

# SQuark Massenbestimmung am CLIC

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# Current Colliders: The Large Hadron Collider

Current Cutting Edge accelerator:  
Large Hadron Collider

*G. Weiglein et al. / Physics Reports 426 (2006) 47–358*

Up to 14 TeV p-p

High Luminosity

Very good detectors

Hadron collider  $\Rightarrow$  p-p

Initial State unknown

Energy

Particle

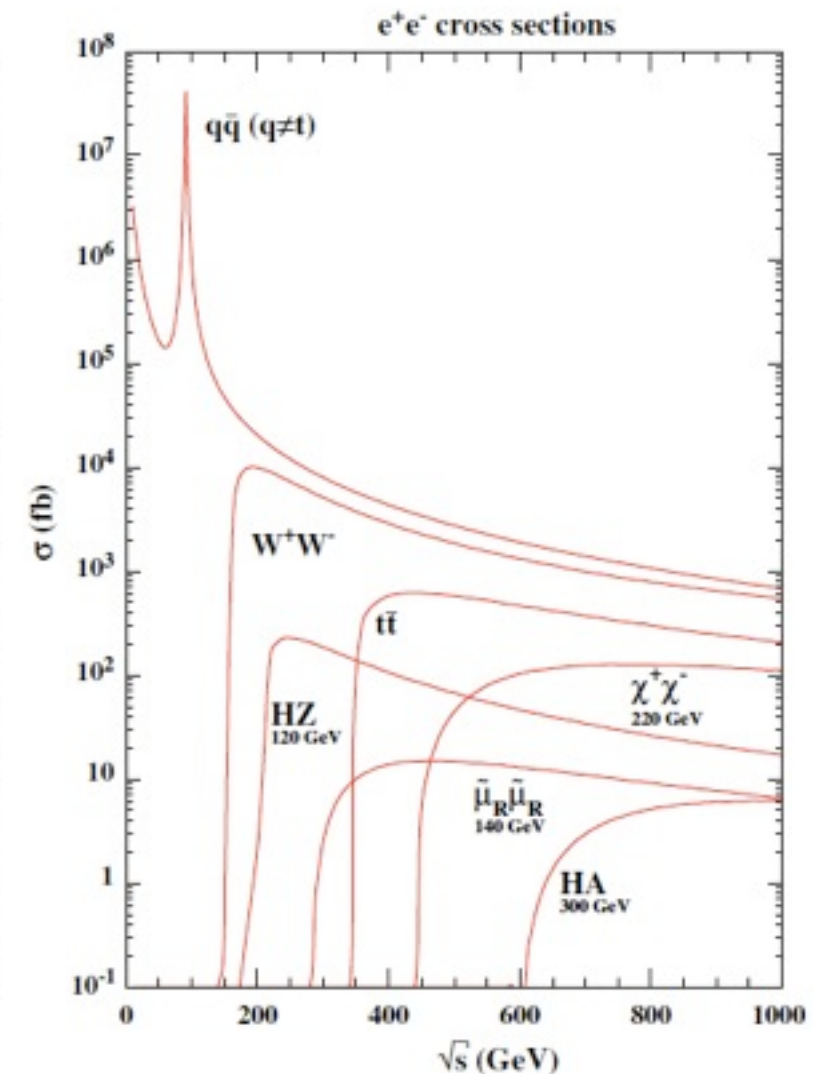
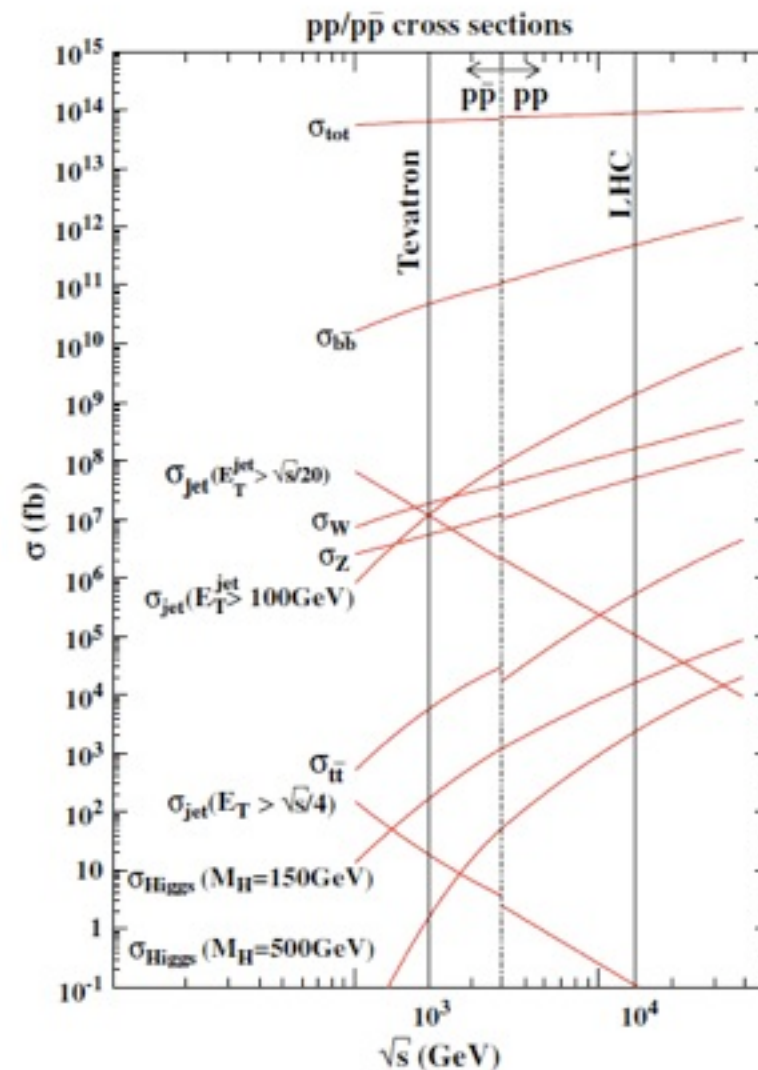
Underlying event(s)

Pile-Up

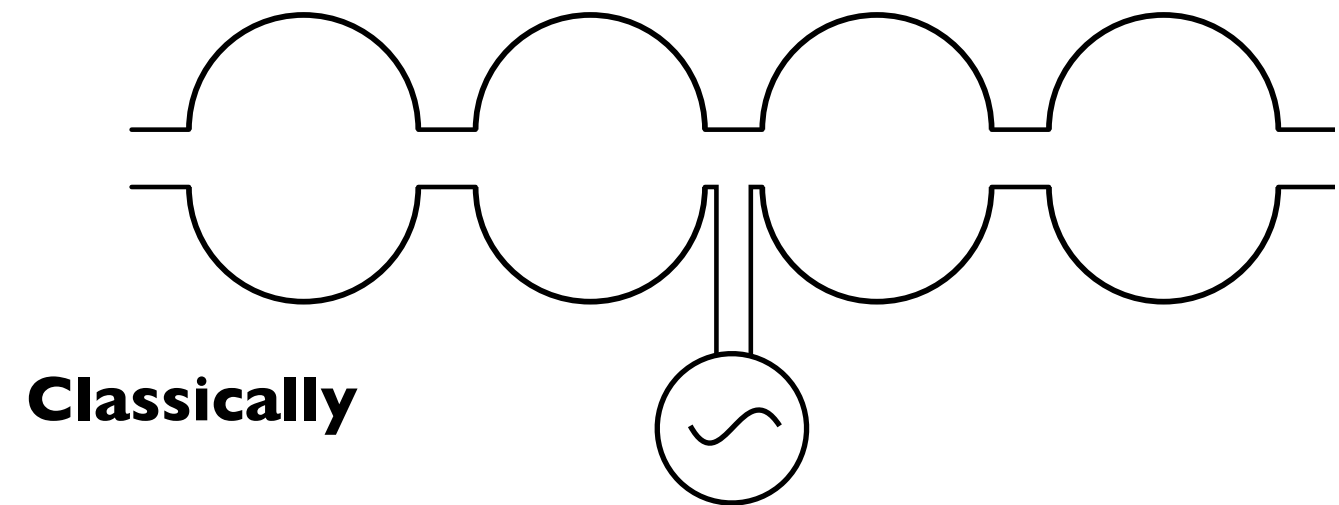
Huge xs for Background

For precision measurements we need a much cleaner environment!

$\Rightarrow$  Lepton Collider



# The Compact Linear Collider

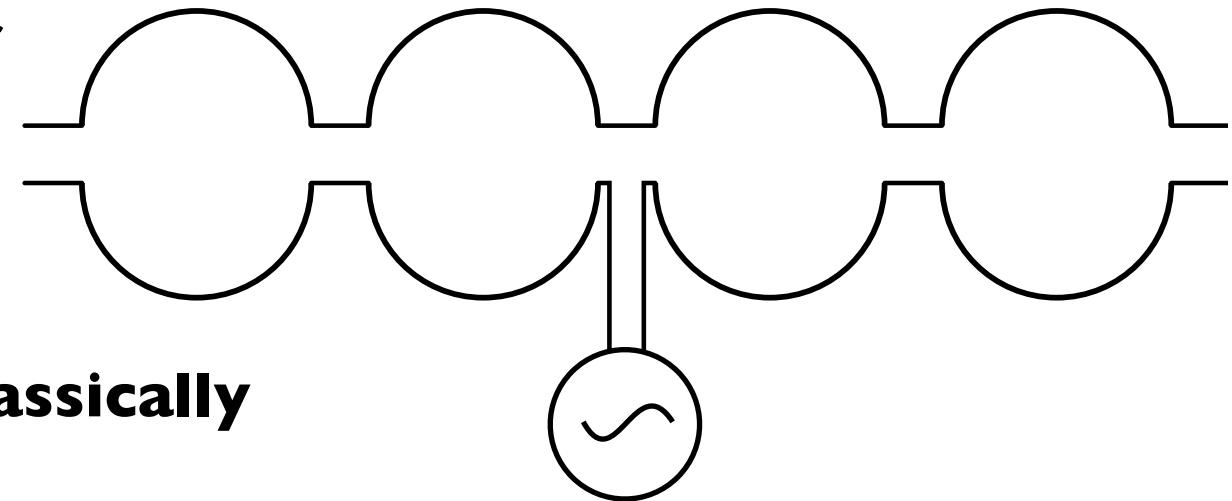


# The Compact Linear Collider



— [ Synchrotron radiation → Needs to be linear accelerator

— [ Acceleration of charged particles via Cavity

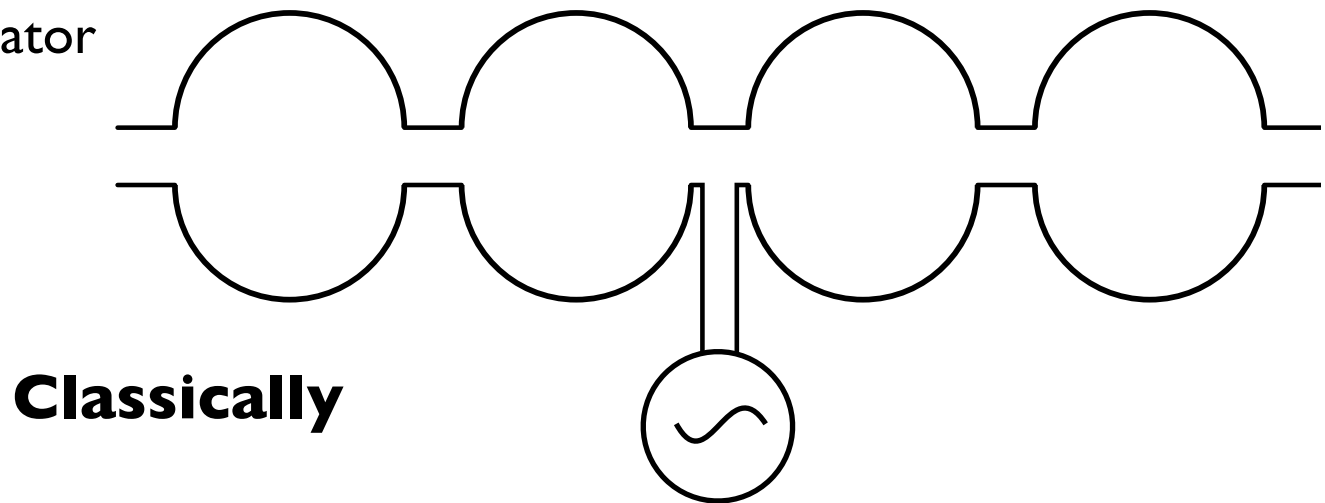


**Classically**

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- [ Synchrotron radiation → Needs to be linear accelerator
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- Limits on Voltage / Frequency



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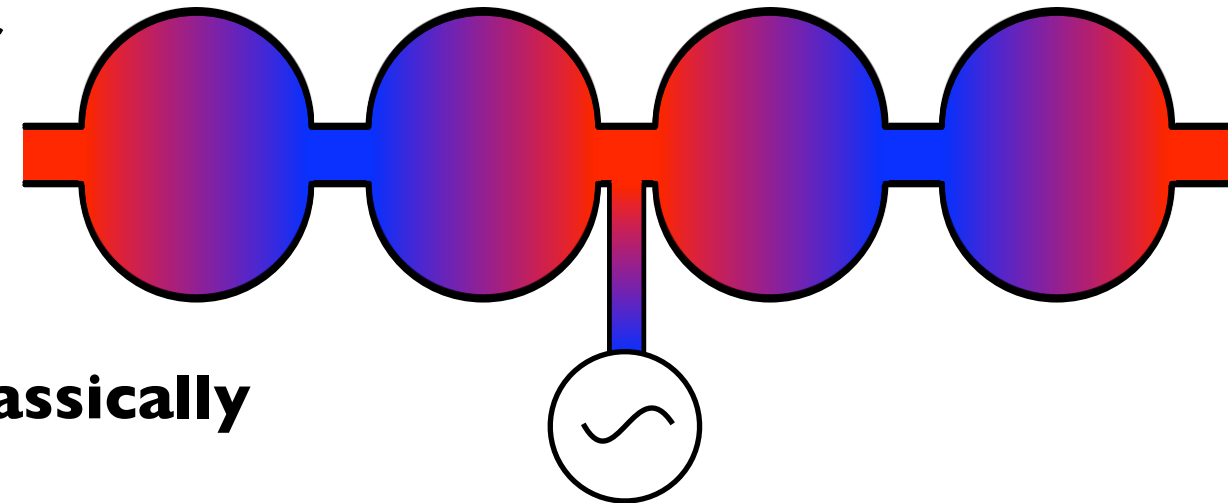


