

PARTICLE PHYSICS SCHOOL MUNICH COLLOQUIUM

MAX-PLANCK-INSTITUT FÜR PHYSIK - DECEMBER 14, 2012

THEORY AND PHENOMENOLOGY OF 331 MODELS



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ON ELEMENTARY PARTICLE PHYSICS



MAX-PLANCK-GESELLSCHAFT

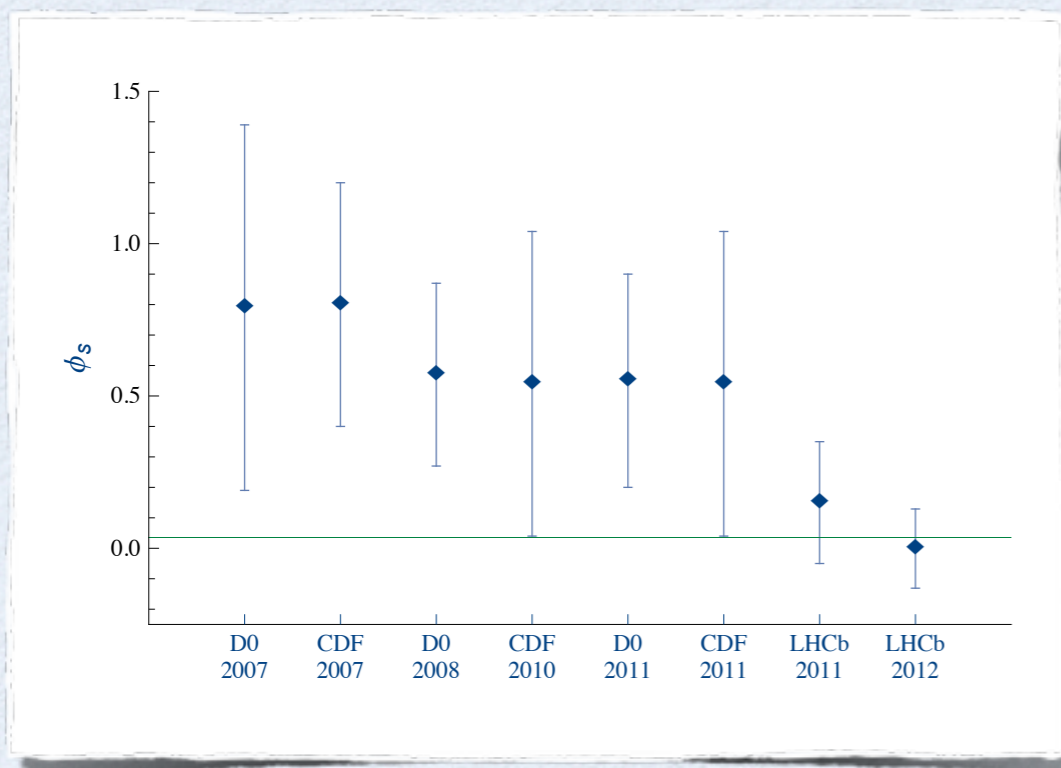


OUTLINE

- Introduction
 - * New data and old tensions in the flavour sector
 - * Motivations for the 331 models
- Theory of the 331 models
 - * General 331 model
 - * A specific realization
- Phenomenology of the 331 models
 - * Constraining the parameter space
 - * Key observables
- Conclusions and Outlook

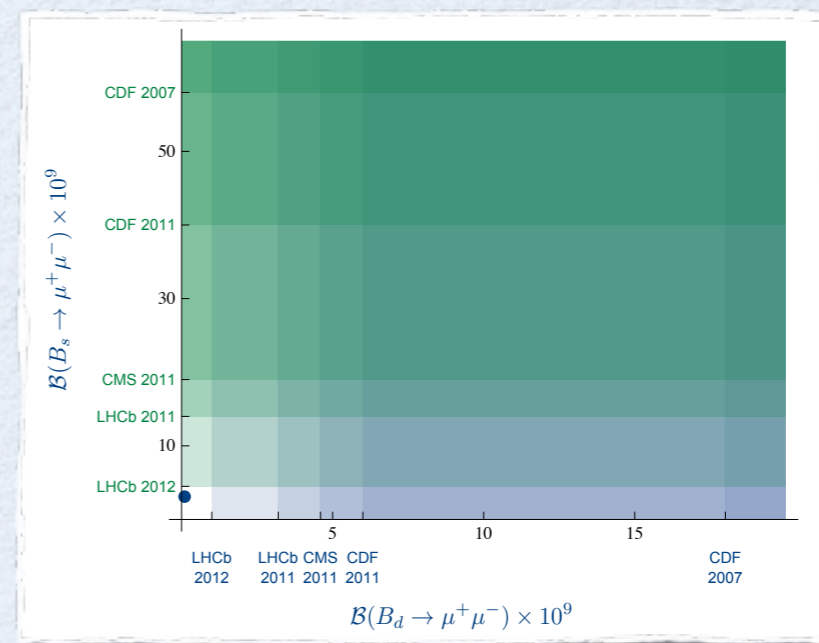
VANISHING HOPES...

$S_{\psi\phi}$: mixing-induced CP asymmetry in the B_s system

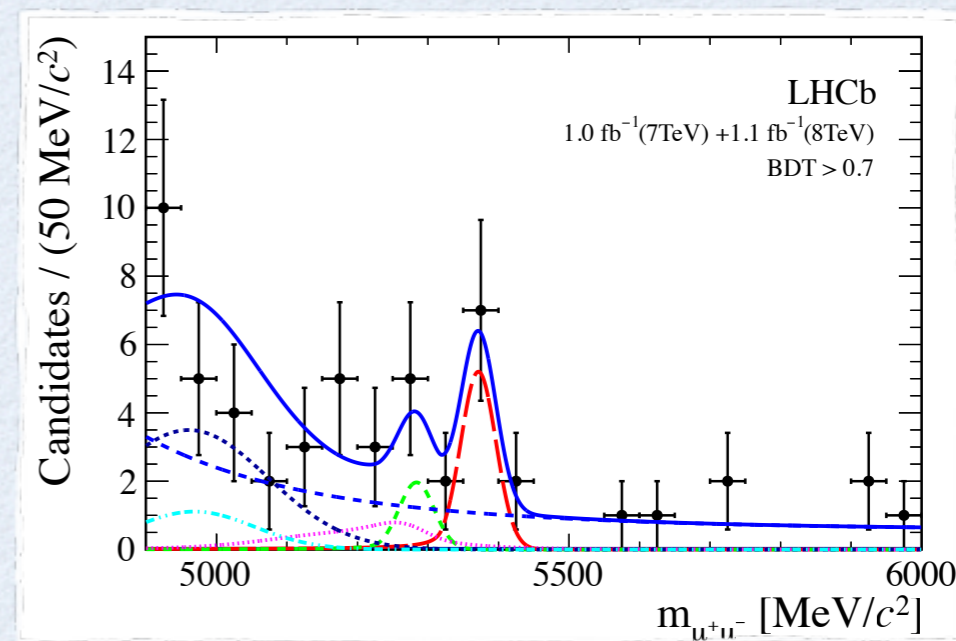


LHCb Collab., PRL **108** (2012)
LHCb Collab., LHCb-CONF-2012-002

$B_{d,s} \rightarrow \mu^+\mu^-$: doubly suppressed and very sensitive to new (pseudo)scalar particles

