

# Measurement of the Top Mass in a Threshold Scan at Linear Colliders

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München  
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MAX-PLANCK-GESELLSCHAFT



# Outline

- 1 Introduction
- 2 Future linear colliders
- 3 The top quark
- 4 Top threshold scan
- 5 Conclusions & Summary



# Motivation & the goal

## Top quark mass:

- cannot be calculated from the Standard Model, it is an input parameter
- important for calculation of electroweak radiative corrections
- connected to strong coupling constant, Higgs Yukawa coupling, Higgs mass, etc.
- issues regarding top mass definitions



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⇒ *statistical* and *systematical* uncertainties of **top quark mass** and **strong coupling constant** at future linear  $e^+e^-$  colliders



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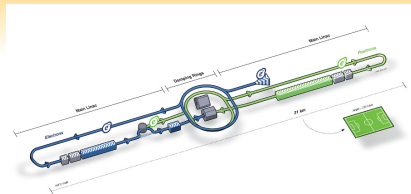
**Method:**  $t\bar{t}$  production threshold scan



# Future linear $e^+e^-$ colliders

## International Linear Collider (ILC):

- $\sqrt{s} = 500$  GeV, length 31 km
- $\sqrt{s} = 1$  TeV, length 53 km (upgrade)
- two interchangeable detector systems
- super-conducting RF cavities

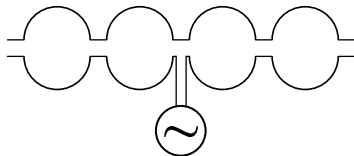




# Accelerating principles

## ILC:

- should use technology of classical super-conducting RF cavities
- average electrical field gradient for  $\sqrt{s} = 500$  GeV is 31.5 MV/m

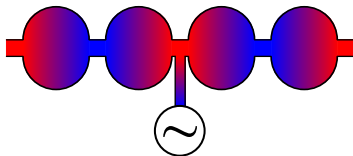




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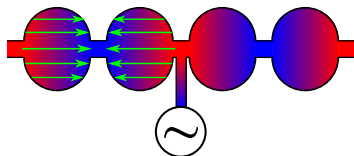
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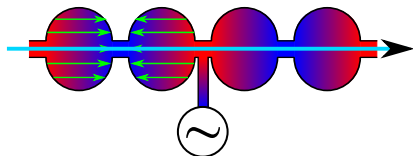
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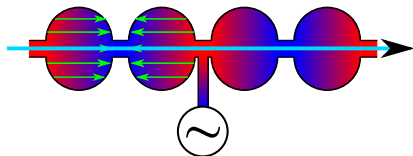
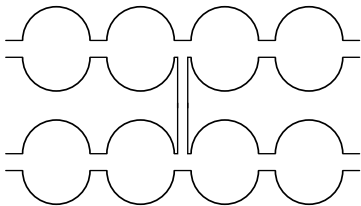
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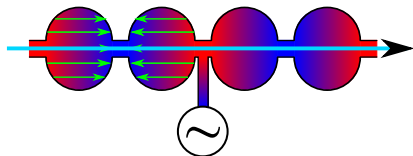
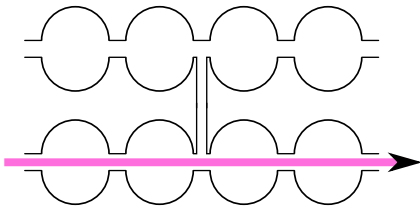
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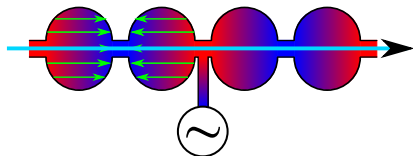
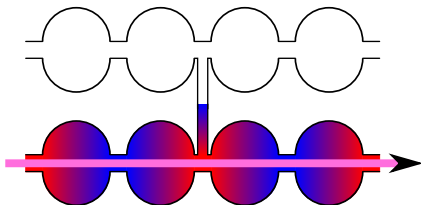
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- low energy/high intensity beam →



