

Dark Matter (and Dark Energy)

- Inventory of the Universe
- the expanding Universe
- Evidence for the Existence of Dark Matter:
 - rotational curves of spiral Galaxies
 - microwave background and cosmic energy density
 - galaxy clusters
- cosmological constraints
- DM: particle candidates and searches
- example: the CRESST experiment

Inventory of the Universe:

(from: CMB, SN Ia, lensing, BAO,...)

Age: 13.798 ± 0.037 Billion years

matter fraction: $31.7\% \pm 0.4\%$ (total)

$4.9\% \pm 0.1\%$ (baryonic matter)

$0.5\% \pm 0.1\%$ (luminous matter)



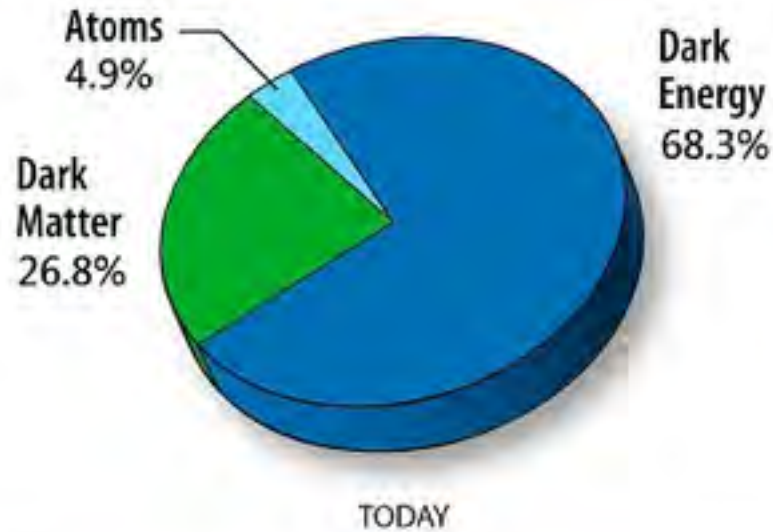
Dark Matter: $26.8\% \pm 0.4\%$ (unknown; non-baryonic!)

Dark Energy: $68.3\% \pm 1\%$ (unknown!)

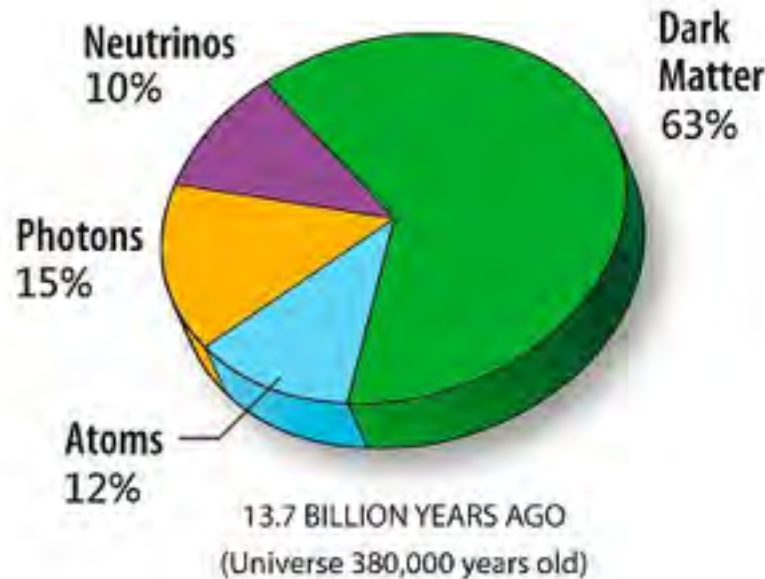
candidates for Dark Matter:

- HDM: massive Neutrinos
- CDM: Axions, SUSY-WIMPs

Inventory of the Universe (PLANCK):



today
 $t \sim 13.7 \cdot 10^9 \text{ y}$



$t \sim 380.000 \text{ y}$



if it's not
dark
it doesn't
matter

The expanding Universe

Hubble's Law:

$$v_{\text{expansion}} = H_0 \cdot \text{distance}$$

Hubble Constant:

$$H_0 = h \cdot 100 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

experimental value:

$$h = 0.683 \pm 0.010$$

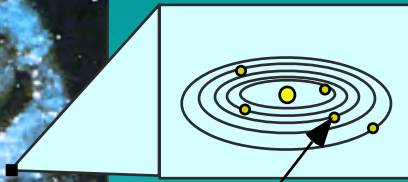
cosmic distances:

$$\begin{aligned} 1 \text{ Mpc} &= 3.26 \cdot 10^6 \text{ yr} \\ &= 3.08 \cdot 10^{22} \text{ m} \end{aligned}$$

expansion age of the Universe:

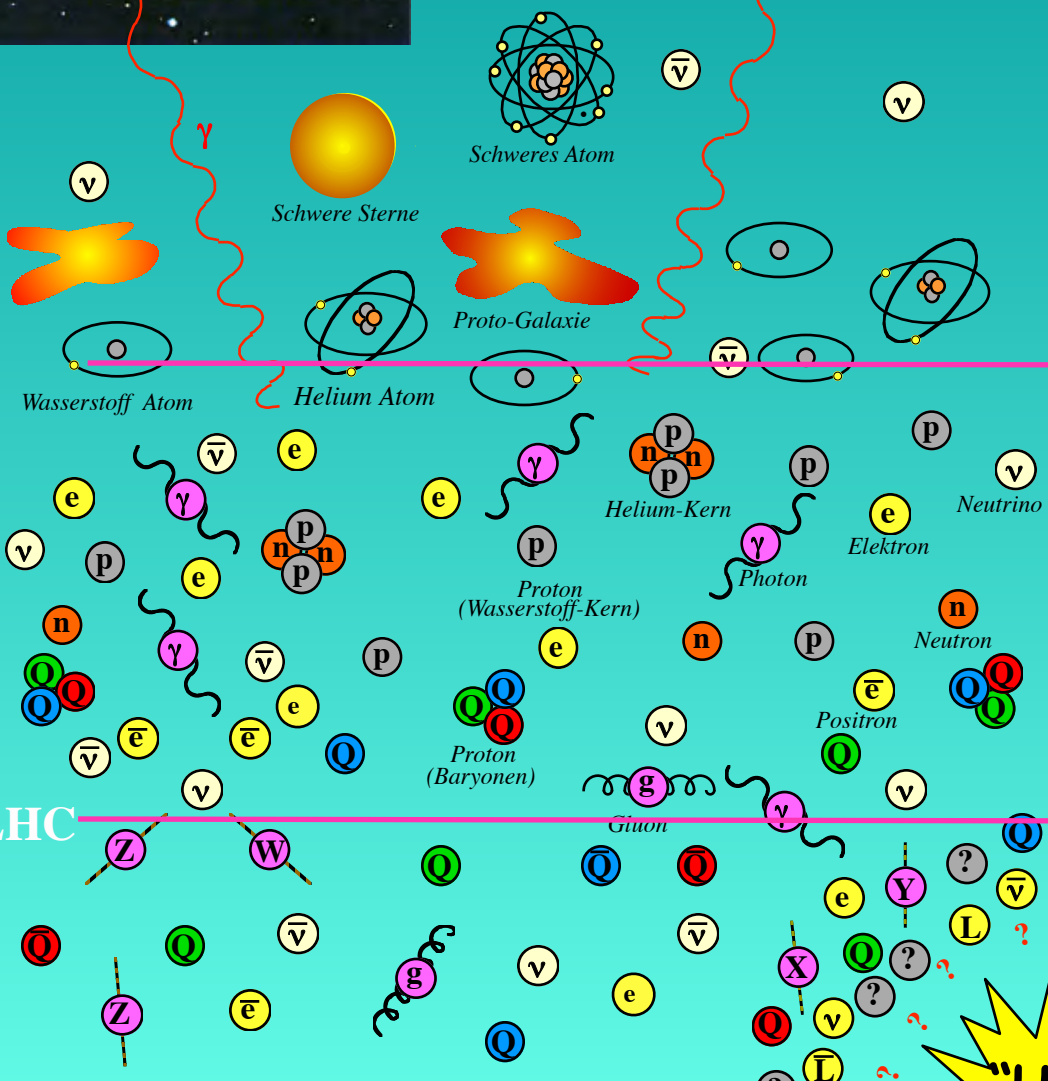
$$t_0 \sim H_0^{-1} = h^{-1} 9.78 \cdot 10^9 \text{ yr}$$

The expanding Universe



Wir sind hier

Zeit



Temperatur	Alter
2.7 K	13.7 Milliarden Jahre

GEGENWART

erste Supernovae

Entstehung von Sternen und Galaxien

11 K	1 Milliarde Jahre
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UNIVERSUM WIRD TRANSPARENT

Bildung von Atomen.
Entkopplung von Strahlung und Materie.

1.000 K	300 000 Jahre
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Nukleosynthese von Helium
Positronen verschwinden

10^{10} K	1 sec.
-------------	--------

Formation von Protonen und Neutronen
Antiquarks verschwinden

10^{15} K	10^{-10} sec
-------------	----------------

Asymmetry $Q-Q \bar{L}-L$

10^{27} K	10^{-34} sec
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Inflation

GROSSE VEREINHEITLICHUNG

10^{31} K	10^{-43} sec
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QUANTEN-GRAVITATION



Astronomie
Teilchenbeschleuniger

LHC

The expanding Universe

components of cosmic matter- and energy-density

contribution ρ of matter components to
total density of the universe:

$$\Omega = \rho / \rho_{\text{crit}}$$

critical density:

$$\begin{aligned}\rho_{\text{crit}} &= 3H_0^2 / (8\pi G_N) \\ &= h^2 1.88 \times 10^{-29} \text{ g cm}^{-3}\end{aligned}$$

$\Omega = 1$: euclidian geometry („flat universe“)

$\Omega < 1$: negative curvature of space („open universe“)

$\Omega > 1$: positive curvature of space („closed universe“)

Global Cosmic Geometry

positive
curvature

$$k = +1$$

$$\Omega_{\text{tot}} > 1$$



negative curvature

$$k = -1, \Omega_{\text{tot}} < 1$$



Euclidean
(flat)

$$k = 0$$

$$\Omega_{\text{tot}} = 1$$



Favored by

⇒ **Inflationary cosmological models**

⇒ **Recent cosmic microwave background measurements**

evidence for existence of Dark Matter

1. cosmological arguments

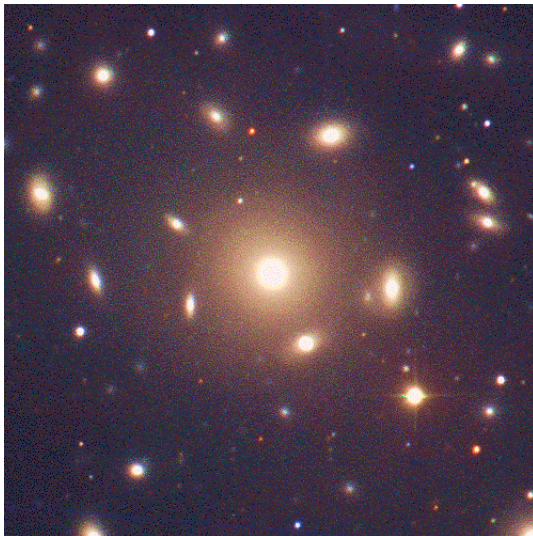
$\Omega_{\text{tot}} = 1$ because,
in an expanding universe,
 Ω_{tot} quickly develops away from 1,
towards 0 or ∞ .

if today $\Omega_{\text{tot}} \sim 1$,
then $\Omega_{\text{tot}} = 1$ is most probable
exact solution.

evidence for existence of Dark Matter

2. Dark Matter in galaxy clusters (Zwicky 1933):

a gravitationally bound many-particle system in equilibrium obeys the Virial Theorem.



