

CKM Angle ϕ_2 From $B \rightarrow \rho\rho$ Decays

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1) Motivation

2a) Measurements of $\mathcal{B}(B^0 \rightarrow \rho\rho)$

2b) Implication for ϕ_2

3) Outlook



CP Violation

Where did the anti-matter go?

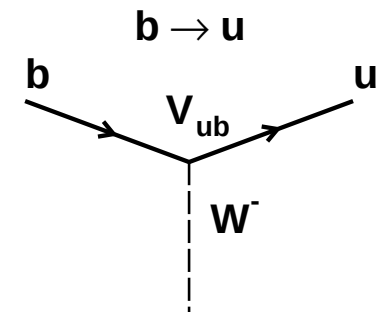
weak interaction violates the combined symmetry C (charge) P (parity),

complex, **unitary** quark-mixing matrix, V_{CKM} (Cabibbo-Kobayashi-Maskawa):

quark flavor transition probabilities V_{ij} ($W^\pm$ exchange).



$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}_{\text{weak}} \equiv \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{mass}}$$



successfully tested BUT NOT able to produce observed asymmetry in our universe!!.

CPV Observables

4 free parameters(3 mixing angles, **1 complex phase**) for 3 generations of quarks

Approx. representation of V_{CKM} in terms of the Cabibbo angle, $\lambda = \sin \theta_C \approx 0.22$

$$V_{\text{CKM}} \approx \mathcal{O} \left(\begin{pmatrix} \boxed{1} & \lambda & \boxed{\lambda^3} \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4) \right) \quad \text{unitarity} \rightarrow \quad \begin{aligned} V_{\text{CKM}} V_{\text{CKM}}^\dagger &= \mathbf{1} \\ \sum_{i=1}^3 V_{ij} V_{ik}^* &= 0, j \neq k \end{aligned}$$

relevant relation for B meson decays

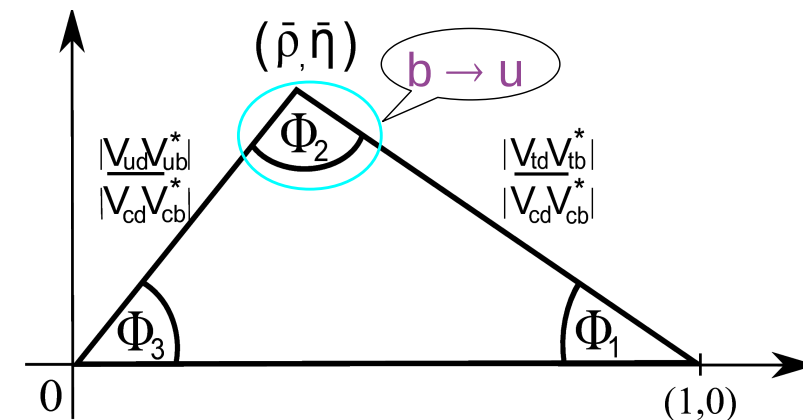
$$\begin{aligned} V_{ud} V_{ub}^* &+ V_{cd} V_{cb}^* &+ V_{td} V_{tb}^* &= 0 \\ \mathcal{O}(\lambda^3) &\quad \mathcal{O}(\lambda^3) &\quad \mathcal{O}(\lambda^3) \end{aligned}$$

can be represented as a triangle in the complex plane $\rightarrow$

sides with similar length $\Rightarrow$ large **CP violation**

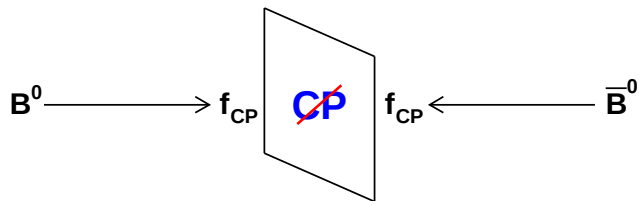
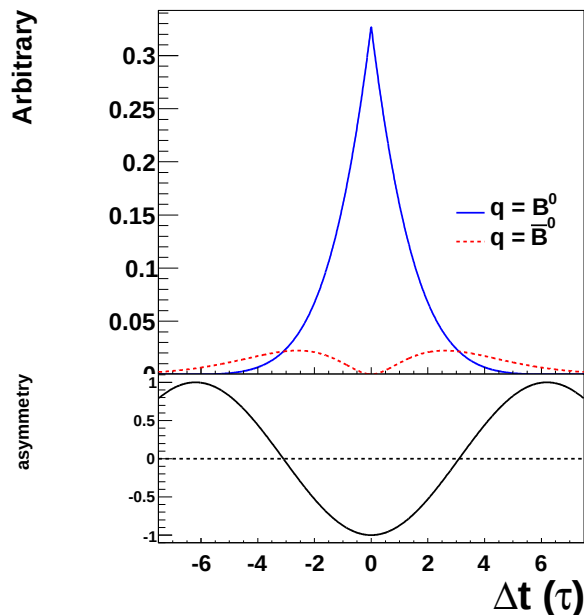
5 observables (3 angles, 2 sides) $\Rightarrow$ over-constraint

confirm SM **or** find new physics



CP Violation in the B System

$$\frac{N_{\bar{B}^0}(\Delta t, f_{CP}) - N_{B^0}(\Delta t, f_{CP})}{N_{\bar{B}^0}(\Delta t, f_{CP}) + N_{B^0}(\Delta t, f_{CP})} = \mathcal{A}_{CP} \cos(\Delta m \Delta t) + \mathcal{S}_{CP} \sin(\Delta m \Delta t), \quad \Delta t = t' - t$$



CP asymmetry parameters:

$\leftarrow \mathcal{A}_{CP}(\text{direct } CP)$

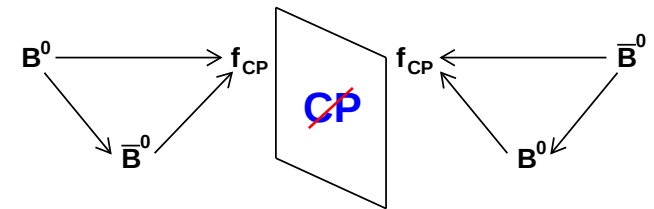
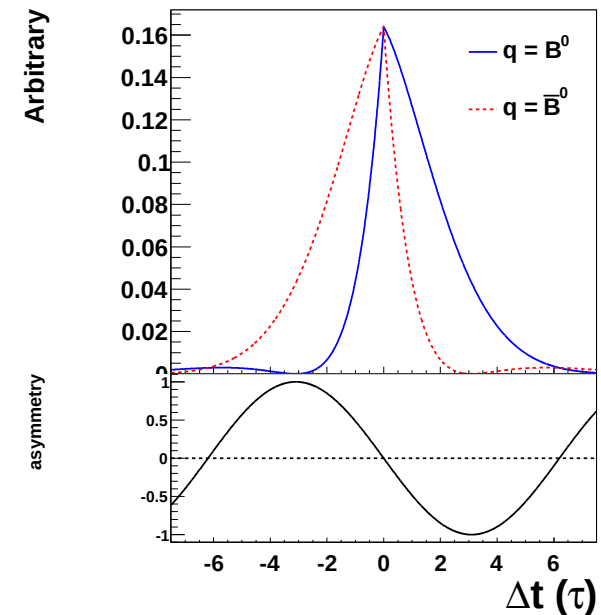
different decay rates

— and —

$\mathcal{S}_{CP}(\text{mix.ind. } CP) \rightarrow$

different time evolution

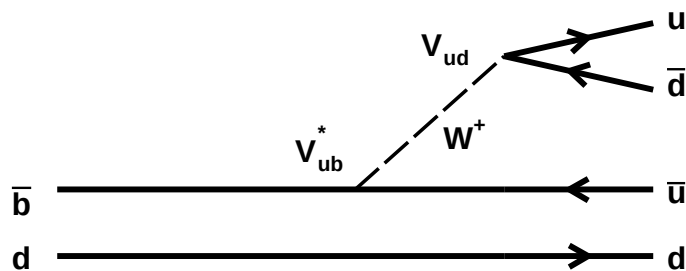
for B and $\bar{B}$ decaying into a CP eigenstate f_{CP}



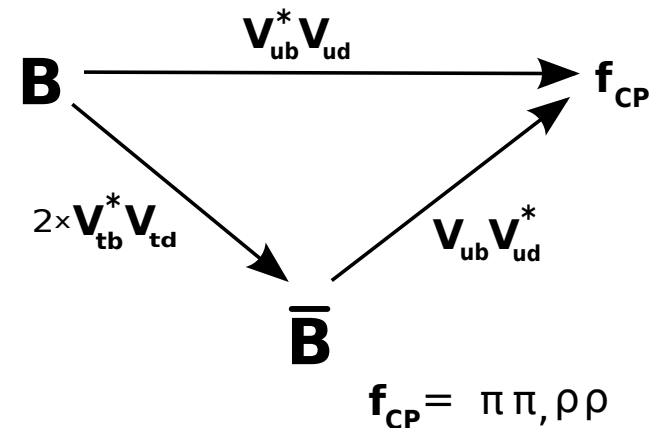
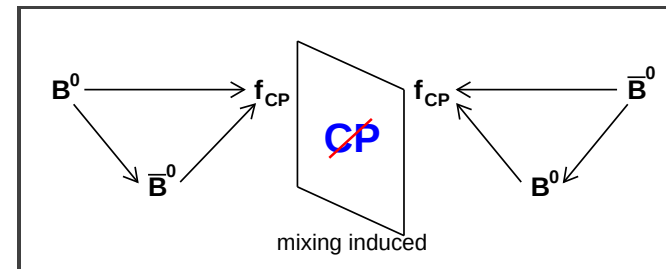
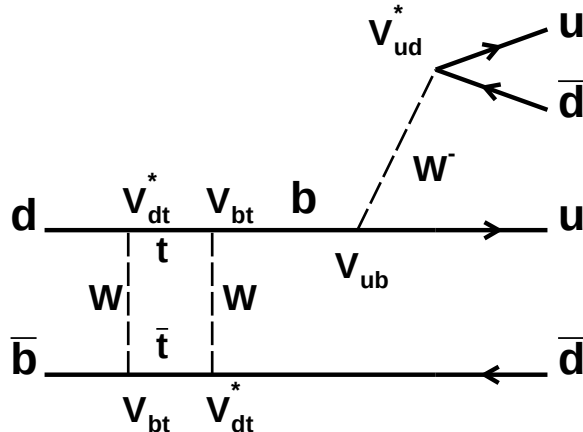
ϕ_2 and Mixing Induced ~~CP~~

- $\phi_2 = \arg\left(\frac{V_{td}V_{tb}^*}{V_{ub}V_{ud}^*}\right)$ accessible through mixing induced ~~CP~~ in $b \rightarrow u$ transitions,

e.g. interference between $B \rightarrow \rho^+ \rho^-$



and $B \rightarrow \bar{B} \rightarrow \rho^+ \rho^-$



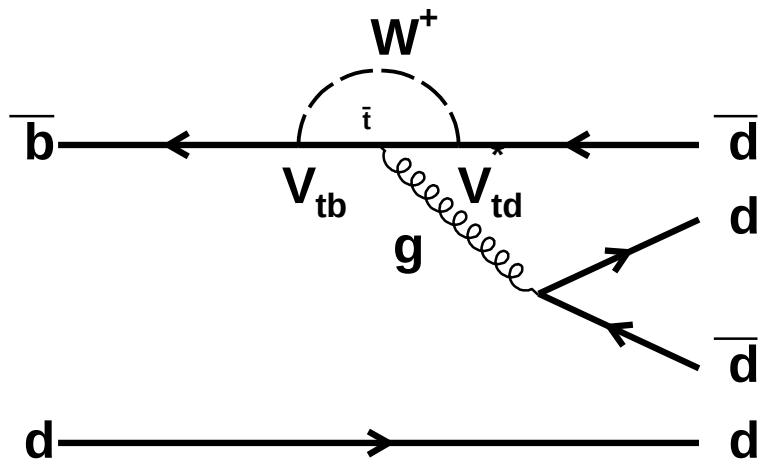
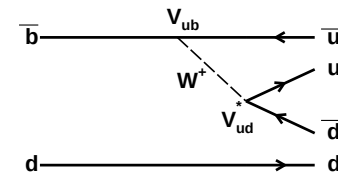
$\Rightarrow$ at tree level:

$$\mathcal{S}_{CP} = \sin(2\phi_2), \quad \mathcal{A}_{CP} = 0$$

Penguin Pollution

At tree level: $\mathcal{S}_{CP} = \sin(2\phi_2)$ and $\mathcal{A}_{CP} = 0$.

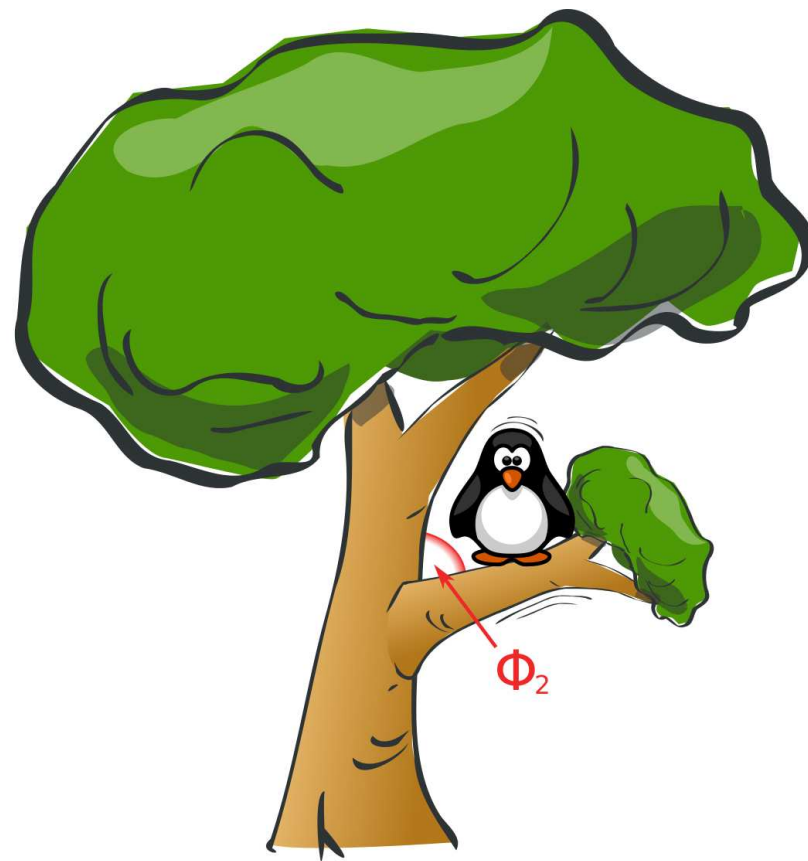
BUT more amplitudes (penguins) can contribute



penguin pollution $\Rightarrow \Delta\phi_2, \mathcal{A}_{CP}$

$\Rightarrow$ measured observable $\phi_2^{eff} = \phi_2 + \Delta\phi_2$

and $\mathcal{A}_{CP} \neq 0$ possible



How the penguin distorts the tree level measurement

Recover ϕ_2

- **extraction of $\Delta\phi_2$ with isospin analysis** (remove penguin pollution) $\phi_2^{eff} = \phi_2 + \Delta\phi_2$

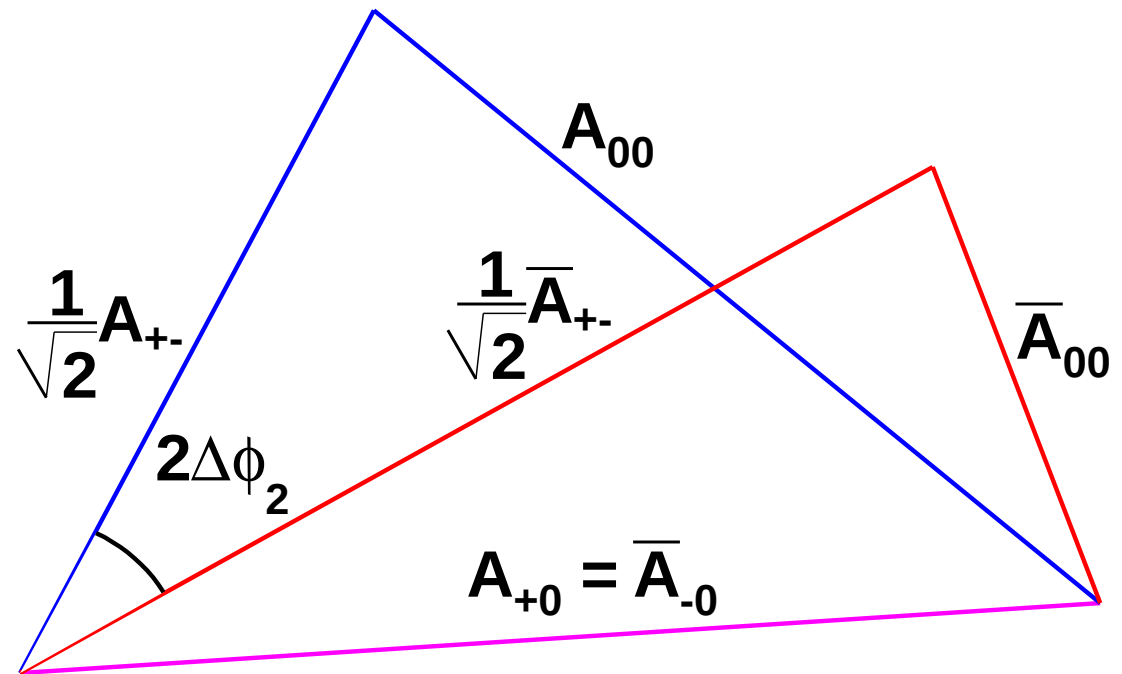
for unflavored isospin triplets, e.g. ρ, π

Bose statistics: $\Rightarrow l=0,2$ (final states);