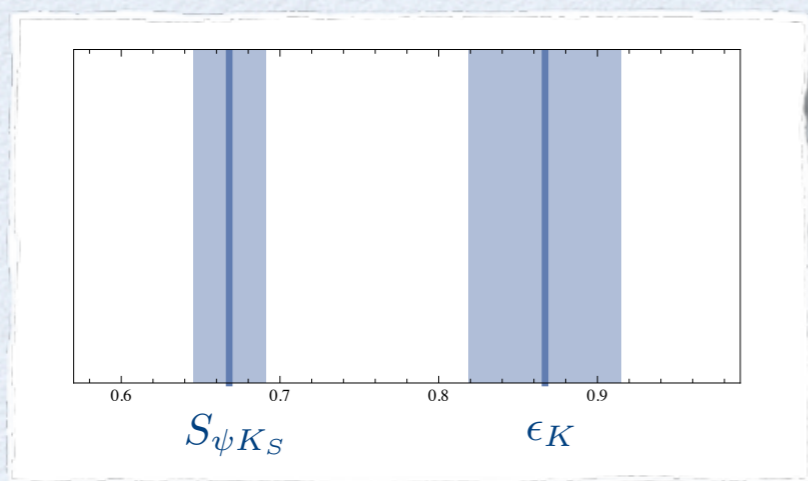


LHCb Collab., Phys. Lett. B **708** (2012)
LHCb Collab., 1203.4493

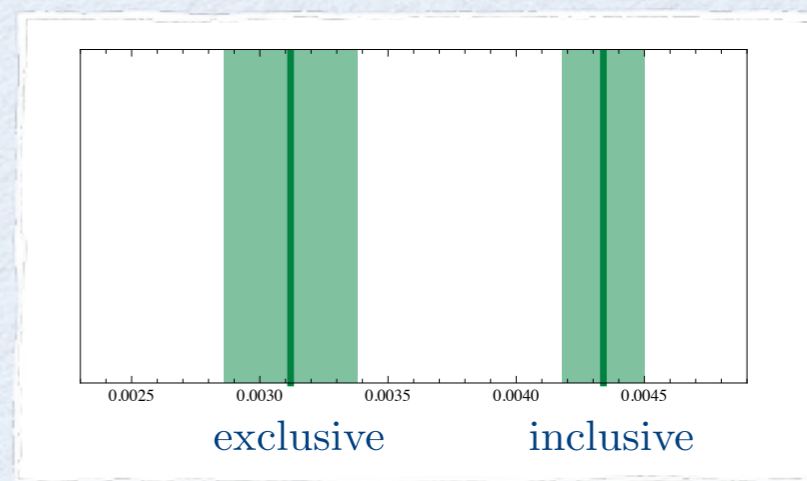


LHCb Collab. @ HCP 2012

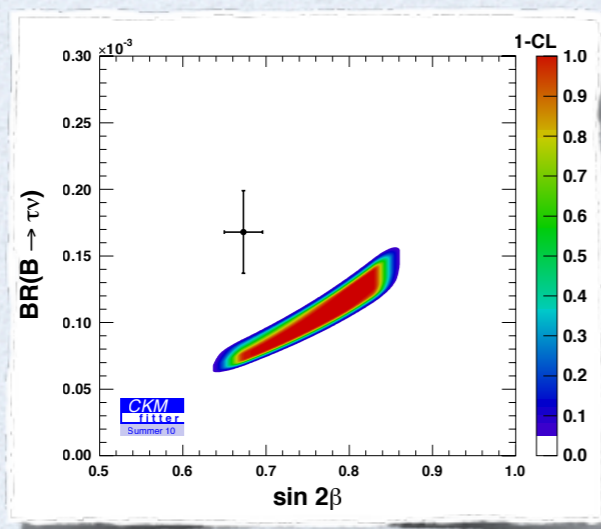
... AND OLD TENSIONS

3.2 σ discrepancywhen extracting $\sin 2\beta$ from ϵ_K and $S_{\psi K_S}$ 

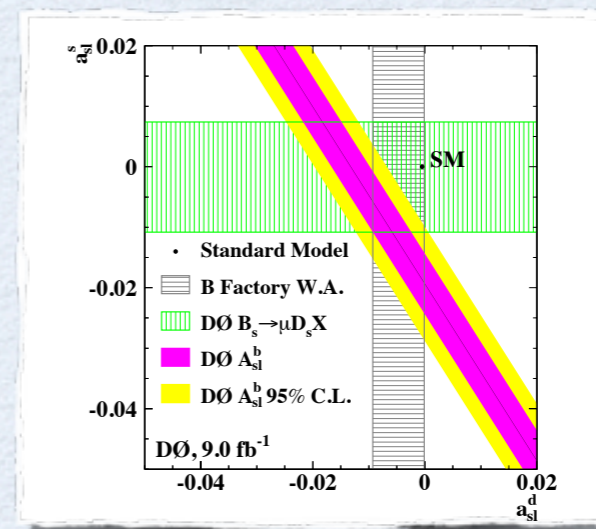
Buras and Guadagnoli, Phys. Rev. D **78** (2008)
 Lunghi and Soni, Phys. Lett. B **708** (2012)

3.3 σ discrepancybetween the determinations of $|V_{ub}|$ 

HPQCD Collab., Phys. Rev. D **73** (2006)
 HFAG, 1010.1589

2.9 σ discrepancybetween $\text{BR}(B \rightarrow \tau \nu)$ and its prediction

Lenz, Nierste and CKMfitter, 1203.0238

3.9 σ deviationof the semileptonic CP asymmetry in $B_{d,s}$ 

D0 Collab., Phys. Rev. D **84** (2011)

MOTIVATIONS FOR STUDYING 331 MODELS

Update the phenomenological analysis of New Physics models

Are they compatible with LHC data?

Can they solve the flavour tensions?

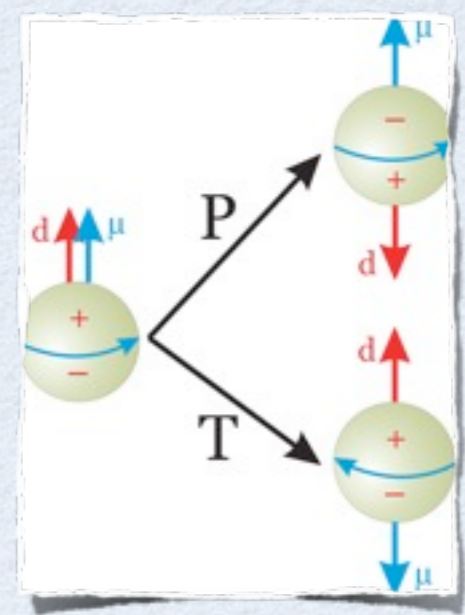
Features of 331 models

Explanation of why just 3 generations

Different treatment of the 3rd generation

Solution to the strong CP problem

	Fermions			Bosons	
Quarks	u up	c charm	t top	γ photon	Force carriers
	d down	s strange	b bottom	Z Z boson	
Leptons	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	
	e electron	μ muon	τ tau	g gluon	



