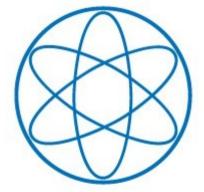
Study of the Internal Bremsstrahlung in the Inert Doublet Model

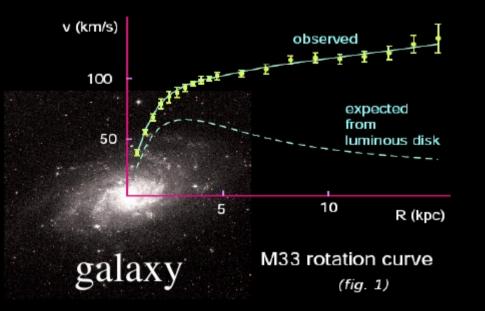
Camilo A. Garcia Cely Technische Universität München

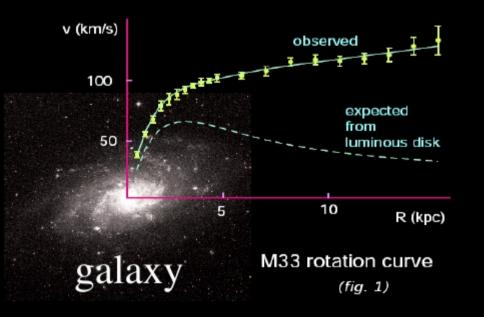
Particle Physics School Colloquium April 12th, 2013

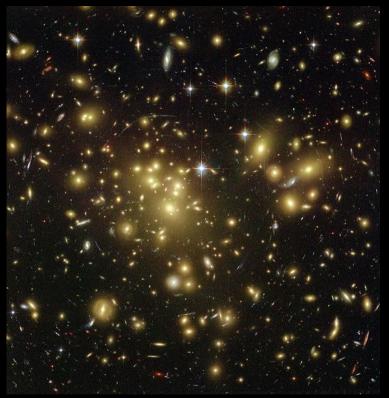


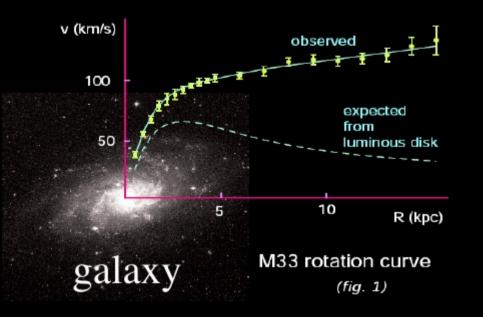


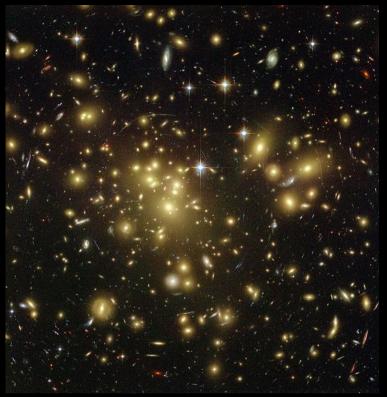
Based on work in progress done under the advice of Pr. Alejandro Ibarra

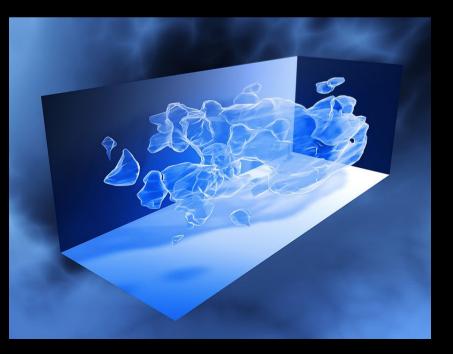


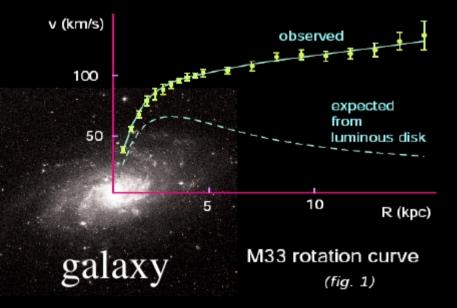


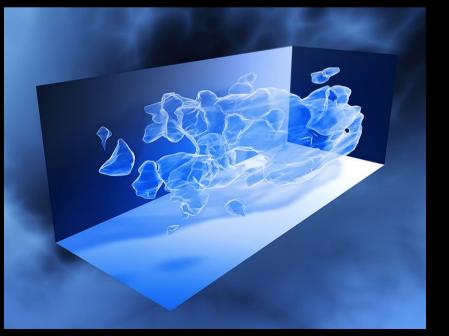




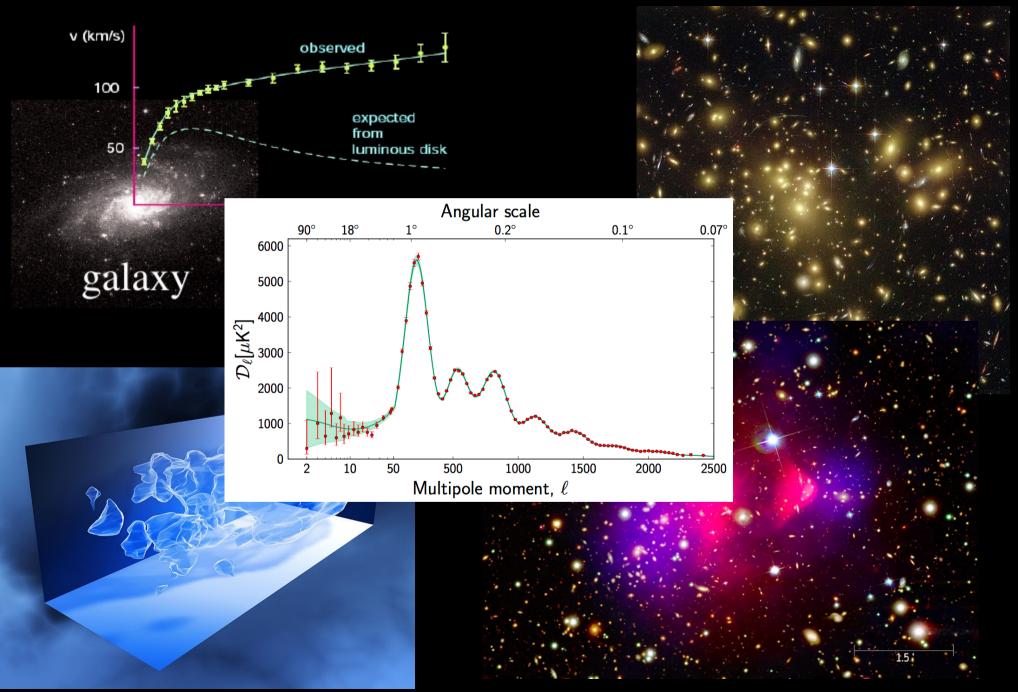












Study of SM plus extra scalar doublets, with a Z_2 symmetry to avoid FCNC.

