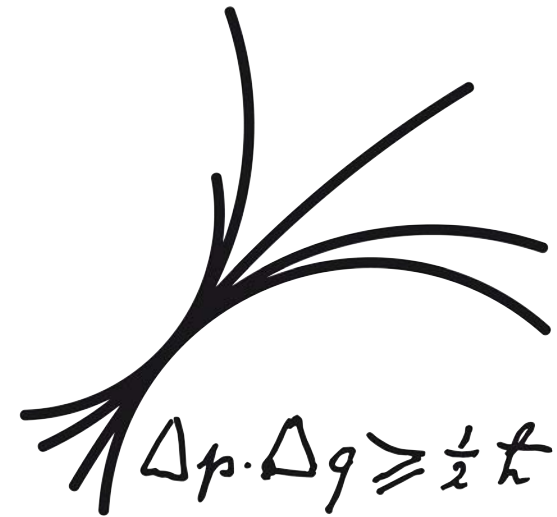


Neutrinos – The Known Unknowns



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MAX-PLANCK-GESELLSCHAFT

Based on:

several decades of research on neutrino physics, including countless sleepless nights for theorists and many exhausting shifts for experimentalists

Final SGGDT Symposium, Ringberg Castle, 19-10-2015

Contents:

1. Neutrinos in the Standard Model
2. What is Neutrino Mixing?
3. Neutrino Masses & Lepton Number Violation
4. Conclusions

1. Neutrinos in the Standard Model

1. Neutrinos in the Standard Model



Standard Model of Elementary Particles

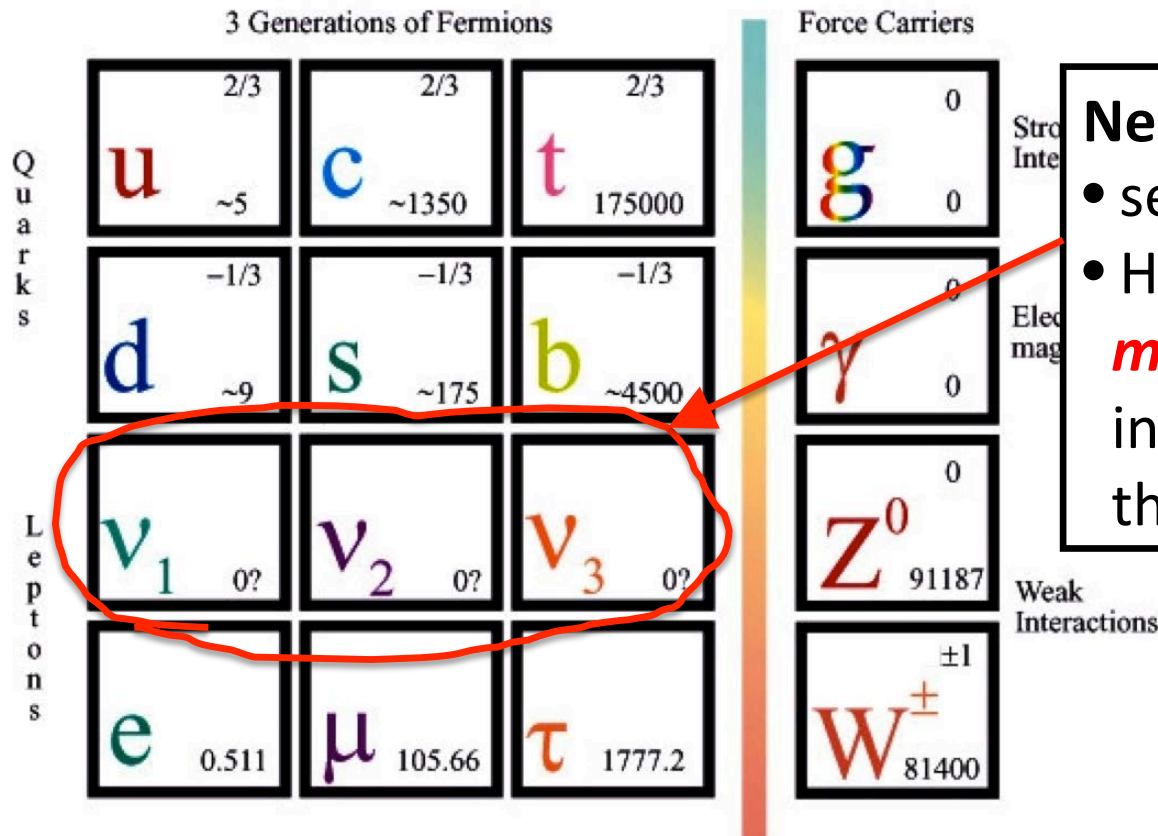
3 Generations of Fermions			Force Carriers	
Q u a r k s	<div><div>2/3</div><div>u</div><div>~5</div></div>	<div><div>2/3</div><div>c</div><div>~1350</div></div>	<div><div>2/3</div><div>t</div><div>175000</div></div>	<div><div>0</div><div>g</div><div>0</div></div> <div>Strong Interactions</div>
	<div><div>-1/3</div><div>d</div><div>~9</div></div>	<div><div>-1/3</div><div>s</div><div>~175</div></div>	<div><div>-1/3</div><div>b</div><div>~4500</div></div>	<div><div>0</div><div>γ</div><div>0</div></div> <div>Electro-magnetism</div>
L e p t o n s	<div><div>0?</div><div>ν₁</div><div>0?</div></div>	<div><div>0?</div><div>ν₂</div><div>0?</div></div>	<div><div>0?</div><div>ν₃</div><div>0?</div></div>	<div><div>0</div><div>Z⁰</div><div>91187</div></div> <div>Weak Interactions</div>
	<div><div>0.511</div><div>e</div><div></div></div>	<div><div>105.66</div><div>μ</div><div></div></div>	<div><div>1777.2</div><div>τ</div><div></div></div>	<div><div>±1</div><div>W[±]</div><div>81400</div></div>

