

A spatial likelihood analysis for MAGIC skymaps

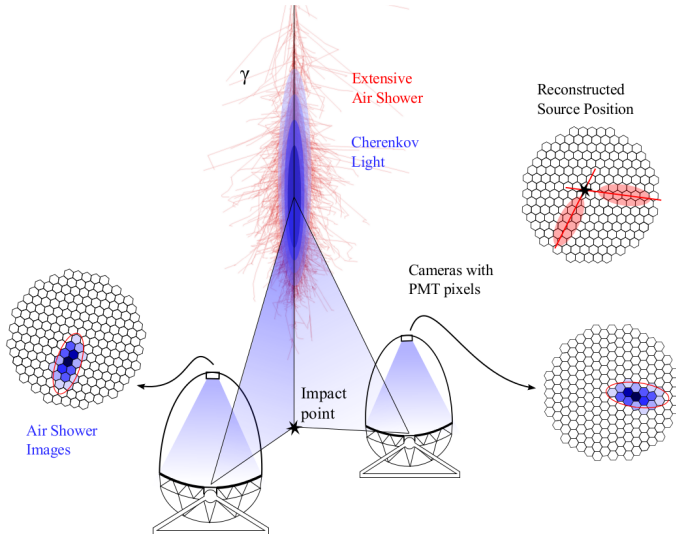
DPG Frühjahrstagung 2016, Hamburg

Marcel C. Strzys,
I. Vovk, and C. Fruck for the MAGIC Collaboration

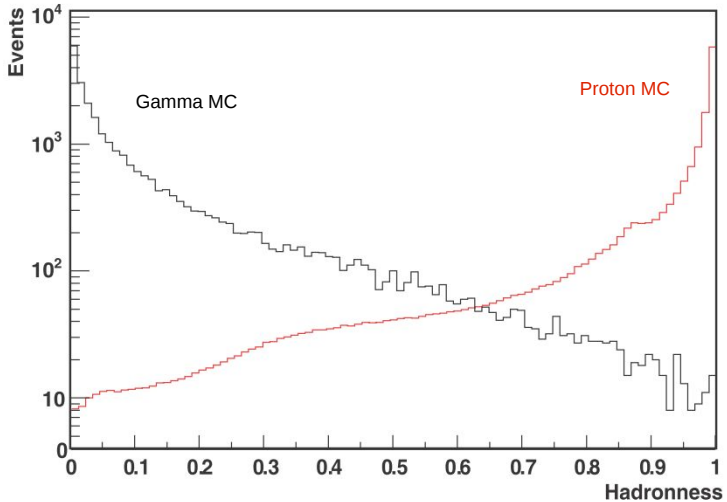
Max-Planck-Institut für Physik

03.02.2016

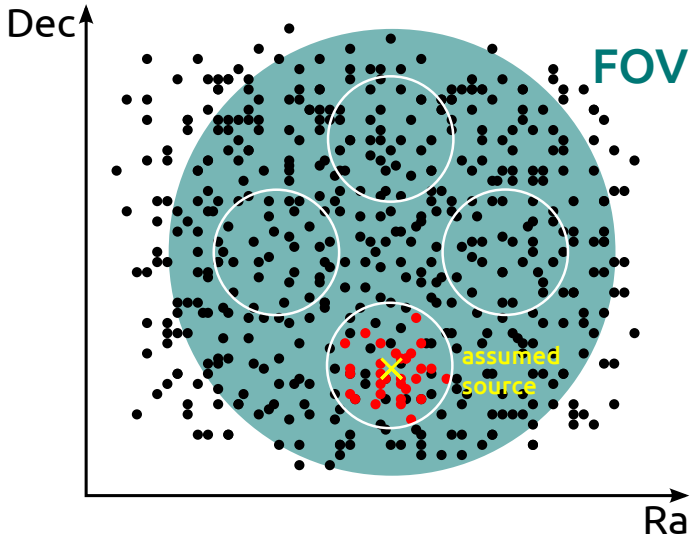
Cherenkov telescope - counting experiments



