ GeV}^2$

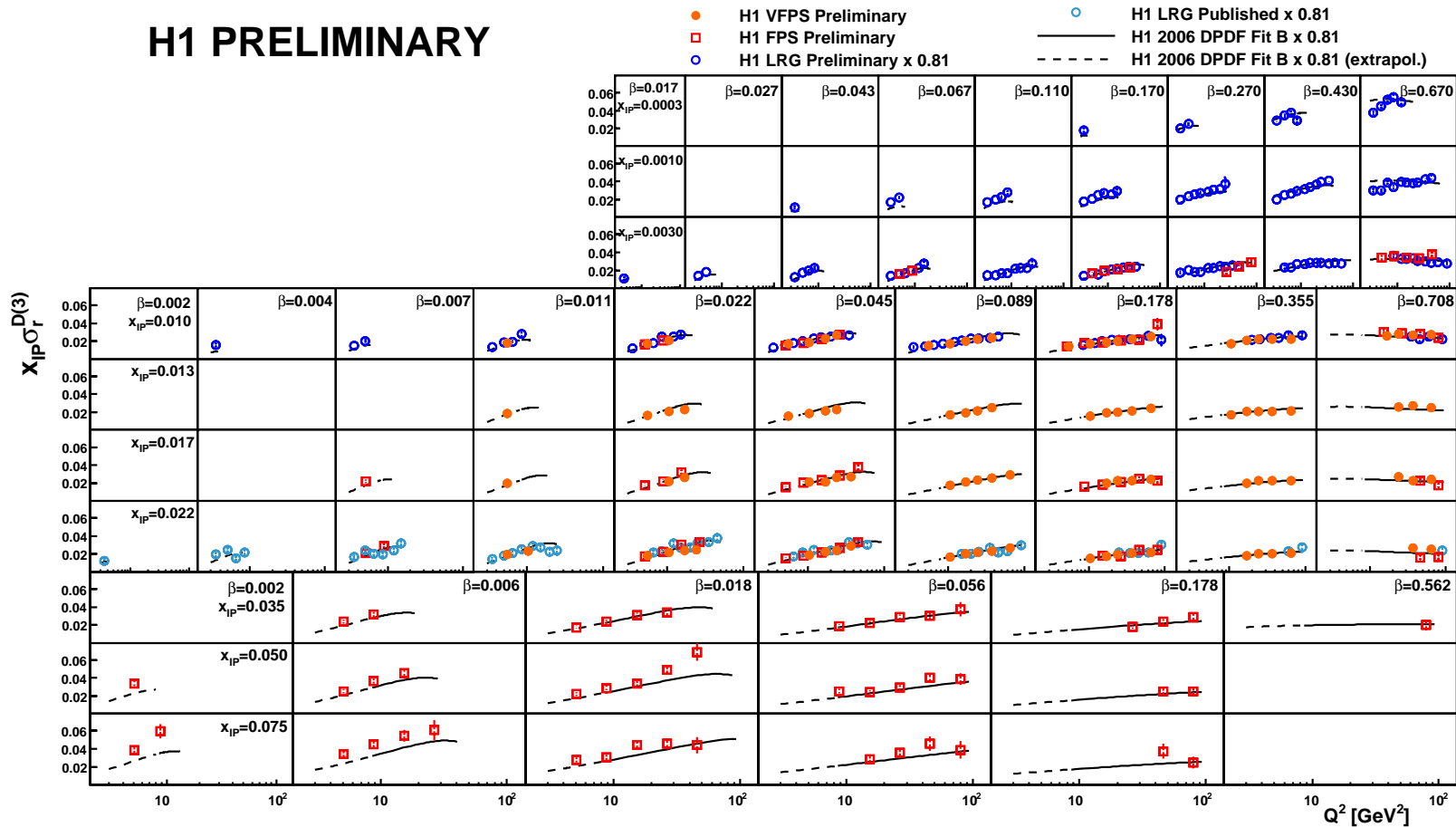
H1 prel-10-014





# $\sigma_r^{D(3)} : \text{VFPS vs FPS vs LRG}$

H1 PRELIMINARY

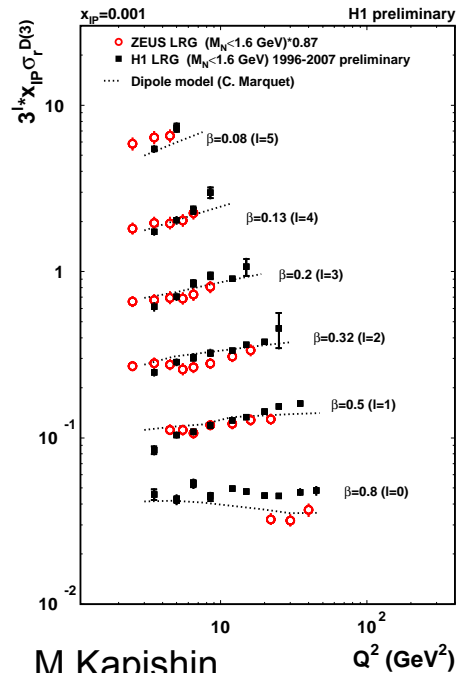
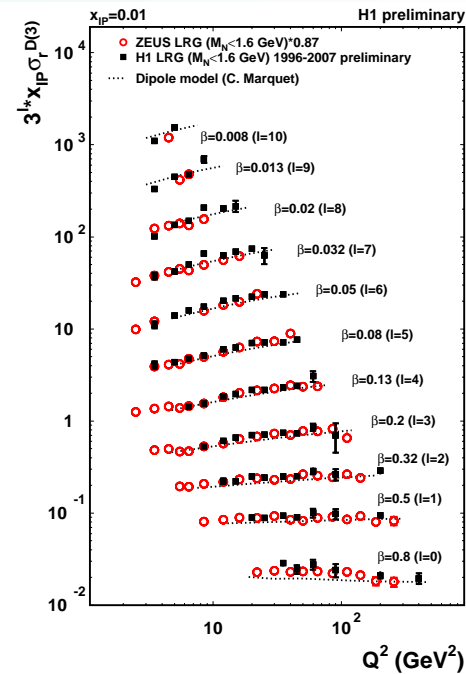
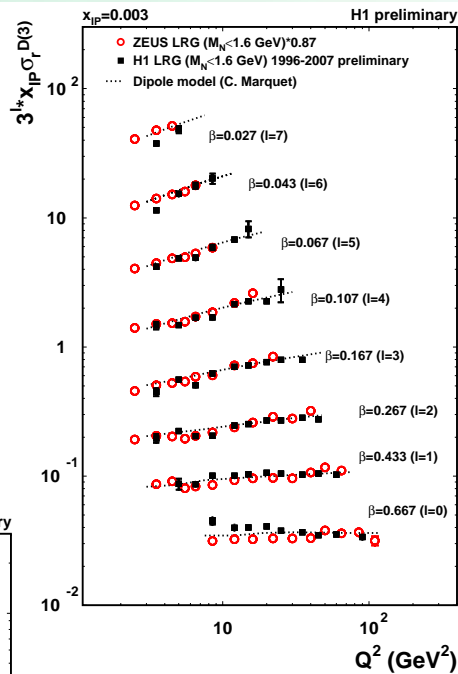
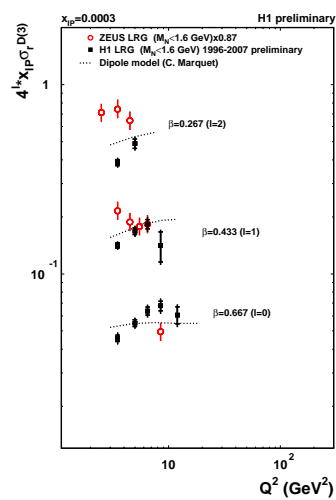