Weinberg and Glashow. '76 Deshpande and E. Ma '77 Study of SM plus extra scalar doublets, Weinberg and Glashow. '76 with a Z_2 symmetry to avoid FCNC. Weinberg and E. Ma '77

One Extra Scalar Doublet + Right-Handed Neutrinos E. Ma. '98

- The dark matter candidate is one the neutral components of the doublet
- The stability of the dark matter is ensured by means of a Z_2 symmetry
- The corresponding canonical see-saw scale of $10^9~{
 m GeV}$ can be reduced to $1~{
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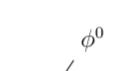
One Extra Scalar Doublet + Right-Handed Neutrinos E. Ma. '98

 ϕ^0 $(\nu_i, l_i) \sim (2, -1/2; +), \quad l_i^c \sim (1, 1; +), \quad N_i \sim (1, 0; -),$ $(\phi^+, \phi^0) \sim (2, 1/2; +), \quad (\eta^+, \eta^0) \sim (2, 1/2; -).$ η^0 η^0 N_k ν_i ν_i

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Phenomenology of Inert Doublet Model

Barbieri et al, Lopez-Honorez et al. T. Hambye et al, Gustaffson et al,....



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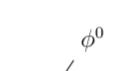
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Let
$$\eta = \begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}} (H + iA) \end{pmatrix}$$
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be the extra doublet, and Φ the SM doublet

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After electroweak symmetry breaking

$$\langle \Phi \rangle = \begin{pmatrix} 0 \\ \frac{v}{\sqrt{2}} \end{pmatrix}$$
, $\langle \eta \rangle = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$ \checkmark Z_2 is not spontaneously broken

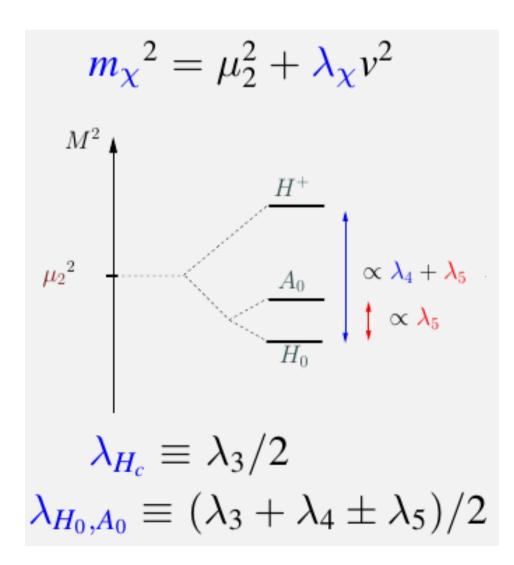
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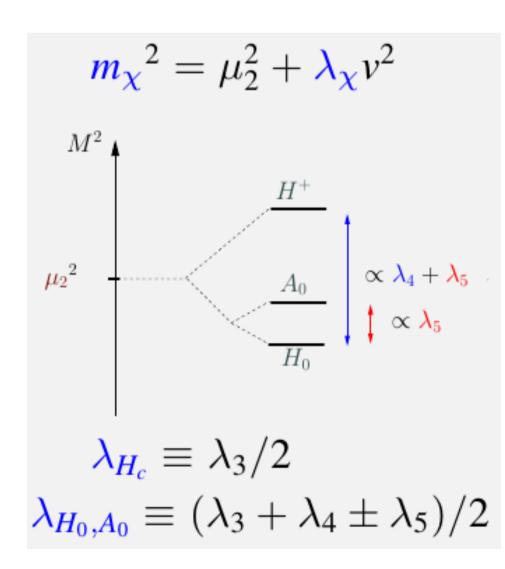
After electroweak symmetry breaking

$$\begin{split} \langle \Phi \rangle &= \begin{pmatrix} 0 \\ \frac{v}{\sqrt{2}} \end{pmatrix}, \qquad \langle \eta \rangle = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \qquad \qquad Z_2 \text{ is not spontaneously broken} \\ V_{Scalar} &= \frac{1}{2} (M_h^2 h^2 + M_{H^0}^2 H^2 + M_{A^0}^2 A^2) + M_{H^+}^2 H^+ H^- + \lambda_1 \left(\frac{1}{4} h^4 + v h^3 \right) \\ &+ \lambda_2 \left(\frac{1}{2} A^2 + \frac{1}{2} H^2 + H^+ H^- \right)^2 + \left(\frac{1}{2} h^2 + v h \right) \left(\lambda_{A^0} A^2 + \lambda_{H^0} H^2 + \lambda_3 H^+ H^- \right)^2 \end{split}$$

$$M_h^2 = -2\mu_1^2 , \qquad M_{H^0}^2 = \mu_2^2 + \lambda_{H^0}v^2 , \qquad M_{A^0}^2 = \mu_2^2 + \lambda_{A^0}v^2 , \qquad M_{H^+}^2 = \mu_2^2 + \frac{1}{2}\lambda_3v^2 + \lambda_{H^0}v^2 , \qquad \lambda_{H^0} = \frac{1}{2}(\lambda_3 + \lambda_4 + \lambda_5) , \qquad \lambda_{A^0} = \frac{1}{2}(\lambda_3 + \lambda_4 - \lambda_5) .$$



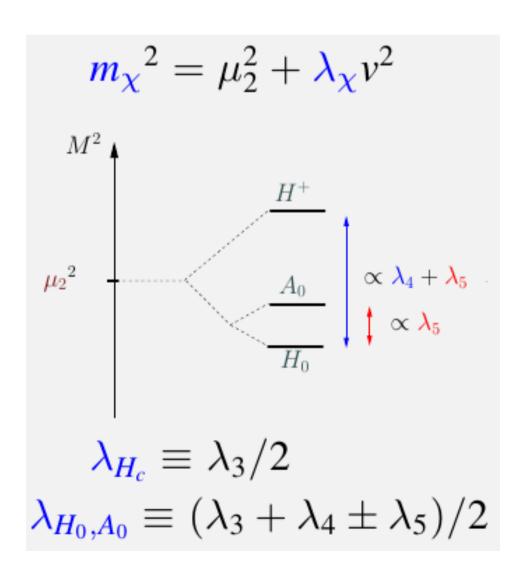
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There are five independent parameters, we take them as

$$M_{H^0} \lambda_2, \lambda_3, \lambda_4$$
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For a heavy dark matter candidate $(M_{H^0} \gg M_W)$ the splitting is relatively small and we expect the particles belonging to the extra doublet to have nearly degenerate masses .