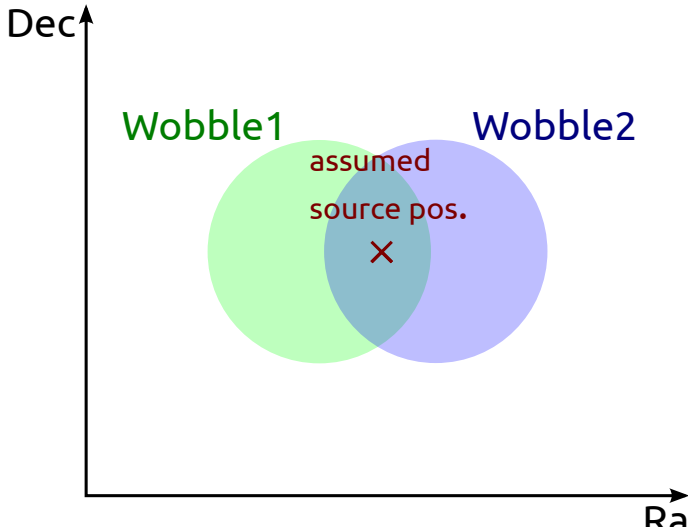
Background - no escape



Counting events - Signal & Background

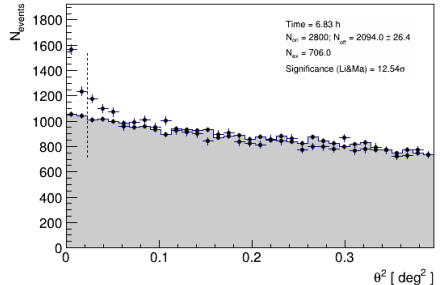


Counting events - Signal & Background



Standard Analysis

- ▶ parametrise distance of events to source
- ▶ significance based on Gaussian likelihood ratio test
- ▶ sky position of excess $\Rightarrow$ skymap
- ▶ excess events in each energy bin $\Rightarrow$ spectrum



Standard Analysis

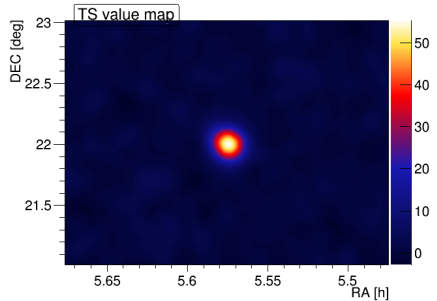
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$$\tilde{S}_{Li, Ma} = \sqrt{2} \left\{ N_{on} \ln \left[\frac{1 + \alpha}{\alpha} \left(\frac{N_{on}}{N_{on} + N_{off}} \right) \right] + N_{off} \ln \left[(1 + \alpha) \left(\frac{N_{off}}{N_{on} + N_{off}} \right) \right] \right\}^{\frac{1}{2}}$$

Li, Ma ApJ 1983 272 317

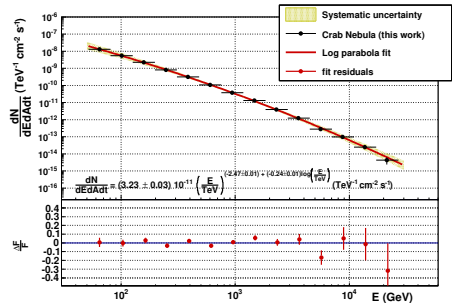
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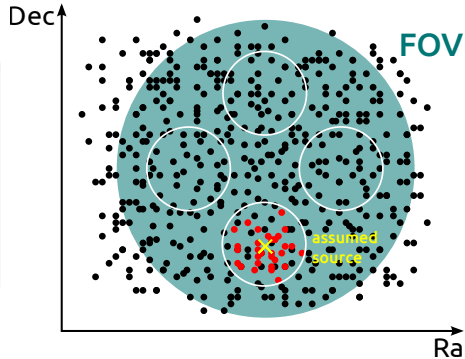
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Aleksić et al. JHEAp 2015 5 30A

