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UNIVERSITÀ DI ROMA



# Higgs boson couplings characterization in the 4-lepton channel with the Run 2 data of the ATLAS Experiment at the LHC

36<sup>th</sup> IMPRS Workshop at Max Planck Institute of Physics

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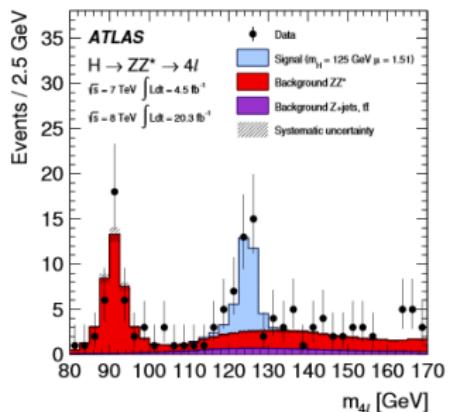
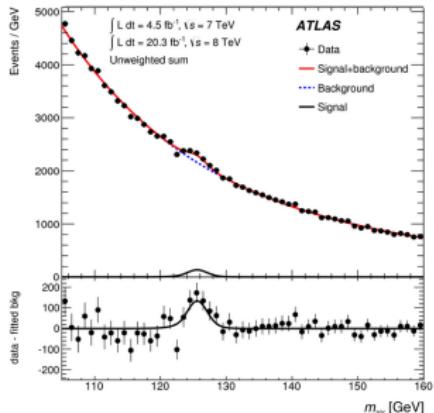
November 7, 2016

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# Outline

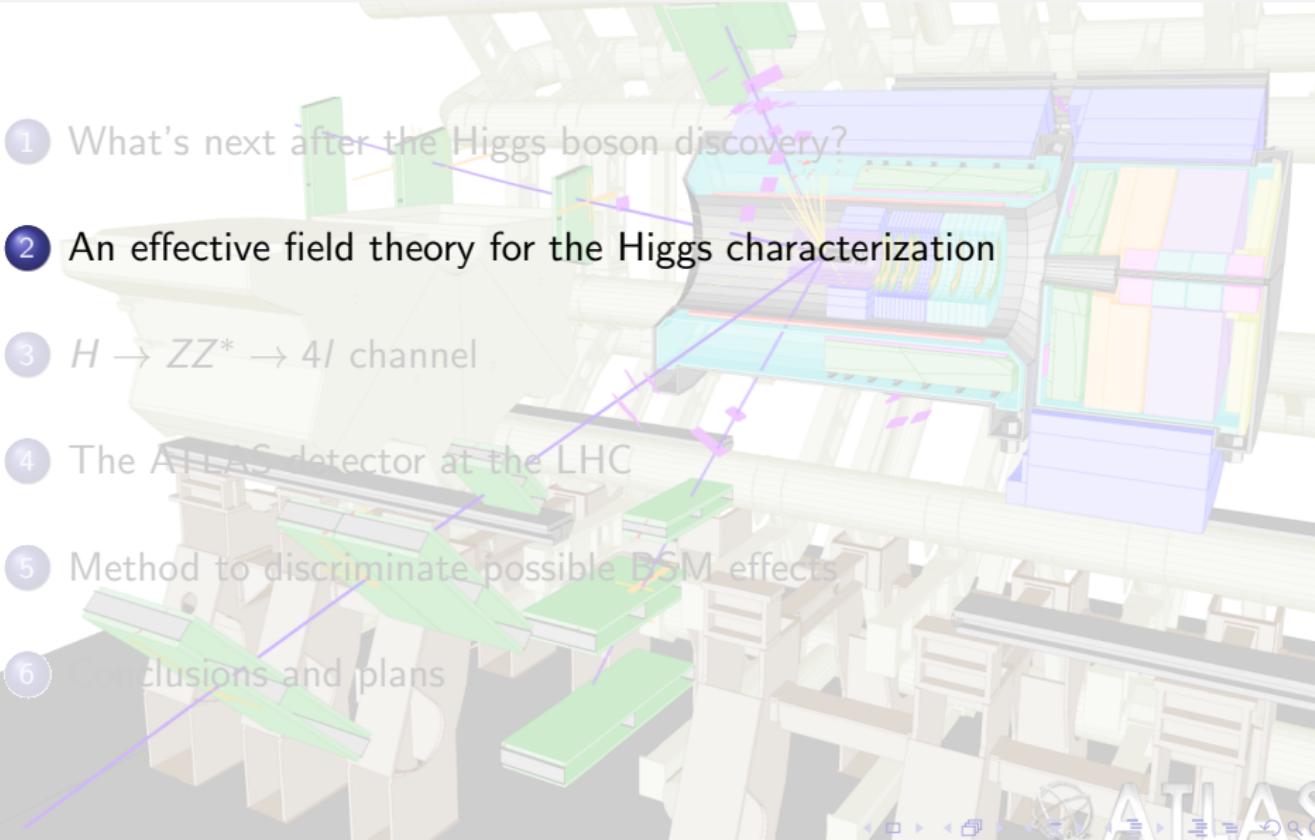
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- ➊ Higgs boson discovery from both ATLAS and CMS experiments
- ➋ exclusion of spin 1 and 2 hypotheses with the Run 1 data
- ➌ search for a discrepancy in the size and structure of the Higgs boson couplings with respect to the SM predictions
- ➍ assuming  $v$ , the vacuum expectation value, the expected values of the Higgs couplings with the vector bosons  $V$  and fermions  $f$  are:

$$g_{HVV} = \frac{2m_V^2}{v} , \quad g_{Hff} = \frac{m_f}{v}$$

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The Lagrangian of interaction of a bosonic state  $X(J^P)$  with spin/parity assignments  $0^+$ ,  $0^-$  with vector bosons can be written as follows [1]:

$$\mathcal{L}_0^V = \left\{ c_\alpha \kappa_{SM} \left[ \frac{1}{2} g_{HZZ} Z_\mu Z^\mu + g_{HWW} W_\mu^+ W^{-\mu} \right] \right. \\ \left. - \frac{1}{4} \left[ c_\alpha \kappa_{H\gamma\gamma} g_{H\gamma\gamma} A_{\mu\nu} A^{\mu\nu} + s_\alpha \kappa_{A\gamma\gamma} g_{A\gamma\gamma} \tilde{A}_{\mu\nu} \tilde{A}^{\mu\nu} \right] \right. \\ \left. - \frac{1}{2} \left[ c_\alpha \kappa_{HZ\gamma} g_{HZ\gamma} Z_{\mu\nu} A^{\mu\nu} + s_\alpha \kappa_{AZ\gamma} g_{AZ\gamma} Z_{\mu\nu} \tilde{A}^{\mu\nu} \right] \right. \\ \left. - \frac{1}{4} \left[ c_\alpha \kappa_{Hgg} g_{Hgg} G_{\mu\nu}^a G^{a,\mu\nu} + s_\alpha \kappa_{Agg} g_{Agg} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \right] \right. \\ \left. - \frac{1}{4} \frac{1}{\Lambda} \left[ c_\alpha \kappa_{HZZ} Z_{\mu\nu} Z^{\mu\nu} + s_\alpha \kappa_{AZZ} Z_{\mu\nu} \tilde{Z}^{\mu\nu} \right] \right. \\ \left. - \frac{1}{2} \frac{1}{\Lambda} \left[ c_\alpha \kappa_{HWW} W_\mu^+ W^{-\mu\nu} + s_\alpha \kappa_{AWW} W_\mu^+ \tilde{W}^{-\mu\nu} \right] \right. \\ \left. - \frac{1}{\Lambda} c_\alpha \left[ \kappa_{H\partial\gamma} Z_\nu \partial_\mu A^{\mu\nu} + \kappa_{H\partial Z} Z_\nu \partial_\mu Z^{\mu\nu} + (\kappa_{H\partial W} W_\nu^+ \partial_\mu W^{-\mu\nu} + h.c.) \right] \right\} X_0$$

SM contribution

- $\kappa_{SM} = 1$
- $c_\alpha = 1$
- all other  $\kappa$ -parameters  
not in the box equal to 0.

Assumption:  $k_{HZZ} = k_{HWW} = k_{HVV}$  and  $k_{AZZ} = k_{AWW} = k_{AVV}$

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bSM couplings  
with W and Z  
studied in this  
analysis

$$- \frac{1}{4} \left[ c_\alpha \kappa_{H\gamma\gamma} g_{H\gamma\gamma} A_{\mu\nu} A^{\mu\nu} + s_\alpha \kappa_{A\gamma\gamma} g_{A\gamma\gamma} A_{\mu\nu} \tilde{A}^{\mu\nu} \right]$$

$$- \frac{1}{2} \left[ c_\alpha \kappa_{HZ\gamma} g_{HZ\gamma} Z_{\mu\nu} A^{\mu\nu} + s_\alpha \kappa_{AZ\gamma} g_{AZ\gamma} Z_{\mu\nu} \tilde{A}^{\mu\nu} \right]$$

$$- \frac{1}{4} \left[ c_\alpha \kappa_{Hgg} g_{Hgg} G_{\mu\nu}^a G^{a,\mu\nu} + s_\alpha \kappa_{Agg} g_{Agg} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \right]$$

$$- \frac{1}{4} \frac{1}{\Lambda} \left[ c_\alpha \kappa_{HZZ} Z_{\mu\nu} Z^{\mu\nu} + s_\alpha \kappa_{AZZ} Z_{\mu\nu} \tilde{Z}^{\mu\nu} \right]$$

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CP-conserving

$$-\frac{1}{4} \left[ c_\alpha \kappa_{Hgg} g_{Hgg} G_{\mu\nu}^a G^{a,\mu\nu} + s_\alpha \kappa_{Agg} g_{Agg} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \right]$$

$$-\frac{1}{4} \frac{1}{\Lambda} \left[ c_\alpha \kappa_{HZZ} Z_{\mu\nu} Z^{\mu\nu} + s_\alpha \kappa_{AZZ} Z_{\mu\nu} \tilde{Z}^{\mu\nu} \right]$$

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$$-\frac{1}{\Lambda} c_\alpha \left[ \kappa_{H\partial\gamma} Z_\nu \partial_\mu A^{\mu\nu} + \kappa_{H\partial Z} Z_\nu \partial_\mu Z^{\mu\nu} + (\kappa_{H\partial W} W_\nu^+ \partial_\mu W^{-\mu\nu} + h.c.) \right] \right\} X_0$$

Assumption:  $k_{HZZ} = k_{HWW} = k_{HVV}$  and  $k_{AZZ} = k_{AWW} = k_{AVV}$

Simona Gargiulo

Higgs boson couplings with  $W^\pm$  and  $Z^0$

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bSM couplings with W and Z studied in this analysis
CP-violating

$$-\frac{1}{4} \frac{1}{\Lambda} \left[ c_\alpha \kappa_{HZZ} Z_{\mu\nu} Z^{\mu\nu} + s_\alpha \kappa_{AZZ} Z_{\mu\nu} \tilde{Z}^{\mu\nu} \right]$$

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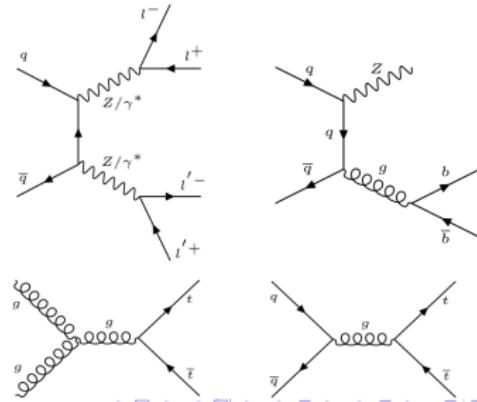
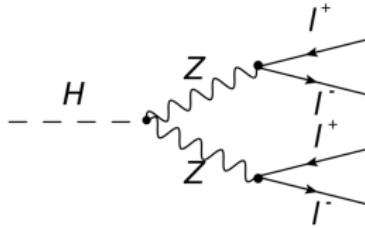
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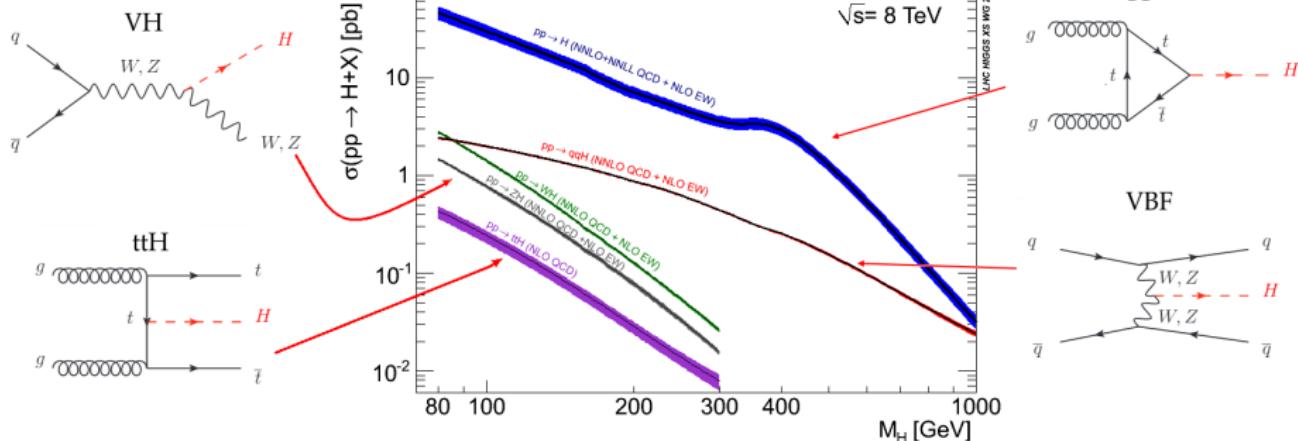
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# $H \rightarrow ZZ^* \rightarrow 4l$ channel

- $\text{BR}(H \rightarrow ZZ^* \rightarrow 4l) = 1.25 \times 10^{-4}$  at  $m_H = 125$  GeV
- $N_{\text{events}}^{\text{exp}} = \sigma_{SM} BRL_{\text{int}} \simeq 694$  with  $L_{\text{int}} = 100 \text{ fb}^{-1}$  at  $\sqrt{s} = 13$  TeV
- clean signature given by the presence of leptons ( $e$  and  $\mu$ ) in the final state
- single and dilepton trigger on  $e$  and  $\mu$
- Higgs boson candidate: quadruplet of two same-flavour, opposite-sign lepton pairs
- leptons in the quadruplet ordered in  $p_T$ :  $p_T > 20$  GeV,  $> 15$  GeV,  $> 10$  GeV,  $> 6$  GeV ( $\mu$ ) and  $> 7$  GeV ( $e$ )
- main backgrounds: irreducible  $pp \rightarrow ZZ^* \rightarrow 4l$ , reducible  $Z + \text{jets}$ ,  $t\bar{t}$





Event candidates divided into three experimental categories: 0jet, 1jet,  $\geq 2$  jets

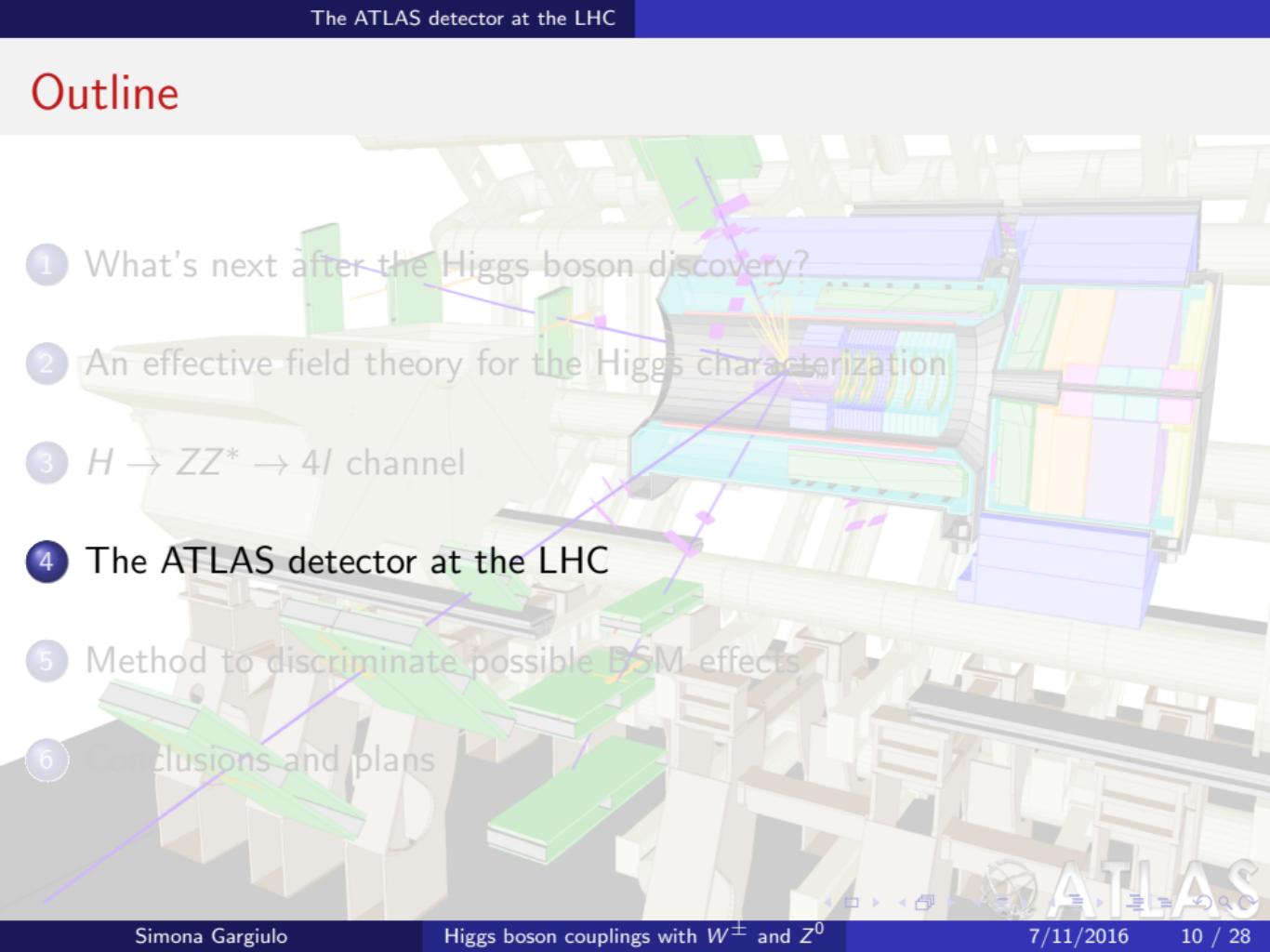
	VBF	hadronic VH	ggF
0jet	0.11	0.032	7.7
1jet	0.59	0.19	6.5
$\geq 2$ jets	2.1	0.62	4.5