Masses are in MeV

+ Higgs + antiparticles

1. Neutrinos in the Standard Model

Standard Model of Elementary Particles



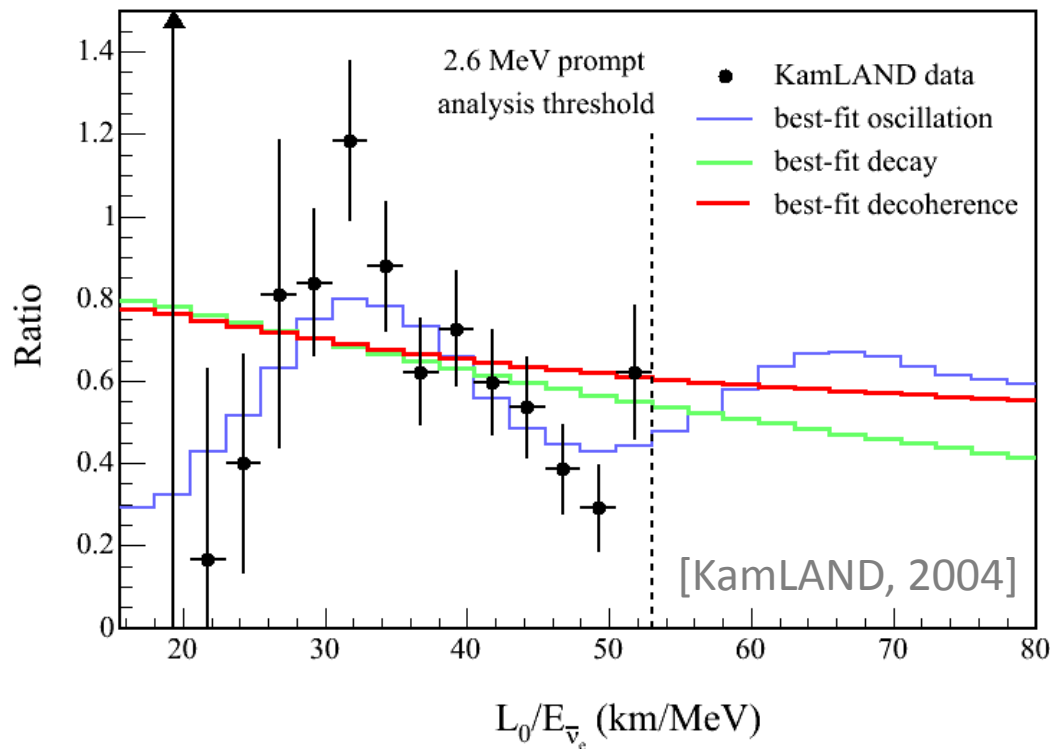
Masses are in MeV

+ Higgs + antiparticles

Neutrinos:

- seem to fit in well
- HOWEVER: they are **massless in the SM** while in reality we have seen that they are massive

1. Neutrinos in the Standard Model



We know from
neutrino
oscillations that
neutrinos MUST
BE massive!!

$$P_{ee} \simeq 1 - \sin^2 2\theta_{13} \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right) \Rightarrow m_2^2 - m_1^2 > 0 \text{ \& \; } |m_3^2 - m_1^2| \neq 0$$

THUS:

at least two light ν 's have non-zero mass!

1. Neutrinos in the Standard Model

In fact, there are **THREE** (not only a single) reasons for neutrinos to be massless in the SM:

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- no right-handed neutrinos ν_R in the SM: if they were present, we could write down a Dirac mass term (as for the other fermions)

$$\mathcal{L}_Y \supset -\bar{L}\tilde{H}y_\nu\nu_R + h.c. \rightarrow -\bar{L}\langle\tilde{H}\rangle y_\nu\nu_R + h.c. = -\bar{\nu}_L m_D \nu_R + h.c.$$

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typical Left-Right Yukawa coupling

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SM-Higgs

Higgs obtains a
"VEV" $v=\langle H\rangle$

coupling \times VEV
is interpreted
as **MASS**

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lepton-number violating (LNV) Yukawa coupling

coupling \times VEV v_T again interpreted as **MASS**

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- no right-handed neutrinos ν_R in the SM
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- only renormalisable couplings in the SM: otherwise, we could write down a direct (LNV!) mass term at mass dimension five

$$\mathcal{L}_5 = \frac{-y_{ij}}{\Lambda} (\overline{L}_i^c H) i\sigma_2 (H L_j)$$

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coupling $\times v^2/\Lambda$ can be interpreted as **MASS**

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 - no Higgs triplets T in the SM
 - only renormalisable couplings in the SM
- *beyond the SM, we quite generically violate (at least) one of these conditions*

THUS: having non-zero neutrino masses is generic, not exotic!!!

2. What is Neutrino Mixing?

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For neutrinos, it holds that:

mass basis \neq flavour basis

BUT:

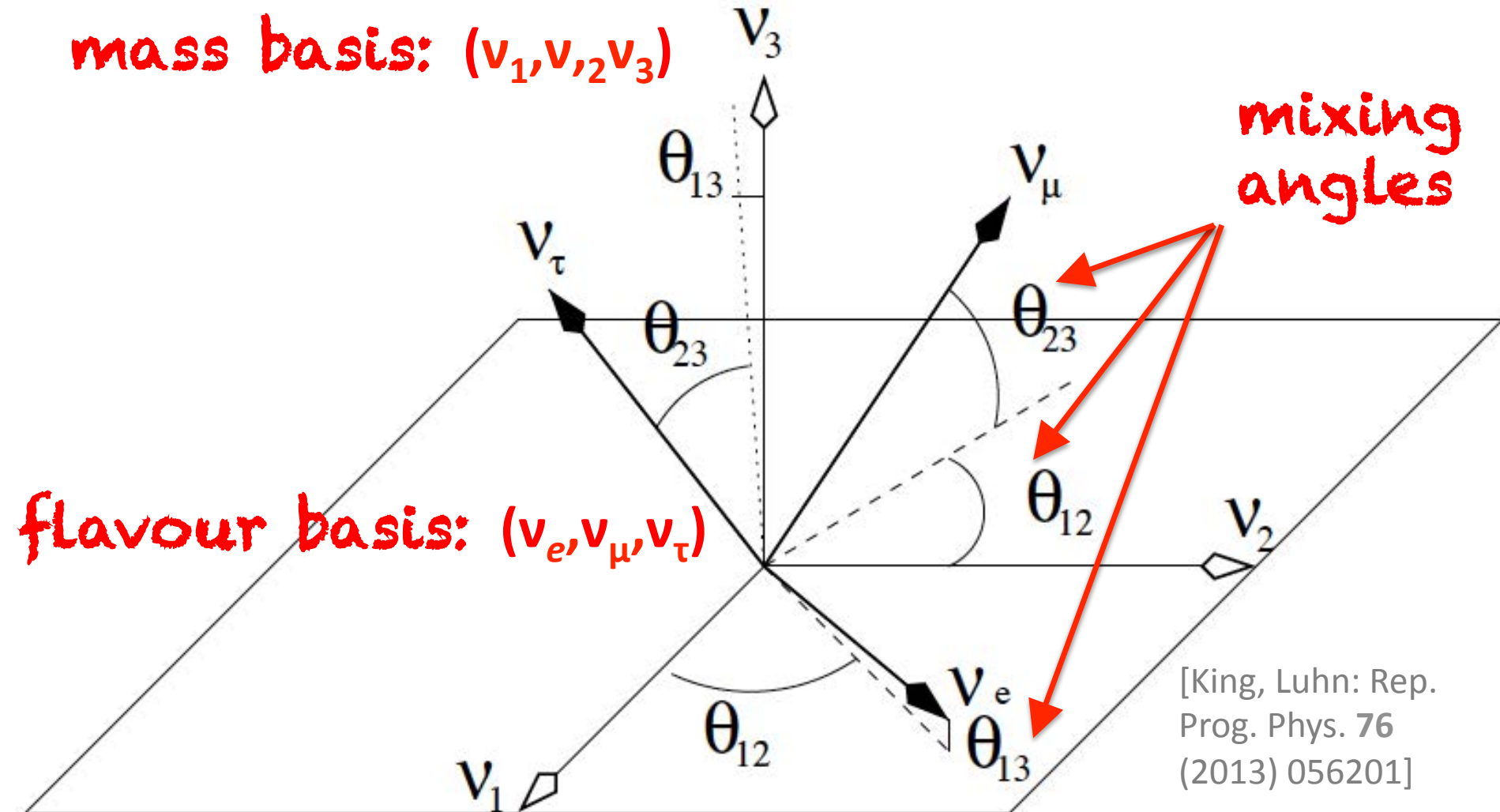
What does that mean?!? In fact, it's simple...

- while an electron e has a well-defined electron mass m_e ...
- ... an electron neutrino ν_e does NOT have an "electron neutrino mass" m_{ν_e} , but instead it is a quantum-mechanical superposition of several mass eigenstates with masses $m_{1,2,3}$

2. What is Neutrino Mixing?

Mathematically, this can be interpreted as a rotation in an abstract "flavour space":

mass basis: (ν_1, ν_2, ν_3)



[King, Luhn: Rep.
Prog. Phys. **76**
(2013) 056201]

2. What is Neutrino Mixing?

The “oscillation parameters” (= mixing angles θ_{12} , θ_{13} , θ_{23} and mass-square differences $m_2^2 - m_1^2$ and $|m_3^2 - m_1^2|$) can be measured:

NuFIT 2.0 (2014)

	Normal Ordering ($\Delta\chi^2 = 0.97$)		Inverted Ordering (best fit)		Any Ordering
	bfp $\pm 1\sigma$	3σ range	bfp $\pm 1\sigma$	3σ range	3σ range
$\sin^2 \theta_{12}$	$0.304^{+0.013}_{-0.012}$	$0.270 \rightarrow 0.344$	$0.304^{+0.013}_{-0.012}$	$0.270 \rightarrow 0.344$	$0.270 \rightarrow 0.344$
$\theta_{12}/^\circ$	$33.48^{+0.78}_{-0.75}$	$31.29 \rightarrow 35.91$	$33.48^{+0.78}_{-0.75}$	$31.29 \rightarrow 35.91$	$31.29 \rightarrow 35.91$
$\sin^2 \theta_{23}$	$0.452^{+0.052}_{-0.028}$	$0.382 \rightarrow 0.643$	$0.579^{+0.025}_{-0.037}$	$0.389 \rightarrow 0.644$	$0.385 \rightarrow 0.644$
$\theta_{23}/^\circ$	$42.3^{+3.0}_{-1.6}$	$38.2 \rightarrow 53.3$	$49.5^{+1.5}_{-2.2}$	$38.6 \rightarrow 53.3$	$38.3 \rightarrow 53.3$
$\sin^2 \theta_{13}$	$0.0218^{+0.0010}_{-0.0010}$	$0.0186 \rightarrow 0.0250$	$0.0219^{+0.0011}_{-0.0010}$	$0.0188 \rightarrow 0.0251$	$0.0188 \rightarrow 0.0251$
$\theta_{13}/^\circ$	$8.50^{+0.20}_{-0.21}$	$7.85 \rightarrow 9.10$	$8.51^{+0.20}_{-0.21}$	$7.87 \rightarrow 9.11$	$7.87 \rightarrow 9.11$
$\delta_{CP}/^\circ$	306^{+39}_{-70}	$0 \rightarrow 360$	254^{+63}_{-62}	$0 \rightarrow 360$	$0 \rightarrow 360$
$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.50^{+0.19}_{-0.17}$	$7.02 \rightarrow 8.09$	$7.50^{+0.19}_{-0.17}$	$7.02 \rightarrow 8.09$	$7.02 \rightarrow 8.09$
$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.457^{+0.047}_{-0.047}$	$+2.317 \rightarrow +2.607$	$-2.449^{+0.048}_{-0.047}$	$-2.590 \rightarrow -2.307$	$\left[+2.325 \rightarrow +2.599 \right]$ $\left[-2.590 \rightarrow -2.307 \right]$

3. Neutrino Masses & LNV

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...this question is intimately connected to neutrinos being Dirac or Majorana particles:

DIRAC

$$\nu \neq \bar{\nu}$$



VS.