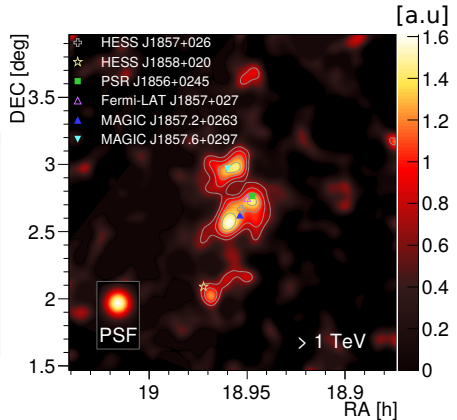
Issues of the “classical” approach

- ▶ θ^2 requires source to be roundish
- ▶ source extends beyond wobble distance
- ▶ overlapping sources



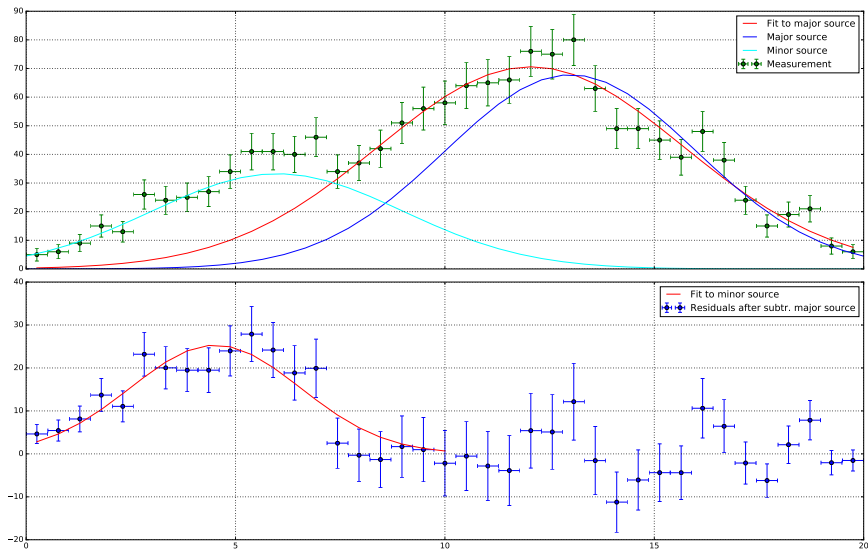
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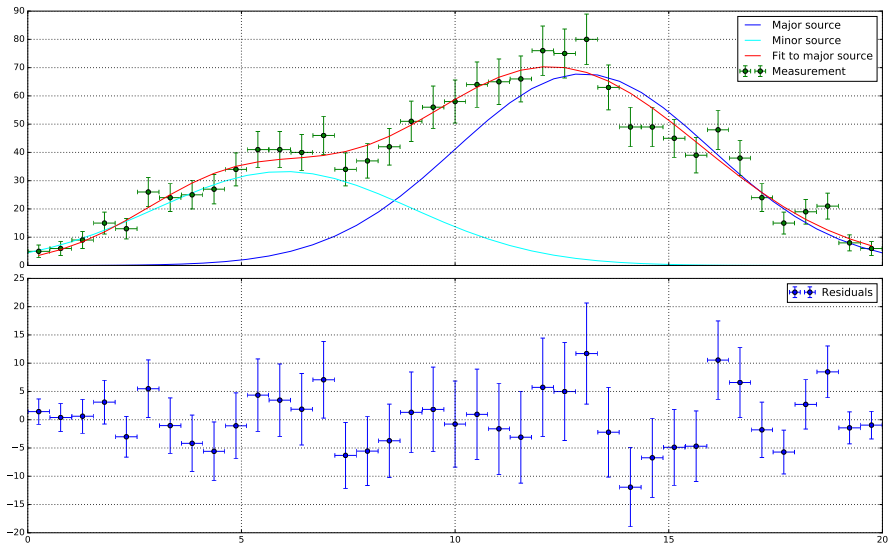


Aleksić et al. A&A 571A 96M

Overlapping sources or sub-structures



Overlapping sources or sub-structures



Poisson likelihood

What to fit?

$$\ln L = \sum_{ij} n_{ij} \ln(\theta_{ij}) - \sum_{ij} \theta_{ij} - \sum \ln(n_{ij}!)$$

with measured counts n in bin (i, j) and expected value of θ_{ij} .