➔ compilation of VFPS, FPS and LRG data vs H1 DPDF Fit B

$$\frac{\text{VFPS}}{\text{FPS}} = 0.96 \pm 0.02(\text{stat.}) \pm 0.11(\text{syst.}) \pm 0.08(\text{norm.})$$



# LRG $\sigma_r^{D(3)}$ : H1 vs ZEUS



H1 prel-10-011

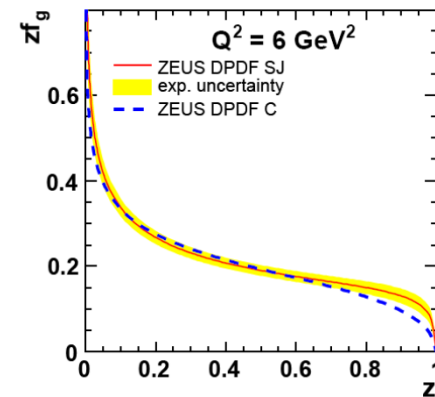
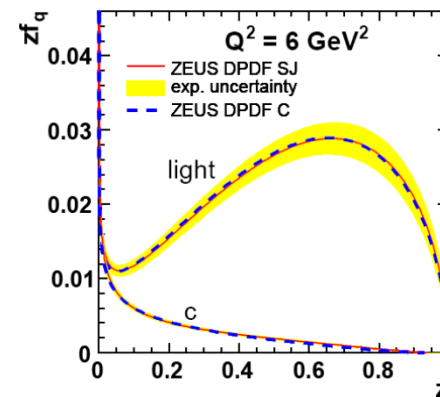
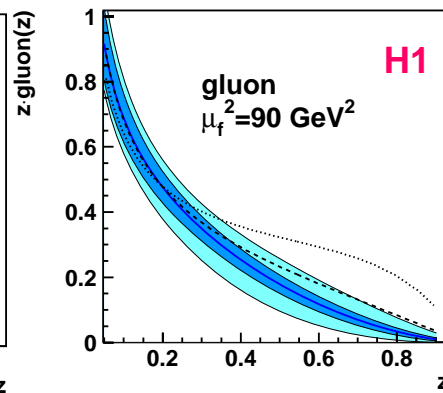
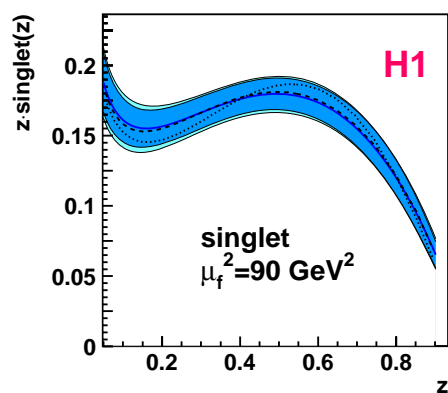
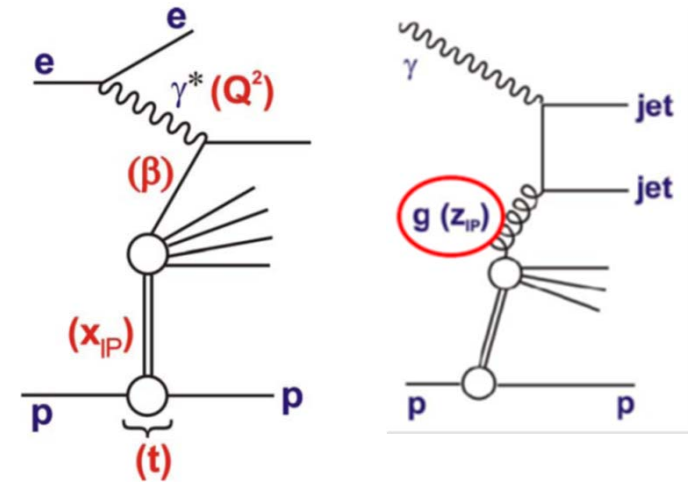
- combined  $370 \text{ pb}^{-1}$  of H1 LRG (HERA-1 and HERA-2) and  $62 \text{ pb}^{-1}$  of ZEUS LRG (HERA-1)
- data are in general agreement, normalization difference of 13% is within quoted uncertainties
- detailed quantitative comparison shows differences at low and high  $\beta$



# Diffractive PDFs: H1 vs ZEUS



- Fit  $\beta$  and  $Q^2$  dependences at fixed  $x_{IP}$
- Parameterize quark singlet and gluon PDFs at starting scale  $Q_0$  and evolve with  $Q^2$  using NLO DGLAP
- Proton vertex factorisation assumption to fit data from different  $x_{IP}$  with complementary  $\beta, Q^2$  coverage
- Inclusive diffractive DIS cross sections constrain quark singlet and gluon (via scaling violations); Dijet DIS cross sections constrain high  $z$  gluon

