Diphoton + 2jets production at NLO

Adriano Lo Presti Institut de Physique Théorique, CEA–Saclay *on behalf of the* BlackHat Collaboration





Zvi Bern, Lance Dixon, Fernando Febres Cordero, Stefan Höche, Harald Ita, David A. Kosower, A. L., Daniel Maître

Max-Planck-Institut <u>für</u> Physik – Munich, Germany 10 January 2014

 $\gamma\gamma+2j$ @ NLO

Diphoton production is a very interesting process at the LHC

Higgs boson decays into a photon pair through massive-quark loop

Prompt diphoton production: background for SM precision measurements

 $\gamma\gamma+2j$ @ NLO

Diphoton production is a very interesting process at the LHC

Higgs boson decays into a photon pair through massive-quark loop

Prompt diphoton production: background for SM precision measurements

With two jets:

Background to the production of the Higgs boson via Vector Boson Fusion (VBF)





Born matrix elements known since the '90s

NLO needed to reduce the large dependence on scales and have the first quantitative prediction.

pp → γγ + 0j
 DIPHOX (Binoth, Guillet,Pilon,Werlen)
 2gammaMC (Bern,Dixon,Schmidt)
 MCFM (Campbel,Ellis,Williams)
 Catani, Cieri, de Florian, Ferrera, Grazzini (2011) (NNLO)

- $pp \rightarrow \gamma\gamma + 1j$ Del Duca, Maltoni, Nagy, Trocsanyi (2003) Gehrmann, Greiner, Heinrich (2013)
- $pp \rightarrow \gamma\gamma + 2j$ Gehrmann, Greiner, Heinrich (2013) Badger, Guffanti, Yundin (2013) (also $\gamma\gamma + 3j$)

BH collaboration: presented at RADCOR2013 , arXiv:1312.0592[hep-ph] , paper to appear

$$\sigma_n^{\text{NLO}} = \int_n \sigma_n^{\text{born}} + \int_n \sigma_n^{\text{virt}} + \int_{n+1} \left(\sigma_{n+1}^{\text{real}} - \sigma_{n+1}^{\text{subtr}} \right) + \int_n \Sigma_n^{\text{subtr}}$$

$$\sigma_n^{\text{NLO}} = \int_n \sigma_n^{\text{born}} + \int_n \sigma_n^{\text{virt}} + \int_{n+1} \left(\sigma_{n+1}^{\text{real}} - \sigma_{n+1}^{\text{subtr}} \right) + \int_n \Sigma_n^{\text{subtr}}$$

COMIX package (Gleisberg, Höche) from within SHERPA used to compute Born and real-emission matrix elements, along with the Catani– Seymour dipole subtraction terms.

$$\sigma_n^{\text{NLO}} = \int_n \sigma_n^{\text{born}} + \int_n \sigma_n^{\text{virt}} + \int_{n+1} \left(\sigma_{n+1}^{\text{real}} - \sigma_{n+1}^{\text{subtr}} \right) + \int_n \Sigma_n^{\text{subtr}}$$

BlackHat used to compute the virtual (one-loop) contribution Numerical implementation of on-shell methods for one-loop amplitudes

$$\sigma_n^{\text{NLO}} = \int_n \sigma_n^{\text{born}} + \int_n \sigma_n^{\text{virt}} + \int_{n+1} \left(\sigma_{n+1}^{\text{real}} - \sigma_{n+1}^{\text{subtr}} \right) + \int_n \Sigma_n^{\text{subtr}}$$

BlackHat used to compute the virtual (one-loop) contribution Numerical implementation of on-shell methods for one-loop amplitudes



Examples of diagrams for the processes $qg \rightarrow \gamma \gamma q'g$ and $qq' \rightarrow \gamma \gamma qq'$.

$$\sigma_n^{\text{NLO}} = \int_n \sigma_n^{\text{born}} + \int_n \sigma_n^{\text{virt}} + \int_{n+1} \left(\sigma_{n+1}^{\text{real}} - \sigma_{n+1}^{\text{subtr}} \right) + \int_n \Sigma_n^{\text{subtr}}$$

