

TRACKING EFFICIENCY DEFINITION

outline

- ★ the problem & the plan
- ★ the idea
- ★ current results
- ★ conclusions

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BelleII Face2Face Tracking Meeting ~ April, 22nd 2015

Definition of the Problem

- ➔ We need to better define our goal in terms of pattern recognition efficiency
- ➔ Not all tracks are the same: there are tracks that are *easy* to find and tracks that are *harder* to find
- ➔ The efficiency that we can reasonably achieve on tracks that are *easy* to find must be higher than the efficiency on tracks that are *hard* to find
- ➔ Let's classify the tracks in three categories:
 - ▶ tracks that are *easy to find* → very high efficiency (let's say 1)
 - ▶ tracks that are *hard to find* → lower (how much?) efficiency
 - ▶ tracks that are *very hard to find* → happier if we find it, happy anyway

The Project

- ➔ Develop a module to be placed after the TrackFinderMCTruth that produces 3 subsets of MCTrackCands:
 - tracks easy to find → easyMCTrackCands
 - tracks hard to find → hardMCTrackCands
 - tracks very hard to find → veryhardMCTrackCands
- ➔ Estimate our pattern recognition efficiencies on the three lists separately
- ➔ The VXD and CDC pattern recognition modules will have separate lists
 - problems for VXD are not the ones of the CDC and vice-versa
 - what is easy to find for the VXD can be hard for the CDC and vice-versa
- ➔ The question is: how do we decide to which category a track belongs
 - I've first focused on the VXD



TrackFinderMCTruth (1)

current PR efficiency definition:

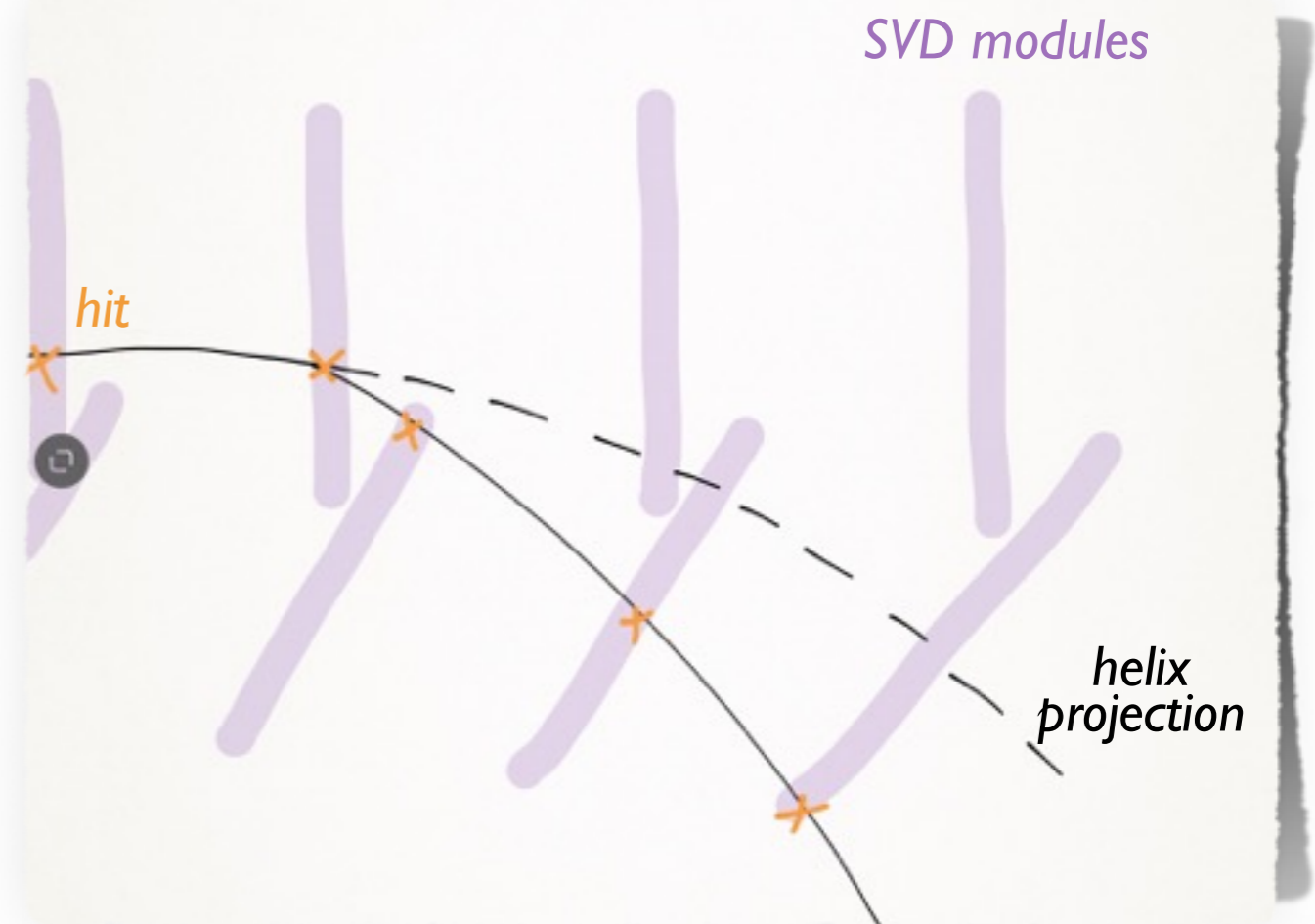
$$\epsilon_{PR} = \frac{\# \text{ MCTrackCand with at least one associated TrackCand}}{\# \text{ MCTrackCand}}$$

TrackFinderMCTruth:

- ✓ factors out geometrical acceptance
- ✓ factors out detector inefficiencies
- ✓ requires a minimum number of hits
- ✓ (set relations with MCParticles)

BUT it does not handle:

- ⦿ kinks & large multiple scattering
- ⦿ tracking volume covering only partially the helix
- ⦿ hits in both outgoing and ingoing helix arms



TrackFinderMCTruth (2)

current PR efficiency definition:

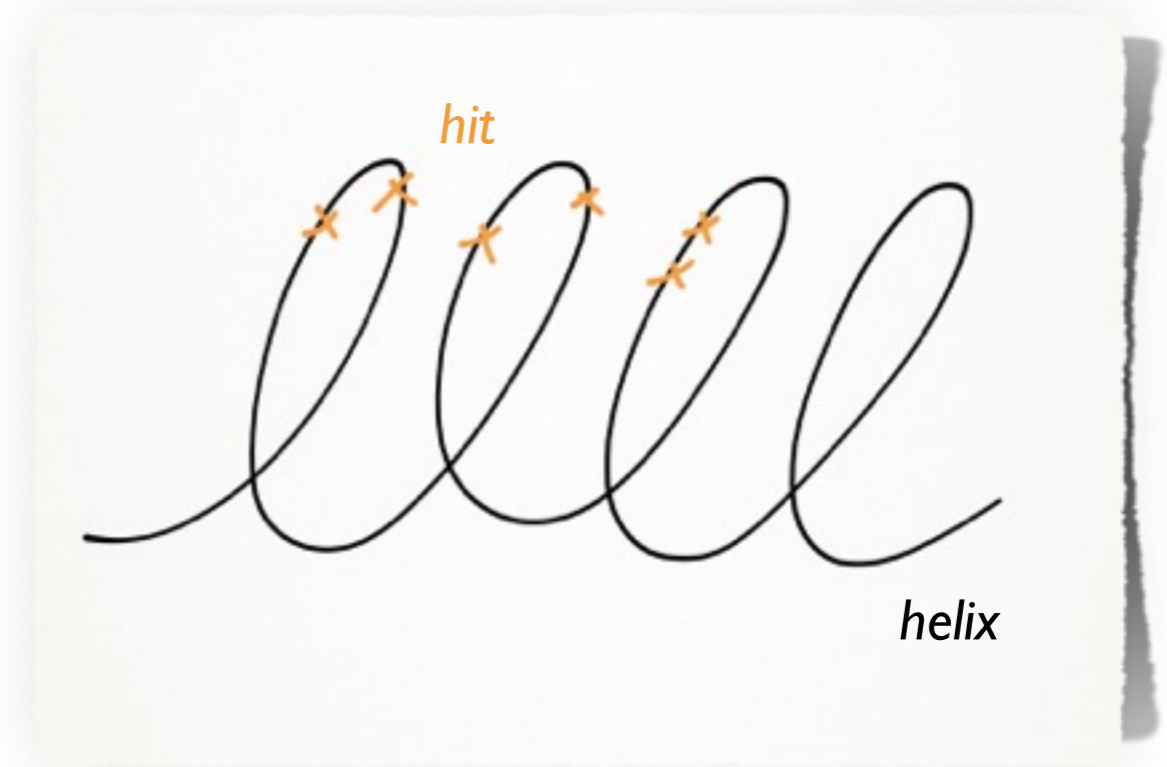
$$\epsilon_{PR} = \frac{\# \text{ MCTrackCand with at least one associated TrackCand}}{\# \text{ MCTrackCand}}$$

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TrackFinderMCTruth (3)

current PR efficiency definition:

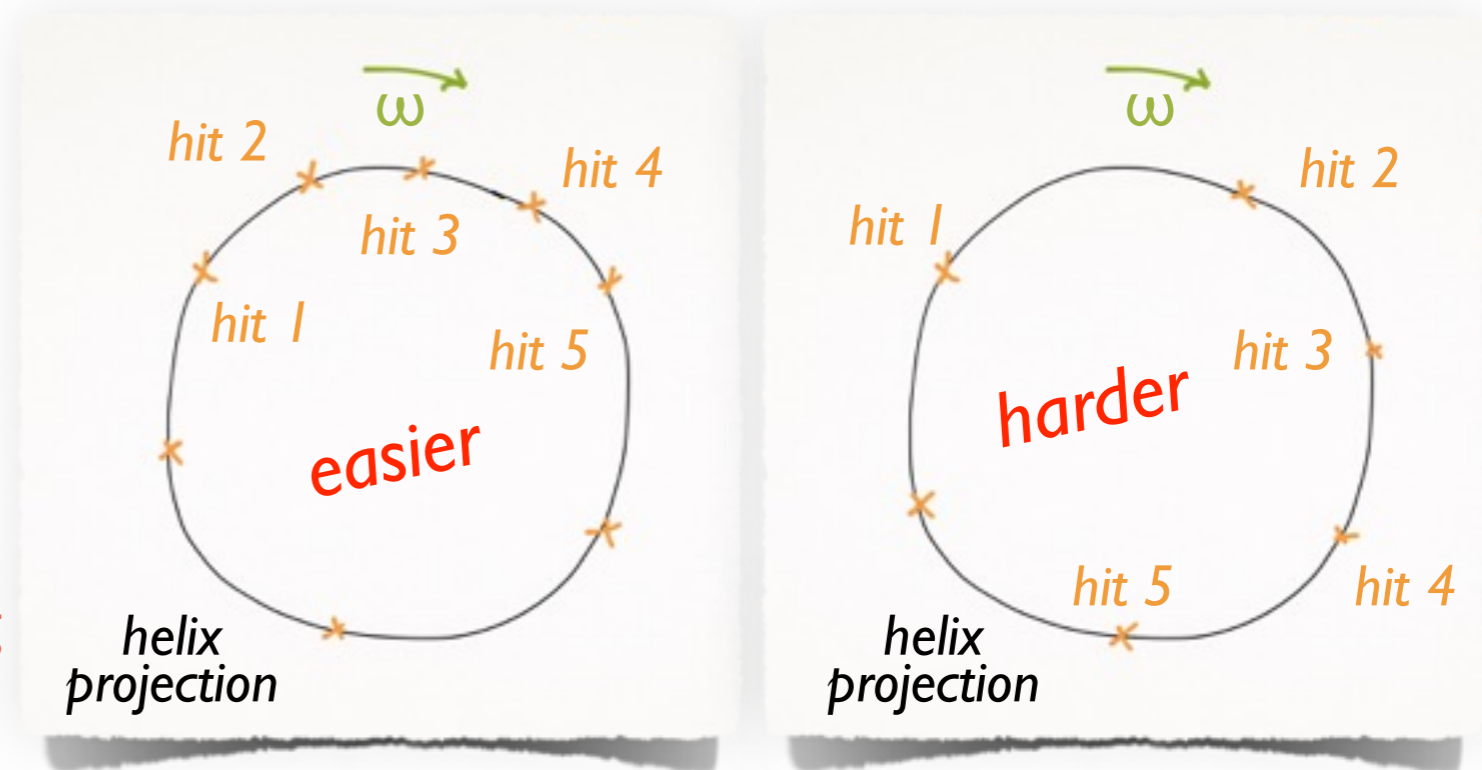
$$\epsilon_{PR} = \frac{\# \text{ MCTrackCand with at least one associated TrackCand}}{\# \text{ MCTrackCand}}$$

TrackFinderMCTruth:

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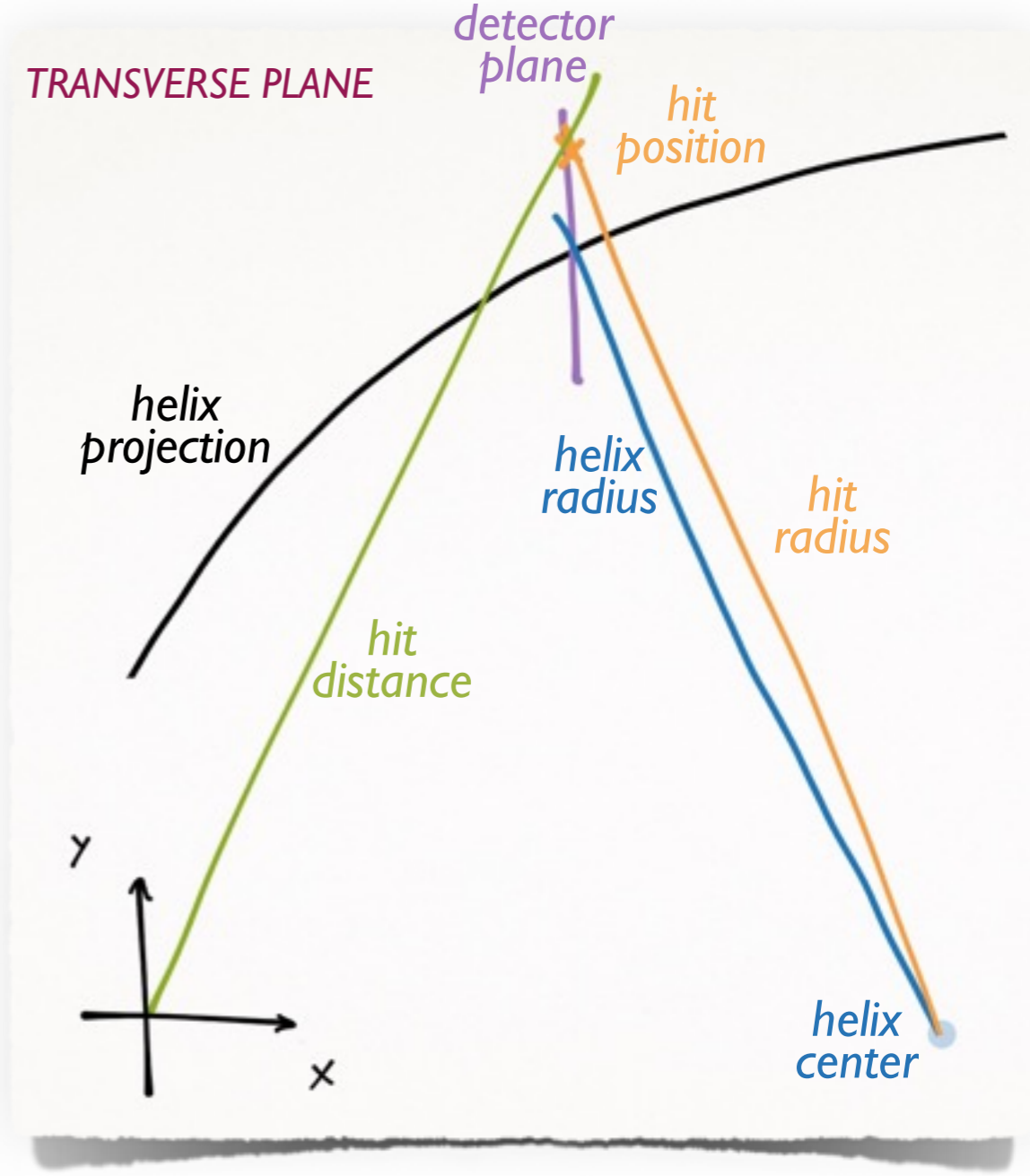
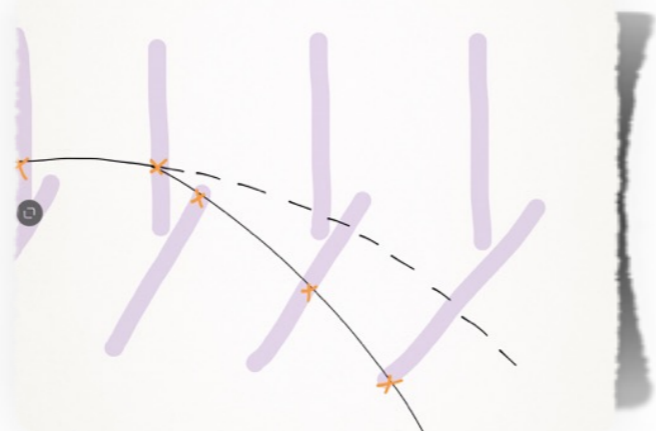
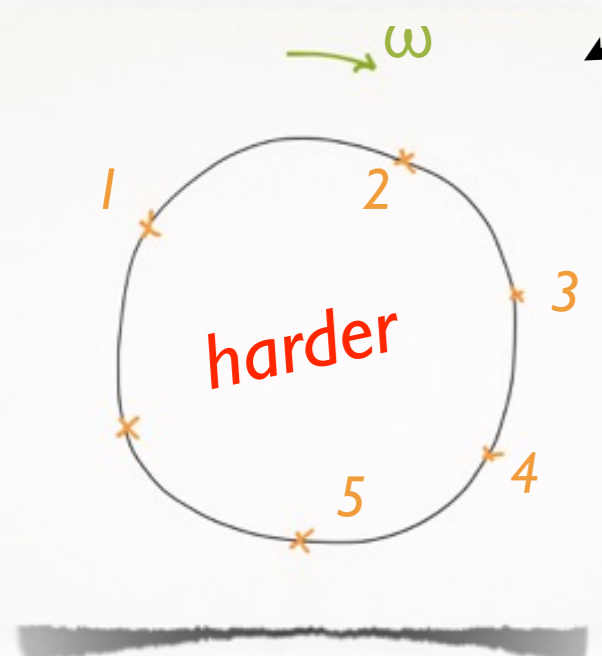
BUT it does not handle:

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Current Status

- ➔ There maybe other classes of “MCTrackCands that are not easy to find”
- ➔ I have developed 2 criteria to reject non-easy-to-find MCTrackCands shown in the previous slides



- ➔ NOTE: the geometry of the problem is complicated, but I have tried to limit the numbers of degrees of freedom:
 - ▶ work on the transverse plane
 - ▶ hit position (distance from helix center and from 0,0)
 - ▶ helix radius
 - ▶ MCParticle informations

Criteria #1

- predict the position of the next hit on the expected detector plane, taking into account multiple scattering

$$\theta_{MS} = \frac{13.6 \text{ MeV}}{\beta c p} Z \sqrt{\frac{X}{X_0}}$$

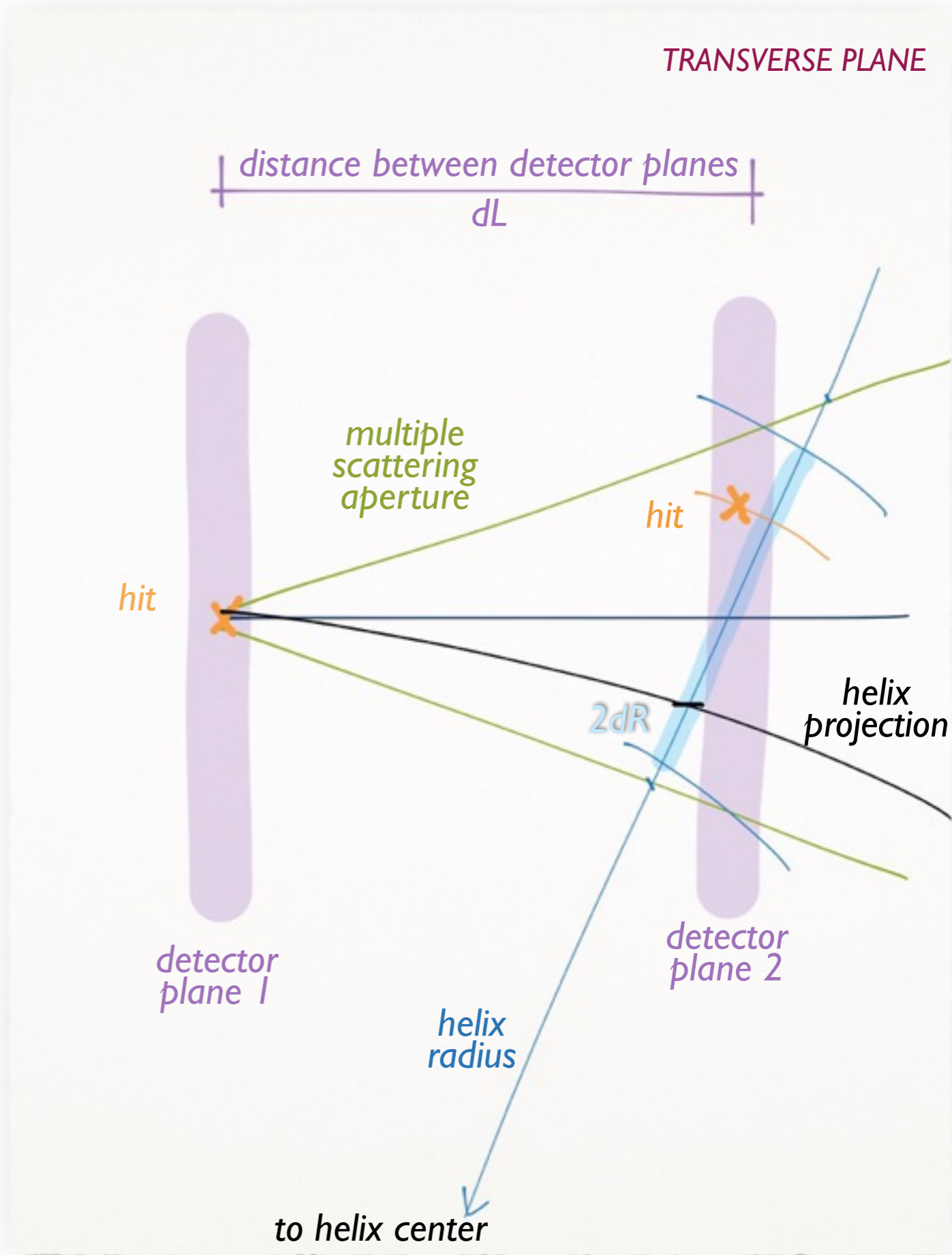
- project the region where the next hit is expected along the helix radius