Conditions on the couplings

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Vacuum Stability

$$\lambda_1 > 0 , \qquad \lambda_2 > 0 , \qquad \lambda_3 > -2(\lambda_1 \lambda_2)^{\frac{1}{2}} ,$$
$$\lambda_3 + \lambda_4 - |\lambda_5| > -2(\lambda_1 \lambda_2)^{\frac{1}{2}} .$$

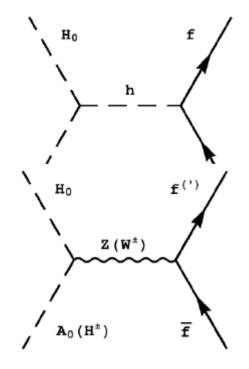
Conditions on the couplings

$$\begin{array}{l} \lambda_1>0\;,\qquad \lambda_2>0\;,\qquad \lambda_3>-2(\lambda_1\lambda_2)^{\frac{1}{2}}\;,\\ \mbox{Vacuum Stability} \\ \lambda_3+\lambda_4-|\lambda_5|>-2(\lambda_1\lambda_2)^{\frac{1}{2}}\;. \end{array}$$

Perturbativity
$$\lambda_i \lesssim 1.$$

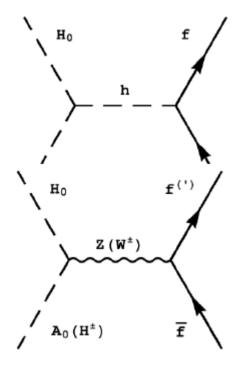
 $m_{H_0} \lesssim m_W$: GeV range $H_0 H_0 \to h^* \to \overline{f}f$ and $H_0 A_0 \to Z^* \to \overline{f}f$

Barbieri PRD06, LLH JCAP06, Gustafsson PRL07, Cao PRD07, Andreas JCAP08,...



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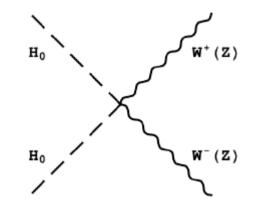
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 $m_{H_0} \gg m_W$: TeV range

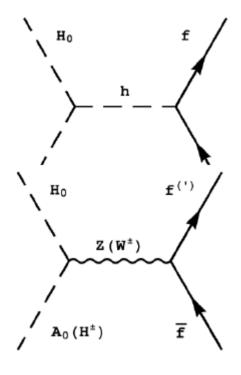
 $H_0H_0 \rightarrow ZZ, WW, hh$

Cirelli NPB06, Hambye JHEP09

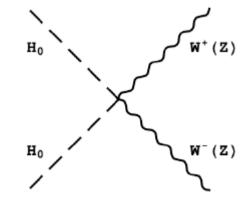


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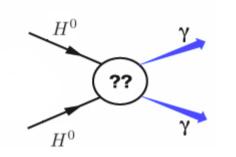
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Indirect Searches



No astrophysical uncertainties "Smoking gun" Potentially low statistics.

Gustaffson et al. 2007

Indirect Searches

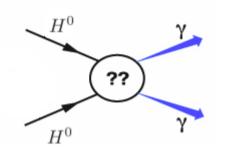


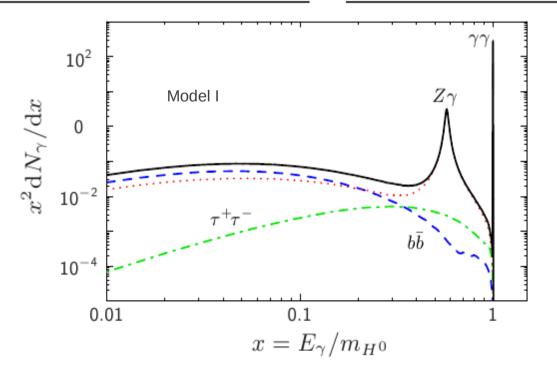
TABLE I: IDM benchmark models. (In units of GeV.)

Model	m_h	m_{H^0}	m_{A^0}	$m_{H^{\pm}}$	μ_2	$\lambda_2 \times 1 \text{ GeV}$
Ι	500	70	76	190	120	0.1
II	500	50	58.5	170	120	0.1
III	200	70	80	120	125	0.1
IV	120	70	80	120	95	0.1

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TABLE II: IDM	benchmark	model	results.
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Model	$v\sigma_{tot}^{v\to 0}$	Branching ratios [%]:	$\Omega_{\rm CDM} h^2$
	$[{\rm cm}^3 {\rm s}^{-1}]$	$\gamma\gamma$ $Z\gamma$ $bar{b}$ $car{c}$ $ au^+ au^-$	
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II	8.2×10^{-29}	29 0.6 60 4 7	0.10
III	8.7×10^{-27}	2 2 81 5 9	0.12
IV	1.9×10^{-26}	$0.04 \ 0.1 \ 85 \ 5 \ 10$	0.11



Gustaffson et al. 2007

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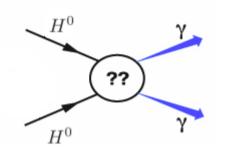


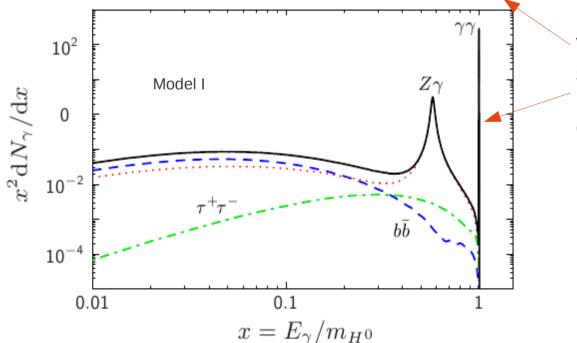
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Very prominent spectral features, but very small cross sections (loop suppressed)

Gustaffson et al. 2007

Let us consider annhibition into a final state $X\bar{X}\gamma$.

No loop suppression, but 3-body phase space suppression!