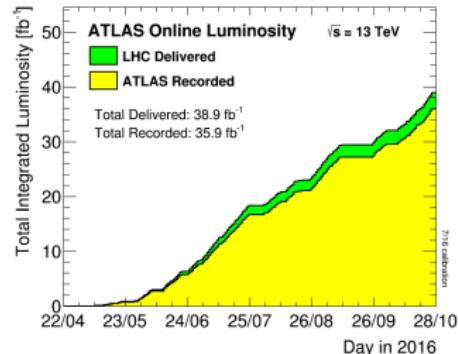
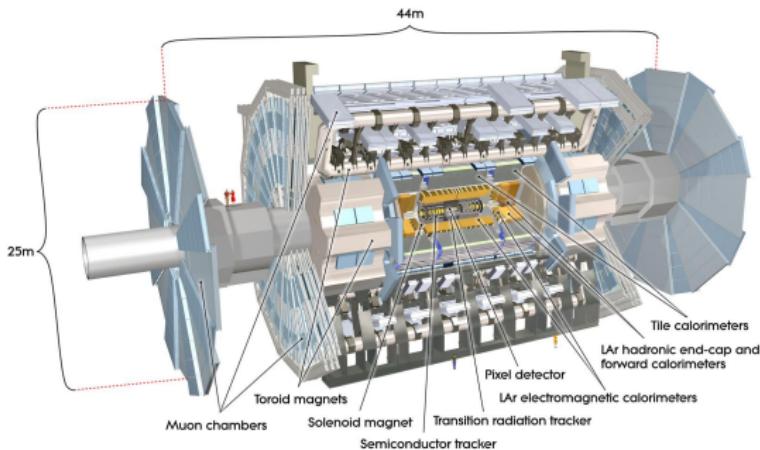
$\geq 2$  jets category divided into two categories with a cut on the reconstructed invariant mass of the two jets  $M_{jj}^{reco}$ :

- if  $M_{jj}^{reco} \geq 120$  GeV: VBF-category
- if  $M_{jj}^{reco} < 120$  GeV: VH-category

**Table:** Yields of VBF, hadronic VH and ggF in each category, for  $L_{int} = 14.8 \text{ fb}^{-1}$  and  $\sqrt{s} = 13 \text{ TeV}$  and after the event selection.

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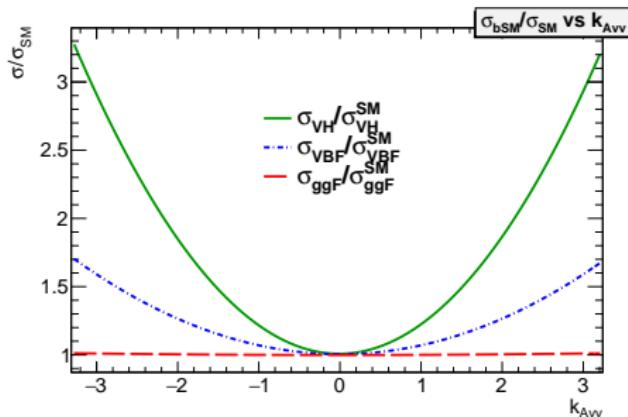
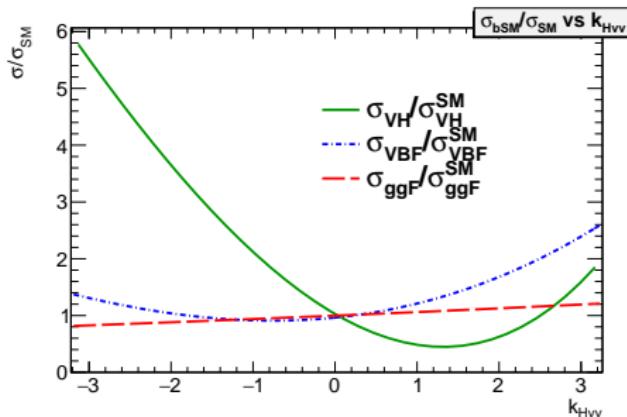


- ① **Magnetic system:** one barrel and two end-cap toroids, central solenoid (2 T)
- ② **Inner detector:** silicon pixels, semiconductor tracker (SCT) and transition radiation tracker (TRT)
- ③ **Electromagnetic calorimeter:** lead-liquid argon detector with accordion geometry
- ④ **Hadronic calorimeter:** iron as absorber and scintillating materials
- ⑤ **Muon spectrometer:** muon chambers with high resolution and standalone muons reconstruction

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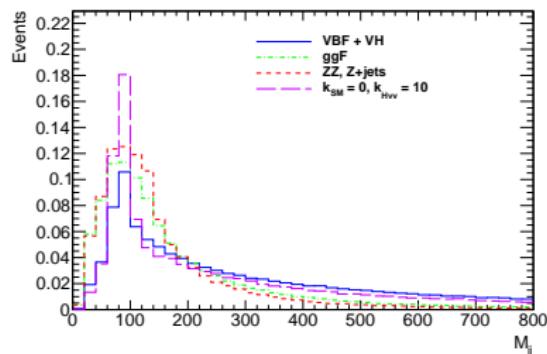
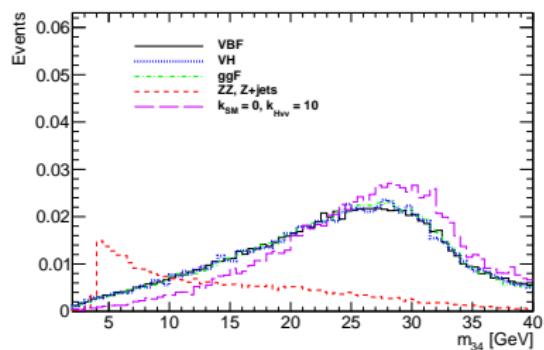
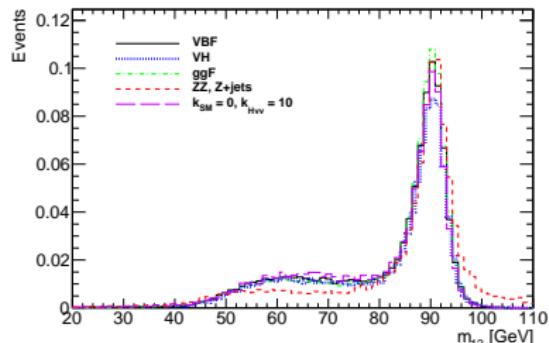
# New physics effects on the signal strength [2]



- VBF and VH mechanisms have a greater sensitivity to the BSM couplings
- The ggF mechanism depends only marginally from the BSM couplings
- The SM and BSM contributions interfere when  $\mu = \frac{\sigma_{\text{BSM}}}{\sigma_{\text{SM}}}$  is a function of  $k_{\text{HVV}}$ . The interference is greater in the case of VH and has an opposite sign compared to that of VBF
- No interference expected when the cross section is a function of  $k_{\text{AVV}}$

# New physics effects on the shape of kinematic differential distributions of signal and backgrounds

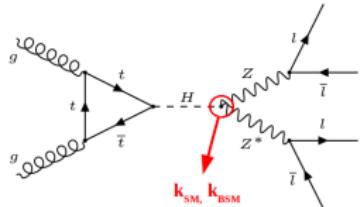
Other discriminating variables



**Need a multivariate analysis to combine the shape of many kinematic distributions.  $\Rightarrow$  Matrix element based observables**

# Definition of the matrix element of a process

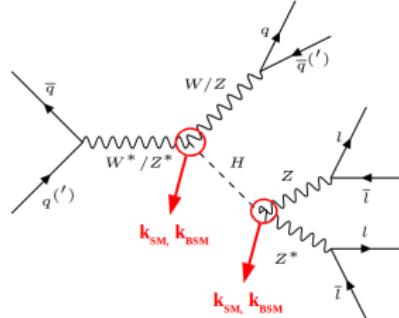
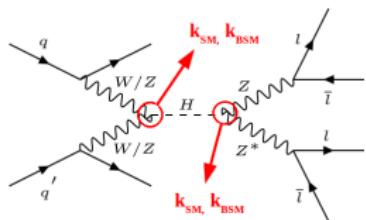
- BSM coupling entering in production or decay vertex (ggF)



$$\mathcal{M}(k_{SM}, k_{BSM}) = k_{SM} \mathcal{M}_{SM} + k_{BSM} \mathcal{M}_{BSM} \quad (1)$$

use of 4 leptons to build the matrix element

- BSM coupling entering in both production and decay vertices (VBF and VH)



$$\mathcal{M}(k_{SM}, k_{BSM}) = (k_{SM} \cdot \mathcal{M}_{SM,p} + k_{BSM} \cdot \mathcal{M}_{BSM,p}) \cdot (k_{SM} \cdot \mathcal{M}_{SM,d} + k_{BSM} \cdot \mathcal{M}_{BSM,d}). \quad (2)$$

use of 4 leptons and 2 jets to build the matrix element

# Optimal Observables (OO) for VBF and VH [3]

$$OO_1 = \frac{\text{Interference}}{|\mathcal{M}_{SM}|^2}$$

$$OO_2 = \frac{|\mathcal{M}_{BSM}|^2}{|\mathcal{M}_{SM}|^2}$$

$$\begin{aligned} |\mathcal{M}(k_{SM}, k_{BSM})|^2 &= k_{SM}^4 |\mathcal{M}_{SM,p}|^2 |\mathcal{M}_{SM,d}|^2 + k_{BSM}^4 |\mathcal{M}_{BSM,p}|^2 |\mathcal{M}_{BSM,d}|^2 + \\ &+ k_{SM}^3 k_{BSM} \left[ |\mathcal{M}_{SM,p}|^2 \Re(|\mathcal{M}_{SM,d}|^* |\mathcal{M}_{BSM,d}|) + \right. \\ &+ \Re(|\mathcal{M}_{SM,p}|^* |\mathcal{M}_{BSM,p}|) |\mathcal{M}_{SM,d}|^2 \Big] + \\ &+ k_{SM}^2 k_{BSM}^2 (|\mathcal{M}_{SM,p}|^2 |\mathcal{M}_{BSM,d}|^2 + |\mathcal{M}_{BSM,p}|^2 |\mathcal{M}_{SM,d}|^2) + \\ &+ k_{BSM}^3 k_{SM} \left[ |\mathcal{M}_{BSM,p}|^2 \Re(|\mathcal{M}_{SM,d}|^* |\mathcal{M}_{BSM,d}|) + \right. \\ &\left. + \Re(|\mathcal{M}_{SM,p}|^* |\mathcal{M}_{BSM,p}|) |\mathcal{M}_{BSM,d}|^2 \right] \end{aligned}$$

I considered as Interference all the terms that are highlighted in red:

$$\begin{aligned} \text{Interference} &= |\mathcal{M}(k_{SM}, k_{BSM})|^2 - k_{SM}^4 |\mathcal{M}_{SM,p}|^2 |\mathcal{M}_{SM,d}|^2 - k_{BSM}^4 |\mathcal{M}_{BSM,p}|^2 |\mathcal{M}_{BSM,d}|^2 - \\ &- k_{SM}^2 k_{BSM}^2 (|\mathcal{M}_{SM,p}|^2 |\mathcal{M}_{BSM,d}|^2 + |\mathcal{M}_{BSM,p}|^2 |\mathcal{M}_{SM,d}|^2) \end{aligned}$$

$\mathcal{M}_{BSM}$  can be  $\mathcal{M}_{kHVV}$  or  $\mathcal{M}_{kAVV}$  → define four optimal observables:  $OO_1^H$ ,  $OO_2^H$ ,  $OO_1^A$ ,  $OO_2^A$ .

$\mathcal{M}_{SM}$ 

- $\Lambda = 10^3$  GeV;
- $k_{SM} = 1$ ;
- all BSM couplings  
 $k_{BSM} = 0$ ;

 $\mathcal{M}_{kHVV}$ 

- $\Lambda = 10^3$  GeV;
- $k_{SM} = 0$ ;
- $k_{HV} = 10$ ;
- all other BSM  
couplings  $k_{BSM} = 0$ ;

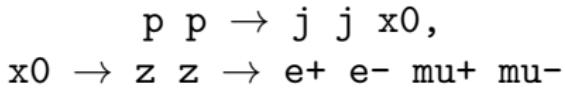
 $\mathcal{M}_{kAVV}$ 

- $\Lambda = 10^3$  GeV;
- $k_{SM} = 0$ ;
- $k_{AV} = 15$ ;
- all other BSM  
couplings  $k_{BSM} = 0$ ;

Each matrix element should be created for both VBF and VH mechanisms.

**VBF**

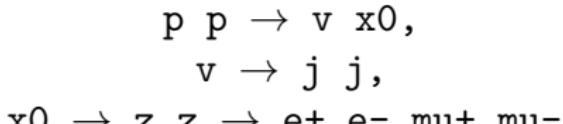
MadGraph [2] NLO process



- 6 particles in the final state:  
2 jets and 4 leptons
- $jetP_T > 30$  GeV

**VH**

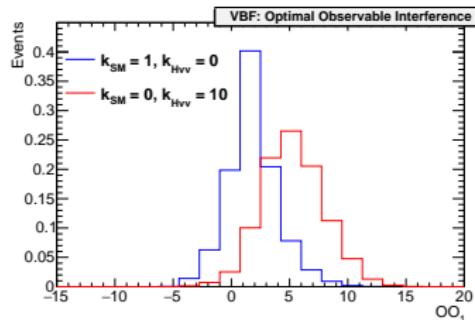
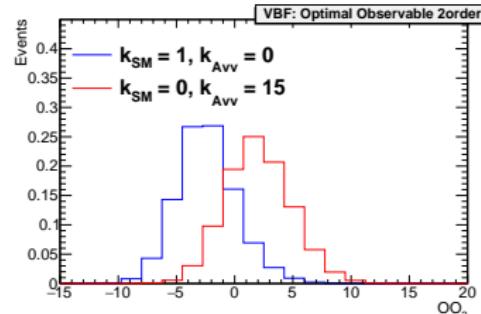
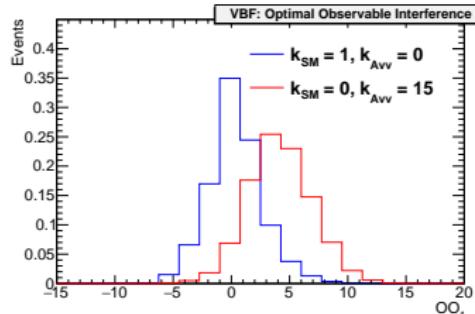
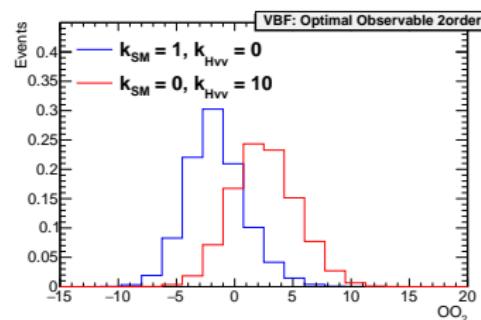
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# OO distributions for the VBF-category

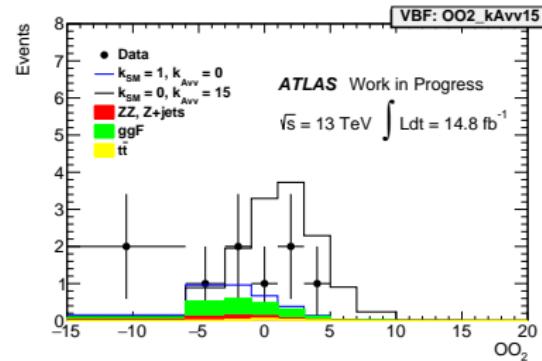
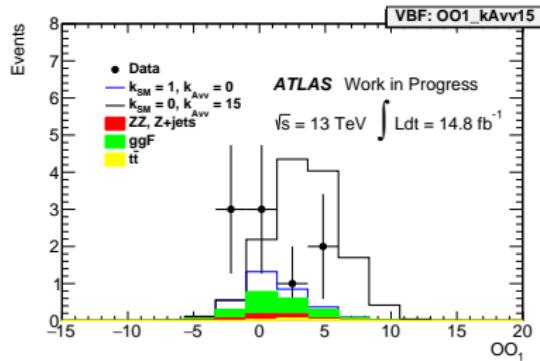
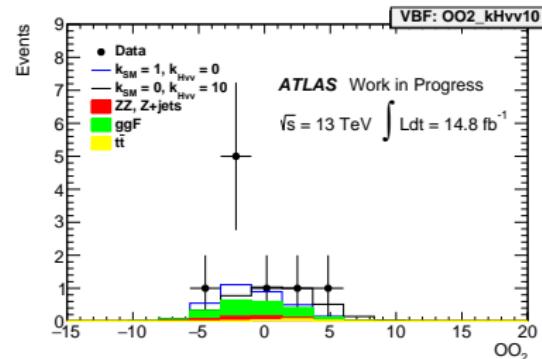
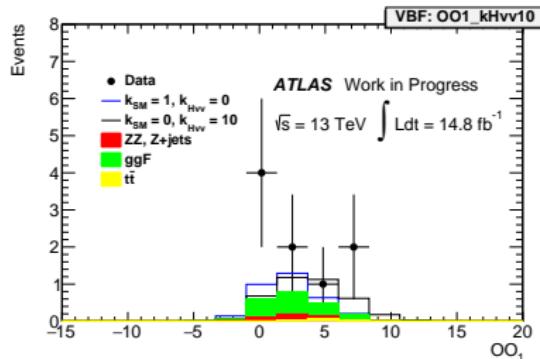
OO for the VH-category

 $OO_1$  $OO_2$ 

These distributions are made using full simulation samples. <sup>1</sup>

<sup>1</sup>Backup slides for those made using MadGraph samples.

