

*Munich, Top Quark Physics Day, 11. August 2014*

***RG-improved fully differential***

***cross sections for  $t\bar{t}$  at hadron colliders***

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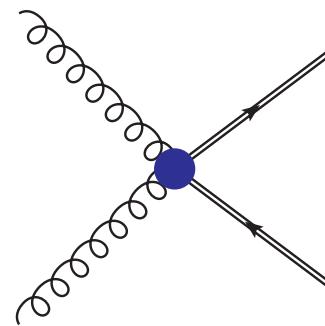
**Paul Scherrer Institut / Universität Zürich**

IN COLLABORATION WITH

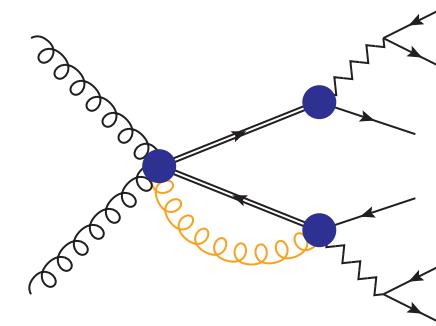
A. BROGGIO AND A. PAPANASTASIOU

## top pair production at hadron colliders

## stable tops



## unstable tops



- $\sigma_{\text{tot}}$  known at NNLO [Bärnreuther, Czakon, Fiedler, Mitov]
- $\sigma_{\text{tot}}$  known at NNLL in threshold expansion [Beneke et al.]
- NNLL known for (PIM and 1PI)
 
$$\frac{d\sigma}{dM_{t\bar{t}} d\cos \theta}$$
 and 
$$\frac{d\sigma}{dp_T dy}$$
  
 [Kidonakis et al; Ahrens et al.]

- closer to experiment
- NLO known (production and decay) for fully differential distributions [Bernreuther et al; Melnikov, Schulze; ...]
- off shell effects known [Bevilacqua et al; Denner et al; Falgari et al; ...]

- NNLL renormalization-group improved calculations for  $d\sigma/(dM_{t\bar{t}} d \cos \theta)$  (PIM) and  $d\sigma/(dp_T dy)$  (1PI) available [Kidonakis et al., Ahrens et al. ...]
- resummation can reproduce dominant (??) terms of fixed-order approach
- generalize resummed cross section to include decay of top quarks
- obtain approximate NNLO corrections to the production part of  $q\bar{q}/gg \rightarrow t\bar{t} \rightarrow W^+ b W^- \bar{b}$  through expansion of resummed results
- implement these and match to fixed-order NLO to obtain 'improved' weight for parton-level Monte Carlo
- investigate 'universality' of method
  - can we compute arbitrary observables?
  - what happens if we say compute the  $p_T$  distribution with the "wrong" PIM kinematics?
- attempt to include most important features of fully differential NNLO corrections
- here this is done for  $t\bar{t}$ , but could think of other processes

## pair-invariant mass (PIM) kinematics

- $h_1(P_1) h_2(P_2) \rightarrow (\textcolor{red}{t} + \bar{t})(p_3 + p_4) + X(p_X)$
- soft limit  $z = (p_3 + p_4)^2/\hat{s} \rightarrow 1$
- factorization of cross section

$$\frac{d\sigma}{dM_{t\bar{t}} d\cos\theta} \simeq \sum_{ij} \int \frac{dz}{z} \int \frac{dx}{x} f_{i/h_1}(x) f_{j/h_2}(\tau/(zx)) (\text{Tr} [\mathbf{H}_{ij} \cdot \mathbf{S}_{ij}^{\text{PIM}}] + \mathcal{O}(1-z))$$

- plus distribution  $P_n(z) = \left[ \frac{\ln^n(1-z)}{1-z} \right]_+$

## one-particle inclusive (1PI) kinematics

- $h_1(P_1) h_2(P_2) \rightarrow \textcolor{red}{t}(p_3) + (\bar{t} + X)(p_4 + p_X)$
- soft limit  $s_4 = (p_4 + p_X)^2 - m_t^2 \rightarrow 0$
- factorization of cross section

$$\frac{d\sigma}{dp_T dy} \simeq \sum_{ij} \int \frac{dx_1}{x_1} \int \frac{dx_2}{x_2} f_{i/h_1}(x_1) f_{j/h_2}(x_2) (\text{Tr} [\mathbf{H}_{ij} \cdot \mathbf{S}_{ij}^{\text{1PI}}] + \mathcal{O}(s_4))$$