$$dR = n dL \theta_{MS}$$

- check if the next-hit distance from the helix center (d) lies in the expected region

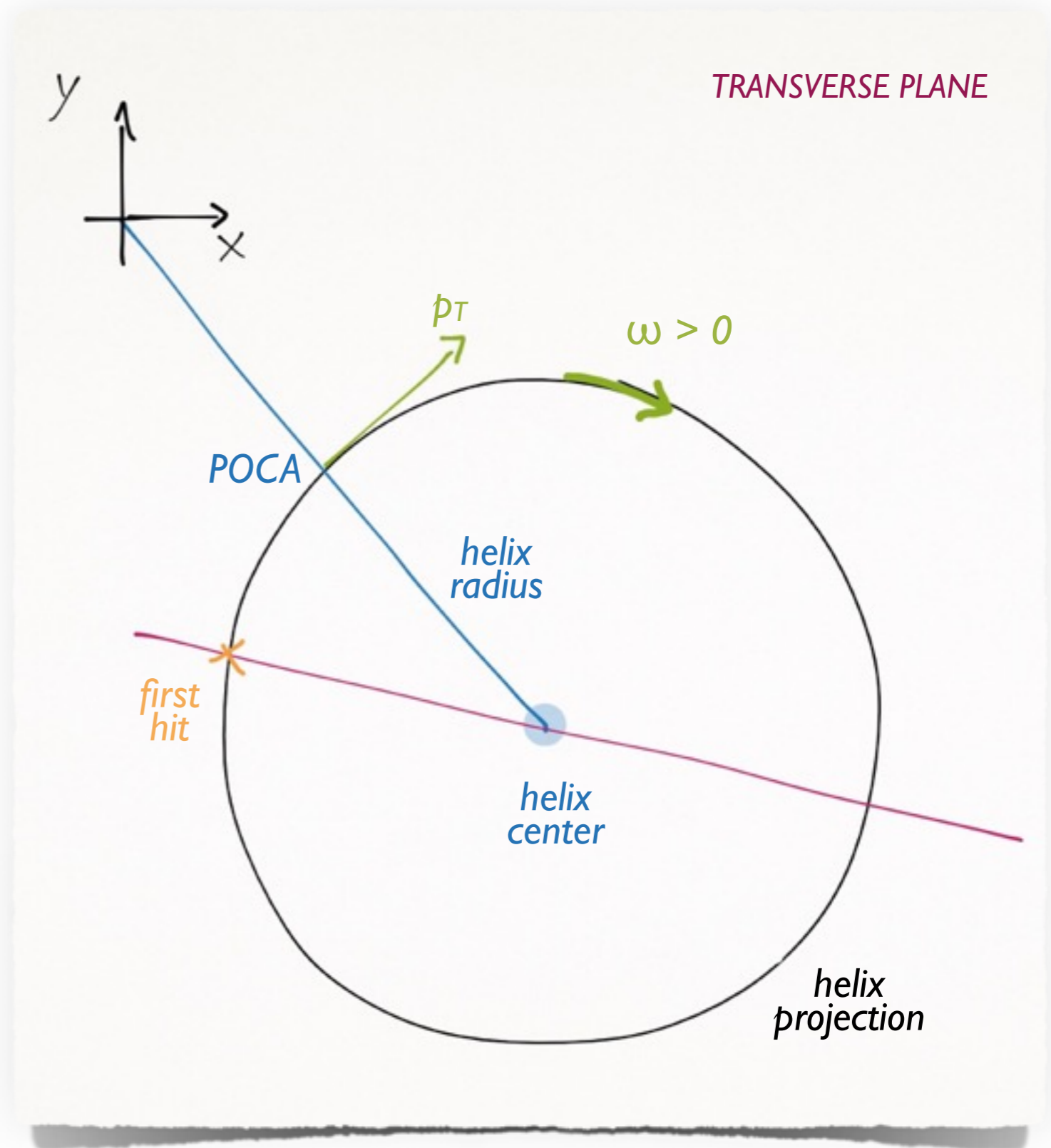
$$|d - R| < dR$$

- If the hit satisfies the criteria, check the next criteria (next slide), otherwise move to the next MCTrackCand



Criteria #2

- ➔ divide the transverse plane into 2 regions given the first hit and the p_T at POCA
- ➔ given the curvature ω and the relative position between the first hit and the helix center, predict the semi-plane where the next hit is expected to be
- ➔ if the next hit belongs to the expected semi-plane, accept the hit and move to the next one (criteria #1), otherwise move to the next MCTrackCand

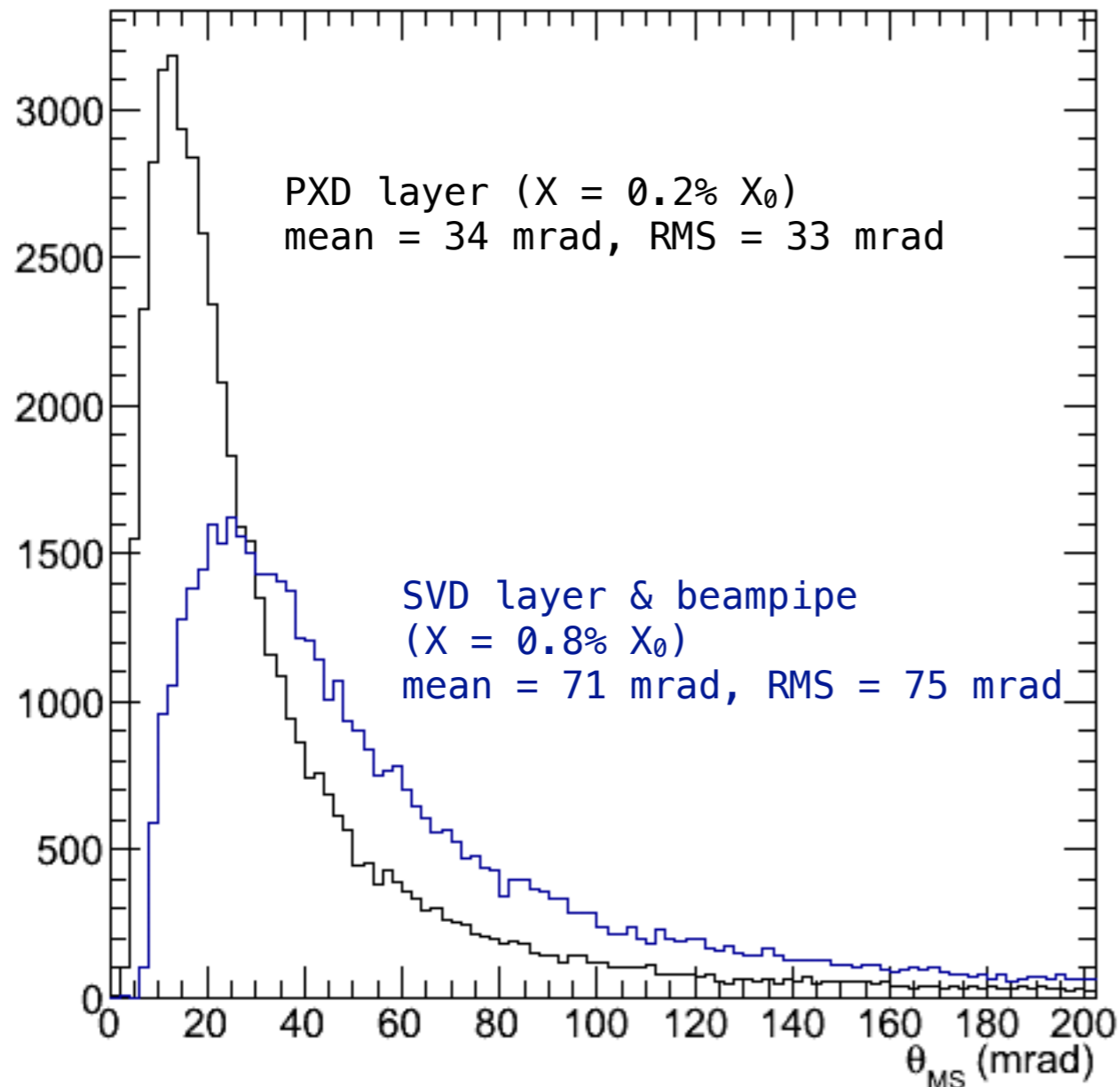


Selection Sequence

- ➔ TrackFinderMCTruth produces the list of MCTrackCands
 - use PXDHits and SVDHits
 - do not use clusters
 - minimum number of one-dimensional hits = 5
- ➔ retrieve the MCParticle related to the MCTrackCand (needed to compute helix radius and θ_{MS})
- ➔ Loop on the TrueHits (PXD and SVD):
 - if the TrueHit satisfies criteria#1 *and* criteria#2 → the hit is accepted
 - otherwise → the hit is rejected & move to the next MCTrackCand
- ➔ If at least 5 TrueHits are accepted → MCTrackCand is classified as *easy-to-find* (easyMCTrackCand)

