

# Probing Randall-Sundrum Model through FCNC

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Ringberg Workshop  
on New Physics, Flavors and Jets

Ringberg, April 28<sup>th</sup> 2009

# Outline

## 1. Motivations for WED:

- ◆ Natural Generation of Hierarchies in Masses and Mixings: Flavor Problem
- ◆ Addressing Gauge-Hierarchy Problem
- ◆ ...

## 2. Randall-Sundrum Scenario:

- ◆ The Model analyzed
- ◆ New Features in the Flavor Sector (FCNC at Tree Level and non Unitarity of CKM)
- ◆ Neutral Meson Mixing: Theory and Numerics
- ◆ Rare Decays of B and K Mesons: Theory and Numerics

## 3. Conclusions

- M. Blanke, A.J.Buras, B.Duling, S.Gori, A.Weiler [JHEP03(2009)001]
- M. Blanke, A. J. Buras, B. Duling, K. Gemmler, S. Gori [JHEP 0903:108,2009]
- M. Albrecht, M. Blanke, A. J. Buras, B. Duling, K. Gemmler arXiv:0903.2415 [hep-ph]
- A. J. Buras, B. Duling, S. Gori ..... arXiv of this week!

# Flavor Problem & its Solution (1)

◆ Experiments tell us:

I. quarks and charged leptons have

$$m_e \approx 0.5 \text{ MeV} , m_\tau \approx 1800 \text{ MeV}, \dots$$

$$m_u \approx 2.5 \text{ MeV} , m_t \approx 170 \text{ GeV}, \dots$$

◆ ... and the theory:

III. at the same time CKM picture describes data surprisingly well

hierarchies

II. also CKM mixing between quark

$$|V_{ud}| \approx 1 , |V_{us}| \approx 0.226$$

$$|V_{cb}| \approx 0.041 , |V_{ub}| \approx 0.0038$$

SM Yukawa couplings have to exhibit an extremely hierarchical structure, **why?**

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SM Yukawa couplings have to exhibit an extremely hierarchical structure, **why?**

→ How to solve it in the WED Contexts?

◆ Preliminaries

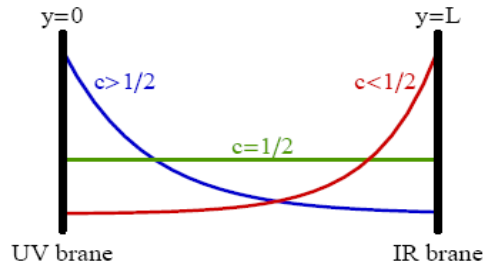
- Gauge fields and matter fields can propagate into the 5<sup>th</sup> dimension
- For each particle species, there is an infinite number of solutions:

Kaluza-Klein tower of particles

- Zero mode solutions (if existent) are identified with the SM particles

# Flavor Problem & its Solution (2)

## Zero Modes of Fermions:



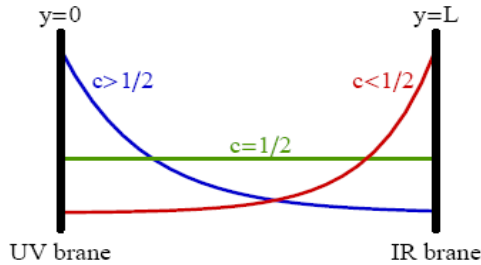
$$ds^2 = e^{-2ky} \eta_{\mu\nu} dx^\mu dx^\nu - dy^2, \quad 0 \leq y \leq L$$

$$f^{(0)}(y, c) = \sqrt{\frac{(1-2c)kL}{e^{(1-2c)kL} - 1}} e^{(\frac{1}{2}-c)ky}$$

Strong dependence on bulk masses

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Strong dependence on bulk masses

## The Solution of the Flavor Problem:

### I. 4D Yukawas in terms of shape functions:

$$Y_{ij} \propto \int_0^L \frac{dy}{L^{3/2}} \lambda_{ij} h(y) f_L^{(0)}(y, c^i) f_R^{(0)}(y, c^j)$$

5D Yukawas

$\lambda_{ij}$  assumed to be **anarchical** and O(1)

Higgs localized on the IR brane:  $h(y) = \sqrt{2(\beta-1)kL} e^{kL} e^{\beta k(y-L)}, \quad \beta > 1$

II. Result: slightly different  $c$  parameters of O(1) lead to a large hierarchy in  $Y_{ij}$

Hierarchy of quark masses and mixings explained by a **purely geometrical approach!** 😊

**BUT** 😞  
Still missing a theory for the bulk masses

Numerical example:

$$c_1 = 0.66, \quad c_2 = 0.59, \quad c_3 = 0.41$$

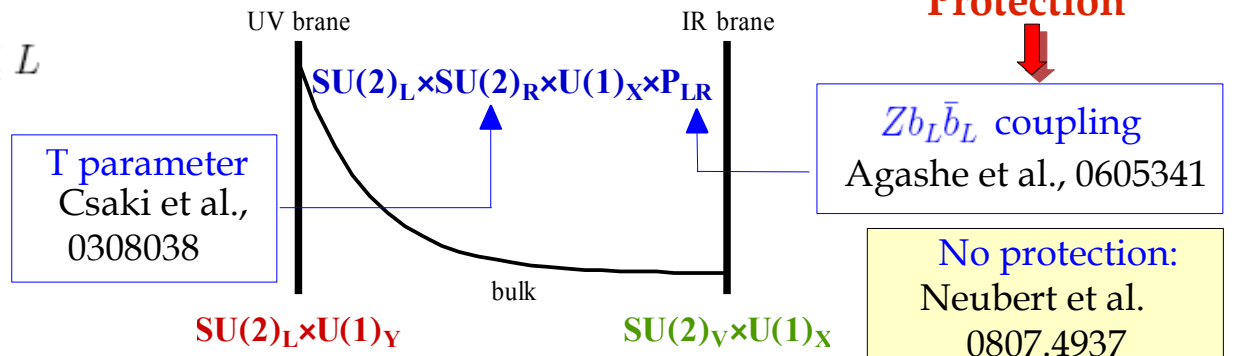
$$Y_1 = 0.0017, \quad Y_2 = 0.017, \quad Y_3 = 0.42$$

