

# Study of the decay $B^0 \rightarrow \omega K_S^0$ at Belle

Veronika Chobanova

March 19th, 2012



Max-Planck-Institut für Physik  
(Werner-Heisenberg-Institut)



Technische Universität München



# Content

Physical Motivation

Methods of the Analysis of the Decay  $B^0 \rightarrow \omega K_S^0$

Measurement of  $\mathcal{BR}(B^0 \rightarrow \omega K^0)$  and  $\tau_{B^0}$

Summary and outlook

# Introduction to $CP$ Violation

- ▶ Universe today is matter dominated
- ▶ Violation of  $CP = C(\text{charge}) \times P(\text{parity})$  symmetry necessary to explain the matter-antimatter asymmetry after the Big Bang
- ▶  $CP$  violation in the Standard Model: *Cabbibo-Kobayashi-Maskawa (CKM) mechanism*
- ▶  $CKM$  mechanism describes the relation between the weak and the mass eigenstates of quarks
- ▶  $CKM$  mechanism expressed through a complex, unitary  $3 \times 3$  matrix

## CKM Matrix

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}_{\text{weak}} = V_{\text{CKM}} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{mass}} \equiv \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{mass}}$$

$V_{ij}$  : quark flavour transition couplings

**$CKM$  mechanism not enough to explain the matter dominance**

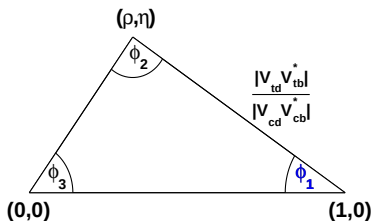
**$\Rightarrow$  New Physics beyond the Standard Model is needed**

# CP Violation in the Standard Model

## Wolfenstein parametrisation

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

$\lambda = \sin \theta_C \approx 0.22$ ,  $\theta_C$ : Cabibbo angle



CKM matrix is unitary

$$\Rightarrow V_{ud} \cdot V_{ub}^* + V_{cd} \cdot V_{cb}^* + V_{td} \cdot V_{tb}^* = 0$$

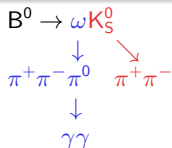
$$\mathcal{O}(\lambda^3) \quad \mathcal{O}(\lambda^3) \quad \mathcal{O}(\lambda^3)$$

relevant for the  $B$  meson system

- Sides with similar size  $\Rightarrow$  large angles, precise determination of the observables (3 angles and 2 sides) possible
- problem over-constrained  $\Rightarrow$  leaves room for New Physics

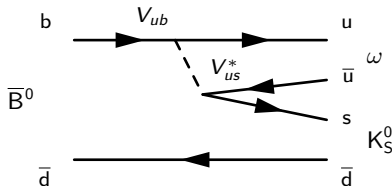
$\phi_1$  most precisely measured from  $b \rightarrow c\bar{c}s$  transitions ("Golden channel"  $B^0 \rightarrow J/\psi K_S^0$ )  
 Decays via charmless  $b \rightarrow sq\bar{q}$  (like  $B^0 \rightarrow \omega K_S^0$ ) transitions sensitive to  $\phi_1$

# The Decay $B^0 \rightarrow \omega K_S^0$



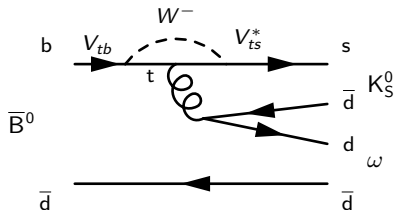
$B^0 \rightarrow \omega K_S^0$  sensitive to  $\phi_1$   
 $B^0 \rightarrow \omega K_S^0$  is a  $CP$  final state

Tree diagram



$$A_{\text{tree}} \propto V_{ub} \cdot V_{us}^* \propto \lambda^3 \cdot \lambda \propto \lambda^4$$

Penguin diagram



$$A_{\text{peng}} \propto V_{tb} \cdot V_{ts}^* \propto 1 \cdot \lambda^2 \propto \lambda^2$$

$\Rightarrow$  Decay is dominated by the penguin contribution

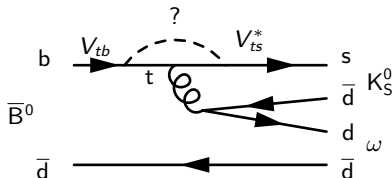
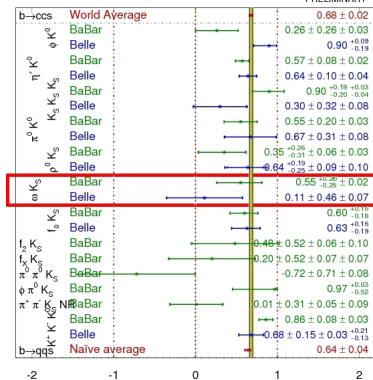
Measurement of

- ▶ The branching fraction  $\mathcal{BR}(B^0 \rightarrow \omega K^0)$
- ▶ The  $CP$  parameters  $\mathcal{A}_{CP}$  and  $\mathcal{S}_{CP} \propto \sin 2\phi_1^{\text{eff}}$  (tree diagram pollution)

# Physical Motivation

## Why the decay $B^0 \rightarrow \omega K_S^0$ ?

- ▶ The Standard Model predicts that  $\sin 2\phi_1^{\text{eff}}$  from  $b \rightarrow sq\bar{q}$  should be larger than from  $b \rightarrow c\bar{c}s$  ( $B^0 \rightarrow J/\psi K_S^0$ ):  $\sin 2\phi_1^{\text{eff}} - \sin 2\phi_1 \in (0.0; 0.2)$
- ▶ Measurements from penguin may be systematically lower (hint at New Physics?)
- ▶ Could be caused by unknown new particle in the loop carrying different weak phase
- ▶ Leads to a shift from  $\sin 2\phi_1$