Multiple Scattering Angle

distribution of θ_{MS} for generic $\Upsilon(4S)$ events



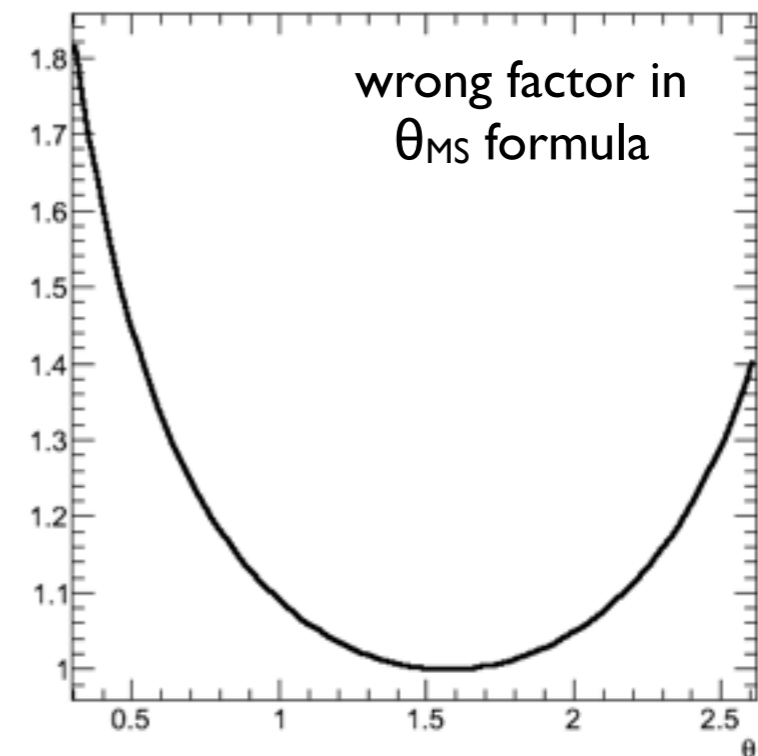
the distribution is ~right within a factor 2 in θ_{MS} .

→ MS angle is computed as

$$\theta_{MC} = \frac{13.6\text{MeV}}{\beta c p_T} Z \sqrt{\frac{X / \sin \theta}{X_0}}$$

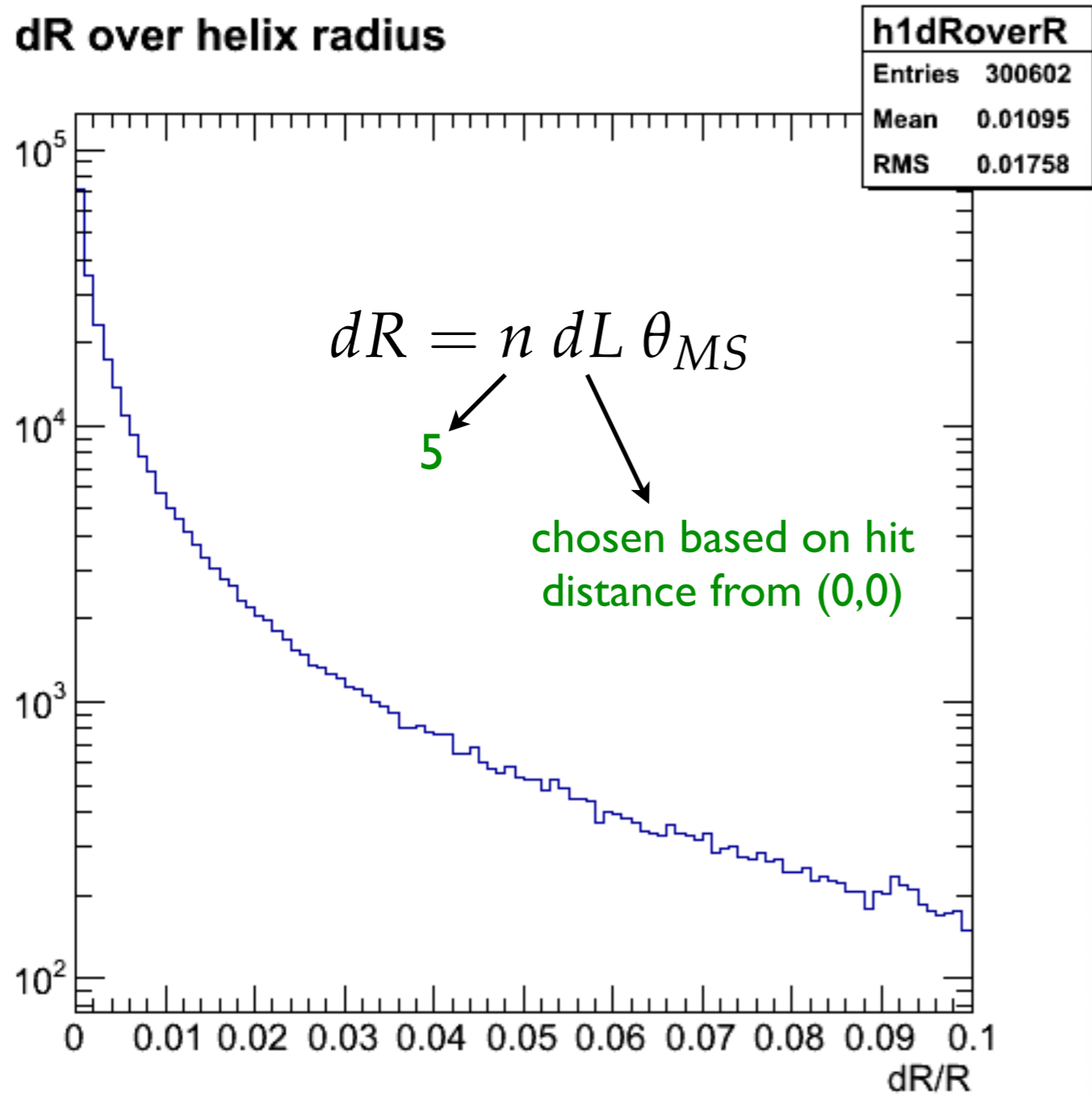
→ polar angle correction is wrong in this study: θ is computed at the vertex, it's not the incident angle on the detector plan

1/TMath::Sqrt(TMath::Sin(θ))

