



# CKM Angle $\phi_2$ From $B \rightarrow \rho\rho$ Decays

Pit Vanhoefer

Max-Planck-Institut für Physik

pvanhoef *at* mpp.mpg.de



Max-Planck-Institut für Physik  
(Werner-Heisenberg-Institut)

1) Motivation

2a) Measurement of  $\mathcal{B}(B^0 \rightarrow \rho^0 \rho^0)$

2b) Implication for  $\phi_2$

3) Outlook



# CP Violation

matter anti-matter asymmetry

weak interaction can violate  $C$ (charge),  $P$ (parity) as well as  $CP$  symmetry

$\Rightarrow$  particle and antiparticle can behave differently

SM has a built-in mechanism that generates  $CP$  violation:  $CKM$  mechanism.

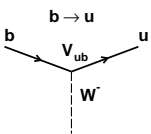
weak and mass Eigenstates are related through a **complex, unitary** matrix:

Cabibbo-Kobayashi-Maskawa  $CKM$  Matrix

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}_{\text{weak}} = V_{CKM} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{mass}} \equiv \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{mass}}$$

elements  $V_{ij}$  are quark flavor transition probabilities ( $W^\pm$  exchange).

BUT NOT able to produce observed asymmetry in our universe.



# CP Violation

4 free parameters(3 mixing angles, 1 complex phase) for 3 generations of quarks

Approx. representation of  $V_{\text{CKM}}$  in terms of the Cabibbo angle,  $\lambda = \sin \theta_C \approx 0.22$

$$V_{\text{CKM}} \approx \mathcal{O} \begin{pmatrix} \boxed{1} & \lambda & \boxed{\lambda^3} \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

unitarity  $\rightarrow$

$$V_{\text{CKM}} V_{\text{CKM}}^\dagger = \mathbf{1}$$

$$\sum_{j=1}^3 V_{jk} V_{ij}^* = 0, i \neq k$$

relevant relation for  $B$  meson decays

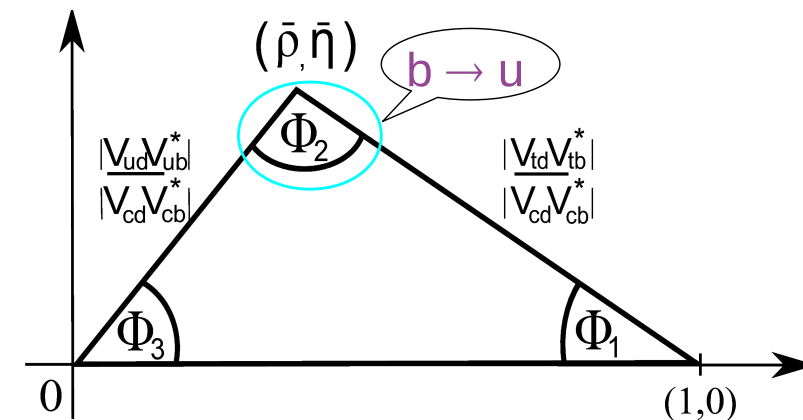
$$\begin{aligned} V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* &= 0 \\ \mathcal{O}(\lambda^3) & \quad \mathcal{O}(\lambda^3) \quad \mathcal{O}(\lambda^3) \end{aligned}$$

can be represented as a triangle in the complex plane  $\rightarrow$

sides with similar length  $\Rightarrow$  large **CP violation**

5 observables (3 angles, 2 sides)  $\Rightarrow$  over-constraint

confirm SM **or** find new physics



# $CP$ Violation in the $B$ System

difference of particle ( $B$ ) and anti-particle ( $\bar{B}$ ):

- complex quantity:  $\lambda_{CP} \equiv \frac{qA_f}{p\bar{A}_f} = e^{-i\phi_W} \frac{|q|}{|p|} \frac{|A_f|}{|\bar{A}_f|} e^{-i\phi_S}$

$A_f(\bar{A}_f)$ : amplitude for  $B(\bar{B}) \rightarrow$  final state  $f$ ,  $p, q$  mixing parameters and  $\phi_{W,S}$ : weak/strong phase differences

$\Rightarrow$  3 different types of  $CP$

A)  $|A_f| \neq |\bar{A}_f| \rightarrow$  different rates for  $B$  and  $\bar{B} \Rightarrow$  **direct  $CP$**   $\rightarrow \mathcal{A}_{CP}$

B)  $|\frac{q}{p}| \neq 1$ :  $CP$  in the mixing (e.g.  $K \leftrightarrow \bar{K}$ ), but in the  $B$  syst.  $p \approx q$

C)  $|A_f| = |\bar{A}_f|$  and  $|p| = |q|$  but  $\mathcal{I}(\lambda_{CP}) \neq 0 \Rightarrow$  **indirect  $CP$**   $\rightarrow \mathcal{S}_{CP}$

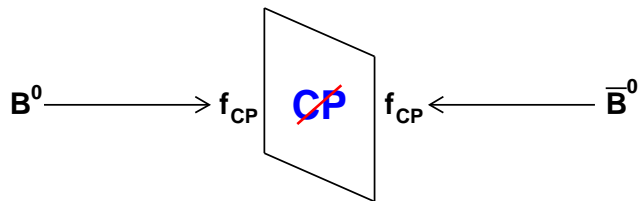
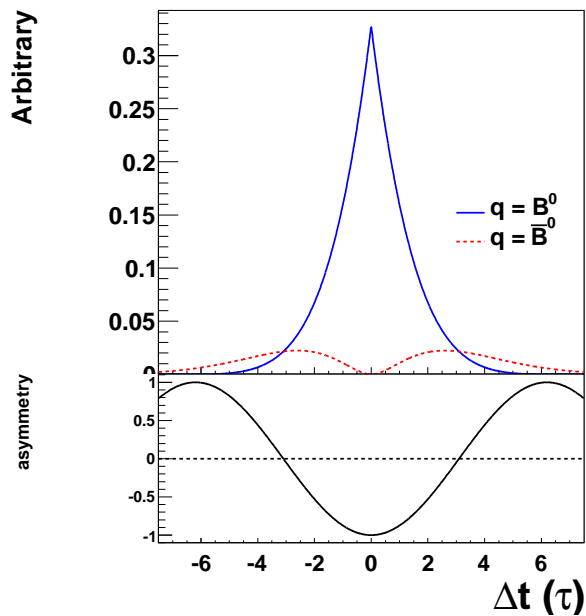
and is interference between A) and B)

- time ( $\Delta t$ ) and flavor ( $q = \pm 1$ ) dependent decay rate

$$\mathcal{P}(\Delta t, q) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \left\{ 1 + q \left[ \mathcal{S}_{CP} \sin(\Delta m_d \Delta t) + \mathcal{A}_{CP} \cos(\Delta m_d \Delta t) \right] \right\}$$

# CP Violation in the B System

$$\frac{N_{B^0}(\Delta t, f_{CP}) - N_{\bar{B}^0}(\Delta t, f_{CP})}{N_{B^0}(\Delta t, f_{CP}) + N_{\bar{B}^0}(\Delta t, f_{CP})} = \mathcal{A}_{CP} \cos(\Delta m \Delta t) + \mathcal{S}_{CP} \sin(\Delta m \Delta t), \quad \Delta t = t' - t$$



CP asymmetry parameters:

← (direct CP)

$$\mathcal{A}_{CP} = \frac{|\lambda_c^2| - 1}{|\lambda_c^2| + 1}$$

different decay rates

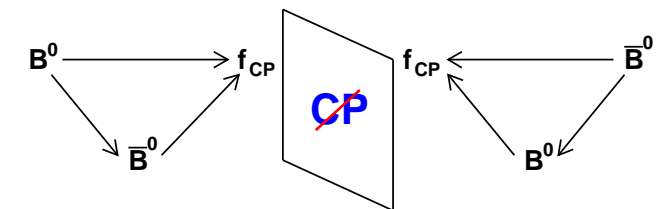
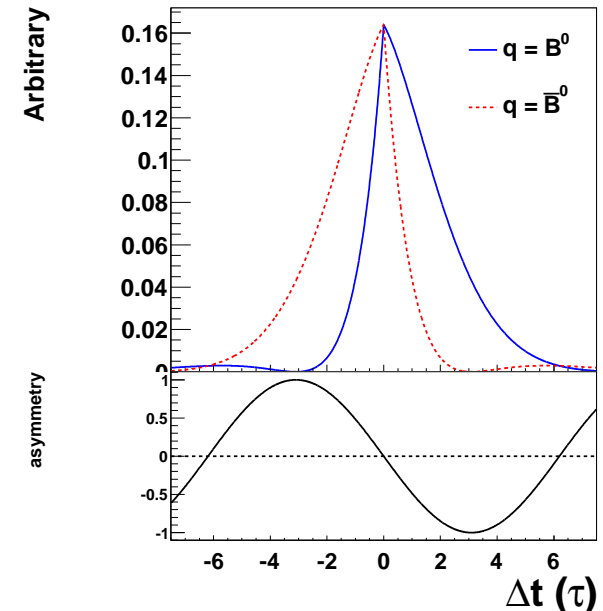
— and —

(indirect CP) →

$$\mathcal{S}_{CP} = \frac{2\mathcal{I}(\lambda_{CP})}{|\lambda_c^2| + 1}$$

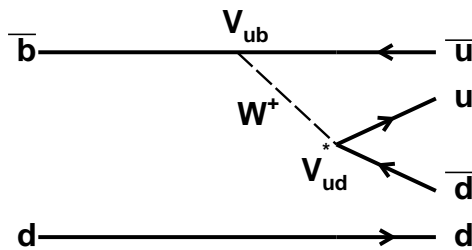
different time evolution

for  $B$  and  $\bar{B}$  decaying into a CP eigenstate  $f_{CP}$

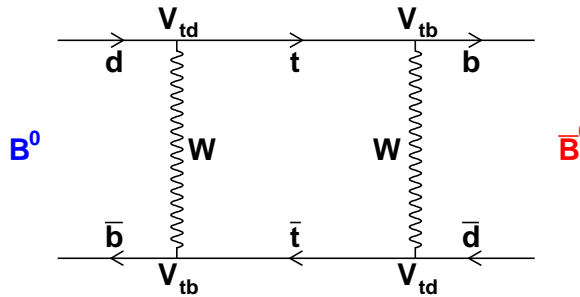


# $\phi_2$ and mixing induced ~~CP~~

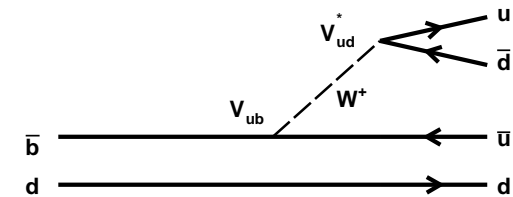
$B \rightarrow \rho^0 \rho^0$



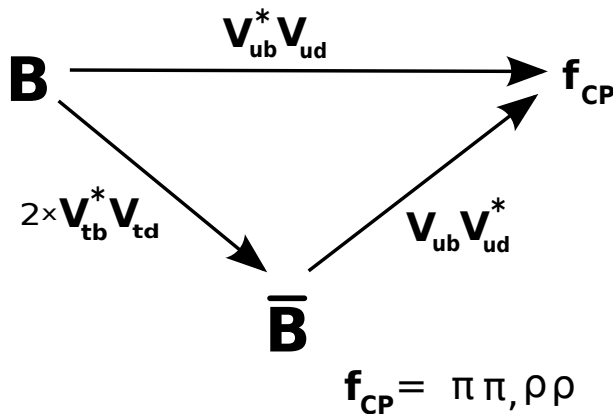
$B\bar{B}$  mixing



same for e.g.  $B \rightarrow \rho^+ \rho^-$ ,  
 $B \rightarrow \pi^+ \pi^-$ ,  $B \rightarrow \pi^0 \pi^0$  ...

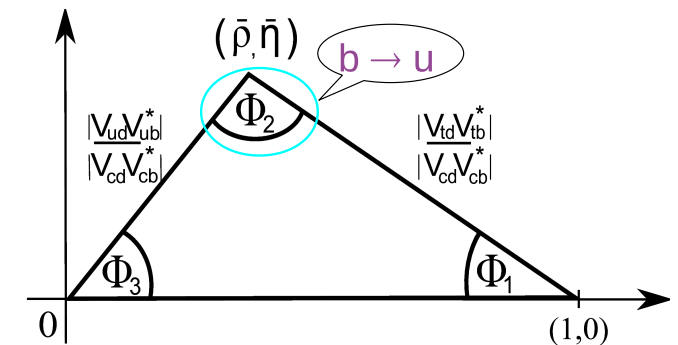


- $\phi_2$  is phase between  $V_{td}V_{tb}^*$  and  $V_{ub}V_{ud}^*$
- $\phi_2$  only through indirect ~~CP~~ in  $b \rightarrow u$  e.g. interference between  $B \rightarrow \rho\rho$  and  $B \rightarrow \bar{B} \rightarrow \rho\rho$



$$\phi_2 = \arg\left(\frac{V_{td}V_{tb}^*}{V_{ub}V_{ud}^*}\right)$$

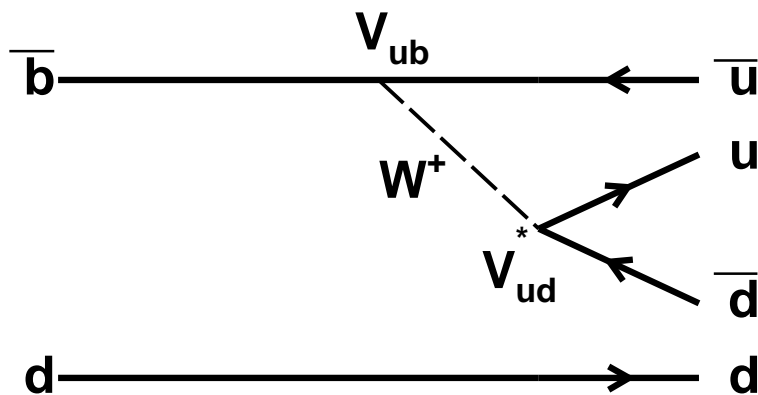
$$\Rightarrow \mathcal{S}_{CP} \sim \sin(2\phi_2)$$



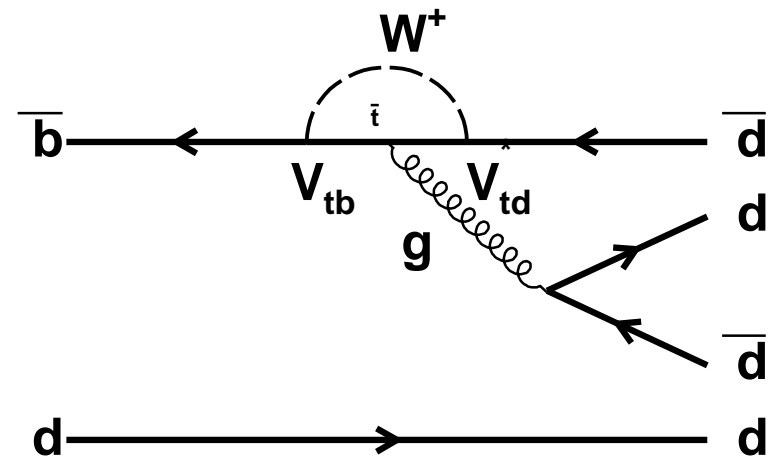
# Living With Pollution

$b \rightarrow u (\rho, \pi, \dots)$  at Tree level: sensitive to  $\phi_2$  ( $\mathcal{S}_{CP}$ ) and no direct  $\mathcal{CP}$  ( $\mathcal{A}_{CP} = 0$ )

