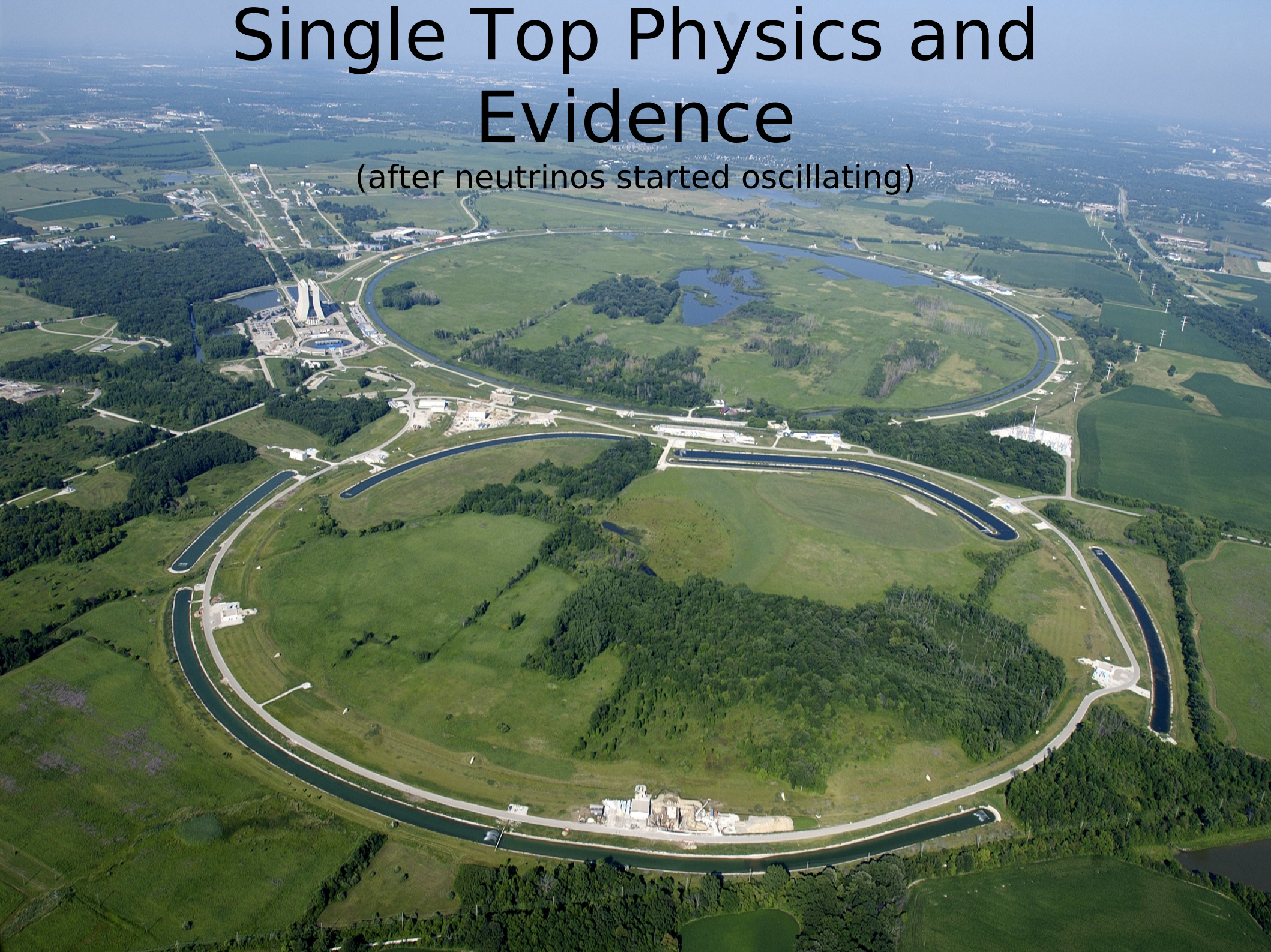


Single Top Physics and Evidence

(after neutrinos started oscillating)



As a start: The Fermilab



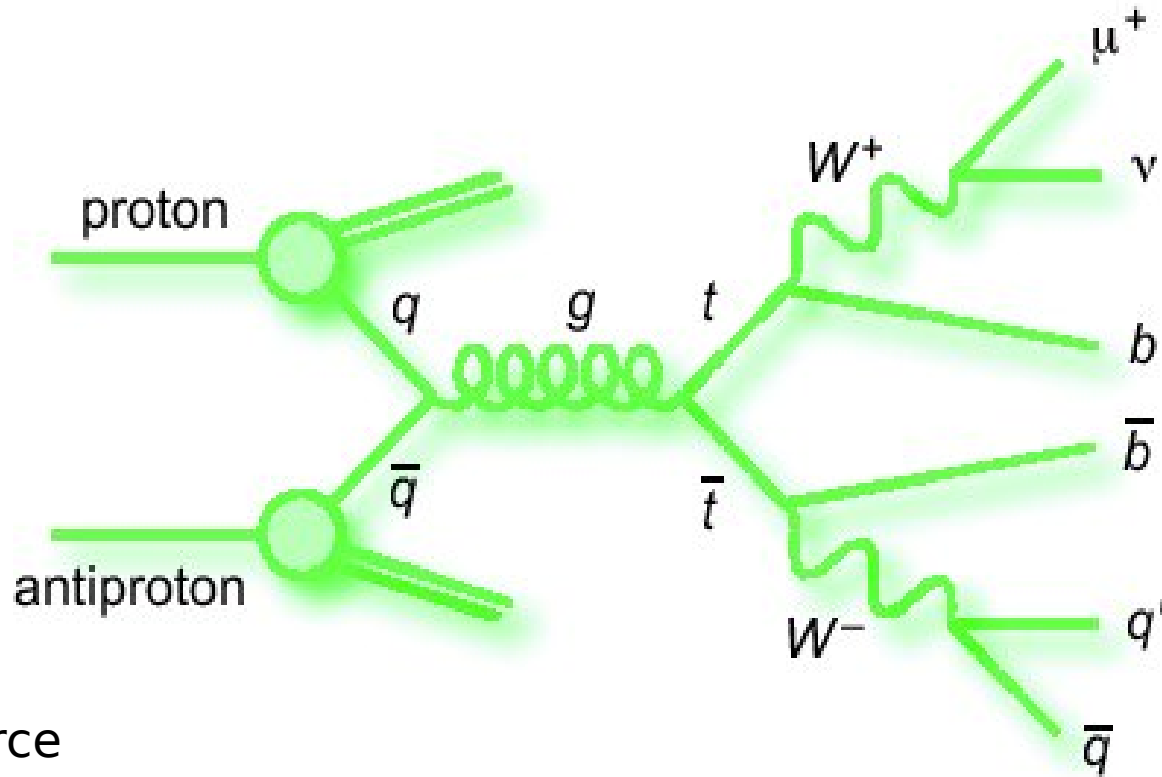
CDF

Tevatron:

- $p \bar{p}$ collider
- $\sqrt{s} = 1.96 \text{ TeV}$
- $\text{circum} = 6.4 \text{ km}$

D0

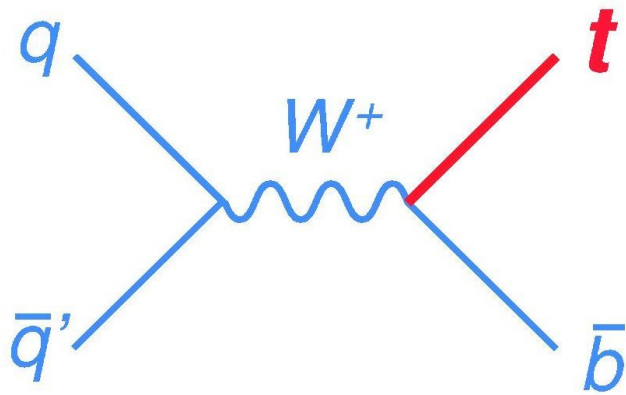
Short Reminder: Top pairs



- strong force
- “typically” 4 jets, with 2 b jets
- cross section: ~ 6.5 pb
- first observation with dataset of $\sim \mathbf{60\ pb^{-1}}$ in 1995 by CDF and D0

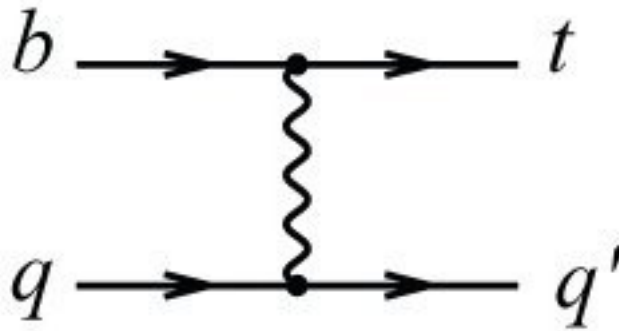
Now, what is this “Single-Top” then?

- **Electroweak** top quark production via **Wtb**-vertex
- SM process BUT not yet observed



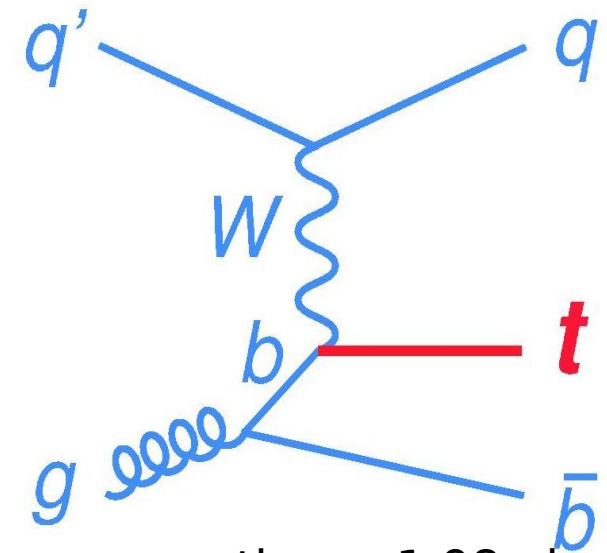
cross section = 0.88 pb

s-channel aka. tb



cross section = 0.08 pb

associated production



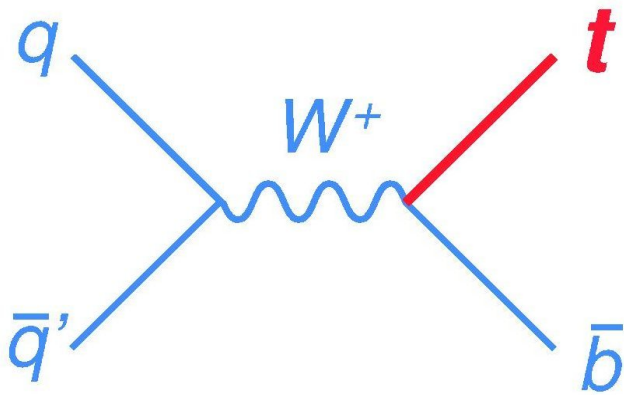
cross section = 1.98 pb

t-channel aka. tqb

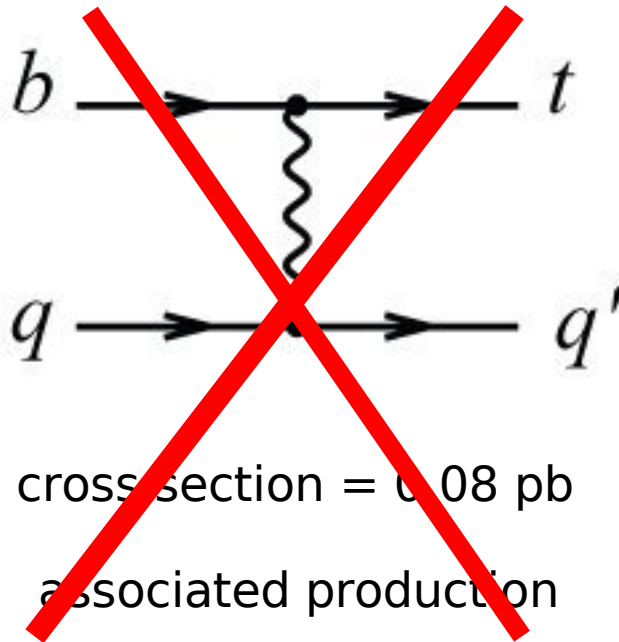
- Top is „standard candle“ for LHC
- Signal of today is background of tomorrow

Now, what is this “Single-Top” then?

