Top Mass Measurement at Linear Colliders

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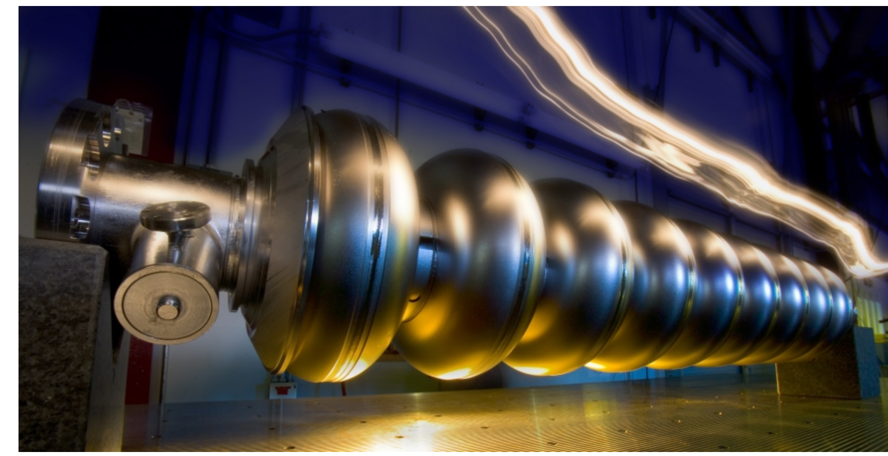
Max-Planck-Institut für Physik
(Werner-Heisenberg-Institut)

Outline

- Introduction: Linear Colliders in brief
- Top quarks in e^+e^- collisions
- Invariant mass
- A ttbar threshold scan at ILC
  - Sensitivities to top parameters
  - Experimental resolution
  - Systematics
- Summary

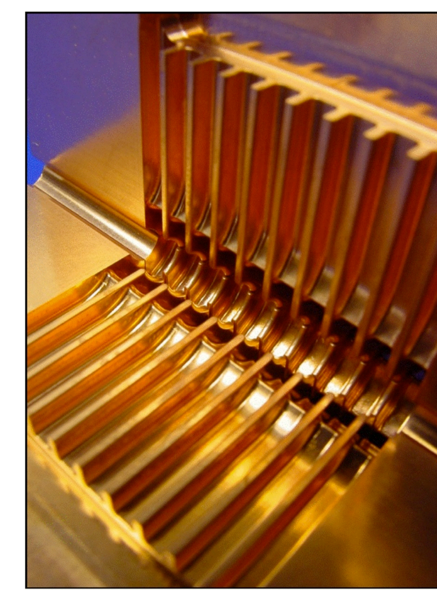
Linear Colliders - In Brief

- Two accelerator concepts for an energy-frontier e^+e^- collider with an energy reach up to the top pair threshold and beyond:
  - ILC - 500 GeV with 250 GeV initial stage, extendable to 1 TeV, based on SCRF with gradients of ~35 MV/m
    TDR completed - almost shovel-ready



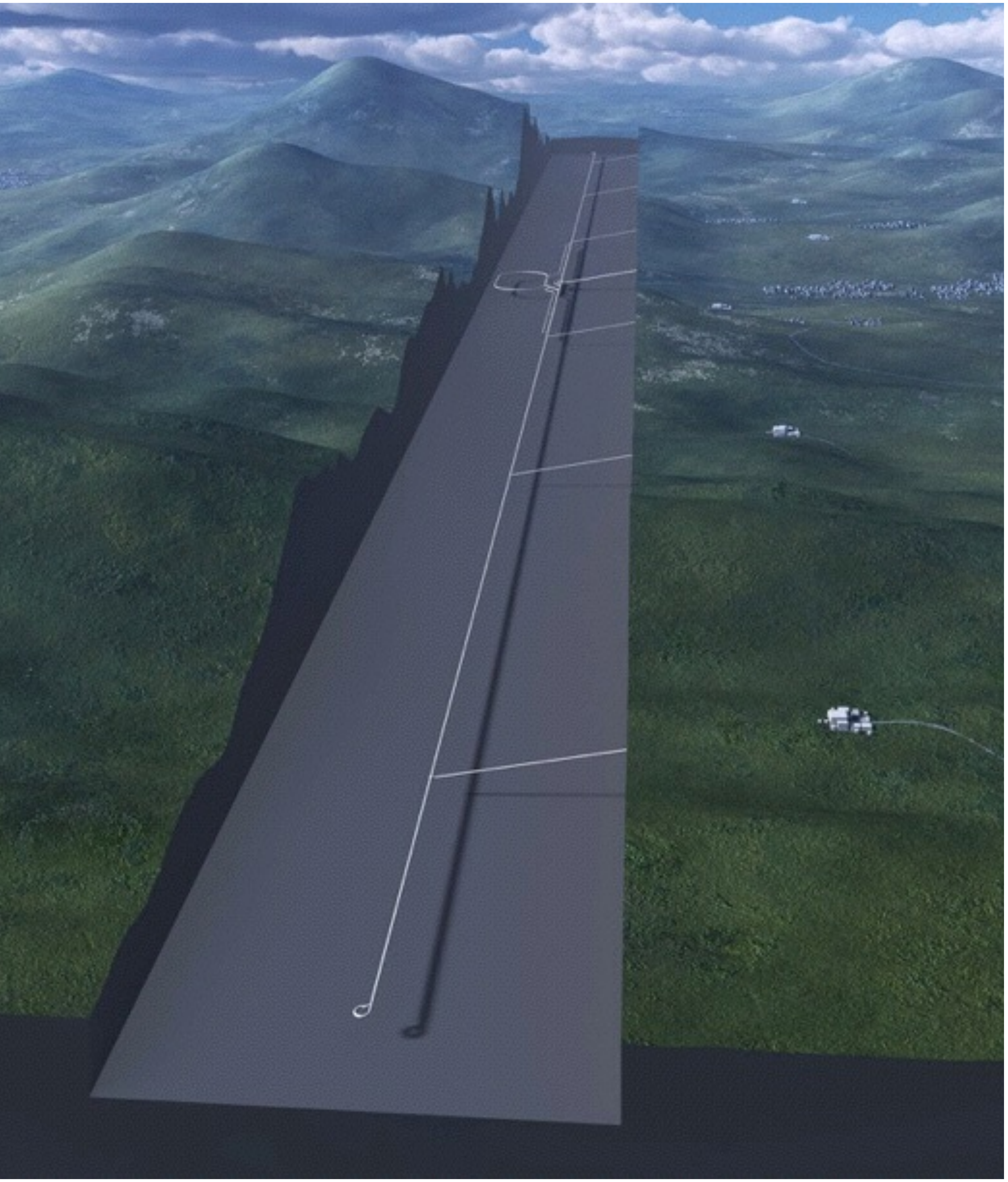
Interest in Japan to host - as a global project

  - CLIC - 3 TeV with 2 lower-energy stages, based on two-beam acceleration with warm RF, gradients of 100 MV/m
    CDR completed - Development phase until ~2018 to reach maturity for construction



- Both provide luminosities on the 1 - 2 x 10^{34} $cm^{-2}s^{-1}$ level at the top threshold, possibilities for threshold scans and polarized beams

Linear Colliders - In Brief



- ILC: Site selected in Japan: Kitakami, near Sendai
  - 30 km for 500 GeV, 50 km for 1 TeV
- Now: Discussions on political levels...

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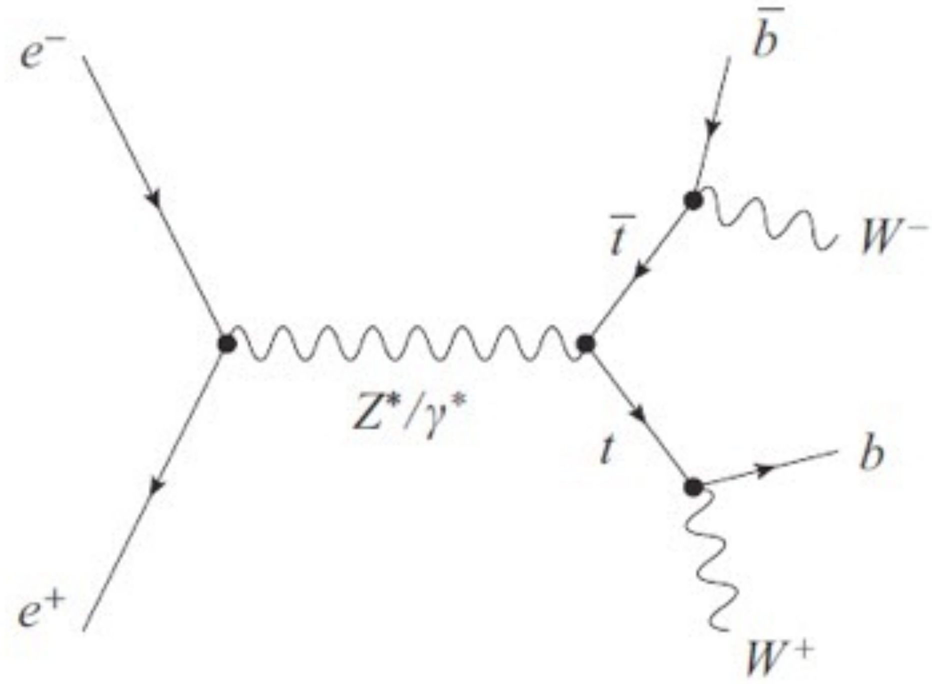
- CLIC: A possible future high energy frontier project at CERN
  - 50 km for 3 TeV
- R&D for accelerator & detectors

Reconstructing Top Quarks at Lepton Colliders

- Driven by production and decay:
  - Production in pairs, decay to W and b



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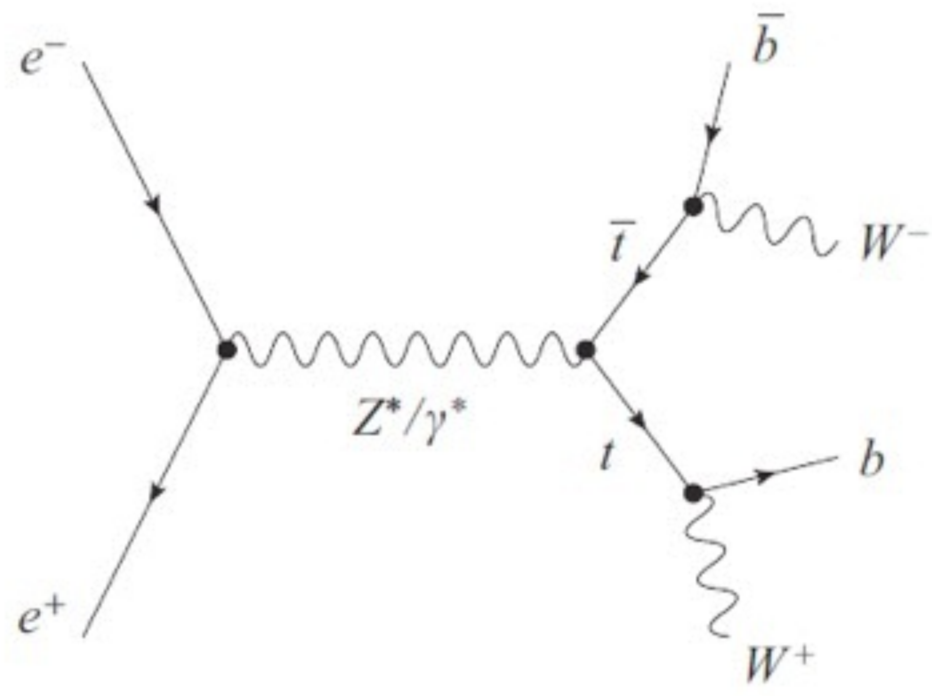
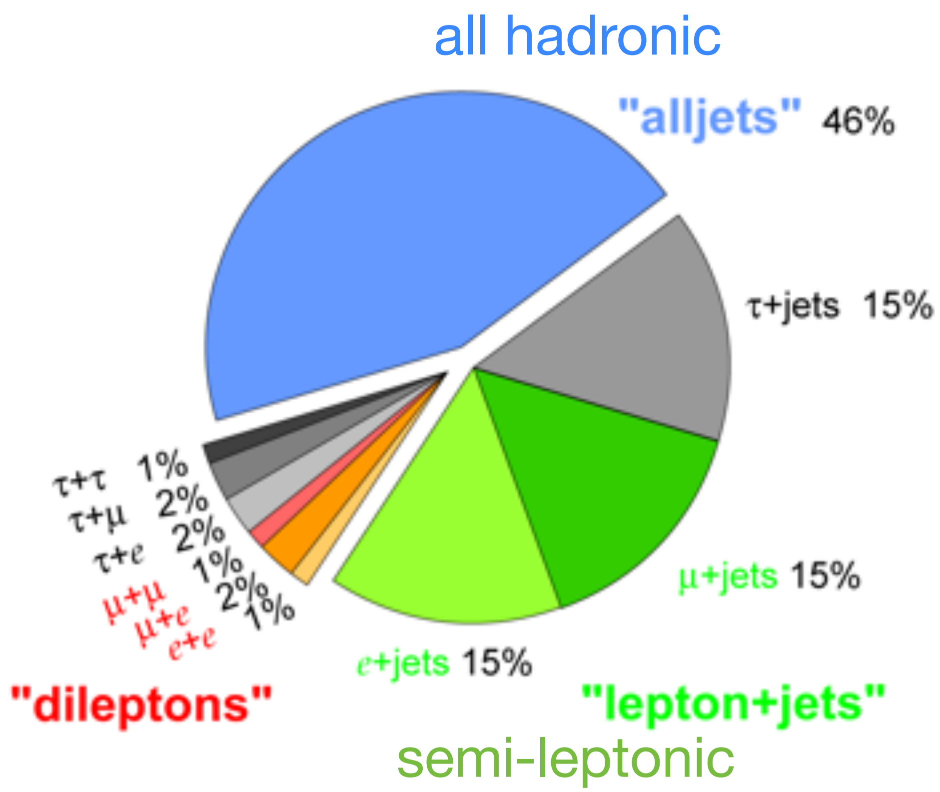


Event signature entirely given by the decay of the W bosons:



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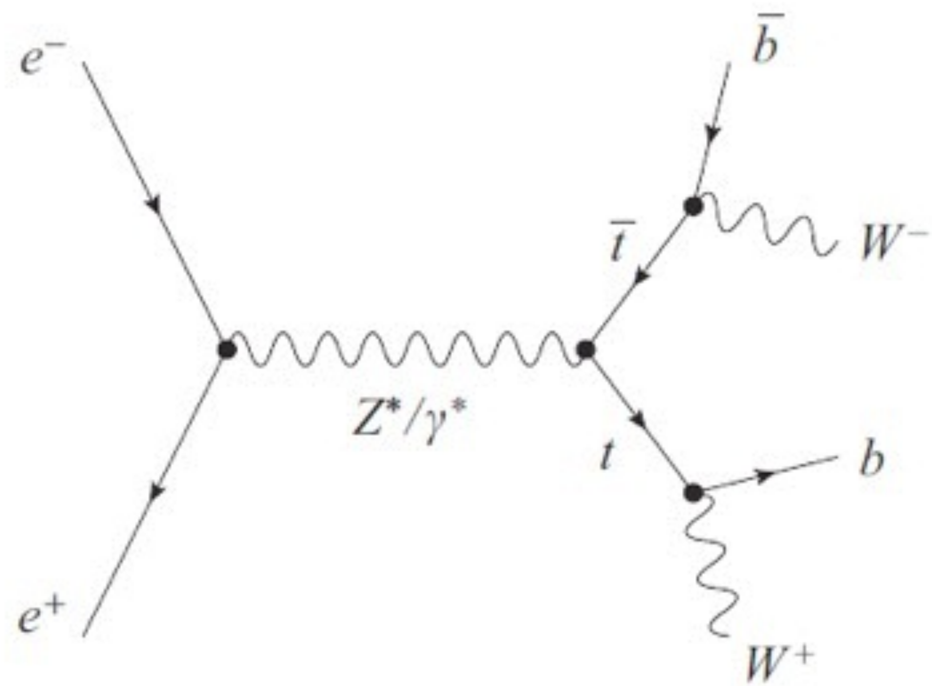

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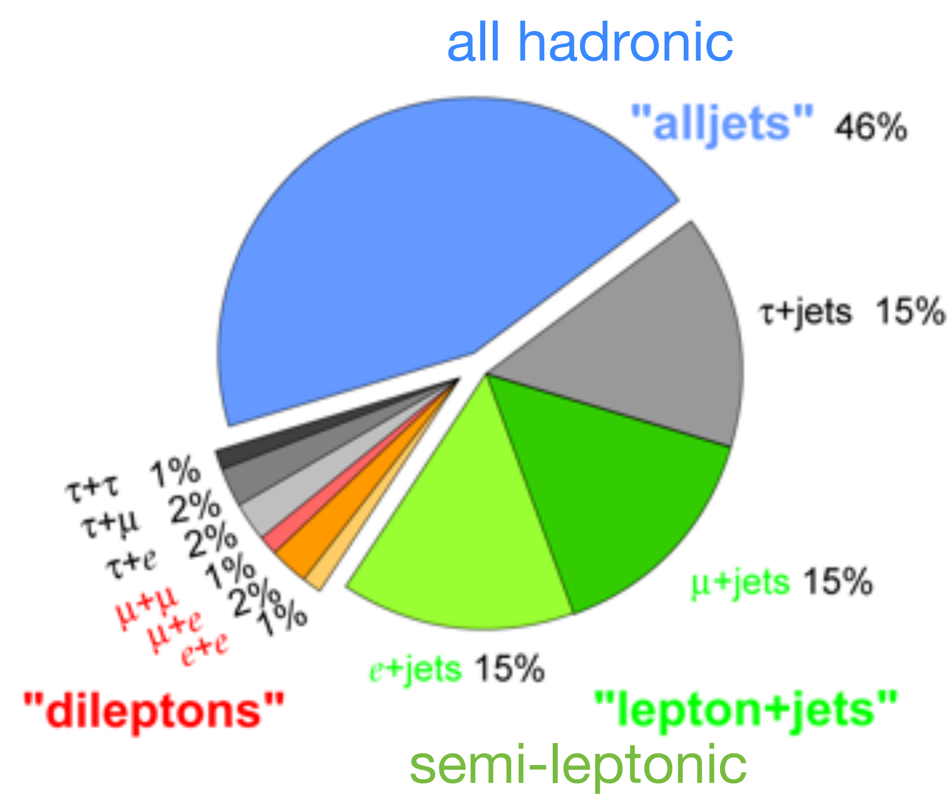


- At hadron colliders: Hard to pick out top pairs from QCD background - Use one and two-lepton final states
- At lepton colliders: Top pairs easy to identify, concentrate on large branching fractions and controllable missing energy (not more than one neutrino!)