# Definition of the Model

## 1. Symmetry group and geometric structure:

$$ds^2 = e^{-2ky} \eta_{\mu\nu} dx^\mu dx^\nu - dy^2, \quad 0 \leq y \leq L$$

$$\begin{cases} e^{-kL} \approx 10^{-16} \\ M_{KK} \approx 2.45ke^{-kL} \approx \mathbf{2.45 TeV} \end{cases}$$



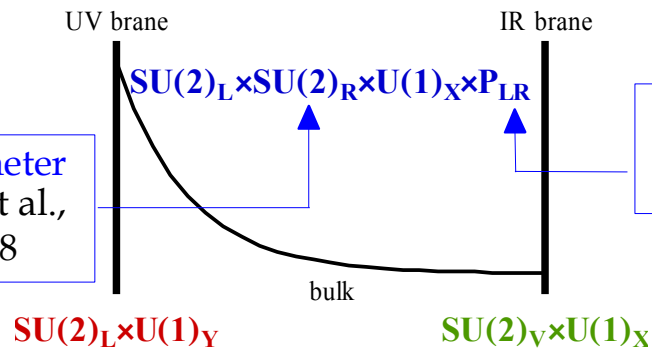
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T parameter  
Csaki et al.,  
0308038



WED with Custodial Protection

$Zb_L\bar{b}_L$  coupling  
Agashe et al., 0605341

No protection:  
Neubert et al.  
0807.4937

## 2. Field content:

### ◆ Gauge bosons:

I. Gauge eigenstates:

$$W_{L\mu}^a(++), \quad B_\mu(++), \quad G_\mu^c(++),$$

$$W_{R\mu}^b(-+), \quad Z_{X\mu}(-+)$$

$$a = 1, 2, 3; \quad b = 1, 2; \quad c = 1, \dots, 8$$

II. Mass eigenstates:

$$W_\mu^\pm, \quad W_{H\mu}^\pm, \quad \tilde{W}_\mu^\pm$$

$$A_\mu, \quad A_\mu^{(1)}$$

$$Z_\mu, \quad Z_{H\mu}, \quad Z'_\mu$$

$$G_\mu^{(0)}, \quad G_\mu^{(1)}$$

Gauge bosons of the SM

### ◆ Higgs boson:

I. Bi-doublet of  $SU(2)_L \times SU(2)_R$

II. EWSB mechanism is not specified

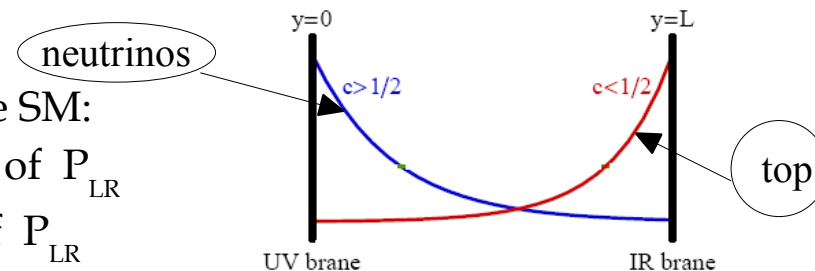
III. Resides on the IR brane

### ◆ Fermions:

I. Different localizations in the bulk of the fermions of the SM:

II. LH down quarks (all three generations) are eigenstates of  $P_{LR}$

III. RH up quarks (all three generations) are eigenstates of  $P_{LR}$





# Protection Mechanism

Generalization of Agashe et al., 0605341

**Theorem:** In theories with  $SU(2)_L \times SU(2)_R \times P_{LR}$  gauge symmetry  
 if a fermion  $F$  has  $T_L = T_R$ ,  $T_L^3 = T_R^3$  or  $T_L^3 = T_R^3 = 0$   
 then  
 its coupling  $ZF\bar{F}$  is **SM like**

**In RS model:** relation not spoiled by the mixing with KK-fermions



Buras, Duling, SG

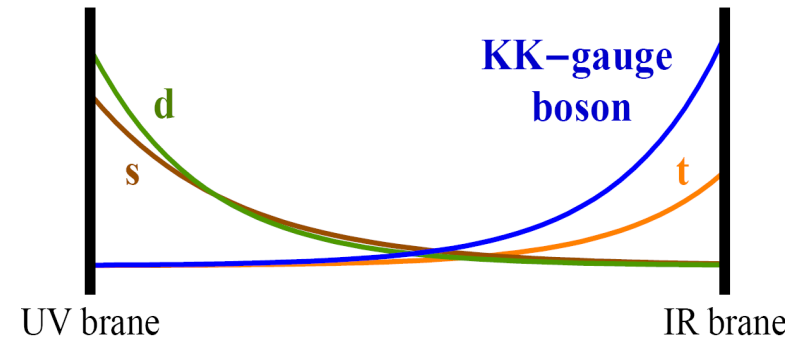
**Consequence for SM fermions:**  $Zd_L^i \bar{d}_L^j$  and  $Zu_R^i \bar{u}_R^j$  are mainly SM like

Blanke, Buras, Duling,  
 Gemmler, SG  
 JHEP 0903:108,2009

Small contributions to flavor violation  
 due to the breaking of  $P_{LR}$  symmetry

# Non Universality & FCNC at Tree Level

- ◆ KK tower of heavy gauge bosons  
...that are all localized towards the IR brane



- ◆ Their couplings to SM fermions are **non-universal**  
...because couplings to SM fermions depend on their localization

$$\Delta_{L,R} \propto \int_0^L dy e^{ky} \left[ f_{L,R}^{(0)}(y, c_\Psi^i) \right]^2 g(y)$$

## Rotation to mass eigenstates:

non universalities



off-diagonal terms

Flavor Changing Neutral Currents at Tree Level

$$\Delta_{L,R} \sim U^\dagger \begin{pmatrix} \clubsuit & & \\ & \spadesuit & \\ & & \heartsuit \end{pmatrix} U$$