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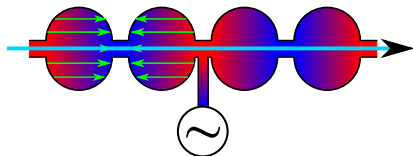
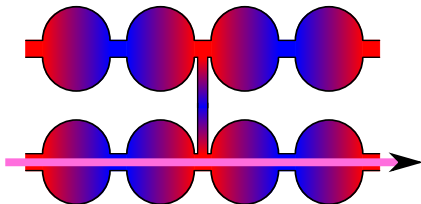
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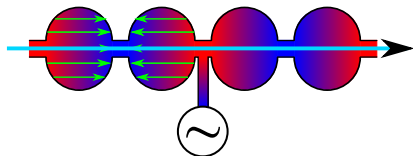
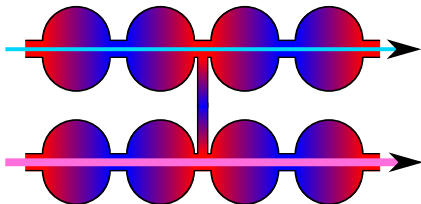
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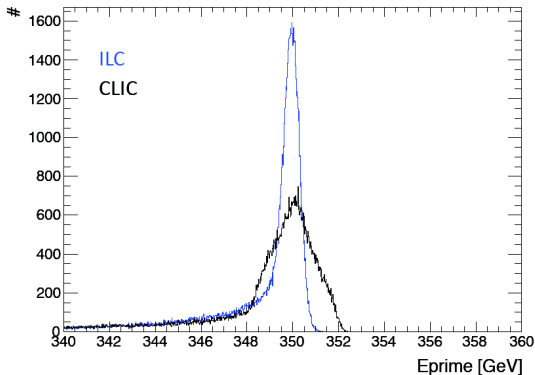
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# ILC and CLIC beam spectra (BS)



- the CLIC beam spectrum has a broader peak than ILC BS

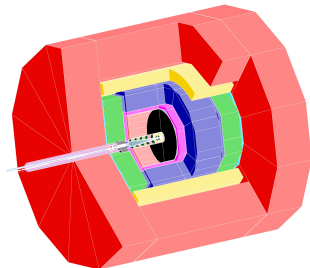
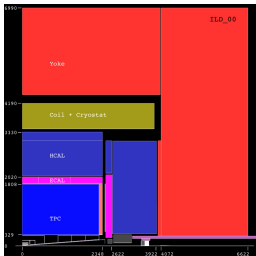
## Question:

is it possible at all to conduct a top threshold scan at the CLIC?



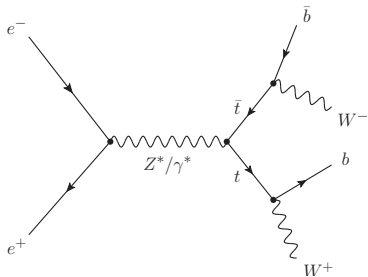
# International Large Detector (ILD)

- effort of ILC and CLIC collaboration overlap extensively
  - CLIC uses modified ILC detectors
  - despite classical onion design of the detector, new concepts are employed to meet the demands
    - highly granular calorimeters
    - high resolution tracker
- ⇒ excellent jet energy resolution

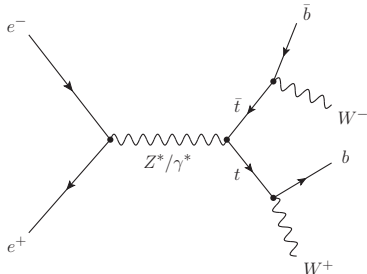


# Top quark properties

- lifetime:  $\tau_{life} \sim 10^{-24}$  s
- hadronization time:  $\tau_{had} \sim 10^{-23}$  s