THEORY OF 331 MODELS

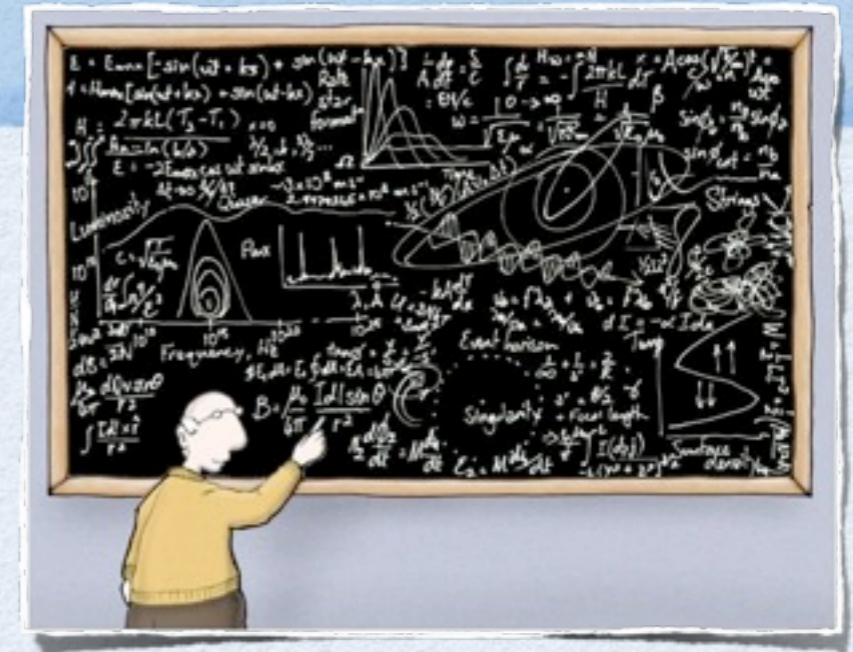
DEFINITION

Gauge group

$$\mathcal{G} = SU(3)_C \otimes SU(3)_L \otimes U(1)_X$$

Charge

$$\hat{Q} = \hat{T}^3 + \beta \hat{T}^8 + X \hat{I} \longrightarrow Y/2$$



Gauge bosons

$$\frac{1}{2} \begin{pmatrix} W_\mu^3 + \frac{1}{\sqrt{3}} W_\mu^8 & \sqrt{2} W_\mu^+ & \sqrt{2} Y_\mu^{Q_Y} \\ \sqrt{2} W_\mu^- & -W_\mu^3 + \frac{1}{\sqrt{3}} W_\mu^8 & \sqrt{2} V_\mu^{Q_V} \\ \sqrt{2} Y_\mu^{-Q_Y} & \sqrt{2} V_\mu^{-Q_V} & -\frac{2}{\sqrt{3}} W_\mu^8 \end{pmatrix}$$

Fermions

$$q_L \sim (3, 3, X_q^L) \rightarrow (3, 2, Y_q^L) \oplus (3, 1, Y_q^L)$$

$$q_R = (3, 1, Y_q^R)$$

$$\ell_L \sim (1, 3, X_\ell^L) \rightarrow (1, 2, Y_\ell^L) \oplus (1, 1, Y_\ell^L)$$

$$\ell_R = (1, 1, Y_\ell^R)$$

THEORY OF 331 MODELS

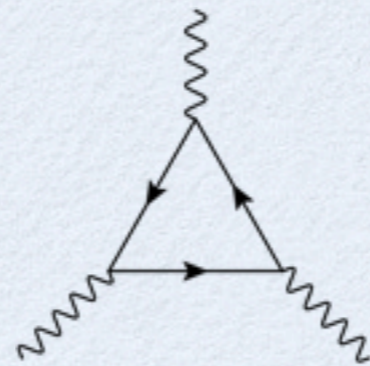
ANOMALY CANCELLATION



Anomaly: a symmetry of the classical action is destroyed by loop corrections.

A **gauge anomaly** leads to the inconsistency of the theory!

Using group theory we can say if a theory is anomaly free:



$$\mathcal{A}^{abc} = \text{Tr} [t^a \{t^b, t^c\}]$$

Results:

$$N_q = N_\ell \equiv N$$

$$t_\ell + 3t_q = \bar{t}_\ell + 3\bar{t}_q = 2N$$

Asymptotic freedom: $N < 5$



$$N = 3$$

$$t_q = 2, \quad \bar{t}_q = 1$$

THEORY OF 331 MODELS
SYMMETRY BREAKING

$$SU(3)_L \otimes U(1)_X \xrightarrow{\langle \Phi_1 \rangle} SU(2)_L \otimes U(1)_Y \xrightarrow{\langle \Phi_2 \rangle} U(1)_Q$$

$$\langle \chi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ u \end{pmatrix}$$

$$\langle \rho \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \\ 0 \end{pmatrix}$$

$$\langle \eta \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} v' \\ 0 \\ 0 \end{pmatrix}$$

$$\langle S_{1\dots 4} \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & 0 & w_i \\ 0 & 0 & 0 \\ w_i & 0 & 0 \end{pmatrix}$$

Gauge bosons
masses and mixing

$$u \gg v, v', w_i$$

$$\downarrow$$

$$m_Y, m_V \gg m_W$$

$$\begin{pmatrix} W_\mu^3 \\ W_\mu^8 \\ X_\mu \end{pmatrix} = U \begin{pmatrix} A_\mu \\ Z_\mu \\ Z'_\mu \end{pmatrix}$$

Fermions
masses and mixing

$$\begin{pmatrix} u_L \\ c_L \\ t_L \end{pmatrix} = W_L \begin{pmatrix} u'_L \\ c'_L \\ t'_L \end{pmatrix}$$

$$\begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix} = V_L \begin{pmatrix} d'_L \\ s'_L \\ b'_L \end{pmatrix}$$

$$W_L^\dagger V_L = V_{\text{CKM}}$$

Different treatment
of the 3rd generation

\downarrow
 W_L and V_L are
both relevant!