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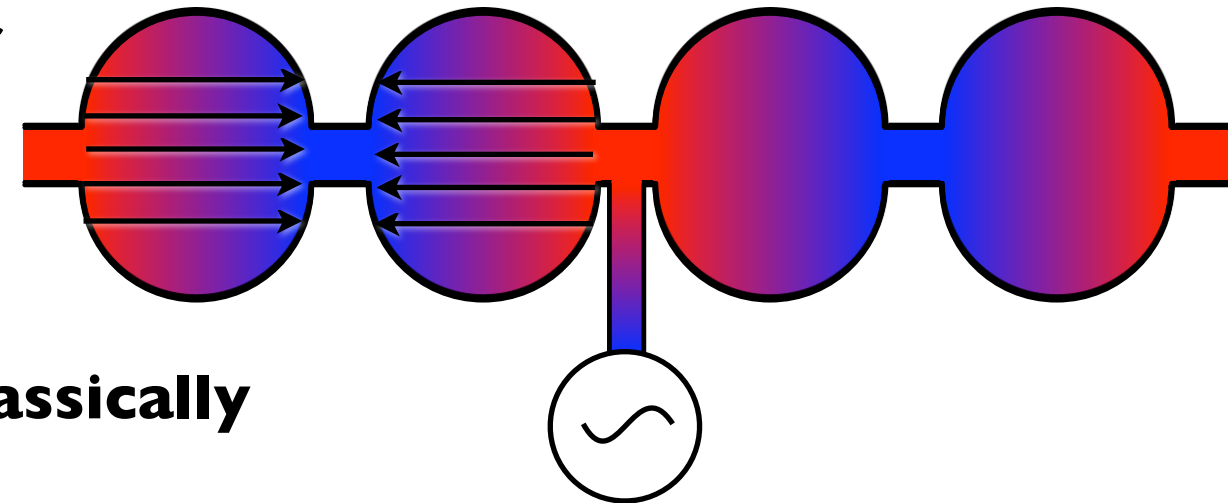


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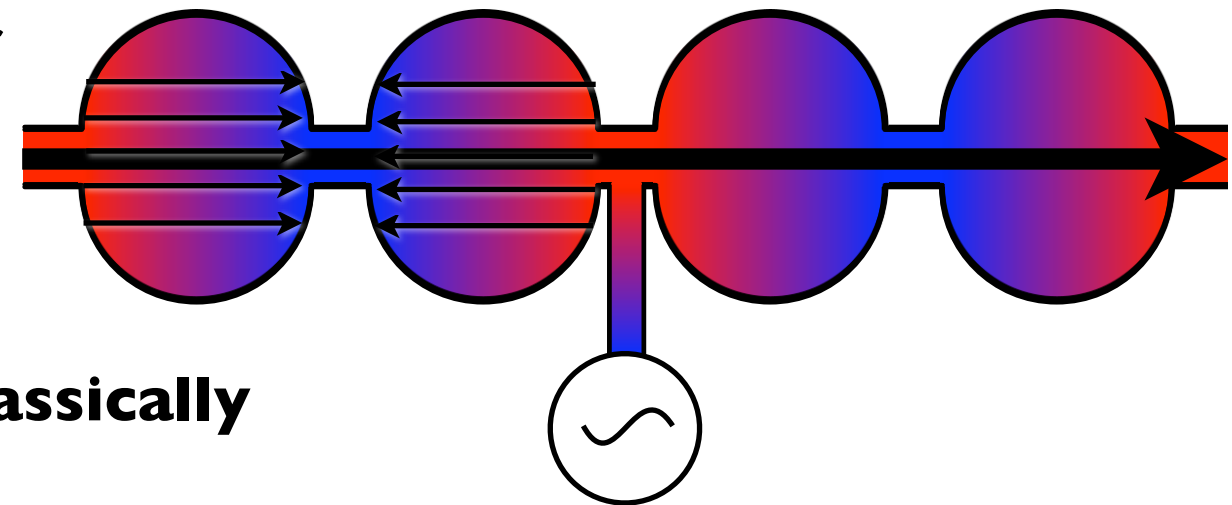


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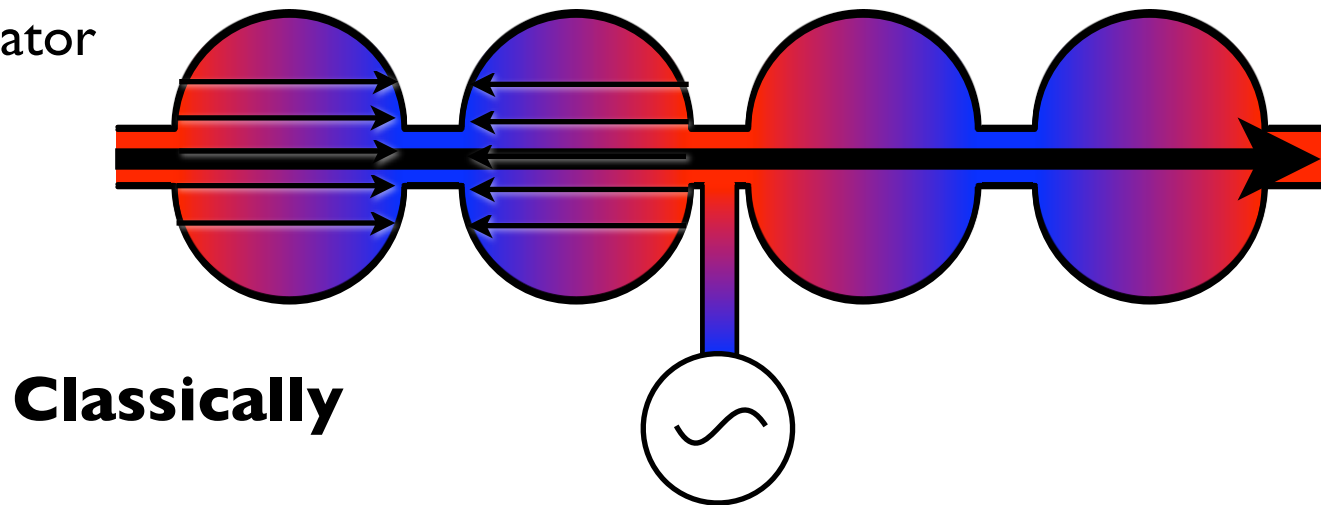


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- [ New way of creating RF:
  - 2nd beam
    - Parallel to actual (high energy) beam
    - Low energy
    - High intensity
  - Extract RF from this beam via a „double cavity“



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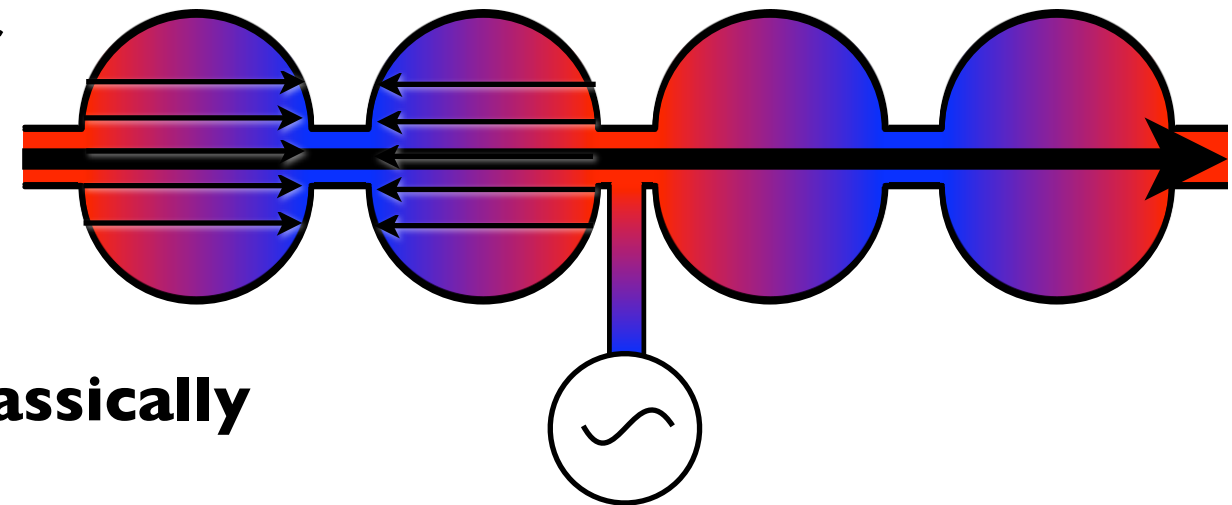
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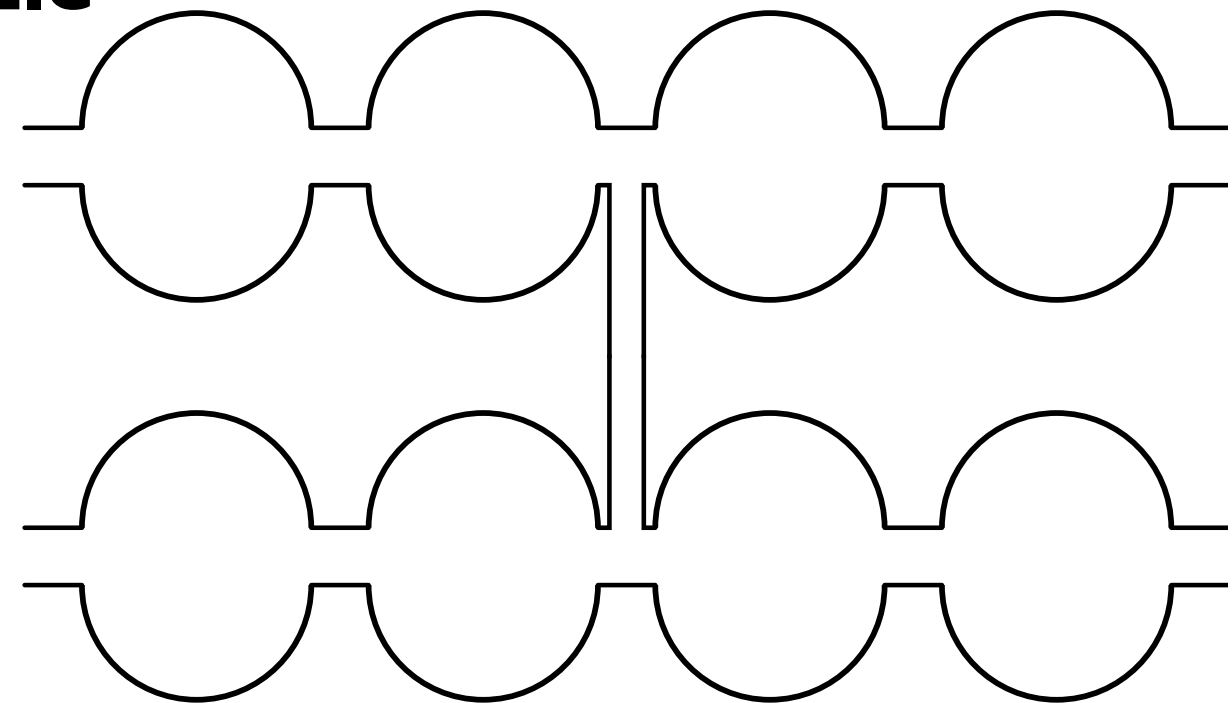
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High Energy / Low Intensity