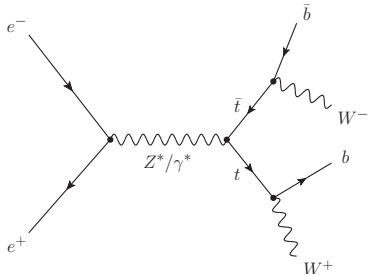
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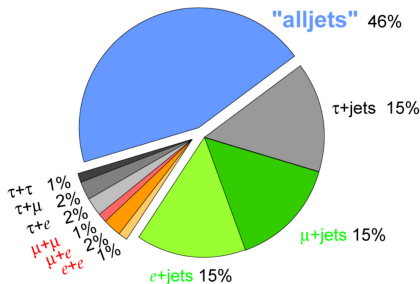
$\Rightarrow$  decays before hadronization

$\Rightarrow$  top mass can be measured directly by reconstructing decay products' invariant mass



# Top decay products

- $b$  quark creates always a  $b$ -jet
- ⇒ event signature is entirely given the  $W$  boson decay:



## Hadron colliders:

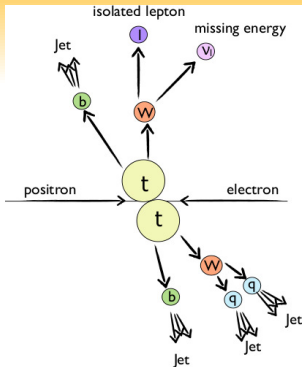
- hard to pick out  $t\bar{t}$  pairs from QCD background
- one and two-lepton final states are used

## Lepton colliders:

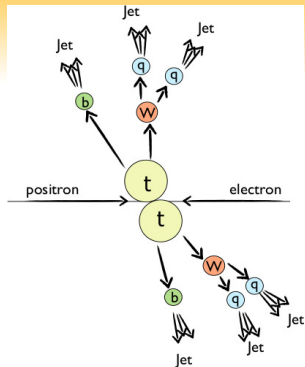
- $t\bar{t}$  pairs easy to identify
- concentrate on large branching fractions
- low missing energy



# $W$ decays used for reconstruction



- 4-jet final state (BR = 45%)
- identified by isolated lepton and  $b$ -jet



- 6-jet final state (BR = 46%)
- identified by  $b$ -jet and reconstructed jet energy originating from  $W$  decay



# Top quark mass definitions

- pole mass
  - defined as the pole of the renormalized quark propagator for  $p \rightarrow M$  (“rest mass”)
  - has an internal ambiguity  $\sim \Lambda_{QCD}$
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- 1S mass
  - defined as half of the mass of fictitious  ${}^3S_1$  toponium ground state for a stable quark
  - position of the total  $t\bar{t}$  production cross section peak remains stable if expressed in terms of 1S mass



# Top quark reconstruction

- top quark decays ( $t \rightarrow Wb$ ) before it hadronizes
- ⇒ its mass can be determined directly from its decay products
- $W \rightarrow 2 \text{ jets or jet} + \text{lepton}$
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## Hadron accelerators

- experiments must deal with high QCD background
- ⇒ usually, final states with one or two leptons are used for the analyses
- ⇒ missing energy taken out by neutrino
- ⇒ lower total branching fraction → lower integrated luminosity



# Top quark measurement at linear lepton colliders

- lepton collider experimental conditions are favorable for the top mass measurement
    - low background compared to hadron colliders
    - better defined initial state of the collision
  - thanks to low background at  $e^+e^-$  accelerators, so called “particle flow” algorithms can be employed
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## Two top mass measurement alternatives:

- invariant mass reconstruction
- threshold scan



# Top mass measurement alternatives

- top mass is not unambiguously defined
- ⇒ cross-check of several measurement methods needed

## Invariant mass reconstruction

- + experimentally well defined
- + can be conducted at any above-threshold energy
- + high integrated luminosity
- cannot determine which top mass was measured



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## Threshold scan:

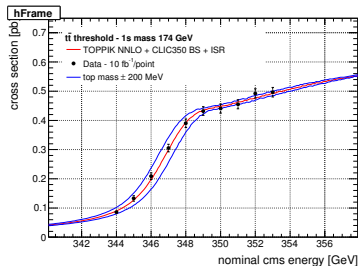
- + theoretically well understood
- + potential of simultaneous measurement of correlated quantities
- + together with known top invariant mass can shed light on top mass definitions
- needs a dedicated accelerator run (Higgs measurements also possible)





# Principle of the threshold scan template fit

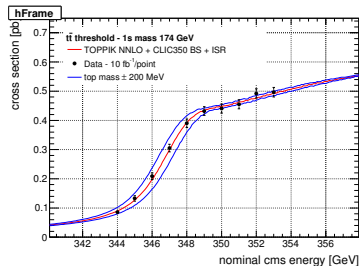
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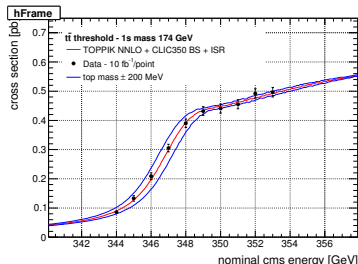
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⇒ fit template

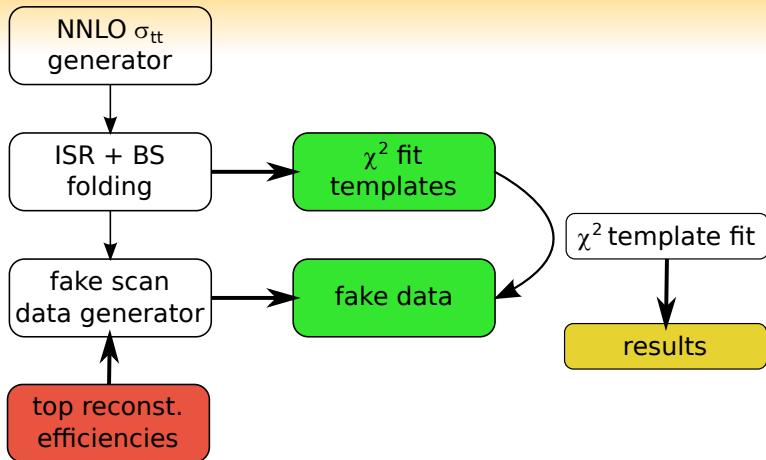


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- ⇒ fit template
- the “measured” data points are fitted with the templates
  - top mass and  $\alpha_s$  are extracted from the fits



# Simulation procedure scheme



# Top mass reconstruction: signal and background at $\sqrt{s} = 350$ GeV

- signal and background events were simulated
- highly optimized top reconstruction has been conducted (by Katja Seidel)

process type	$e^+e^- \rightarrow$	cross-section* $\sigma$ (fb)
signal	$t\bar{t}$	400
background	$WW$	11400
background	$ZZ$	673
background	$WWZ$	10
background	$q\bar{q}$	24500

\* cross-sections corrected for Initial State Radiation (ISR) and beam spectrum



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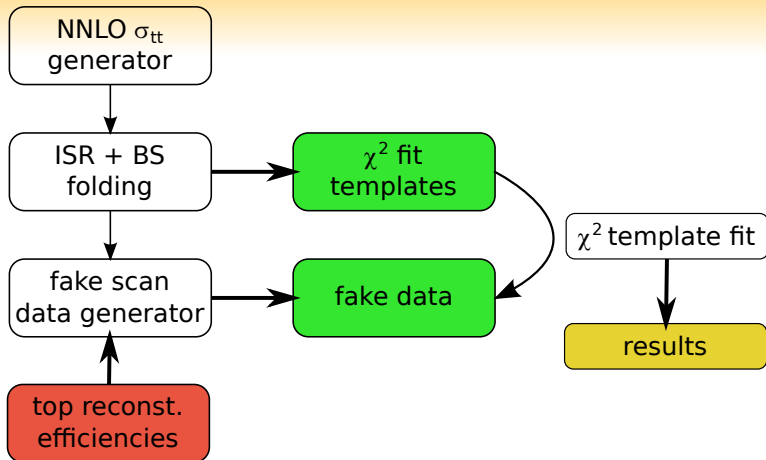
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- ⇒ resulting top reconstruction- and background rejection efficiencies were used for further simulation

