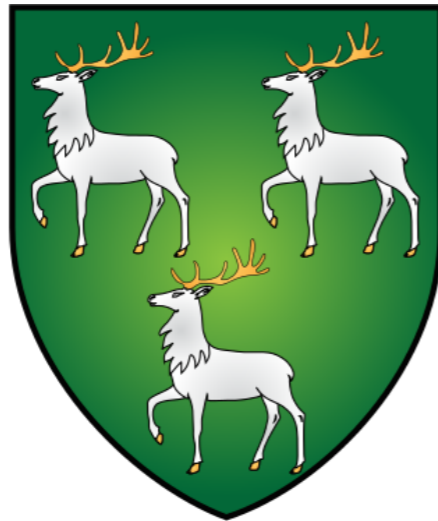


# Top-quark measurements at LHCb

Rhorry Gauld



# Contents

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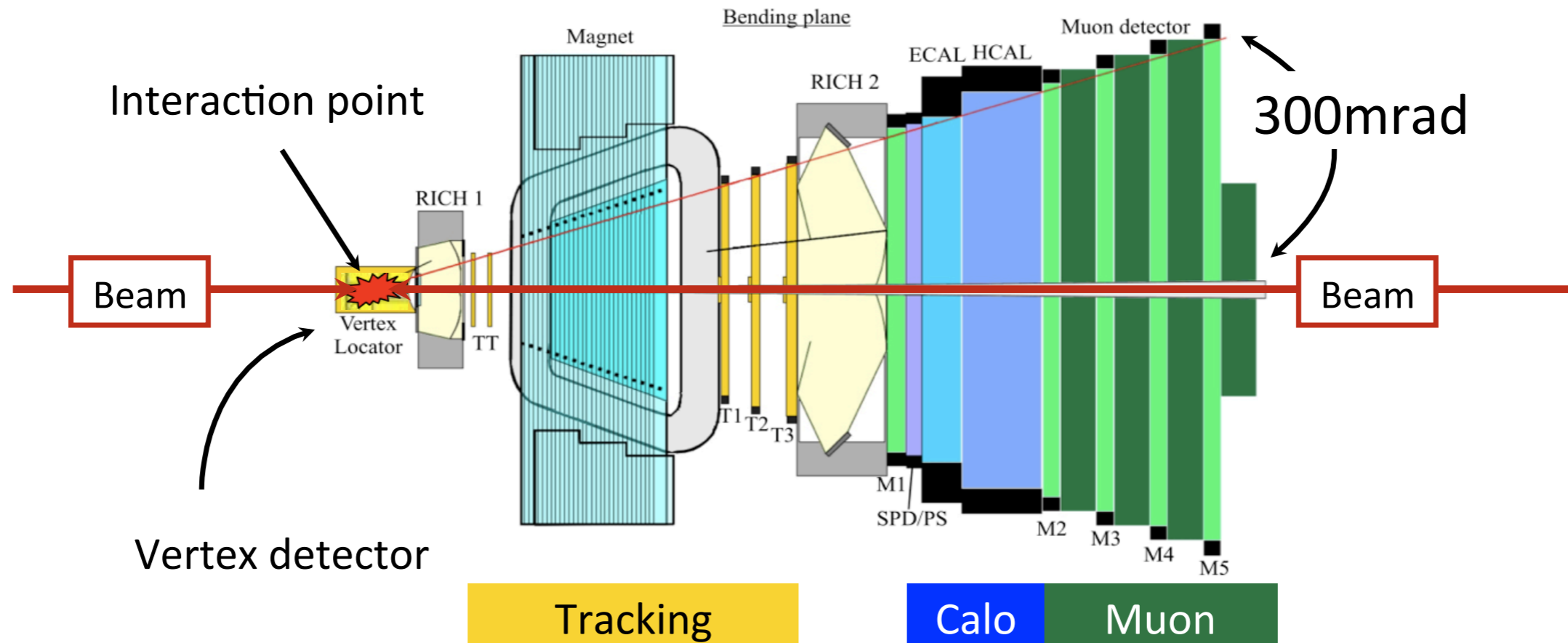
- Introduction and motivations
- Feasibility of cross section measurements
  - arXiv 1311.1810
- Charge asymmetry measurements
  - coming soon

**D  
O N  
O T B  
E L I E  
V E A T H  
I N G H A I  
S C H S A Y S**

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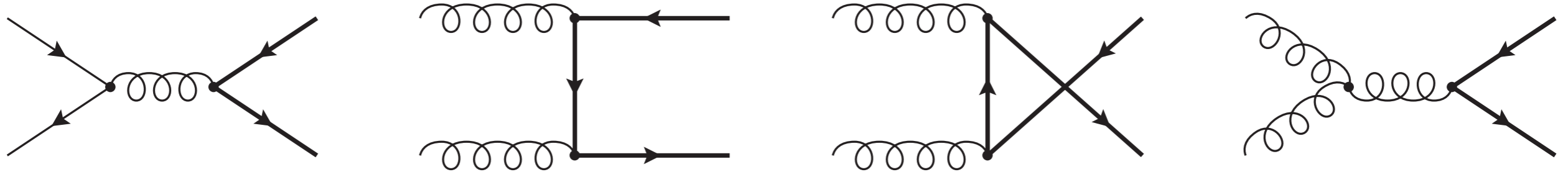
[www.eyechartmaker.com](http://www.eyechartmaker.com)

# LHCb - important details

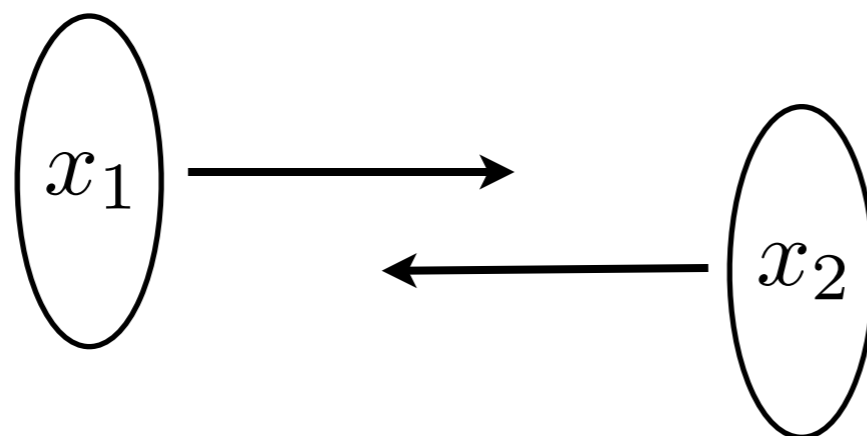


- LHCb: a general purpose detector instrumented within  $2 \leq \eta \leq 5$
- Recorded/Potential luminosity:
- (2011): 1.1  $\text{fb}^{-1}$   $\sqrt{s} = 7 \text{ TeV}$
  - (2012): 2.1  $\text{fb}^{-1}$   $\sqrt{s} = 8 \text{ TeV}$
  - (2015-2017):  $\sim 5 \text{ fb}^{-1}$   $\sqrt{s} = 13 \text{ TeV}$
  - (2020-2030):  $\sim 50 \text{ fb}^{-1}$   $\sqrt{s} = 14 \text{ TeV}$

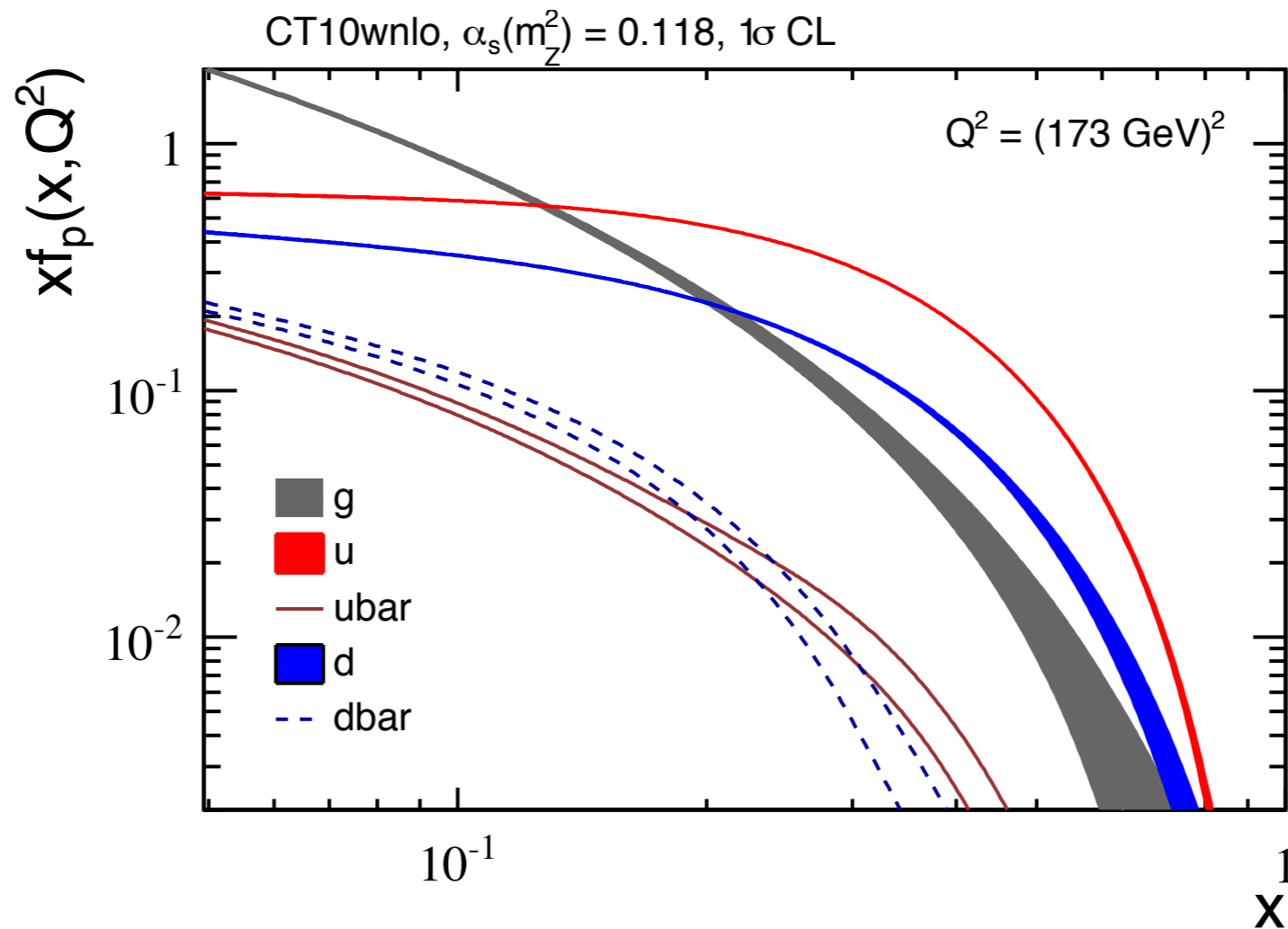
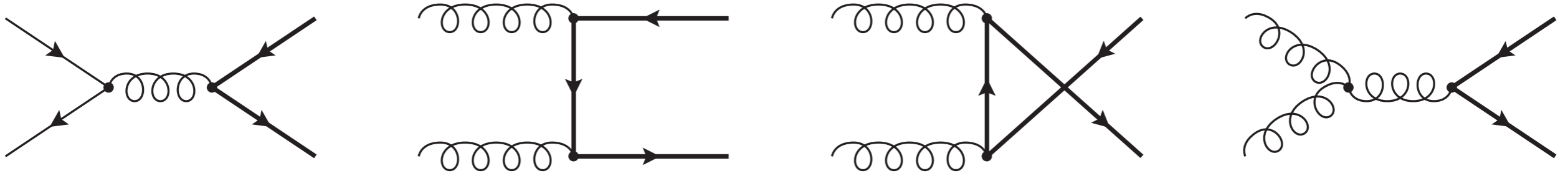
# Why study forward ttbar?



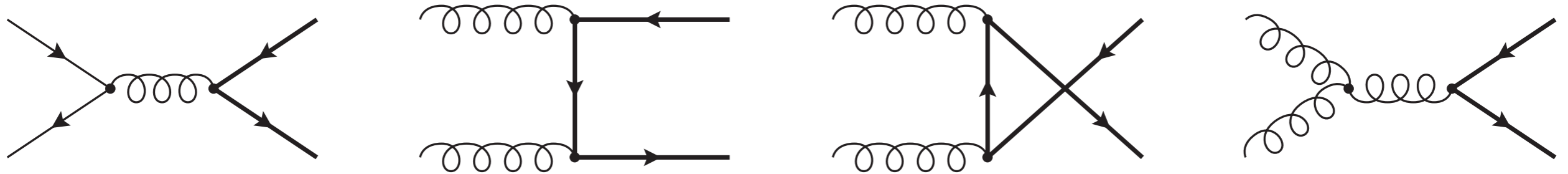
$$x_{1,(2)} = \frac{m_T}{\sqrt{\hat{s}}} (e^{(-)y_3} + e^{(-)y_4})$$



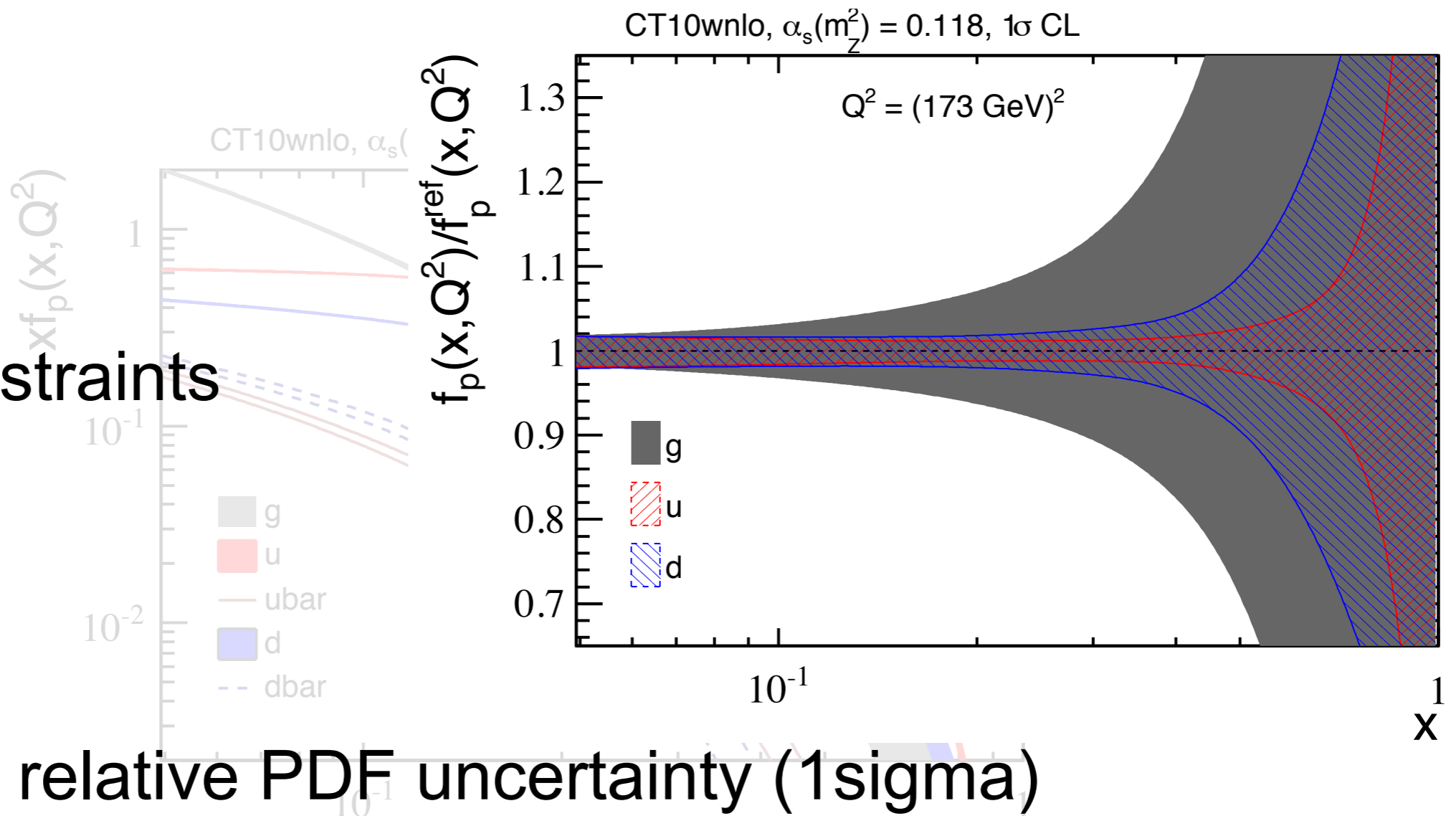
# Why study forward ttbar?



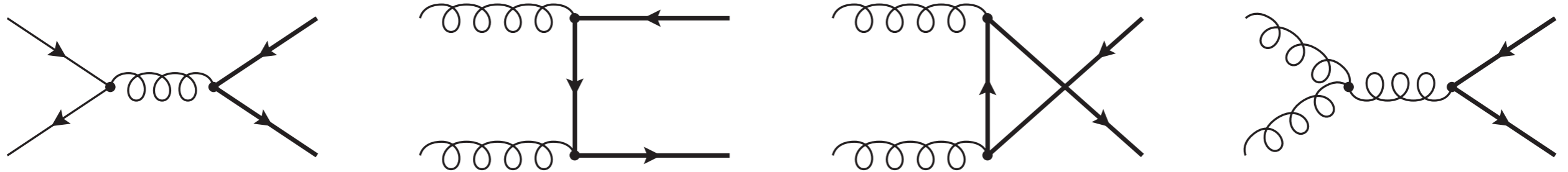
# Why study forward $t\bar{t}$ ?



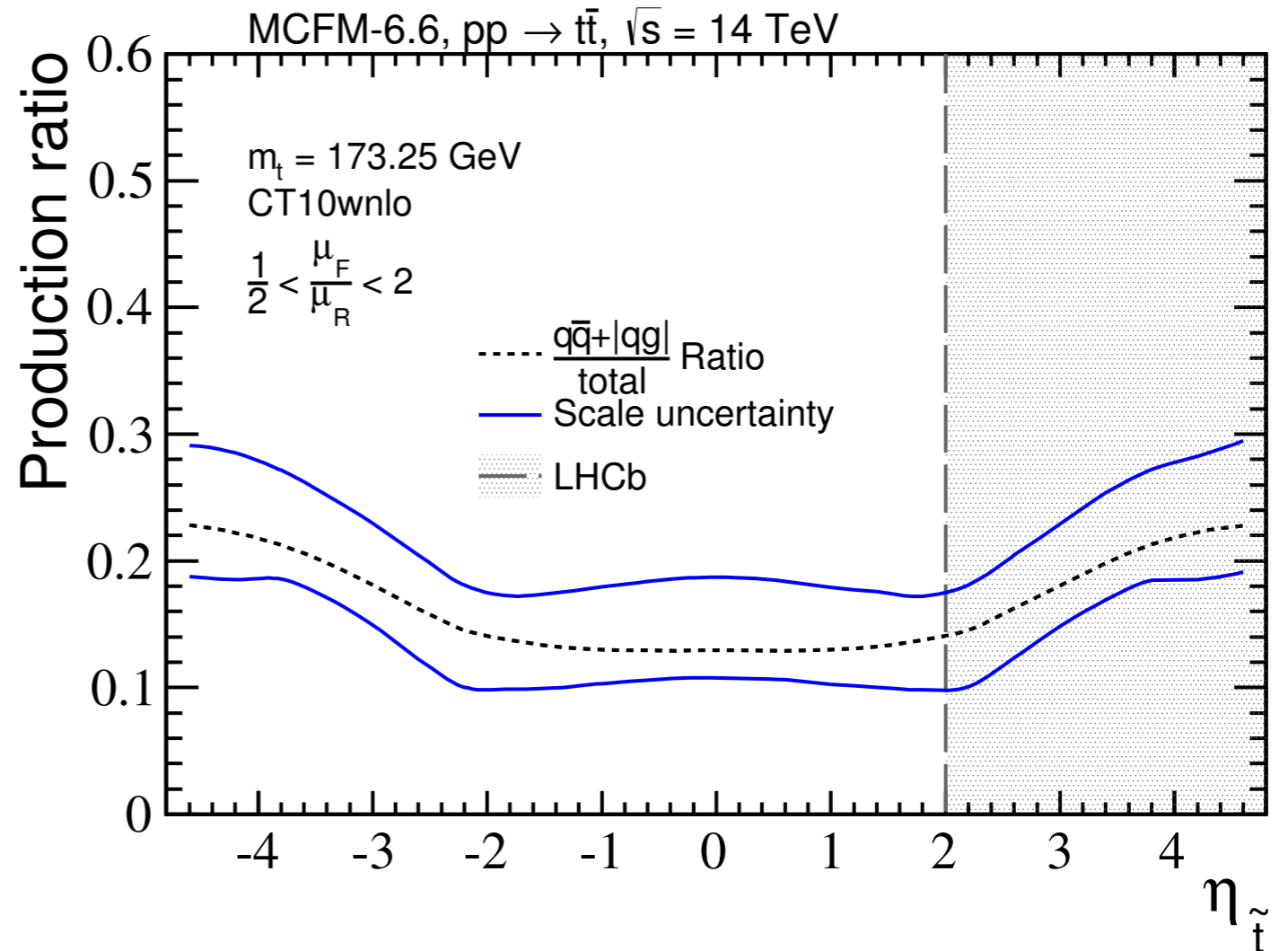
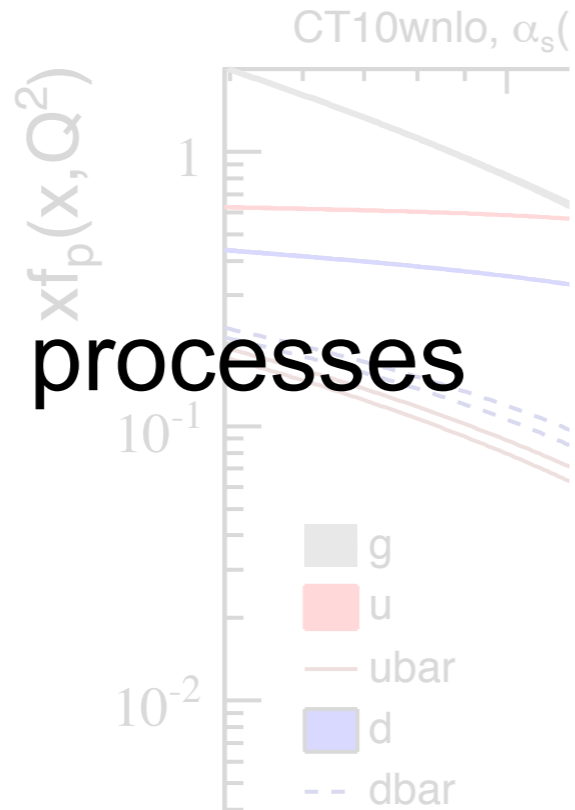
## 1) PDF constraints



