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# String Phenomenology

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## String Phenomenology

- classify different setups in ST which lead to SM-like physics
- within each setup, construct examples with low energy physics as close as possible to SM

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D-branes

Dp-branes  $\equiv$  (p+1)-dimensional subspaces on which open strings can end



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closed sector  $\longrightarrow$  dynamics of the vacuum



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e.g. single type II Dp-brane in flat 10d, massless modes

• U(1) gauge boson localized on the brane (enhanced to U(N) with multiple branes and Chan-Paton indexes)



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RR charged, via  $\int_{W_{n+1}} C_{p+1}$  (see anomaly cancellation) Flat Dp-branes preserve 1/2 of the 32 supercharges of type II  $\longrightarrow$  BPS state  $\Rightarrow$  charge-tension relation



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then compactify and split  $V_{X_6} = V_\Sigma V_\perp$  to obtain (note  $g_{YM} \sim V_\Sigma^{-1/2}$ )

$$M_{PI}^2 g_{YM}^2 = \frac{M_s^{11-p} V_\perp}{g_s}$$

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i.e. generate large Planck mass in 4d with low string scale, by increasing  $V_{\perp} \longrightarrow$  hierarchy problem recast in geometrical terms

• start with bosons; NN, ND, DN, DD  $\rightarrow$  only  $\nu = \#$  (ND+DN) matters (even number)

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• zero-point NS energy: 
$$(8 - \nu) \left( -\frac{1}{24} - \frac{1}{48} \right) + \nu \left( \frac{1}{24} + \frac{1}{48} \right)$$

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SUSY breaking condition

$$Q_{lpha}+P ilde{Q}_{lpha}=Q_{lpha}+P(P^{-1}P') ilde{Q}_{lpha}$$

 $\rightarrow$  write  $P^{-1}P' = e^{i\pi(J_1+...+J_{\nu/2})}$ , where each  $e^{i\pi J}$  has eigenvalues  $\pm i \rightarrow$  SUSY unbroken for v = multiple of 4

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- for all  $\theta_j = 0, \ \psi^i, \ i = 1, \dots, 8 \xrightarrow{GSO} 8_C$ : too many components to be chiral in 4d
- for non zero angles,  $\psi^i, \ i = 1, \dots, 4 \xrightarrow{GSO}$  chiral fermion in 4d.

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Simple configuration  $T^6 = T^2 \times T^2 \times T^2$ , with 3-cycles  $\Pi_a$  factorized as products of 1-cycles and  $(n_a^i, m_a^i)$  wrapping numbers in horizontal and vertical directions:



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- $6_a 6_b + 6_b 6_a \longrightarrow I_{ab}$  replicated chiral left-handed fermions in the bi-fundamental  $(N_a, \bar{N_b})$

RR tadpole cancellation, cf. coupling  $\int_{W_{p+1}} C_{p+1}$ , requires (see also Gauss law)

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construct e.g. hypercharge  $Q_Y$ 

Nicolò Piazzalunga (Univ. Padova)

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VQL SU(2)

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Yukawa couplings  $\sim e^{-Area}$   $\sum_{su(3)}^{U_{3}} \sum_{su(3)}^{U_{1}} \sum_{su(3)}^{U_{1}} (go to F-theory for better results)$ 

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Thank you for your attention!