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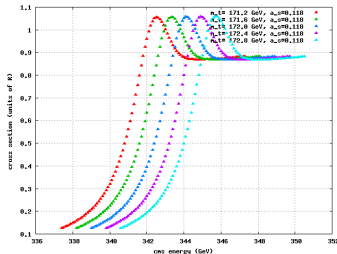


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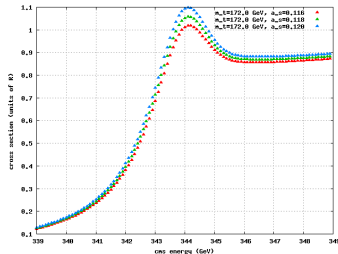


# $t\bar{t}$ production cross-section generator

- theory based next-to-next-to-leading order (NNLO) calculation (“TOPPIK” by Hoang & Teubner, Phys.Rev.D60:114027,1999)
- input parameters: top mass, top Width, strong coupling constant, Higgs mass, Yukawa coupling, (LO, NLO, NNLO)
- production channel:  $e^+e^- \rightarrow Z^*/\gamma^* \rightarrow t\bar{t}$



varying  $m_t$

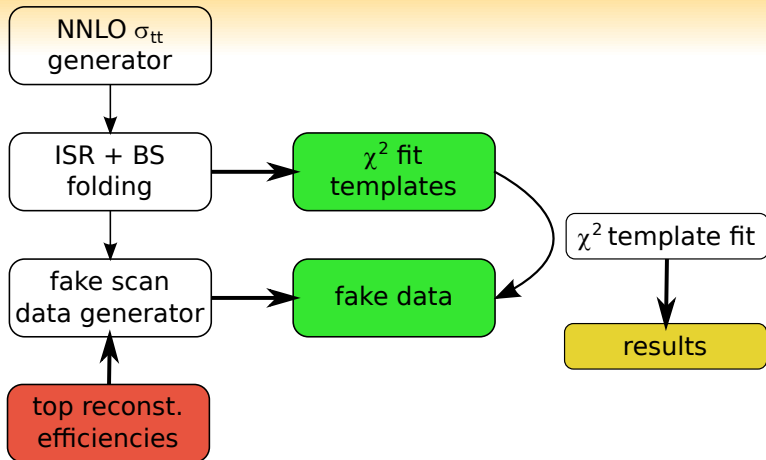


varying  $\alpha_s$





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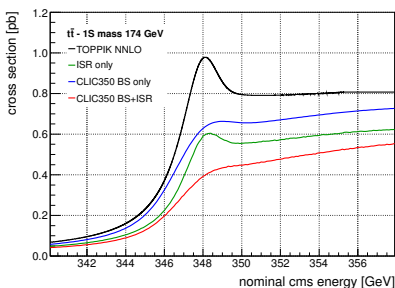
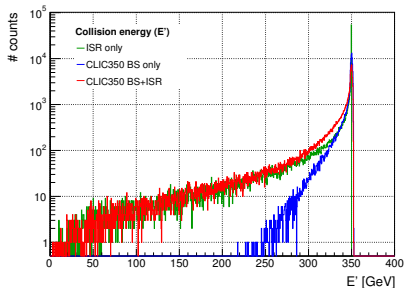