- plus distribution  $P_n(s_4) = \left[ \frac{1}{s_4} \ln^n \left( \frac{s_4}{m_t^2} \right) \right]_+$

- compute modified hard function: glue together one-loop helicity amplitudes for production [Badger, Sattler, Yundin] and decay (narrow-width approximation)
- soft functions and structure of RGE [Ferroglio et al; Ahrens et al.] not affected
- obtain approximate NLO (for consistency checks only) and NNLO corrections by expansion in  $\alpha_s$  → coefficients of plus distributions
- e.g. for PIM @ NNLL → NNLO:

$$\text{Tr} [\mathbf{H}_{ij} \cdot \mathbf{S}_{ij}] \sim D_3 P_3(z) + D_2 P_2(z) + D_1 P_1(z) + D_0 P_0(z) + C_0 \delta(1-z) + R(z)$$

- restore dependence on final-state particles → weight of events in Monte Carlo

$$D_i(M_{t\bar{t}}, \cos \theta) \rightarrow D_i(\{p_i\})$$

- different resummation, PIM and 1PI (and different approximations in phase space)
- we include

$$\text{Tr} [\mathbf{H}_{ij}^{(1)} \cdot \mathbf{S}_{ij}^{(1)}] \quad \text{fully} \quad \text{get } P_1, P_0 \text{ and } \delta \text{ terms}$$

$$\text{Tr} [\mathbf{H}_{ij}^{(0)} \cdot \mathbf{S}_{ij}^{(2)}] \quad \text{partially} \quad \text{get } P_3, P_2, P_1 \text{ and } P_0 \text{ terms, } \delta \text{ terms missing}$$

$$\text{Tr} [\mathbf{H}_{ij}^{(2)} \cdot \mathbf{S}_{ij}^{(0)}] \quad \text{not at all} \quad \delta \text{ terms missing}$$

successive improvements: approximate NLO (nLO) → NLO → approximate NNLO (nNLO)  
only in production part, decay always fixed NLO

$$d\sigma_{\text{full}}^{\text{nLO}} = (\Gamma_t^{\text{NLO}})^{-2} \left\{ \left( d\sigma_{t\bar{t}}^{(0)} + d\tilde{\sigma}_{t\bar{t}}^{(1)} \right) \otimes d\Gamma_{t \rightarrow l^+ \nu_l b}^{(0)} \otimes d\Gamma_{\bar{t} \rightarrow l^- \bar{\nu}_l \bar{b}}^{(0)} \right.$$

$$+ d\sigma_{t\bar{t}}^{(0)} \otimes d\Gamma_{t \rightarrow l^+ \nu_l b}^{(1)} \otimes d\Gamma_{\bar{t} \rightarrow l^- \bar{\nu}_l \bar{b}}^{(0)}$$

$$\left. + d\sigma_{t\bar{t}}^{(0)} \otimes d\Gamma_{t \rightarrow l^+ \nu_l b}^{(0)} \otimes d\Gamma_{\bar{t} \rightarrow l^- \bar{\nu}_l \bar{b}}^{(1)} \right\}$$

$$d\sigma_{\text{full}}^{\text{NLO}} = (\Gamma_t^{\text{NLO}})^{-2} \left\{ \left( d\sigma_{t\bar{t}}^{(0)} + d\sigma_{t\bar{t}}^{(1)} \right) \otimes d\Gamma_{t \rightarrow l^+ \nu_l b}^{(0)} \otimes d\Gamma_{\bar{t} \rightarrow l^- \bar{\nu}_l \bar{b}}^{(0)} \right.$$

$$\left. + \dots \text{decay corrections as for } d\sigma_{\text{full}}^{\text{nLO}} \right\}$$