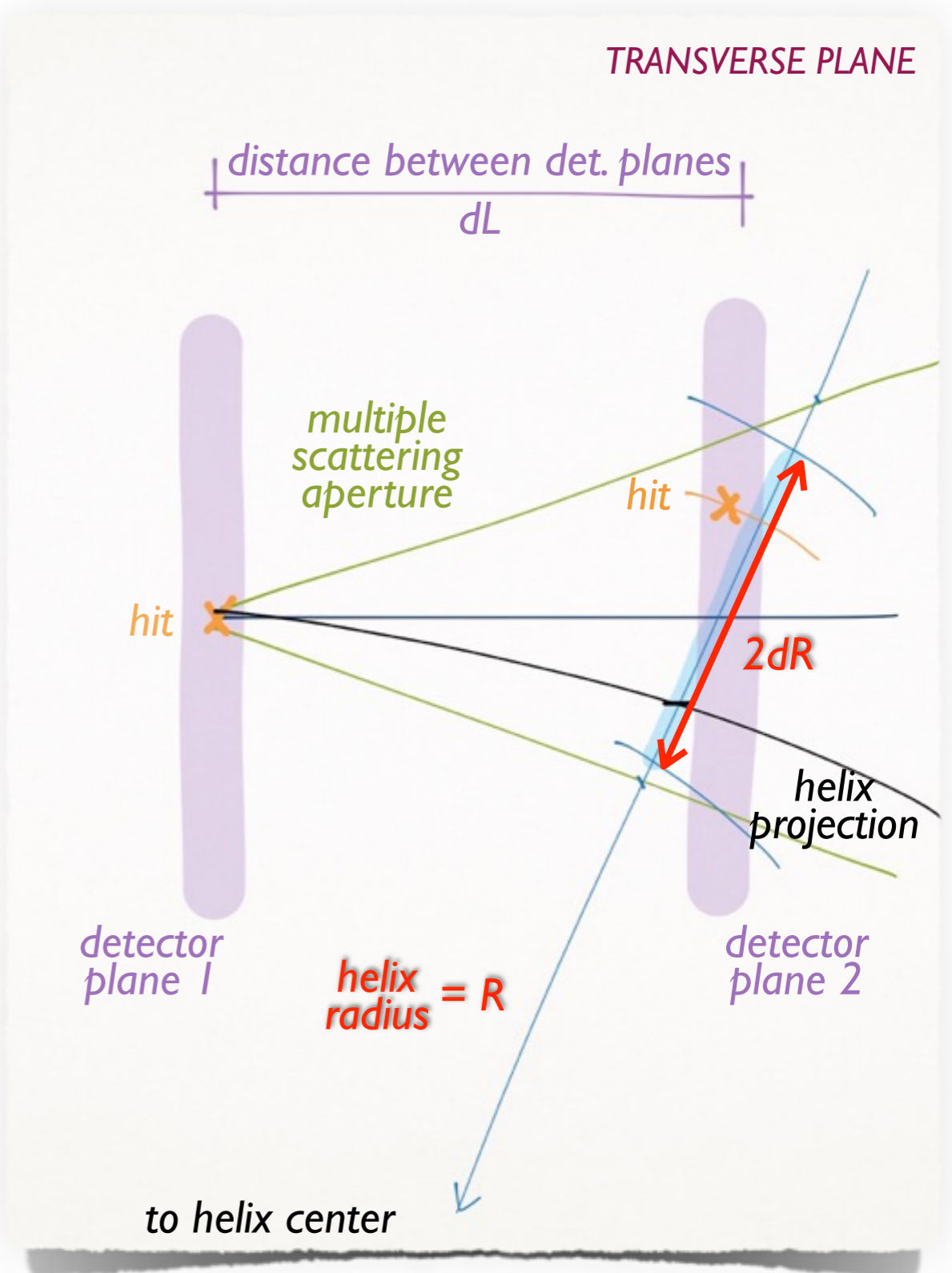


Multiple Scattering Effect

dR over helix radius



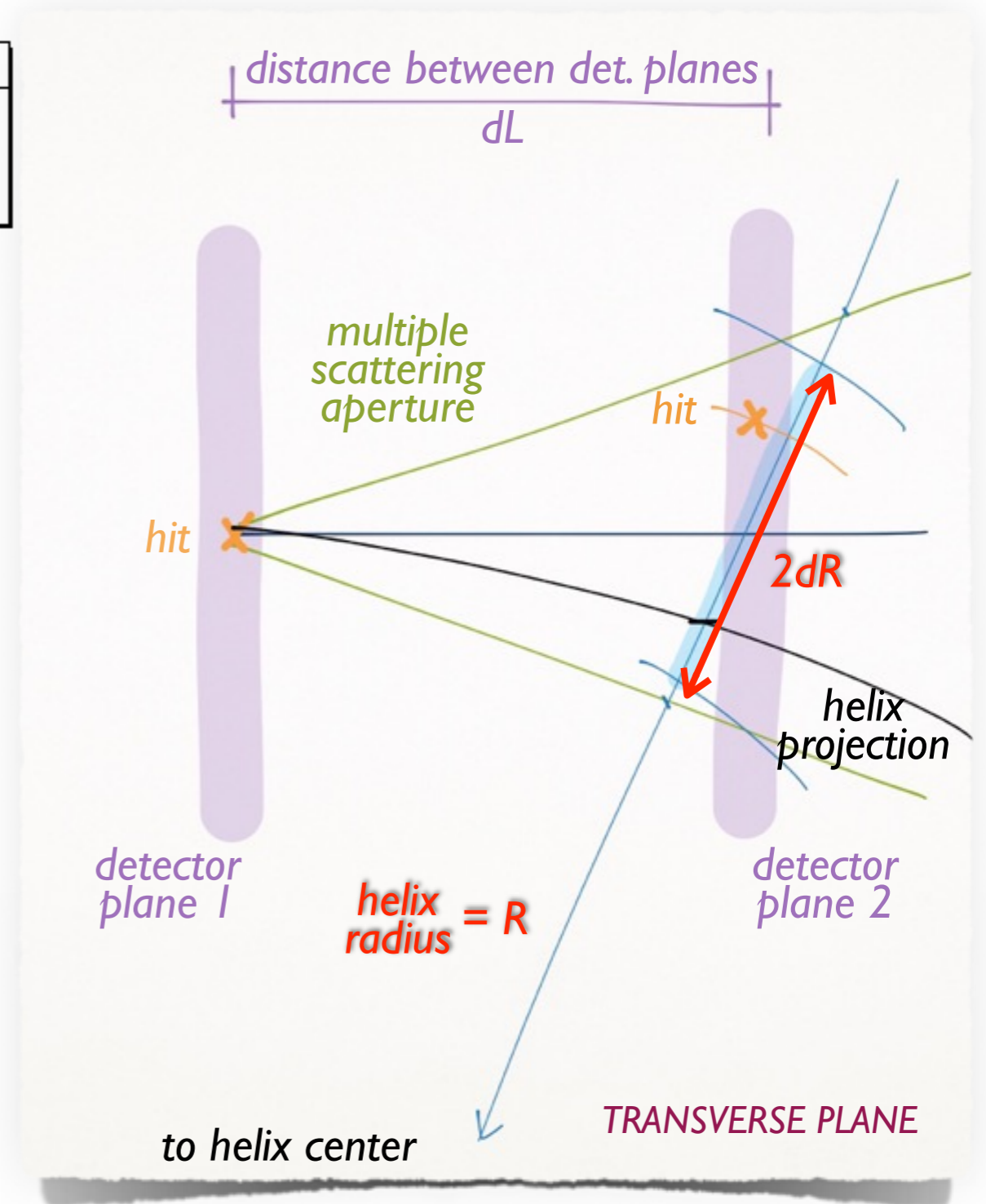
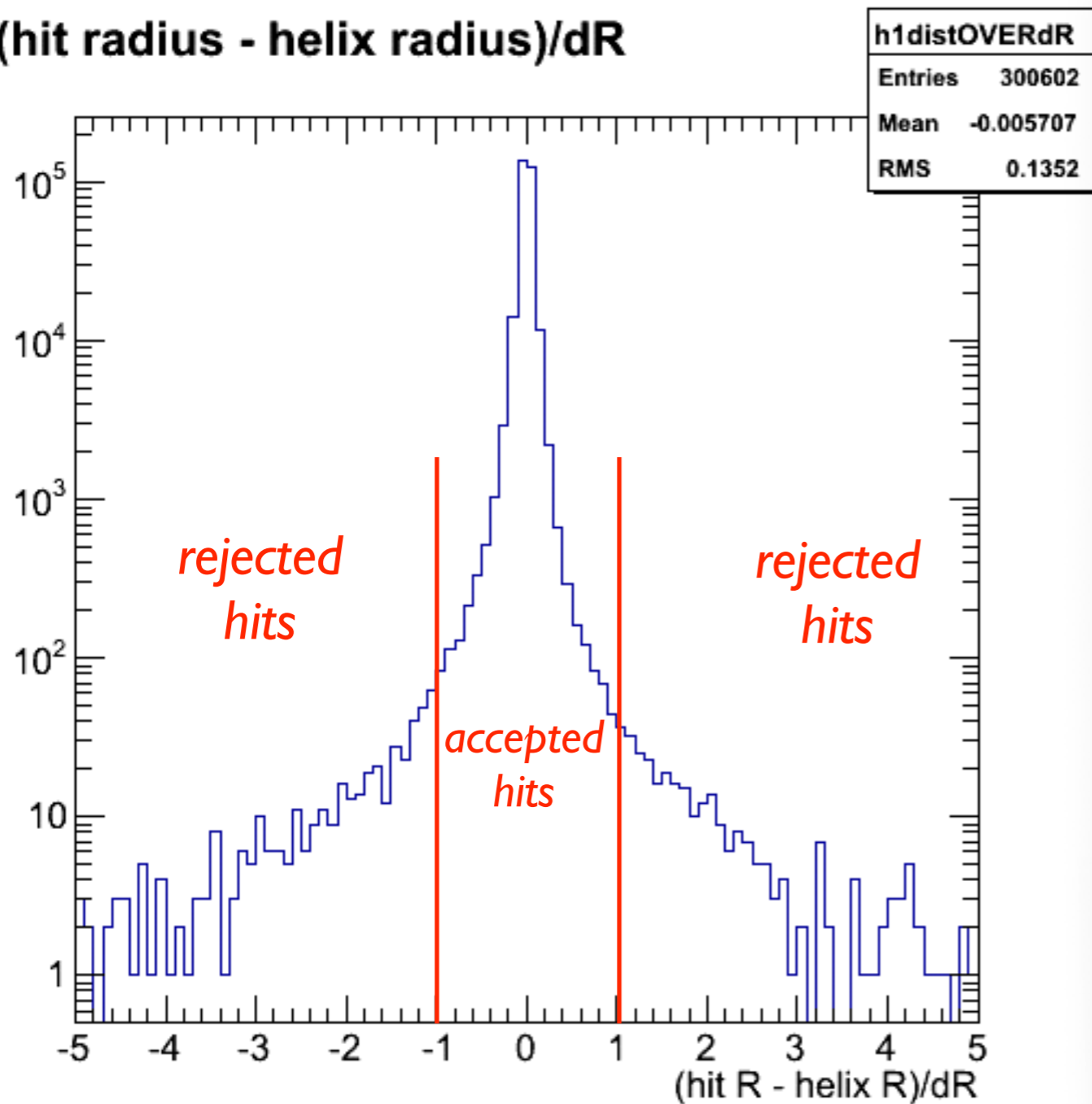
➔ Multiple Scattering perturbs the helix by 1% on average



Criteria #1 at work

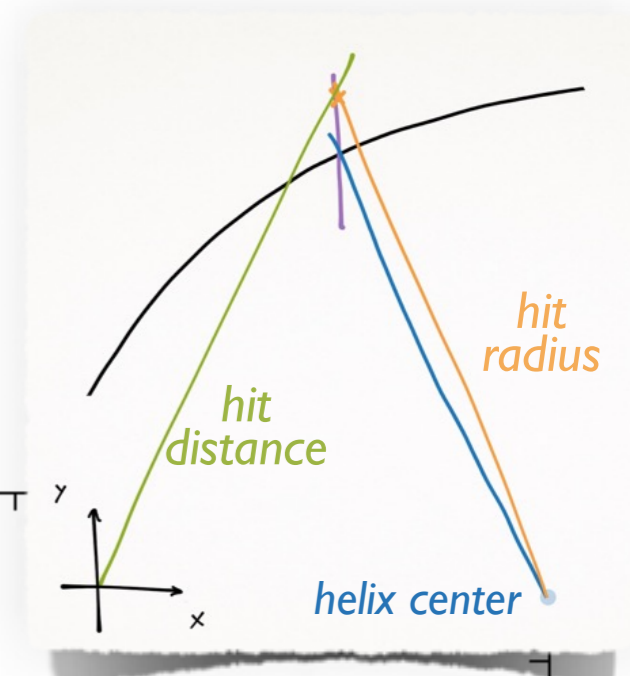
$$|d - R| < dR$$

(hit radius - helix radius)/dR

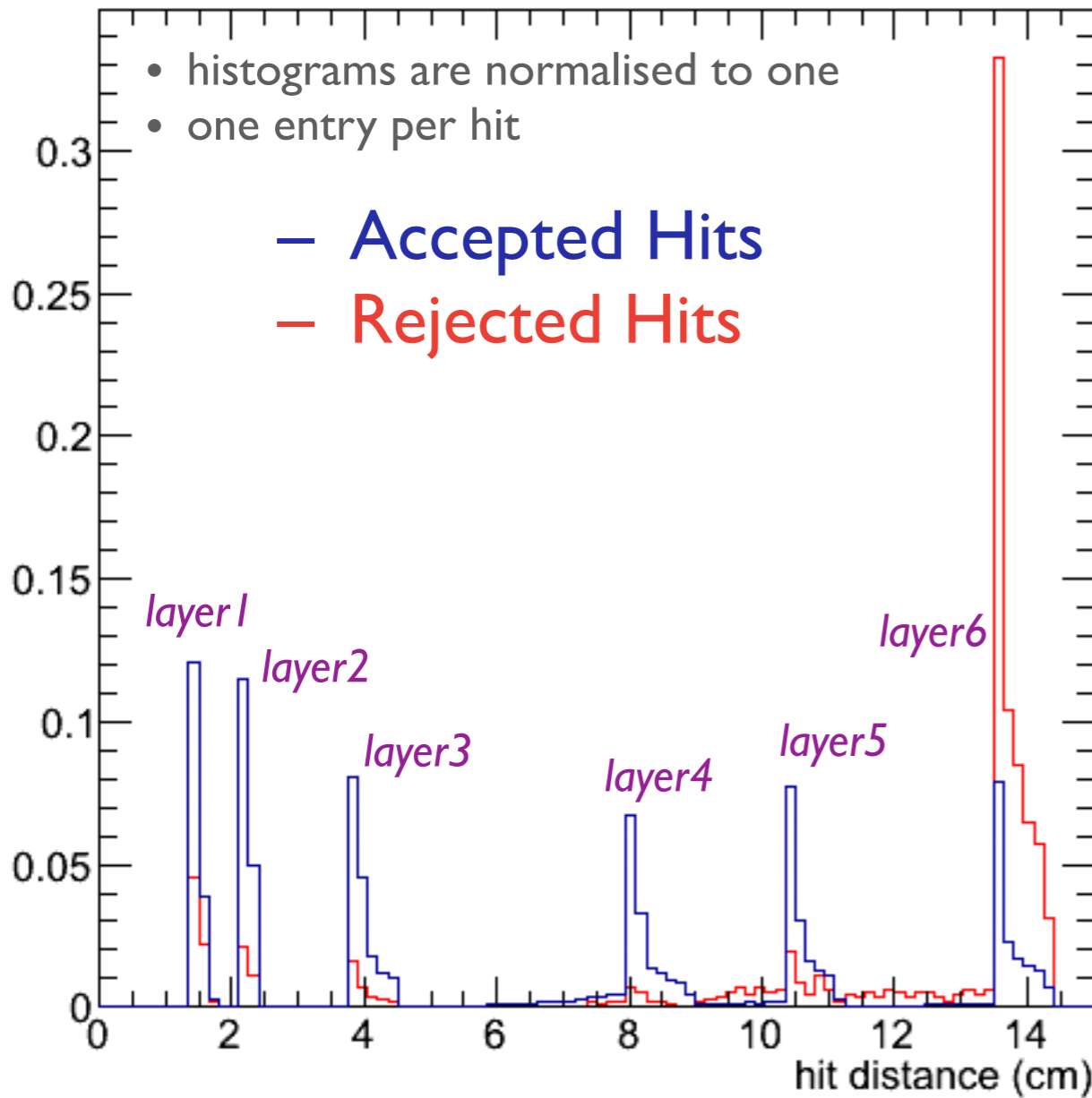


➔ asymmetric distribution, higher left tail since no energy loss taken into account: the correction is symmetric while the physical effect (energy loss) is not.