 $\sin(2\phi_1^{\text{eff}})$ 
**HFAG**  
 Beauty 2011  
 PRELIMINARY


# CP Violation in the $B$ Meson System

## Time-dependent CP asymmetry

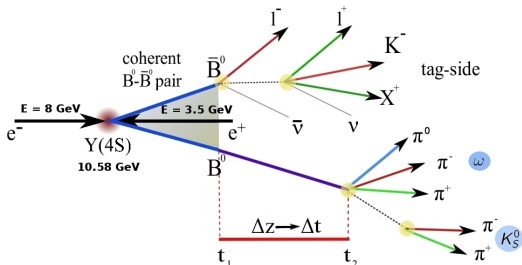
$$a_{CP}(\Delta t, f_{CP}) = \frac{N_{\bar{B}^0}(\Delta t, f_{CP}) - N_{B^0}(\Delta t, f_{CP})}{N_{\bar{B}^0}(\Delta t, f_{CP}) + N_{B^0}(\Delta t, f_{CP})} = \mathcal{A}_{CP} \cos(\Delta m \Delta t) + \mathcal{S}_{CP} \sin(\Delta m \Delta t)$$

$\mathcal{A}_{CP}$ : measure for the **direct** CP violation

$B^0 \rightarrow f_{CP} \neq \bar{B}^0 \rightarrow f_{CP}$

$\mathcal{S}_{CP}$ : measure for the **mixing induced** CP violation

$B^0 \rightarrow \bar{B}^0 \rightarrow f_{CP} \neq \bar{B}^0 \rightarrow B^0 \rightarrow f_{CP}$



$B^0$  or  $\bar{B}^0$ ?

→ Look at the other  $B$  (tag-side):

If  $l^- \Rightarrow \bar{B}^0$  on the tag-side and  $B^0$  on the CP-side

If  $l^+ \Rightarrow B^0$  on the tag-side and  $\bar{B}^0$  on the CP-side

**$\Delta t$  measurement**

Asymmetric beam energies at KEKB

⇒ Boost of the center of mass system

Measurement of  $\Delta z \sim 100 \mu\text{m}$  instead of  $\Delta t \sim \text{ps}$

Obtain  $\Delta t = \Delta z / c \langle \beta \gamma \rangle$

# Approach

## Goals

Study new methods to measure  $\mathcal{BR}(B^0 \rightarrow \omega K_S^0)$ ,  $\mathcal{A}_{CP}$  and  $\mathcal{S}_{CP}$  and minimize the statistical and and systematic uncertainties

## Approach

- ▶ Build an algorithm to reconstruct  $B^0 \rightarrow \omega K_S^0$
- ▶ Study the backgrounds ( $q\bar{q}$ , other B decays)
- ▶ Build an improved model to discriminate signal and background (multidimensional fit)
- ▶ Test the model

So far: "Blind Analysis". Study only from Monte Carlo (MC) samples

- ▶ Apply model to the real data
- ▶ Determine  $\mathcal{BR}(B^0 \rightarrow \omega K_S^0)$ ,  $\mathcal{A}_{CP}$  and  $\mathcal{S}_{CP}$  and the uncertainties from the full data set of Belle

# Previous Measurements of $B^0 \rightarrow \omega K_S^0$

|              | <b><math>B\bar{B}</math>-pairs</b> | $\mathcal{BR}(B^0 \rightarrow \omega K^0)$       | $\mathcal{A}_{CP}$              | $\mathcal{S}_{CP}$                  |
|--------------|------------------------------------|--------------------------------------------------|---------------------------------|-------------------------------------|
| <b>Belle</b> | $388 \times 10^6$                  | $(4.4^{+0.8}_{-0.7} \pm 0.4) \times 10^{-6}$ [1] | -                               | -                                   |
| <b>Belle</b> | $535 \times 10^6$                  | -                                                | $-0.09 \pm 0.29 \pm 0.06$       | $0.11 \pm 0.46 \pm 0.07$ [2]        |
| <b>BaBar</b> | $467 \times 10^6$                  | $(5.4 \pm 0.8 \pm 0.3) \times 10^{-6}$           | $0.52^{+0.22}_{-0.20} \pm 0.03$ | $0.55^{+0.26}_{-0.29} \pm 0.02$ [3] |

[1] PhysRevD.74.111101

[2] PhysRevD.76.091103

[3] PhysRevD.79.052003

**Full data set of Belle  $772 \times 10^6$   $B\bar{B}$  pairs**

## Challenging analysis

- ▶  $\mathcal{BR}(B^0 \rightarrow \omega K^0) \sim 10^{-6}$  (small)
- ▶ Large background contribution from  $q\bar{q}$  (u, d, s, c) background

## Our method

- ▶ Use loose cuts on the observables for maximum signal sensitivity
- ▶ Multidimensional fit to the modelled probability density functions to extract  $\mathcal{BR}(B^0 \rightarrow \omega K^0)$ ,  $\mathcal{A}_{CP}$ ,  $\mathcal{S}_{CP}$  and their uncertainties

# Measurement of $\mathcal{BR}(B^0 \rightarrow \omega K^0)$

Extract  $\mathcal{BR}(B^0 \rightarrow \omega K^0)$  by a 6D extended unbinned maximum likelihood fit

## Fit observables

$$\Delta E = E_{\text{rec}}^{\text{CMS}} - E_{\text{beam}}^{\text{CMS}}$$

$\mathcal{F}_{B\bar{B}/q\bar{q}}$ : Fisher discriminant, event-shape dependent

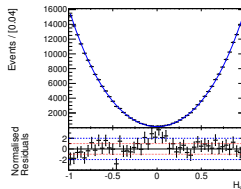
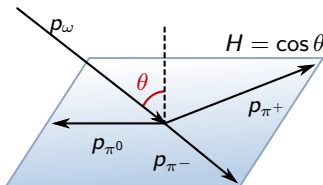
$m_{3\pi}$ : mass of the reconstructed  $3\pi$  final state