MAJORANA

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Dirac mass
term \rightarrow 1

:

0

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Just not true....

Correct is:

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→ beyond Feynman diagram level, there exist processes (“sphalerons”) that conserve (B-L) but violate (B+L)

→ lepton number is **NOT** sacrosanct

3. Neutrino Masses & LNV

Thus, new physics beyond the SM generically violates lepton number:

- e.g. triplet Yukawa coupling:

$$\mathcal{L}_{Y_T} = -\bar{L} i \sigma_2 T y_T L^c + h.c.$$



Each has lepton number +1

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- right-handed neutrinos can form a so-called **Majorana mass term**:

$$\mathcal{L}_M = -\frac{1}{2} \overline{(\nu_R)^c} M_R \nu_R + h.c.$$


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3. Neutrino Masses & LNV

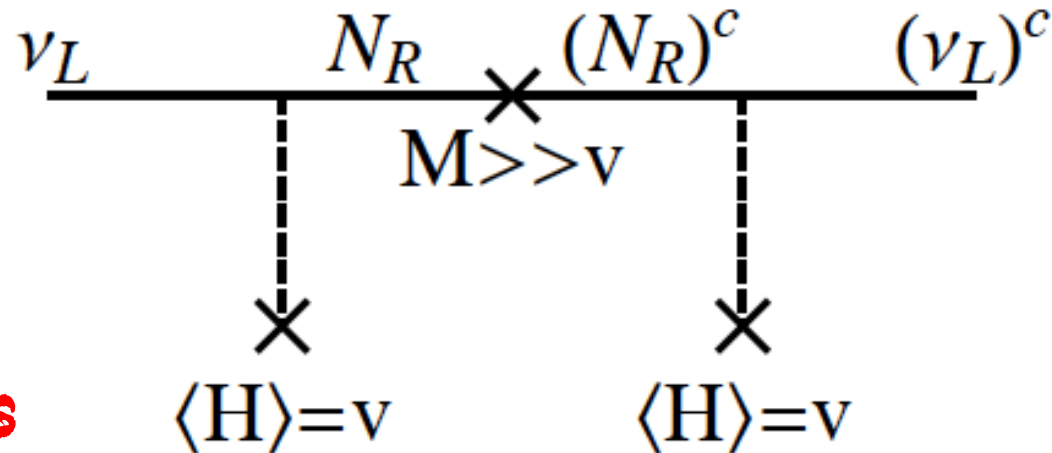
The latter possibility is often used to “explain” why neutrino masses are so small:

LH and RH neutrinos

$$\mathcal{L}_\nu = -\frac{1}{2}(\overline{\nu_L}, \overline{(N_R)^c}) \begin{pmatrix} 0 & m_D \\ m_D^T & M_R \end{pmatrix} \begin{pmatrix} (\nu_L)^c \\ N_R \end{pmatrix} + h.c.$$

$$m_\nu = -m_D M_R^{-1} m_D^T$$

Effectively, large
RH neutrino masses
“suppress” light LH
neutrino masses



“SEESAW MECHANISM”

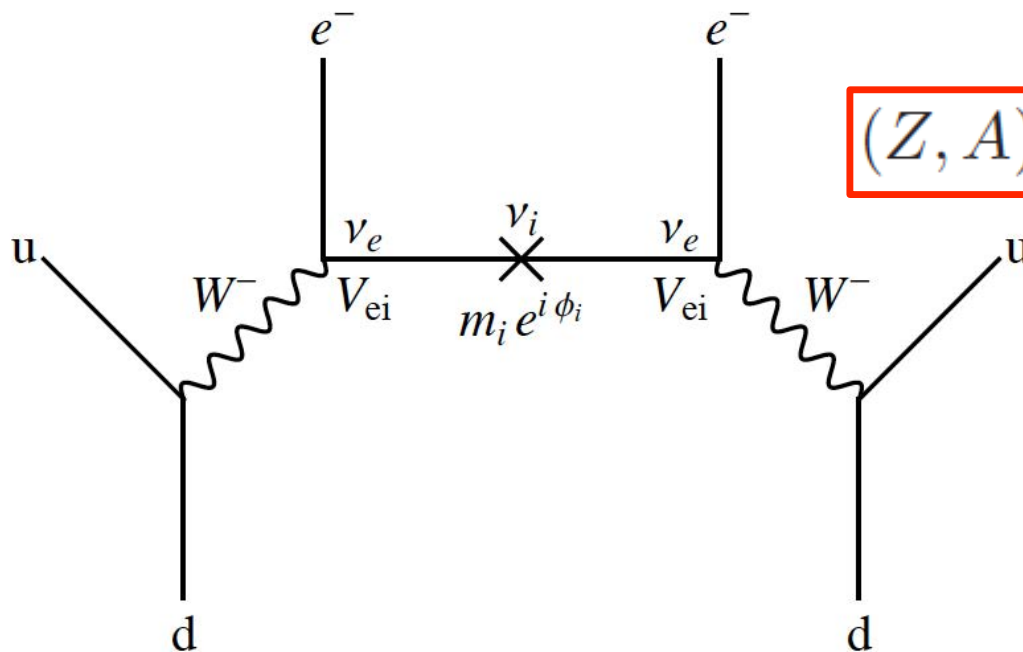
3. Neutrino Masses & LNV

Experimental consequences: LNV processes

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Experimental consequences: LNV processes

- *neutrinoless double beta decay* ($0\nu\beta\beta$)



$$(Z, A) \rightarrow (Z + 2, A) + e^- + e^-$$

Clearly violates
lepton number
by two units

→ THE REASON WE ARE HERE THIS WEEK!!!