Analysis Challenges & Event Simulation - CLIC

- Key reconstruction challenge at CLIC: pile-up of γγ -> hadrons background, rejected with timing & p_t cuts and with jet finding based on k_t algorithm
  - Also relevant for ILC: No pile-up, but several γγ -> hadrons events / BX - Jet finding now follows CLIC experience

- Event generation with PYTHIA (for ttbar, LO) and WHIZARD, depending on final state
- Full GEANT4 detector simulation
- Reconstruction with PandoraPFA

no direct simulation of threshold - currently using NNLO cross sections - *TOPPIK, Hoang & Teubner* -

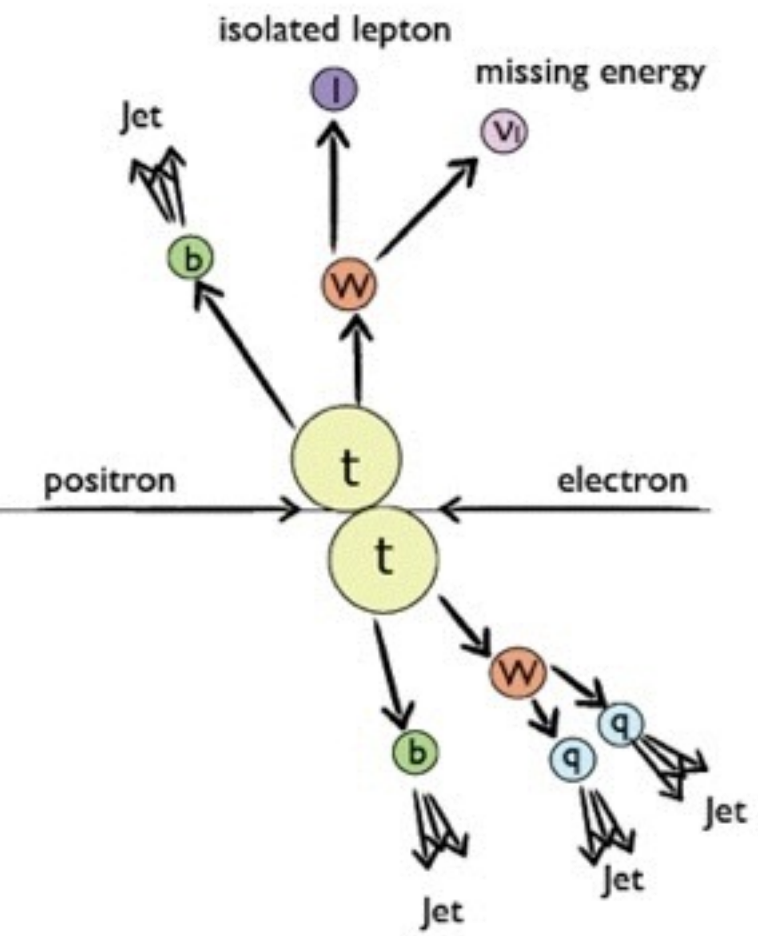
type	final state	σ 500 GeV	σ 352 GeV
Signal (m_{top} = 174 GeV)	$t\bar{t}$	530 fb	450 fb
Background	WW	7.1 pb	11.5 pb
Background	ZZ	410 fb	865 fb
Background	$q\bar{q}$	2.6 pb	25.2 pb
Background	WWZ	40 fb	10 fb

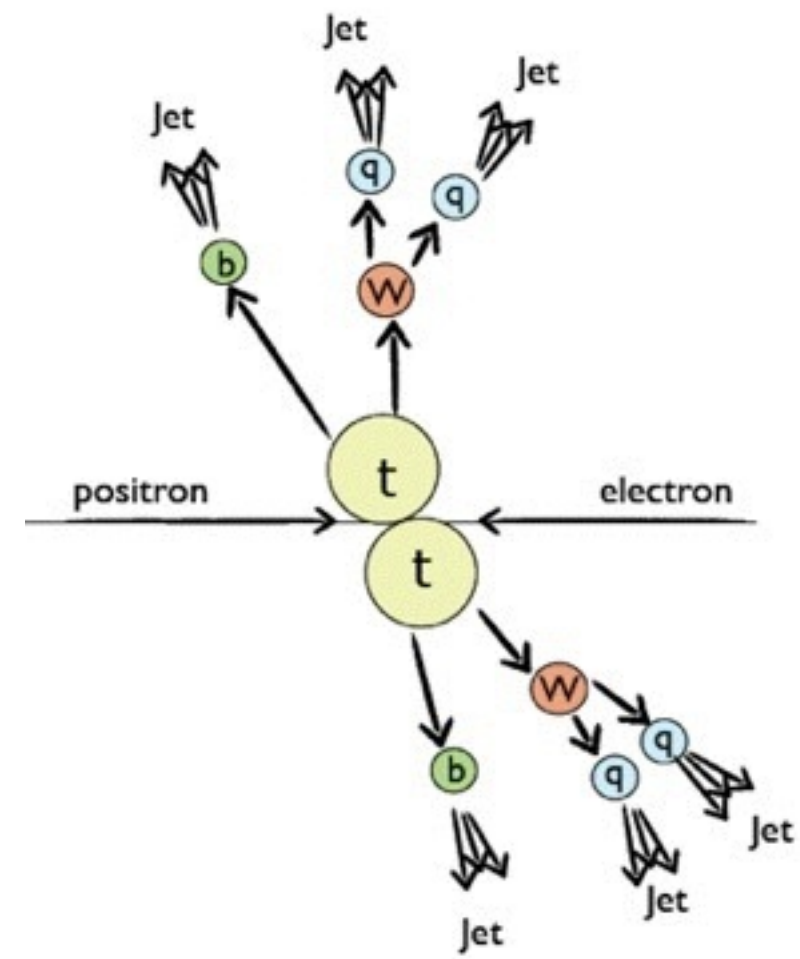
both at and above threshold 100 fb^{-1} assumed

… in addition: single top may be worth considering

Identifying & Reconstructing Top Quarks

- Strategy depends on targeted ttbar final state





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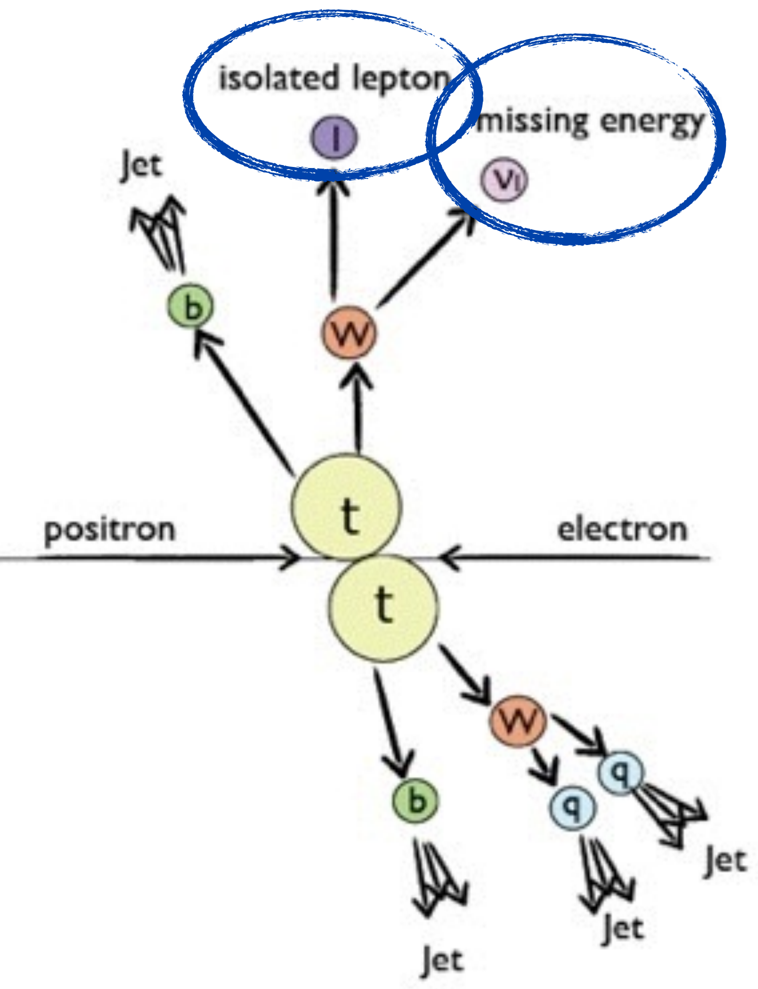
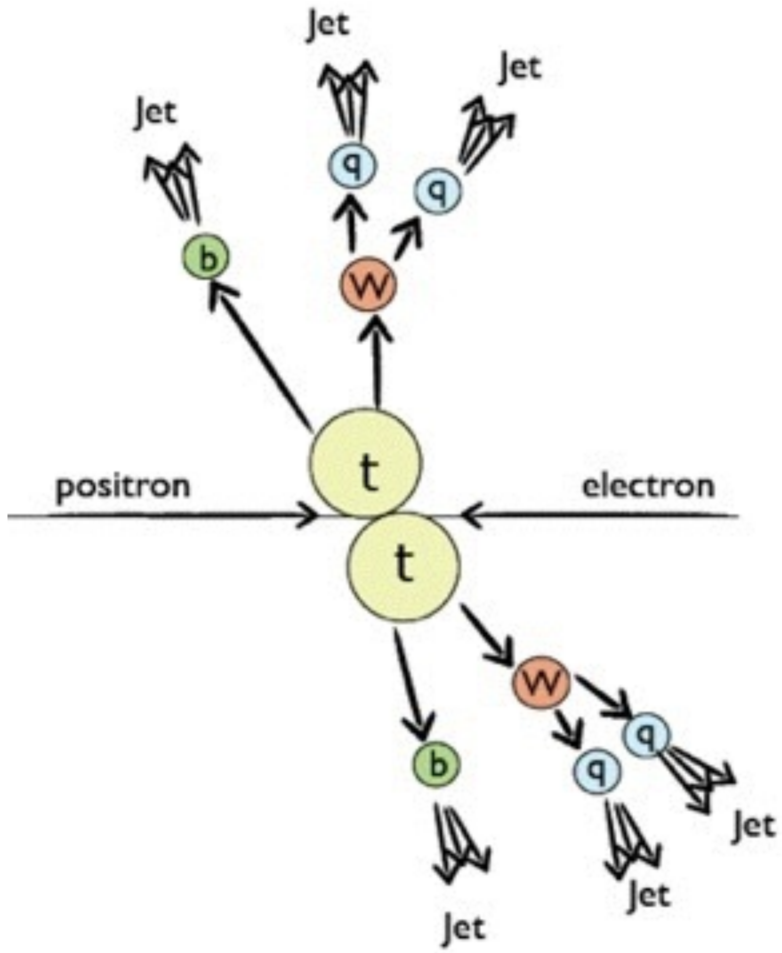


Semi-leptonic:

- isolated lepton ID, momentum measurement
- missing energy measurement



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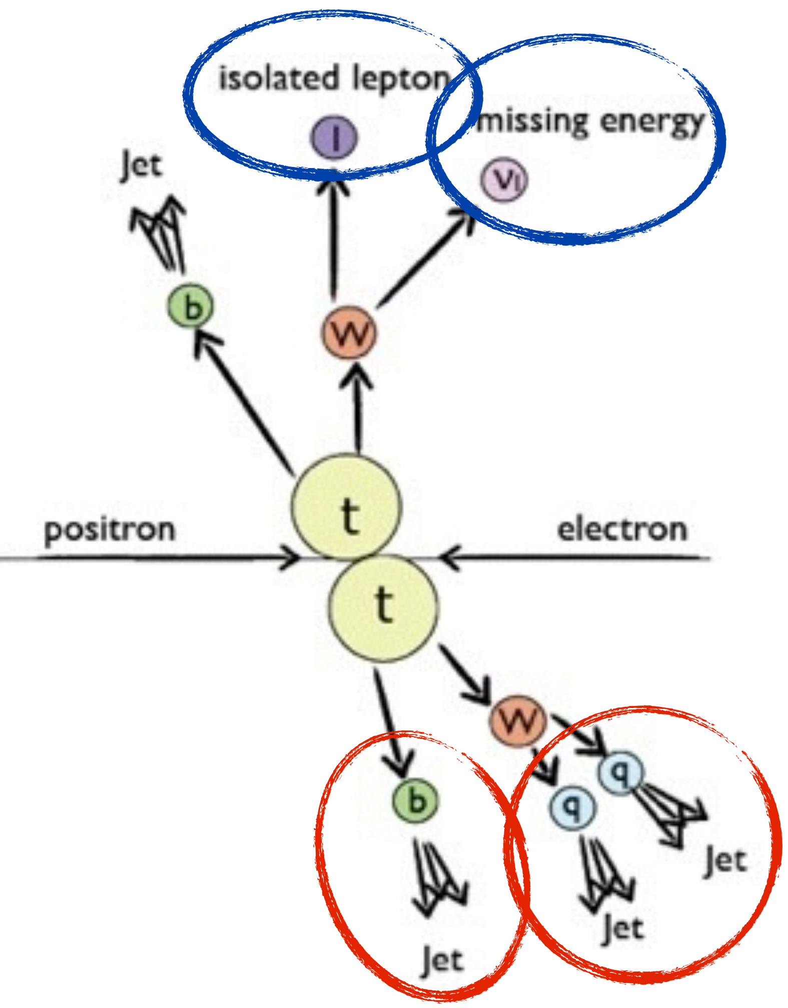

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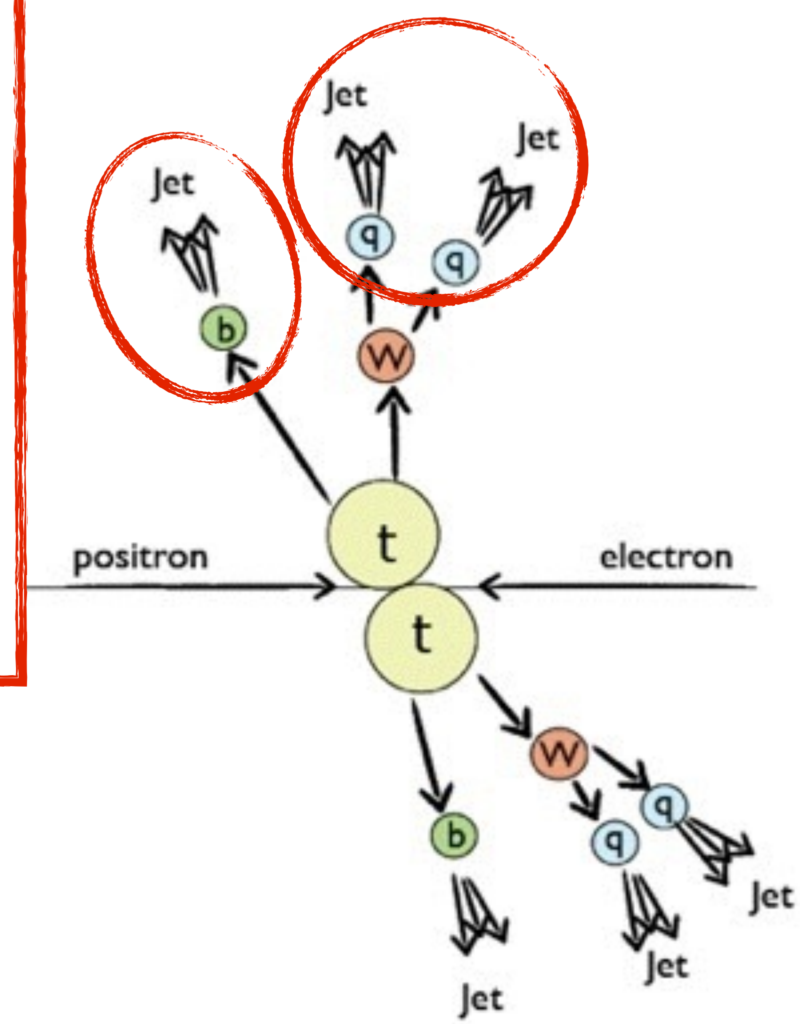
Universal

- Flavor tagging:
  - b - identification
  - b/c separation
- b-Jet energy measurement
- light Jet reconstruction & energy measurement