BUT more amplitudes (penguins) can contribute



$\Rightarrow \phi_2$



penguin pollution  $\Rightarrow \Delta\phi_2, \mathcal{A}_{CP}$

$\Rightarrow$  measured observable  $\phi_2^{eff} = \phi_2 + \Delta\phi_2$

$\rightarrow$  extraction of  $\Delta\phi_2$  with isospin analysis is possible

$\mathcal{A}_{CP} \neq 0 \Rightarrow$  direct  $\mathcal{CP}$

$\mathcal{S}_{CP} \neq 0 \Rightarrow$  indirect  $\mathcal{CP}$



# Recover $\phi_2$

- **extraction of  $\Delta\phi_2$  with isospin analysis** (remove penguin pollution)

for unflavored isospin triplets, e.g.  $\rho, \pi$

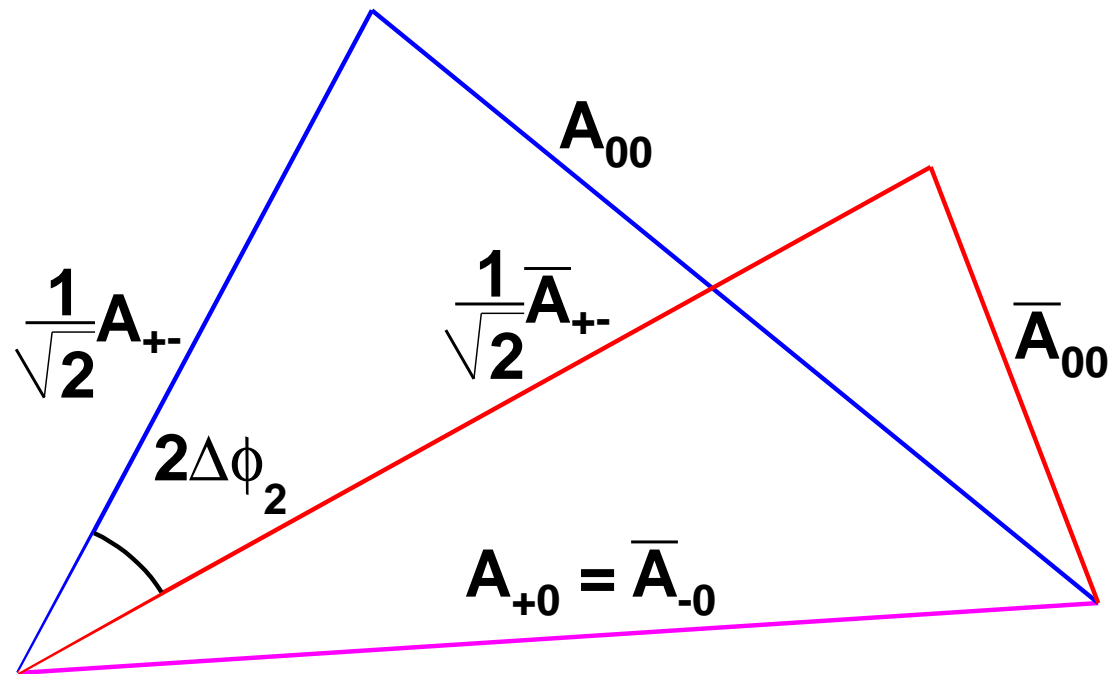
Bose statistics:  $\Rightarrow l=0,2$  (final states);

tree  $l=0,2$ ;

penguin:  $l=0$  only (gluon;  $l=0$ )

allows to formulate relations of the decay amplitudes  $A$

e.g.  $\bar{A}^{+-} = \mathcal{A}(\bar{B} \rightarrow \rho^+ \rho^-)$



- $\frac{1}{\sqrt{2}} A^{+-} + A^{00} = A^{+0}$

- $\frac{1}{\sqrt{2}} \bar{A}^{+-} + \bar{A}^{00} = \bar{A}^{-0}$

- $A^{+0} = \bar{A}^{-0}$  (no penguin)

$\Rightarrow$  geometrical considerations reveal  $\Delta\phi_2$

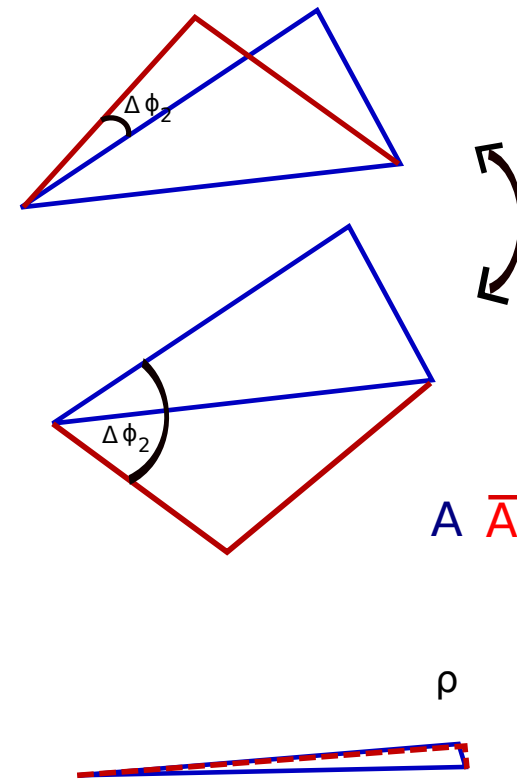
# Recover $\phi_2$

In  $b \rightarrow u$  transitions

- measurement of  $\Delta t$  provides  $\sin(2\phi_{2,eff}) = \sin(2(\phi_2 + \Delta\phi_2))$
- extraction of  $\Delta\phi_2$  through isospin analysis possible  
but  $2(\sin) \times 4(\Delta\phi_2) = 8$  fold ambiguity

In the  $\rho$  system the SM predicts small penguin pollution

- $\phi_2$  from  $B^0 \rightarrow \rho^+ \rho^-$
- $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$  relatively very small  
multiple solutions due to  $\Delta\phi_2$  overlap  $\Rightarrow$  only 2 fold ambiguity
- current error on  $\phi_2$  dominated by the  $\rho$  system  
 $\Rightarrow$  this talk: measurement of  $\mathcal{B}(B^0 \rightarrow \rho^0 \rho^0)$



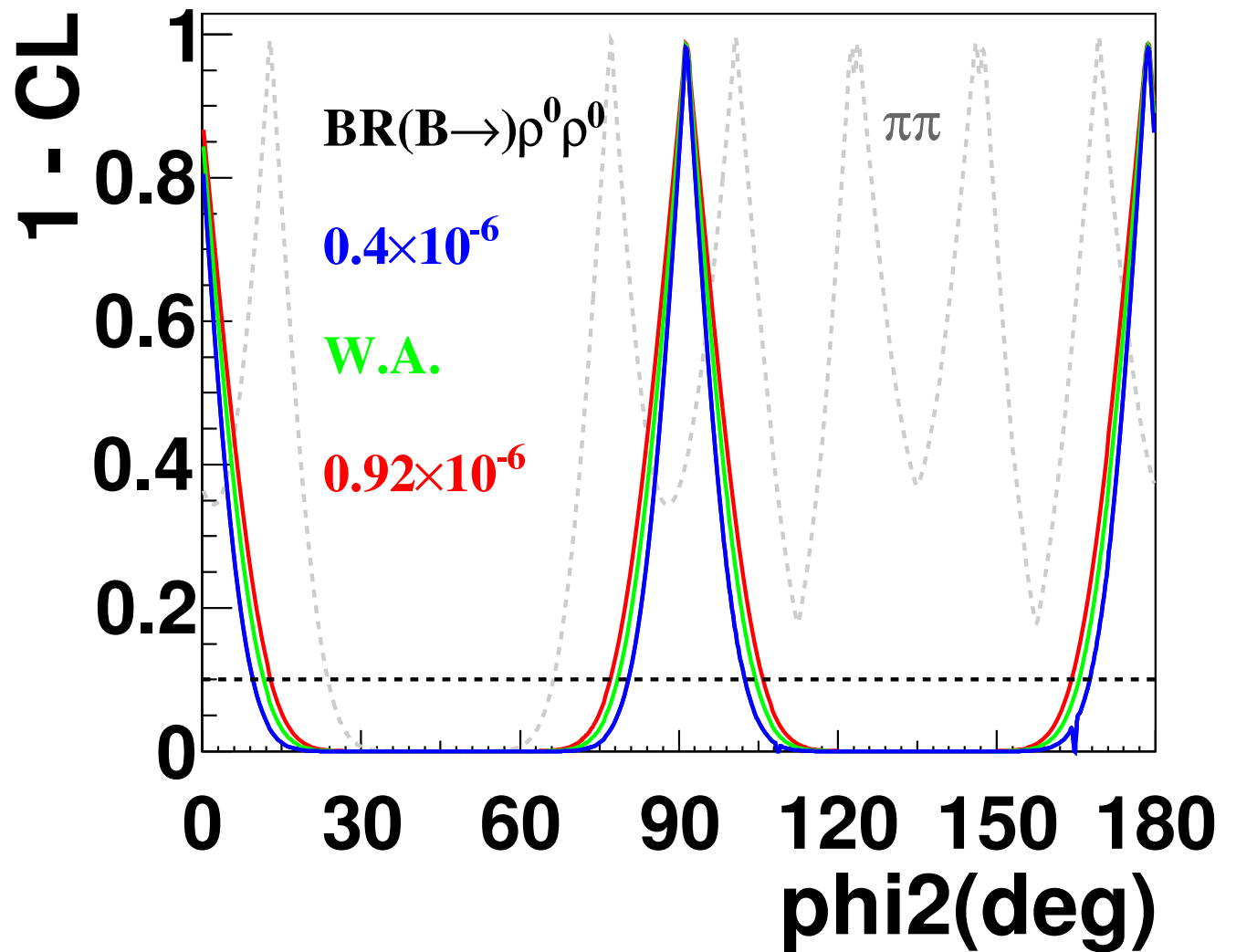
# Impact on $CKM$ Angle $\phi_2$

- variation of  
 $BR(B^0 \rightarrow \rho^0 \rho^0)$   
in isospin analysis

$$\text{W.A.} = (0.73 \pm 0.28) \times 10^{-6}$$

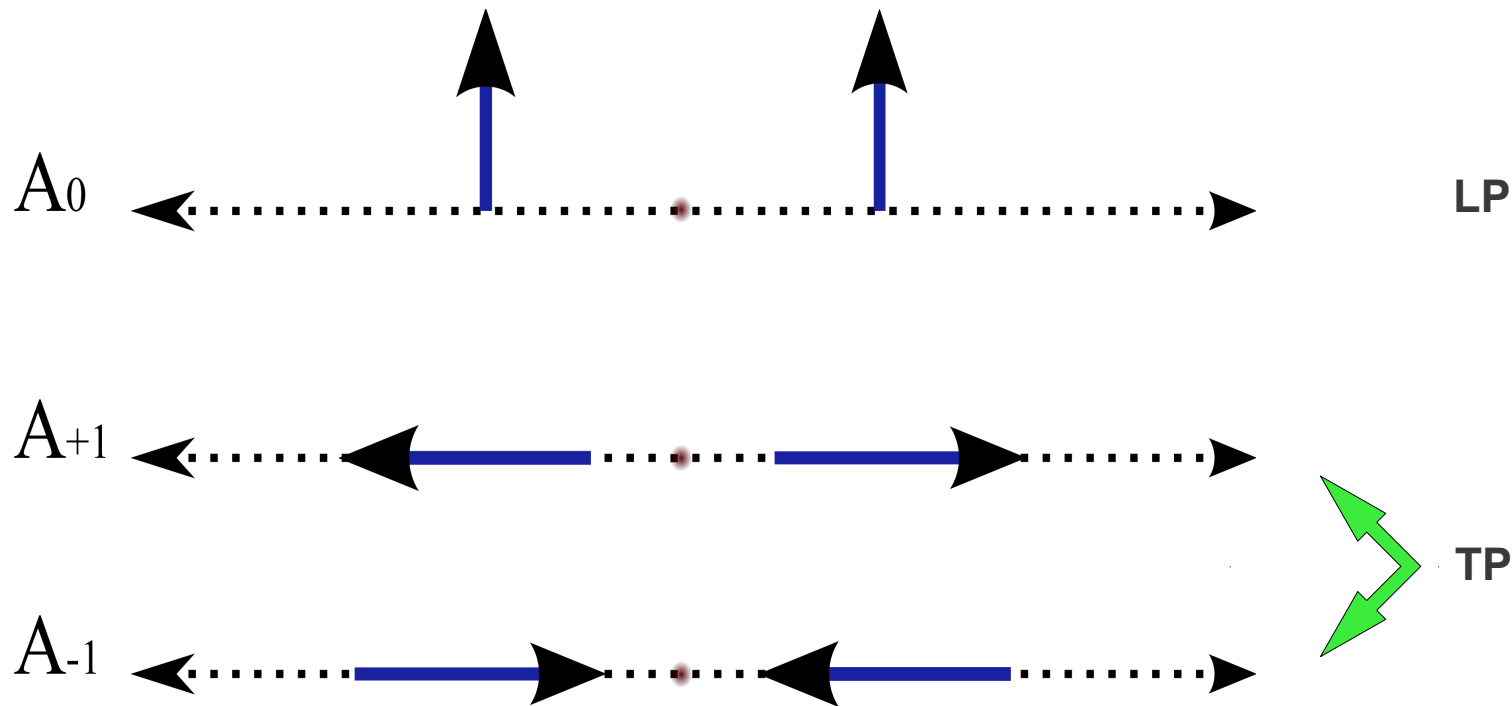
prev. Belle

Babar



# $B \rightarrow VV$

3 different polarization amplitudes contribute  $\rightarrow$  important for  $CP$  measurements



- only longitudinal(LP;  $A_0$ ) is a pure  $CP$  eigenstate (even)
- transversal(TP) states are a mixture of  $CP$  even and odd states

SM: LP dominant,  $f_L \sim 1 - (m_V^2/m_B^2) \sim 1$  (fraction of LP:  $f_L = \frac{|A_0|^2}{\sum |A_i|^2}$ )

# Break

**Aiming at a better understanding of the  $CKM$  angle  $\phi_2$**

$1^{st}$ : extraction of signal from all events = signal + backgrounds  $\leftrightarrow$  **branching fraction**

– rare  $B$  decays are extremely background dominated (esp. at a  $e^+e^-$  collider)

→ multivariate analysis

$2^{nd}$ : measurement of **time and flavor dependent decay rate**  $\rightarrow \mathcal{A}_{CP}, \mathcal{S}_{CP}$

–  $b \rightarrow u$ : observable  $\mathcal{S}_{CP} \sim \sin(2\phi_2^{eff})$  **polluted by penguins**

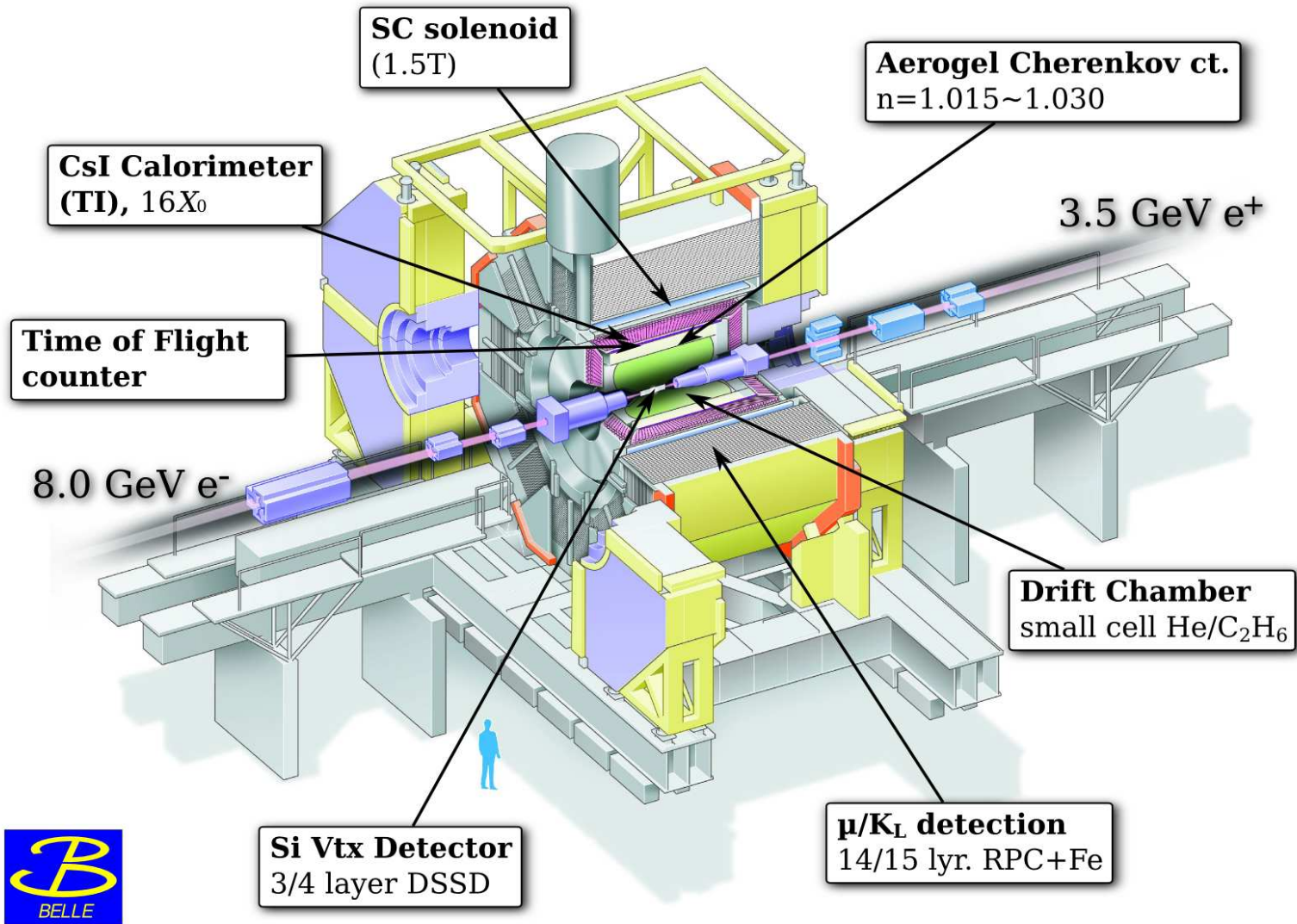
$3^{rd}$  remove pollution with **isospin analysis**