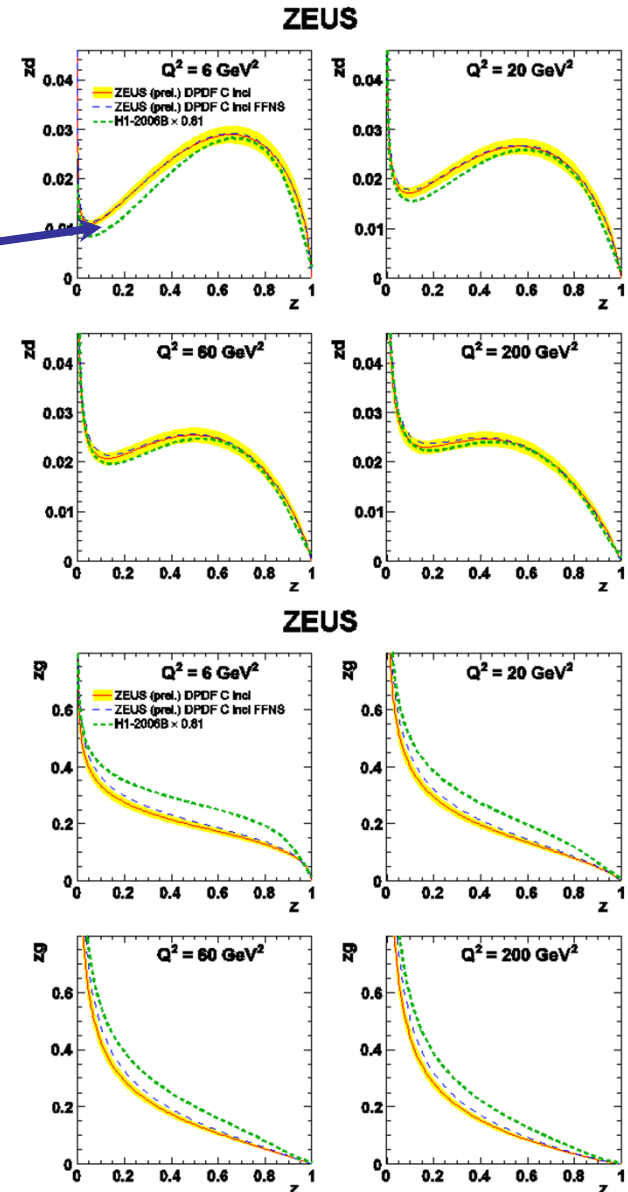
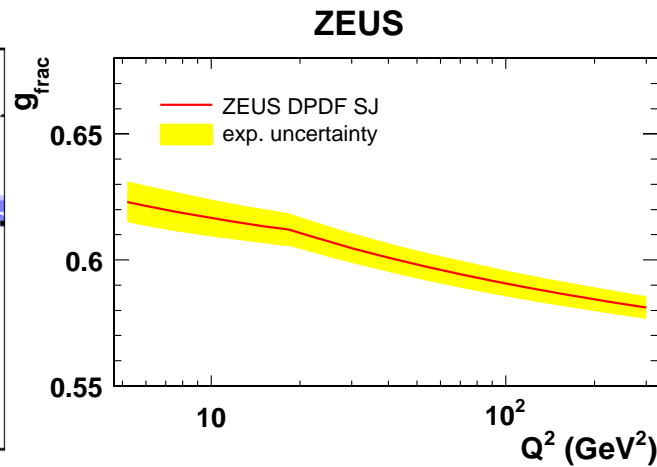
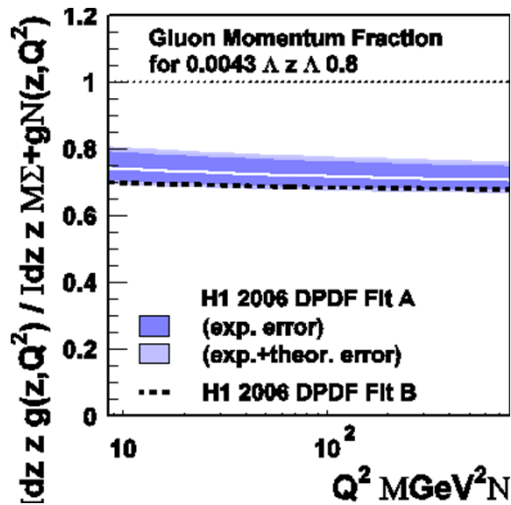




# Diffraction PDFs: H1 vs ZEUS



- Recent ZEUS DPDF fits to inclusive LRG & LPS & diffractive Dijet DIS consistent with previous H1 DPDF fits up to normalization factor in data



- Overall ratio of gluon to quark density is 70:30 (H1) or 60:40 (ZEUS) → similar to inclusive PDFs at low  $x$

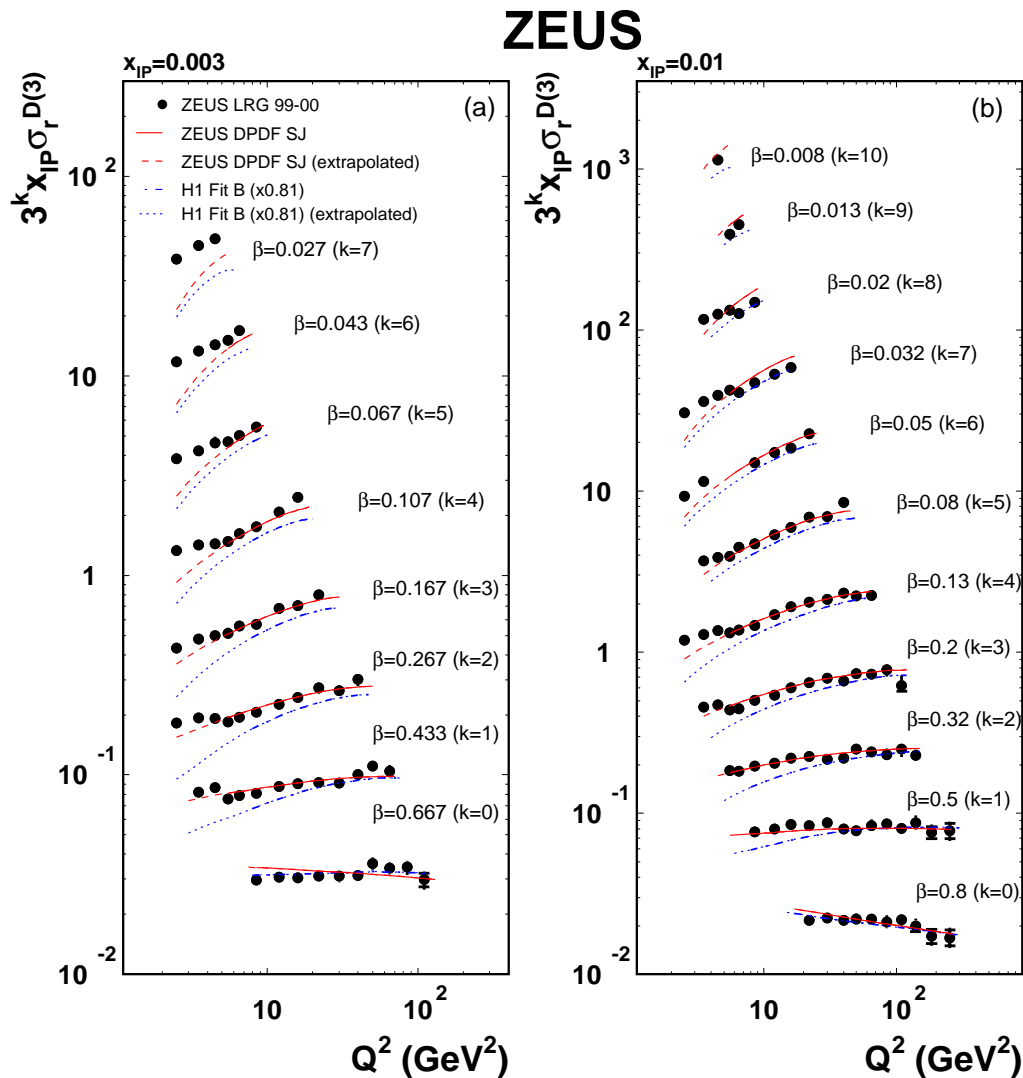
NP B831 (2010) 1

M.Kapishin

Inclusive Diffraction at HERA



# Diffractive PDFs: H1 vs ZEUS



→ H1 DPDF Fit B and ZEUS DPDF Fit SJ predict somewhat different behavior at low  $Q^2$

→ fits reflect difference in normalization of H1 and ZEUS LRG data

→ need to understand differences in H1 and ZEUS LRG data sets to combine them and perform a QCD fit