Coma Galaxy Cluster

$$\text{Virial Theorem:} \quad 2\langle E_{kin} \rangle = -\langle E_{grav} \rangle$$

$$E_{kin} = mv^2 / 2, \quad E_{grav} = G_N M_r m / r$$

$$\Rightarrow \langle v^2 \rangle \approx G_N M \langle r^{-1} \rangle$$

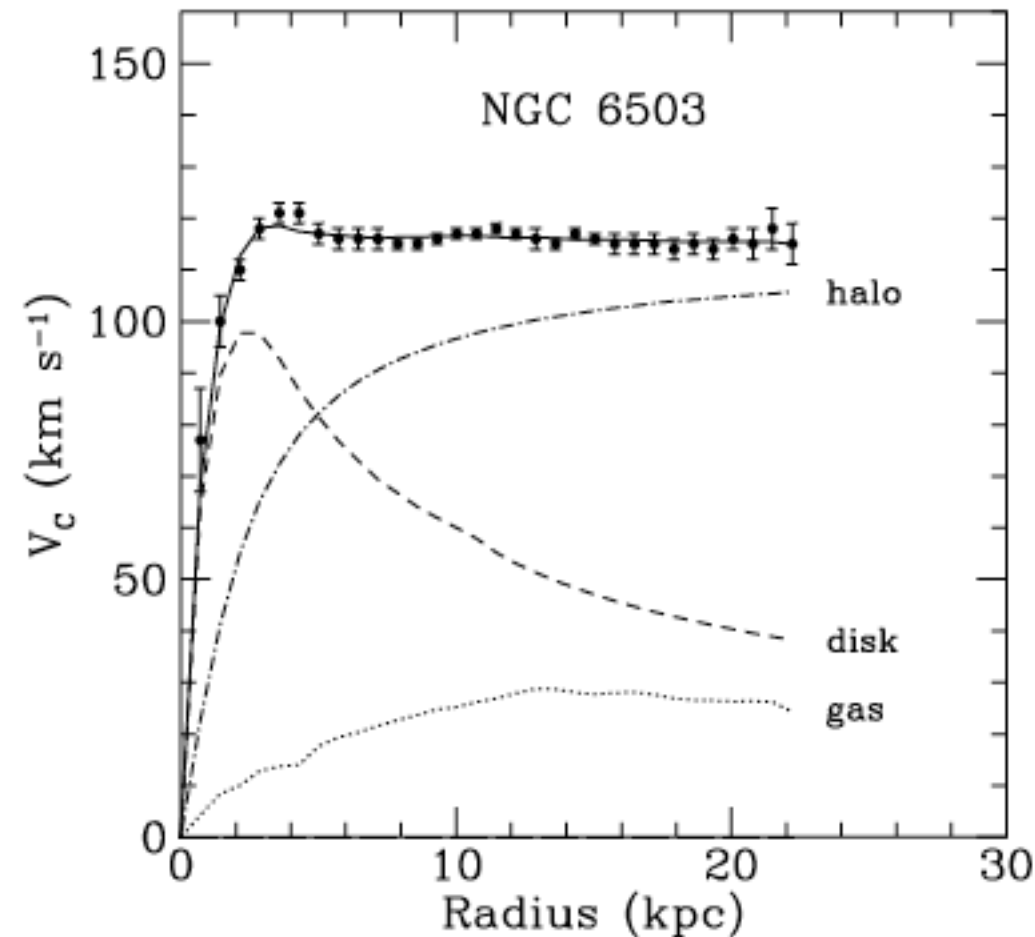
measurement of dispersion of velocity and geometrical size provides estimate of M (total mass)

result: $M \sim 400 \cdot$ visible mass!

(not commonly believed in for long!)

evidence for existence of Dark Matter

3. rotational curves of spiral galaxies

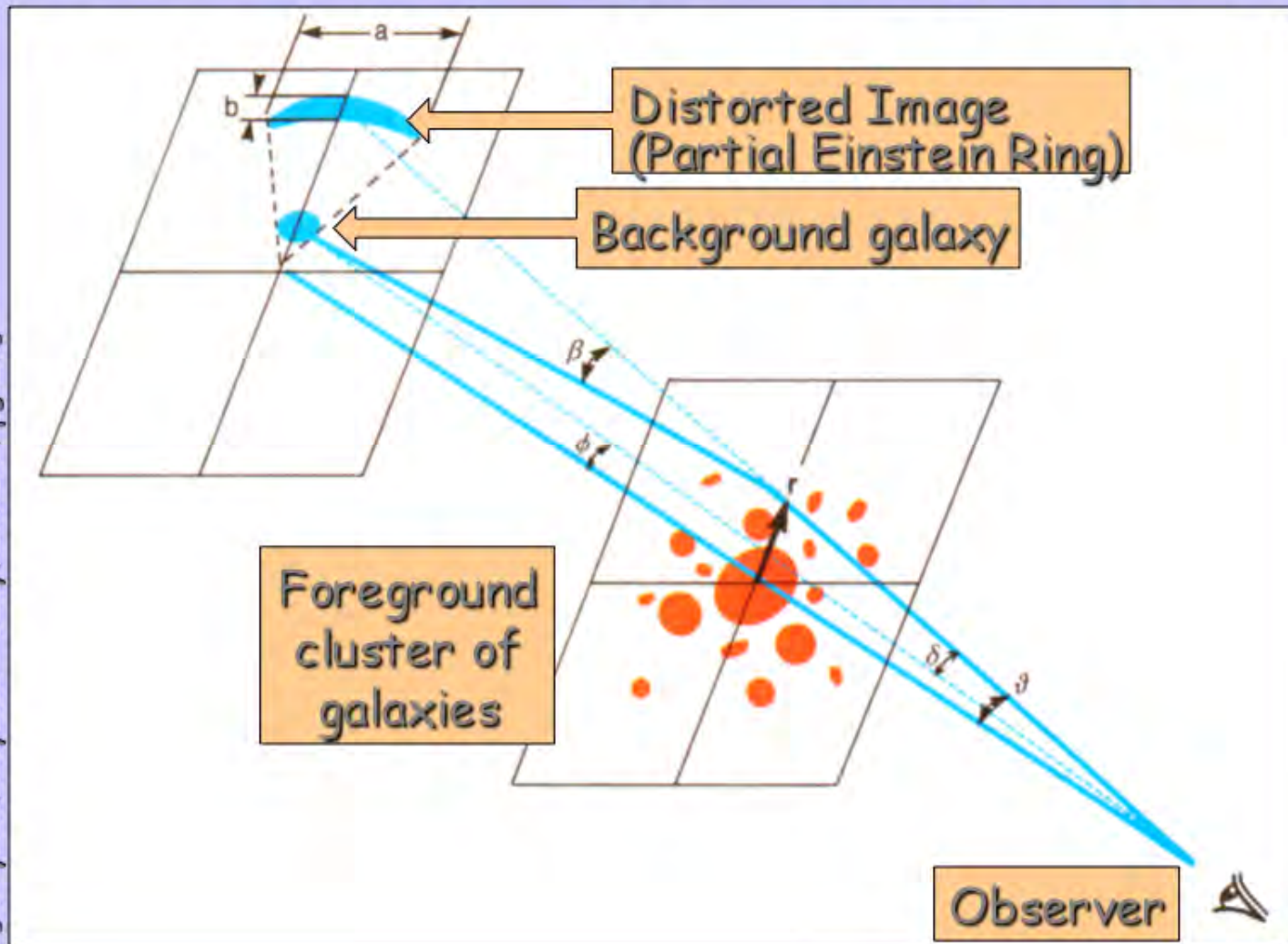


- expectation outside of galactic centre (Kepler): $v_{\text{rot}} = \sqrt{G_N M / r}$
 - measurement: 21 cm emission line of neutral Hydrogen (possible to much larger distances than optical observations)
 - result: \sim constant distribution up to largest distances
- > „spherical halo“ of Dark Matter (not only in disk !)
- in our own galaxy:
 v_{rot} (plateau) $\sim 220 \text{ km s}^{-1}$;
halo with $\sim 300 \text{ MeV cm}^{-3}$
(ca. 1 H-Atom per 3 cm^3 !)

evidence for existence of Dark Matter

4. galaxy clusters, gravitational lensing

Giant Arcs - Gravitationally Lensed Background Galaxies



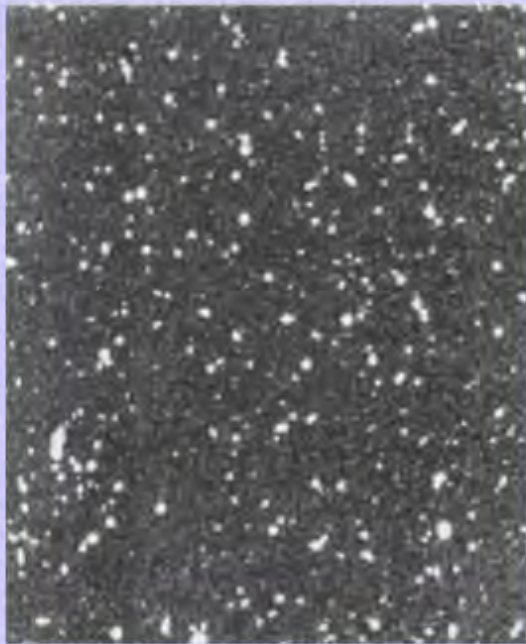
[A. Tyson, Physics Today, 1992:6, pg.24]

evidence for existence of Dark Matter

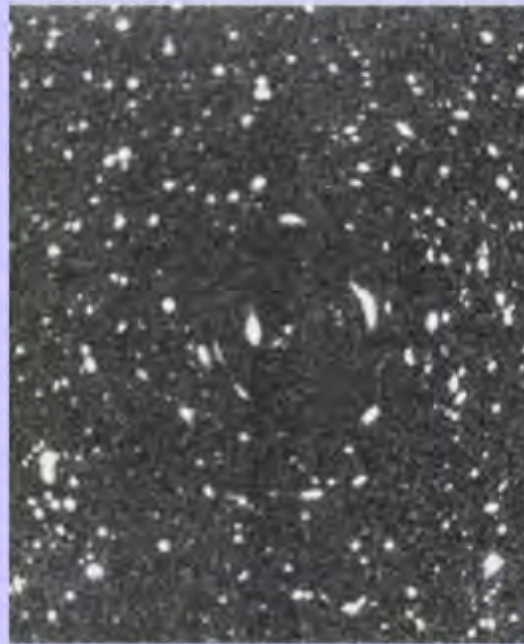
4. galaxy clusters, gravitational lensing

Weak Lensing Effect - Computer Simulation

[A.Tyson, *Physics Today*, 1992:6, pg.24]



Field of distant background galaxies ...



... seen through a spherical, transparent mass distribution, representing a foreground galaxy cluster.



Same with twice the cluster mass.

evidence for existence of Dark Matter

4. galaxy clusters, gravitational lensing



... agrees with large mass/light ratio
resulting from Zwicky's method!

Gravitational Lens in Abell 2218

HST · WFPC2

PF95-14 · ST ScI OPO · April 5, 1995 · W. Couch (UNSW), NASA

cosmological boundary conditions

could Dark Matter be composed of hadronic, non-luminous matter, as e.g. neutron stars, cold molecular hydrogen clouds, or Black Holes?