**CLIC**



Low Energy / High Intensity

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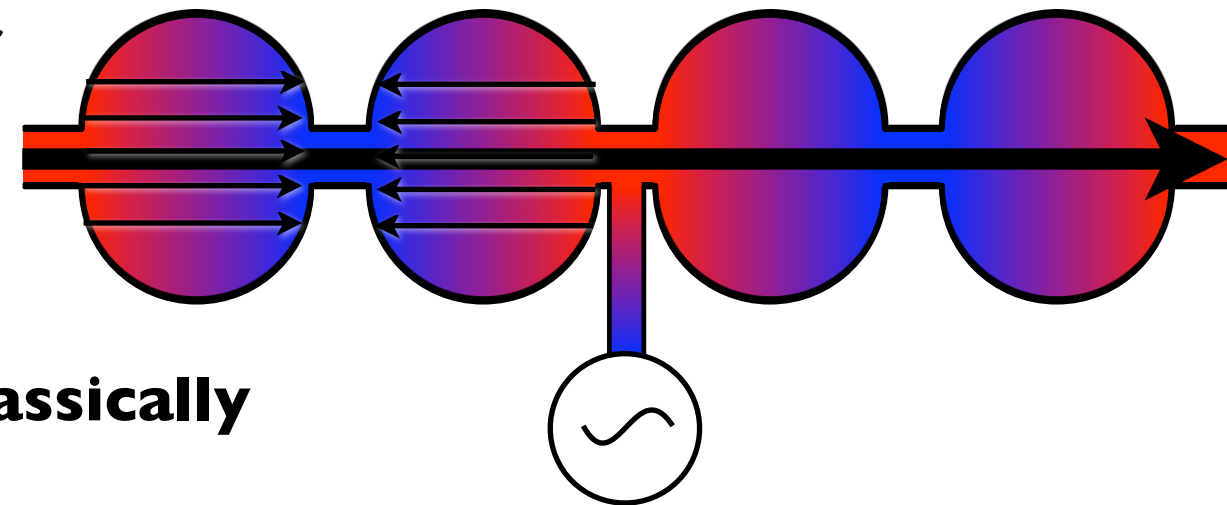
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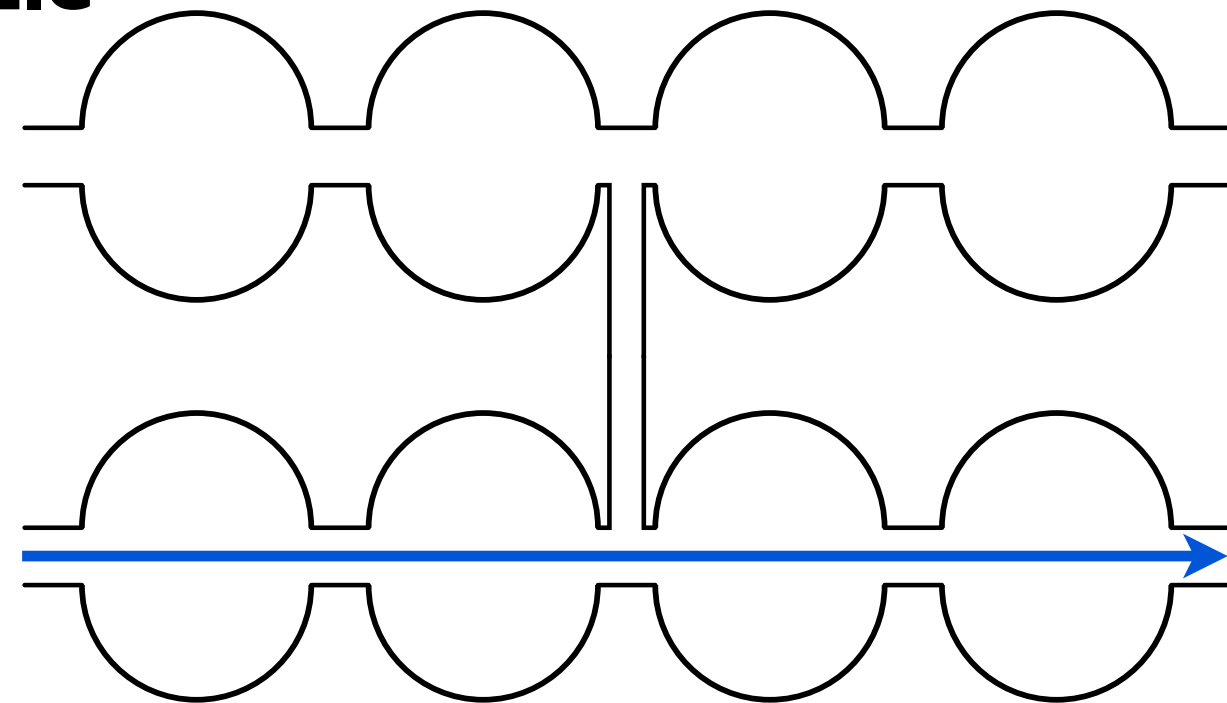
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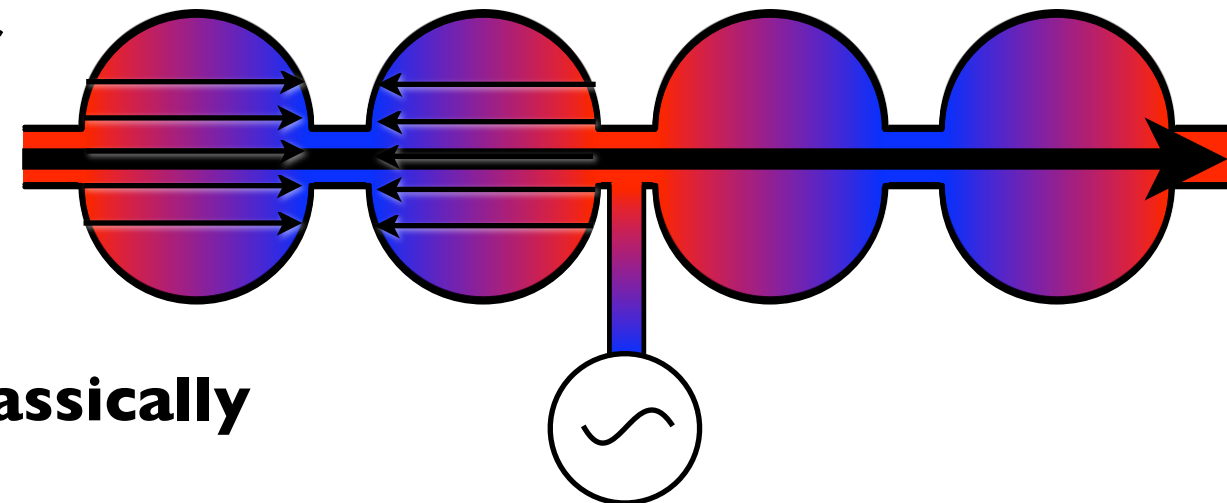
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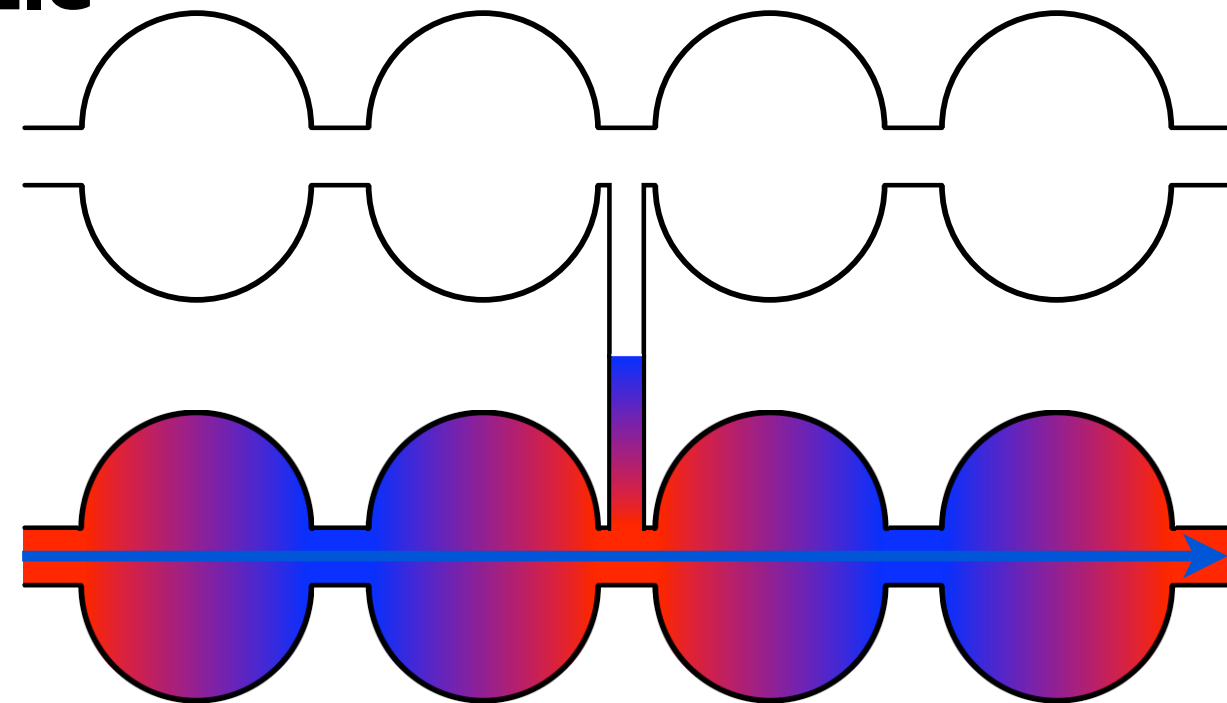
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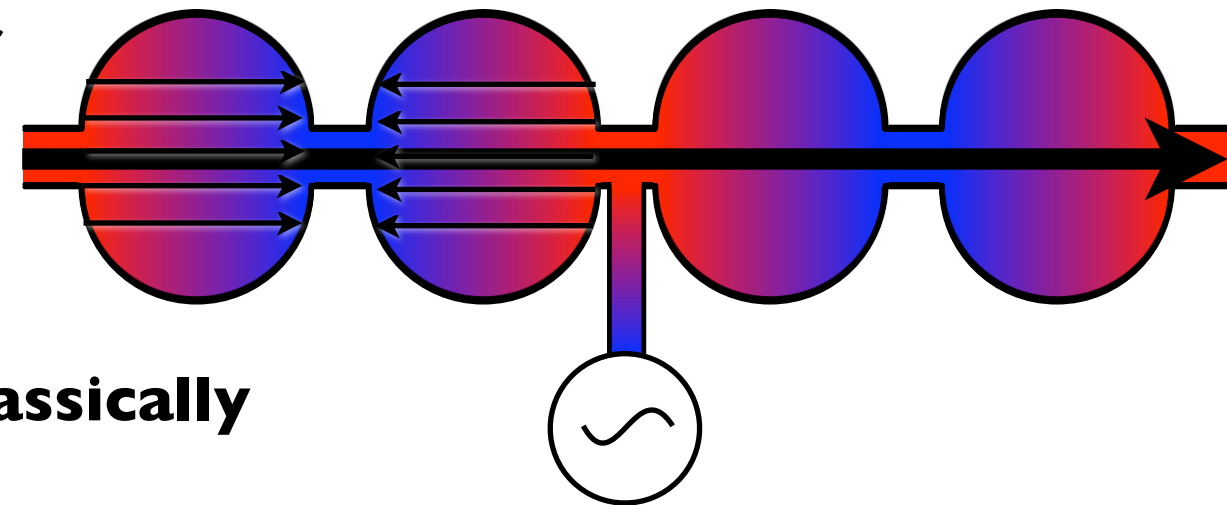
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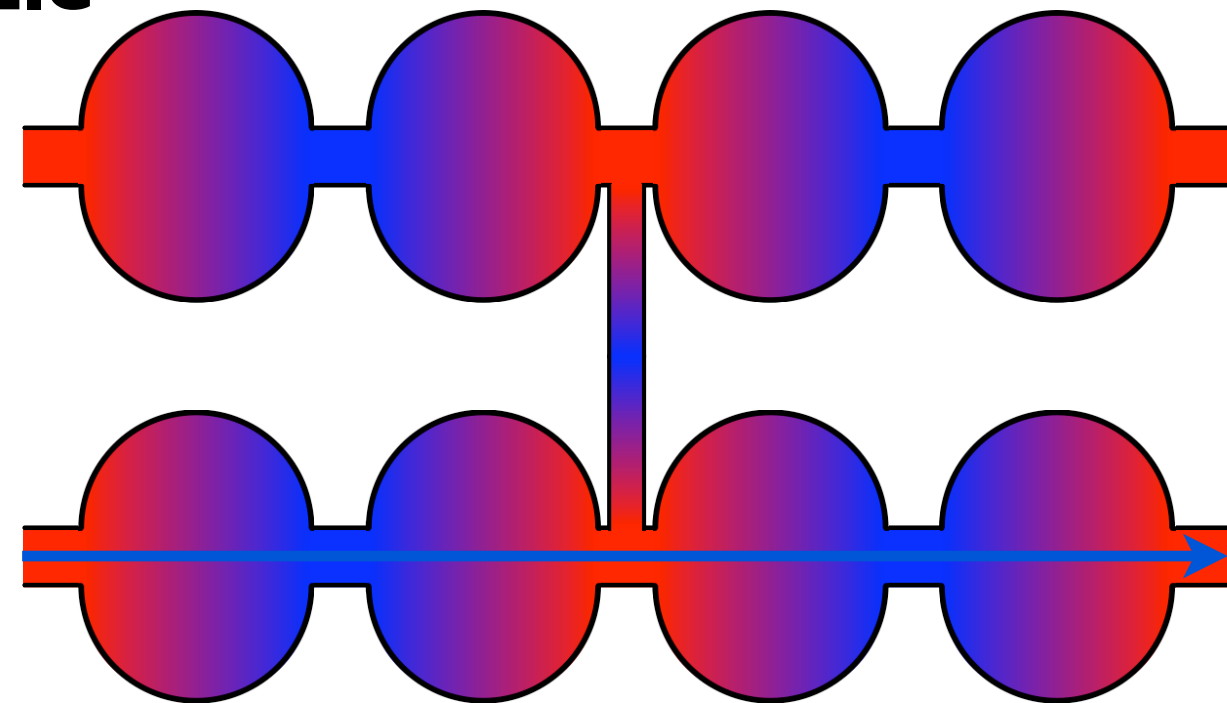
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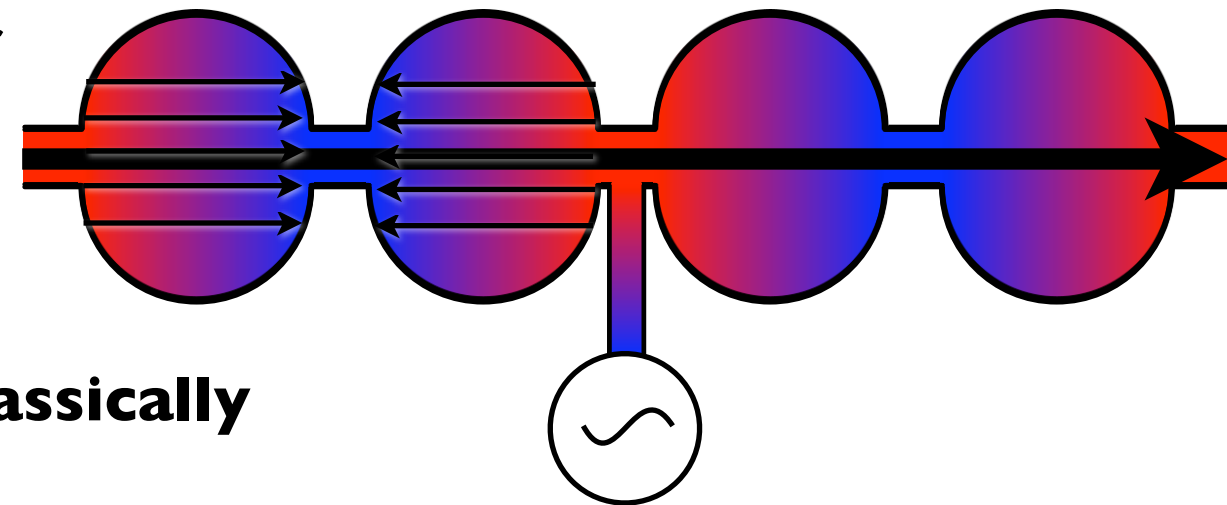
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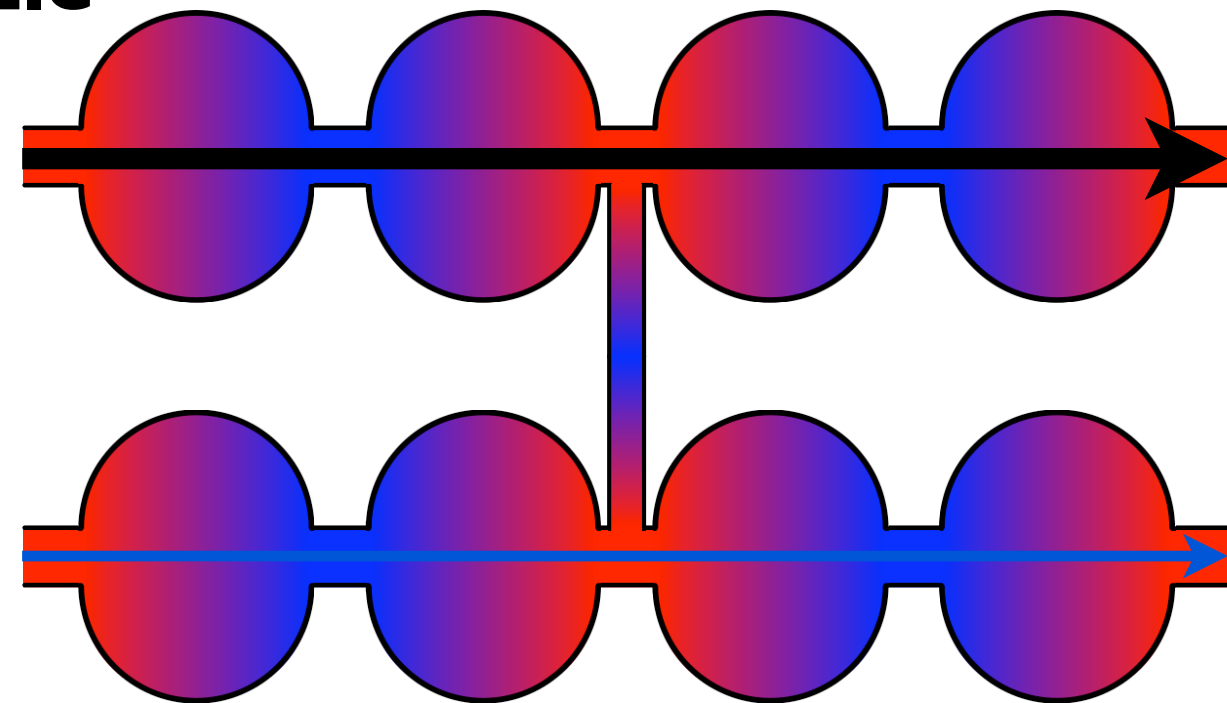
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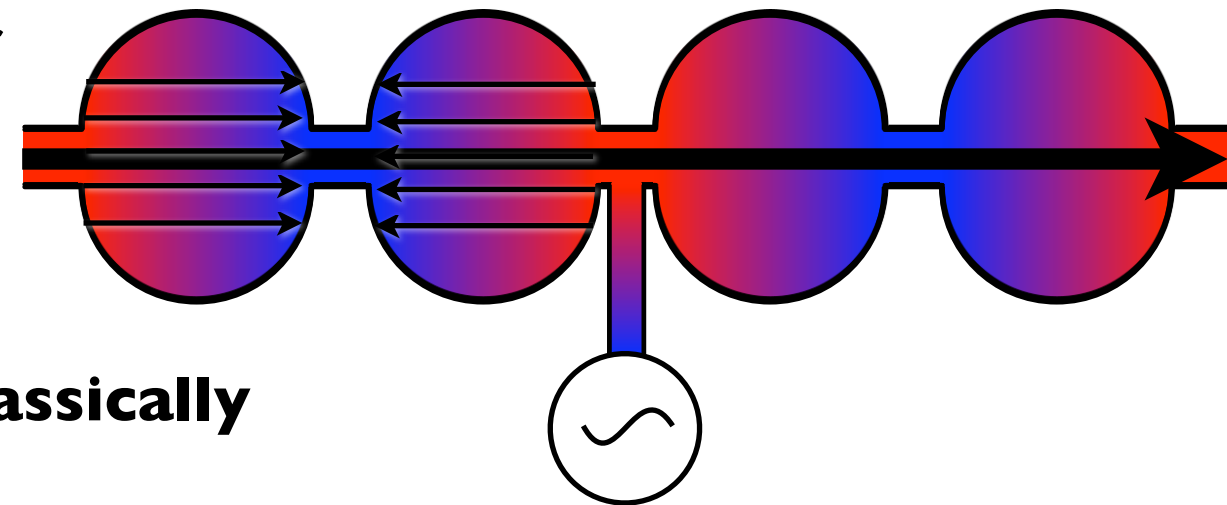
— More than 100MeV/m possible

