

# Nuclear Parton Distribution Function (PDF)

*Nuclear Corrections & Uncertainties  
for LHC & Beyond*

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Conspirators:

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J. Owens, J. Morfin, C. Keppel, ...

Ringberg  
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# Heavy Target Data Essential for Determining Separate Parton Flavors

- Charged Current Neutrino data complement Neutral Current to extract PDF flavors
- Neutrino data requires heavy targets (Fe, Pb)
- Nuclear Corrections must be applied to heavy target data.

## *Tension between data sets*

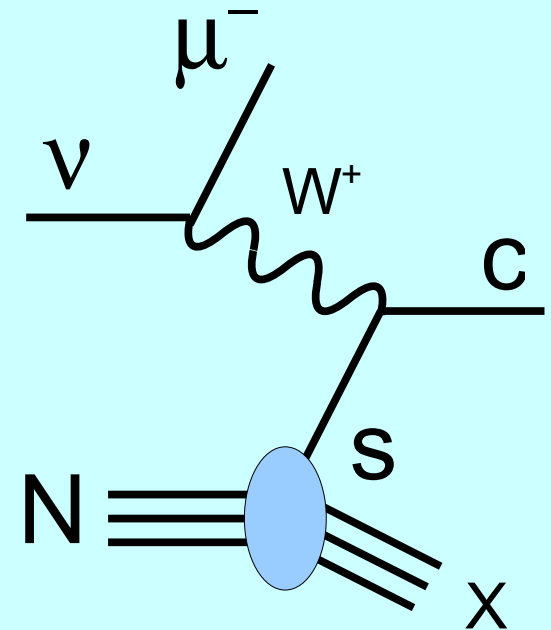
Charged Current (CC) &  
Neutral Current (NC) DIS

CC: Heavy Targets

NC: Light Targets

NuTeV Neutrino DIS  
& E866 Drell-Yan  
affects d/u ratio

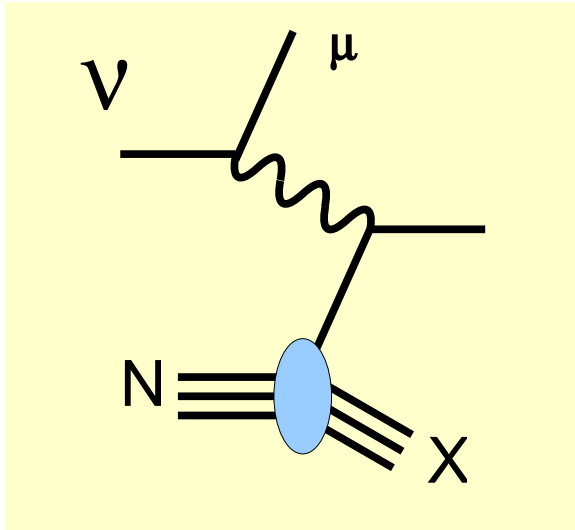
Neutrino Charm Production:  
can determine  $s(x)$



# NEW DATA SETS

# New & Updated Data Sets

## Deeply Inelastic Scattering



## NuTeV

Neutrinos on Iron

$\langle E_\nu \rangle = 120 \text{ GeV}$

860K nu

230K nubar

1170+966 points

## Chorus

Neutrinos on lead

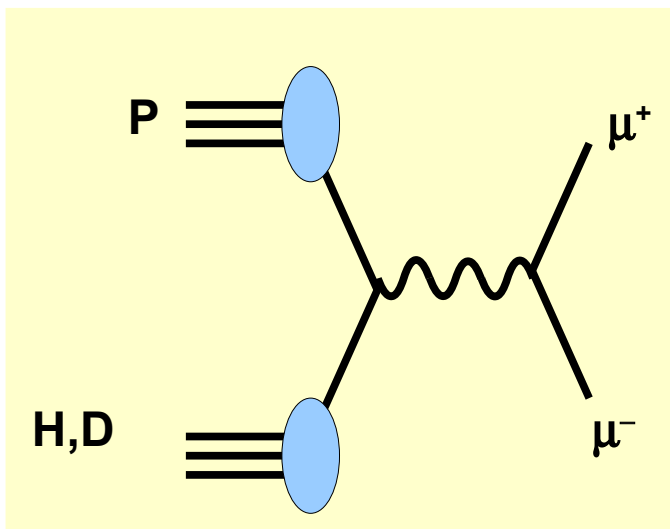
$0.01 < x < 0.7$

$10 < E_\nu < 200 \text{ GeV}$

$p_\mu > 5 \text{ GeV}$

412 points

## Drell-Yan



## E866 NuSea:

800 GeV proton beam  
on hydrogen & deuterium

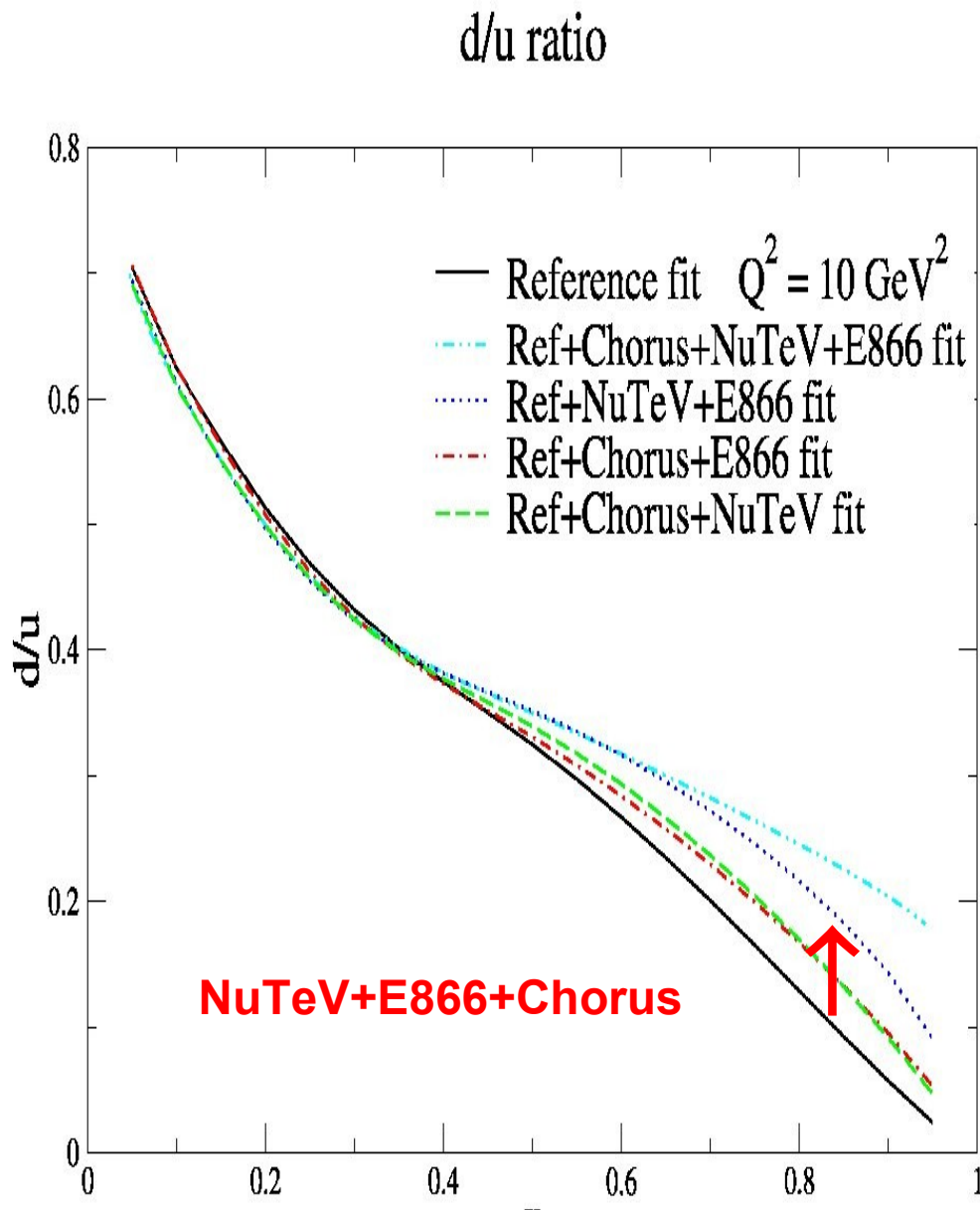
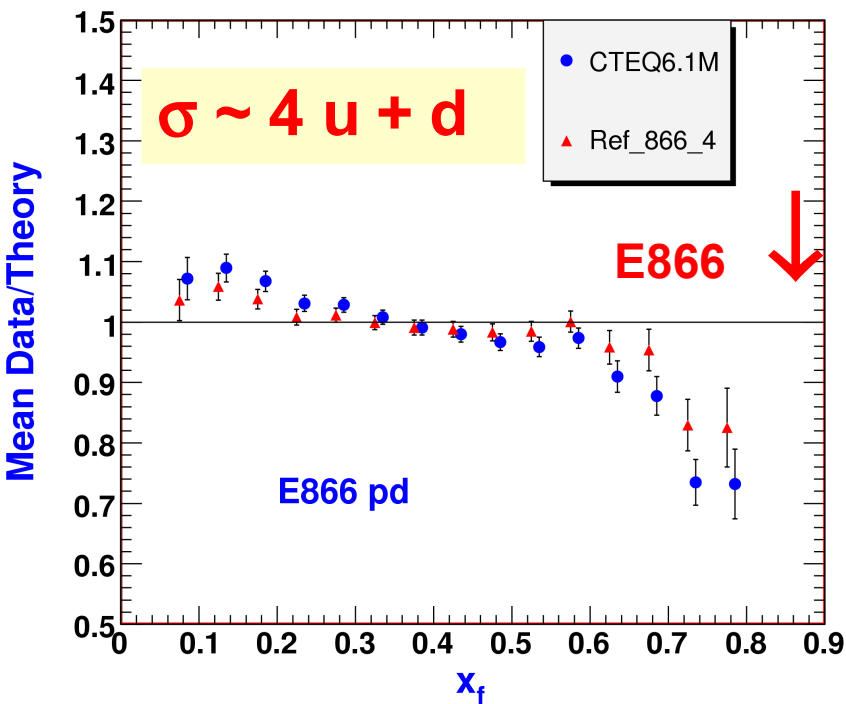
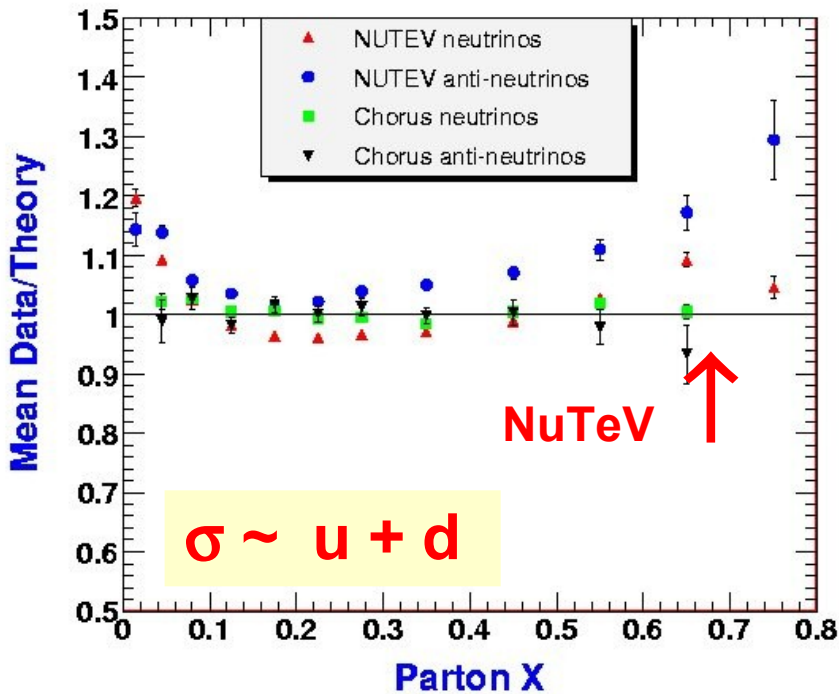
140K DY muon pairs

$M_{\mu\mu} > 4.5 \text{ GeV}$  (*Hi Mass*)