# Effects of ISR and BS on cross-section shape

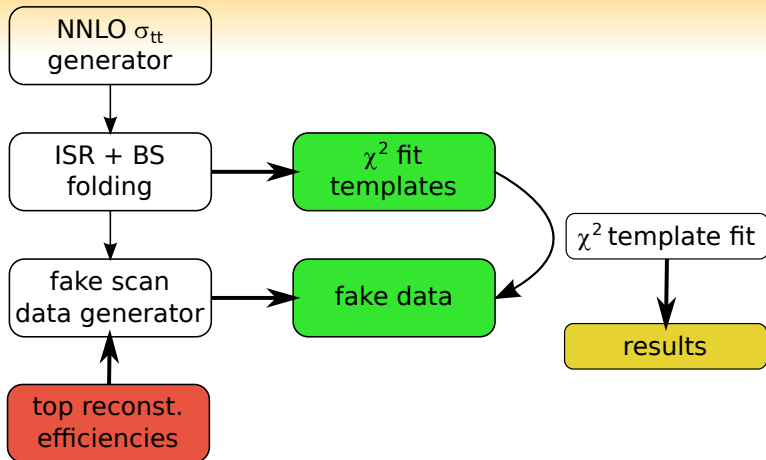
to get  $t\bar{t}$  production cross-section at a  $e^+e^-$  collider, two effects have to be taken into account

- Initial State Radiation (ISR)
- Beam Spectra (BS)

these two distributions are folded with pure physical cross-section



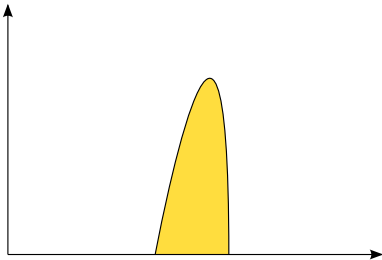
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# Template $\chi^2$ fit

- $\sigma_n^{meas}$  ..... measured cross-section  
 $\sigma_n^{template}$  ..... simulated cross-section  
 $\Gamma_n^{meas}$  ..... measured cross-section uncertainty  
 in  $n$ -th energy bin

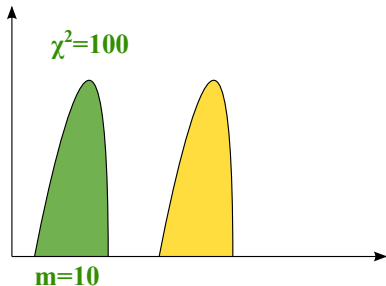
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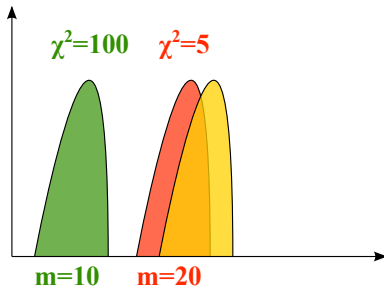
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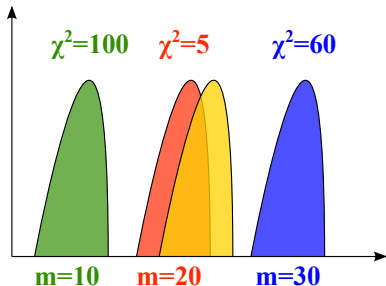
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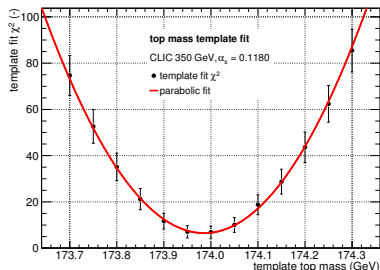
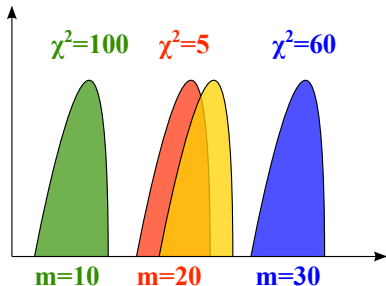
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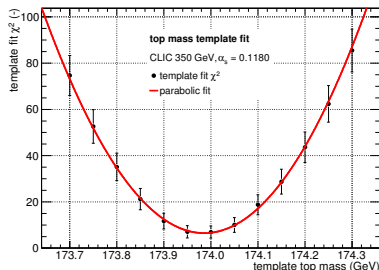
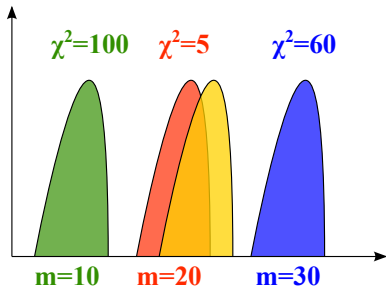