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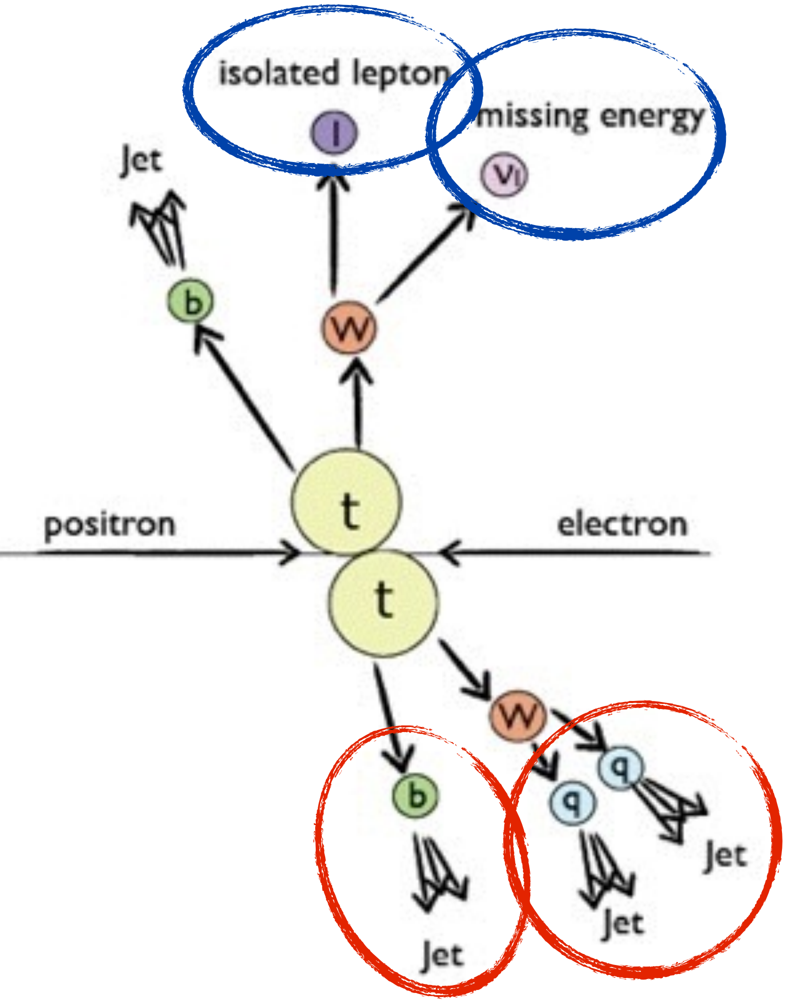

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Universal
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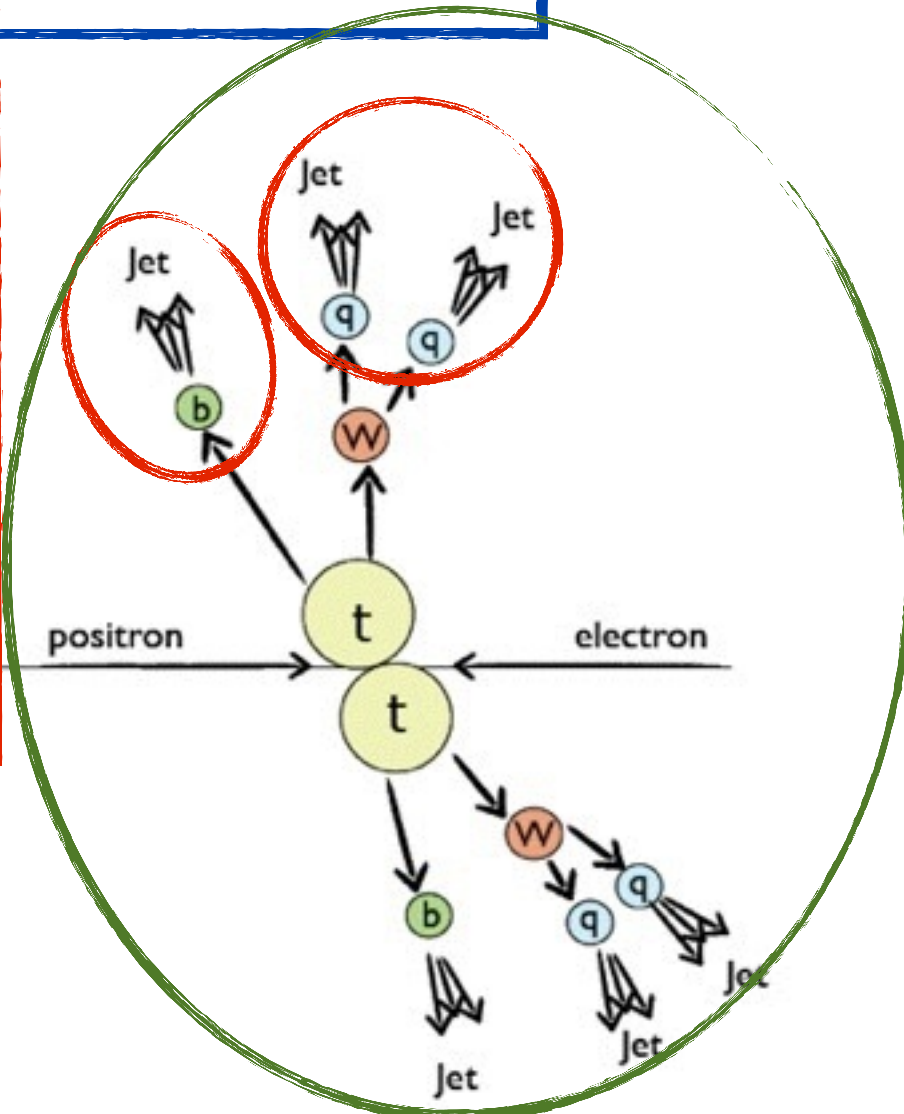
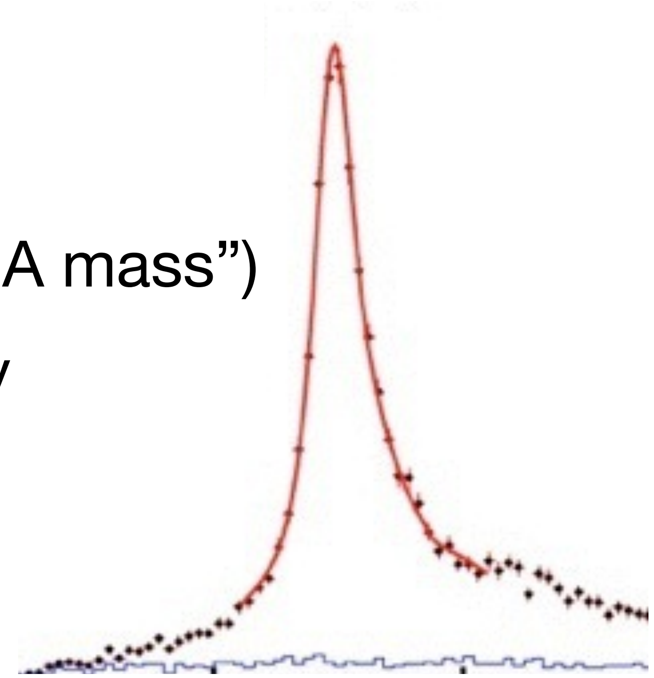
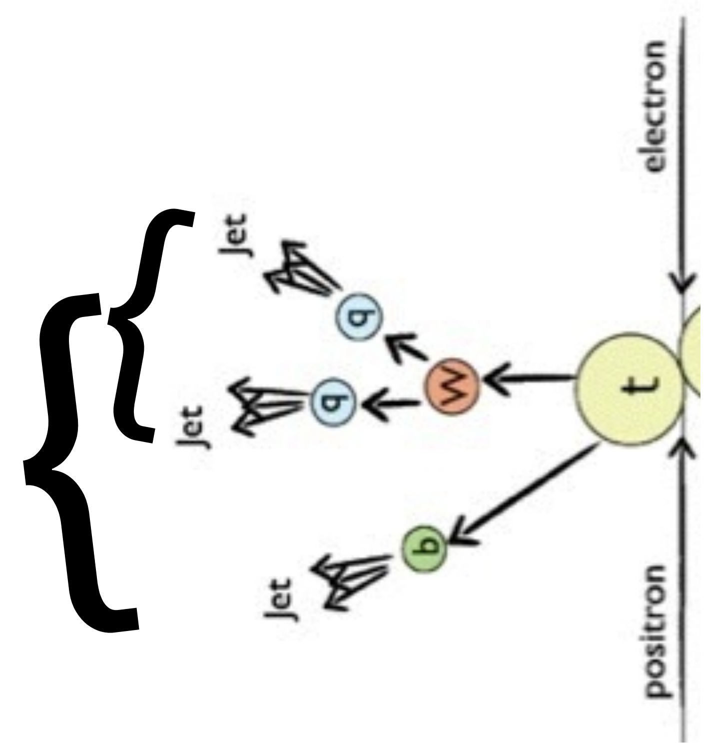
All-hadronic
- global hadronic energy reconstruction



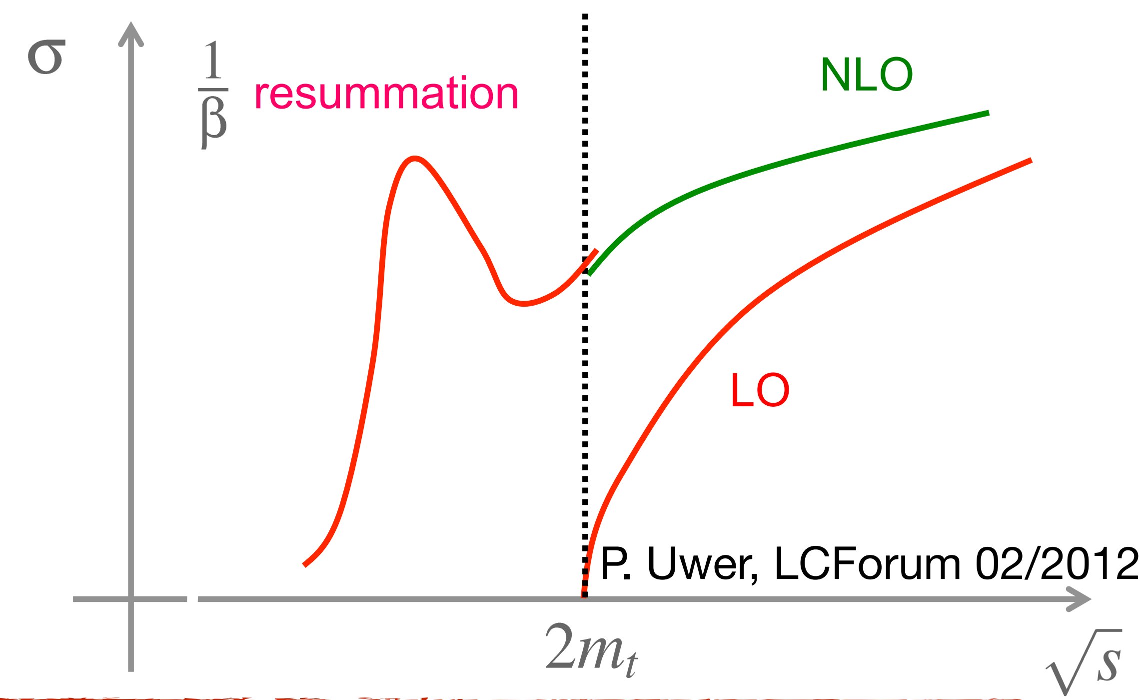
Top Mass at e^+e^- Colliders

- Measurement in top pair production, two possibilities, each with advantages and dis-advantages:
  - Invariant mass
    - experimentally well defined (but not theoretically: “PYTHIA mass”)
    - can be performed at arbitrary energy above threshold: high integrated luminosity

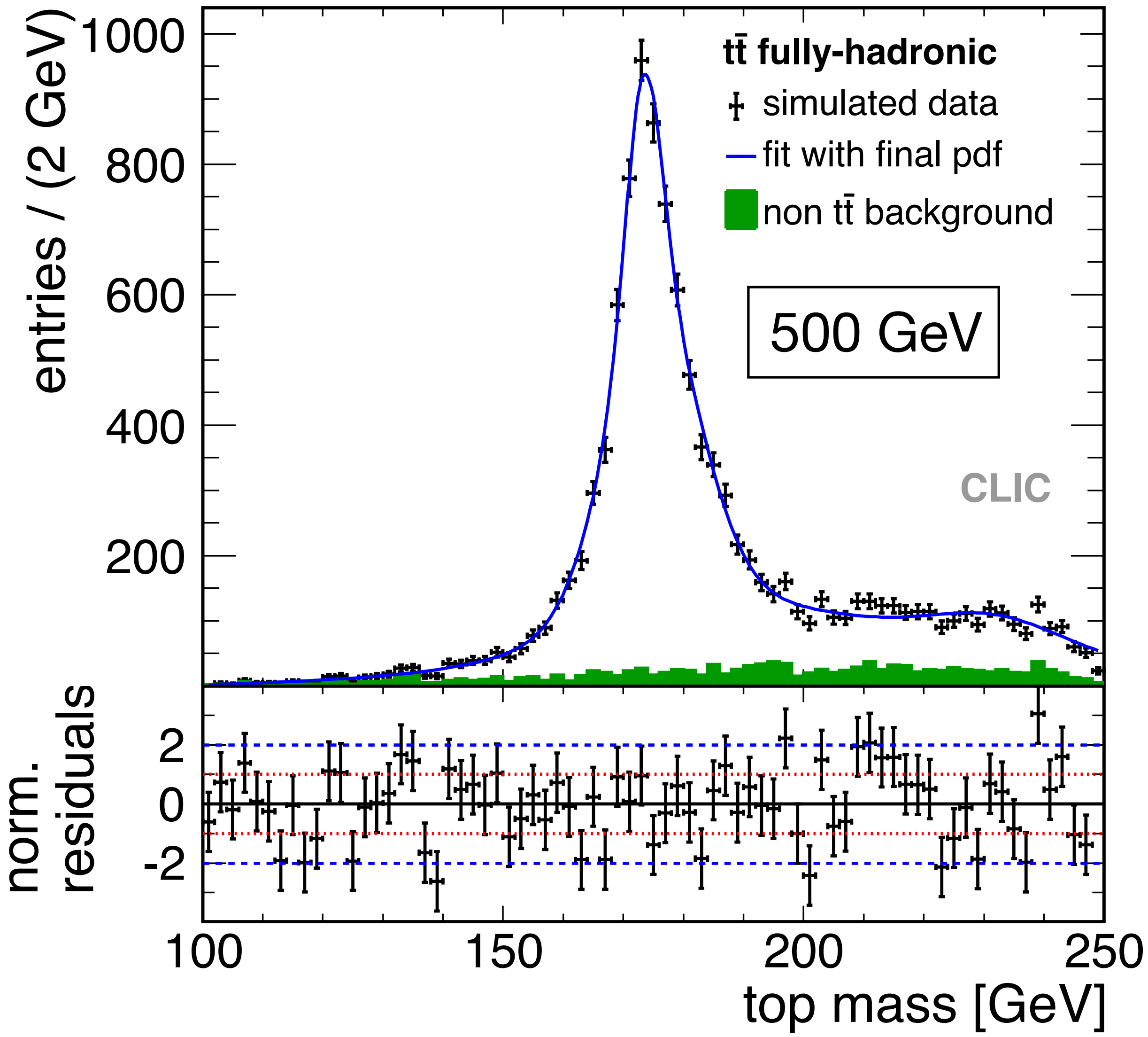




  - Threshold scan
    - theoretically well understood, can be calculated to higher orders
    - needs dedicated running of the accelerator (but is also in a sweet spot for Higgs physics)
    - The “ultimate” mass measurement at a LC!



