

# Family symmetries.

G.G.Ross, Ringberg Castle, April 2009



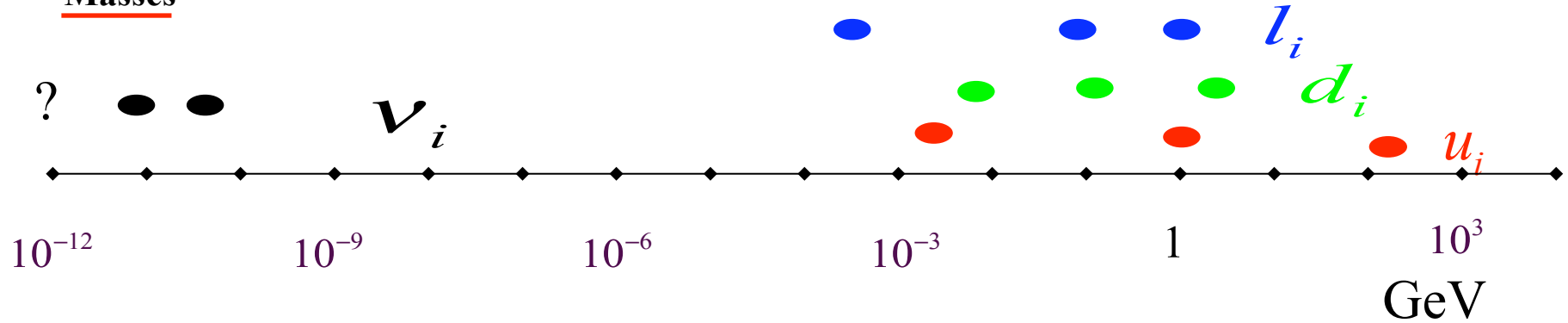
# Family symmetries.

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- $q \leftrightarrow l$       Neutrino v/s quark masses and mixing?  
See-saw with sequential domination
- Symmetry      GUT  
Family      Abelian, Non-Abelian, Discrete, String?
- Tri-bi-maximal mixing      Non-Abelian discrete symmetry

**DATA :**

Masses



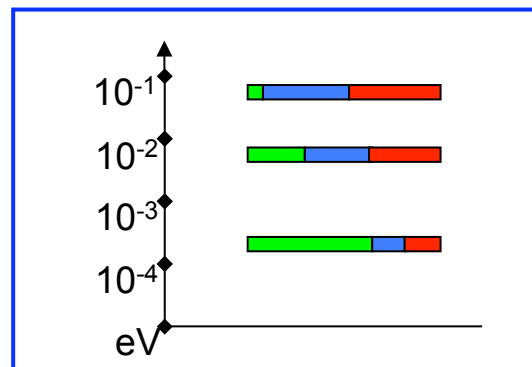
Mixing

Quarks

Leptons

$$V_{CKM} \approx \begin{pmatrix} 1 & 0.218-0.224 & 0.002-0.005 \\ 0.218-0.224 & 1 & 0.032-0.048 \\ 0.004-0.015 & 0.03-0.048 & 1 \end{pmatrix}$$

$$V_{MNS} = \begin{pmatrix} 0.79-0.88 & 0.48-0.61 & < 0.2 \\ 0.27-0.49 & 0.45-0.71 & 0.52-0.82 \\ 0.28-0.5 & 0.51-0.65 & 0.57-0.81 \end{pmatrix}$$



$$\approx \begin{pmatrix} \sqrt{\frac{2}{3}} & \frac{1}{\sqrt{3}} & \sim 0 \\ -\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & -\frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

Bi-Tri Maximal  
Mixing ...  
Discrete  
Non Abelian  
Structure?

DATA :

$$L_{Yukawa} = Y_{ij}^u Q^i u^{c,j} H + Y_{ij}^d Q^i d^{c,j} \bar{H}$$

$$M_{ij}^u = Y_{ij}^u \langle H^0 \rangle \quad M_{ij}^d = Y_{ij}^d \langle \bar{H}^0 \rangle$$

$$M^u = V_L^\dagger \underline{M_{Diag}^u} V_R$$

$$M^d = U_L^\dagger \underline{M_{Diag}^d} U_R$$

$$\underline{V_{CKM}} = V_L^\dagger U_L$$

The data for quarks is *consistent* with a very symmetric structure :

$$\frac{M^{d,u}}{m^{b,t}} \simeq \begin{pmatrix} \langle \epsilon^4 & \epsilon^3 & \epsilon^3 \\ \epsilon^3 & \epsilon^2 & \epsilon^2 \\ \epsilon^3 & \epsilon^2 & 1 \end{pmatrix} \quad \begin{array}{l} \epsilon^d = 0.15 \\ \epsilon^u = 0.05 \end{array}$$

O(1) coefficients suppressed

$q \leftrightarrow l$  symmetry?

Charged leptons are consistent with a similar form

$$\frac{M^{d,l,u}}{m^{b,\tau,t}} \simeq \begin{pmatrix} < \varepsilon^4 & \varepsilon^3 & \varepsilon^3 \\ \varepsilon^3 & a\varepsilon^2 & a\varepsilon^2 \\ \varepsilon^3 & a\varepsilon^2 & 1 \end{pmatrix} \quad \begin{array}{l} \varepsilon^d = 0.15, \quad a^d = 1 \\ \varepsilon^l = 0.15, \quad a^l = -3 \\ \varepsilon^u = 0.05, \quad a^u = 1 \end{array}$$