# OO distributions for the VBF-category with $14.8 \text{ fb}^{-1}$ of data



# Estimation of expected OO sensitivity

- Use the binned OO distributions
- calculate the Poisson probability to obtain the number of events relative to a certain BSM coupling  $k_{test}$ ,  $n_i^{injected}(k_{test})$ , if one expects a number  $n_i^{expected}(k_{BSM})$
- $k_{SM} = 1$  in the fit
- ggF and backgrounds included but considered independent from the BSM coupling

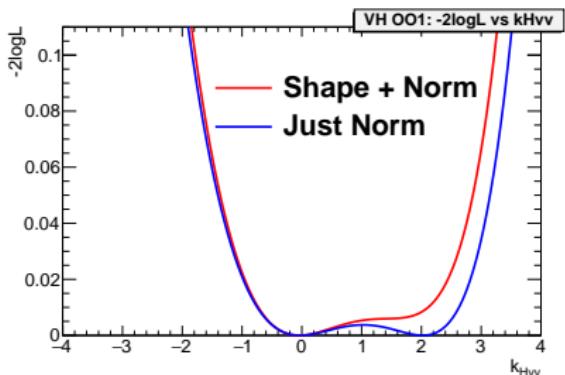
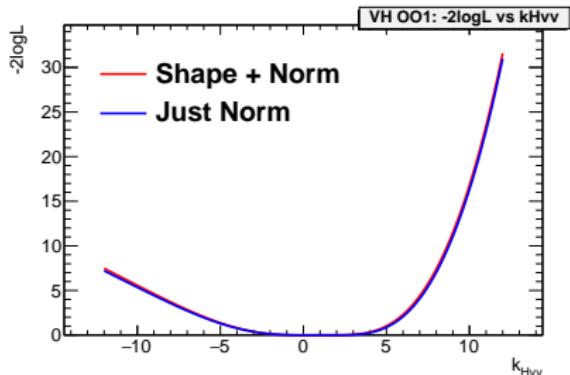
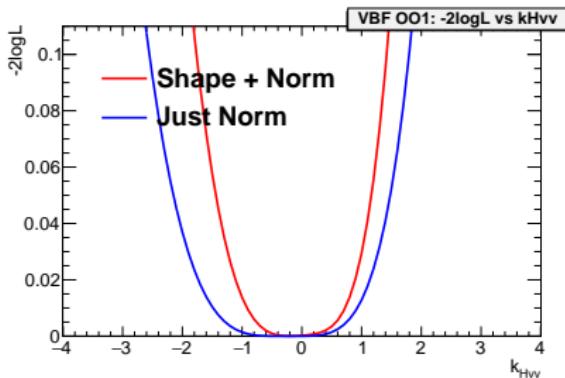
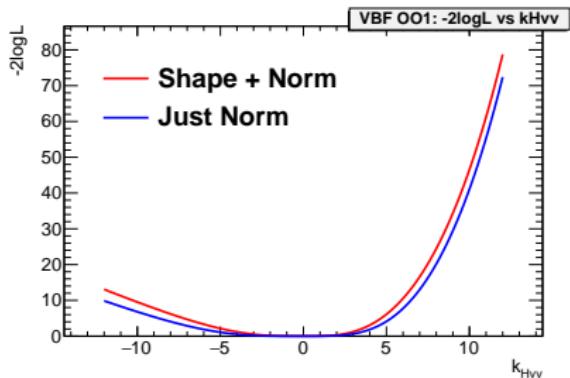
$$L(k_{BSM}) = \prod_{i=1}^{N_{bin}} \text{Poisson}(n_i^{injected}(k_{test}), n_i^{expected}(k_{BSM}))$$

- $n_i^{expected}(k_{BSM})$ , obtained using the morphing technique [4]
- $n_i^{injected}(k_{test})$ , yield of the  $i^{th}$  bin of the injected histogram relative to  $k_{test}$ ;
- $N_{bin}$ , total number of bins of the histograms.

# Fit to $k_{Hvv} = 0$ using $OO_1^H$

( $L = 14.8 \text{ fb}^{-1}$ )

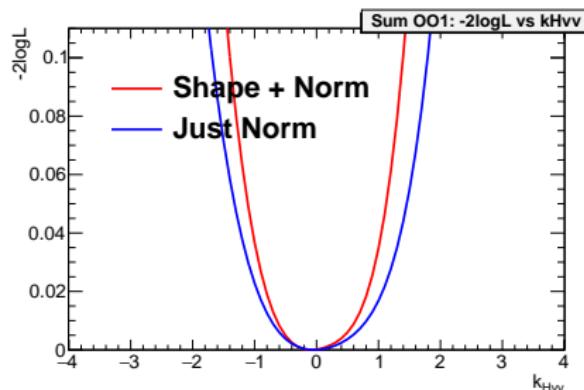
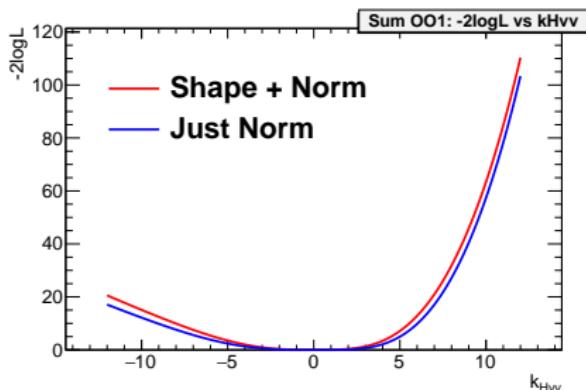
Fit to  $k_{Hvv} = 0$  using  $OO_2^H$



# Fit to $k_{Hvv} = 0$ using $OO_1^H$

( $L = 14.8 \text{ fb}^{-1}$ )

Fits using MadGraph samples



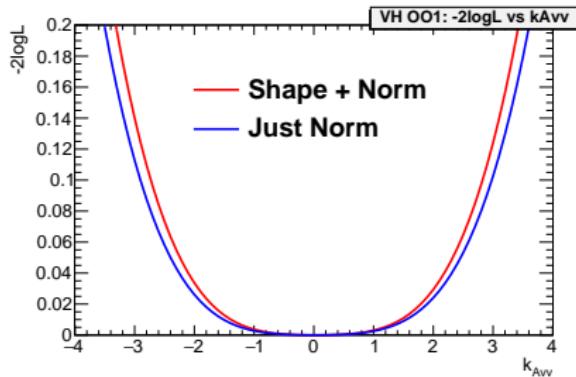
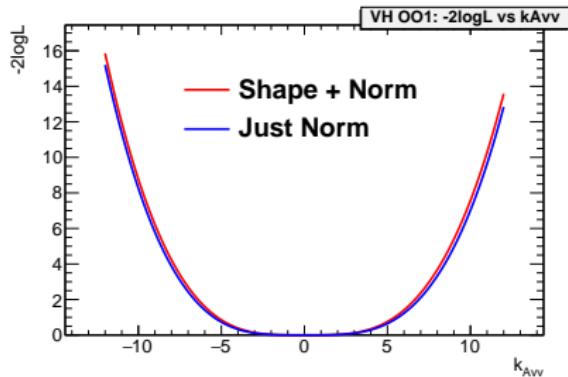
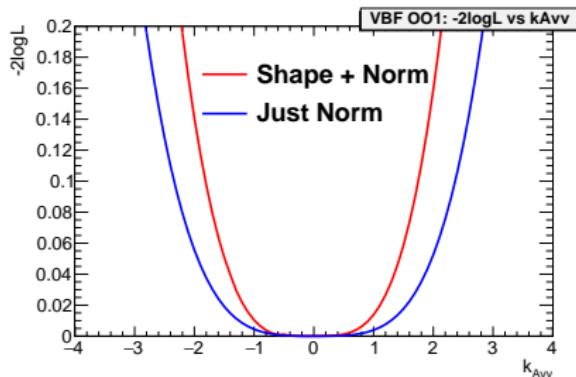
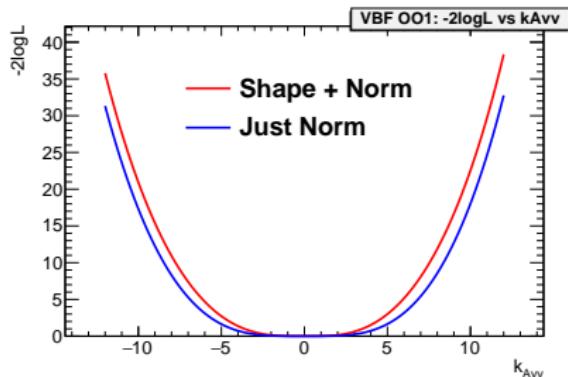
Optimal observables		Cross section alone	
Observable	$k_{HVV}$	Observable	$k_{HVV}$
$OO_1^H$	[-5.2, 4.1]	$OO_1^H$ (single bin)	[-6.1, 4.7]

**Table:** Expected 95% confidence intervals on  $k_{HVV}$  for  $OO_1^H$  and for the sum between the VBF and VH loglikelihoods.

# Fit to $k_{Avv} = 0$ using $OO_1^A$

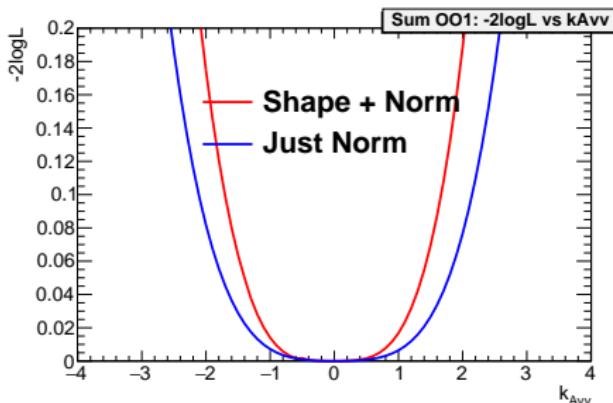
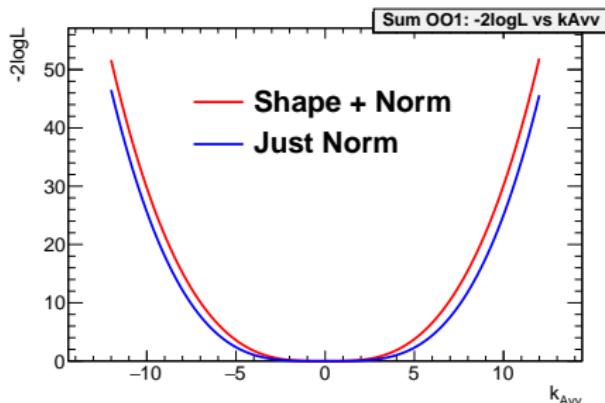
( $L = 14.8 \text{ fb}^{-1}$ )

Fit to  $k_{Avv} = 0$  using  $OO_2^A$



# Fit to $k_{AVV} = 0$ using $OO_1^A$

( $L = 14.8 \text{ fb}^{-1}$ )

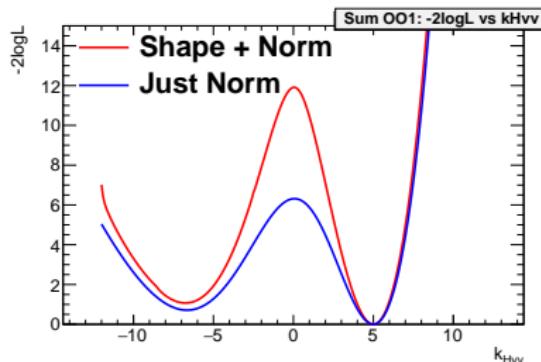
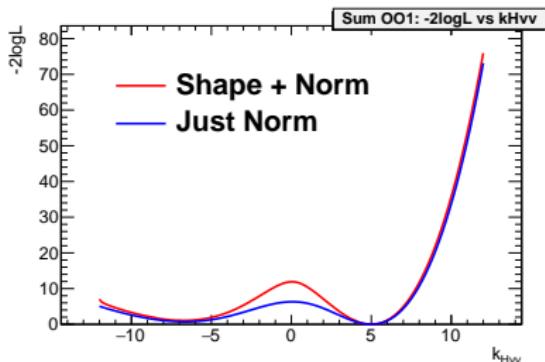
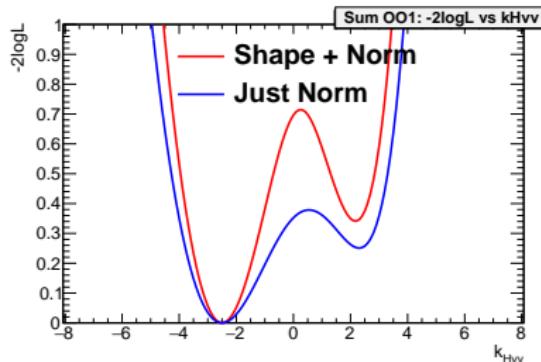
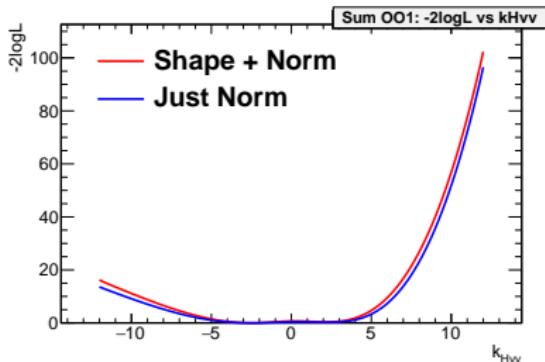


Optimal observables		Cross section alone	
Observable	$k_{AVV}$	Observable	$k_{AVV}$
$OO_1^A$	$[-5.1, 5.0]$	$OO_1^A$ (single bin)	$[-5.8, 5.8]$

Table: Expected 95% confidence intervals on  $k_{AVV}$  for  $OO_1^A$  and for the sum between the VBF and VH loglikelihoods.

# Fit to $k_{HVV} = -2.5$ and $k_{HVV} = 5$ using $OO_1^H$ ( $L = 14.8 \text{ fb}^{-1}$ )

Other fit closure tests



# Outline

- 
- 1 What's next after the Higgs boson discovery?
  - 2 An effective field theory for the Higgs characterization
  - 3  $H \rightarrow ZZ^* \rightarrow 4l$  channel
  - 4 The ATLAS detector at the LHC
  - 5 Method to discriminate possible BSM effects
  - 6 Conclusions and plans

# Conclusions and plans

## Conclusions:

- The use of matrix element based observables enables to increase the sensitivity to the BSM couplings with respect to the one obtained using the cross section alone;
- with higher statistics, order of  $100 \text{ fb}^{-1}$ , it will be possible to further improve the expected 95% confidence levels on the BSM couplings <sup>2</sup>.

## Plans:

- addition of the 1jet category;
- exploit the OO to do a fit without fixing  $k_{SM} = 1$  and discriminate between  $k_{HVV}$  and  $k_{AVV}$ ;

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<sup>2</sup>The performances of this analysis on a dataset of  $300 \text{ fb}^{-1}$  can be found in the backup slides.

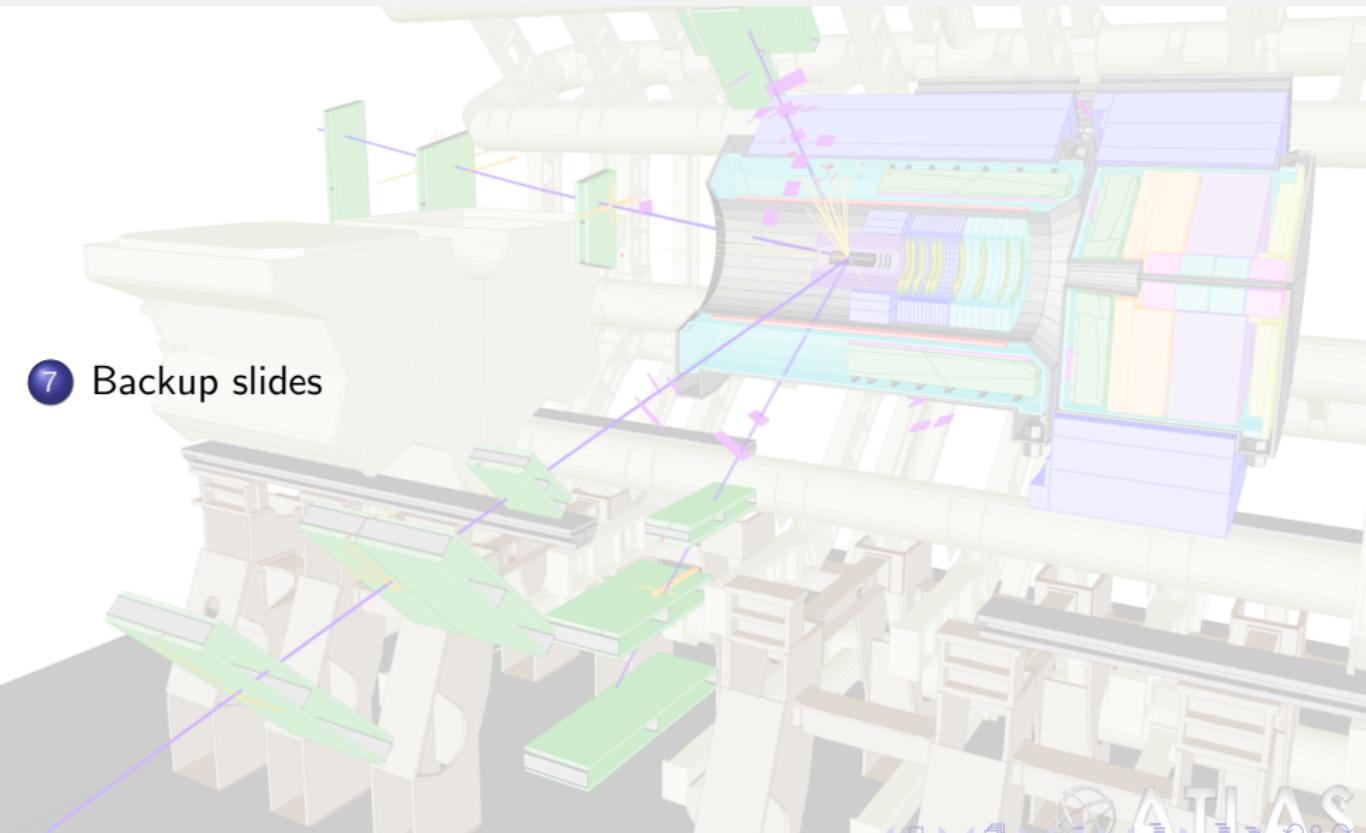
## Bibliography

-  P. Artoisenet, P. de Aquino, F. Demartin, R. Frederix, S. Frixione, F. Maltoni, M. K. Mandal, P. Mathews, K. Mawatari, V. Ravindran, S. Seth, P. Torrielli, M. Zaro, "A framework for the Higgs characterisation", (21 Jan 2014)  
arXiv:1306.6464 [hep-ph].
-  J. Alwall, R. Frederix, S. Frixione, V. Hirschi, F. Maltoni, O. Mattelaer, H.-S. Shao, T. Stelzer, P. Torrielli, M. Zaro, "The automated computation of tree-level and next-to-leading order differential cross sections, and their matching to parton shower simulations",  
arXiv:1405.0301v2 [hep-ph].
-  OPAL Technical note,  
Dave Charlton, Alun Llyod, "Measurement of Triple Gauge Coupling Parameters with Optimal Observables for  $W^+W^- \rightarrow l^+\nu l^-\bar{\nu}$  Events at  $\sqrt{s} = 189$  GeV",  
arXiv:hep-ph/0209229v1.
-  ATLAS NOTE "A morphing technique for signal modelling in a multidimensional space of coupling parameters", ATL-PHYS-PUB-2015-047  
<https://cds.cern.ch/record/2143180?ln=it>.