Non universalities

- ◆ New sources of flavor and CP violation beyond CKM: **model is non-MFV**

# FCNC for the Z boson of the SM

Two sources of FCNC at tree level: due to EWSB we have

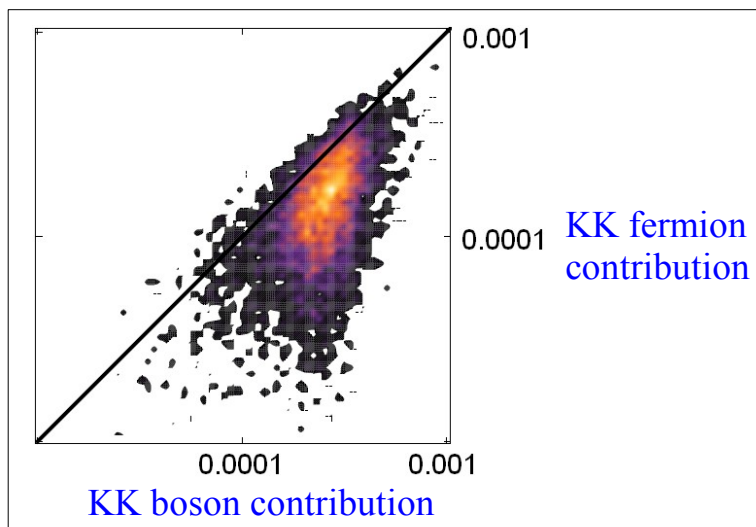
◆ Mixing between gauge bosons:  $Z = aZ^{(0)} + bZ^{(1)} + cZ_X^{(1)}$   
 Flat shape function  $\swarrow$   $\nwarrow$  Localized towards the IR brane  
 $\rightarrow$  Z: NOT flat shape function  $\rightarrow$  **FCNC**

◆ Mixing between SM and KK fermions:  $Up = (u, U^i), \text{ Down} = (d, D^i)$   
 $\left\{ \begin{array}{l} Up \rightarrow Up^{mass} \\ Down \rightarrow Down^{mass} \end{array} \right.$  In this rotation **FCNCs appear**  
 $\swarrow$   $\nwarrow$  1<sup>st</sup> KK-fermions

Example:

$$Zt_L\bar{c}_L$$

$$\frac{|\Delta_Z^{KK} - \Delta_Z^{SM}|}{|\Delta_Z^{SM}|}$$



General feature:  
1<sup>st</sup> KK fermion contributions  
**subdominant**

Buras, Duling, SG

# Unitarity of CKM matrix

$$V_{CKM} = \frac{\sqrt{2}}{g^{AD}} \tilde{U}_L G_L(W^+) \tilde{D}_L$$

$$U_L = \left( \begin{array}{c|c} \tilde{U}_L & \\ \hline & \end{array} \right)$$

$$D_L = \left( \begin{array}{c|c} \tilde{D}_L & \\ \hline & \end{array} \right)$$

Rotation matrices for  
Up and Down quarks

Two sources of non unitarity: due to EWSB we have

Mixing between gauge bosons



non universality in  $G_L(W^+)$

Mixing between SM and 1<sup>st</sup> KK fermions:



$$V_{CKM}^{18 \times 12} = \frac{\sqrt{2}}{g^{AD}} U_L G_L(W^+) D_L \text{ is unitary}$$

Numerically: gauge boson contribution predominant

$$\begin{cases} V_{CKM} \cdot V_{CKM}^\dagger = \mathbb{1} + \mathcal{O}\left(\frac{v^2}{M_{KK}^2}\right) \\ V_{CKM}^\dagger \cdot V_{CKM} = \mathbb{1} + \mathcal{O}\left(\frac{v^2}{M_{KK}^2}\right) \end{cases}$$

Largest contributions when quarks of the  
third family involved: **2%** effects

Comparison with experimental bounds:

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 > 0.9982 \quad (PDG, 2007)$$

We are inside this limit for **95%**  
of the points analyzed

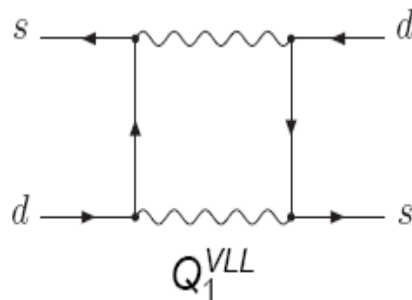
# Meson Mixing: some Theoretical Aspects

Example:

$K^0 - \bar{K}^0$  mixing

## Standard Model

Process through boxes



action of the GIM-mechanism

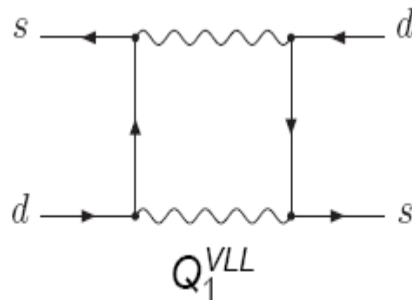
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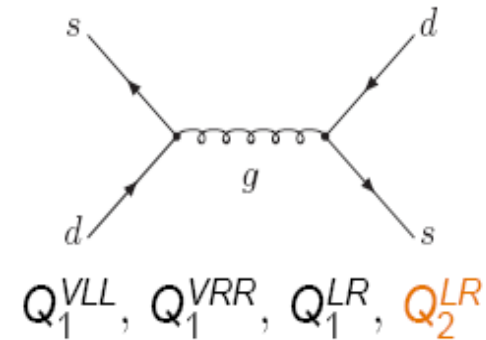
Process through boxes



action of the GIM-mechanism

## Warped Extra Dimensions

Process already at tree level



Operators involved:

$$Q_1^{VLL} = (\bar{s}\gamma_\mu P_L d) (\bar{s}\gamma_\mu P_L d) \quad (\text{also in the SM})$$

$$Q_1^{VRR} = (\bar{s}\gamma_\mu P_R d) (\bar{s}\gamma_\mu P_R d)$$

$$Q_1^{LR} = (\bar{s}\gamma_\mu P_L d) (\bar{s}\gamma_\mu P_R d)$$

$$Q_2^{LR} = (\bar{s}P_L d)(\bar{s}P_R d) \quad (\text{only for gluons})$$

Particles exchanged at tree level:

- ◆ KK gluons
- ◆ KK photons
- ◆  $Z, Z_H, Z'$

# Operator Structure in Meson Mixing

## ◆ In the K system:

- Large **chiral enhancement** of  $Q_2^{\text{LR}} \propto \left(\frac{m_K}{m_s + m_d}\right)^2$
- Strong **RG running** of  $Q_2^{\text{LR}}$

$Q_2^{\text{LR}}$  dominates  $\longrightarrow$  contribution of the gluons is predominant

## ◆ In the B system:

- Less pronounced **chiral enhancement** of  $Q_2^{\text{LR}} \propto \left(\frac{m_B}{m_b + m_{d,s}}\right)^2$
- A bit weaker **RG running** of  $Q_2^{\text{LR}}$

Both  $Q_1^{\text{VLL}}$  and  $Q_2^{\text{LR}}$  are important  $\longrightarrow$  EW gauge bosons are competitive (missed in the literature)

## ◆ In both systems:

- Z boson not relevant:
  - I. left-handed couplings protected by  $P_{\text{LR}}$
  - II. right-handed couplings enter only at higher order

# Our Approach to the Analysis of Meson Mixing

## Previous analysis:

Csaki, Falkowski, Weiler, [JHEP 0809:008,2008]

tension between anarchic Yukawas,  $\varepsilon_K$ , and a low high energy scale  $M_{KK}$

**totally anarchic Yukawas and constraint from  $\varepsilon_K \rightarrow M_{KK} \geq 21 \text{ TeV}$**



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**totally anarchic Yukawas and constraint from  $\varepsilon_K \rightarrow M_{KK} \geq 21 \text{ TeV}$**

## Issues ( $\varepsilon_K$ and beyond)

Blanke, Buras, Duling, SG, Weiler, [JHEP03(2009)001]

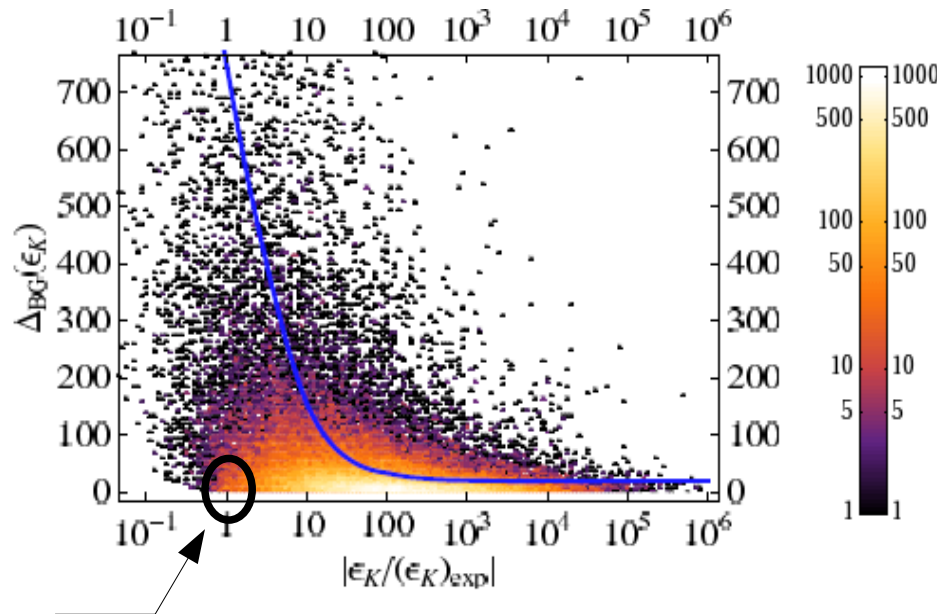
- ◆ Consider full operator basis and NLO RG running
- ◆ Take into account also **EW contributions**
- ◆ Partially give up complete anarchy of Yukawas
- ◆ Fix a **high energy scale in the reach of LHC** ( $M_{KK} \sim (2-3) \text{ TeV}$ )
- ◆ Fit all the well measured  $\Delta F=2$  observables
- ◆ Identify areas in parameter space with only **moderate fine tuning**
- ◆ Make prediction for the not well measured  $\Delta F=2$  observables

# $\epsilon_K$ : the most Challenging Observable

Our definition of fine tuning:

$$\left(\frac{1}{t}\right)_{BG} = \max_i \frac{d \log(Obs.)}{d \log(x_i)} = \max_i \frac{x_i}{Obs.} \frac{d Obs.}{dx_i}$$

Barbieri, Giudice  
Nucl.Phys.B306:63



- ◆ Generically  $\epsilon_K \sim 10^2 \epsilon_K^{\text{exp}}$
  - ◆ Average of the fine tuning decreases with increasing  $\epsilon_K$
- ◆ Parameter sets with moderate fine tuning and  $\epsilon_K \sim \epsilon_K^{\text{exp}}$  exist