## Symmetry 1.

## GUT relations

*e.g.*  $SU(4) \subset SO(10)$

$$\Psi_\alpha = \begin{pmatrix} d \\ d \\ d \\ l \end{pmatrix}$$

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# GUT relations

e.g.  $SU(4) \subset SO(10)$

$$\Psi_\alpha = \begin{pmatrix} d \\ d \\ d \\ l \end{pmatrix}$$

$$\text{Det}(M^l) = \text{Det}(M^d) |_{M_X}$$

$\bar{\Psi} \quad \Psi_\alpha$

$$\frac{M^{d,l}}{m_3} = \begin{pmatrix} < \varepsilon^4 & \varepsilon^3 & \varepsilon^3 \\ \varepsilon^3 & a\varepsilon^2 & a\varepsilon^2 \\ \varepsilon^3 & a\varepsilon^2 & 1 \end{pmatrix}$$

$$\frac{m_b}{m_\tau}(M_X) = 1$$

$$\varepsilon^d = 0.15, \quad a^d = 1$$

$$\varepsilon^l = 0.15, \quad a^l = -3$$

# Symmetry 1.

# GUT relations

e.g.  $SU(4) \subset SO(10)$

$$\Psi_\alpha = \begin{pmatrix} d \\ d \\ d \\ l \end{pmatrix}$$

$$\langle \Sigma_{45} \rangle$$

||

$$\bar{\Psi}^{-\alpha} \begin{pmatrix} 1 & & & \\ & 1 & & \\ & & 1 & \\ & & & -3 \end{pmatrix} \Psi_\alpha$$

$$\frac{m_s}{m_\mu}(M_X) = \frac{1}{3}$$

Georgi Jarlskog

$$\frac{M^{d,l}}{m_3} = \begin{pmatrix} \langle \varepsilon^4 & \varepsilon^3 & \varepsilon^3 \\ \varepsilon^3 & a\varepsilon^2 & a\varepsilon^2 \\ \varepsilon^3 & a\varepsilon^2 & 1 \end{pmatrix}$$

$$\varepsilon^d = 0.15, \quad a^d = 1$$

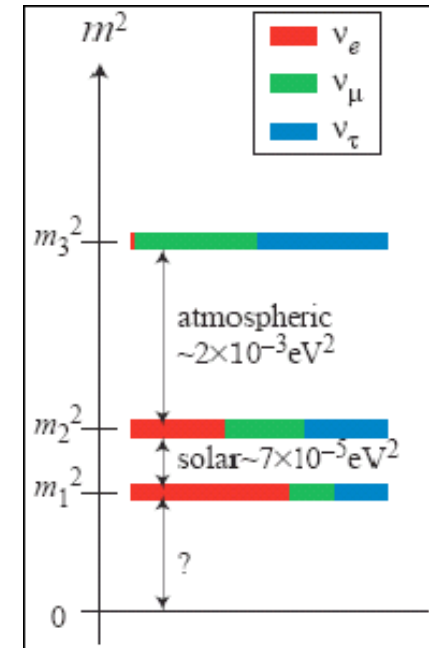
$$\varepsilon^l = 0.15, \quad a^l = -3$$



# Neutrinos ???

$$L_{eff}^{\nu} = m_3 \bar{\phi}_{23}^i \nu_i \bar{\phi}_{23}^j \nu_j + m_2 \bar{\phi}_{123}^i \nu_i \bar{\phi}_{123}^j \nu_j$$

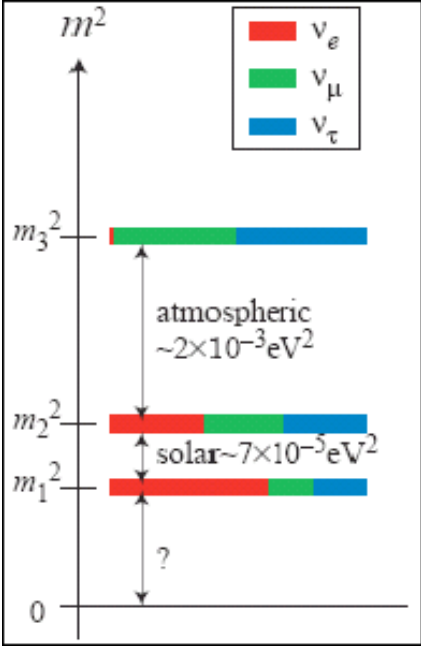
$$\langle \bar{\phi}_{23} \rangle^i = (0, -1, 1), \quad \langle \bar{\phi}_{123} \rangle^i = (1, 1, 1)$$



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Can one have a unified description of quark, charged lepton **and** neutrinos?

*c.f.*  $L_{Dirac}^{q,l} = m_3 \bar{\phi}_3^i \psi_i \bar{\phi}_3^j \psi_j^c + \dots$

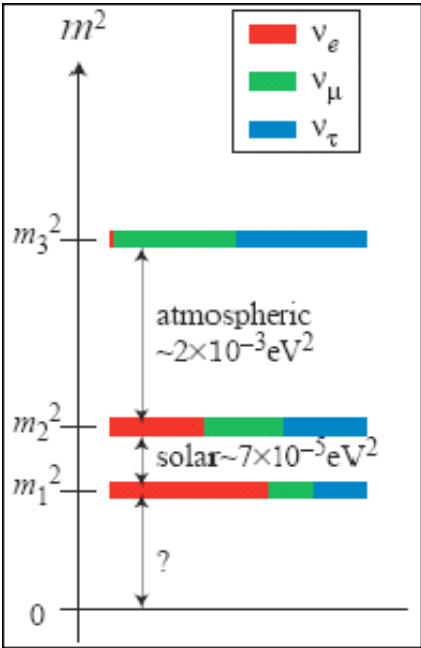
$$\langle \bar{\phi}_3 \rangle^i = (0, 0, 1) \quad ???$$