$\Delta t$ : time difference between the two B decays

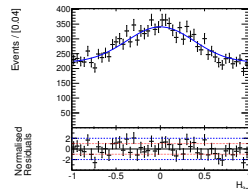
$q = 1$  for  $B^0$  and  $q = -1$  for  $\bar{B}^0$

**New in this analysis:** Helicity angles  $\mathcal{H}_{3\pi}$ , powerful observable for background discrimination

Multidimensional analysis  $\Rightarrow$  model for signal and background necessary



$\mathcal{H}_{3\pi}$  Signal



$\mathcal{H}_{3\pi}$   $q\bar{q}$  bkg

# Toy MC studies

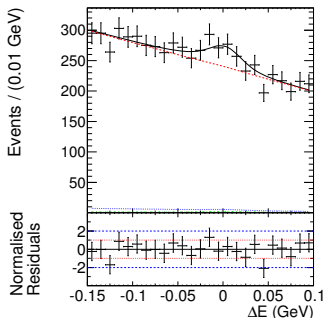
Test the model with Toy MC

**Expected number of events**

signal  $\sim 230$

$q\bar{q} \sim 5300$

$B\bar{B} \sim 130$



Projection of

$$\Delta E = E_{B_{\text{rec}}}^{\text{CMS}} - E_{\text{beam}}^{\text{CMS}}$$

Full data set of Belle:  $772 \times 10^6 B\bar{B}$  pairs

**Expectations for the statistical uncertainty of:**

►  $\mathcal{BR}(B^0 \rightarrow \omega K^0)$

| BaBar (final) | Belle (previous) | Belle (current) |
|---------------|------------------|-----------------|
| 13% *         | 13% **           | 9.2% **         |

►  $\mathcal{A}_{CP}$

| BaBar (final) | Belle (previous) | Belle (current) |
|---------------|------------------|-----------------|
| 0.20 *        | 0.24 **          | 0.19 **         |

►  $S_{CP}$

| BaBar (final) | Belle (previous) | Belle (current) |
|---------------|------------------|-----------------|
| 0.26 *        | 0.38 **          | 0.28 **         |

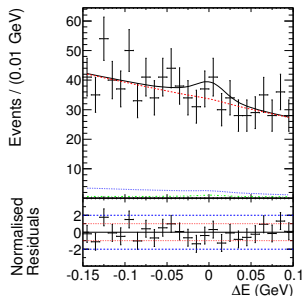
\* Final result of BaBar

\*\* Scaled to the full data set of Belle

⇒ **Our method is better than the previous Belle analysis**

# Results from the Fit to the Data

Projection of  
 $\Delta E = E_{B_{\text{rec}}}^{\text{CMS}} - E_{\text{beam}}^{\text{CMS}}$



Black: Full PDF  
 Total background  
 $B\bar{B}$  background

Partial box opening with  $152 \times 10^6 B\bar{B}$  pairs  
 (Full statistics:  $772 \times 10^6 B\bar{B}$  pairs)  
 Unbinned maximum likelihood fit to 6  
 observables

**Preliminary Result from  $152 \times 10^6 B\bar{B}$  pairs**

$$\mathcal{BR}(B^0 \rightarrow \omega K^0) = [4.94^{+1.28}_{-1.14}(\text{stat})] \times 10^{-6}$$

$$\tau_{B^0} = [1.522 \pm 0.35(\text{stat})] \text{ ps (cross-check)}$$

- ▶ Belle  $388 \times 10^6 B\bar{B}$  pairs  
 $\mathcal{BR}(B^0 \rightarrow \omega K^0) = [4.4^{+0.8}_{-0.7} \pm 0.4] \times 10^{-6}$
- ▶ World average  
 $\mathcal{BR}(B^0 \rightarrow \omega K^0) = [5.0 \pm 0.6] \times 10^{-6}$   
 $\tau_{B^0} = [1.519 \pm 0.007] \text{ ps}$

# Summary and outlook

## Summary

- ▶ The decay  $B^0 \rightarrow \omega K_S^0$  is sensitive to the angle  $\phi_1$ . A possible deviation in the measurement of  $\sin 2\phi_1$  could be a hint at New Physics
- ▶ We have built a model which improves the results than the previous Belle analysis
- ▶ Method was successfully applied to a subset of Belle's data

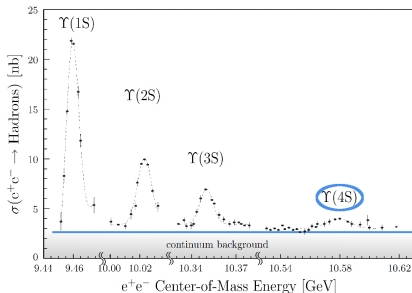
## Outlook

- ▶ Add additional variables to the fit to improve the signal-background separation power
- ▶ Further reduce the systematic uncertainties by performing a simultaneous fit to the control sample  $B^+ \rightarrow \omega K^+$  (same kinematics as  $B^0 \rightarrow \omega K_S^0$ )
- ▶ With this improvement the results from the full Belle statistics will dominate the world average for  $\mathcal{A}_{CP}$  and  $\mathcal{S}_{CP}$  and  $\mathcal{BR}(B^0 \rightarrow \omega K^0)$
- ▶ But: Accuracy still too limited to challenge the Standard Model  $\Rightarrow$  Belle II should provide more statistics for a precise measurement

**Thank you  
for your attention**

# Backup

# CP Violation Measurement



## B Meson production

- $\Upsilon(4S)$  resonance decays almost exclusively into a  $B\bar{B}$  pair
- $\Upsilon(4S)$ :  $J^P = 1^-$   
 $B$ :  $J^P = 0^-$