$0.020 < x < 0.345$

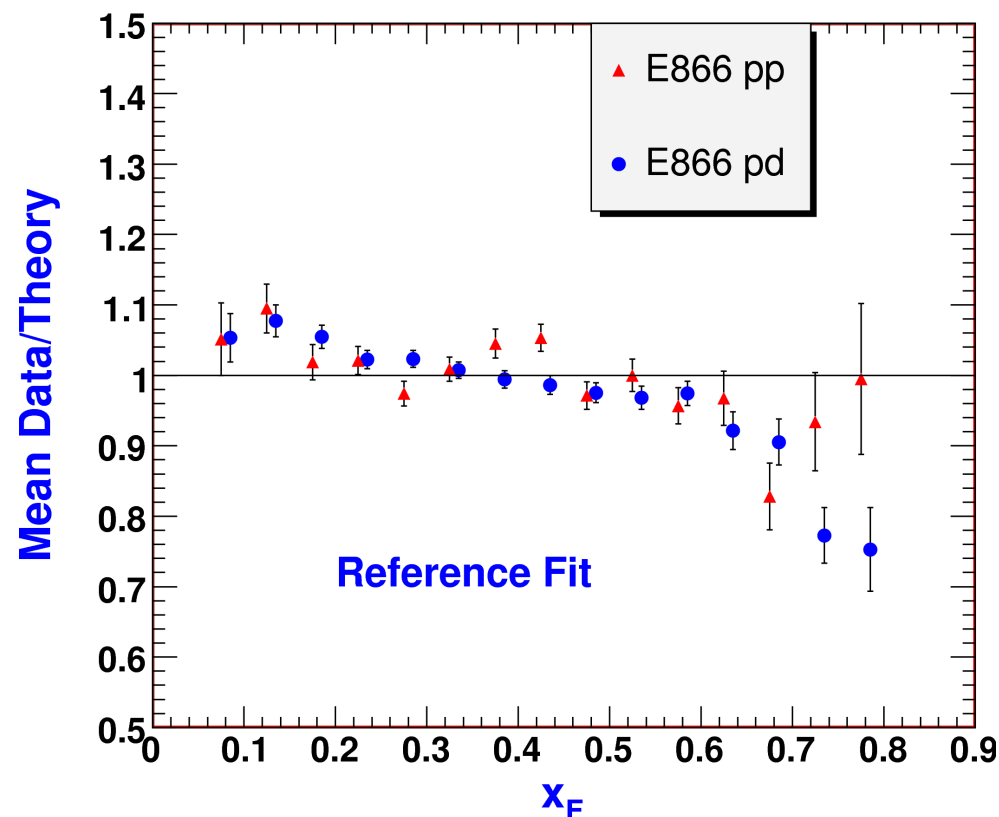
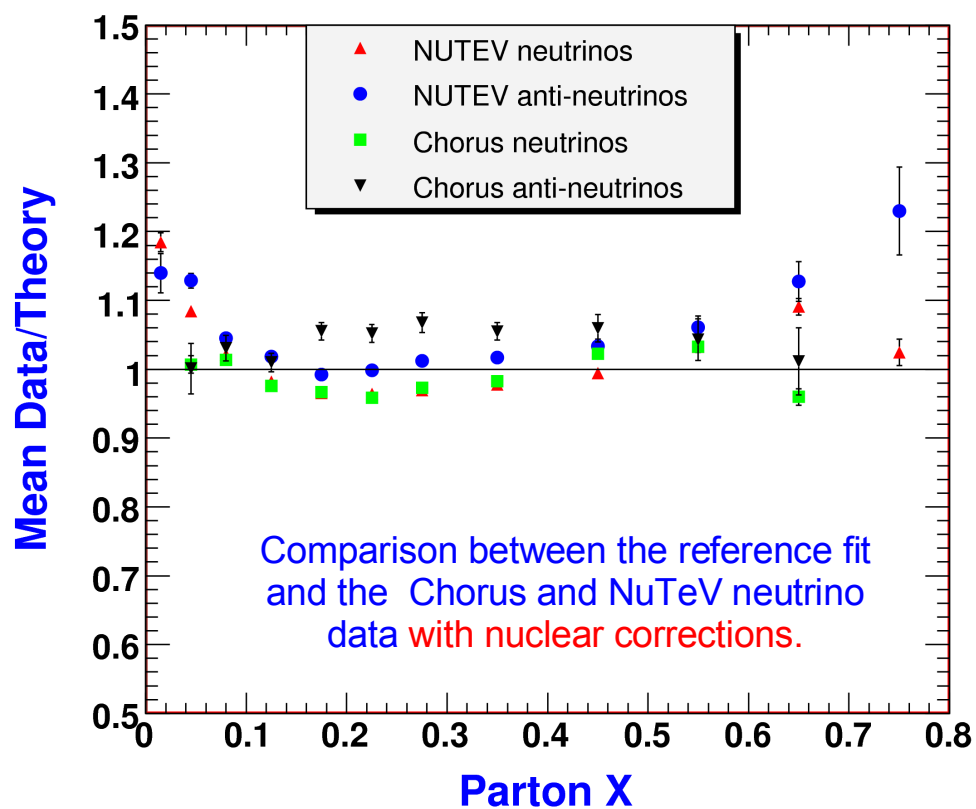
184+191 points

# How do new data affect the PDF's



J.F. Owens, J. Huston, C.E. Keppel, S. Kuhlmann,  
 J.G. Morfin, F. Olness, J. Pumplin, D. Stump,  
 Phys.Rev.D75:054030,2007.

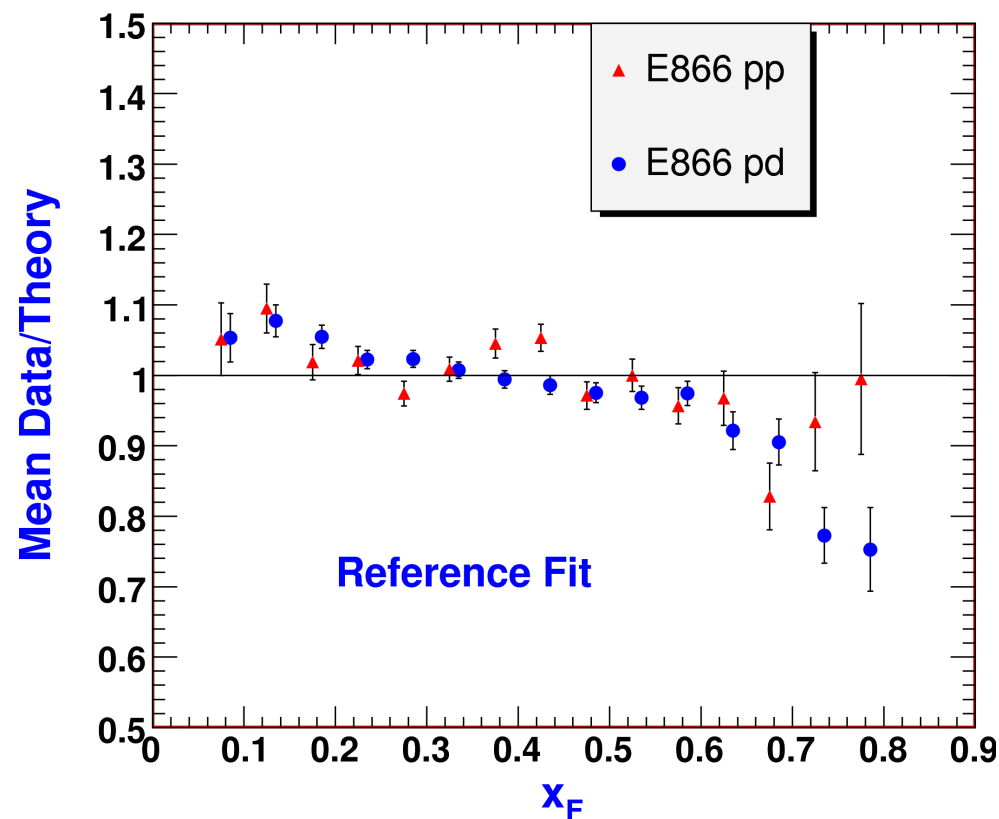
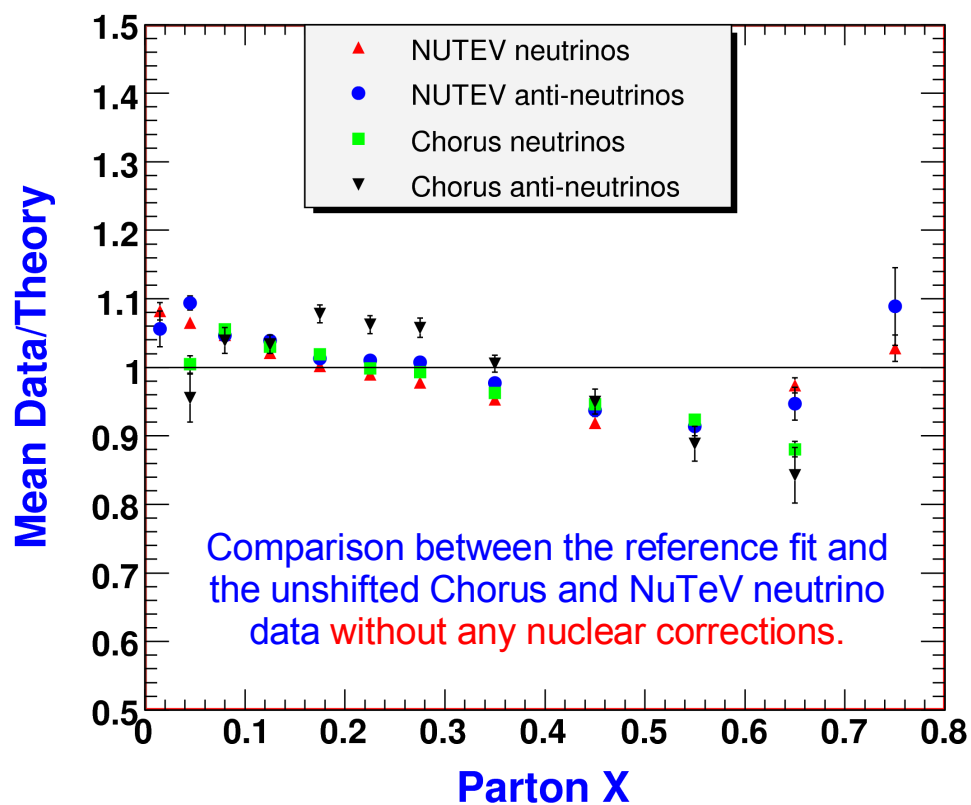
# Could nuclear corrections be different for CC (W) or NC ( $\gamma, Z$ ) processes???



“Thus, these results suggest on a purely phenomenological level that the nuclear corrections may well be very similar for the nu and nubar cross sections and that the overall magnitude of the corrections may well be smaller than in the model used in this analysis.”

$\chi=7453/5062$  Reference Fit  
 $\chi=6606/5062$  Mod Nuclear Fit

# Could nuclear corrections be different for CC (W) or NC ( $\gamma, Z$ ) processes???



“Thus, these results suggest on a purely phenomenological level that the nuclear corrections may well be very similar for the nu and nubar cross sections and that the overall magnitude of the corrections may well be smaller than in the model used in this analysis.”