# Neutrinos ???

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See-Saw

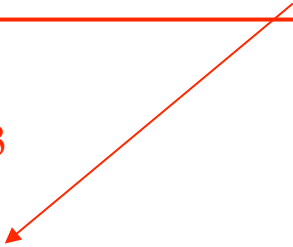


Quarks, charged leptons, neutrinos **can** have similar Dirac mass :

$$L_{Dirac}^{q,l,\nu} = \alpha \psi_i \bar{\phi}_3^i \psi_j^c \bar{\phi}_3^j + \beta \left( \psi_i \bar{\phi}_{123}^i \psi_j^c \bar{\phi}_{23}^j + \psi_i \bar{\phi}_{23}^i \psi_j^c \bar{\phi}_{123}^j \right) + \gamma \psi_i \bar{\phi}_{23}^i \psi_j^c \bar{\phi}_{23}^j \Sigma_{45} \quad \alpha > \beta$$

$$\frac{M^{Dirac}}{m_3} = \begin{pmatrix} \langle \epsilon^4 \rangle & \epsilon^3 + \epsilon^4 & -\epsilon^3 + \epsilon^4 \\ \epsilon^3 + \epsilon^4 & a\epsilon^2 + \epsilon^3 & -a\epsilon^2 + \epsilon^3 \\ -\epsilon^3 + \epsilon^4 & -a\epsilon^2 + \epsilon^3 & 1 \end{pmatrix}$$

$$\begin{aligned} \epsilon^d &= 0.15, & a^d &= 1 \\ \epsilon^l &= 0.15, & a^e &= -3 \\ \epsilon^u &= 0.05, & a^u &= 1 \\ \epsilon^v &= 0.05, & a^v &= 0 \end{aligned}$$

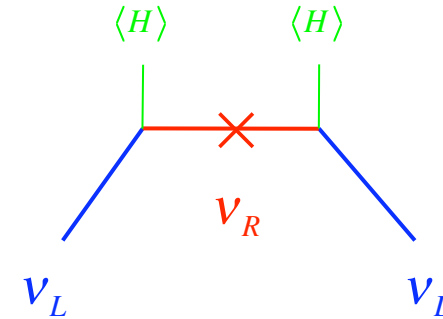


- “See-saw” with sequential domination

$$M_\nu = M_D^\nu M_M^{-1} M_D^{\nu T}$$

Minkowski  
Gell-Mann,  
Ramond,  
Slansky;  
Yanagida,  
King

$$M_M \approx \begin{pmatrix} M_1 & & \\ & M_2 & \\ & & M_3 \end{pmatrix} \quad M_1 < M_2 \ll M_3$$



$$L_{Dirac}^\nu = \alpha \psi_i \phi_{i3}^{\bar{i}} \psi_j^c \phi_{j3}^{\bar{j}} + \beta \left( \psi_i \phi_{i23}^{\bar{i}} \psi_j^c \phi_{j23}^{\bar{j}} + \psi_i \phi_{i23}^{\bar{i}} \psi_j^c \phi_{j123}^{\bar{j}} \right) \quad \alpha > \beta$$

$$L_{eff}^\nu = \frac{\beta^2}{M_1} \psi_i \phi_{i123}^i \psi_j \phi_{j123}^j + \frac{\beta^2}{M_2} \psi_i \phi_{i23}^i \psi_j \phi_{j23}^j + \frac{(\alpha + \beta)^2}{M_3} \psi_i \phi_{i3}^i \psi_j \phi_{j3}^j$$

● “See-saw” with sequential domination

$$M_\nu = M_D^\nu M_M^{-1} M_D^{\nu T}$$

Minkowski  
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$$M_M \approx \begin{pmatrix} M_1 & & \\ & M_2 & \\ & & M_3 \end{pmatrix}$$

$$M_1 \ll M_2 \ll M_3$$



small

$$L_{Dirac}^\nu = \alpha \psi_i \phi_{i3}^{\bar{i}} \psi_j^c \phi_{j3}^{\bar{j}} + \beta \left( \psi_i \phi_{i23}^{\bar{i}} \psi_j^c \phi_{j23}^{\bar{j}} + \psi_i \phi_{i23}^{\bar{i}} \psi_j^c \phi_{j123}^{\bar{j}} \right) \quad \alpha > \beta$$

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# Symmetry 2.

# Family symmetry

## Non-Abelian family symmetry

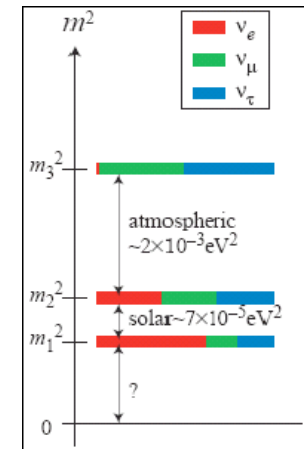
Promote  $\phi_i$  to fields transforming under  $SU(3)_{\text{family}}$

$$\frac{\phi_3}{M} = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$

$$\frac{\phi_{23}}{M} = \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix} \epsilon$$

$$\frac{\phi_{123}}{M} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} \epsilon^2$$

Messenger mass



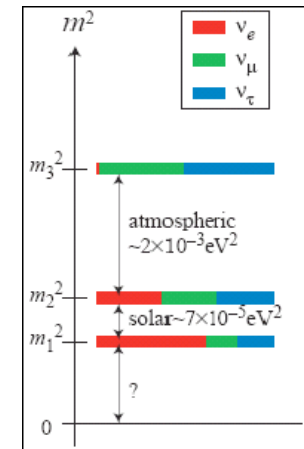
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Vacuum alignment ???