⇒  $B$  meson pair in a p-wave  
 ⇒ asymmetric wave function  
 ⇒  $B$  mesons have opposite flavour  
 $B\bar{B}$  pair coherent

$$m_{\Upsilon(4S)} = 10.58 \text{ GeV}/c^2 \approx 2 \times m_B$$

$$m_B = 5.28 \text{ GeV}/c^2$$

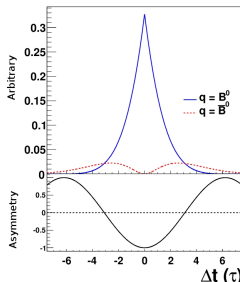
# CP Violation in the B Meson System

## Time-dependent CP asymmetry

$$a_{CP}(\Delta t, f_{CP}) = \frac{N_{\bar{B}^0}(\Delta t, f_{CP}) - N_{B^0}(\Delta t, f_{CP})}{N_{\bar{B}^0}(\Delta t, f_{CP}) + N_{B^0}(\Delta t, f_{CP})} = \mathcal{A}_{CP} \cos(\Delta m \Delta t) + \mathcal{S}_{CP} \sin(\Delta m \Delta t)$$

$\mathcal{A}_{CP}$  measure for the **direct** CP violation

$B^0 \rightarrow f_{CP} \neq \bar{B}^0 \rightarrow f_{CP}$

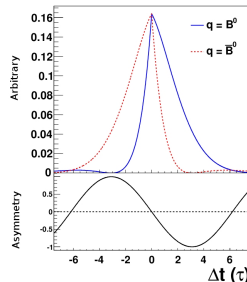


$$\mathcal{A}_{CP} = 1$$

$$\mathcal{S}_{CP} = 0$$

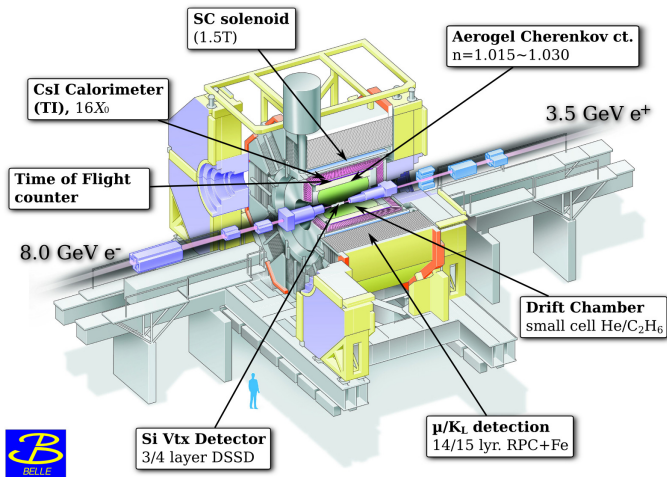
$\mathcal{S}_{CP}$  measure for the **mixing induced** CP violation

$B^0 \rightarrow \bar{B}^0 \rightarrow f_{CP} \neq \bar{B}^0 \rightarrow B^0 \rightarrow f_{CP}$



$$\mathcal{A}_{CP} = 0$$

$$\mathcal{S}_{CP} = 1$$



# Toy MC Study

# Toy MC Study

100 pseudo-experiments generated:

907 events for SVD1 and 5554 events for SVD2

|        | $N_{\text{Sig}}$ | $N_{q\bar{q}}$ | $N_{B^0\bar{B}^0}^{\text{Charm}}$ | $N_{B^+B^-}^{\text{Charm}}$ | $N_{B^0\bar{B}^0}^{\text{Charmless}}$ | $N_{B^+B^-}^{\text{Charmless}}$ | $N_{B^0\bar{B}^0}^{\text{PB, Charm}}$ | $N_{\text{Mis}}$ |
|--------|------------------|----------------|-----------------------------------|-----------------------------|---------------------------------------|---------------------------------|---------------------------------------|------------------|
| # SVD1 | 37               | 849            | 4                                 | 4                           | 4                                     | 3                               | 6                                     | 0                |
| # SVD2 | 196              | 5241           | 12                                | 28                          | 25                                    | 19                              | 31                                    | 2                |

$$N_{\text{Sig}} = \mathcal{B}(B^0 \rightarrow \omega K_S^0) \sum_i (N_{B\bar{B}}^i \epsilon_{\text{Rec}}^i \eta^i), \quad i = [\text{SVD1}, \text{SVD2}],$$

$$\mathcal{B}(B^0 \rightarrow \omega K_0^S) = 2.5 \cdot 10^{-6}$$

Free parameters in the fit

- ▶  $\mathcal{BR}(B^0 \rightarrow \omega K_S^0)$ ,  $\mathcal{A}_{CP}$  and  $\mathcal{S}_{CP}$
- ▶  $N_{q\bar{q}}^{1,2}$
- ▶  $N_{B^0\bar{B}^0}^{\text{Charm};1,2}$
- ▶  $\Delta E$  slope for  $q\bar{q}$ ,  $C_{q\bar{q}}^{1,2}(\Delta E)$

# Toy MC studies for $B^0 \rightarrow \omega K_S^0$

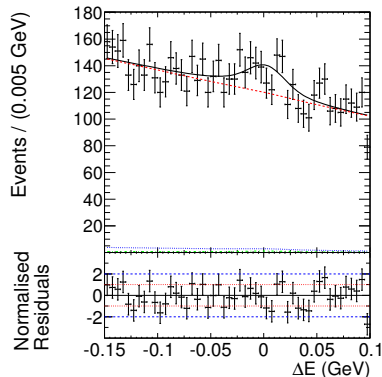
Test the model with Toy MC

**Expected number of events**

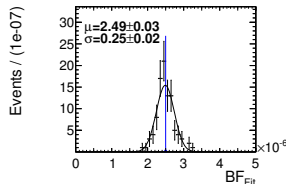
signal  $\sim 230$

$q\bar{q} \sim 5300$

$B\bar{B} \sim 130$



**Expectations for  $\mathcal{BR}(B^0 \rightarrow \omega K^0)$**



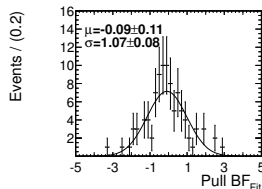
Uncertainty 9.2%

Error scaled to final data sets

Belle (previous): 13% , BaBar: 13%

⇒ Our method is better

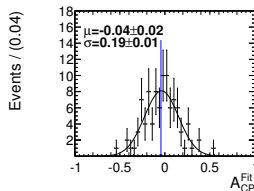
**Pull distribution of  $\mathcal{BR}(B^0 \rightarrow \omega K^0)$**