Reconstruction and kinematic Mass - Performance



- Very low non-ttbar background
  - S/B ~8.5 (12) for FH (SL) at 500 GeV
  - S/B ~4.5 directly above threshold
- High reconstruction efficiency
  - 34% (44%) for FH (SL) at 500 GeV
  - 92% for selected decay modes at threshold

Analysis at threshold optimized for significance, not highest reconstruction quality

Mass fit - Result:

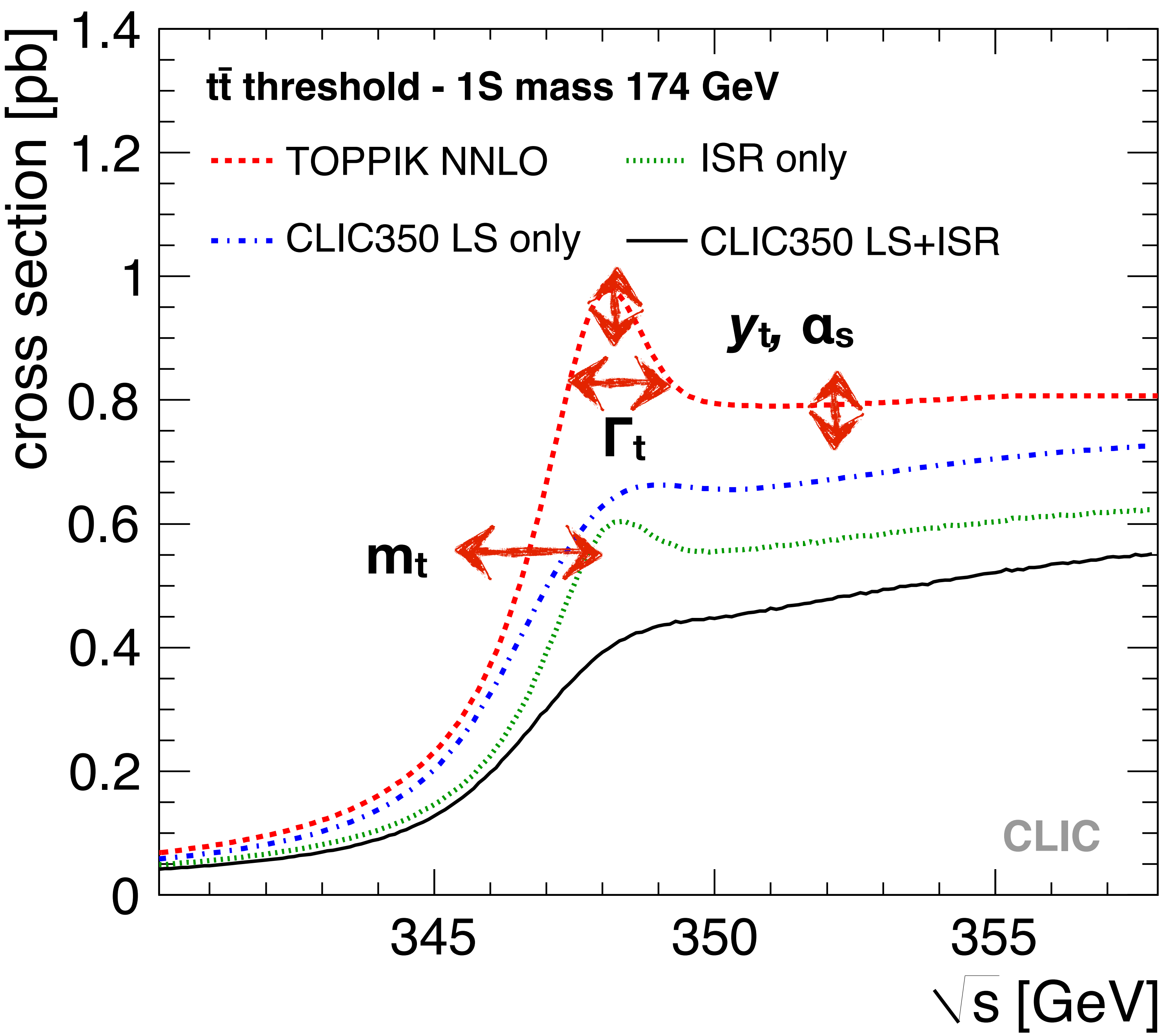
stat. uncertainty on m_t: 80 MeV (FH + SL)

stat. uncertainty on Γ_t: 220 MeV (FH + SL)

exp. systematics of similar order

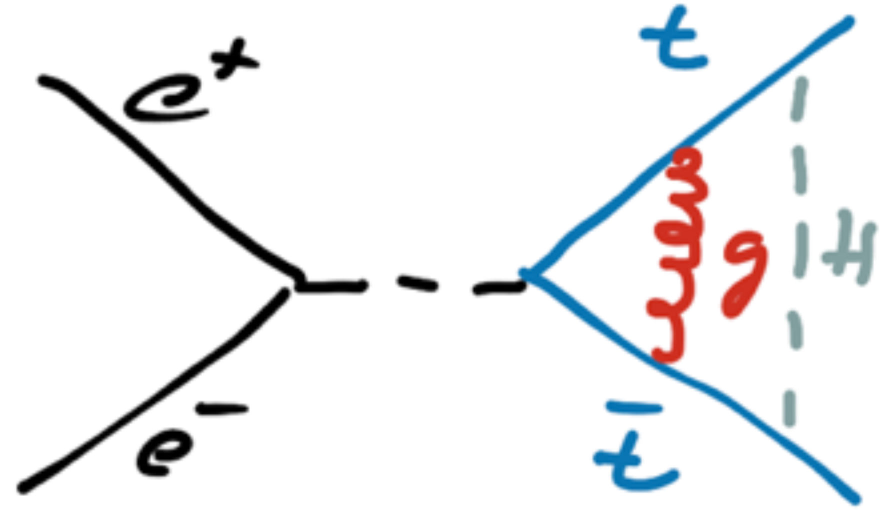
Full simulations with a detailed detector model, signal, physics & machine backgrounds

The Top Threshold - Ultimate Sensitivity



The cross-section around the threshold is affected by several properties of the top quark and by QCD

- Top mass, width, Yukawa coupling
- Strong coupling constant

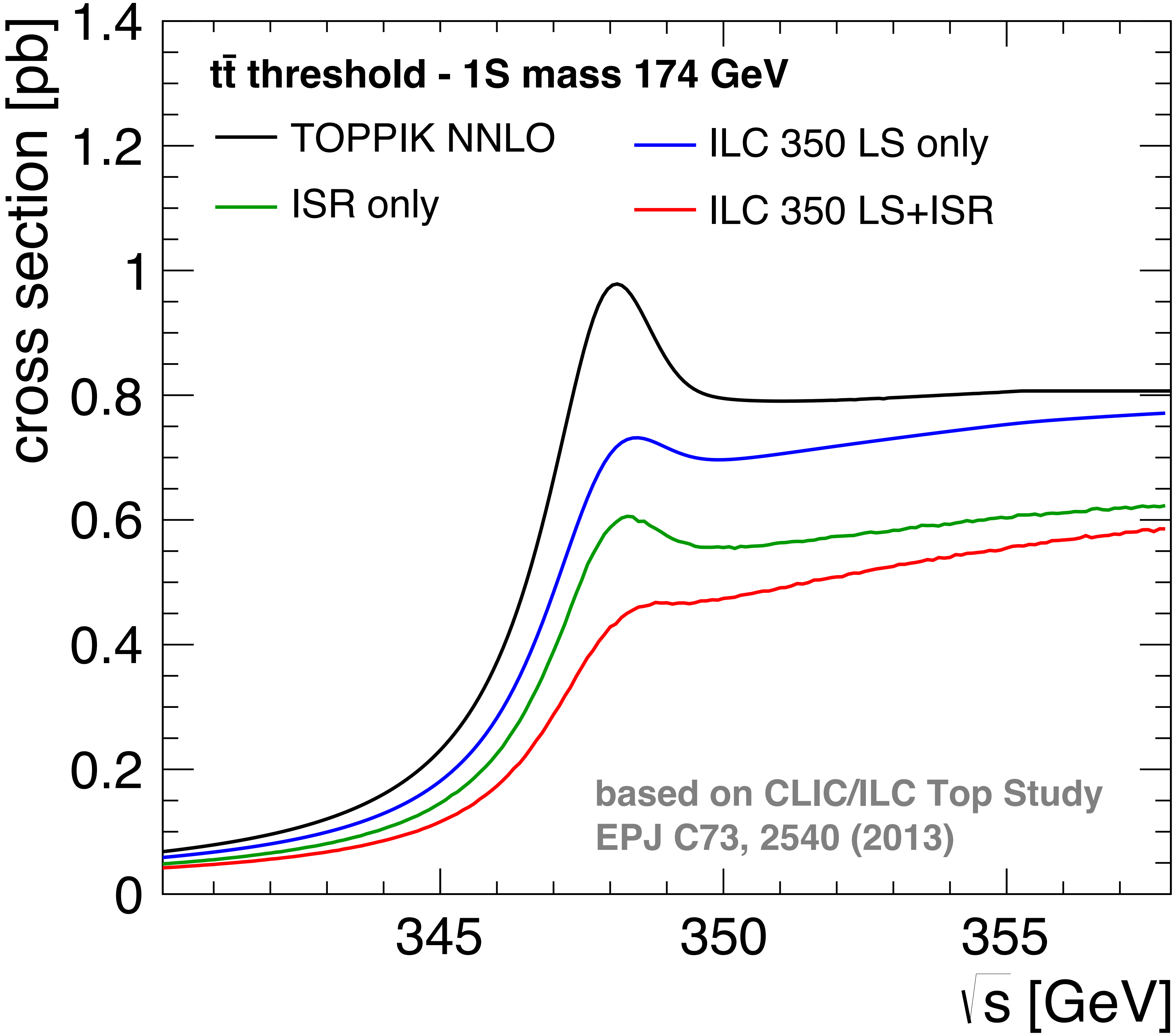


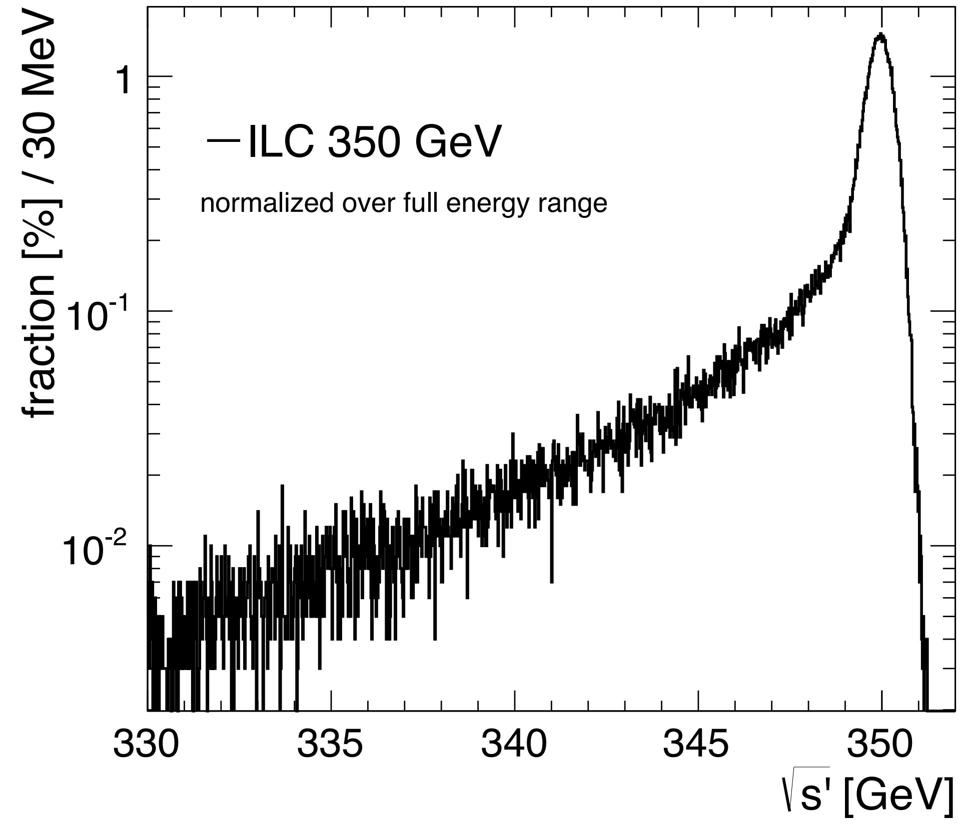
Here: Extract mass and α_s

- Effects of some parameters are correlated; dependence on Yukawa coupling rather weak - precise external α_s helps

From Theory to Experiment: Collider Effects

- The luminosity spectrum of the collider and ISR affect the shape of the threshold





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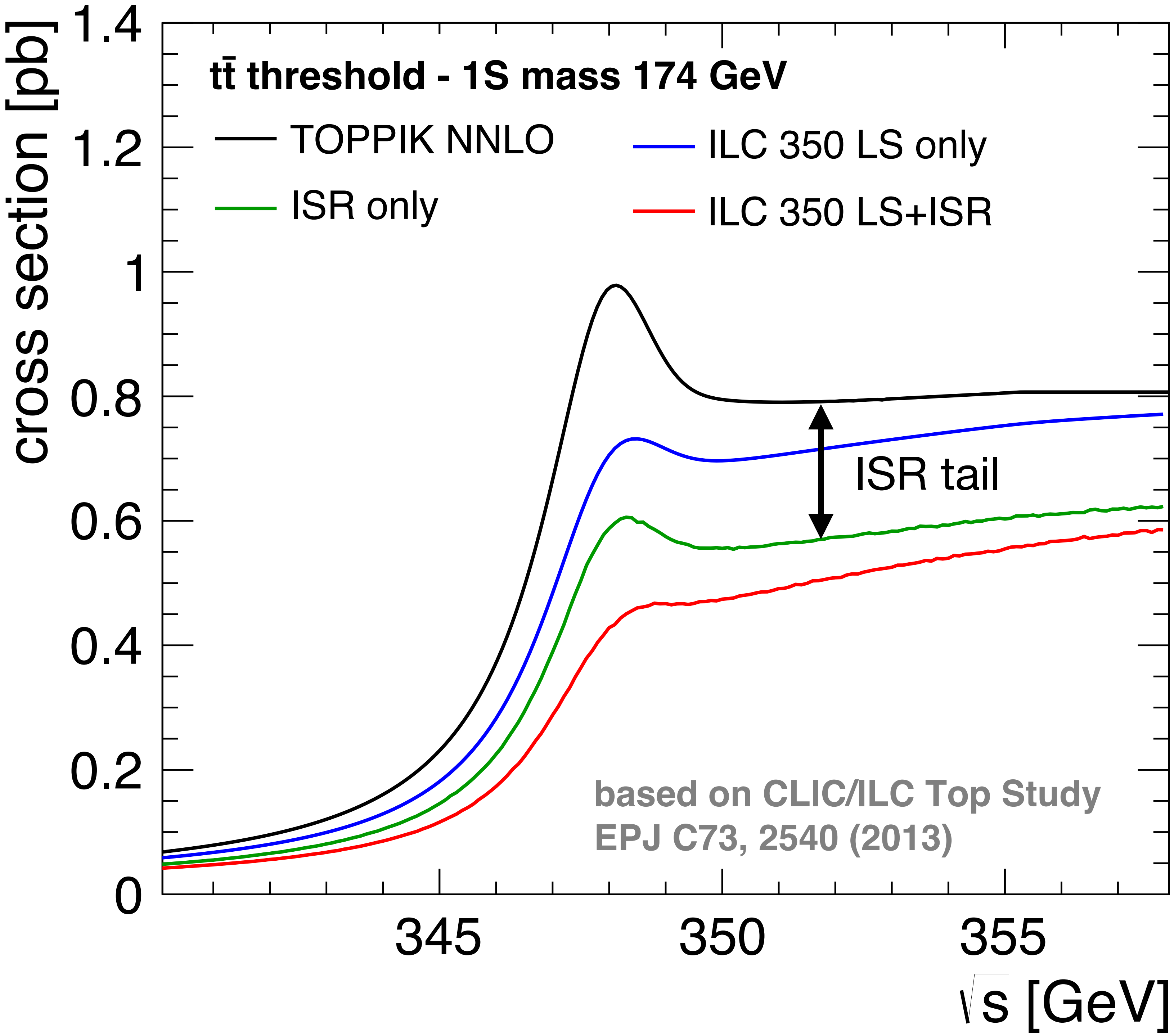

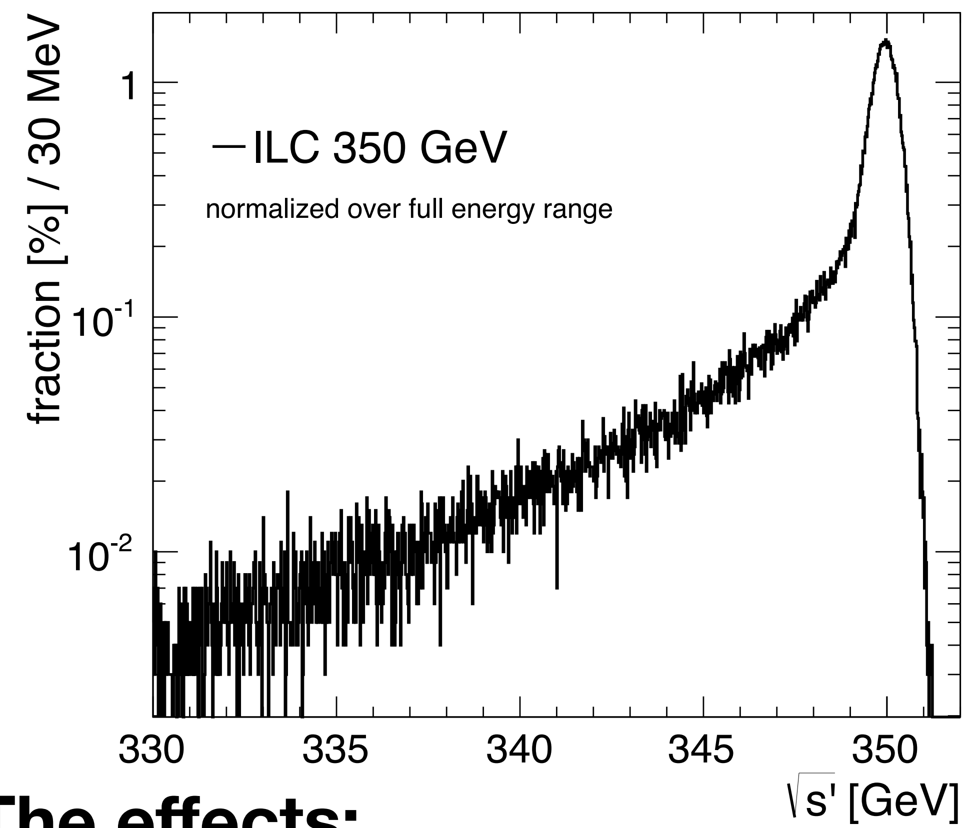

The effects:

- ISR tail: lowering of effective L at top energy

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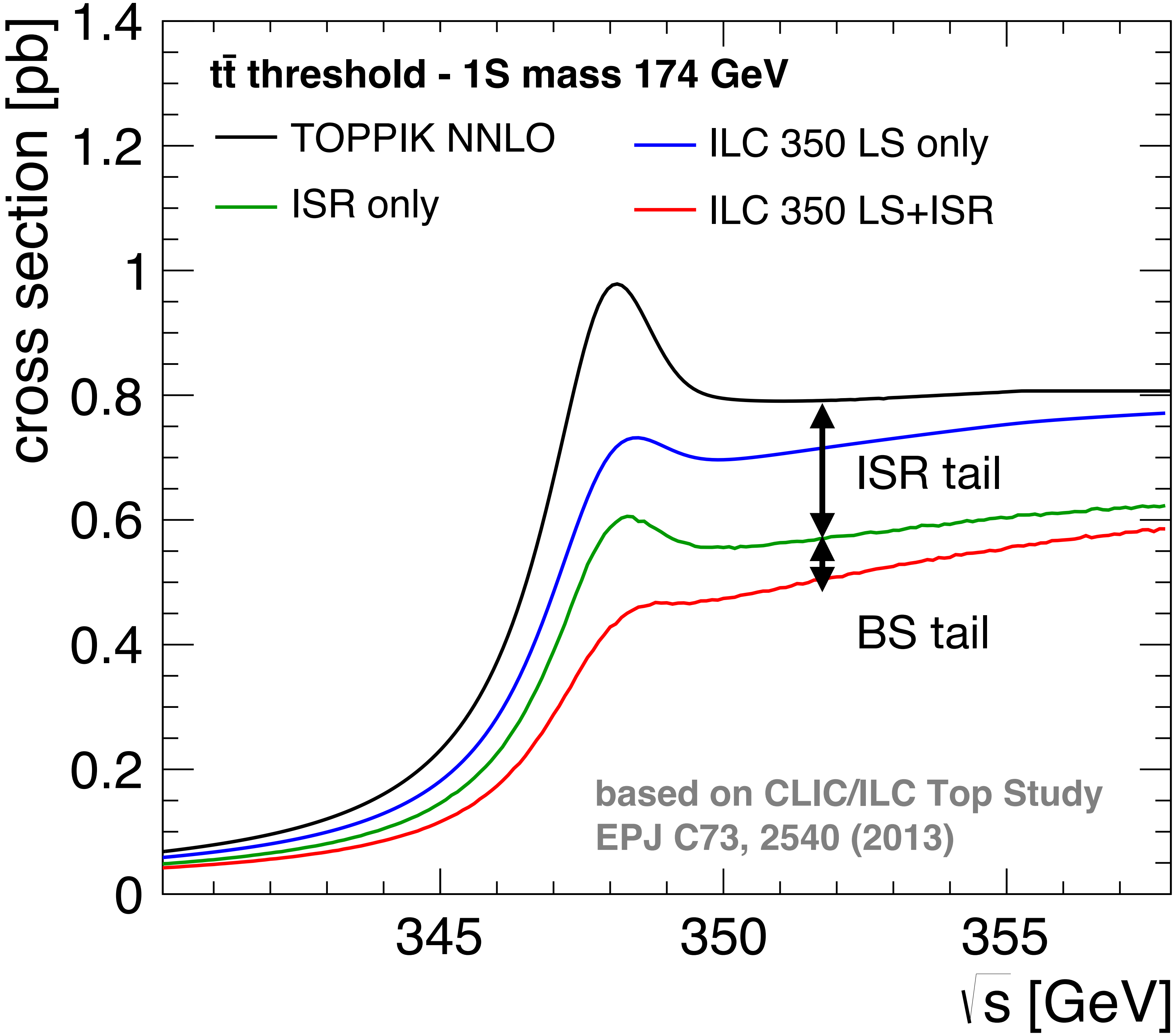

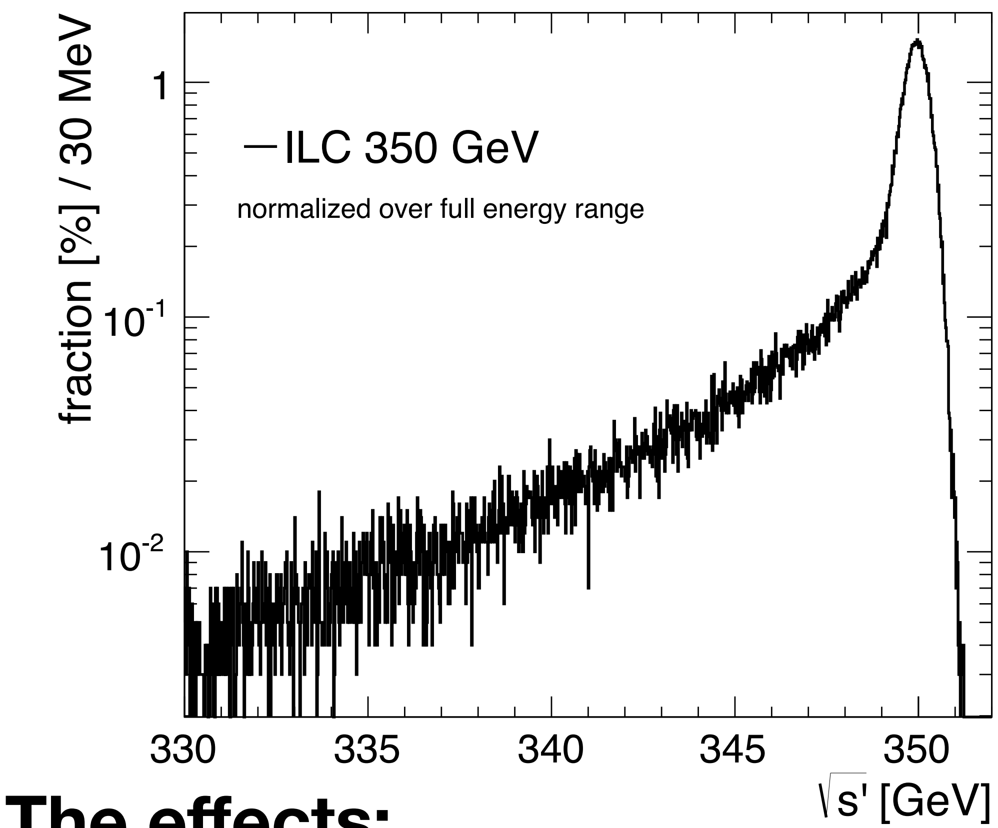

The effects:

- ISR tail: lowering of effective L at top energy
- BS tail: lowering of effective L at top energy

From Theory to Experiment: Collider Effects

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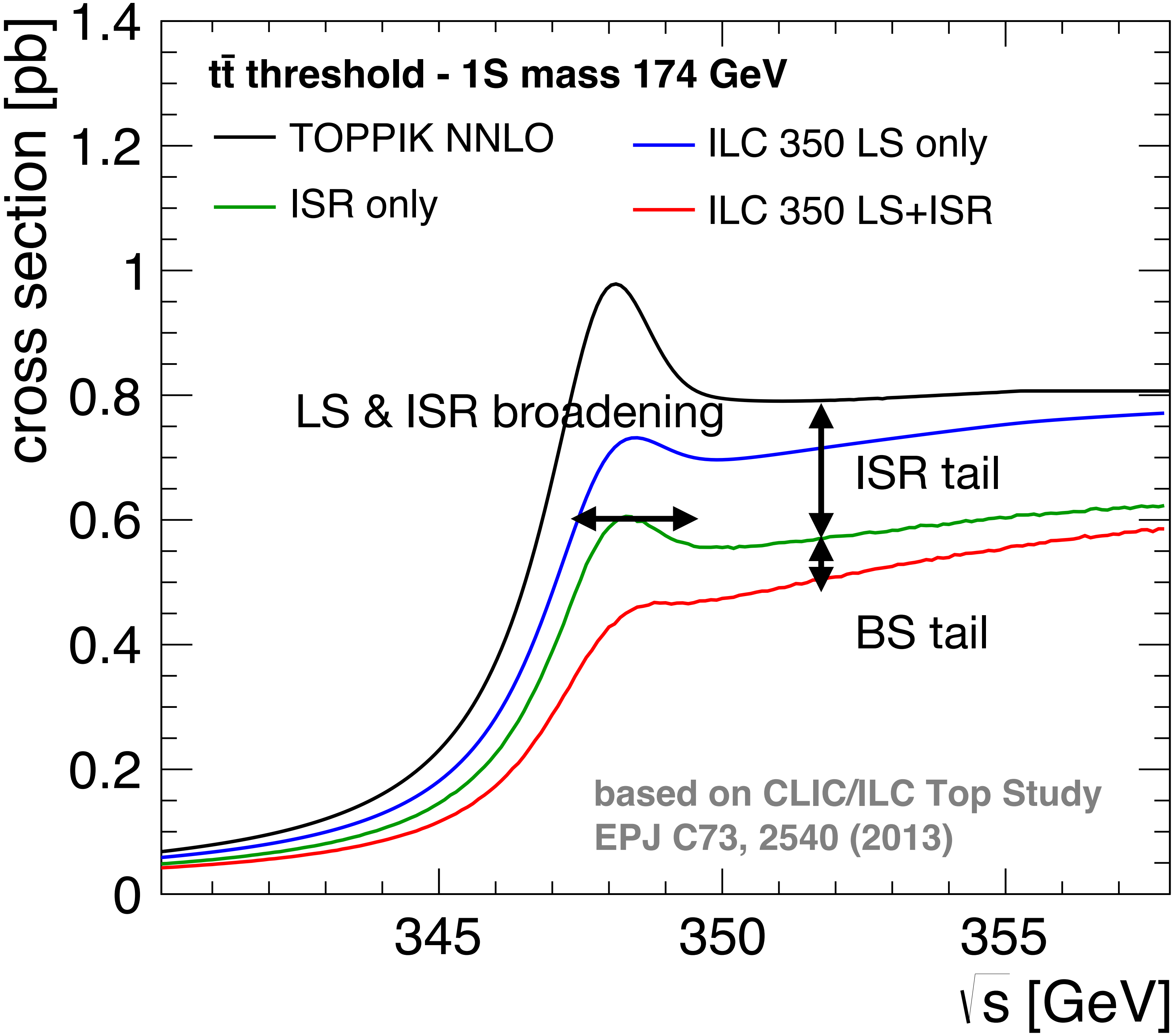
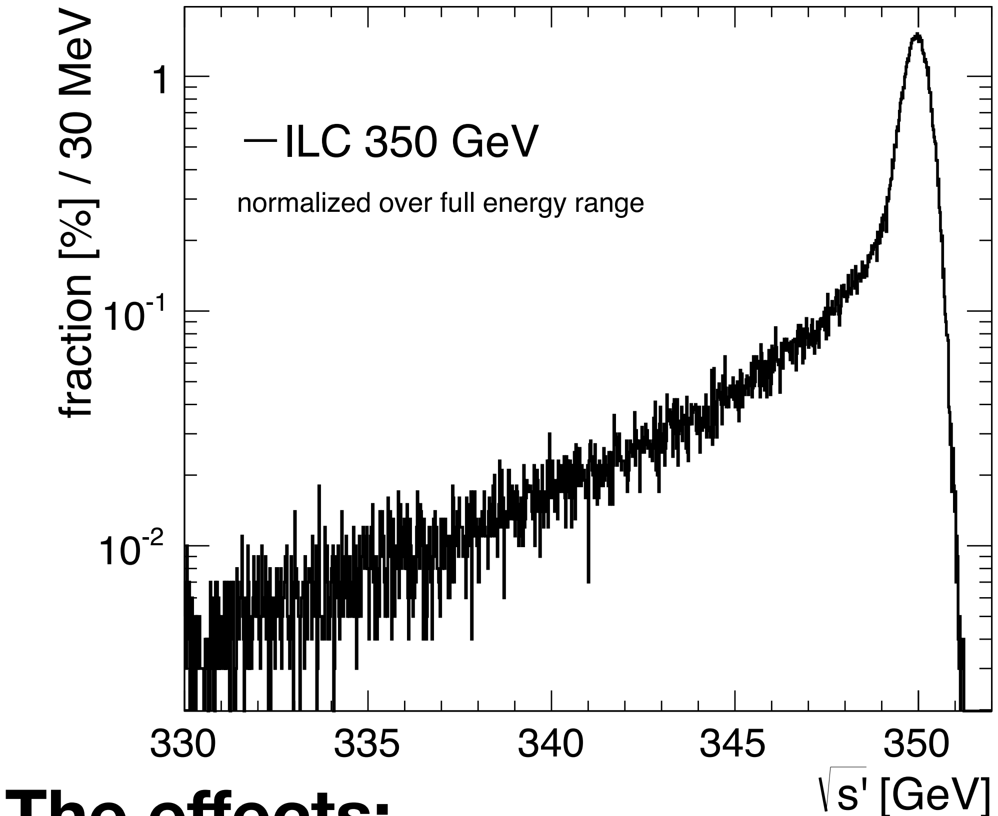
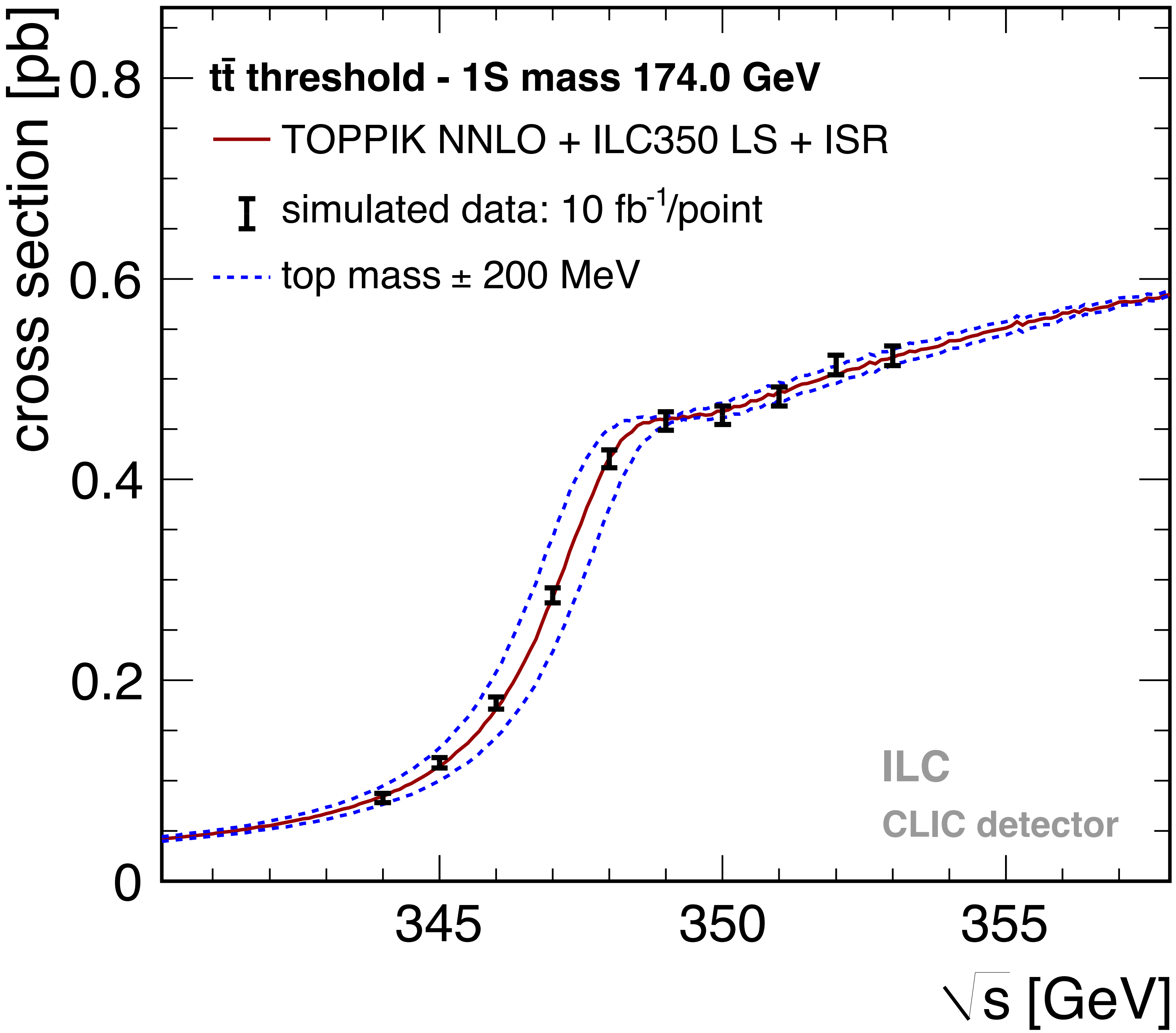




The effects:

- ISR tail: lowering of effective L at top energy
- BS tail: lowering of effective L at top energy
- LS & ISR broadening: smearing of Xsection due to beam energy spread, BS tail and ISR