THEORY OF 331 MODELS

331 MODEL: $\beta = 1/\sqrt{3}$

Fermions

$$\begin{pmatrix} u \\ d \\ D \end{pmatrix} \quad \begin{pmatrix} c \\ s \\ S \end{pmatrix} \quad \begin{pmatrix} b \\ -t \\ T \end{pmatrix}$$

Gauge bosons

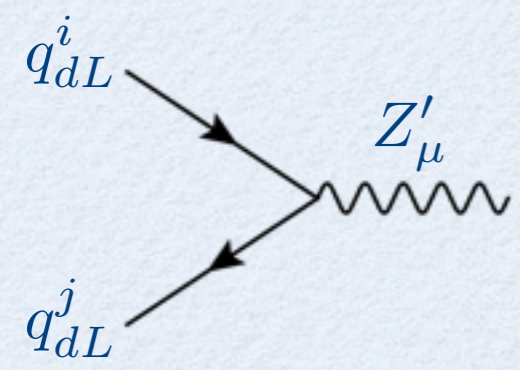
$$\frac{1}{2} \begin{pmatrix} \dots & \sqrt{2}W_\mu^+ & \sqrt{2}Y_\mu^+ \\ \sqrt{2}W_\mu^- & \dots & \sqrt{2}V_\mu^0 \\ \sqrt{2}Y_\mu^- & \sqrt{2}\bar{V}_\mu^0 & \dots \end{pmatrix} \quad \begin{pmatrix} A_\mu \\ Z_\mu \\ Z'_\mu \end{pmatrix}$$

Higgs sector



Feynman rules: what to take home

Y^+, V^0, \bar{V}^0 only interact with $D, S, T \longrightarrow$ all phenomenologically irrelevant



$$V_L = \begin{pmatrix} \tilde{c}_{12}\tilde{c}_{13} & \tilde{s}_{12}\tilde{c}_{23}e^{i\delta_3} - \tilde{c}_{12}\tilde{s}_{13}\tilde{s}_{23}e^{i(\delta_1-\delta_2)} & \tilde{c}_{12}\tilde{c}_{23}\tilde{s}_{13}e^{i\delta_1} + \tilde{s}_{12}\tilde{s}_{23}e^{i(\delta_2+\delta_3)} \\ -\tilde{c}_{13}\tilde{s}_{12}e^{-i\delta_3} & \tilde{c}_{12}\tilde{c}_{23} + \tilde{s}_{12}\tilde{s}_{13}\tilde{s}_{23}e^{i(\delta_1-\delta_2-\delta_3)} & -\tilde{s}_{12}\tilde{s}_{13}\tilde{c}_{23}e^{i(\delta_1-\delta_3)} - \tilde{c}_{12}\tilde{s}_{23}e^{i\delta_2} \\ -\tilde{s}_{13}e^{-i\delta_1} & -\tilde{c}_{13}\tilde{s}_{23}e^{-i\delta_2} & \tilde{c}_{13}\tilde{c}_{23} \end{pmatrix} \quad (6)$$

$$\propto i g v_{3i}^* v_{3j}$$

Z' mediates FCNCs governed by 4 parameters:

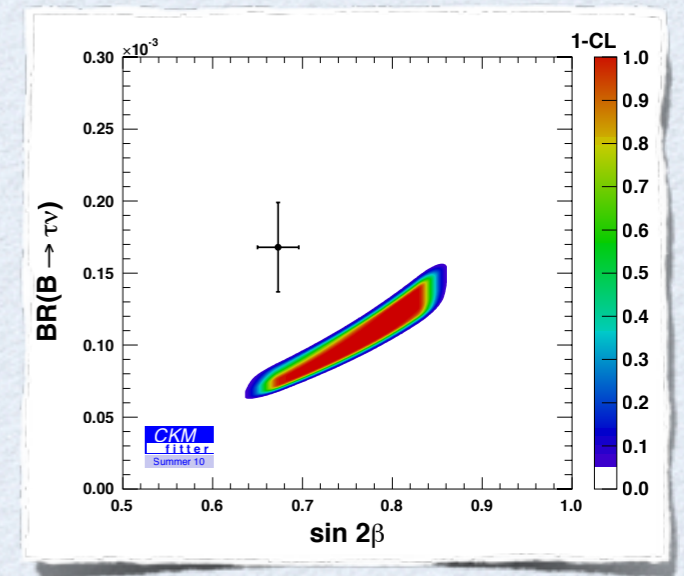
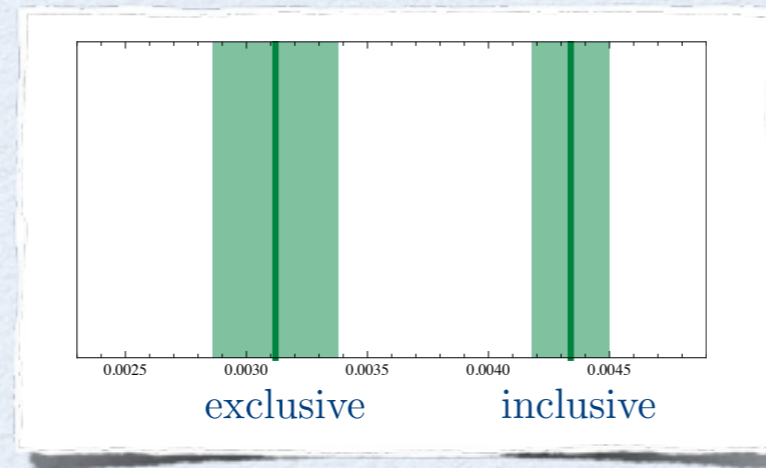
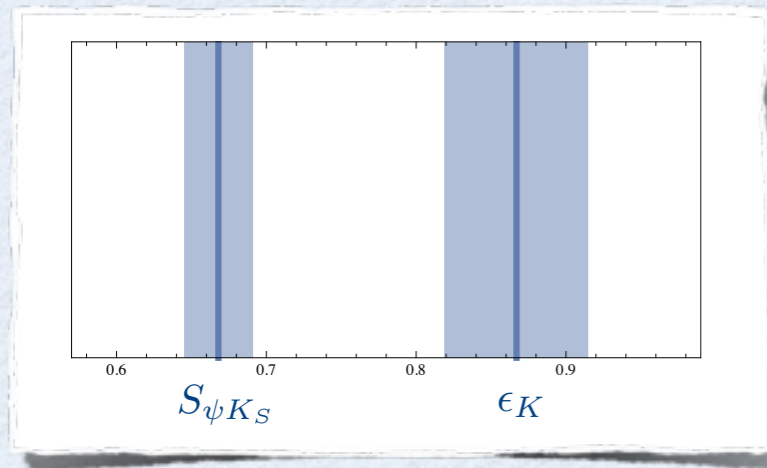
$s_{13} \quad s_{23} \quad \delta_1 \quad \delta_2$

TENSIONS IN THE UNITARITY TRIANGLE: $\epsilon_K - S_{\psi K_S}$ VS. V_{ub}

sin2 β from...

Determination of $|V_{ub}|$...

Prediction of BR(B \rightarrow τ ν)...



Scenario 1

exclusive (small) V_{ub}
 ϵ_K below the data of 1-2 σ
 $S_{\psi K_S}$ in agreement with data
 BR(B \rightarrow τ ν) below data of 3 σ

Scenario 2

inclusive (large) V_{ub}
 ϵ_K in agreement with data
 $S_{\psi K_S}$ above the data of 2-3 σ
 BR(B \rightarrow τ ν) below data of 1 σ

FCNCs AND THE PARAMETER SPACE

$$i\mathcal{L}_{\text{FCNC}} = i \left[\Delta^{sd} (\bar{s}\gamma^\mu P_L d) + \Delta^{bd} (\bar{b}\gamma^\mu P_L d) + \Delta^{bs} (\bar{b}\gamma^\mu P_L s) \right] Z'_\mu$$