BlackHat used to compute the virtual (one-loop) contribution Numerical implementation of on-shell methods for one-loop amplitudes



nf-term loop diagram:

closed fermion loop, but photons do not couple directly to it.

$$\sigma_n^{\text{NLO}} = \int_n \sigma_n^{\text{born}} + \int_n \sigma_n^{\text{virt}} + \int_{n+1} \left(\sigma_{n+1}^{\text{real}} - \sigma_{n+1}^{\text{subtr}} \right) + \int_n \Sigma_n^{\text{subtr}}$$

BlackHat used to compute the virtual (one-loop) contribution Numerical implementation of on-shell methods for one-loop amplitudes



Charge-weighted fermion loop pieces:

closed fermion loop, at least one photon couples directly to it.

$$\sigma_n^{\text{NLO}} = \int_n \sigma_n^{\text{born}} + \int_n \sigma_n^{\text{virt}} + \int_{n+1} \left(\sigma_{n+1}^{\text{real}} - \sigma_{n+1}^{\text{subtr}} \right) + \int_n \Sigma_n^{\text{subtr}}$$

BlackHat used to compute the virtual (one-loop) contribution Numerical implementation of on-shell methods for one-loop amplitudes



Light-by-light scattering contribution:

have no corresponding tree-level amplitudes and are finite.

$$\sigma_n^{\text{NLO}} = \int_n \sigma_n^{\text{born}} + \int_n \sigma_n^{\text{virt}} + \int_{n+1} \left(\sigma_{n+1}^{\text{real}} - \sigma_{n+1}^{\text{subtr}} \right) + \int_n \Sigma_n^{\text{subtr}}$$

BlackHat used to compute the virtual (one-loop) contribution Numerical implementation of on-shell methods for one-loop amplitudes

Used previously for				
$W, Z/\gamma^* + 3j,$	$W, Z/\gamma^* + 4j,$	W+5j,	4 Jet,	
high- $p_T W$ polarization, $\gamma + n$ -jet / $Z + n$ -jet ratios			ratios	

$$\sigma_n^{\text{NLO}} = \int_n \sigma_n^{\text{born}} + \int_n \sigma_n^{\text{virt}} + \int_{n+1} \left(\sigma_{n+1}^{\text{real}} - \sigma_{n+1}^{\text{subtr}} \right) + \int_n \Sigma_n^{\text{subtr}}$$

BlackHat used to compute the virtual (one-loop) contribution Numerical implementation of on-shell methods for one-loop amplitudes

Used previously for				
$W, Z/\gamma^* + 3j,$	$W, Z/\gamma^* + 4j,$	W+5j,	4 Jet,	
high- $p_T W$ polariza	ation, $\gamma + n$ -je	$\gamma + n$ -jet / $Z + n$ -jet ratios		

SHERPA (Höche,Krauss,Schönherr,Schumann,Siegert,Winter,Zapp) used to manage the partonic subprocesses and to integrate over phase space.

Britto et al. (BCFW, 2005), Bern, Dixon, Dunbar, Kosower (1994), Bern, Dixon, Kosower (1998, 2006), Brandhuber, McNamara, Spence, Travaglini (2005), Anastasiou, Britto, Feng, Kunszt, Mastrolia (2007); Ellis, Giele, Kunszt, Melnikov, Zanderighi (2008), Ossola, Papadopoulos, Pittau (2007),

. and many others.

$$Ampl = \sum_{j \in Basis} c_j \operatorname{Int}_j + Rational$$

Britto et al. (BCFW, 2005), Bern, Dixon, Dunbar, Kosower (1994), Bern, Dixon, Kosower (1998, 2006), Brandhuber, McNamara, Spence, Travaglini (2005), Anastasiou, Britto, Feng, Kunszt, Mastrolia (2007); Ellis, Giele, Kunszt, Melnikov, Zanderighi (2008), Ossola, Papadopoulos, Pittau (2007),

... and many others.

$$Ampl = \sum_{j \in Basis} c_j \operatorname{Int}_j + Rational$$

Int_{*i*} \rightarrow Known integral basis (Passarino-Veltman):