3. Neutrino Masses & LNV

Experimental consequences: LNV processes

- **neutrinoless double beta decay ($0\nu\beta\beta$)**
- **μ^-e^+ conversion in muonic atoms**
 - ... also violates lepton number by two units
 - ... great experimental advances expected
- **(di-)muonium conversion**
 - ... leptonic bound states (e.g. $e^+\mu^-$)
 - ... quite generically hard to measure
- **lepton number violating processes at future lepton colliders (e.g. $e^+e^+ \rightarrow l^-l^- + 4W^+$)**
 - ... may be an interesting route to go

3. Neutrino Masses & LNV

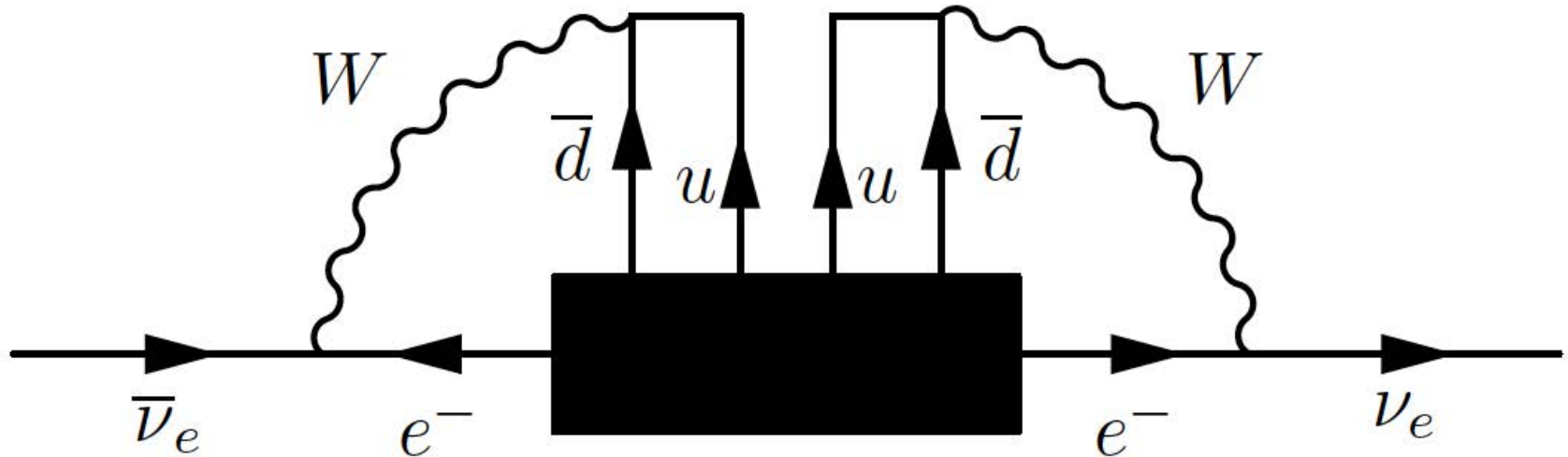
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[Schechter, Valle: Phys.
Rev. D25 (1982) 2951]

**Schechter-Valle theorem: ANY $0\nu\beta\beta$ -operator
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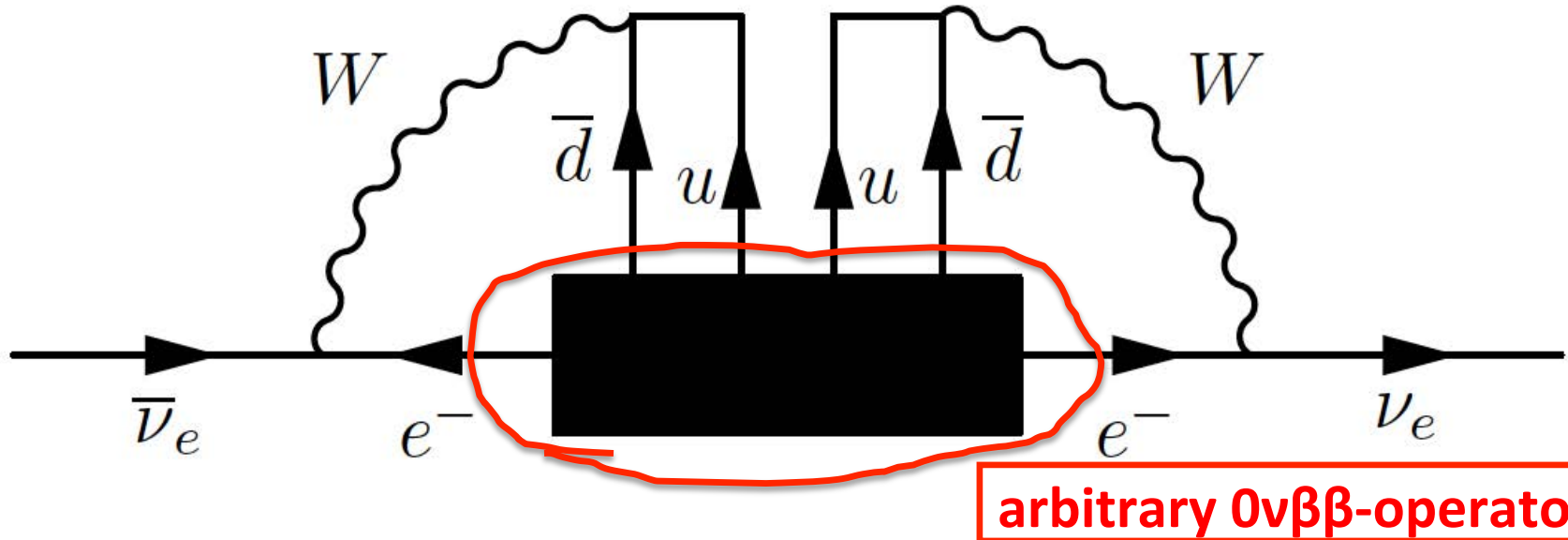