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## Family symmetry

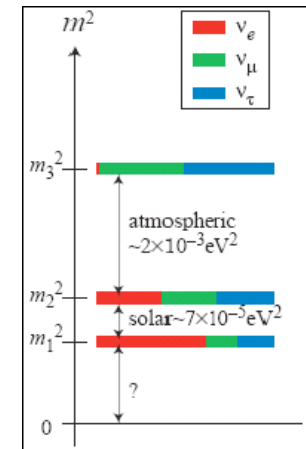
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Vacuum alignment ???  $\Rightarrow$  Discrete non Abelian symmetry



# List of models with discrete flavour symmetry

(incomplete, by symmetry)

- $S_3$ : Pakvasa et al.(1978), Derman(1979), Ma(2000), Kubo et al.(2003), Chen et al.(2004), Grimus et al.(2005), Dermisek et al (2005), Mohapatra et al.(2006), Morisi(2006), Caravaglios et al.(2006), Haba et al(2006),...Mondragon
- $S_4$ : Pakvasa et al.(1979), Derman(1979), Lee et al.(1994), Mohapatra et al.(2004),Ma(2006), Hagedorn et al.(2006), Caravaglios et al.(2006), Lampe(2007), Sawanaka(2007), ...
- $A_4$ : Wyler(1979), Ma et al.(2001), Babu et al.(2003), Altarelli et al.(2005-8), He et al.(2006), Bazzocchi, Morisi, et al.(2007/8), King et al.(2007),...Luca
- $D_4$ : Seidl(2003), Grimus et al.(2003/4), Kobayashi et al.(2005), ...
- $D_5$ : Ma(2004), Hagedorn et al.(2006), ...
- $D_n$ : Chen et al.(2005), Kajiyama et al.(2006), Frampton et al.(1995/6,2000), Frigerio et al (2005), Babu et al.(2005), Kubo(2005),...
- $T'$ : Frampton et al.(1994,2007), Aranda et al.(1999,2000),Feruglio et al.(2007), Chen et al.(2007), ...
- $\Delta_n$ : Kaplan et al.(1994), Schmaltz(1994), Chou et al.(1997), de Madeiros Varzielas et al(2006/7).
- $T_7$ : Luhn et al.(2007).

## Non Abelian discrete symmetries

*e.g.*  $Z_3 \rtimes Z_n$

$\phi_i$	$Z_3\phi_i$	$Z_n\phi_i$	
$\phi_1$	$\rightarrow \phi_2$	$\rightarrow \alpha\phi_1$	$\alpha^n = 1$
$\phi_2$	$\rightarrow \phi_3$	$\rightarrow \alpha^2\phi_2$	
$\phi_3$	$\rightarrow \phi_1$	$\rightarrow \alpha^{-3}\phi_3$	

$$\Delta(3n^2) \quad n = 2, \quad \Delta(12) \equiv A_4$$

$$n = 3, \quad \Delta(27)$$

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## Choice of discrete symmetry

- Vacuum structure :  $Z_3 \ltimes Z_n \rightarrow \begin{cases} Z_3, & \langle \phi \rangle = (1,1,1) \quad \lambda > 0 \\ Z_n, & \langle \phi \rangle = (0,0,1) \quad \lambda < 0 \end{cases}$

$$V(\phi) = -m^2 \phi^{\dagger i} \phi_i + \dots + \lambda m^2 \phi^{\dagger i} \phi_i \phi^{\dagger i} \phi_i$$

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- Quasi-degenerate neutrinos  $D \subset SO(3)$  e.g.  $A_4$   $m\psi^i\psi^i + ..$

GGR, Serna,  
Varzielas

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- Quasi-degenerate neutrinos  $D \subset SO(3)$  e.g.  $A_4$   $m\psi^i\psi^i + ..$
- GUT :  $A_4 \times SU(5), S_3 \times E_6, \dots$   $q \leftrightarrow l$  ✗ Altarelli et al, Caravaglios et al  
 $\Delta(27) \times SO(10)$  ✓ GGR, Varzielas

# A complete model

$$\Delta(27) \otimes SO(10) \otimes G \quad (G = R \otimes U(1))$$

Varzielas, GGR

- $\psi_i^c, \psi_i \in (16, 3) \Rightarrow$  No mass while SU(3) unbroken
- Spontaneous symmetry breaking

$$\begin{array}{cccc} \bar{\phi}_3^i & \bar{\phi}_{23}^i & \bar{\phi}_{123}^i & H_{45} \\ (1, \bar{3}) & (1, \bar{3}) & (1, \bar{3}) & (45, 1) \end{array}$$

c.f. Georgi-Jarskog

$$\begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}, \quad \begin{pmatrix} 0 \\ -1 \\ 1 \end{pmatrix} \varepsilon M, \quad \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} \varepsilon^2 M, \quad M$$

$$P_Y = \frac{1}{M^2} \bar{\phi}_3^i \psi_i \bar{\phi}_3^j \psi_j^c H + \frac{1}{M^3} \bar{\phi}_{23}^i \psi_i \bar{\phi}_{23}^j \psi_j^c H H_{45} + \frac{1}{M^2} \bar{\phi}_{23}^i \psi_i \bar{\phi}_{123}^j \psi_j^c H + \frac{1}{M^2} \bar{\phi}_{123}^i \psi_i \bar{\phi}_{23}^j \psi_j^c H$$