- tree $l=0,2$;
- penguin: $l=0$ only (gluon; $l=0$)

allows to formulate relations of the decay amplitudes A

e.g. $\bar{A}^{+-} = \mathcal{A}(\bar{B} \rightarrow \rho^+ \rho^-)$

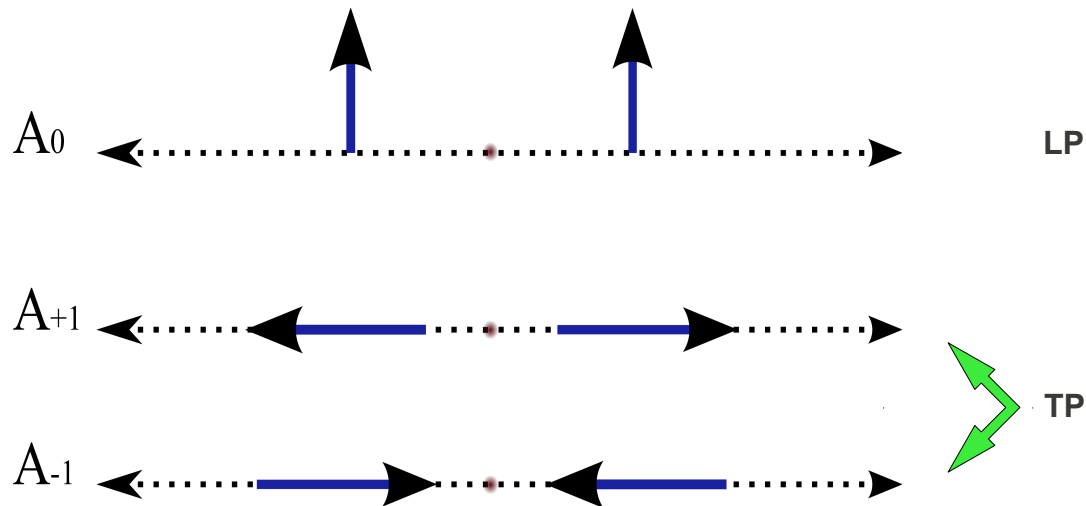


- $\frac{1}{\sqrt{2}}A^{+-} + A^{00} = A^{+0}$
- $\frac{1}{\sqrt{2}}\bar{A}^{+-} + \bar{A}^{00} = \bar{A}^{-0}$
- $A^{+0} = \bar{A}^{-0}$ (no penguin)

$\Rightarrow$ geometrical considerations reveal $\Delta\phi_2$

$B \rightarrow VV$

scalar $\rightarrow$ vector vector ($\rho : J^{PC} = 1^{--}$) $\Rightarrow$ three different polarization amplitudes



- $A_0 \rightarrow$ longitudinal(LP):
pure CP eigenstates
 $\eta_{CP} = +1$
- $A_{\pm 1} \rightarrow$ transversal(TP):
mixture of CP even and odd states
 $\eta_{CP} = +1, -1$

SM: LP dominant, $f_L \sim 1 - (m_V^2/m_B^2) \sim 1$

fraction of LP:
$$f_L = \frac{|A_0|^2}{\sum |A_i|^2}$$

$$\mathcal{S}_{CP} = \eta_{CP} \sin(2\phi_2^{\text{eff}})$$

measure $f_L \Rightarrow$ separate longitudinal (CP -even) and transverse (CP -even&odd) polarization

Measuring ϕ_2

In $b \rightarrow u$ transitions (e.g. $B \rightarrow \pi\pi, \rho\rho, \dots$)

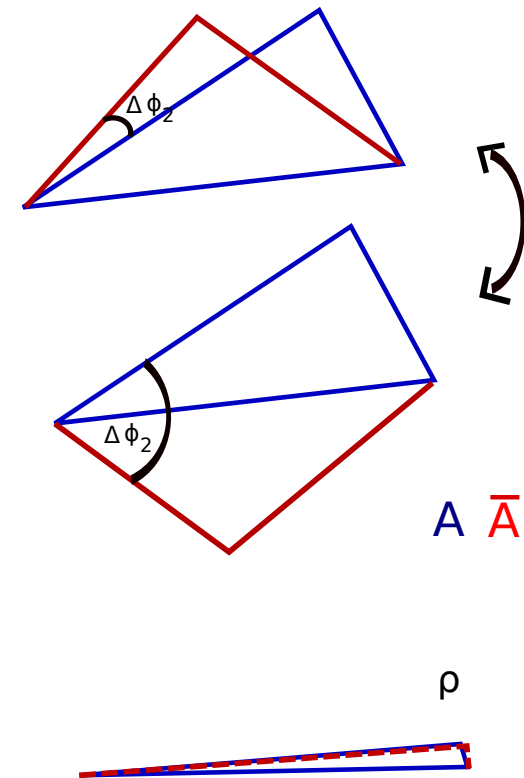
- measurement of $\Delta t, q$ provides $\sin(2\phi_{2,eff}) = \sin(2(\phi_2 + \Delta\phi_2))$
- extraction of $\Delta\phi_2$ through isospin analysis possible
but $2(\sin) \times 4(\Delta\phi_2) = 8$ fold ambiguity

In the $B \rightarrow \rho\rho$ system the SM predicts small penguin pollution

- ϕ_2 from $B^0 \rightarrow \rho^+ \rho^-$ (LP only)
- $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$ relatively very small
multiple solutions due to $\Delta\phi_2$ overlap $\Rightarrow$ only 2 fold ambiguity
- current error on ϕ_2 dominated by the ρ system

Need: **Branching Fractions, f_L and CPV parameters of:**

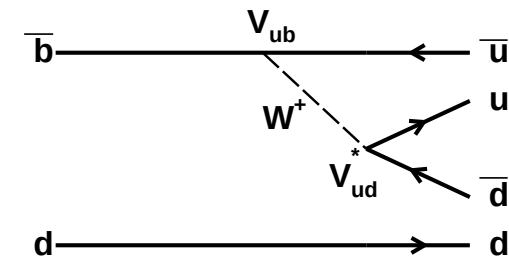
$B^0 \rightarrow \rho^+ \rho^-$, $B^0 \rightarrow \rho^0 \rho^0$ and $B^+ \rightarrow \rho^+ \rho^0$



Previous Measurements

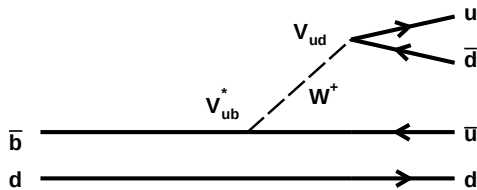
Experiment	BELLE	BaBar
$\mathcal{BR}(\times 10^{-6})$	$0.4 \pm 0.4 \pm 0.25$	$0.92 \pm 0.32 \pm 0.14$
f_L	1(assumed)	$0.75 \pm 0.11 \pm 0.04$
$\mathcal{A}_{CP}^L$	-	$-0.2 \pm 0.8 \pm 0.3$
$\mathcal{S}_{CP}^L$	-	$0.3 \pm 0.7 \pm 0.2$
$B\bar{B}$ pairs ($\times 10^6$)	656.7	465

$B^0 \rightarrow \rho^0 \rho^0$ (color-suppressed)



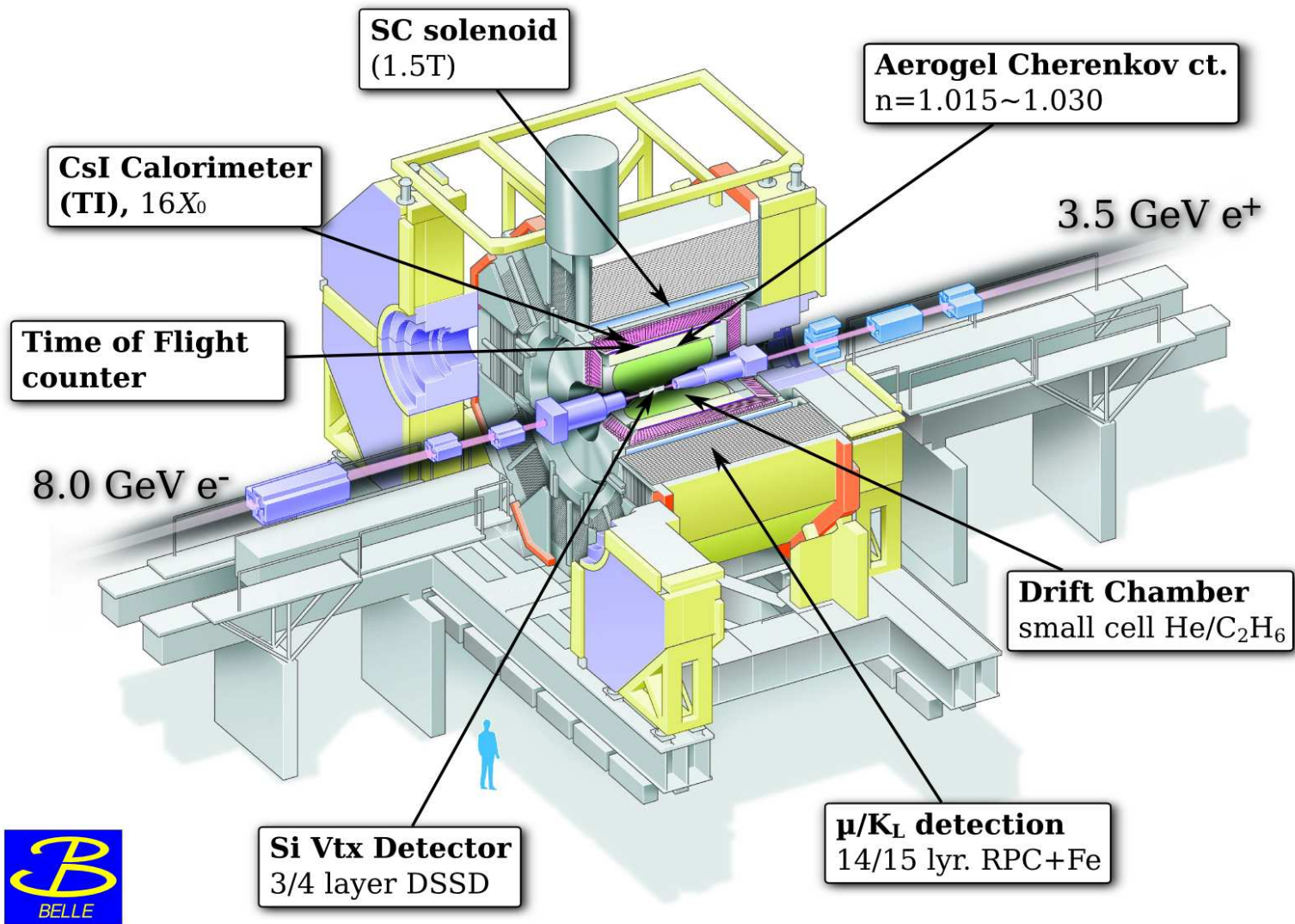
————— two independent measurements —————

$B^0 \rightarrow \rho^+ \rho^-$



Experiment	BELLE	BaBar
$\mathcal{BR}(\times 10^{-6})$	$22.8 \pm 3.8^{+2.3}_{-2.6} (*)$	$25.5 \pm 2.1^{+3.6}_{-3.9}$
f_L	$0.941^{+0.034}_{-0.040} \pm 0.030 (*)$	$0.992 \pm 0.024^{+0.026}_{-0.013}$
$\mathcal{A}_{CP}^L$	$0.16 \pm 0.21 \pm 0.08$	$-0.01 \pm 0.15 \pm 0.06$
$\mathcal{S}_{CP}^L$	$0.19 \pm 0.30 \pm 0.08$	$-0.17 \pm 0.20^{+0.05}_{-0.06}$
$B\bar{B}$ pairs ($\times 10^6$)	$535^{(*)} 200)$	384

The Experimental Setup



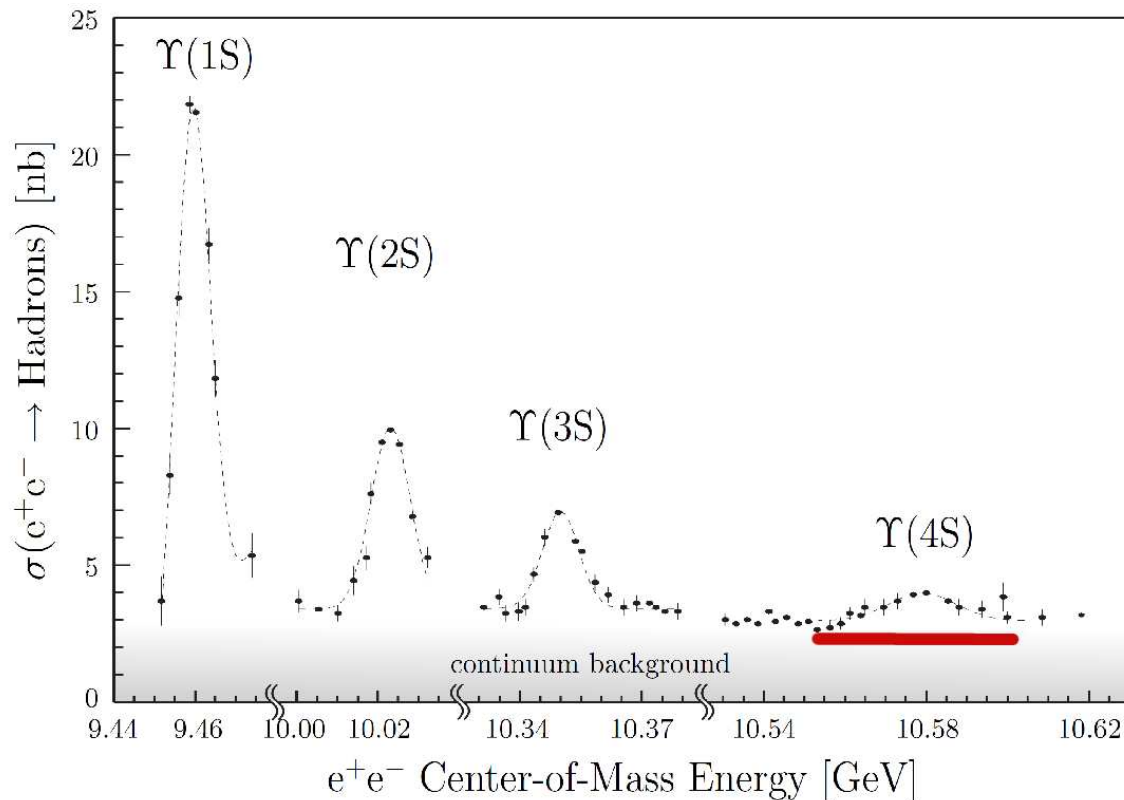
- located in Japan
- asymmetric e^+e^- collider (KEKB)
(3.5 GeV on 8 GeV)
- luminosity world-record
 $\int L dt = 1014 fb^{-1}$
 $\sim 772 \times 10^6 B\bar{B}$ pairs

Belle Detector

- tracking
- PID



Where the B s come from



$$m(\Upsilon(4S)) = 10.58 \text{ GeV}/c^2 \sim 2 \times m(B)$$

$$m(B) = 5.28 \text{ GeV}/c^2$$

- Υ states: $b\bar{b}$ bound states
- $\Upsilon(4S)$ exclusively into $B\bar{B}$ pairs
- $\Upsilon(4S)$: $J^{PC} = 1^{--}$
- B : $J^{PC} = 0^{--}$
 $\rightarrow B$ pair in p-wave
- asymmetric wave function
 $\rightarrow B$ s have opposite flavor:

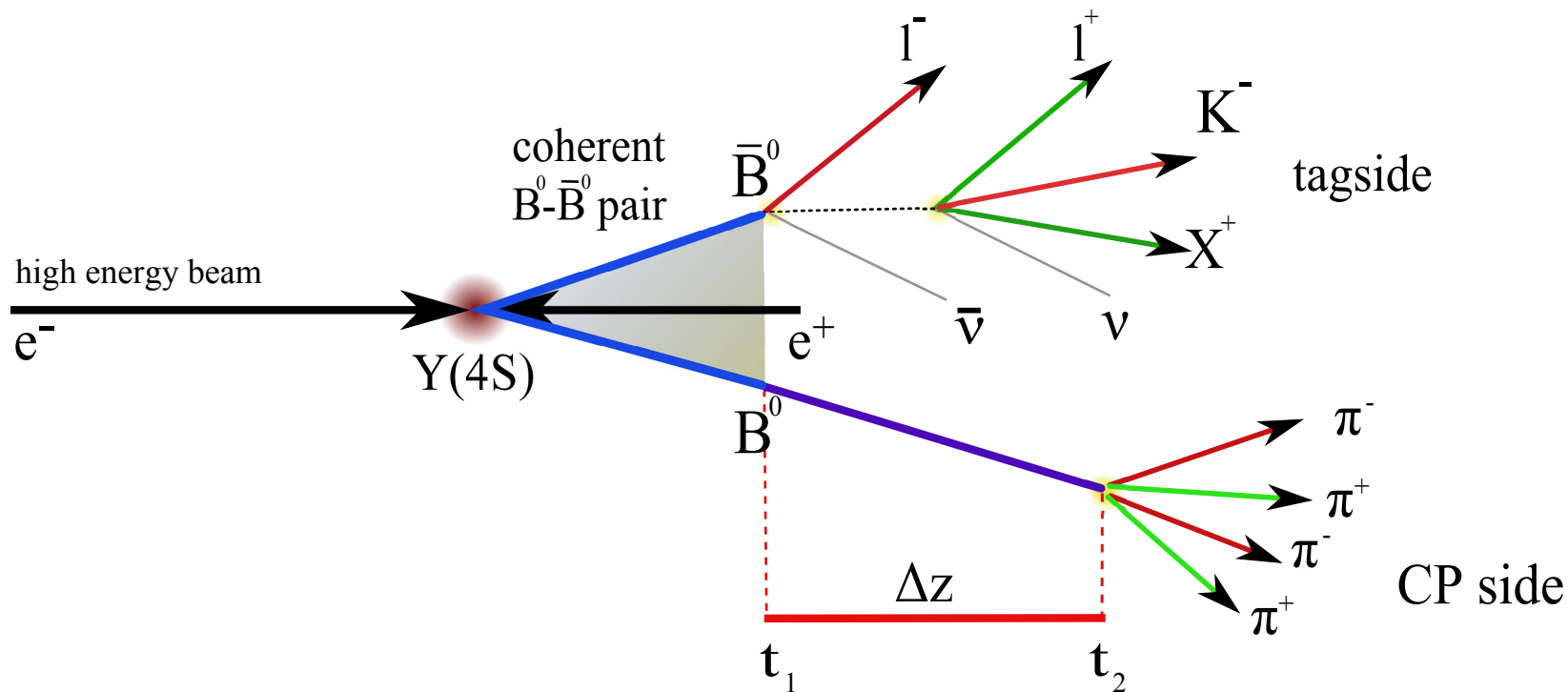
continuum: $e^+e^- \rightarrow q\bar{q}$
 (u,d,s,c)

gives large contribution

CP Violation Measurement

different decay time-dependency for B and $\bar{B}$ decaying into a CP eigenstate

$$\frac{N_{\bar{B}^0}(\Delta t, f_{CP}) - N_{B^0}(\Delta t, f_{CP})}{N_{\bar{B}^0}(\Delta t, f_{CP}) + N_{B^0}(\Delta t, f_{CP})} = \mathcal{A}_{CP} \cos(\Delta m \Delta t) + \mathcal{S}_{CP} \sin(\Delta m \Delta t)$$