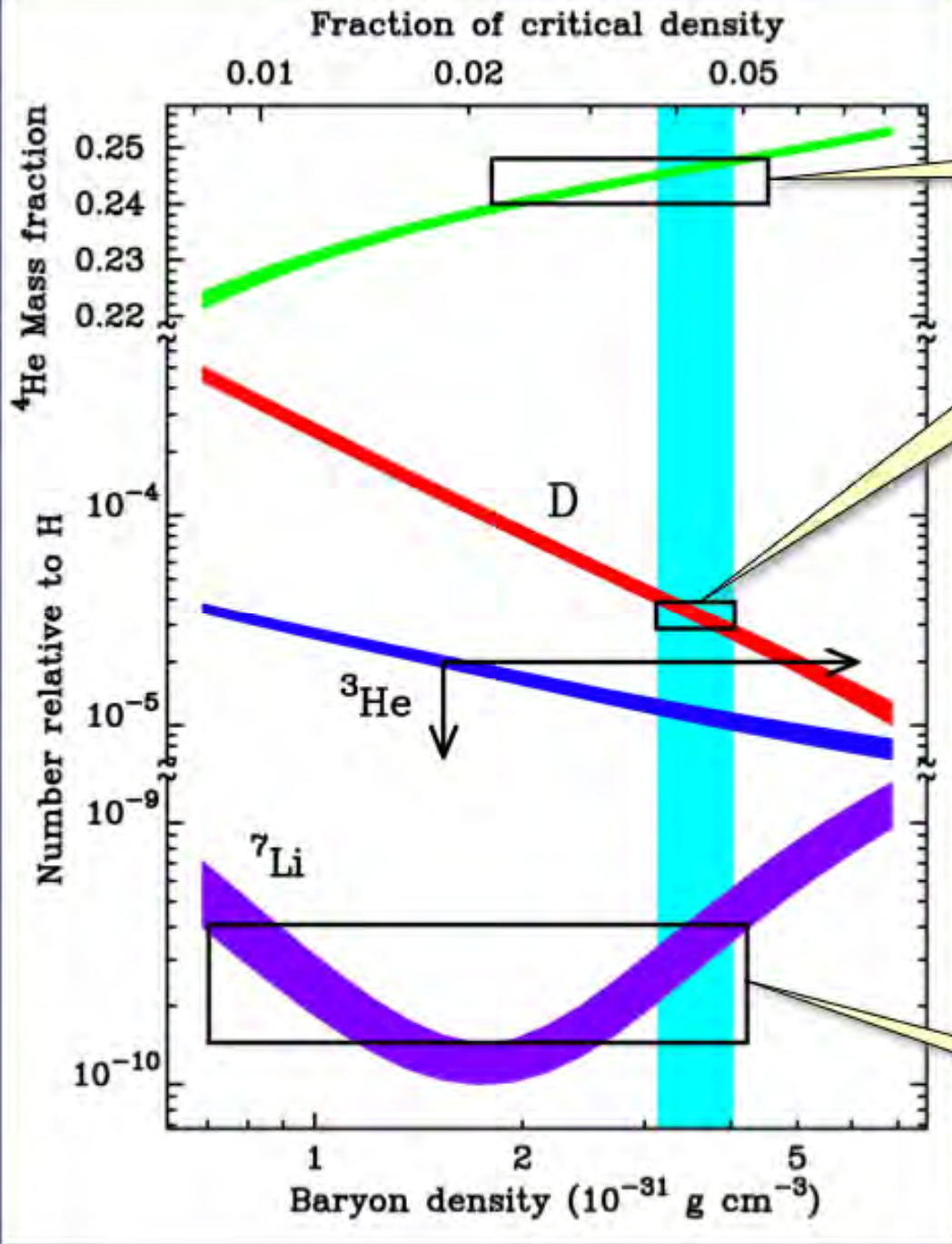
No!

reason: baryon density of universe is limited by so-called „Big Bang Nucleosynthesis:“

about 3 minutes after the Big Bang,
Helium (22%-25% of total mass)
as well as traces of D, He³ und Li⁷ are created
from protons and neutrons.

their relative amounts only depend on
cosmic density of baryons!

BBN Concordance



Helium 4

Deuterium

Cosmic baryon density implied by deuterium abundance:

$$\Omega_b h^2 = 0.019 \pm 0.0024$$

Lithium

[astro-ph/9903300]

cosmological boundary conditions

structure formation

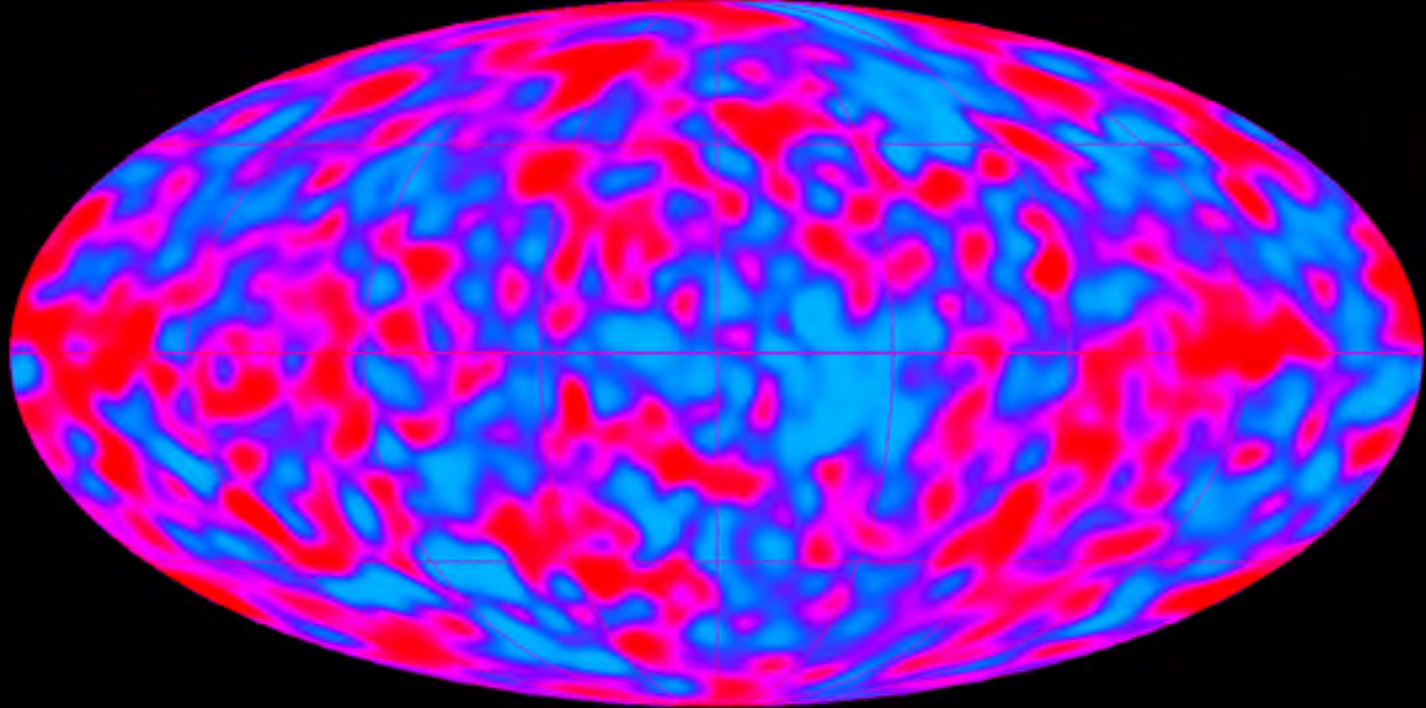
Standard Theory of cosmic structure formation:

- at an early stage, the universe was almost entirely homogenous...
- except of tiny density modulations, leading to conglomeration (by gravitation) of mass and built-up of galaxies.
- modulations originate from quantum fluctuations, which blew up, in a period of exponential expansion („inflationary universe“), to macroscopic scales

cosmological boundary conditions

structure formation

- amplitude of density fluctuations at an early stage (e.g. at decoupling of photons, about 300.000 years after Big Bang) reveals composition of matter and energy of early universe
- measurements of granularity of cosmic (2.7 K) microwave background (COBE; WMAP; Planck) shows: these amplitudes are too small to explain today's structure, if only baryonic matter and photons present.
- weakly interacting matter would work best, not being influenced by (electromagnetic) radiation.

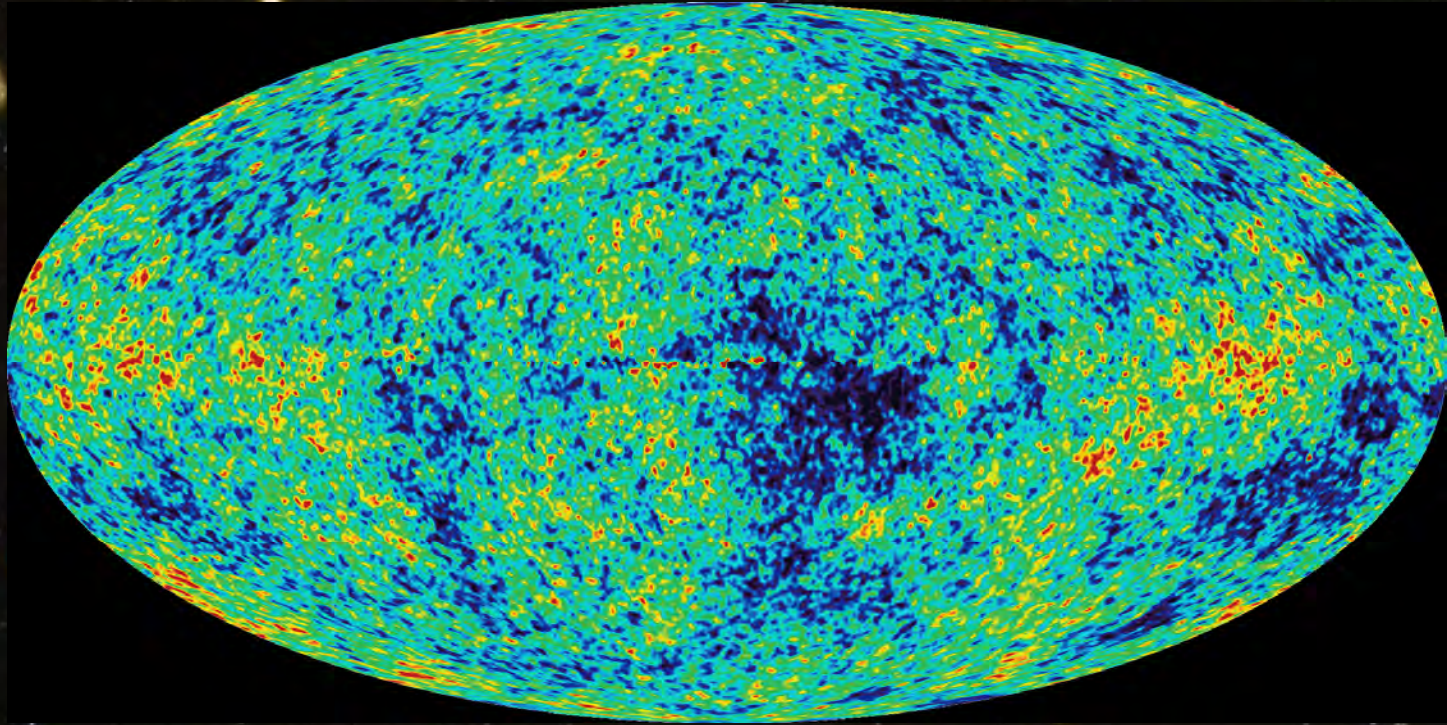


COBE Satellit

John Mather and George Smoot
Nobelpreis 2006

Messung der Anisotropie und der Granularität
der kosmischen 2.7 Kelvin Hintergrundstrahlung:

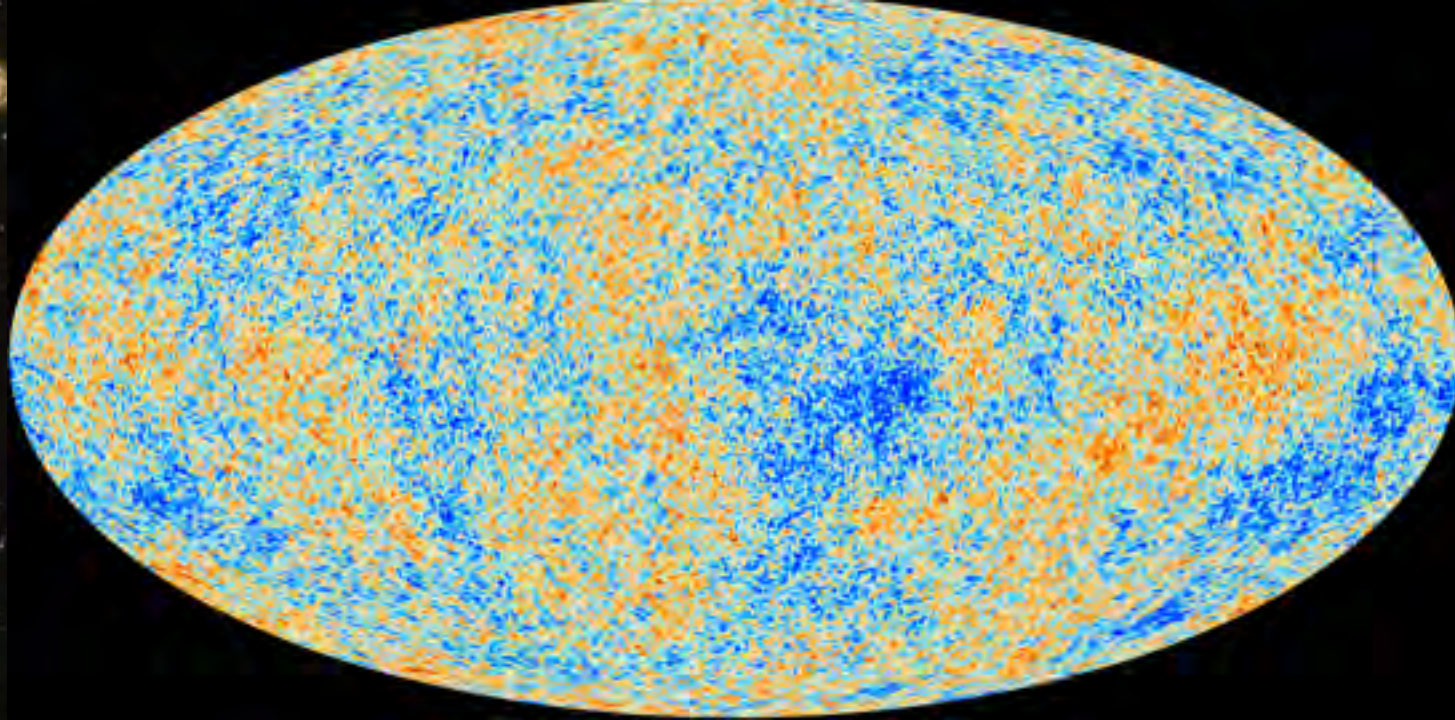
„Photographie“ der Dichtestruktur des Universums
als es transparent wurde (380.000 Jahre n.U.)



**WMAP Satellit
(Wilkinson Microwave Anisotropy Probe)**

Messung der Anisotropie und der Granularität
der kosmischen 2.7 Kelvin Hintergrundstrahlung:

„Photographie“ der Dichtestruktur des Universums
als es transparent wurde (380.000 Jahre n.U.)



Planck Satellit (2013)

Messung der Anisotropie und der Granularität
der kosmischen 2.7 Kelvin Hintergrundstrahlung:

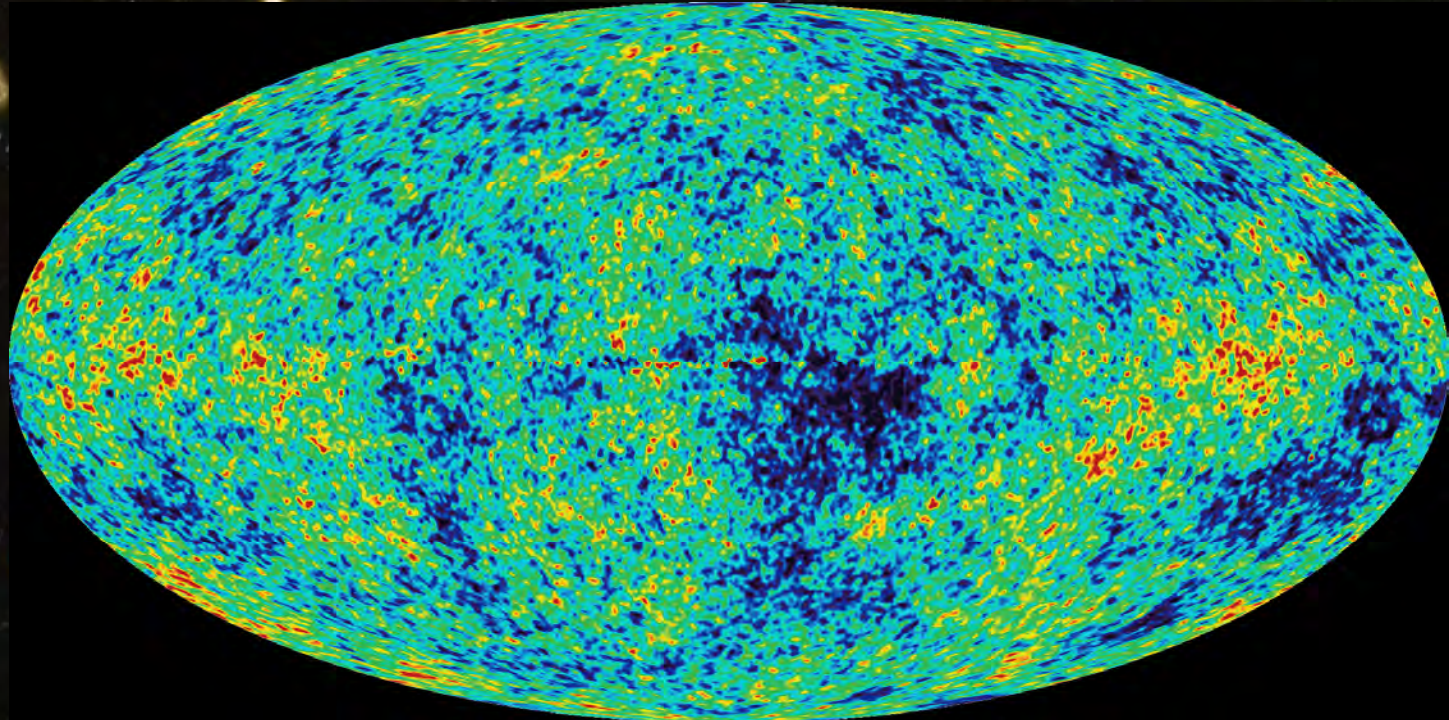
„Photographie“ der Dichtestruktur des Universums
als es transparent wurde (380.000 Jahre n.U.)

Planck Satellit

(gestartet 15.5.2009)



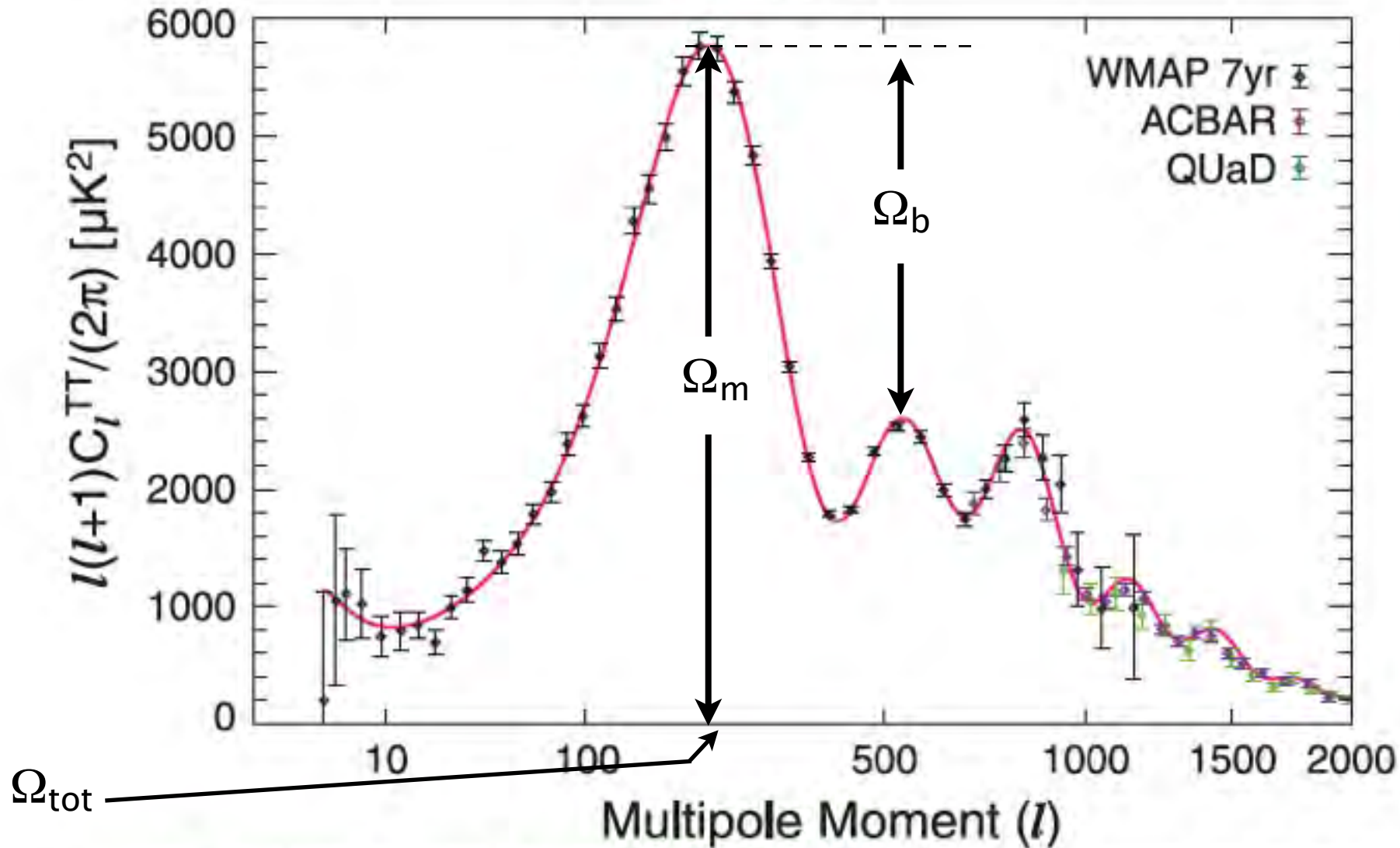
3-faches Auflösungsvermögen und 10-fache Lichtstärke (verglichen mit WMAP) → Messung bis $l \sim 2500$



Messung der Anisotropie und der Granularität
der kosmischen 2.7 Kelvin Hintergrundstrahlung

(Effekte der Heimatgalaxie sowie Dipol aus Bewegung der Erde
und des Sonnensystems sind subtrahiert)

Analyse: Temperaturunterschied zweier Punkte auftragen
gegen den Winkelabstand; „Multipolanalyse“ (Dipol: min-max bei
180°, Quadrupol: 90°,...)