— 3 TeV: ~50km length  
(incl. beam delivery system)

➔ Compact Linear Collider: CLIC

— 300 Bunches / Train

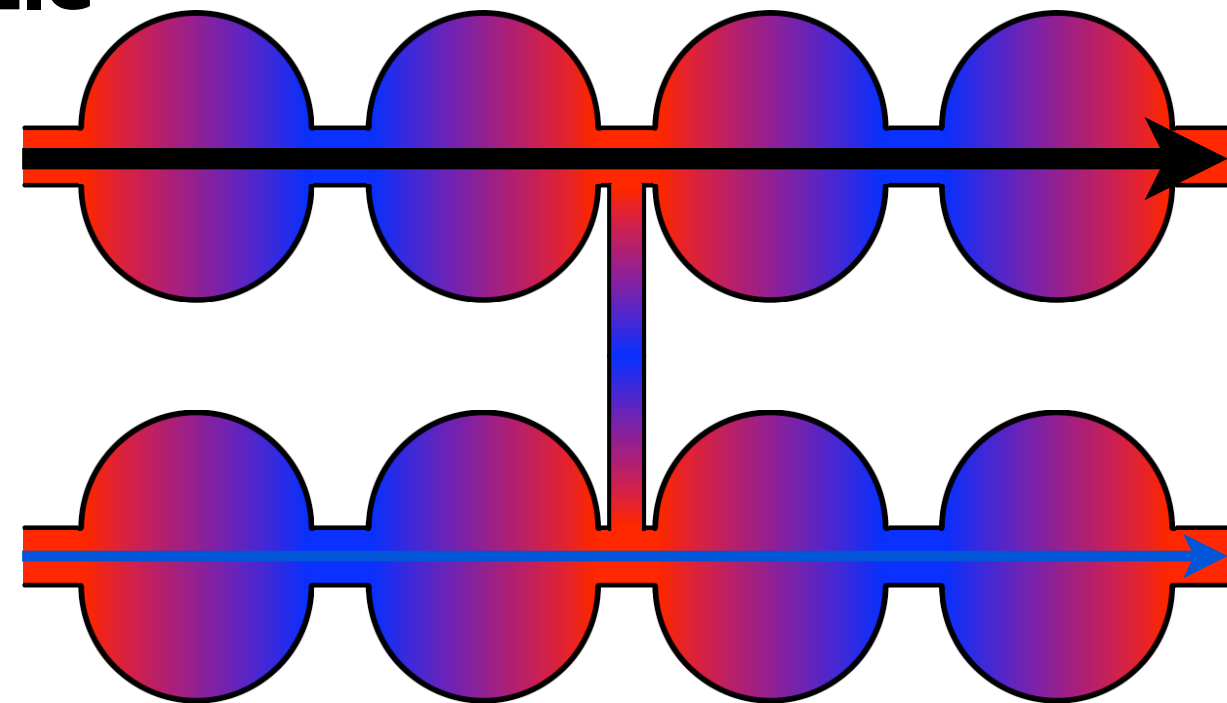
— 0.5 ns Repetition Rate



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# The CLIC Conceptional Design Report: A Benchmark

|             |                    | particle                   | mass [GeV] |
|-------------|--------------------|----------------------------|------------|
| $m_0$       | $= 303\text{GeV}$  | $\chi_1^0$                 | 328.3      |
| $A_0$       | $= -750\text{GeV}$ | $\tilde{u}_R, \tilde{c}_R$ | 1125.7     |
| $\mu$       | $> 0$              | $\tilde{d}_R, \tilde{s}_R$ | 1116.1     |
| $\tan\beta$ | $= 24$             | $\tilde{g}_R$              | 1239.7     |
| $M_1$       | $= 780\text{GeV}$  |                            |            |
| $M_2$       | $= 940\text{GeV}$  |                            |            |
| $M_3$       | $= 540\text{GeV}$  |                            |            |

— To show the Capabilities of CLIC:  
Conceptional Design Report (CDR)

— Check performance of Detector/Accelerator

— Dedicated SUSY Scenario

— Benchmark: Measurement of mass of right handed SQuarks

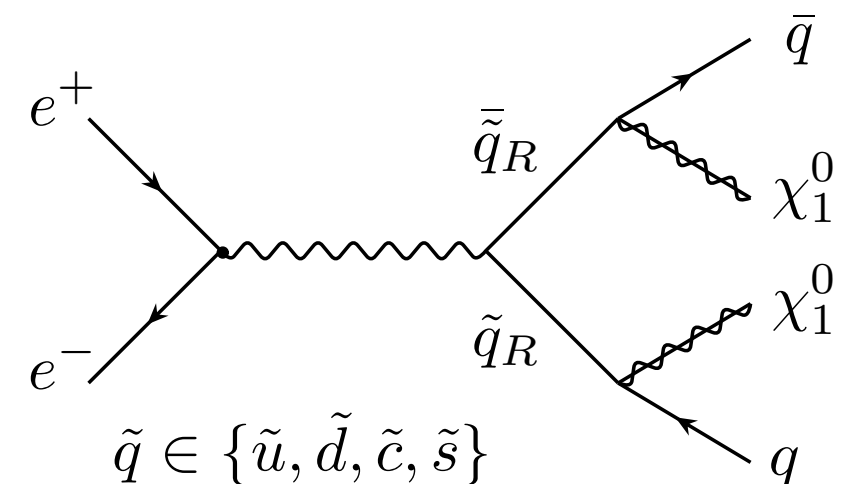
— Decay almost exclusively into 2 Quarks plus Neutralino

— Low crosssection ( $\sim 3000$  events after 5 years running)

— Event shape: 2 Quarks +  $E_{\text{miss}}$

— Very general (not bound to this SUSY scenario)

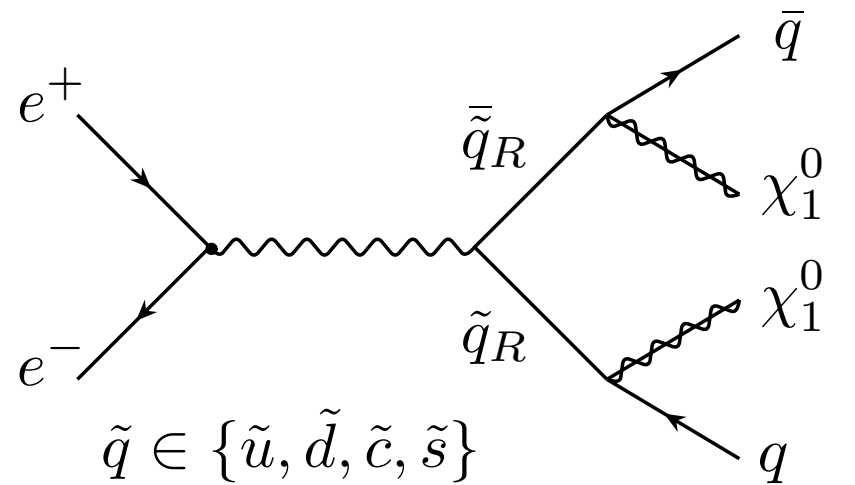
— Easy to identify



$$e^+e^- \rightarrow \tilde{q}_R \tilde{\bar{q}}_R$$

$$\tilde{q}_R \xrightarrow{99.7\%} q + \chi_1^0$$

# The Process + Background



$$e^+ e^- \rightarrow \tilde{q}_R \bar{\tilde{q}}_R$$

$$\tilde{q}_R \xrightarrow{99.7\%} q + \chi_1^0$$

|                      | Final State    | $\sigma$               |
|----------------------|----------------|------------------------|
| Signal               | qqXX (u,d,s,c) | $\sim 1.45 \text{ fb}$ |
| SM                   | qq             | $\sim 3000 \text{ fb}$ |
|                      | qqee           | $\sim 3300 \text{ fb}$ |
| SM $E_{\text{miss}}$ | qqvv           | $\sim 1500 \text{ fb}$ |
|                      | qqev           | $\sim 5300 \text{ fb}$ |
|                      | TTVV           | $\sim 130 \text{ fb}$  |
| SUSY                 | qqvvXX         | $\sim 1.0 \text{ fb}$  |
|                      | qqlvXX         | $\sim 8.5 \text{ fb}$  |
|                      | qqllXX         | $\sim 0.6 \text{ fb}$  |

no  $E_{\text{miss}}$

dominant BG

Signal Process signature:

2 Jets +  $E_{\text{miss}}$

Background

Dominated by SM Neutrino Processes

Crosssection 3-4 orders higher!

