

Resonances at the TeV: Higgs-like boson, but a strongly interacting EWSBS

Rafael L. Delgado

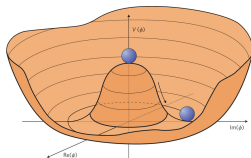


A.Dobado, Felipe J.Llanes-Estrada

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PRL **114** (2015) 221803, PRD **91** (2015) 075017, JHEP **1407** (2014) 149,
JHEP **1402** (2014) 121 and J. Phys. G: Nucl. Part. Phys. **41** (2014) 025002

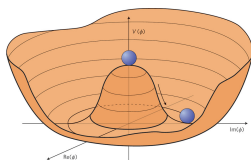
Empirical situation



doi:10.1038/nphys1874

- Electroweak symmetry breaking:
 $SU(2)_L \times SU(2)_R \rightarrow SU(2)_C$
- Three would-be Goldstone bosons ω .
- Equivalence theorem: for $s \gg 100 \text{ GeV}$,
Identify them with the longitudinal components
of W and Z.
- A 125-126 GeV scalar “Higgs” resonance φ .

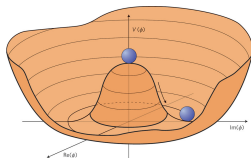
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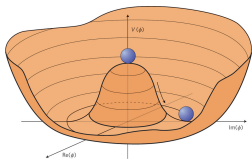
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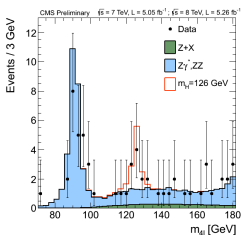
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arXiv:1207.7235 [hep-ex]

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New physics? 600 GeV

GAP

—— H (125.9 GeV, PDG 2013)

==== W (80.4 GeV), Z (91.2 GeV)

- IMPORTANT: No new physics!! *If there is any...*
- Four scalar light modes, a strong gap.
- Natural: further spontaneous symmetry breaking at $f > v = 246 \text{ GeV}$?

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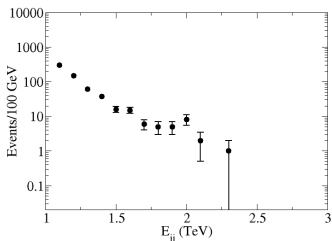
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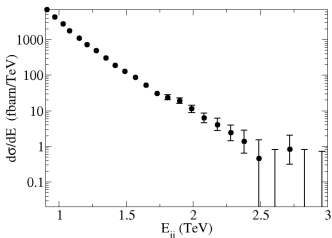
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ATLAS excess in two-jet events



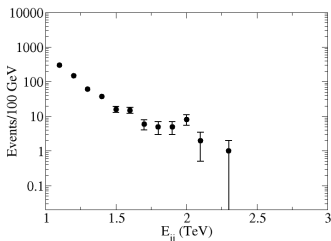
[ATLAS], 1506.00962 [hep-ex]



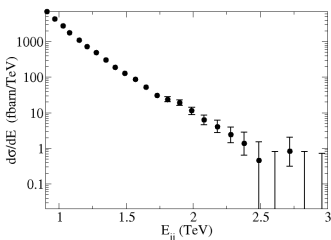
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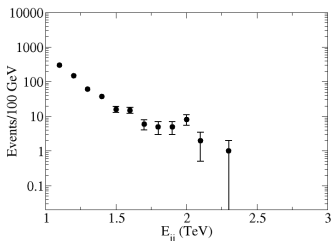
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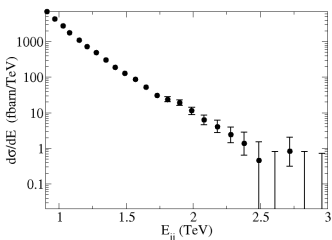
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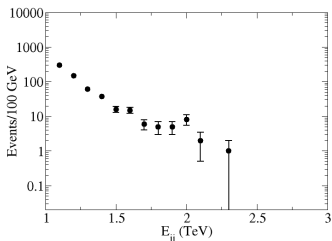
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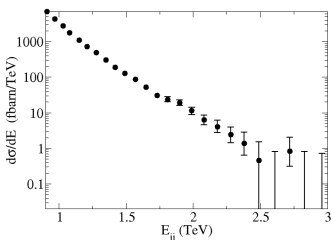
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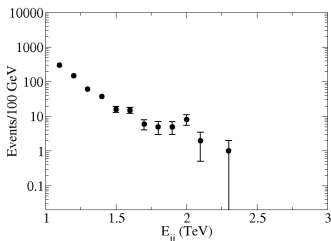
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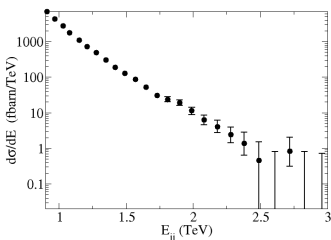
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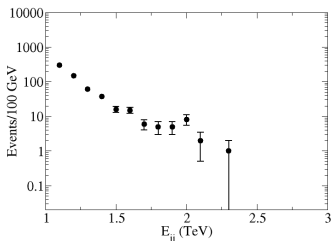
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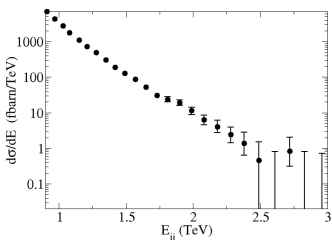
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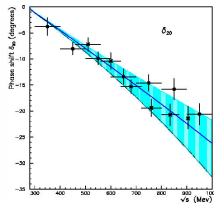
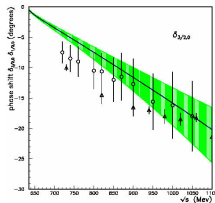
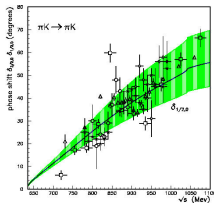
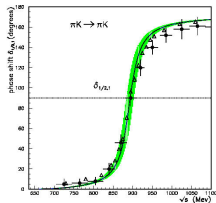
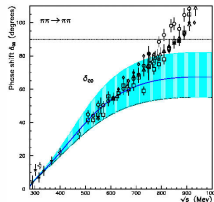
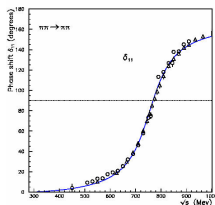
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Effective Field Theory + Unitarity: similarity with low-energy (i.e.: hadronic) physics

Chiral Perturbation Theory plus Dispersion Relations.