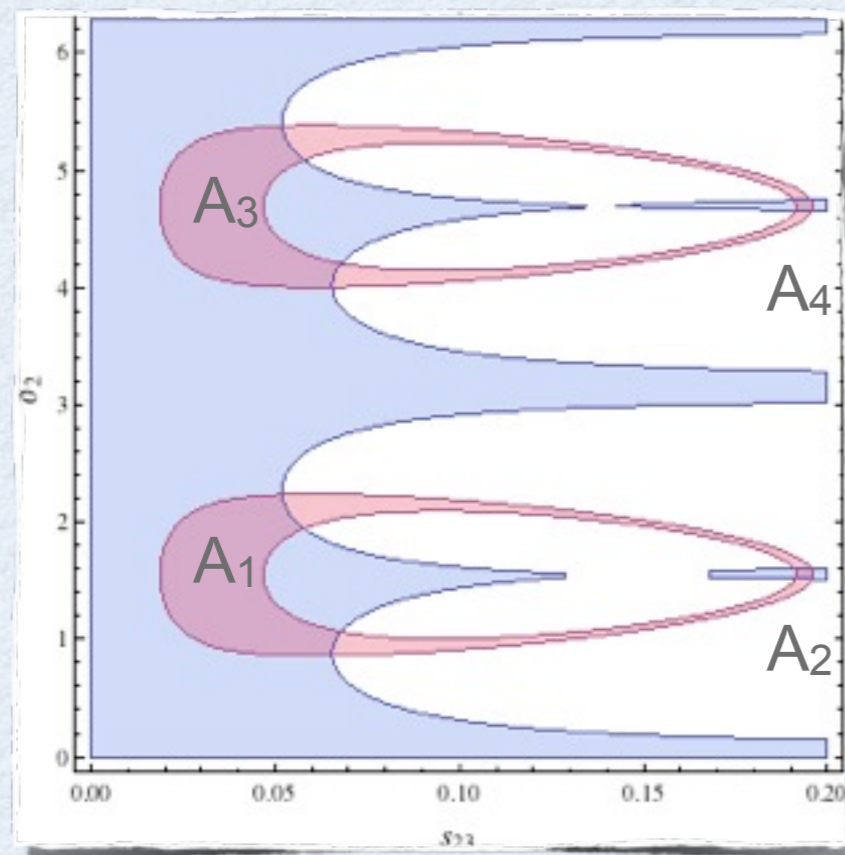
$$\Delta^{sd} = 0.61 g s_{13} s_{23} e^{i(\delta_2 - \delta_1)}$$

$$\Delta^{bd} = -0.61 g s_{13} e^{-i\delta_1}$$

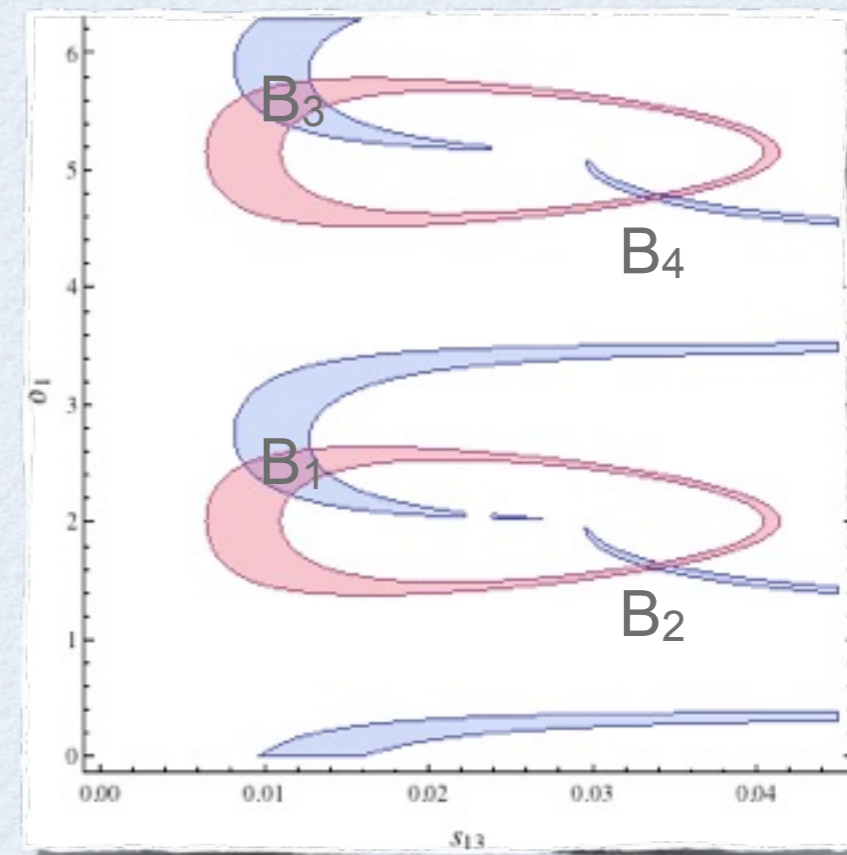
$$\Delta^{bs} = -0.61 g s_{23} e^{-i\delta_2}$$

B_d observables depend only from s_{13} and δ_1 , B_s observables only from s_{23} and δ_2