The WMAP 7-year temperature power spectrum (Larson et al. 2010), along with the temperature power spectra from the ACBAR (Reichardt et al. 2009) and QUaD (Brown et al. 2009) experiments. We show the ACBAR and QUaD data only at $l \geq 690$, where the errors in the WMAP power spectrum are dominated by noise. We do not use the power spectrum at $l > 2000$ because of a potential contribution from the SZ effect and point sources. The solid line shows the best-fitting 6-parameter flat Λ CDM model to the WMAP data alone (see the 3rd column of Table 1 for the maximum likelihood parameters).

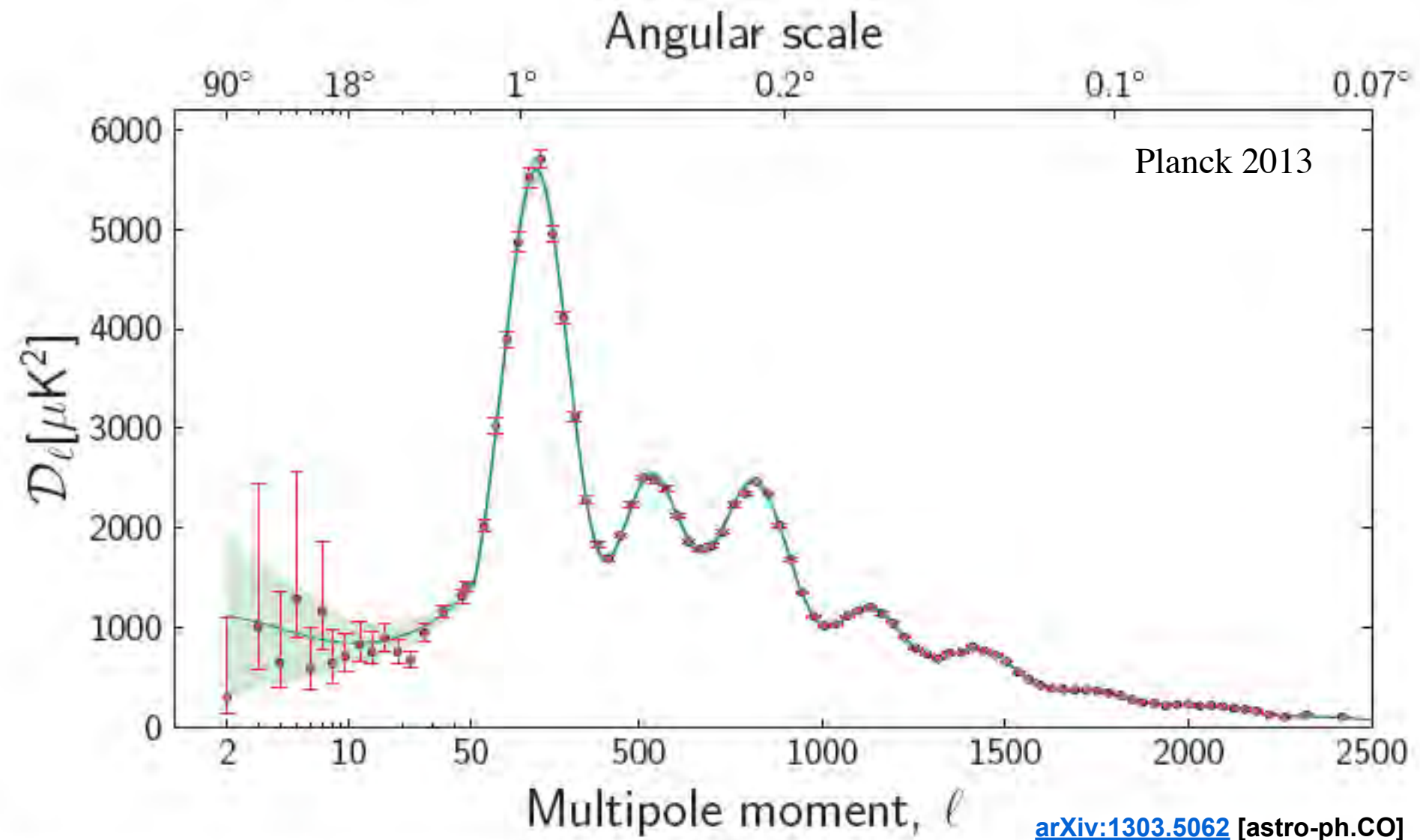


Fig. 19. The temperature angular power spectrum of the primary CMB from *Planck*, showing a precise measurement of seven acoustic peaks, that are well fit by a simple six-parameter Λ CDM theoretical model (the model plotted is the one labelled [Planck+WP+highL] in Planck Collaboration XVI (2013)). The shaded area around the best-fit curve represents cosmic variance, including the sky cut used. The error bars on individual points also include cosmic variance. The horizontal axis is logarithmic up to $\ell = 50$, and linear beyond. The vertical scale is $\ell(\ell + 1)C_\ell/2\pi$. The measured spectrum shown here is exactly the same as the one shown in Fig. 1 of Planck Collaboration XVI (2013), but it has been rebinned to show better the low- ℓ region.

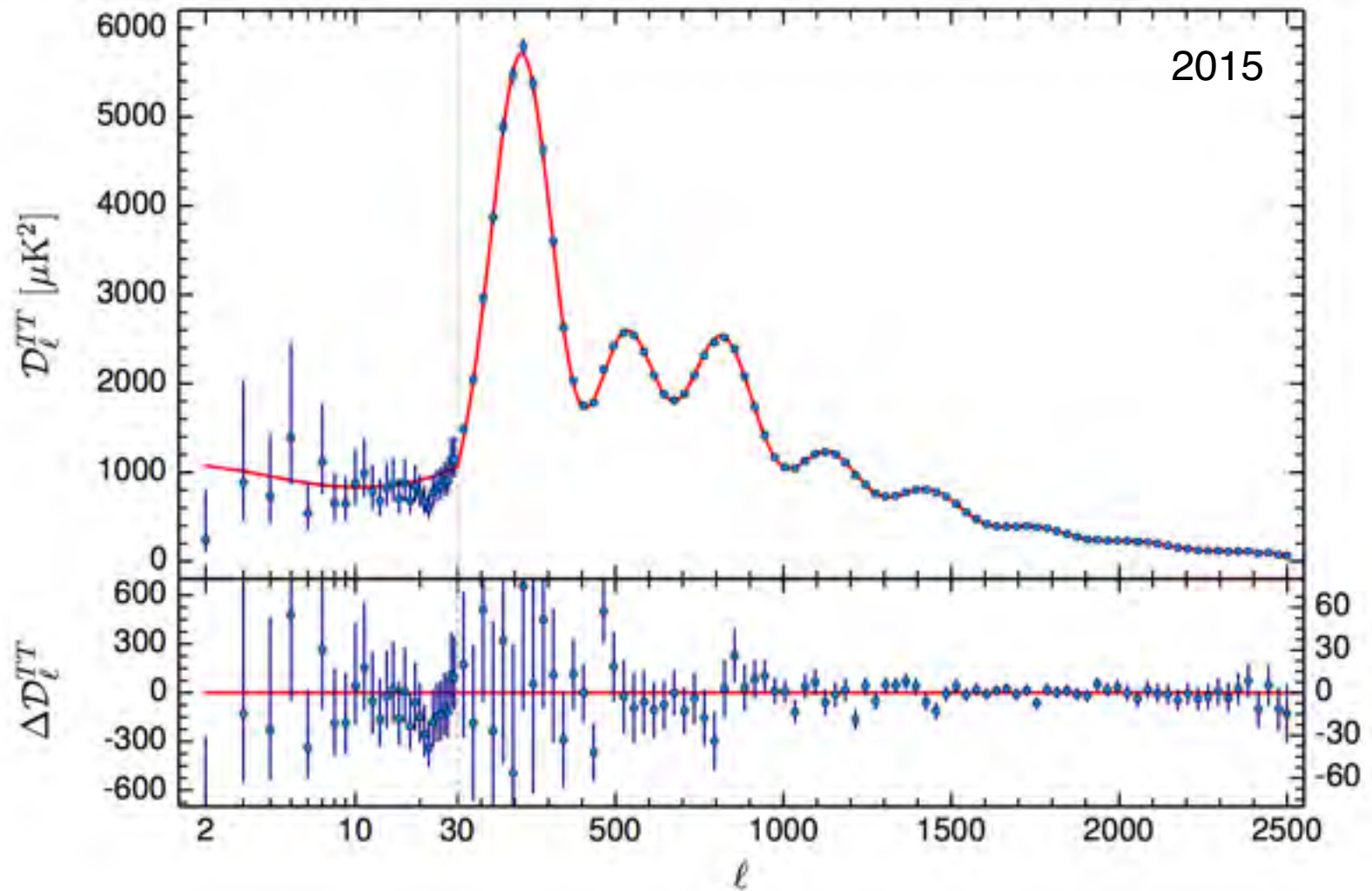


Fig. 1. The *Planck* 2015 temperature power spectrum. At multipoles $\ell \geq 30$ we show the maximum likelihood frequency averaged temperature spectrum computed from the *Planck* cross-half-mission likelihood with foreground and other nuisance parameters determined from the MCMC analysis of the base Λ CDM cosmology. In the multipole range $2 \leq \ell \leq 29$, we plot the power spectrum estimates from the *Commander* component-separation algorithm computed over 94% of the sky. The best-fit base Λ CDM theoretical spectrum fitted to the *Planck* TT+lowP likelihood is plotted in the upper panel. Residuals with respect to this model are shown in the lower panel. The error bars show $\pm 1\sigma$ uncertainties.

newest inventory of the Universe (Planck):

[arXiv:1303.5062](https://arxiv.org/abs/1303.5062) [astro-ph.CO]

[arXiv:1502.15082](https://arxiv.org/abs/1502.15082) [astro-ph.CO]

Age: 13.799 ± 0.038 billion years

$\Omega_{\text{dark energy}}$ $69,2\% \pm 1,2\%$

$\Omega_{\text{cold dark matter}}$ $25,9\% \pm 1,2\%$

Ω_{baryons} $4,9\% \pm 0,1\%$

Ω_{m} $30,8\% \pm 1,2\%$

H_0 $67,8 \pm 0,9$ km / s / Mpc

further cosmological measurements of fraction of dark energy:

– Supernovae type Ia as „standard candles“

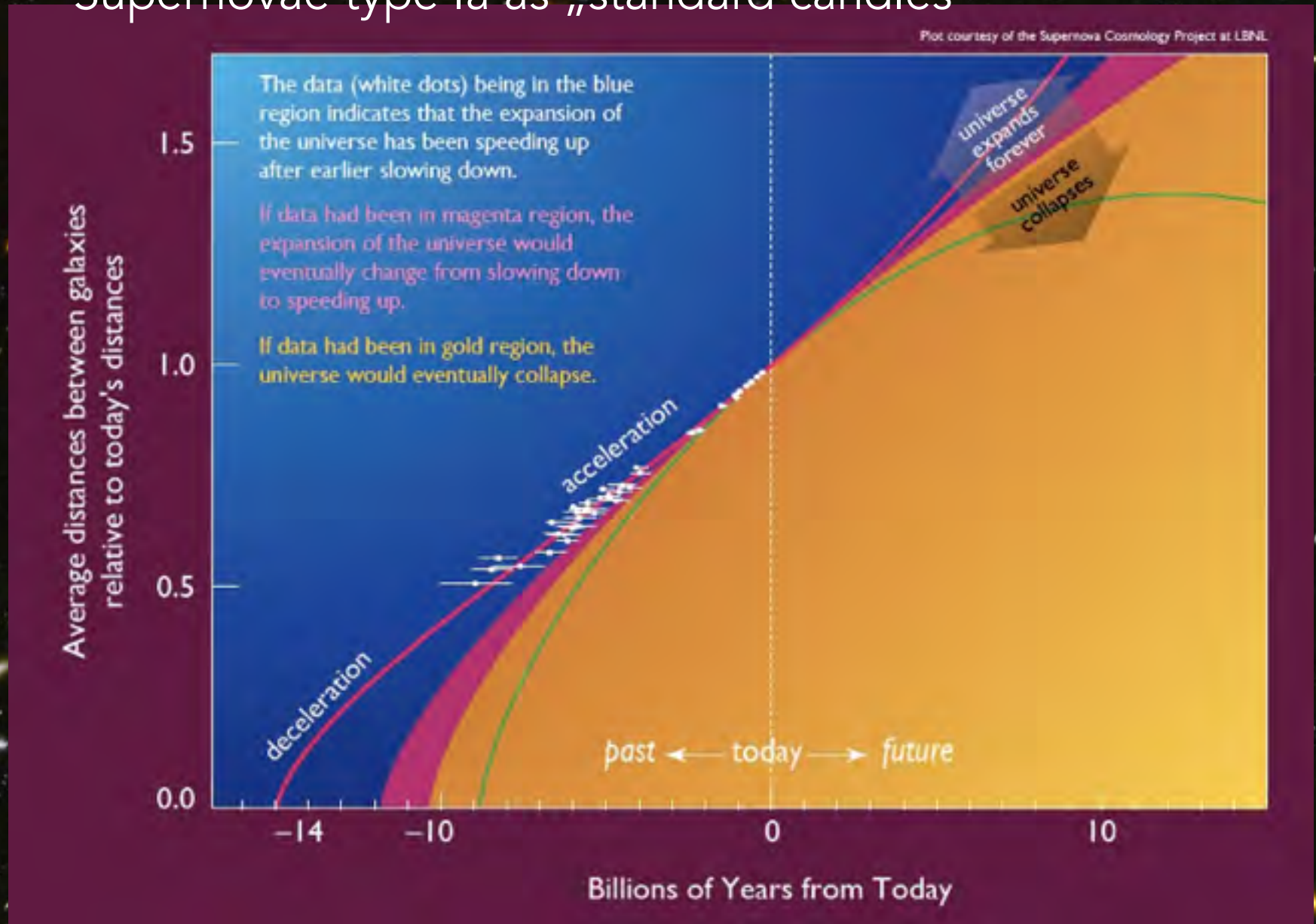
measurement of the history of cosmic expansion:
Supernovae (type Ia) as standard candles (i.e objects known absolute brightness).

type I: no hydrogen lines in spectrum

(progenitor is carbon-oxygen white dwarf in binary system, accreting mass beyond the Chandrasekhar limit of $\sim 1.44 M_{\text{sun}}$)

type Ia: additional Si absorption lines

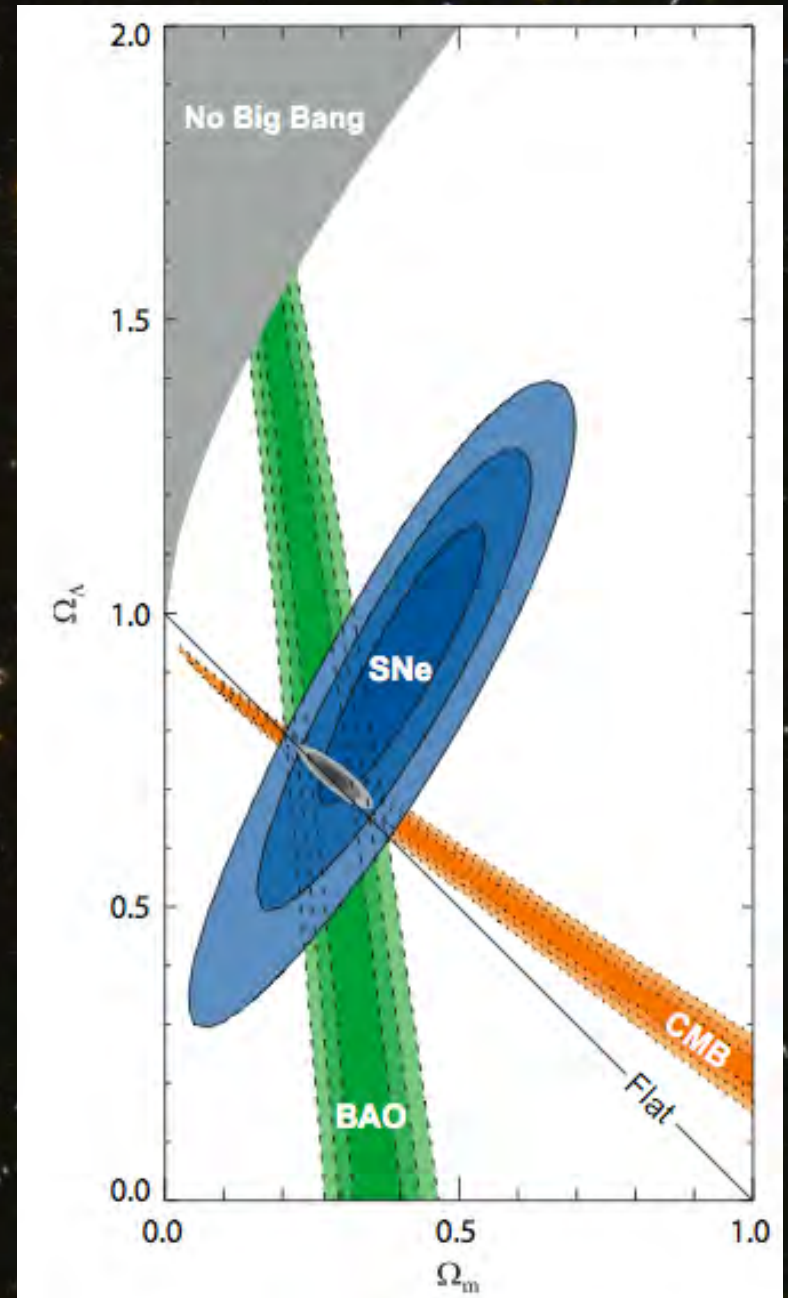
further cosmological measurements of fraction of dark energy:
– Supernovae type Ia as „standard candles“



CMB: Cosmic Microwave Background
(WMAP)

SNe: Supernovae Ia

BAO: Baryon Accoustic Oscillations
(aus Sloan Digital Sky Survey
der Galaxien)



general candidates for Dark Matter (particle physics):

- HDM: massive Neutrinos
 - „hot“: relativistic; would wash out primordial structures (too) rapidly to explain today's structure
- CDM: Axions, SUSY-WIMPs
 - „cold“: massive and non-relativistic; preserves primordial structure.
- Dark Energy: ... **no** clue in (exp.) particle physics... !

Supersymmetry (SUSY)

- provides cancellation of divergent radiative corrections → solves hierarchy problem
- postulates symmetry between fermions und bosons:
new fermion- (boson-) partners for all known fundamental bosons (fermions)

particles	Spin	SUSY particles	Spin
Quark Q	1/2	Squark \tilde{Q}	0
Lepton l	1/2	Slepton \tilde{l}	0
Photon γ	1	Photino $\tilde{\gamma}$	1/2
Gluon g	1	Gluino \tilde{g}	1/2
W^\pm	1	Wino \tilde{W}^\pm	1/2
Z^0	1	Zino \tilde{Z}^0	1/2

- Higgs structure in Minimal Supersymmetric Standard Model (MSSM):
2 complex Higgs-doublets (8 free scalar parameters) → 5 physical Higgs fields:
 H^\pm, H_1^0, H_2^0, A^0 . consistency requirement: $M_{H_1^0} \leq 130 \text{ GeV}$
- gauginos ($\tilde{\gamma}, \tilde{W}^\pm, \tilde{Z}$) mix with higgsinos and therefore result in
4 charginos ($\chi_{1,2}^\pm$) und 4 neutralinos ($\chi_{1,2,3,4}^0$)

Supersymmetry (SUSY)

- 124 free parameters (!!) to describe masses and couplings of all SUSY particles; one of these: angle β , with $\tan(\beta) = v_1/v_2$. Only known constraint: $(v_1^2 + v_2^2) = 246 \text{ GeV}^2$
- new conserved quantity: "R-parity": $R = (-1)^{3(B-L)+2S}$ (B, L: Baryon-/Lepton-number; S: Spin); $R = +1$ for normal matter particles, $R = -1$ für supersymmetric sparticles
- if R-parity conserved:
 - SUSY particles are produced in pairs
 - SUSY sparticles all decay into "lightest Susy Particle", LSP, which itself is stable.
 - cosmological arguments: LSP carries no electric and no colour charge \leftrightarrow only weak and gravitat. interactions!
 \rightarrow in particle reactions, leads to missing energy (like neutrinos).
- Supersymmetry with masses of $O(1 - 10 \text{ TeV})$ leads to change of energy dependence of coupling constants, such that "unification" occurs at $E \sim 10^{16} \text{ GeV}$
 \rightarrow proton lifetime $\gg 10^{32}$ years (beyond current experimental sensitivity) within SUSY-GUT.
- LSP is main candidate for Cold Dark Matter (CDM).

Search for Dark Matter

- direct:
 - Large Hadron Collider ... (direct production and investigation of its properties)
 - Search for WIMP* scattering in cryo-detectors
- indirect:
 - WIMP pair annihilation inside Earth, Sun, centers of galaxies (into 2 photons, or Neutrino-Antineutrino; neutrino-telescopes as ICECUBE; cosmic ray exps.)
- furthermore:
 - search for non-luminous, baryonic matter (MACHOS, massive compact halo objects)
- primordial black holes ...?