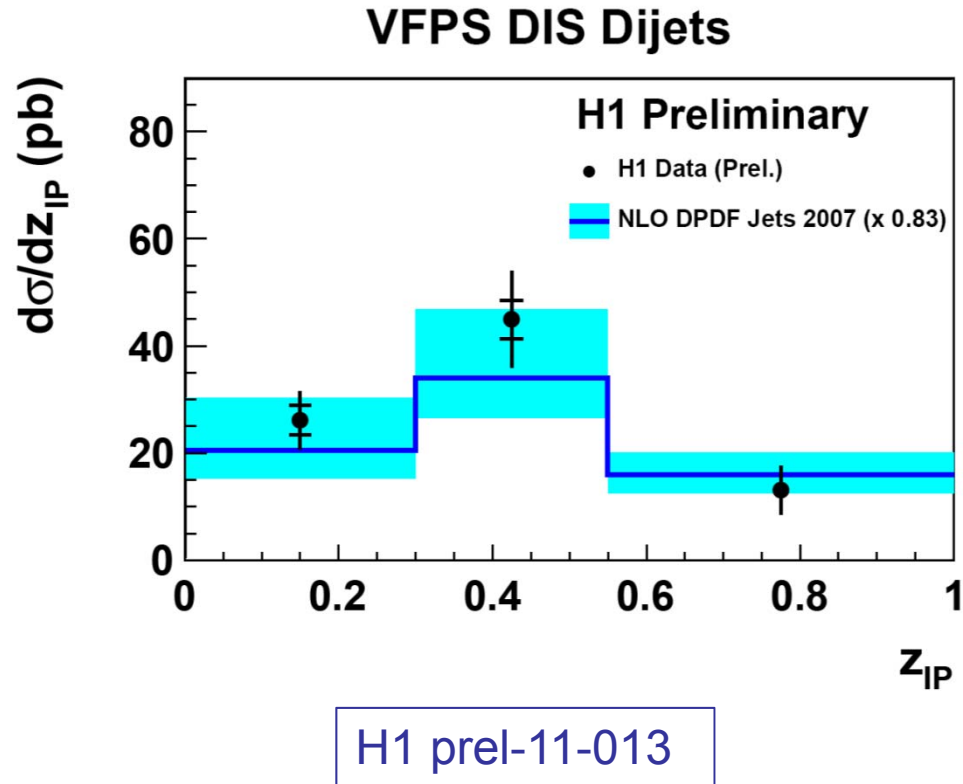
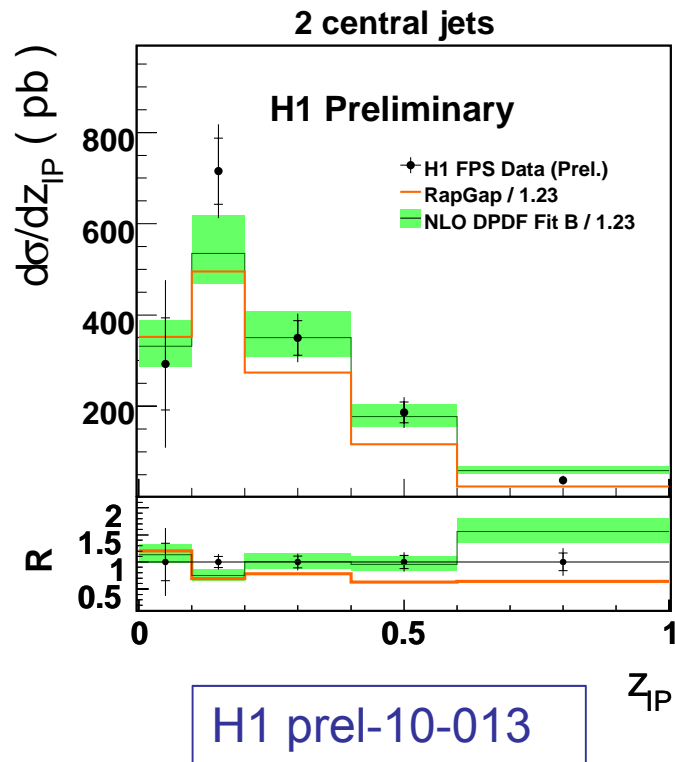
→ most of H1 LRG data (1999-2000 HERA-1 and HERA-2) are still preliminary



# Central Jets in DIS with tagged proton

FPS:  $x_{IP} < 0.1$ ,  $p_{T1}^* > 5\text{GeV}$ ,  
 $p_{T1}^* > 4\text{GeV}$ ,  $-1 < \eta_{lab} < 2.5$

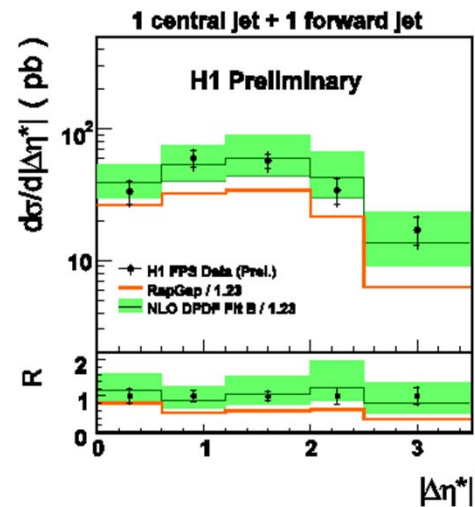
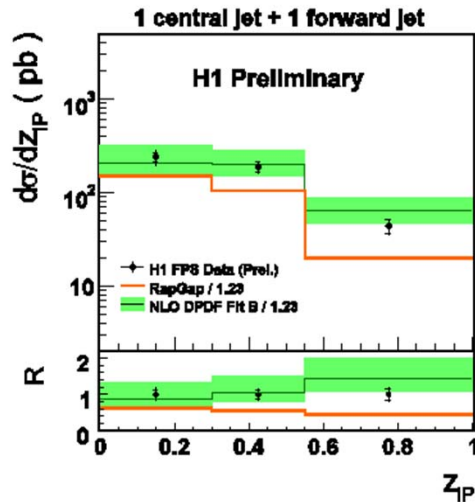
VFPS:  $0.009 < x_{IP} < 0.024$ ,  $p_{T1}^* > 5.5\text{GeV}$ ,  
 $p_{T1}^* > 4\text{GeV}$ ,  $-3 < \eta^* < 0$



→ NLO predictions based on DPDFs H1 Jets an H1 Fit B describe central dijet production in DIS with tagged leading proton



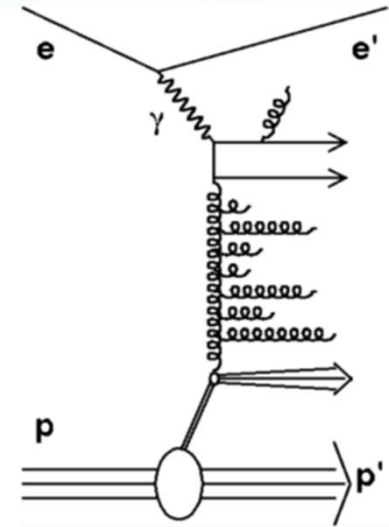
# Forward Jets in DIS with tagged proton