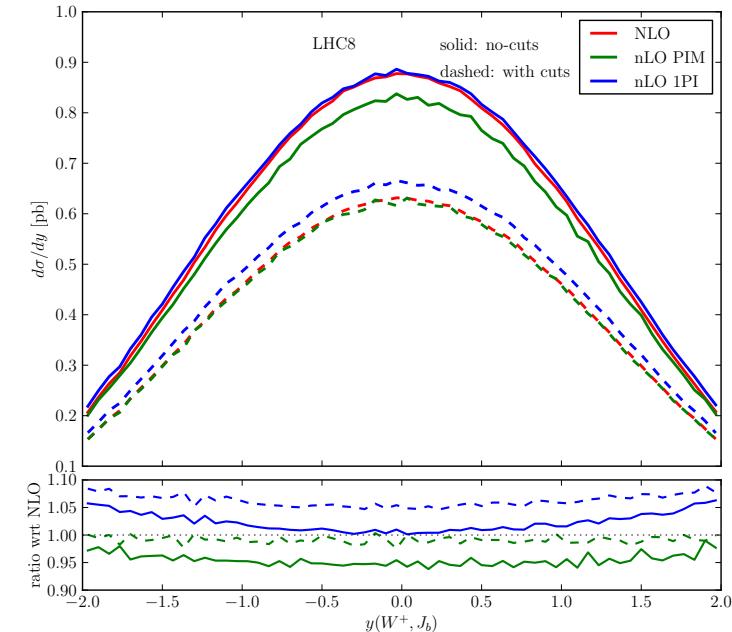
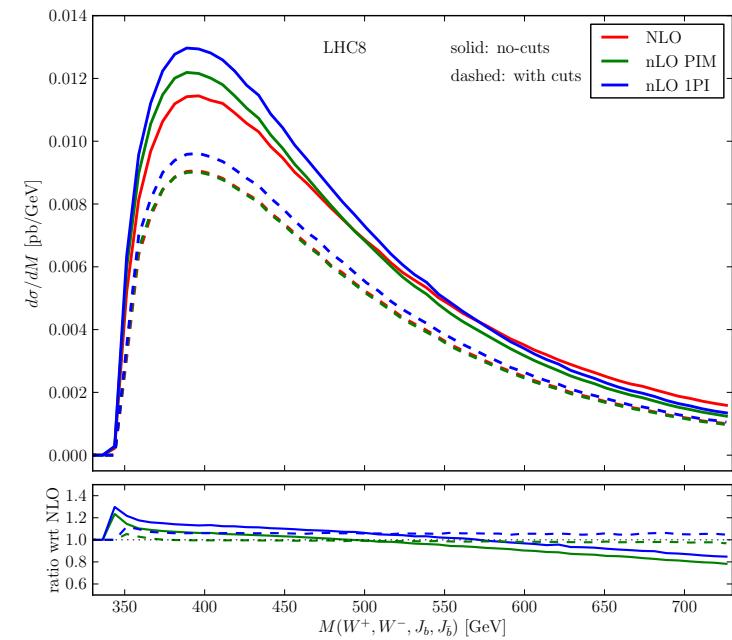
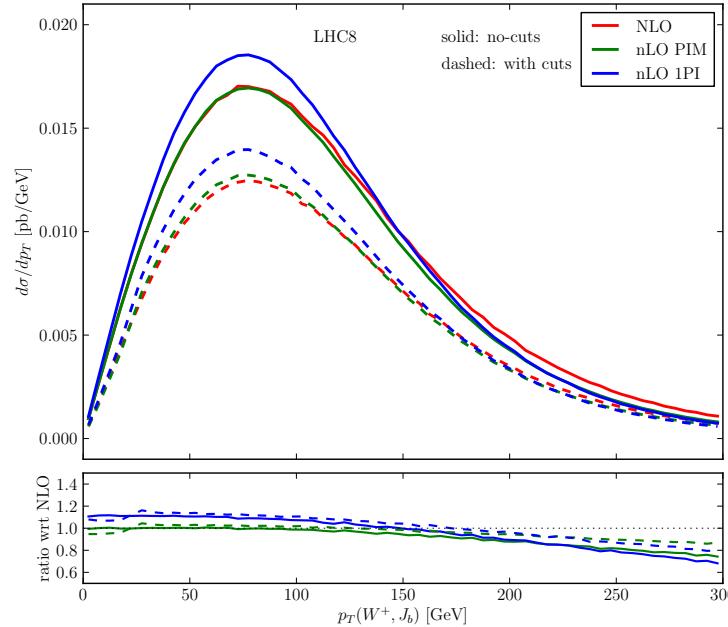
$$d\sigma_{\text{full}}^{\text{nNLO}} = (\Gamma_t^{\text{NLO}})^{-2} \left\{ \left( d\sigma_{t\bar{t}}^{(0)} + d\sigma_{t\bar{t}}^{(1)} + d\tilde{\sigma}_{t\bar{t}}^{(2)} \right) \otimes d\Gamma_{t \rightarrow l^+ \nu_l b}^{(0)} \otimes d\Gamma_{\bar{t} \rightarrow l^- \bar{\nu}_l \bar{b}}^{(0)} \right.$$