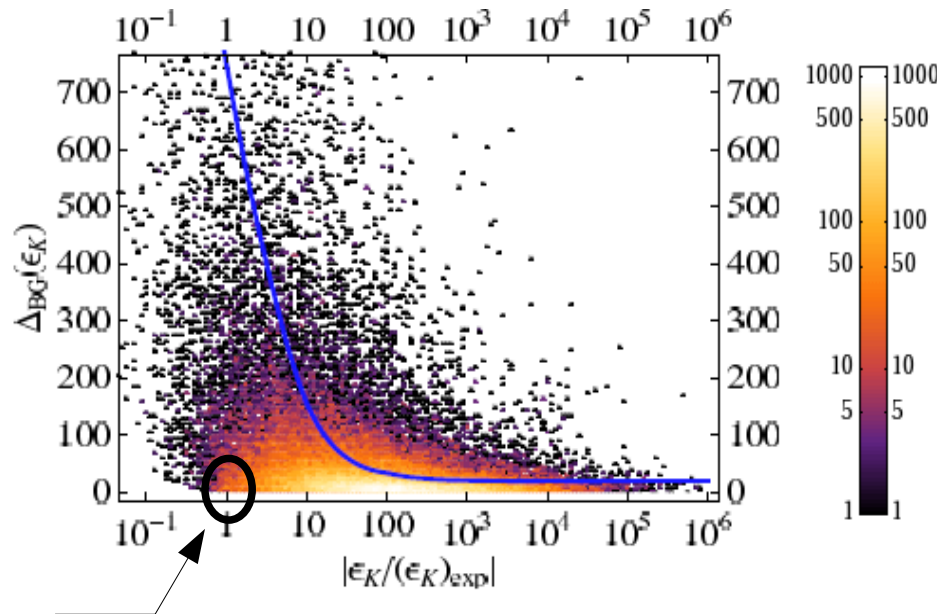
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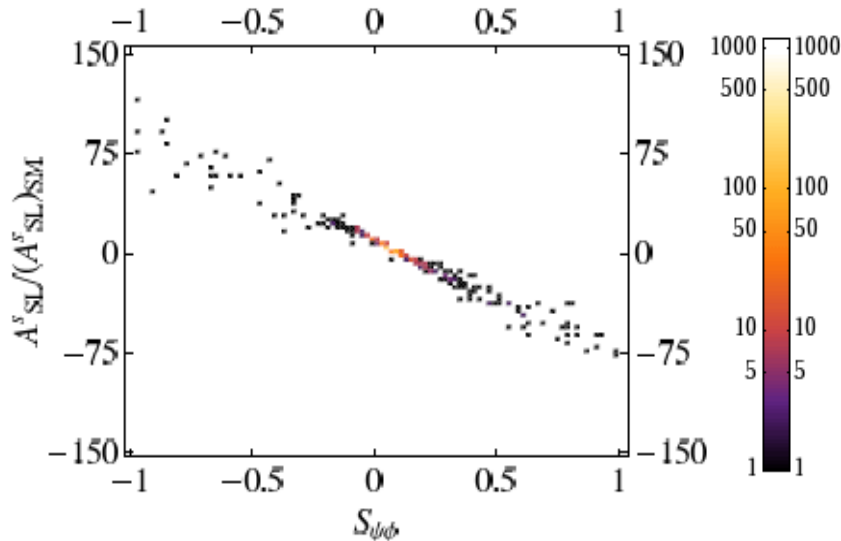


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fitting SM quark masses and CKM elements within  $2\sigma$

No problem in fitting all the other well measured  $\Delta F=2$  observables ( $\Delta M_{K'}, \Delta M_{d'}, \Delta M_{s'}, S_{\psi K_s}$ ) with small fine tuning

# Predictions for Observables not Measured yet



- ◆  $S_{\psi\phi}$  can be enhanced well beyond the SM prediction  $\sim 0.04$
- ◆ **Strong correlation** between the 2 observables exists

CDF,  $D\phi$  hint at  $S_{\psi\phi} \sim 0.4$



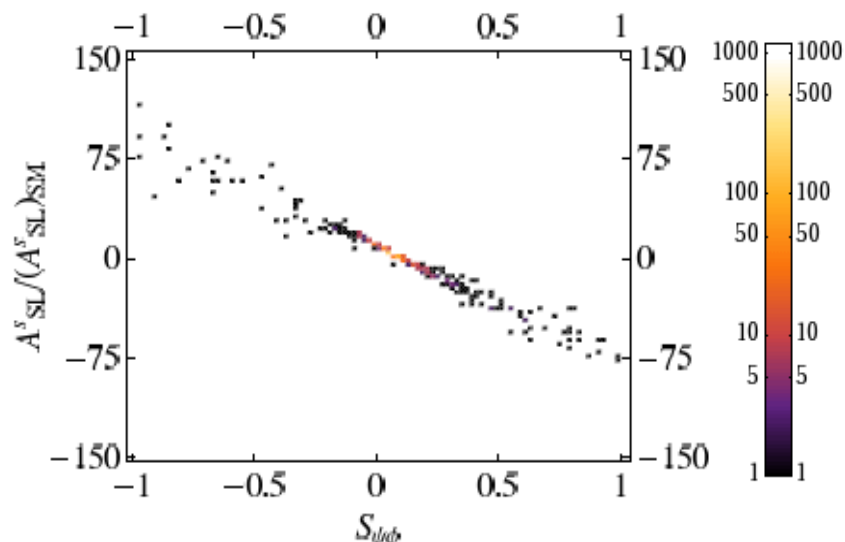
significant effects in  $A^s_{SL}$

fitting SM quark masses and CKM elements within  $2\sigma$

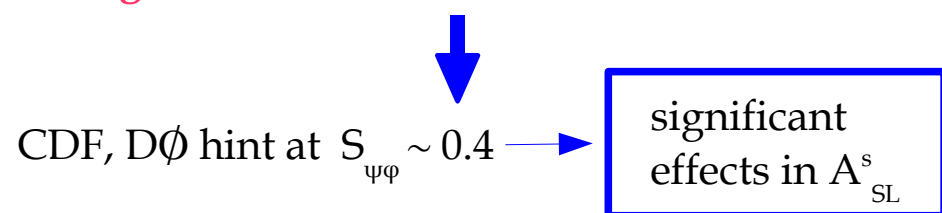
&

fitting all the well measured  $\Delta F=2$  observables, with small fine tuning ( $\leq 20$ )

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fitting SM quark masses and CKM elements within  $2\sigma$   
&

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## Small summary of the results in meson mixing:

It is possible to:

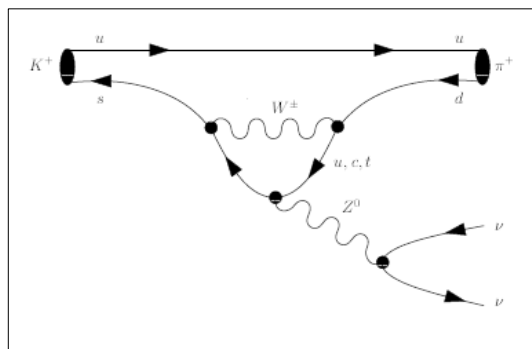
- ◆ Fit SM quark masses and CKM mixings
- ◆ Address the tension with  $\epsilon_K$  even with a low KK scale
- ◆ Fit all the precisely measured  $\Delta F=2$  observables
- ◆ Obtain large deviations from the SM of the not yet measured observables ( $S_{\psi\phi}$ )