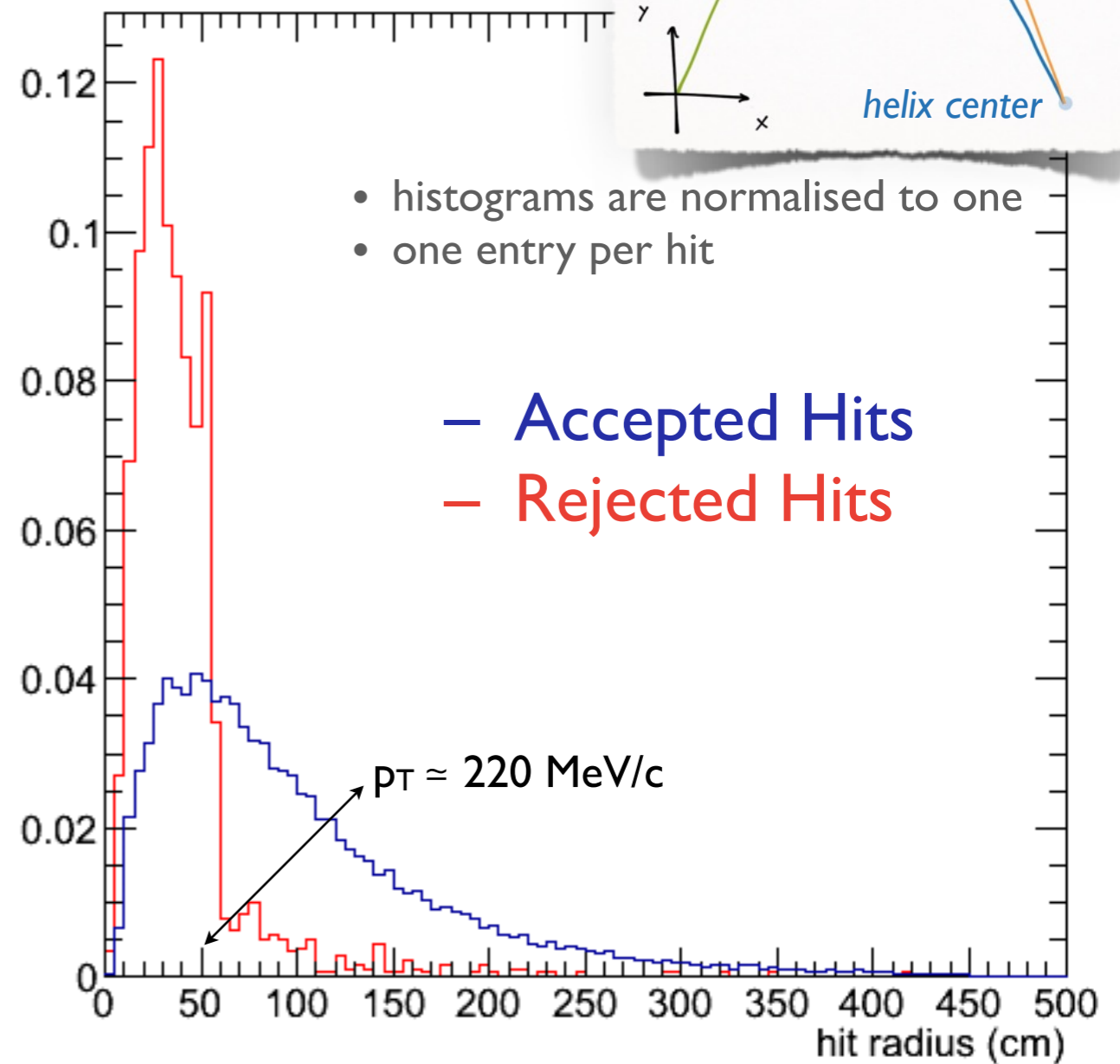
Which Hits are Rejected?



Hit Distance



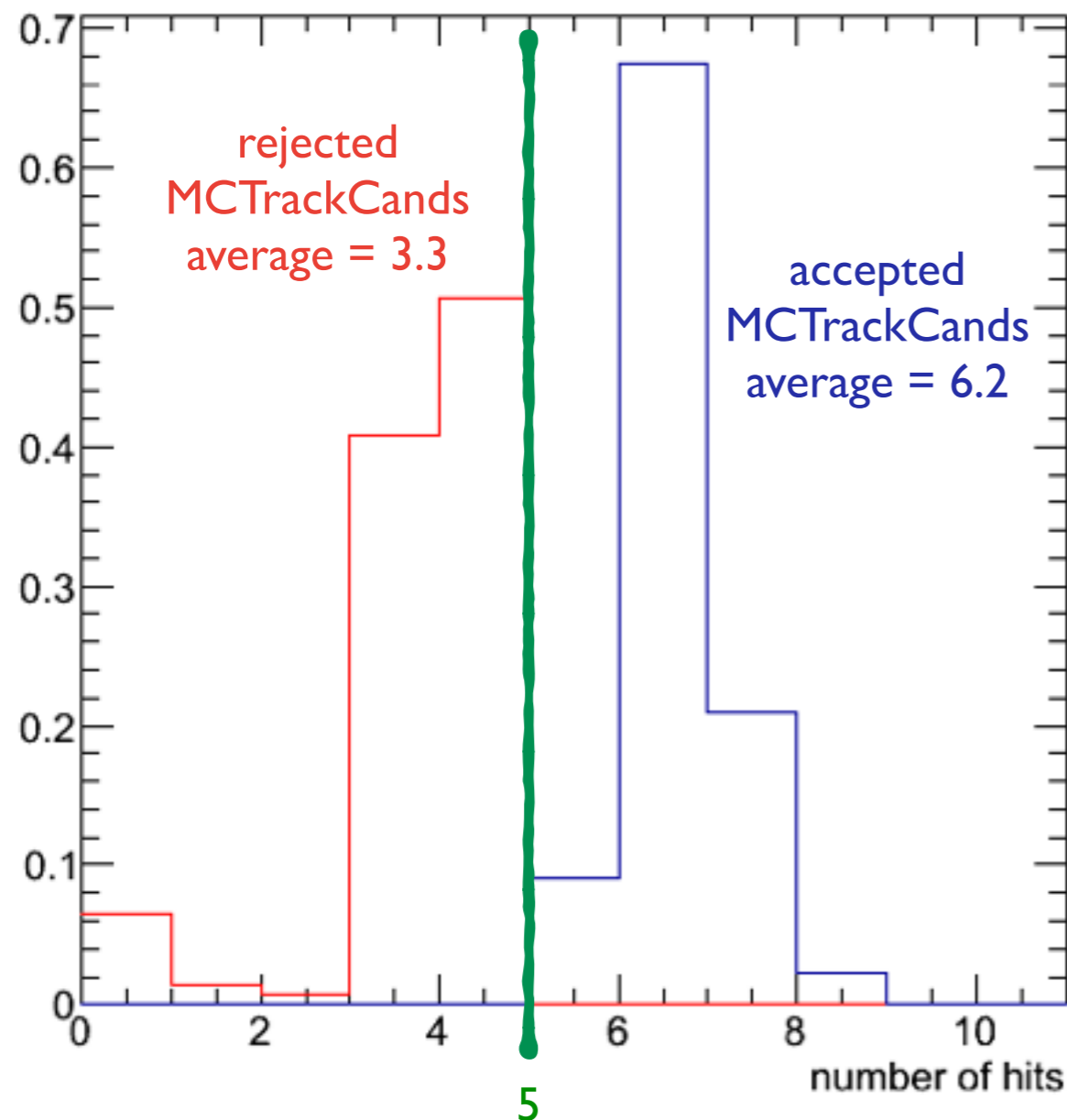
Hit Radius



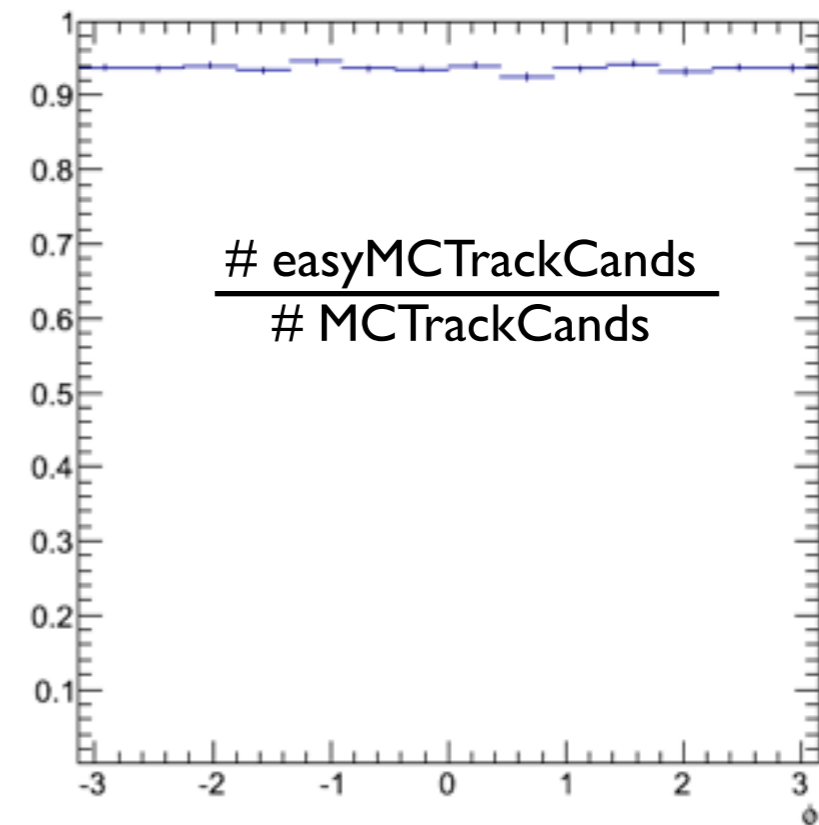
- ➔ Most of the reject hits are in Layer6, and a smaller fraction in the wedge part of the SVD
- ➔ Most of the reject hits belong to low transverse momentum tracks ($R < 70 \text{ cm} \leftrightarrow p_T < 300 \text{ MeV}/c$)