$\chi=7453/5062$  Reference Fit  
 $\chi=6606/5062$  Mod Nuclear Fit

# TMC

## Target Mass Corrections



## A Review of Target Mass Corrections:

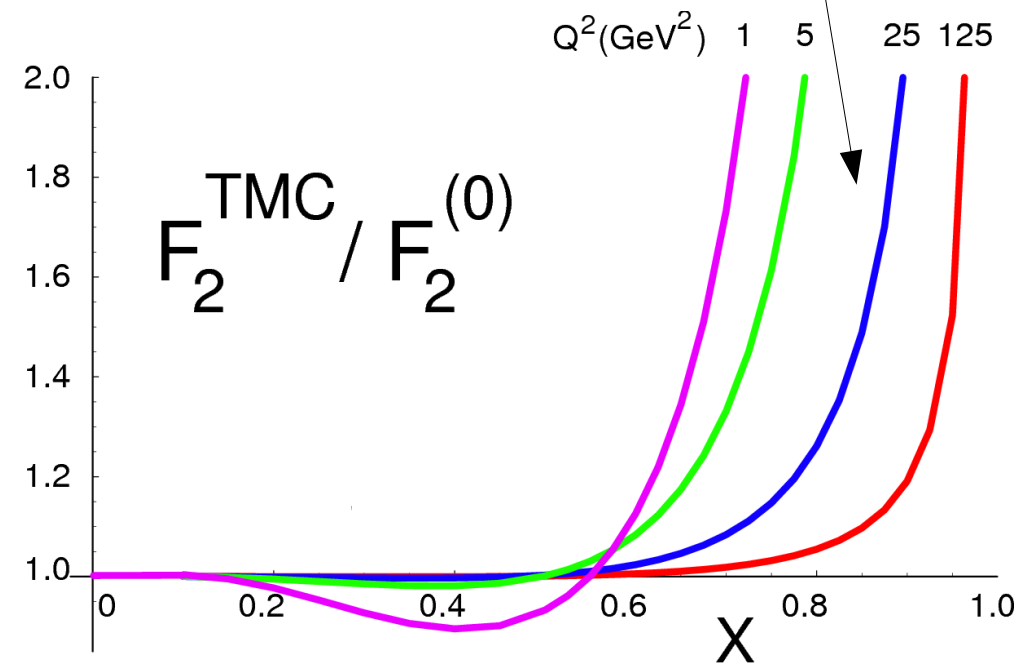
$$F_j^{\text{TMC}}(x, Q^2) = \sum_{i=1}^5 \boxed{A_j^i F_i^{(0)}(\eta, Q^2)} + B_j^i h_i(\eta, Q^2) + C_j g_2(\eta, Q^2)$$

leading term; from Parton Model

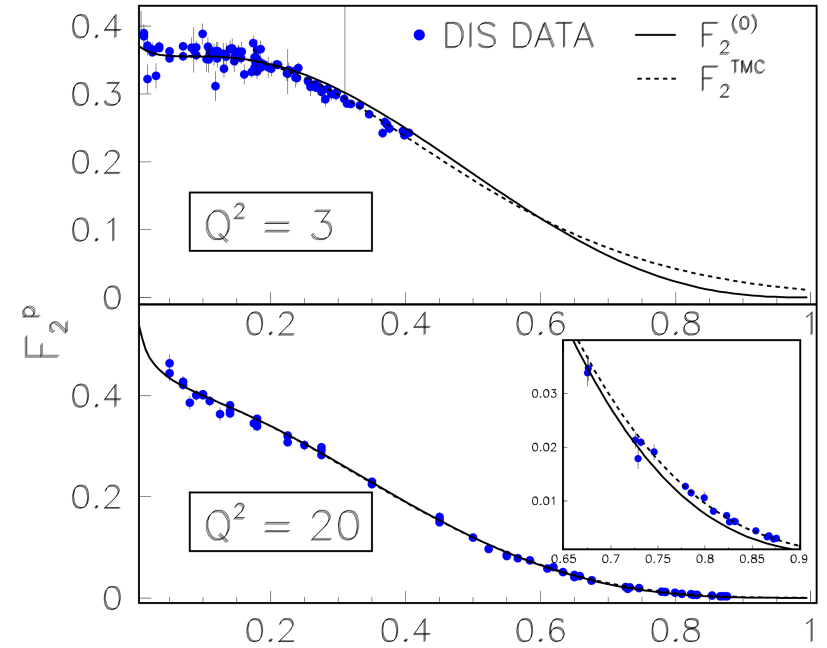
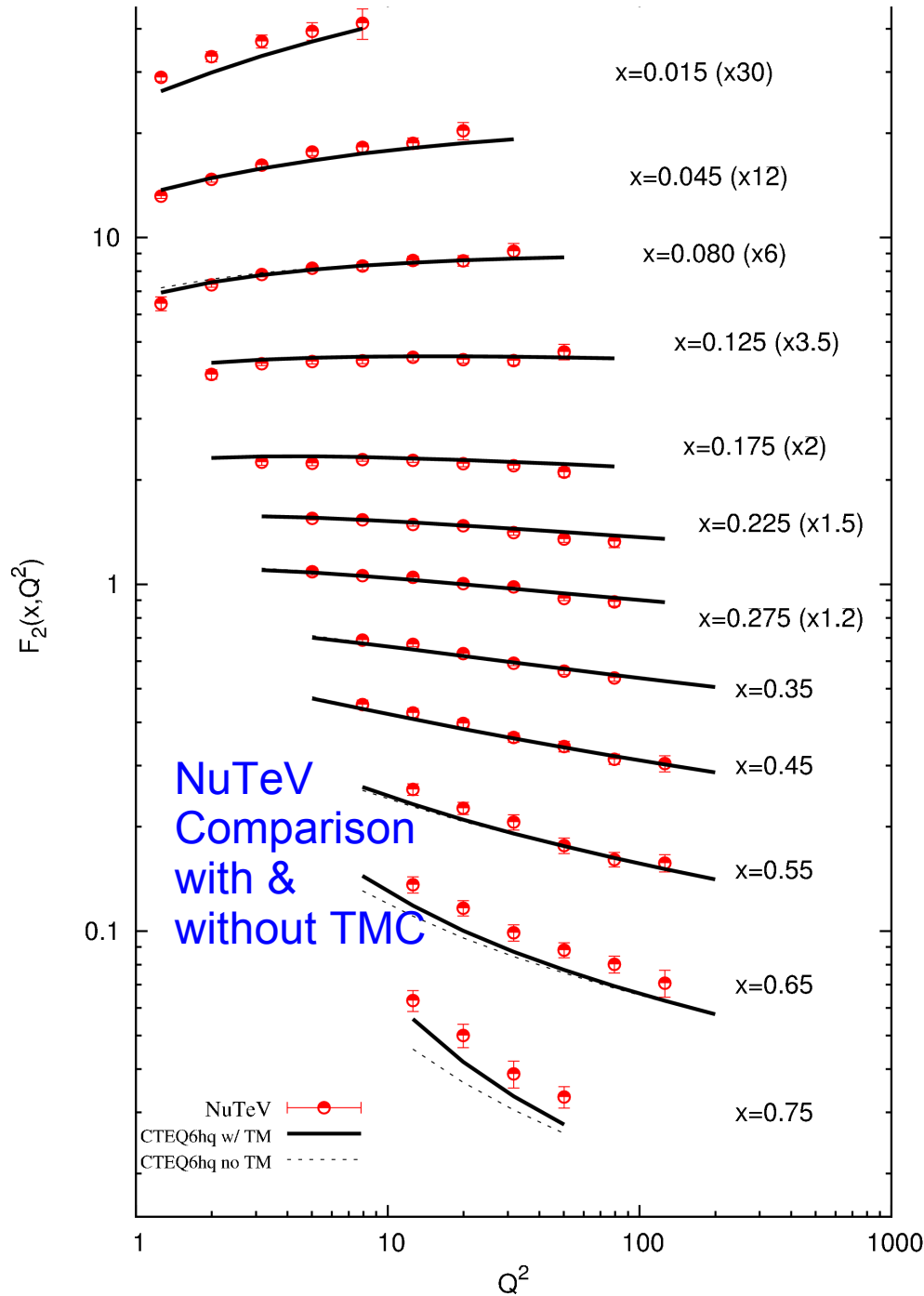
- Obtain general structure:
- Valid at any order: LO, NLO,...
- Quark masses are included; both  $m_i$  and  $m_f$
- Recover known results
  - Georgi, Politzer
  - Barbieri et al
  - Kretzer & Reno

• **The definitive reference for TMC**

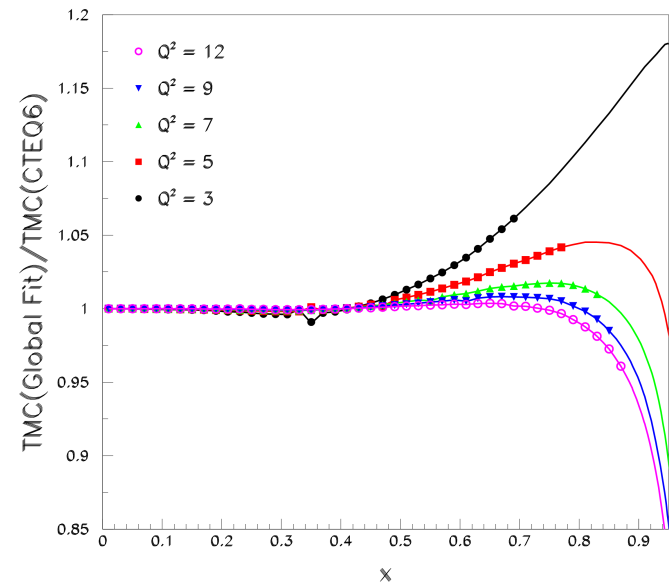
TMC important at large  $x$ , small  $Q^2$



# A Review of Target Mass Corrections:



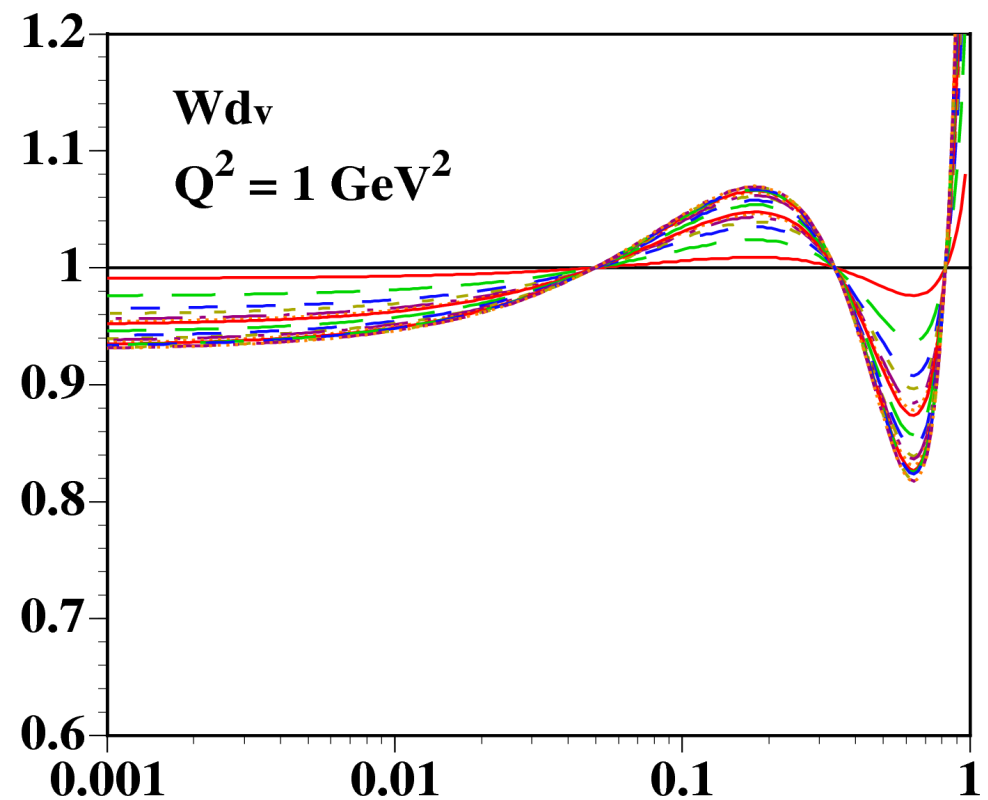
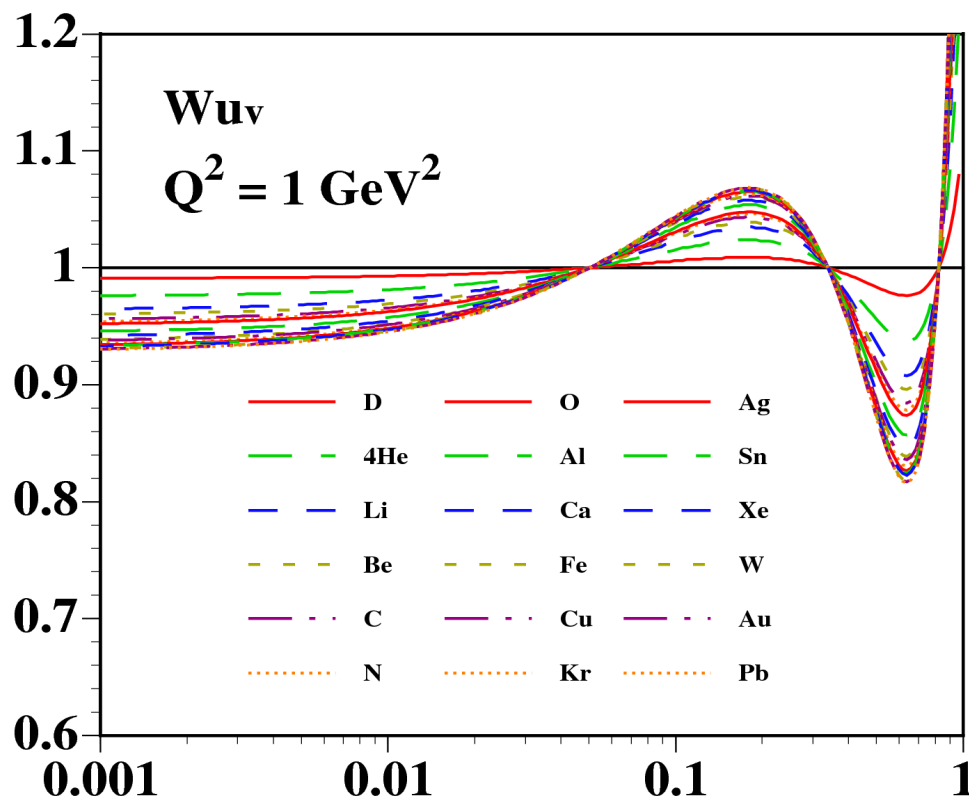
## Comparison of PDF+TMC vs “Unfolding” Method