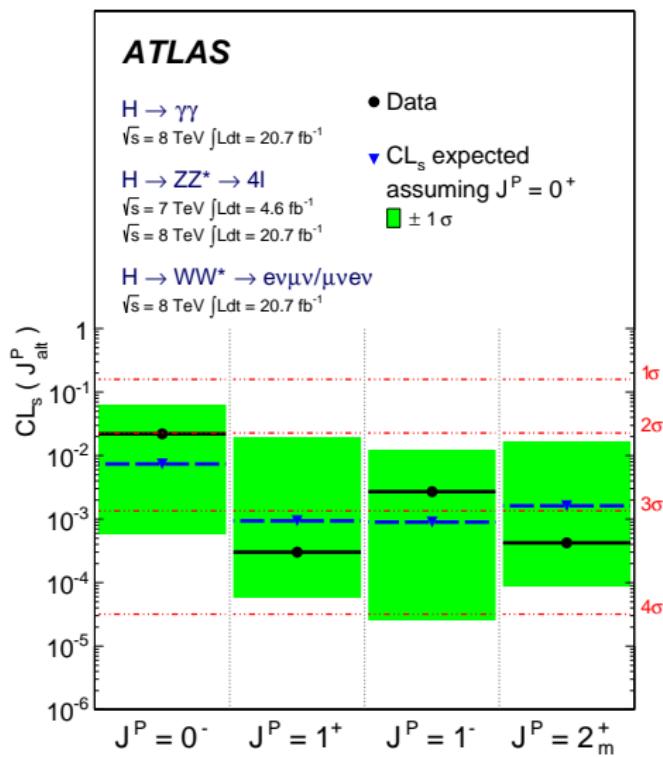
# Outline

7

## Backup slides



# Evidence for the spin-0 nature of the Higgs boson



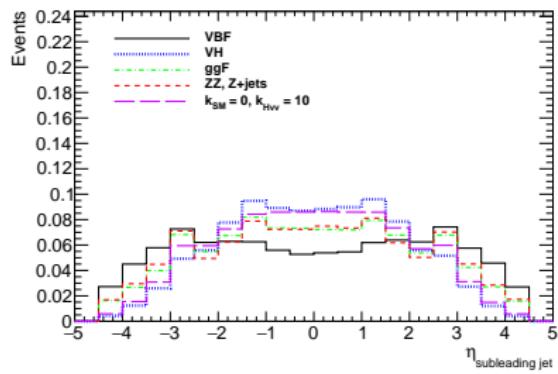
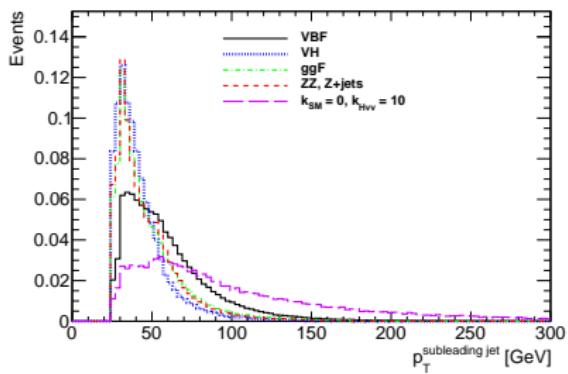
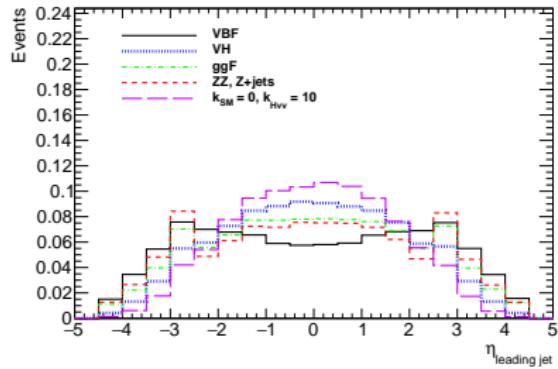
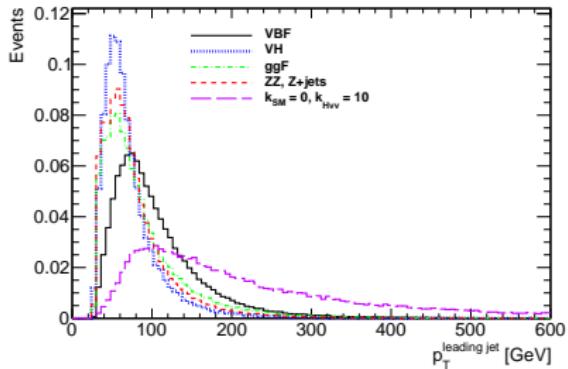
# Event selection criteria

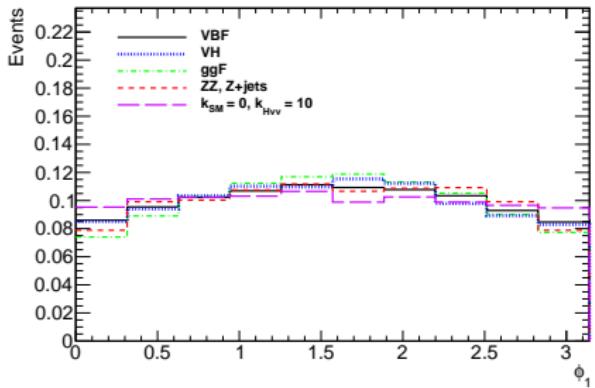
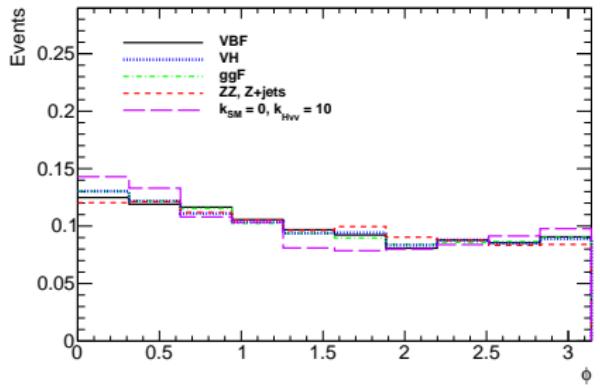
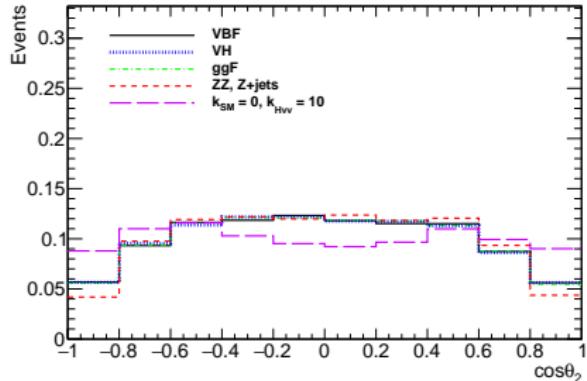
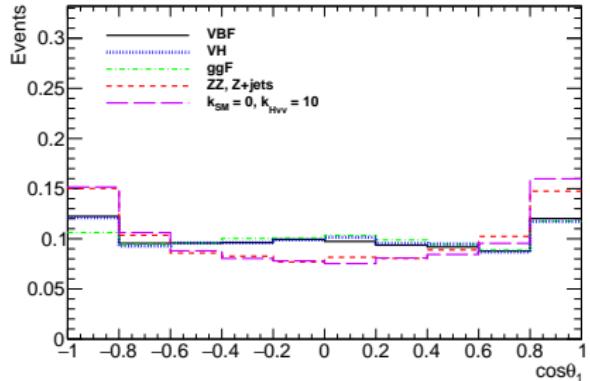
$H \rightarrow ZZ^* \rightarrow 4l$

$p_T$ , $E_T$ and $\eta$ cuts
Electrons: $E_T > 7$ GeV, $ \eta  < 2.47$
Combined, standalone and segment-tagged muons: $p_T > 5$ GeV
Calo-tagged muons: $p_T > 15$ GeV, $ \eta  < 0.1$
Jets: $p_T > 30$ GeV
Leptons in the quadruplets
First lepton: $p_T > 20$ GeV
Second lepton: $p_T > 15$ GeV
Third lepton: $p_T > 10$ GeV
Maximum one calo-tagged or standalone muon per quadruplet
<i>Leading dilepton mass:</i> $50 < m_{12} < 106$ GeV
<i>Sub-leading dilepton mass:</i> $12 < m_{34} < 115$ GeV
Isolation
Electron track isolation ( $\Delta R \leq 0.20$ ): $\sum E_T/E_T < 0.15$
Electron calorimetric isolation ( $\Delta R \leq 0.20$ ): $\sum E_T/E_T < 0.20$
Muon track isolation ( $\Delta R \leq 0.30$ ): $\sum p_T/p_T < 0.15$
Muon calorimetric isolation ( $\Delta R \leq 0.20$ ): $\sum E_T/p_T < 0.30$
Impact parameter significance
Electrons: $ d_0/\sigma_{d_0}  < 5$
Muons: $ d_0/\sigma_{d_0}  < 3$
Leptons: $ (z_0 - z_{pv})\sin\theta  < 0.5$ mm

# Leptons and jets discriminating variables

Experimental categories





# Definition of interference between SM and BSM matrix elements

OO definition

**One non-SM coupling in the production or decay vertex**

$$\mathcal{M}(k_{SM}, k_{BSM}) = k_{SM}\mathcal{M}_{SM} + k_{BSM}\mathcal{M}_{BSM}$$

Squaring this expression, one obtains:

$$|\mathcal{M}(k_{SM}, k_{BSM})|^2 = k_{SM}^2 |\mathcal{M}_{SM}|^2 + k_{BSM}^2 |\mathcal{M}_{BSM}|^2 + 2k_{SM}k_{BSM} \Re(\mathcal{M}_{SM}^* \mathcal{M}_{BSM})$$

Therefore, the interference in the case of the ggF production mode is given by:

$$\text{Interference} = 2\Re(\mathcal{M}_{SM}^* \mathcal{M}_{BSM}) =$$

$$= \frac{1}{k_{SM}k_{BSM}} \left( |\mathcal{M}(k_{SM}, k_{BSM})|^2 - k_{SM}^2 |\mathcal{M}_{SM}|^2 - k_{BSM}^2 |\mathcal{M}_{BSM}|^2 \right)$$

# Definition of interference between SM and BSM matrix elements

OO definition

## One non-SM coupling in both production and decay

$$\mathcal{M}(k_{SM}, k_{BSM}) = (k_{SM} \cdot \mathcal{M}_{SM,p} + k_{BSM} \cdot \mathcal{M}_{BSM,p}) \cdot (k_{SM} \cdot \mathcal{M}_{SM,d} + k_{BSM} \cdot \mathcal{M}_{BSM,d}).$$

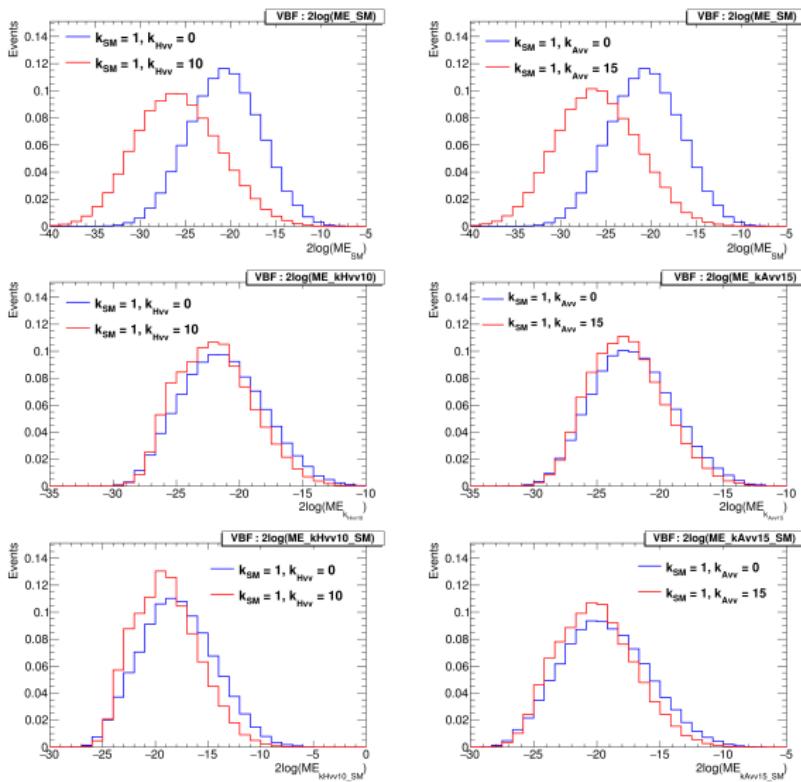
Squaring this expression, one obtains:

$$\begin{aligned} |\mathcal{M}(k_{SM}, k_{BSM})|^2 &= k_{SM}^4 |\mathcal{M}_{SM,p}|^2 |\mathcal{M}_{SM,d}|^2 + k_{BSM}^4 |\mathcal{M}_{BSM,p}|^2 |\mathcal{M}_{BSM,d}|^2 + \\ &\quad + k_{SM}^3 k_{BSM} \left[ |\mathcal{M}_{SM,p}|^2 \Re(|\mathcal{M}_{SM,d}|^* |\mathcal{M}_{BSM,d}|) + \right. \\ &\quad \left. + \Re(|\mathcal{M}_{SM,p}|^* |\mathcal{M}_{BSM,p}|) |\mathcal{M}_{SM,d}|^2 \right] + \\ &\quad + k_{SM}^2 k_{BSM}^2 (|\mathcal{M}_{SM,p}|^2 |\mathcal{M}_{BSM,d}|^2 + |\mathcal{M}_{BSM,p}|^2 |\mathcal{M}_{SM,d}|^2) + \\ &\quad + k_{BSM}^3 k_{SM} \left[ |\mathcal{M}_{BSM,p}|^2 \Re(|\mathcal{M}_{SM,d}|^* |\mathcal{M}_{BSM,d}|) + \right. \\ &\quad \left. + \Re(|\mathcal{M}_{SM,p}|^* |\mathcal{M}_{BSM,p}|) |\mathcal{M}_{BSM,d}|^2 \right] \end{aligned}$$

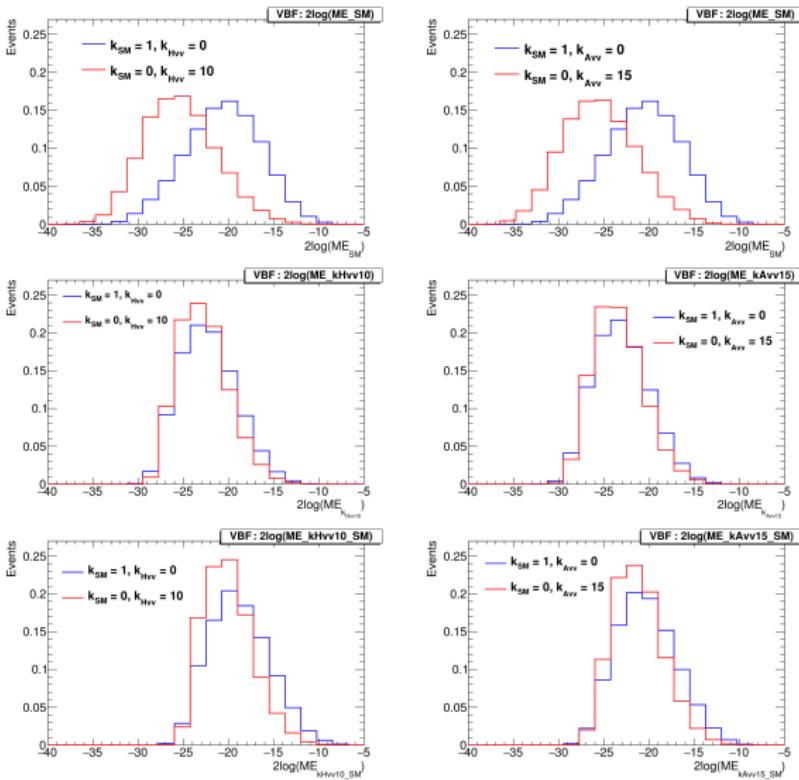
One can call Interference all the terms that are highlighted in red:

$$\begin{aligned} \text{Interference} &= |\mathcal{M}(k_{SM}, k_{BSM})|^2 - k_{SM}^4 |\mathcal{M}_{SM,p}|^2 |\mathcal{M}_{SM,d}|^2 - k_{BSM}^4 |\mathcal{M}_{BSM,p}|^2 |\mathcal{M}_{BSM,d}|^2 - \\ &\quad - k_{SM}^2 k_{BSM}^2 (|\mathcal{M}_{SM,p}|^2 |\mathcal{M}_{BSM,d}|^2 + |\mathcal{M}_{BSM,p}|^2 |\mathcal{M}_{SM,d}|^2) \end{aligned}$$