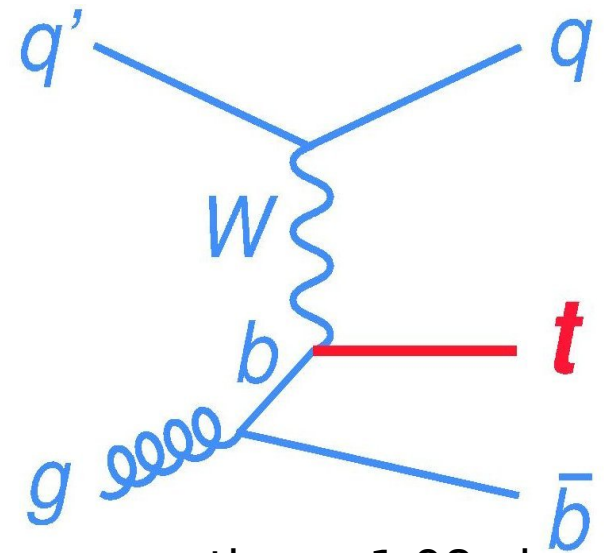
- **Electroweak** top quark production via **Wtb**-vertex
- SM process BUT not yet observed



cross section = 0.88 pb
s-channel aka. tb



cross section = 0.08 pb
associated production



cross section = 1.98 pb
t-channel aka. tqb

- Top is „standard candle“ for LHC
- Signal of today is background of tomorrow

Why is it interesting?

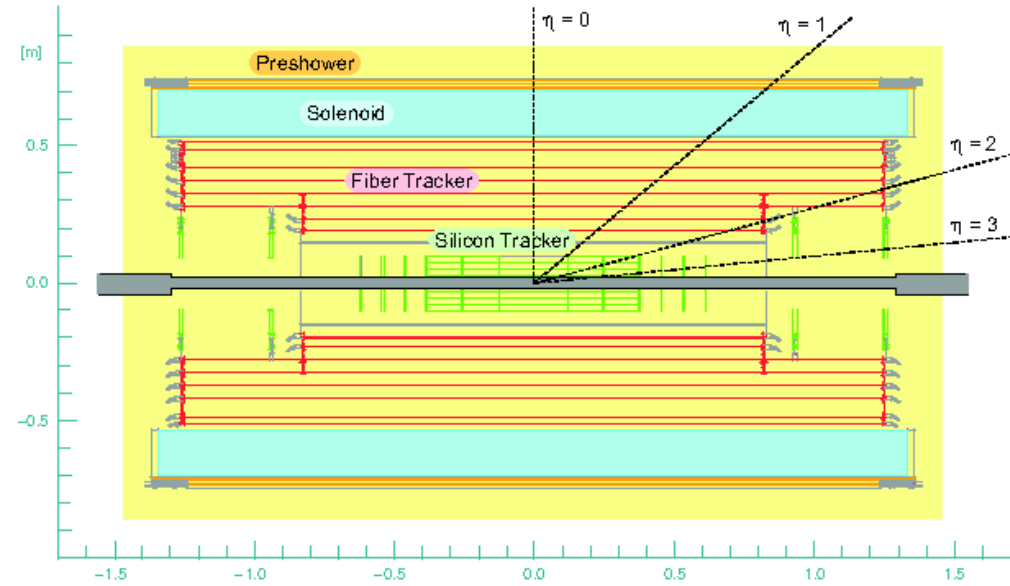
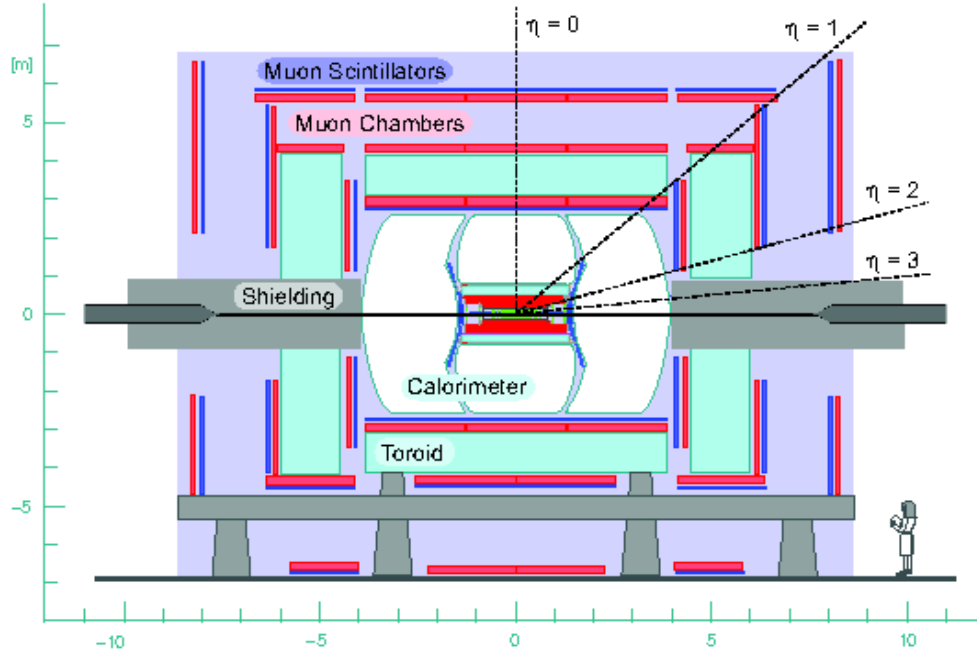
- Lifetime is of order 10^{-24} s, decays before it hadronizes
 - Possible to really measure its (kinematic) mass!
 - Measure Spin of top directly
- Not yet observed!
- Only way to measure $|V_{tb}|$ directly and with little assumptions



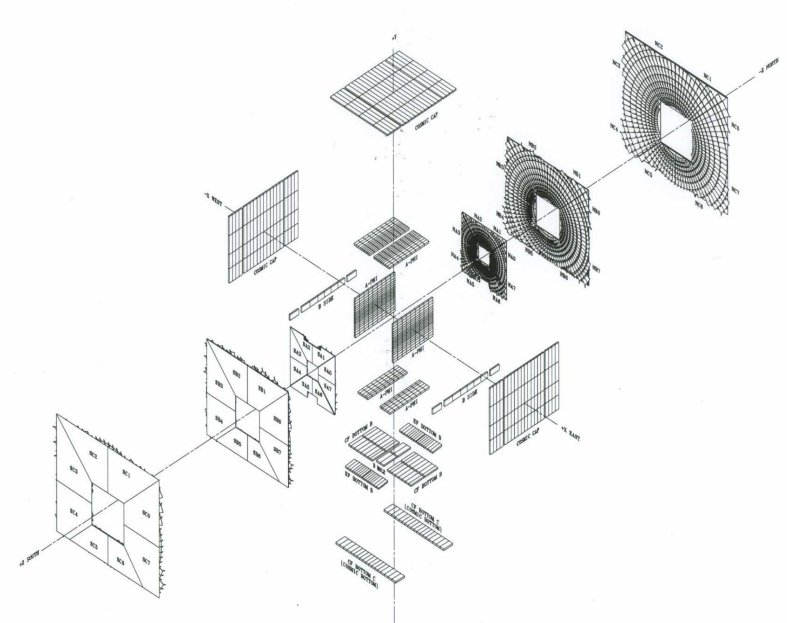
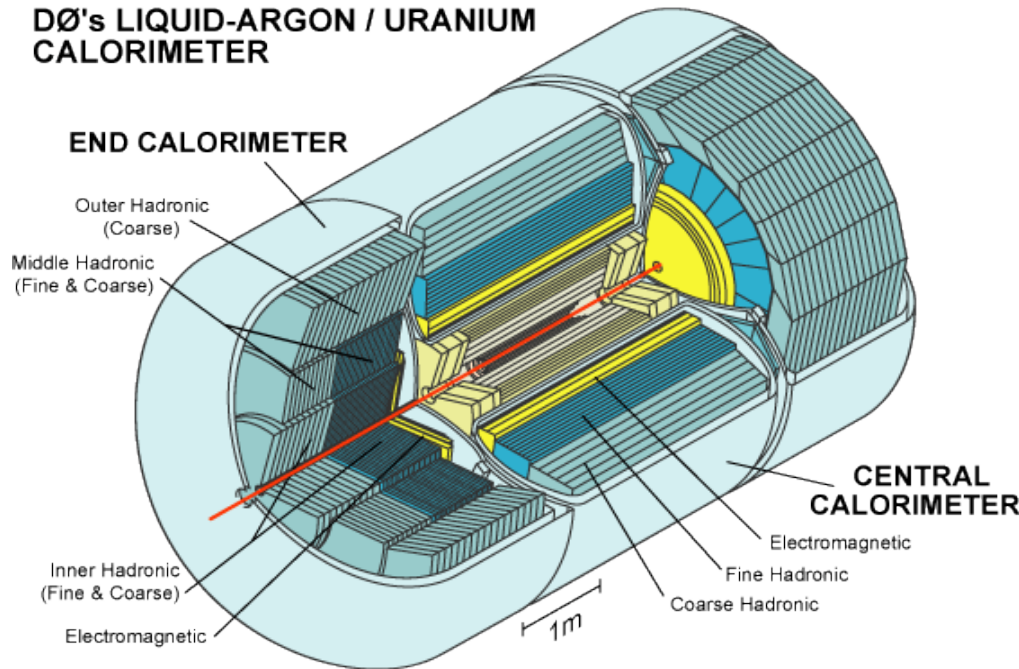
When Trish discovers Ned works exclusively with top quarks, she will be putty in his hands.

- Because it is sexy, obviously! :)

Just quickly: The D0 Detector

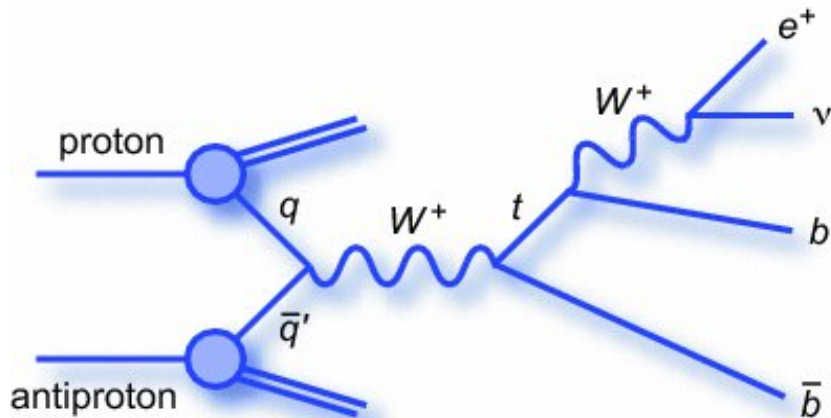


DØ's LIQUID-ARGON / URANIUM CALORIMETER



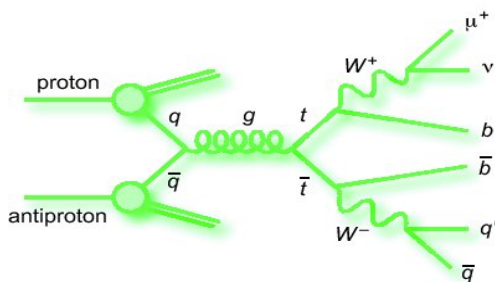
Why is it so difficult?