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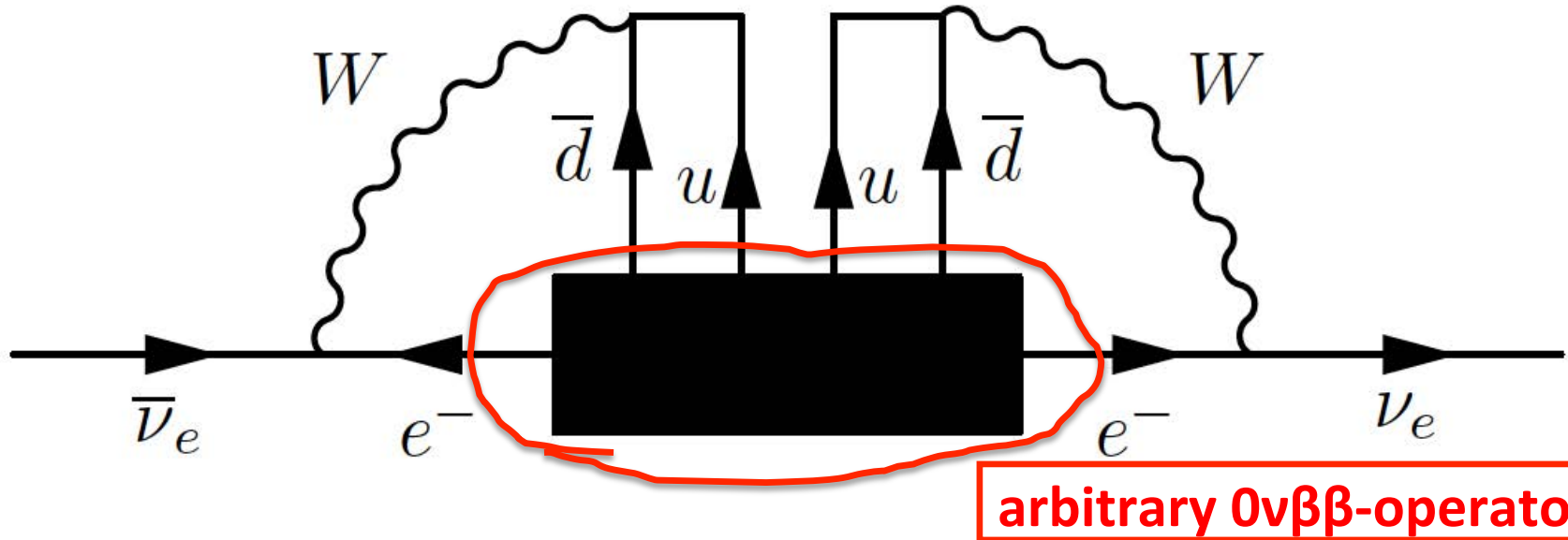


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TRUE... unless the operator is $\bar{u}P_L d \bar{u}P_L d \bar{e}P_L e^c$
... then the mass contribution is zero!!!

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Drawing a Feynman
diagram is just not
enough to derive very
strong conclusions!

arbitrary $0\nu\beta\beta$ -operator

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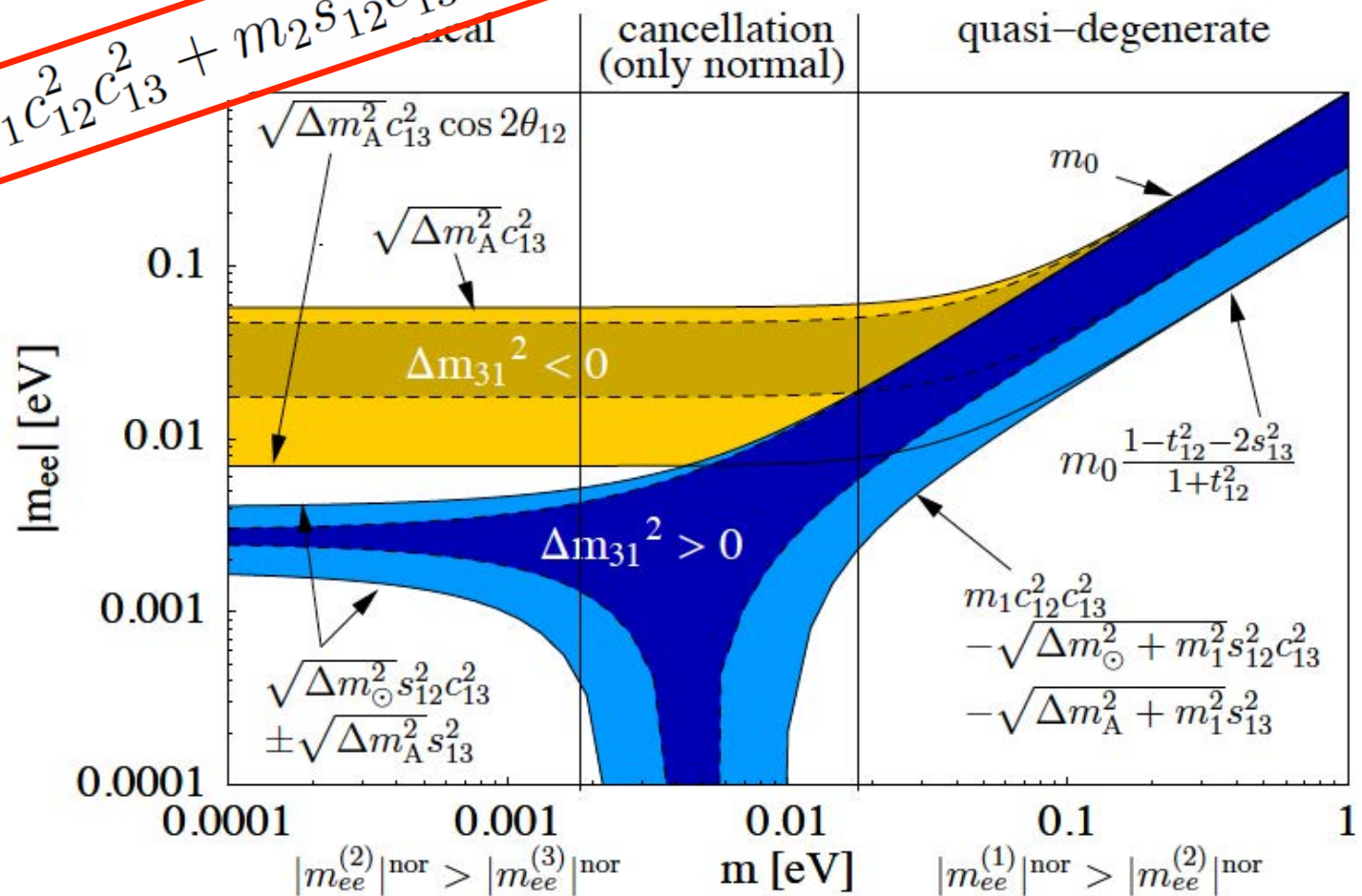
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IF $\nu\nu\beta\beta$ is mediated by light neutrino exchange, **THEN** the amplitude constrains the effective neutrino mass $|m_{ee}|$:

$$|m_{ee}|_{\text{PDG}} = |m_1 c_{12}^2 c_{13}^2 + m_2 s_{12}^2 c_{13}^2 e^{i\alpha_{21}} + m_3 s_{13}^2 e^{i(\alpha_{31}-2\delta)}|$$



[Lindner, AM,
Rodejohann:
Phys. Rev. **D73**
(2006) 053005]

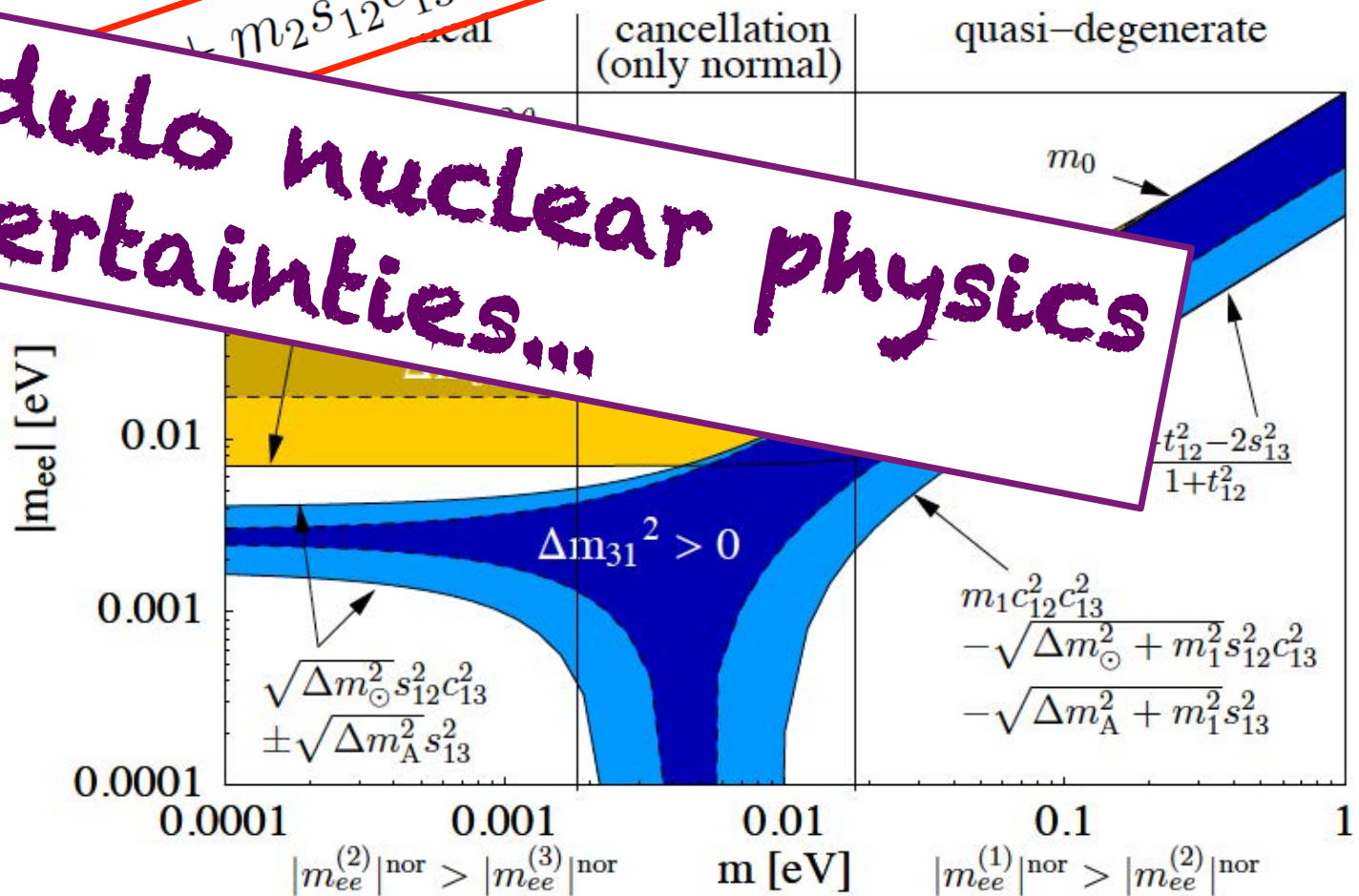
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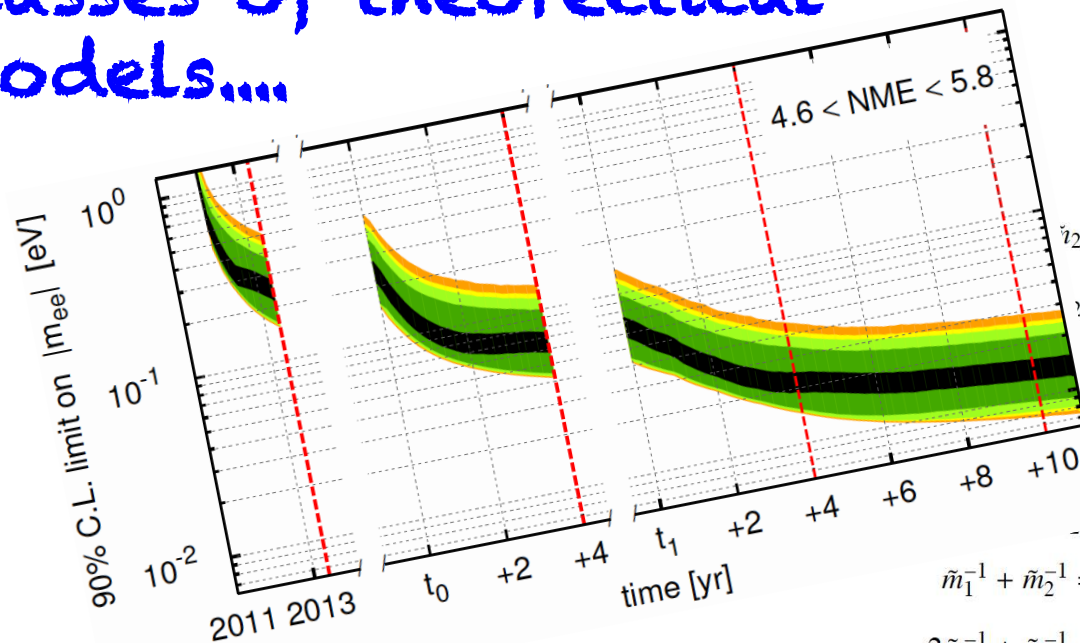
Modulo nuclear uncertainties...