Good Background rejection needed

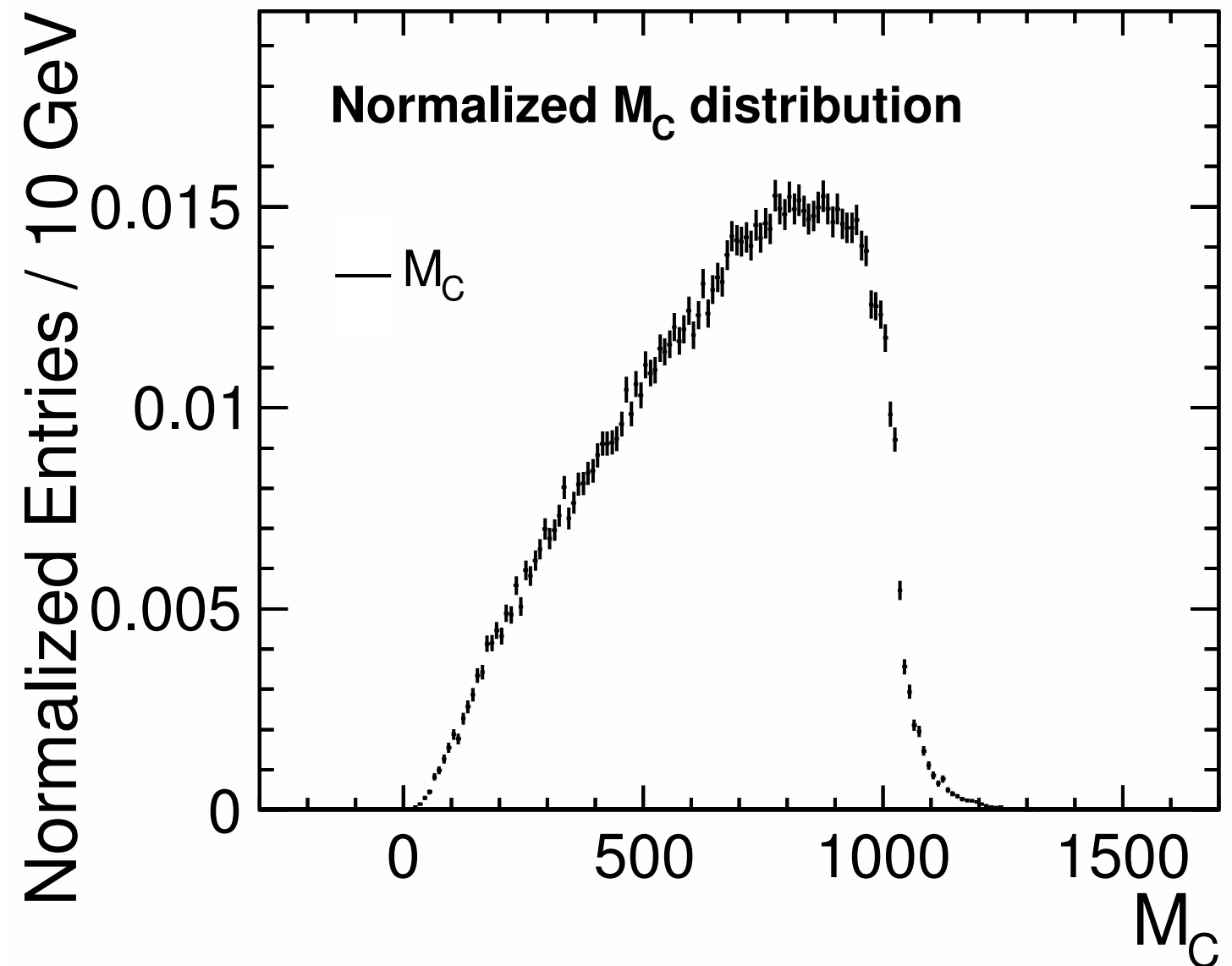
first step:  $p_t > 600 \text{ GeV}$

➡ only SM  $E_{\text{miss}}$  relevant

# Measurement Techniques: $M_C$

$$\begin{aligned} M_C^2 &= (E_1 + E_2)^2 - (\vec{p}_1 - \vec{p}_2)^2 \\ &= 2(E_1 E_2 + \vec{p}_1^2 \vec{p}_2^2) \end{aligned}$$

- Modification of invariant Mass
- Use @ LHC as transversal variant
- Neutralino mass has to be known
- Squark mass extraction:
  - Formula (using the upper edge)
  - Template Fit (used in this analysis)



$$M_{C,\max} = \frac{m_{\tilde{q}}^2 - m_{\chi}^2}{m_{\tilde{q}}}$$

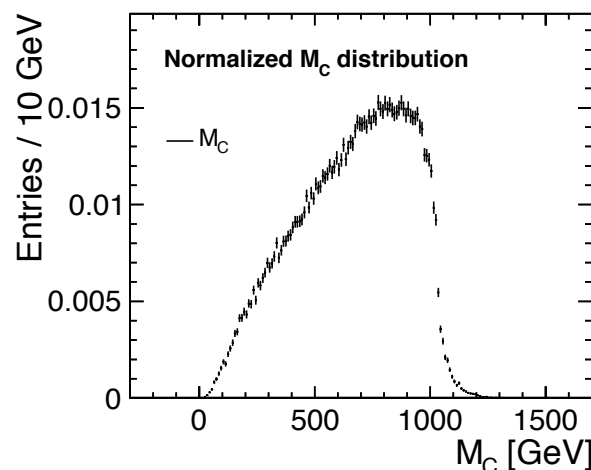
# $M_C$ : Signal plus Background

After full reconstruction:  $p_t > 600\text{GeV}$

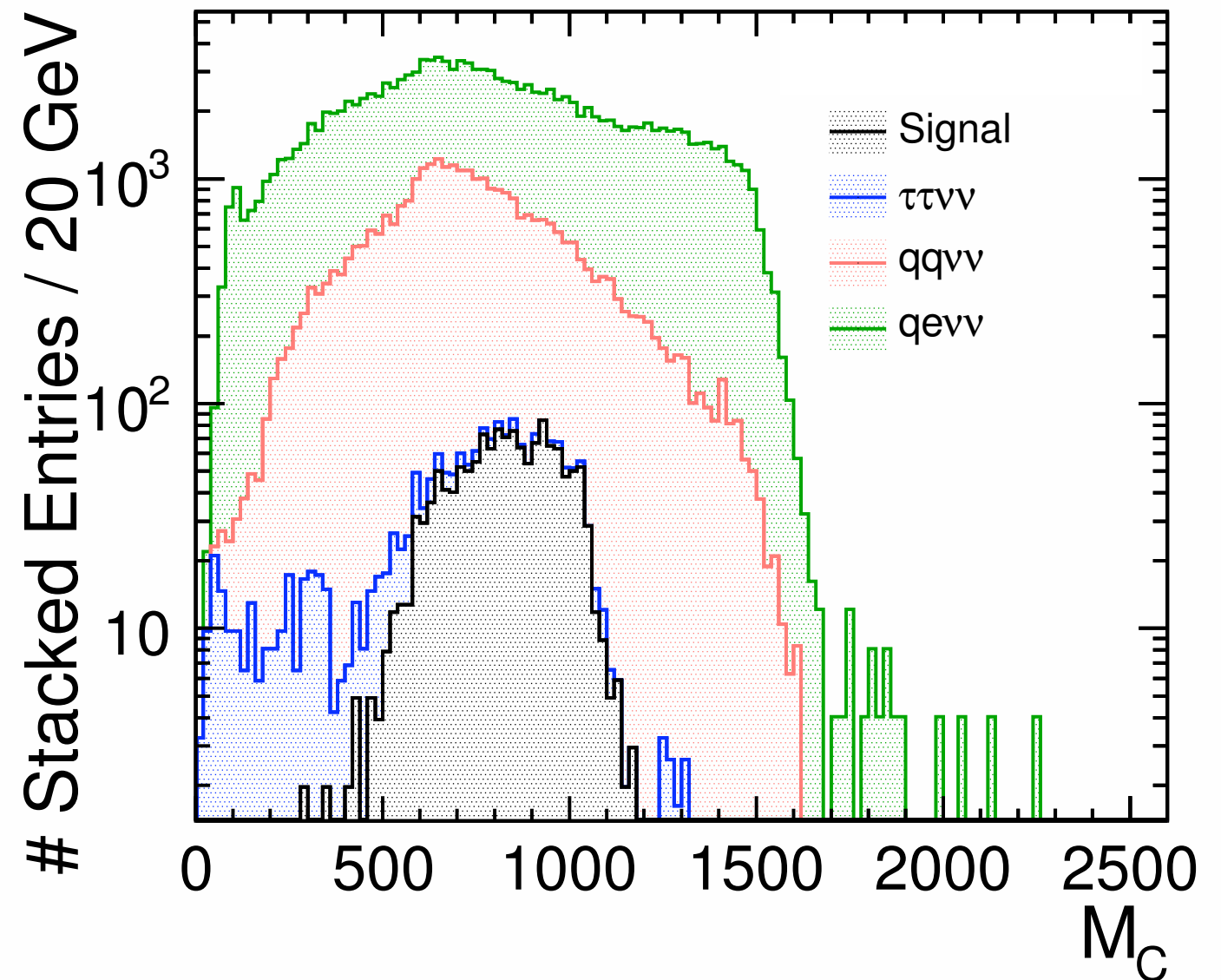
$$\Rightarrow S/B = 1/1000$$

Background rejection needed

- Cut based
- ID Cuts on various distributions (e.g.  $E_{\text{vis}}$ , Jet angle,/energy, ...)
- proved inefficient
- Multi dimensional Analysis
- Boosted Decision Trees



| $p_t > 600\text{GeV}$ | # Events |
|-----------------------|----------|
| Signal                | 1430     |
| Background            | 145000   |



# Background rejection: Boosted Decision Trees

Background rejection with Boosted Decision Trees:

Framework:  
TMVA (ROOT package)

Splitting Data into 2 independent samples:

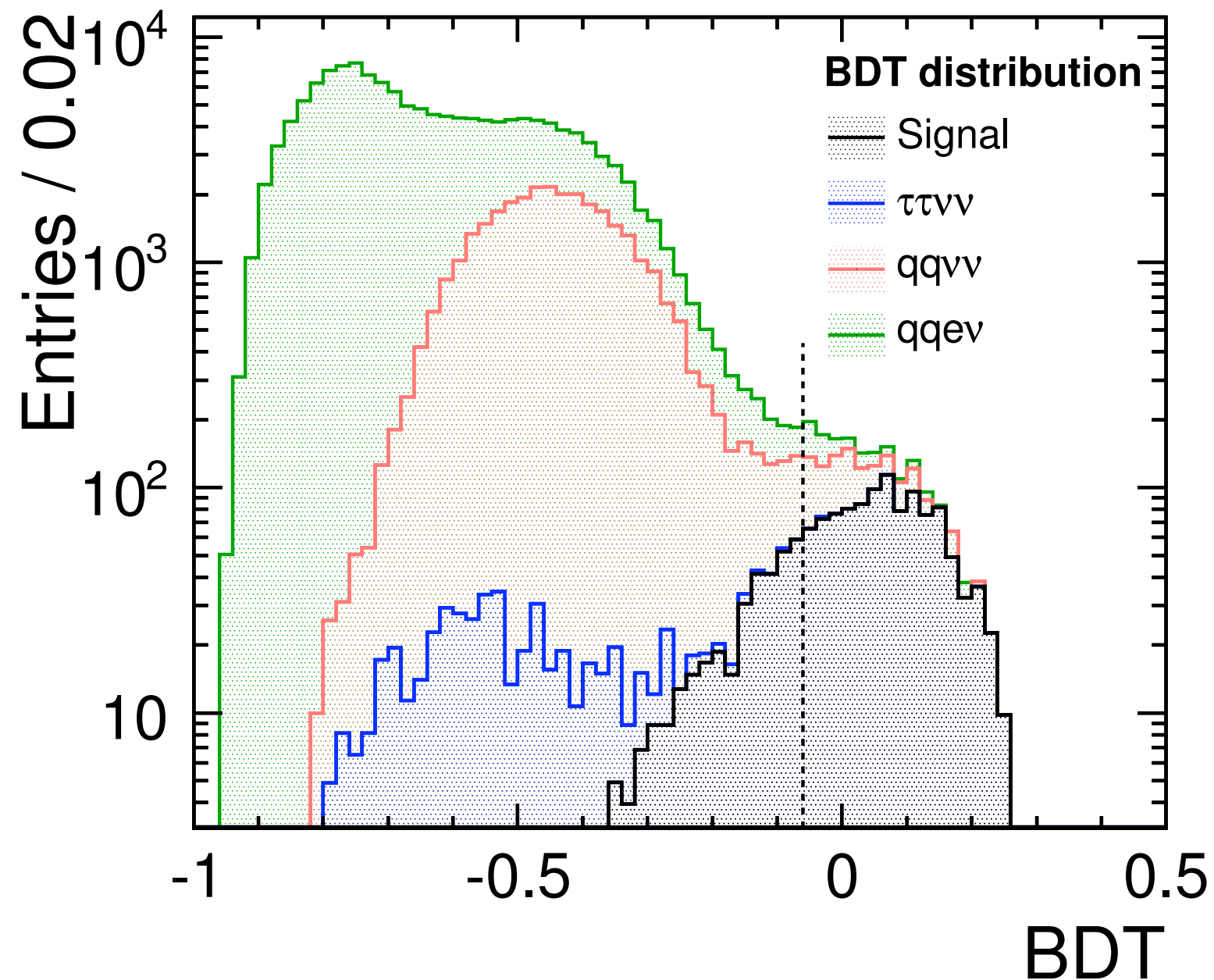
1. Training and Testing

2. Analysis

Used BDT Cut

BDT > -0.05

$S/\sqrt{S+B} \approx 25$



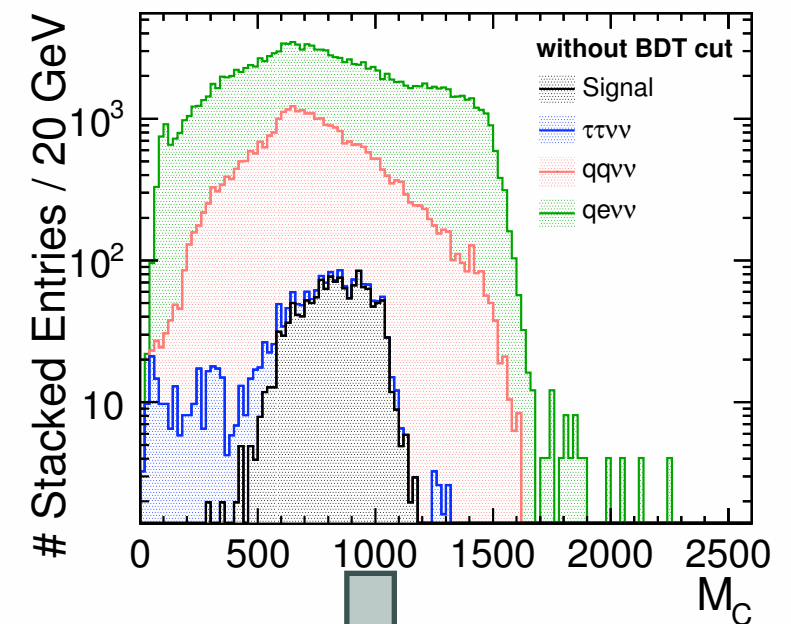
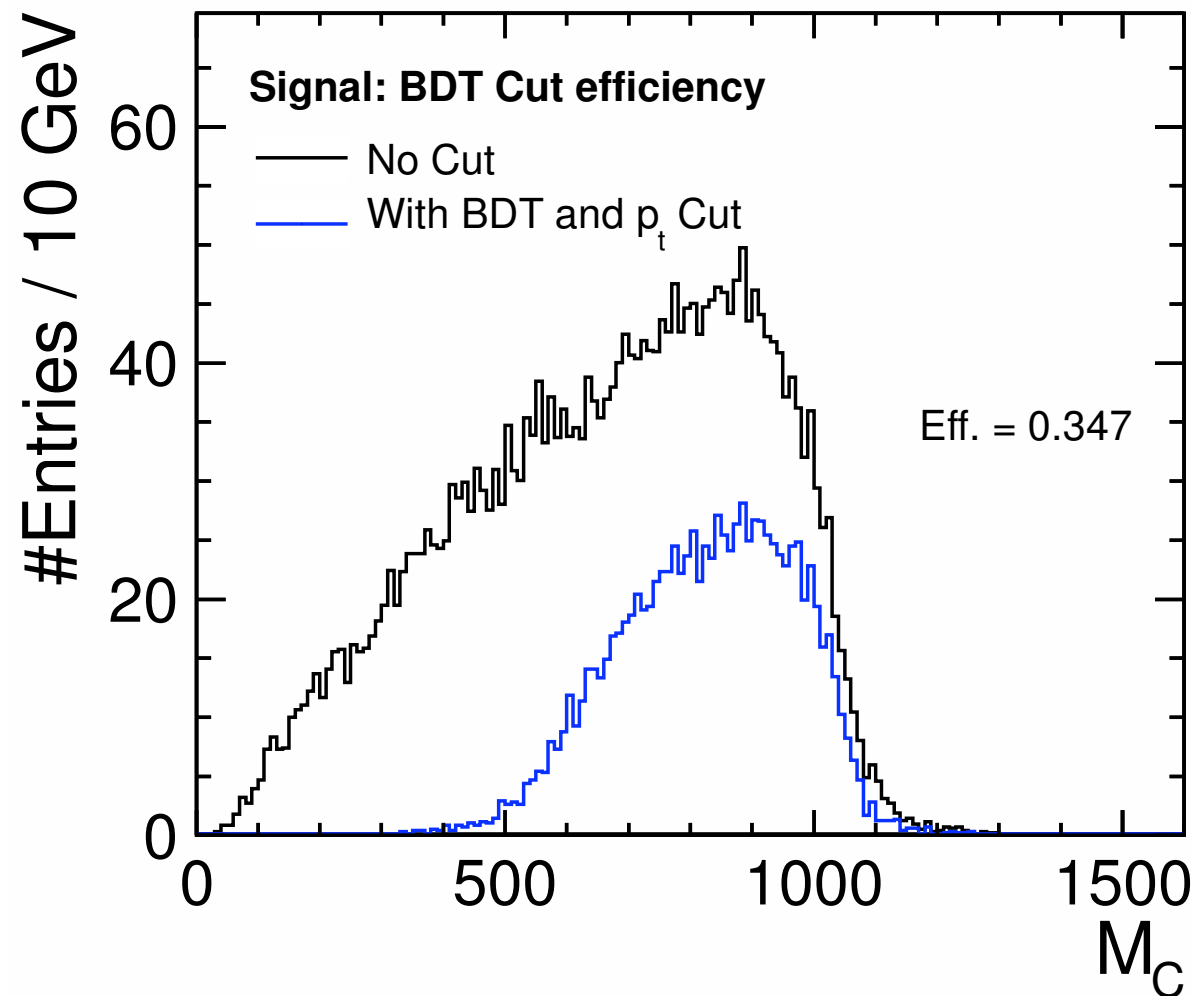
# Background rejection: Boosted Decision Trees: Cut eff.

After BDT and  $p_t$  Cut:

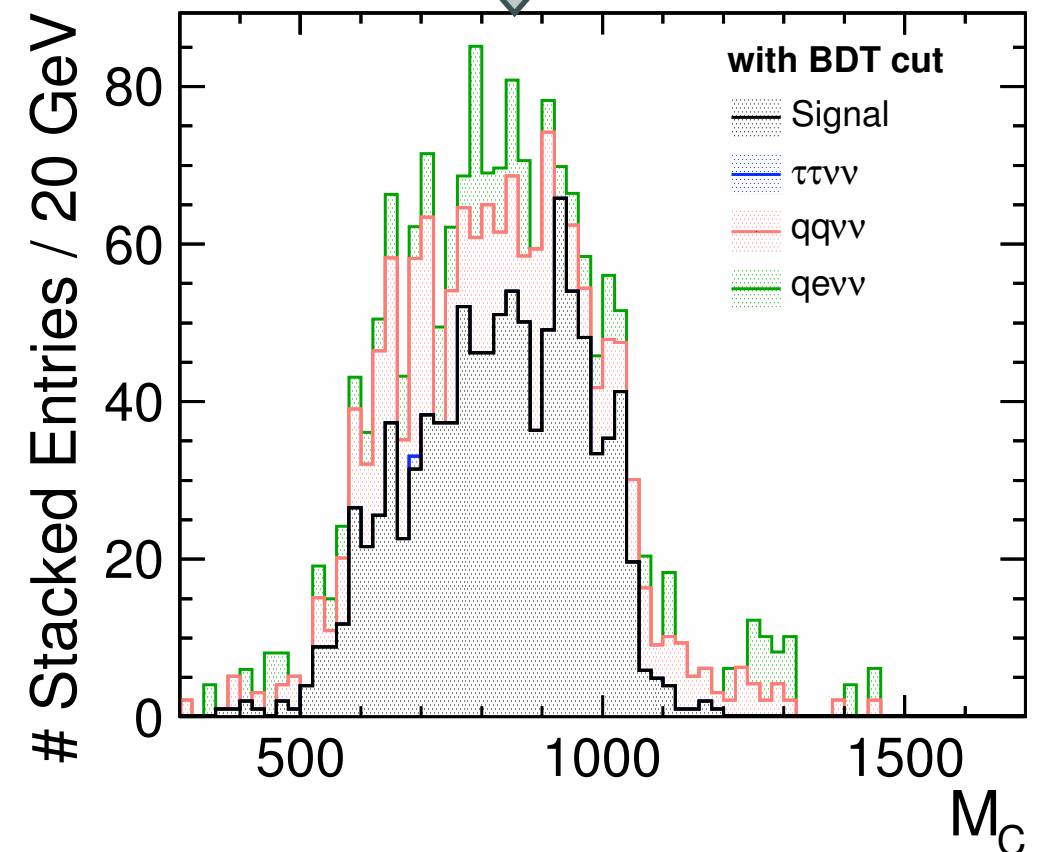
Purity: 0.60

Cut efficiency: 0.347

(determined from independent sample)



Cut on BDT



# Background rejection: Fit Background

- $M_C$  Distribution not Background free after BDT cut
  - Fit Background on Train Sample
    - Gaussian
  - Subtract Fit on Analysis Sample

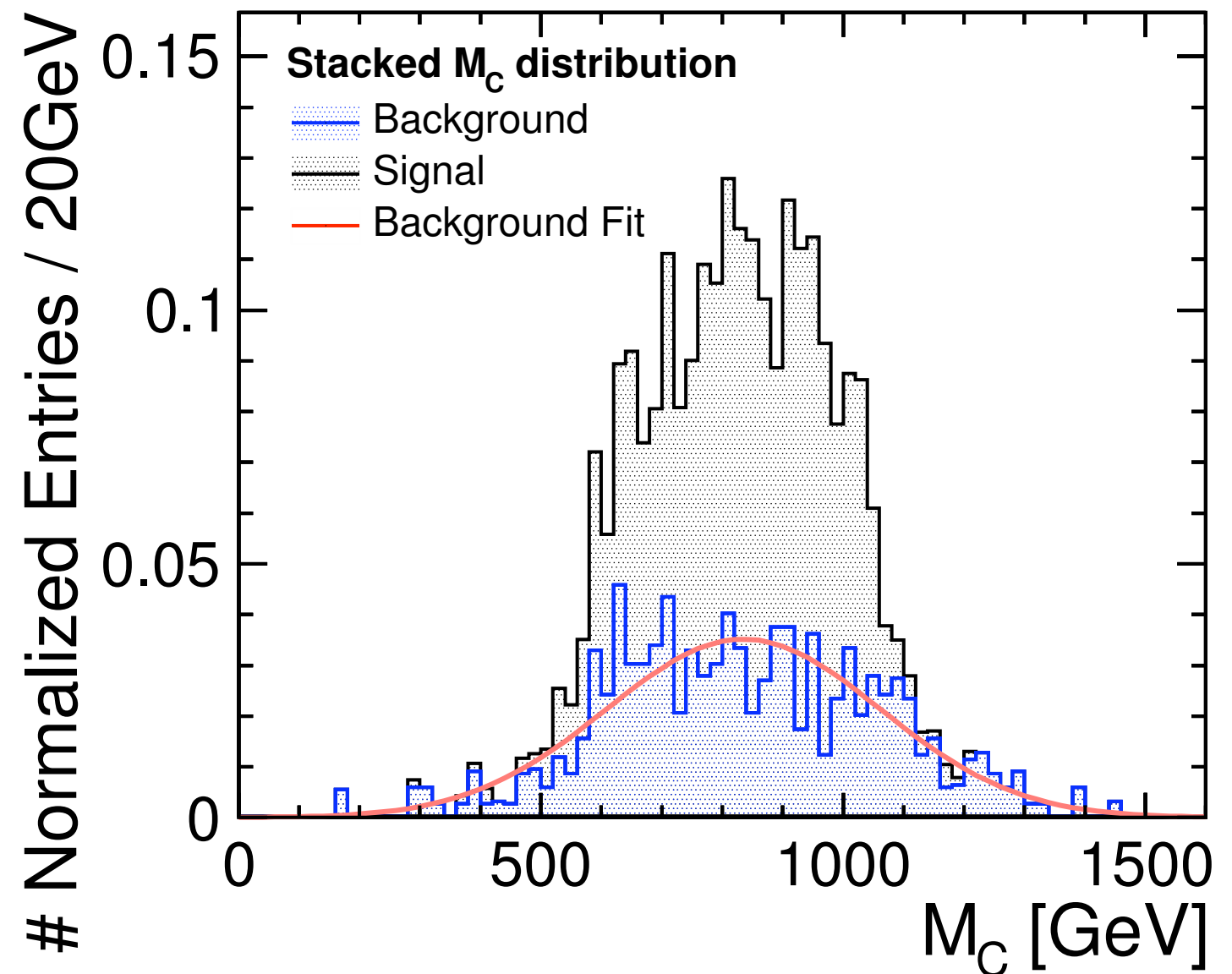
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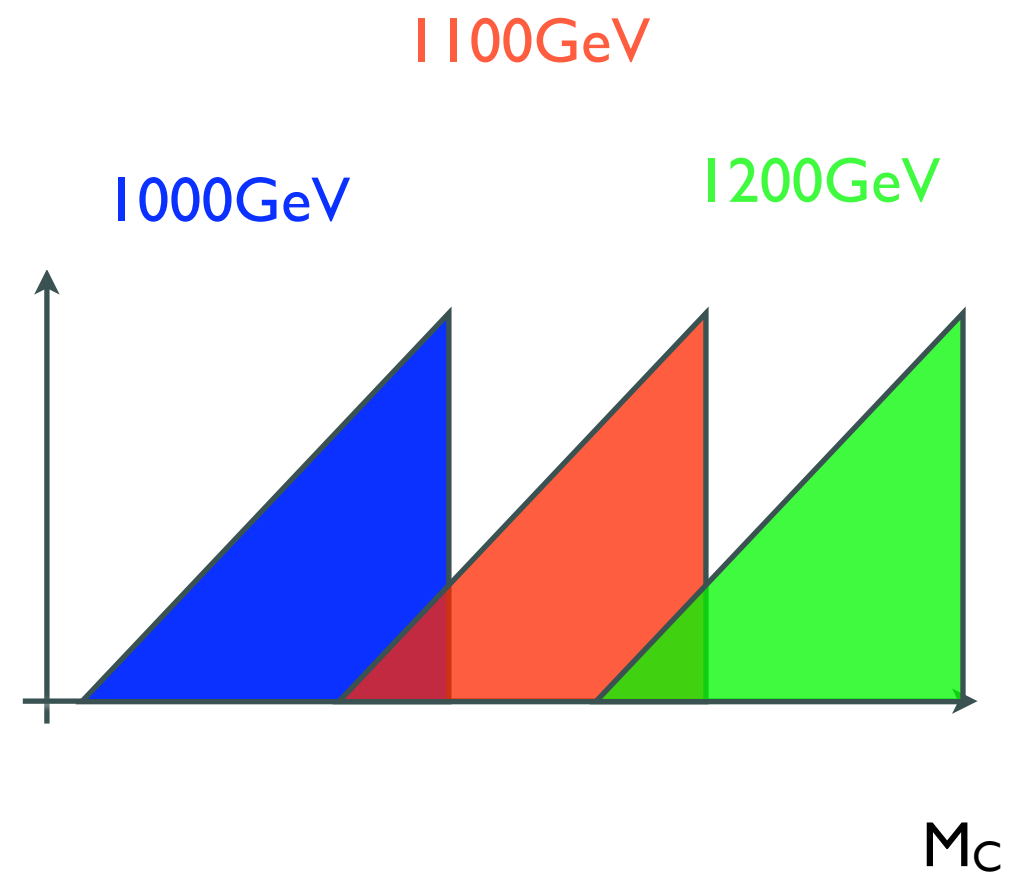
# Squark mass extraction: Template Fit