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In general, one can single out two situations where photons emitted from virtual charged particles may give an even more important contribution to the total IB spectrum than FSR: i) the three-body final state $X\bar{X}\gamma$ satisfies a symmetry of the initial state that cannot be satisfied by the two-body final state $X\bar{X}$ or ii) X is a boson and the annihilation into $X\bar{X}$ is dominated by t-channel diagrams. T. Bringmann et al. 2008

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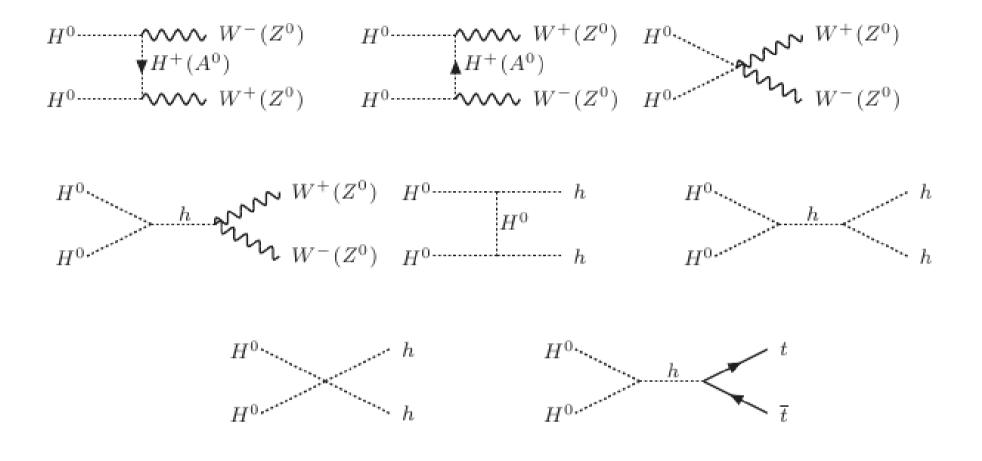
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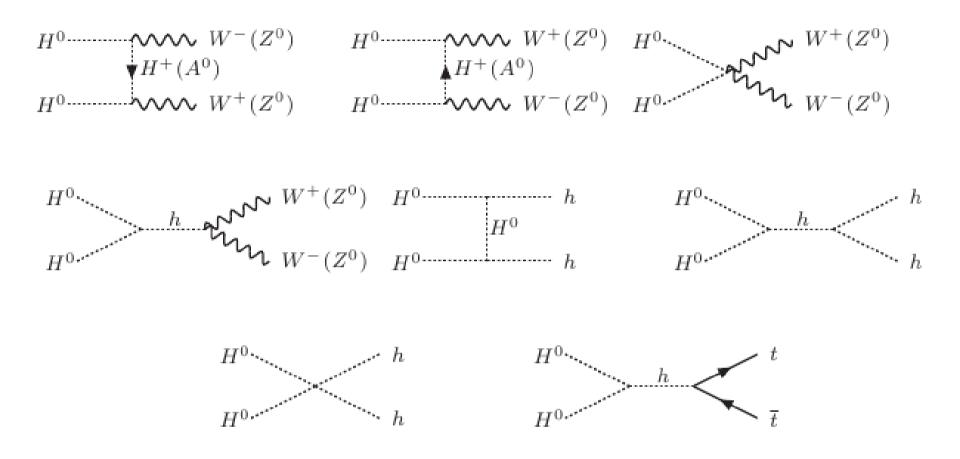
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That is the case for the inert doublet model in the high mass regime if X is a W boson!

Annihilation diagrams



Annihilation diagrams

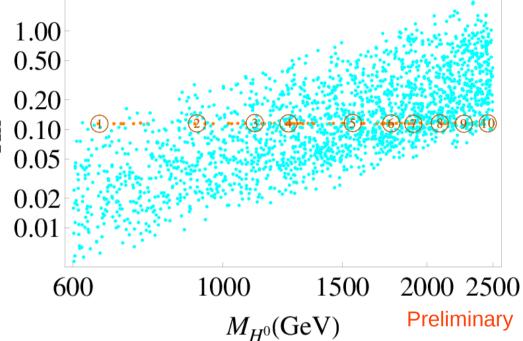


Why the t-channel?

$$D_t(p_W) \propto \left((p_{H^0} - p_W)^2 - M_{H^+}^2 \right)^{-1} \\\approx \left(M_{H^0}^2 + M_W^2 - M_{H^+}^2 - 2M_{H^0} E_W \right)^{-1}$$

If H^0 and H^+ are almost degenerate in mass, one thus finds an enhancement for small E_W .





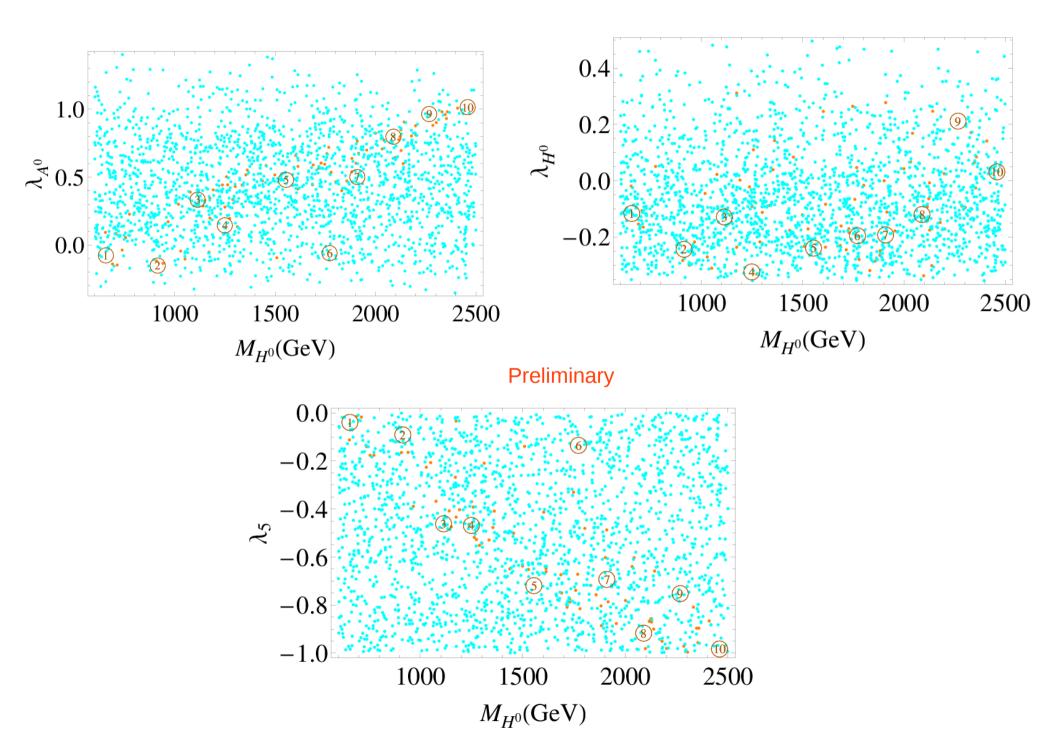
BMP	λ_2	λ_3	λ_4	λ_5	$M_{H^0}({\rm GeV})$	$M_{H^+}({ m GeV})$	$M_{A^0}({\rm GeV})$	Br(WW)	Br(ZZ)	Br(hh)	$\mathrm{Br}(t\overline{t})$
1	0.32	0.02	-0.21	-0.04	657.	663.	659.	42.	41.	14.	2.
2	0.47	-0.48	0.08	-0.09	915.	915.	918.	55.	21.	23.	2.
3	0.23	0.14	0.06	-0.46	1114.	1119.	1126.	25.	67.	8.	0.
4	0.85	-0.44	0.26	-0.46	1249.	1251.	1260.	45.	18.	35.	2.
5	0.52	0.03	0.21	-0.71	1554.	1559.	1568.	12.	71.	16.	0.
6	0.93	0.91	-1.20	-0.13	1771.	1782.	1773.	85.	8.	7.	0.
7	0.68	0.84	-0.53	-0.68	1909.	1919.	1920.	55.	40.	5.	0.
8	0.19	0.18	0.49	-0.90	2089.	2092.	2102.	8.	90.	2.	0.
9	0.90	0.78	0.39	-0.74	2267.	2269.	2277.	26.	71.	3.	0.
10	0.93	0.61	0.43	-0.97	2459.	2462.	2471.	18.	82.	0.	0.