ΔM_s and $S_{\psi\phi}$

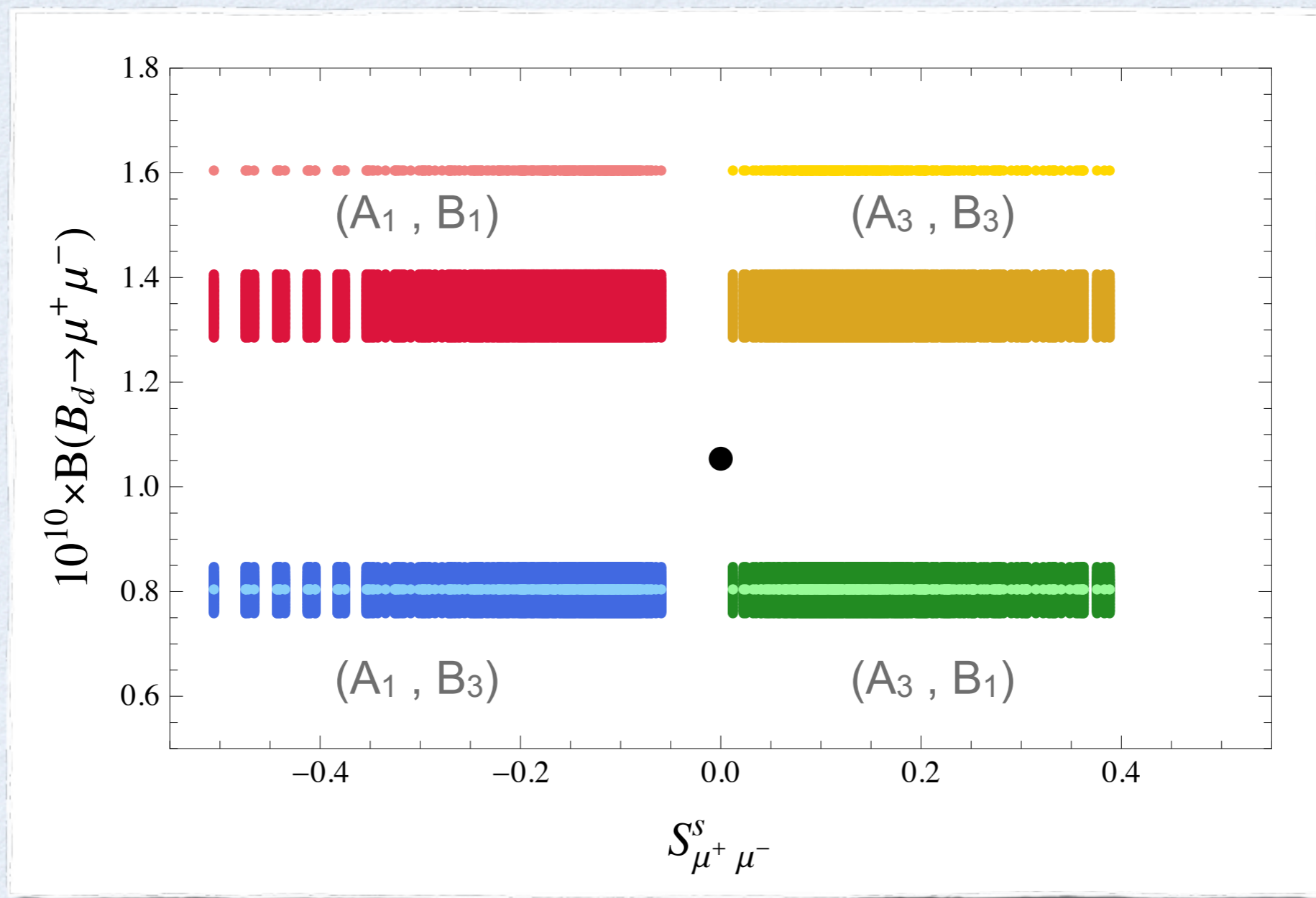


ΔM_d and $S_{\psi K_s}$



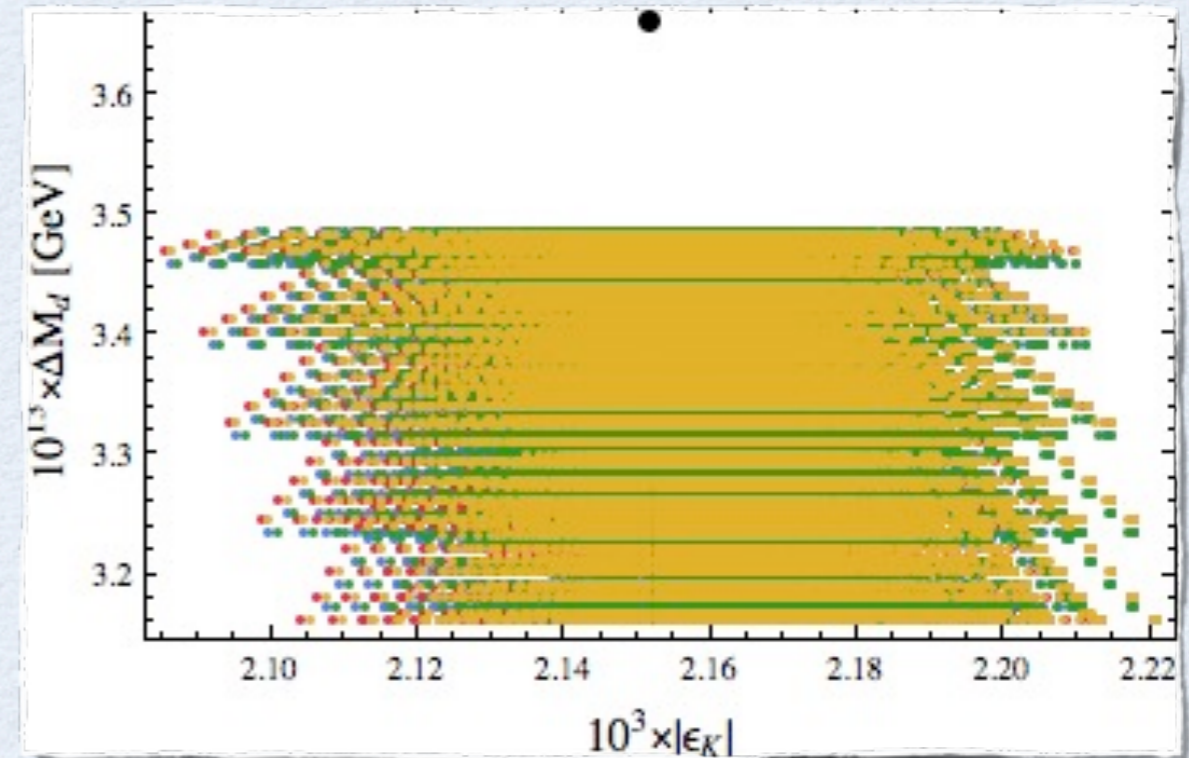