Britto et al. (BCFW, 2005), Bern, Dixon, Dunbar, Kosower (1994), Bern, Dixon, Kosower (1998, 2006), Brandhuber, McNamara, Spence, Travaglini (2005), Anastasiou, Britto, Feng, Kunszt, Mastrolia (2007); Ellis, Giele, Kunszt, Melnikov, Zanderighi (2008), Ossola, Papadopoulos, Pittau (2007),

... and many others.

$$Ampl = \sum_{j \in Basis} c_j \operatorname{Int}_j + Rational$$

Int
$$_i \rightarrow$$
 Known integral basis (Passarino-Veltman):

 I_{4}^{3m} I_{5}^{2m} I_{2}

Integrals universal and well tabulated

Aim of the calculation is to compute coefficients and rational terms

Britto et al. (BCFW, 2005), Bern, Dixon, Dunbar, Kosower (1994), Bern, Dixon, Kosower (1998, 2006), Brandhuber, McNamara, Spence, Travaglini (2005), Anastasiou, Britto, Feng, Kunszt, Mastrolia (2007); Ellis, Giele, Kunszt, Melnikov, Zanderighi (2008), Ossola, Papadopoulos, Pittau (2007),

... and many others.

$$Ampl = \sum_{j \in Basis} c_j \operatorname{Int}_j + Rational$$

Int
$$_i \rightarrow$$
 Known integral basis (Passarino-Veltman):

 I_{4}^{3m} I_{3}^{3m} I_{2}^{3m}

Integrals universal and well tabulated

Aim of the calculation is to compute coefficients and rational terms

 $c_j \rightarrow$ Unitarity in D=4 : rational functions of spinors.

Rational \rightarrow On-shell Recursion; D-dimensional unitarity

BlackHat

1) BH computes *primitive amplitudes*:

Integrals given by analytic formulae.

- Coefficients: computed using contour integral at ∞ [D. Forde ('07)] The contour integrals are computed numerically by using a discrete Fourier sum
- Rational: D-dim unitarity via massive integral basis [S. Badger ('09)]

Coefficients reduce to products of trees.

Required tree amplitudes computed numerically (on-shell recursion relations).

BlackHat

1) BH computes *primitive amplitudes*:

Integrals given by analytic formulae.

- Coefficients: computed using contour integral at ∞ [D. Forde ('07)] The contour integrals are computed numerically by using a discrete Fourier sum
- Rational: D-dim unitarity via massive integral basis [S. Badger ('09)]

Coefficients reduce to products of trees. Required tree amplitudes computed numerically (on-shell recursion relations).

2) It assembles these into complete colour-ordered amplitudes.

BlackHat

1) BH computes *primitive amplitudes*:

Integrals given by analytic formulae.

- Coefficients: computed using contour integral at ∞ [D. Forde ('07)] The contour integrals are computed numerically by using a discrete Fourier sum
- Rational: D-dim unitarity via massive integral basis [S. Badger ('09)]

Coefficients reduce to products of trees. Required tree amplitudes computed numerically (on-shell recursion relations).

2) It assembles these into complete colour-ordered amplitudes.

3) Sum of the loop-tree interference over colours (leading/subleading)

One needs to be able to re-evaluate cross section and distributions with different choices of

- observables
- cuts
- jet algorithms
- PDF
- renormalization and factorization scales
- ...

One needs to be able to re-evaluate cross section and distributions with different choices of

- observables
- cuts
- jet algorithms
- PDF
- renormalization and factorization scales
- ...

In order to have small statistical uncertainty we need to compute hard matrix elements in million of different phase-space points. This calculation is computationally very demanding.

SHERPA is used to create weighted events, which are stored in ROOT n-tuples.