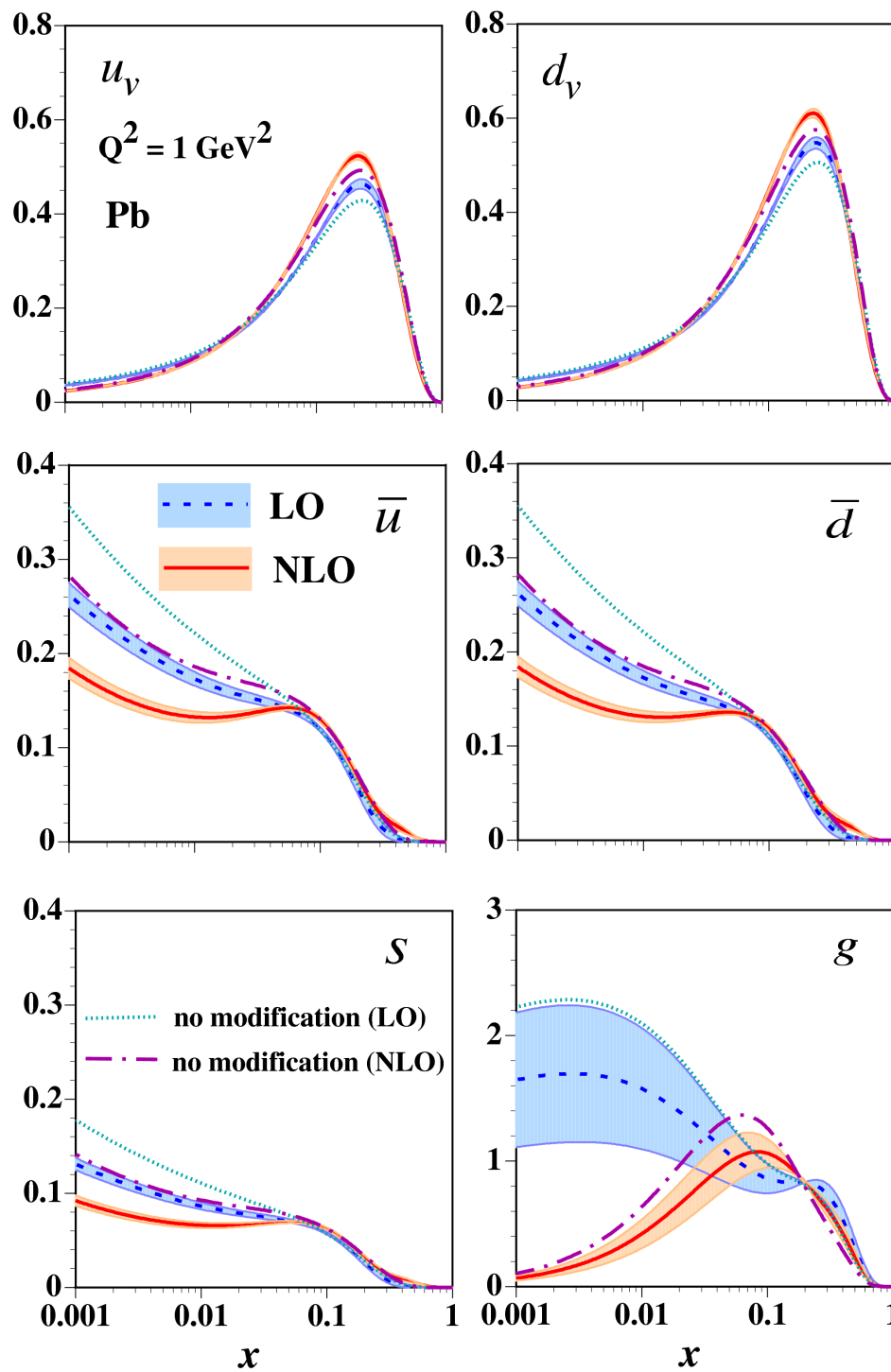
# Nuclear PDFs

$$f_i^A(x, Q_0^2) = w_i(x, A, Z) f_i(x, Q_0^2)$$

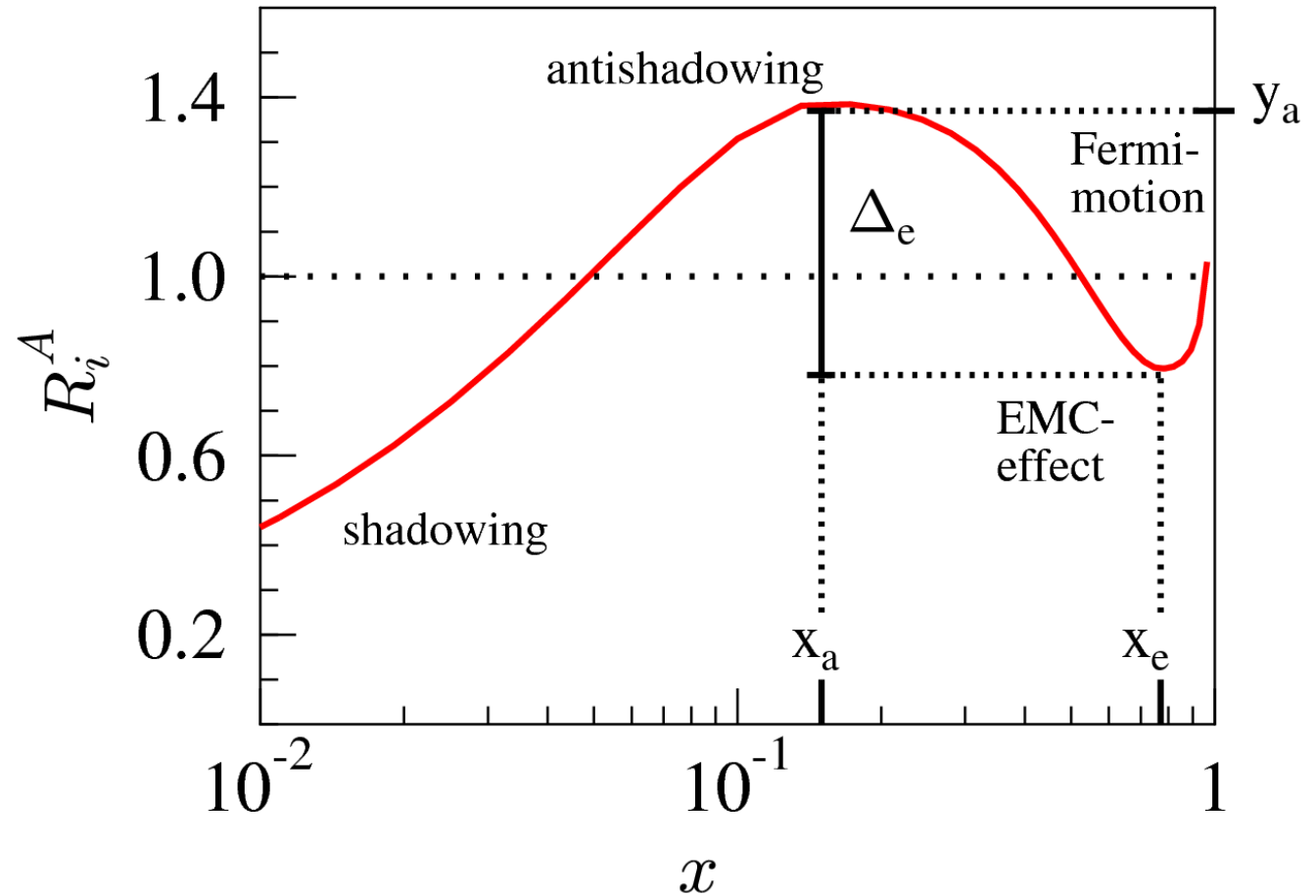
$$w_i(x, A, Z) = 1 + \left(1 - \frac{1}{A^\alpha}\right) \frac{a_i + b_i x + c_i x^2 + d_i x^3}{(1-x)^{\beta_i}}$$



Lead  
nPDFs



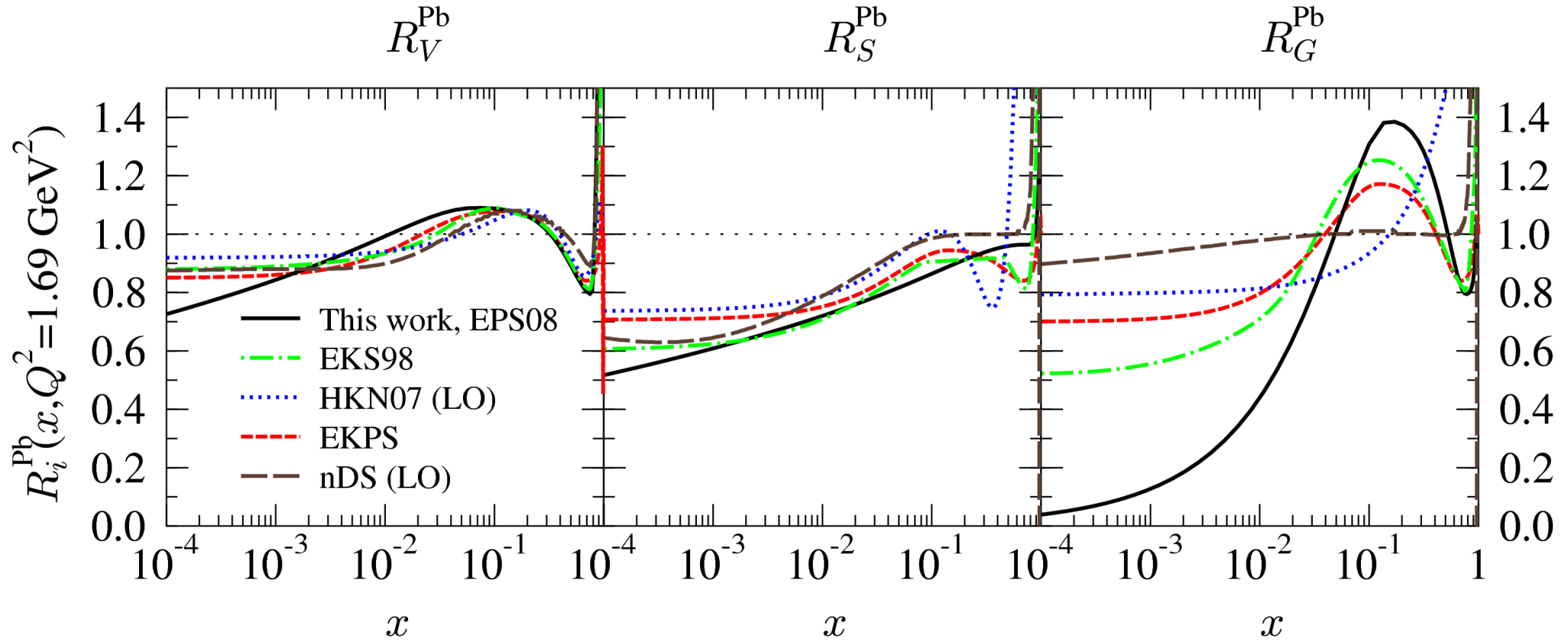
$$f_i^A(x, Q^2) = R_i^A(x, Q^2) f_i(x, Q^2)$$



$$R_1^A(x) = c_0^A + (c_1^A + c_2^A x^{\alpha^A}) [\exp(-x/x_a^A) - \exp(-x_a^A/x_a^A)], \quad x \leq x_a^A$$

$$R_2^A(x) = a_0^A + a_1^A x + a_2^A x^2 + a_3^A x^3, \quad x_a^A \leq x \leq x_e^A$$

$$R_3^A(x) = \frac{b_0^A - b_1^A x}{(1-x)^{\beta^A}} + b_2^A (x - x_e^A)^2, \quad x_e^A \leq x \leq 1.$$



Relate general  
Nuclear  $A$   
to  $A=1$  (proton)