* WIMP: Weakly Interacting Massive Particle



Max-Planck-Institut für Physik
(Werner-Heisenberg-Institut)

The CRESST Dark Matter Search

Collaboration

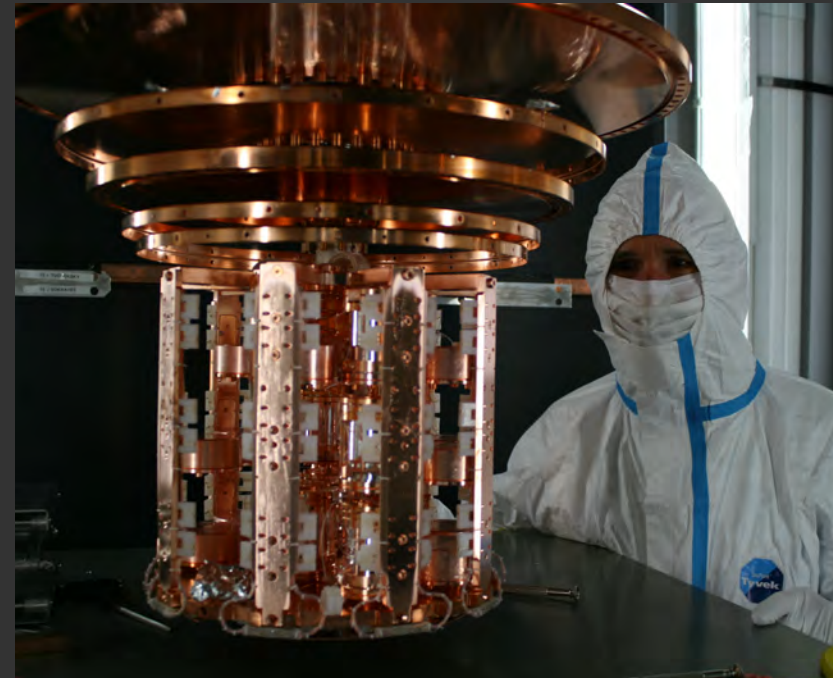
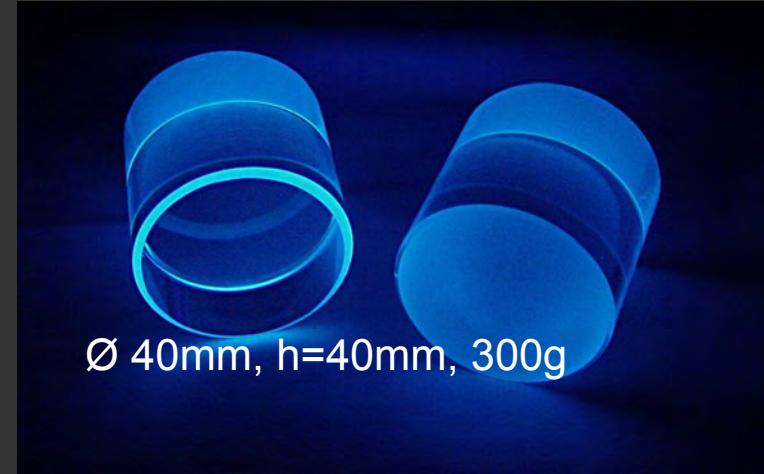
MPI für Physik, Oxford University,
TU München, Universität Tübingen
Laboratori Nazionali del Gran Sasso

Cryogenic Dark Matter search

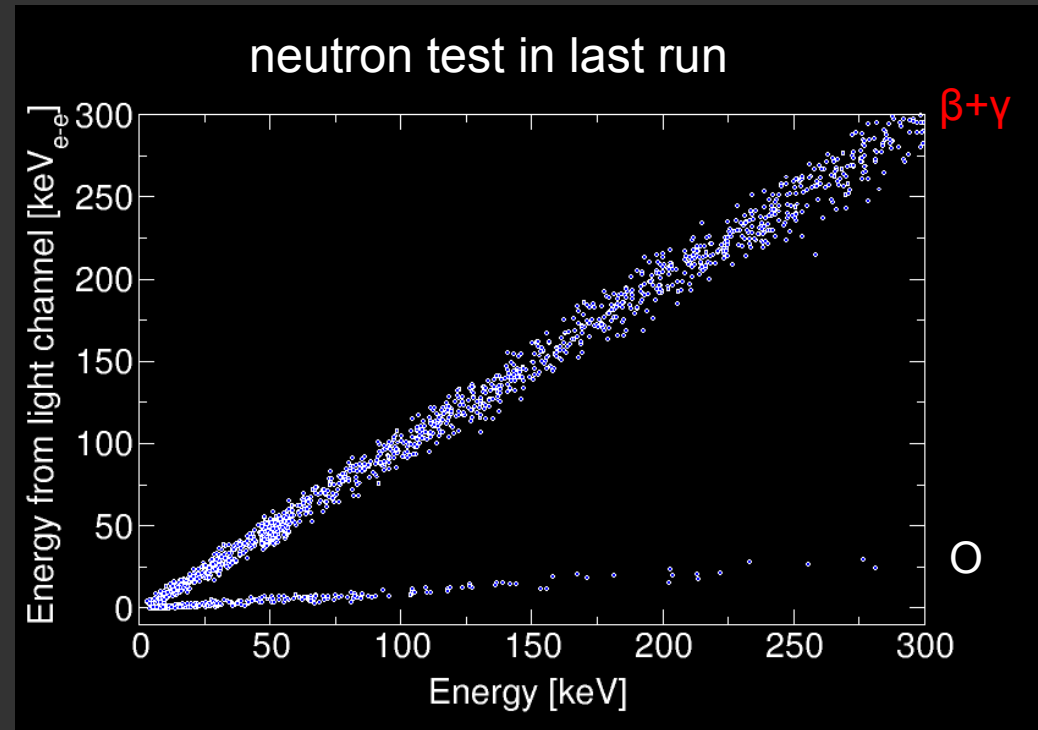
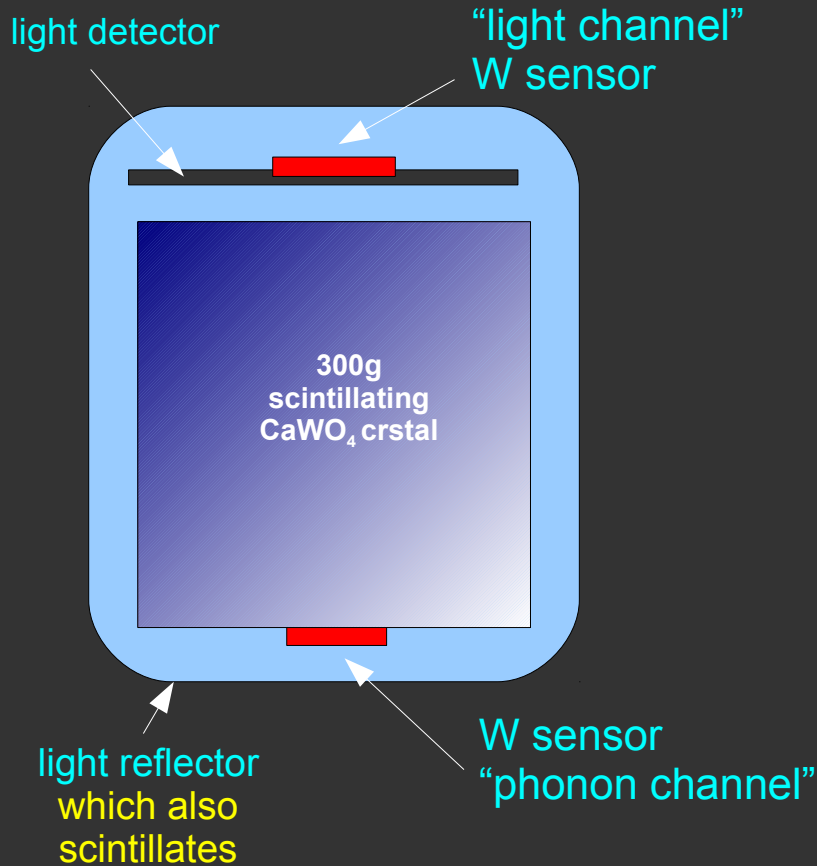
Located in hall A of LNGS

Scintillating CaWO_4 target crystals

Up to 33 crystals in modular
structure (10 kg target)



CRESST Detectors



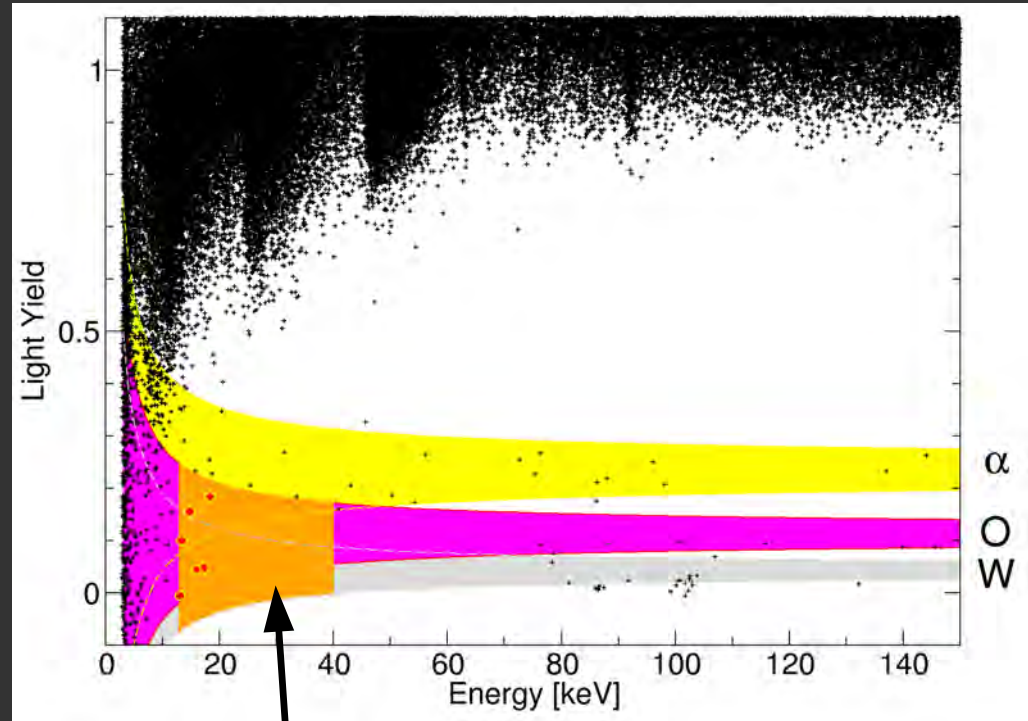
- Phonon channel measures deposited energy with sub keV resolution and accuracy
- Light channel serves to distinguish types of interaction
- Types of recoiling nuclei distinguished by different slopes in energy-light plane

Discrimination of Event Types

$$\text{Light Yield} = \frac{E_{\text{light}}}{E_{\text{phonon}}}$$

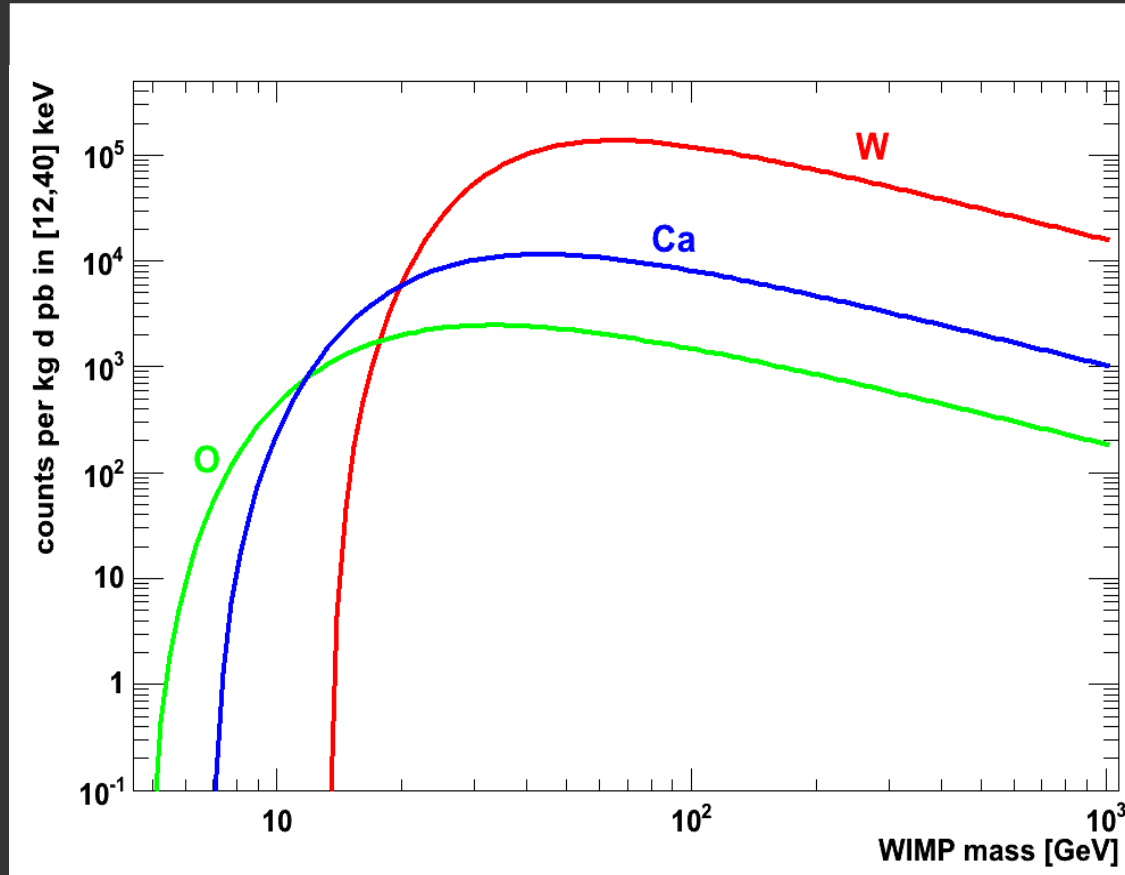
Event types characterized by different light yield