Fraction of easyMCTrackCands/MCTrackCands

Average # Hits per MCTrackCands

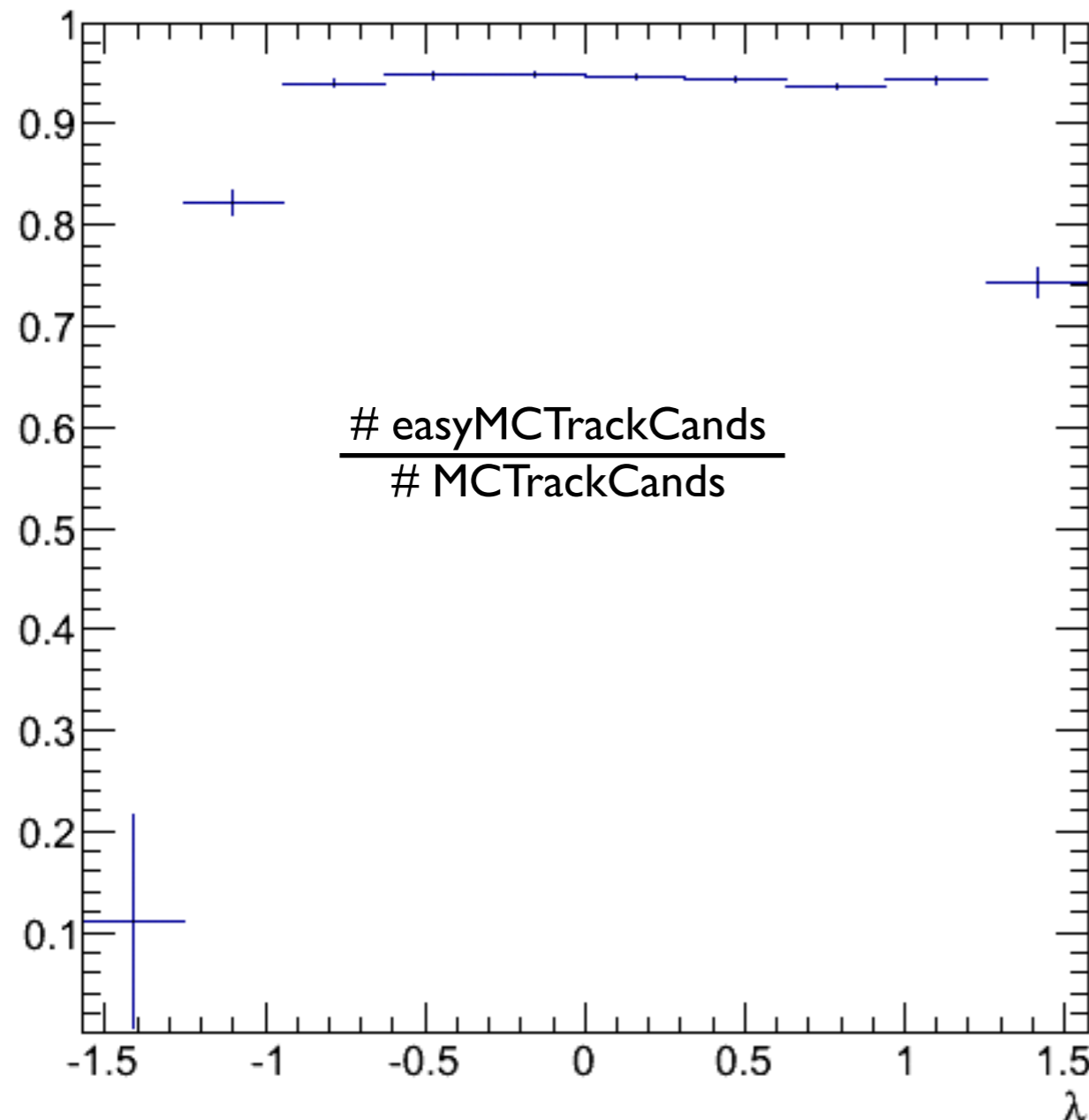


- ➔ 5k $\Upsilon(4S)$ generic decays, Belle II geometry
- ➔ 50k MCTrackCands (PXD&SVD TrueHits, no use of clusters, # of I-D hits > 5)
- ➔ fraction of MCTrackCands classified as *easy to find* = $(93.7 \pm 0.1)\%$, homogeneously distributed in ϕ :



easyMTrackCand Acceptance

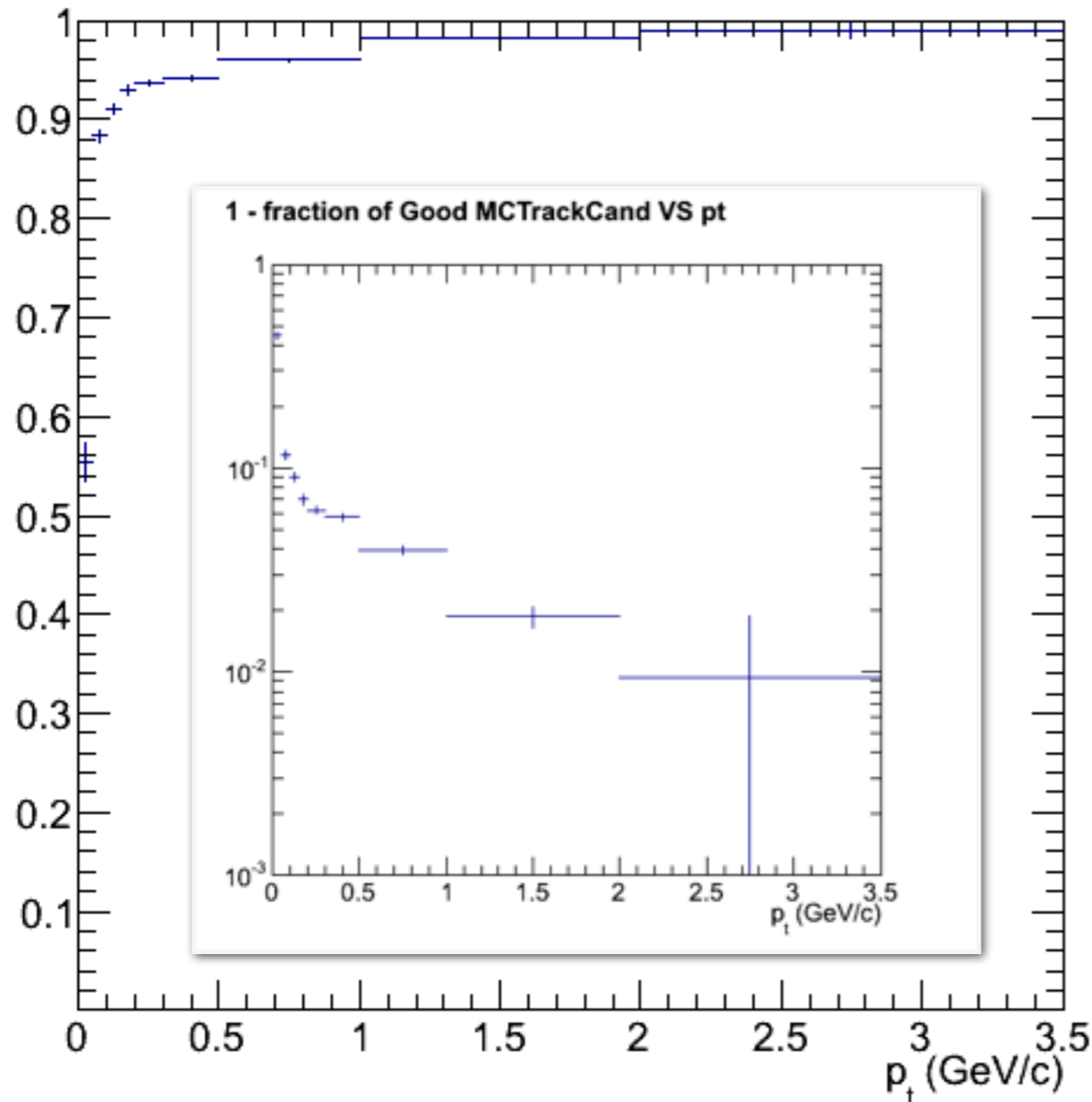
fraction of Good MTrackCand VS λ



- ➔ only ~10% of MTrackCands in the backward direction are easy to find, but there is low statistics there
- ➔ 75% of MTrackCands are easy to find in the forward direction
 - selection criteria applied to hits in the *wedge* part of the SVD results in a looser selection
- ➔ 95% of the MTrackCands in the central region are easy to find