$$\left. + \dots \text{decay corrections as for } d\sigma_{\text{full}}^{\text{nLO}} \right\}$$

For validation of nLO and nNLO approximation 'switch off' decay corrections

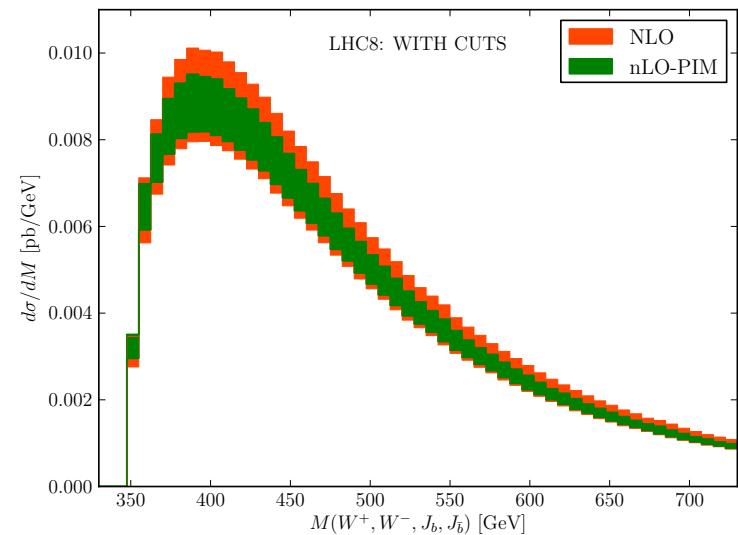
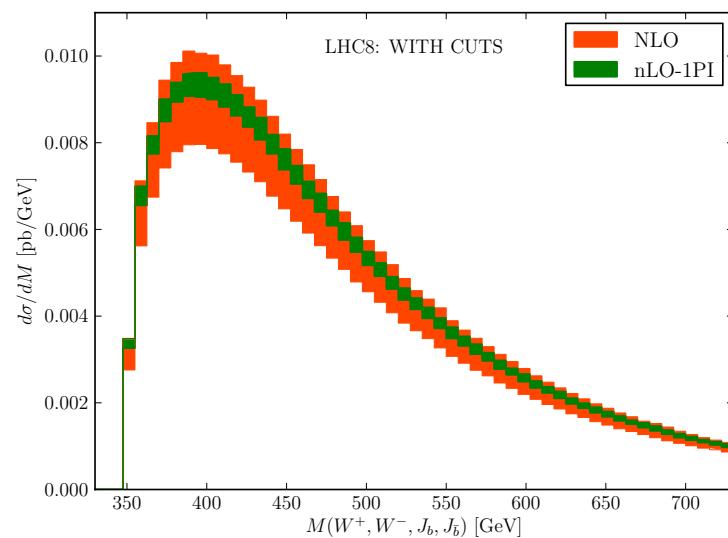
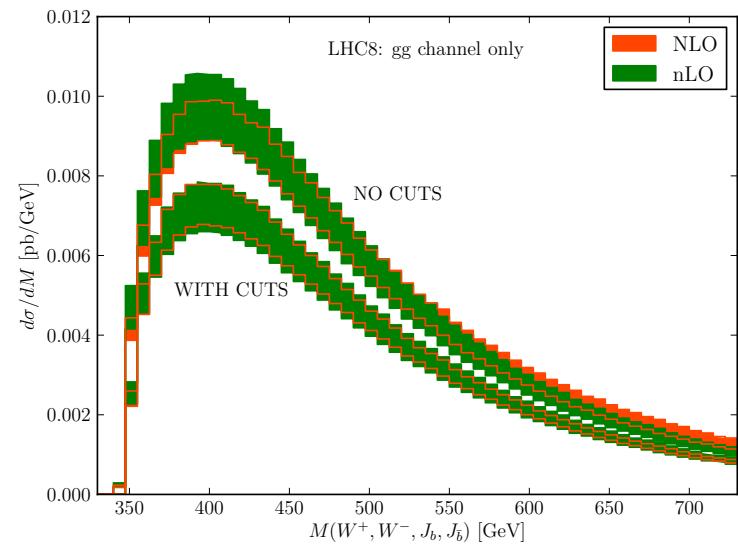
## check (in)dependence on kinematics