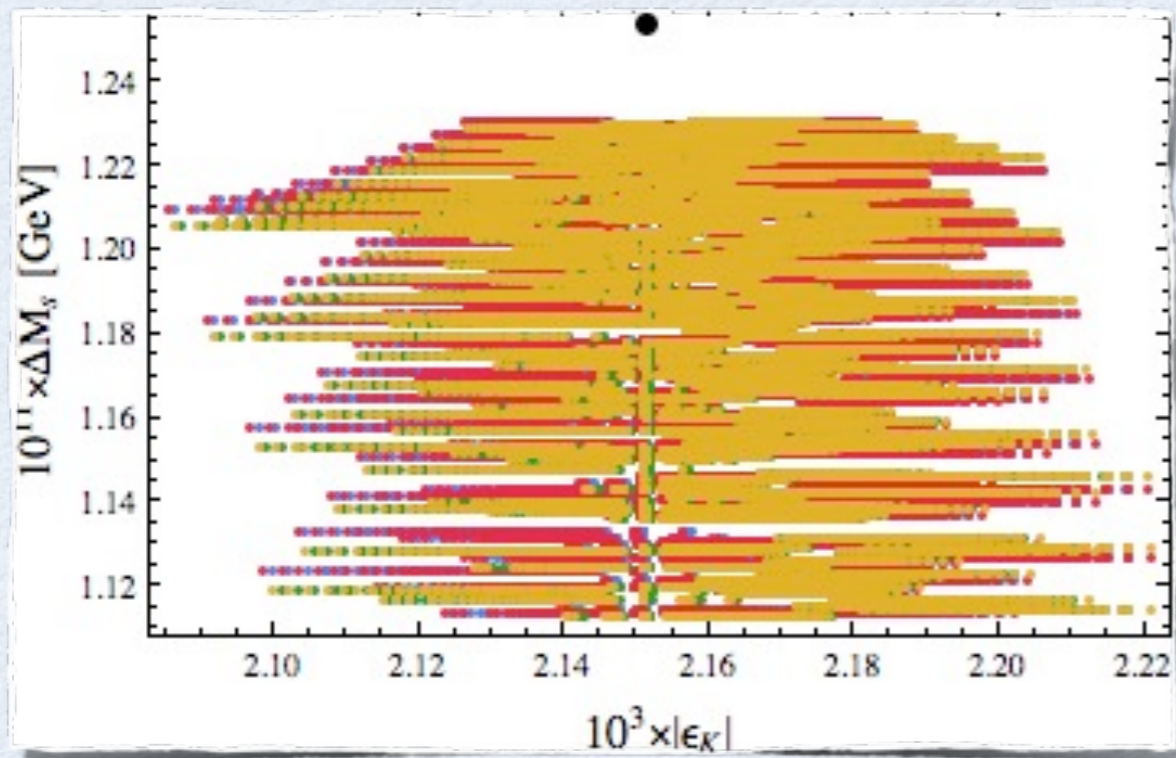
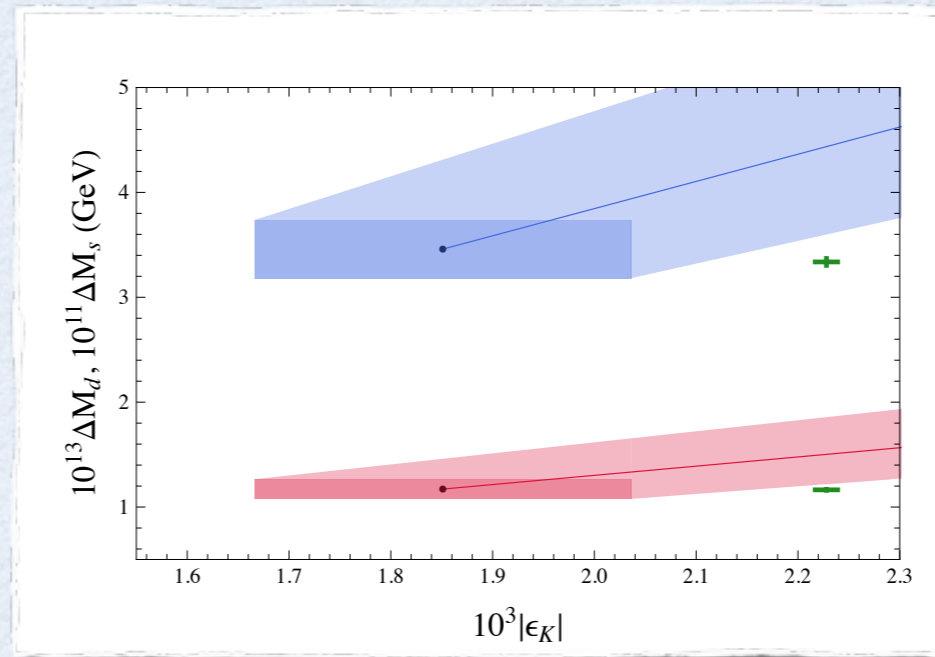
$B_{d,s} \rightarrow \mu^+ \mu^-$ AND THE PARAMETER SPACE