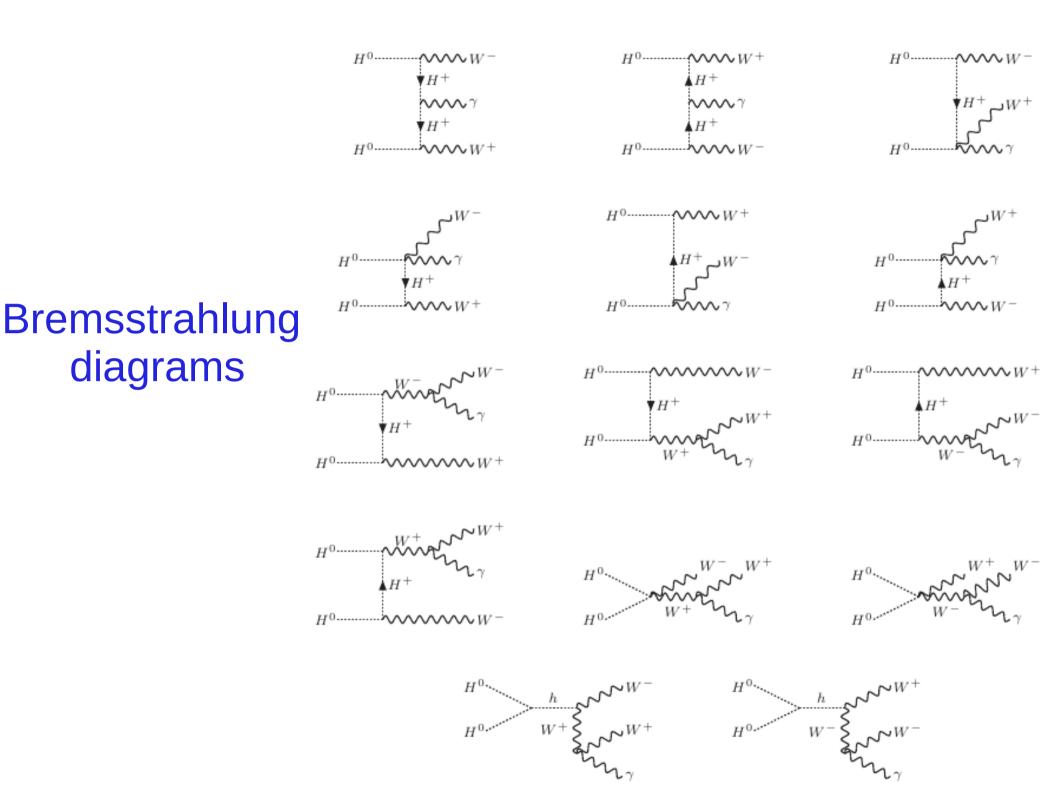
using micrOMEGAS G. Bélanger, F. Boudjema, A. Pukhov, A. Semenov,...