- compute  $M_{t\bar{t}}$  (right),  $p_T(t)$  (bottom left) and  $y(t)$  (bottom right) for LHC 8
- compute **NLO**, **nLO PIM**, **nLO 1PI**
- compute with (dashed) and without (solid) cuts
- even “wrong” resummation gives reasonable results
- PIM seems to do better than 1PI !?



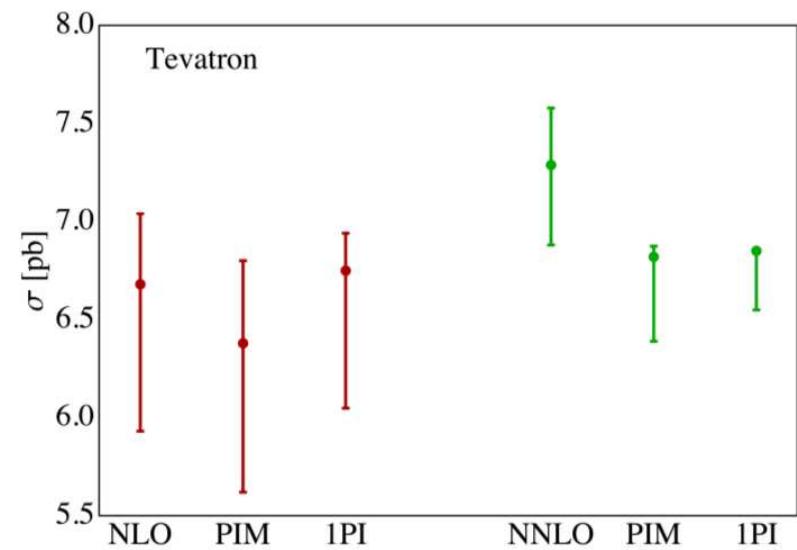
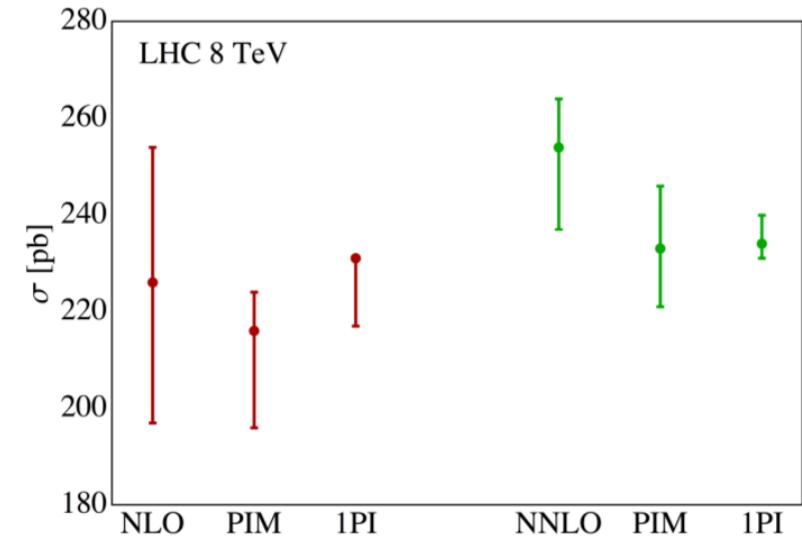
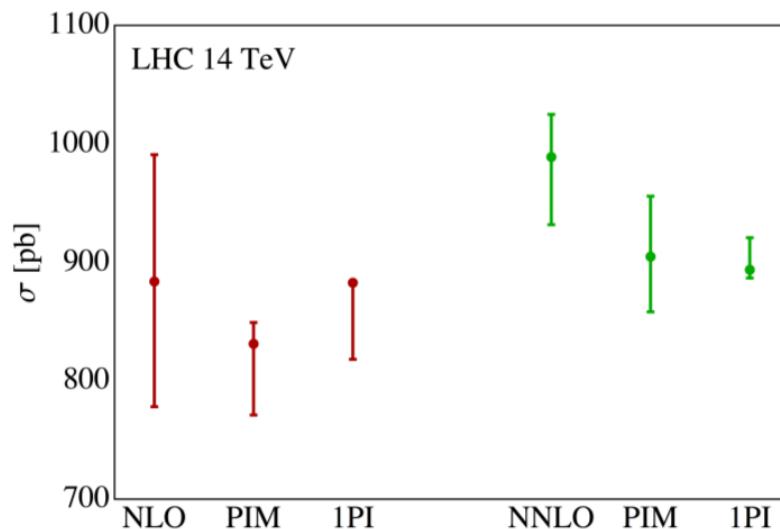
## uncertainty bands (for $M_{t\bar{t}}$ at LHC 8)