# Why study forward ttbar?



## 2) q-initiated processes



$|q\bar{q}|/\text{total}$  for top quark pseudorapidity distribution

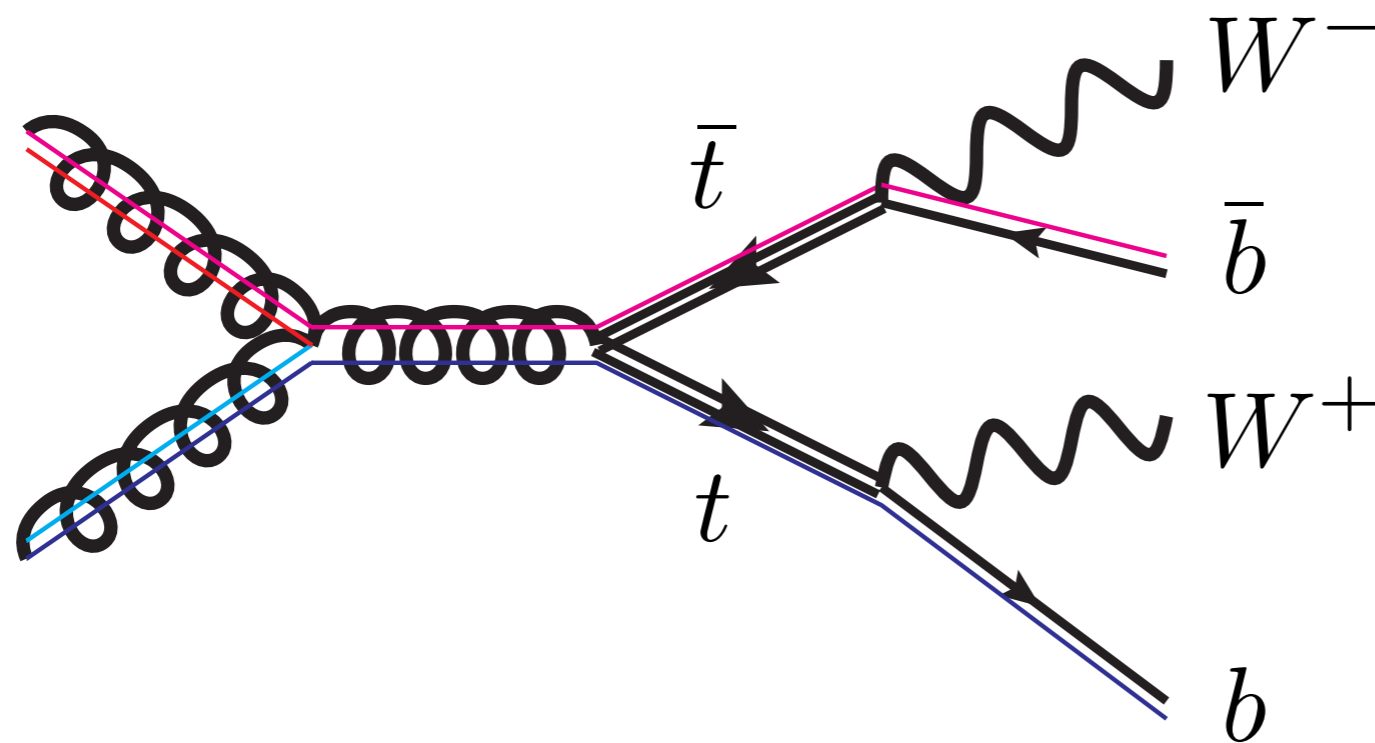
# cross section measurements



# Final state selection

Top studies at LHCb proposed here,  
[arXiv:1103.3747](#) A. Kagan, J. Kamenik, G. Perez, S. Stone  
[arXiv:1311.1810](#) RG (this work)

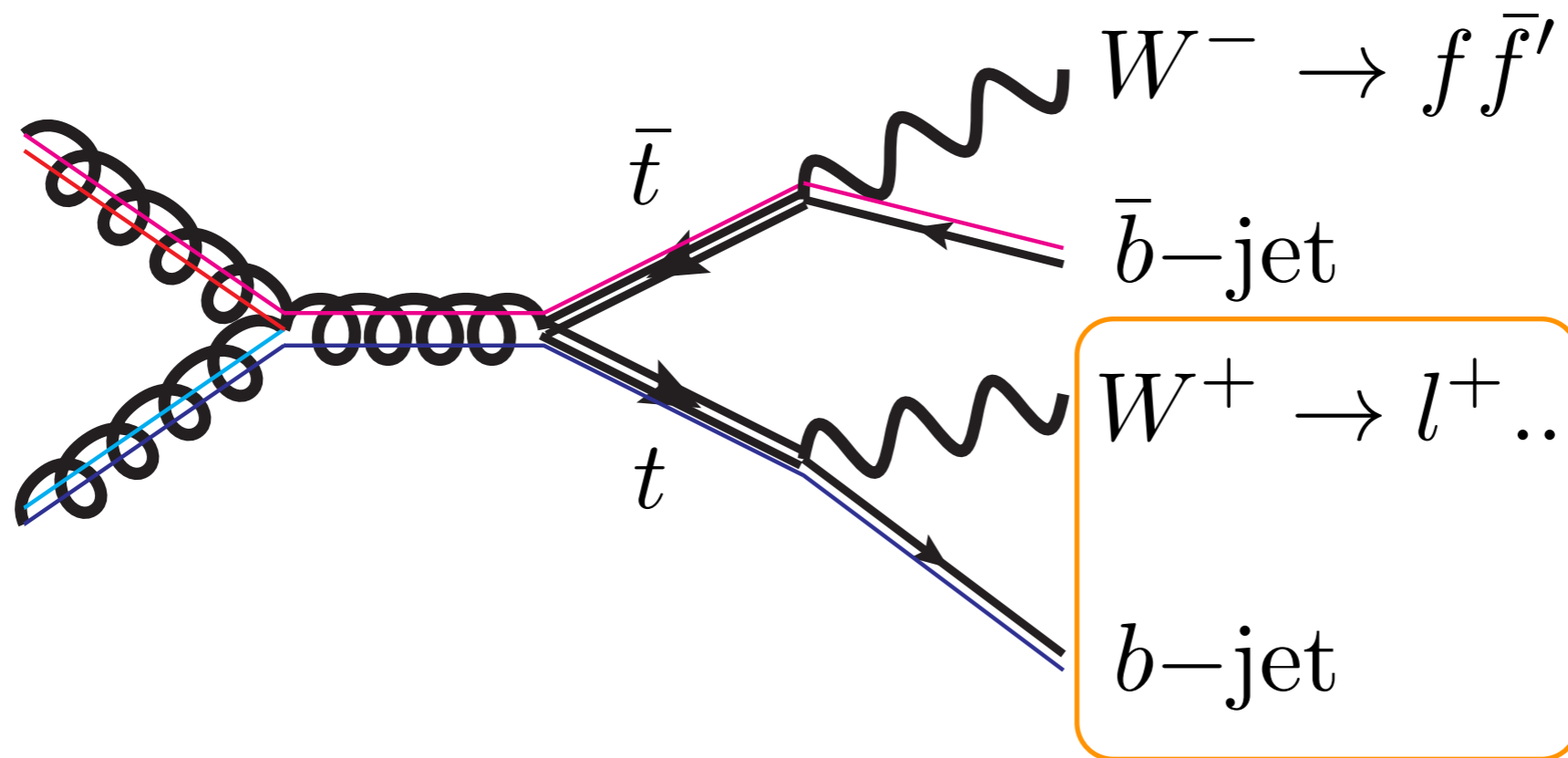
## Have to select realistic final states



# Final state selection

Top studies at LHCb proposed here,  
[arXiv:1103.3747](#) A. Kagan, J. Kamenik, G. Perez, S. Stone  
[arXiv:1311.1810](#) RG (this work)

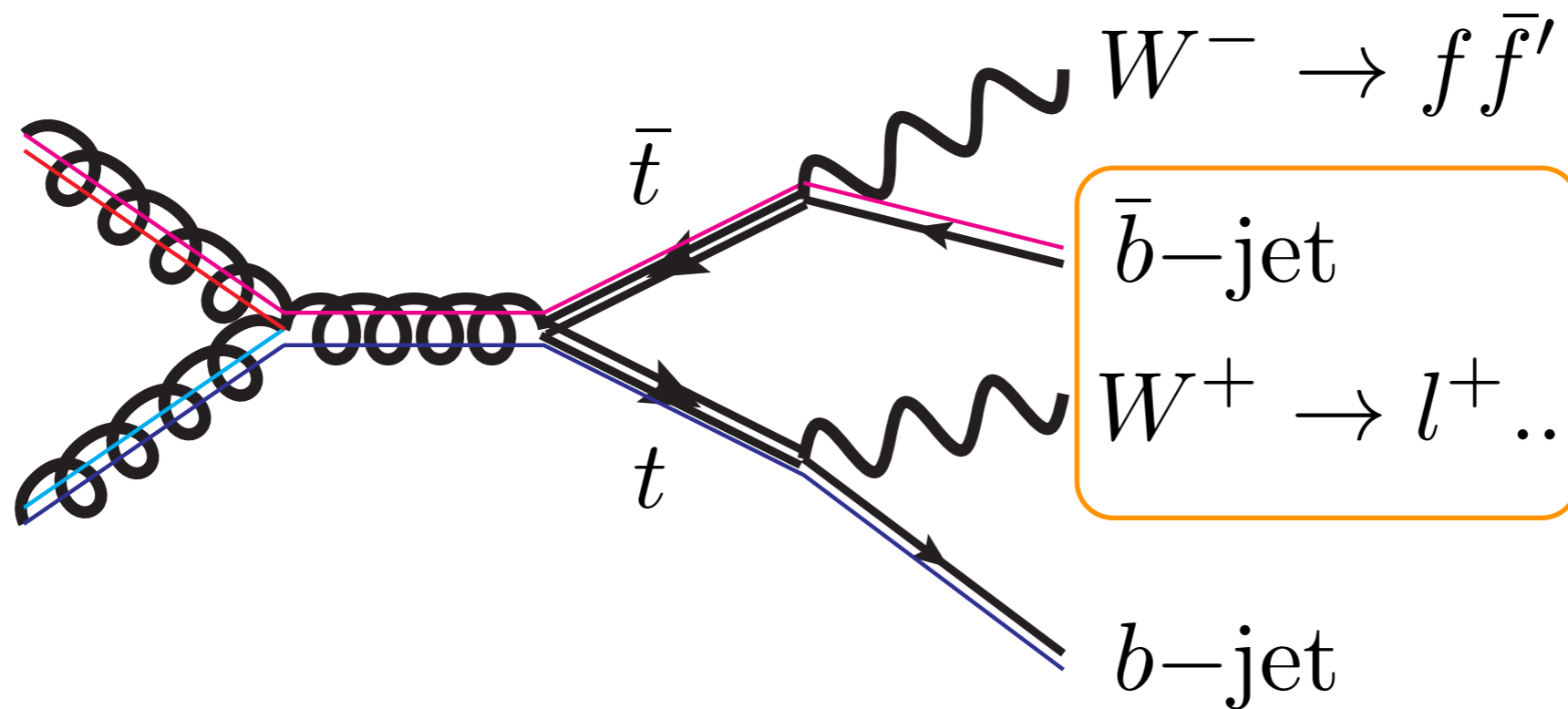
## Have to select realistic final states



# Final state selection

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## Have to select realistic final states



# Final state selection

Top studies at LHCb proposed here,  
[arXiv:1103.3747](#) A. Kagan, J. Kamenik, G. Perez, S. Stone  
[arXiv:1311.1810](#) RG (this work)

single-lepton  $t\bar{t} \rightarrow l^{\mp} b X$

di-lepton  $t\bar{t} \rightarrow e^{\pm} \mu^{\mp} b X$

# Single-lepton

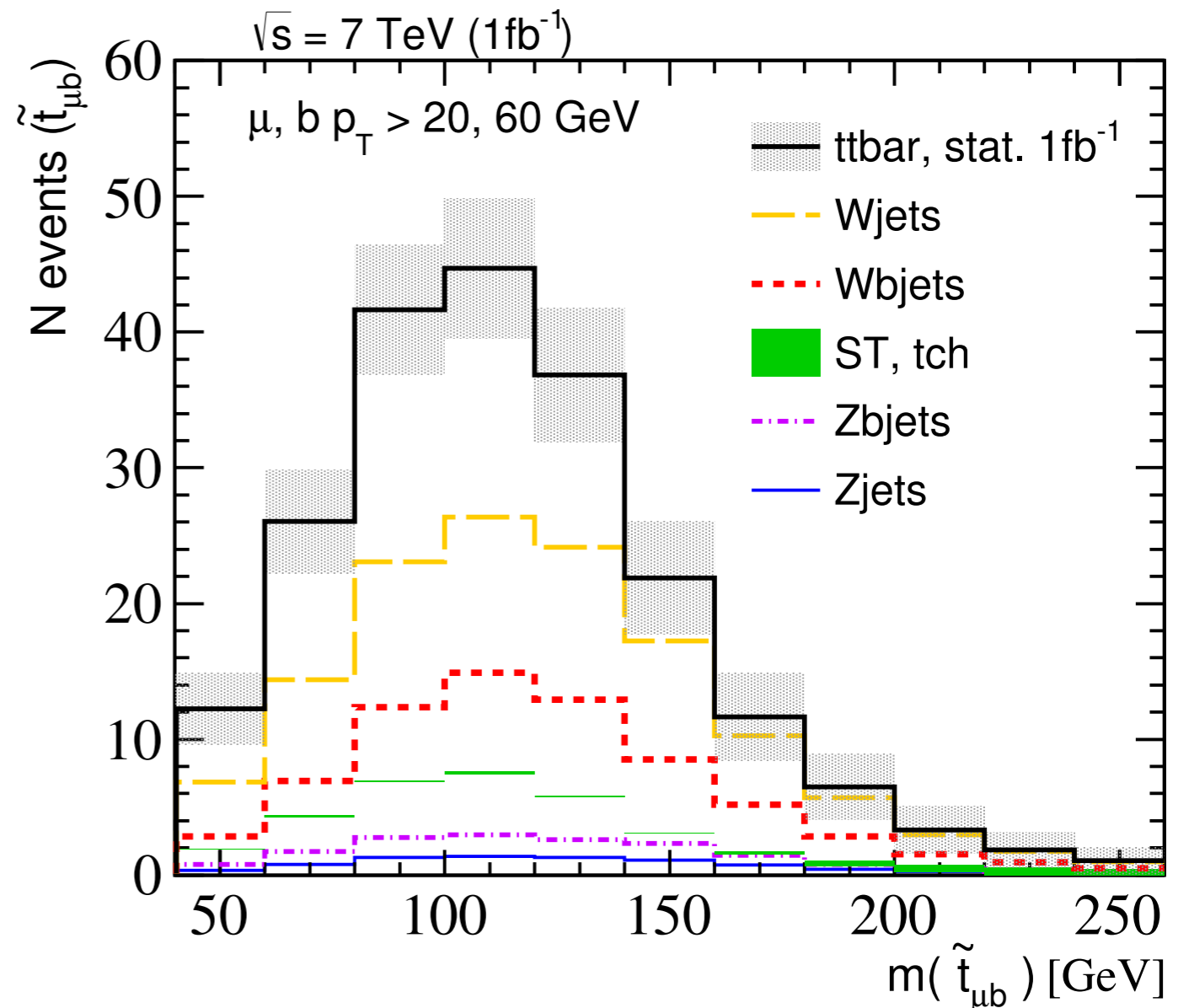
- generate samples (**POWHEG**) and match to parton shower (**Pythia8176**)
- apply realistic cuts: **l pT > 20 GeV** and **b pT > 60 GeV**
- apply b-tagging efficiencies: 70% efficiency and 1% mis-tag (non b-jet)
- apply muon efficiencies: 75% (trigger, identification, reconstruction)
- apply muon isolation:  $dR(\mu, j/b) > 0.5$

$7 \text{ TeV}$

$l^\pm b$

N events expected

2011 - 1 fb



# Single-lepton

- generate samples (**POWHEG**) and match to parton shower (**Pythia8176**)
- apply realistic cuts: **l pT > 20 GeV** and **b pT > 60 GeV**
- apply b-tagging efficiencies: 70% efficiency and 1% mis-tag (non b-jet)
- apply muon efficiencies: 75% (trigger, identification, reconstruction)
- apply muon isolation:  $dR(\mu, j/b) > 0.5$

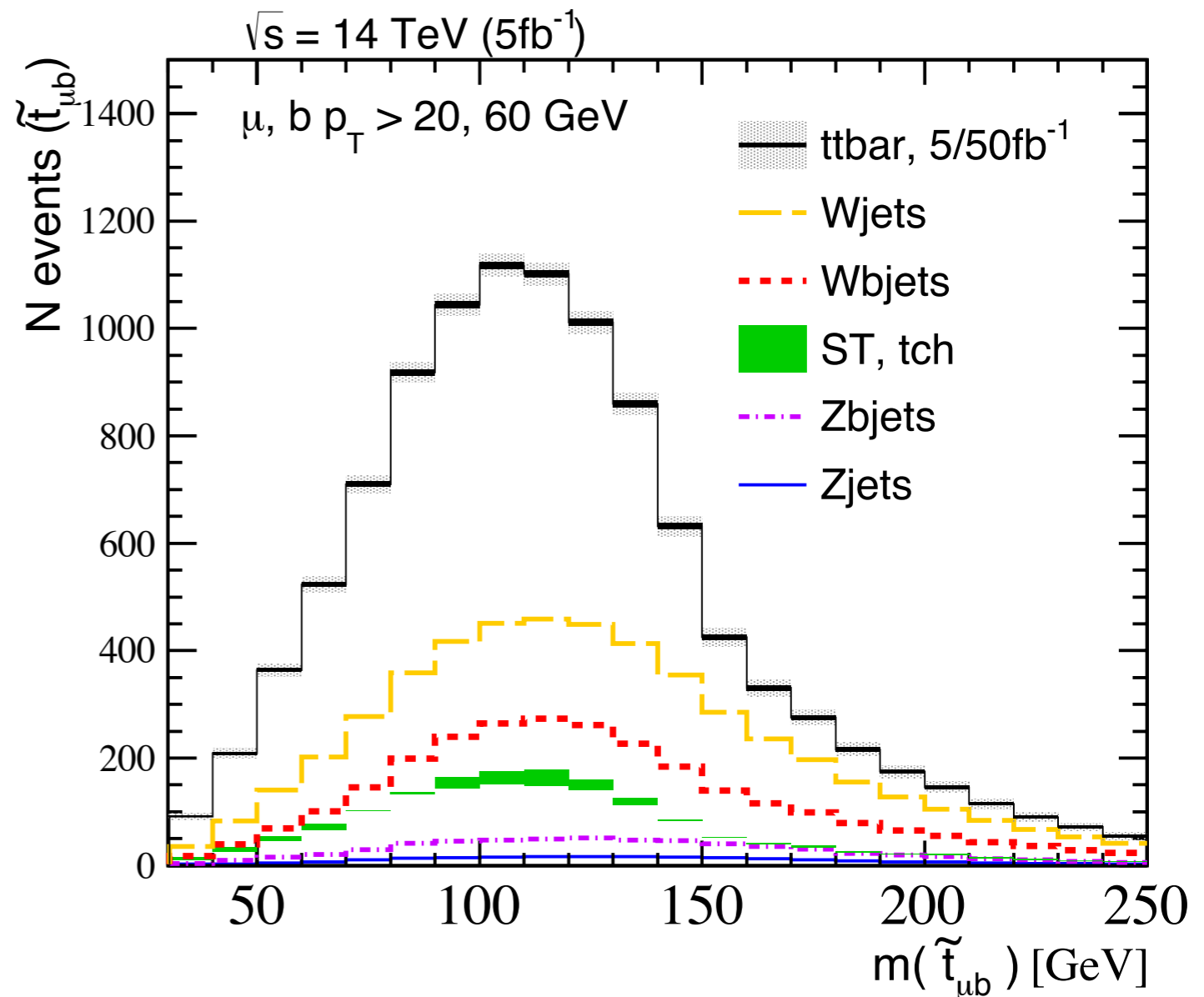
$14 \text{ TeV}$

$l^\pm b$

N events expected

2017 - 5 fb

2030 - 50 fb



# Di-lepton

- generate samples (**POWHEG**) and match to parton shower (**Pythia8176**)
- apply realistic cuts:  $\mu/e/b$   $p_T > 20$  GeV
- apply b-tagging efficiencies: 90% efficiency and 5% mis-tag (non b-jet)
- apply muon efficiencies: 75% (trigger, identification, reconstruction)
- apply muon isolation:  $dR(\mu, j/b) > 0.5$