New H1 analysis of Dijet production in DIS with leading proton tagged in FPS:

Forward jet:  $p_T^* > 4.5 \text{ GeV}$ ,  $1 < \eta_{\text{fwd}} < 2.8$

Central jet:  $p_T^* > 3.5 \text{ GeV}$ ,  $-1 < \eta_{\text{cen}} < \eta_{\text{fwd}}$



→ extended  $x_{\text{IP}}$  and  $\eta$  range compared to LRG dijet DIS data

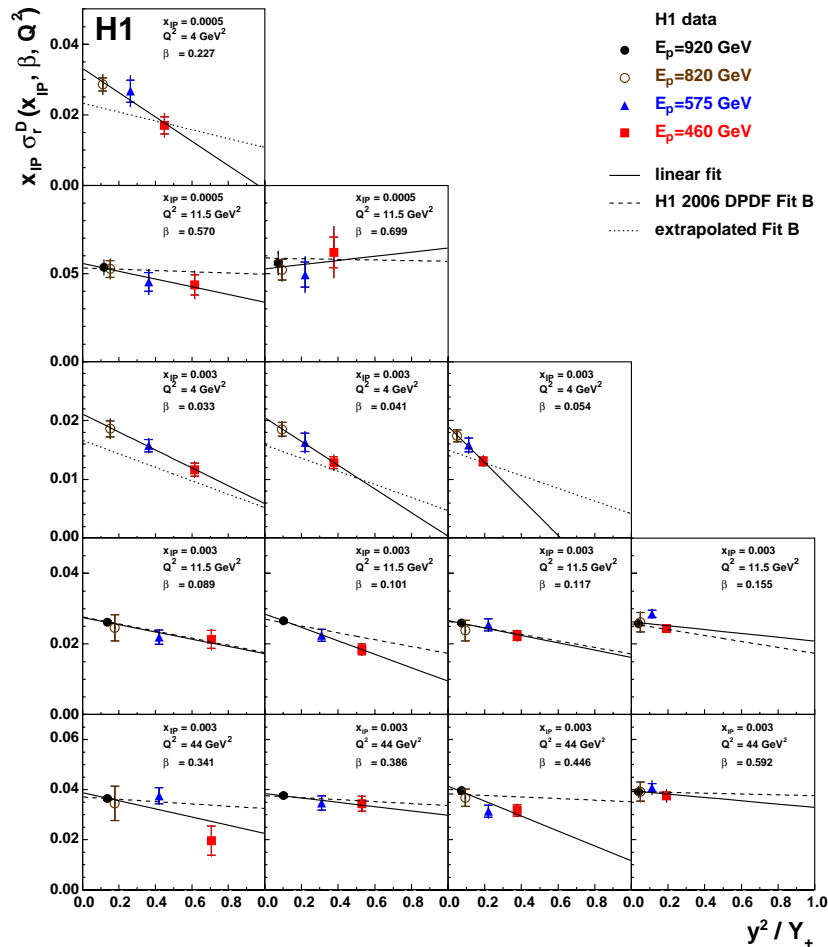
→ dijet selection with DGLAP  $p_t$  ordering broken

→ no evidence for configurations beyond DGLAP & DPDF predictions





# Linear fits to extract $F_L^D$



$$\sigma_r^{D(4)} = F_2^{D(4)} - \frac{y^2}{2(1-y+y^2/2)} F_L^{D(4)}$$

→ measure  $\sigma_r^D$  at fixed  $Q^2, x_{IP}, \beta$ , but different  $y$  using LRG data at different proton beam energies

→ perform linear fits to extract  $F_L^D$

→ analysis published for full range  $Q^2 > 2.5$  GeV<sup>2</sup>

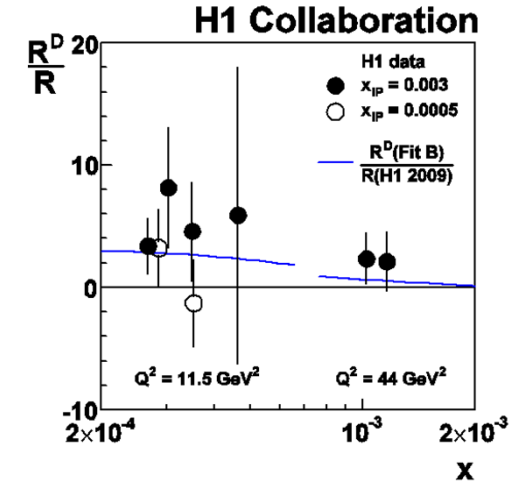
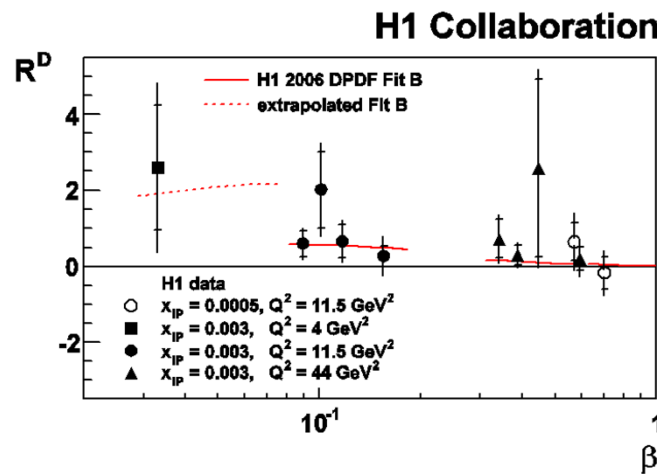
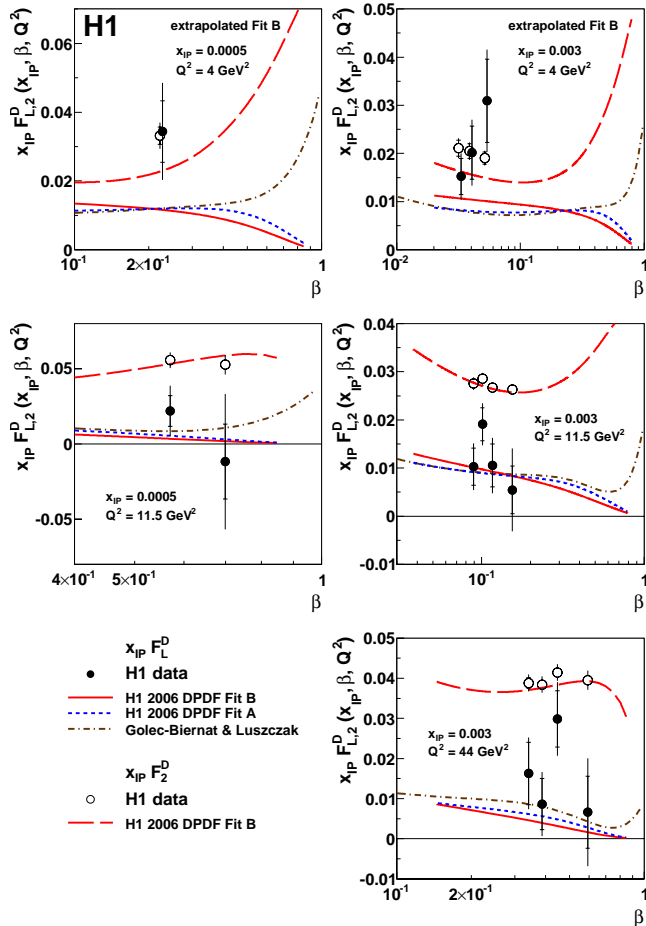
arXiv:1107.3420