No bias, correct error estimation

# Toy MC studies for $\mathcal{A}_{CP}$ and $\mathcal{S}_{CP}$

## Expectations for $\mathcal{A}_{CP}$

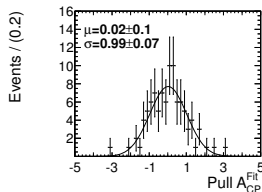


Uncertainty  $\pm 0.19$

Error scaled to final data set

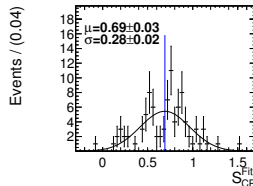
Belle (previous):  $\pm 0.24$ , BaBar:  $\pm 0.20$

## Pull distribution of $\mathcal{A}_{CP}$



No bias, correct error estimation

## Expectations for $\mathcal{S}_{CP}$

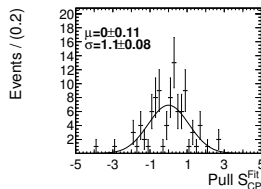


Uncertainty  $\pm 0.28$

Error scaled to final data set

Belle (previous):  $\pm 0.38$ , BaBar:  $\pm 0.26$

## Pull distribution of $\mathcal{S}_{CP}$



No bias, correct error estimation

# B Reconstruction

$$B^0 \rightarrow \omega K_S, \omega \rightarrow \pi^+ \pi^- \pi^0$$

## General selection criteria for the reconstruction

### $\pi^+$ candidates

- ▶  $L_{K/\pi} < 0.9$  in order to remove tracks consistent with kaon hypothesis

### $\pi^0$ candidates

- ▶  $118 \text{ MeV}/c^2 < m(\gamma\gamma) < 150 \text{ MeV}/c^2$ , mass fit  $\chi^2 < 50$
- ▶  $E_\gamma > 50 \text{ MeV}$  in ECL barrel,  $E_\gamma > 100 \text{ MeV}$  in ECL endcap

### $K_S$ candidates

- ▶ “Good  $K_S$ ” cut
- ▶  $0.482 \text{ GeV}/c^2 < m(\pi^+ \pi^-) < 0.514 \text{ GeV}/c^2$  ( $m(K_S) \pm 16 \text{ MeV}$ )

### $\omega$ candidates

- ▶  $0.73 \text{ GeV}/c^2 < m(\pi^+ \pi^- \pi^0) < 0.83 \text{ GeV}/c^2$  ( $m(\omega) \pm 50 \text{ MeV}$ )

# B Reconstruction

## $B^0$ candidates

- ▶  $M_{bc} > 5.27 \text{ GeV}/c^2$  and  $-0.15 \text{ GeV} < \Delta E < 0.1 \text{ GeV}$
- ▶ Best  $B$  selection: best  $M_{bc} = \sqrt{(E_{beam}^{cms})^2 - (p_B^{cms})^2}$

Reconstruction efficiency: 13.2% for SVD1 and 16.8% for SVD2

Misreconstruction fraction: 2.3% for SVD1 and 2.4% for SVD2

$\sim 230$  events expected (118 for previous analysis)

Fit to  $\Delta E$ ,  $\mathcal{F}_{B\bar{B}/q\bar{q}}$ ,  $m_{3\pi}$ ,  $\mathcal{H}_{3\pi}$ ,  $\Delta t$ ,  $q$

Fit region:

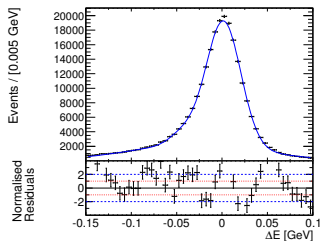
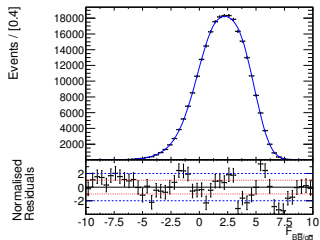
- ▶  $-0.15 \text{ GeV} < \Delta E < 0.1 \text{ GeV}$
- ▶  $-2 < \mathcal{F}_{B\bar{B}/q\bar{q}} < 2$
- ▶  $0.73 \text{ GeV}/c^2 < m_{3\pi} < 0.83 \text{ GeV}/c^2$
- ▶  $-1 < \mathcal{H}_{3\pi} < 1$
- ▶  $-70 \text{ ps} < \Delta t < 70 \text{ ps}$

## Signal Model

# Signal Model

## Signal model correlation matrix

|                                   | $\Delta E$ | $\mathcal{F}_{B\bar{B}/q\bar{q}}$ | $m_{3\pi}$ | $\mathcal{H}_{3\pi}$ | $\Delta t$ |
|-----------------------------------|------------|-----------------------------------|------------|----------------------|------------|
| $\Delta E$                        | 1          | 0.012                             | 0.29       | -0.003               | 0.007      |
| $\mathcal{F}_{B\bar{B}/q\bar{q}}$ |            | 1                                 | 0.001      | 0.001                | 0.003      |
| $m_{3\pi}$                        |            |                                   | 1          | -0.003               | 0.004      |
| $\mathcal{H}_{3\pi}$              |            |                                   |            | 1                    | 0.001      |
| $\Delta t$                        |            |                                   |            |                      | 1          |

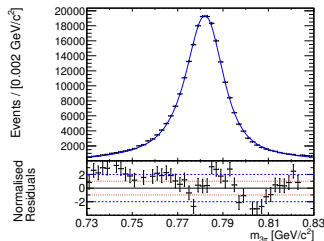
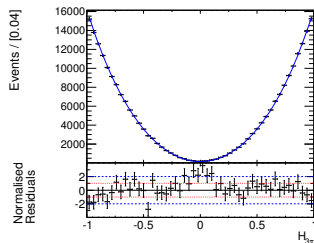
Signal MC  $\Delta E$  and  $\mathcal{F}_{B\bar{B}/q\bar{q}}$  $\Delta E$  signal MC $\mathcal{F}_{B\bar{B}/q\bar{q}}$  signal MC