# ME distributions on VBF MadGraph samples



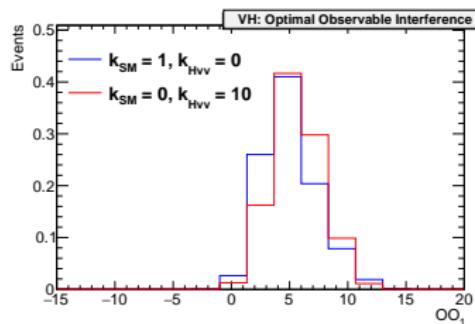
# ME distributions using events of the VBF-category



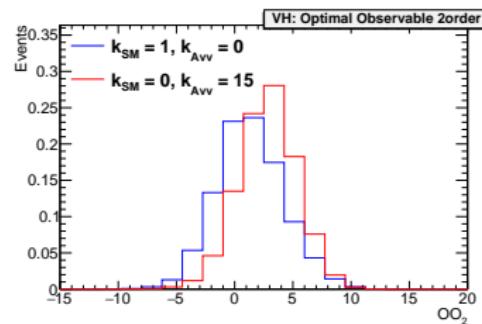
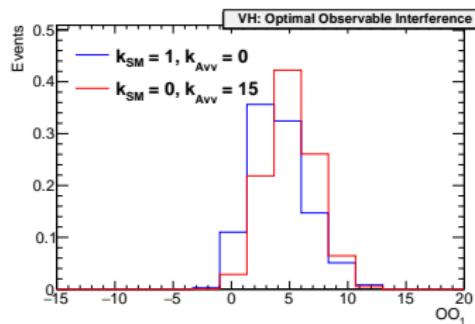
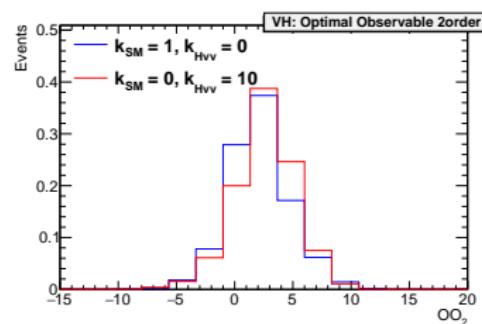
# OO distributions for the VH-category

OO for the VBF-category

$OO_1$



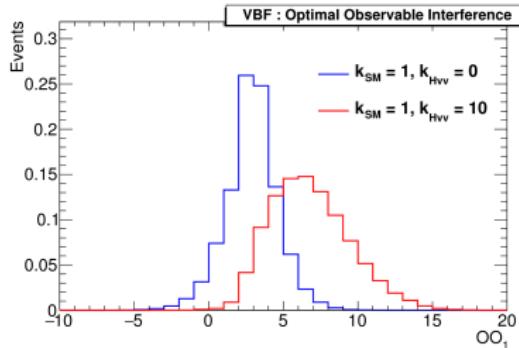
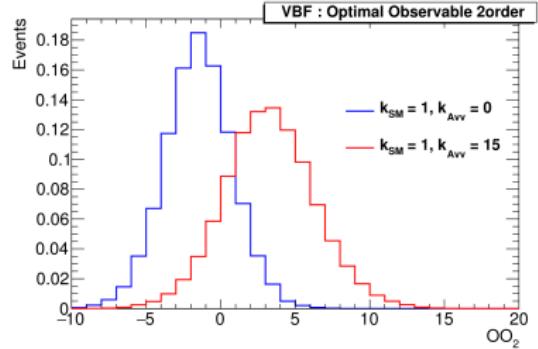
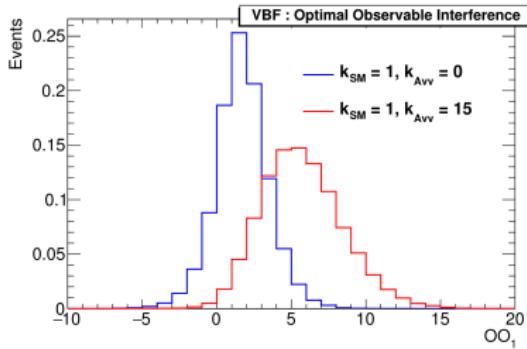
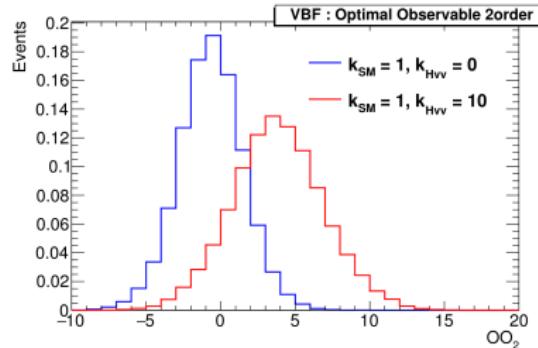
$OO_2$



These distributions are made using full simulation samples.

# VBF OO distributions using MadGraph samples

OO distributions

 $OO_1$  $OO_2$ 

# Implementation of the morphing technique

Morphing method

The morphing method can be introduced to describe the dependence of a given observable  $T$  on an arbitrary set of non-SM Higgs boson couplings  $\vec{k}_{target} = k_{SM}, k_{BSM,1}, \dots, k_{BSM,n}$  to known particles. This dependence is described by a morphing function:

$$T_{out}(\vec{k}_{target}) = \sum_i w_i(\vec{k}_{target}; \vec{k}_i) T_{in}(\vec{k}_i),$$

where  $T_{in}$  are values or differential distributions obtained from Monte Carlo simulation of the signal for a given coupling configuration  $\vec{k}_i$ .

$T_{in}$  are normalised to their expected cross sections such that the physical observable  $T_{out}$  includes both the correct shape and the correct cross section prediction.

# Morphing with one non-SM coupling parameter in the production or decay vertex

Morphing method

The simpler case is that of the ggF process in which the  $k_{BSM}$  coupling with W and Z enters only in decay.

As  $T(k_{SM}, k_{BSM}) \propto |\mathcal{M}(k_{SM}, k_{BSM})|^2$ , one can write the input distributions for arbitrary input parameters  $\vec{k}_i$ :

$$T_{in}(k_{SM,i}, k_{BSM,i}) = k_{SM,i}^2 \cdot \mathcal{M}_{SM}^2 + k_{BSM,i}^2 \cdot \mathcal{M}_{BSM}^2 + 2k_{SM,i}k_{BSM,i} \cdot \Re(\mathcal{M}_{SM}^* \mathcal{M}_{BSM})$$

where  $i = 1, 2, 3$ .

$$\begin{aligned} T_{out}(k_{SM}, k_{BSM}) &= (a_{11}k_{SM}^2 + a_{12}k_{BSM}^2 + a_{13}k_{SM}k_{BSM})T_{in}(k_{SM,1}, k_{BSM,1}) + \\ &= + (a_{21}k_{SM}^2 + a_{22}k_{BSM}^2 + a_{23}k_{SM}k_{BSM})T_{in}(k_{SM,2}, k_{BSM,2}) + \\ &= + (a_{31}k_{SM}^2 + a_{32}k_{BSM}^2 + a_{33}k_{SM}k_{BSM})T_{in}(k_{SM,3}, k_{BSM,3}) \end{aligned}$$

# Morphing with one non-SM coupling parameter in the production or decay vertex

Morphing method

To find the unknown variables  $a_{ij}$  one can observe that if:

$$\vec{k}_{target} = \vec{k}_i \quad \Rightarrow \quad T_{out} = T_{in}$$

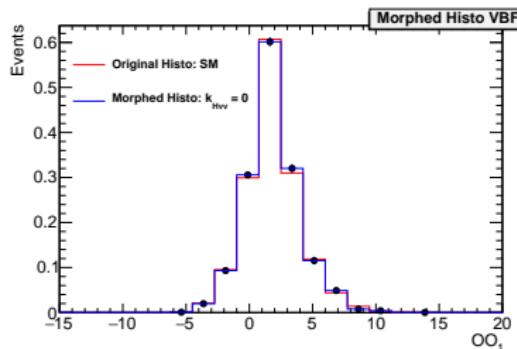
This suggests that  $a_{ij}$  coefficients can be found by solving the following condition:

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix} \cdot \begin{pmatrix} k_{SM,1}^2 & k_{SM,2}^2 & k_{SM,3}^2 \\ k_{BSM,1}^2 & k_{BSM,2}^2 & k_{BSM,3}^2 \\ k_{SM,1}k_{BSM,1} & k_{SM,1}k_{BSM,1} & k_{SM,1}k_{BSM,1} \end{pmatrix} = \mathbb{I}$$

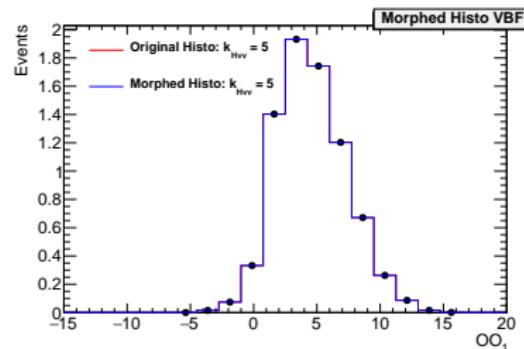
This procedure should be repeated also for the VBF process for which the number of  $T_{in}$  input distributions will be 5.

# Morphing validation: VBF-category

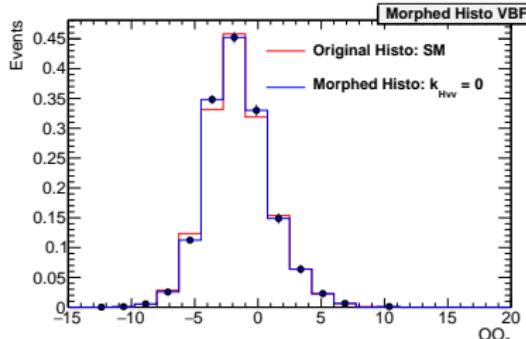
Not base



Base

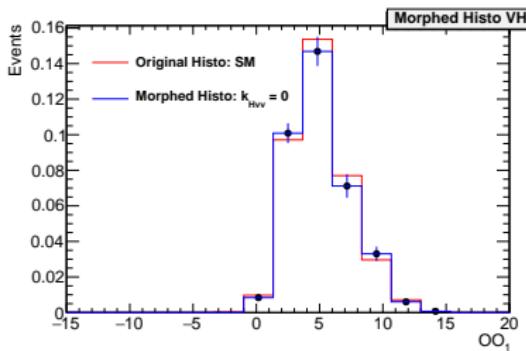


Not base

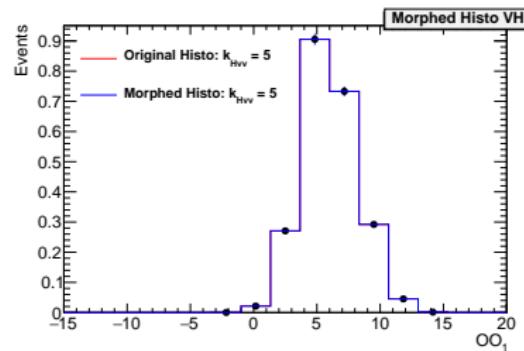


# Morphing validation: VH-category

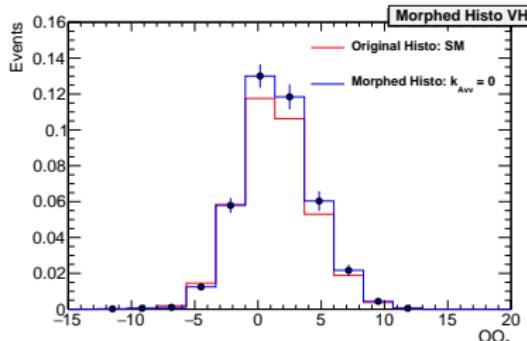
Not base



Base



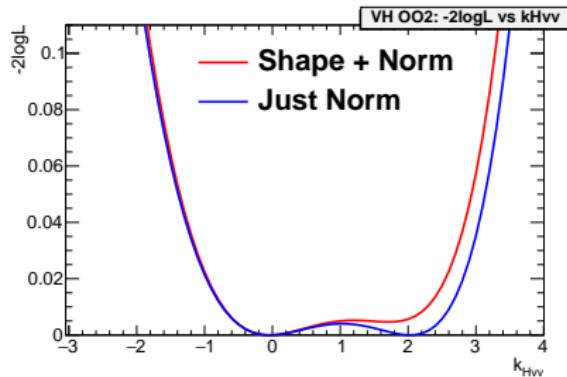
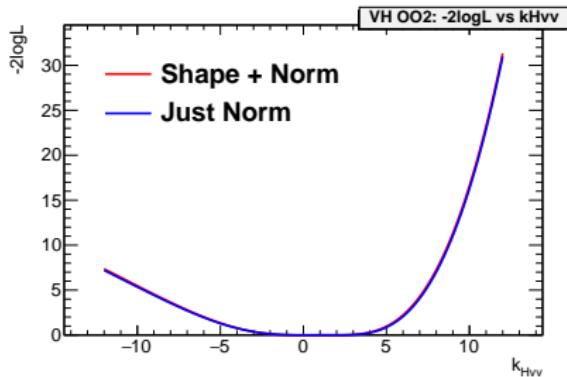
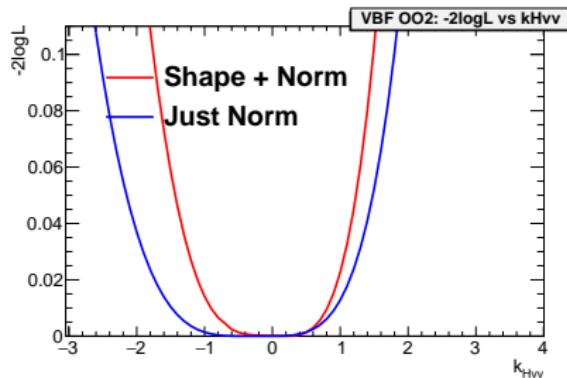
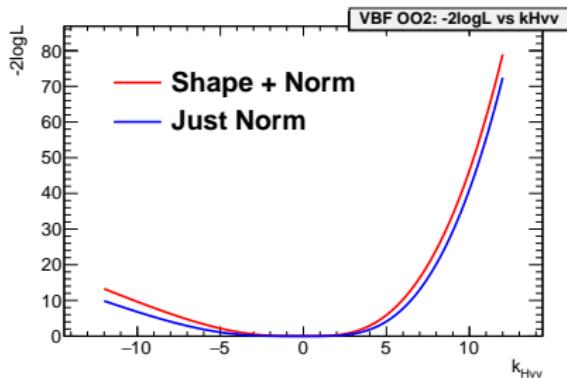
Not base



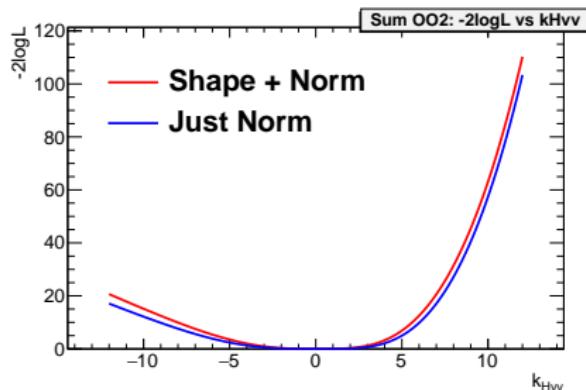
# Fit to $k_{Hvv} = 0$ using $OO_2^H$

( $L = 14.8 \text{ fb}^{-1}$ )

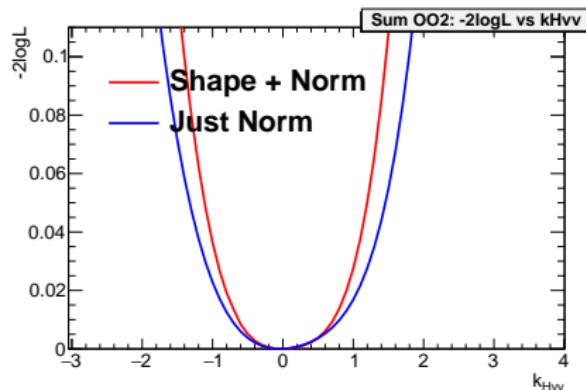
Fit to  $k_{Hvv} = 0$  using  $OO_1^H$



# Fit to $k_{Hvv} = 0$ using $OO_2^H$



( $L = 14.8 \text{ fb}^{-1}$ )



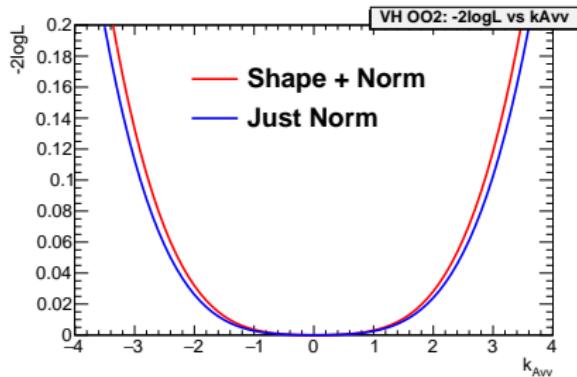
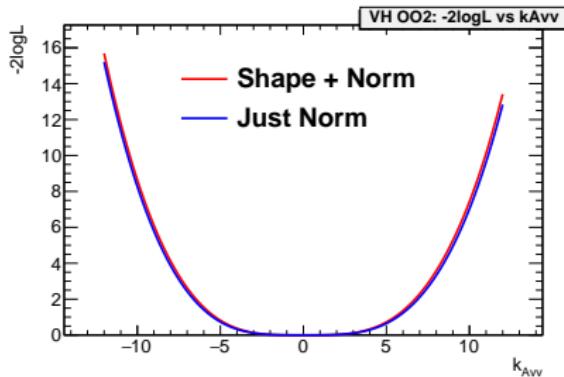
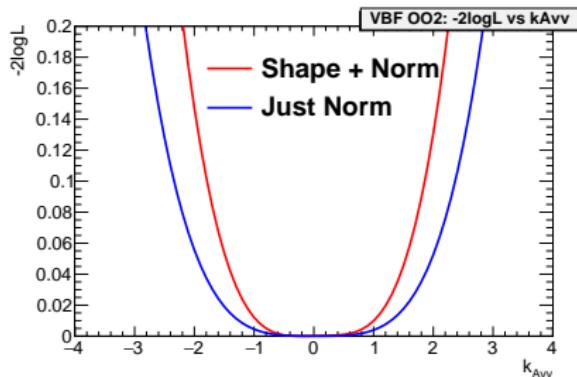
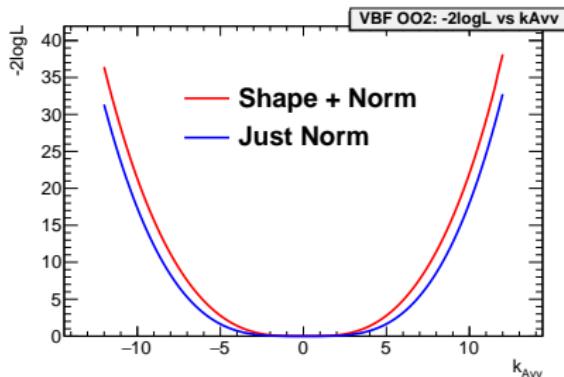
Optimal observables		Cross section alone	
Observable	$k_{Hvv}$	Observable	$k_{Hvv}$
$OO_2^H$	[-5.2, 4.2]	$OO_2^H$ (single bin)	[-6.1, 4.7]

Table: Expected 95% confidence intervals on  $k_{Hvv}$  for  $OO_2^H$  and for the sum between the VBF and VH loglikelihoods.