Simultaneous description of $\pi\pi \rightarrow \pi\pi$ and $\pi K\pi K \rightarrow \pi K\pi K$ up to 800-1000 MeV including resonances.

Lowest order ChPT (Weinberg Theorems) and even one-loop computations are only valid at very low energies.



A. Dobado, J.R. Peláez

Validity range of unitarization procedures

IJ	00	02	11	20	22
Method of choice	Any	N/D IK	IAM	Any	N/D IK

- The studied methods, excluding the naive K-matrix one, give compatible results inside their validity ranges.
- The IAM method cannot be used when $A^{(0)} = 0$, because it would give a vanishing value.
- The N/D and the IK methods cannot be used if $D + E = 0$, because in this case computing $A_L(s)$ and $A_R(s)$ is not possible.
- The naive K-matrix method,

$$A_0^K(s) = \frac{A_0(s)}{1 - iA_0(s)},$$

fails because it is not analytical in the 1st. Riemann sheet and, consequently, it is not a proper partial wave compatible with microcausality.

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We have no clue of what, how or if new physics...

Most general NLO Lagrangian for ω , h at low energy

$$\begin{aligned}\mathcal{L} = & \left[1 + 2a\frac{h}{v} + b\left(\frac{h}{v}\right)^2 \right] \frac{\partial_\mu \omega^a \partial^\mu \omega^b}{2} \left(\delta^{ab} + \frac{\omega^a \omega^b}{v^2} \right) \\ & + \frac{4a_4}{v^4} \partial_\mu \omega^a \partial_\nu \omega^a \partial^\mu \omega^b \partial^\nu \omega^b + \frac{4a_5}{v^4} \partial_\mu \omega^a \partial^\mu \omega^a \partial_\nu \omega^b \partial^\nu \omega^b \\ & + \frac{2d}{v^4} \partial_\mu h \partial^\mu h \partial_\nu \omega^a \partial^\nu \omega^a + \frac{2e}{v^4} \partial_\mu h \partial^\mu \omega^a \partial_\nu h \partial^\nu \omega^a \\ & + \frac{1}{2} \partial_\mu h \partial^\mu h + \frac{g}{v^4} (\partial_\mu h \partial^\mu h)^2\end{aligned}$$

Particular cases of the theory

- $a^2 = b = 1$, SM
- $a^2 = b = 0$, Higgsless ECL¹
- $a^2 = 1 - \frac{v^2}{f^2}$, $b = 1 - \frac{2v^2}{f^2}$, $SO(5)/SO(4)$ MCHM²
- $a^2 = b = \frac{v^2}{f^2}$, Dilaton³

¹See J. Gasser and H. Leutwyler, *Annal Phys.* **158** (1984) 142
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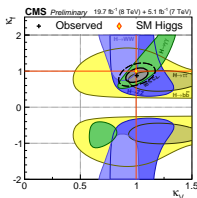
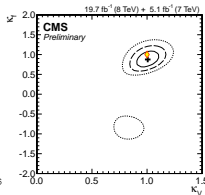
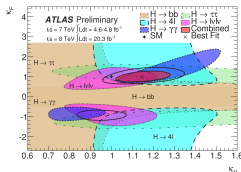
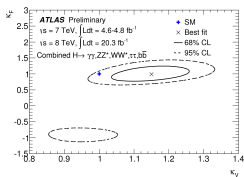
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Experimental bounds on low-energy constants

- As it would require measuring the coupling of two Higgses, there is no experimental bound over the value of b parameter⁴. Over a , at a confidence level of 2σ (95%),

- CMS⁵ $a \in (0.88, 1.15)$
- ATLAS⁶ $a \in (0.96, 1.34)$



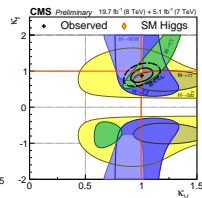
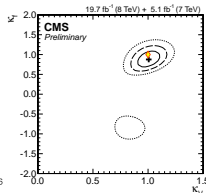
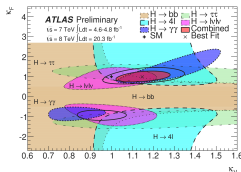
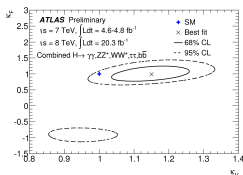
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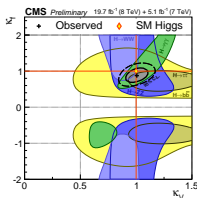
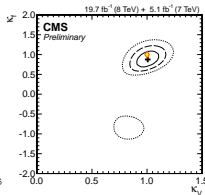
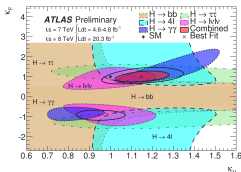
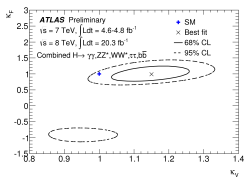
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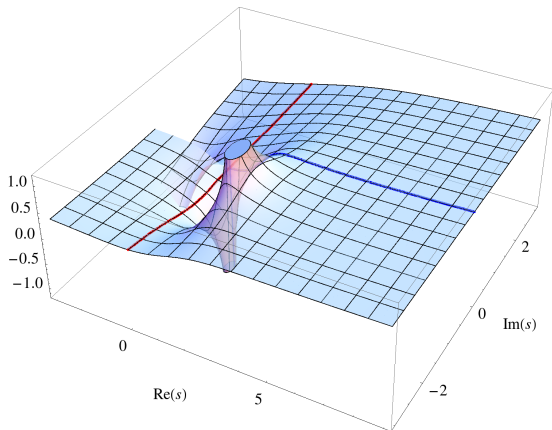
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Resonance from $W_L W_L \rightarrow hh$