# $F_2^D$ and $F_L^D$ structure functions

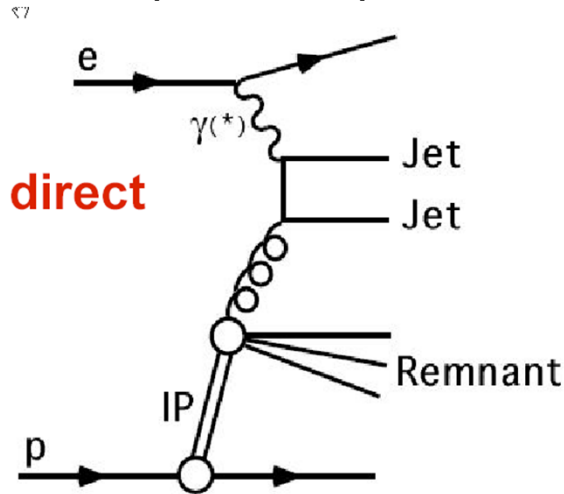
$$R = \sigma_L / \sigma_T \rightarrow F_L^D / (F_2^D - F_L^D)$$



- $F_2^D$  and  $F_L^D$  extracted in bins of  $Q^2$ ,  $x_{IP}$  and  $\beta$
- ➔  $F_2^D$  and  $F_L^D$  data agree with H1 DPDF Fits
- Ratio of  $R^D$  to  $R(\text{incl DIS})$  ➔ longitudinal component is larger in diffraction

# Test of Factorisation: Dijet Photo-production

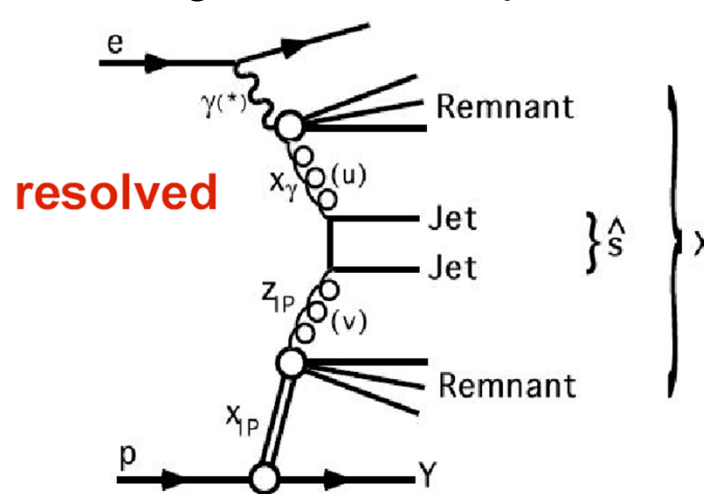
small point-like photon



**direct**

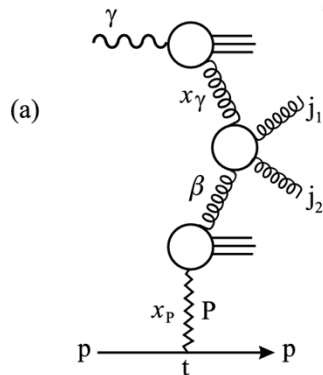
$$x_\gamma = 1$$

large hadron-like photon



**resolved**

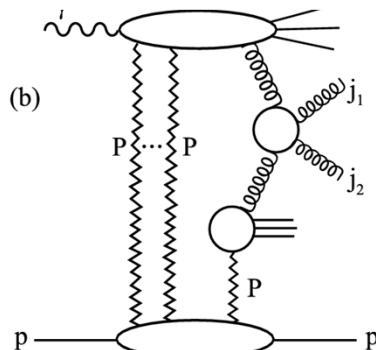
$$x_\gamma < 1$$



(a)

**direct**

M.Kapishin



(b)

**resolved**

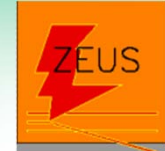
Inclusive Diffraction at HERA

□  $Q^2 \sim 0$ , hard scale  $\rightarrow E_t^{\text{jet}}$  process sensitive to **gluon** density

□ Factorisation in Dijet PhP **expected to be valid in direct photo-production but broken in resolved photo-production** (secondary re-scattering, multi-pomeron exchanges)



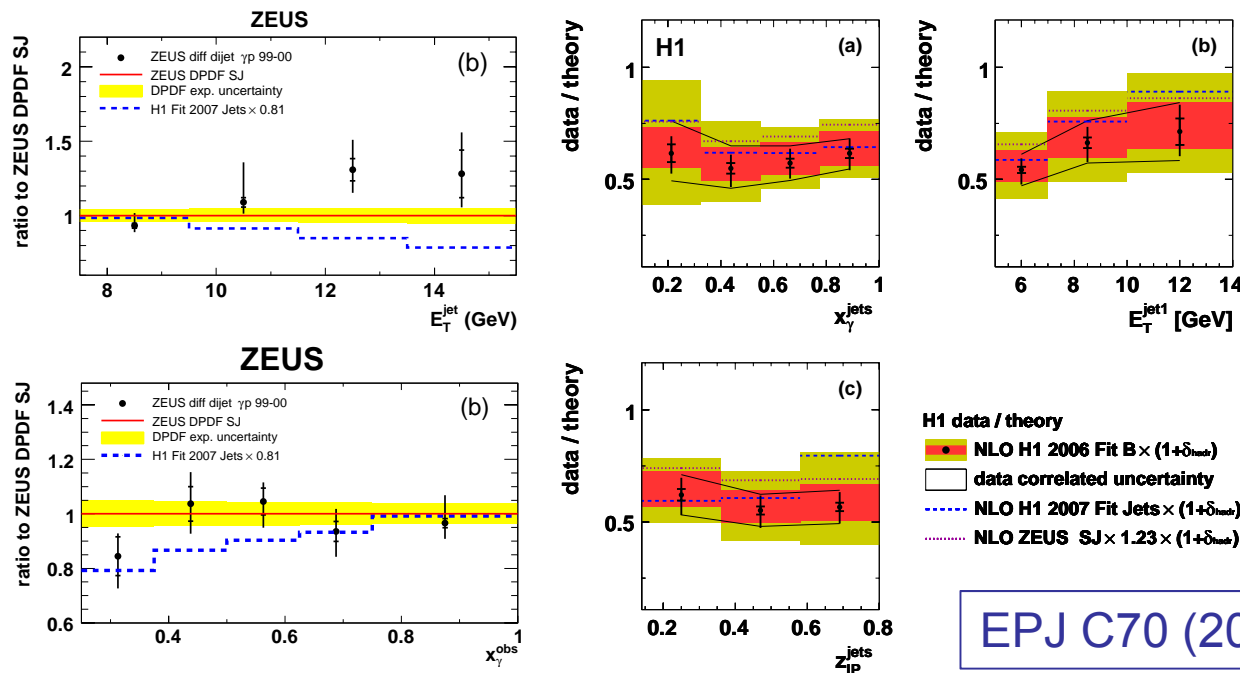
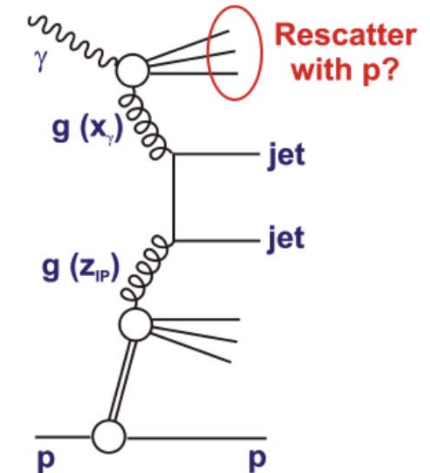
# Diffractive Dijet Photo-production