- e.g. with  $B \rightarrow \rho^+\rho^-, \rho^0\rho^0, \rho^+\rho^0$

$\Rightarrow$  several measurements of branching fractions and  $CP$  parameters needed to pin down  $\phi_2$

$1^{st}$  and  $2^{nd}$  can be performed in one step

# The Experimental Setup



- located in Japan
- asymmetric  $e^+e^-$  collider (KEKB)  
(3.5  $GeV$  on 8  $GeV$ )
- luminosity world-record  
 $\int Ldt = 1014 fb^{-1}$   
 $\sim 772 \times 10^6 B\bar{B}$  pairs

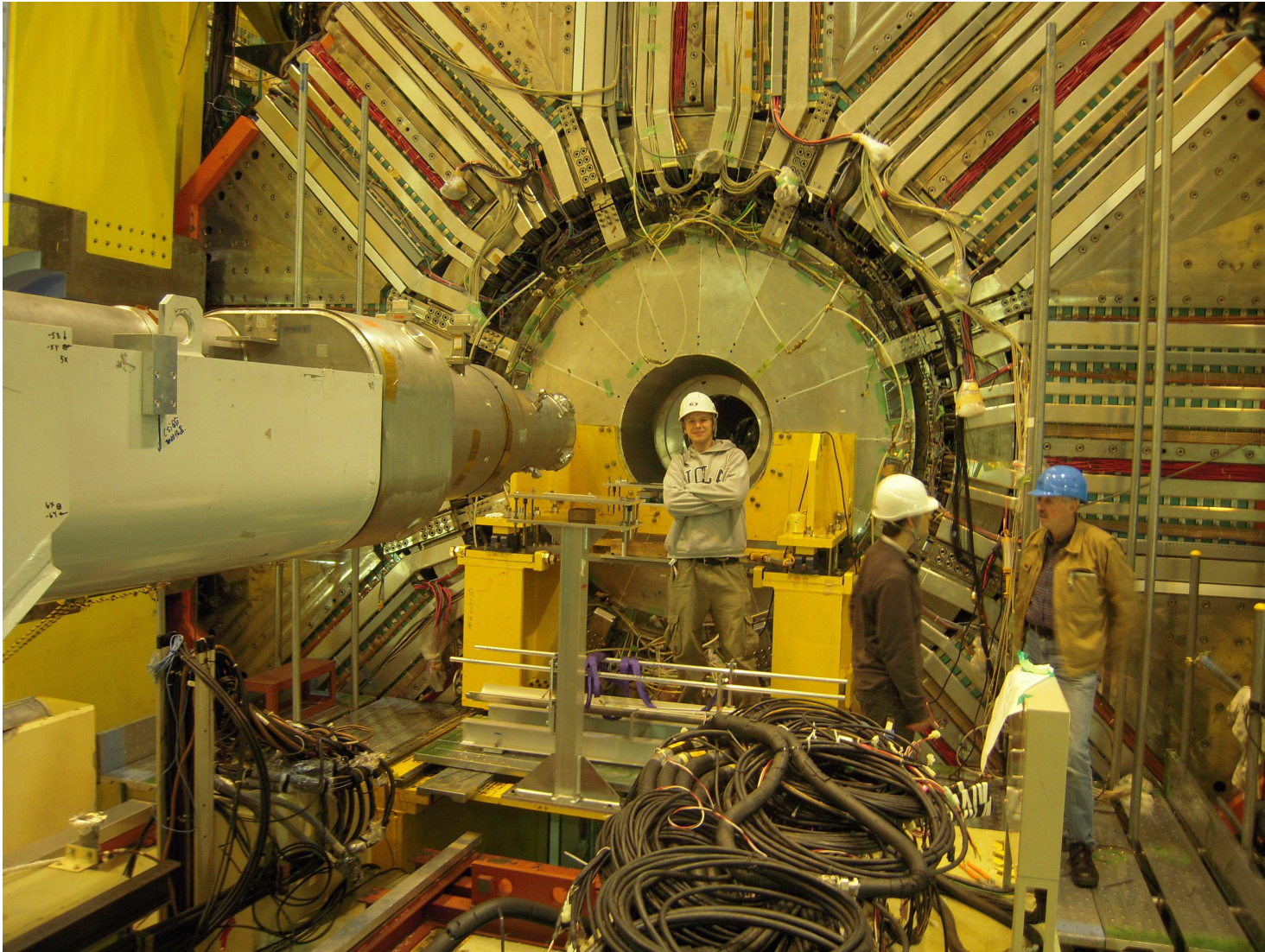
Belle Detector

- tracking
- PID



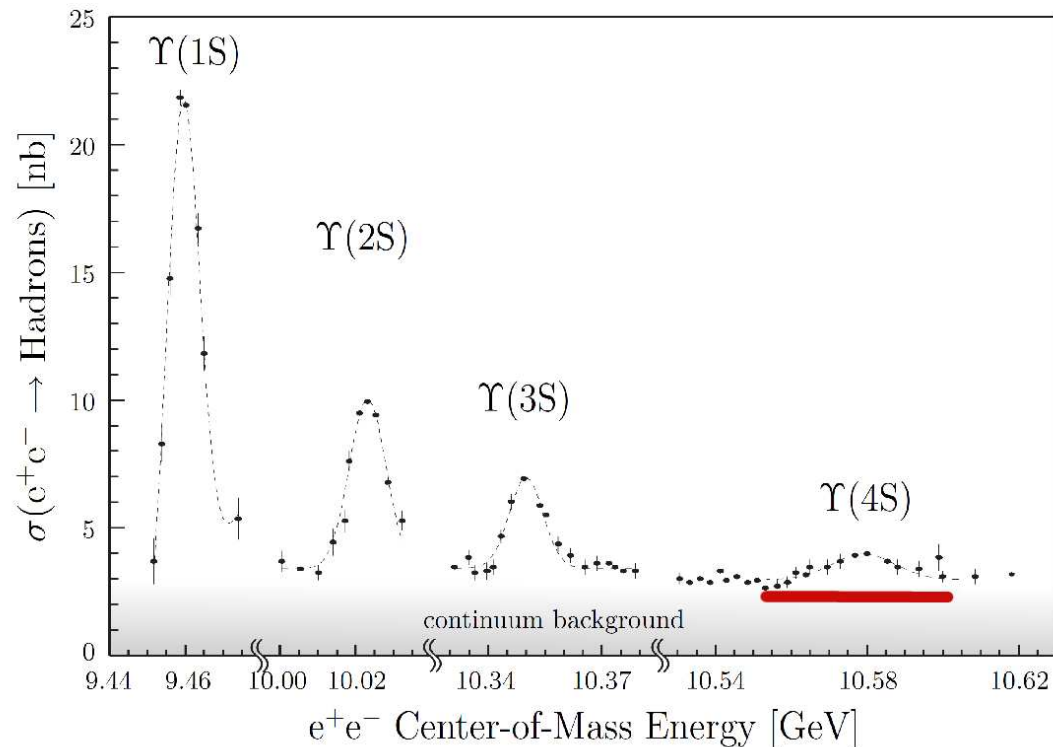


# The Belle Detector



# $CP$ Violation measurement

Where the  $B$ s come from:



$$m(\Upsilon(4S)) = 10.58 \text{ GeV}/c^2 \sim 2 \times m(B)$$

$$m(B) = 5.28 \text{ GeV}/c^2$$

- $\Upsilon$  states:  $b\bar{b}$  bound states
- $\Upsilon(4S)$  exclusively into  $B\bar{B}$  pairs
- $\Upsilon(4S)$ :  $J^{PC} = 1^{--}$
- $B$  :  $J^{PC} = 0^{--}$   
 $\rightarrow B$  pair in p-wave
- asymmetric wave function  
 $\rightarrow B$ s have opposite flavor:

**continuum:**  $e^+e^- \rightarrow q\bar{q}$

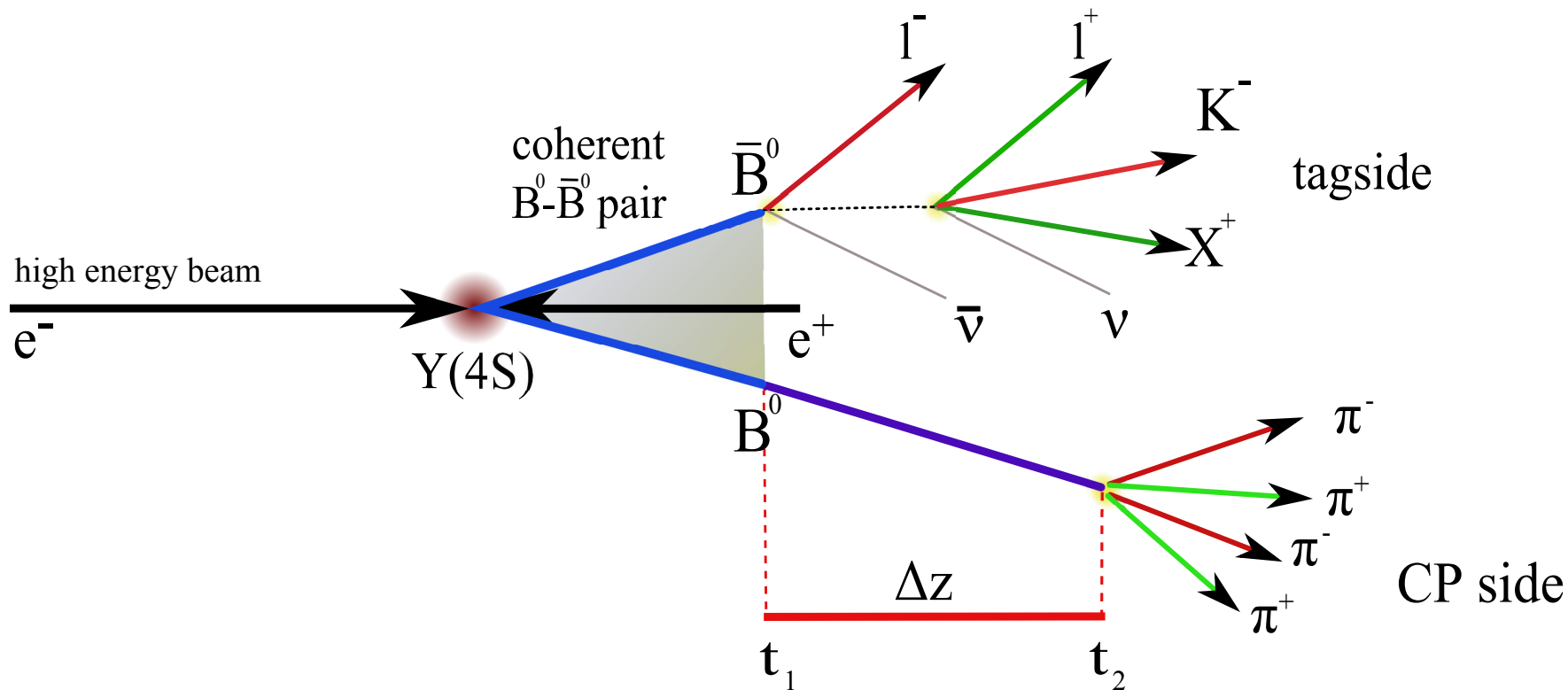
(u,d,s,c)

gives large contribution



# $CP$ Violation measurement

different decay time-dependency for  $B$  and  $\bar{B}$  decaying into a  $CP$  eigenstate, indirect  $CP$



- $\Upsilon(4S)$  resonance right on  $B\bar{B}$  production threshold ( $B\bar{B} \sim$  at rest in CMS)
- $\Upsilon(4S) \rightarrow$  entangled  $B\bar{B}$  pair  $\Rightarrow$  opposite side flavor tagging possible
- asymmetric beam energies  $\Rightarrow$  boost of the CMS  $\Rightarrow \Delta t \rightarrow \Delta z$  ( $\Delta t \sim ps, \Delta z \sim \mu m$ )

# Flavor Tagging

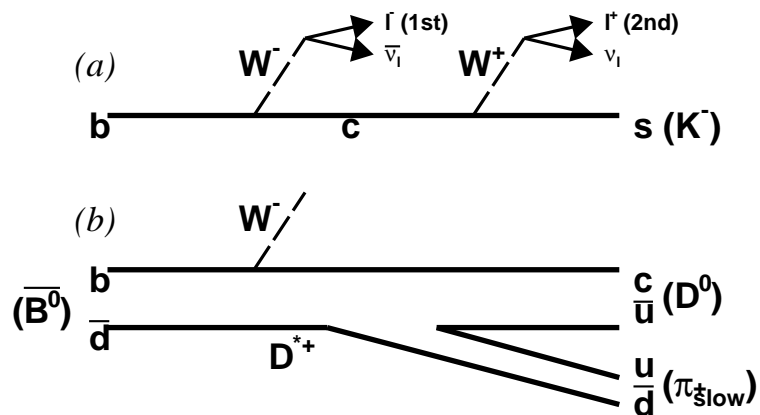
towards CPV measurement

$\Upsilon(4S) \rightarrow$  coherent  $B\bar{B}$  pair

one  $B \equiv B_{CP}$  decays into final state of interest.

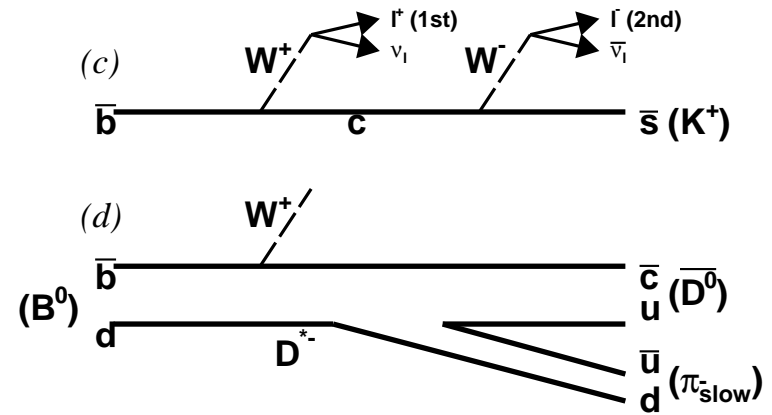
use flavor specific decays of the other  $B \equiv B_{tag}$  to determine the flavor of  $B_{CP}$ ; e.g.

$\bar{B}$  decays



VS

$B$  decays



# Reconstruction of $(B^0 \rightarrow \rho^0 \rho^0)$

$$B^0 \rightarrow \rho^0 \rho^0$$
$$\rho^0 \rightarrow \pi^+ \pi^-$$

$\Rightarrow$  4 charged  $\pi$ s in the detector

- **select  $\pi^\pm$  candidates:** PID criterias
- **reconstruct  $\rho^0$  candidates from  $\pi^+ \pi^-$  pairs**

$\rho^0(770)$ : broad resonance ( $\Gamma \sim 149 \text{ MeV}$ )

$\rightarrow m_{\pi^+ \pi^-} \in [0.52, 1.15] \text{ GeV}/c^2$

excludes  $K_S^0(0.49 \text{ GeV})$

- **reconstruct  $B^0$  candidates from  $\rho^0 \rho^0$  pairs**
- charm and strange vetos (due to combinatorics)  $\rightarrow$  removes peaking BKG

- vertexing ( $\Delta z$ )
- flavor tagging ( $B$  or  $\bar{B}$ )
- select best  $B^0$  candidate ( $M_{bc}$  closest to  $B$  mass)

$$M_{bc} \equiv \sqrt{E_{beam}^2 - \vec{p}_{B_{rec}}^2}$$

- continuum identification
- randomize events to remove asymmetry due to ordering in the reconstruction

$\Rightarrow$  end up with a  $B$  candidate

being a potential mother of two  $\rho^0$ s

also from background!!