BH-SHERPA *n*-tuple branches id, nparticle, px, py, pz, E, x1, x2, x1p, x2p, id1, id2, kf alpha_power, alpha_s, fac_scale, ren_scale, weight, weight2, me_wgt, me_wgt2, nuwgt, usr_wgts, part

Changing the scale: Virtual contribution

$$w = m \cdot f_1(\mathbf{id1}, \mathbf{x1}, \mu_F) f_2(\mathbf{id2}, \mathbf{x2}, \mu_F) \frac{\alpha_s(\mu_R)^n}{(\mathbf{alphas})^n}$$
$$m = \mathbf{me_wgt2} + l \mathbf{usr_wgts}[0] + \frac{l^2}{2} \mathbf{usr_wgts}[1]$$
$$l = \ln\left(\frac{\mu_R^2}{\mathbf{ren_scale}^2}\right)$$

BH-SHERPA *n*-tuple branches id, nparticle, px, py, pz, E, x1, x2, x1p, x2p, id1, id2, kf alpha_power, alpha_s, fac_scale, ren_scale, weight, weight2, me_wgt, me_wgt2, nuwgt, usr_wgts, part

Changing the scale: Virtual contribution

$$w = m \cdot f_1(\mathbf{id1}, \mathbf{x1}, \mu_F) f_2(\mathbf{id2}, \mathbf{x2}, \mu_F) \frac{\alpha_s(\mu_R)^n}{(\mathbf{alphas})^n}$$
$$m = \mathbf{me_wgt2} + l \mathbf{usr_wgts}[0] + \frac{l^2}{2} \mathbf{usr_wgts}[1]$$
$$l = \ln\left(\frac{\mu_R^2}{\mathbf{ren_scale}^2}\right)$$

Sufficient information can be stored to re-evaluate cross sections and distributions without the need of re-computing the hard matrix elements

Photon isolation criterion

We are interested in photons which originated in the hard interaction.

Must isolate photons from surrounding hadronic radiation.

Photon isolation criterion

We are interested in photons which originated in the hard interaction.

Must isolate photons from surrounding hadronic radiation.

We use Frixione isolation: radially-dependent E_{T} limit [Frixione, 1998]

$$\sum_{p} E_{Tp} \theta(\delta - R_{p\gamma}) \le E(\delta) \quad \text{with} \quad E(\delta) = E_T^{\gamma} \epsilon \left(\frac{1 - \cos \delta}{1 - \cos \delta_0}\right)^n$$

$$(\varepsilon = 0.5, \delta_0 = 0.4, n = 1)$$

The dependence on the parameters n and ε typically weak.



$\gamma\gamma+2j$ with BlackHat

Approximations: No top-contributions, the other five quarks treated as massless

γγ + 0-jet: confirmed HELAC (PS points) and MCFM (PS points & after integration)

γγ + 1-jet: confirmed GoSam (PS points & after integration)
γγqqg also confirmed against previous analytic calculation (L. Dixon)

γγ + 2-jet: confirmed GoSam (PS points) total cross section confirmed against Gehrmann, Greiner, Heinrich

γγ+jets (incl.) @ LO&NLO : cross sections



 $\gamma\gamma+2$ jet production: modest NLO correction small gg $\rightarrow\gamma\gamma$ gg contribution (~2% of total cross section)







Summary

- We have presented a full NLO calculation for $pp \rightarrow \gamma\gamma+2jets$
- We have included the one loop $gg \rightarrow \gamma \gamma gg$ contribution

It contributes to the $\sim 2\%$ of the total cross section

- We have considered total cross sections and distributions with and without cuts on m_{jj} and $\Delta \eta_{jj}$ to highlight kinematic region where Vector Boson Fusion (VBF) dominates
- The NLO corrections : ~20% (without VBF cuts) ~10% (with VBF cuts)
- Larger corrections at small leading-jet's p_T and small diphoton and dijet invariant masses

Thank you for the attention!