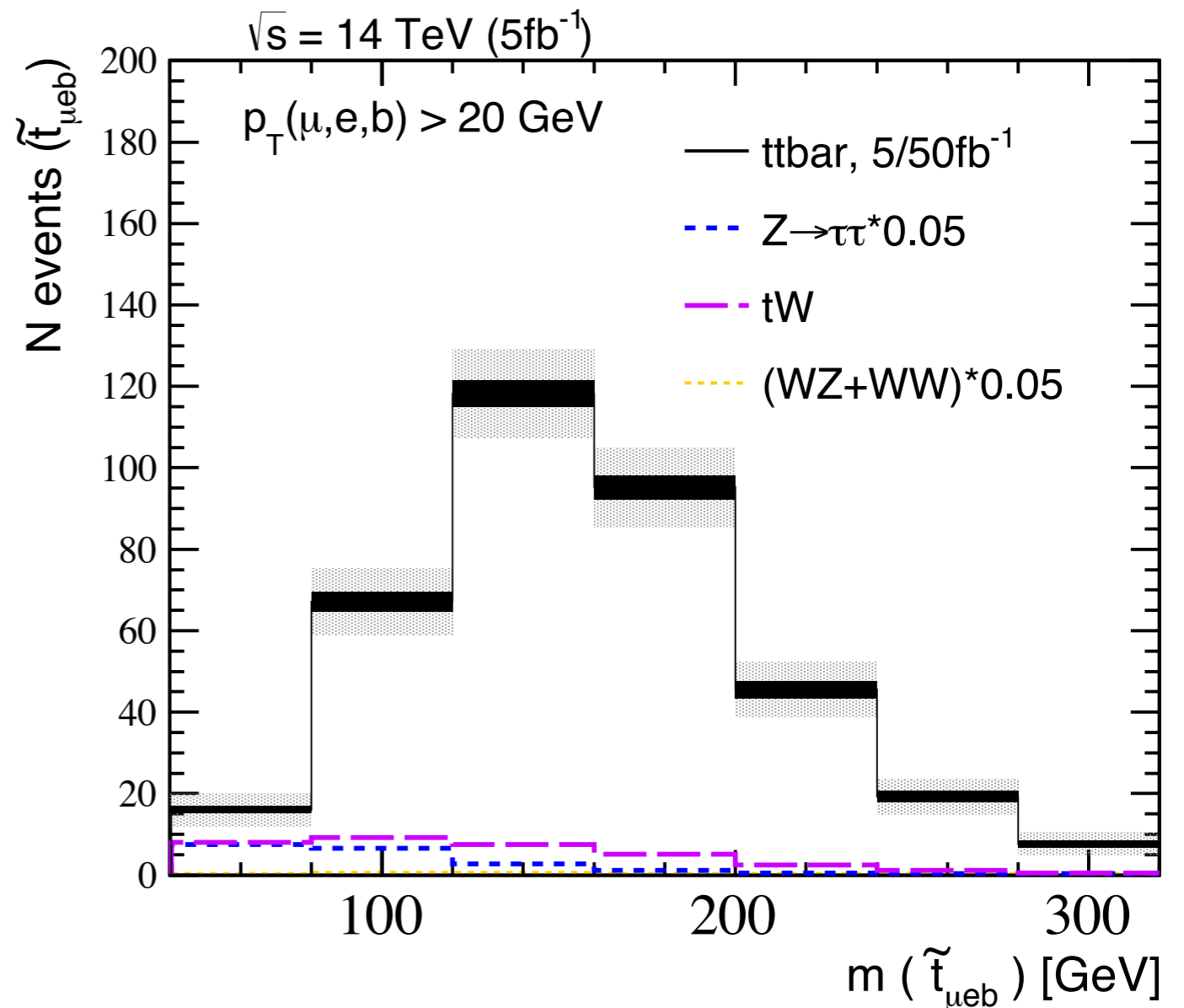
$14$  TeV

$\mu e b$

N events expected

2017 - 5 fb

2030 - 50 fb

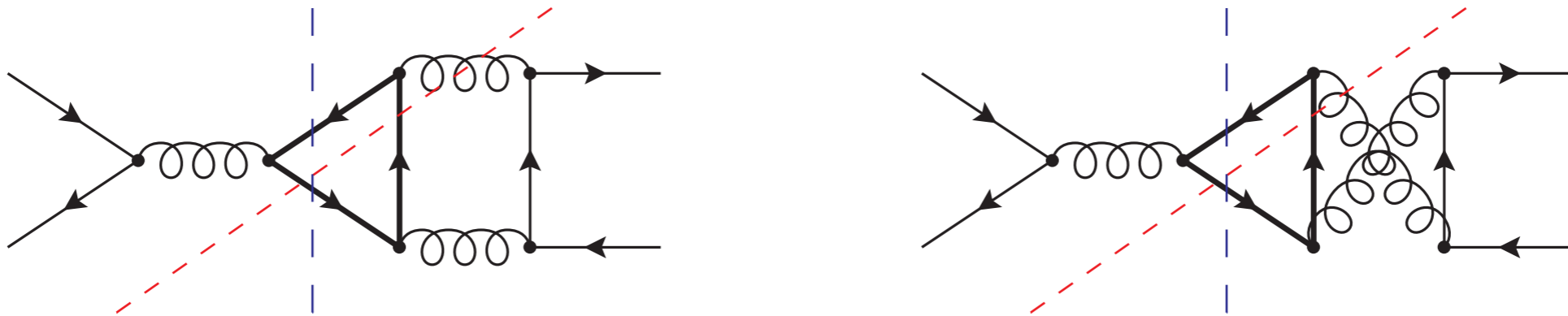


# leptonic asymmetries for LHCb (all at 14 TeV)



# Overview

$$\sigma_{(a)s} = \frac{1}{2} \int_0^1 d \cos \theta \left( \frac{d\sigma^{pp \rightarrow t\bar{t}X}}{d \cos \theta} \underset{(-)}{+} \frac{d\sigma^{pp \rightarrow \bar{t}tX}}{d \cos \theta} \right)$$



$$\sigma_a^{s(1)} = \frac{1}{2} \int_0^1 d \cos \theta \left( \left( \mathcal{C}_{\text{left}} \frac{d\sigma_{\text{left}}(p_3, p_4)}{d \cos \theta} + \mathcal{C}_{\text{right}} \frac{d\sigma_{\text{right}}(p_3, p_4)}{d \cos \theta} \right) - \left( \mathcal{C}_{\text{left}} \frac{d\sigma_{\text{left}}(p_4, p_3)}{d \cos \theta} + \mathcal{C}_{\text{right}} \frac{d\sigma_{\text{right}}(p_4, p_3)}{d \cos \theta} \right) \right)$$

Phys. Lett. B195(1987) 74 F. Halzen, P. Hoyer, and C. Kim

Nucl. Phys. B327 (1989) 49 P. Nason, S. Dawson, and R. K. Ellis

[arXiv:hep-ph/9802268](https://arxiv.org/abs/hep-ph/9802268), [arXiv:hep-ph/9807420](https://arxiv.org/abs/hep-ph/9807420) J.H.Kuhn, G. Rodrigo

... and many others since

# Structure in perturbation theory

$$\begin{aligned}
 A_c &= \frac{\alpha_s^3 \sigma_a^{s(1)} + \alpha_s^4 \sigma_a^{s(2)} + \alpha_s^2 \alpha_e \sigma_a^{e(1)} + \alpha_s^2 \alpha_w \sigma_a^{w(1)} + \dots}{\alpha_s^2 \sigma_s^{s(0)} + \alpha_s^3 \sigma_s^{s(1)} + \alpha_s^4 \sigma_s^{s(2)} + \dots}, \\
 &= \alpha_s \frac{\sigma_a^{s(1)}}{\sigma_s^{s(0)}} + \alpha_e \frac{\sigma_a^{e(1)}}{\sigma_s^{s(0)}} + \alpha_w \frac{\sigma_a^{w(1)}}{\sigma_s^{s(0)}} + \alpha_s^2 \frac{1}{\sigma_s^{s(0)}} \left( \sigma_a^{s(2)} - \frac{\sigma_a^{s(1)} \sigma_s^{s(1)}}{\sigma_s^{s(0)}} \right) \dots
 \end{aligned}$$

# Structure in perturbation theory

$$A_c = \frac{\alpha_s^3 \sigma_a^{s(1)} + \alpha_s^4 \sigma_a^{s(2)} + \alpha_s^2 \alpha_e \sigma_a^{e(1)} + \alpha_s^2 \alpha_w \sigma_a^{w(1)} + \dots}{\alpha_s^2 \sigma_s^{s(0)} + \alpha_s^3 \sigma_s^{s(1)} + \alpha_s^4 \sigma_s^{s(2)} + \dots},$$

$$= \alpha_s \frac{\sigma_a^{s(1)}}{\sigma_s^{s(0)}} + \alpha_e \frac{\sigma_a^{e(1)}}{\sigma_s^{s(0)}} + \alpha_w \frac{\sigma_a^{w(1)}}{\sigma_s^{s(0)}} + \alpha_s^2 \frac{1}{\sigma_s^{s(0)}} \left( \frac{\sigma_a^{s(2)}}{\sigma_s^{s(0)}} - \frac{\sigma_a^{s(1)} \sigma_s^{s(1)}}{\sigma_s^{s(0)}} \right) \dots$$

# Structure in perturbation theory

$$A_c = \frac{\alpha_s^3 \sigma_a^{s(1)} + \alpha_s^4 \sigma_a^{s(2)} + \alpha_s^2 \alpha_e \sigma_a^{e(1)} + \alpha_s^2 \alpha_w \sigma_a^{w(1)} + \dots}{\alpha_s^2 \sigma_s^{s(0)} + \alpha_s^3 \sigma_s^{s(1)} + \alpha_s^4 \sigma_s^{s(2)} + \dots},$$

$$= \alpha_s \frac{\sigma_a^{s(1)}}{\sigma_s^{s(0)}} + \alpha_e \frac{\sigma_a^{e(1)}}{\sigma_s^{s(0)}} + \alpha_w \frac{\sigma_a^{w(1)}}{\sigma_s^{s(0)}} + \alpha_s^2 \frac{1}{\sigma_s^{s(0)}} \left( \frac{\sigma_a^{s(2)}}{\sigma_s^{s(0)}} - \frac{\sigma_a^{s(1)} \sigma_s^{s(1)}}{\sigma_s^{s(0)}} \right) \dots$$

NLO in production and decay (MCFM)  
[arXiv:1204.1513](https://arxiv.org/abs/1204.1513) J. Campbell and R. K. Ellis

# Structure in perturbation theory

$$A_c = \frac{\alpha_s^3 \sigma_a^{s(1)} + \alpha_s^4 \sigma_a^{s(2)} + \alpha_s^2 \alpha_e \sigma_a^{e(1)} + \alpha_s^2 \alpha_w \sigma_a^{w(1)} + \dots}{\alpha_s^2 \sigma_s^{s(0)} + \alpha_s^3 \sigma_s^{s(1)} + \alpha_s^4 \sigma_s^{s(2)} + \dots},$$

$$= \alpha_s \frac{\sigma_a^{s(1)}}{\sigma_s^{s(0)}} + \alpha_e \frac{\sigma_a^{e(1)}}{\sigma_s^{s(0)}} + \alpha_w \frac{\sigma_a^{w(1)}}{\sigma_s^{s(0)}} + \alpha_s^2 \frac{1}{\sigma_s^{s(0)}} \left( \frac{\sigma_a^{s(2)}}{\sigma_s^{s(0)}} - \frac{\sigma_a^{s(1)} \sigma_s^{s(1)}}{\sigma_s^{s(0)}} \right) \dots$$

$$R_{q\bar{q}}^{\text{QED}}(\mu) = \frac{36Q_q Q_t \alpha_e}{5\alpha_s}, \quad R_{qg}^{\text{QED}}(\mu) = \frac{24Q_q Q_t \alpha_e}{5\alpha_s}$$

Apply rescaling of couplings and colour factors

NLO in production and decay (MCFM)  
[arXiv:1204.1513](https://arxiv.org/abs/1204.1513) J. Campbell and R. K. Ellis

# Single-lepton asymmetry

$$A^l = \int_{2.0}^{4.5} d\eta_l \left( \frac{d\sigma^{l^+b}/d\eta_l - d\sigma^{l^-b}/d\eta_l}{d\sigma^{l^+b}/d\eta_l + d\sigma^{l^-b}/d\eta_l} \right) \quad \begin{array}{l} 2.0 < \eta(l, b) < 4.5 \\ p_T(l/b) > 20/60 \text{ GeV} \\ \Delta R(l^\pm, \text{jet}) \geq 0.5 \end{array}$$

Signal contribution to **numerator**

Computed with NNPDF2.3 NLO as 119 PDFs

$N^l$ (fb)		$\mu = m_t/2$	$\mu = m_t$	$\mu = 2m_t$
$\mathcal{O}(\alpha_s^3)$	$u\bar{u}$	41.85	30.90	24.37
	$d\bar{d}$	18.09	12.87	9.91
	$ug$	1.90	1.22	0.85
	$dg$	0.72	0.45	0.34
$\mathcal{O}(\alpha_s^2\alpha_e)$	Total	7.05	5.79	4.97
Total		69.60	51.23	40.44

# Single-lepton asymmetry

$$A^l = \int_{2.0}^{4.5} d\eta_l \left( \frac{d\sigma^{l^+b}/d\eta_l - d\sigma^{l^-b}/d\eta_l}{d\sigma^{l^+b}/d\eta_l + d\sigma^{l^-b}/d\eta_l} \right) \quad \begin{array}{l} 2.0 < \eta(l, b) < 4.5 \\ p_T(l/b) > 20/60 \text{ GeV} \\ \Delta R(l^\pm, \text{jet}) \geq 0.5 \end{array}$$

Signal contribution to **denominator**  
 Computed with various LO/NLO NNPDF2.3 PDFs

PDF	$D^l$ (fb), 14 TeV			$A^l$ (%)
	$\mu = m_t/2$	$\mu = m_t$	$\mu = 2m_t$	
NLO 119	4626	3512	2742	1.48 (2)
LO 119	6225	4663	3586	1.12 (2)
LO 130	6761	4961	3752	1.05 (3)

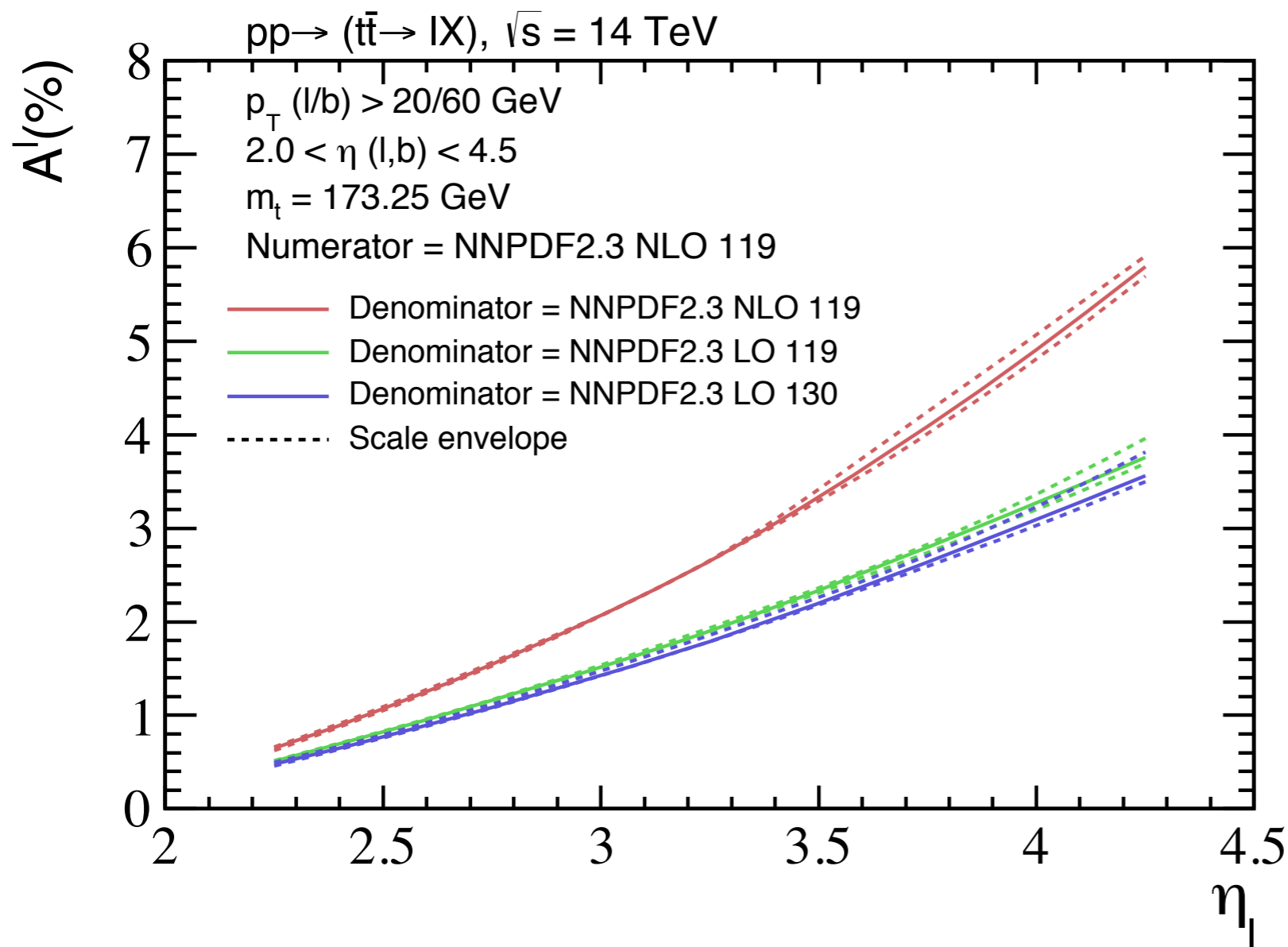
# Single-lepton asymmetry

$$A^l = \int_{2.0}^{4.5} d\eta_l \left( \frac{d\sigma^{l^+b}/d\eta_l - d\sigma^{l^-b}/d\eta_l}{d\sigma^{l^+b}/d\eta_l + d\sigma^{l^-b}/d\eta_l} \right)$$

$$2.0 < \eta(l, b) < 4.5$$

$$p_T(l/b) > 20/60 \text{ GeV}$$

$$\Delta R(l^\pm, \text{jet}) \geq 0.5$$

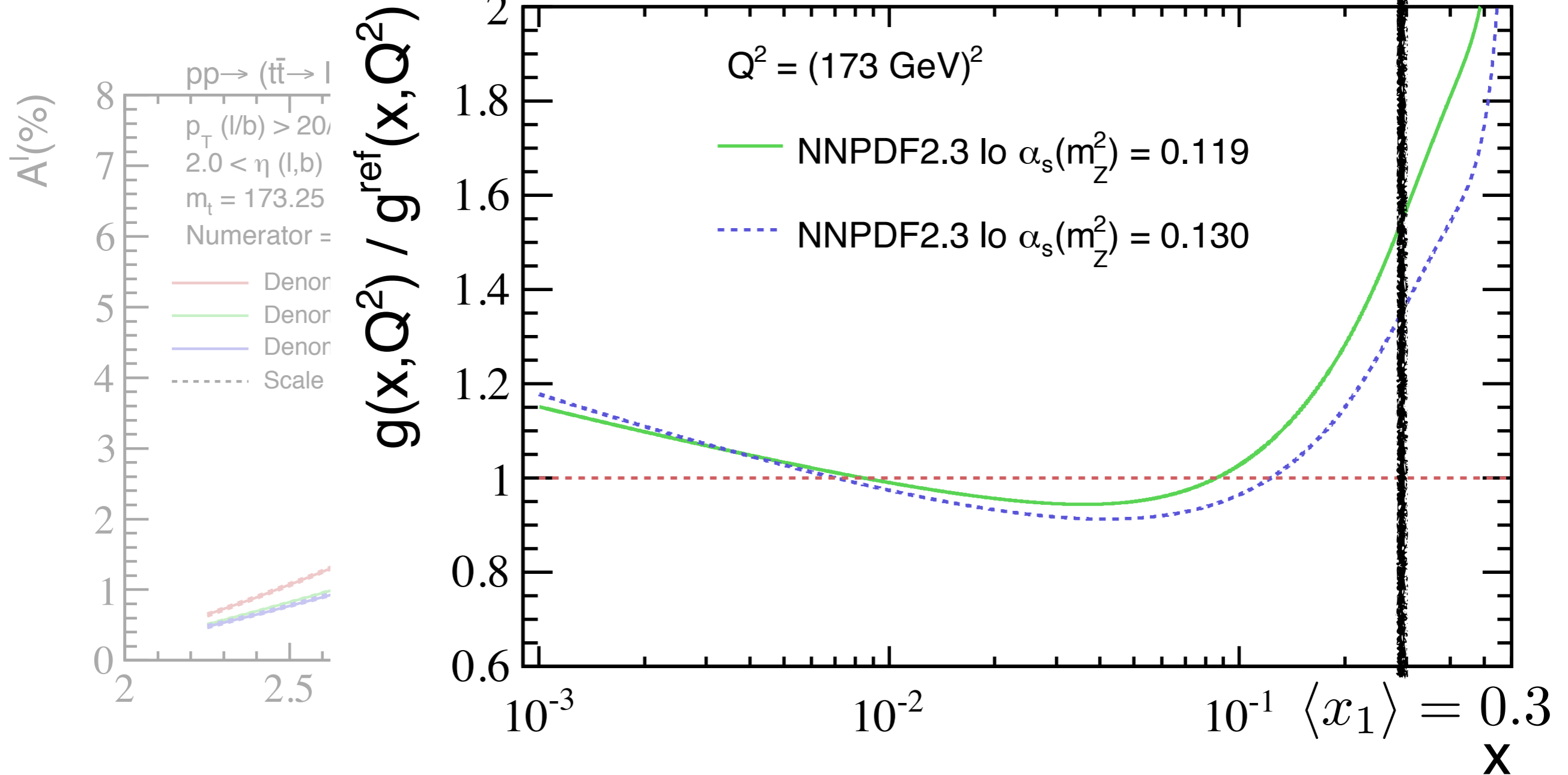




# Single-lepton asymmetry

$$A^l = \int_{2.0}^{4.5} d\eta_l \left( \frac{d\sigma^{l^+b}}{d\eta_l} - \frac{d\sigma^{l^-b}}{d\eta_l} \right)$$

$2.0 < \eta(l, b) < 4.5$   
 $m_{-}(l/b) \sim 20/60 \text{ GeV}$   
 gluon PDF ratio,  $g^{\text{ref}} = \text{NNPDF2.3 nlo } \alpha_s(m_Z^2) = 0.119$