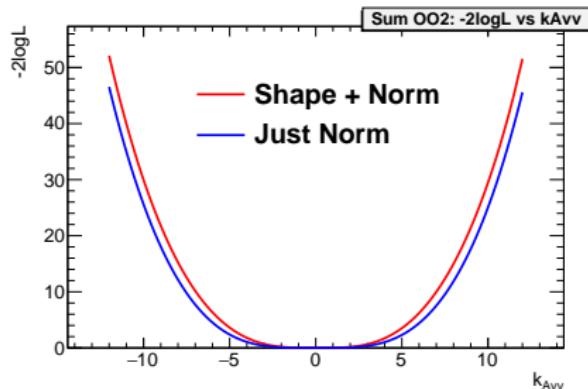
# Fit to $k_{Avv} = 0$ using $OO_2^A$

$(L = 14.8 \text{ fb}^{-1})$

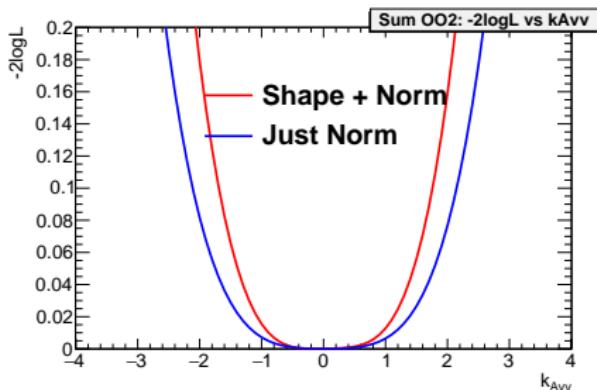
Fit to  $k_{Avv} = 0$  using  $OO_1^A$



# Fit to $k_{AVV} = 0$ using $OO_2^A$

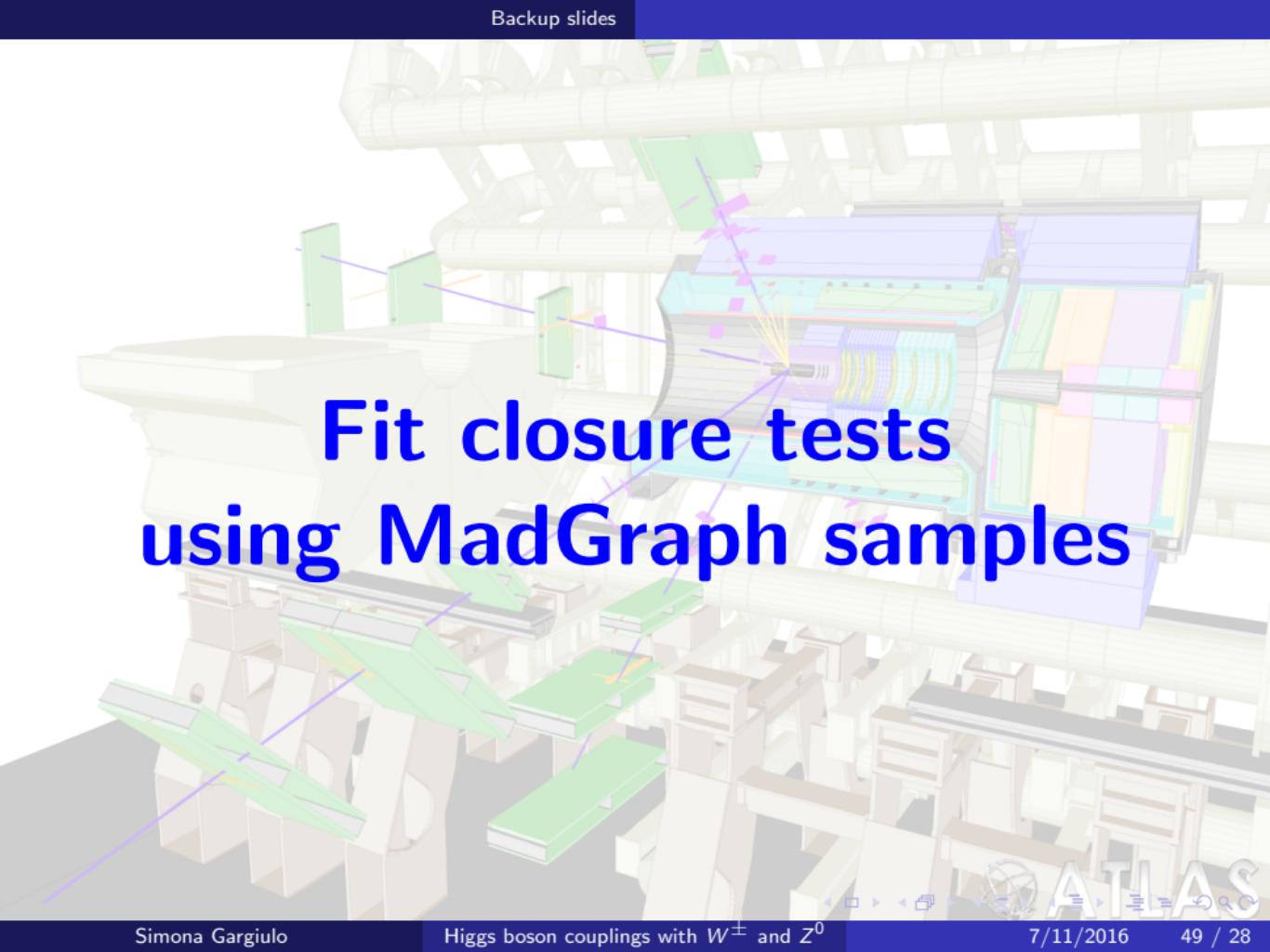


( $L = 14.8 \text{ fb}^{-1}$ )



Optimal observables		Cross section alone	
Observable	$k_{AVV}$	Observable	$k_{AVV}$
$OO_2^A$	[-5.1, 5.1]	$OO_2^A$ (single bin)	[-5.8, 5.8]

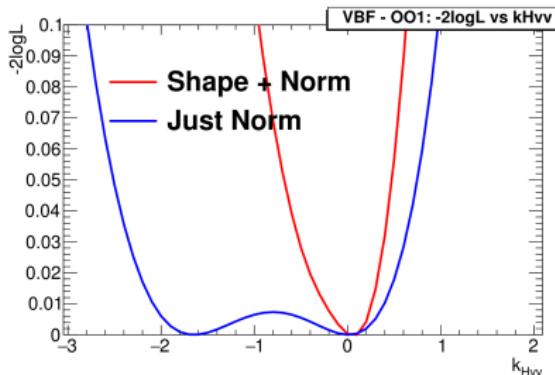
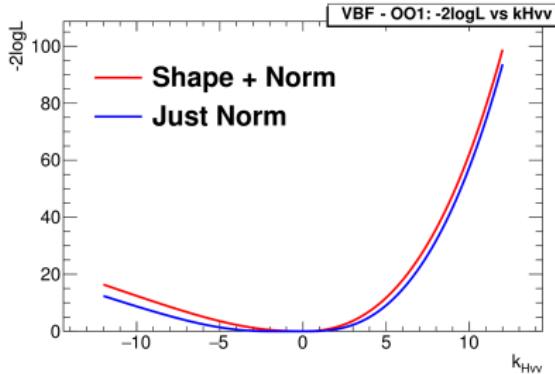
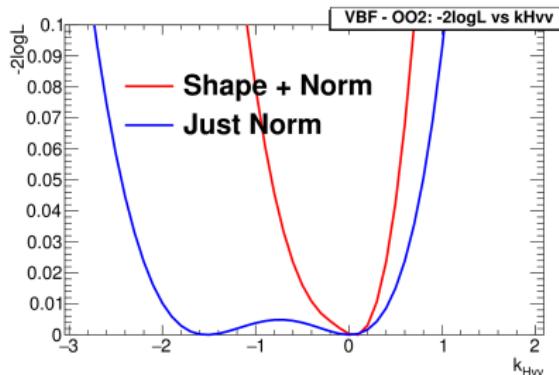
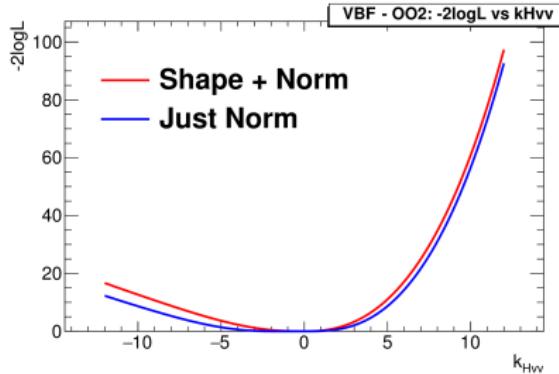
**Table:** Expected 95% confidence intervals on  $k_{AVV}$  for  $OO_2^A$  and for the sum between the VBF and VH loglikelihoods.



# Fit closure tests using MadGraph samples

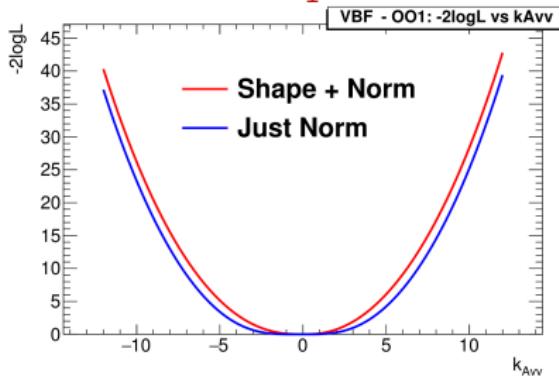
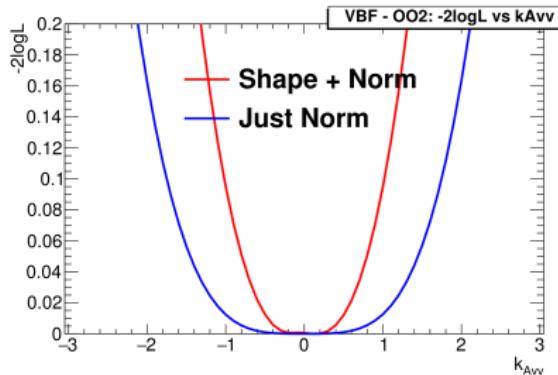
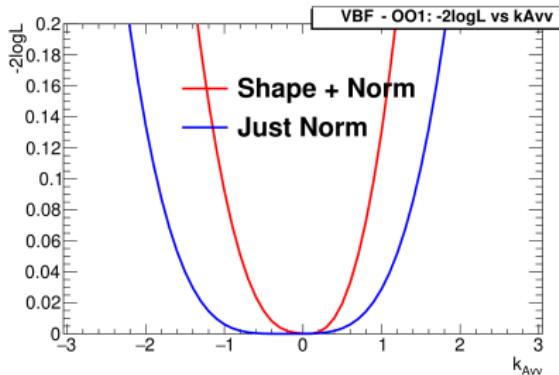
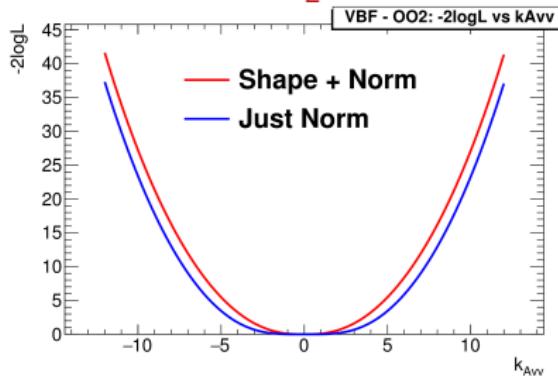
# Fit to $k_{Hvv} = 0$ on a VBF sample

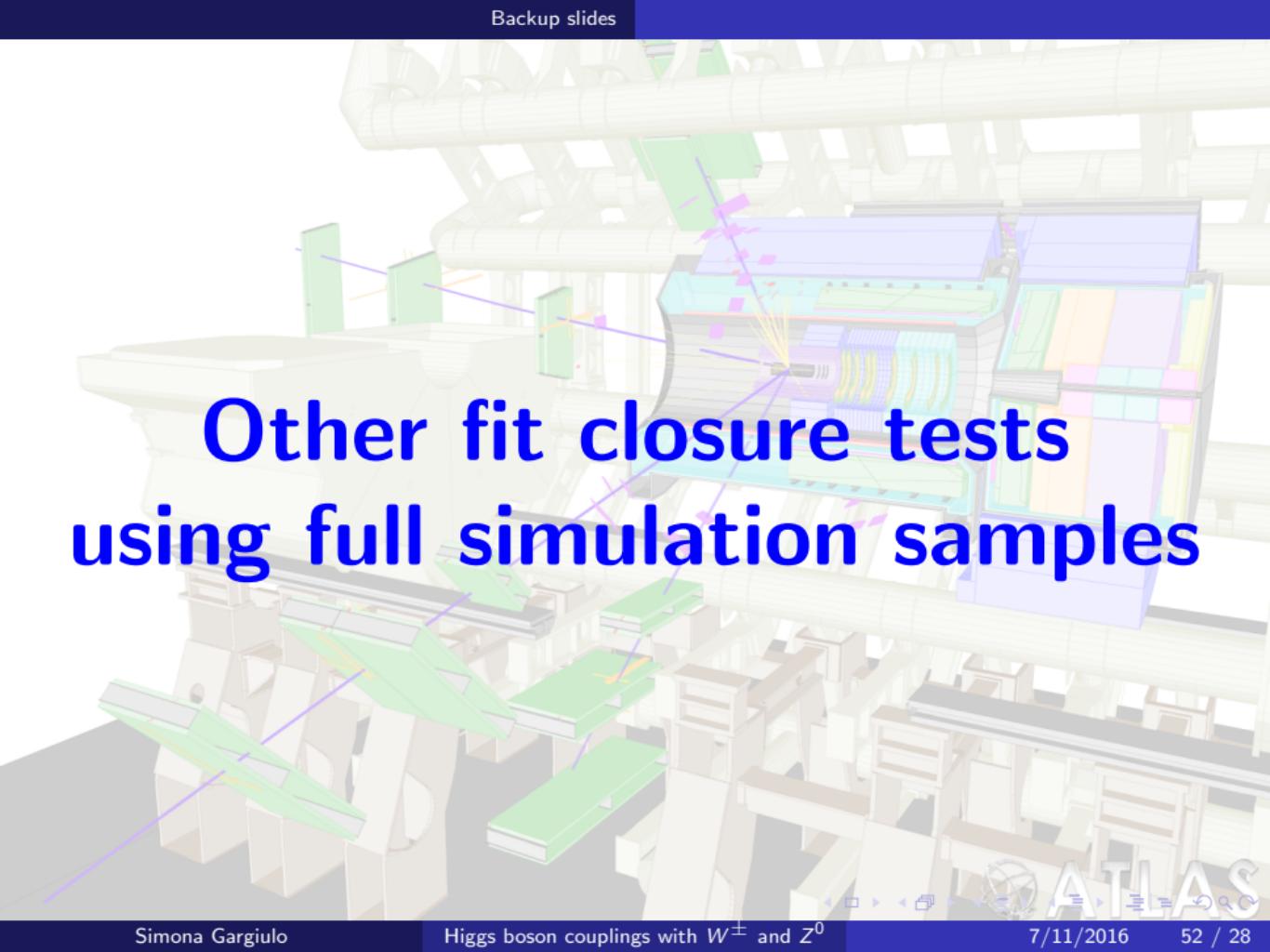
$(L = 14.8 \text{ fb}^{-1})$

OO<sub>1</sub>OO<sub>2</sub>

# Fit to $k_{A\bar{V}V} = 0$ on a VBF sample ( $L = 14.8 \text{ fb}^{-1}$ )

Fits on full sim samples

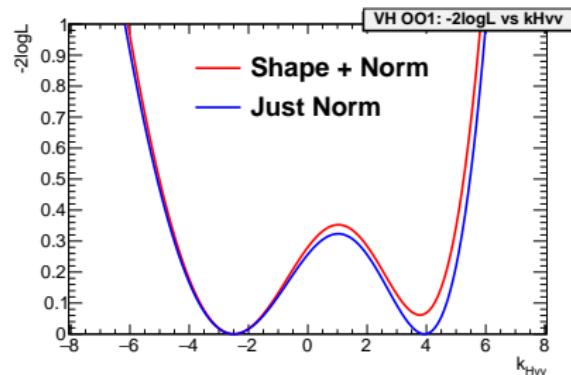
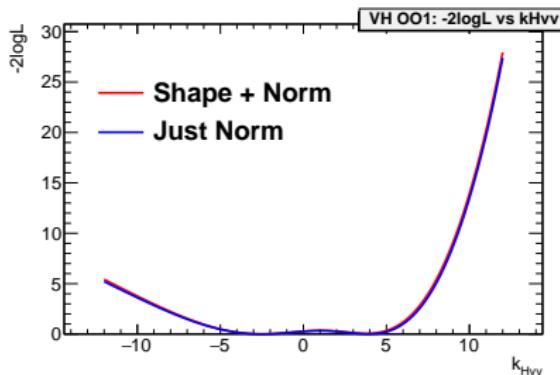
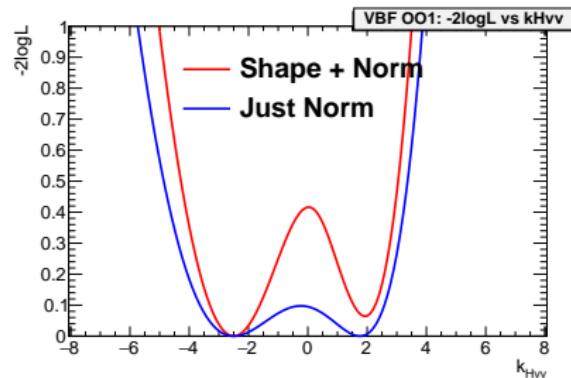
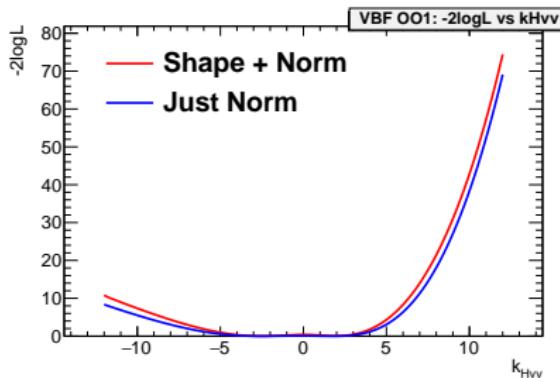
**OO<sub>1</sub>****OO<sub>2</sub>**