## Triple Gaussian

$$\begin{aligned} \mathcal{P}_{\text{Sig}}(\Delta E) = & f_1 G(\Delta E; \mu_1, \sigma_1) \\ & + f_2 G(\Delta E; \mu_2, \sigma_2) \\ & + (1 - f_1 - f_2) G(\Delta E; \mu_3, \sigma_3) \end{aligned}$$

Triple Gaussian in each  $r$ -bin  $l$ 

$$\begin{aligned} \mathcal{P}_{\text{Sig},l}(\mathcal{F}_{B\bar{B}/q\bar{q}}) = & f_{1,l} G(\mathcal{F}_{B\bar{B}/q\bar{q}}; \mu_{1,l}, \sigma_{1,l}) \\ & + f_{2,l} G(\Delta E; \mu_{2,l}, \sigma_{2,l}) \\ & + (1 - f_{1,l} - f_{2,l}) G(\Delta E; \mu_{3,l}, \sigma_{3,l}) \end{aligned}$$

Signal MC  $m_{3\pi}$  and  $\mathcal{H}_{3\pi}$  $m_{3\pi}$  signal MC $\mathcal{H}_{3\pi}$  signal MC

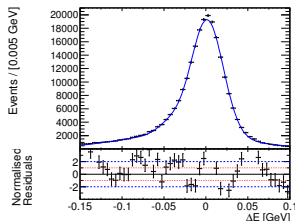
## Triple Gaussian

$$\begin{aligned} \mathcal{P}_{\text{Sig}}(m_{3\pi}) = & f_1 G(m_{3\pi}; \mu_1, \sigma_1) \\ & + f_2 G(m_{3\pi}; \mu_2, \sigma_2) \\ & + (1 - f_1 - f_2) G(m_{3\pi}; \mu_3, \sigma_3) \end{aligned}$$

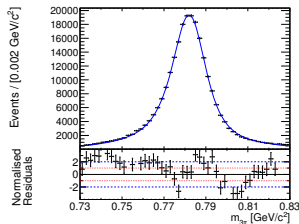
## 4th order Chebyshev

$$\mathcal{P}_{\text{Sig}}(\mathcal{H}_{3\pi}) = \sum_{i=0}^4 c_i C_i(\mathcal{H}_{3\pi})$$

# $\Delta E$ signal MC



$\Delta E$  signal MC



$m_{3\pi}$  signal MC

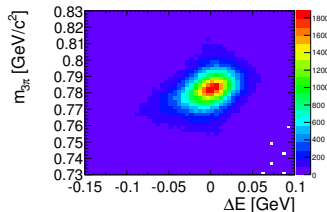
$$\mathcal{P}_{\text{Sig}}(\Delta E) = f_1 G(\Delta E; \mu_1, \sigma_1) + f_2 G(\Delta E; \mu_2, \sigma_2) + (1 - f_1 - f_2) G(\Delta E; \mu_3, \sigma_3)$$

$$\mathcal{P}_{\text{Sig}}(m_{3\pi}) = f_1 G(m_{3\pi}; \mu_1, \sigma_1) + f_2 G(m_{3\pi}; \mu_2, \sigma_2) + (1 - f_1 - f_2) G(m_{3\pi}; \mu_3, \sigma_3)$$

Correlations modeled by

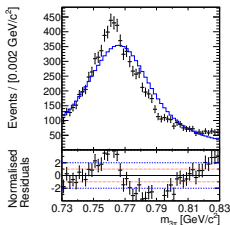
$$\mu_1(m_{3\pi}) = \mu_0 + A \cdot \Delta E \text{ and}$$

$$\sigma_1(m_{3\pi}) = \sigma_0 + B \cdot \Delta E^2$$

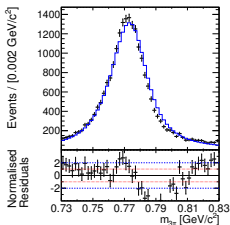


29% corr. between  $\Delta E$  and  $m_{3\pi}$

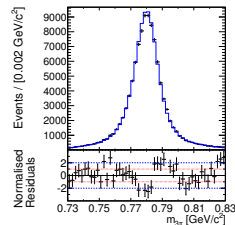
# $\omega$ mass projection in bins of $\Delta E$



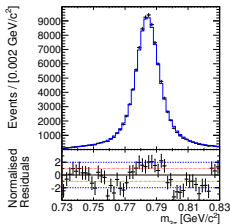
$-0.15 \text{ GeV} < \Delta E < -0.1 \text{ GeV}$



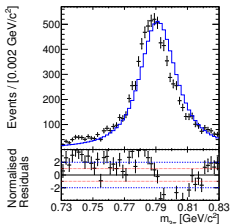
$-0.1 \text{ GeV} < \Delta E < -0.05 \text{ GeV}$



$-0.05 \text{ GeV} < \Delta E < 0. \text{ GeV}$



$0. \text{ GeV} < \Delta E < 0.05 \text{ GeV}$

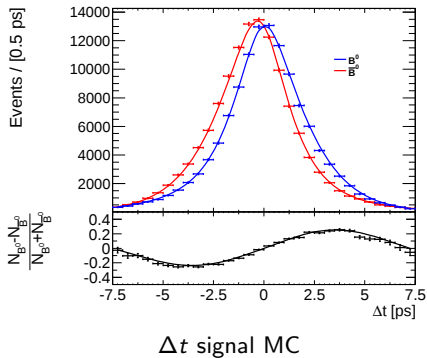


$0.05 \text{ GeV} < \Delta E < 0.1 \text{ GeV}$

$m_{3\pi}$  peak shifts to the right as  $\Delta E$  increases

Width of  $m_{3\pi}$  peak shrinks for small values of  $|\Delta E|$

Model in the first and last bin may be good enough because very few ( $\sim 10$ ) events expected there