# Measurement of $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$

Extraction of  $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$  and  $f_L$

6D extended unbinned likelihood fit with the variables

$\Delta E$ ,  $2 \times m_{\pi^+ \pi^-}$ ,  $\mathcal{F}$ ,  $2 \times \cos \theta_{\text{Hel}}$

$$\Delta E \equiv E_{B_{rec}} - E_{beam}$$

The model consists of **17 components** which are:

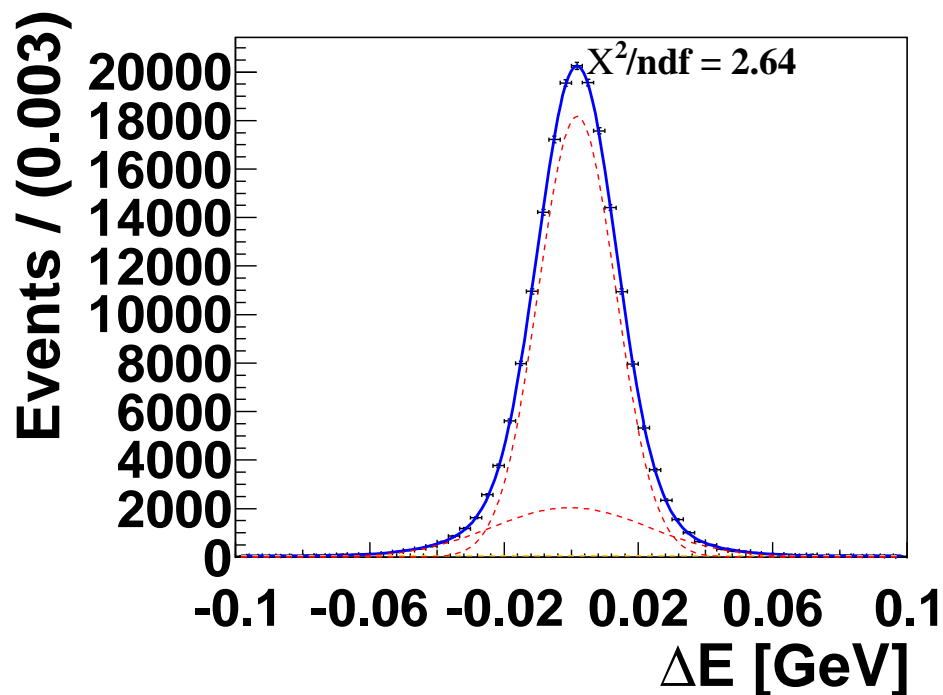
- |   |  |
|---|--|
|   | modeled using  |
| – $2 \times$ signal ( $L$ pol, $T$ pol);  | MC   |
| – $2 \times$ misreconstructed signal ( $L$ pol, $T$ pol);   | MC   |
| – continuum ( $e^+ e^- \rightarrow q\bar{q}$ );   | data taken at $\sqrt{s} = 10.50 \text{ GeV} < m(\Upsilon(4S))$ |
| – $4 \times B\bar{B}$ : charm and charmless $B^0(B^\pm)$ decays;  | MC   |
| – $8 \times$ peaking BKG ( $4\pi$ s finalstates);   | MC   |
| $\pi^+ \pi^- \pi^+ \pi^-$ , $a_1^\pm \pi^\mp$ , $a_2^\pm \pi^\mp$ , $b_1^\pm \pi^\mp$ , $f_0 f_0$ , $f_0 \pi^+ \pi^-$ , $\rho^0 \pi^+ \pi^-$ , $f_0 \rho^0$ . | <b>BR known</b>  |

# Model for $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$

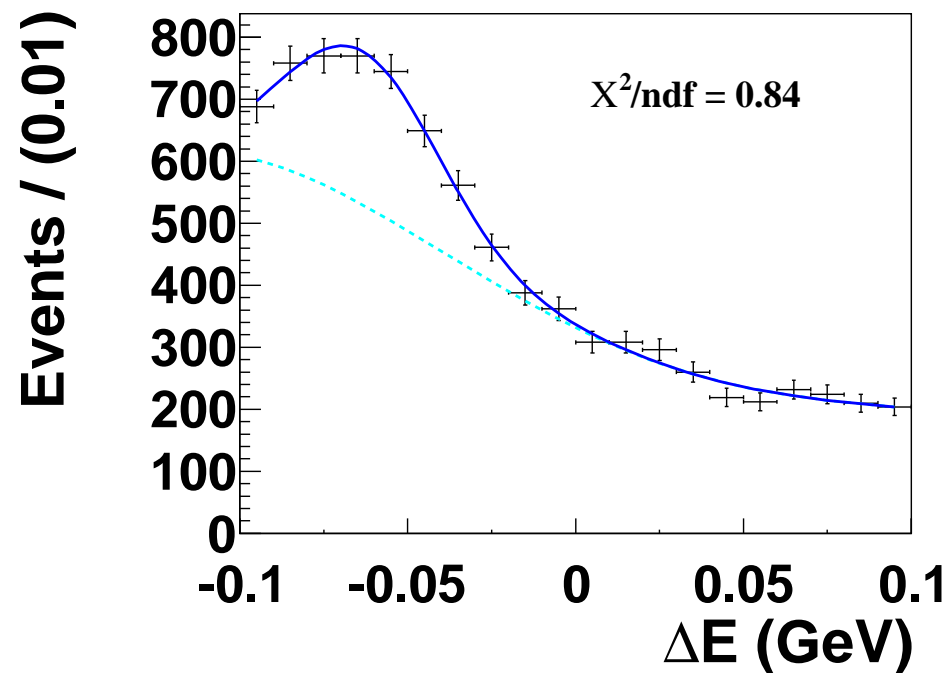
$$\Delta E \equiv E_{B_{rec}} - E_{beam}$$

- signal MC( $L$  pol)

- neutral charm decays



$\mathcal{PDF}(\Delta E) = 2 \times$  bifurcated gaussian

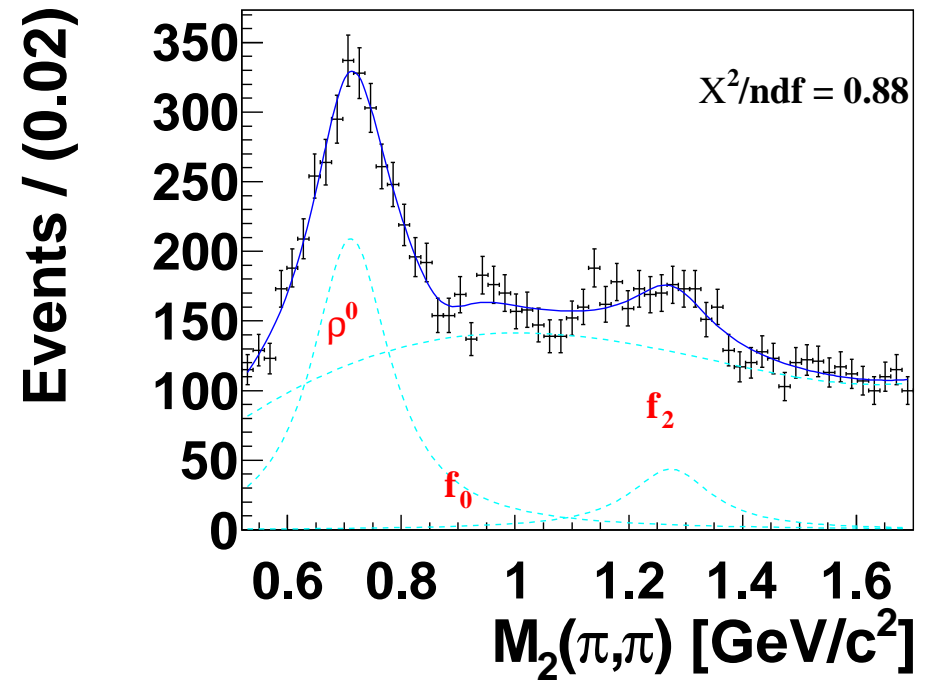
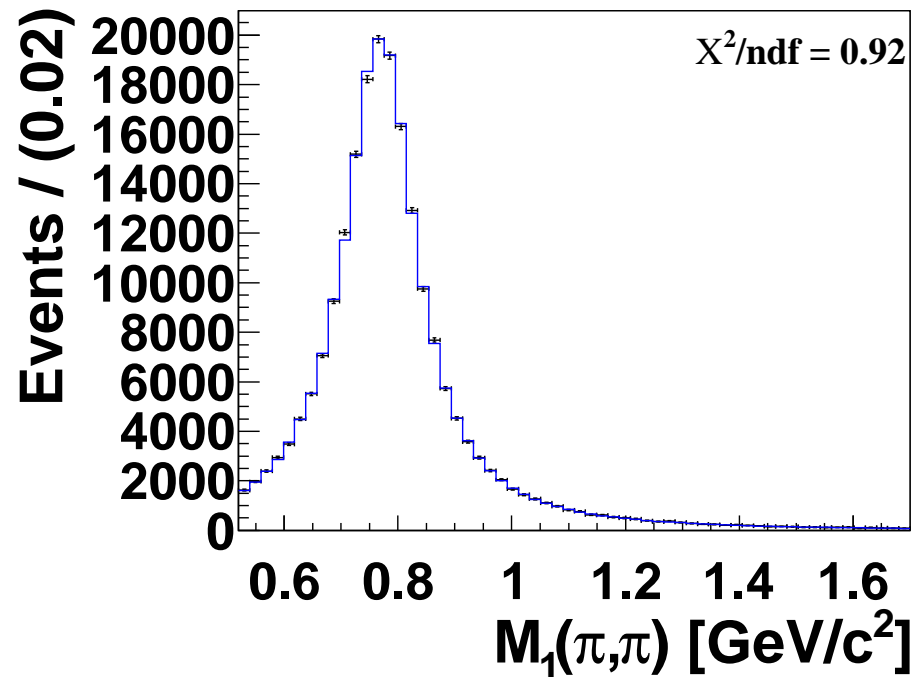


$\mathcal{PDF}(\Delta E) = \text{gaussian} + \sum_{i=1}^8 \text{chebychev}_i$

# Model for $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$

- signal MC( $L$  pol)

- neutral charmless decays



$$\mathcal{PDF}(m_{\pi^+\pi^-}) = \epsilon_{rec}(m_{\pi^+\pi^-}) \times \text{Breit-Wigner}$$

$$\mathcal{PDF}(m_{\pi^+\pi^-}) = 2 \times \text{Breit-Wigner} + \text{gaussian} + \sum_{i=1}^4 \text{chebychev}_i$$

# Helicity

- e.g. for  $B \rightarrow \rho^0 \rho^0$

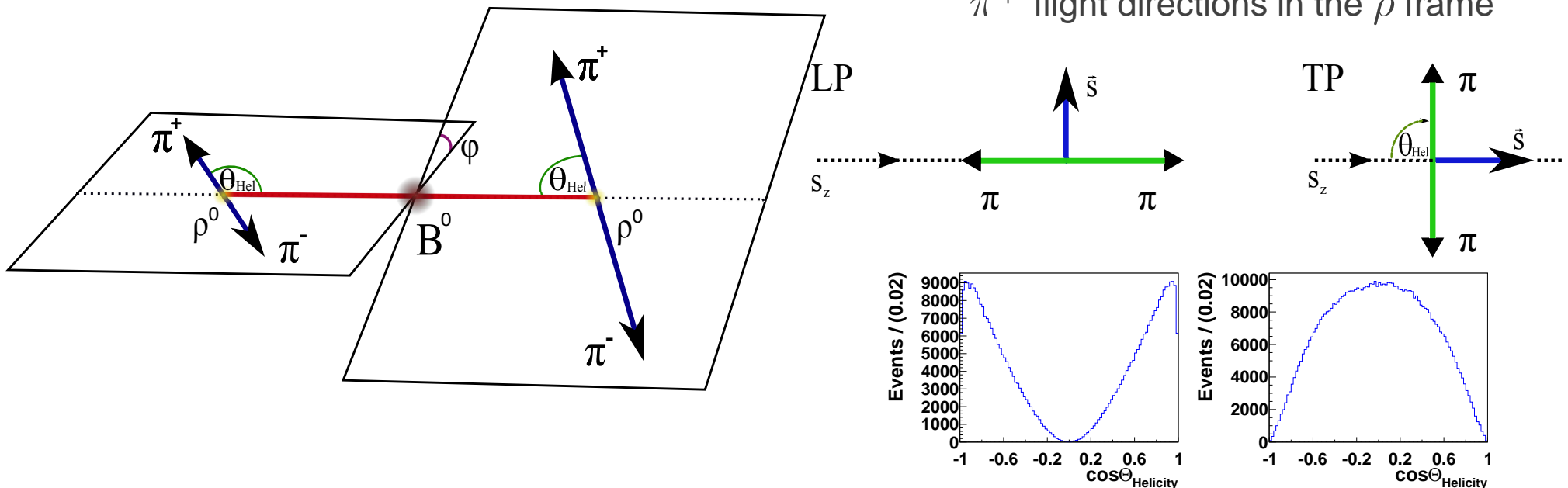
$$J^{CP}: \rho^0 = 1^{--} ; \pi^\pm = 0^-$$

$$\rho^0 \rightarrow \pi^+ \pi^-$$

2 different polarizations, longitudinal ( $L$  pol,  $CP$  even) and transversal ( $T$  pol,  $CP$  even & odd)

$f_L$ : fraction of  $L$  pol, through helicity analysis (SM:  $L$  pol dominant)

$\theta_{Hel}$ : angle between the  $B^0$  and the  $\pi^+$  flight directions in the  $\rho$  frame

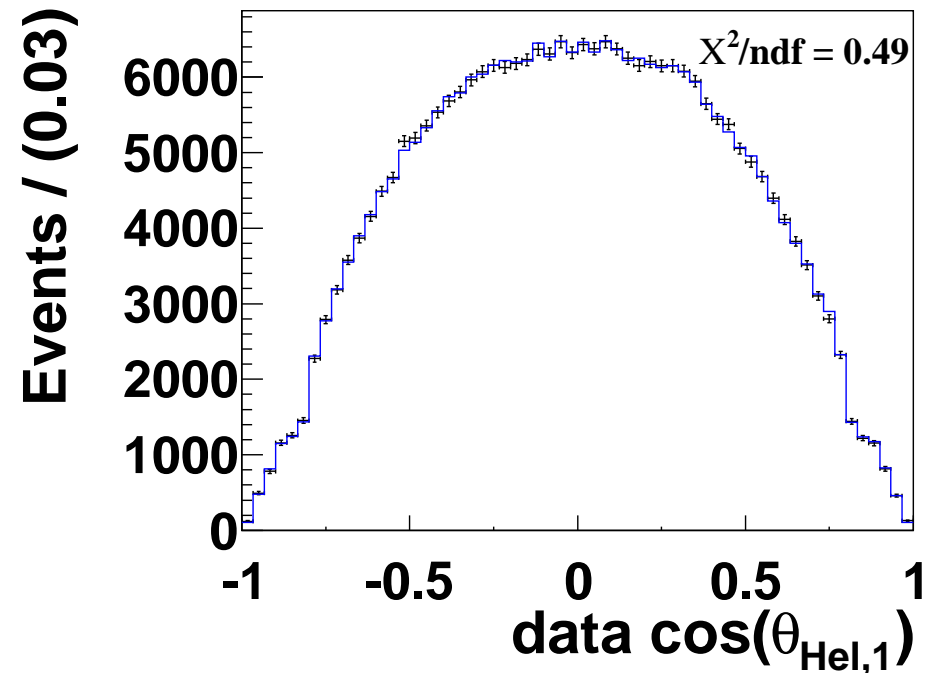
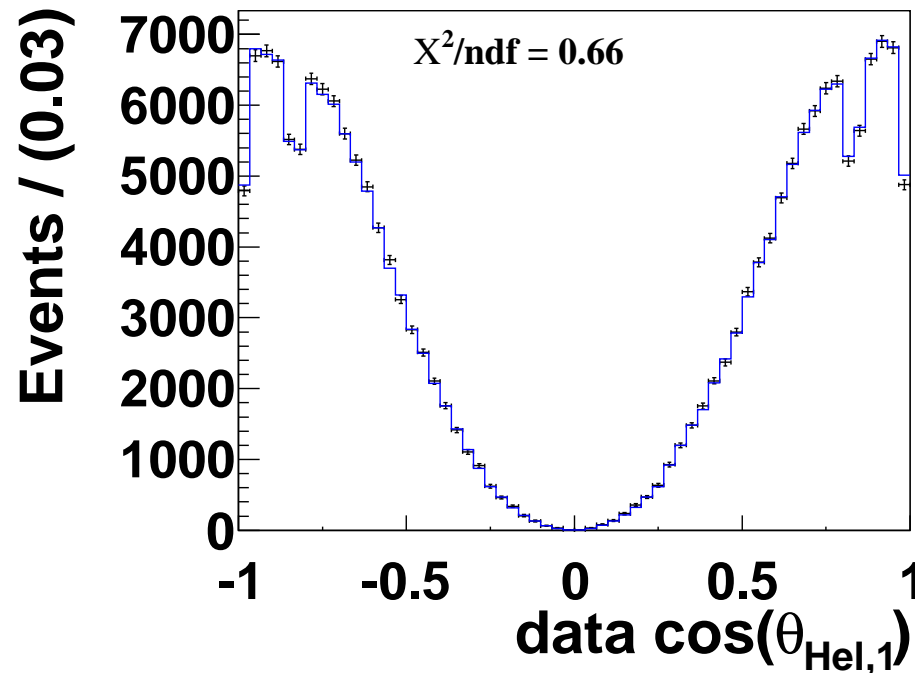


# Model for $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$

Helicity: weighted with reconstruction efficiency histogram

● signal MC( $L$  pol)

● signal MC( $T$  pol)