- take envelope of scale dependence  $m_t/2 \leq \mu \leq 2 m_t$  and {PIM, 1PI}
- overestimates uncertainty for single channel (*gg* right) → to compensate 'missing' other channels (*qg*)
- 1PI and PIM separately (bottom) give consistent results (scale dependence of 1PI alone "too small")



## check quality of nNLO approximation

- compare total cross section nNLO (PIM and 1PI) to NNLO [Top++]
- scale variation  $m_t/2 \leq \mu \leq 2 m_t$
- for LHC 8 and LHC 14 nLO and nNLO give reasonable approximations (a bit low)
- for Tevatron nNLO has only marginal overlap with NNLO



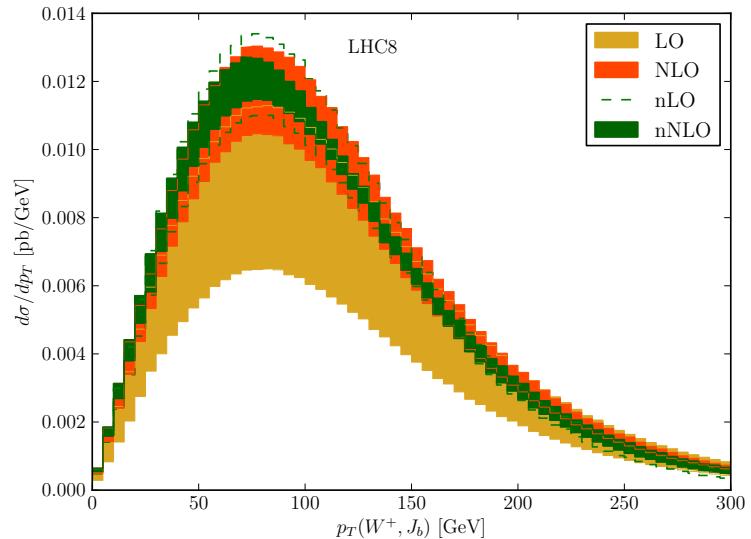
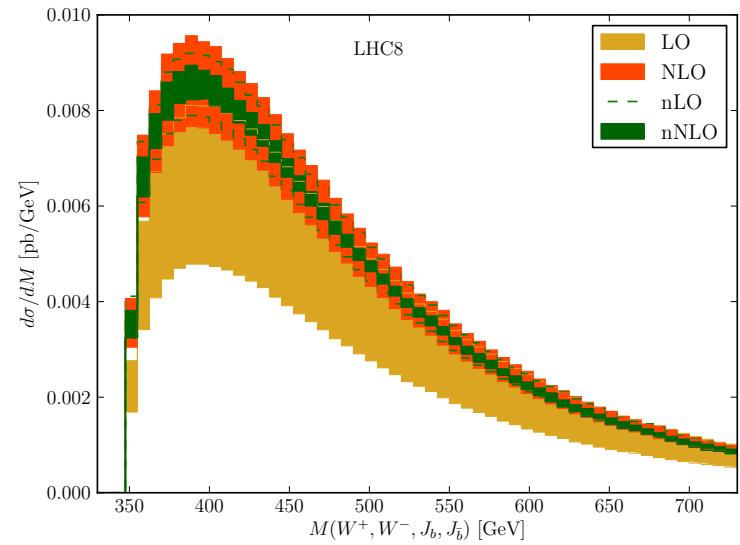
- cluster final state partons into jets
- reconstruct top  $t \doteq J_b + \ell + \nu$
- MSTW2008 NLO/NNLO pdf
- cuts:  $p_T(J_{b/\bar{b}}) > 15 \text{ GeV}$   
 $E_T(\ell^\pm) > 15 \text{ GeV}$   
 $E_T > 20 \text{ GeV}$   
 $M(W^+, W^-, J_b, J_{\bar{b}}) > 350 \text{ GeV}$