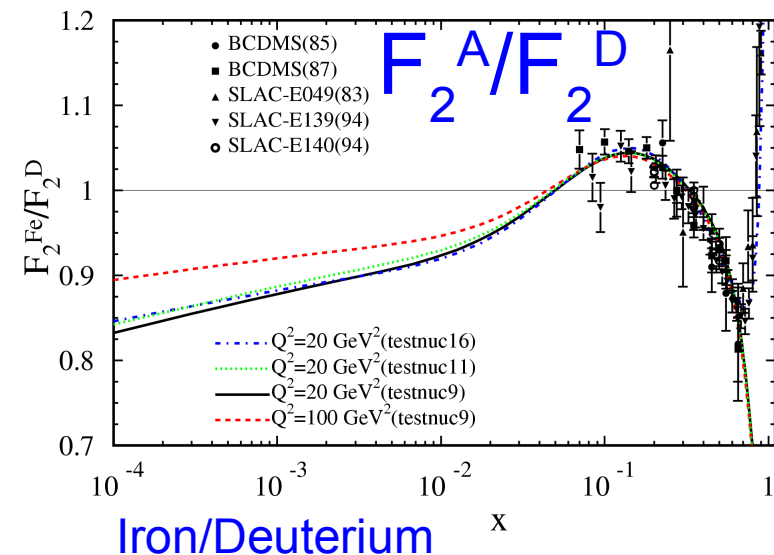
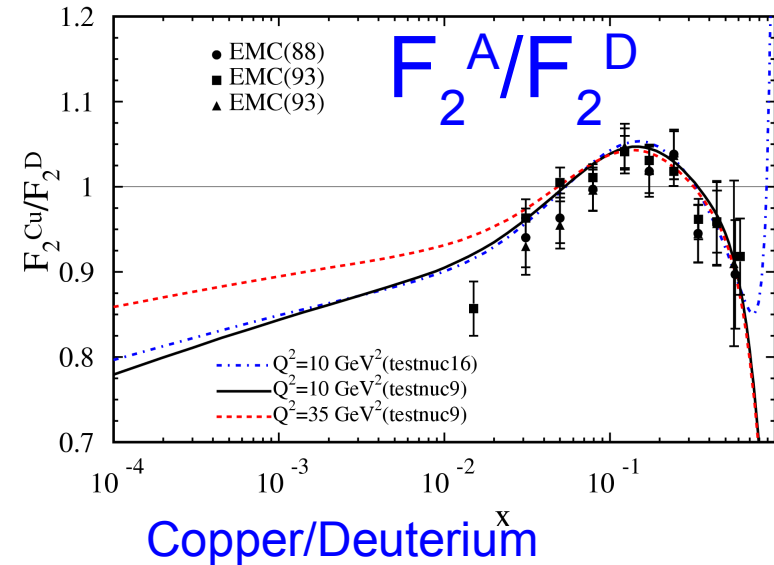
*Allows CTEQ PDFs as a simple limit*



# Nuclear PDF and Correction Factors

- ✓ CTEQ global fit extended  
can handle various nuclear targets
- ✓ CTEQ Data + nuclear DIS & DY  
[~15 targets; ~2000+ data]
- ✓ A-dependence modeled;  
NLO fits work well

**Nuclear Corrections  
affect proton PDFs**



Nuclear PDFs from neutrino deep inelastic scattering.

I. Schienbein, J.Y. Yu, C. Keppel, J.G. Morfin, F. Olness, J.F. Owens.

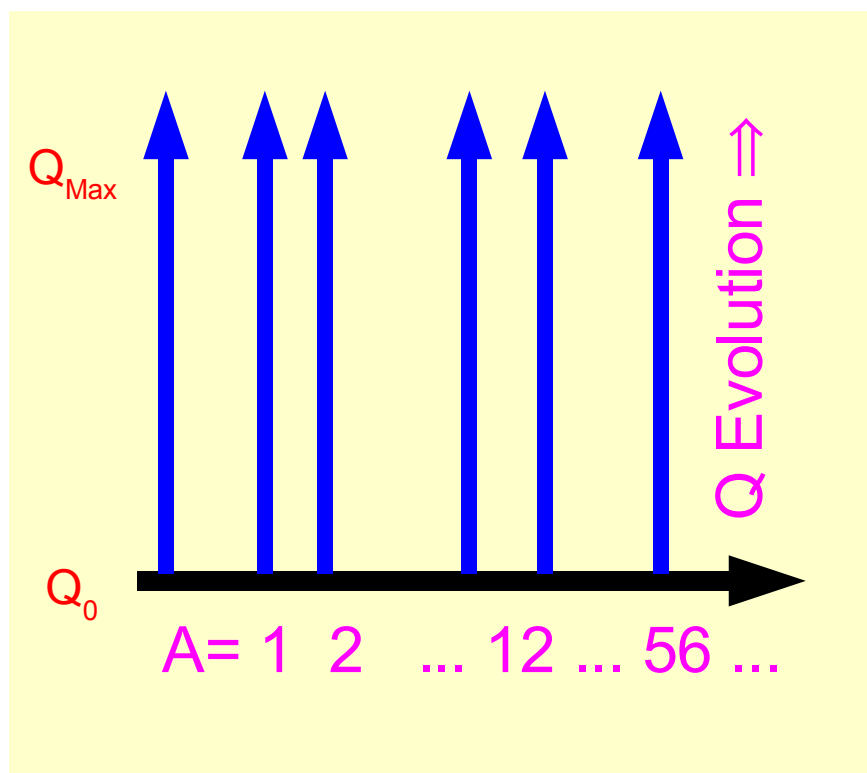
Phys.Rev.D77:054013,2008.