# Rare Decays: some Theoretical Aspects

Example:

$$K^+ \rightarrow \pi^+ \nu \bar{\nu}$$

## Standard Model



first at **one loop level**

I. The effective Hamiltonian:

$$\mathcal{H}_{eff}^{SM} \propto V_{ts}^* V_{td} X_{SM} (\bar{s} \gamma_\mu P_L d) (\bar{\nu} \gamma_\mu P_L \nu)$$

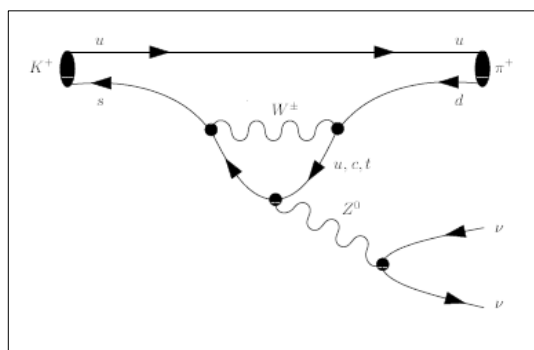
Only operator involved

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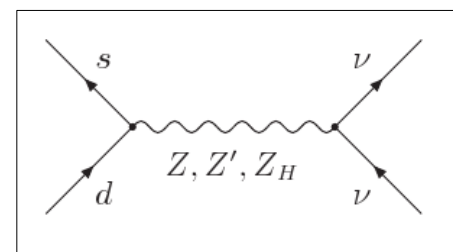
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Only operator involved

## Warped Extra Dimensions



additional diagrams at tree level

I. Modification of the coefficient of the SM operator

II. New operator is induced:

$$\mathcal{H}_{eff}^{new} \propto V_{ts}^* V_{td} X^V (\bar{s} \gamma_\mu d) (\bar{\nu} \gamma_\mu P_L \nu)$$

III. Main contributions from the coupling of Z to right handed down quarks

# Rare Decays: K physics vs B physics

$$s \rightarrow d \bar{\nu} \nu \quad vs \quad (b \rightarrow d \bar{\nu} \nu \quad \vee \quad b \rightarrow s \bar{\nu} \nu)$$

## Effective Hamiltonian:

$$\mathcal{H}_{eff}^{tot} \propto V_{tq_1}^* V_{tq_2} (X_{SM} + X_{q_1, q_2}^{V-A}) (\bar{q}_1 \gamma_\mu (1 - \gamma_5) q_2) (\bar{\nu} \gamma_\mu (1 - \gamma_5) \nu) + \\ + V_{tq_1}^* V_{tq_2} X_{q_1, q_2}^V (\bar{q}_1 \gamma_\mu q_2) (\bar{\nu} \gamma_\mu (1 - \gamma_5) \nu)$$

$$q_1 \rightarrow q_2 \bar{\nu} \nu$$

## where the new functions:

$$X_{q_1, q_2}^{V-A, V} \propto \frac{1}{\lambda_t^{(q)}} F^{V-A, V} (\Delta_L^{\nu\nu}, \Delta_{L, R}^{q_1, q_2})$$

$$\text{K meson: } \lambda_t^{(q)} = V_{ts}^* V_{td} \approx 4 \cdot 10^{-4}$$

$$\text{B mesons: } \lambda_t^{(q)} = V_{tb}^* V_{tq} \approx 10^{-2}, \quad q = d, s$$

## Main Messages:

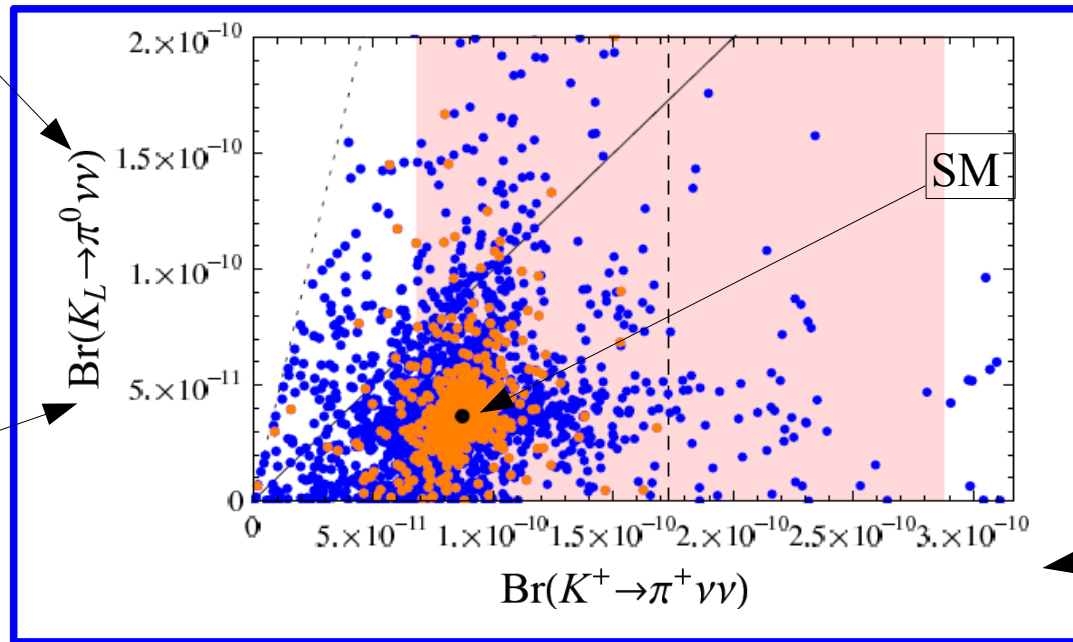
- I. Non universalities
- II. Expected: bigger contributions of new physics in the K sector
- III. X function is now complex  $\rightarrow$  new sources of CP violation