- **First**, what is signature in detector => what is background?



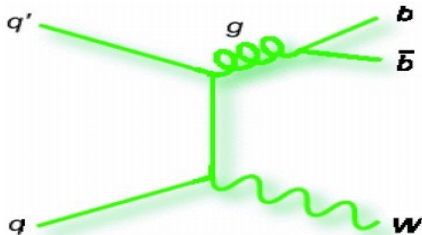
- one isolated lepton
- $\text{miss}E_T$
- 2-3 jets
- at least one b tags

Typical background:



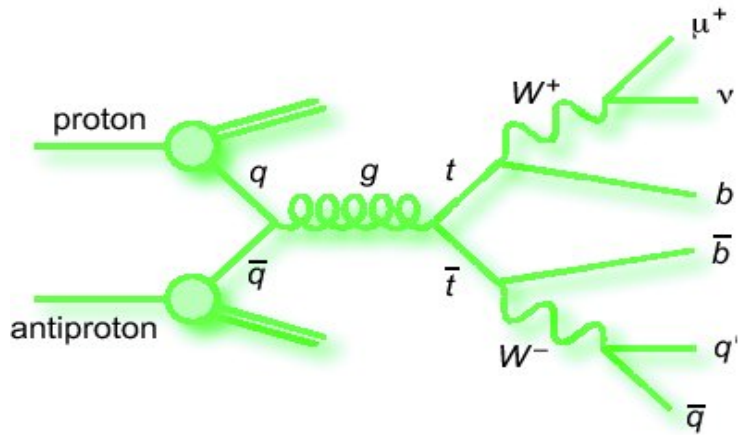
$t\bar{t}$: x-section: ~ 6.5 pb

- **QCD bkg**

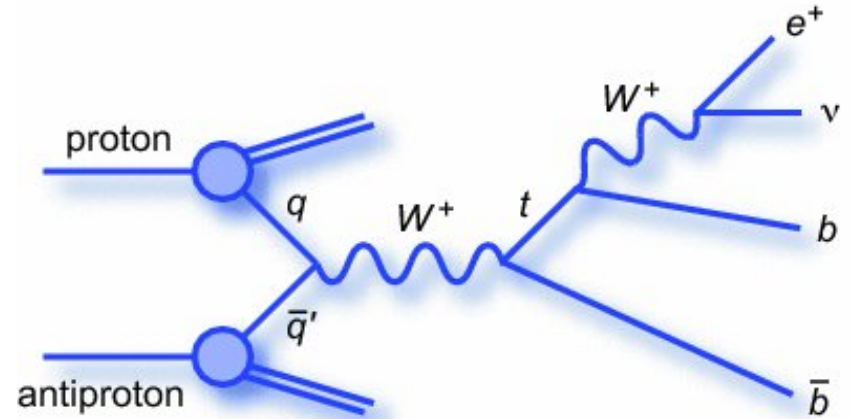


W +jets: x-section: $\sim 80 - 200$ pb

Why is it so difficult?

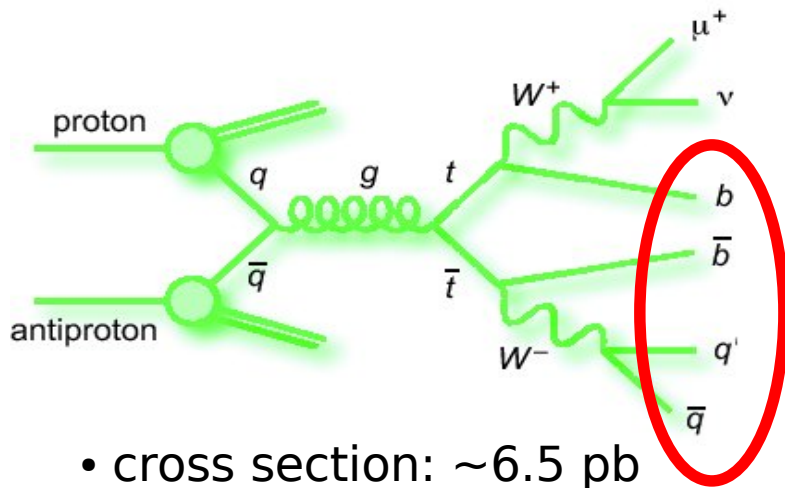


• cross section: ~ 6.5 pb
first observation, $\sim \mathbf{60\ pb^{-1}}$ data
in 1995

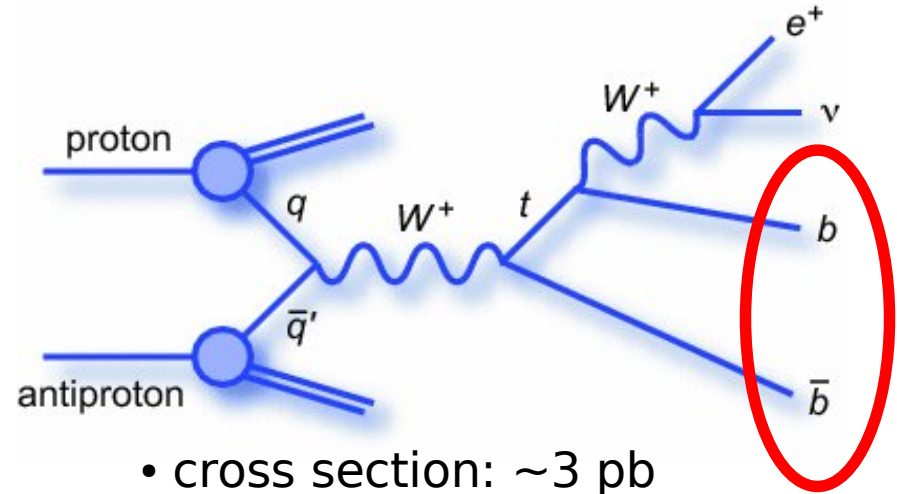


• cross section: ~ 3 pb
first evidence with dataset of $\sim \mathbf{900\ pb^{-1}}$
in 2006

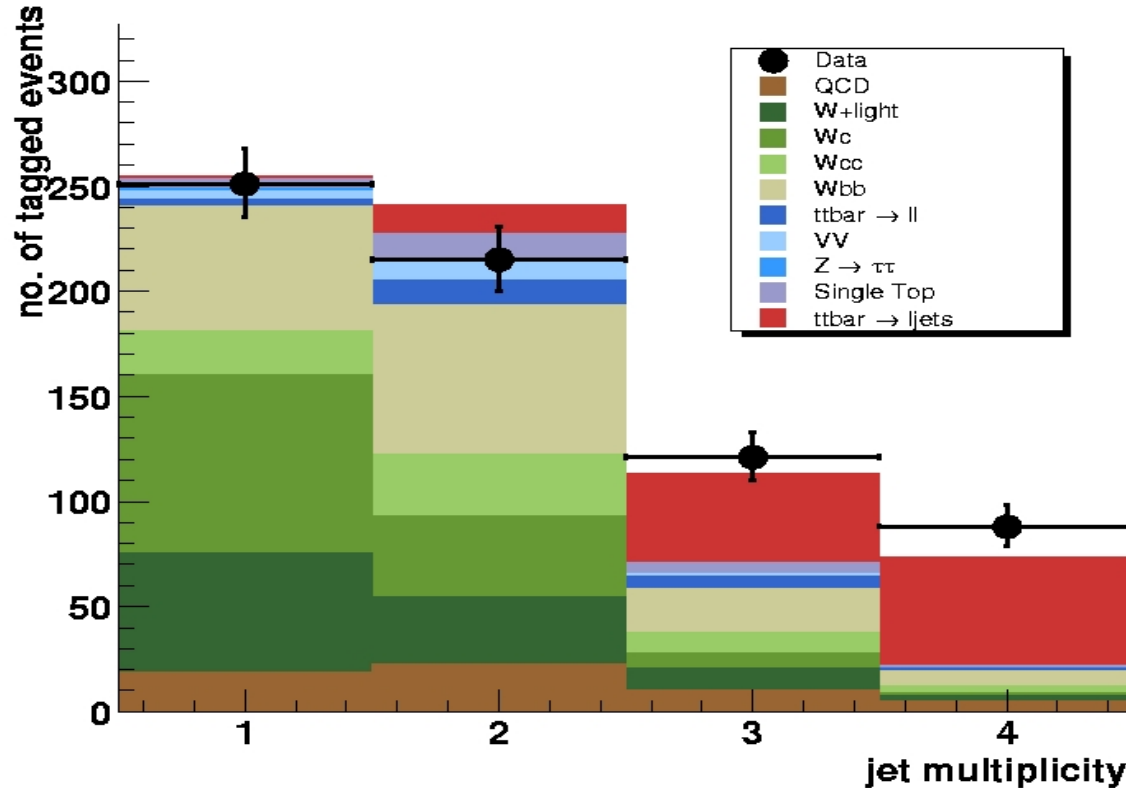
Why is it so difficult?



• cross section: ~ 6.5 pb
 first observation, ~ 60 pb⁻¹ data
 in 1995



• cross section: ~ 3 pb
 first evidence with dataset of ~ 900 pb⁻¹
 in 2006



Ok, how did they do it?

3 different multivariate analyses:

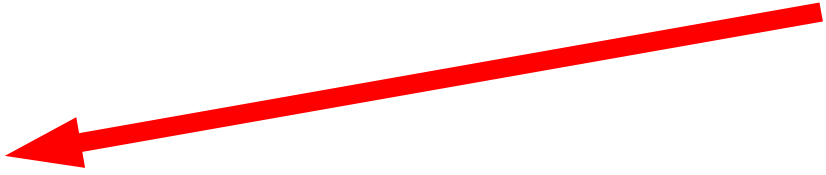
- Boosted Decision Trees (DT)
- Bayesian Neural Network (BNN)
- Matrix Element Analysis (ME)

• all yield a discriminant: **$D(\mathbf{x}) = p(\mathbf{x}|\mathbf{S}) / (p(\mathbf{x}|\mathbf{S}) + p(\mathbf{x}|\mathbf{B}))$**

• Each analysis based on different numerical method to approximate the $D(\mathbf{x})$

Ok, how did they do it?

3 different multivariate analyses:

- Boosted Decision Trees (DT) 
- Bayesian Neural Network (BNN)
- Matrix Element Analysis (ME)

• all yield a discriminant: $\mathbf{D(x)} = \mathbf{p(x|S)} / (\mathbf{p(x|S)} + \mathbf{p(x|B)})$

• Each analysis based on different numerical method to approximate the $D(x)$

Ok Boosted DTs, wth?