Gap survival probability:

- ZEUS ( $E_T > 7.5$  GeV) : no evidence for gap distraction
- H1 ( $E_T > 5$  GeV): survival probability  $< 1$  at  $2\sigma$ ,  
 → QCD factorisation breaking

$$\sigma(\text{H1 data}) / \sigma(\text{NLO}) = 0.58 \pm 0.12 (\text{exp.}) \pm 0.14 (\text{scale}) \pm 0.09 (\text{DPDF})$$



- gap survival has little dependence on  $x_\gamma$
- hint of dependence on jet  $E_T$

EPJ C70 (2010) 15



# Summary



- HERA continue to provide unique diffractive DIS data sensitive to structure of color singlet exchange.
- **Agreement** in detail between different analysis methods
- **Proton vertex factorisation** is a good model for diffractive DIS at HERA
- **First combination** of H1 and ZEUS diffractive data with tagged proton give consistent results
- **High statistics H1 and ZEUS LRG data** are in general agreement but require detailed combination
- **Diffractive PDFs** are constrained in QCD fits and tested
- $F_L^D$  structure function is measured by H1
- H1 and ZEUS results for **gap survival** in diffractive dijet photo-production are not conclusive

# Backup slides



# Regge fit

- Assume **proton vertex factorisation** for IP and IR

$$F_2^{D(4)}(\beta, Q^2, x_{IP}, t) = f_{IP}(x_{IP}, t) \cdot F_2^{IP}(\beta, Q^2) + n_{IR} \cdot f_{IR}(x_{IP}, t) \cdot F_2^{IR}(\beta, Q^2)$$

- Parameterization of  $x_{IP}$  and  $t$  dependences for *IP* and *IR*:

$$f_{IP}(x_{IP}, t) = \frac{e^{B_{IP}t}}{x_{IP}^{2\alpha_{IP}(t)-1}} \quad \frac{d\sigma}{dt} \sim \exp B|t|$$

$$\alpha_{IP}(t) = \alpha_{IP}(0) + \alpha'_{IP} t \quad B = B_{IP} + 2\alpha'_{IP} \ln(1/x_{IP})$$

- Fixed parameters for *IR* (as in H1 DPDF Fits):  $\alpha_{IR}(0)=0.5$ ,  $\alpha'_{IR}=0.3 \text{ GeV}^{-2}$ ,  $B_{IR}=1.6 \text{ GeV}^{-2}$ ,  $F_2^{IR}(\beta, Q^2) - \pi$  structure function,  $F_L^D$  contribution corrected using H1 2006 DPDF fit B
- Free parameters:  $\alpha_{IP}(0)$ ,  $\alpha'_{IP}$ ,  $B_{IP}$ ,  $n_{IR}$  and *IP* normalization  $F_2^{IP}(\beta, Q^2)$  in every  $(\beta, Q^2)$  bin



# Results of Regge fits



New H1 FPS  
HERA-2 result:

$$\alpha_{IP}(t) = \alpha_{IP}(0) + \alpha'_{IP} t$$

$$B = B_{IP} + 2\alpha'_{IP} \ln(1/x_{IP})$$

$$\alpha_{IP}(0) = 1.10 \quad 0.02 \text{ (exp.)} \quad 0.03 \text{ (model)}$$

$$\alpha'_{IP} = 0.04 \quad 0.02 \text{ (exp.)} \quad \begin{matrix} 0.08 \\ 0.60 \end{matrix} \text{ (model) GeV}^{-2}$$

$$B_{IP} = 5.73 \quad 0.25 \text{ (exp.)} \quad \begin{matrix} 0.80 \\ 0.90 \end{matrix} \text{ (model) GeV}^{-2}$$

$$\rightarrow \alpha_{IP}(0) \approx \alpha_{IP}(\text{soft}) \sim 1.08$$

$$\rightarrow \alpha'_{IP} \approx 0 \rightarrow \text{no "shrinkage"} \quad (\alpha'_{IP}(\text{soft}) \sim 0.25 \text{ GeV}^{-2})$$

$$\rightarrow B_{IP} \text{ consistent with hard process}$$

Compare with published HERA results:

H1 FPS HERA-1 parameterization:

ZEUS LPS Regge fit:

$$\alpha_{IP}(0) = 1.114 \pm 0.022 \text{ (exp.)} \pm_{0.020}^{0.040} \text{ (model)}$$

$$\alpha_{IP}(0) = 1.11 \pm 0.02 \text{ (stat.)} \pm_{0.02}^{0.01} \text{ (syst.)} \pm 0.02 \text{ (model)}$$