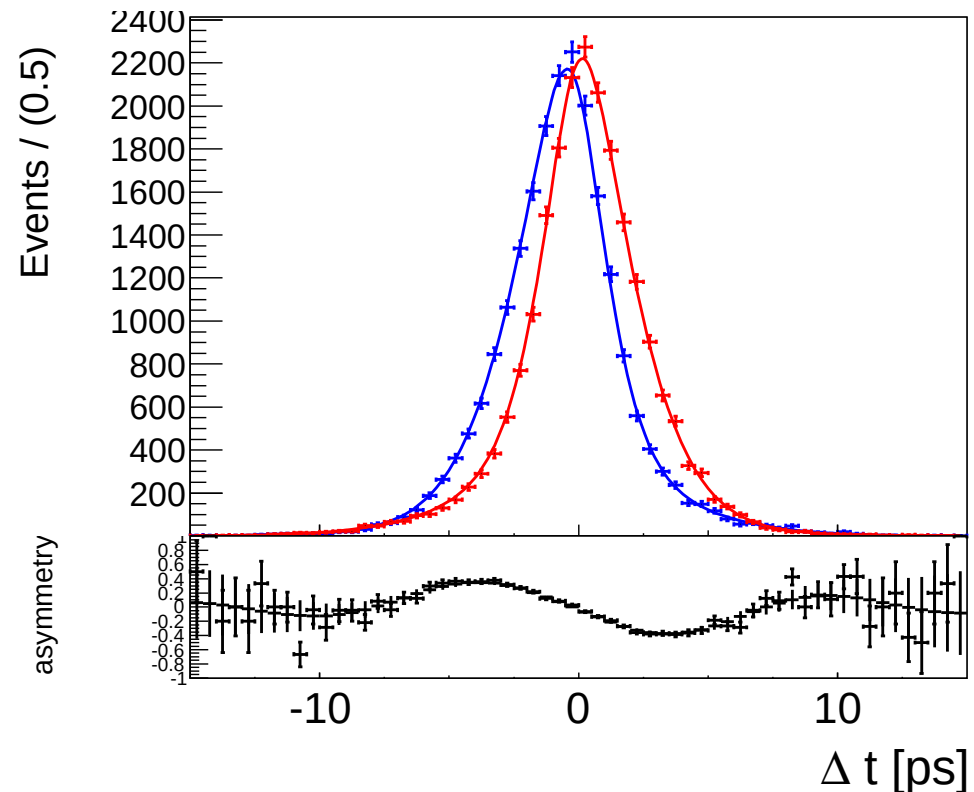


- $\Upsilon(4S) \rightarrow$ entangled $B\bar{B}$ pair ($\sim$ at rest in CMS) $\Rightarrow$ opposite side flavor tagging possible
- asymmetric beam energies $\Rightarrow$ boost of the CMS $\Rightarrow \Delta t \rightarrow \Delta z$ ($\Delta t \sim 1.5ps$, $\Delta z \sim 100\mu m$)

Δt

$$\Gamma(\Delta t, q) = \frac{e^{-\Delta t/\tau_B}}{4\tau_B} \left(1 + (1 - 2w_l)q[\mathcal{S}_{CP} \sin(\Delta t \Delta m_d) + \mathcal{A}_{CP} \cos(\Delta t \Delta m_d)] \right)$$

- tagging eff: $\sim 30\%$
(dominant dilution from misPID)
- wrong tag fraction included as a binned dilution factor $1 - 2w_l$
- convoluted with **resolution fct.**
 - a) detector resolution
 - b) smearing due to non primary tag-side tracks
 - c) kinematic approx.,



signal MC: $\phi_2^{\text{generated}} = 45^\circ \Rightarrow \mathcal{S}_{CP} = 1$

Helicity Measurement

separate longitudinal(CP even) and transversal(CP even & odd) states

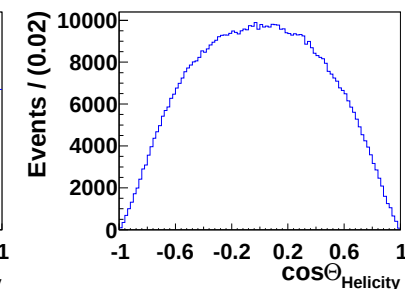
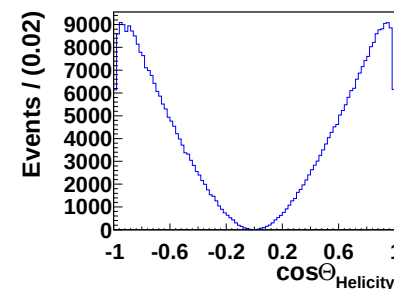
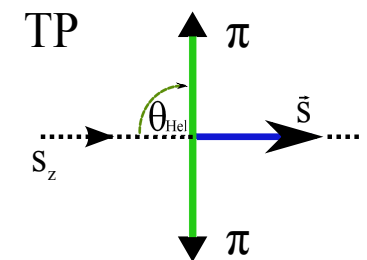
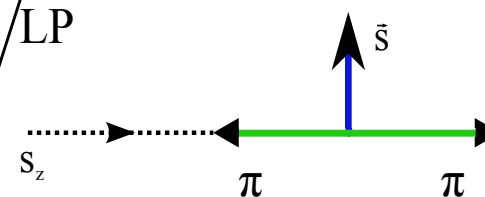
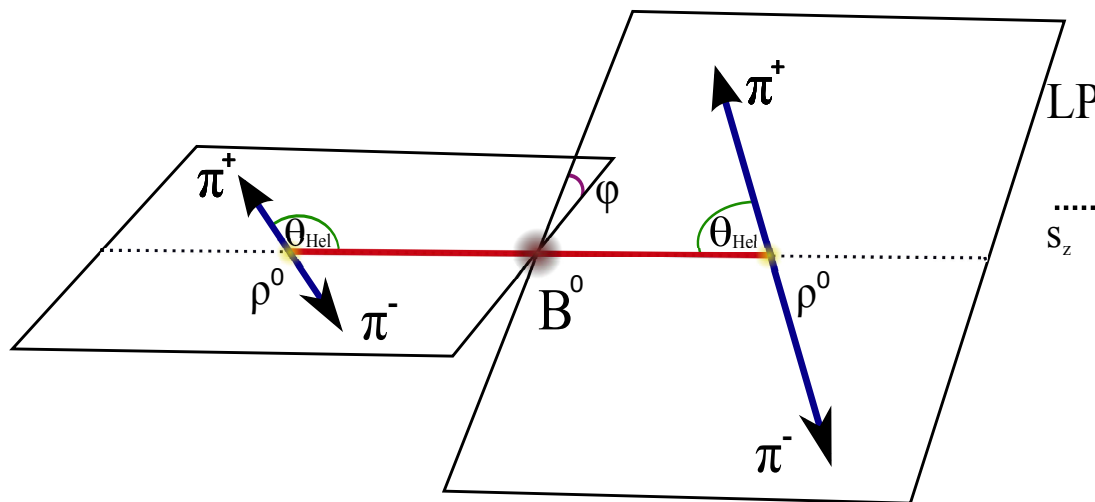
consider two signal components, fit $\cos(\theta_{Hel}) \rightarrow f_L$ (fraction of LP)

- e.g. for $B \rightarrow \rho^0 \rho^0$

$$J^{CP}: \rho^0 = 1^{--} ; \pi^\pm = 0^-$$

$$\rho^0 \rightarrow \pi^+ \pi^-$$

θ_{Hel} : angle between the B^0 and the π^+ flight directions in the ρ frame



Reconstruction of $(B^0 \rightarrow \rho\rho)$

combine particles seen by detector

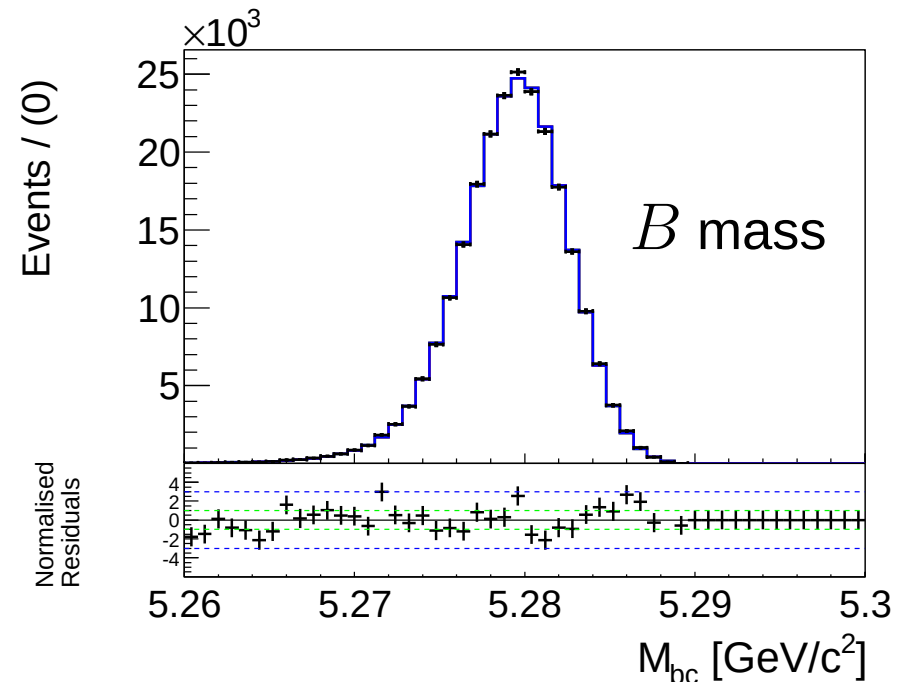
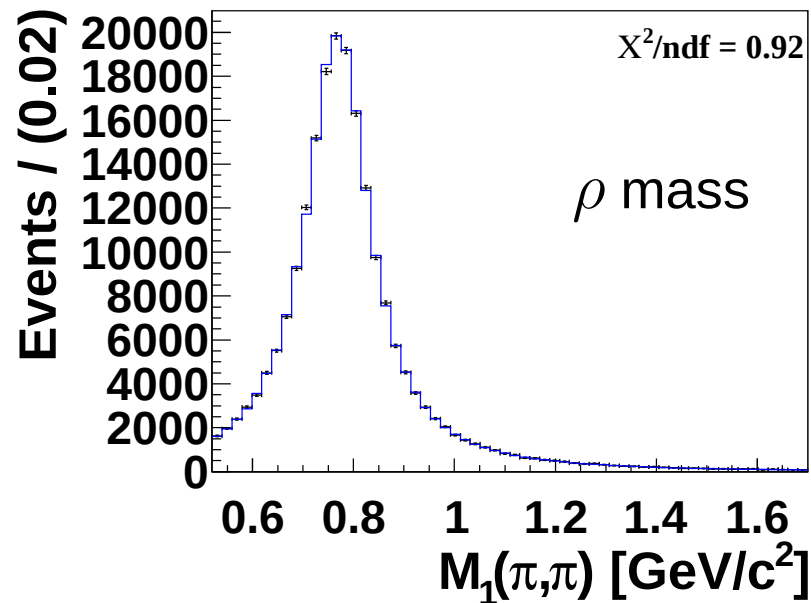
$$B^0 \rightarrow \rho^0 \rho^0$$

$$\rho^0 \rightarrow \pi^+ \pi^-$$

$$B^0 \rightarrow \rho^+ \rho^-$$

$$\rho^\pm \rightarrow \pi^\pm \pi^0$$

$$\pi^0 \rightarrow \gamma\gamma$$



$$M_{bc} \equiv \sqrt{E_{beam}^2 - \vec{p}_{B_{rec}}^2}$$

$\rho : m_0 \sim 770 \text{ MeV}, \Gamma \sim 150 \text{ MeV}$

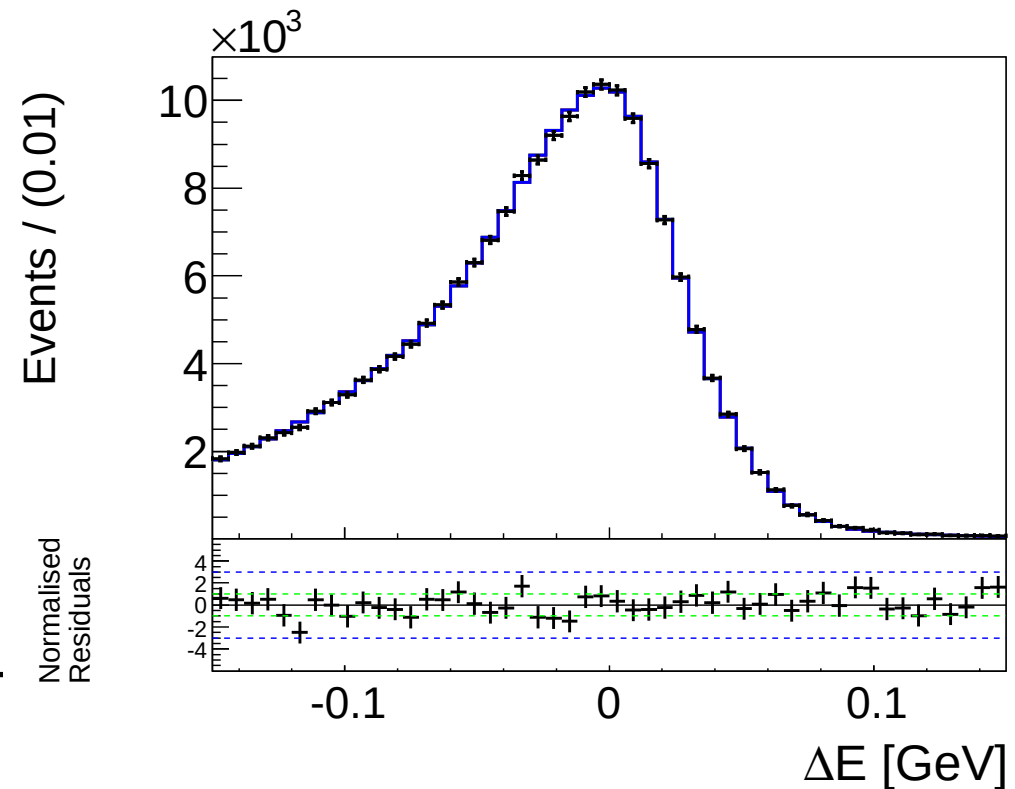
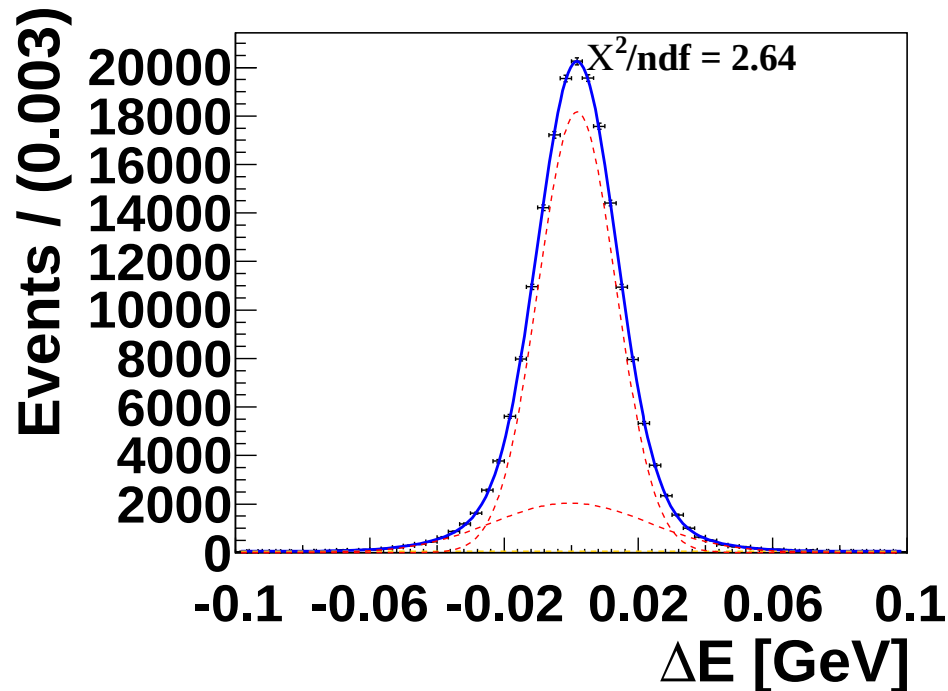
What a difference two π^0 s make

$$\Delta E \equiv E_{B_{rec}} - E_{beam}$$

$$(\pi^0 \rightarrow \gamma\gamma)$$

• signal MC: $B^0 \rightarrow \rho^0 \rho^0$

$$B^0 \rightarrow \rho^+ \rho^-$$



$$4\pi^\pm$$

$$2\pi^\pm, 2\pi^0$$

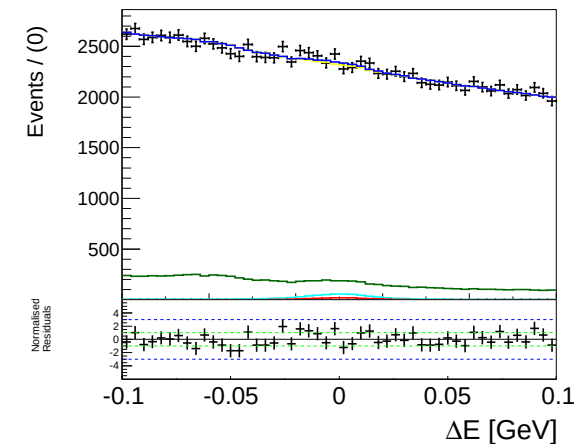
Separate Signal from Background

multivariate (blind) analysis

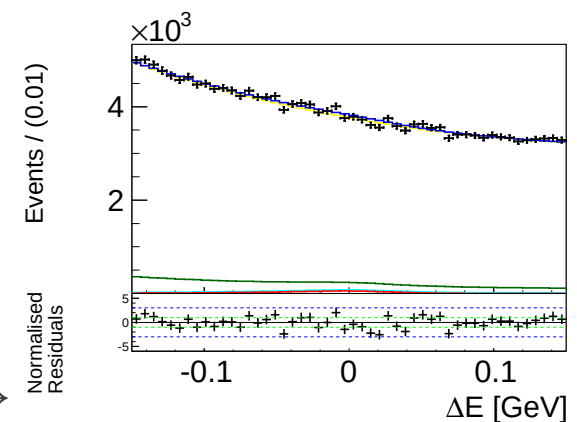
- rare B decays are extremely BKG dominated: several sources
 - continuum: $e^+e^- \rightarrow q\bar{q}$, $q = u, d, s, c$ dominant
 - B decays with same final state: e.g. $B \rightarrow \pi\pi\pi\pi, \rho\pi\pi, \dots$
 - interference needs to be considered!! (here systematics)
 - combinatorial BKG from other B decays
- hard cuts destroys also signal yield (**rare decays**)
 - ⇒ multidimensional fit:
 - (6D for $B \rightarrow \rho^0\rho^0$ and 8D for $B \rightarrow \rho^+\rho^-$)
- consider each background separately
 - (17 for $B \rightarrow \rho^0\rho^0$ and even more for $B \rightarrow \rho^+\rho^-$)
- ⇒ simultaneous fit of $\mathcal{B}$, f_L (and CPV parameters for $B \rightarrow \rho^+\rho^-$)

full projection:

$B \rightarrow \rho^0\rho^0$ (data)