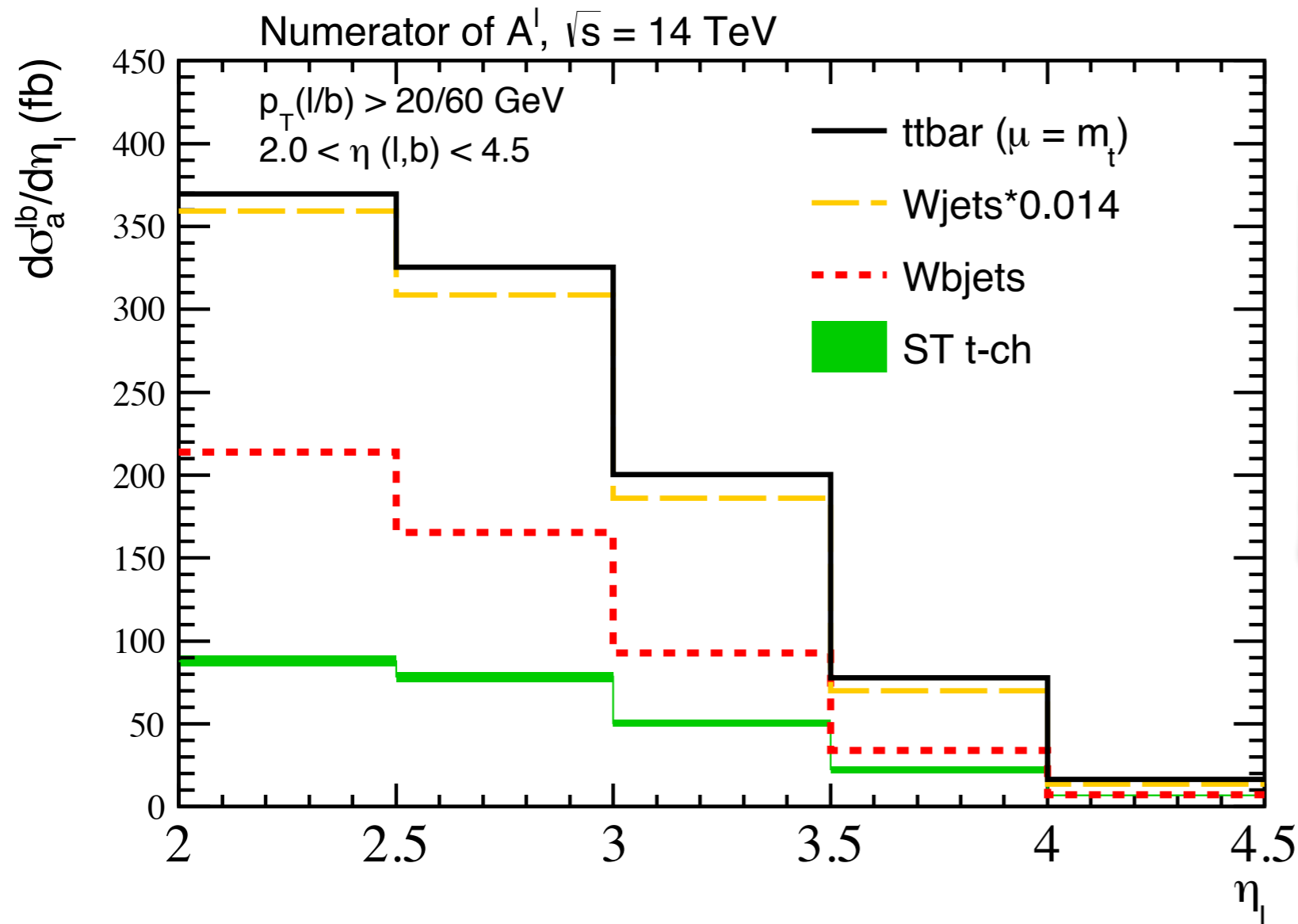
# What about backgrounds!?

$$A^l = \int_{2.0}^{4.5} d\eta_l \left( \frac{d\sigma^{l^+b}/d\eta_l - d\sigma^{l^-b}/d\eta_l}{d\sigma^{l^+b}/d\eta_l + d\sigma^{l^-b}/d\eta_l} \right)$$

$$2.0 < \eta(l, b) < 4.5$$

$$p_T(l/b) > 20/60 \text{ GeV}$$

$$\Delta R(l^\pm, \text{jet}) \geq 0.5$$



Fit backgrounds  
 experimentally:  
 $l^\pm j, l^\pm bj, l^\pm bb$   
 control channels

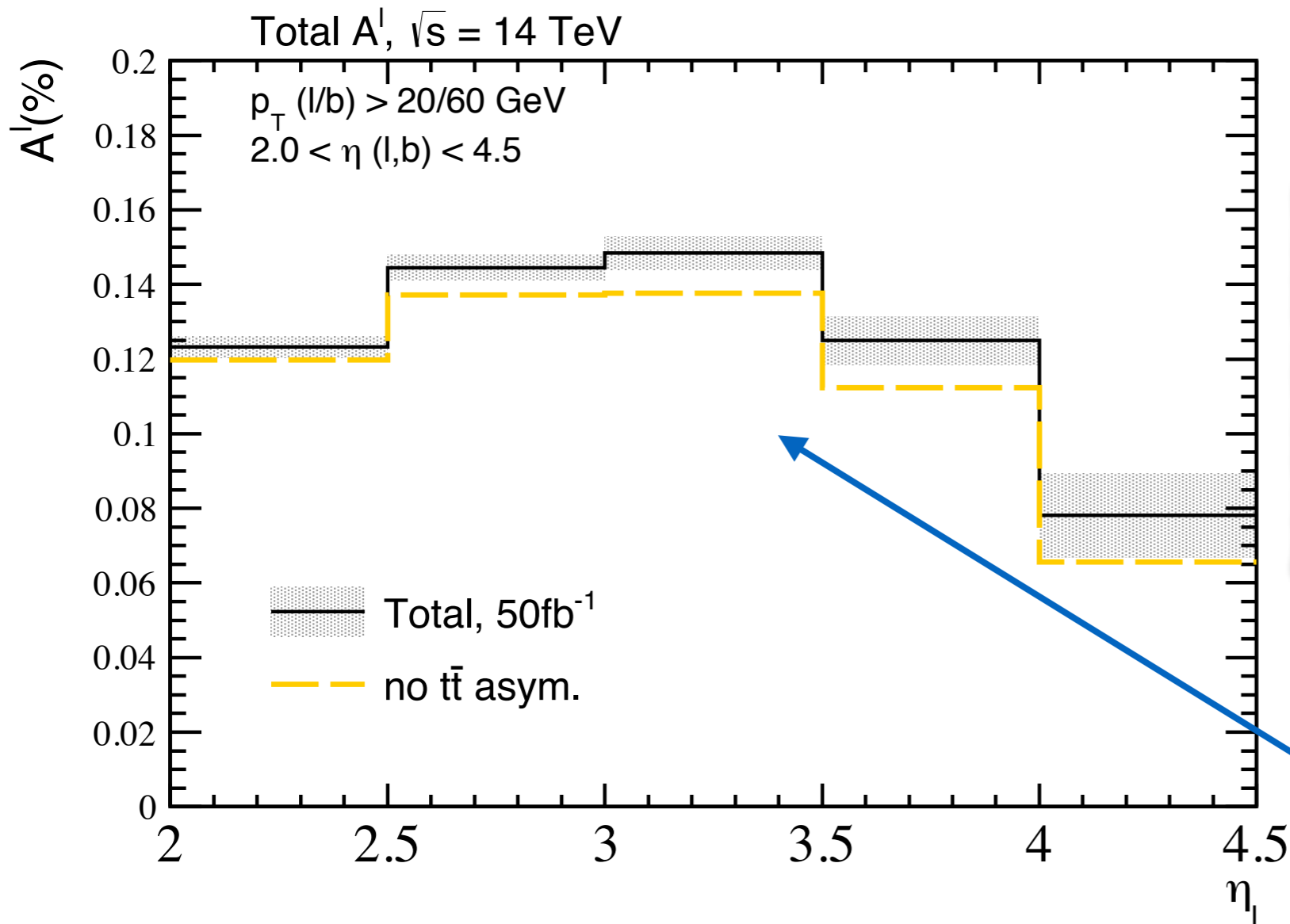
# What about backgrounds!?

$$A^l = \int_{2.0}^{4.5} d\eta_l \left( \frac{d\sigma^{l^+b}/d\eta_l - d\sigma^{l^-b}/d\eta_l}{d\sigma^{l^+b}/d\eta_l + d\sigma^{l^-b}/d\eta_l} \right)$$

$$2.0 < \eta(l, b) < 4.5$$

$$p_T(l/b) > 20/60 \text{ GeV}$$

$$\Delta R(l^\pm, \text{jet}) \geq 0.5$$



Statistical uncertainty only

$$\chi^2_{\text{no } t\bar{t} \text{ asym}} = 13.76$$

Excluded beyond  $3\sigma$

Sensitivity in bins

$$2.5 < \eta_l < 4.0$$

# Di-lepton asymmetry

$$A_{fb}^{ll} = \int d\Delta_y \frac{(d\sigma^{\mu eb}(\Delta_y > 0) - d\sigma^{\mu eb}(\Delta_y < 0)) / d\Delta_y}{d\sigma^{\mu eb} / d\Delta_y}$$

$2.0 < \eta(e, \mu, b) < 4.5$   
 $p_T(e, \mu, b) > 20 \text{ GeV}$   
 $\Delta R(l^\pm, \text{jet}) \geq 0.5$

Signal contribution to **numerator**

Computed with NNPDF2.3 NLO as 119 PDFs

$N_{fb}^{ll}$ (fb)		$\mu = m_t/2$	$\mu = m_t$	$\mu = 2m_t$
$\mathcal{O}(\alpha_s^3)$	$u\bar{u}$	0.889	0.659	0.490
	$d\bar{d}$	0.319	0.232	0.176
	$ug$	0.095	0.070	0.045
	$dg$	0.031	0.021	0.013
$\mathcal{O}(\alpha_s^2\alpha_e)$	Total	0.163	0.134	0.107
Total		1.498	1.116	0.832

# Di-lepton asymmetry

$$A_{fb}^{ll} = \int d\Delta_y \frac{(d\sigma^{\mu eb}(\Delta_y > 0) - d\sigma^{\mu eb}(\Delta_y < 0)) / d\Delta_y}{d\sigma^{\mu eb} / d\Delta_y}$$

$2.0 < \eta(e, \mu, b) < 4.5$   
 $p_T(e, \mu, b) > 20 \text{ GeV}$   
 $\Delta R(l^\pm, \text{jet}) \geq 0.5$

Signal contribution to **denominator**  
 Computed with various LO/NLO NNPDF2.3 PDFs

PDF	$D_{fb}^{ll}$ (fb), 14 TeV			$A_{fb}^{ll}$ (%)
	$\mu = m_t/2$	$\mu = m_t$	$\mu = 2m_t$	
NLO 119	110.4	85.0	67.4	1.30 (7)
LO 119	160.7	120.7	93.3	0.91 (2)
LO 130	176.6	130.0	98.8	0.85 (1)

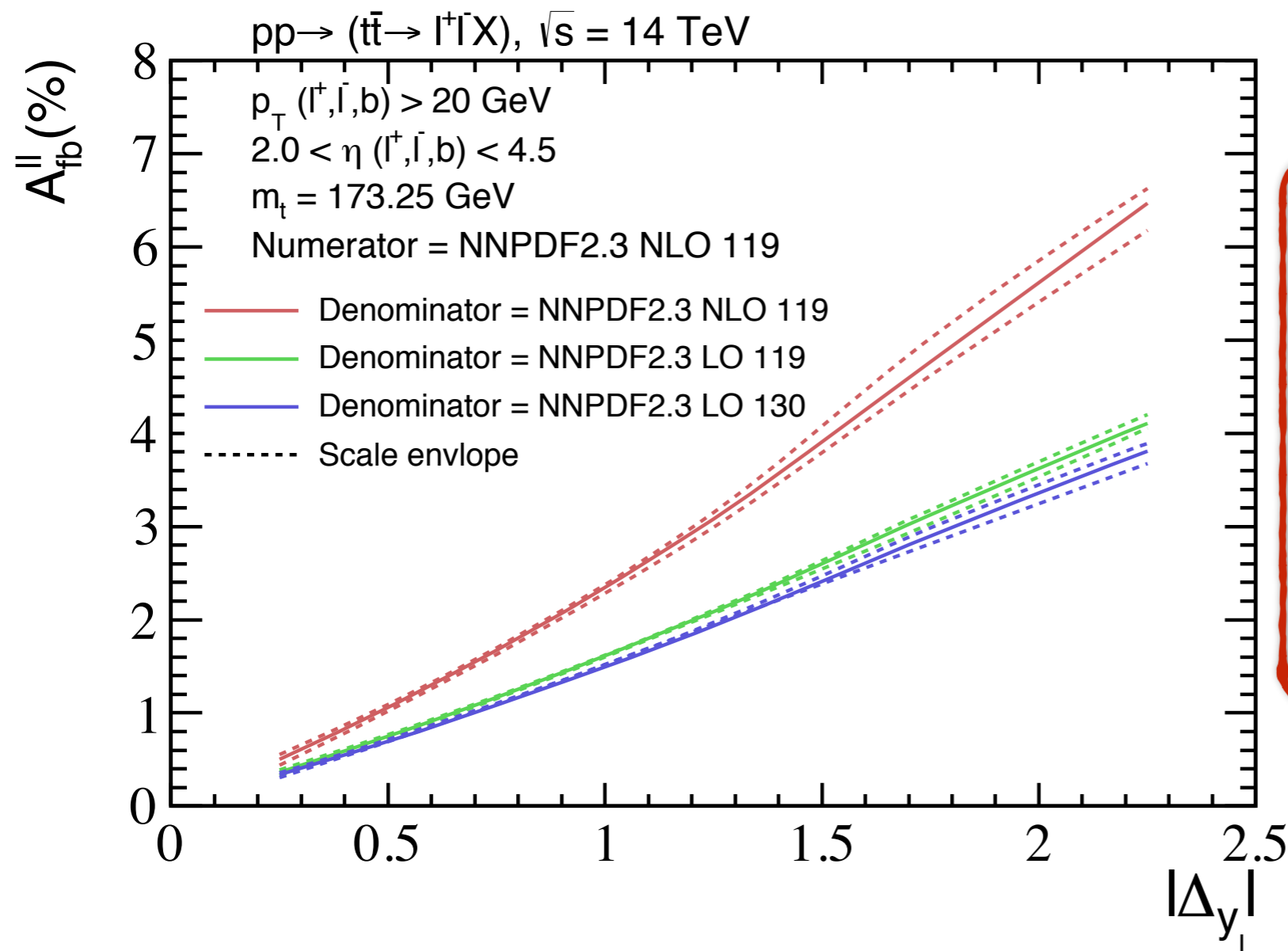
# Di-lepton asymmetry

$$A_{fb}^{ll} = \int d\Delta_y \frac{(d\sigma^{\mu eb}(\Delta_y > 0) - d\sigma^{\mu eb}(\Delta_y < 0)) / d\Delta_y}{d\sigma^{\mu eb} / d\Delta_y}$$

$$2.0 < \eta(e, \mu, b) < 4.5$$

$$p_T(e, \mu, b) > 20 \text{ GeV}$$

$$\Delta R(l^\pm, \text{jet}) \geq 0.5$$



Statistical uncertainty only

expect ~6k events

$$A \simeq 1.30\%(\textit{theo})$$

$$\delta A \simeq \pm 1.30\%(\textit{stat})$$

not significant..

# Conclusion

---

- LHCb can measure  $t\bar{t}b$  cross section
  - first of its kind at high pseudorapidity
- Charge asymmetry measurements possible
  - single-lepton channel promising
  - experimentally still challenging...
  - a background fit in many channels necessary



Thank you for your attention!

Thank you for your attention!



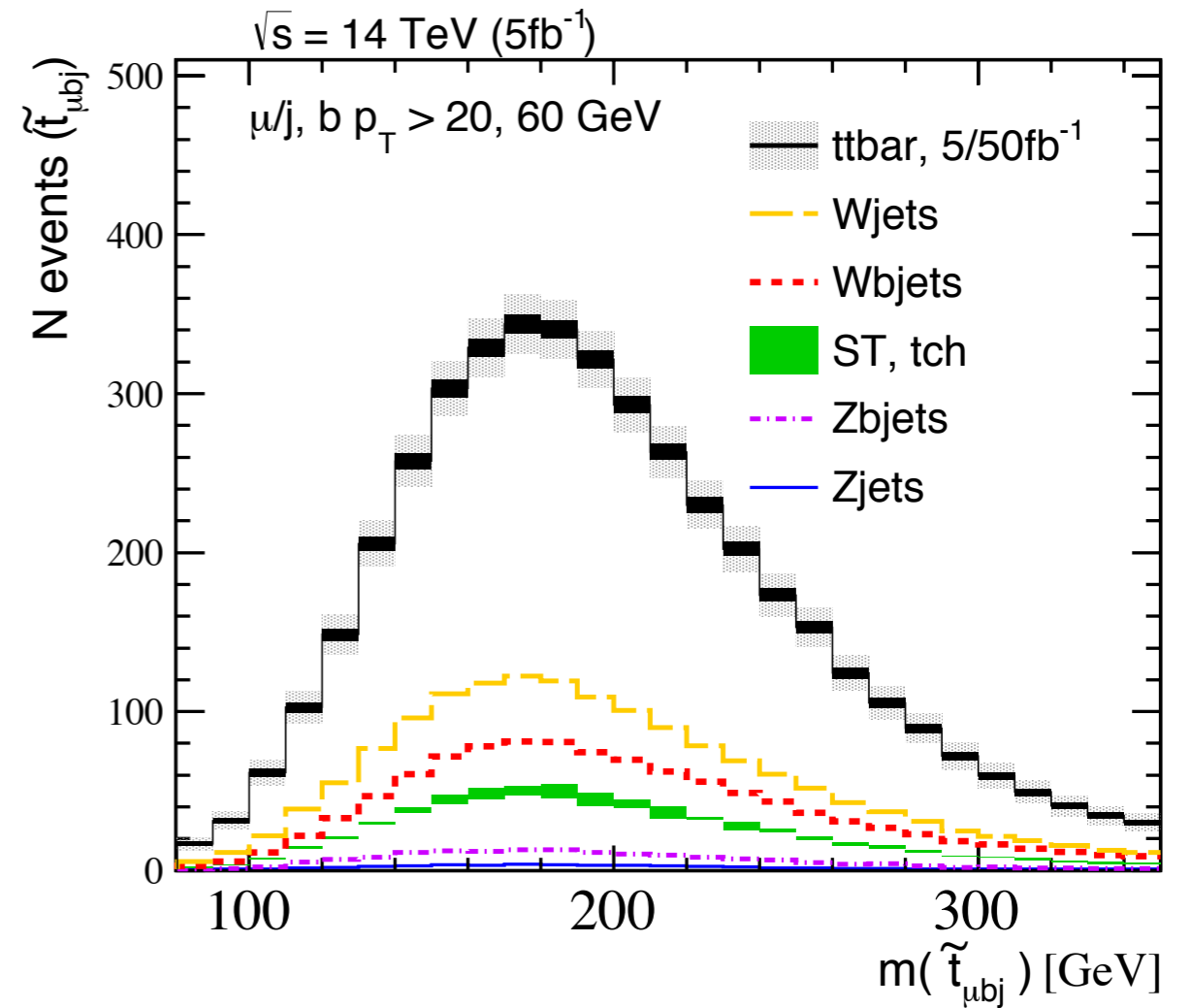
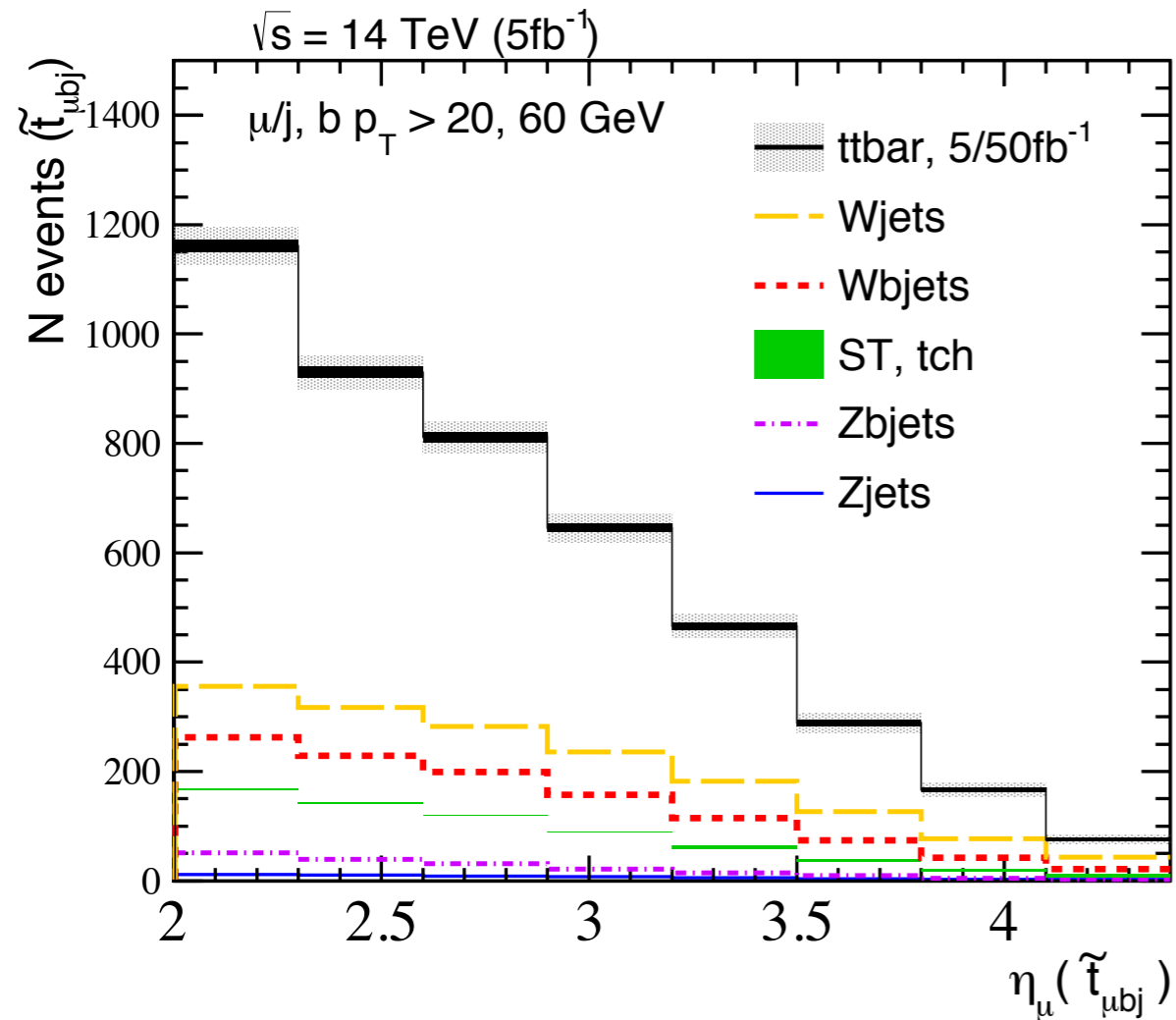
# Feasibility - event yield