$$\alpha'_{IP} = 0.06_{-0.06}^{+0.19} \text{ GeV}^{-2}$$

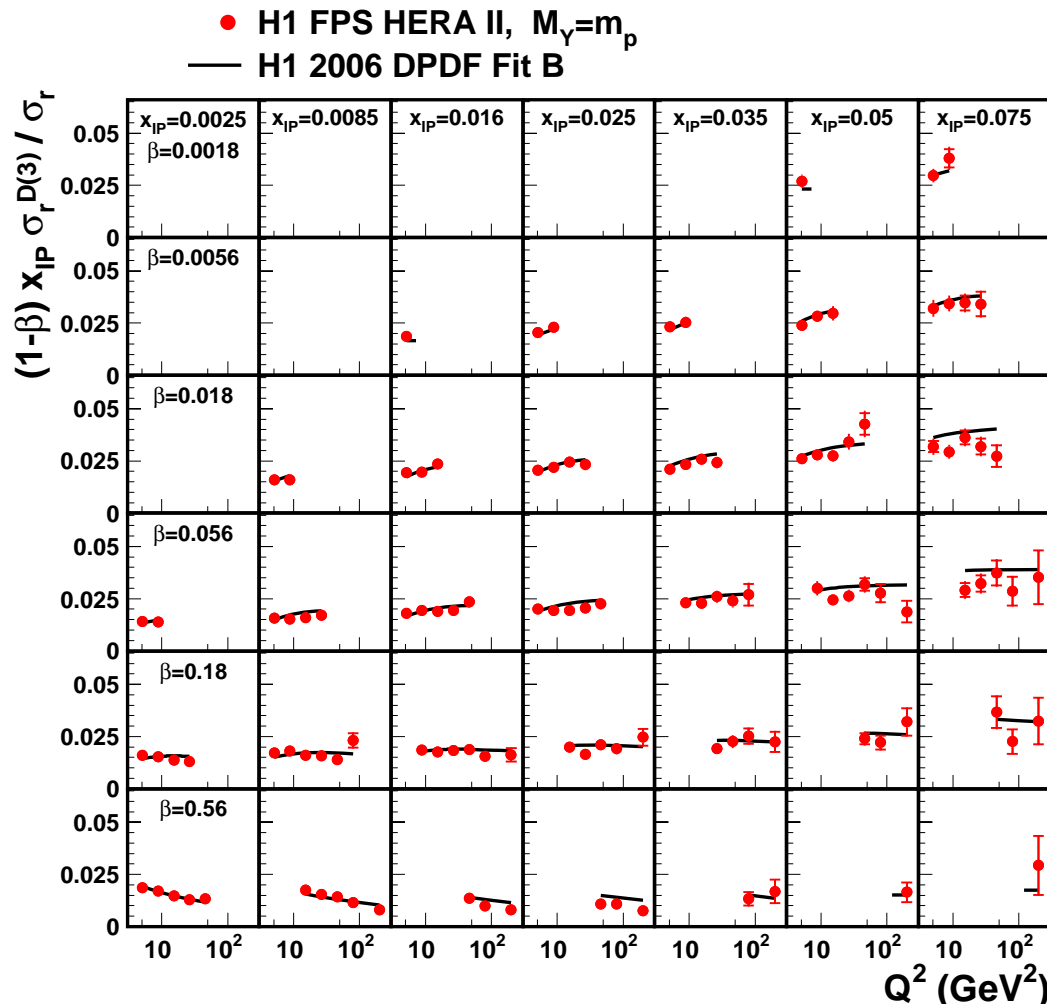
$$\alpha'_{IP} = -0.01 \pm 0.06 \text{ (stat.)} \pm_{0.08}^{0.04} \text{ (syst.)} \pm 0.04 \text{ (model) GeV}^{-2}$$

$$B_{IP} = 5.5_{+0.7}^{-2.0} \text{ GeV}^{-2}$$

$$B_{IP} = 7.1 \pm 0.7 \text{ (stat.)} \pm_{0.7}^{1.4} \text{ (syst.) GeV}^{-2}$$



# Ratio $\sigma_r^{D(3)}/\sigma_r^{incl}$ : $Q^2$ dependence



$Q^2$ -dependence in  $(x_{IP}, \beta)$  bins  
 $M_x > 2$  GeV,  $|t| < 1$  GeV<sup>2</sup>

→ Ratio is flat or weakly rises with  $Q^2$  except at highest  $\beta$

→ similar shape of diffractive and inclusive quark PDF in proton at low  $x = x_{IP} \beta$

→ extract  $\ln Q^2$  derivative sensitive to gluon PDF

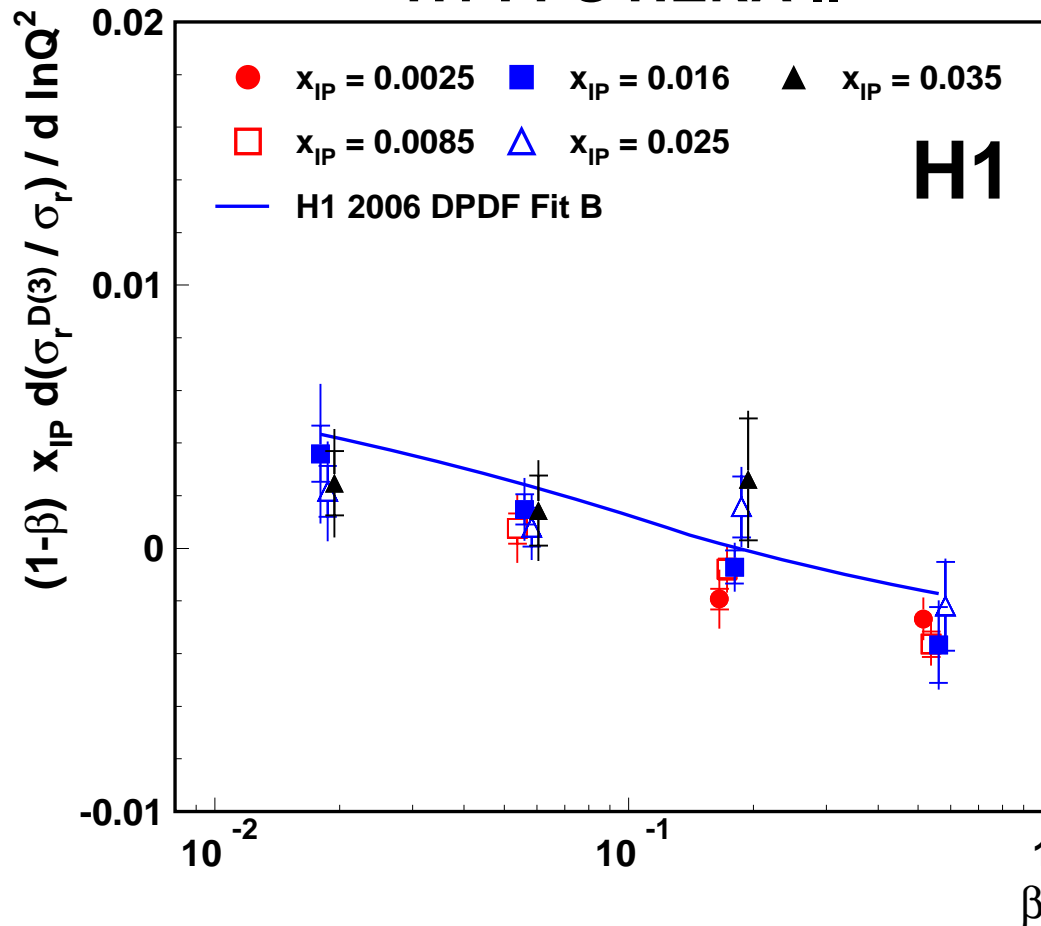




# Ratio $\sigma_r^{D(3)} / \sigma_r^{incl}$ : $\ln Q^2$ derivative

- Slope  $D$ :  $(1-\beta)x_{IP}\sigma_r^D / \sigma_r^{incl} = A + D \ln Q^2 \rightarrow \ln Q^2$ -dependence in selected  $(x_{IP}, \beta)$  bins

## H1 FPS HERA II



- $\ln Q^2$  slope is consistent with zero within  $3\sigma$  of exp. uncertainties

$\rightarrow (\text{gluon/quark})^{diff} \sim (\text{gluon/quark})^{incl}$   
in proton at low  $x=x_{IP}\beta$

- weak decrease of  $\ln Q^2$  slope with  $\beta$  reproduced by DPDF / PDF predictions