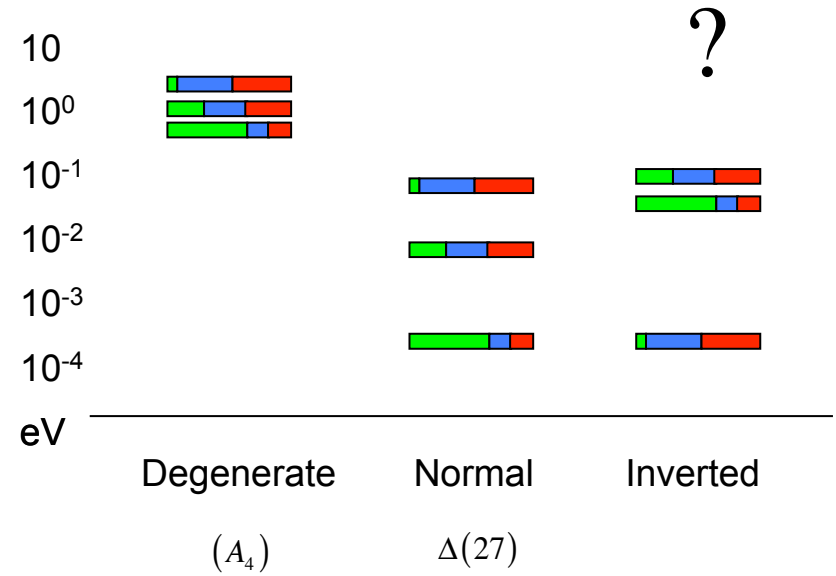
only terms allowed by G

# Neutrino Parameters

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- Tri-bi-maximal mixing

Degenerate and normal spectra favoured





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- Tri-bi-maximal mixing

Degenerate and normal spectra favoured

- Mixing angles

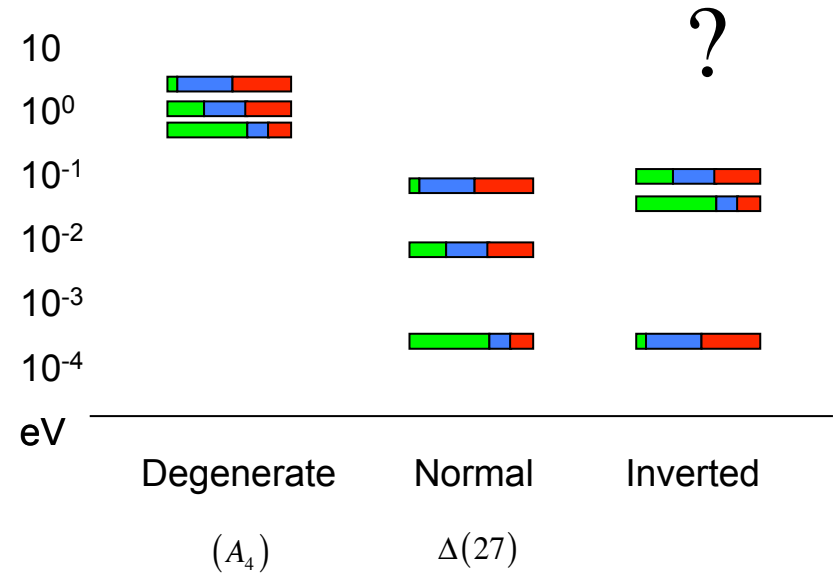
$$\sin^2 \theta_{12} \approx \frac{1}{3} \pm 0.03$$

$$\sin^2 \theta_{23} \approx \frac{1}{2} \pm 0.03$$

$$\sin \theta_{13} \approx \sqrt{\frac{m_e}{2m_\mu}} = 0.053 \pm 0.05 \quad (3 \pm 3^\circ)$$

From charged lepton mixing

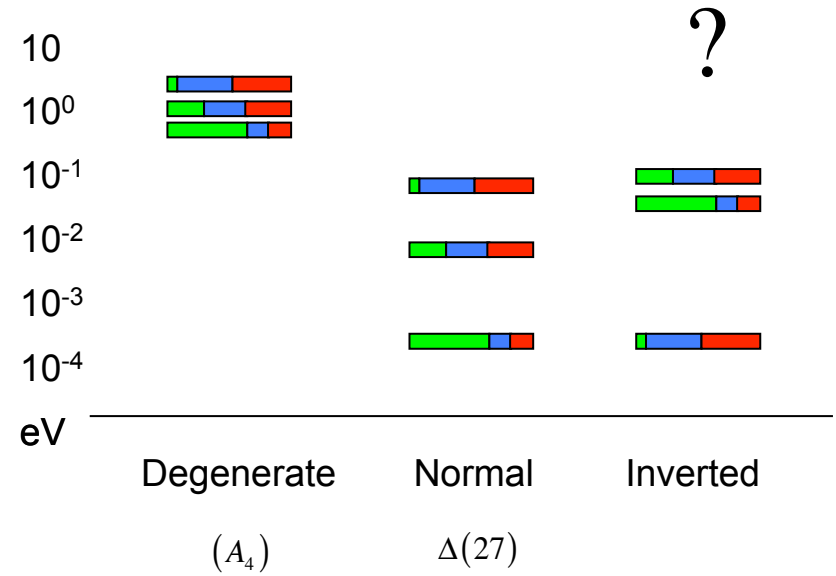
King; GGR, Varzielas



# Neutrino Parameters

## ● Tri-bi-maximal mixing

Degenerate and normal spectra favoured

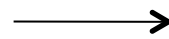


## ● Mixing angles

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$$\sin^2 \theta_{23} \approx \frac{1}{2} \pm 0.03$$

$$\sin \theta_{13} \approx \sqrt{\frac{m_e}{2m_\mu}} = 0.053 \pm 0.05 \quad (3 \pm 3^\circ)$$



$$\theta_{12} + \frac{1}{\sqrt{2}} \frac{\theta_c}{3} \cos(\delta - \pi) \approx 35.26 \pm 2^\circ$$