Some other channels (loose cuts)

- generate  $t\bar{t}$  (**POWHEG**) and match to parton shower (**Pythia8176**)
- build  $R = 0.5$  anti-kt jets (j)
- truth match parton level b-quarks to jets within  $dR < 0.5$  (b)
- apply loose cuts:  $l(e,\mu) p_T > 4$  GeV and  $j/b p_T > 20$  GeV
- apply acceptance cuts:  $2.0 < l, j/b \text{ eta} < 4.5$

Data	$1\text{fb}^{-1}$	$2\text{fb}^{-1}$	$5/50\text{fb}^{-1}$
$d\sigma(\text{fb})$	7 TeV	8 TeV	14 TeV
$lb$	285 $\pm$ 52	504 $\pm$ 94	4366 $\pm$ 663
$lbj$	97 $\pm$ 21	198 $\pm$ 35	2335 $\pm$ 323
$lbb$	32 $\pm$ 6	65 $\pm$ 12	870 $\pm$ 116
$lbbj$	10 $\pm$ 2	26 $\pm$ 4	487 $\pm$ 76
$l^+l^-$	44 $\pm$ 9	79 $\pm$ 15	635 $\pm$ 109
$l^+l^-b$	19 $\pm$ 4	39 $\pm$ 8	417 $\pm$ 79

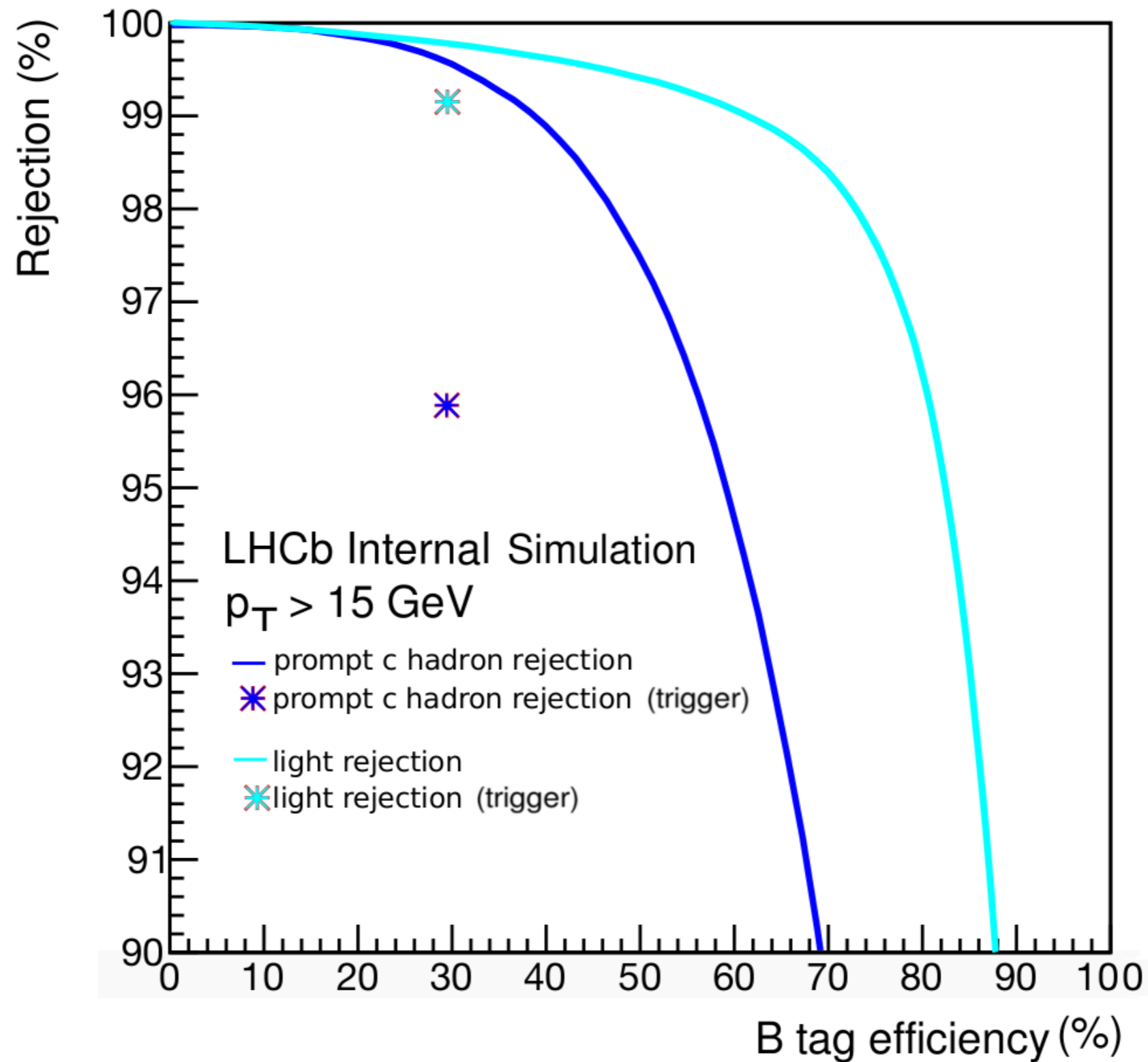
# Single-lepton 14 TeV (l $\bar{b}j$ )



14 TeV

$l^{\pm} b j$

# LHCb b-tagging



# Theoretical systematics

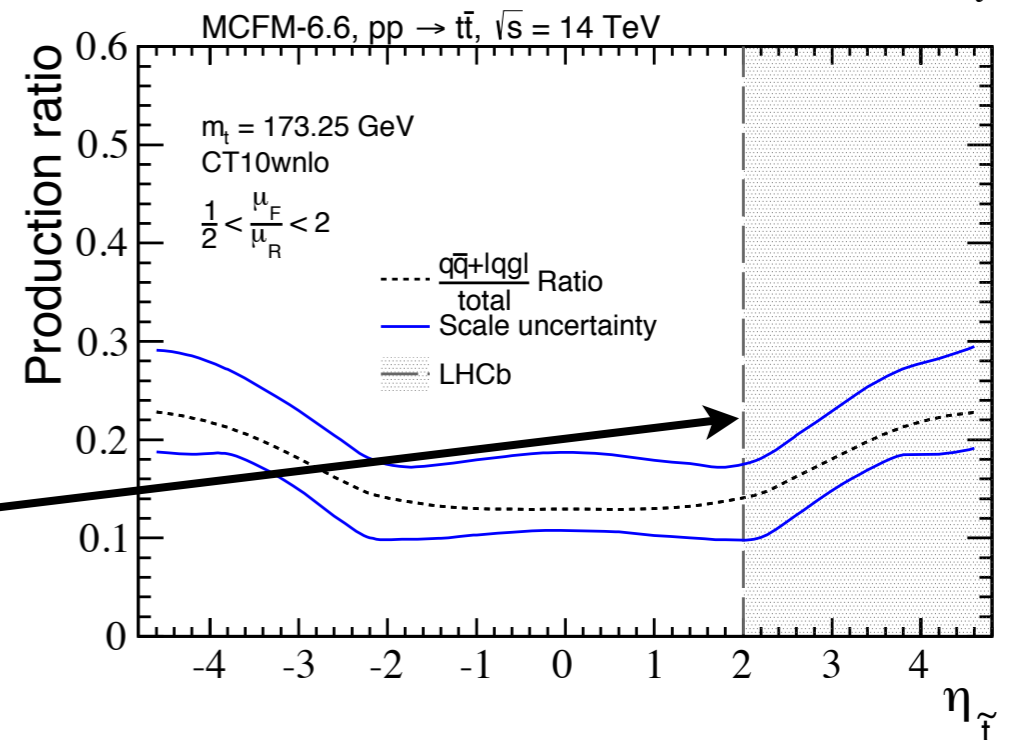
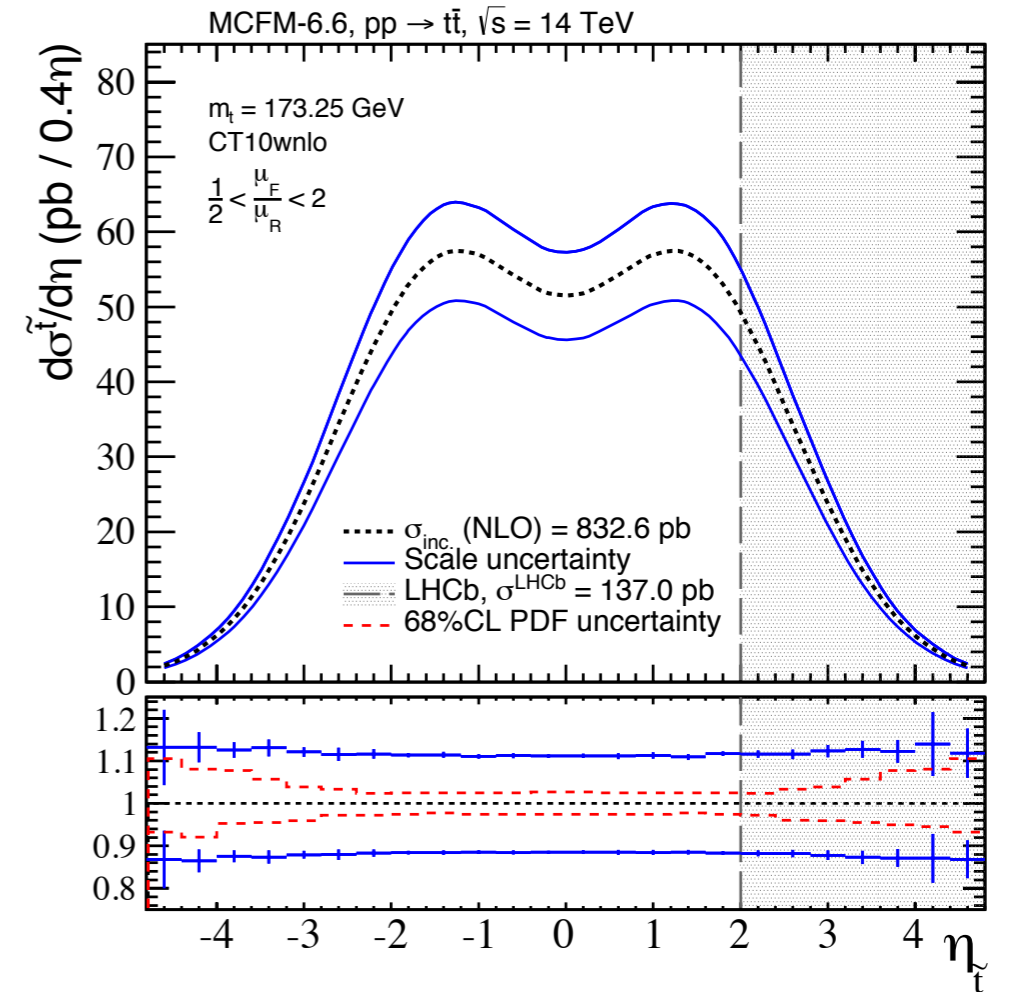
$$\frac{d\sigma^{\tilde{t}}}{dX} = \frac{1}{2} \left( \frac{d\sigma^t}{dX} + \frac{d\sigma^{\bar{t}}}{dX} \right)$$

$$\sigma^{\text{LHCb}} = \int_{\eta=2} \frac{d\sigma^{\tilde{t}}}{d\eta}$$

Production mechanism ratio:

$$\frac{q\bar{q} + |qg|}{total}$$

LHCb probes unique region



# Theoretical systematics

$$\sigma = \int dx_a dx_b \underbrace{f_a(x_a, \mu_F^2)}_{\text{PDF}} \underbrace{f_b(x_b, \mu_F^2)}_{\text{PDF}} \underbrace{\hat{\sigma}(\mu_f, \mu_R, m^2, \beta)}_{\text{Scale}}$$

Strong coupling

$$\hat{\sigma}(\beta) = \frac{\alpha_s^2}{m^2} \left( \sigma_{ij}^{(0)} + \alpha_s \sigma_{ij}^{(1)} + \alpha_s^2 \sigma_{ij}^{(2)} + \mathcal{O}(\alpha_s^3) \right)$$

Top mass

$$\beta = \sqrt{1 - 4m^2/s}$$

$$\frac{1}{2} < \frac{\mu_F}{\mu_R} < 2$$

$$\delta\text{PDF} = 1\sigma\text{CL}$$

$$\alpha_s(M_Z) = 0.1184 \pm 0.0007$$

$$\delta m_t = 1.5 \text{ GeV}$$

# strong coupling

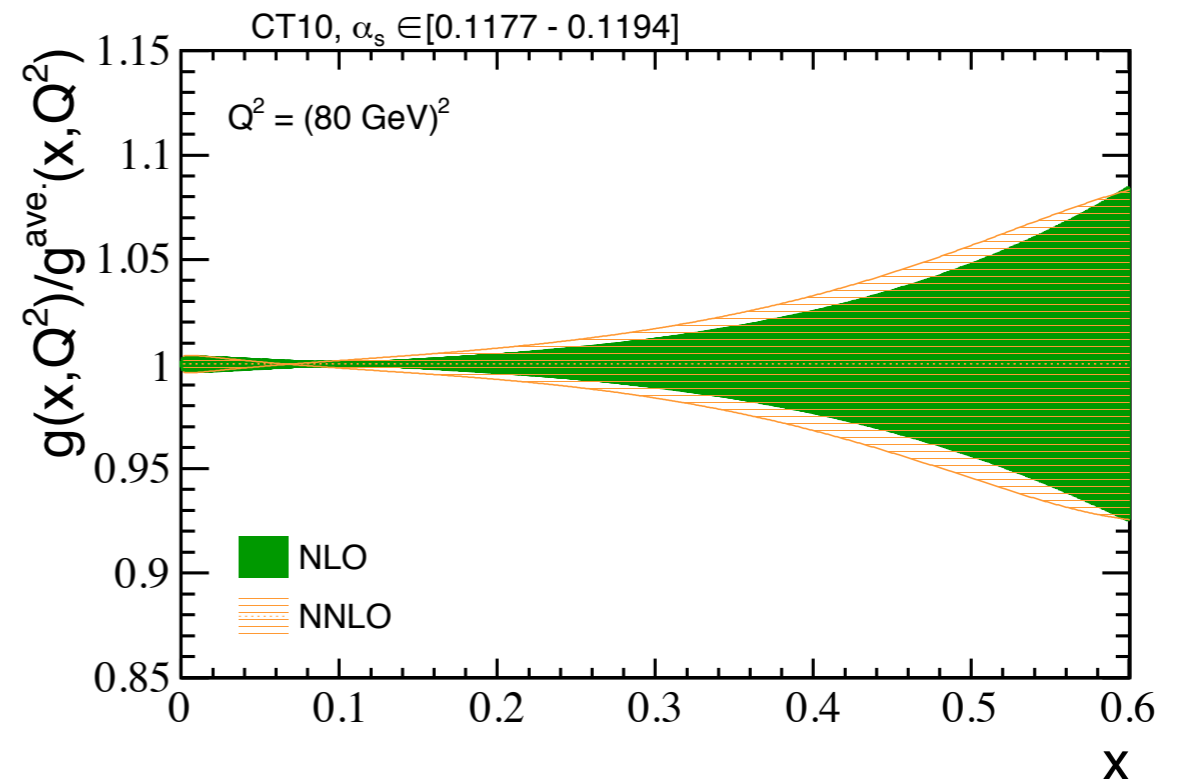
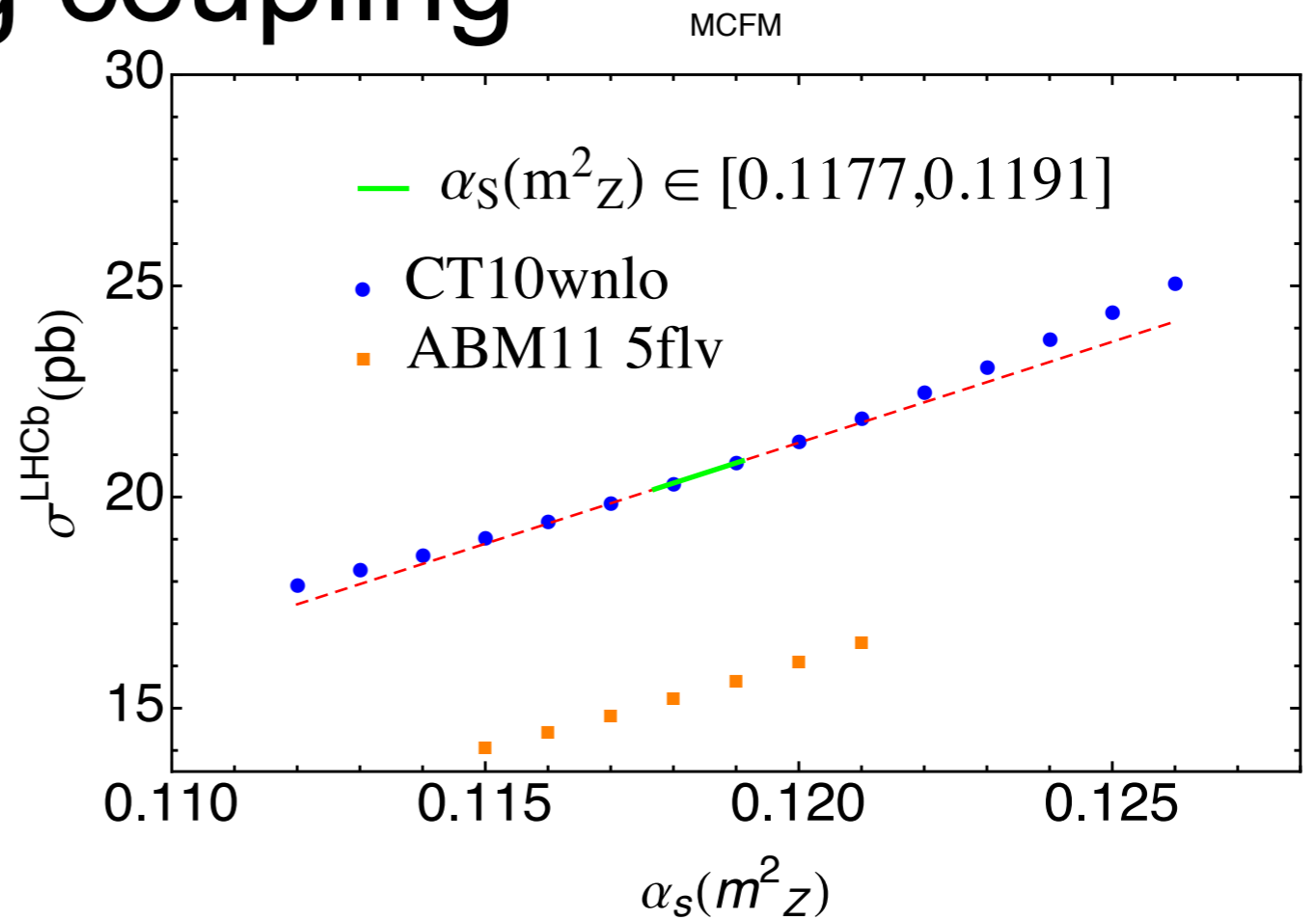
$\sigma^{LHCb}$  vs.  $\alpha_s(M_Z)$

Current PDG value

$$\alpha_s(M_Z) = 0.1184 \pm 0.0007$$

gluon PDF uncertainty  
for  $\delta\alpha_s$

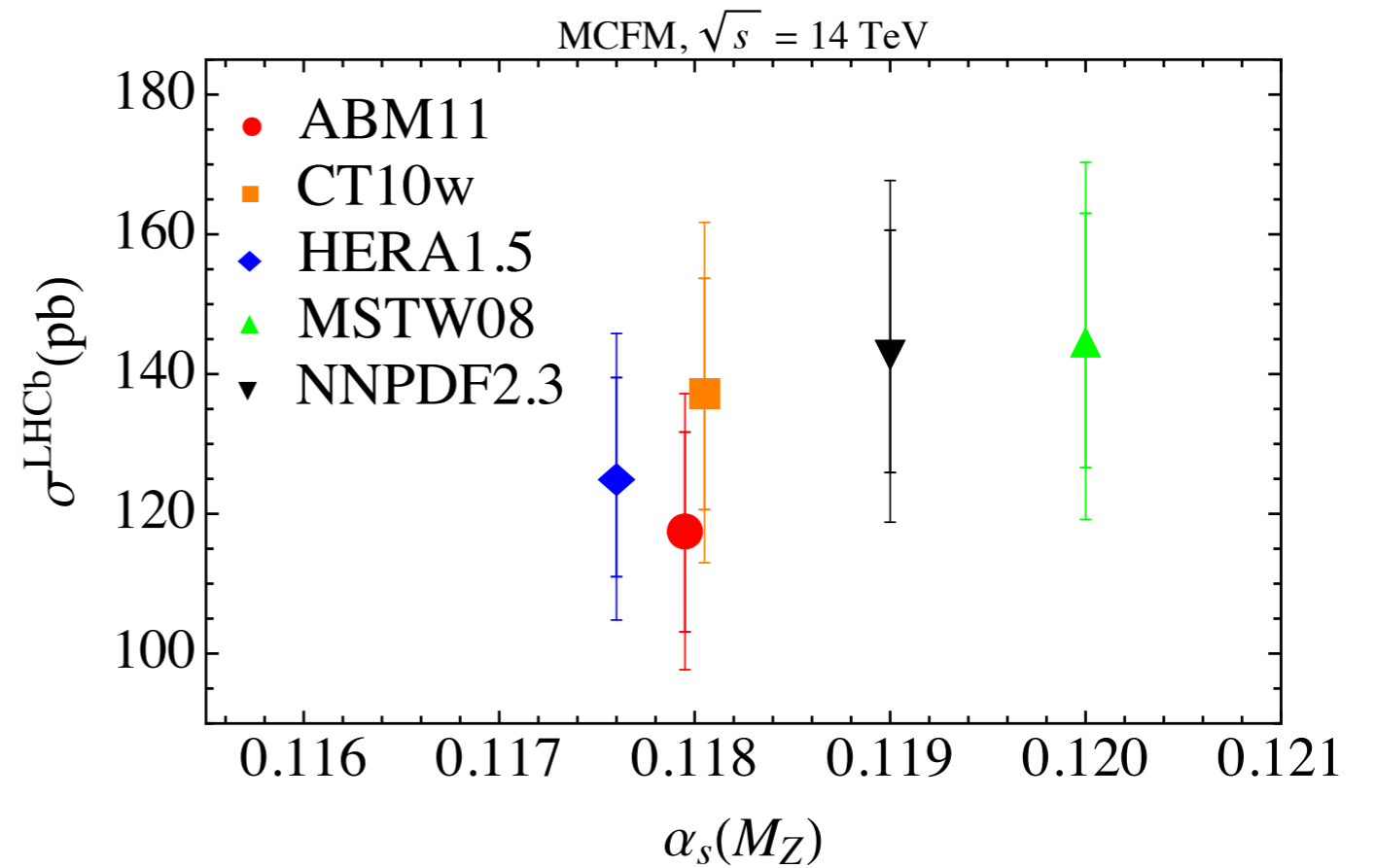
$$\delta\alpha_s \rightarrow \delta\sigma^{LHCb} = 1.3\%$$