# Other fit closure tests using full simulation samples

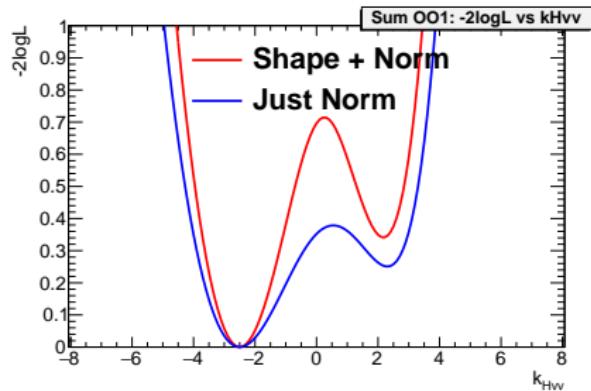
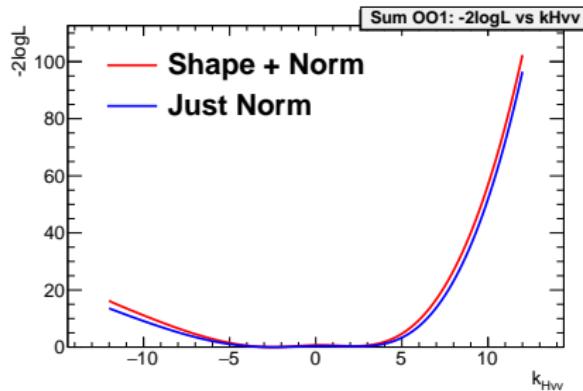
Fit to  $k_{Hvv} = -2.5$  using  $OO_1^H$

( $L = 14.8 \text{ fb}^{-1}$ )



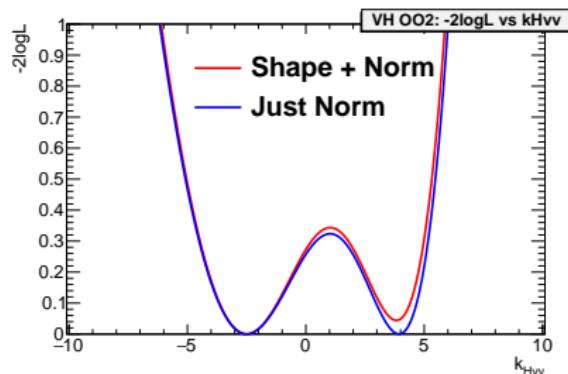
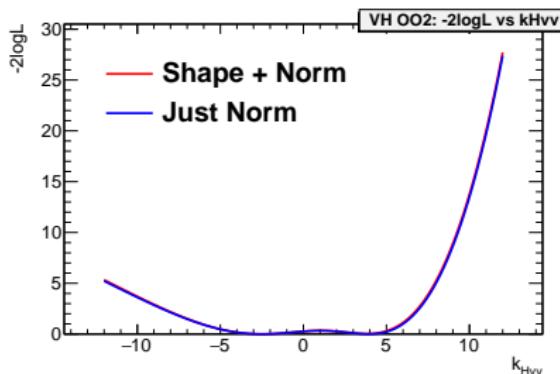
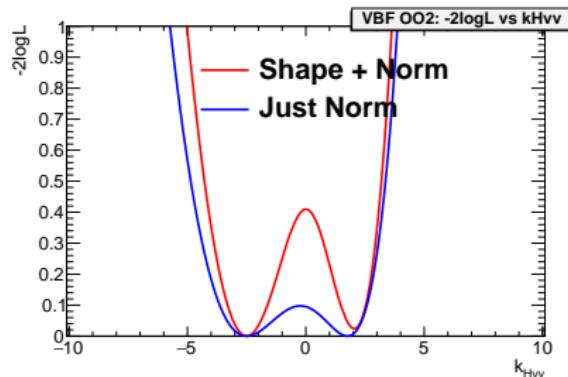
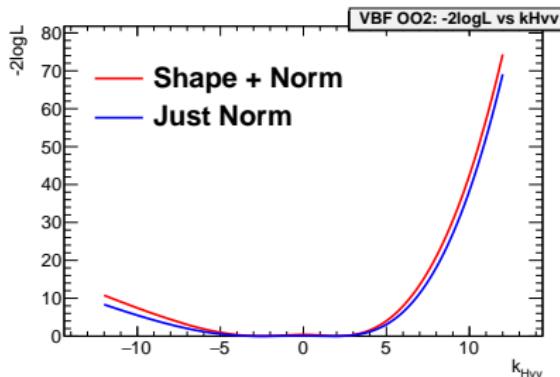
Fit to  $k_{Hvv} = -2.5$  using  $OO_1^H$

( $L = 14.8 \text{ fb}^{-1}$ )



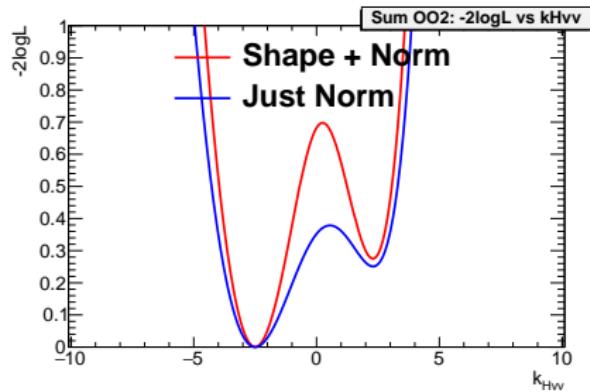
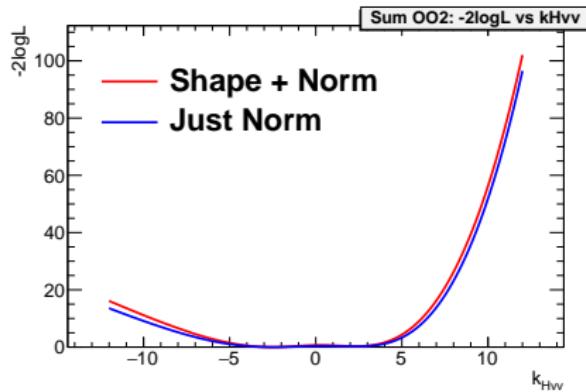
# Fit to $k_{Hvv} = -2.5$ using $OO_2^H$

( $L = 14.8 \text{ fb}^{-1}$ )



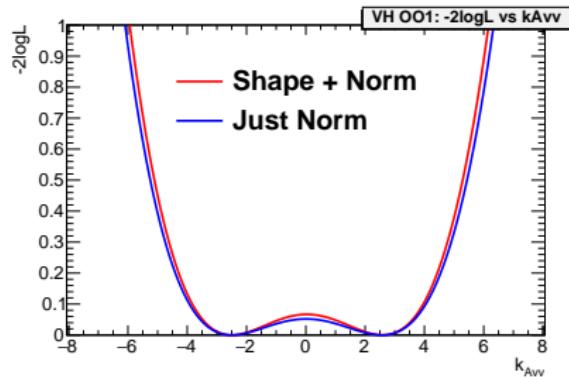
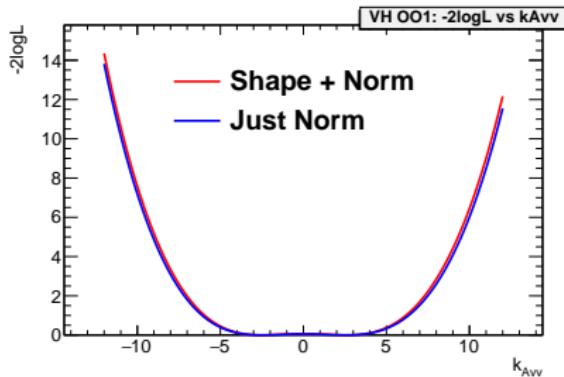
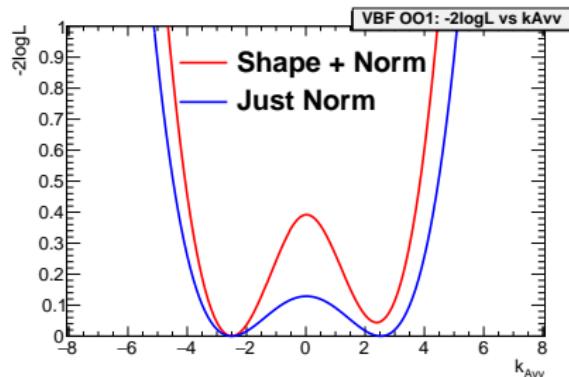
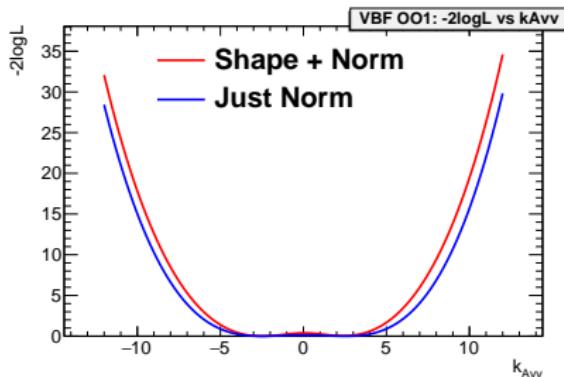
Fit to  $k_{Hvv} = -2.5$  using  $OO_2^H$

( $L = 14.8 \text{ fb}^{-1}$ )

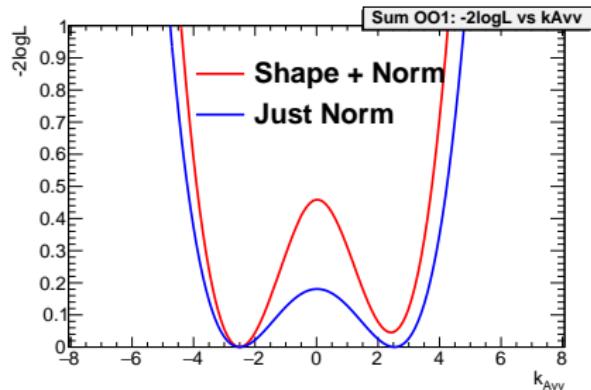
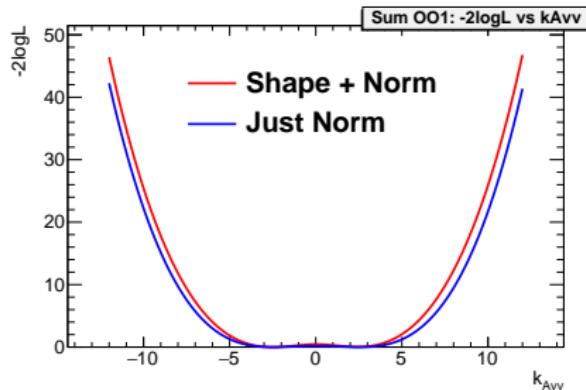


# Fit to $k_{Avv} = -2.5$ using $OO_1^A$

( $L = 14.8 \text{ fb}^{-1}$ )

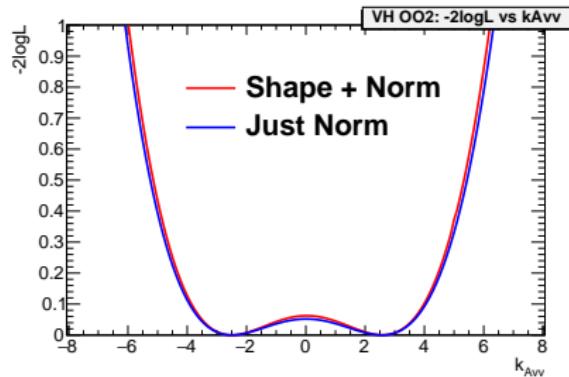
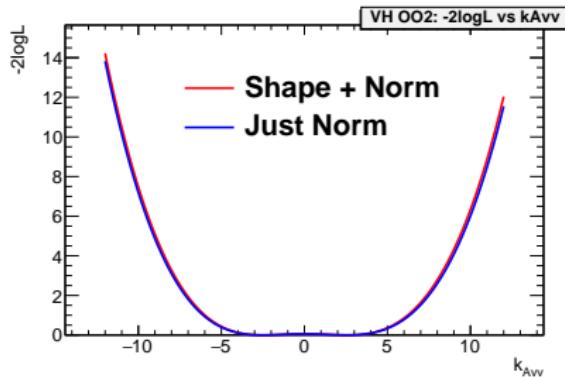
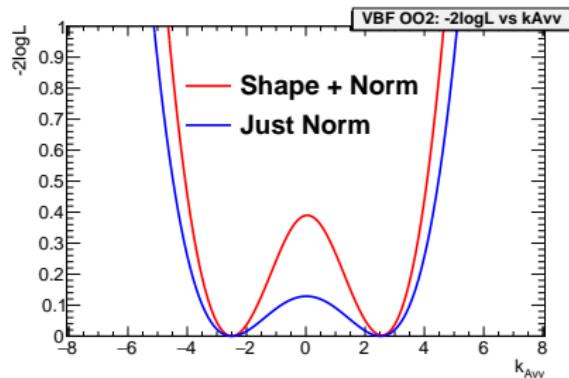
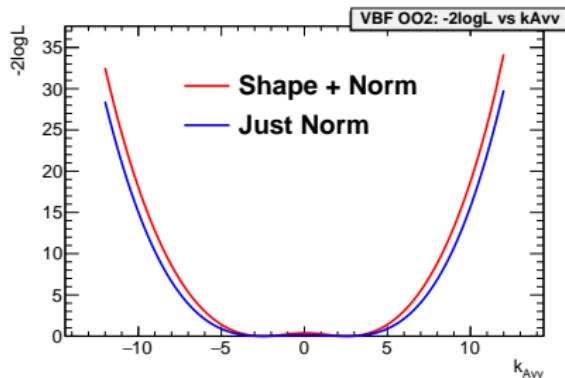


# Fit to $k_{Avv} = -2.5$ using $OO_1^A$ $(L = 14.8 \text{ fb}^{-1})$



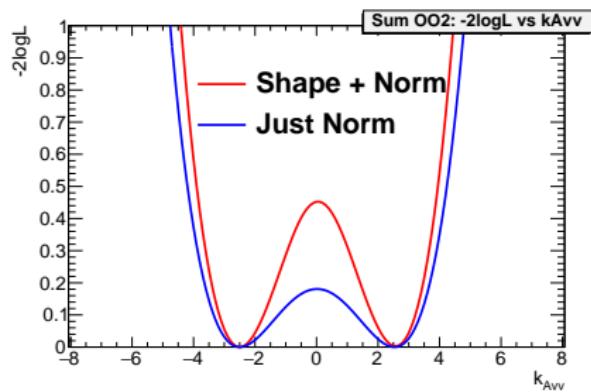
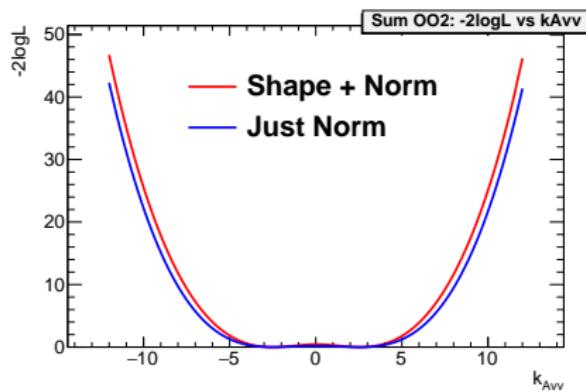
# Fit to $k_{Avv} = -2.5$ using $OO_2^A$

( $L = 14.8 \text{ fb}^{-1}$ )