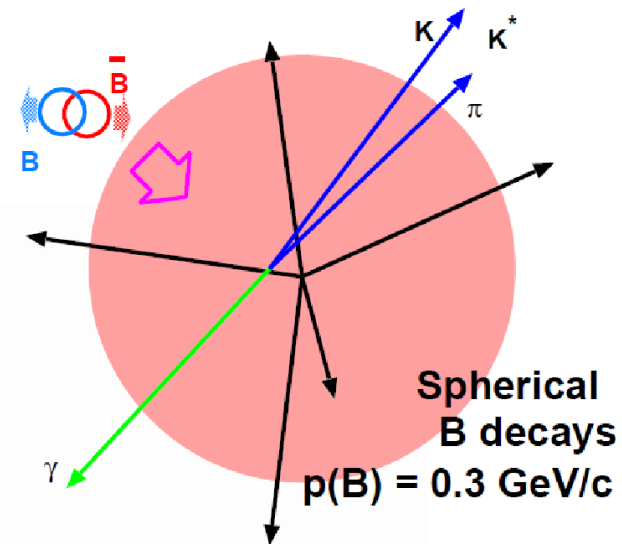
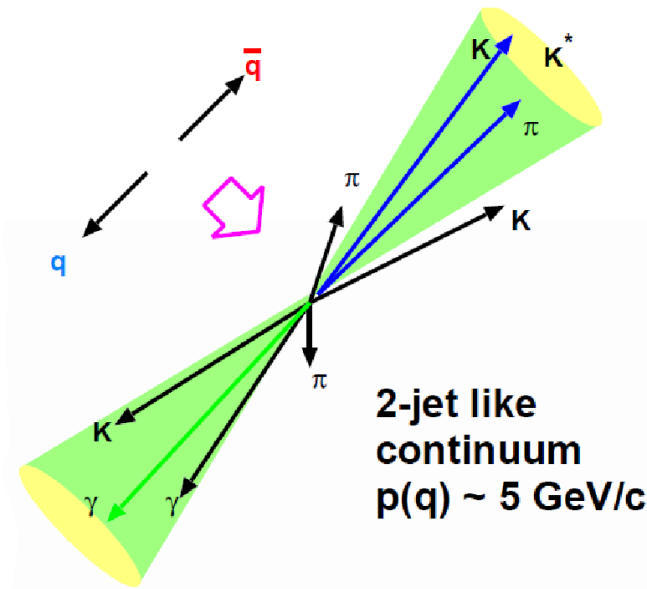
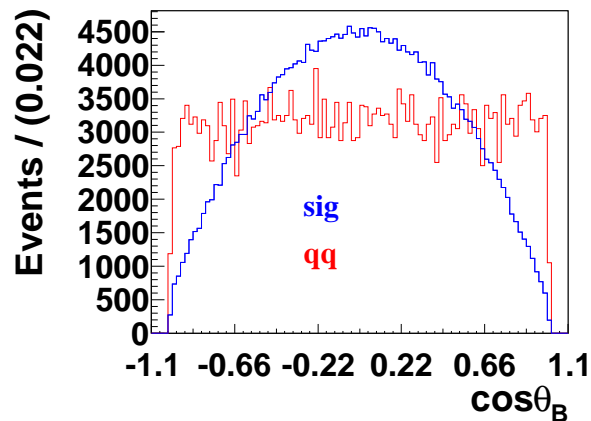
$$\frac{1}{\Gamma} \frac{d^2\Gamma}{d \cos \theta_{\text{Hel}}^1 d \cos \theta_{\text{Hel}}^2} = \frac{9}{4} \left( f_L \cos^2 \theta_{\text{Hel}}^1 \cos^2 \theta_{\text{Hel}}^2 + \frac{1}{4} (1 - f_L) \sin^2 \theta_{\text{Hel}}^1 \sin^2 \theta_{\text{Hel}}^2 \right)$$



# Continuum Identification

$e^+e^- \rightarrow q\bar{q}$ , ( $q = u, d, s, c$ ) gives biggest contribution ( $N_{q\bar{q}}/N_{sig} \sim 1000$ )

- combined eventshape variables using fisher discriminant  $\rightarrow \mathcal{F}$
- $\cos(\theta_B)$  ( $B$  flight direction)

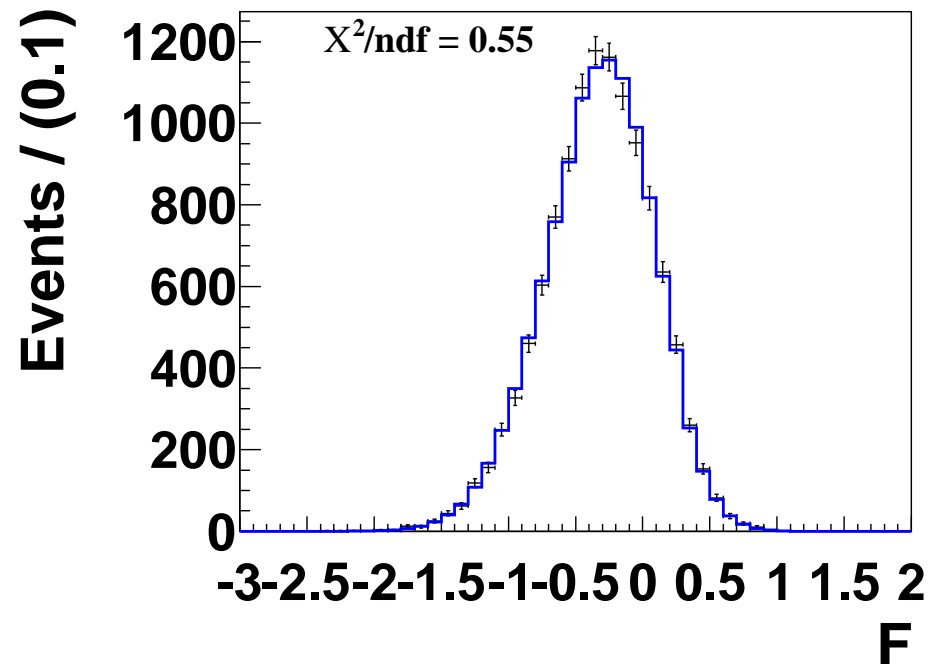
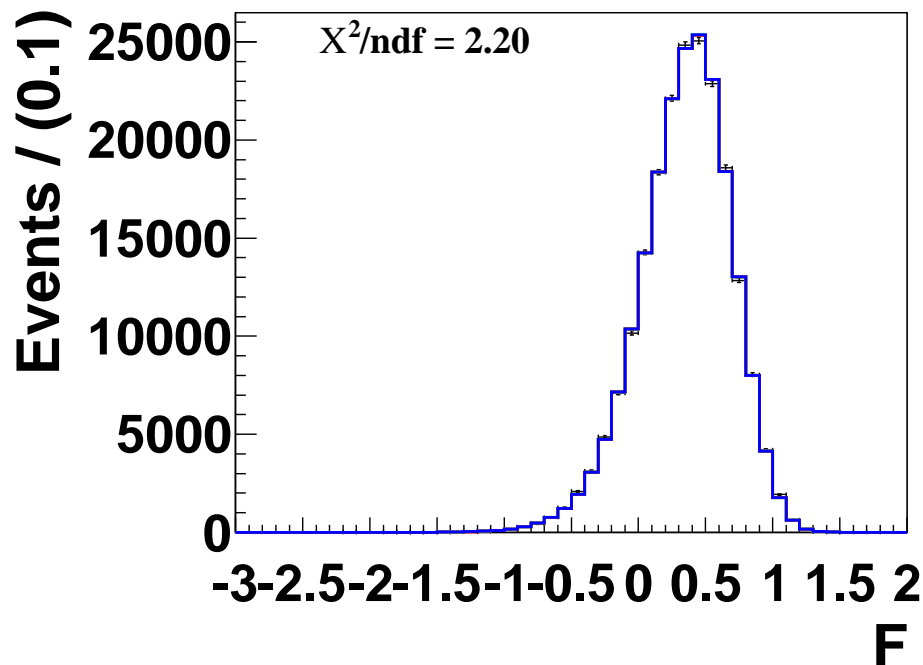


- fox-wolfram moments:  $H_l = \sum_{i,j} \frac{|\vec{p}_i||\vec{p}_j|}{s} P_l(\cos\phi_{ij})$  with legendre poly.  $P_l$
- thrust, sphericity, ...

# Model for $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$

$F$  consists of eventshape variables:  $B\bar{B} \rightarrow$  spherical,  $q\bar{q} \rightarrow$  2 jet like

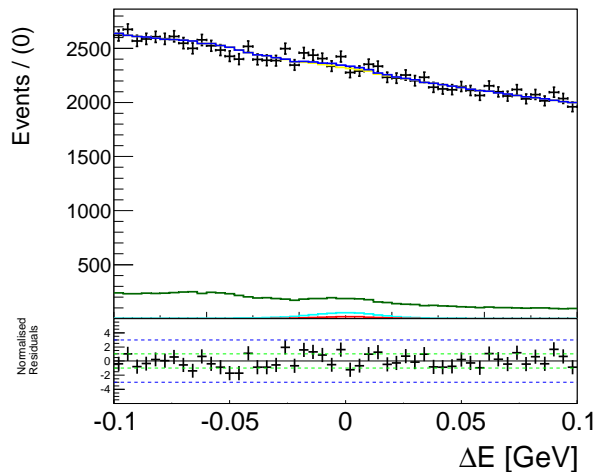
- signal MC( $L$  pol)
- continuum



$\mathcal{PDF} =$  double bifurcated gaussian

# Result: $B^0 \rightarrow \rho^0 \rho^0$

Full Projection

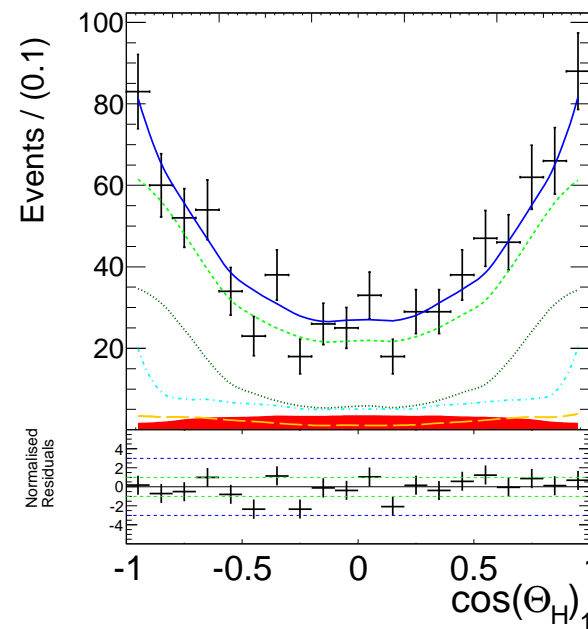
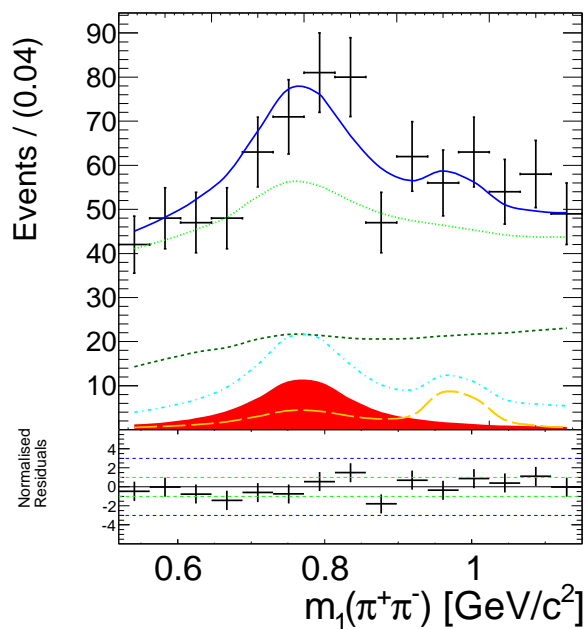
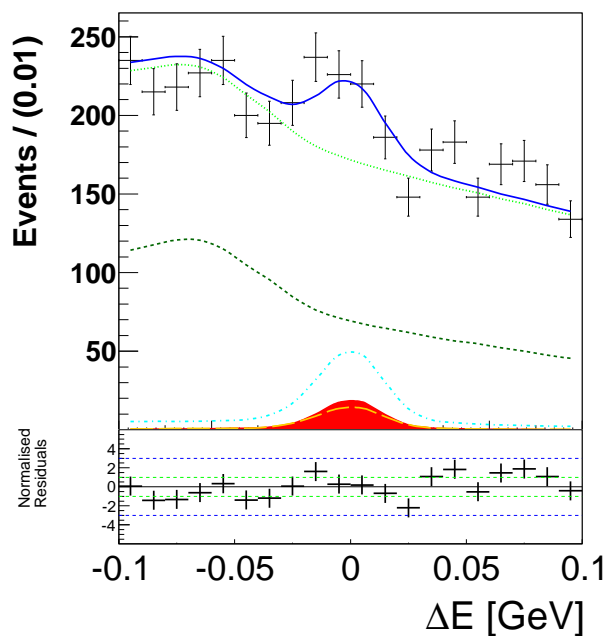


PRELIMINARY

*New results, arXiv:1212.4015*

Signal enhanced projections

$B^0 \rightarrow \rho^0 \rho^0$ ,  $B^0 \rightarrow f_0 \rho^0$ ,  $4\pi$  final states,  
 $B\bar{B}$  bkg, total non-peaking bkg, total



# Result: $B^0 \rightarrow \rho^0 \rho^0$

- 6D fitter:

**PRELIMINARY**

*New results, arXiv:1212.4015*

$\Delta E, m_{\pi^+\pi^-}, m_{\pi^+\pi^-}, \cos \theta_{\text{Hel}}, \cos \theta_{\text{Hel}}, \mathcal{F}_{s/b}$  ( $m_{\pi^+\pi^-}$  is invariant  $\rho^0$  mass)

mode	branching fraction $\times 10^{-6}$	events	significance
$\mathcal{B}(B^0 \rightarrow \rho^0 \rho^0)$	$< 1.5$ $(1.02 \pm 0.30 \pm 0.22)$	$166 \pm 49$	U.L. $\sim 3\sigma$
$f_L = 0.21^{+0.18}_{-0.22} \pm 0.11$			
$\mathcal{B}(B^0 \rightarrow f_0 \rho^0) \times (f_0 \rightarrow \pi^+ \pi^-)$	$(0.86 \pm 0.27 \pm 0.15)$	$149 \pm 47$	$3.0\sigma$ 1st evidence
$\mathcal{B}(B^0 \rightarrow f_0 f_0) \times (f_0 \rightarrow \pi^+ \pi^-)^2$	$< 0.2$	$-5 \pm 17$	U.L.
$\mathcal{B}(B^0 \rightarrow \rho^0 \pi^+ \pi^-)$	$< 12.2$	$33 \pm 82$	U.L.
$\mathcal{B}(B^0 \rightarrow f_0 \pi^+ \pi^-) \times (f_0 \rightarrow \pi^+ \pi^-)$	$< 3.1$	$-27 \pm 43$	U.L.
$\mathcal{B}(B^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-)$	$< 11.7$	$-25 \pm 54$	U.L.

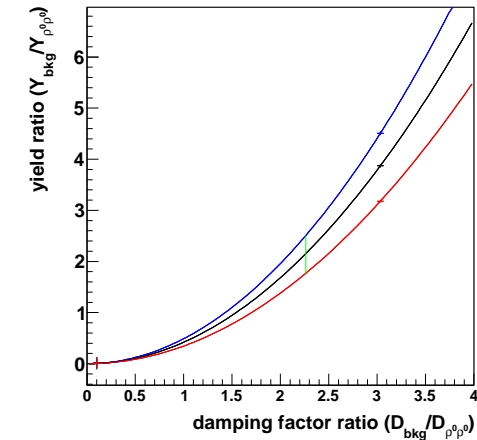
- $B^0 \rightarrow \rho^0 \rho^0$  suffers from large systematic uncertainty through interference with  $B \rightarrow a_1^\pm \pi^\mp$
- previous Belle result:  $-\mathcal{B}(B^0 \rightarrow \rho^0 \rho^0)_{\text{prev.}} < 1.0 \times 10^{-6}$ , assuming  $f_L = 1$

$$-\mathcal{B}(B^0 \rightarrow f_0 \rho^0)_{\text{prev.}} < 0.3 \times 10^{-6} \quad (657 \times 10^6 B\bar{B} \text{ pairs})$$

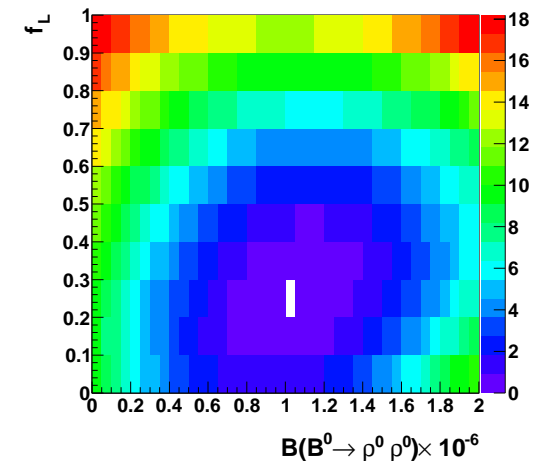
# Systematic Uncertainties

Category	$\delta\mathcal{B}(B^0 \rightarrow \rho^0 \rho^0)$ (%)	$\delta f_L$
$N(B\bar{B})$	1.4	—
Tracking	1.4	—
Particle identification	2.5	—
Mis-reconstruction fraction	1.3	$< 0.001$
$\rho^0$ shape	0.2	$< 0.001$
Model shape	5.1	0.08
Histogram shape	5.2	0.03
$\mathcal{B}(B^0 \rightarrow a_1\pi)$	0.4	0.03
$\mathcal{B}(B^0 \rightarrow b_1\pi)$	$< 0.1$	$< 0.001$
$\mathcal{B}(B^0 \rightarrow a_2\pi)$	$< 0.1$	$< 0.001$
Fit bias	1.9	0.03
Interference	19.2	0.03
$\rho^0 \pi\pi$ helicity	6.3	0.05
Total	22.0	0.11

interference with  $a_1\pi$



likelihood scan incl. syst.