Order	PDF	$\sigma(\text{pb})$	$\delta_{\text{scale}}$ (pb)	$\delta_{\text{PDF}}$ (pb)	$\delta_{\alpha_s}$ (pb)	$\delta_{m_t}$ (pb)	$\delta_{\text{total}}$ (pb)
NNLO* (inc.)	ABM	832.0	+18.7 (+2.2%) -27.4 (-3.3%)	+25.1 (+3.0%) -25.1 (-3.0%)	+0.0 (+0.0%) -0.0 (-0.0%)	+34.9 (+4.2%) -33.7 (-4.1%)	+61.7 (+7.4%) -69.7 (-8.4%)
NLO(inc.)		771.9	+91.0 (+11.8%) -92.4 (-12.0%)	+9.4 (+1.2%) -9.4 (-1.2%)	+0.0 (+0.0%) -0.0 (-0.0%)	+32.3 (+4.2%) -31.9 (-4.1%)	+124.7 (+16.1%) -125.7 (-16.3%)
NLO(LHCb)		117.2	+14.5 (+12.3%) -14.1 (-12.0%)	+2.0 (+1.7%) -2.0 (-1.7%)	+0.0 (+0.0%) -0.0 (-0.0%)	+5.2 (+4.4%) -5.1 (-4.3%)	+20.0 (+17.1%) -19.5 (-16.7%)
NNLO* (inc.)	CT10	952.8	+23.3 (+2.4%) -34.5 (-3.6%)	+22.4 (+2.3%) -19.9 (-2.1%)	+14.0 (+1.5%) -14.0 (-1.5%)	+39.2 (+4.1%) -37.8 (-4.0%)	+70.6 (+7.4%) -79.5 (-8.3%)
NLO(inc.)		832.6	+97.0 (+11.7%) -96.7 (-11.6%)	+19.6 (+2.4%) -20.2 (-2.4%)	+9.2 (+1.1%) -9.2 (-1.1%)	+34.0 (+4.1%) -33.3 (-4.0%)	+137.4 (+16.5%) -136.6 (-16.4%)
NLO(LHCb)		137.0	+16.7 (+12.2%) -16.4 (-12.0%)	+5.0 (+3.6%) -4.6 (-3.4%)	+1.8 (+1.3%) -1.8 (-1.3%)	+5.9 (+4.3%) -5.8 (-4.2%)	+24.7 (+18.0%) -24.0 (-17.5%)
NNLO* (inc.)	HERA	970.5	+22.1 (+2.3%) -22.0 (-2.3%)	+15.7 (+1.6%) -25.7 (-2.6%)	+12.8 (+1.3%) -12.8 (-1.3%)	+39.6 (+4.1%) -38.4 (-4.0%)	+66.6 (+6.9%) -70.0 (-7.2%)
NLO(inc.)		804.2	+91.9 (+11.4%) -87.6 (-10.9%)	+16.1 (+2.0%) -21.9 (-2.7%)	+5.3 (+0.7%) -5.3 (-0.7%)	+33.4 (+4.1%) -32.4 (-4.0%)	+129.3 (+16.1%) -127.1 (-15.8%)
NLO(LHCb)		124.7	+14.8 (+11.8%) -13.7 (-11.0%)	+3.0 (+2.4%) -3.0 (-2.4%)	+1.1 (+0.9%) -1.1 (-0.9%)	+5.5 (+4.4%) -5.3 (-4.3%)	+21.1 (+16.9%) -19.9 (-15.9%)
NNLO* (inc.)	MSTW	953.6	+22.7 (+2.4%) -33.9 (-3.6%)	+16.2 (+1.7%) -17.8 (-1.9%)	+12.8 (+1.3%) -12.8 (-1.3%)	+39.1 (+4.1%) -37.9 (-4.0%)	+66.9 (+7.0%) -77.7 (-8.1%)
NLO(inc.)		885.6	+107.2 (+12.1%) -105.7 (-11.9%)	+16.0 (+1.8%) -19.4 (-2.2%)	+10.1 (+1.1%) -10.1 (-1.1%)	+36.2 (+4.1%) -35.3 (-4.0%)	+148.1 (+16.7%) -147.3 (-16.6%)
NLO(LHCb)		144.4	+18.6 (+12.8%) -17.8 (-12.3%)	+3.5 (+2.4%) -3.9 (-2.7%)	+1.9 (+1.3%) -1.9 (-1.3%)	+6.2 (+4.3%) -6.1 (-4.2%)	+25.9 (+18.0%) -25.2 (-17.5%)
NNLO* (inc.)	NNPDF	977.5	+23.6 (+2.4%) -35.4 (-3.6%)	+16.4 (+1.7%) -16.4 (-1.7%)	+12.2 (+1.3%) -12.2 (-1.3%)	+40.4 (+4.1%) -39.1 (-4.0%)	+68.9 (+7.0%) -80.0 (-8.1%)
NLO(inc.)		894.5	+107.6 (+12.0%) -101.0 (-11.3%)	+12.8 (+1.4%) -12.8 (-1.4%)	+9.9 (+1.1%) -9.9 (-1.1%)	+36.6 (+4.1%) -35.8 (-4.0%)	+147.6 (+16.5%) -140.3 (-15.7%)
NLO(LHCb)		142.5	+18.1 (+12.7%) -16.6 (-11.7%)	+3.0 (+2.1%) -3.0 (-2.1%)	+2.0 (+1.4%) -2.0 (-1.4%)	+6.2 (+4.4%) -6.1 (-4.3%)	+25.2 (+17.7%) -23.7 (-16.6%)

# Summary of theory systematics (NLO)

$$\delta_{\text{total}} = \delta_{\text{scale}} + (\delta_{\text{PDF}}^2 + \delta_{\alpha_s}^2 + \delta_{m_t}^2)^{\frac{1}{2}}$$



$$\delta_X^{\text{ratio}} = \frac{\delta_X^{\text{LHCb}}}{\delta_X^{\text{NLO}}}$$

PDF	$\delta_{\text{scale}}^{\text{ratio}}$	$\delta_{\text{PDF}}^{\text{ratio}}$	$\delta_{\alpha_s}^{\text{ratio}}$	$\delta_{m_t}^{\text{ratio}}$	$\delta_{\text{total}}^{\text{ratio}}$
ABM	+1.05 -1.00	+1.40 -1.40	+0.00 -0.00	+1.05 -1.05	+1.06 -1.02
CT10	+1.05 -1.03	+1.55 -1.40	+1.20 -1.20	+1.06 -1.05	+1.09 -1.07
HERA	+1.04 -1.01	+1.19 -0.90	+1.33 -1.33	+1.07 -1.06	+1.05 -1.01
MSTW	+1.06 -1.03	+1.35 -1.23	+1.13 -1.13	+1.05 -1.06	+1.07 -1.05
NNPDF	+1.05 -1.03	+1.45 -1.45	+1.27 -1.27	+1.07 -1.07	+1.07 -1.06



# Constraining the gluon PDF

Perform a bayesian reweighting based on statistical inference.

[arXiv:1012.0836](#) NNPDF collaboration

[arXiv:1205.4024](#) G. Watt, R. S. Thorne, applied technique to MSTW hessian set

I apply the technique to CT10w and NNPDF2.3 NLO sets

## Recipe for Hessian reweighting

1) Calculate observables from eigenvector set

$$\{X_0(\mathcal{S}_0), X_1^-(\mathcal{S}_1^-), X_1^+(\mathcal{S}_1^+), \dots, X_N^-(\mathcal{S}_N^-), X_N^+(\mathcal{S}_N^+)\}$$

2) Generate random observables from these (storing random numbers)

$$X(\mathcal{S}_k) = X(\mathcal{S}_0) + \sum_{j=1}^N [X(\mathcal{S}_j^\pm) - X(\mathcal{S}_0)] |R_{kj}|$$

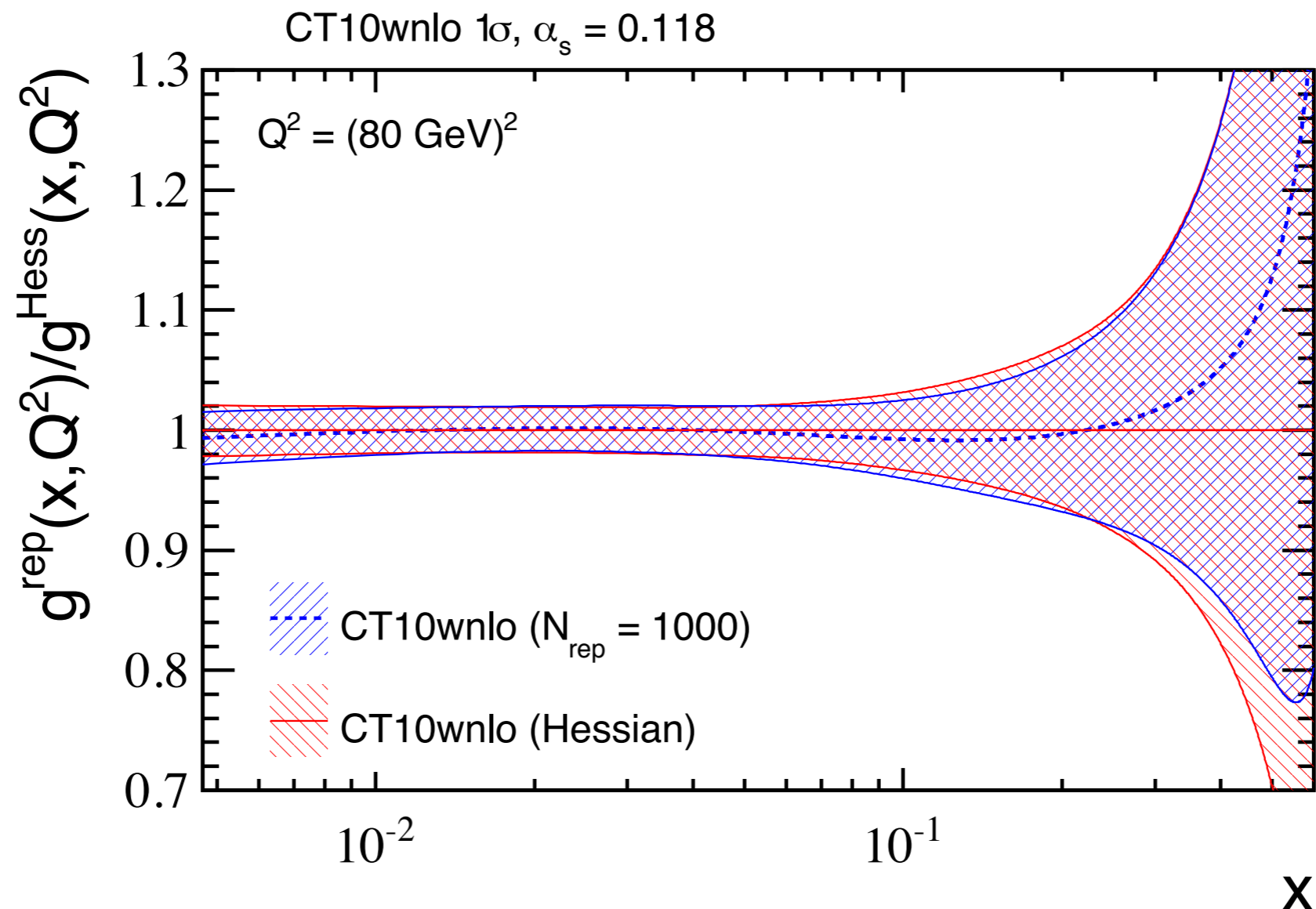
3) Apply a reweighting based on a 'measured' observable (e.g. cross-section)

$$W_k(\chi_k^2) = (\chi_k^2)^{\frac{1}{2}(N_{pts.} - 1)} \exp\left(-\frac{1}{2}\chi_k^2\right)$$

4) Apply these weights to the other observables (gluon PDF, ttbar asymmetry etc.)

# Follow the recipe - steps 1, 2

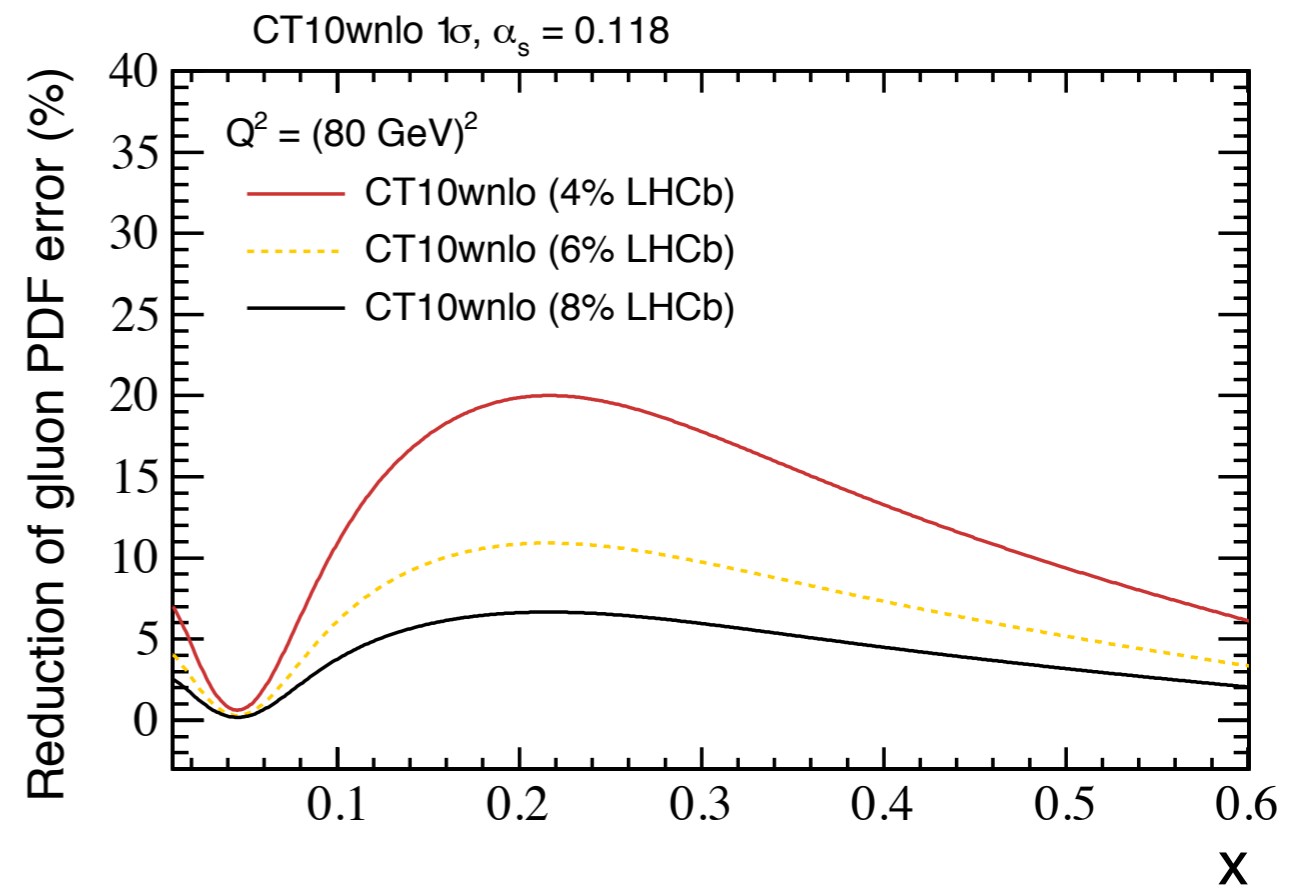
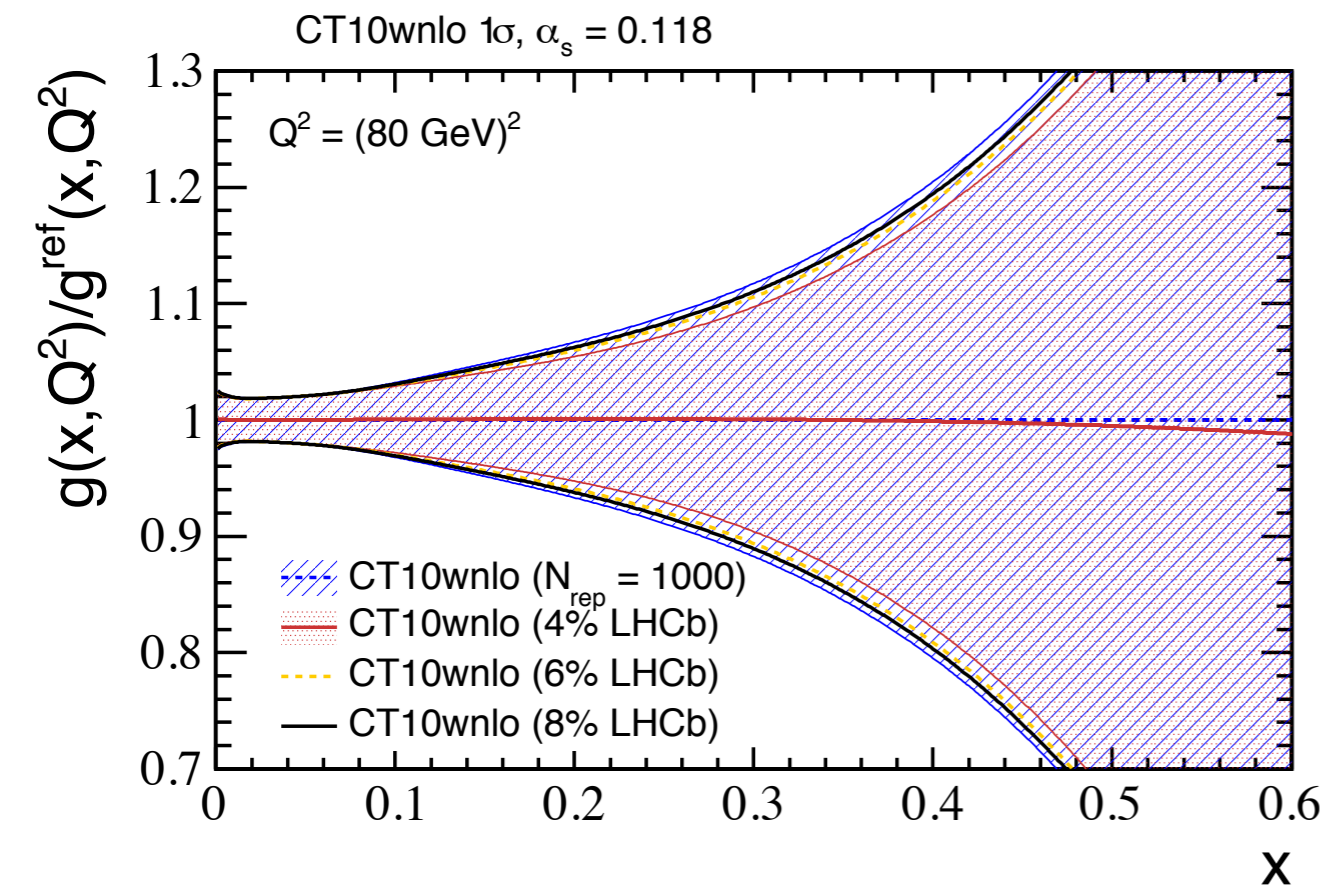
- 1) Choose observable as evolved gluon PDF,  $g^{\text{Hess}}(x, [Q = 80 \text{ GeV}]^2)$
- 2) Generate 1000 Replicas and compare,  $g^{\text{rep}}(x, [Q = 80 \text{ GeV}]^2)$