Likelihood ratio test

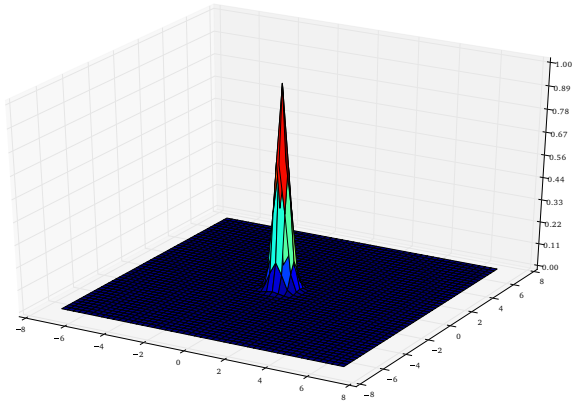
$$T_s = -2 (\ln L_0 - \ln L_1)$$

$$\sim \chi_n^2 \text{ distributed (Wilk's theorem)}$$

Fermi-LAT like approach: Mattox et al. ApJ 1996 461 396M

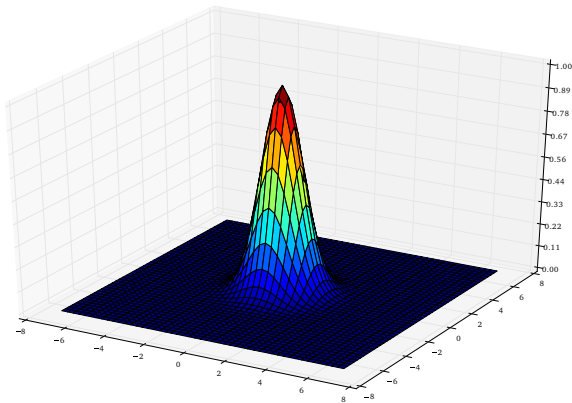
How to construct the model

- ▶ source model
- ▶ convolve with PSF
- ▶ add background
- ▶ scale with acceptance



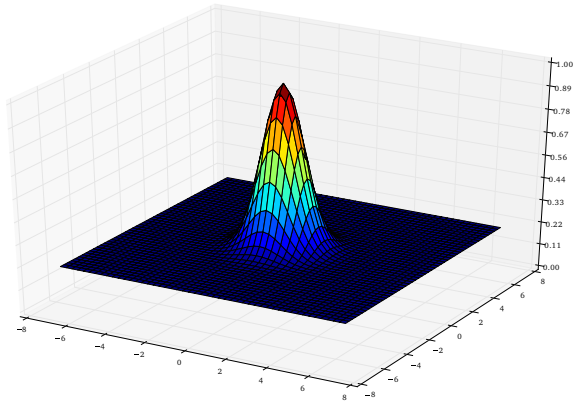
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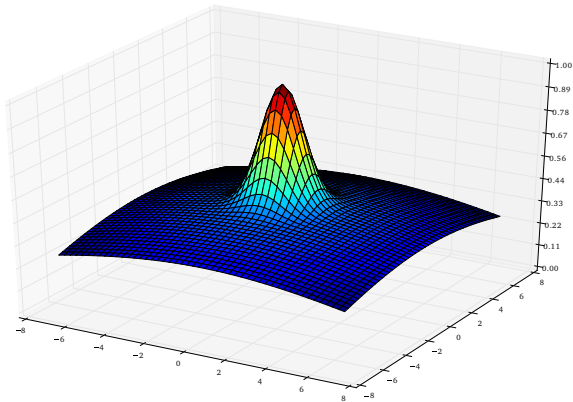
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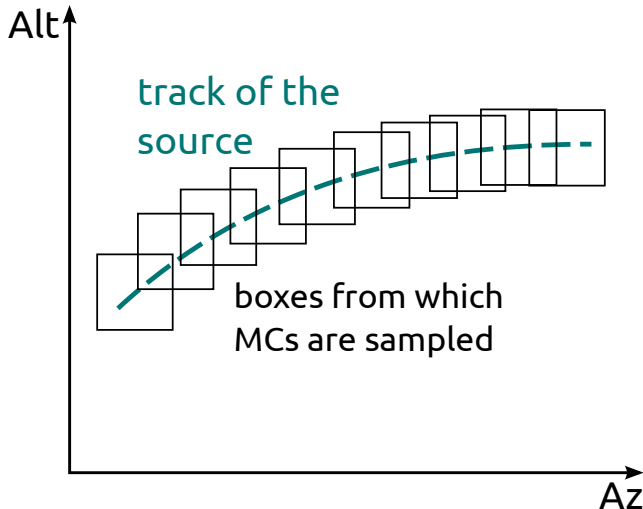