Backup slides

We split the calculation in parts B, I, RS, V (subsequently spit in sub-parts). The physical observables (distributions, total cross sections...) are constructed by summing the sub-parts

$$\langle \mathcal{O} \rangle = \sum_{t \in T, p \in P_t} \mathcal{O}^{(t,p)}$$

Each of these parts is calculated summing over the weighted events

$$\langle \mathcal{O}^{(t,p)} \rangle = \frac{1}{N_{t,p}} \sum_{e=1}^{N_{t,p}} w_{t,p,e} \mathcal{O}_{t,p,e}$$

We split the calculation in parts B, I, RS, V (subsequently spit in sub-parts). The physical observables (distributions, total cross sections...) are constructed by summing the sub-parts

$$\langle \mathcal{O} \rangle = \sum_{t \in T, p \in P_t} \mathcal{O}^{(t,p)}$$

Each of these parts is calculated summing over the weighted events

$$\langle \mathcal{O}^{(t,p)} \rangle = \frac{1}{N_{t,p}} \sum_{e=1}^{N_{t,p}} w_{t,p,e} \mathcal{O}_{t,p,e}$$

For each part the error is calculated as

$$\epsilon_{\mathcal{O}}^{t,p} = \frac{1}{\sqrt{N_{t,p}(N_{t,p}-1)}} \left[\sum_{e=1}^{N_{t,p}} (w_{t,p,e}\mathcal{O}_{t,p,e})^2 - \frac{1}{N_{t,p}} \left(\sum_{e=1}^{N_{t,p}} w_{t,p,e}\mathcal{O}_{t,p,e} \right)^2 \right]^{1/2}$$

The errors of the different sub-parts are then summed in quadrature



Changing the scale: Born and Real contribution

$$w = \mathbf{me}_{-}\mathbf{wgt2} \cdot f_1(\mathbf{id1}, \mathbf{x1}, \mu_F) f_2(\mathbf{id2}, \mathbf{x2}, \mu_F) \frac{\alpha_s(\mu_R)^n}{(\mathbf{alphas})^n}$$

 $n(\dots)n$

BH-SHERPA *n*-tuple branches id, nparticle, px, py, pz, E, x1, x2, x1p, x2p, id1, id2, kf alpha_power, alpha_s, fac_scale, ren_scale, weight, weight2, me_wgt, me_wgt2, nuwgt, usr_wgts, part

Changing the scale: Virtual contribution

$$w = m \cdot f_1(\mathbf{id1}, \mathbf{x1}, \mu_F) f_2(\mathbf{id2}, \mathbf{x2}, \mu_F) \frac{\alpha_s(\mu_R)^n}{(\mathbf{alphas})^n}$$
$$m = \mathbf{me_wgt2} + l \mathbf{usr_wgts}[0] + \frac{l^2}{2} \mathbf{usr_wgts}[1]$$
$$l = \ln\left(\frac{\mu_R^2}{\mathbf{ren_scale}^2}\right)$$

BH-SHERPA *n*-tuple branches id, nparticle, px, py, pz, E, x1, x2, x1p, x2p, id1, id2, kf alpha_power, alpha_s, fac_scale, ren_scale, weight, weight2, me_wgt, me_wgt2, nuwgt, usr_wgts, part

$$w = m \cdot \frac{\alpha_s(\mu_R)^n}{(\mathbf{alphas})^n}$$

$$m = \omega_0 \cdot f_1(\mathbf{id1}, \mathbf{x1}, \mu_F) f_2(\mathbf{id2}, \mathbf{x2}, \mu_F)$$

$$+ \left(f_{1,a}^1 \omega_1 + f_{1,a}^2 \omega_2 + f_{1,a}^3 \omega_3 + f_{1,a}^4 \omega_4\right) f_{2,b}(x_b)$$

$$+ \left(f_{2,b}^5 \omega_1 + f_{2,b}^6 \omega_2 + f_{2,b}^7 \omega_3 + f_{2,b}^8 \omega_4\right) f_{1,a}(x_a)$$

$$\omega_0 = \mathbf{me_wgt2} + l \mathbf{usr_wgts}[0] + \frac{l^2}{2} \mathbf{usr_wgts}[1]$$

$$l = \ln\left(\frac{\mu_R^2}{\mathbf{ren_scale}^2}\right)$$

$$\omega_i = \mathbf{usr_wgts}[i+1] + \mathbf{usr_wgts}[i+9] \ln\left(\frac{\mu_F^2}{\mathbf{fac_scale}^2}\right)$$

Changing the scale. Integrated subtraction contribution











Frixione epsilon dependence