Antusch, King

From charged lepton mixing

King; GGR, Varzielas

# Neutrino Parameters

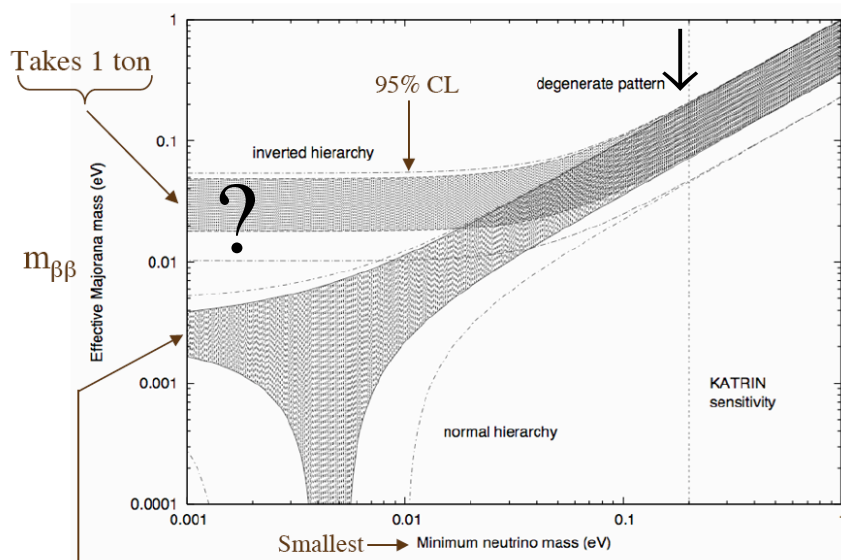
- Tri-bi-maximal mixing

Degenerate and normal spectra possible

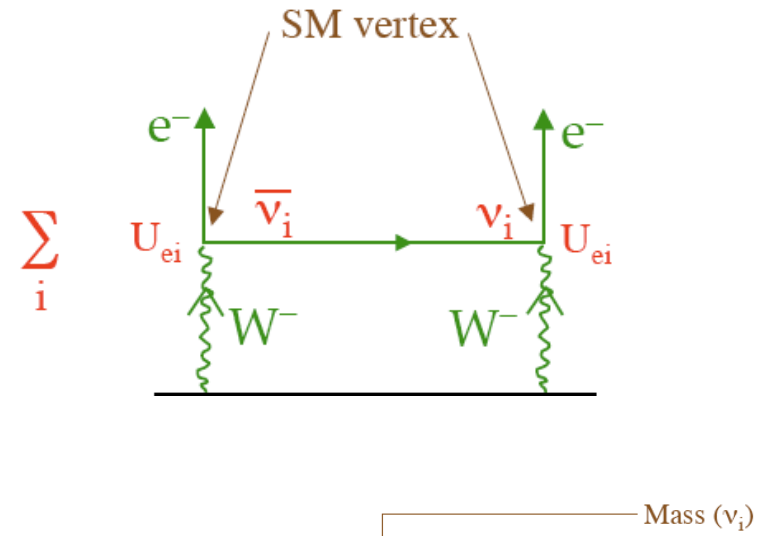
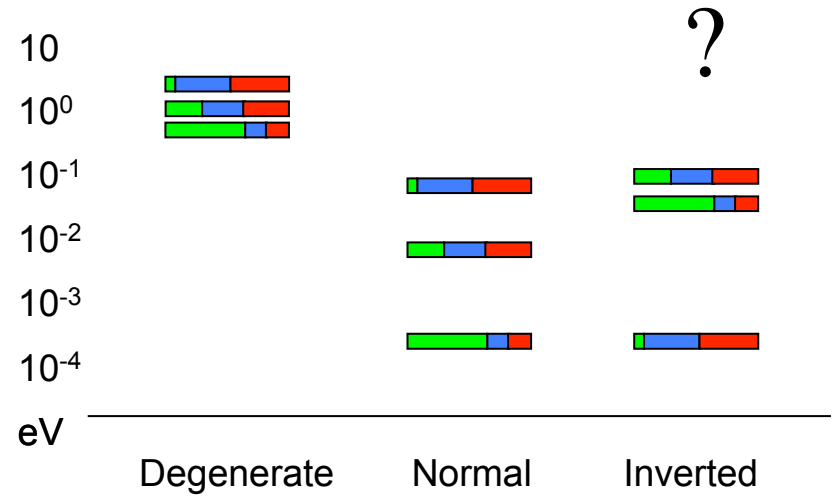
- Neutrinoless double  $\beta$  decay

(3 light neutrinos)

... Ivo's talk



*$m_{\beta\beta}$  For Each Hierarchy*



$$\text{Amp}[0\nu\beta\beta] \propto \left| \sum m_i U_{ei}^2 \right| \equiv m_{\beta\beta}$$

# Sequential see saw and (1,1) texture zero

(1,1) texture zero

$$\frac{M^{Dirac}}{m_3} = \begin{pmatrix} < \varepsilon^4 & \varepsilon^3 + \varepsilon^4 & -\varepsilon^3 + \varepsilon^4 \\ \varepsilon^3 + \varepsilon^4 & a\varepsilon^2 + \varepsilon^3 & -a\varepsilon^2 + \varepsilon^3 \\ -\varepsilon^3 + \varepsilon^4 & -a\varepsilon^2 + \varepsilon^3 & 1 \end{pmatrix}$$

# Sequential see saw and (1,1) texture zero

Quark sector zero  $\Rightarrow |V_{us}| = \left| \sqrt{\frac{m_d}{m_s}} - e^{i\delta} \sqrt{\frac{m_u}{m_c}} \right|$

(1,1) texture zero

$$\frac{M^{Dirac}}{m_3} = \begin{pmatrix} < \varepsilon^4 & \varepsilon^3 + \varepsilon^4 & -\varepsilon^3 + \varepsilon^4 \\ \varepsilon^3 + \varepsilon^4 & a\varepsilon^2 + \varepsilon^3 & -a\varepsilon^2 + \varepsilon^3 \\ -\varepsilon^3 + \varepsilon^4 & -a\varepsilon^2 + \varepsilon^3 & 1 \end{pmatrix}$$