A Threshold Scan at ILC

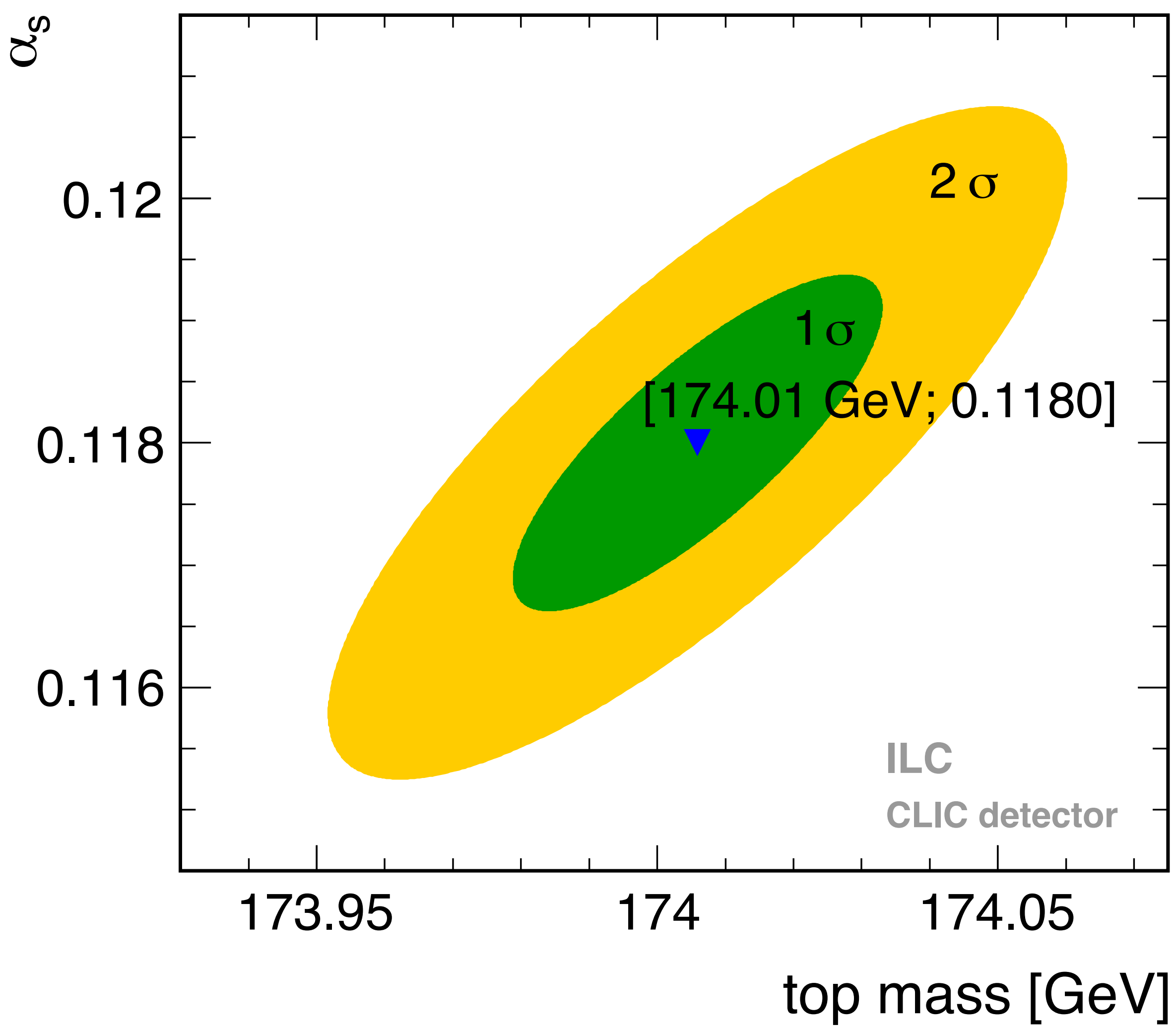


- Assume 10 points, 100 fb^{-1} total: 1 year running at full luminosity
- Top mass (and α_s for 2D fit) extracted with a template fit of the threshold shape

NB: Assuming unpolarized beams - LC beams can be polarized, increasing cross-sections / reducing backgrounds

EPJ C73, 2540 (2013)

Statistical Precision from Threshold Scan



- Additional possibilities:
  - With high precision external α_s the Top Yukawa coupling can be measured with ~ 7% (stat) precision
  - The top width can also be included in the fit - uncertainties (stat) ~ 30 MeV

arXiv:1310.0563

Fit Results

[MeV]	Δm	theory 1%/3%	α_s
ILC - 1D Fit	21	18/55	21

[MeV]	Δm	theory 1%/3%	Δα	theory 1%/3%
ILC - 2D Fit	27	5/9	0.0008	0.0009/0.0022

EPJ C73, 2540 (2013)

Systematics on Mass

- Incomplete - but looked at several key aspects:
  - Theory uncertainties currently based on simple scaling of cross section (1%, 3%) (10 MeV up to ~50 MeV, depending on fit strategy -> uncertainty mostly absorbed in α_s uncertainty for combined fits) - More sophisticated studies planned, based on results by Beneke *et al.*, see next talk
  - Non-ttbar background: 5% uncertainty results in 18 MeV uncertainty on mass (After selection, the non-ttbar background cross section is ~ 70 fb, so 5% uncertainty can be reached with ~ 6 fb^{-1} below threshold)
  - Beam energy: Expect 10^{-4} precision on CMS energy: ~30 MeV uncertainty on mass - potential for further improvement?
  - Luminosity spectrum - first study based on CLIC 3 TeV model (substantially more complicated than ILC): ~ 6 MeV uncertainty from fit of LS parameters

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“Interpretation” uncertainty:
Theory uncertainties are incurred when transforming the 1S mass used to describe the threshold to the MSbar mass - currently *O* ~ 100 MeV, depending on α_s precision and number of orders - significant reduction possible when needed

Systematics: High-level Summary

- Measurements at the top threshold are will likely be systematics limited

Mass:

- *Statistical* uncertainty for 100 fb^{-1} (reasonably modest program)
  ~ 25 MeV (stat)
- *Experimental* Systematics
  - Beam Energy: **~ 30 MeV**
  - Non-ttbar background, selection efficiencies: **~ 10 MeV**
  - Luminosity Spectrum: **~ 6 MeV**
- *Theory* Systematics
  - Expected to be significant, naive estimates provide numbers of up to *O* 100 MeV - Requires a dedicated study!

More after this…

http://lcws14.vinca.rs

LCWS2014 - Belgrade, October 6 - 10, 2014 - Top, QCD & Loopverein session

Interested to present your work? Let me know!

Summary

- Linear colliders will be capable of producing top quarks in a very clean environment: Excellent conditions for precision mass measurements
- The invariant mass can be reconstructed with an experimental precision of *O* 100 MeV (stat+ syst), but suffers from substantial theoretical uncertainties
- A threshold scan provides the ultimate mass precision in a theoretically well-understood setting
  - Statistical uncertainties on the 25 MeV level, with comparable experimental systematics
  - Theoretical uncertainties still need investigation to provide a reliable estimate - first studies coming soon

Summary

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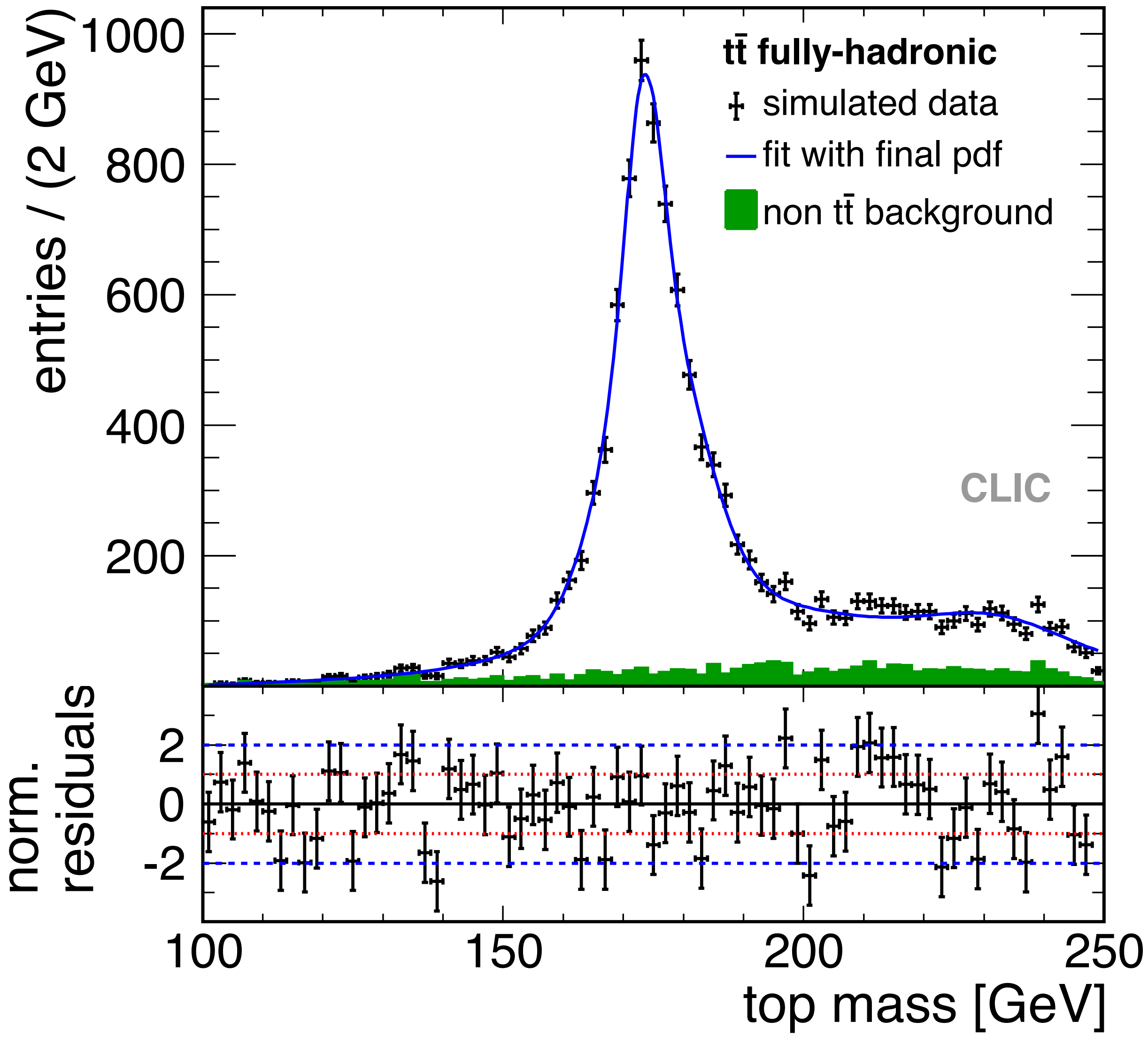
Overall: Linear Colliders provide the potential for 100 MeV total uncertainty on the top quark mass

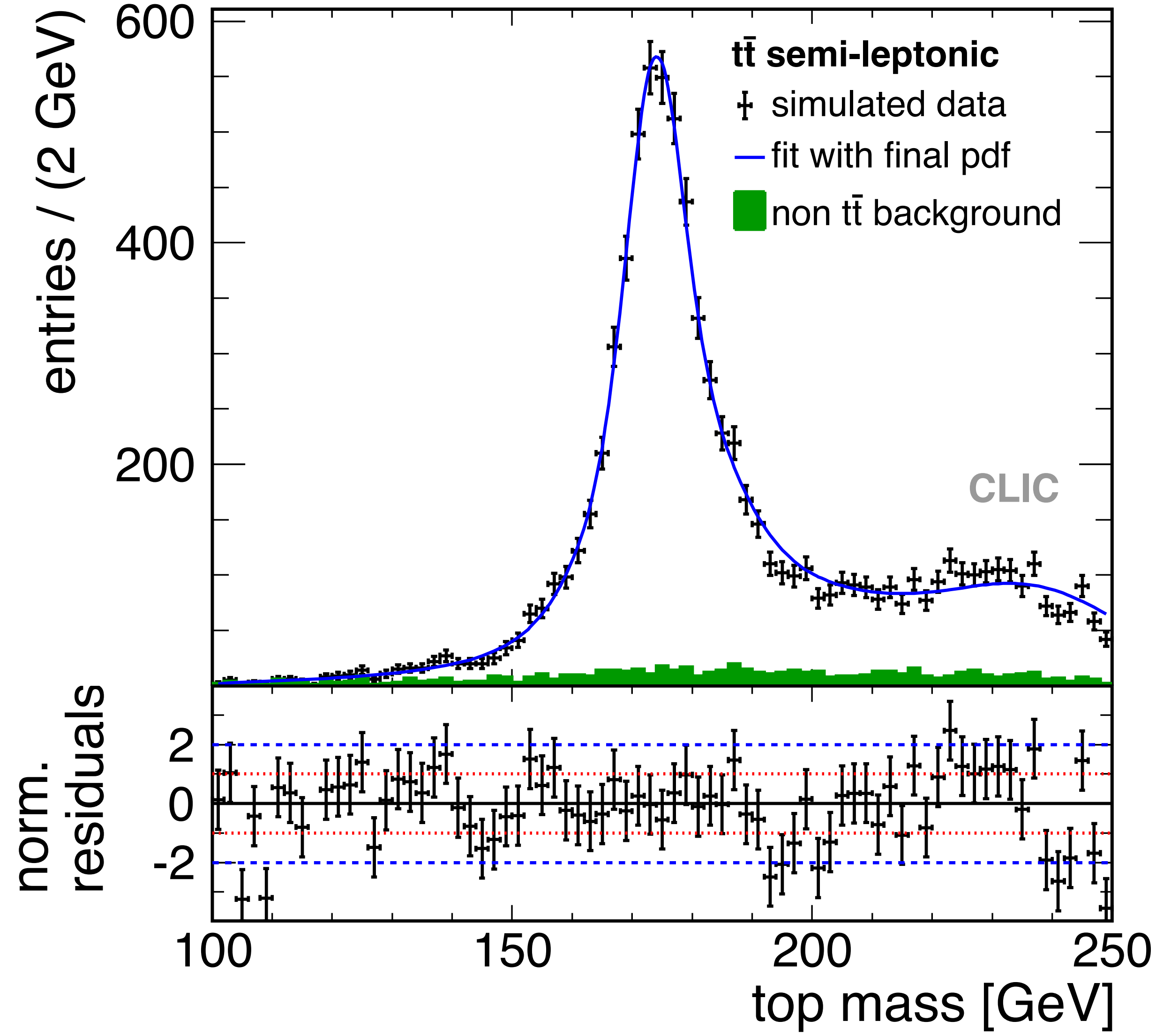
Backup

Analysis Strategy

- Identify the type of top decay according to number of isolated leptons
  - all-hadronic (0 leptons), semi-leptonic (1 lepton), leptonic (>1 lepton) -> rejected
- Jet clustering (exclusive k_t algorithm) according to classification: 6 or 4 jets
- Flavor-tagging: Identify the two most likely b-jet candidates
- W pairing: Jets / leptons into W bosons
  - Unique in the semi-leptonic case: 1 W from two light jets, 1 W from lepton & missing Energy
  - 3 possibilities (4 light jets) in all-hadronic case - Pick combination with minimal deviation from nominal W mass
- Kinematic fit - Use Energy/momentum conservation to constrain event
  - Performs the matching of W bosons an b-Jets to t candidates
  - Enforces equal t and anti-t mass: Only one mass measurement per event
  - Provides already good rejection on non-tt background
- Additional background rejection with likelihood method based on event variables (sphericity, b-tags, multiplicity, W masses, d_{cut}, top mass w/o kin fit)

Mass Reconstruction Above Threshold





- Width less constrained than mass: substantial detector effects (peak width ~ 5 GeV compared to 1.4 GeV top width)

channel	m_{top}	Δm_{top}	Γ_{top}	$\Delta\Gamma_{\text{top}}$
fully-hadronic	174.049	0.099	1.47	0.27
semi-leptonic	174.293	0.137	1.70	0.40
combined	174.133	0.080	1.55	0.22

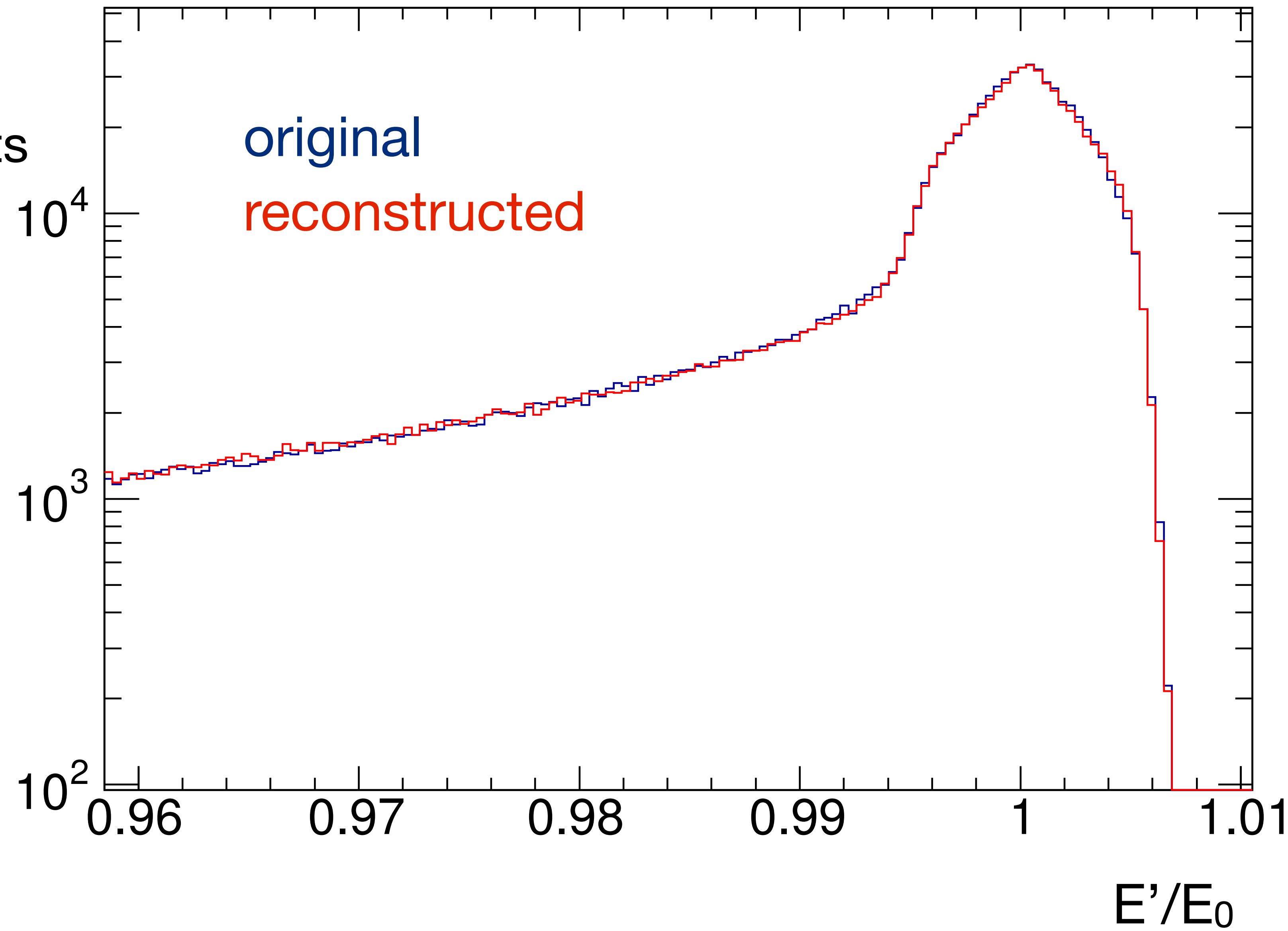
Systematics - Invariant Mass above Threshold