$a = 1$, $b = 2$, IAM,
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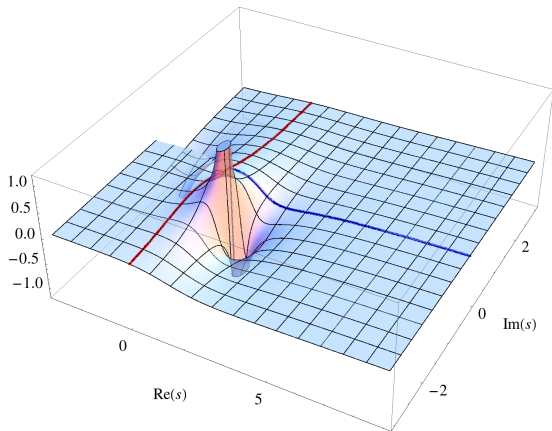


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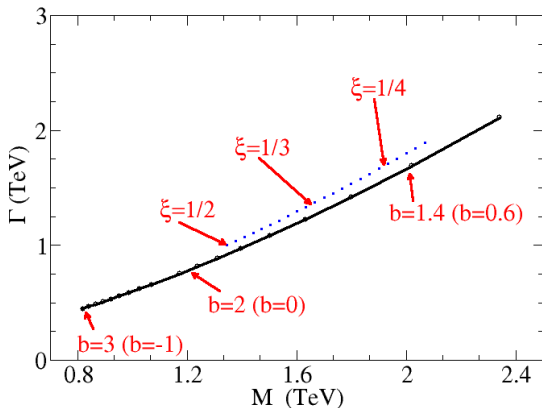
PRL **114** (2015) 221803



Motion of the resonance mass and width

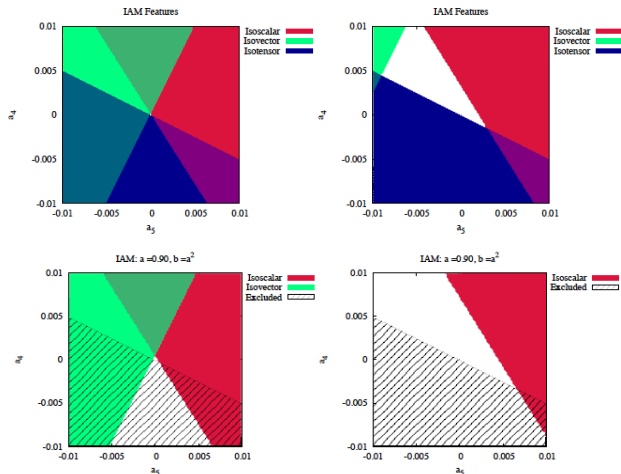
Dependence on b with $a^2 = 1$ fixed (upper curve) and for $a = 1\xi$ and $b = 12\xi$ with $\xi = v/f$ as in the MCHM (lower blue curve).

PRL **114** (2015) 221803

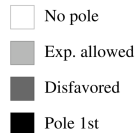
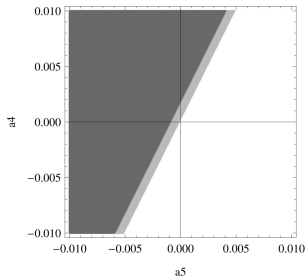
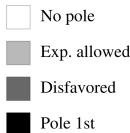
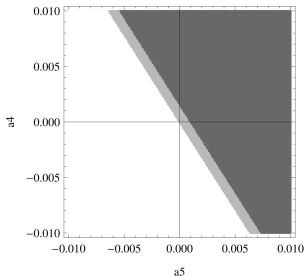


Resonances in $W_L W_L \rightarrow W_L W_L$ due to a_4 and a_5 paramet.

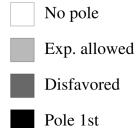
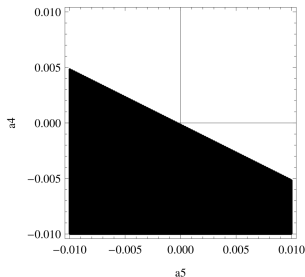
Espru, Yencho,
Mescia
PRD**88**, 055002
PRD**90**, 015035
At right, exclusion
regions include reso-
nances with
 $M_{S,V} < 600$ GeV.