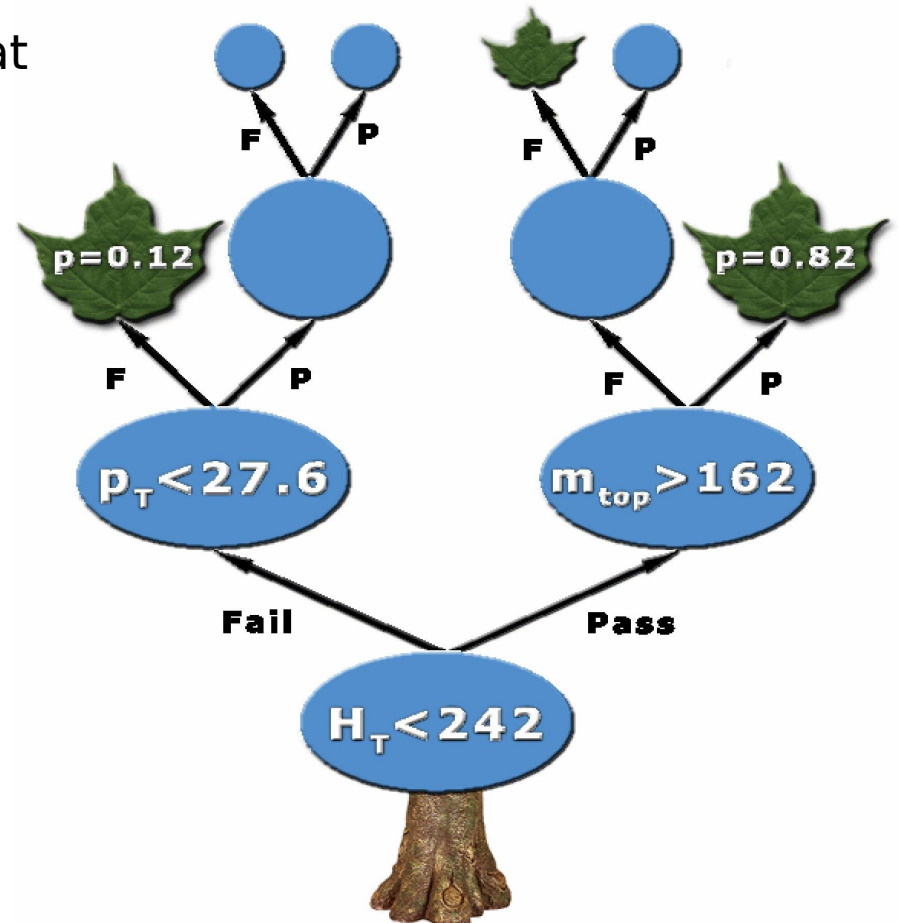
- A decision trees employs a machine-learning technique that extends a cut based analysis into a multivariate algorithm
- Boosting is a process that can be used on any weak classifier (defined as any classifier that does little better than random guessing)

- DT is created by creating 2 branches at each non terminal node
- Terminal nodes called leaves
- Each leaf has a purity value p ($= D$)

$$p = s / (s + b)$$

s = sum w_i (signal)

b = sum w_i (background)



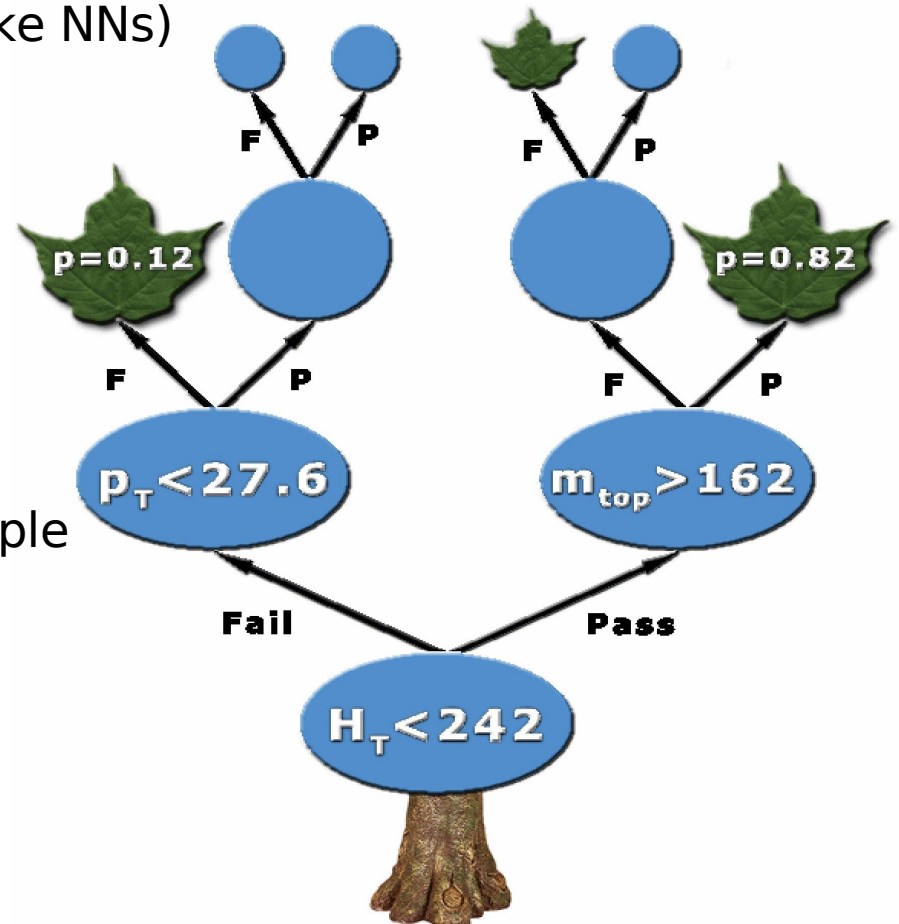
(Dis)Advantages of DTs

Pros:

- Events which fail a cut are still considered in Analysis!
- Tree is human readable! => know why event is called Bkg or Signal
- DT is insensitive to extra variables! (unlike NNs)
- Training is fast!

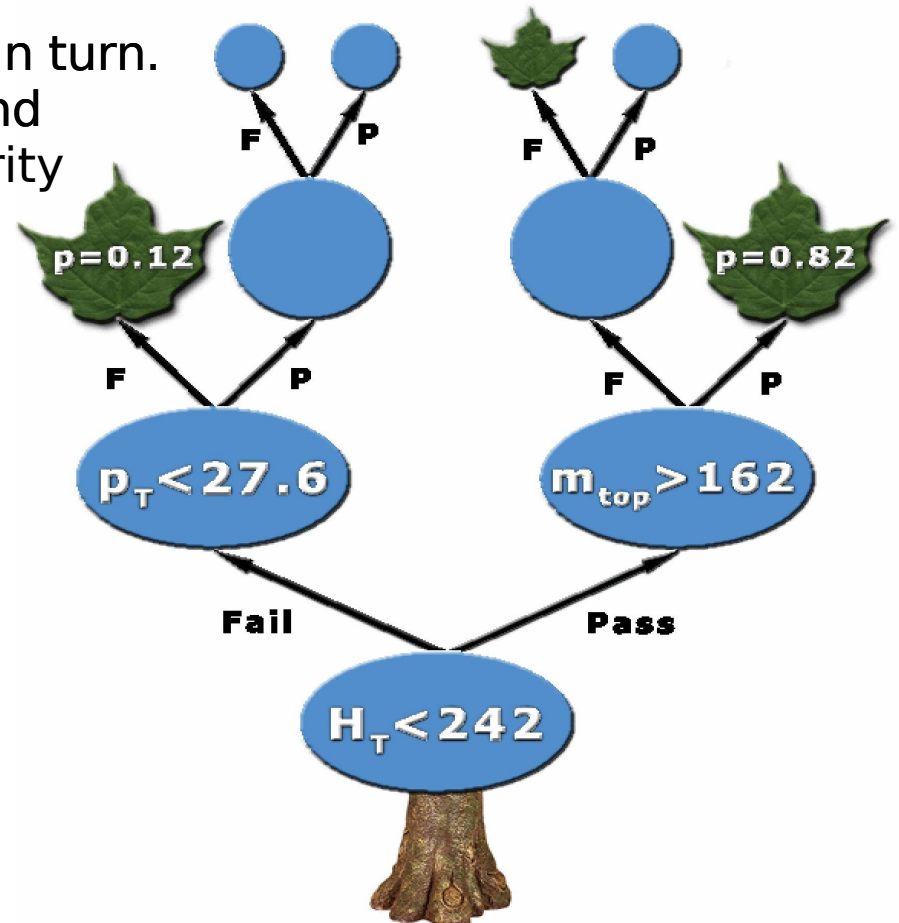
Cons:

- Tree depends extremely on training sample
take care what you do!
- Discrete discriminant,
since number of leaves is finite



Training of DTs

1. Normalize signal trainings sample to background trainings sample
i.e. $\text{Sum}(w_S) = \text{Sum}(W_B)$
2. Create first node containing full sample
3. Sort events according to each variable in turn.
best splitting value is found
i.e. get highest/lowest purity
4. Sample is divided into 2 sub-samples
5. If statistics are too low,
node becomes a leaf
6. Repeat 3-5



How to split...

Goal: find split S that:
 maximizes purity
 or
 maximizes decrease of impurity

Splitting: some measure i of impurity at node t

- should be max for equal mix of s and b
- should be min for either only s or b
- symmetric in s and b
- concave to always reward purer nodes

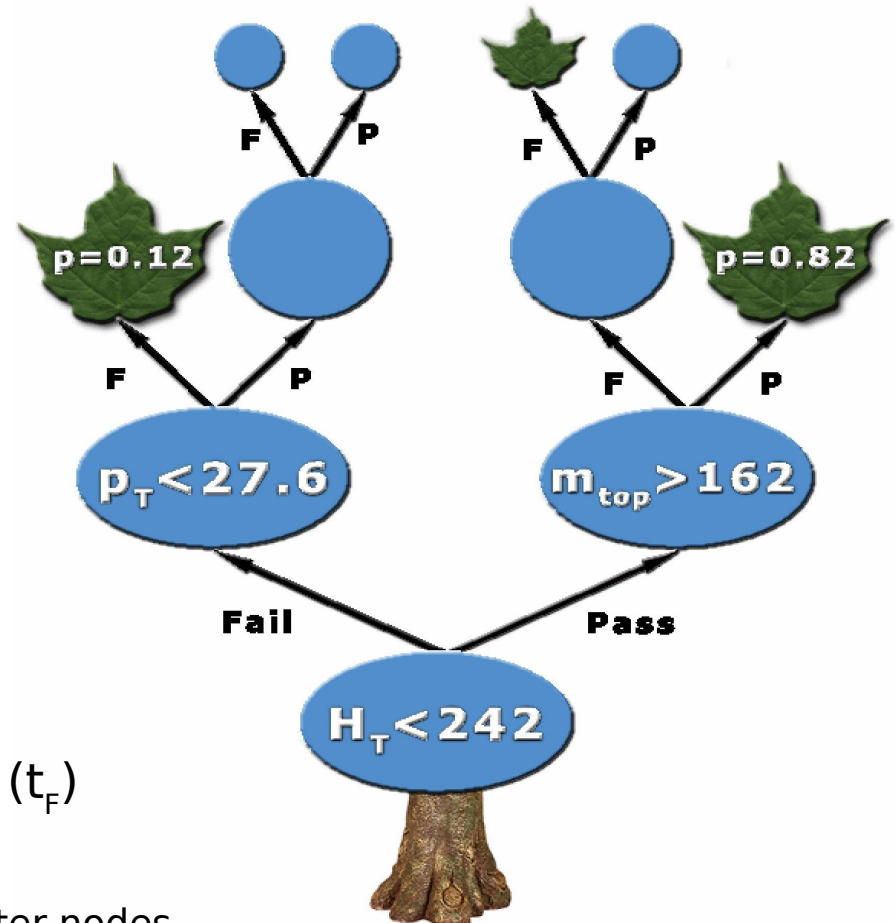
=> Gini index (measure of impurity):

$$i_{\text{Gini}} = 2*sb / (s+b)^2$$

decrease of impurity:

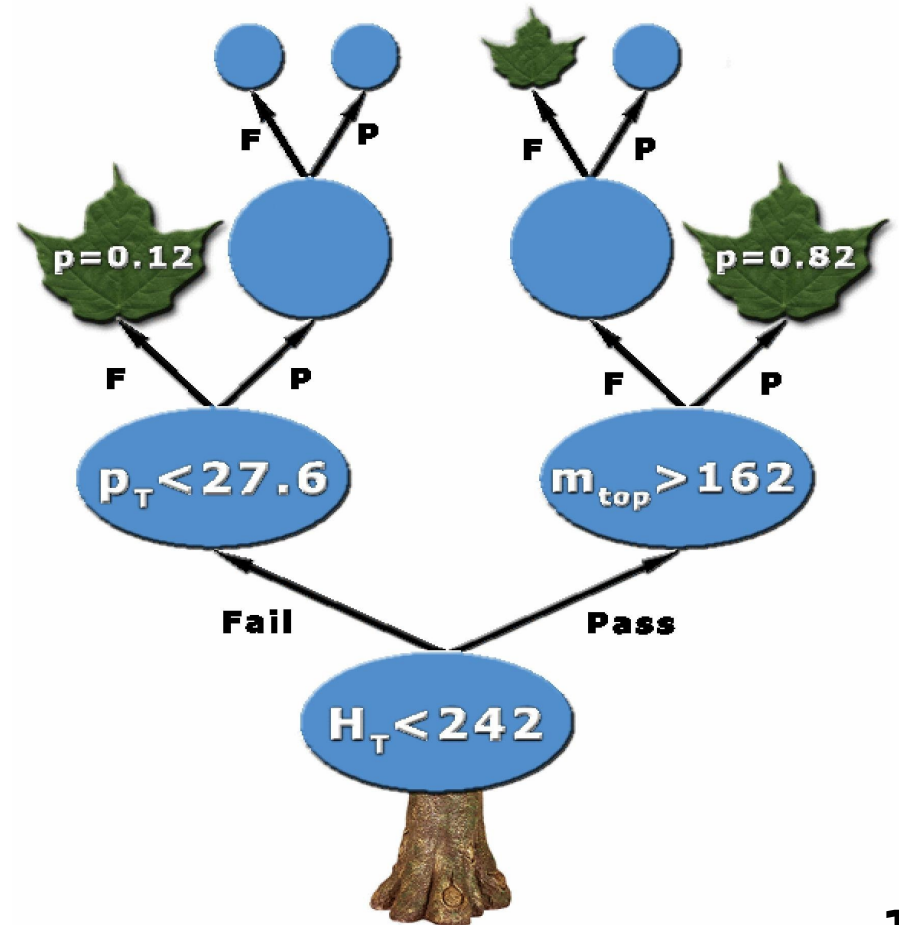
$$\Delta i_{\text{Gini}}(S,t) = i_{\text{Gini}}(t) - p_P i_{\text{Gini}}(t_P) - p_F i_{\text{Gini}}(t_F)$$

$t_{P/F}$ daughter node, $p_{P/F}$ fractions of events in daughter nodes



...and boost

- let one tree run
- reweight events
- make new tree with new weights
- new tree will work “harder” on misclassified events
- calculate discriminant



...and boost (a bit complicated...)

- x_i set of PID variables
- $y_i = 1$ if signal event
= 0 if bkg event
- initial weight of each event is $1/N$
- $T_m(x_i) = -1$ if event on bkg leaf
= 1 if event on signal leaf

$I(y_i, T_m(x_i)) = 1$ if $y_i \neq T_m(x_i)$ wrong classification
 $= 0$ if $y_i = T_m(x_i)$ correct classification

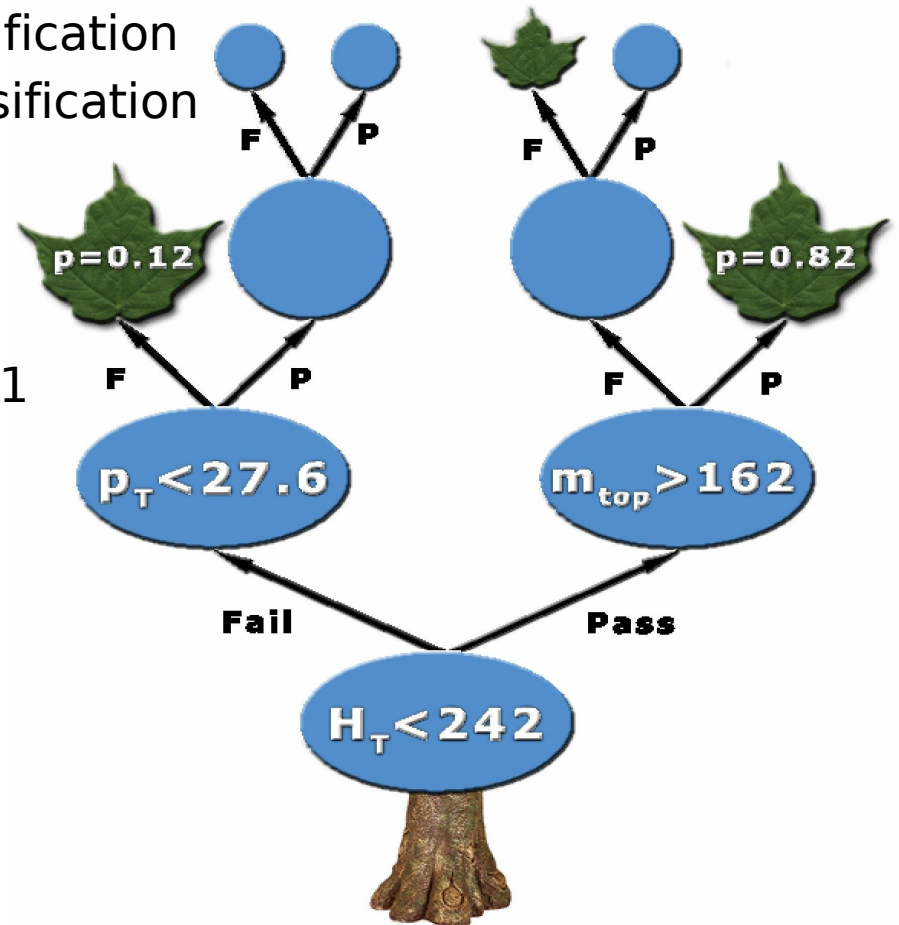
- define error function

$$err_m = \frac{\sum_i w_i * I(y_i, T_m(x_i))}{\sum_i w_i}$$

$$0 \leq err_m \leq 1$$

- define "boost" function

$$\alpha_n = \beta * \ln\left(\frac{1 - err_m}{err_m}\right)$$



...and boost (a bit complicated...)

$$\text{err}_m = \frac{\sum_i w_i * I(y_i, T_m(X_i))}{\sum_i w_i} \quad \text{if better than random: } \text{err}_m < 0.5$$

$$\alpha_n = \beta * \ln\left(\frac{1 - \text{err}_m}{\text{err}_m}\right)$$

- each misclassified event gets new weight according to α_m

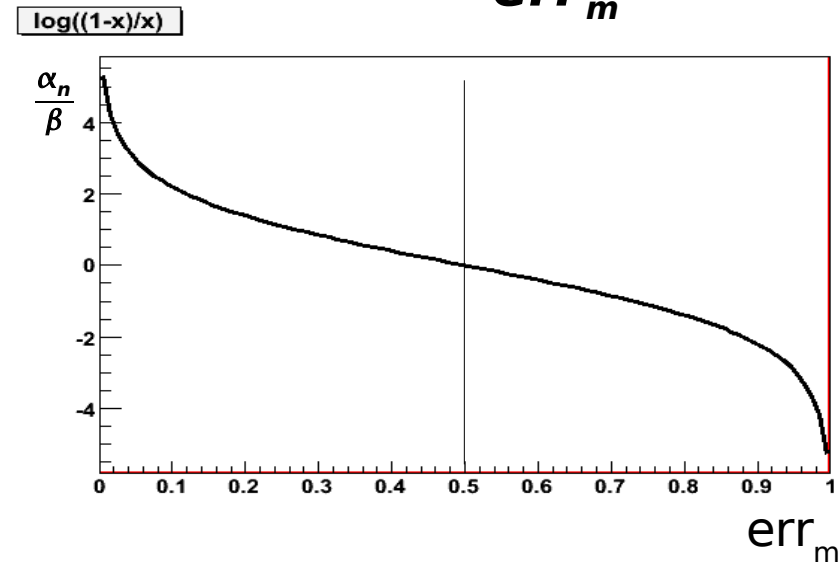
$$w_i \rightarrow w_i * e^{\alpha_n * I(y_i, T_m(X_i))}$$

- create new tree with new weights of events
- each tree tries to optimize purity in leaves through differences in Gini index

$$i_{\text{Gini}} = 2 * sb / (s+b)^2$$

$$\mathbf{s} = \text{sum } w_i(\text{signal})$$

$$\mathbf{b} = \text{sum } w_i(\text{background})$$



- since each misclassified event gets bigger weight, next tree tries harder to classify this event correctly

Redefine Discriminant:

$$D(x_i) = \frac{1}{\sum_n \alpha_n} \sum_n \alpha_n D_n(x_i)$$

What is the input?

3 classes of input variables: Overall 49 (!) variables

Object kinematics:

$p_T(\text{jet1}), p_T(\text{jet2}), p_T(\text{tag1}), p_T(l), \dots$

Angular variables:

$\cos(\text{jet1}, l)_{\text{lab}}, \text{delR}(\text{jet1}, \text{jet2}), \cos(\text{jet2}, \text{alljets})_{\text{alljets}}, \dots$

Event kinematics:

$\text{miss}E_T, M_T(W), M(\text{alljets}), H(\text{alljets}), \text{Centrality}, \dots$

What is the input?