- efficient discrimination of nuclear recoils from β/γ -background
- WIMP signals expected in nuclear recoil bands



WIMP search region ROI includes O, Ca, and W bands

Types of Recoils in CaWO_4

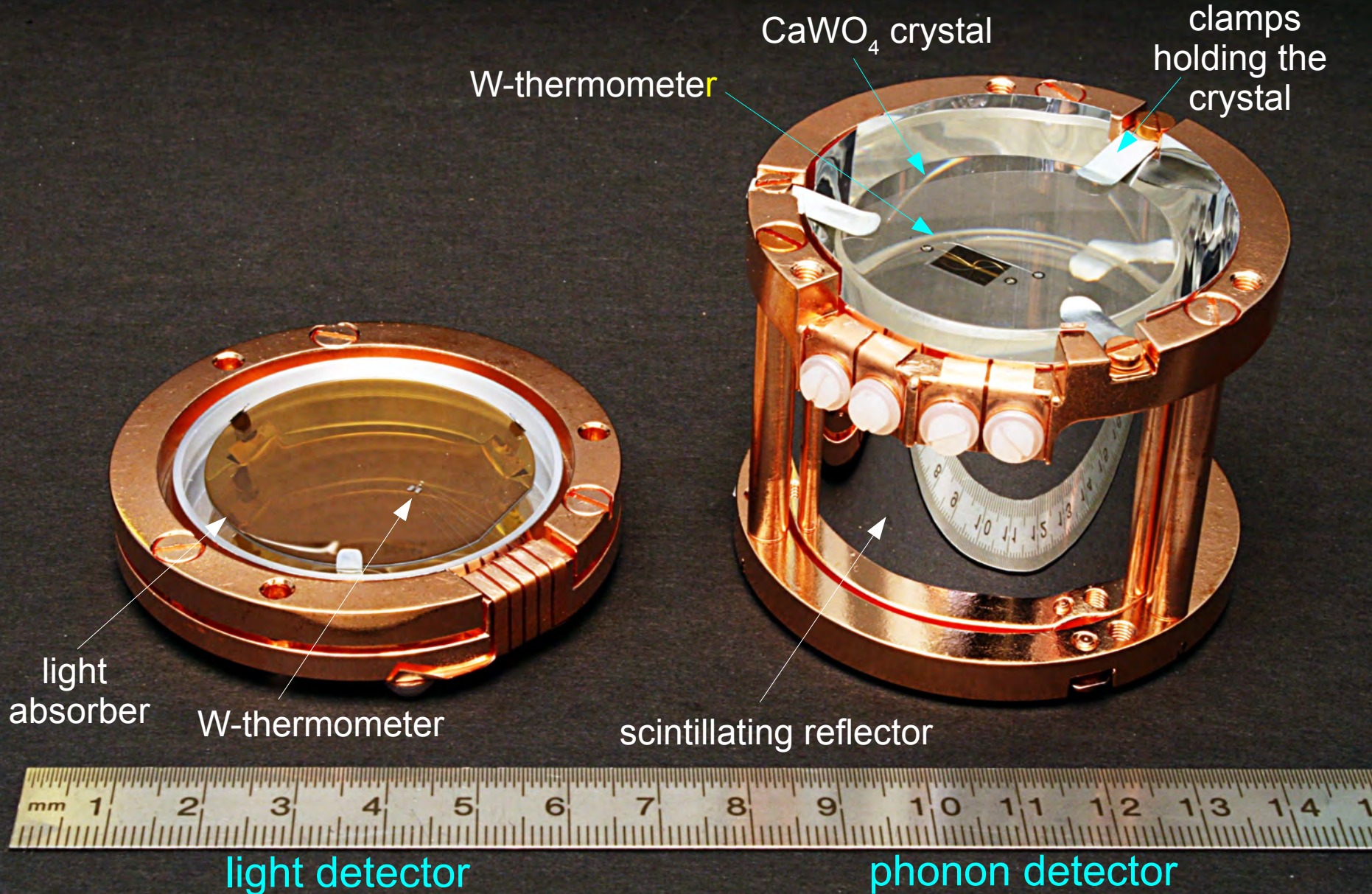


Assuming:

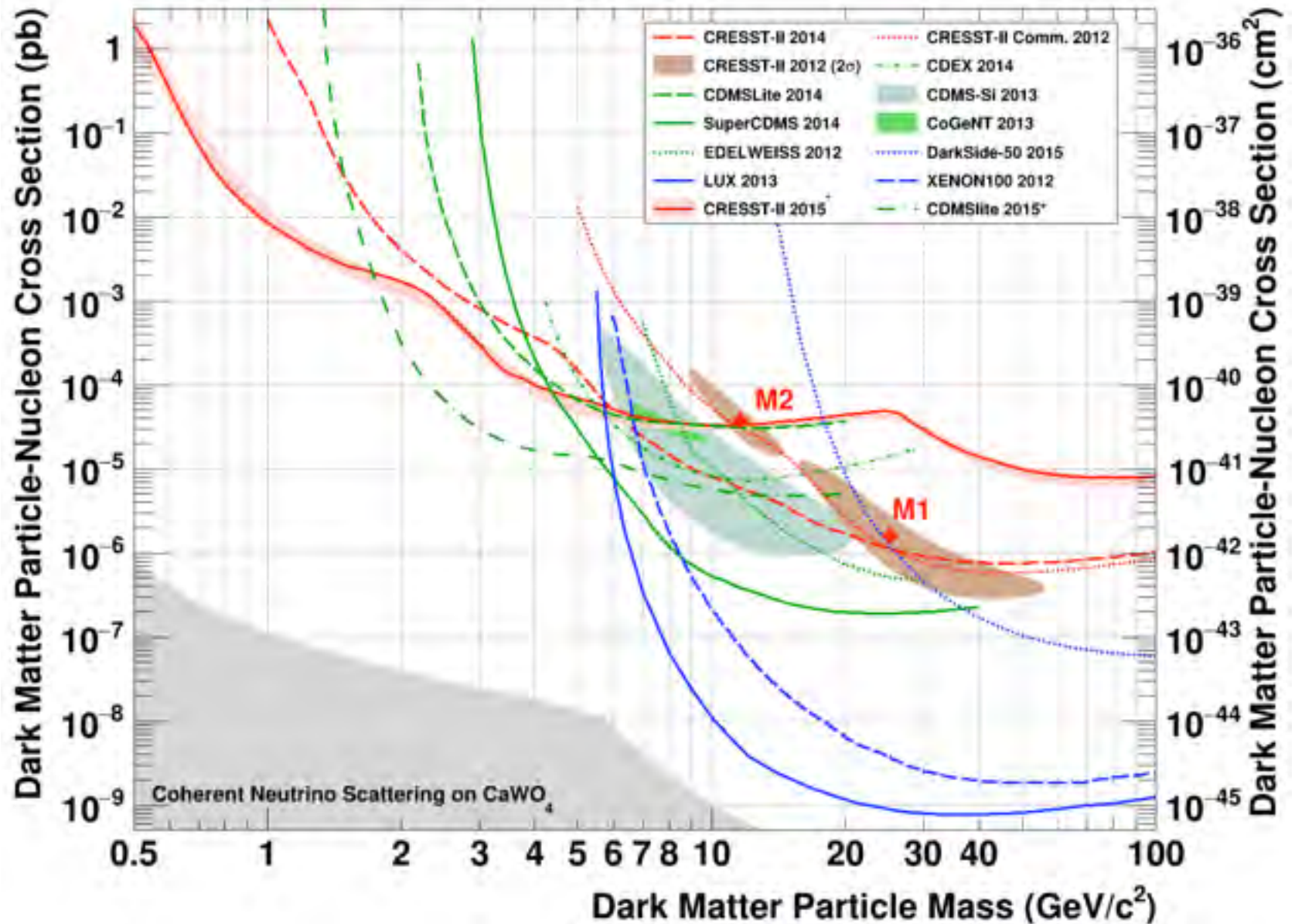
- $\sigma \propto A^2$
- detection in 12 to 40 keV range

- For $M < 10$ GeV only oxygen
 - Calcium important around 10 GeV
 - Tungsten dominates at larger WIMP masses due to $\sigma \propto A^2$
- type of recoils, together with the recoil energy spectrum, offers very detailed information on mass of possible WIMP

300 g Detector Module



Status of direct DM (WIMP) Searches



Summary

- non-baryonic Dark Matter (and Dark Energy) dominate mass-/energy density of Universe ($\sim 95\%$)
- Evidence for DM: from rotation of galaxies, structure formation, granularity of cosmic microwave background,
- only small contribution of hot dark matter (e.g. Neutrinos)
- candidates for cold dark matter: (SUSY) WIMPs, Axions,....
- indirect search: e.g. cosmic WIMP Annihilation;
direct search: WIMP scattering in cryo detectors; LHC;
- nature of Dark Energy can only be studied by cosmological (astrophysical) means

literature:

- G. Bertone, D. Hooper, J. Silk: *Particle Dark Matter: Evidence, Candidates and Constraints*, hep-ph/0404157.
- John A. Peacock, *Cosmological Physics*, Cambridge University Press 1999.
- div. Kosmologie Artikel in: particle data group, pdg.lbl.gov
- M. Kowalski et al., *Improved Cosmological Constraints from New, Old and Combined Supernova Datasets*, arXiv:0804.4142v1
- D. Eisenstein et al., *Detection of the Baryon Acoustic Peak in the Large-Scale Correlation Function of SDSS Luminous Red Galaxies*, arXiv:astro-ph/0501171v1
- Planck 2013 results. I. Overview of products and scientific results Planck Collaboration (P.A.R. Ade (Cardiff U.) *et al.*). Mar 20, arXiv:1303.5062 [astro-ph.CO]
- **Planck 2015 results. XIII. Cosmological parameters** Planck Collaboration (P.A.R. Ade (Cardiff U.) *et al.*). Feb 5, 2015. arXiv:1502.01589 [astro-ph.CO]