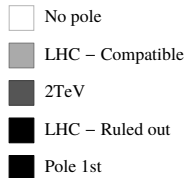
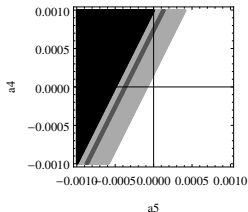
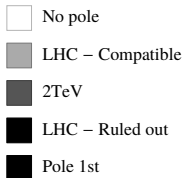
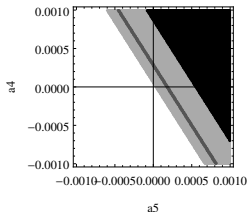
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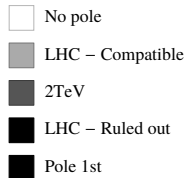
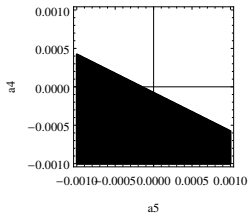
- $a = 0.90$, $b = a^2$
PRD **91** (2015) 075017
- From left, clockwise,
 $J = 00, 11, 20$
- Excluding resonances
 $M_S < 700 \text{ GeV}$, $M_V < 1.5 \text{ TeV}$



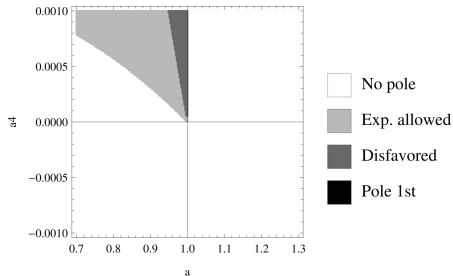
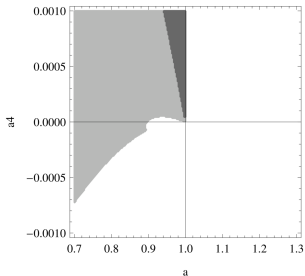
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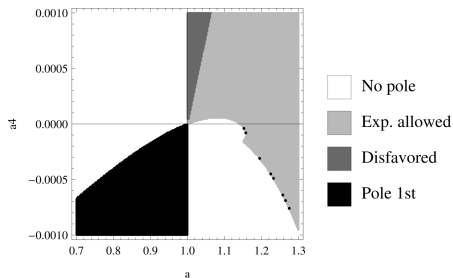
- $a = 0.95$, $b = a^2$
arXiv:1509.00441 [hep-ph]
- From left, clockwise,
 $IJ = 00, 11, 20$
- Excluding resonances
 $M_S < 700 \text{ GeV}$, $M_V < 1.5 \text{ TeV}$
- Compat. with P.Arnau, D.Espru,
F.Mescia, 1508.00174 [hep-ph]



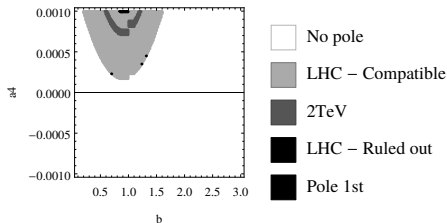
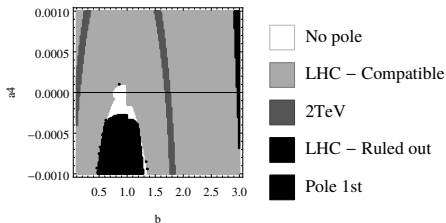
Resonances in $W_L W_L \rightarrow W_L W_L$ due to a and a_4 parameters



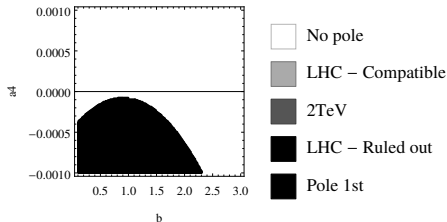
- $b = a^2$
PRD **91** (2015) 075017
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 $J = 00, 11, 20$
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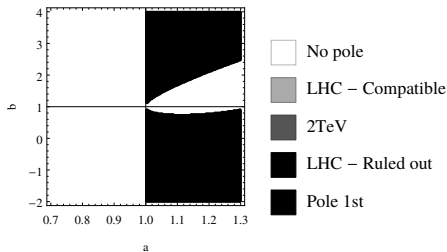
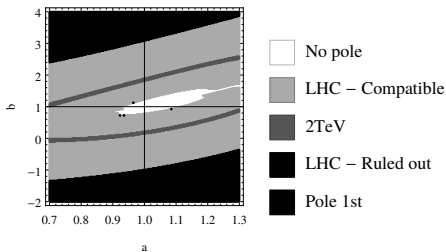
Resonances in $W_L W_L \rightarrow W_L W_L$ due to b and a_4 parameters



- $a = 0.95$
arXiv:1509.04725 [hep-ph]
- From left, clockwise,
 $IJ = 00, 11, 20$
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Resonances in $W_L W_L \rightarrow W_L W_L$ due to a and b parameters

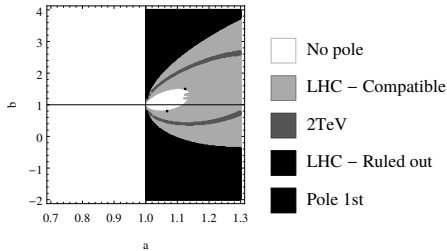


- PRL & PRD **91** (2015) 075017, arXiv:1509.00441 [hep-ph]

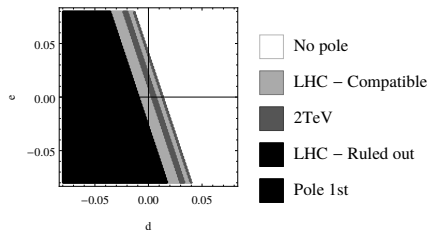
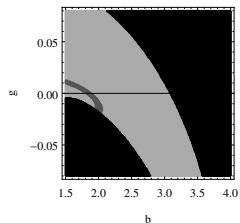
- From left, clockwise, $IJ = 00, 11, 20$

- Excluding resonances $M_S < 700 \text{ GeV}$, $M_V < 1.5 \text{ TeV}$

- Constraint over b even without data about $W_L W_L \rightarrow hh$ and $hh \rightarrow hh$ scattering processes.