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— Squark mass extraction with  $M_C$ :Template Fit

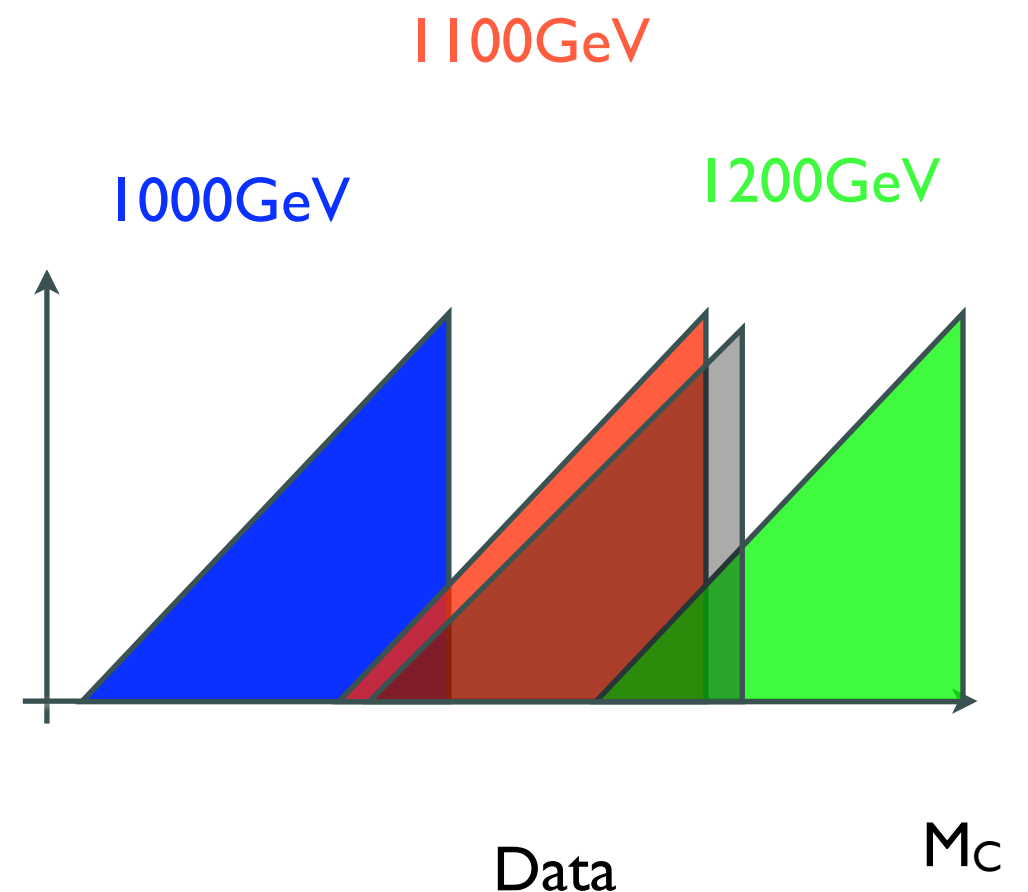
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- Squark mass extraction with  $M_C$ :Template Fit
  - Create templates in steps of 3 GeV



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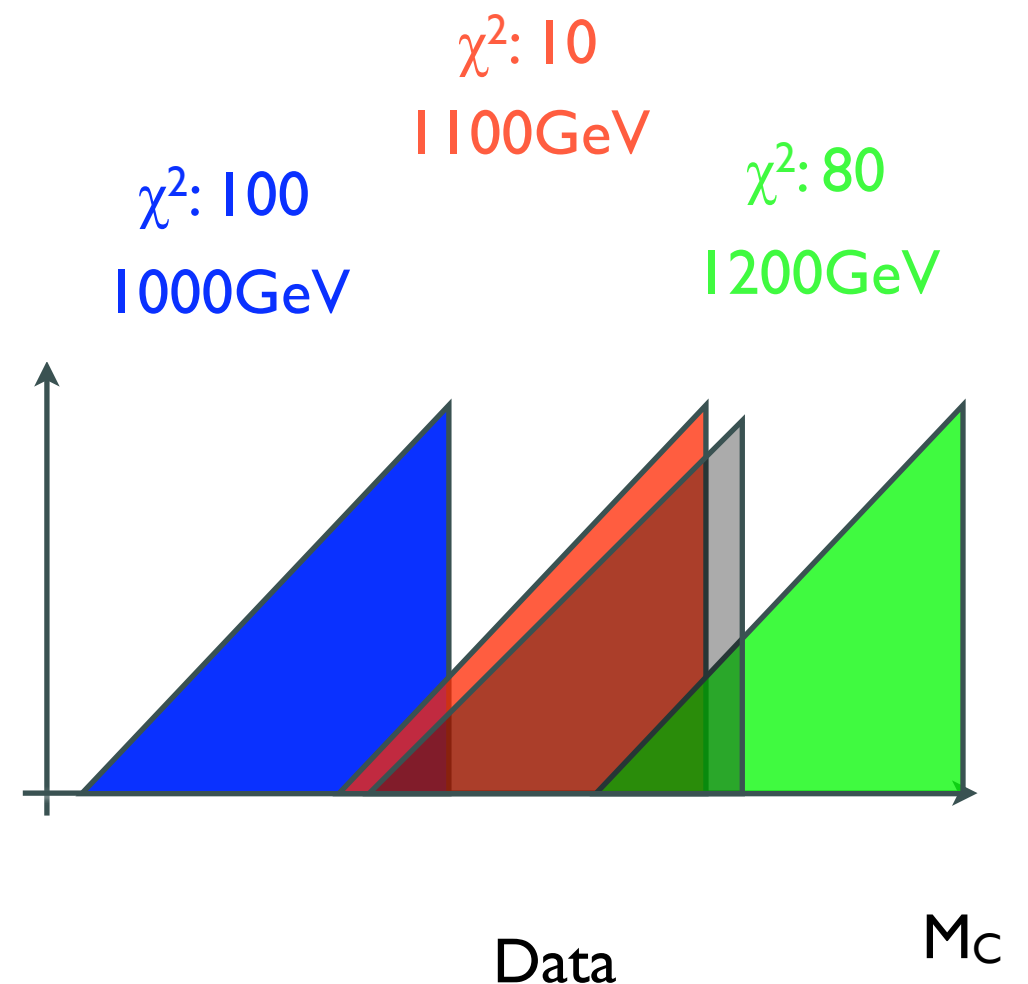
# Squark mass extraction: Template Fit

$$\chi^2 = \sum_n^{\text{bins}} \frac{\Delta_n^2}{\sigma_{n,t}^2 + \sigma_{n,m}^2}$$

— Squark mass extraction with  $M_C$ : Template Fit

— Create templates in steps of 3 GeV

— Compare template with Data via  $\chi^2$



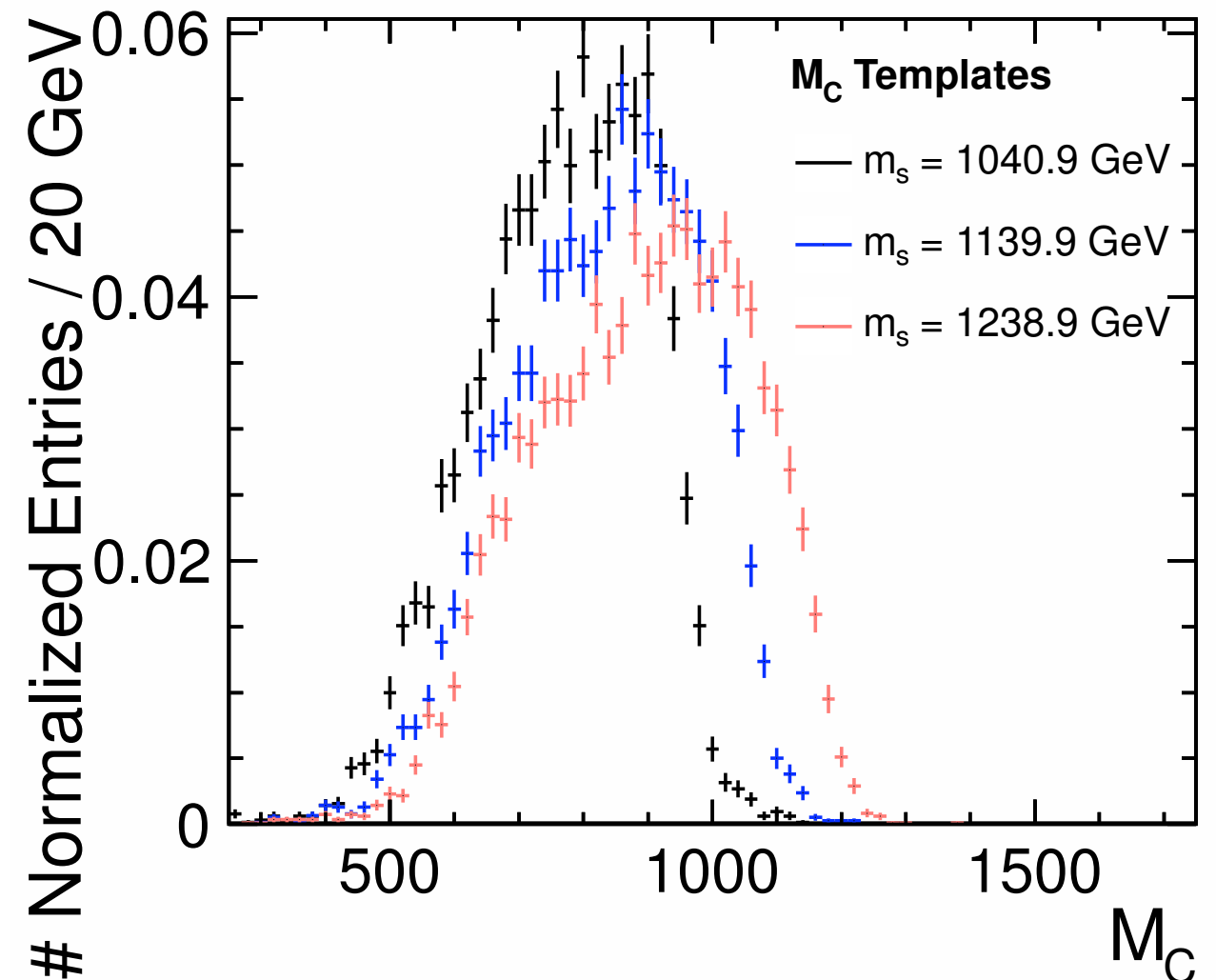
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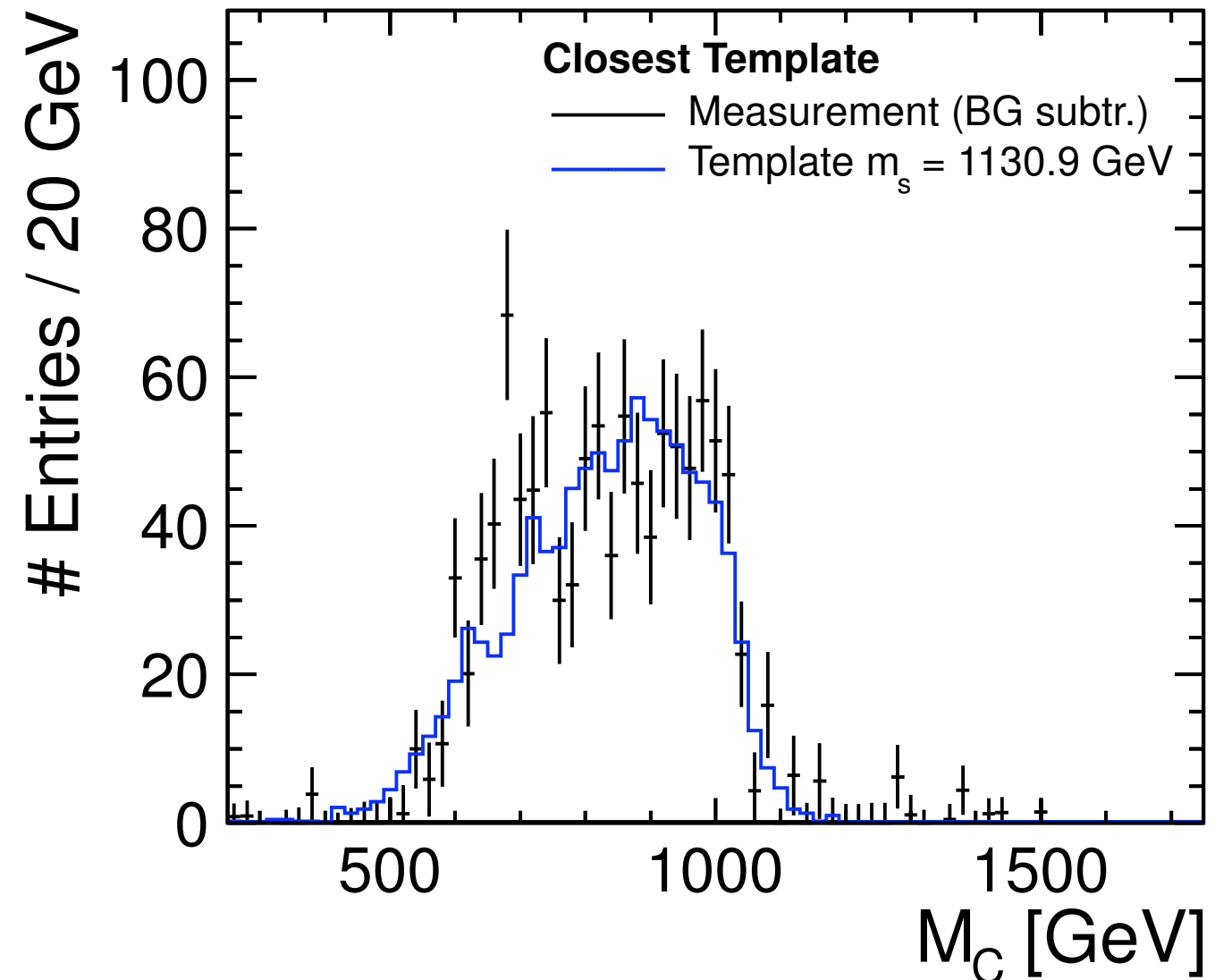
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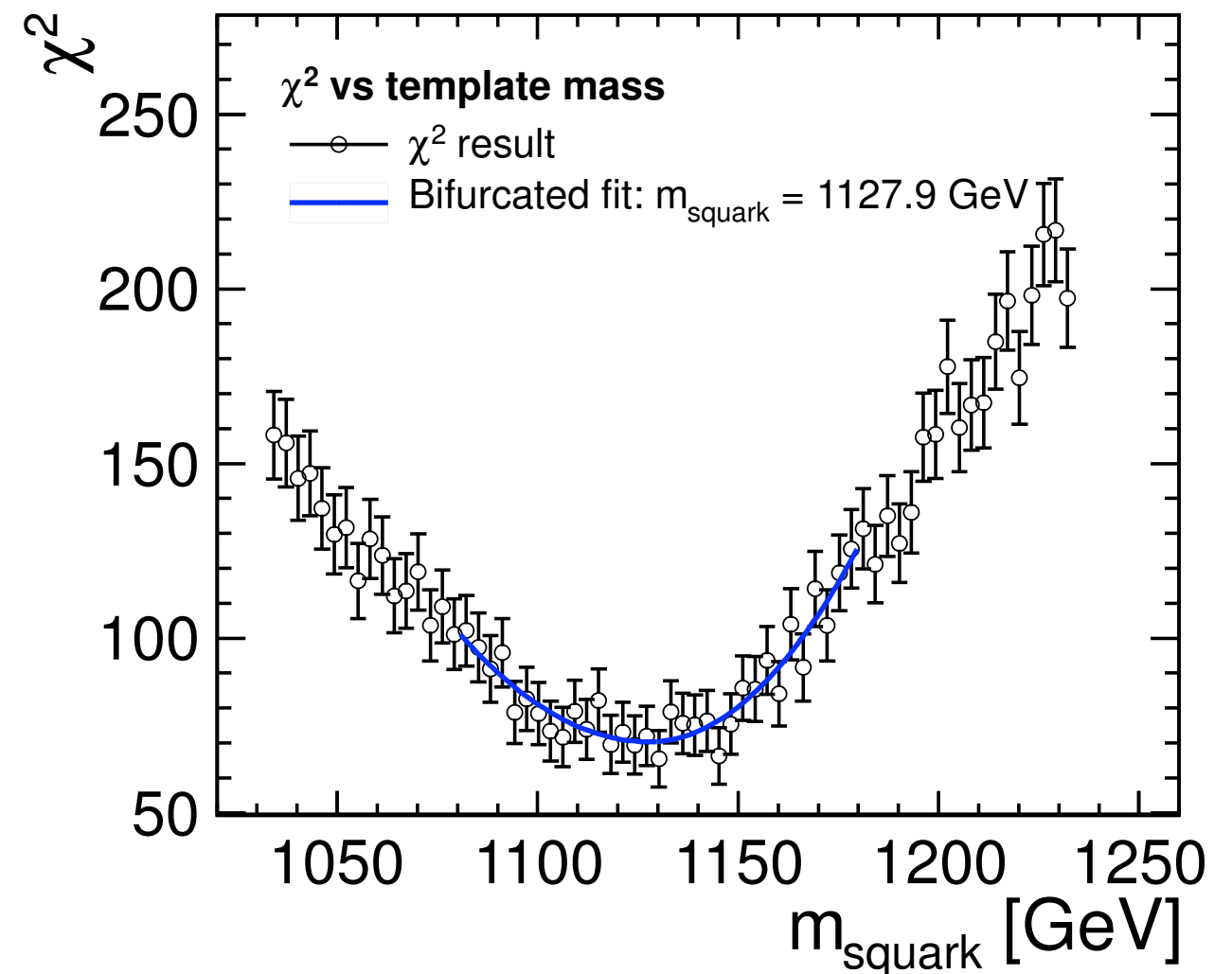
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— Fit resulting parabola