Combining B_d and B_s observables \rightarrow univocal selection of the parameter space area

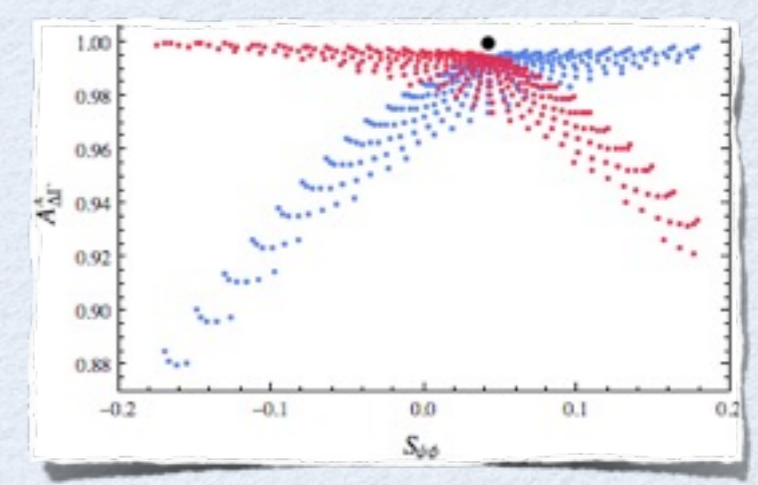
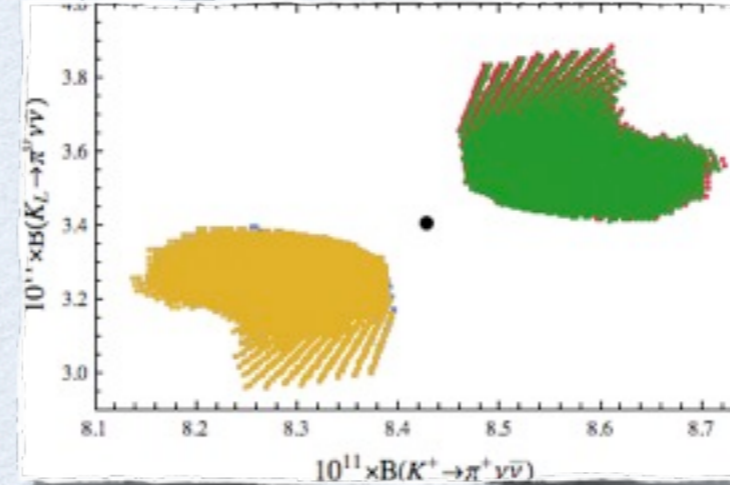
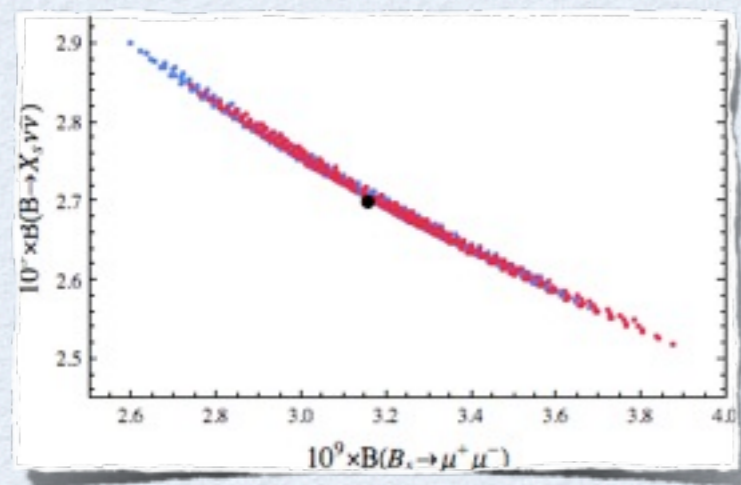
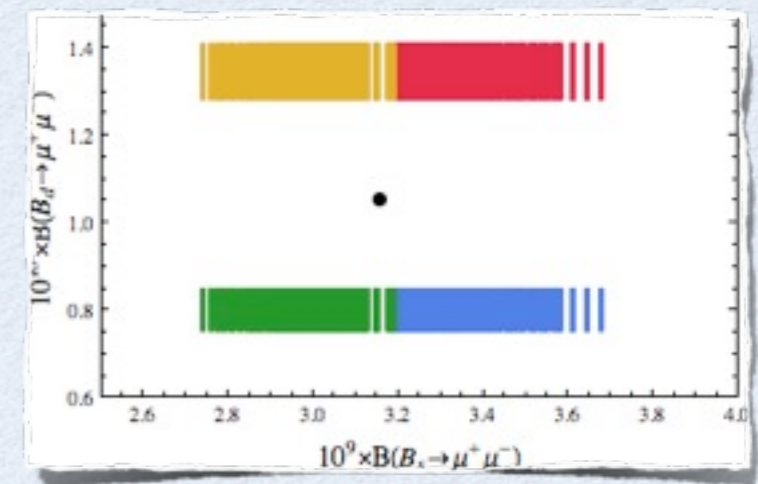
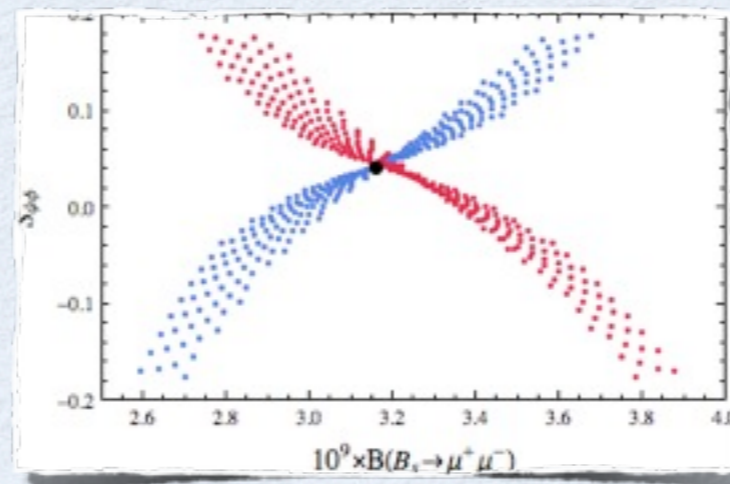
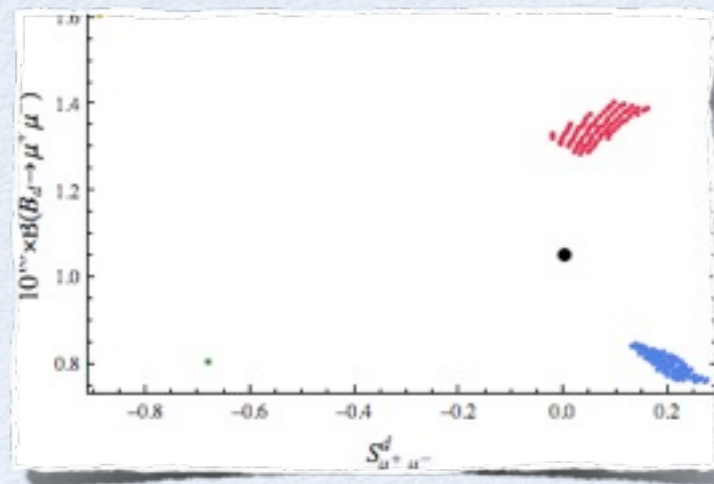
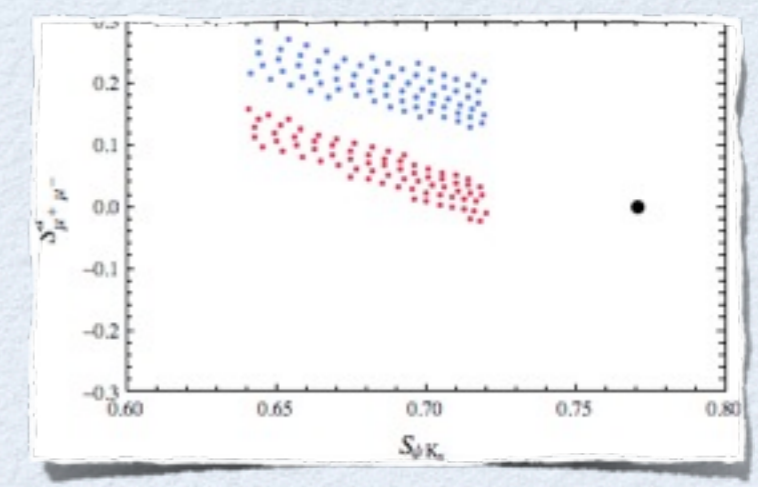
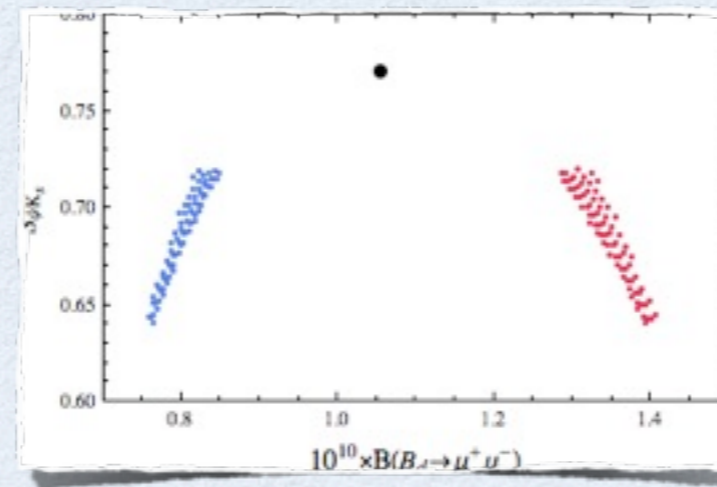
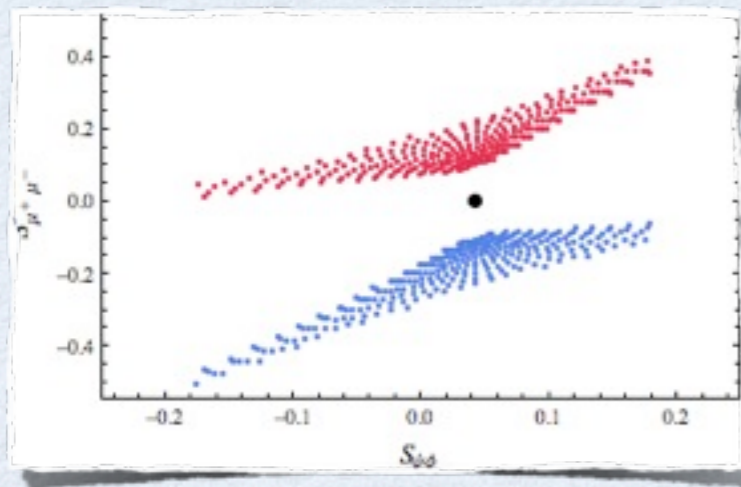


MOVING TO THE K SECTOR: ϵ_K VS $\Delta M_{d,s}$

SM
&
Constrained MFV



MORE OBSERVABLES AND CORRELATIONS



CONCLUSIONS

- Last data from LHCb indicates that the SM has passed also to the tests of $S_{\psi\phi}$ and $B_{d,s} \rightarrow \mu^+\mu^-$; nevertheless, 1-3 σ tensions in flavour observables continue to seriously afflict the SM.
- The 331 models are worth of study since they explain why there are just 3 generations of fermions. They feature a Z' which mediate tree-level FCNCs with few new parameters.
- The parameter space will be strongly constrained in the next future: the model can survive and relax many flavour tensions, or can be ruled out.

THANKS!