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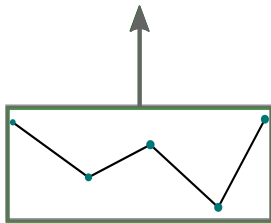
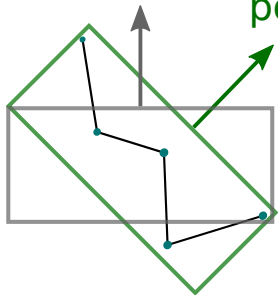


Get the IRF right $\Rightarrow$ Alt/Az dependence

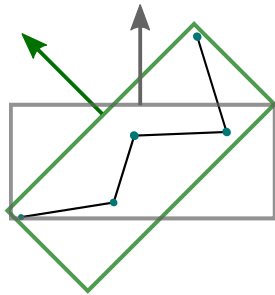


Mind rotational frames - Alt/Az vs. Ra/Dec

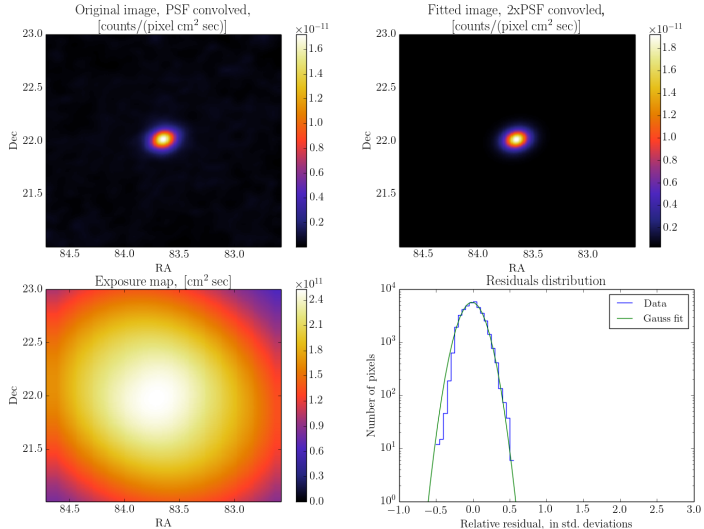
to north
pole



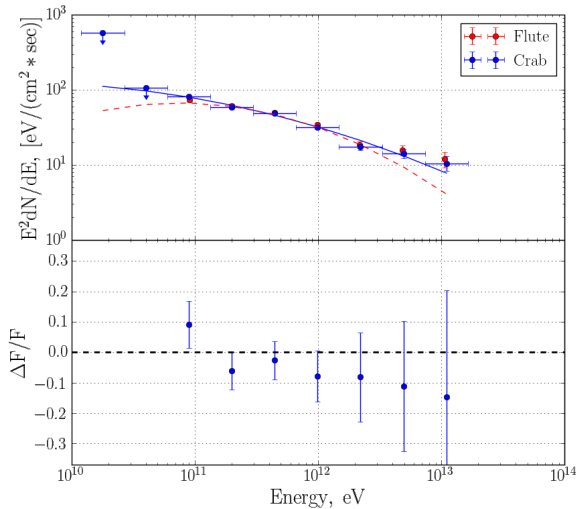
to zenith



Example on the standard candle - Crab Nebula



Example on the standard candle - Crab Nebula



Thank you for your attention and interest!

- ▶ “classical” analysis method has weaknesses for non-point sources
- ▶ Poisson likelihood offers versatile and consistent approach
- ▶ construction of IRF and models non-trivial task