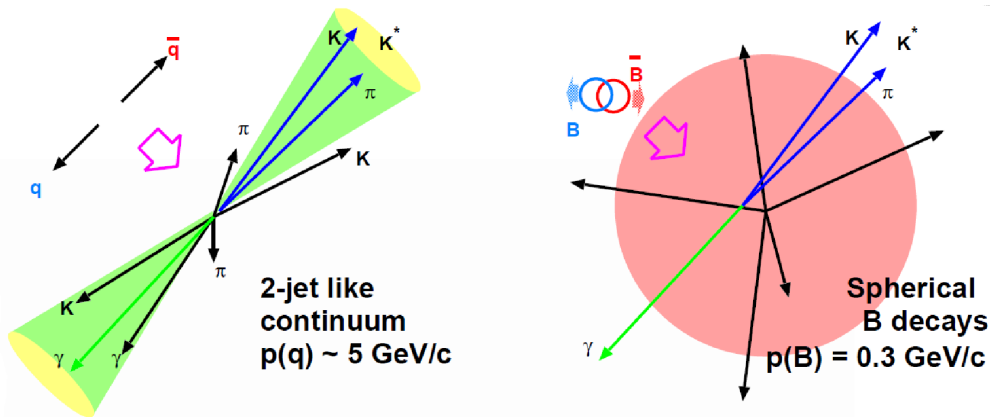


$B \rightarrow \rho^+\rho^-$ (MC)

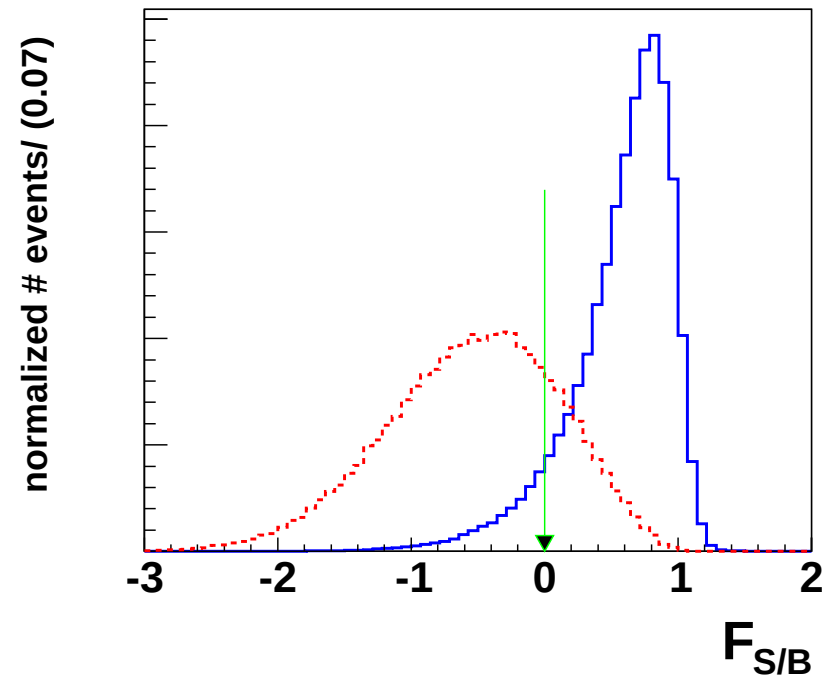


Continuum Identification

- $e^+e^- \rightarrow q\bar{q}$, ($q = u, d, s, c$) gives biggest contribution ($N_{q\bar{q}}/N_{sig} \sim 1000$)
- combine $\mathcal{O}(10)$ eventshape-dependent variables with Fisher discriminant $\rightarrow \mathcal{F}_{S/B}$



- include $\mathcal{F}_{S/B}$ in fit and apply loose cut
 $\rightarrow$ reject $\sim 80\%$ $q\bar{q}$ events
 BUT still huge contribution



$B\bar{B}, q\bar{q}$; same normalisation

Result: $B^0 \rightarrow \rho^0 \rho^0$

6D fit to $\Delta E, \mathcal{F}_{S/B}, m_1(\pi^+\pi^-), m_2(\pi^+\pi^-), \cos \theta_{\text{Hel}}^1, \cos \theta_{\text{Hel}}^2$

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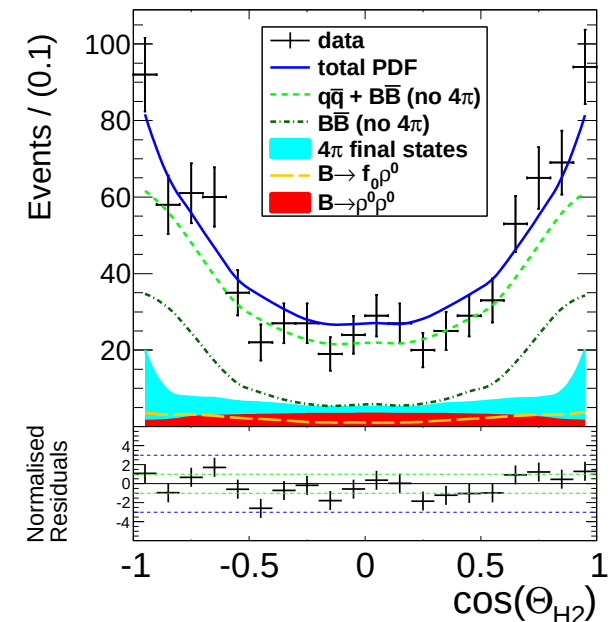
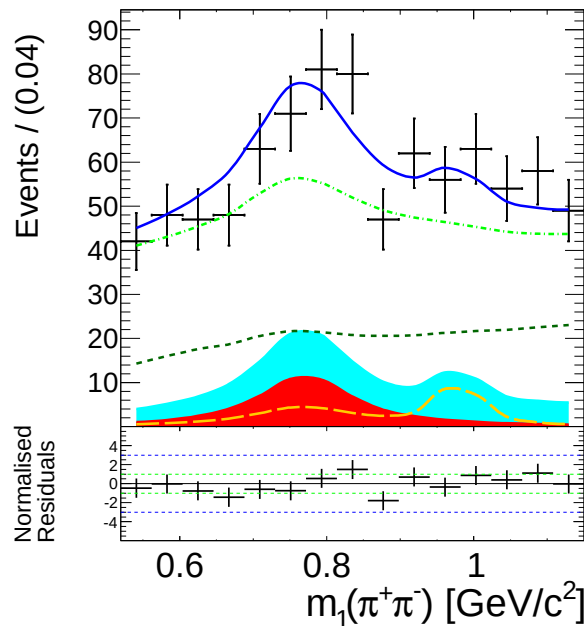
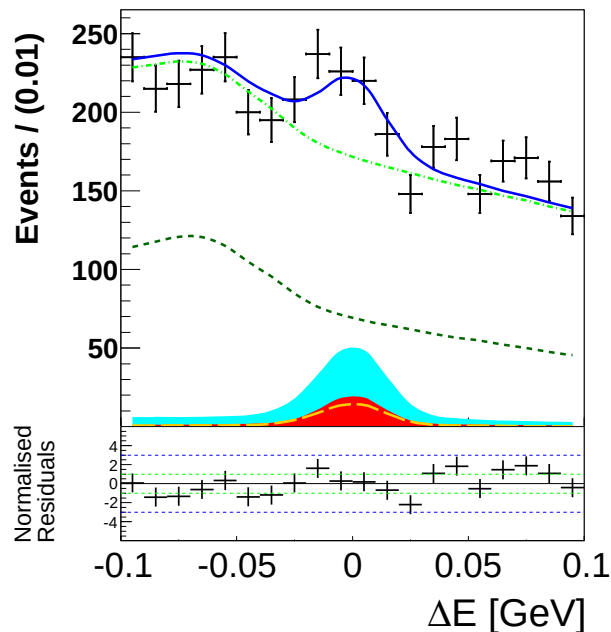
arXiv:1212.4015

$$\mathcal{B}(B^0 \rightarrow \rho^0 \rho^0) = (1.02 \pm 0.30 \pm 0.15) \times 10^{-6}, 3.4\sigma$$

$$f_L = 0.21_{-0.22}^{+0.18} \pm 0.15$$

also 1^{st} evidence of $B^0 \rightarrow f_0 \rho^0$ (3.1σ)

Signal enhanced projections

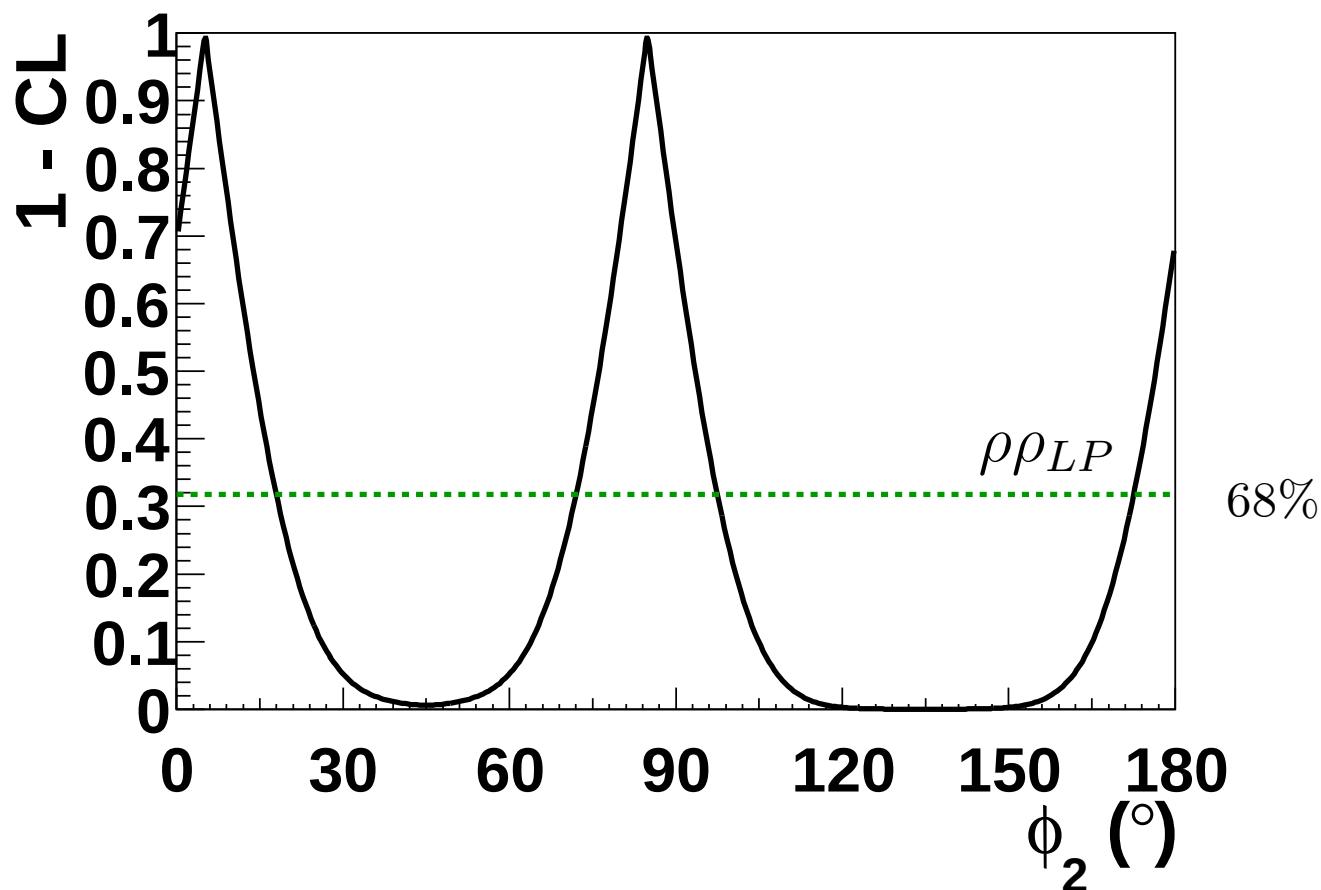


ϕ_2 from $B \rightarrow \rho\rho$ Decays

isospin analysis

inputs: Belle results

- $\mathcal{B}, f_L$ of
 $B^0 \rightarrow \rho^+ \rho^-$
 $B^0 \rightarrow \rho^0 \rho^0$
 $B^+ \rightarrow \rho^- \rho^0$
- $\mathcal{S}_{CP}, \mathcal{A}_{CP}$ of
 $B^0 \rightarrow \rho^+ \rho^-$

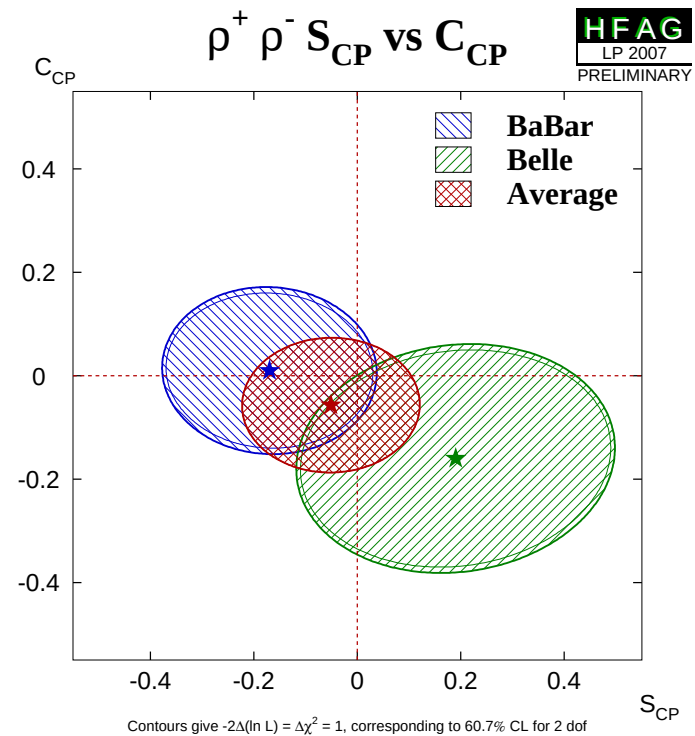
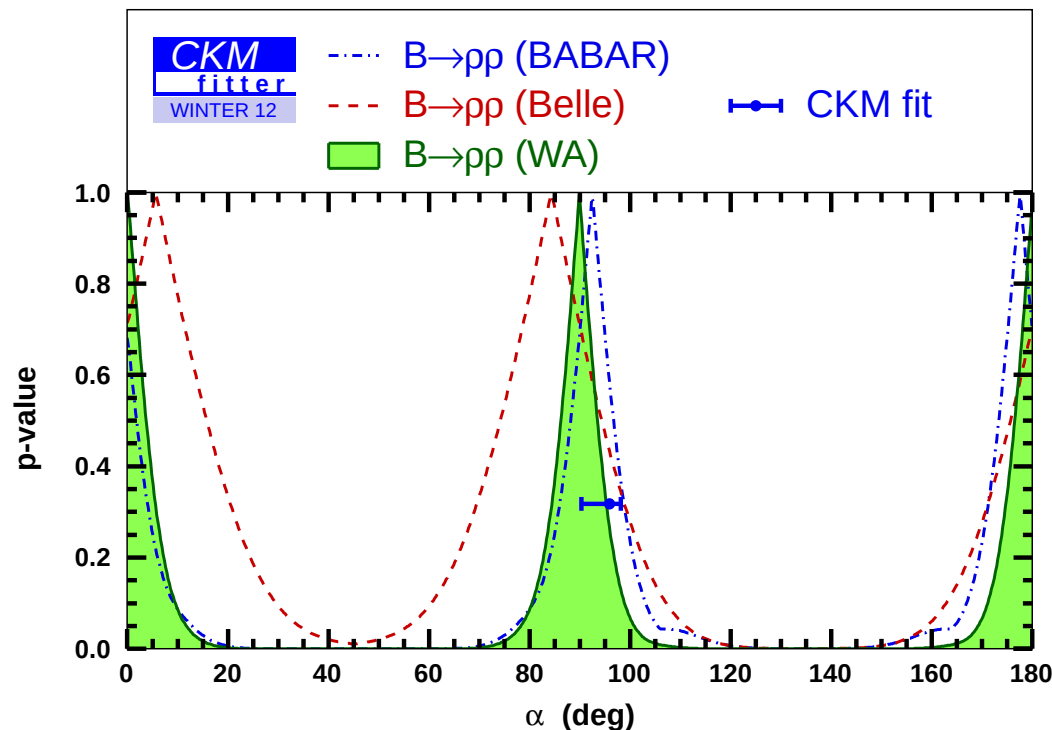


$$\phi_2 = (84.9 \pm 13.5)^\circ, \quad \Delta\phi_2 = (0 \pm 10.4)^\circ$$

arXiv:1212.4015

Comparison with BaBar

BaBar's uncertainty on $\phi_2(\alpha)$ ($\rho\rho$ system) $\sim 7^\circ$



Belle NEEDS UPDATES on $B^0 \rightarrow \rho^+ \rho^-$ and $B^+ \rightarrow \rho^+ \rho^0$!!