# Nuclear PDF evolution

$$xf(x) = x^{a_1} (1-x)^{a_2} e^{a_3 x} (1 + e^{a_4 x})^{a_5}$$

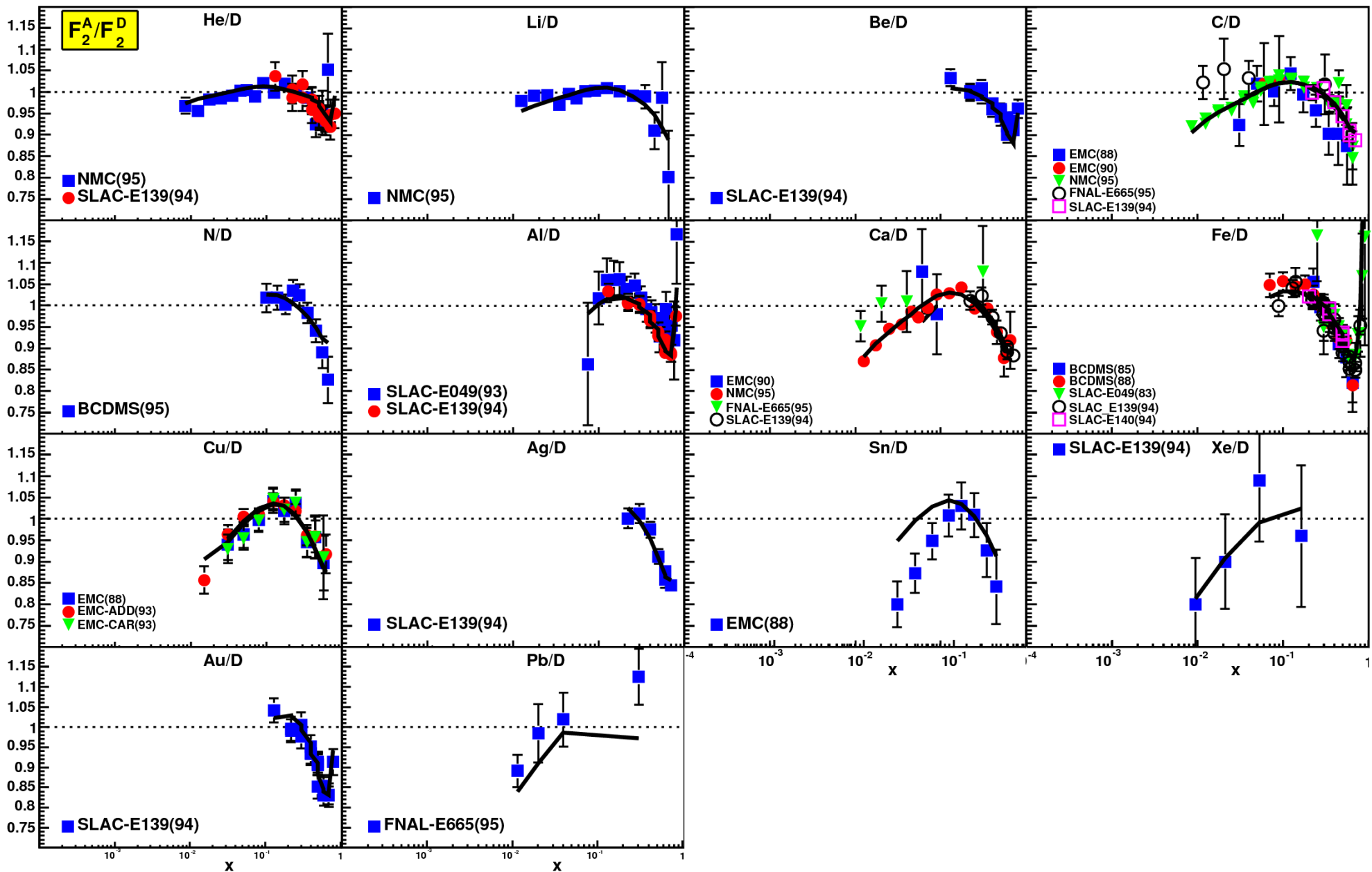
$$a_i \rightarrow a_i(A)$$

$$a_k = a_{k,0} + a_{k,1} (1 - A^{-a_{k,2}})$$

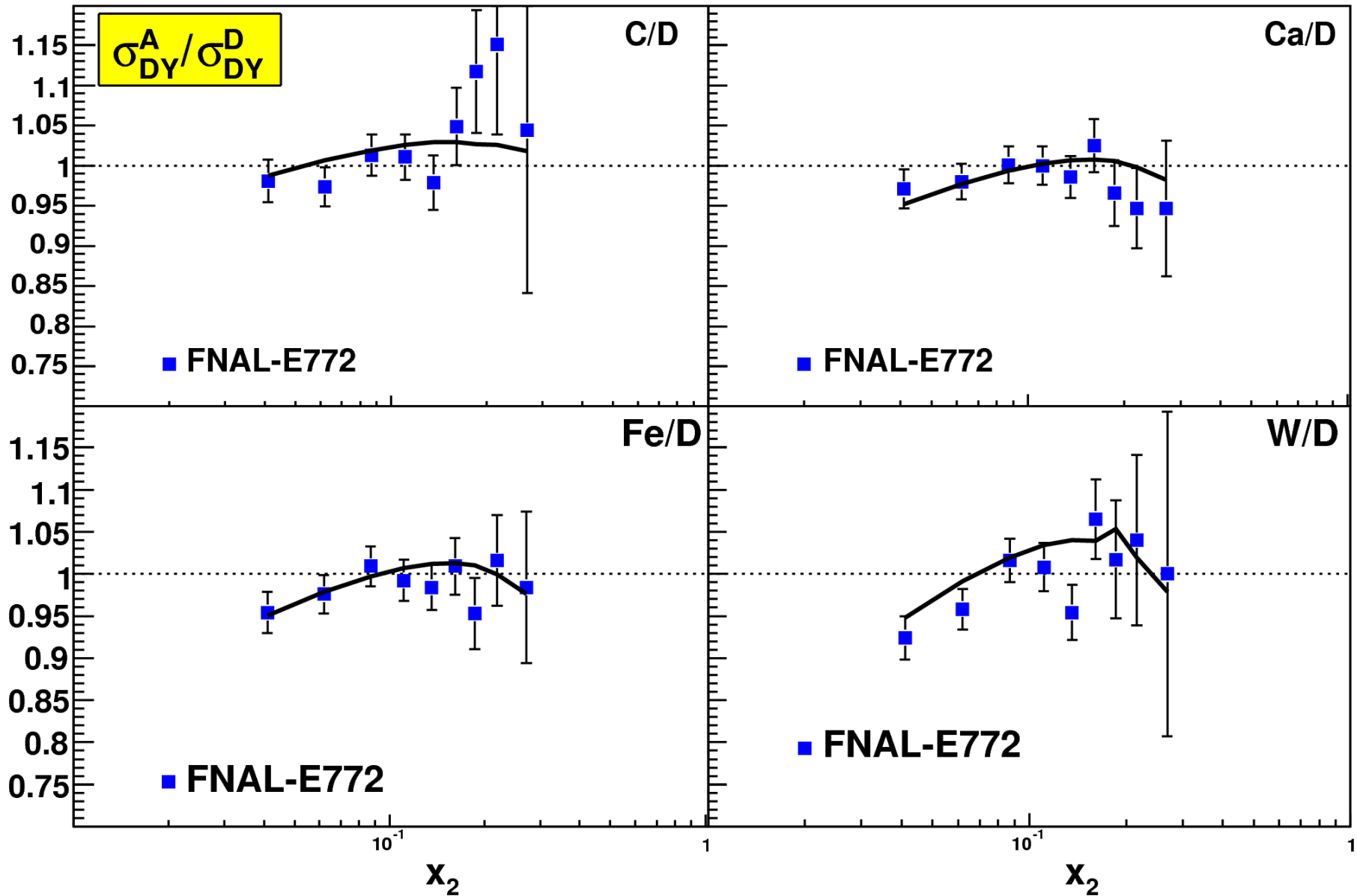


Observable	Experiment	Ref.	# data	$\chi^2$ A1L	$\chi^2$ A1M	$\chi^2$ A1A	ID
$F_2^A/F_2^D$ : He/D	SLAC-E139	[18]	18	9.8	6.82	6.28	5141
	NMC-95,re	[19]	16	35.6	16.91	18.31	5124
	Hermes	[20]	92	134.0	72.14	71.05	5156
Li/D	NMC-95	[21]	15	45.0	18.80	19.68	5115
Be/D	SLAC-E139	[18]	17	52.7	21.48	20.75	5138
	C/D	EMC-88	[22]	9	10.3	7.29	7.11
C/D	EMC-90	[23]	2	0.2	0.14	0.11	5110
	SLAC-E139	[18]	7	31.3	4.06	4.51	5139
	NMC-95,re	[19]	16	13.9	16.12	16.62	5114
	NMC-95	[21]	15	13.9	7.13	7.26	5113
	FNAL-E665-95	[24]	4	23.4	8.81	8.29	5125
N/D	BCDMS-85	[25]	9	12.1	6.94	7.26	5103
Hermes		[20]	92	94.5	62.42	58.94	5157
	Al/D	SLAC-E049	[26]	18	32.2	20.42	20.38
SLAC-E139		[18]	17	22.12	6.50	8.05	5136
	Ca/D	EMC-90	[23]	2	5.5	1.47	1.37
SLAC-E139		[18]	7	14.2	2.07	1.53	5140
	NMC-95,re	[19]	15	48.6	12.75	13.74	5121
	FNAL-E665-95	[24]	4	16.2	7.88	7.67	5126
Fe/D	BCDMS-85	[25]	6	5.3	3.91	4.39	5102
	BCDMS-87	[27]	10	35.0	8.58	9.81	5101
SLAC-E049		[28]	14	8.8	10.39	6.24	5131
	SLAC-E139	[18]	23	43.4	35.14	35.31	5132
	SLAC-E140	[29]	6	16.8	2.93	4.87	5133
	Cu/D	EMC-88	[22]	9	7.1	4.24	4.47
EMC-93(addendum)		[30]	10	14.4	6.13	6.89	5104
	EMC-93(chariot)	[30]	9	9.8	6.18	6.53	5105
Kr/D	Hermes	[20]	84	120.7	64.53	62.98	5158
Ag/D	SLAC-E139	[18]	7	22.5	4.04	2.88	5135
Sr/D	EMC-88	[22]	8	28.3	19.82	20.09	5108
Xe/D	FNAL-E665-92(em cut)	[31]	4	4.0	0.65	0.61	5127
Au/D	SLAC-E139	[18]	18	48.6	8.22	7.89	5137
Pb/D	FNAL-E665-95	[24]	4	20.3	7.77	7.45	5129
$F_2^A/F_2^{A'}$ :							
Be/C	NMC-96	[32]	15	14.3	5.87	5.82	5112
Al/C	NMC-96	[32]	15	14.1	5.17	5.19	5111
Ca/C	NMC-96	[19]	20	21.7	31.47	35.73	5120
NMC-96		[32]	15	19.8	5.39	5.31	5119
Fe/C	NMC-96	[32]	15	25.9	9.54	9.35	5143
Sr/C	NMC-96	[33]	144	312.5	102.82	96.29	5159
Pb/C	NMC-96	[32]	15	13.4	7.31	8.09	5116
C/Li	NMC-96	[19]	20	49.7	21.82	20.37	5123
Ca/Li	NMC-96	[19]	20	38.3	24.62	23.53	5122
$\sigma_{DY}^{PA}/\sigma_{DY}^{PA'}$ :							
C/D	FNAL-E772-90	[34]	9	14.3	7.26	6.88	5203
Ca/D	FNAL-E772-90	[34]	9	14.1	3.81	3.33	5204
Fe/D	FNAL-E772-90	[34]	9	21.7	3.71	3.15	5205
W/D	FNAL-E772-90	[34]	9	49.7	11.07	11.27	5206
Fe/Be	FNAL-E866-99	[35]	28	38.3	29.95	29.33	5201
W/Be	FNAL-E866-99	[35]	28	38.3	25.54	25.30	5202
<b>Total:</b>			<b>958</b>	<b>1514.4</b>	<b>777.0</b>	<b>768.3</b>	

# Fit to Nuclear DIS Data



# Fit to Nuclear DY Data



# Make Nuclear “A” Dependence an *Dynamic* Component of Fit

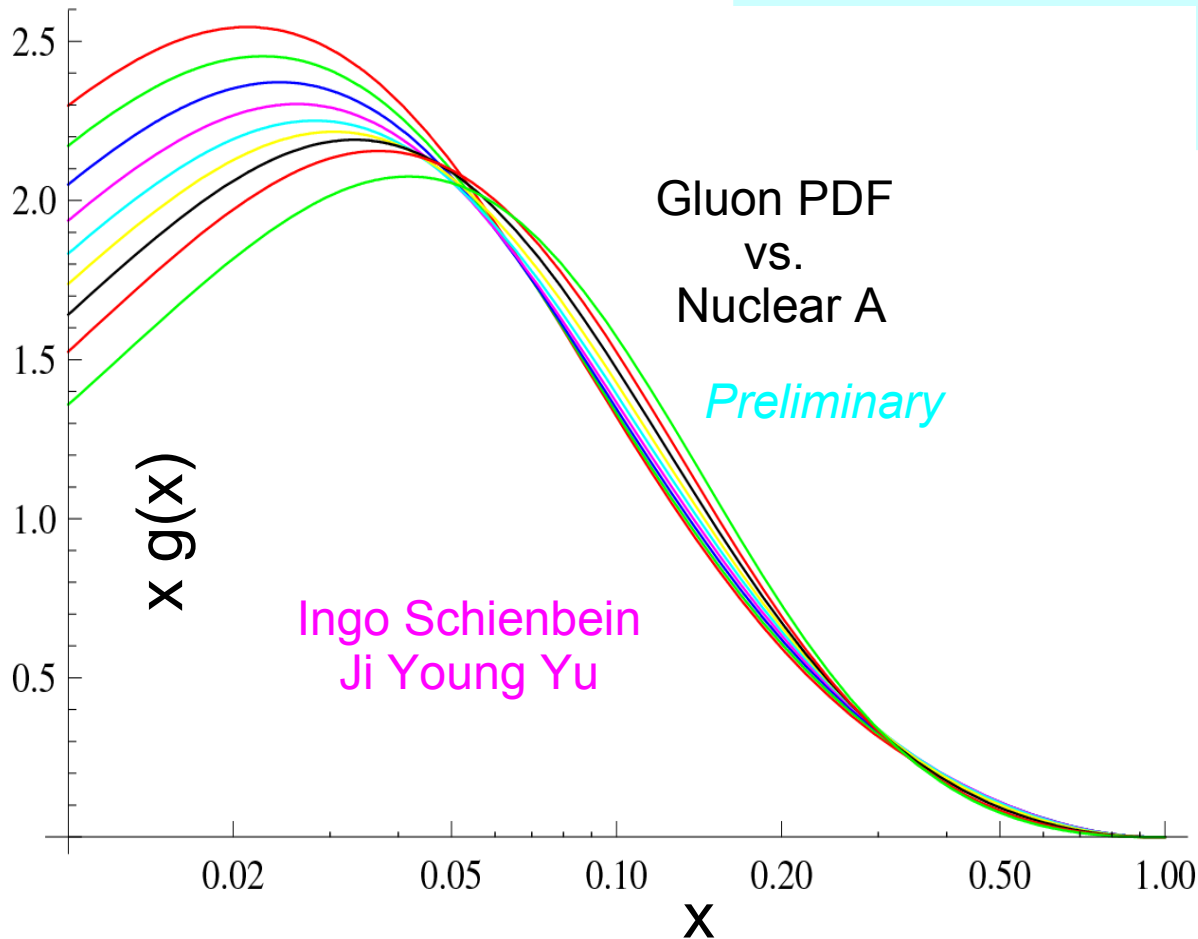
Yields full NLO nuclear PDFs:  $f_i(x, Q, A)$

Designed to reduce to proton PDF in limit  $A \rightarrow 1$

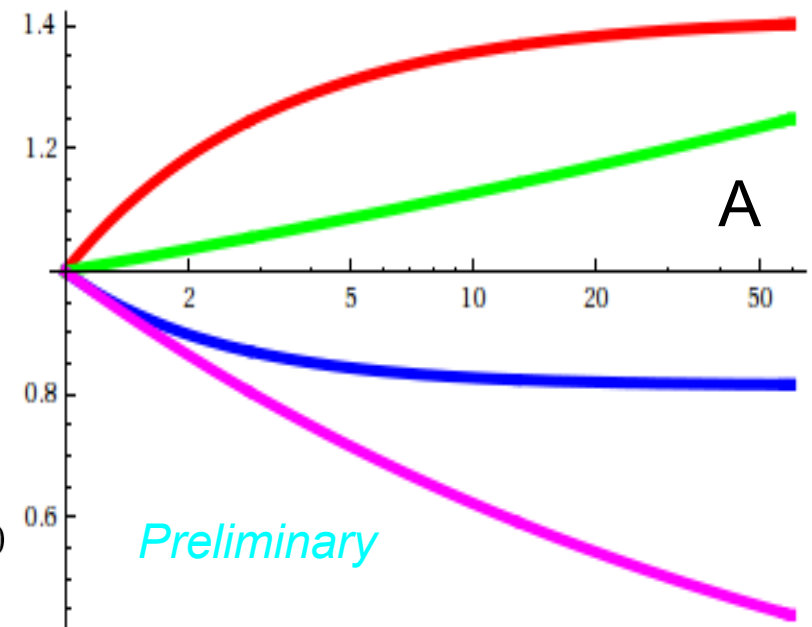
*Nuclear corrections  
not written in stone!*