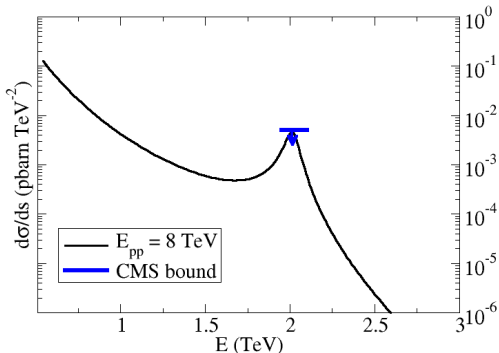


Resonances in $W_L W_L \rightarrow W_L W_L$ due to b , g , d and e parameters



Effective Theory, PRD **91** (2015) 075017, isoscalar channels ($I = J = 0$).

Compatibility of a 2 TeV resonance with CMS bounds



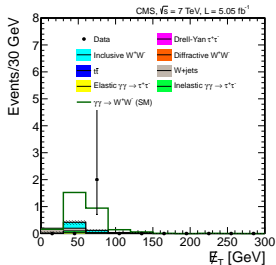
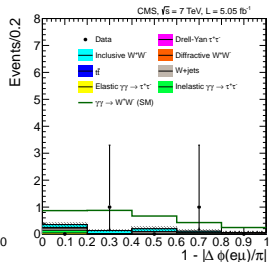
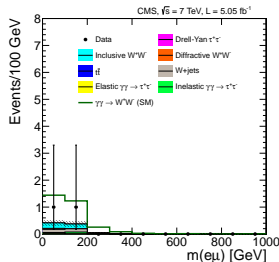
$a = 0.9$, $b = a^2$, $a_4 = 7 \times 10^{-4}$, all the other NLO parameters set to zero (scale $\mu = 3$ TeV). Plotted against the CMS bound⁷.

A. Dobado, F. K. Guo and F. J. Llanes-Estrada, arXiv:1508.03544 [hep-ph].

⁷[CMS Collaboration], JHEP **1408**, 173 (2014)

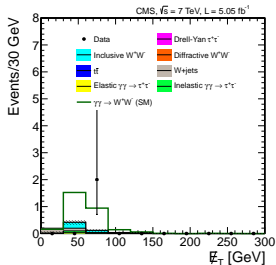
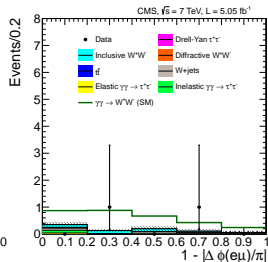
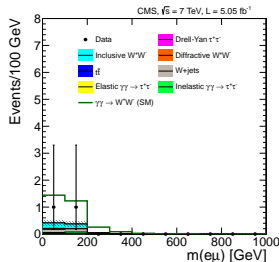
- We also consider⁸ the case of the $\gamma\gamma \rightarrow W_L^+ W_L^-$ and $\gamma\gamma \rightarrow Z_L Z_L$ scattering (unitarization is work in progress).

- Current efforts for measuring these channels (although only 2 events measured).
- Graphs from CMS, JHEP **07** (2013) 116.
- Wait for LHC Run-II and CMS-TOTEM.



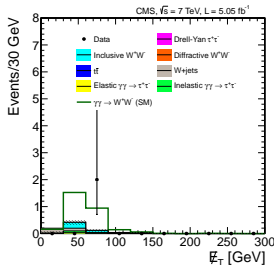
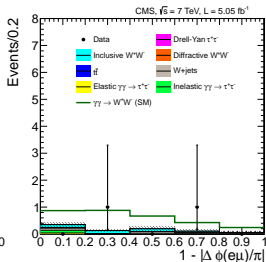
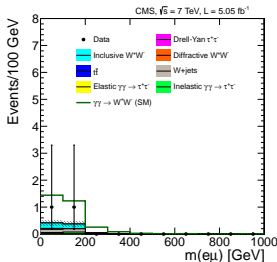
⁸R.L. Delgado, A. Dobado, M.J. Herrero, J.J. Sanz-Cillero, JHEP **1407** (2014) 149

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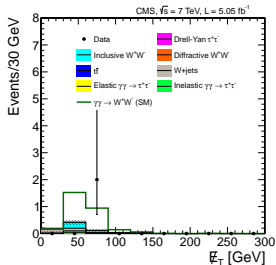
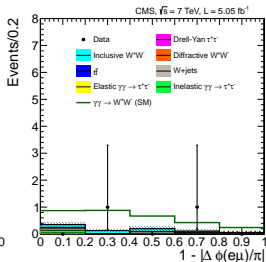
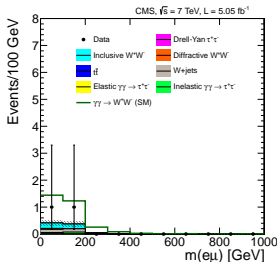
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- One loop computation for the process $\gamma\gamma \rightarrow \omega_L^a \omega_L^b$.
- Simple result compared with the complexity of the computation.

$$\begin{aligned}\mathcal{M} &= ie^2(\epsilon_1^\mu \epsilon_2^\nu T_{\mu\nu}^{(1)})A(s, t, u) + ie^2(\epsilon_1^\mu \epsilon_2^\nu T_{\mu\nu}^{(2)})B(s, t, u) \\ T_{\mu\nu}^{(1)} &= \frac{s}{2}(\epsilon_1 \epsilon_2) - (\epsilon_1 k_2)(\epsilon_2 k_1) \\ T_{\mu\nu}^{(2)} &= 2s(\epsilon_1 \Delta)(\epsilon_2 \Delta) - (t - u)^2(\epsilon_1 \epsilon_2) \\ &\quad - 2(t - u)[(\epsilon_1 \Delta)(\epsilon_2 k_1) - (\epsilon_1 k_2)(\epsilon_2 \Delta)] \\ \Delta^\mu &= p_1^\mu - p_2^\mu\end{aligned}$$