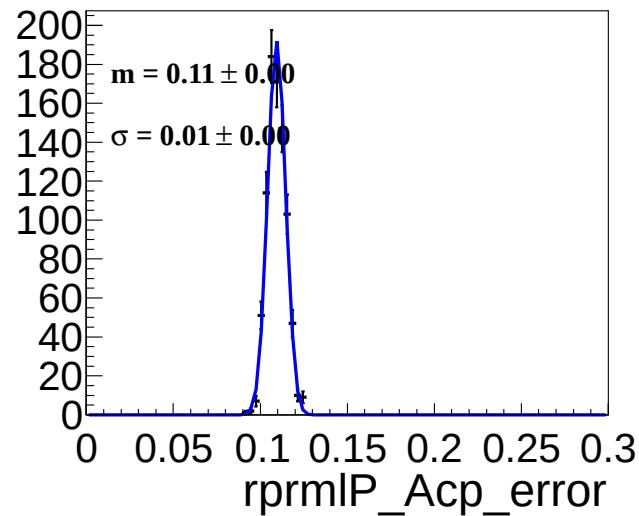
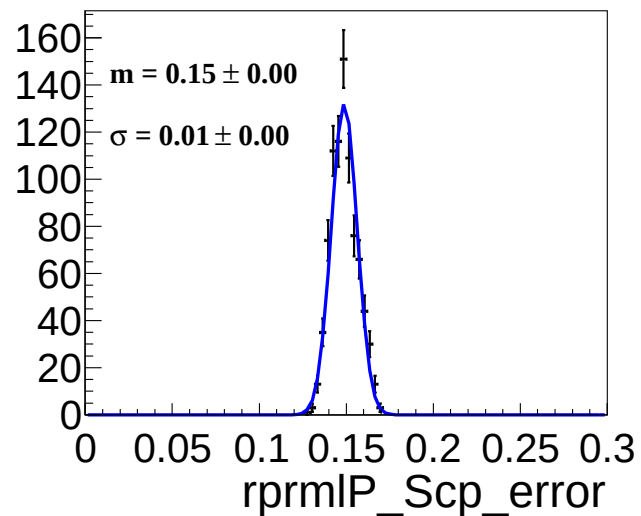
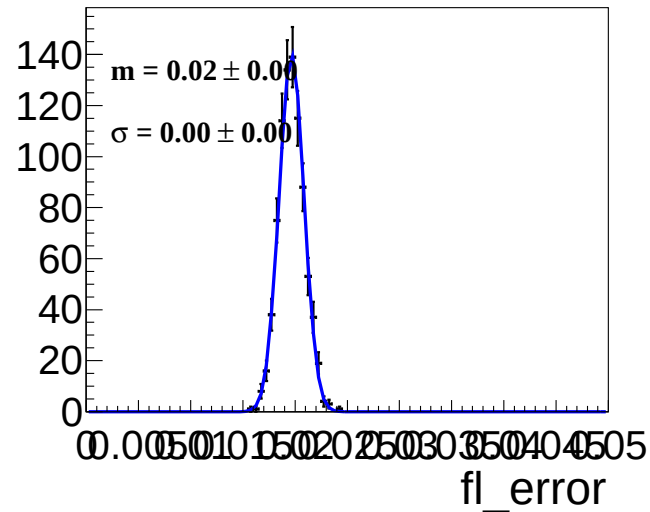
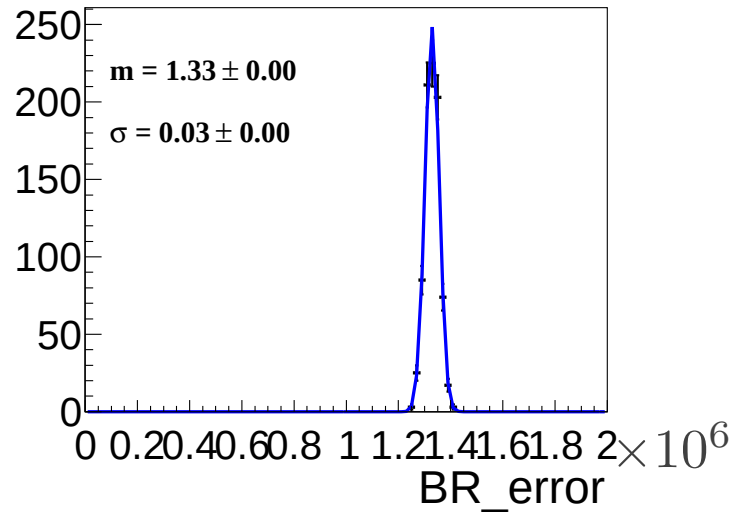
$$B \rightarrow \rho^{\pm} \rho^{\mp,0}$$

- previous measurements

Experiment	BELLE	BaBar
$\mathcal{BR}^{+-}(\times 10^{-6})$	$22.8 \pm 3.8^{+2.3}_{-2.6}$	$25.5 \pm 2.1^{+3.6}_{-3.9}$
f_L^{+-}	$0.941^{+0.034}_{-0.040} \pm 0.030$	$0.992 \pm 0.024^{+0.026}_{-0.013}$
$\mathcal{A}_{CP}^{+-}$	$0.16 \pm 0.21 \pm 0.07$	$-0.01 \pm 0.15 \pm 0.06$
$\mathcal{S}_{CP}^{+-}$	$0.19 \pm 0.30 \pm 0.07$	$-0.17 \pm 0.20^{+0.05}_{-0.06}$
$N_{B\bar{B}} \times 10^6$	535*	384
$\mathcal{BR}^{\pm 0}(\times 10^{-6})$	$31.7 \pm 7.1^{+3.8}_{-6.7}$	$23.7 \pm 1.4 \pm 1.4$
$f_L^{\pm 0}$	$0.948 \pm 0.106 \pm 0.021$	$0.950 \pm 0.015 \pm 0.006$
$\mathcal{A}_{CP}^{\pm 0}$	$0.00 \pm 0.22 \pm 0.03$	$0.054 \pm 0.055 \pm 0.010$
$N_{B\bar{B}} \times 10^6$	85	465

* : Belle only updated CP parameters; $\mathcal{BR}$, f_L from 275 $B\bar{B}$ pairs

Outlook



- 1st toyMC studies for $B \rightarrow \rho^+ \rho^-$
- MODEL NOT YET FINALIZED !!!

prev. BELLE
$\mathcal{BR}^{+-} (\times 10^{-6}) =$ $22.8 \pm 3.8^{+2.3}_{-2.6}$
$f_L^{+-} =$ $0.941^{+0.034}_{-0.040} \pm 0.030$
$\mathcal{A}_{CP}^{+-} =$ $0.16 \pm 0.21 \pm 0.07$
$\mathcal{S}_{CP}^{+-} =$ $0.19 \pm 0.30 \pm 0.07$

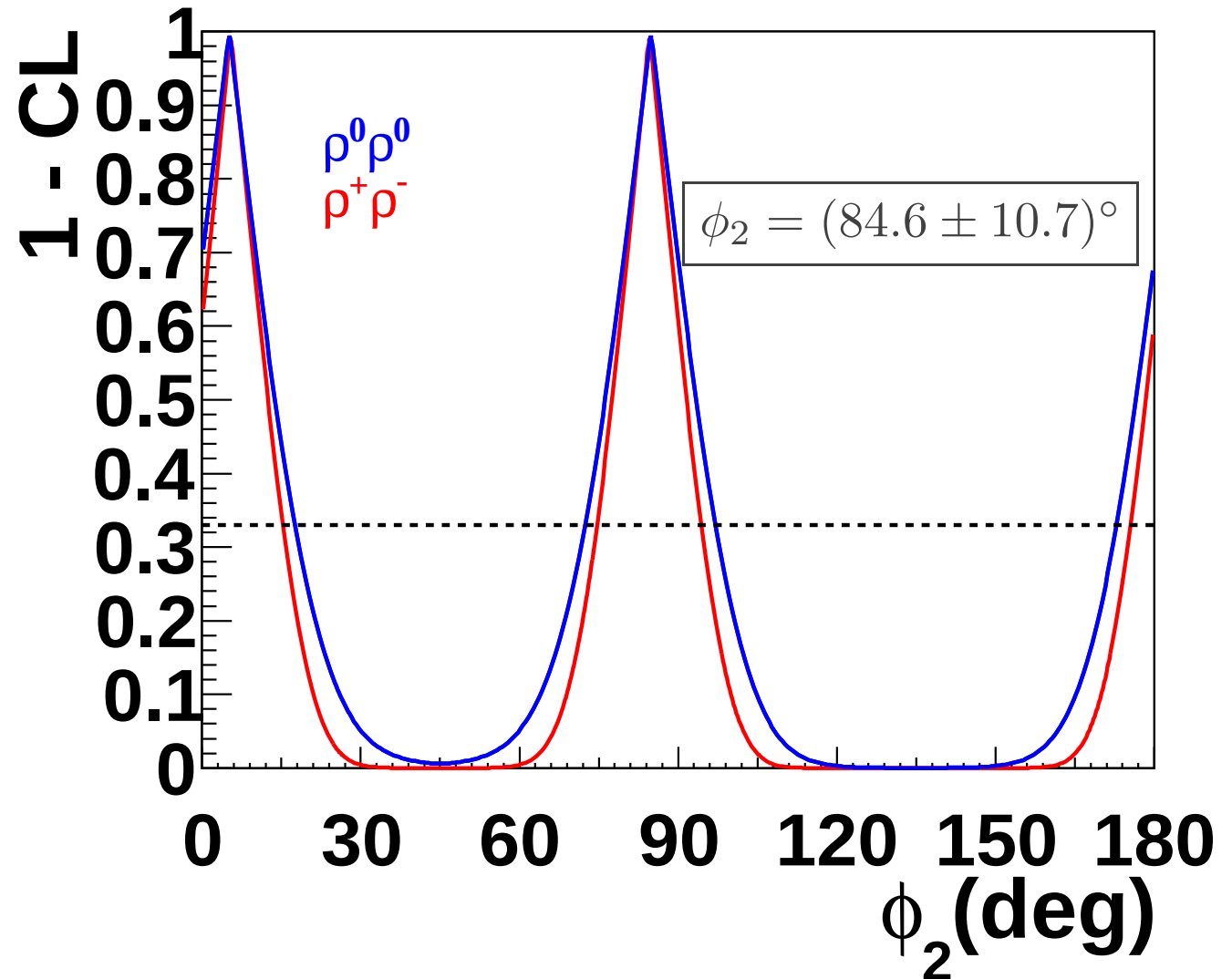
Outlook II

use expected errors for
 $B \rightarrow \rho^+ \rho^-$ in isospin
analysis

(see previous page)

$\mathcal{B}(B \rightarrow \rho^+ \rho^-)$ dom-
inated by syst. $\rightarrow \delta =$
 2.5×10^{-6}

mean values remain un-
changed

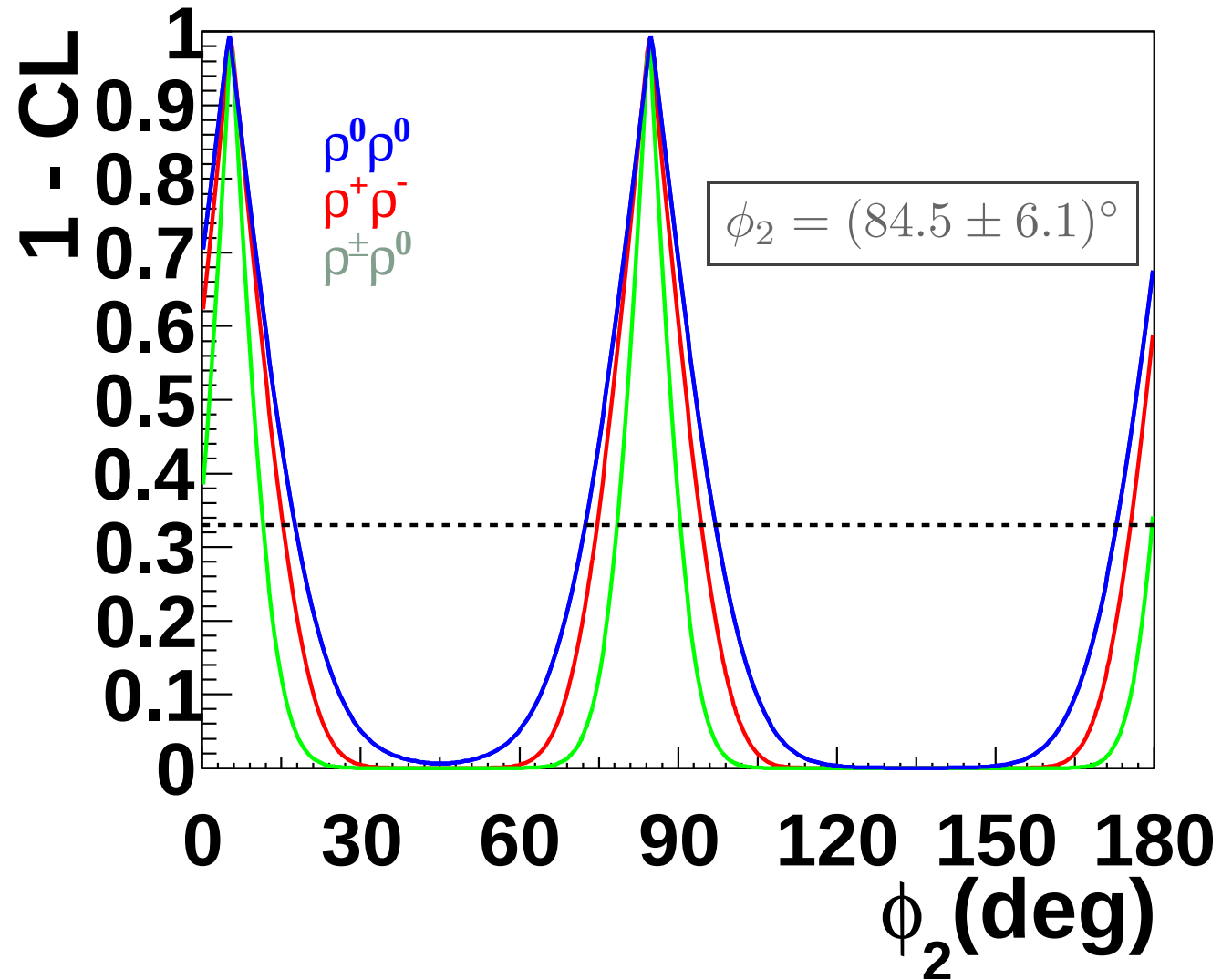


Outlook II

assume similar errors for
 $\mathcal{BR}(B^\pm \rightarrow \rho^\pm \rho^0)$ as
for $\mathcal{BR}(B \rightarrow \rho^+ \rho^-)$ in
isospin analysis

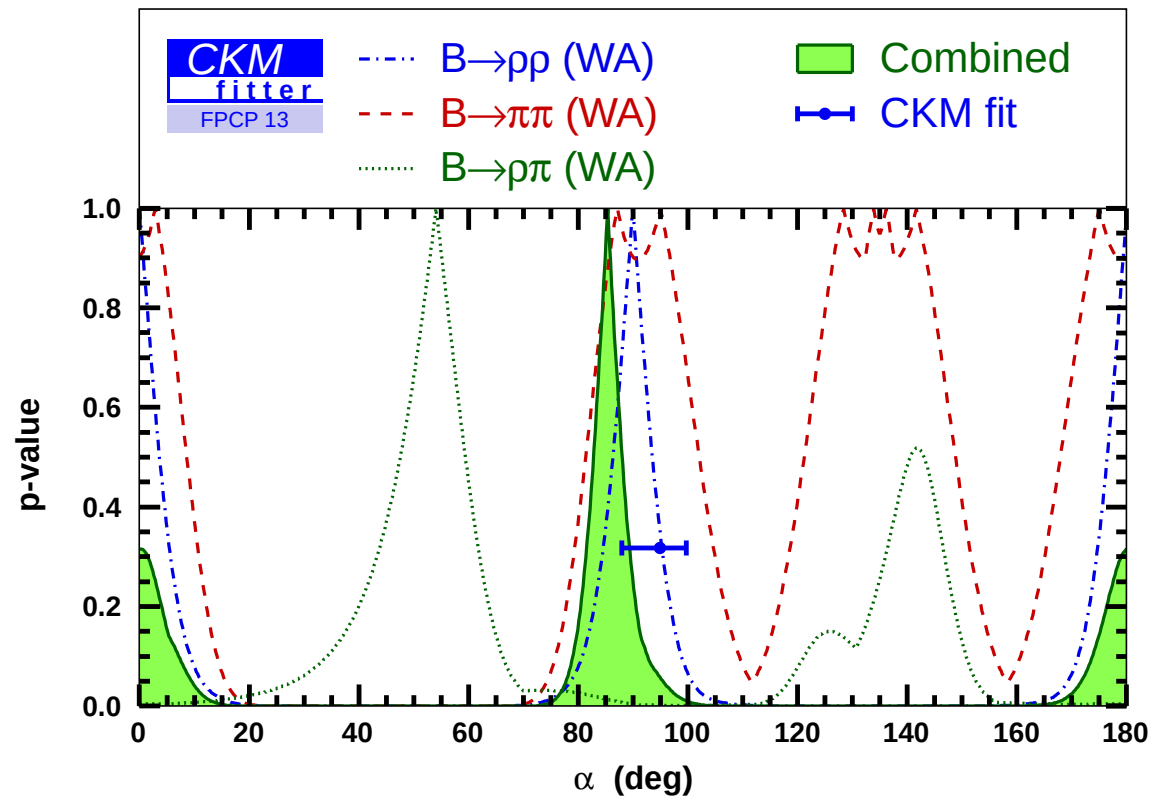
mean values remain un-
changed

This is how Belle's final
word on ϕ_2 from $B \rightarrow$
 $\rho\rho$ might look like



Current Status of ϕ_2

combine measurements from $B \rightarrow \pi\pi$, $B \rightarrow \rho\rho$ and $B \rightarrow \rho\pi$ $\phi_2 = (88.7^{+4.6}_{-4.2})^\circ$



Summary & Outlook

- presented measurement of $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$ (acc. by PRD)

$$\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0) = (1.02 \pm 0.30 \pm 0.15) \times 10^{-6}. \quad 3.4\sigma$$

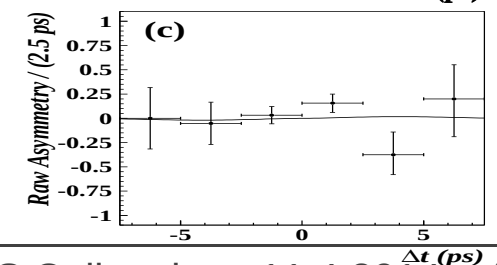
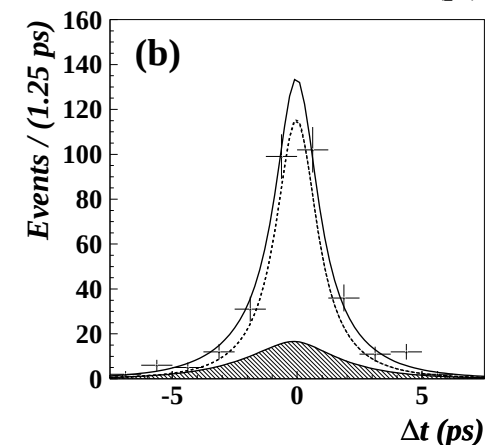
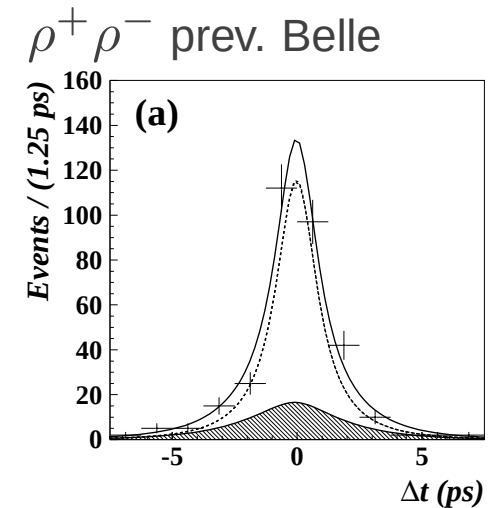
$$f_L = 0.21_{-0.22}^{+0.18}(\text{stat.}) \pm 0.15(\text{syst.})$$

- and used it in isospin analysis

$$\phi_2 = (84.9 \pm 13.5)^\circ$$

-
- currently working on the final update of $B^0 \rightarrow \rho^+ \rho^-$

→ measurement of branching fraction, polarization
and CP asymmetries.