Input  $\tau_{B^0} = 1.534$  ps

SVD1  $\tau_{B^0} = 1.522 \pm 0.006$  ps ( $2\sigma$  from input)

SVD2  $\tau_{B^0} = 1.517 \pm 0.005$  ps ( $3.4\sigma$ )

Input  $\mathcal{A}_{CP} = 0$

SVD1  $\mathcal{A}_{CP} = -0.053 \pm 0.007$  ( $7.6\sigma$ )

SVD2  $\mathcal{A}_{CP} = -0.037 \pm 0.006$  ( $6.2\sigma$ )

Input  $\mathcal{S}_{CP} = 0.689$

SVD1  $\mathcal{S}_{CP} = +0.697 \pm 0.010$  ( $0.8\sigma$ )

SVD2  $\mathcal{S}_{CP} = +0.690 \pm 0.008$  ( $0.1\sigma$ )

$$\mathcal{P}_{\text{Sig}}(\Delta t, q) = (1 - f_{ol}) \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \cdot$$

$$\left[ 1 - q\Delta w + q(1 - 2w) \left( \mathcal{A}_{CP} \cos(\Delta m \Delta t) + \mathcal{S}_{CP} \sin(\Delta m \Delta t) \right) \right]$$

$$\otimes R_{B^0 \bar{B}^0} + f_{ol} \mathcal{P}_{ol}$$

## Continuum Model

Sideband

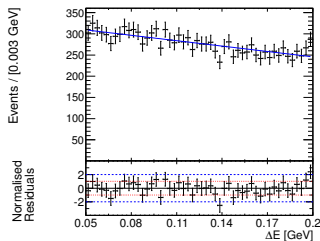
$$\begin{aligned} 5.2 \text{ GeV}/c^2 < M_{bc} < 5.25 \text{ GeV}/c^2 \\ 0.05 \text{ GeV} < \Delta E < 0.2 \text{ GeV} \end{aligned}$$

# Continuum Model

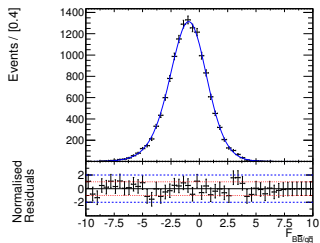
## Continuum model correlation matrix

|                                   | $\Delta E$ | $\mathcal{F}_{B\bar{B}/q\bar{q}}$ | $m_{3\pi}$ | $\mathcal{H}_{3\pi}$ | $\Delta t$ |
|-----------------------------------|------------|-----------------------------------|------------|----------------------|------------|
| $\Delta E$                        | 1          | 0.007                             | 0.005      | 0.001                | 0.012      |
| $\mathcal{F}_{B\bar{B}/q\bar{q}}$ |            | 1                                 | 0.002      | 0.005                | 0.007      |
| $m_{3\pi}$                        |            |                                   | 1          | -0.015               | 0.005      |
| $\mathcal{H}_{3\pi}$              |            |                                   |            | 1                    | -0.001     |
| $\Delta t$                        |            |                                   |            |                      | 1          |

# Continuum $\Delta E$ and $\mathcal{F}_{B\bar{B}/q\bar{q}}$



$\Delta E$  continuum



$\mathcal{F}_{B\bar{B}/q\bar{q}}$  continuum

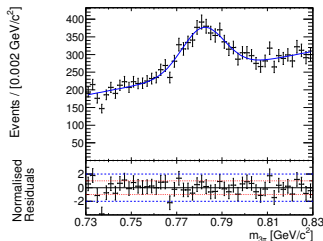
First order Chebyshev

$$\mathcal{P}_{q\bar{q}}(\Delta E) = \sum_{i=0}^1 c_i C_i(\Delta E)$$

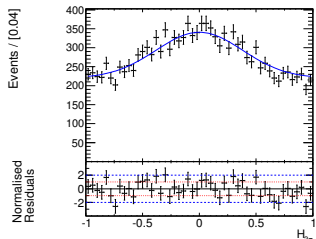
Double Gaussian in each  $r$ -bin  $l$  for SVD2,  
single Gaussian for SVD1

$$\mathcal{P}_{q\bar{q},l}(\mathcal{F}_{B\bar{B}/q\bar{q}}) = fG(\mathcal{F}_{B\bar{B}/q\bar{q}}; \mu_{1,l}, \sigma_{1,l}) + (1-f)G(\Delta E; \mu_{2,1}, \sigma_{2,1})$$

# Continuum $m_{3\pi}$ and $\mathcal{H}_{3\pi}$



$m_{3\pi}$  continuum



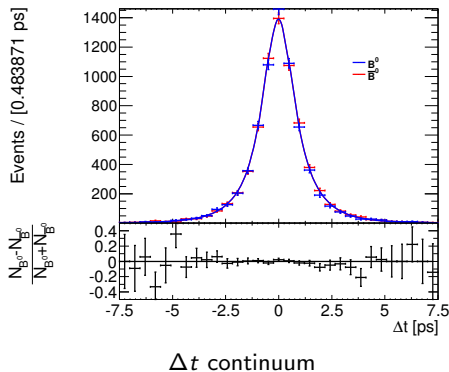
$\mathcal{H}_{3\pi}$  continuum

Gaussian + 1st order Chebyshev

$$\mathcal{P}_{q\bar{q}}(m_{3\pi}) = fG(m_{3\pi}, \mu, \sigma) + (1-f) \sum_{i=0}^1 c_i C_i(m_{3\pi})$$

Gaussian + 1st order Chebyshev

$$\mathcal{P}_{q\bar{q}}(\mathcal{H}_{3\pi}) = fG(\mathcal{H}_{3\pi}, \mu, \sigma) + (1-f) \sum_{i=0}^1 c_i C_i(\mathcal{H}_{3\pi})$$