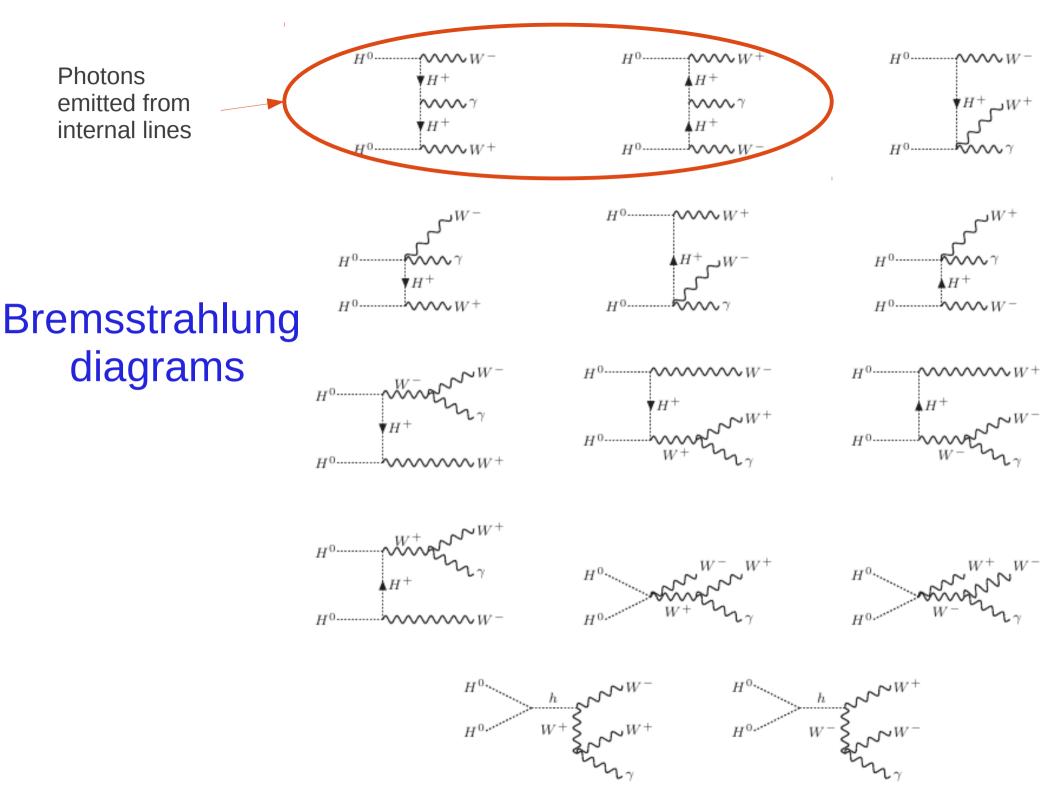
Benchmark points

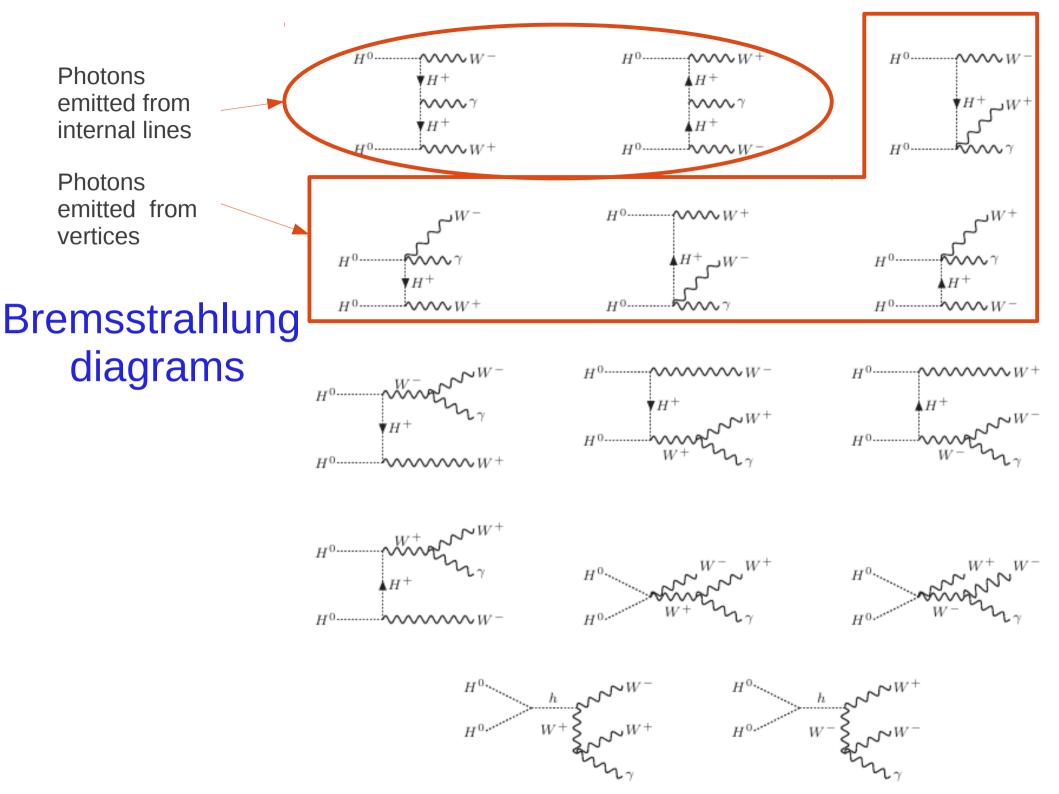
BMP

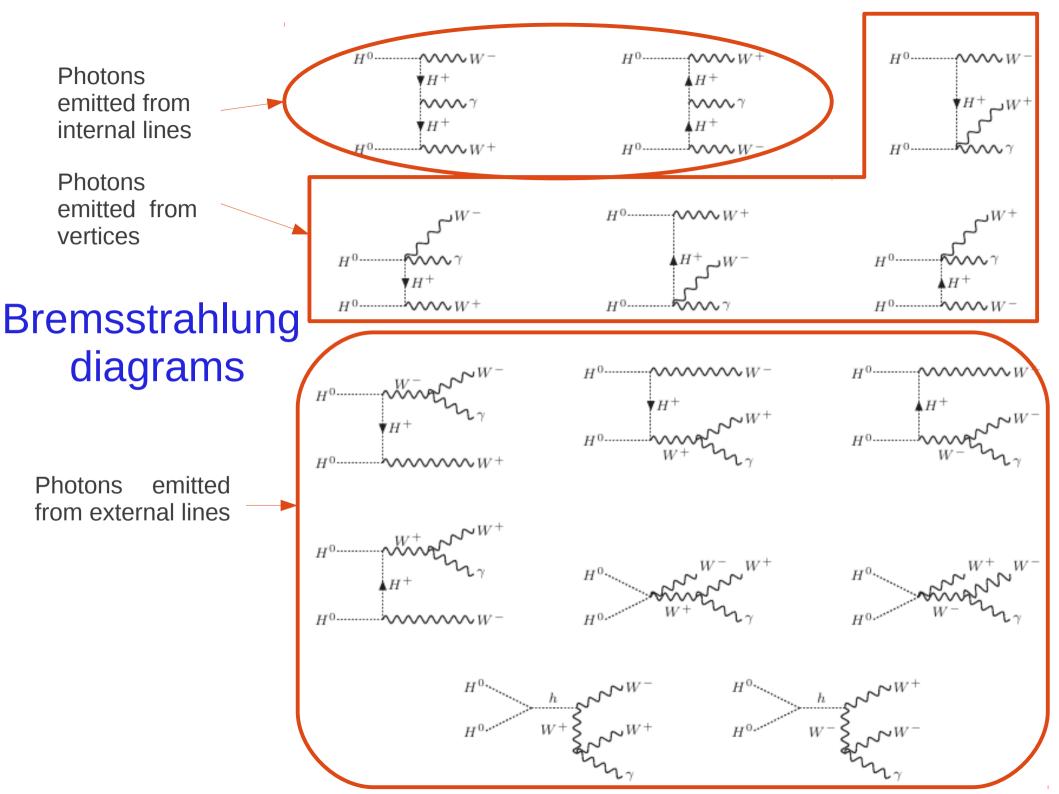
$\begin{bmatrix} 1.00 \\ 0.50 \\ 0.20 \\ 0.10 \\ 0.05 \\ 0.02 \\ 0.01 \end{bmatrix} \textcircled{3} (2 \cdot - (3 \cdot (2 \cdot - (3 \cdot (2 \cdot$												
600 1000 150									$00\ 25$			
$M_{H^0}(\text{GeV})$ Preliminary												
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	0.52	0.03	0.21	0.71	1554.	1559.		1568.	12.	71.	16.	0.
	0.93	0.91	-1.20	-0.13	1771.	1782.		1773.	85.	8.	7.	0.
	0.68	0.84	-0.53	-0.68	1909.	1919.		1920.	55.	40.	5.	0.
	0.19	0.18	0.49	-0.90	2089.	2092.		2102.	8.	90.	2.	0.
	0.90	0.78	0.39	-0.74	2267.	2269.		2277.	26.	71.	3.	0.
	0.93	0.61	0.43	-0.97	2459.	2462		2471.	18.	82.	0.	0.