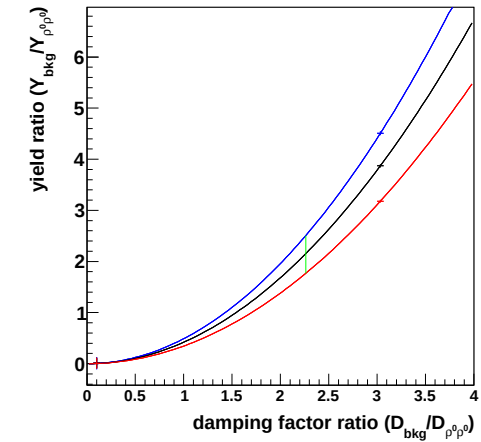


BACKUP

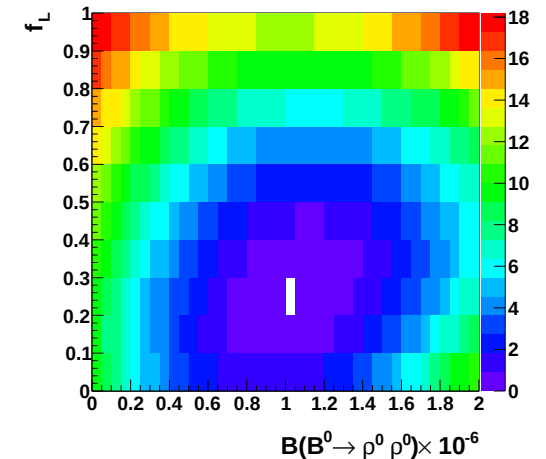
Systematic Uncertainties

Category	$\delta\mathcal{B}(B^0 \rightarrow \rho^0 \rho^0)$ (%)	δf_L
$N(B\bar{B})$	1.4	—
Tracking	1.4	—
Particle identification	2.5	—
Mis-reconstruction fraction	1.3	< 0.001
ρ^0 shape	0.2	< 0.001
Model shape	5.1	0.08
Histogram shape	5.2	0.03
$\mathcal{B}(B^0 \rightarrow a_1 \pi)$	0.4	0.03
$\mathcal{B}(B^0 \rightarrow b_1 \pi)$	< 0.1	< 0.001
$\mathcal{B}(B^0 \rightarrow a_2 \pi)$	< 0.1	< 0.001
Fit bias	1.9	0.03
Interference	19.2	0.03
$\rho^0 \pi \pi$ helicity	6.3	0.05
Total	22.0	0.11

interference with $a_1 \pi$



likelihood scan incl. syst.



$B \rightarrow VV$

naive SM predictions

amplitude ratios:

$$\mathbf{A}_0 : \mathbf{A}_+ : \mathbf{A}_- = 1 : \frac{m_V}{m_B} : \frac{m_V^2}{m_B^2}$$

fraction of longitudinal polarized states f_L :

$$f_L = \frac{|\mathbf{A}_0|^2}{|\mathbf{A}_0|^2 + |\mathbf{A}_+|^2 + |\mathbf{A}_-|^2} \sim 1 - \frac{m_V^2}{m_B^2}$$

theoretical status:

LP (A_0)

calculable using QCD factorization in the heavy quark limit

Beneke, Buchalla, Neubert, Sachrajda: arXiv:hep-ph: 0104110, 9905312, 0006124

TP

suppressed by powers of (Λ_{QCD}/m_B)
amplitudes do NOT factorize $\Rightarrow$ hard to calculate (divergences)

M. Beneke, J. Rohrer and D. Yang : arXiv:hep-ph: 0612290

$B \rightarrow VV$

measurements

tree dominated: ($\rho, \omega, \dots$)

$$f_L \sim 1 \quad \checkmark$$

penguin dominated: ($K^*, \phi, \dots$)

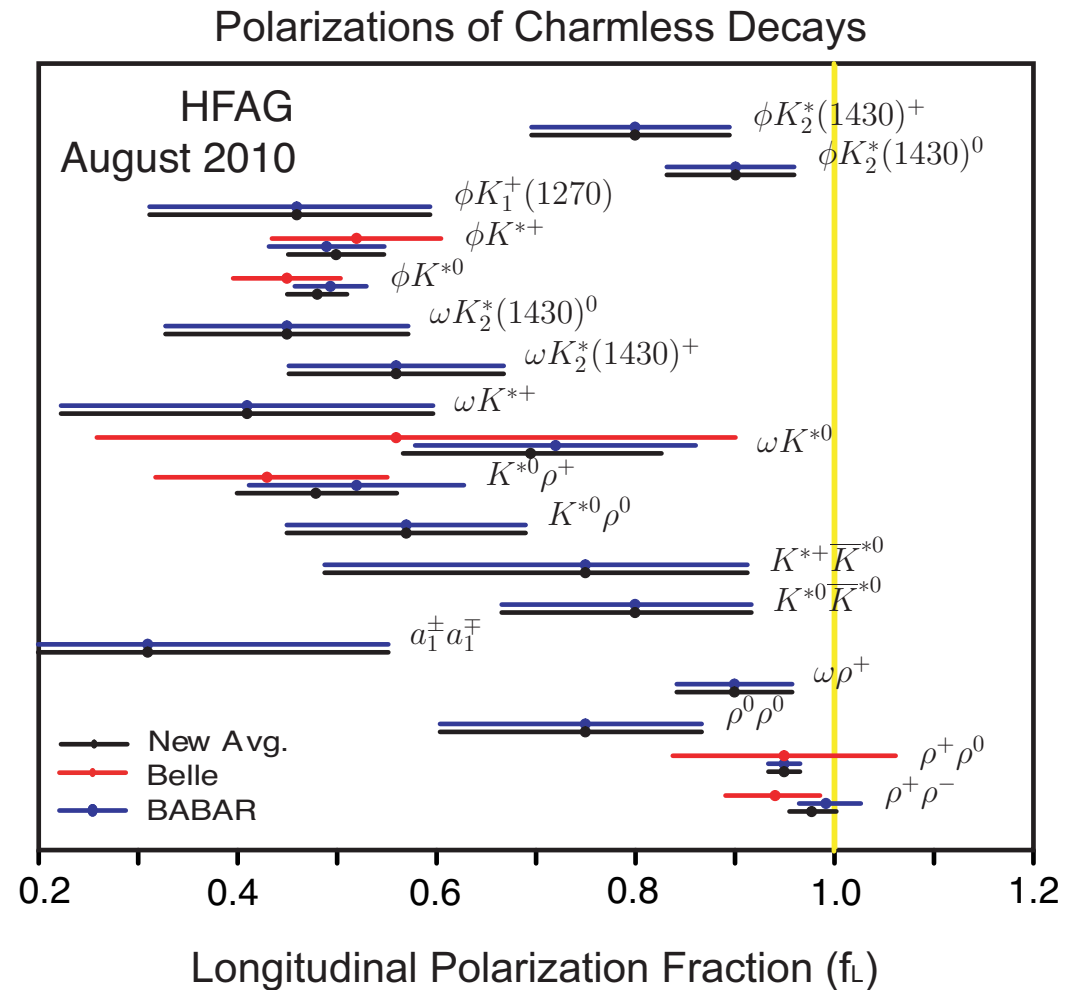
$$f_L \sim 0.5 \quad ?$$

e.g. K^* naive expectation:

$$f_L \sim 1 - \left(\frac{m_{K^*}}{m_B}\right)^2 \sim 0.97$$

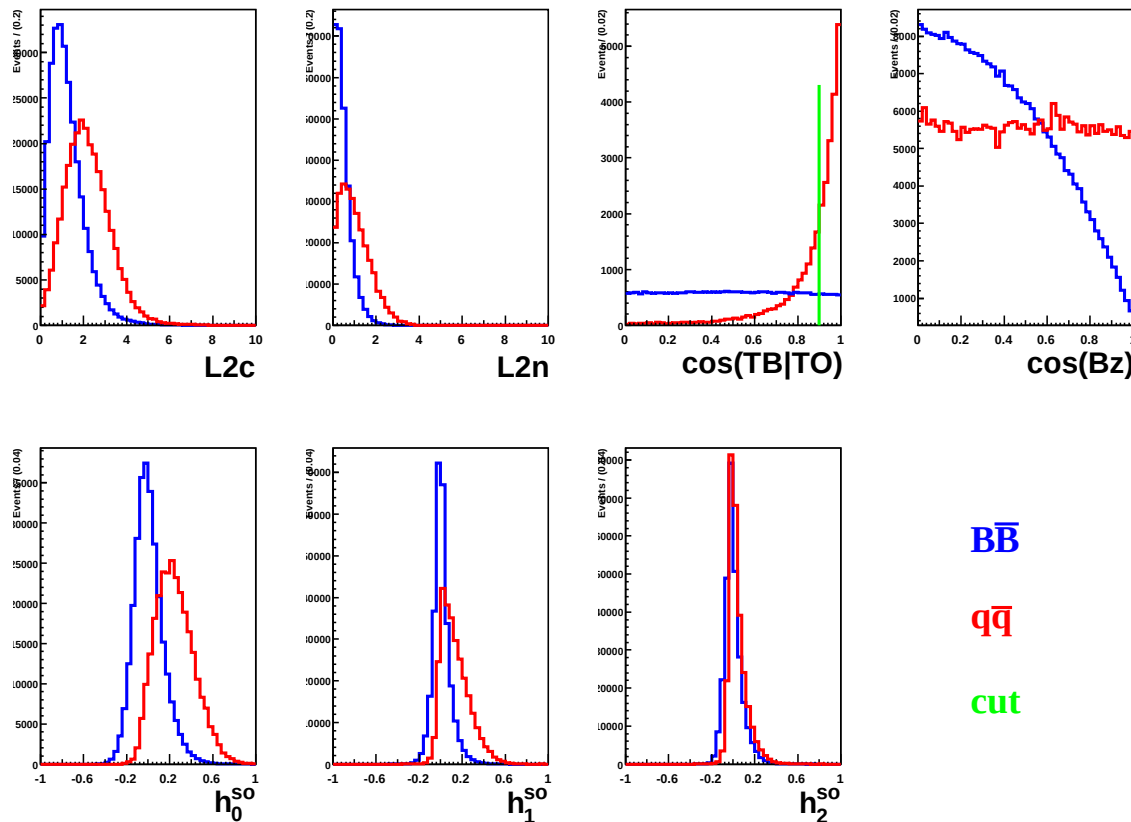
→ “**helicity puzzle**”

topic of ongoing research



Continuum Identification

What I use.



- momentum sum relative to thrust axis L_2
- angle between the 2 B s thrust axis
- B flight direction
- fox wolfram moments

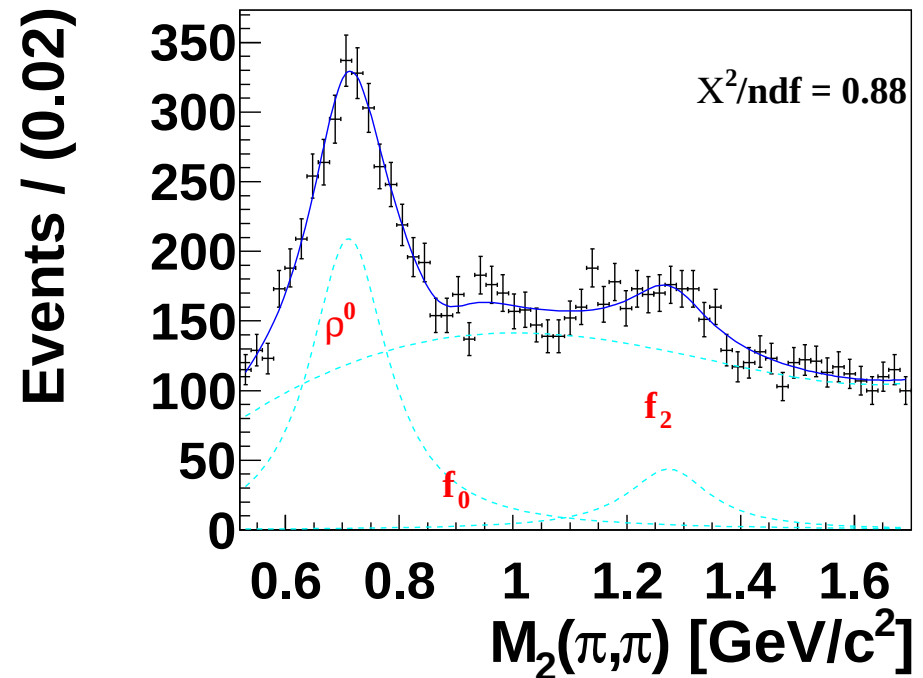
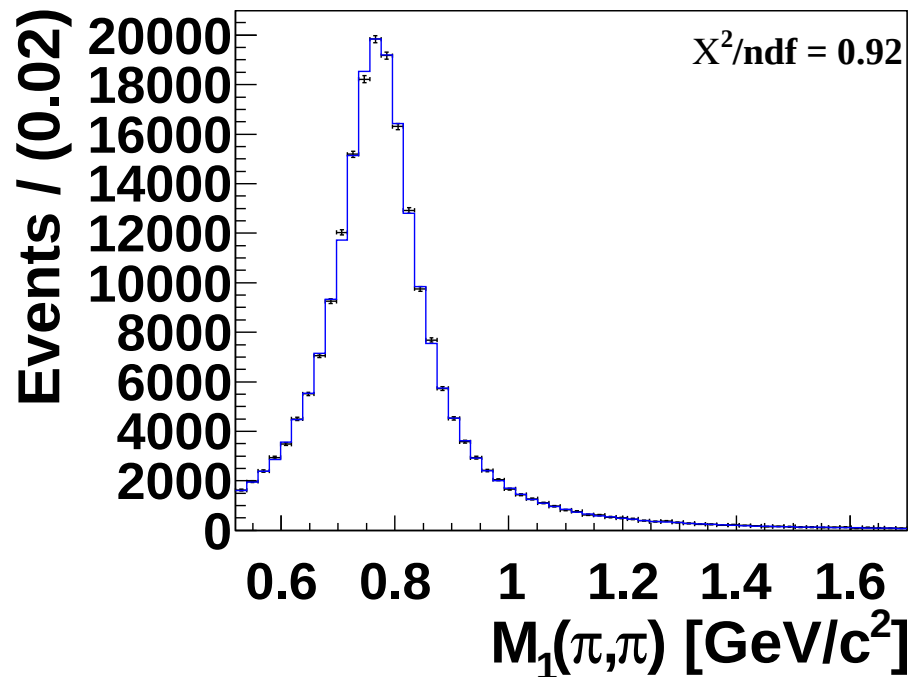
cut: $\cos(TB|TO) < 0.9$

removes $\sim 60\% q\bar{q}$

Model for $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$

- signal MC(L pol)

- neutral charmless decays



$$\mathcal{PDF}(m_{\pi^+\pi^-}) = \epsilon_{rec}(m_{\pi^+\pi^-}) \times \text{Breit-Wigner}$$

$$\mathcal{PDF}(m_{\pi^+\pi^-}) = 2 \times \text{Breit-Wigner} + \text{gaussian} + \sum_{i=1}^4 \text{chebychev}_i$$

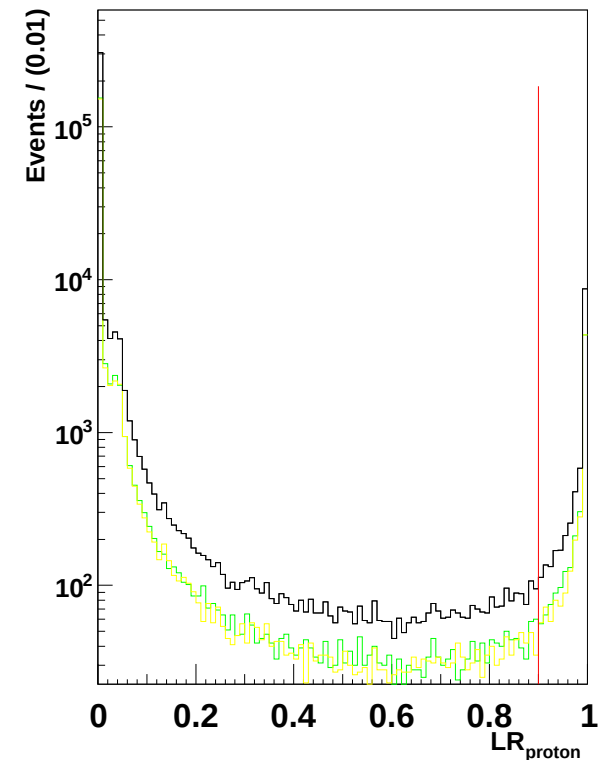
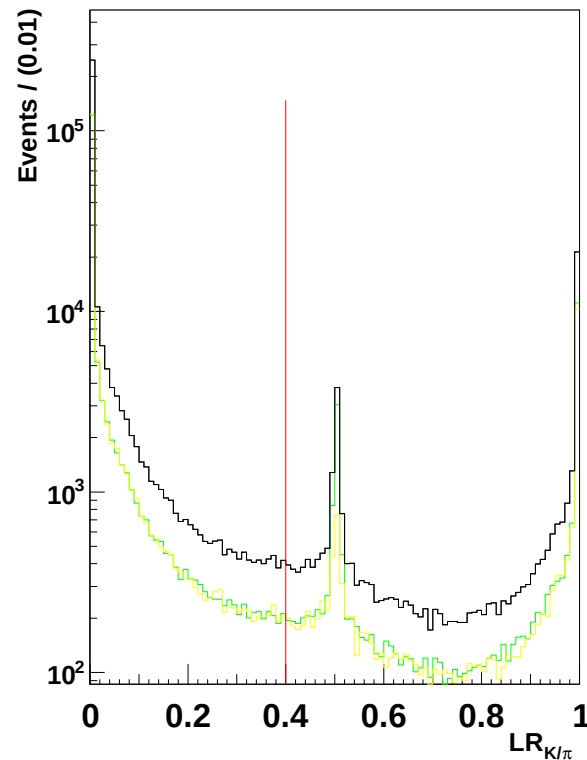
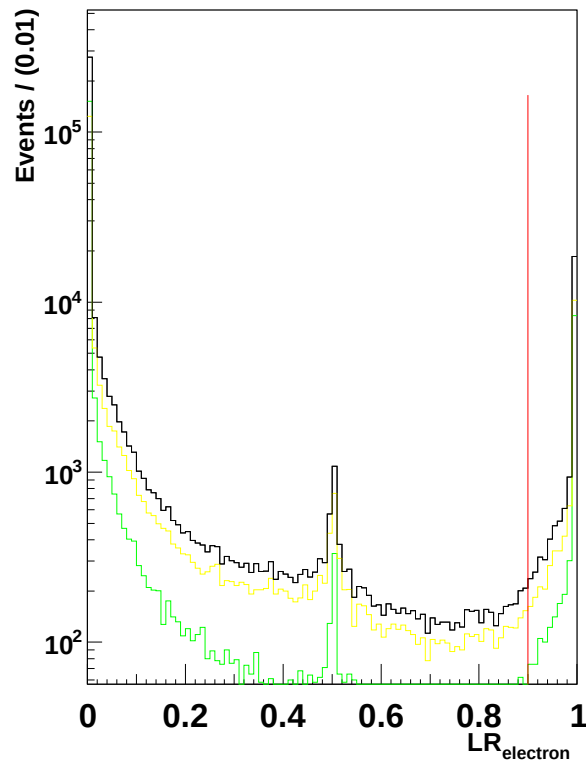
Rec: PID Criterias