# $\phi_2$ from $B \rightarrow \rho\rho$ Decays

## isospin analysis

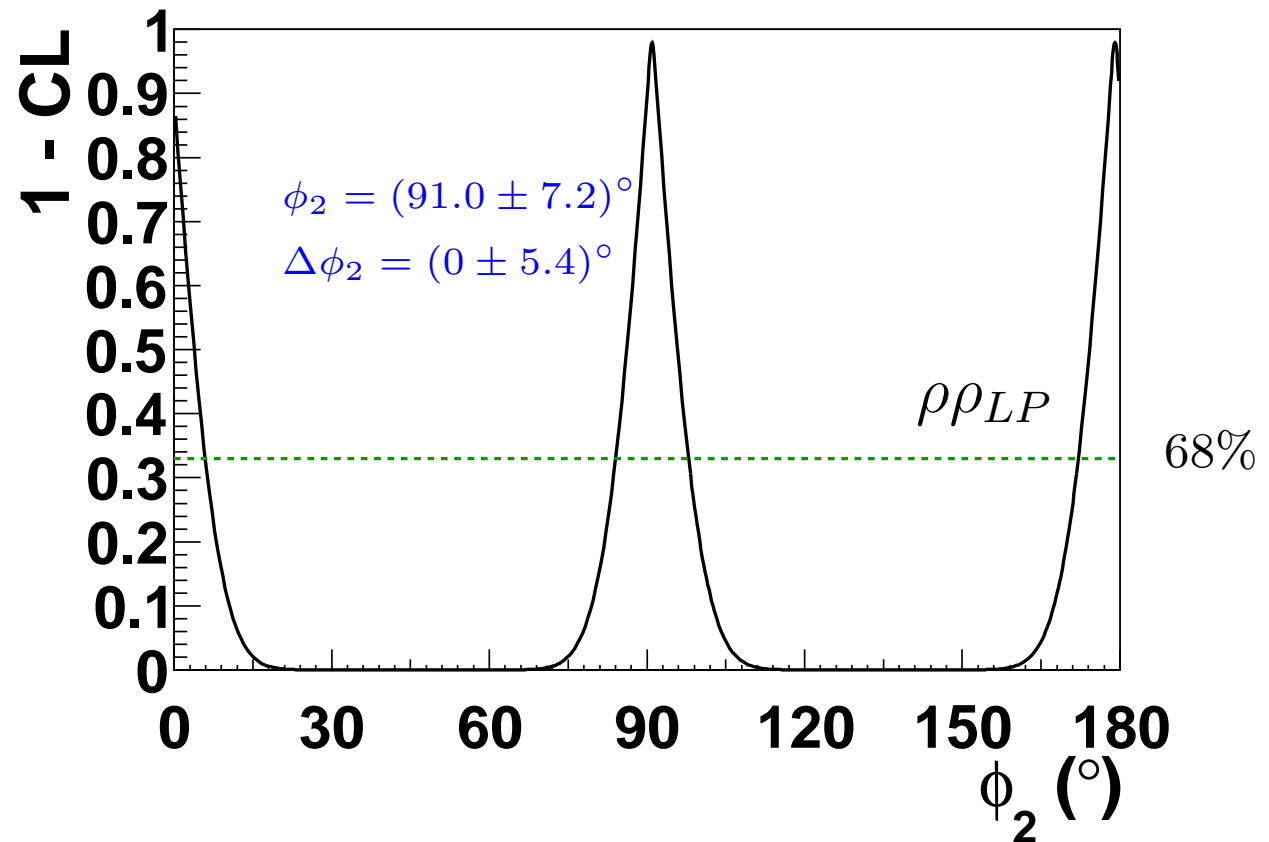
inputs:

- my result on

$$B^0 \rightarrow \rho^0 \rho^0|_{LP}$$

$$\mathcal{B}(B^0 \rightarrow \rho^0 \rho^0)|_{LP} = (0.21 \pm 0.36) \times 10^{-6}$$

- and world averages else



same scan with the world average

$$\mathcal{B}(B^0 \rightarrow \rho^0 \rho^0) = (0.74 \pm 0.28) \times 10^{-6} \rightarrow \phi_2 = (90.9 \pm 8.4)^\circ$$

# Summary & Outlook

- presented measurement of  $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$  (arXiv:1212.4015)

preliminary results (presented at CKM 2012)

$$\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0) = (1.02 \pm 0.30(\text{stat.}) \pm 0.22(\text{syst.})) \times 10^{-6}$$

$$f_L = 0.21_{-0.22}^{+0.18}(\text{stat.}) \pm 0.11(\text{syst.})$$

- and used it in isospin analysis

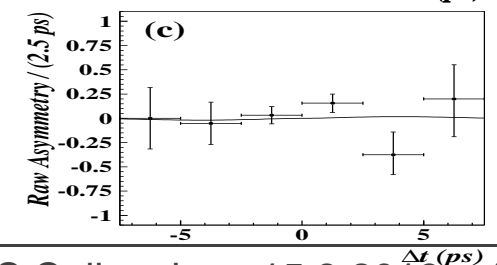
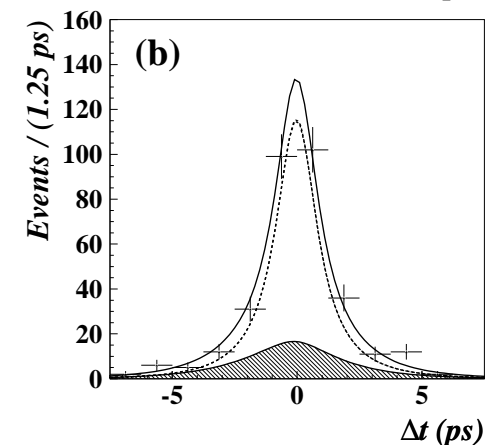
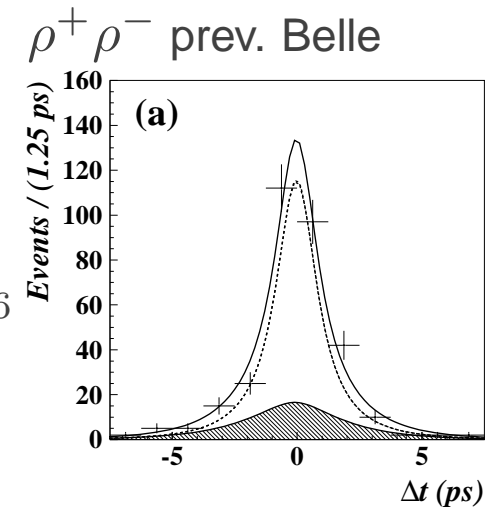
$$\phi_2 = (91.0 \pm 7.2)^\circ$$

- currently working on the final update of  $B^0 \rightarrow \rho^+ \rho^-$

→ measurement of branching fraction, polarization

and  $CP$  asymmetries.

- most precise measurement of  $\phi_2$  in the  $B \rightarrow \rho\rho$  system ?



# BACKUP



# $B \rightarrow VV$

## naive SM predictions

amplitude ratios:

$$A_0 : A_+ : A_- = 1 : \frac{m_V}{m_B} : \frac{m_V^2}{m_B^2}$$

fraction of longitudinal polarized states  $f_L$ :

$$f_L = \frac{|A_0|^2}{|A_0|^2 + |A_+|^2 + |A_-|^2} \sim 1 - \frac{m_V^2}{m_B^2}$$

theoretical status:

### LP ( $A_0$ )

calculable using QCD factorization in the heavy quark limit

*Beneke, Buchalla, Neubert, Sachrajda: arXiv:hep-ph: 0104110, 9905312, 0006124*

### TP

suppressed by powers of  $(\Lambda_{QCD}/m_B)$   
amplitudes do NOT factorize  $\Rightarrow$  hard to calculate (divergences)

*M. Beneke, J. Rohrer and D. Yang : arXiv:hep-ph: 0612290*

# $B \rightarrow VV$

## measurements

tree dominated: ( $\rho, \omega, \dots$ )

$$f_L \sim 1 \quad \checkmark$$

penguin dominated: ( $K^*, \phi, \dots$ )

$$f_L \sim 0.5 \quad ?$$

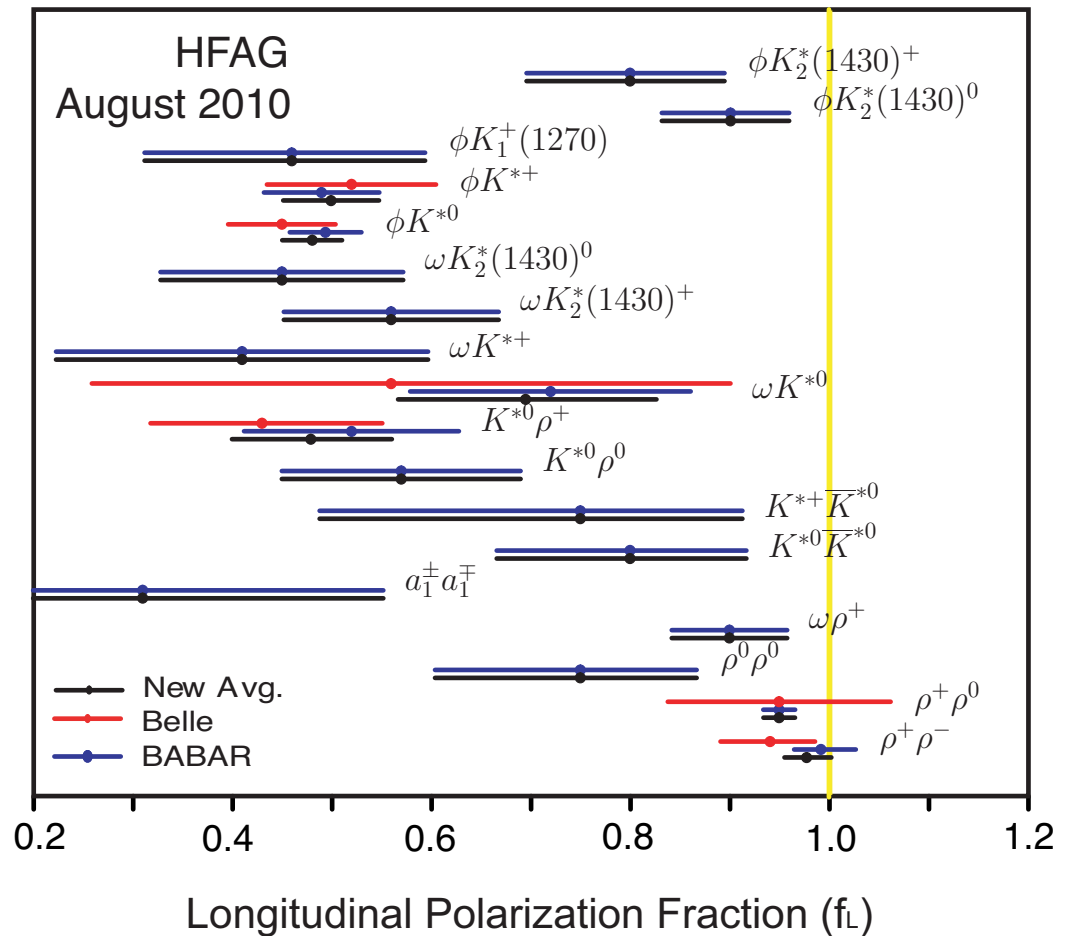
e.g.  $K^*$  naive expectation:

$$f_L \sim 1 - \left(\frac{m_{K^*}}{m_B}\right)^2 \sim 0.97$$

→ “**helicity puzzle**”

topic of ongoing research

## Polarizations of Charmless Decays



# Helicity

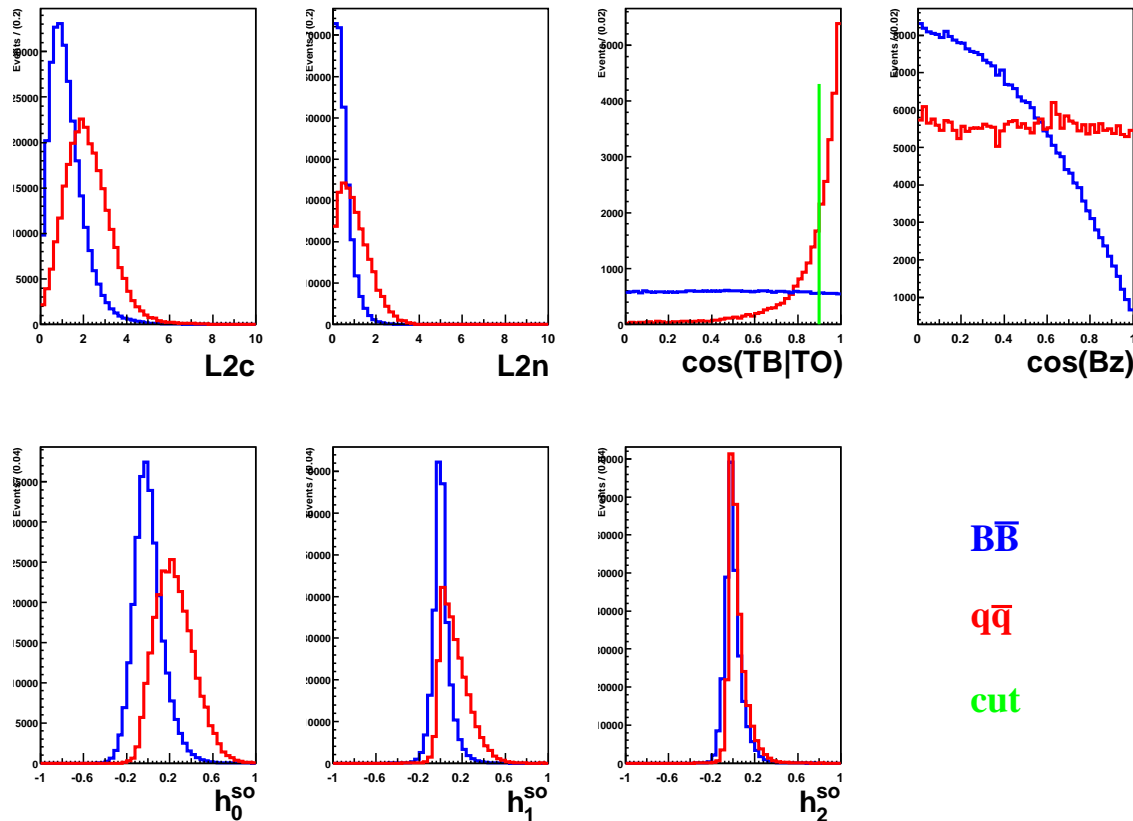
$f_L$  not only over fit to  $\cos(\Theta_H)$ .

- in fact i build models for two signal components, LP and TP.
- they only share the same shape for the  $\rho$  mass.
- slightly different  $\Delta E$  and  $\mathcal{F}$  due to different momentum distributions.
- $\cos(\Theta_H)$  gives best discrimination

$\Rightarrow$  fit a common branching ratio and obtain the yields for each polarization by fitting also  $f_L$ .

# Continuum Identification

What I use.