$$x f(x) = x^{a_1} (1 - x)^{a_2} e^{a_3 x} (1 + e^{a_4 x})^{a_5}$$

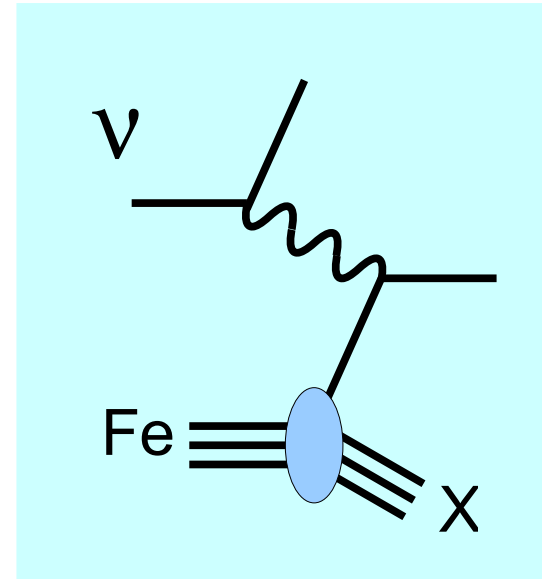
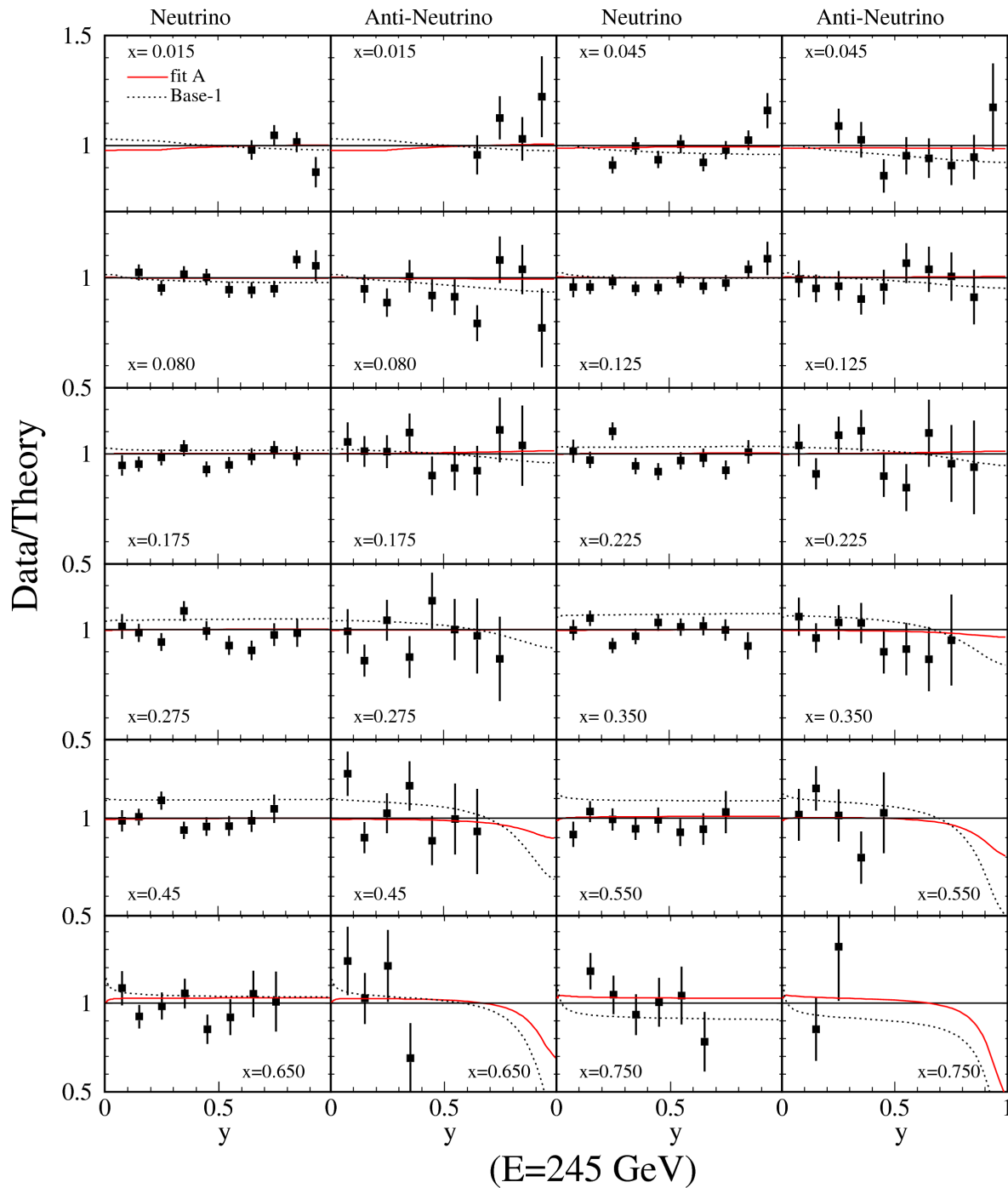
$$a_i \rightarrow a_i(A)$$



$a_i(A)/a_i(A=1)$  coefficients  
vs. Nuclear A



# Use Nuclear Data to Extract Nuclear PDFs Directly: *(Model Independent)*

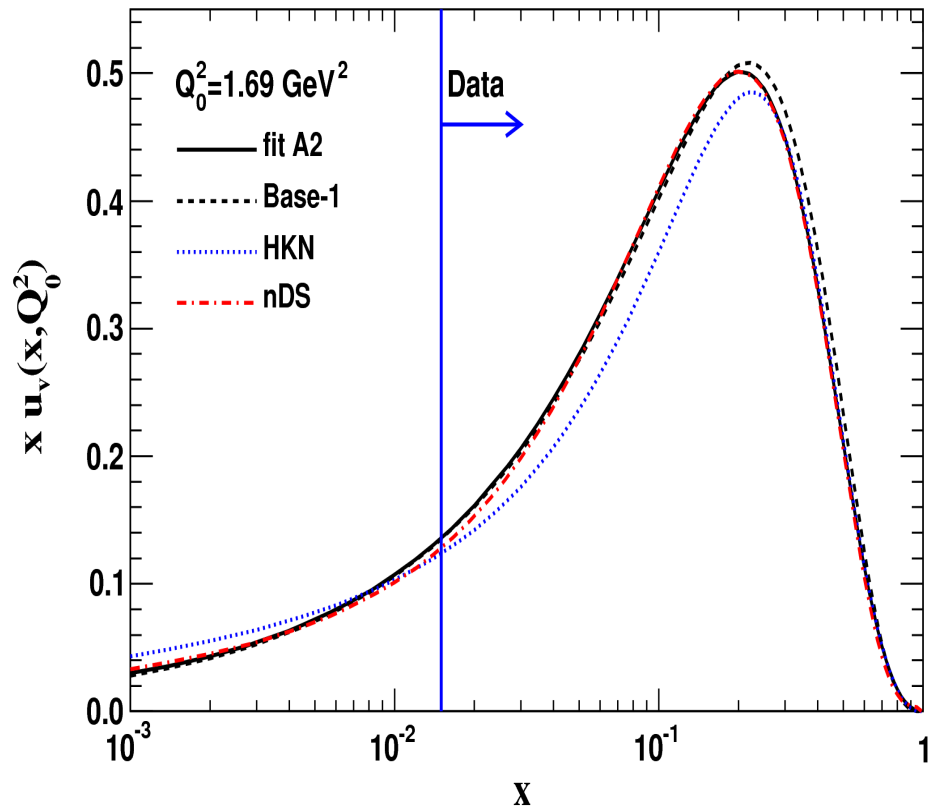


Comparison of  
NuTeV Iron data  
with  
Nuclear PDF Fit

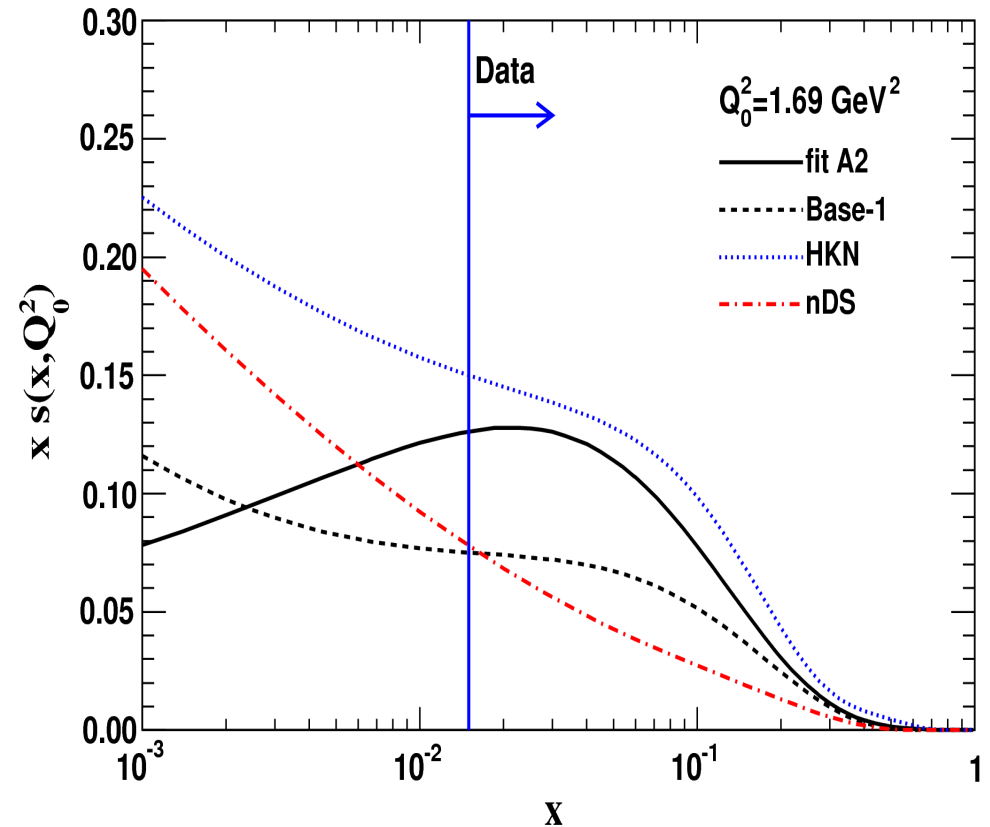
using CTEQ values  
fix  $g(x)$  &  $\bar{d}/\bar{u}$

# Use Nuclear Data to Extract Nuclear PDFs Directly: *(Model Independent)*

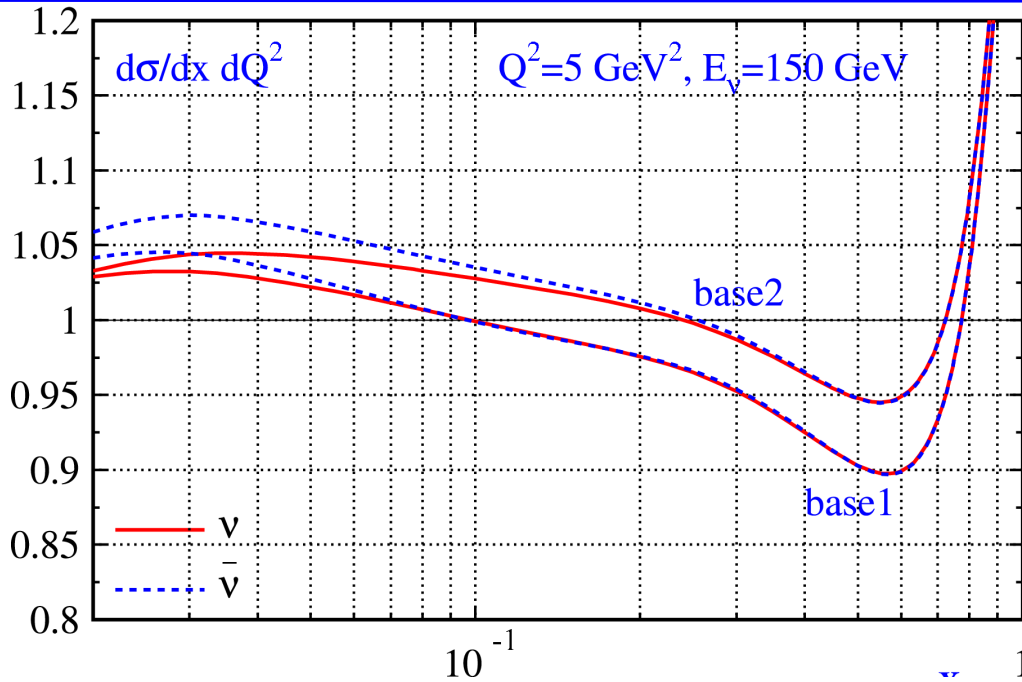
## $u(x, Q)$



## $s(x, Q)$



# Nuclear Correction Factors depend on A, Q, and Observable

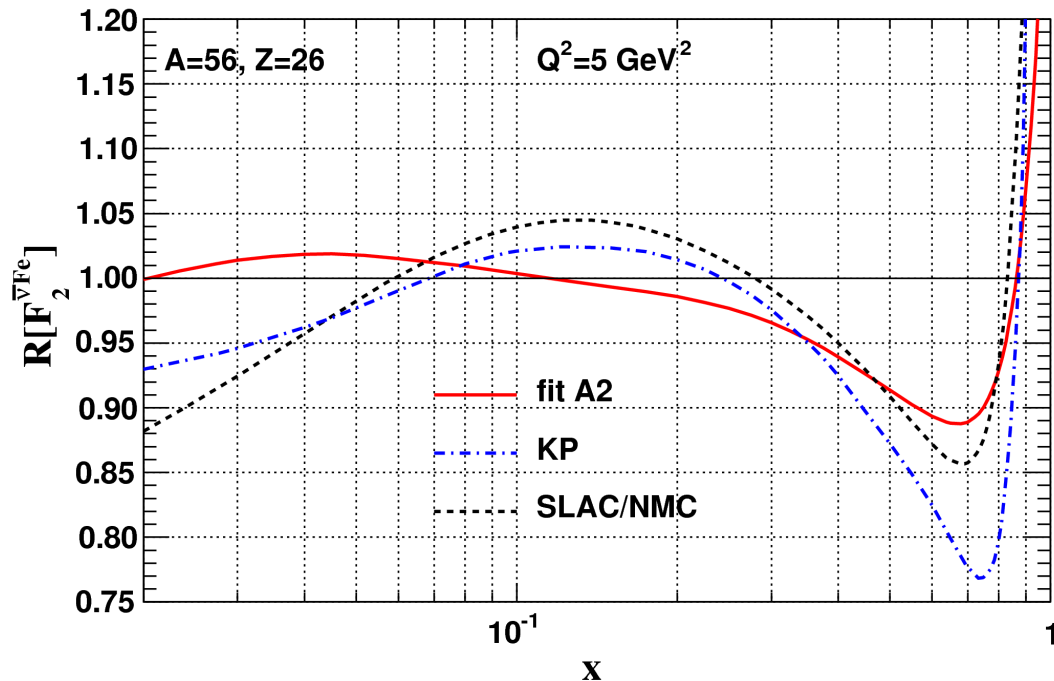


## Nuclear Correction Factors:

- 1) Extract Iron PDFs
- 2) Use Iron PDFs to compute Iron  
⇒ Proton correction factors