- information from different subdetectors $\rightarrow$ likelihood ratios $\mathcal{LR}_{i/j}$
- charged tracks from signal MC: standard set of cuts $\rightarrow$ syst. are known

$$\mathcal{LR}_e < 0.9$$

$$\mathcal{LR}_{K/\pi} < 0.4$$

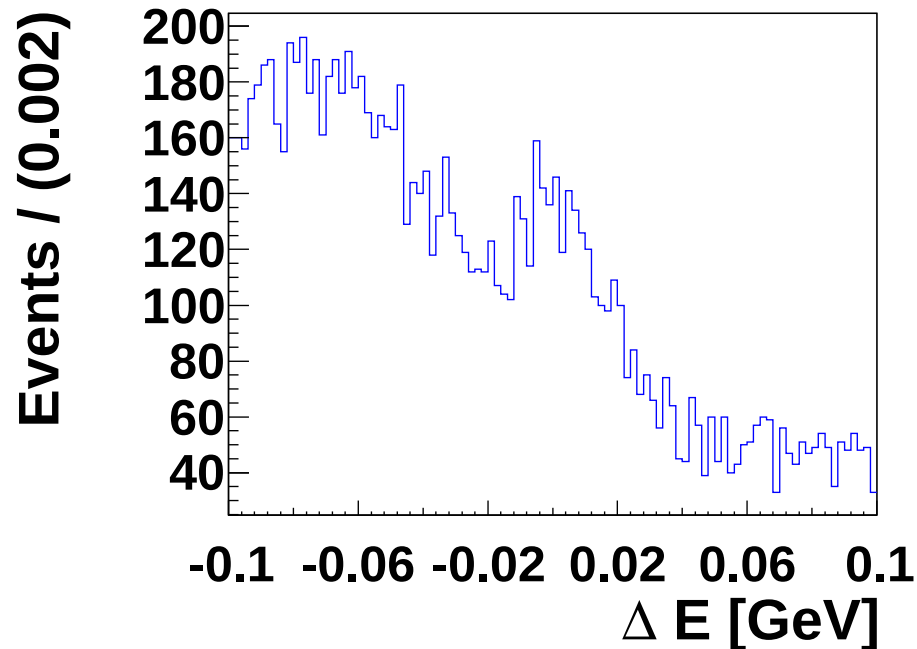
$$\mathcal{LR}_{p/\pi} < 0.9$$



- require that tracks (somehow) origin at the IP: $|dr| < 0.5\text{cm}$ & $|dz| < 5\text{cm}$

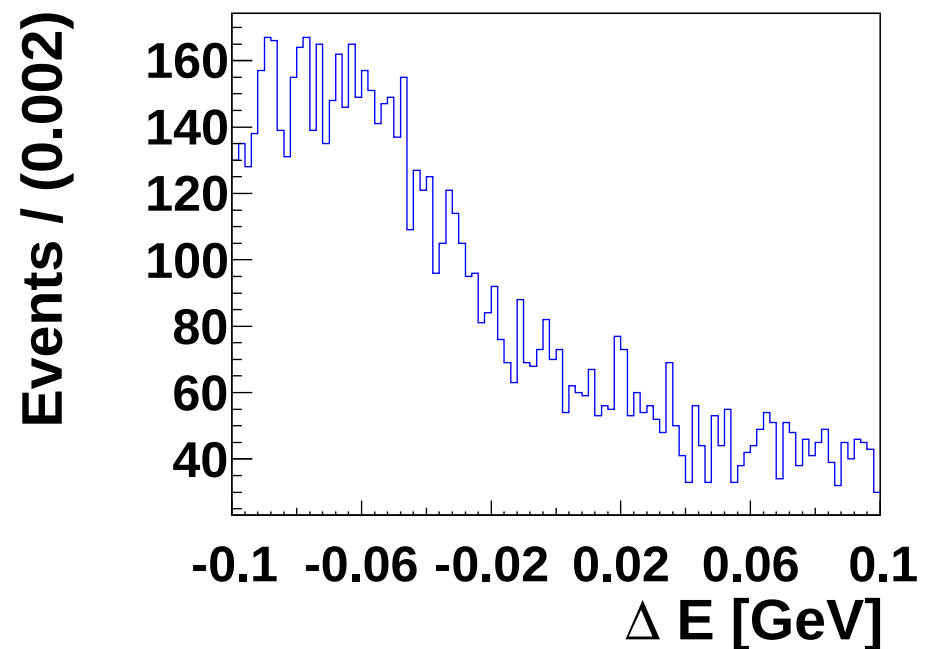
Rec: Charm and Strange Vetos

- removes signal like features coming from background with similar final state topology, e.g. $B^0 \rightarrow D^-(\pi^-\pi^+\pi^-\pi^+)\pi^+$ or wrong PID;
- $$(\Delta E = E_{Brec} - E_{beam})$$



before

and



after vetos

Rec: Charm and Strange Vetos

Cuts on $M(\pi\pi)$:

$$D^0 : 1.86484 \pm 0.02 [GeV/c^2]$$

$$K_s : 0.493677 \pm 0.018 [GeV/c^2]$$

Cuts on $M(\pi\pi\pi)$:

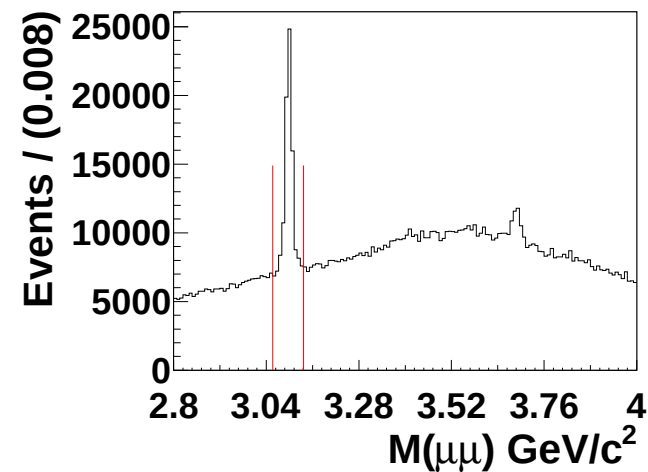
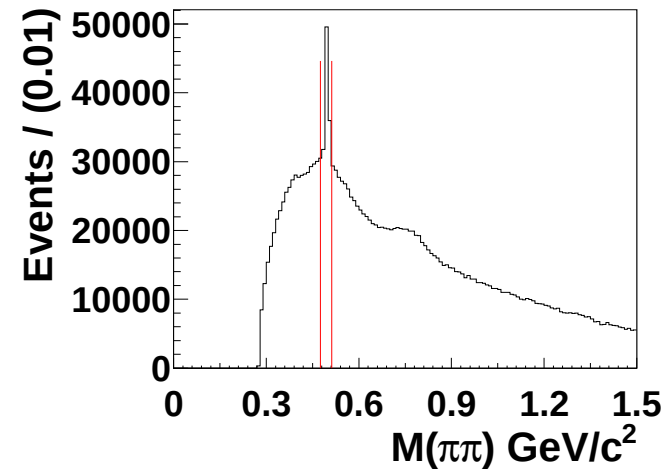
$$D^\pm : 1.8696 \pm 0.02 [GeV/c^2]$$

$$D_s^\pm : 1.96849 \pm 0.02 [GeV/c^2]$$

Cuts on $M(\mu\mu)$:

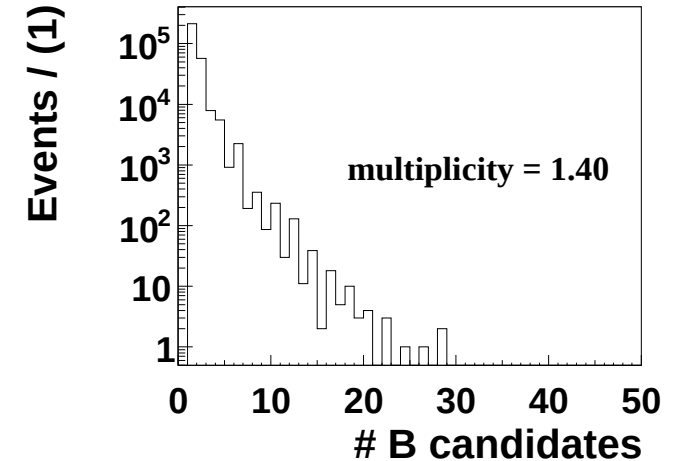
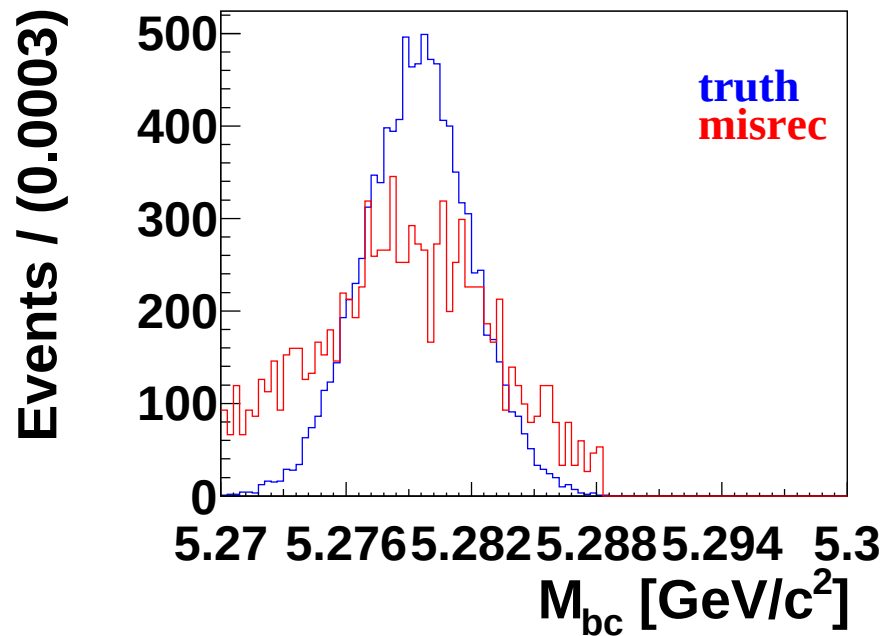
$$J\Psi : 3.0969 \pm 0.04 [GeV/c^2]$$

$\rightarrow$ loss in $\epsilon_{rec} < 4\%$

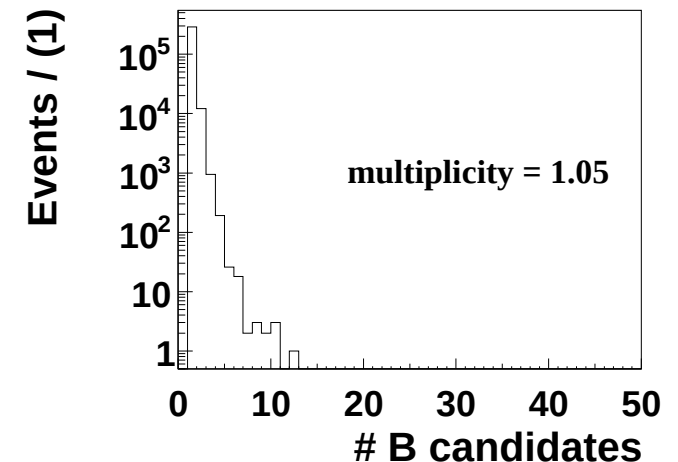


Rec: BCS

- BCS: best candidate selection



$L(\text{top})$ and T pol



if 2 candidates with same $M_{bc} = \sqrt{E_{beam}^2 - \vec{p}_B^2}$

⇒ choose combination with highest π^+ and lowest π^- momentum

→ purity = 76%(L); 92%(T)

Measurement of $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$

Extraction of $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$ and f_L

6D extended unbinned likelihood fit with the variables

$$\Delta E, \quad 2 \times m_{\pi^+ \pi^-}, \quad \mathcal{F}, \quad 2 \times \cos \theta_{\text{Hel}}$$

$$\Delta E \equiv E_{B_{\text{rec}}} - E_{\text{beam}}$$

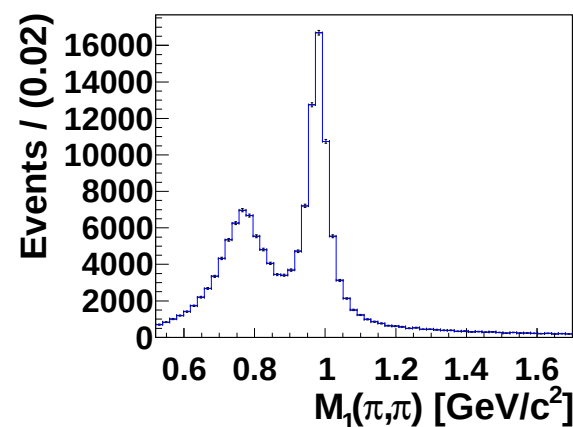
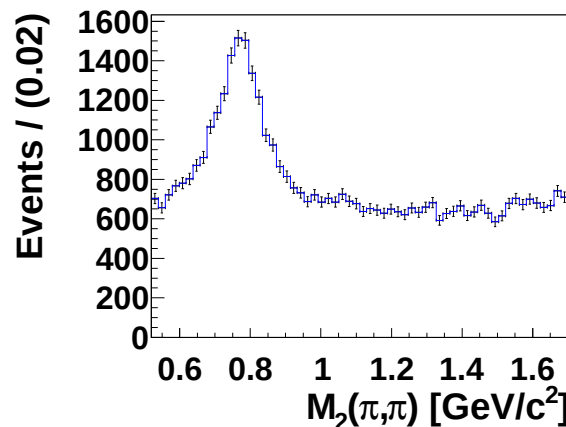
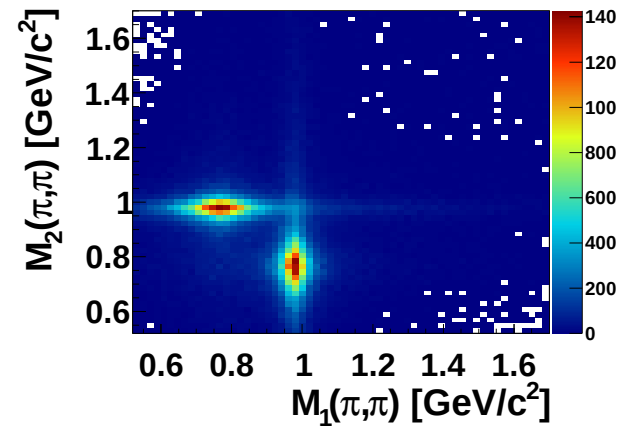
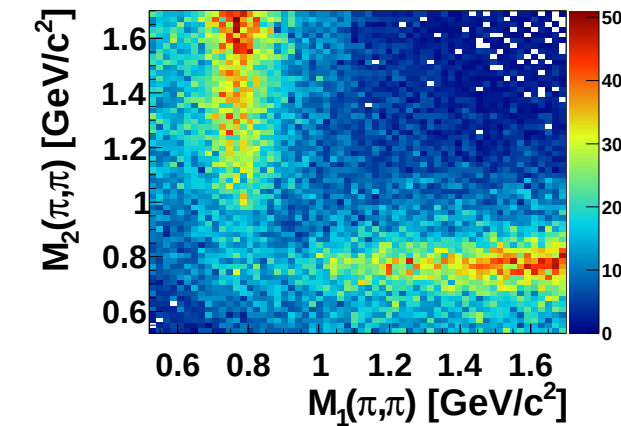
The model consists of **17 components** which are:

modeled using

- $2 \times$ signal (L pol, T pol); MC
 - $2 \times$ misreconstructed signal (L pol, T pol); MC
 - continuum ($e^+ e^- \rightarrow q \bar{q}$); data taken at $\sqrt{s} = 10.50 \text{ GeV} < m(\Upsilon(4S))$
 - $4 \times B \bar{B}$: charm and charmless $B^0(B^\pm)$ decays; MC
 - $8 \times$ peaking BKG (4π s finalstates); MC
- $\pi^+ \pi^- \pi^+ \pi^-$, $a_1^\pm \pi^\mp$, $a_2^\pm \pi^\mp$, $b_1^\pm \pi^\mp$, $f_0 f_0$, $f_0 \pi^+ \pi^-$, $\rho^0 \pi^+ \pi^-$, $f_0 \rho^0$. BR known

Correlations!

sometimes correlated multidimensional $\mathcal{PDF}$ needed
e.g. $a_1\pi$ or $f_0\rho^0$ (peaking bkg: ΔE shape similar to signal)



Motivation

$$B \rightarrow \text{light } VV \quad (|B^0\rangle = |\bar{b}d\rangle)$$

light hadronic vector states: $\rho, \omega, a_1, b_1, \phi, K^*, \dots$

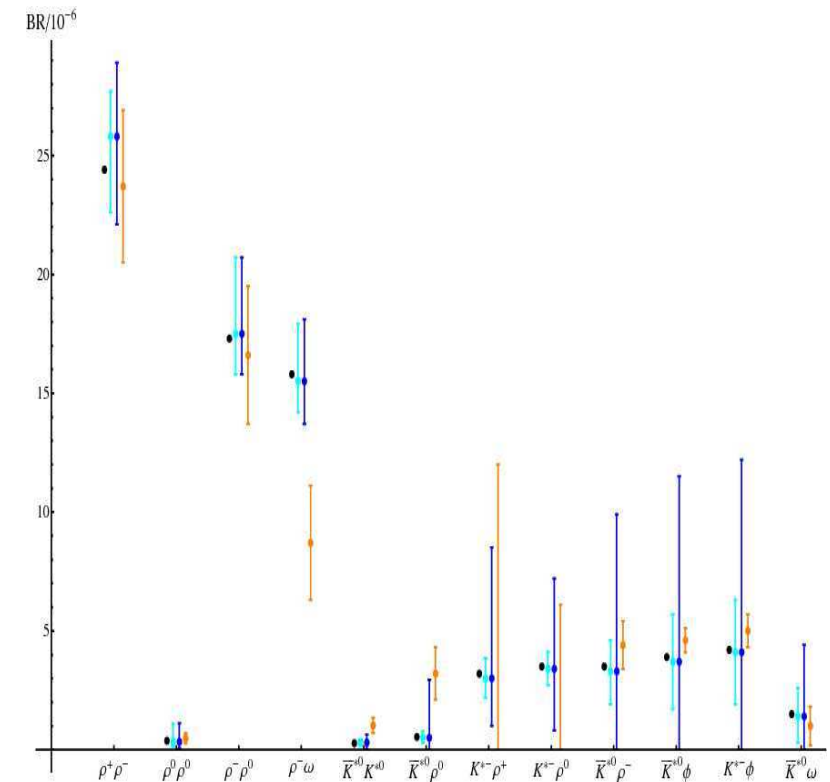
$\Rightarrow$ rich field of physics with different types of amplitudes

tree, QCD/EW penguin, weak annihilation

but: light $\leftrightarrow$ rare (CKM suppressed)

$\Rightarrow$ experimental difficulties

- extract flavor parameters, e.g. *CP* asymmetries
- find (hints of) new physics
- helps understanding
 - a) QCD, b) helicity structure, c)...