- Still incomplete, but some key issues were investigated:
  - Possible bias from top mass and width assumptions in detector resolution: Below statistical error, no indication for bias found
  - Jet Energy Scale: Reconstruction of W bosons can be used to fix this to better than 1% for light jets, assume similar precision for b jets from Z and ZZ events: Systematics below statistical uncertainties of the measurement
  - Color Reconnection: Not studied yet - depends on space-time overlap of final-state partons from t and anti-t decay - Expected to be less than in WW at LEP2: Comparable or smaller systematics on mass - less than 100 MeV

The key issue - and open question:
Above threshold the “PYTHIA mass” is measured - not well defined theoretically
➩ Substantial uncertainties in the interpretation of the measurements, far outweighs statistical uncertainties
➩ Some theory work in this direction already exists, but more is needed (also in in terms of connecting theory and experimental observables)

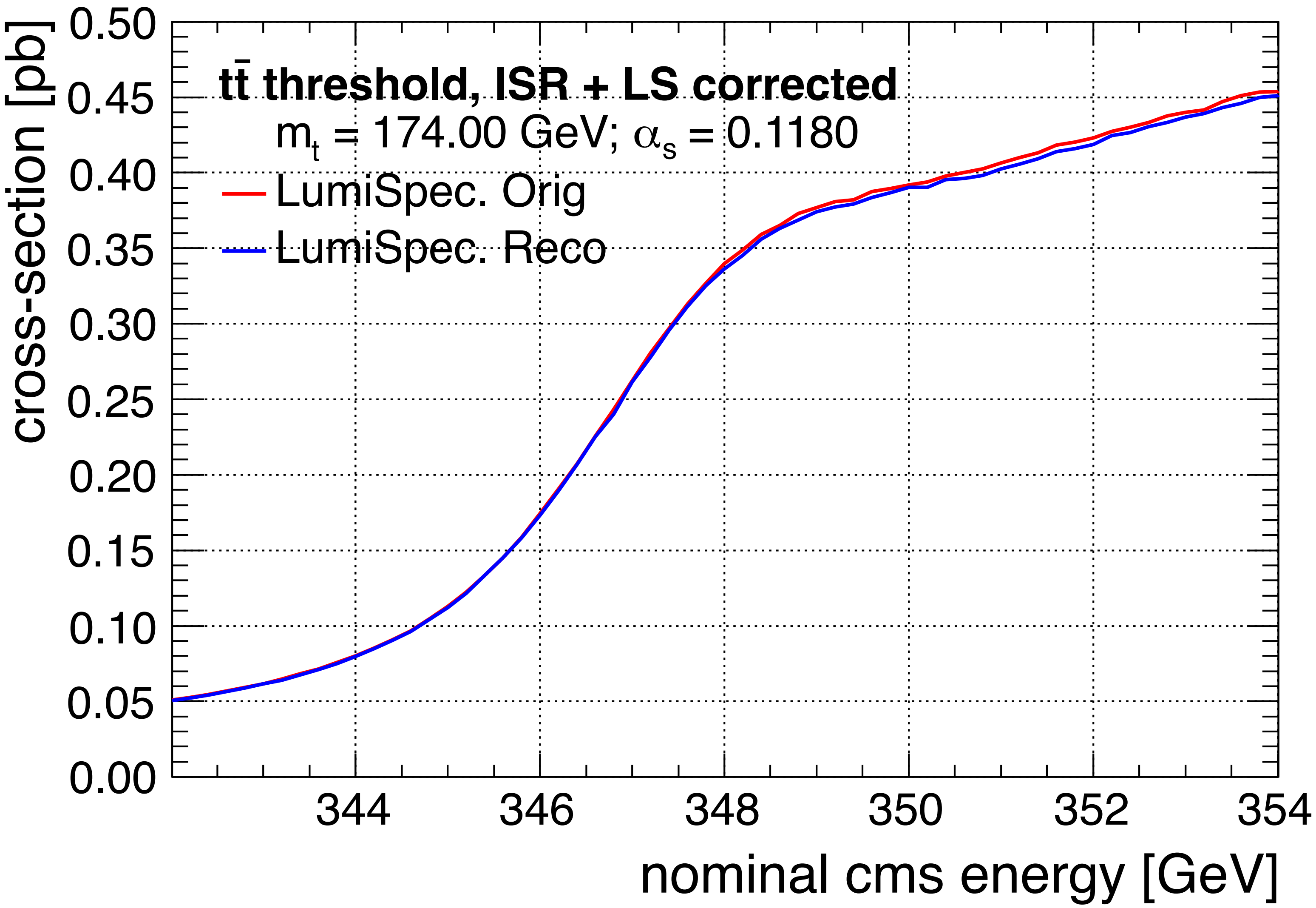
Systematics - Luminosity Spectrum

- Initial back-of-the envelope studies indicated possible systematics of 10s of MeV - mainly related to the shape of the main luminosity peak
- The challenge: Determining the shape (and normalization) of the luminosity spectrum from data
  - Accessible via energy and angle of $e^{\pm}$ from Bhabha events
  - Parametrized by a complex 19 parameter function, parameters determined from fits to Bhabha events (details: arXiv:1309.0372)



First CLIC study: application of 3 TeV model to 350 GeV - not yet full simulations, scaled uncertainties

Systematics - Luminosity Spectrum



- Impact of reconstructed luminosity spectrum on threshold behavior
  - Currently still a small bias: slightly reduced peak luminosity in model (0.7% too low)
  - Reason understood, straight-forward to correct

Global Results Summary - Luminosity Spectrum uncertainty for CLIC:

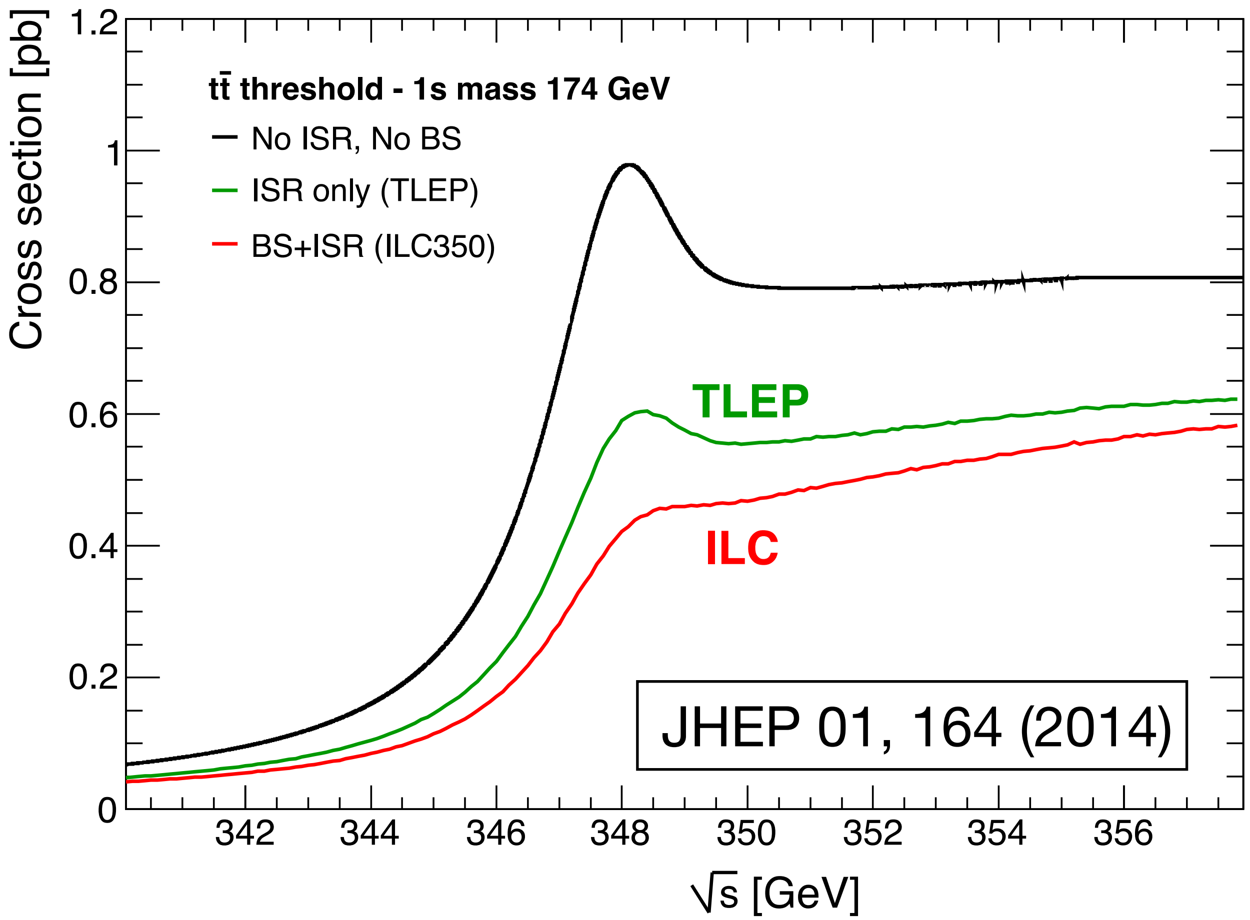
1D fit: Δm_t = (± 22 (stat) ± **5.3** (lumi parameters) - **22** (lumi reco)) MeV

2D fit: Δm_t = (± 34 (stat) ± **6.0** (lumi parameters) + **5.5** (lumi reco)) MeV

$\Delta \alpha_s$ = (± 9 (stat) ± **2.5** (lumi parameters) + **10** (lumi reco)) x 10^{-4}

Top Threshold at FCCee (TLEP)

- Naive Dream:



(this plot was made by taking it from the ILC analysis presented here, simply relabelling the "ISR only" curve)

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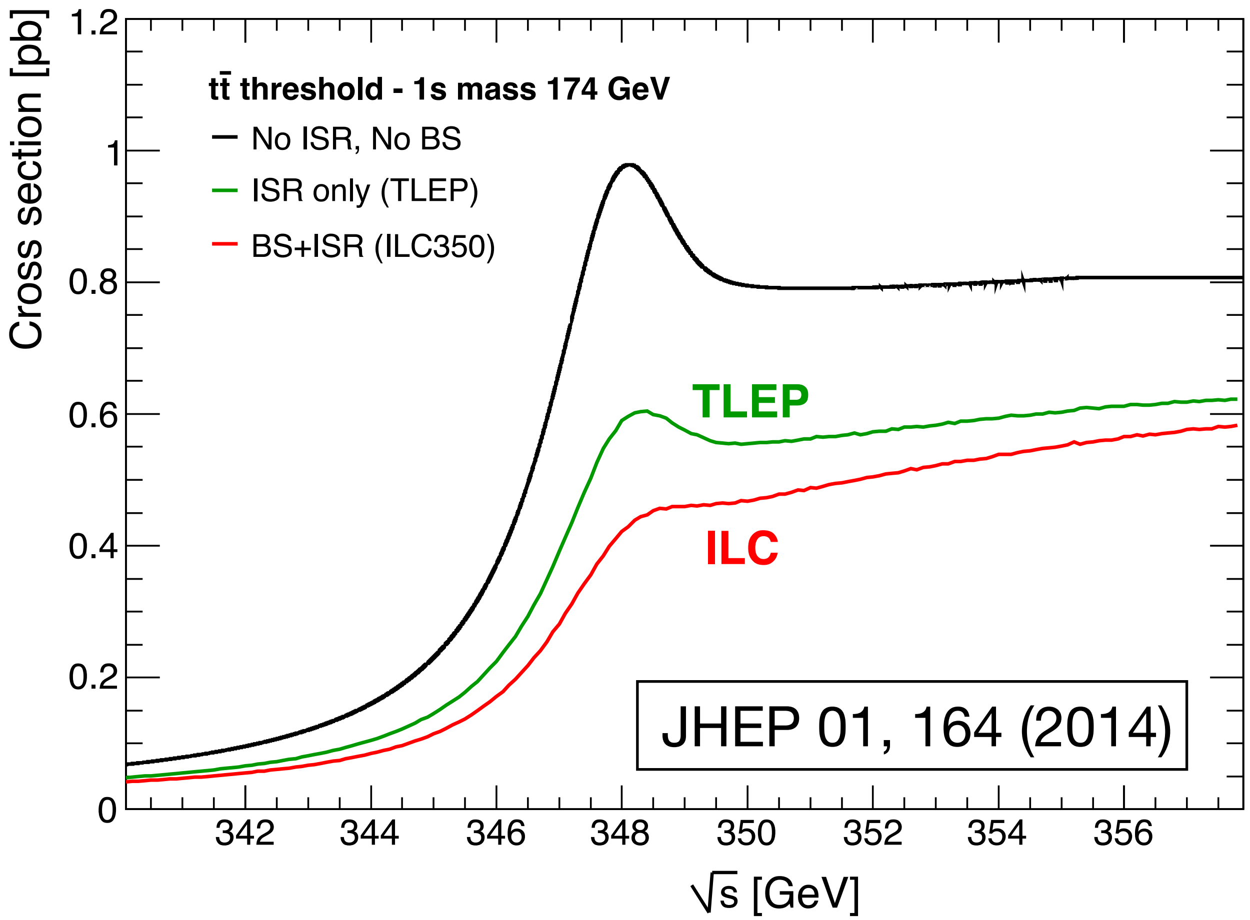