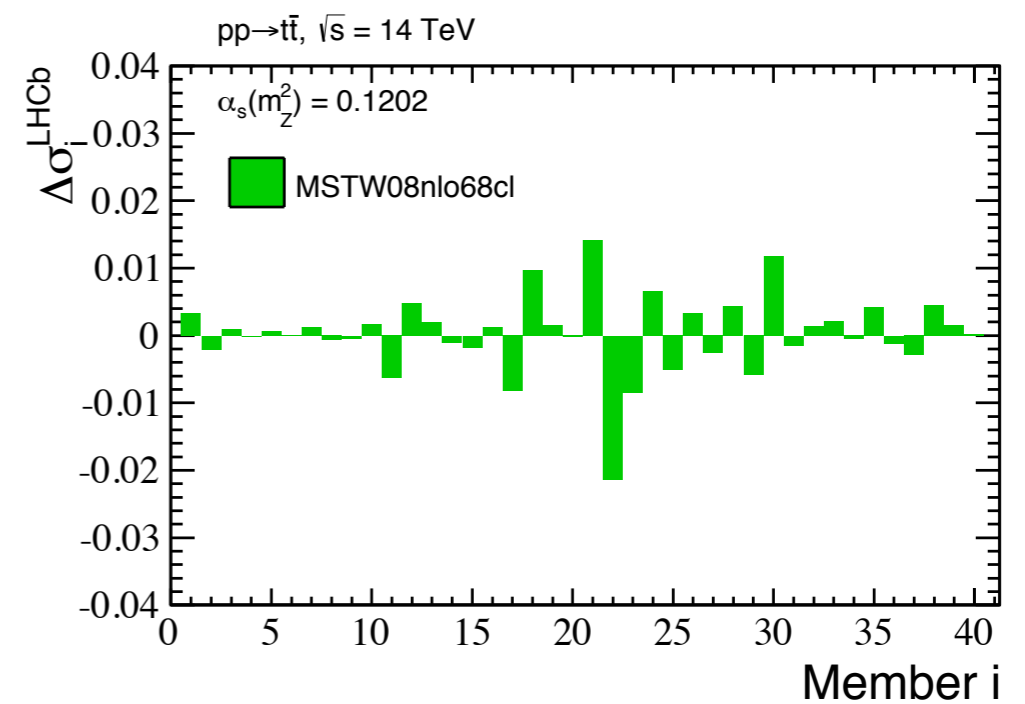
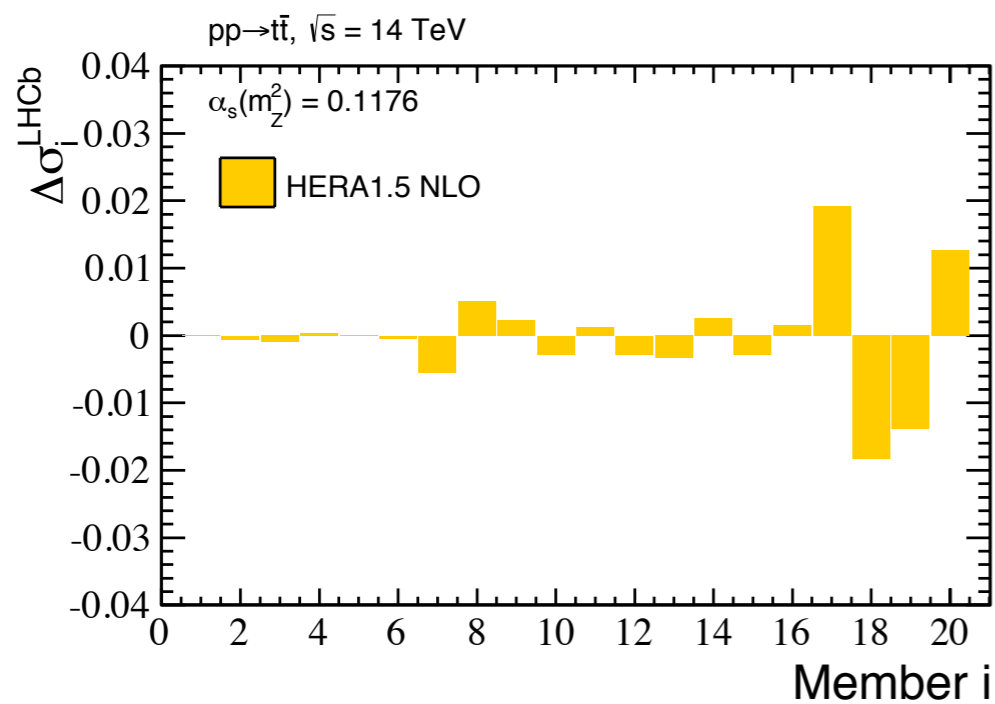
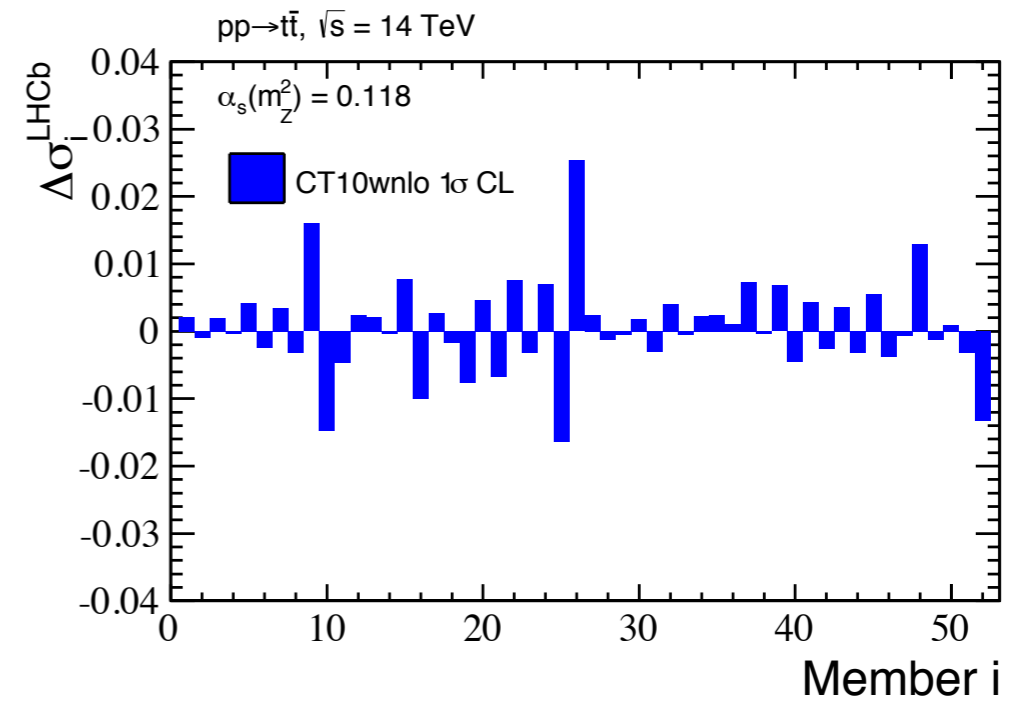
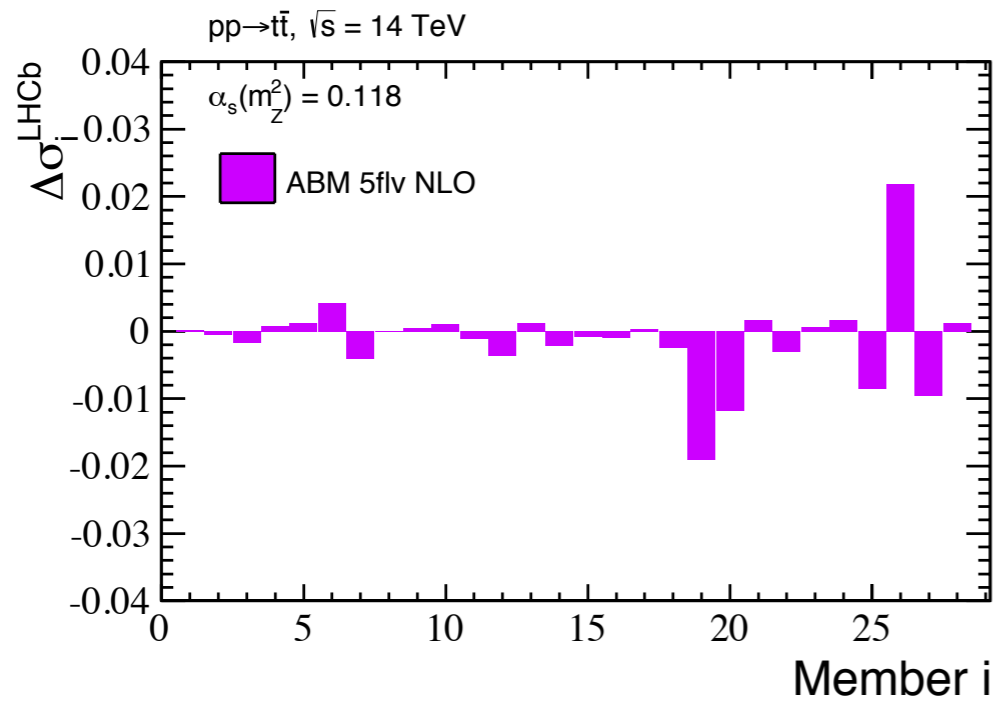
# Follow the recipe - steps 3, 4

3) Pick some pseudo LHCb cross-section data,  $\bar{X}_0 = \frac{1}{N_{\text{rep}}} \sum_{k=1}^{N_{\text{rep}}} X_0(\mathcal{S}_0)[1 + R_{k0}]$

4) Apply weights found using pseudodata to reweight evolved gluon PDF

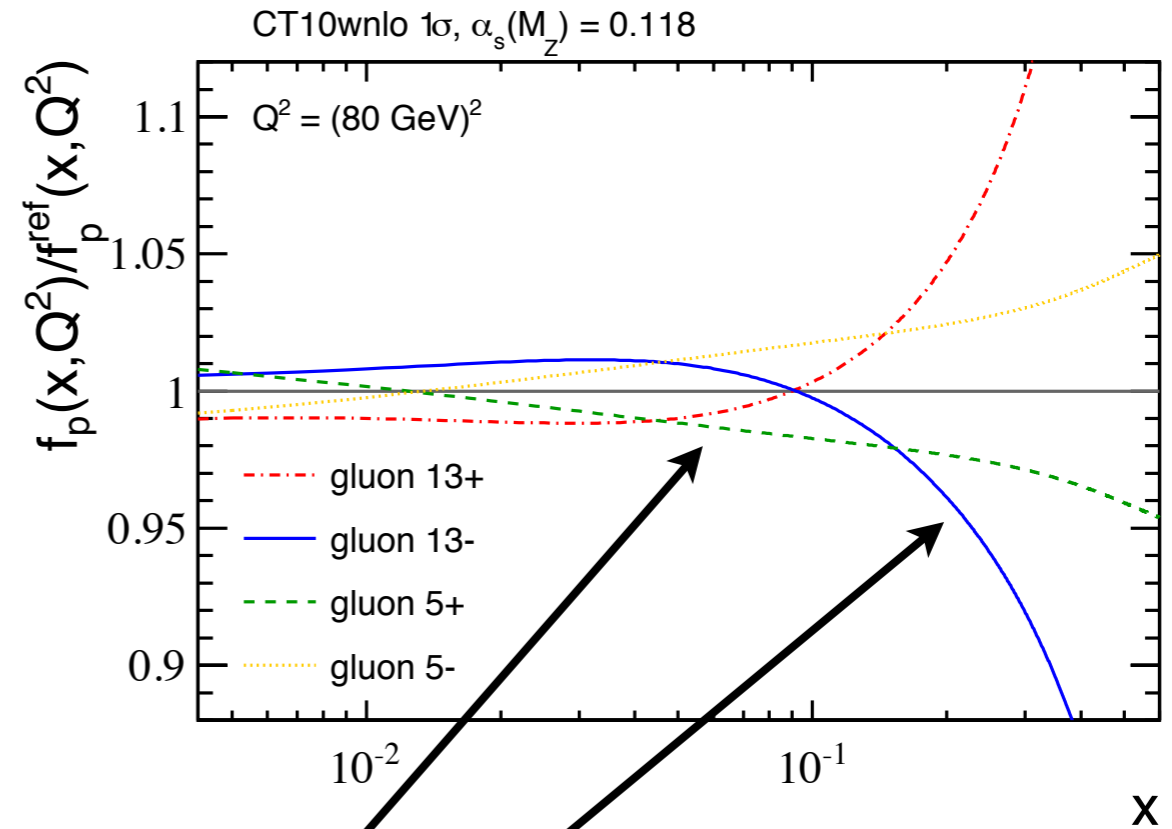
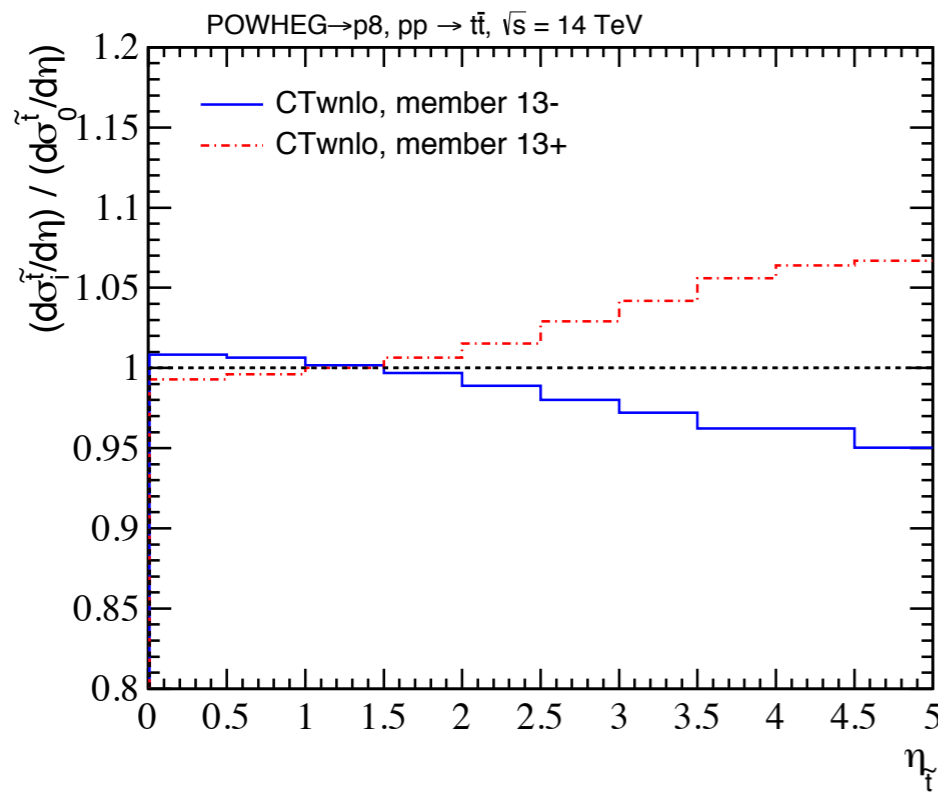


# Summary of eigenvector sensitivity



$$\Delta X_j^\pm = \frac{X(\mathcal{S}_j^\pm) - X(\mathcal{S}_0)}{X(\mathcal{S}_0)}$$

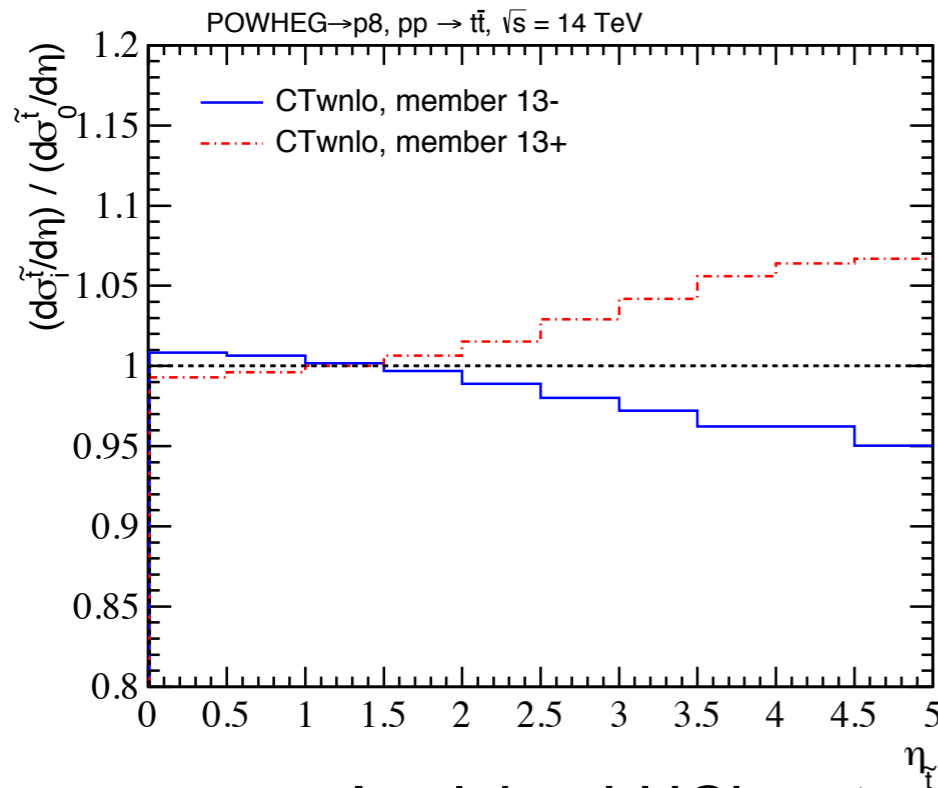
# Effect of LHCb analysis cuts



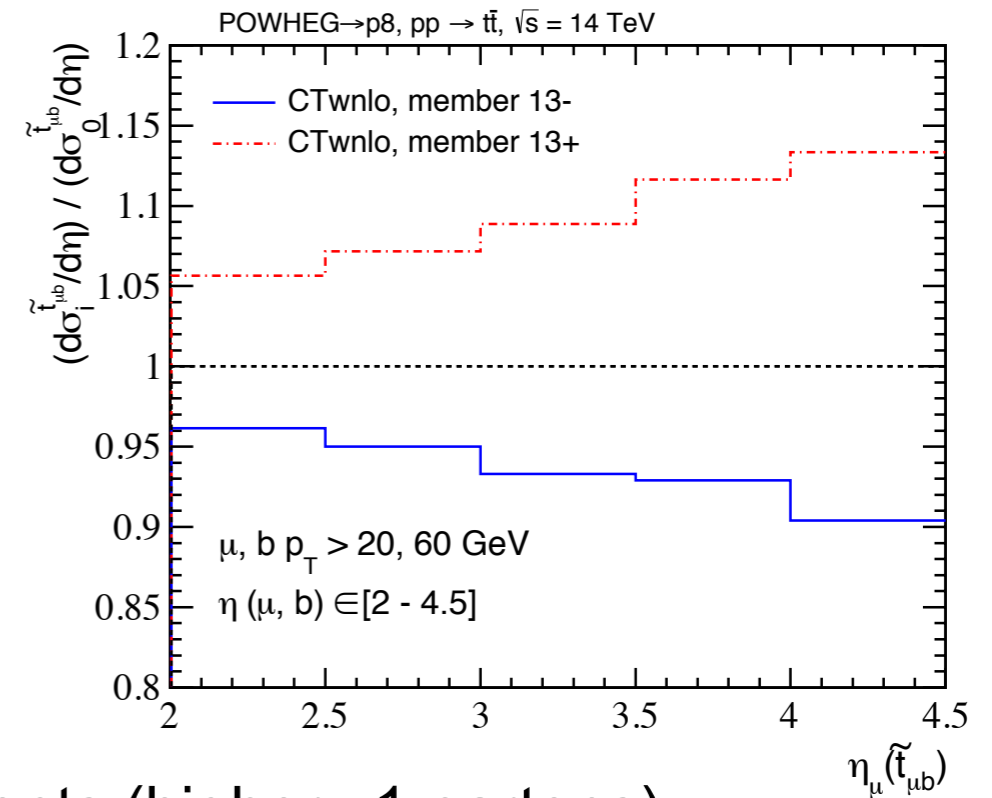
Central production,  $x < 0.1$

Forward production,  $x > 0.1$

# Effect of LHCb analysis cuts

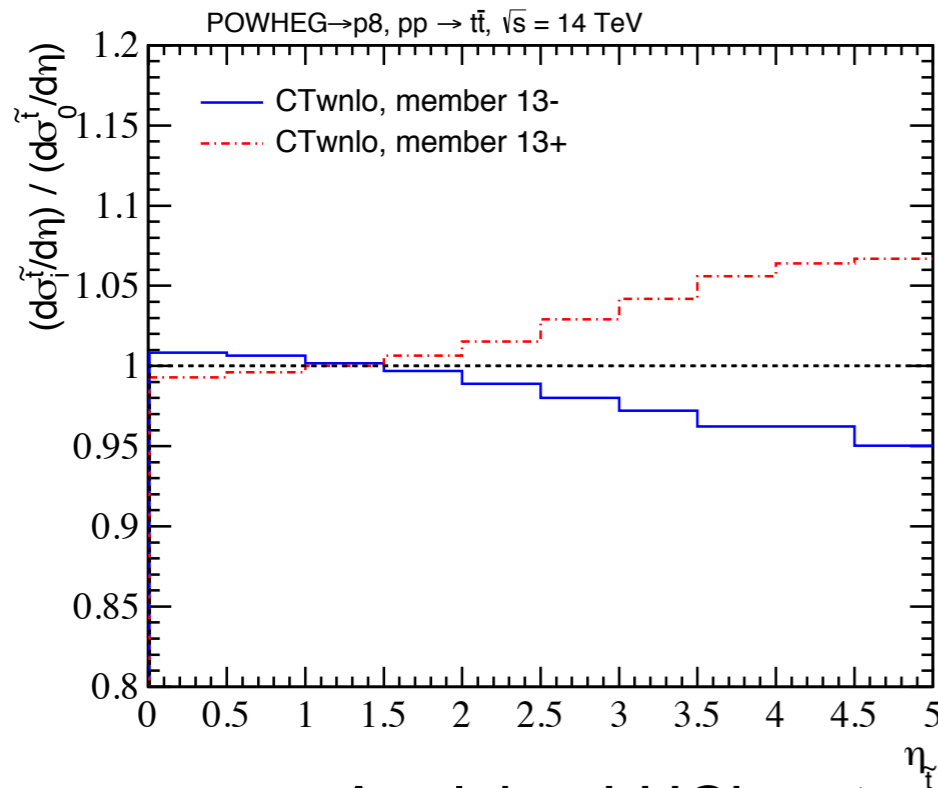


Apply  
LHCb  
analysis  
cuts

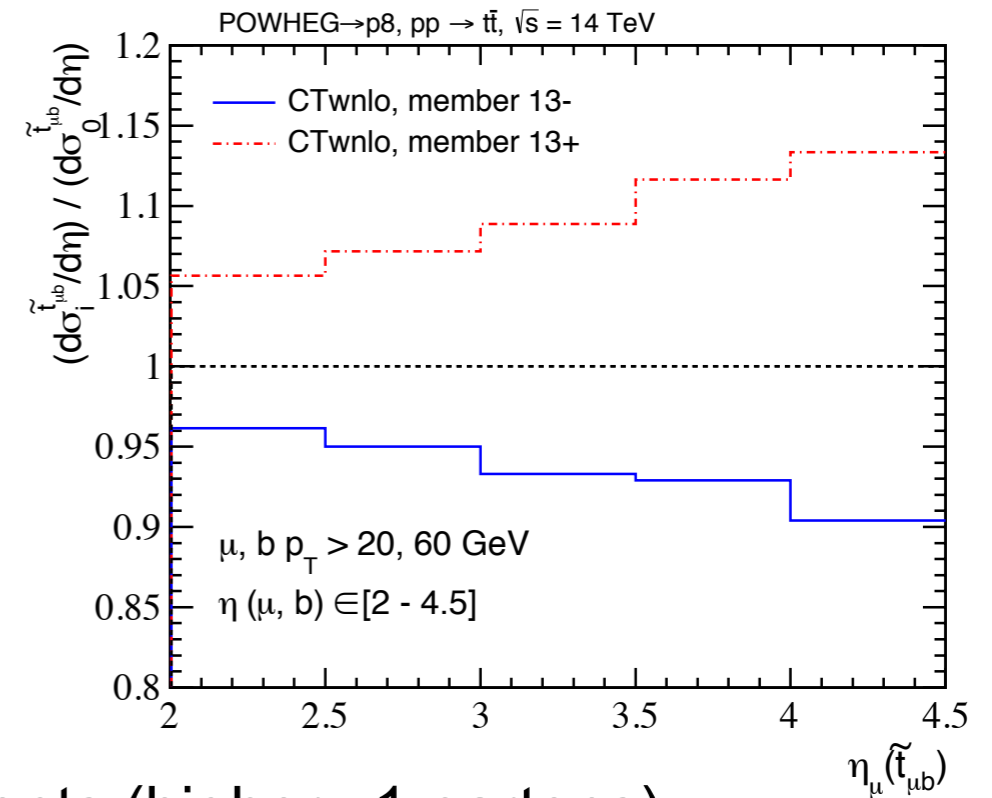


Applying LHCb cuts selects harder events (higher x1 partons)