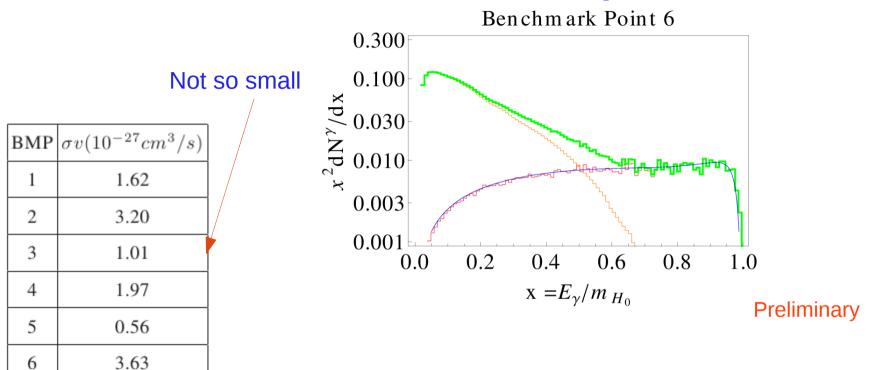




BMP	$\sigma v (10^{-27} cm^3/s)$
1	1.62
2	3.20
3	1.01
4	1.97
5	0.56
6	3.63
7	2.86
8	0.47
9	1.99
10	1.21

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4	1.97	
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6	3.63	
7	2.86	
8	0.47	
9	1.99	
10	1.21	