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Repeat the fit 5000× with different measurement sets  
 ⇒ statistical uncertainty



# Recent hadron collider uncertainties of the top mass

## CDF, Tevatron

$$\delta m_t^{(inv)} = 510_{(\text{stat.})} \oplus 710_{(\text{syst.})} \text{ MeV}$$

$$\Rightarrow \delta m_t^{(\overline{\text{MS}})} = O(1) \text{ GeV}$$



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## CMS, LHC

$$\delta m_t^{(inv)} = 380_{(\text{stat.})} \oplus 910_{(\text{syst.})} \text{ MeV}$$

$$\Rightarrow \delta m_t^{(\overline{\text{MS}})} = O(1) \text{ GeV}$$



# CLIC threshold scan uncertainties

**1D fit result (external input:  $\delta\alpha_s = 0.0007$ ,  $\alpha_s = 0.1180$ )**

$$\delta m_t^{(1S)} = 21_{(\text{stat.})} \pm 6_{(\text{thr. syst.})} \pm 11_{(\text{bkg. syst.})} \pm 21_{(\alpha_s \text{ syst.})} \text{ MeV}$$

$$\delta m_t^{(1S)} = 21_{(\text{stat.})} \oplus 43_{(\text{syst.})} \text{ MeV}$$

$$\Rightarrow \delta m_t^{(\overline{\text{MS}})} = 100 \text{ MeV}$$



# CLIC threshold scan uncertainties

## 1D fit result (external input: $\delta\alpha_s = 0.0007$ , $\alpha_s = 0.1180$ )

$$\delta m_t^{(1S)} = 21_{(\text{stat.})} \pm 6_{(\text{thr. syst.})} \pm 11_{(\text{bkg. syst.})} \pm 21_{(\alpha_s \text{ syst.})} \text{ MeV}$$

$$\delta m_t^{(1S)} = 21_{(\text{stat.})} \oplus 43_{(\text{syst.})} \text{ MeV}$$

$$\Rightarrow \delta m_t^{(\overline{\text{MS}})} = 100 \text{ MeV}$$

## 2D fit result (from fit: $\delta\alpha_s = 0.0015$ )

$$\delta m_t^{(1S)} = 33_{(\text{stat.})} \pm 6_{(\text{thr. syst.})} \pm 16_{(\text{bkg. syst.})} \text{ MeV}$$

$$\delta m_t^{(1S)} = 33_{(\text{stat.})} \oplus 17_{(\text{syst.})} \text{ MeV}$$

$$\Rightarrow \delta m_t^{(\overline{\text{MS}})} = 142 \text{ MeV}$$



# Conclusions

- Top threshold scan is feasible at the CLIC
  - $m_t$  statistical uncertainty for the ILC is by 22% lower
  - precise knowledge of the beam spectrum is more important than a narrow distribution
- ⇒ CLIC beam spectrum is good enough



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## Further performed studies:

- sensitivity to top width, Yukawa coupling and Higgs mass is not high enough
- $1\sigma$  luminosity-spectrum-induced systematic uncertainty of the top mass is  $\approx 6 \text{ MeV}$



# Summary

## Future $e^+e^-$ colliders:

- linear accelerators with  $\sqrt{s}$  of 500 to 3000 GeV (ILC, CLIC)
- equipped with highly precise tracking systems and highly granular calorimeters to reach excellent jet-energy resolution
- offer clean experimental environment for precise measurement of the top quark mass





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## Top threshold scan:

- $t\bar{t}$  pair production cross section measured around production threshold
- top quark mass can be extracted from that curve
- simulation for the CLIC and ILC has been completed
- top quark mass and strong coupling constant  $\alpha_s$  can be obtained with a help of the template fit technique
- statistical and systematical uncertainties determined