*No “model” input*

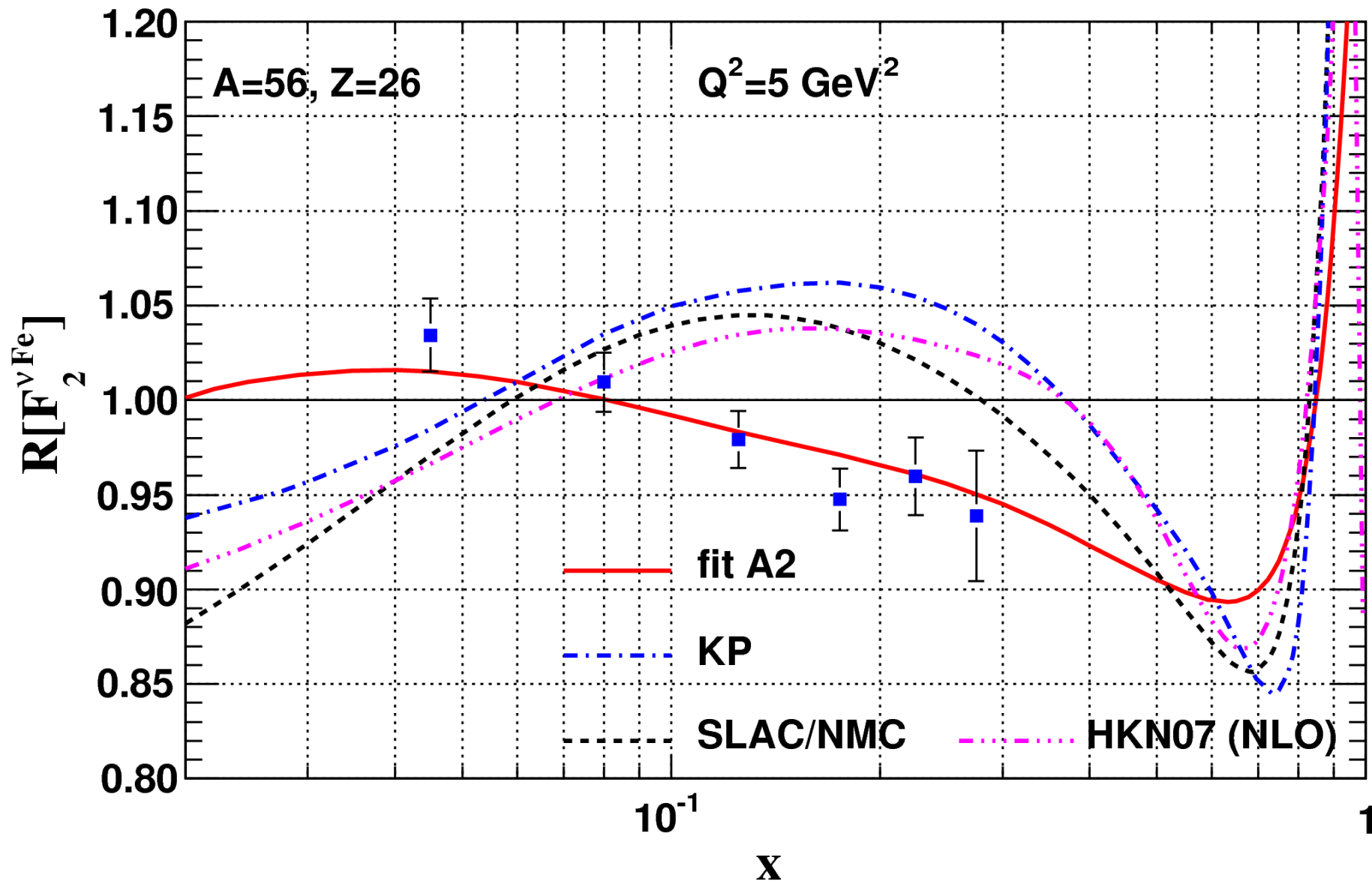
- 3) Nuclear correction depends  
on Q, A, & observable
- 4) Compare with SLAC/NMC & KP



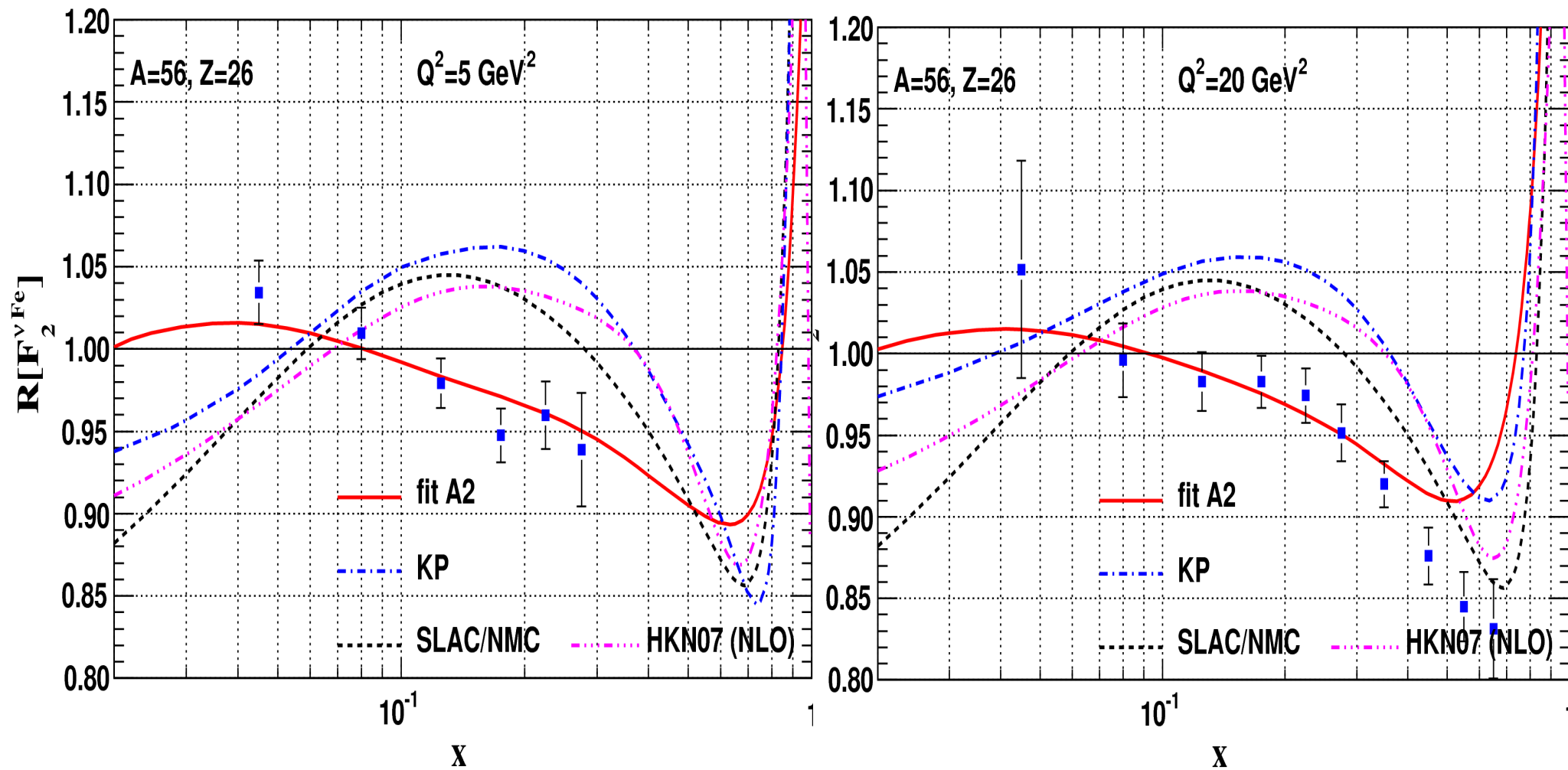
$$R[\mathcal{O}] = \frac{\mathcal{O}[Nucleon]}{\mathcal{O}[proton]}$$



# Nuclear Correction Factors depend on A, Q, and Observable



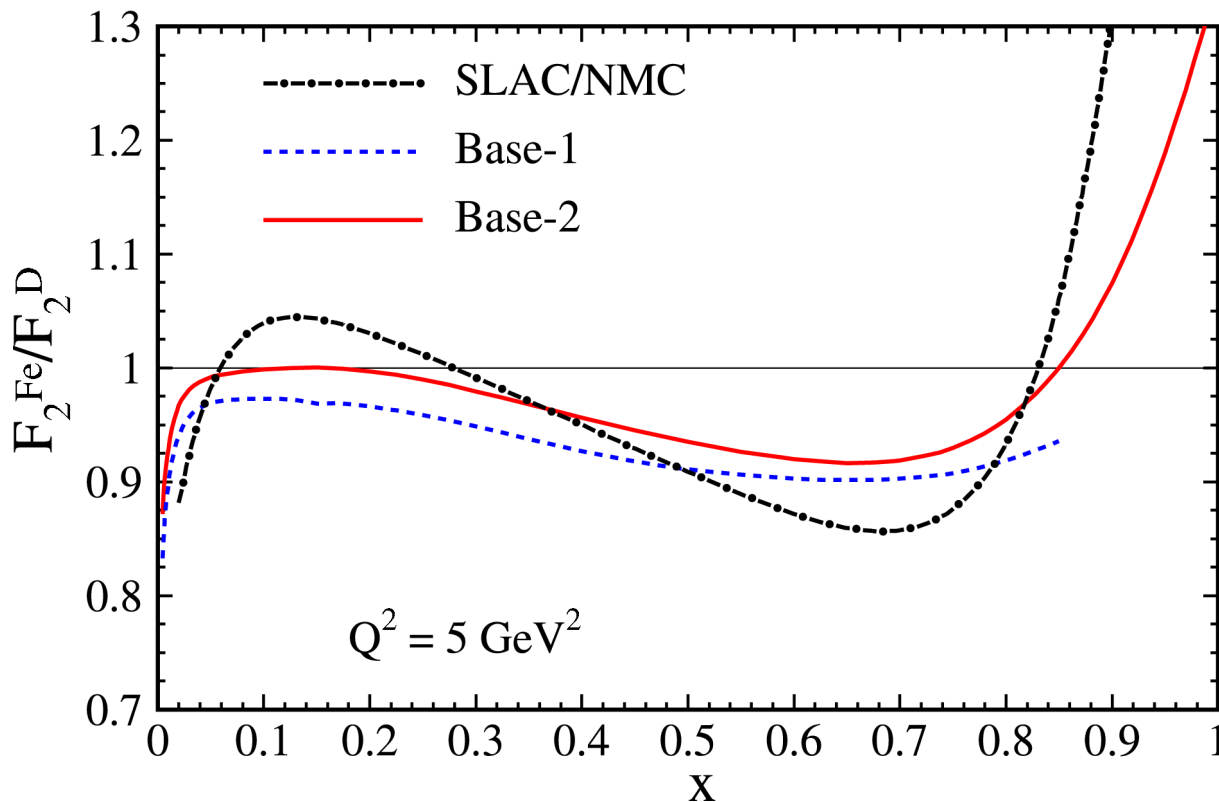
# Nuclear Correction Factors depend on A, Q, and Observable



# Could nuclear corrections be different for CC (W) or NC ( $\gamma, Z$ ) processes???

$$R[\mathcal{O}] = \frac{\mathcal{O}[\text{Nucleon}]}{\mathcal{O}[\text{proton}]}$$

Use CC Iron PDFs to compute  
NC DIS Nuclear Corrections



**Question:**  
**How to resolve differences???**

1) There might be a compromise set of nuclear corrections that adequately satisfies both NC and CC data

2) It may be necessary to apply separate CC and NC corrections

# Conclusions

# Conclusions

## Important to quantify PDF Uncertainties

... both “known” and “unknown”

At LHC, heavy quarks play a prominent role  $\{s, c, b \dots\}$ ,  
... *even in W/Z production*

## Tensions between various data sets:

Historically, CC and NC

NuTeV & E866 impact on d/u ratio

## New global fitting program includes heavy target effects **DYNAMICALLY**

Nuclear corrections are not “carved in stone”

Incorporates proper errors and systematics

May allow for a “compromise” fit

## Extensible to all nuclear A values

Yields NLO nuclear PDFs:  $f_i(x, Q, A)$

***Important ingredient for standard CTEQ fits***