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$$M(\gamma\gamma \rightarrow zz)_{\text{LO}} = 0$$

$$A(\gamma\gamma \rightarrow zz)_{\text{NLO}} = \frac{2ac_\gamma^r}{v^2} + \frac{(a^2 - 1)}{4\pi^2 v^2}$$

$$B(\gamma\gamma \rightarrow zz)_{\text{NLO}} = 0$$

$$A(\gamma\gamma \rightarrow \omega^+\omega^-)_{\text{LO}} = 2sB(\gamma\gamma \rightarrow \omega^+\omega^-)_{\text{LO}} = -\frac{1}{t} - \frac{1}{\mu}$$

$$A(\gamma\gamma \rightarrow \omega^+\omega^-)_{\text{NLO}} = \frac{8(a_1^r - a_2^r + a_3^r)}{v^2} + \frac{2ac_\gamma^r}{v^2} + \frac{(a^2 - 1)}{8\pi^2 v^2}$$

$$A(\gamma\gamma \rightarrow \omega^+\omega^-)_{\text{NLO}} = 0$$

- The next steps will be...
 - implement the unitarized scattering amplitudes in a Monte Carlo framework,
 - introduce fermion loops (work in progress),
 - non-vanishing values for M_H , M_W , M_Z ,
 - and a full computation without using the equivalence theorem.
- Besides, we are working on the $t\bar{t} \rightarrow \omega_L \omega_L$ channel.
- In collaboration with María Jesús Herrero and Juan José Sanz Cillero (UAM - IFT/CSIC), we are unitaryzing the $\gamma\gamma$ scattering amplitudes.
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Conclusions

- New scalar particle + mass gap
- New physics would very likely imply strong interactions, in elastic $W_L W_L$ and inelastic $\rightarrow hh$ scattering.
- For $a^2 = b \neq 1$, strong elastic interactions are expected for $W_L W_L$, and a second, broad scalar analogous to the σ in nuclear physics possibly appears. We identify a pole at 800 GeV or above in the second Riemann sheet very clearly, the question is whether it corresponds to a physical particle since it is so broad.
- Even if $a \simeq 1$, with small λ_i (higher powers of h), but we allow $b > a^2$, one can have strong dynamics resonating between the $W_L W_L$ and hh channels, likewise possibly generating a new scalar pole of the scattering amplitude in the sub-TeV region.
- This fact allows to constrain b even in the absence of data about $W_L W_L \rightarrow hh$ and $hh \rightarrow hh$, just looking at the $W_L W_L$ scattering.
- Finally, as an exception, for $a^2 = b = 1$, we recover the Minimal Standard Model with a light Higgs which is weakly interacting.

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- Higgsless model (now experimentally excluded) \rightarrow unitarity violation in WW scattering \rightarrow new physics.
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Back Slides

Partial Waves

The form of the partial wave is

$$\begin{aligned} A_{IJ}(s) &= \frac{1}{64\pi} \int_{-1}^1 d(\cos \theta) P_J(\cos \theta) A_I(s, t, u) \\ &= A_{IJ}^{(0)} + A_{IJ}^{(1)} + \dots \end{aligned}$$

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As $A_{IJ}(s)$ must be scale independent,

$$B(\mu) = B(\mu_0) + (D + E) \log \frac{\mu^2}{\mu_0^2}$$

Unitarization procedures

$$A^{IAM}(s) = \frac{[A^{(0)}(s)]^2}{A^{(0)}(s) - A^{(1)}(s)}$$

$$A^{N/D}(s) = \frac{A^{(0)}(s) + A_L(s)}{1 - \frac{A_R(s)}{A^{(0)}(s)} + \frac{1}{2}g(s)A_L(-s)}$$

$$A^{IK}(s) = \frac{A^{(0)}(s) + A_L(s)}{1 - \frac{A_R(s)}{A^{(0)}(s)} + g(s)A_L(s)}$$

$$A_0^K(s) = \frac{A_0(s)}{1 - iA_0(s)}$$

$$A_L(s) = \pi g(-s)Ds^2$$

$$A_R(s) = \pi g(s)Es^2$$

$$g(s) = \frac{1}{\pi} \left(\frac{B(\mu)}{D+E} + \log \frac{-s}{\mu^2} \right)$$

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Validity range of unitarization procedures

IJ	00	02	11	20	22
Method of choice	Any	N/D IK	IAM	Any	N/D IK

- The IAM method cannot be used when $A^{(0)} = 0$, because it would give a vanishing value.
- The N/D and the IK methods cannot be used if $D + E = 0$, because in this case computing $A_L(s)$ and $A_R(s)$ is not possible.
- The naive K-matrix method,

$$A_0^K(s) = \frac{A_0(s)}{1 - iA_0(s)},$$

fails because it is not analytical in the first Riemann sheet and, consequently, it is not a proper partial wave compatible with microcausality.

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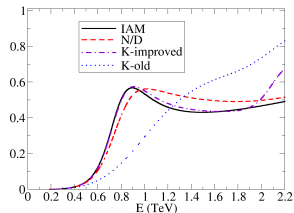
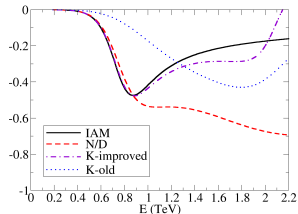
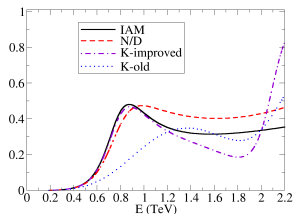
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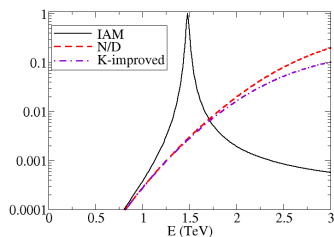
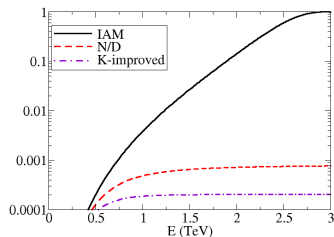
Scalar-isoscalar channels



From left to right and top to bottom, elastic $\omega\omega$, elastic hh , and cross channel $\omega\omega \rightarrow hh$, for $a = 0.88$, $b = 3$, $\mu = 3$ TeV and all NLO parameters set to 0.