Bartsch, Buchalla, Kraus: arXiv: 0810.0249

Toy MC Studies for $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$

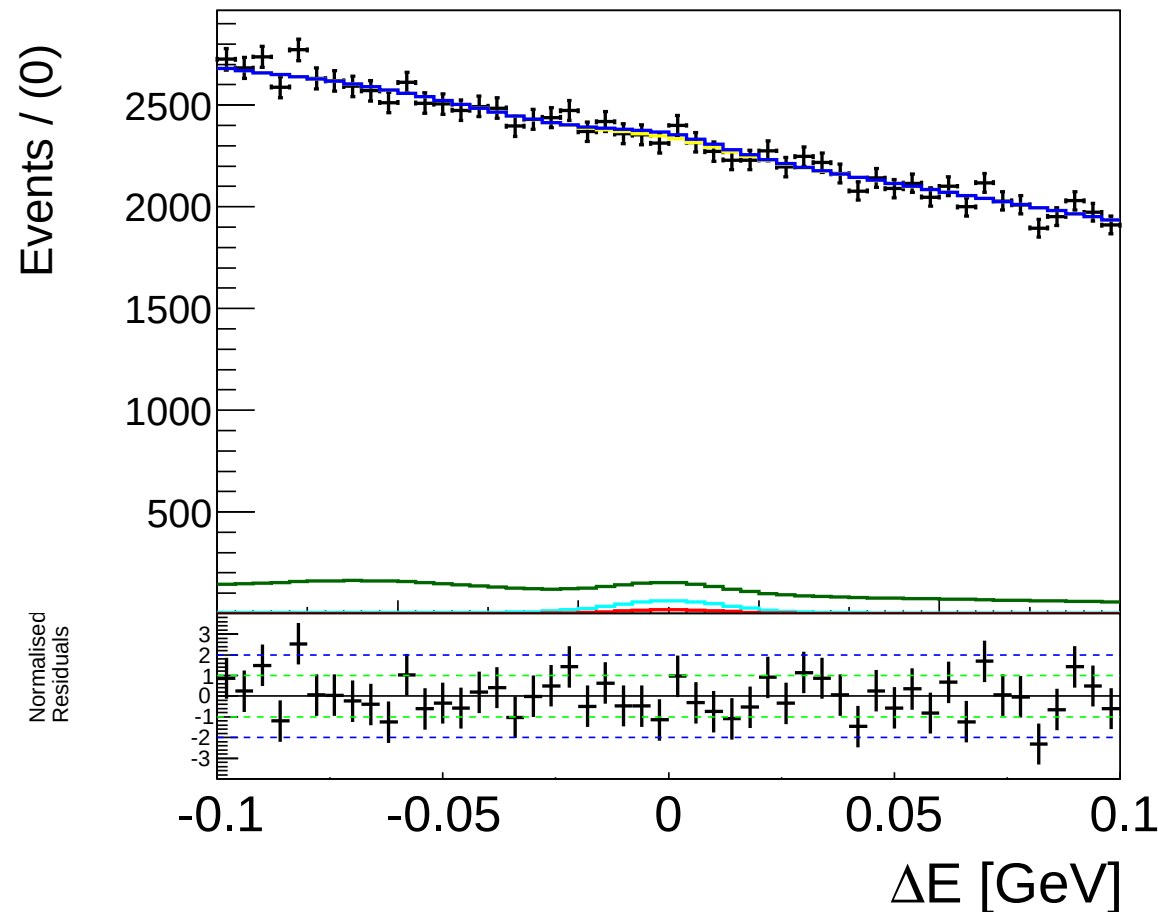
Estimate the fitter's ability to find signal with Toy MC, proj. into ΔE .

expected Nr of events:

- **signal**: ~ 100
- **4π ff**: ~ 650
(using world averages)
- **$B\bar{B}$** : ~ 4500
- **all**: ~ 110000

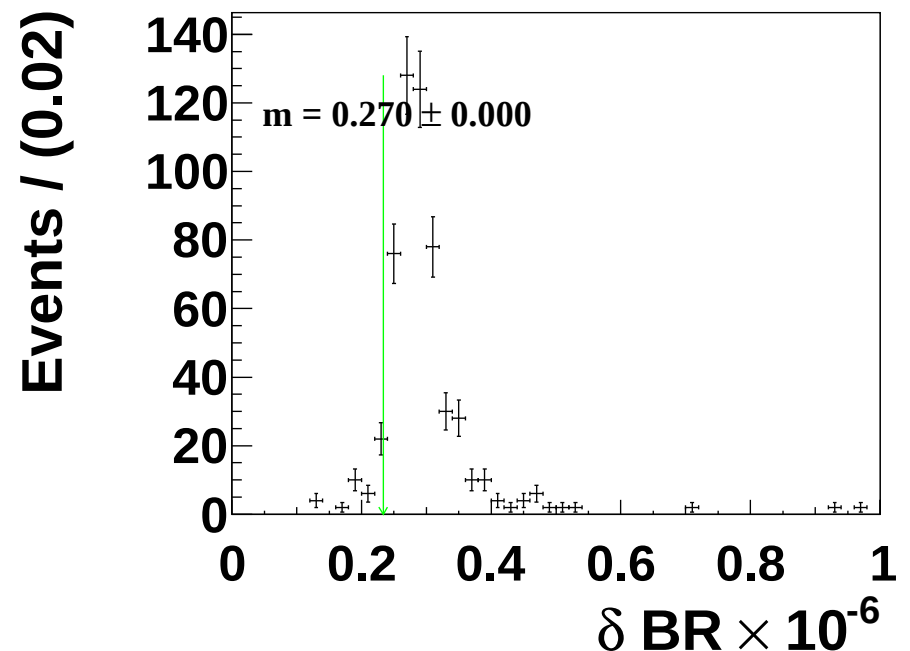
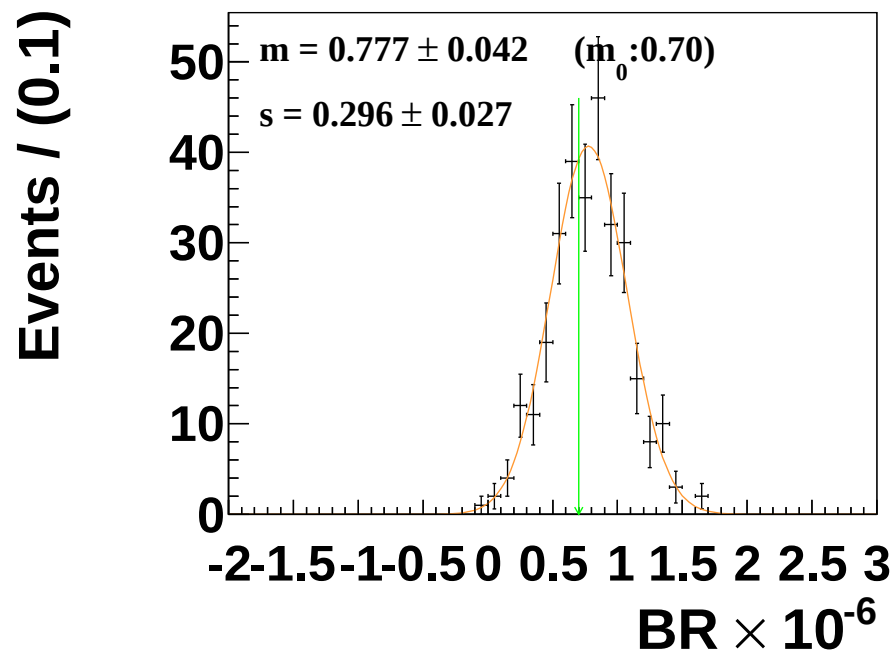
Fit Region:

$$\begin{aligned} 5.27 < M_{bc} < 5.29 \quad [GeV/c^2] \\ -0.1 < \Delta E < 0.1 \quad [GeV] \\ 0.52 < m(\pi^+ \pi^-) < 1.15 [GeV/c^2] \\ -1 < \cos(\theta_H) < 1 \end{aligned}$$



Toy MC Studies for $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$

- performed fits on 300 toy MC samples



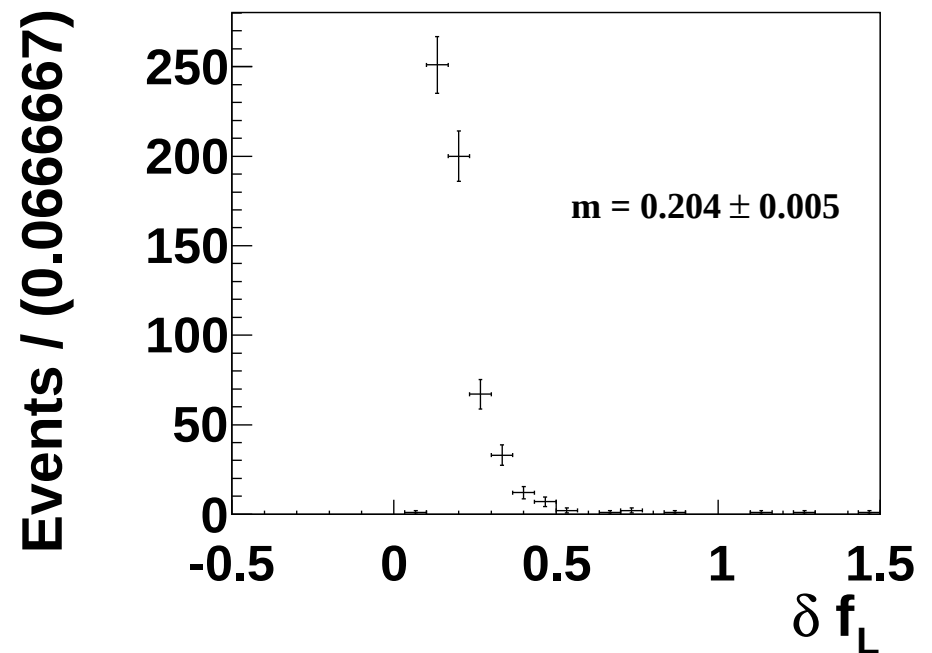
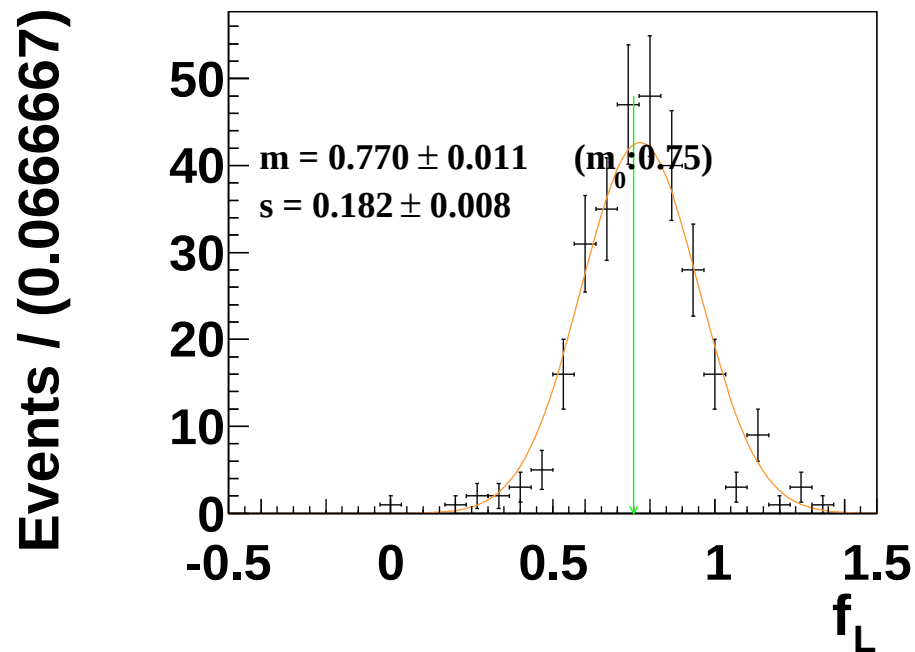
green line is input value

indicates 3σ significance

$\Rightarrow$ on the edge of a observation with a 3σ significance

Toy MC Studies for $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$

- performed fits on 300 toy MC samples



green line is input value

$\Rightarrow$ measurement of f_L possible

Flavor Tagging

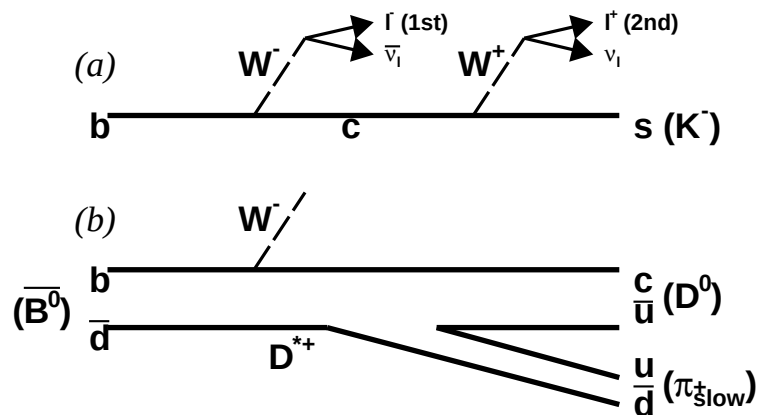
towards CPV measurement

$\Upsilon(4S) \rightarrow$ coherent $B\bar{B}$ pair

one $B \equiv B_{CP}$ decays into final state of interest.

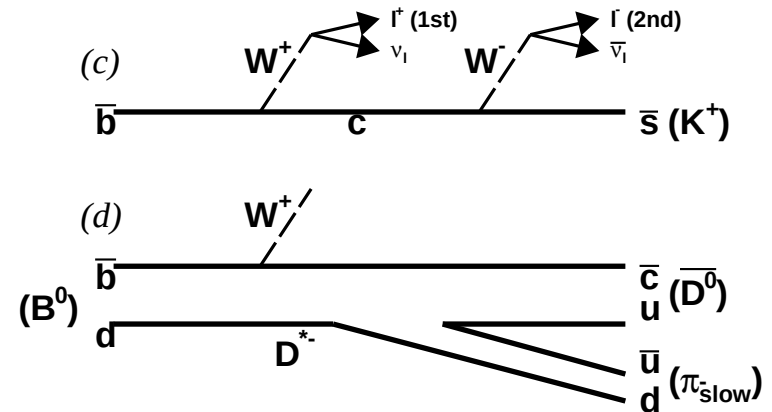
use flavor specific decays of the other $B \equiv B_{tag}$ to determine the flavor of B_{CP} ; e.g.

$\bar{B}$ decays



VS

B decays

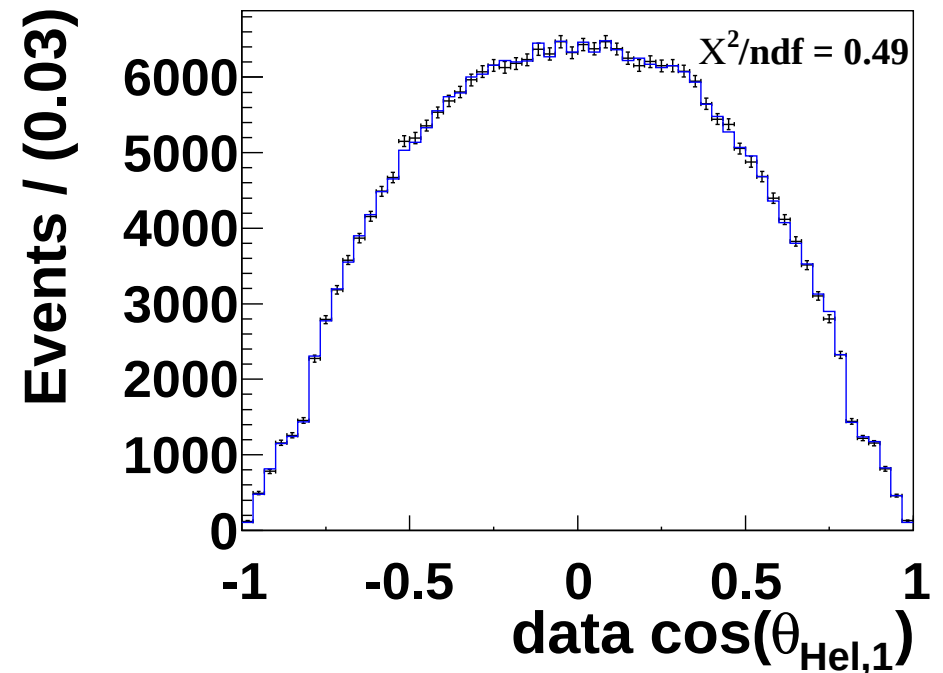
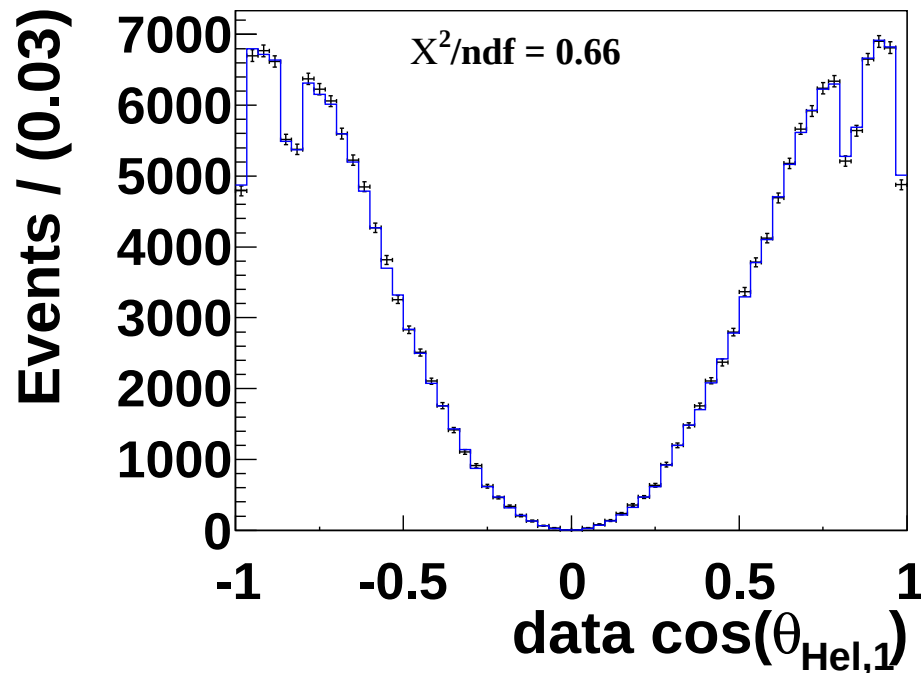


Model for $\mathcal{BR}(B^0 \rightarrow \rho^0 \rho^0)$

Helicity: weighted with reconstruction efficiency histogram

● signal MC(L pol)

● signal MC(T pol)



$$\frac{1}{\Gamma} \frac{d^2\Gamma}{d\cos\theta_{\text{Hel}}^1 d\cos\theta_{\text{Hel}}^2} = \frac{9}{4} \left(f_L \cos^2 \theta_{\text{Hel}}^1 \cos^2 \theta_{\text{Hel}}^2 + \frac{1}{4} (1 - f_L) \sin^2 \theta_{\text{Hel}}^1 \sin^2 \theta_{\text{Hel}}^2 \right)$$