- momentum sum relative to thrust axis  $L_2$
- angle between the 2  $B$ s thrust axis
- $B$  flight direction
- fox wolfram moments

cut:  $\cos(TB|TO) < 0.9$

removes  $\sim 60\% qq$

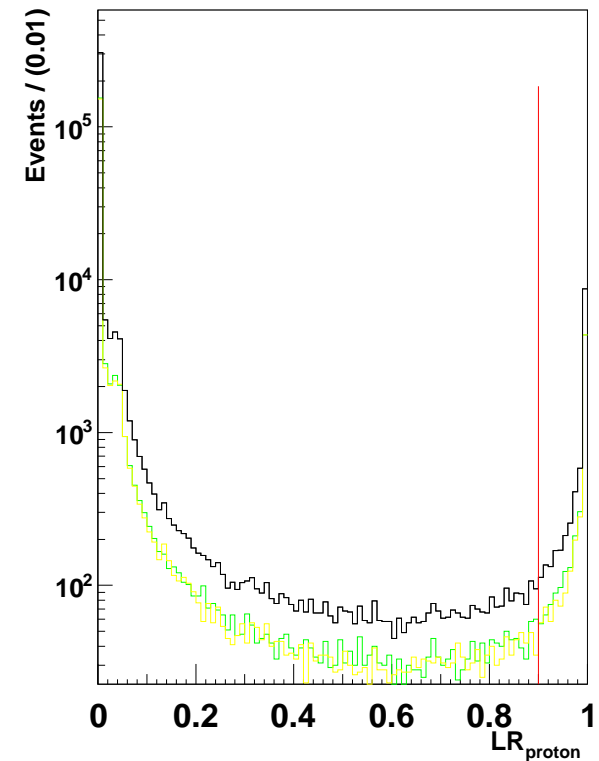
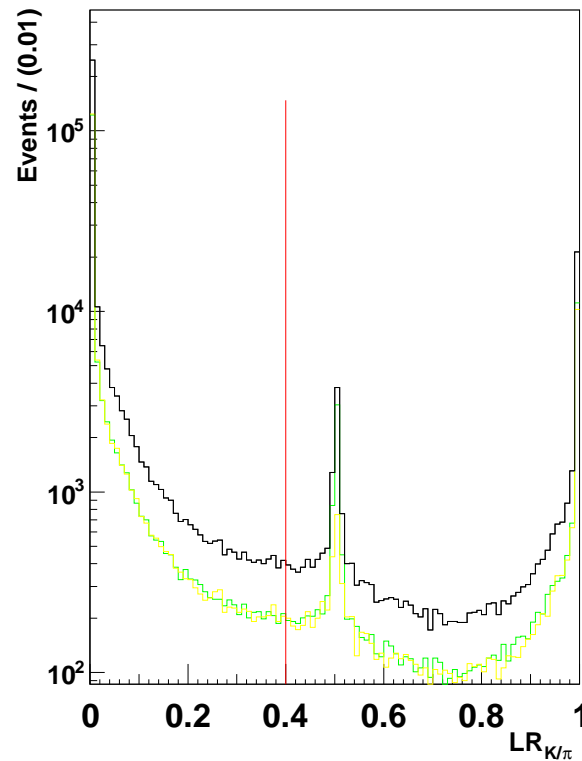
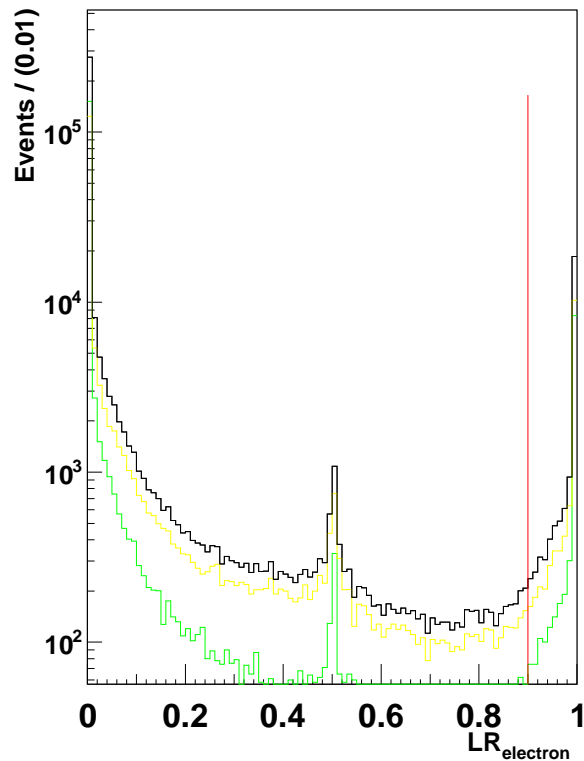
# Rec: PID Criterias

- information from different subdetectors  $\rightarrow$  likelihood ratios  $\mathcal{LR}_{i/j}$
- charged tracks from signal MC: standard set of cuts  $\rightarrow$  syst. are known

$$\mathcal{LR}_e < 0.9$$

$$\mathcal{LR}_{K/\pi} < 0.4$$

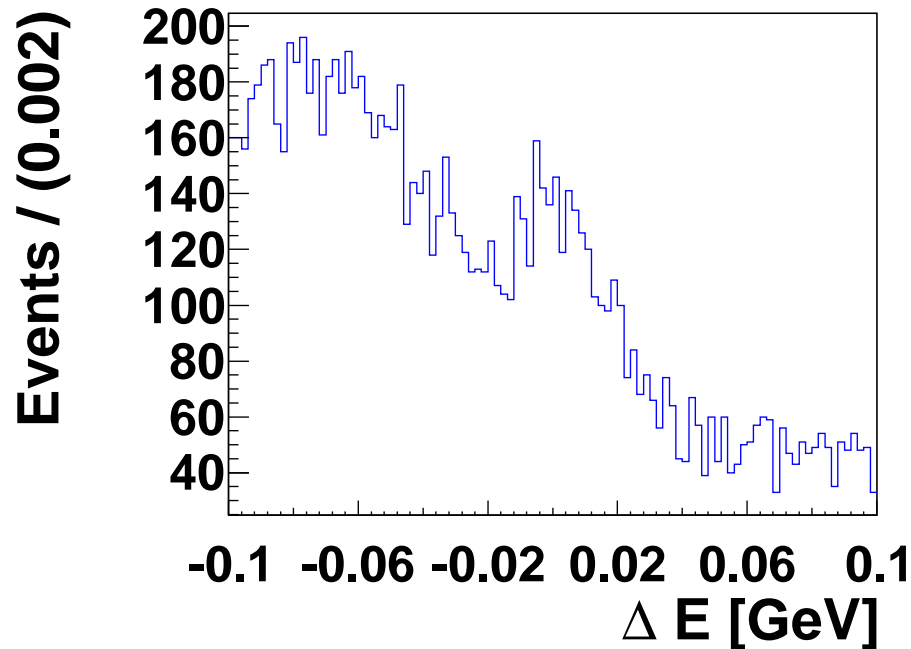
$$\mathcal{LR}_{p/\pi} < 0.9$$



- require that tracks (*somehow*) origin at the IP:  $|dr| < 0.5\text{cm}$  &  $|dz| < 5\text{cm}$

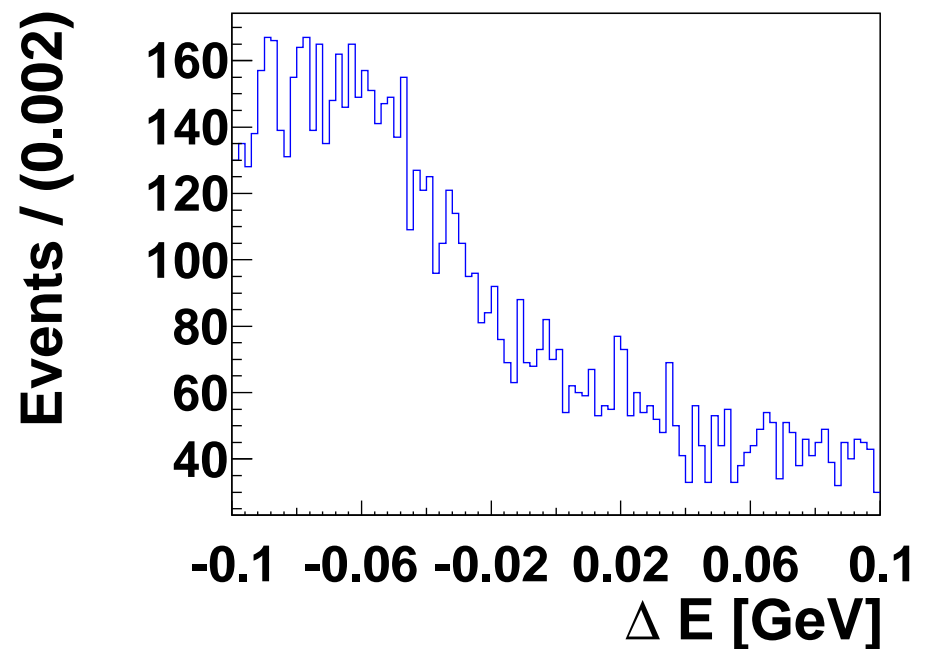
# Rec: Charm and Strange Vetos

- removes signal like features coming from background with similar final state topology, e.g.  $B^0 \rightarrow D^-(\pi^-\pi^+\pi^-\pi^+)$  or wrong PID;  $(\Delta E = E_{Brec} - E_{beam})$



before

and



after vetos

# Rec: Charm and Strange Vetos

Cuts on  $M(\pi\pi)$ :

$$D^0 : 1.86484 \pm 0.02 [GeV/c^2]$$

$$K_s : 0.493677 \pm 0.018 [GeV/c^2]$$

Cuts on  $M(\pi\pi\pi)$ :

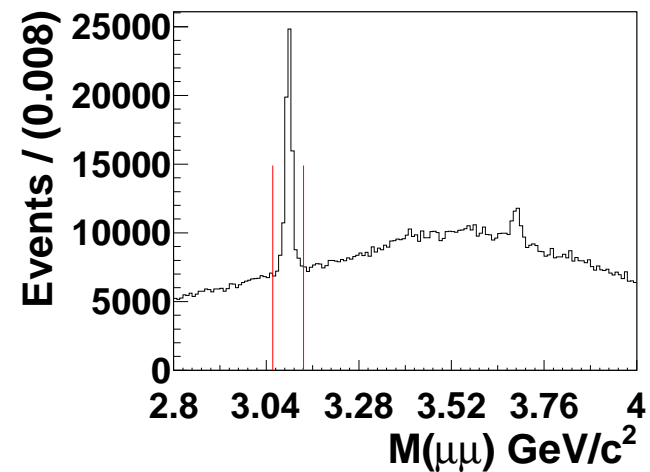
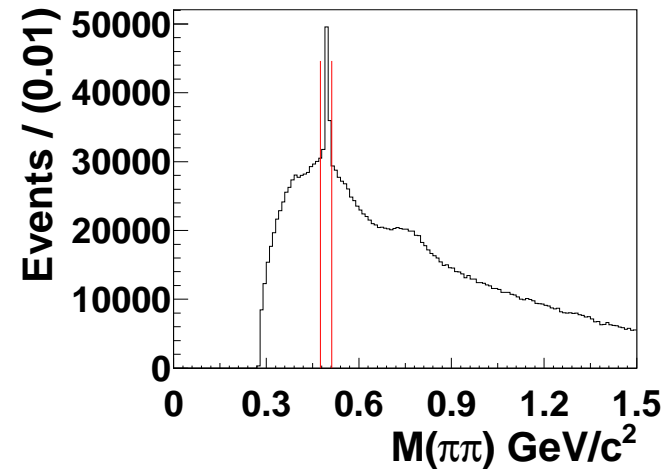
$$D^\pm : 1.8696 \pm 0.02 [GeV/c^2]$$

$$D_s^\pm : 1.96849 \pm 0.02 [GeV/c^2]$$

Cuts on  $M(\mu\mu)$ :

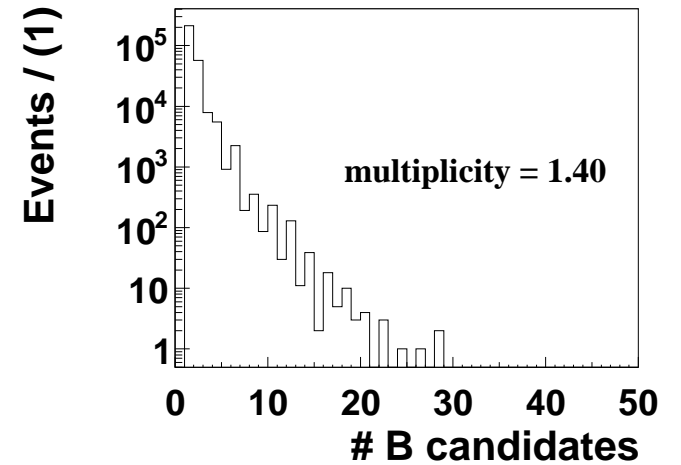
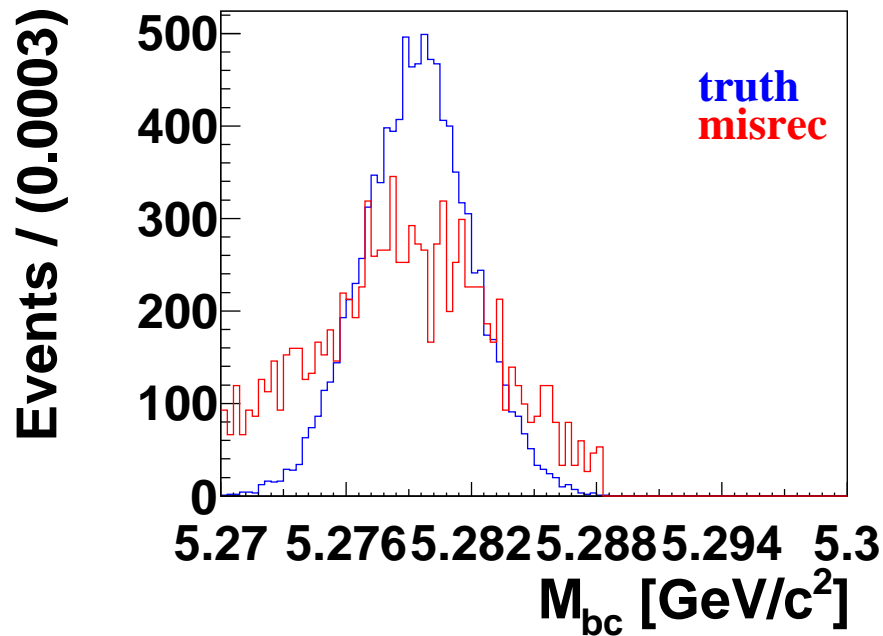
$$J\Psi : 3.0969 \pm 0.04 [GeV/c^2]$$

→ loss in  $\epsilon_{rec} < 4\%$

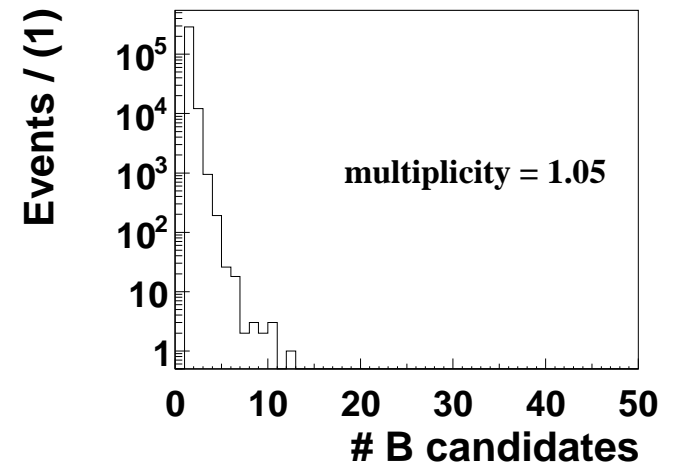


# Rec: BCS

- BCS: best candidate selection



$L(\text{top})$  and  $T$  pol



if 2 candidates with same  $M_{bc} = \sqrt{E_{beam}^2 - \vec{p}_B^2}$

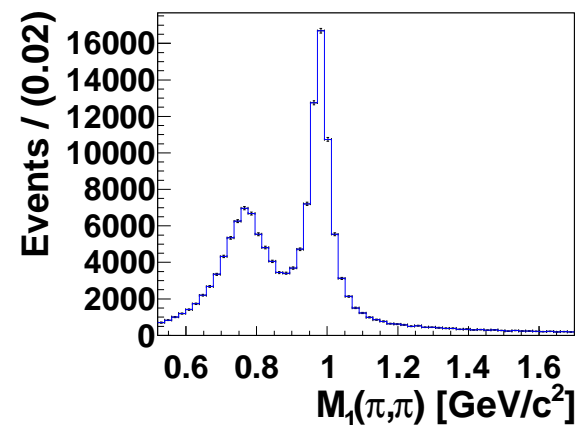
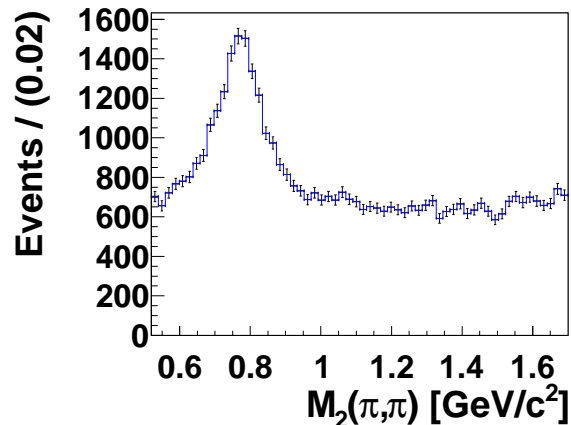
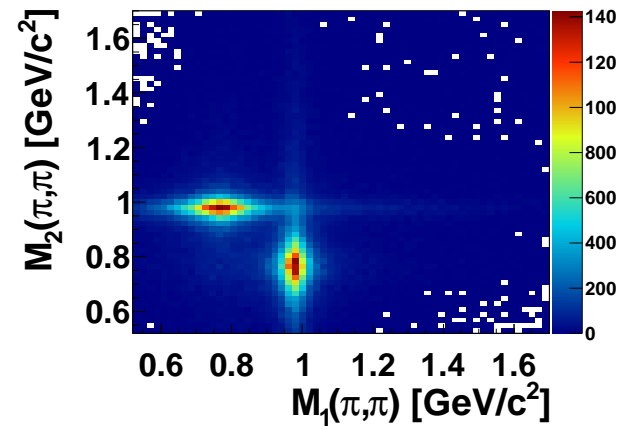
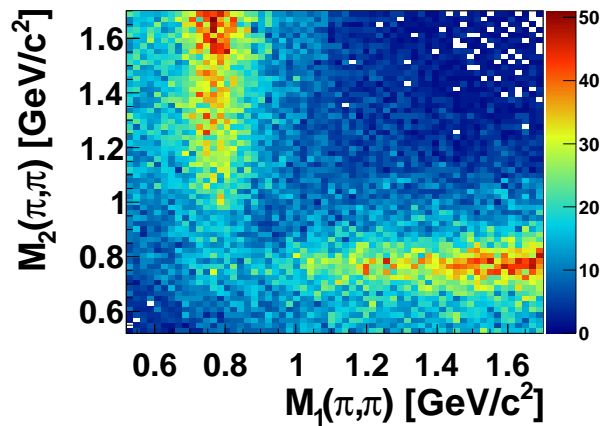
⇒ choose combination with highest  $\pi^+$  and lowest  $\pi^-$  momentum