PRL **114** (2015) 221803, PRD **91** (2015) 075017.

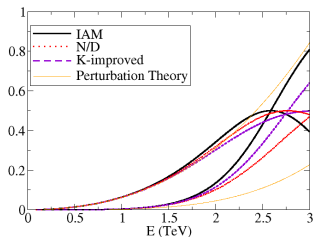
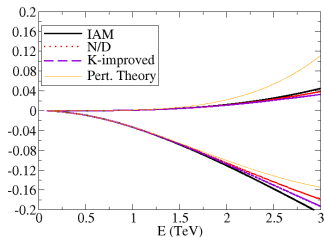
Vector-isovector channels



We have taken $a = 0.88$ and $b = 1.5$, but while for the left plot all the NLO parameters vanish, for the right plot we have taken $a_4 = 0.003$, known to yield an IAM resonance according to the Barcelona group, PRD **90** (2014) 015035.

PRD **91** (2015) 075017.

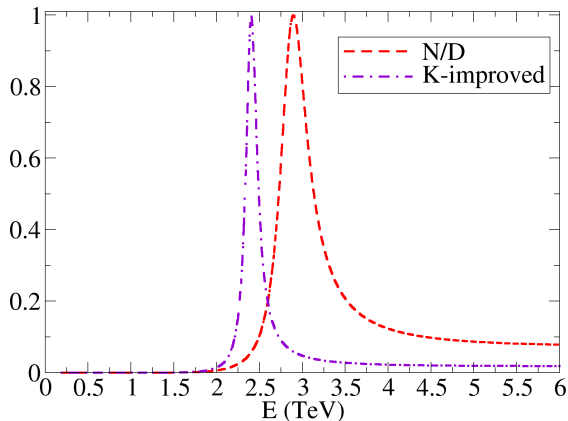
Scalar-isotensor channels ($IJ = 20$)



From left to right, $a = 0.88$, $a = 1.15$. We have taken $b = a^2$ and the NLO parameters set to zero. Both real and imaginary part shown. Real ones correspond to bottom lines at left and upper at low E at right.

PRD **91** (2015) 075017.

Isotensor-scalar channels ($IJ = 02$)



$a = 0.88$, $b = a^2$, $a_4 = -2a_5 = 3/(192\pi)$, all the other NLO param. set to zero.
PRD **91** (2015) 075017.

I) IAM method

This method needs a NLO computation,

$$\tilde{t}^\omega = \frac{t_0^\omega}{1 - \frac{t_0^\omega}{t_1^\omega}},$$

where

$$t_1^\omega = s^2 \left(D \log \left[\frac{s}{\mu^2} \right] + E \log \left[\frac{-s}{\mu^2} \right] + (D + E) \log \left[\frac{\mu^2}{\mu_0^2} \right] \right)$$

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Check at tree level

We have checked⁹, for the tree level case,

$$\begin{aligned}\mathcal{L} &= \frac{1}{2}g(\varphi/f)\partial_\mu\omega^a\partial^\mu\omega^b\left(\delta_{ab} + \frac{\omega^a\omega^b}{v^2 - \omega^2}\right) \\ &\quad + \frac{1}{2}\partial_\mu\varphi\partial^\mu\varphi - \frac{1}{2}M_\varphi^2\varphi^2 - \lambda_3\varphi^3 - \lambda_4\varphi^4 + \dots \\ g(\varphi/f) &= 1 + \sum_{n=1}^{\infty} g_n \left(\frac{\varphi}{f}\right)^n = 1 + 2\alpha\frac{\varphi}{f} + \beta\left(\frac{\varphi}{f}\right)^2 + \dots\end{aligned}$$

where $a \equiv \alpha v/f$, $b = \beta v^2/f^2$, and so on, the concordance with the methods

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II) K matrix

$$\tilde{T} = T(1 - J(s)T)^{-1}, \quad , J(s) = -\frac{1}{\pi} \log \left[\frac{-s}{\Lambda^2} \right],$$

so that, for \tilde{t}_ω ,

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III) Large N

$N \rightarrow \infty$, with v^2/N fixed. The amplitude A_N to order $1/N$ is a Lippmann-Schwinger series,

$$A_N = A - A \frac{N!}{2} A + A \frac{N!}{2} A \frac{N!}{2} A - \dots$$

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Note: actually, $N = 3$. For the (iso)scalar partial wave (chiral limit, $I = J = 0$),

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(elastic scattering at tree level only $\beta = \alpha^2$. See ref. J.Phys. G41 (2014) 025002). Ansatz

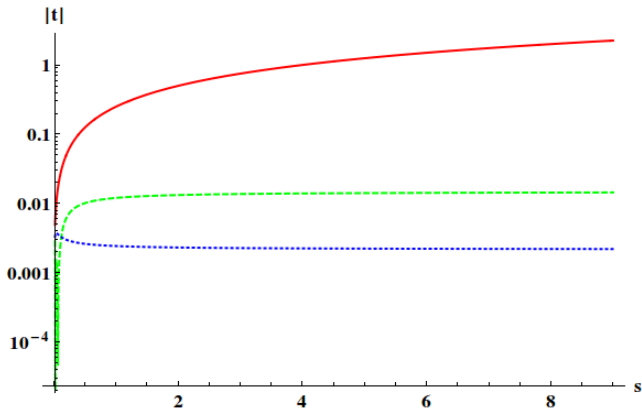
$$\tilde{t}^\omega(s) = \frac{N(s)}{D(s)},$$

where $N(s)$ has a left hand cut (and $\text{Im } N(s > 0) = 0$)
 $D(s)$ has a right hand cut (and $\Im D(s < 0) = 0$);

$$D(s) = 1 - \frac{s}{\pi} \int_0^\infty \frac{ds' N(s')}{s'(s' - s - i\epsilon)}$$