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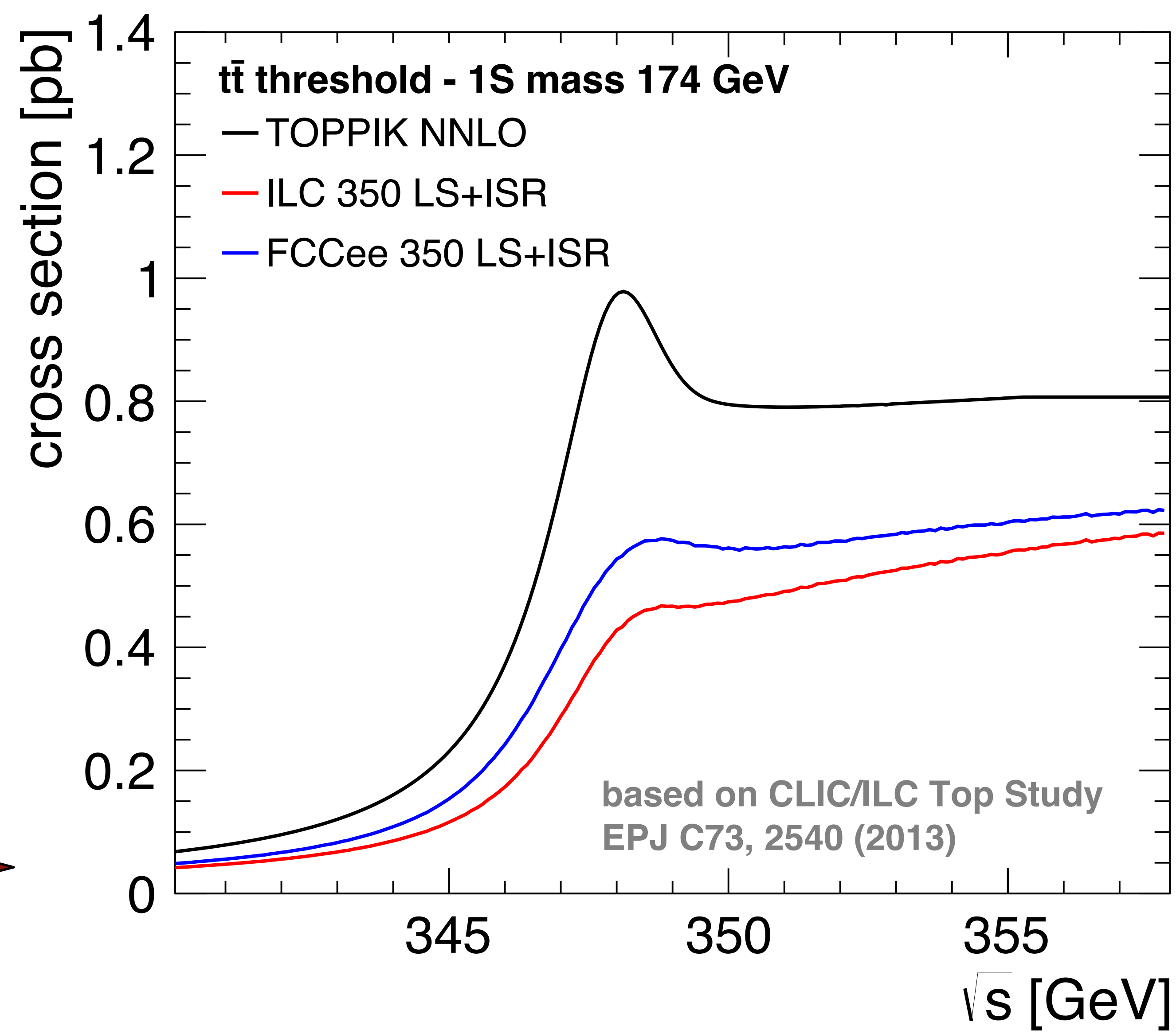
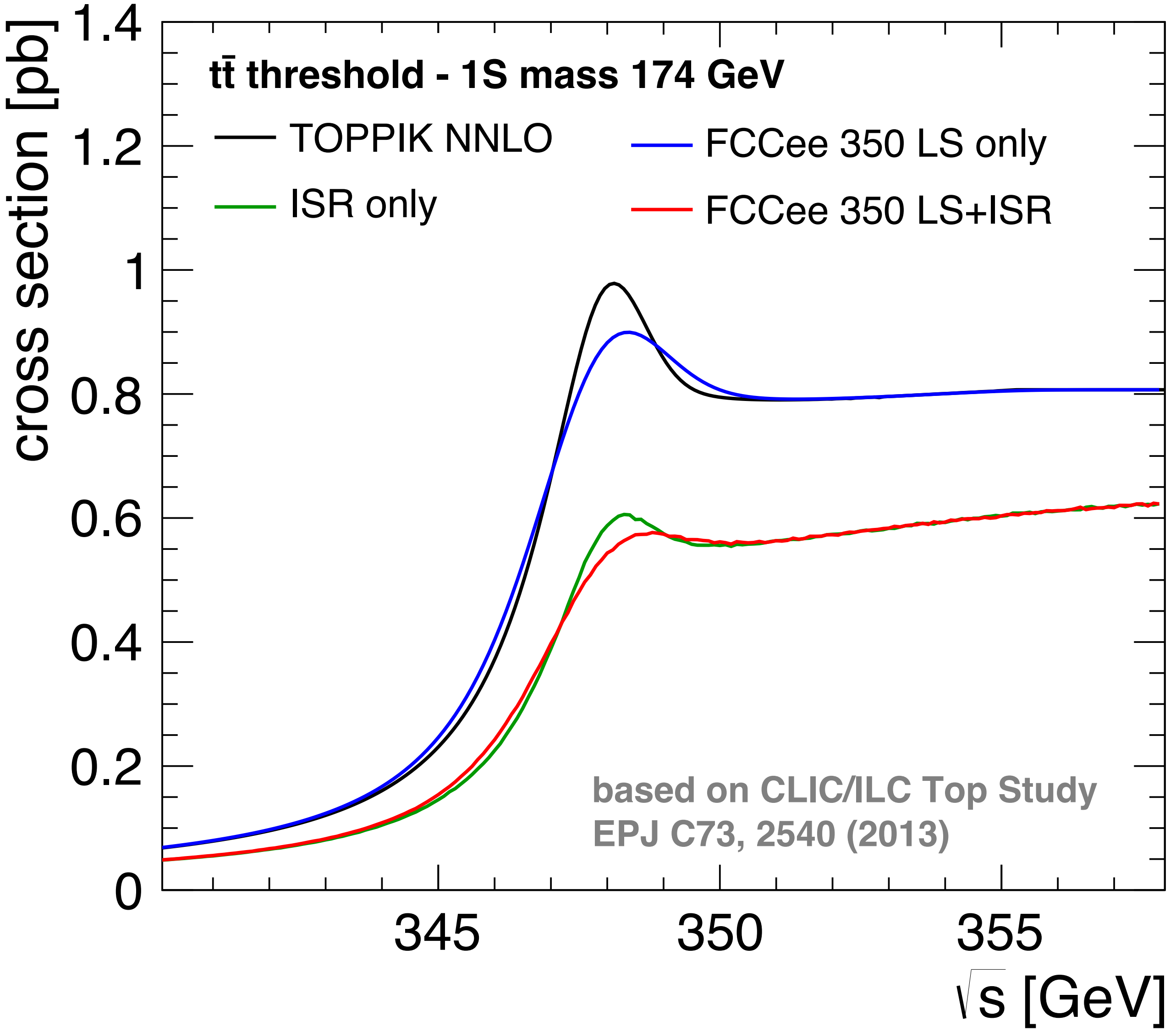
adding FCC Luminosity spectrum

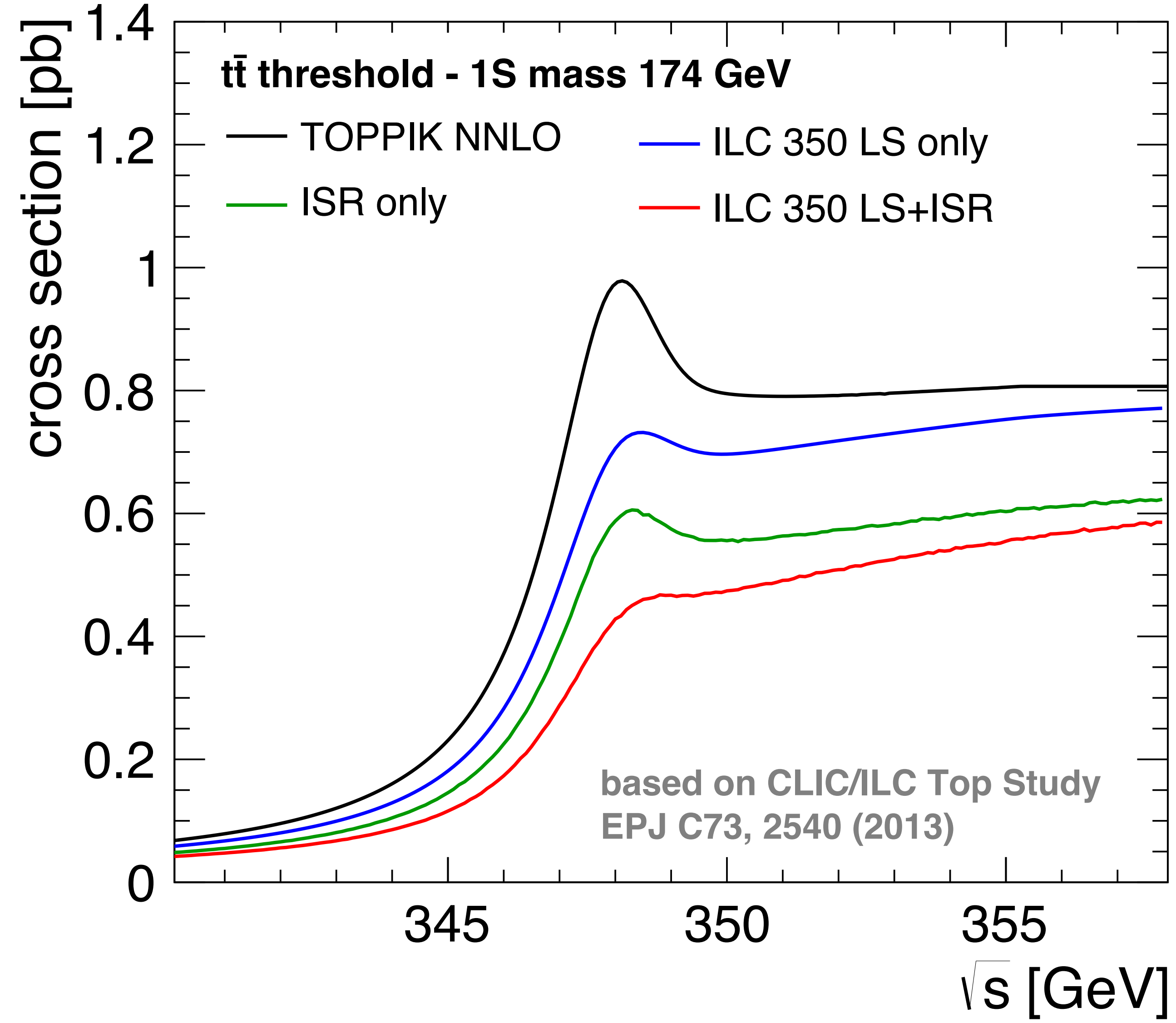
- More realistic luminosity spectrum for FCCee (assuming perfect gaussian with 0.19% spread)



Modifications to the XSection - FCCee vs ILC



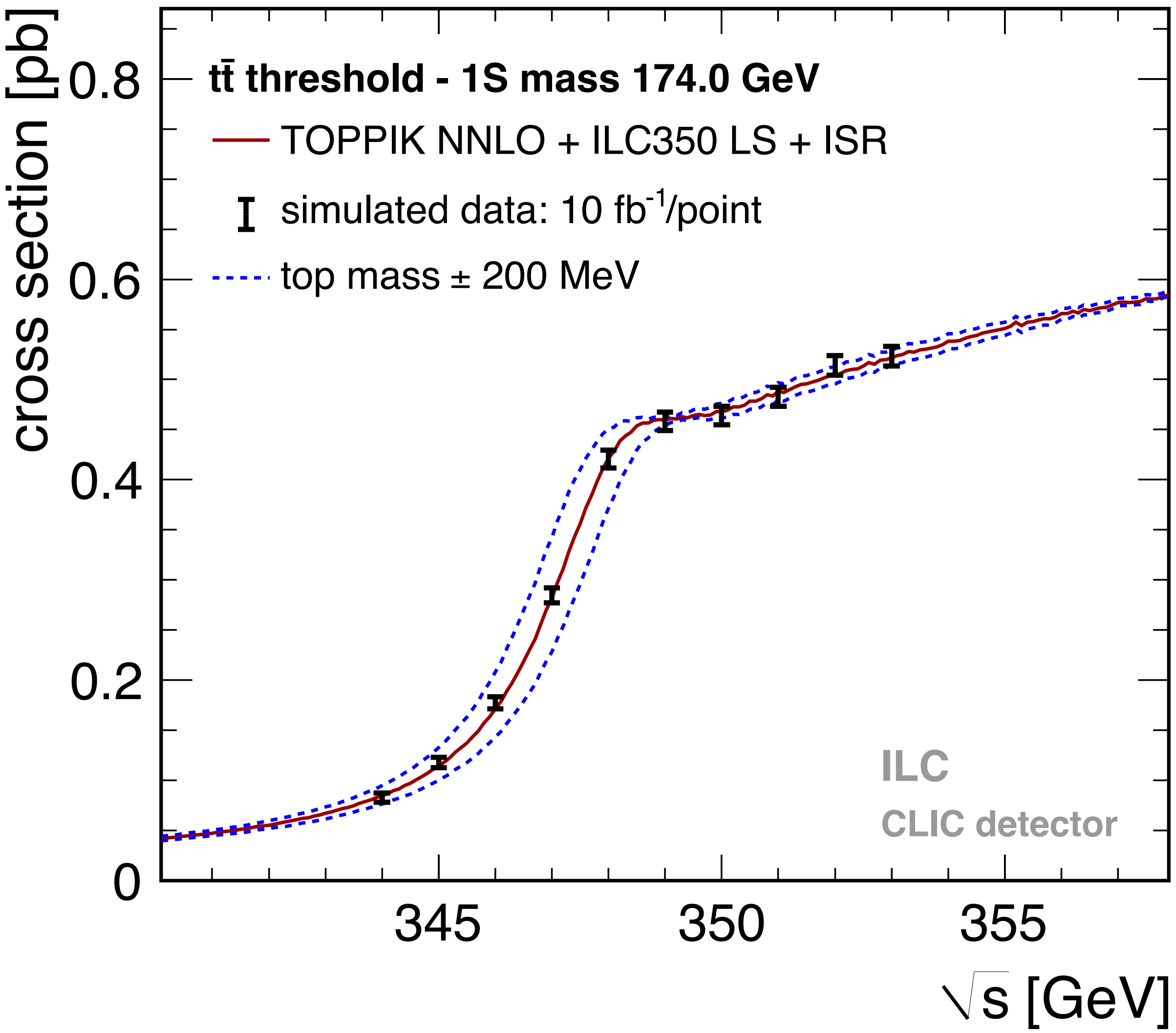
- The beam energy spread washes out the cross section peak at both ILC and FCCee

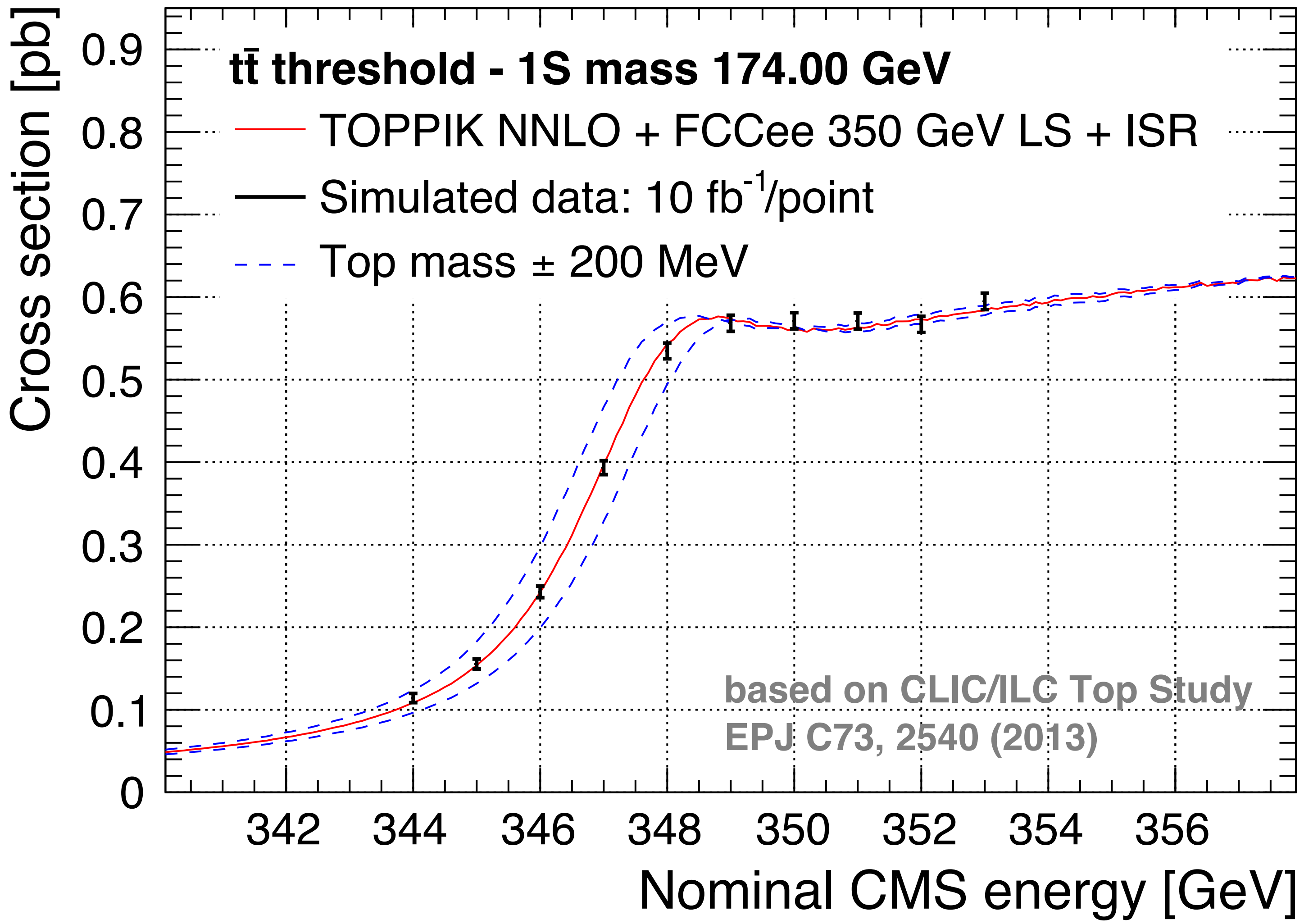


- In the peak region the top threshold at FCCee is by no means just the ISR-corrected cross-section!

Consequences on Precision

- Comparing ILC and FCCee - assuming identical detector performance





Simulated data points - same integrated luminosity

NB: Assuming unpolarized beams - LC beams can be polarized, increasing cross-sections / reducing backgrounds

Consequences on Precision

- Statistical uncertainties on
  - mass ~ 20% smaller at FCCee than at ILC
  - α_s ~ 13% smaller at FCCee than at ILC

NB: Assuming unpolarized beams - LC beams can be polarized, increasing cross-sections / reducing backgrounds

▸ To a large extent due to different effective luminosity (> 99%):
  - ILC: 54% (incl. ISR)
  - FCCee: 67% (incl ISR)

~ 25% less at ILC

Impact on systematics negligible or much smaller (some change of α_s sensitivity of 1D fit due to changed cross-section shape in particular above threshold)

With higher integrated luminosity (500 fb^{-1} vs 100 fb^{-1}) the statistical uncertainties scale as expected - systematics remain unchanged