Lifetime+prompt

$$\mathcal{P}_{q\bar{q}}(\Delta t) = (1 - f_{ol}) \left[ (1 - f_{\delta}) \frac{e^{-|\Delta t|/\tau_{q\bar{q}}}}{2\tau_{q\bar{q}}} + f_{\delta} \delta(\Delta t - \mu_{\delta}) \right] \otimes R_{q\bar{q}} + f_{ol} \mathcal{P}_{ol}$$

## Neutral Charm Model (peaking background)

Peaking background (three pions and a  $K_S^0$  final states)

$$B^0 \rightarrow D^{*-} \pi^+, \text{ with } D^{*-} \rightarrow \bar{D}^0 \pi^- \text{ and } \bar{D}^0 \rightarrow K_S^0 \pi^0$$

$$B^0 \rightarrow D^- \pi^+, \text{ with } D^- \rightarrow K_S^0 \pi^- \pi^0$$

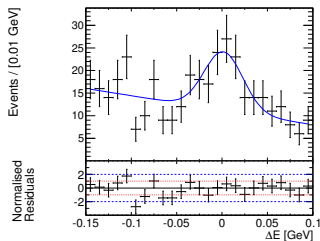
$$B^0 \rightarrow D^- \rho^+, \text{ with } D^- \rightarrow K_S^0 \pi^- \text{ and } \rho^+ \rightarrow \pi^0 \pi^+$$

# Neutral Charm Model (peaking background)

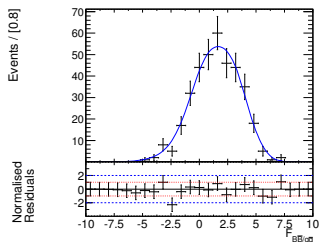
## Neutral Charm model (peaking background) correlation matrix

|                                   | $\Delta E$ | $\mathcal{F}_{B\bar{B}/q\bar{q}}$ | $m_{3\pi}$ | $\mathcal{H}_{3\pi}$ | $\Delta t$ |
|-----------------------------------|------------|-----------------------------------|------------|----------------------|------------|
| $\Delta E$                        | 1          | -0.019                            | 0.066      | -0.05                | -0.041     |
| $\mathcal{F}_{B\bar{B}/q\bar{q}}$ |            | 1                                 | 0.018      | 0.066                | -0.033     |
| $m_{3\pi}$                        |            |                                   | 1          | -0.043               | 0.065      |
| $\mathcal{H}_{3\pi}$              |            |                                   |            | 1                    | 0.019      |
| $\Delta t$                        |            |                                   |            |                      | 1          |

# Peaking Background $\Delta E$ and $\mathcal{F}_{B\bar{B}/q\bar{q}}$



$\Delta E$  peaking background



$\mathcal{F}_{B\bar{B}/q\bar{q}}$  peaking background

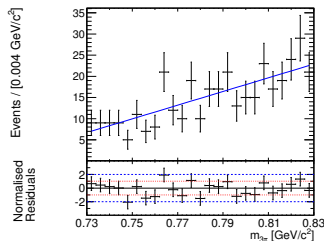
First order Chebyshev + Gaussian

$$\mathcal{P}_{B^0\bar{B}^0}^{\text{Charm, pb}}(\Delta E) = fG(\Delta E; \mu, \sigma) + (1 - f) \sum_{i=0}^1 c_i C_i(\Delta E)$$

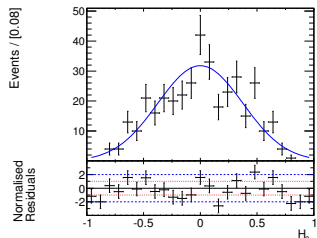
Shape fixed from signal MC, free main mean  $\mu_{1,1}$

$$\mathcal{P}_{B^0\bar{B}^0}^{\text{Charm, pb, 1}}(\mathcal{F}_{B\bar{B}/q\bar{q}}) = f_1 G(\mathcal{F}_{B\bar{B}/q\bar{q}}; \mu_{1,1}, \sigma_{1,1}) + f_2 G(\Delta E; \mu_{2,1}, \sigma_{2,1}) + (1 - f_1 - f_2) G(\Delta E; \mu_{3,1}, \sigma_{3,1})$$

# Neutral charm $m_{3\pi}$ and $\mathcal{H}_{3\pi}$



$m_{3\pi}$  peaking background



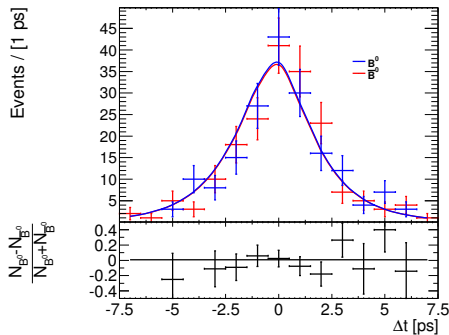
$\mathcal{H}_{3\pi}$  peaking background

Shape fixed from signal MC, Chebyshev 1st order added

$$\mathcal{P}_{B^0\bar{B}^0}^{\text{Charm, pb}}(m_{3\pi}) = f\mathcal{P}_{\text{Sig}}(m_{3\pi}) + (1-f) \sum_{i=0}^1 c_i C_i(m_{3\pi})$$

Gaussian

$$\mathcal{P}_{B^0\bar{B}^0}^{\text{Charm, pb}}(\mathcal{H}_{3\pi}) = G(\mathcal{H}_{3\pi}; \mu, \sigma)$$



$\Delta t$  peaking background,  $\mathcal{A} = 0$ ,  $S = 0$

$$\mathcal{P}_{B^0 \bar{B}^0}^{\text{Charm, pb}}(\Delta t, q) = (1 - f_{ol}) \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}}.$$

$$\left[ 1 - q\Delta w + q(1 - 2w) \left( \mathcal{A}_{CP} \cos(\Delta m \Delta t) + \mathcal{S}_{CP} \sin(\Delta m \Delta t) \right) \right] \\ \otimes R_{B^0 \bar{B}^0} + f_{ol} \mathcal{P}_{ol}$$