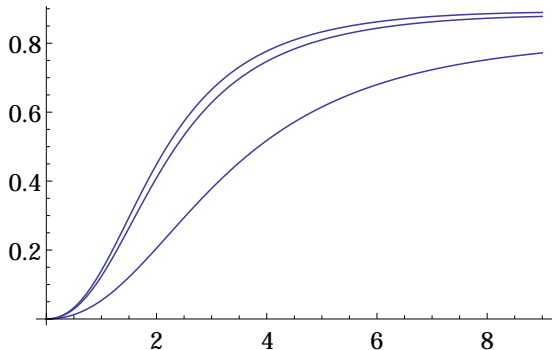
$$N(s) = \frac{s}{\pi} \int_{-\infty}^0 \frac{ds' \text{Im } N(s')}{s'(s' - s - i\epsilon)}$$

Coupled channels, tree level amplitudes



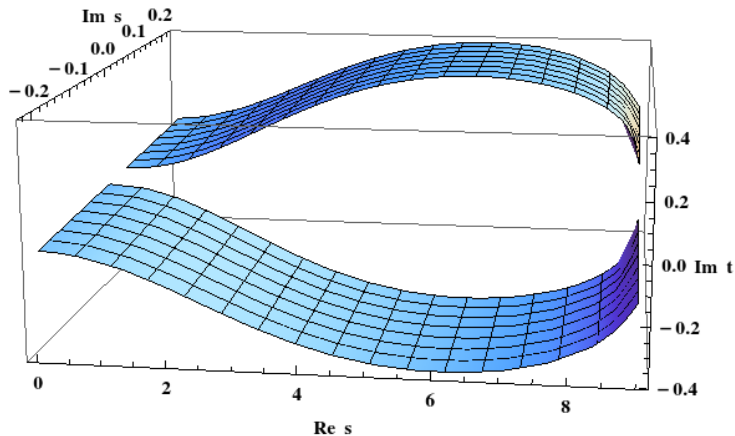
$f = 2v$, $\beta = \alpha^2 = 1$, $\lambda_3 = M_\varphi^2/f$, $\lambda_4 = M_\varphi^2/f^2$. OX axis: s in TeV^2 .

Tree level, modulus of \tilde{t}_ω , K matrix

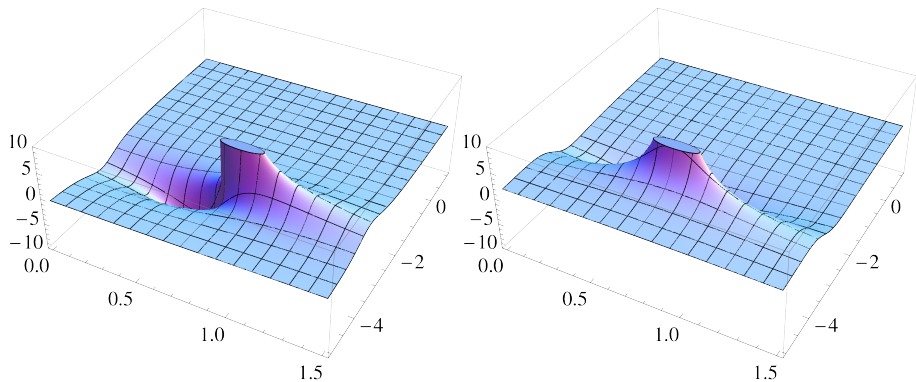


- All units in TeV.
- From top to bottom, $f = 1.2, 0.8, 0.4$ TeV
- $\Lambda = 3$ TeV
- $\mu = 100$ GeV

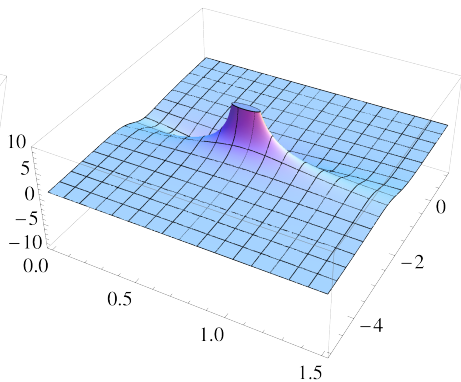
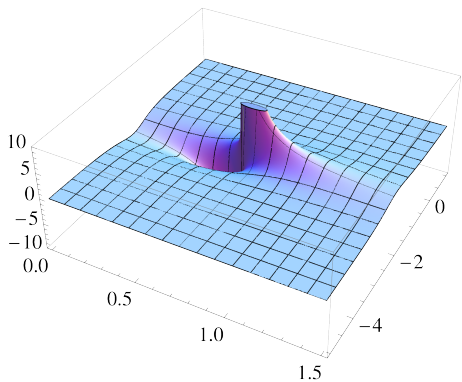
$\text{Im } t_\omega$ in the N/D method,
 $f = 1 \text{ TeV}$, $\beta = 1$, $m = 150 \text{ GeV}$



Re t_ω and Im t_ω , large N , $f = 400$ GeV



Re t_ω and Im t_ω , large N , $f = 4$ TeV



Tree level, motion of the pole position of t_ω
K-matrix, $M_\phi = 125 \text{ GeV}$, $f \in (250 \text{ GeV}, 6 \text{ TeV})$