— Minimum =  $m_{\text{squark}} = 1127.9 \text{ GeV}$



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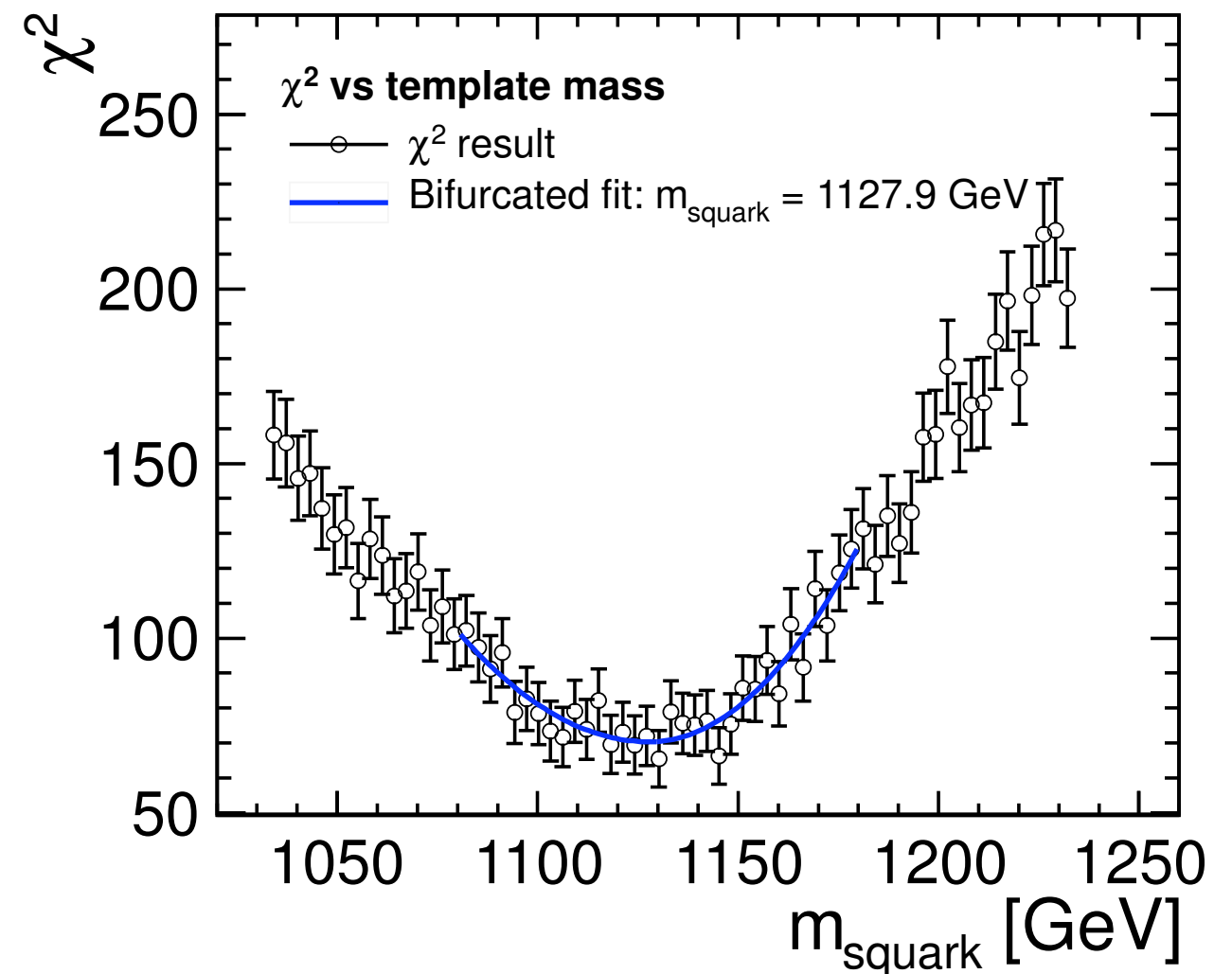
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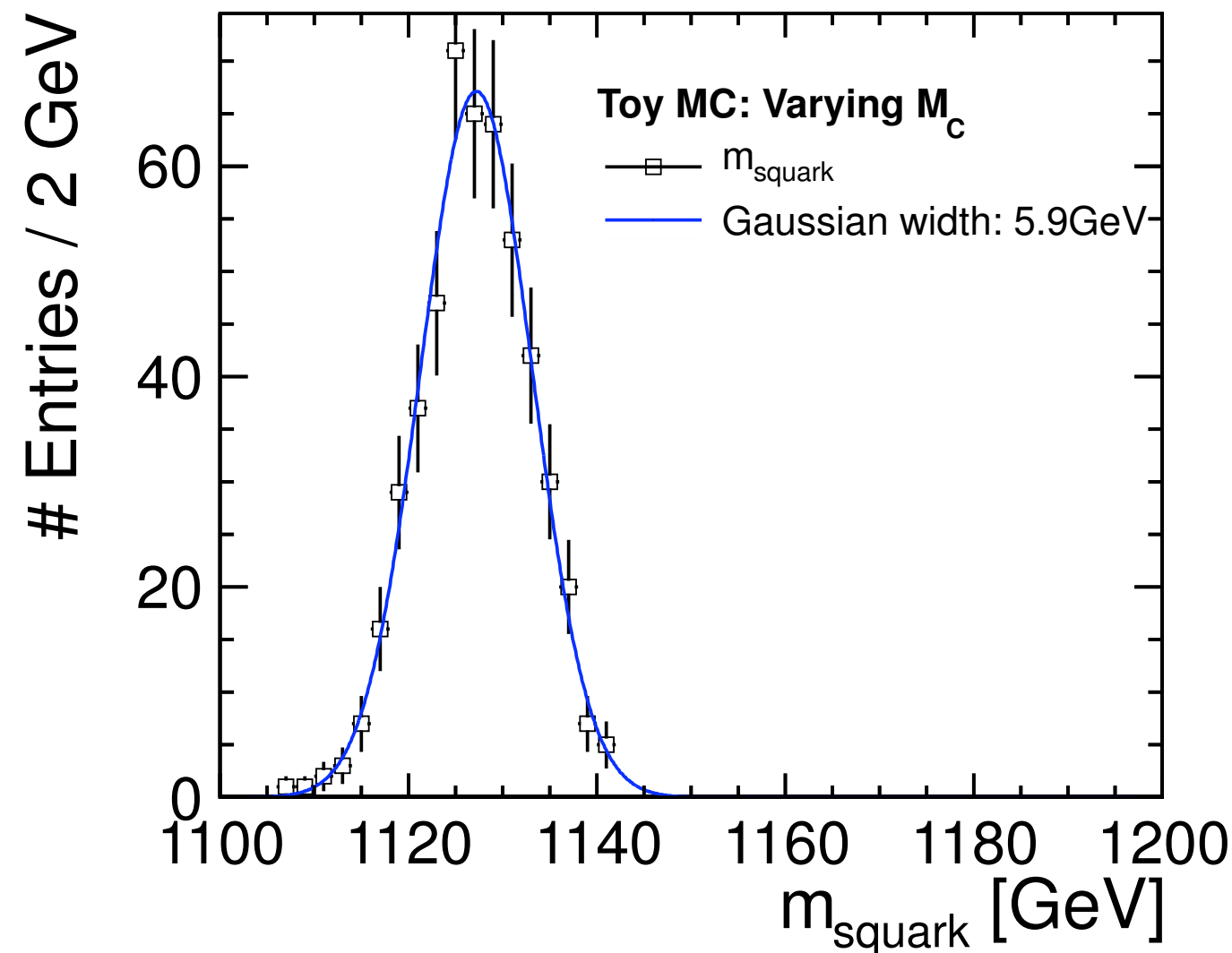
— Minimum =  $m_{\text{squark}} = 1127.9 \text{ GeV}$

— Templates created via 4-Vector smearing  
(no full simulation)



# Squark mass measurement: Statistical Error

- Extract statistical error with a Toy-MC
  - Repeat 500 times:
    - Bin-by-bin Gaussian smearing of measured  $M_C$  distribution
    - Extract  $m_{\text{squark}}$  for smeared  $M_C$
- Final result within  $1\sigma$  of input value



$$m_{\text{squark}} = 1127.9 \text{ GeV} \pm 5.9 \text{ GeV}_{(\text{stat})}$$

$$m_{\text{squark,input}} = 1123.7 \text{ GeV}$$

# Crosssection

## — [ Crosssection measurement

- Analysis done for Luminosity of  $L = 2000 \text{ fb}^{-1}$
- Subtract the Background from  $M_C$  distribution using the Fit
- Integral = # Events after BDT and  $p_t$  cut ( $N_{\text{after cut}}$ )
- Cut efficiency  $\epsilon$  of BDT and  $p_t$  cut known

$$N_{\text{real}} = \frac{N_{\text{after cut}}}{\epsilon}$$

$$\sigma = \frac{N_{\text{real}}}{\mathcal{L}} = \frac{N_{\text{after cut}}}{\epsilon \mathcal{L}}$$

$$\sigma_{\text{squark}} = (1.51 \pm 0.07) \text{ fb}$$

$$\sigma_{\text{squark,input}} = 1.47 \text{ fb}$$

# Summary

- [ New accelerator technology: Compact Linear Collider
- [ Conceptional Design Report Benchmark: Squark pair production
  - Decay mainly into 2 jets and missing energy
- [ Background rejection done with Boosted Decision Trees
- [ Remaining Background fitted with Gaussian
- [ Squark mass extracted via Template Fit
- [ Statistical Error extracted with a Toy-MC

# Event Classification: Boosted Decision Trees

- Decision trees are used for general classification
  - here: Signal (+1) vs Background (-1)
- „Weak Learner“:
  - Gives better results than flipping a coin
- Boosting: ( $\Rightarrow$  „Strong Learner“)
  - Tree building requires training sample
    - Choose cut with maximum splitting of BG/Signal
  - Apply trees on sample:
    - Check if classification was correct
    - Weight misclassified events higher in next step
  - Build next tree
- $\Rightarrow$  Forest of Trees
  - Classification via majority vote:
- $\Rightarrow$  single variable BDT  $\in [-1; +1]$