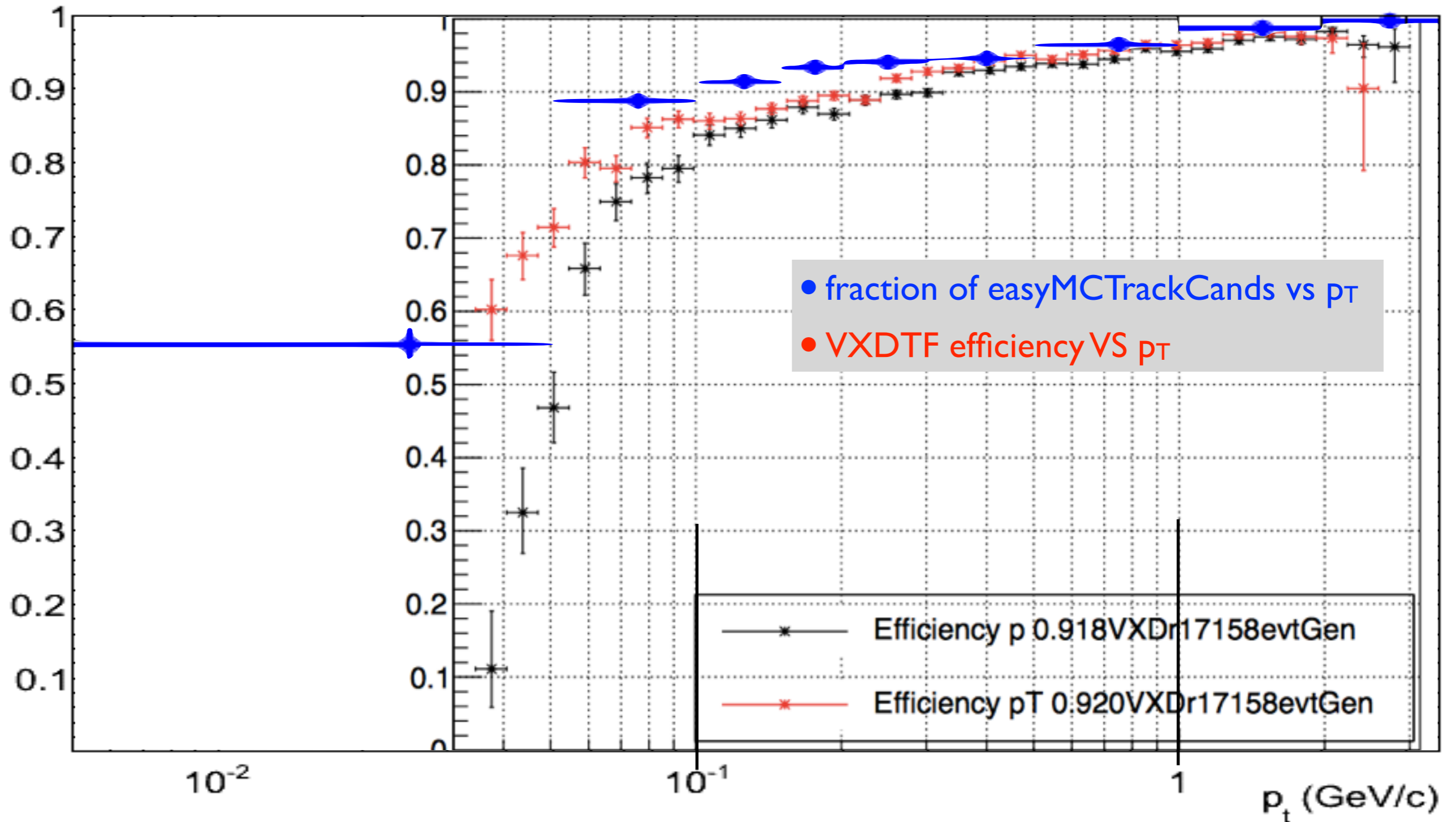
easyMCTrackCands VS p_T

fraction of Good MCTrackCand VS p_T



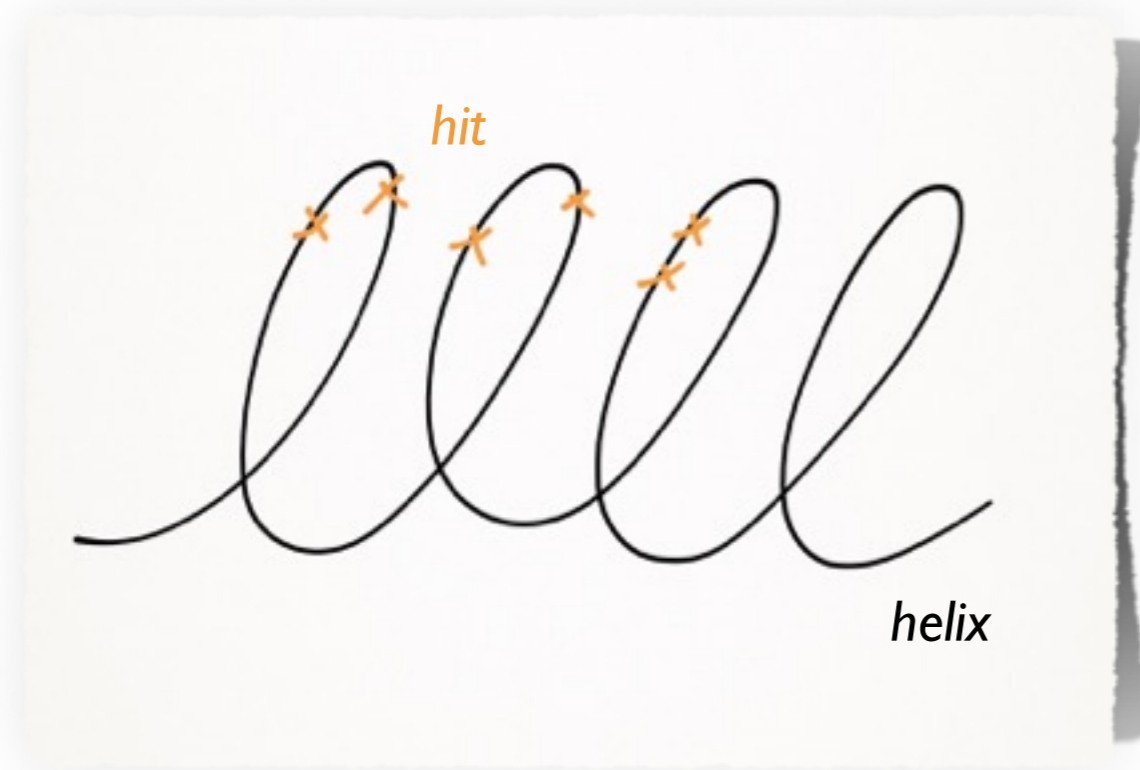
- ➔ 55% of tracks with $p_T < 100$ MeV/c are easy to find
- ➔ fraction of easyMCTrckCands jumps to 88% for $100 \text{ MeV/c} < p_T < 200 \text{ MeV/c}$
- ➔ $p_T > 2\text{GeV/c}$ only 1% of tracks are not easy-to-find

Comparison with the VXDTF efficiency



Possible Improvements in the Selection Criteria

- ➔ correct the computation of θ_{MS} using the incident momentum (from TrueHit)
- ➔ can take into account (small) energy loss
 - same approach as MS: allow for a “small” energy loss and recompute the helix radius and position
- ➔ should get rid of MCTrackCands as:



- can use the time information associated to the hit:
 - estimate the time needed to complete one lap in the transverse plane (using E and p_T)
 - cut on the next-hit time

Conclusions

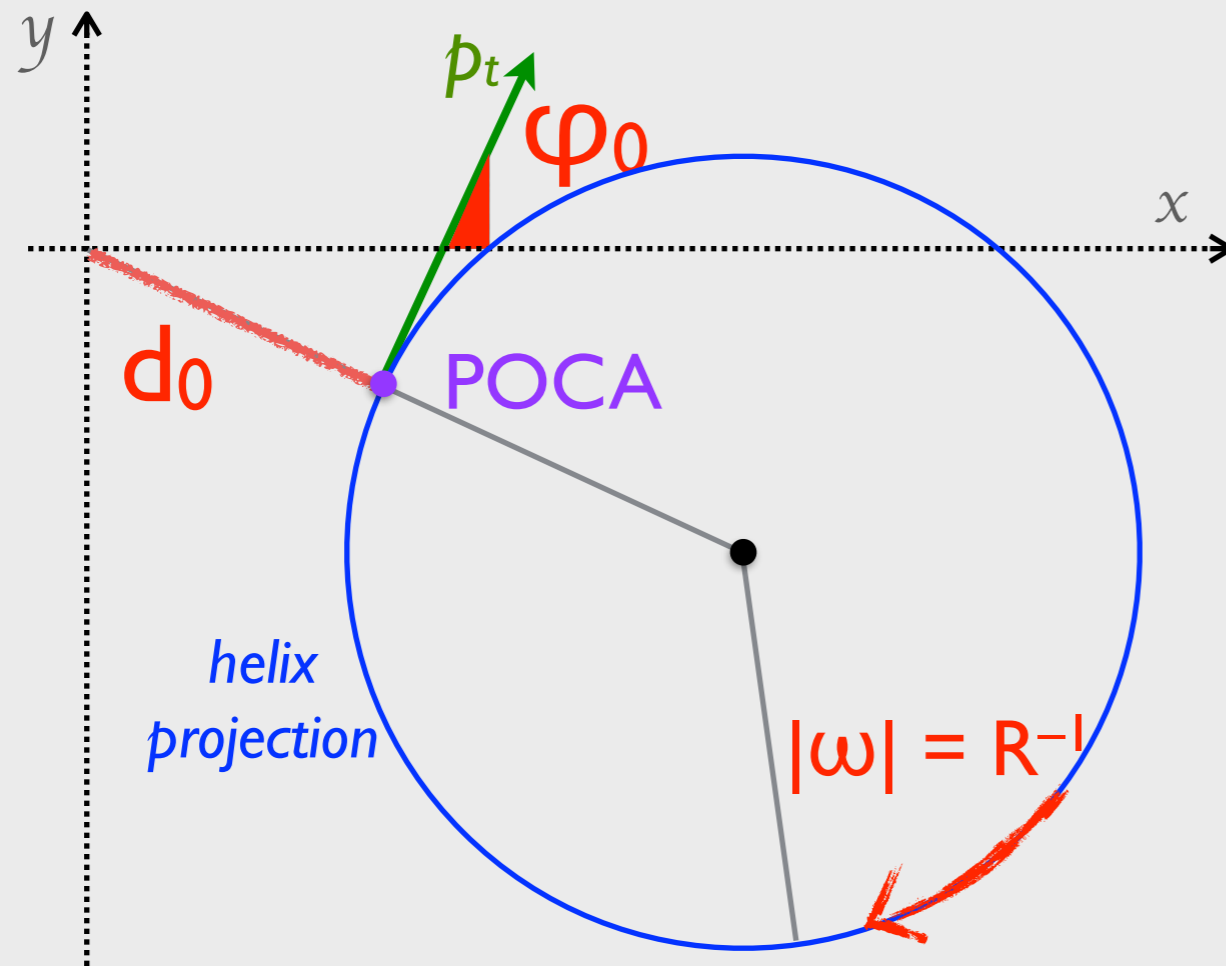
- ➔ The results of the first studies for a re-definition of efficiency for our pattern recognition have been shown
 - reasonable results, probably going in the right direction
- ➔ Already have ideas to improve the selection criteria for silicon
- ➔ Should soon start to design the module:
 - it should be flexible enough to add/change the selection criteria
 - can help in the development and study of the criteria since the produced TrackCand lists can be studied in more details (e.g. using the display).
- ➔ PXD is in the game, we should remove it and see what happens
- ➔ the problem in the CDC needs a similar dedicated effort

Thank You!



Track Parameterisation

TRANSVERSE PLANE



- POCA = Point Of Closest Approach
- d_0 is the 2d signed distance of the POCA from the z axis, the sign depends on the angular momentum of the track (>0 in the fig.)
- φ_0 is the angle between p_t and the x axis at the POCA, $\varphi_0 \in [-\pi, \pi]$
- the sign of ω , the curvature, is the same as the charge of the track (>0 in the fig.)

LONGITUDINAL VIEW

- $\tan\lambda$ is the ratio of p_z and p_t , $\lambda \in [-\pi, \pi]$
- z_0 is the signed distance of the POCA from the transverse plane