→ purity = 76%( $L$ ); 92%( $T$ )



# Correlations!

sometimes correlated multidimensional  $\mathcal{PDF}$  needed  
e.g.  $a_1\pi$  or  $f_0\rho^0$  (peaking bkg:  $\Delta E$  shape similar to signal)



# Motivation

$$B \rightarrow \text{light } VV \quad (|B^0\rangle = |\bar{b}d\rangle)$$

light hadronic vector states:  $\rho, \omega, a_1, b_1, \phi, K^*, \dots$

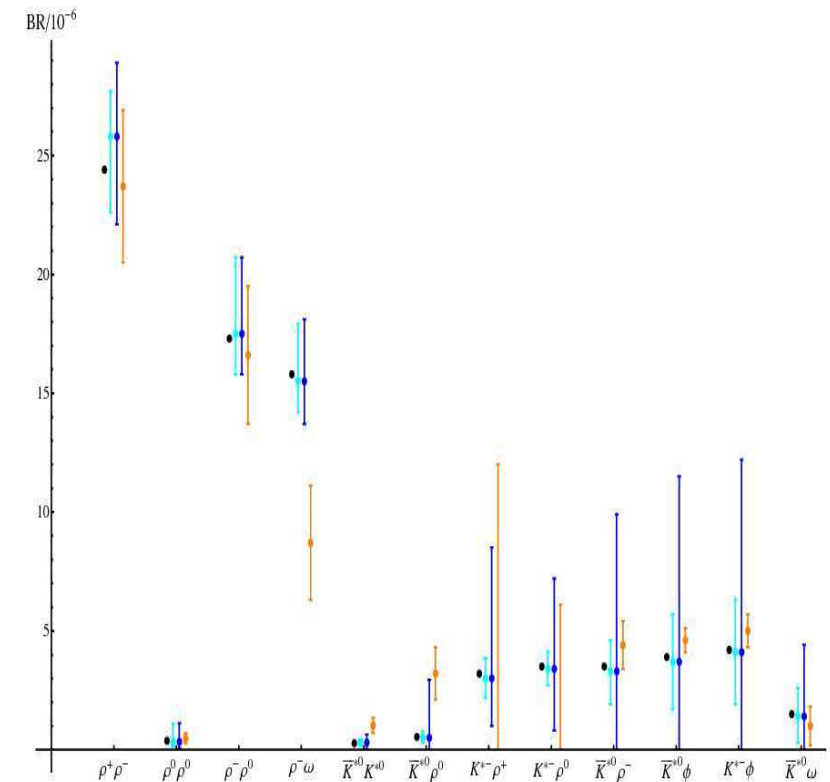
$\Rightarrow$  rich field of physics with different types of amplitudes

tree, QCD/EW penguin, weak annihilation

but: light  $\leftrightarrow$  rare (CKM suppressed)

$\Rightarrow$  experimental difficulties

- extract flavor parameters, e.g.  **$CP$  asymmetries**
- find (hints of) new physics
- helps understanding
  - a) QCD,
  - b) helicity structure,
  - c)...



*Bartsch, Buchalla, Kraus: arxiv: 0810.0249*

$$B^0 \rightarrow \rho^0 \rho^0$$

- previous measurements

Experiment	BELLE	BaBar
$BR(\times 10^{-6})$	$0.4 \pm 0.4 \pm 0.25$	$0.92 \pm 0.32 \pm 0.14$
$f_L$	-	$0.75 \pm 0.11 \pm 0.04$
$\mathcal{A}_{CP}^L$	-	$-0.2 \pm 0.8 \pm 0.3$
$\mathcal{S}_{CP}^L$	-	$0.3 \pm 0.7 \pm 0.2$
$B\bar{B}$ pairs ( $\times 10^6$ )	656.7	465

$\Rightarrow$  no observation made at Belle (yet) although more data available ( $\sim 2\times$ )

challenging analysis

- rare decay:  $BR \leq 10^{-6}$
- large backgrounds
- helicity structure

$\Rightarrow$

new method on full data set

- no cut-based but multivariate analysis, including eventshape and  $f_L$

# Toy MC Studies for $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$

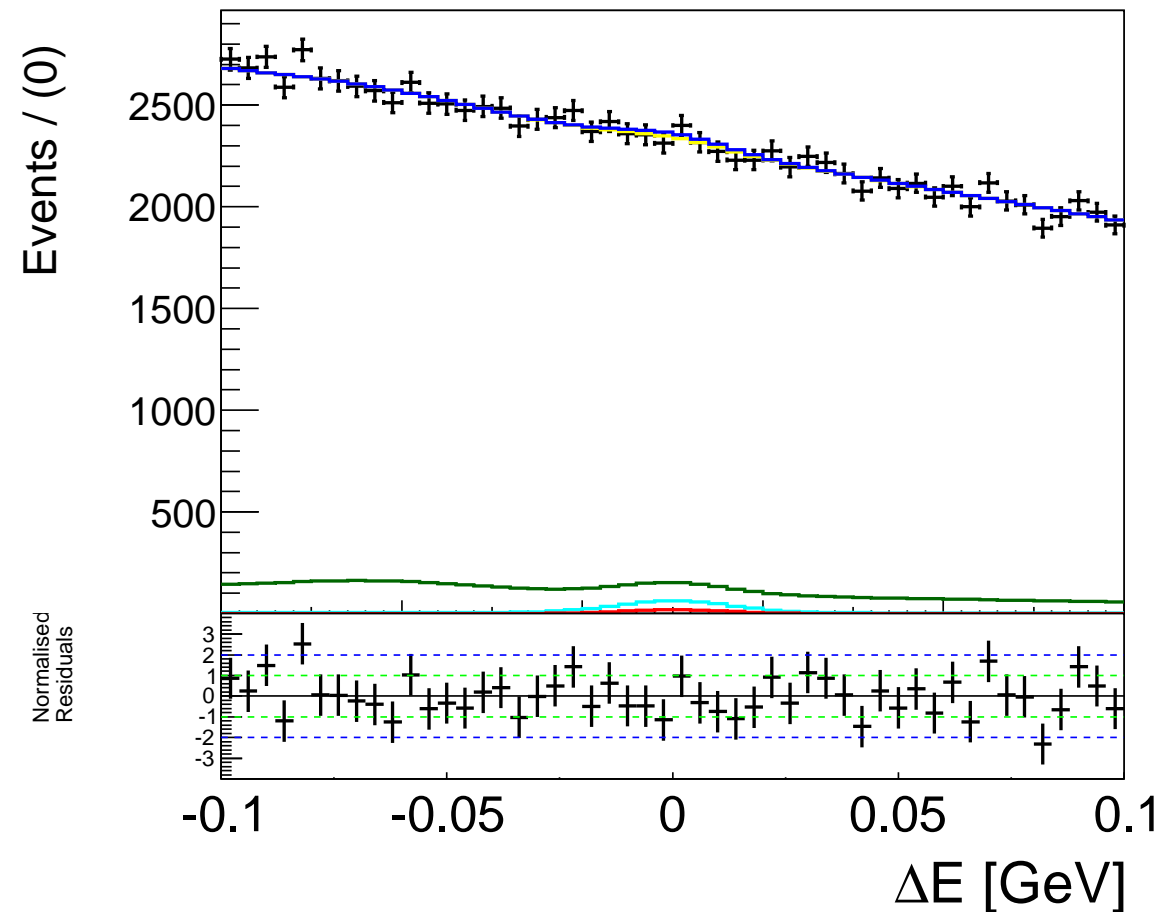
Estimate the fitter's ability to find signal with Toy MC, proj. into  $\Delta E$ .

**expected Nr of events:**

- **signal**:  $\sim 100$
- **4  $\pi$ s ff**:  $\sim 650$   
(using world averages)
- **$B\bar{B}$** :  $\sim 4500$
- **all**:  $\sim 110000$

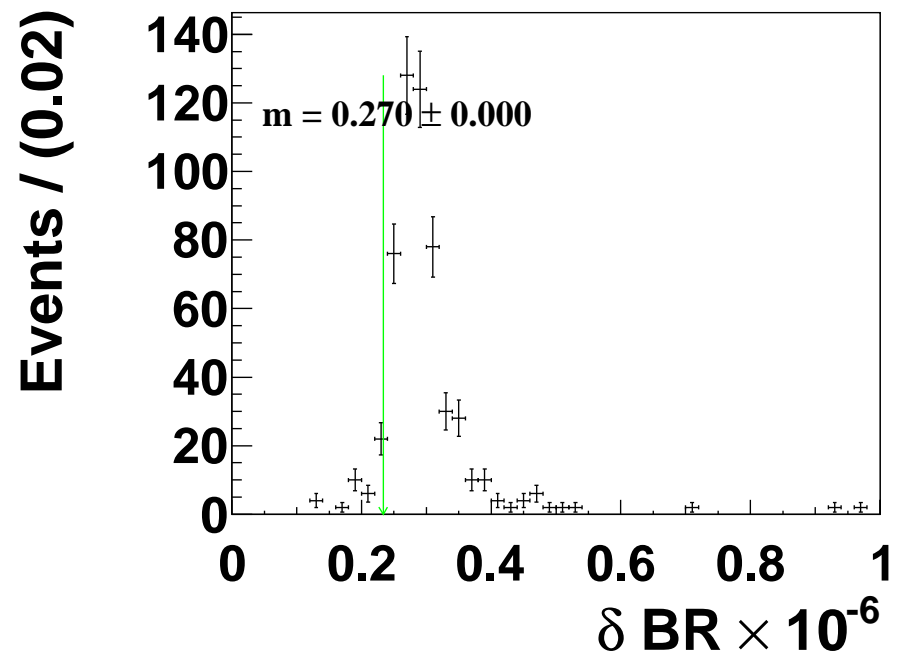
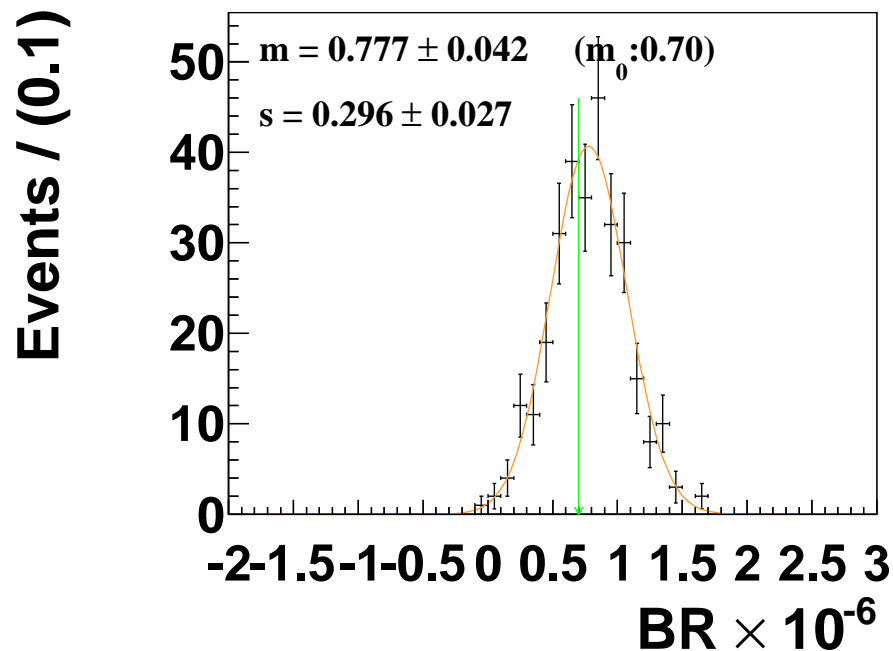
**Fit Region:**

$$5.27 < M_{bc} < 5.29 \quad [GeV/c^2]$$
$$-0.1 < \Delta E < 0.1 \quad [GeV]$$
$$0.52 < m(\pi^+ \pi^-) < 1.15 [GeV/c^2]$$
$$-1 < \cos(\theta_H) < 1$$



# Toy MC Studies for $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$

- performed fits on 300 toy MC samples



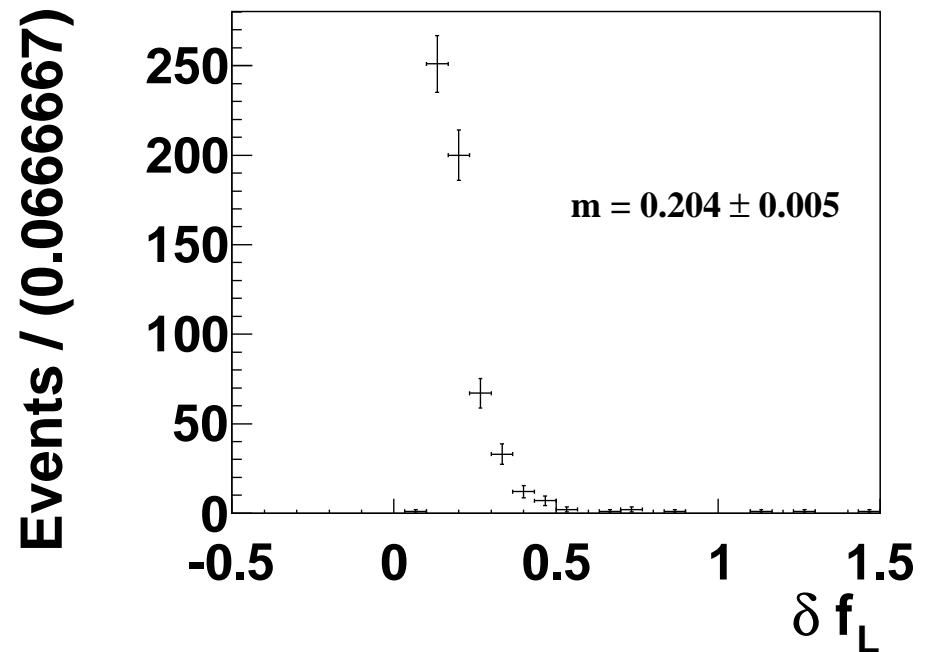
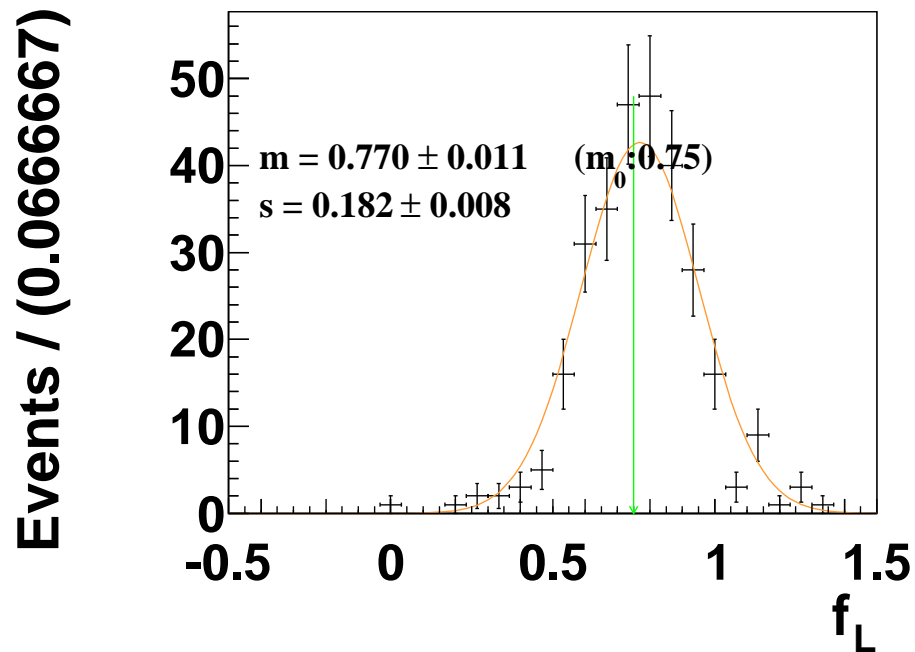
green line is input value

indicates  $3\sigma$  significance

$\Rightarrow$  on the edge of a observation with a  $3\sigma$  significance

# Toy MC Studies for $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$

- performed fits on 300 toy MC samples



green line is input value

$\Rightarrow$  measurement of  $f_L$  possible