Not so small



7

8

9

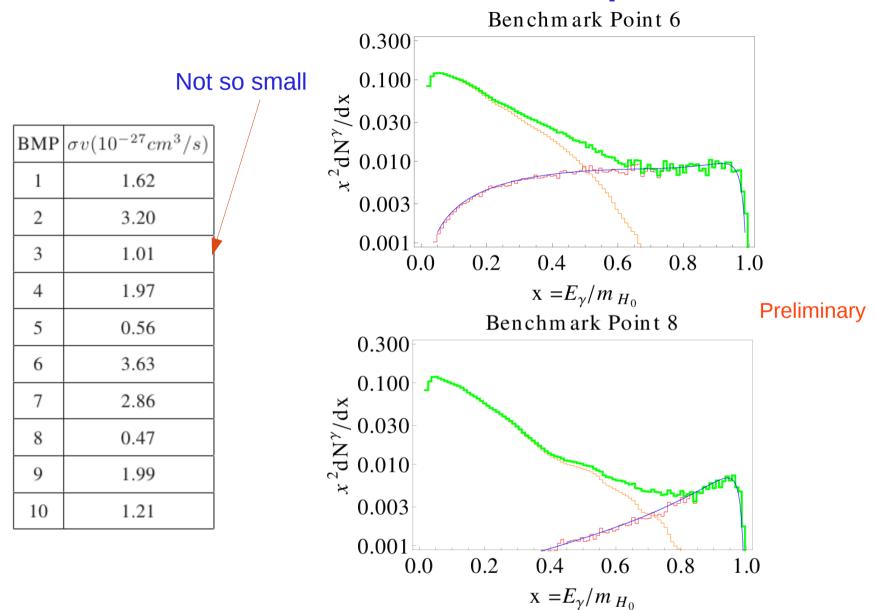
10

2.86

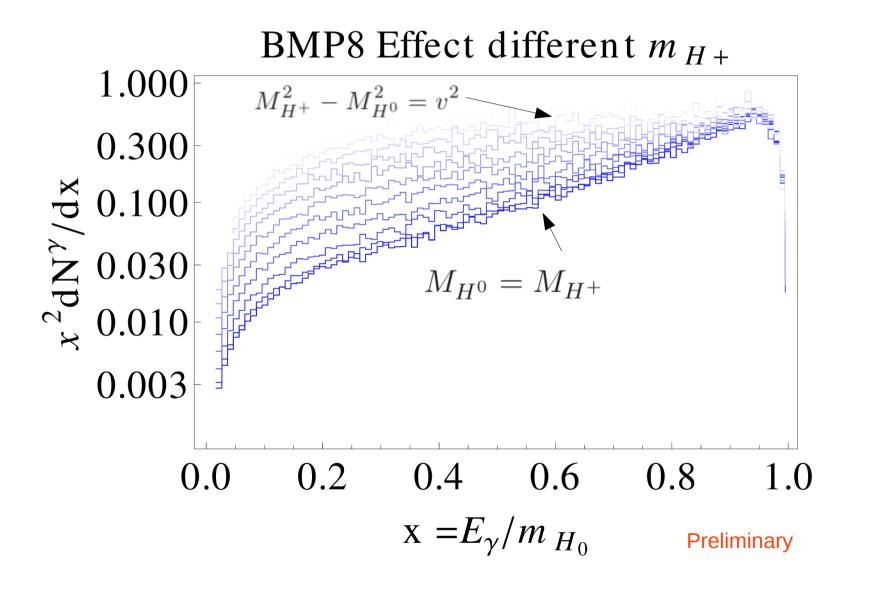
0.47

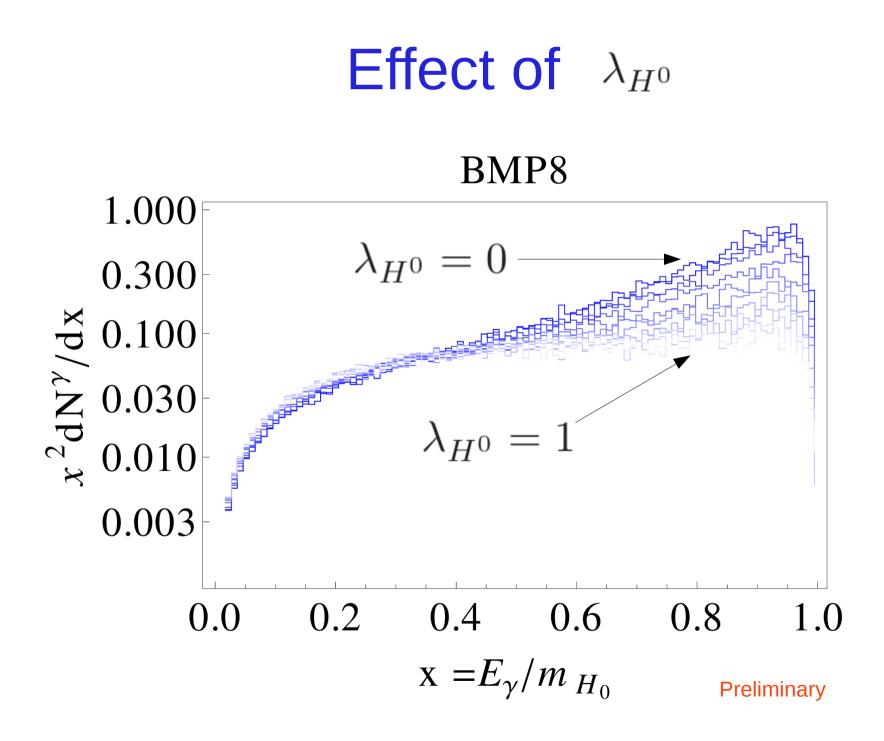
1.99

1.21

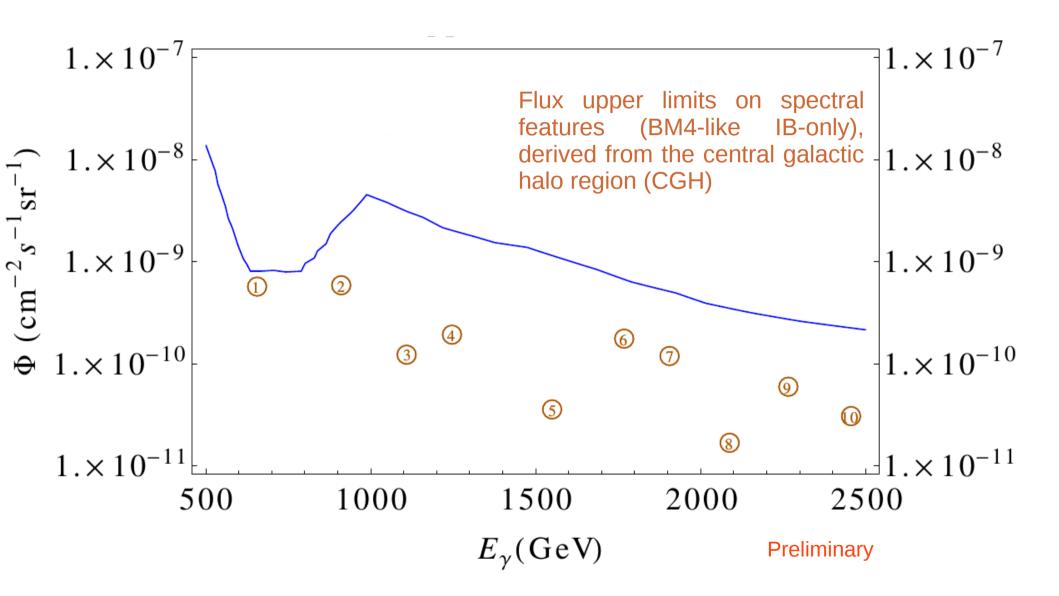


Effect of the mass splitting $(\lambda_4 + \lambda_5)$



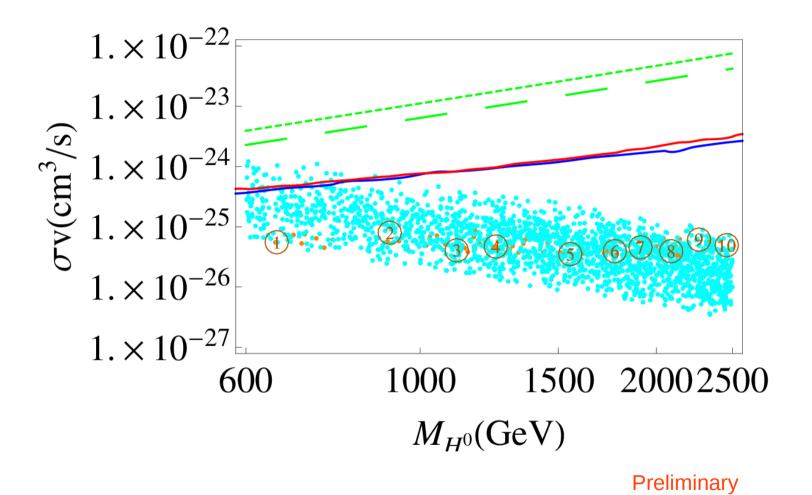


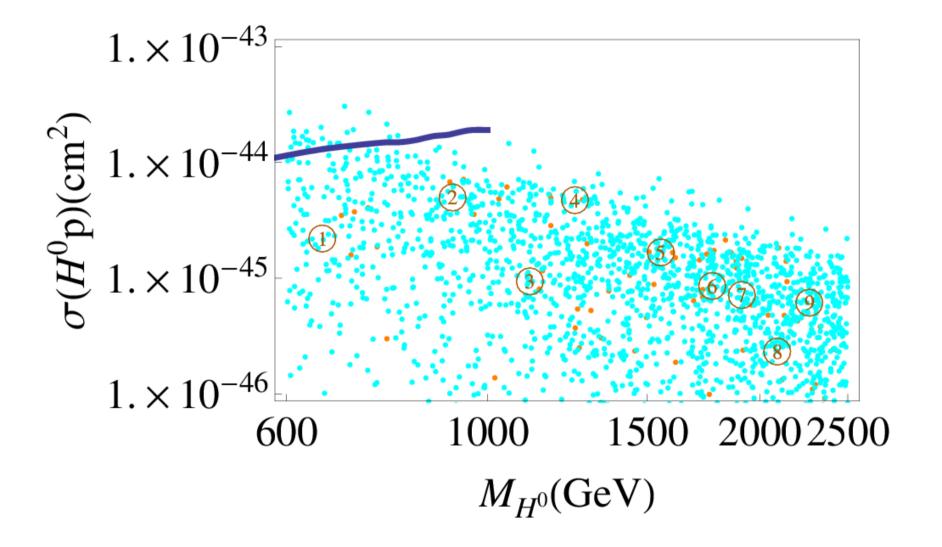
H.E.S.S. searches for photon-like signatures



Conclusions

- Internal Bremsstrahlung signatures are present in the high-mass regime of the inert doublet model.
- In the case of small quartic couplings -or near degeneracy of the exotic scalar bosons- the feature is more prominent.
- For heavy inert dark matter, internal bremsstrahlung signatures might be more relevant than mono-energetic photons in indirect searches.





Preliminary