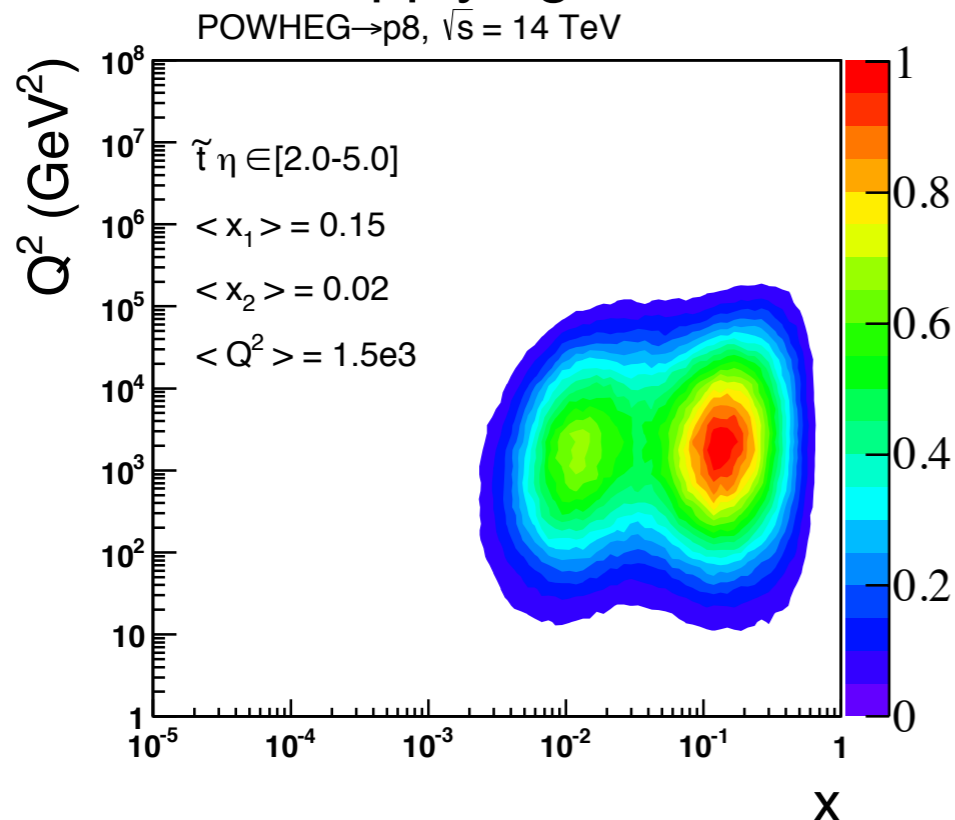
# A few more comments



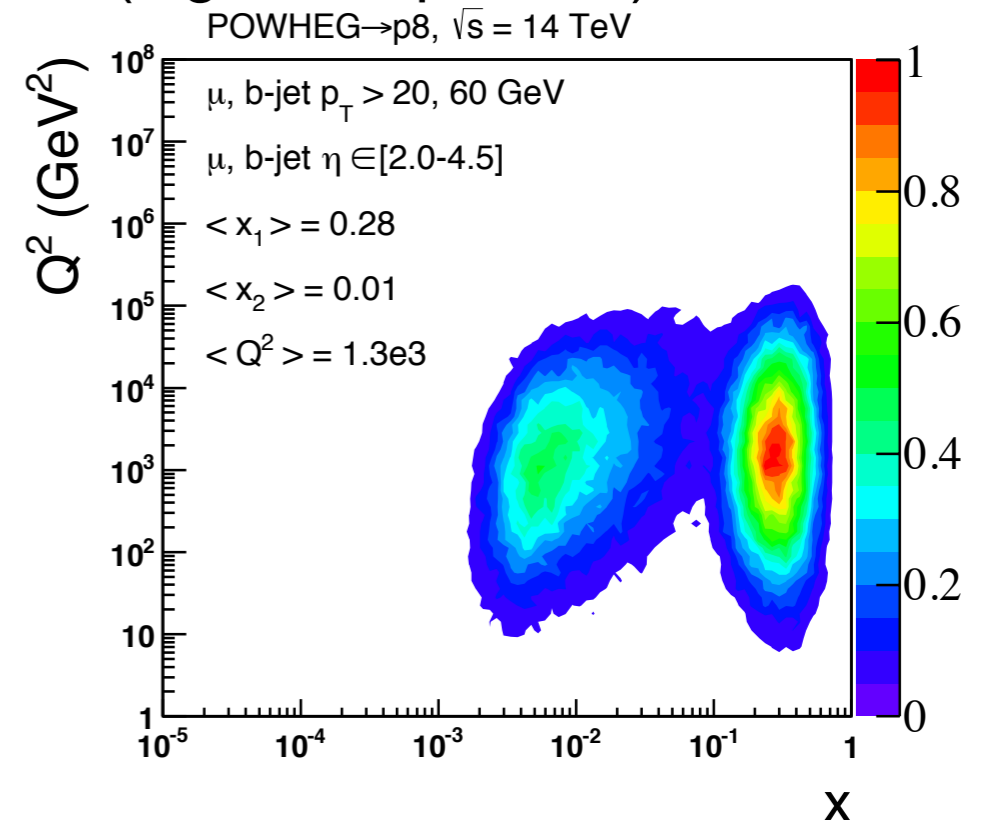
Apply  
LHCb  
analysis  
cuts



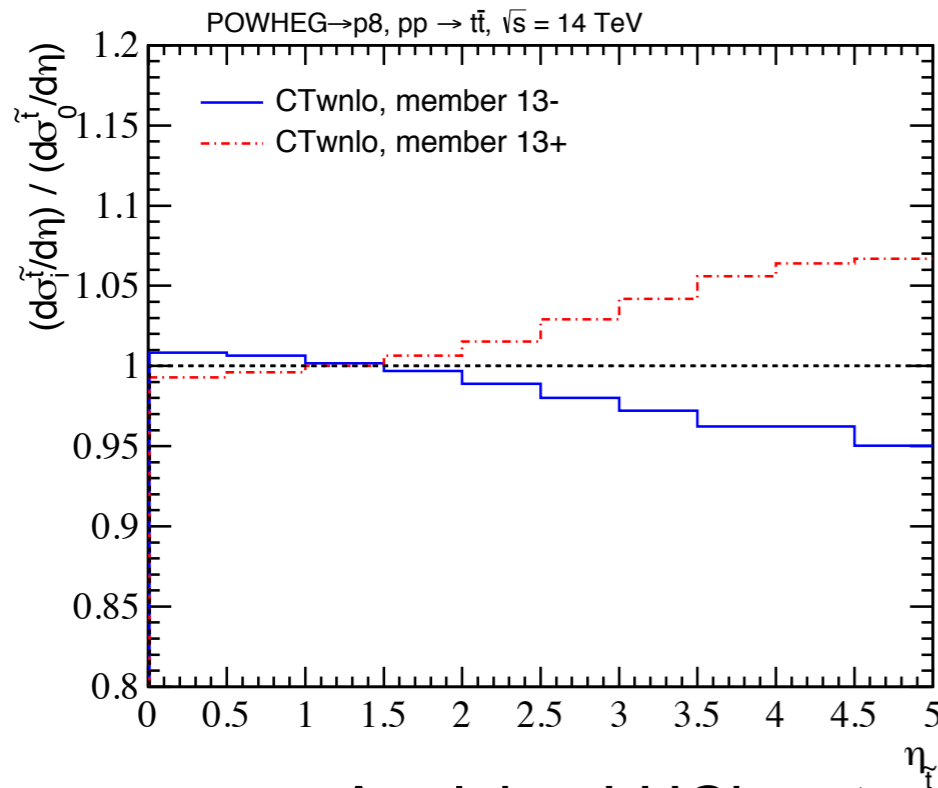
Applying LHCb cuts selects harder events (higher  $x_1$  partons)



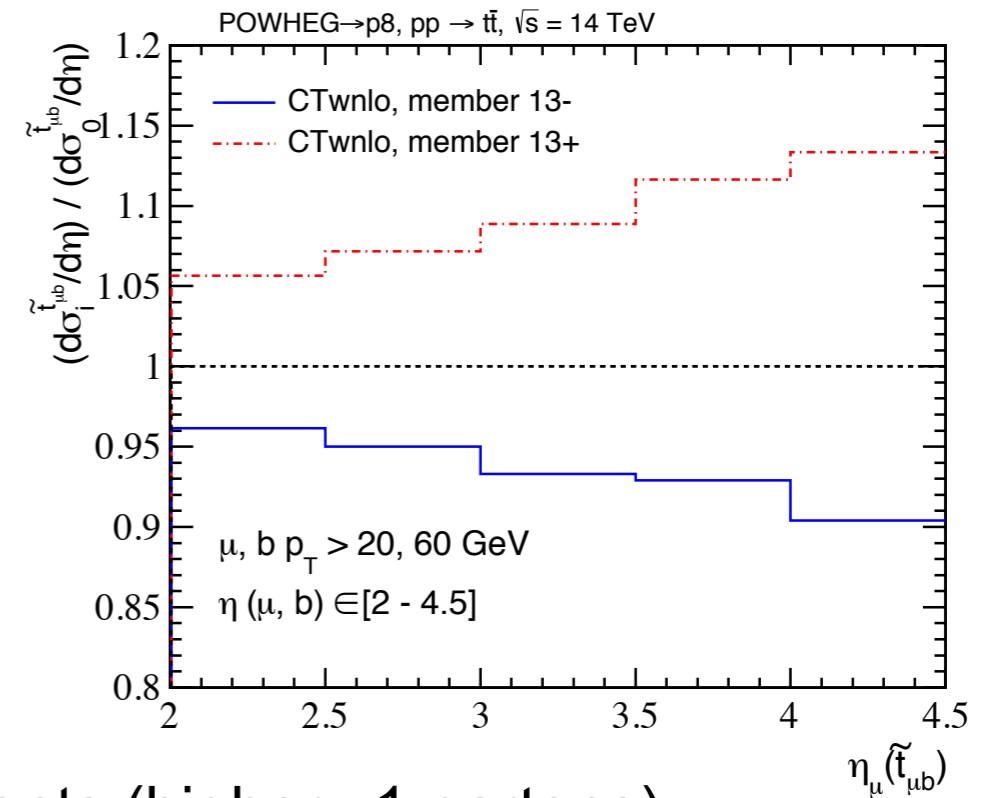
Apply  
LHCb  
analysis  
cuts



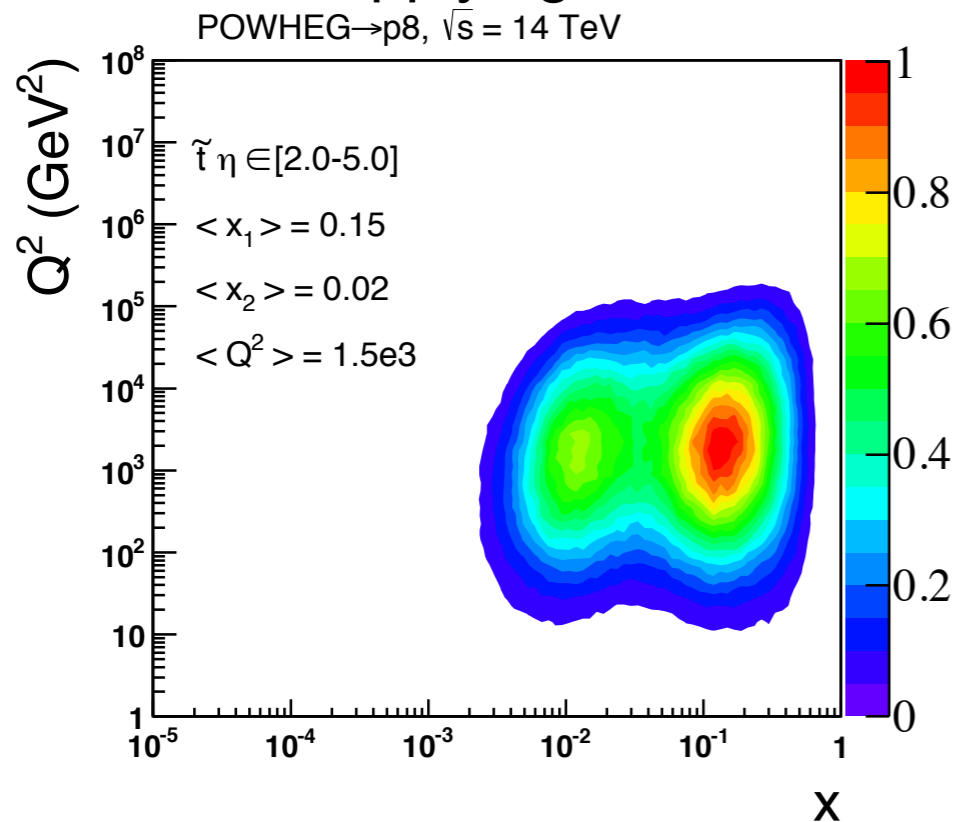
# A few more comments



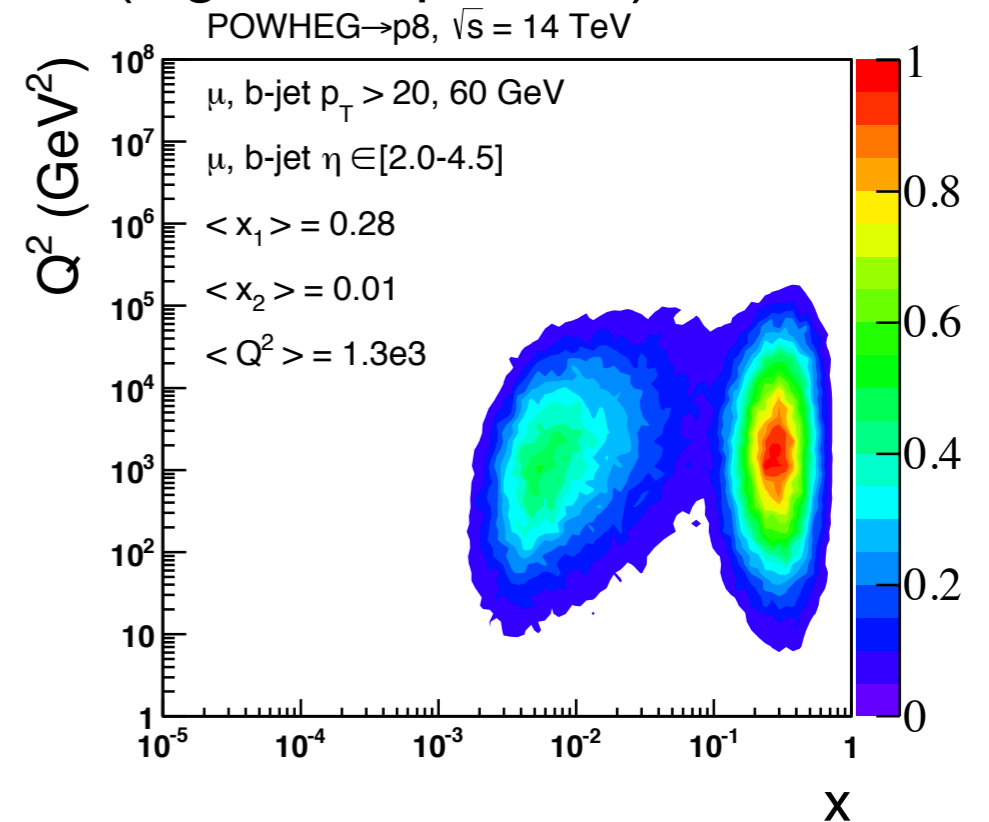
Apply  
LHCb  
analysis  
cuts



Applying LHCb cuts selects harder events (higher  $x_1$  partons)

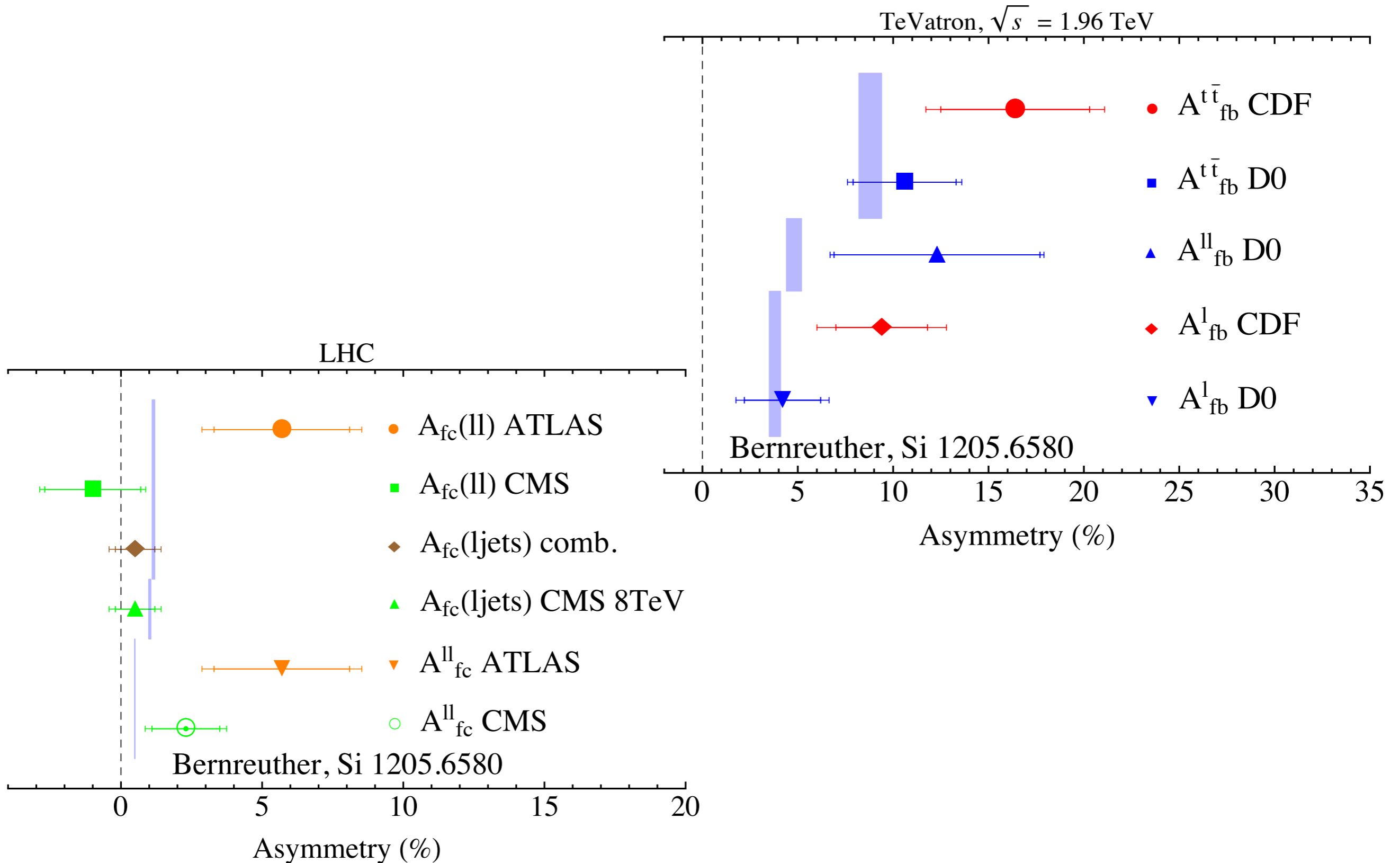


Apply  
LHCb  
analysis  
cuts





# Asymmetry summaries



# LHC 8TeV Asym Systematics

CMS-PAS-TOP 12 033  
8TeV

Systematic uncertainty	shift in inclusive $A_C$	range of shifts in differential $A_C$
JES	0.001	0.001 – 0.005
JER	0.001	0.001 – 0.005
Pileup	0.001	0.000 – 0.003
b tagging	0.000	0.001 – 0.003
Lepton ID/sel. efficiency	0.002	0.001 – 0.003
Generator	0.003	0.001 – 0.015
Hadronization	0.000	0.000 – 0.016
$p_T$ weighting	0.001	0.000 – 0.003
$Q^2$ scale	0.003	0.000 – 0.009
W+jets	0.002	0.001 – 0.007
Multijet	0.001	0.002 – 0.009
PDF	0.001	0.001 – 0.003
Unfolding	0.002	0.001 – 0.004
Total	0.006	0.007 – 0.022