3 classes of input variables: Overall 49 (!) variables

Object kinematics:

$p_T(\text{jet1}), p_T(\text{jet2}), p_T(\text{tag1}), p_T(l), \dots$

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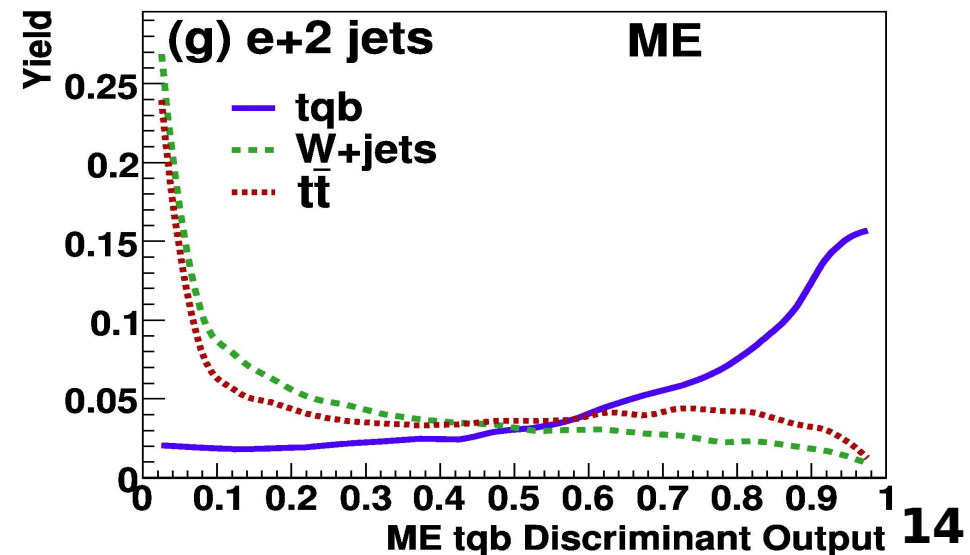
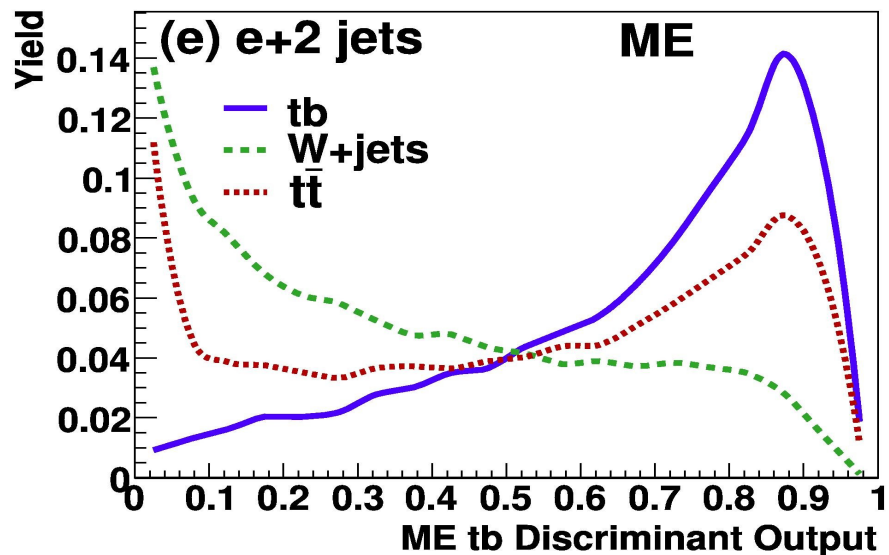
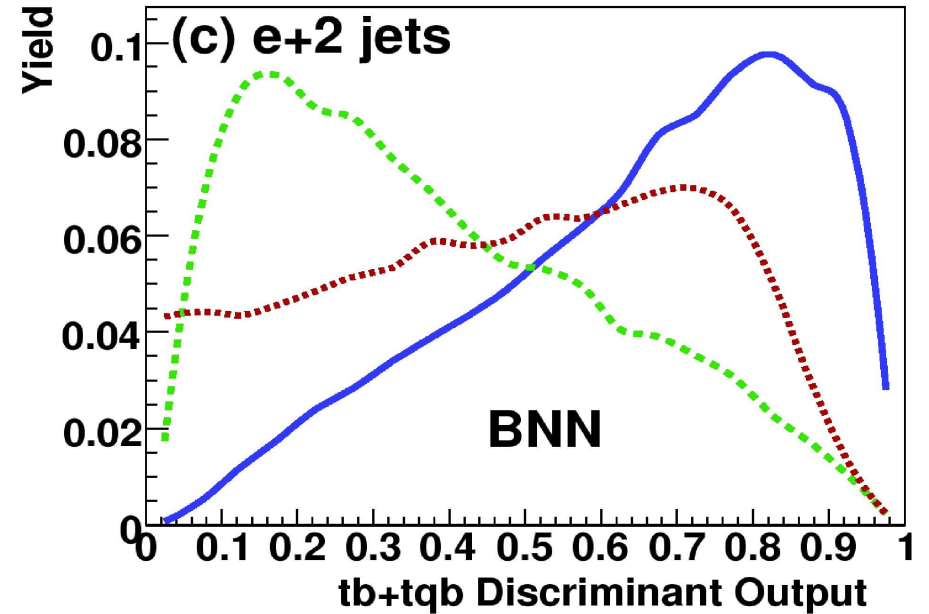
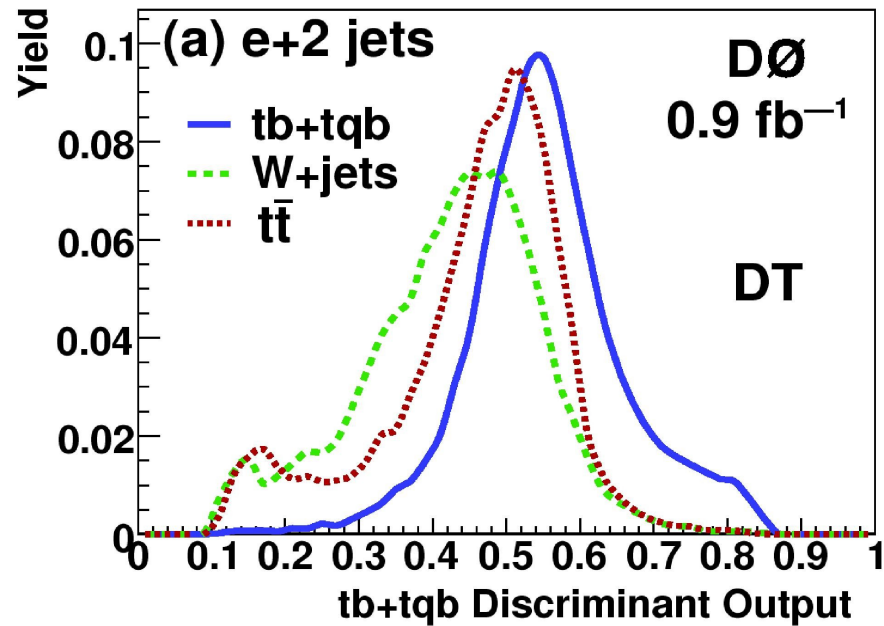
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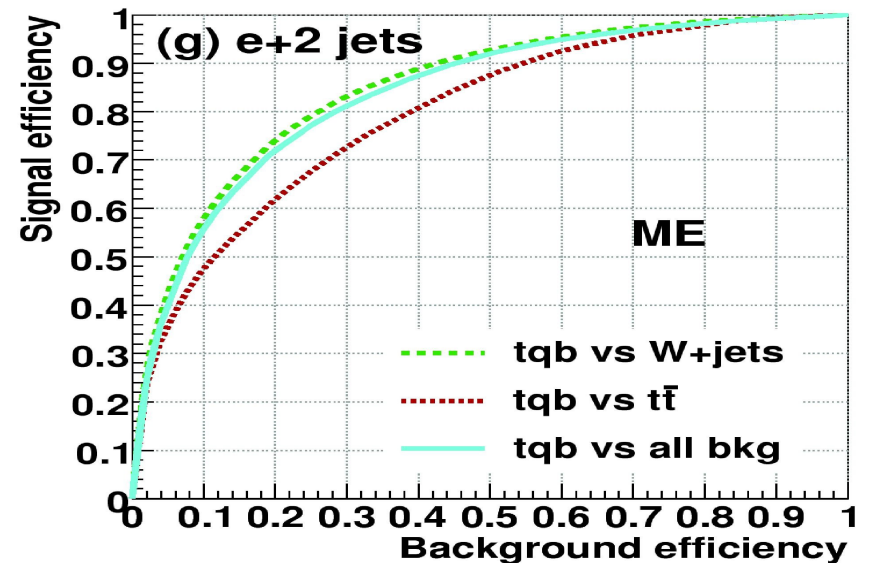
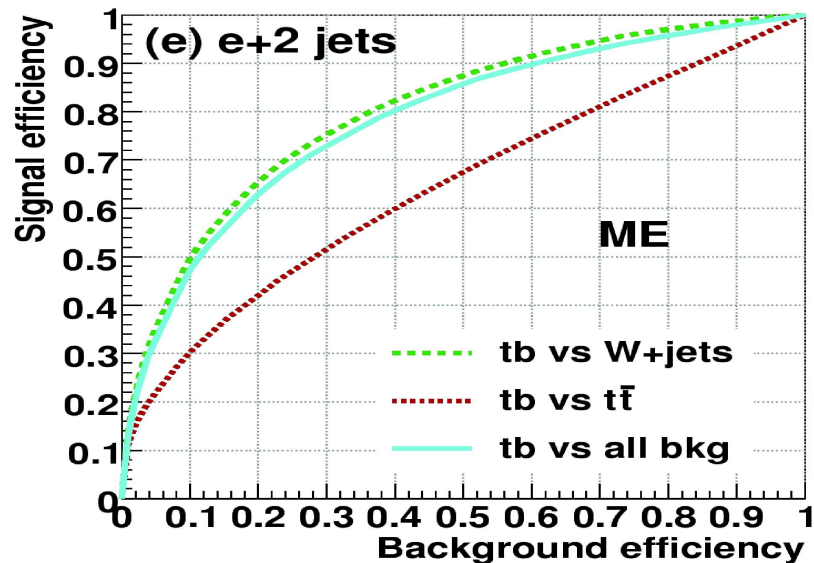
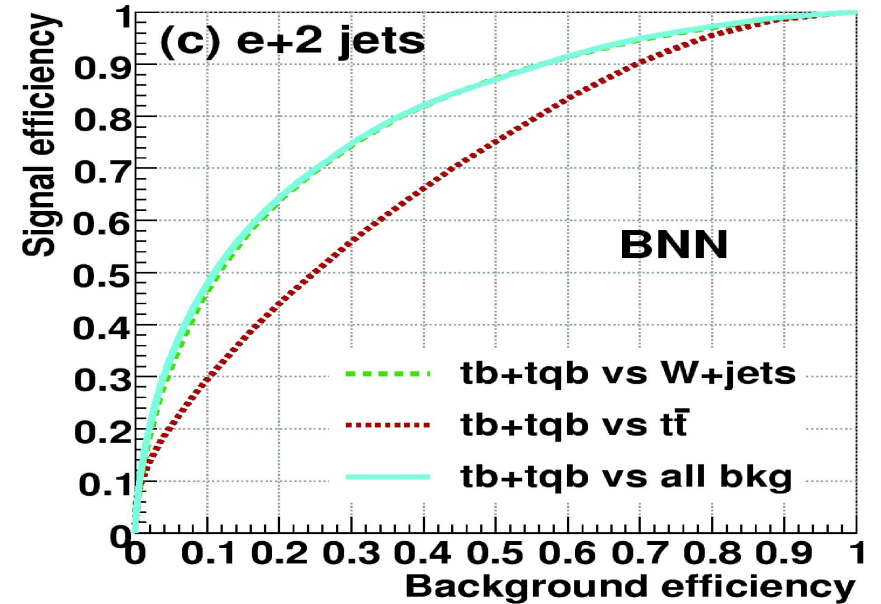
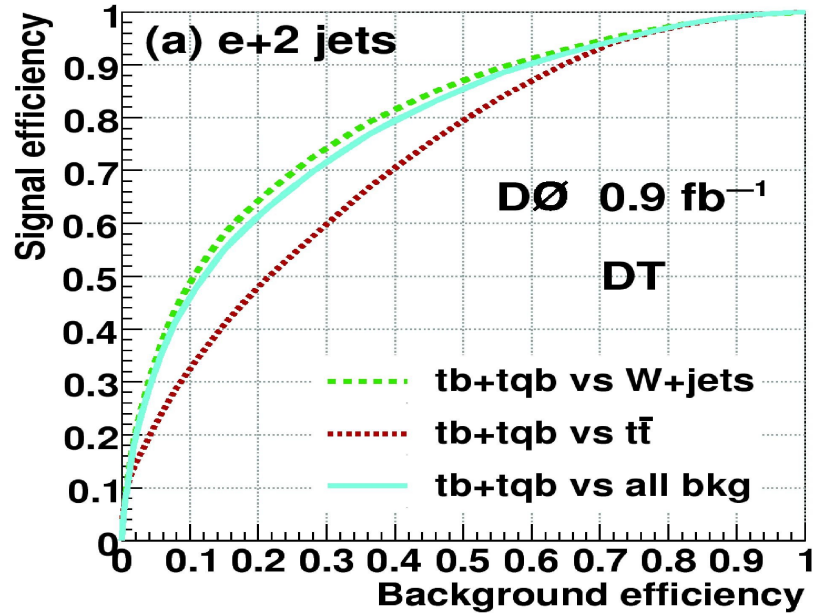
• Why use so many variables if ~ handfull of right variables give you **ALL** information?