# Sequential see saw and (1,1) texture zero

Lepton sector zero  $\Rightarrow \sin^2 \theta_{23} \simeq \frac{1}{2}$ ,  $\sin \theta_{13} \simeq \sqrt{\frac{m_e}{2m_\mu}}$

(1,1) texture zero

$$\frac{M^{Dirac}}{m_3} = \begin{pmatrix} < \varepsilon^4 & \varepsilon^3 + \varepsilon^4 & -\varepsilon^3 + \varepsilon^4 \\ \varepsilon^3 + \varepsilon^4 & a\varepsilon^2 + \varepsilon^3 & -a\varepsilon^2 + \varepsilon^3 \\ -\varepsilon^3 + \varepsilon^4 & -a\varepsilon^2 + \varepsilon^3 & 1 \end{pmatrix}$$

# SUSY flavour and CP problem : soft SUSY breaking terms

Leading term degenerate

$$\begin{aligned}
 (\hat{m}_{f,f^c}^2)_{\bar{a}b} = & m_{3/2}^2 \left[ \delta_{\bar{a}b} \left( k_0^{f,f^c} + l_0^{f,f^c} \frac{\langle X^\dagger X \rangle}{M_{Pl}^2} - l_0^{f,f^c} \frac{F_{X^\dagger} F_X}{m_{3/2}^2 M_{Pl}^2} \right) \right. \\
 & \left. + \sum_A \frac{\langle \phi_A^* \rangle_{\bar{a}} \langle \phi_A \rangle_b}{M_f^2} \left( k_A^{f,f^c} (1 - x_A x_A^*) - l_A^{f,f^c} \frac{F_{X^\dagger} F_X}{m_{3/2}^2 M_{Pl}^2} \right) - k_4^{f,f^c} \delta_{\bar{a}b} \frac{\langle \Sigma^* \rangle \langle \Sigma \rangle}{M_\Sigma^2} x_\Sigma x_\Sigma \right]
 \end{aligned}$$

FCNC

# SUSY flavour and CP problem : soft SUSY breaking terms

Leading term degenerate

$$\begin{aligned}
 (\hat{m}_{f,f^c}^2)_{\bar{a}b} = & m_{3/2}^2 \left[ \delta_{\bar{a}b} \left( k_0^{f,f^c} + l_0^{f,f^c} \frac{\langle X^\dagger X \rangle}{M_{Pl}^2} - l_0^{f,f^c} \frac{F_{X^\dagger} F_X}{m_{3/2}^2 M_{Pl}^2} \right) \right. \\
 & \left. + \sum_A \frac{\langle \phi_A^* \rangle_{\bar{a}} \langle \phi_A \rangle_b}{M_f^2} \left( k_A^{f,f^c} (1 - x_A x_A^*) - l_A^{f,f^c} \frac{F_{X^\dagger} F_X}{m_{3/2}^2 M_{Pl}^2} \right) - k_4^{f,f^c} \delta_{\bar{a}b} \frac{\langle \Sigma^* \rangle \langle \Sigma \rangle}{M_\Sigma^2} x_\Sigma x_\Sigma \right]
 \end{aligned}$$

FCNC

$$F_\phi = \frac{\partial W}{\partial \phi} + \phi^* W, \quad \langle W \rangle = m_{3/2}$$

Determined by Yukawa structure

$$\begin{aligned}
 A_{abc} \propto & \left\langle F_X \left( \partial_X \frac{K_{\text{hid}}}{M_{Pl}^2} \right) Y_{abc} + \sum_\Phi F_\Phi \partial_\Phi Y_{abc} \right. \\
 & \left. - \left( F_X (\tilde{K}^{-1})_{d\bar{e}} \partial_X \tilde{K}_{\bar{e}a} Y_{dbc} + \sum_\Phi F_\Phi (\tilde{K}^{-1})_{d\bar{e}} \partial_\Phi \tilde{K}_{\bar{e}a} Y_{dbc} + \text{cyclic}(a, b, c) \right) \right\rangle
 \end{aligned}$$



# SUSY flavour and CP problem : soft SUSY breaking terms

Leading term degenerate

$$\begin{aligned}
 (\hat{m}_{f,f^c}^2)_{\bar{a}b} &= m_{3/2}^2 \left[ \delta_{\bar{a}b} \left( k_0^{f,f^c} + l_0^{f,f^c} \frac{\langle X^\dagger X \rangle}{M_{Pl}^2} - l_0^{f,f^c} \frac{F_{X^\dagger} F_X}{m_{3/2}^2 M_{Pl}^2} \right) \right. \\
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 \end{aligned}$$

Misalignment of Yukawa and A-terms?

e.g.  $P = Y_{ij} Q_i q_j^c H_a \propto \left(\frac{\theta}{M}\right)^{\alpha(i,j)} Q_i q_j^c H_a$

$$A_{ij} Y_{ij} \tilde{Q}_i \tilde{q}_j^c H_a = (3 + \alpha(i,j)) m_{3/2} Y_{ij} \tilde{Q}_i \tilde{q}_j^c H_a$$

$$F_{\phi,\Sigma} = m_{3/2} \langle \phi, \Sigma \rangle, \text{ "natural" value}$$

GGR, Vives

(Here  $\alpha(i,j) = 2$  so  $Y$  and  $A$  aligned if  $F_\Sigma = 0$ )

suppression factor  $\left(\frac{m_{3/2}}{M_\phi}\right)^2$  possible

Antusch et al

## CP ?

$$\phi_A = \text{Arg}(Am_{1/2}^*), \quad \phi_B = \text{Arg}(Bm_{1/2}^*) < 10^{-2} ?$$

SUSY CP problem has a simple solution in familon models:

- CP invariant in underlying theory (string compactification)
- Spontaneously broken in **flavour changing** familon sector

Dine, Leigh, MacIntyre

GGR, Velasco Sevilla, Vives

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## CP violation and FCNC

Mass insertion bounds

$$(\delta_{LL}^f)_{ij} = \frac{(m_{\tilde{f}LL}^2)_{ij}}{\langle m_{\tilde{f}} \rangle_{LL}^2}, \quad (\delta_{RR}^f)_{ij} = \frac{(m_{\tilde{f}RR}^2)_{ij}}{\langle m_{\tilde{f}} \rangle_{RR}^2}, \quad (\delta_{LR}^f)_{ij} = \frac{(m_{\tilde{f}LR}^2)_{ij}}{\langle m_{\tilde{f}} \rangle_{LR}^2}$$

Most stringent bounds  
(Determined by A terms)

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### EDMs

$$|\text{Im}(\delta_{LR}^u)_{11}| \approx 2 \times 10^{-7} \frac{A_0}{100 \text{ GeV}} \left( \frac{500 \text{ GeV}}{\langle \tilde{m}_u \rangle_{LR}} \right)^2 \left( \frac{\bar{\epsilon}}{0.13} \right)^3 \left( \frac{\epsilon}{0.05} \right)^2 |y_1^f + y_2^f| |x_{123} - x_{23} - x_\Sigma| \sin \phi_1, \quad \leq 10^{-6} |_{\text{Expt}}$$

$$|\text{Im}(\delta_{LR}^d)_{11}| \approx 5 \times 10^{-7} \frac{A_0}{100 \text{ GeV}} \left( \frac{500 \text{ GeV}}{\langle \tilde{m}_d \rangle_{LR}} \right)^2 \left( \frac{\bar{\epsilon}}{0.13} \right)^5 \frac{10}{\tan \beta} |y_1^f + y_2^f| |x_{123} - x_{23} - x_\Sigma| \sin \phi_1, \quad \leq 10^{-6} |_{\text{Expt}}$$

$$|\text{Im}(\delta_{LR}^\ell)_{11}| \approx 2 \times 10^{-7} \frac{A_0}{100 \text{ GeV}} \left( \frac{200 \text{ GeV}}{\langle \tilde{m}_\ell \rangle_{LR}} \right)^2 \left( \frac{\bar{\epsilon}}{0.13} \right)^5 \frac{10}{\tan \beta} |y_1^f + y_2^f| |x_{123} - x_{23} - x_\Sigma| \sin \phi_1, \quad \leq 10^{-7} |_{\text{Expt}}$$

### $\mu \rightarrow e\gamma$

$$|(\delta_{LR}^\ell)_{12}| \approx 1 \times 10^{-4} \frac{A_0}{100 \text{ GeV}} \frac{(200 \text{ GeV})^2}{\langle \tilde{m}_l \rangle_{LR}^2} \frac{10}{\tan \beta} \left( \frac{\bar{\epsilon}}{0.13} \right)^3 |y_1| |x_{123} - x_{23} - x_\Sigma| \quad \leq 10^{-5} |_{\text{Expt}}$$

Antusch, King, Malinsky, GGR  
Calibbi, Jones-Perez, Vives

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Dine, Leigh, MacIntyre

GGR, Velasco Sevilla, Vives

## CP violation and FCNC

$$F_\Sigma \simeq 0$$

### EDMs

$$|\text{Im}(\delta_{LR}^u)_{11}| \lesssim 2 \times 10^{-8} \frac{A_0}{100 \text{ GeV}} \left( \frac{500 \text{ GeV}}{\langle \tilde{m}_u \rangle_{LR}} \right)^2 \left( \frac{\bar{\epsilon}}{0.15} \right)^3 \left( \frac{\epsilon}{0.05} \right)^3 \sin \phi_1 \leq 10^{-6} |_{\text{Expt}}$$

$$|\text{Im}(\delta_{LR}^d)_{11}| \sim 2 \times 10^{-7} \frac{A_0}{100 \text{ GeV}} \left( \frac{500 \text{ GeV}}{\langle \tilde{m}_d \rangle_{LR}} \right)^2 \left( \frac{\bar{\epsilon}}{0.15} \right)^6 \frac{10}{\tan \beta} \sin \phi_1 \leq 10^{-6} |_{\text{Expt}}$$

$$|\text{Im}(\delta_{LR}^\ell)_{11}| \sim 6 \times 10^{-8} \frac{A_0}{100 \text{ GeV}} \left( \frac{200 \text{ GeV}}{\langle \tilde{m}_e \rangle_{LR}} \right)^2 \left( \frac{\bar{\epsilon}}{0.15} \right)^6 \frac{10}{\tan \beta} \sin \phi_1 \leq 10^{-7} |_{\text{Expt}}$$

### $\mu \rightarrow e\gamma$

$$|(\delta_{LR}^e)_{12}| \lesssim |(\delta_{LR}^\ell)_{12}| \sim 3 \times 10^{-5} \frac{A_0}{100 \text{ GeV}} \frac{(200 \text{ GeV})^2}{\langle \tilde{m}_l \rangle_{LR}^2} \frac{10}{\tan \beta} \left( \frac{\bar{\epsilon}}{0.15} \right)^4 \leq 10^{-5} |_{\text{Expt}}$$

Antusch, King, Malinsky, GGR

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$$m_{\beta\beta}$$

- Sparticle masses, CP violation and FCNC

SUSY models: sparticles have related mass structure

$(m^2 \phi_i^\dagger \phi_i \dots$  degeneracy split by small fermion mass related terms)

*FCNC* :  $L_i, B_i$  violation – close to present bounds

$(\mu \rightarrow e\gamma, \text{mercury EDM within a factor of } 10 \text{ of present limits})$