consider  $M_{tt} \doteq M(W^+, W^-, J_b, J_{\bar{b}})$

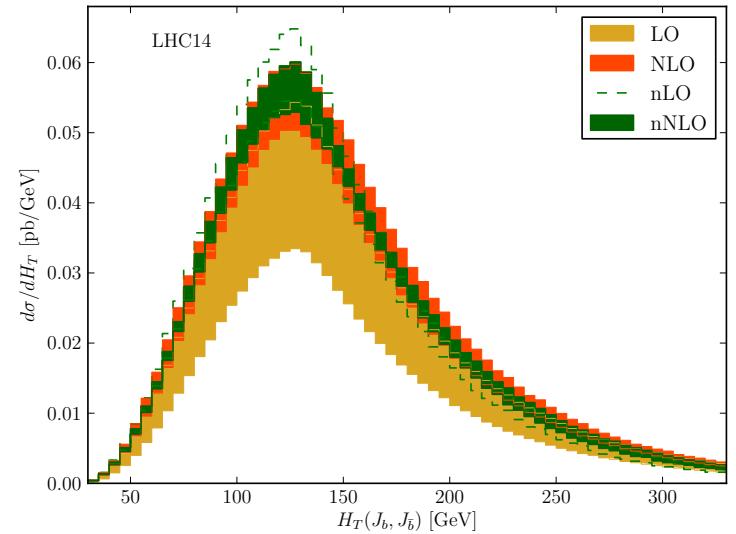
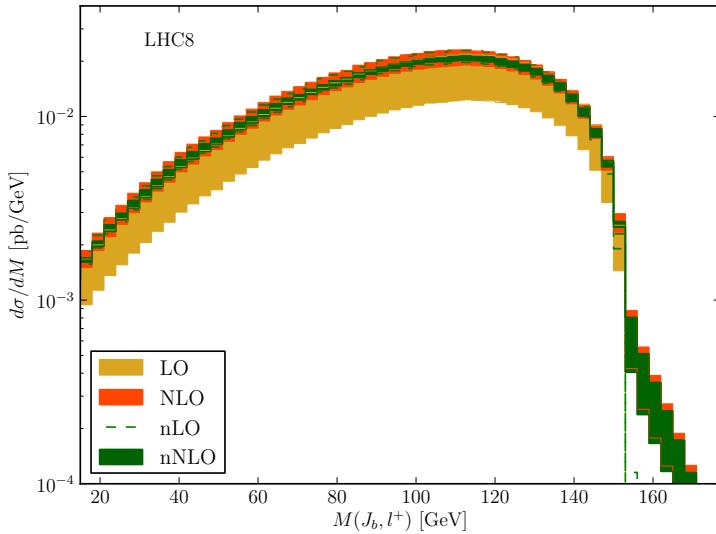
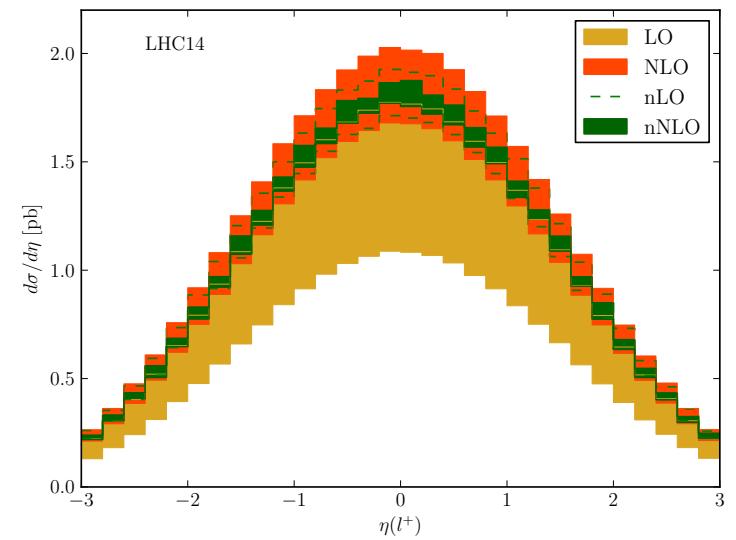
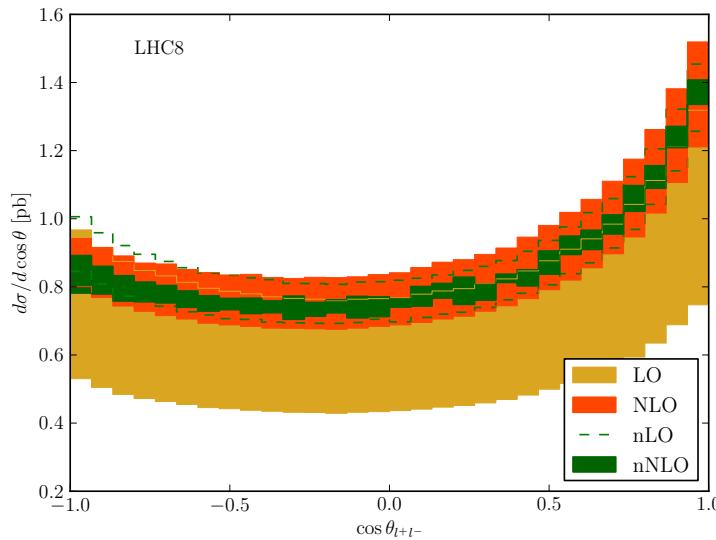
consider  $p_T(t) \doteq p_T(J_b, W^+)$

stable perturbative behaviour

theory error band: envelope of scale variation **and** {PIM, 1PI} implementations



## arbitrary distributions for LHC 8 and LHC 14



- we have generalized PIM and 1PI NNLL resummation to include top (and  $W$ ) decay in narrow width approximation
- we obtain a parton level Monte Carlo with approximate NNLO corrections for production of  $t\bar{t}$  and decay included at NLO
- generic features of resummation **remarkably robust** under change PIM  $\leftrightarrow$  1PI  
 $\Rightarrow$  empirical evidence that results can be used for other observables than  $M_{tt}$ ,  $p_T(t)$  and  $y(t)$  and allow for cuts to be applied
- theoretical error must include PIM  $\leftrightarrow$  1PI variation (as well as scale variation)
- further improvements
  - note: nLO approximation to NLO is better than nNLO to NNLO ( $\delta$  terms missing, would need 2-loop soft function and 2-loop virtual correction with spin information)
  - mismatch between production and decay  
 $\Rightarrow$  include decay at NNLO [Gao, Li, Zhu; Brucherseifer, Caola, Melnikov]
  - study impact of relaxing approximations ( $z = 1$ ,  $s_4 = 0$ ) made in phase space integration
  - other processes