- **True** there is no more information in derived var. then in fundamental ones
- **BUT** for some **numerical approx.** methods it is easier to provide an accurate $D(x)$ if use constructed variables

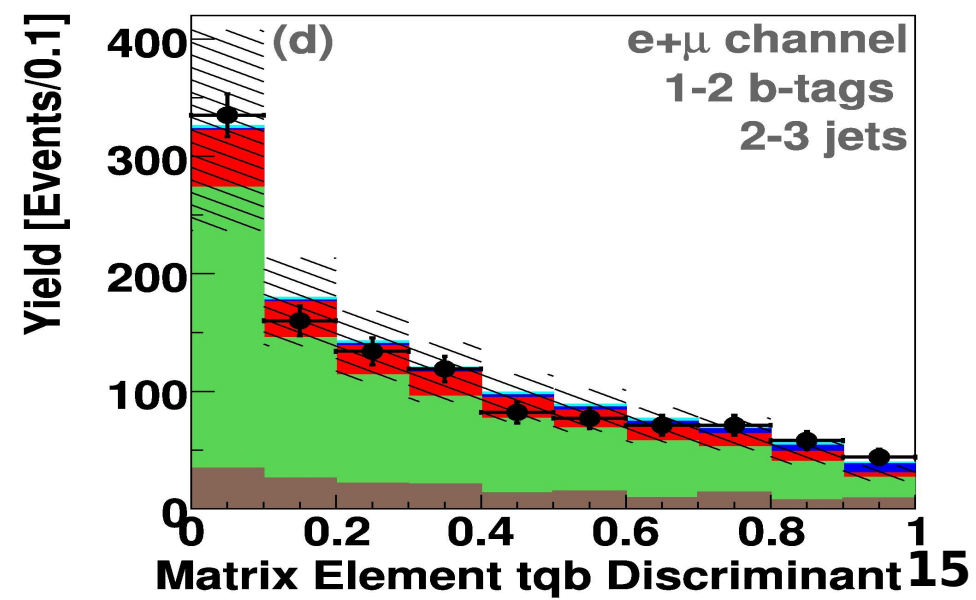
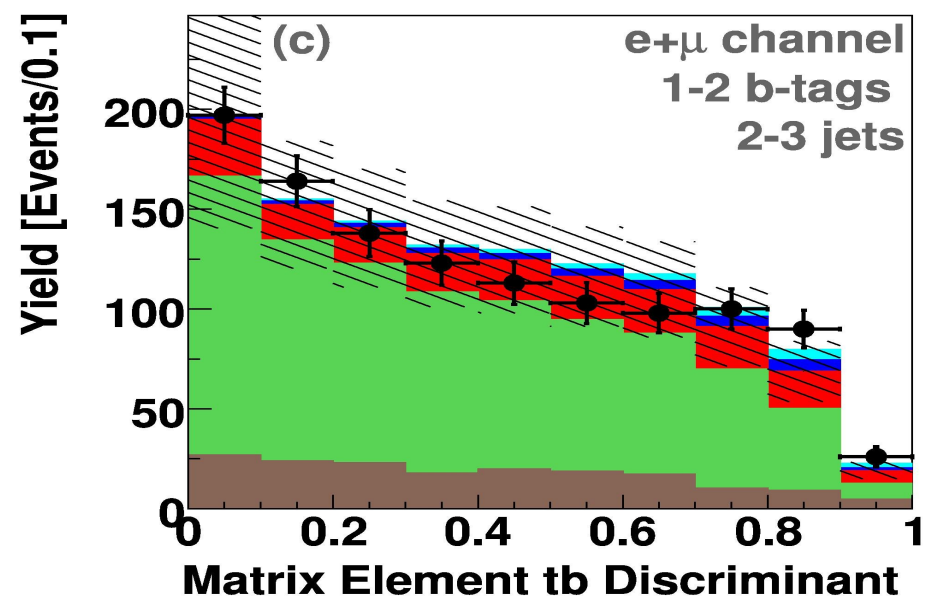
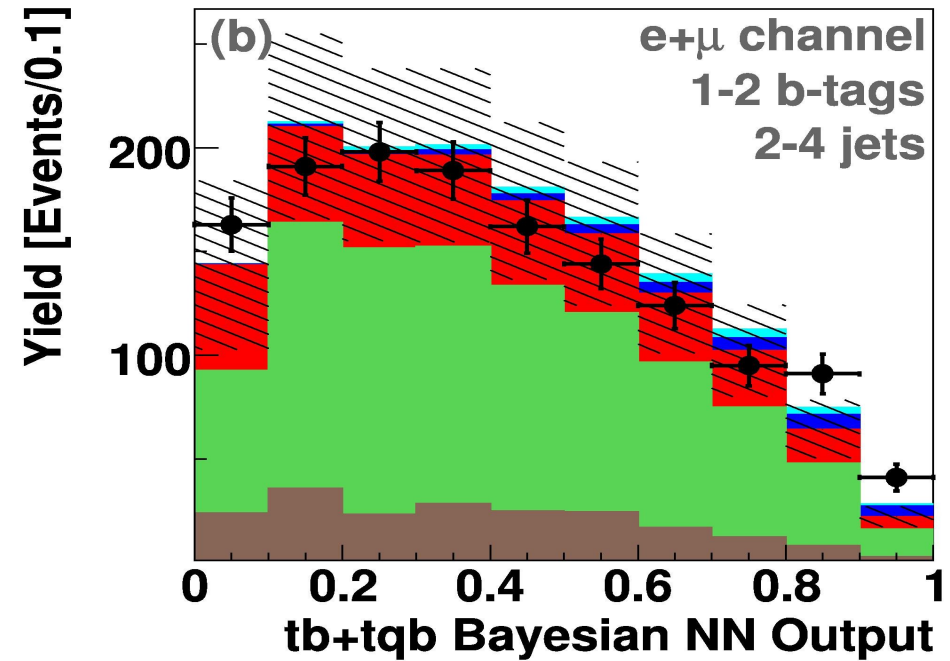
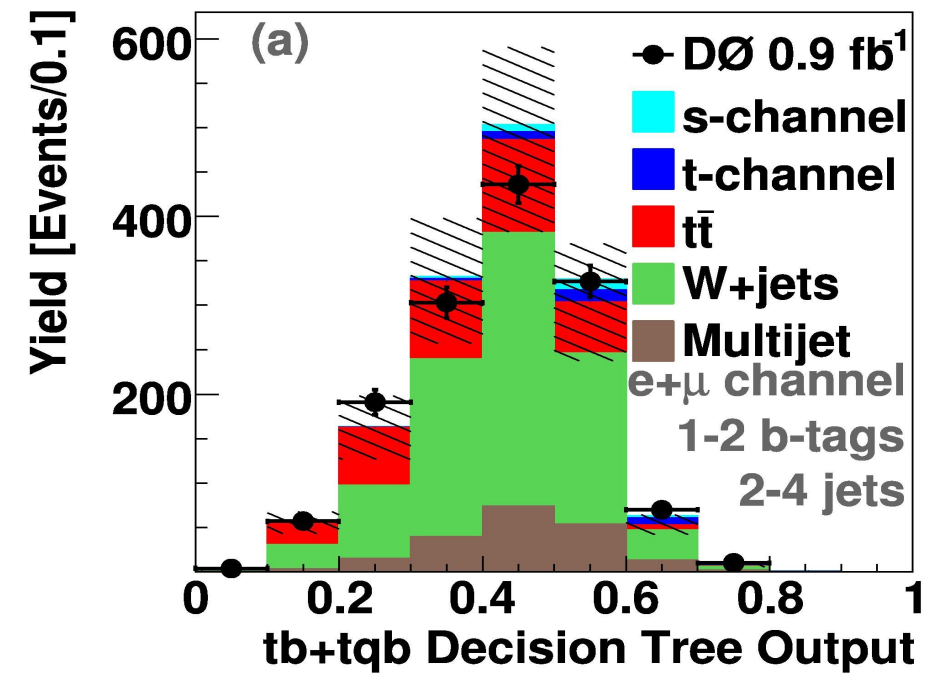
And what is the output?



And what is the output?



How does it compare to data?



Finally, Results!

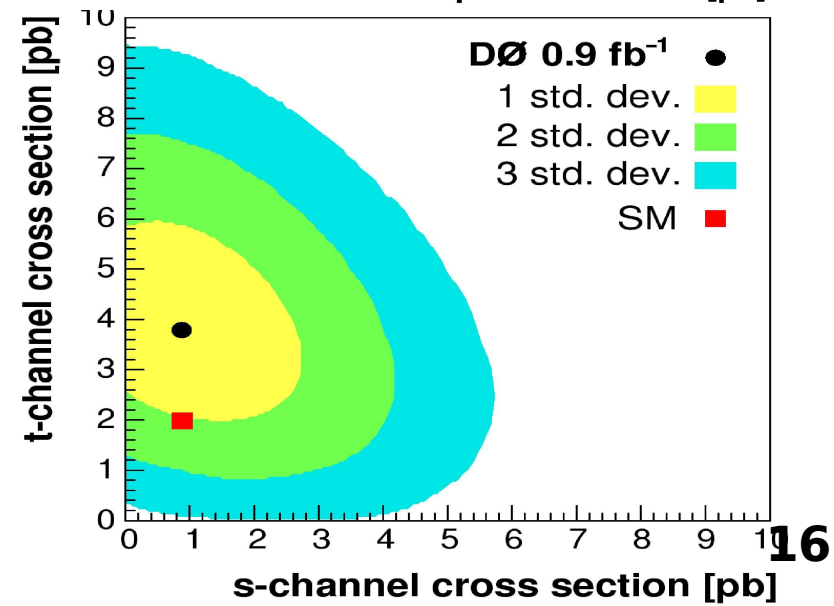
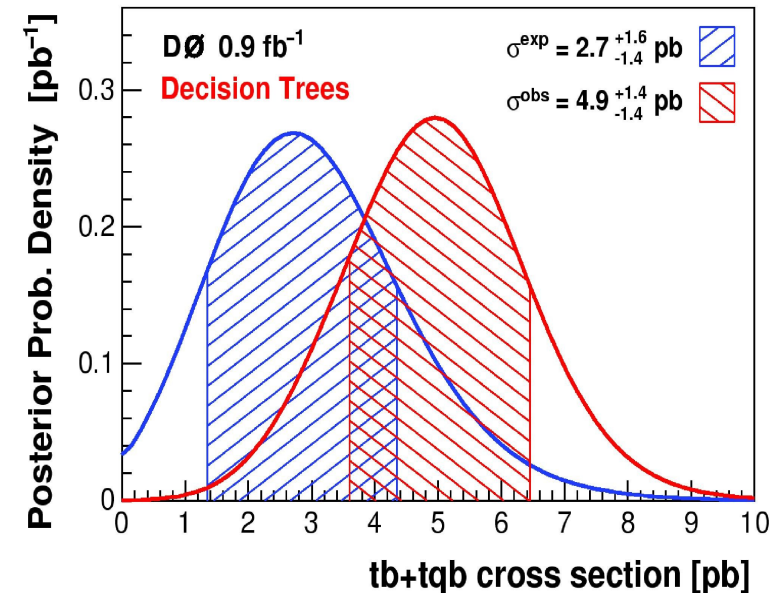
Applying a Bayesian Analysis:

- find *expected cross section* by setting $N_{\text{data}} = (\text{theoretical}) N_{\text{Sig}} + N_{\text{Bkg}}$

- $\sigma(\text{exp}) = 2.7^{+1.6}_{-1.4}$ pb (DT)
- $2.7^{+1.5}_{-1.5}$ pb (BNN)
- $2.8^{+1.6}_{-1.4}$ pb (ME)

- *measured (observed) cross section* :

- $\sigma(\text{obs}) = 4.9^{+1.4}_{-1.4}$ pb (DT)
- $4.4^{+1.6}_{-1.4}$ pb (BNN)
- $4.8^{+1.6}_{-1.4}$ pb (ME)

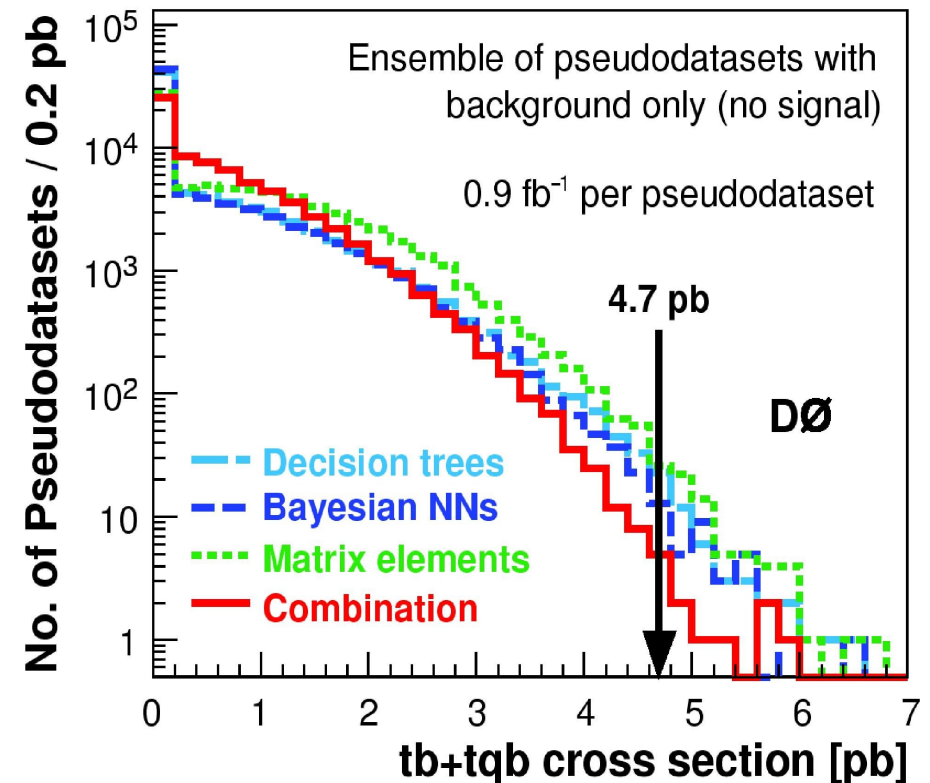


Maybe its all only background?

- find out the **significance** of the expected / observed x-section with **Ensemble-Tests**
 - use background only MC ensemble with all uncertainties
 - set background to estimated yield value
 - run analysis and count how often background only yields exp/obs x-section
 - calculate p-value => significance

Analysis	Expected Results		
	Expected cross section [pb]	Expected p -value	Expected significance (std. dev.)
DT	2.7	0.018	2.1
BNN	2.7	0.016	2.2
ME	2.8	0.031	1.9
Combined	2.8	0.011	2.3

Analysis	Observed Results		
	Measured cross section [pb]	Measured p -value	Measured significance (std. dev.)
DT	4.9	0.00037	3.4
BNN	4.4	0.00083	3.1
ME	4.8	0.00082	3.2
Combined	4.7	0.00014	3.6



Defines EVIDENCE, more than 3 sigma! 17

Is it compatible with signal?

- find out with **Ensemble-Tests**
 - use background and signal MC ensemble with all uncertainties
 - set background and signal to estimated yield value
 - run analysis and count how often ensemble yields observed x-section
- In $\sim 10\%$ of all cases the observed x-section is seen
 - => It is **compatible** with background + signal hypothesis
- => D0 was lucky

I remember something about $|V_{tb}|$

Reminder:

- **with** 3 generations and unitarity: $|V_{tb}| = 0.999100^{+0.000034}_{-0.000004}$
- **without** 3 generations and **without** unitarity: $0.07 \leq |V_{tb}| \leq 0.993$
- to extract $|V_{tb}|$ is straight forward, since $\sigma \sim |V_{tb}|^2$

assumptions:

- $|V_{td}|^2 + |V_{ts}|^2 \ll |V_{tb}|^2$ ok since measured before
- Vertex Wtb is V-A type, but allowed for anomalous strength $f_1^L > 1$!

$$|V_{tb} * f_1^L| = 1.31^{+0.25}_{-0.21}$$

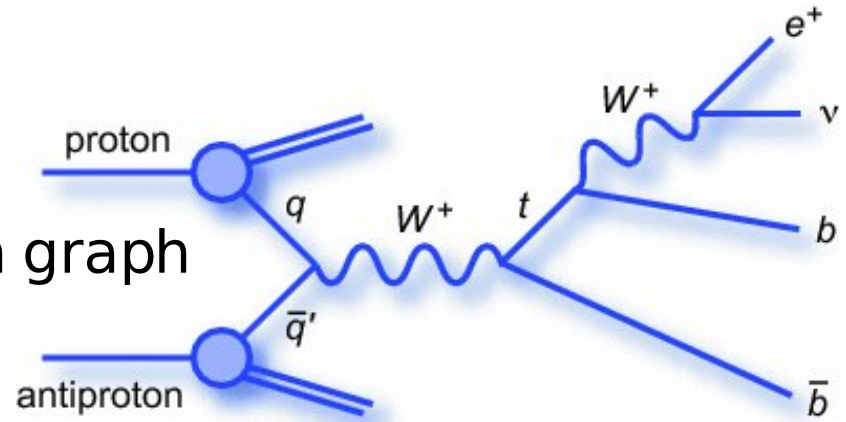
- Vertex Wtb is V-A type, but $f_1^L = 1$!

$$|V_{tb}| = 1.00^{+0.00}_{-0.12}$$

95% C.L. lower limit: $|V_{tb}| > 0.68$

Summary

- This is a “Single Top” feynman graph



- There is **evidence** for ST with 3.6 sigma significance
- The **observed** x-section is 4.7 ± 1.3 pb (combined)
- First direct measurements of $|V_{tb}|$

- $|V_{tb} f_1^L| = 1.31^{+0.25}_{-0.21}$

- $0.68 < |V_{tb}| \leq 1$ at 95% C.L.

- AFTER analysis was done, new theoretical x-section published: x-sect = 3.21 ± 0.21

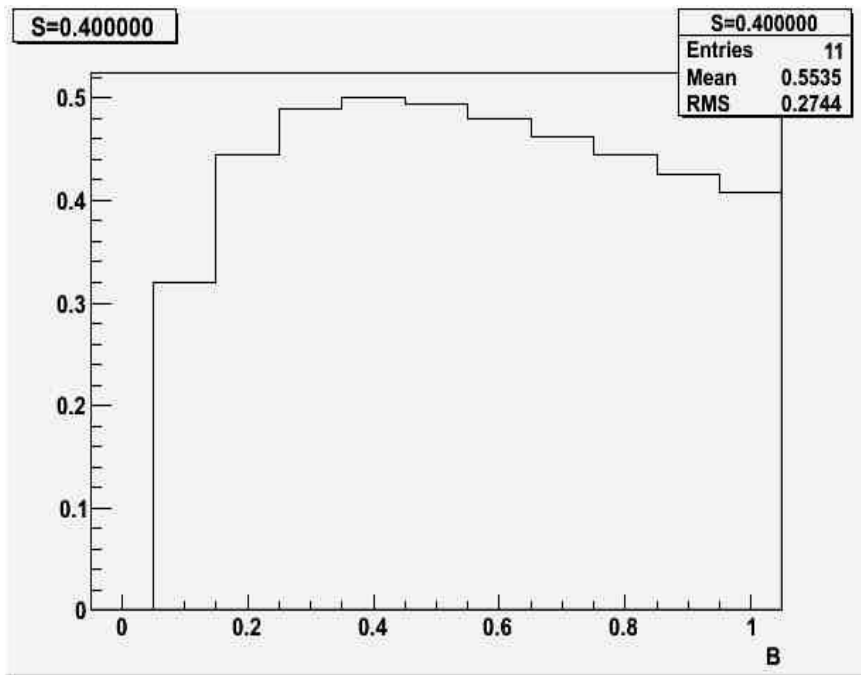
Lunch!

Enjoy your meal !

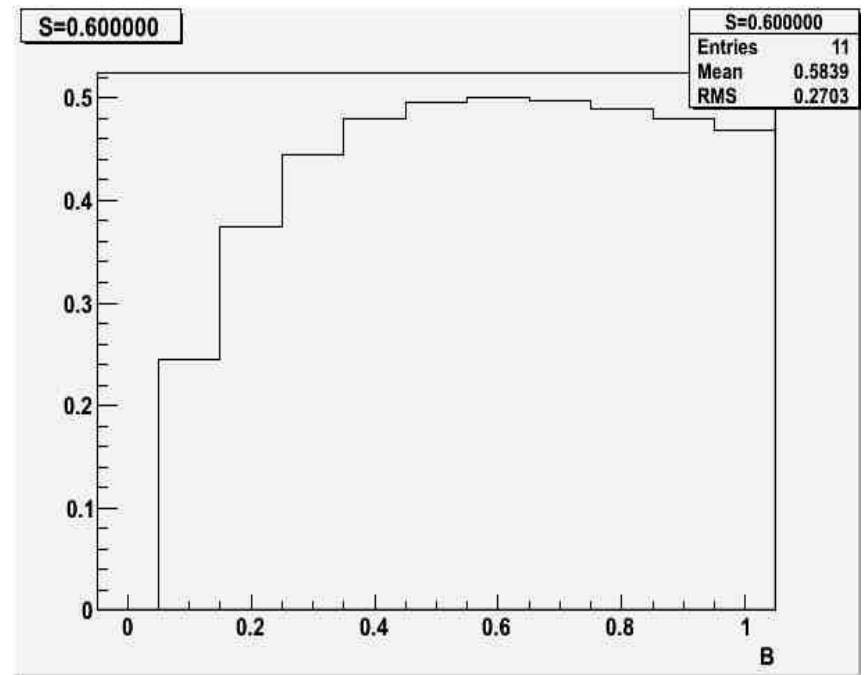
Backup

Gini index: $i_{\text{Gini}} = 2*sb / (s+b)^2$

s fixed and b varied [0,1]



s = 0.4



s = 0.6

Gini index max. for same amount signal and bkg