# Rare Decays of K mesons...

Theoretically very clean and very sensitive to  $Im(X_{SM} + X_{sd}^V + X_{sd}^{V-A})$

Possible deviation of **500%** from the SM



1) Points which satisfy all the  $\Delta F=2$  constraints;  
2) Also small fine tuning is imposed ( $\epsilon_K$ )

Possible deviation of **200%** from the SM

◆ Values predicted by the SM:

$$Br(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.4 \pm 0.8) 10^{-11}$$

$$Br(K_L \rightarrow \pi^0 \nu \bar{\nu}) = (2.9 \pm 0.4) 10^{-11}$$

◆ Experimental bounds:

$$Br(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (17.3^{+11.5}_{-10.5}) 10^{-11}$$

$$Br(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 2.1 \cdot 10^{-7} \quad (90\% CL)$$

◆ Some Observations:

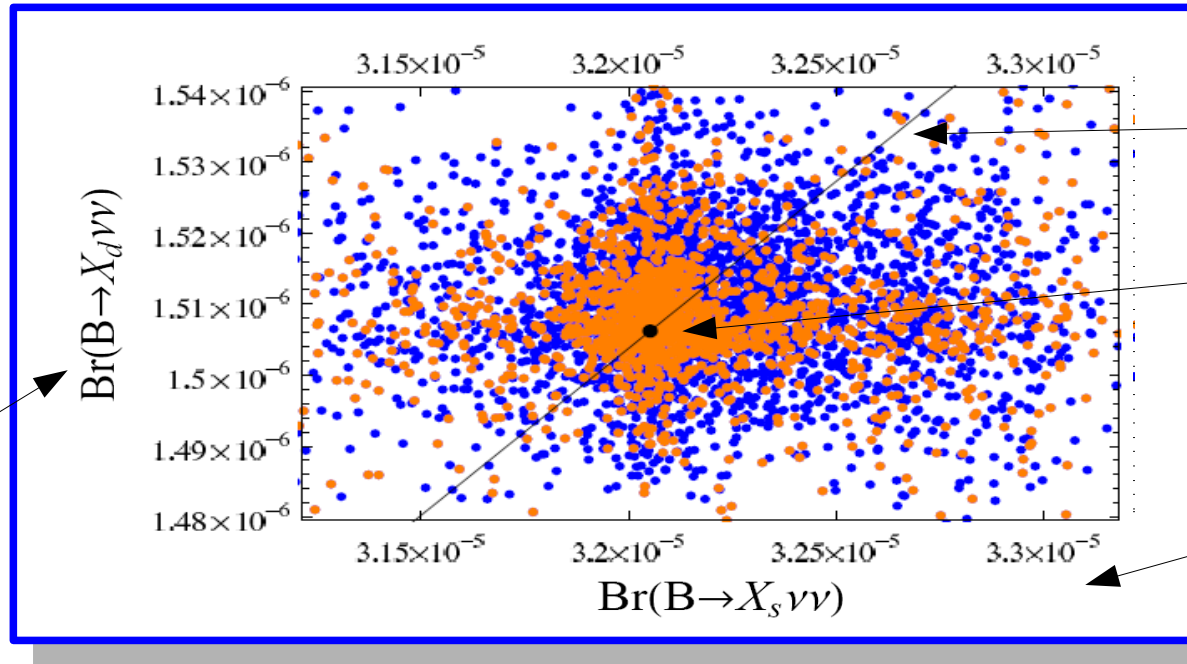
- I. It is possible to have **simultaneously big contributions** for both the branching ratios
- II. The most part of the points stays **in the experimental range** for  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

# ...and Rare Decays of B mesons

## Inclusive Decay

Possible deviation  
of **3%** from  
the SM

**B decays not  
very sensitive  
to new physics**



Model  
with **MFV**

SM

Possible deviation  
of **5%** from  
the SM

◆ Values predicted by the SM:

$$Br(B \rightarrow X_s \nu \bar{\nu}) \approx 3.2 \cdot 10^{-5}$$

$$Br(B \rightarrow X_d \nu \bar{\nu}) \approx 1.5 \cdot 10^{-6}$$

◆ Experimental bounds:

$$Br(B \rightarrow X_s \nu \bar{\nu}) < 64 \cdot 10^{-5}$$

$$Br(B \rightarrow X_d \nu \bar{\nu}) < ??$$

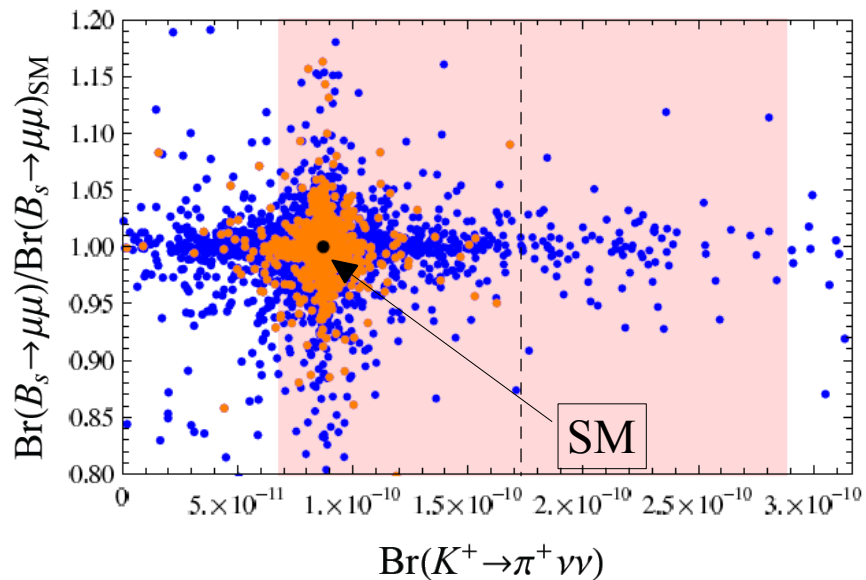
◆ Some Observations:

I. In general:  $\frac{Br(B \rightarrow X_d \nu \bar{\nu})}{Br(B \rightarrow X_s \nu \bar{\nu})} = \frac{|V_{td}|^2}{|V_{ts}|^2} P$  where  $P \equiv \frac{|X_d^{V-A} + X_d^V/2|^2 + |X_d^V/2|^2}{|X_s^{V-A} + X_s^V/2|^2 + |X_s^V/2|^2}$

I. Very **clean correlation** between the two observables in models with MFV:  
**P=1 (universality)**; in WED we have deviations

# Correlations

## B physics vs K physics



$\text{Br}(K^+ \rightarrow \pi^+ \nu \nu)$

### I. SM prediction

$$\text{Br}(B_s \rightarrow \mu^+ \mu^-) = (3.35 \pm 0.32) \cdot 10^{-9}$$

### II. Measurement

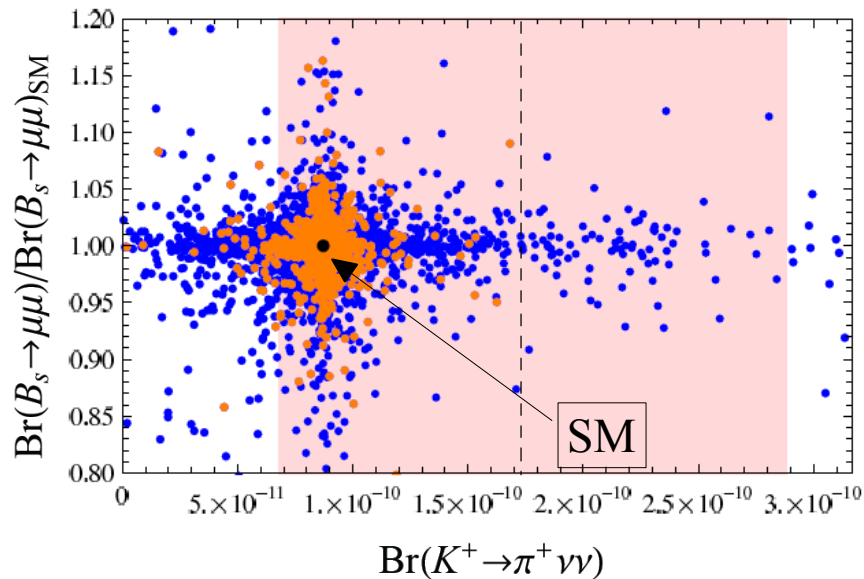
$$\text{Br}(B_s \rightarrow \mu^+ \mu^-) < 4.7 \cdot 10^{-8}$$

For the two decays:

Possible deviations of **15%** in the B system;  
Possible deviations of **200%** in the K system

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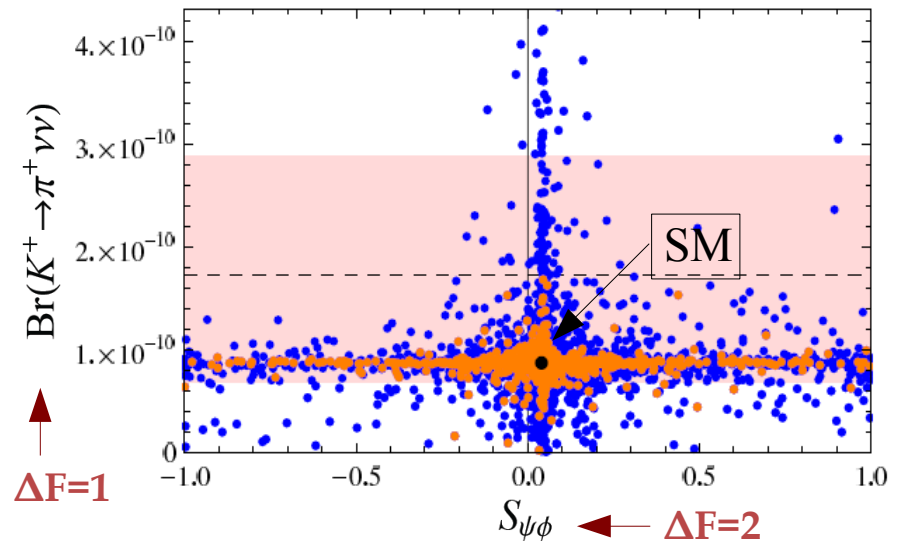
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## $\Delta F=1$ vs $\Delta F=2$ observables



### I. SM prediction

$$S_{\psi\phi} \approx 0.04, \quad Br(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.4 \pm 0.8) 10^{-11}$$

### II. Measurements

$$S_{\psi\phi} \approx 0.4, \quad Br(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (17.3^{+11.5}_{-10.5}) 10^{-11}$$

Difficult to obtain simultaneously  
large deviations from the SM  
for both observables

# Conclusions

## Warped Extra Dimension with custodial Protection shows:

### ◆ Elegant way to address:

- I. Flavor Problem
- II. Gauge-Hierarchy Problem
- III. ...

Testability at LHC since

$$M_{KK} \approx (2 - 3) TeV$$



### ◆ In the Flavor Sector:

#### I. Existence of regions of parameter space which:

- Fit masses of SM quarks and CKM elements
- Reproduce all the well measured  $\Delta F=2$  observables ( $\epsilon_{K'}$ ,  $\Delta M_{K'}$ ,  $\Delta M_{d'}$ ,  $\Delta M_{s'}$ ,  $S_{\psi K_s}$ )
- Have a **small amount of fine tuning** on the observables  $\rightarrow$  **Address the problem with  $\epsilon_K$**
- Can predict possible **large deviations** from the SM of observables not measured yet ( $S_{\psi\phi}$ ,  $A_{SL}^s$ )

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#### II. Restricting to these regions:

If future measurements of  $S_{\psi\phi}$  are:

- large: Branching ratios of **K meson** decays are small, **SM like**
- small: Room for **large deviations of K** meson decays from SM

**In any case B** meson decays can **deviate** only **slightly** from the SM

Predictions of the theory