[Lindner, AM,
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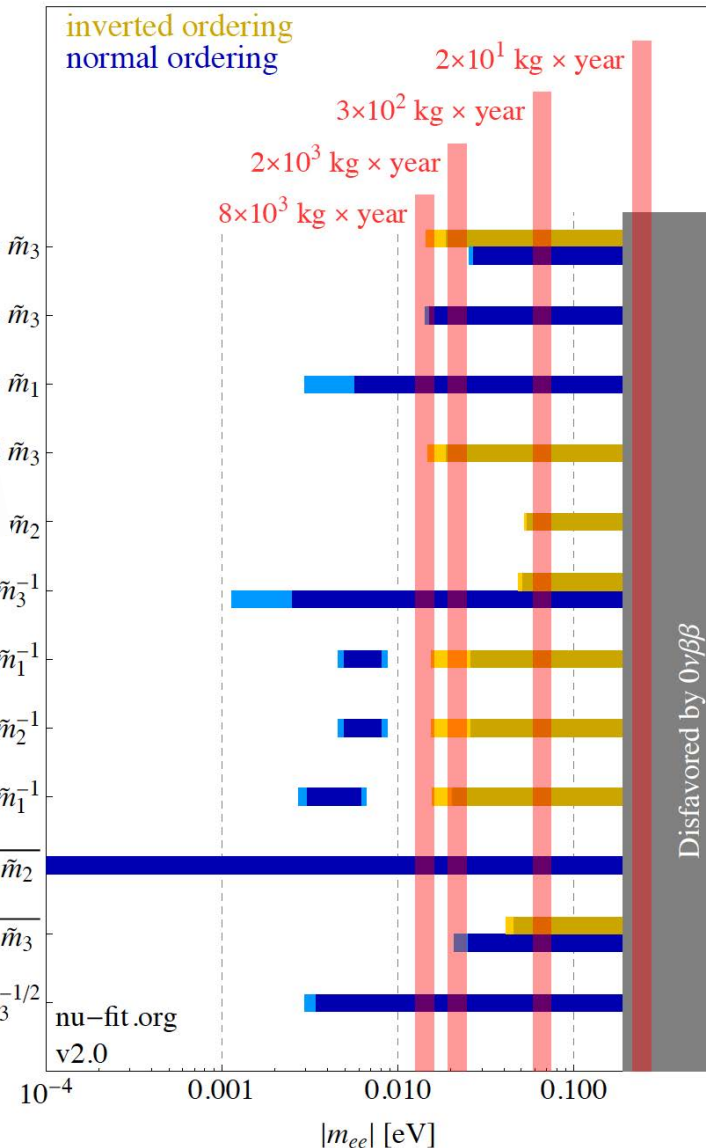
3. Neutrino Masses & LNV

In the long run, we may nevertheless probe classes of theoretical models....



... in particular if theorists and experimentalists collaborate!!!

$$\begin{aligned} \tilde{m}_1^{-1} + \tilde{m}_2^{-1} &= \tilde{m}_3^{-1} \\ 2\tilde{m}_2^{-1} + \tilde{m}_3^{-1} &= \tilde{m}_1^{-1} \\ \tilde{m}_1^{-1} + \tilde{m}_3^{-1} &= 2\tilde{m}_2^{-1} \\ \tilde{m}_3^{-1} \pm 2i\tilde{m}_2^{-1} &= \tilde{m}_1^{-1} \\ \sqrt{\tilde{m}_1} \pm \sqrt{\tilde{m}_3} &= 2\sqrt{\tilde{m}_2} \\ \sqrt{\tilde{m}_1} &= 3\sqrt{\tilde{m}_2} + 3\sqrt{\tilde{m}_3} \\ \tilde{m}_1^{-1/2} + \tilde{m}_2^{-1/2} &= 2\tilde{m}_3^{-1/2} \end{aligned}$$



5. Conclusions

- **Neutrinos...** probably hold mysteries because they just seem not to be like SM-fermions
- **Neutrino mixing...** is experimentally established and suggests to go even further
- **Neutrinoless double beta decay...** *would revolutionise the field if seen*

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 - **Neutrino mixing...** is experimentally established and suggests to go even further
 - **Neutrinoless double beta decay...** would revolutionise the field if seen
- ... so please do your best!!! ;-)



**THANK
YOU!!!**