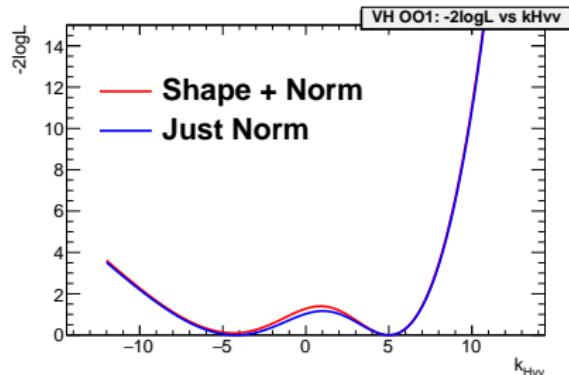
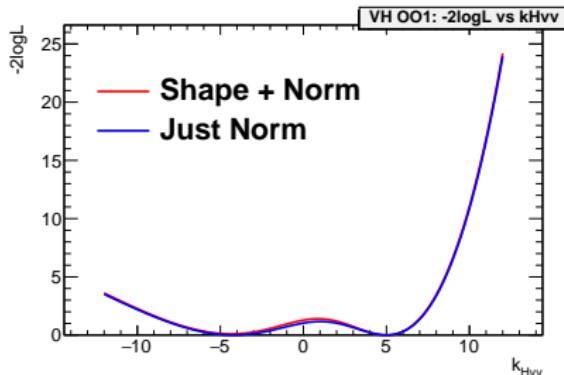
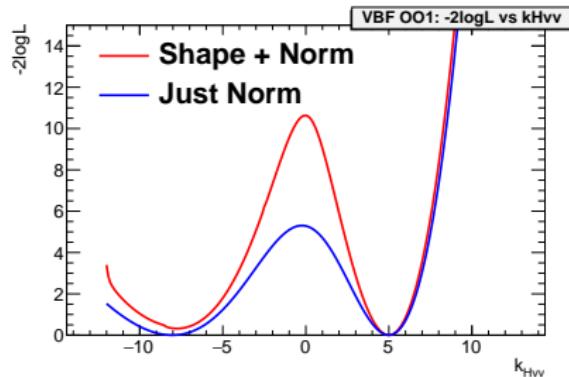
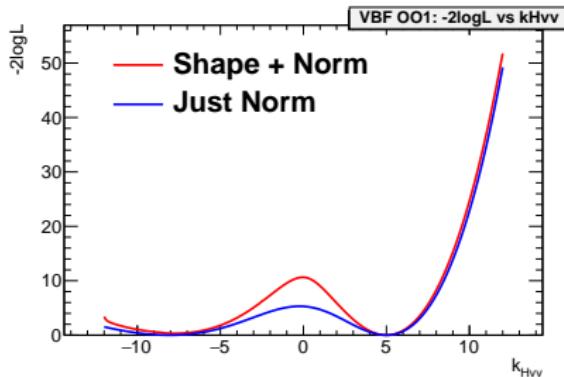
# Fit to $k_{Avv} = -2.5$ using $OO_2^A$

( $L = 14.8 \text{ fb}^{-1}$ )



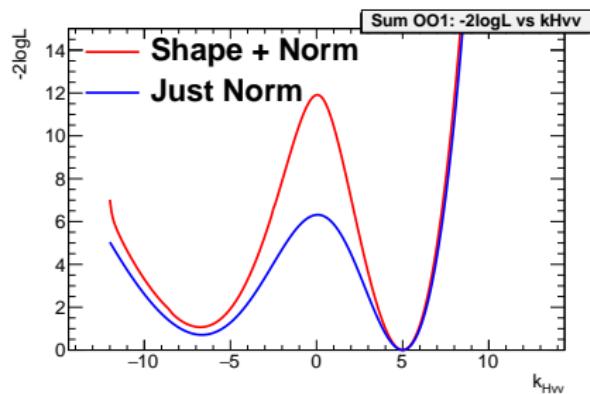
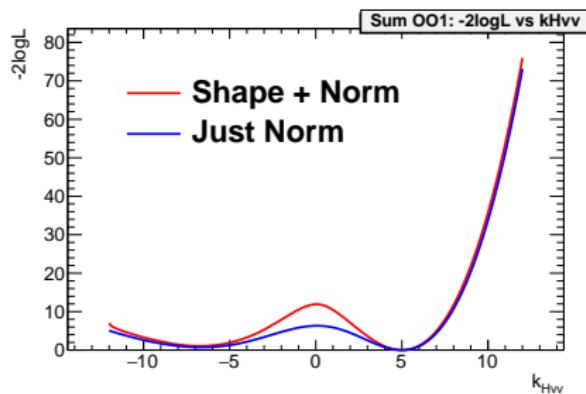
# Fit to $k_{Hvv} = 5$ using $OO_1^H$

$(L = 14.8 \text{ fb}^{-1})$



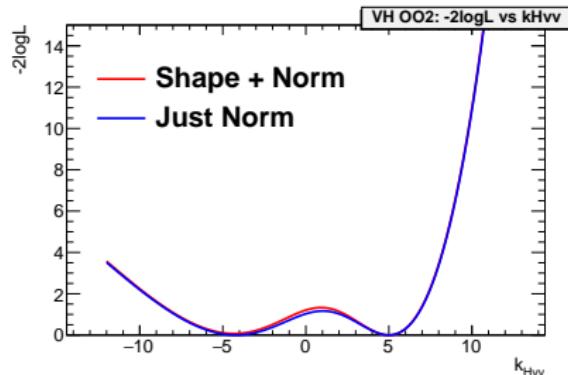
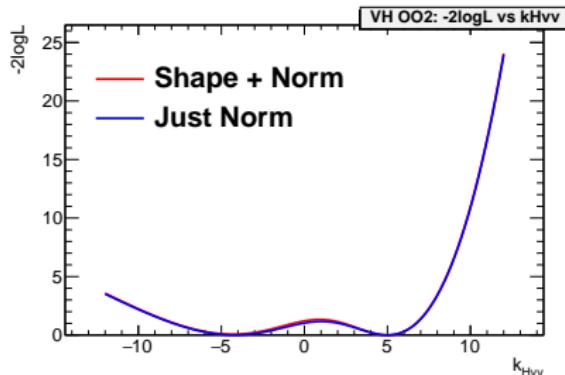
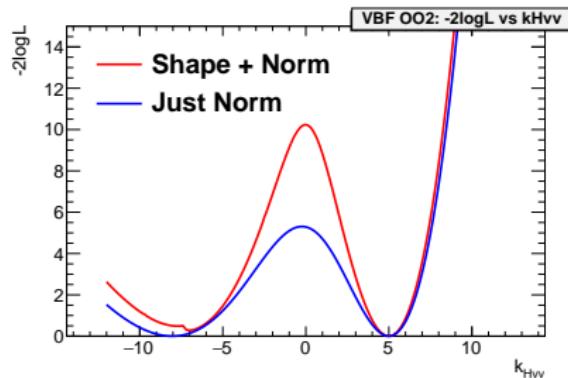
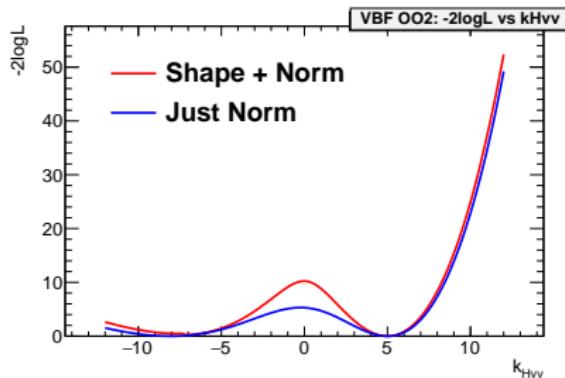
# Fit to $k_{Hvv} = 5$ using $OO_1^H$

( $L = 14.8 \text{ fb}^{-1}$ )



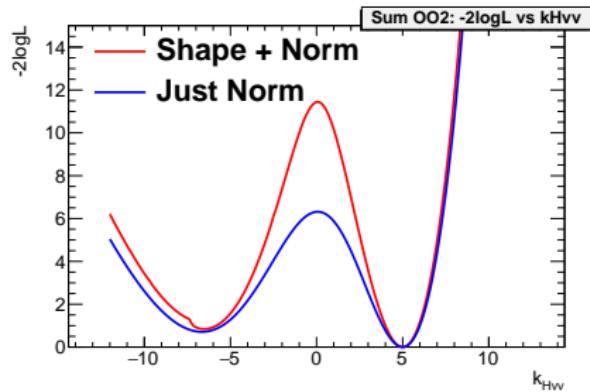
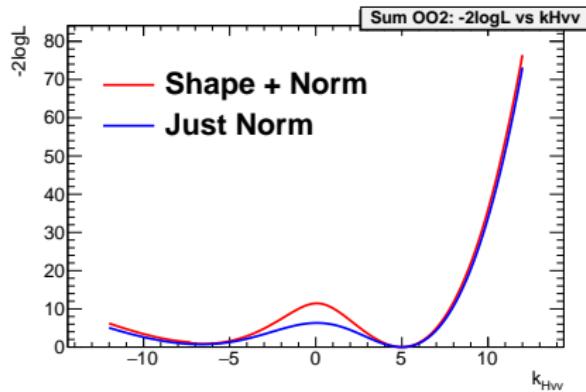
# Fit to $k_{Hvv} = 5$ using $OO_2^H$

$(L = 14.8 \text{ fb}^{-1})$



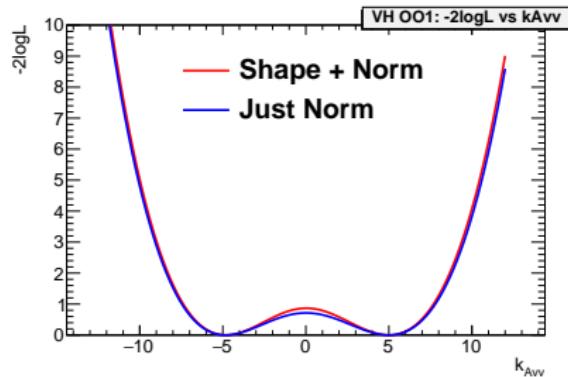
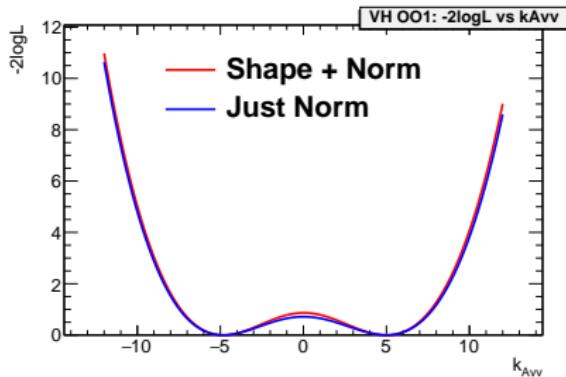
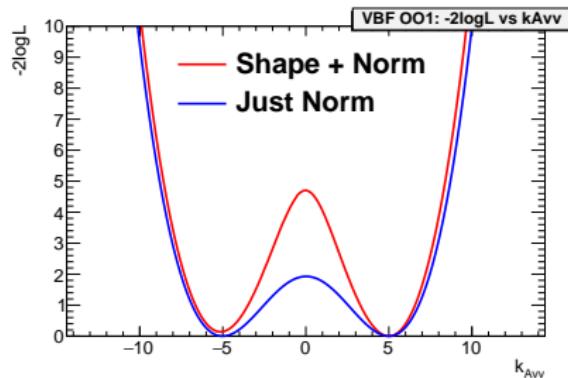
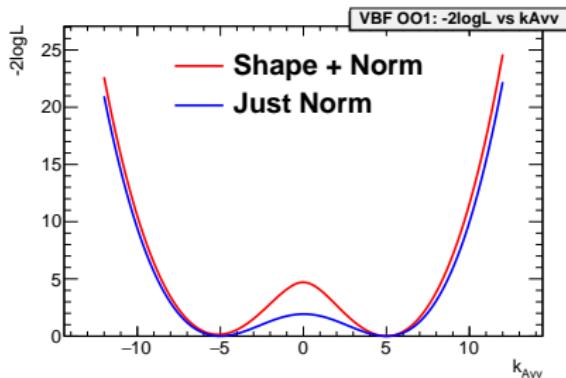
# Fit to $k_{Hvv} = 5$ using $O\!O_2^H$

( $L = 14.8 \text{ fb}^{-1}$ )



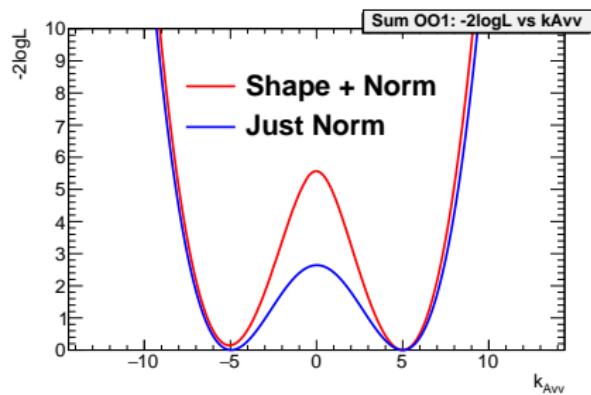
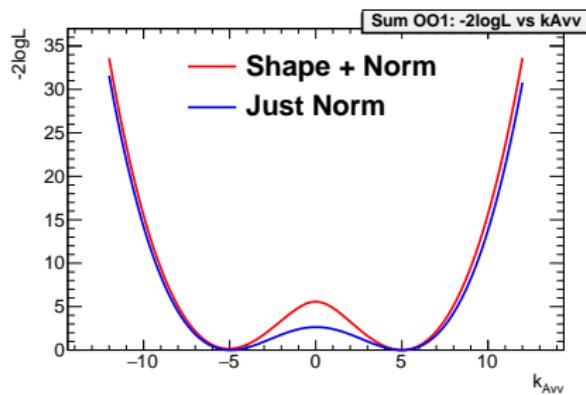
# Fit to $k_{Avv} = 5$ using $OO_1^A$

( $L = 14.8 \text{ fb}^{-1}$ )



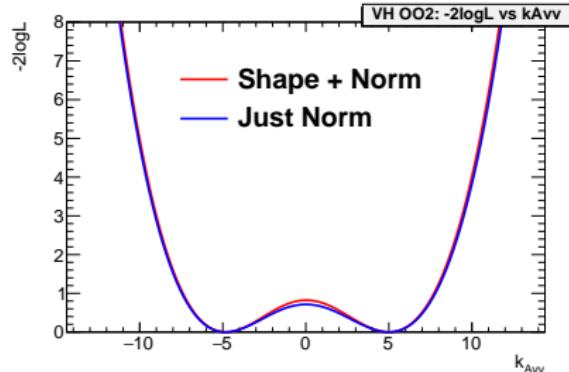
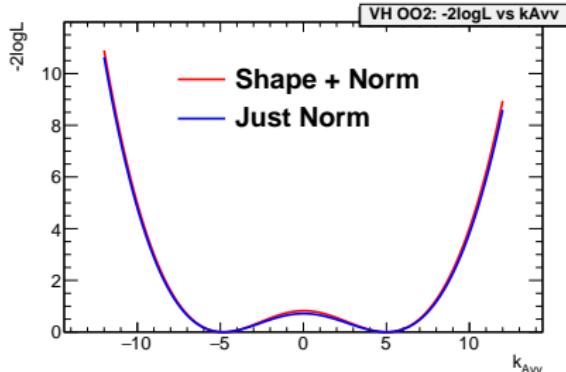
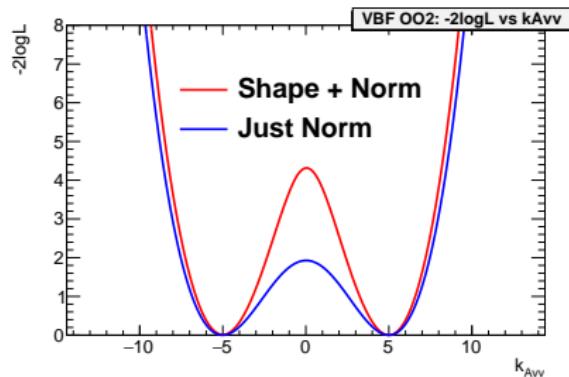
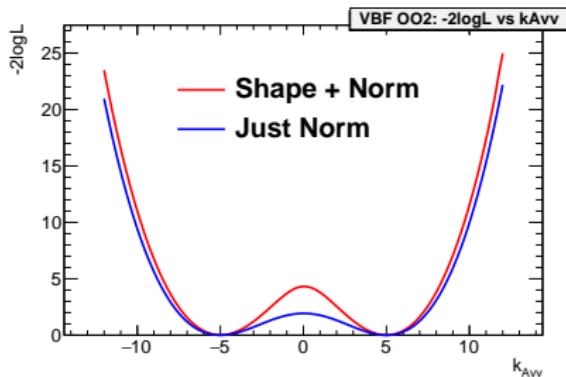
# Fit to $k_{Avv} = 5$ using $OO_1^A$

( $L = 14.8 \text{ fb}^{-1}$ )



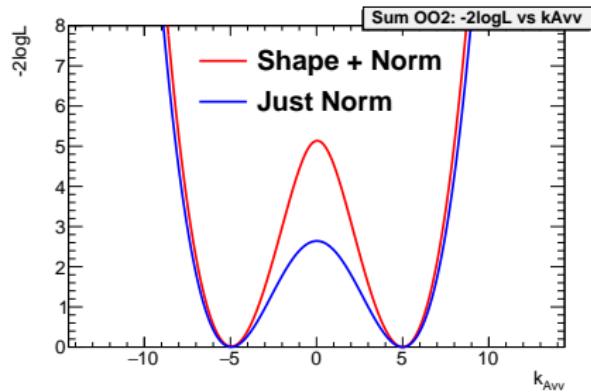
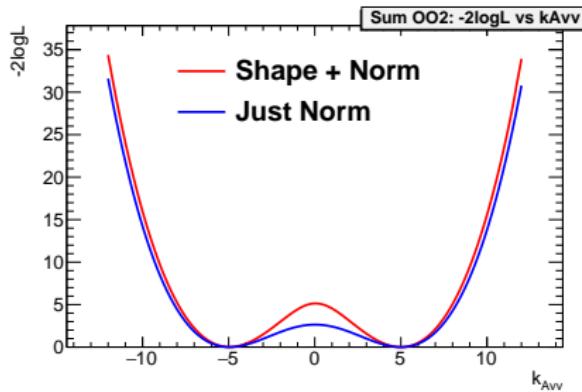
# Fit to $k_{Avv} = 5$ using $O\!O_2^A$

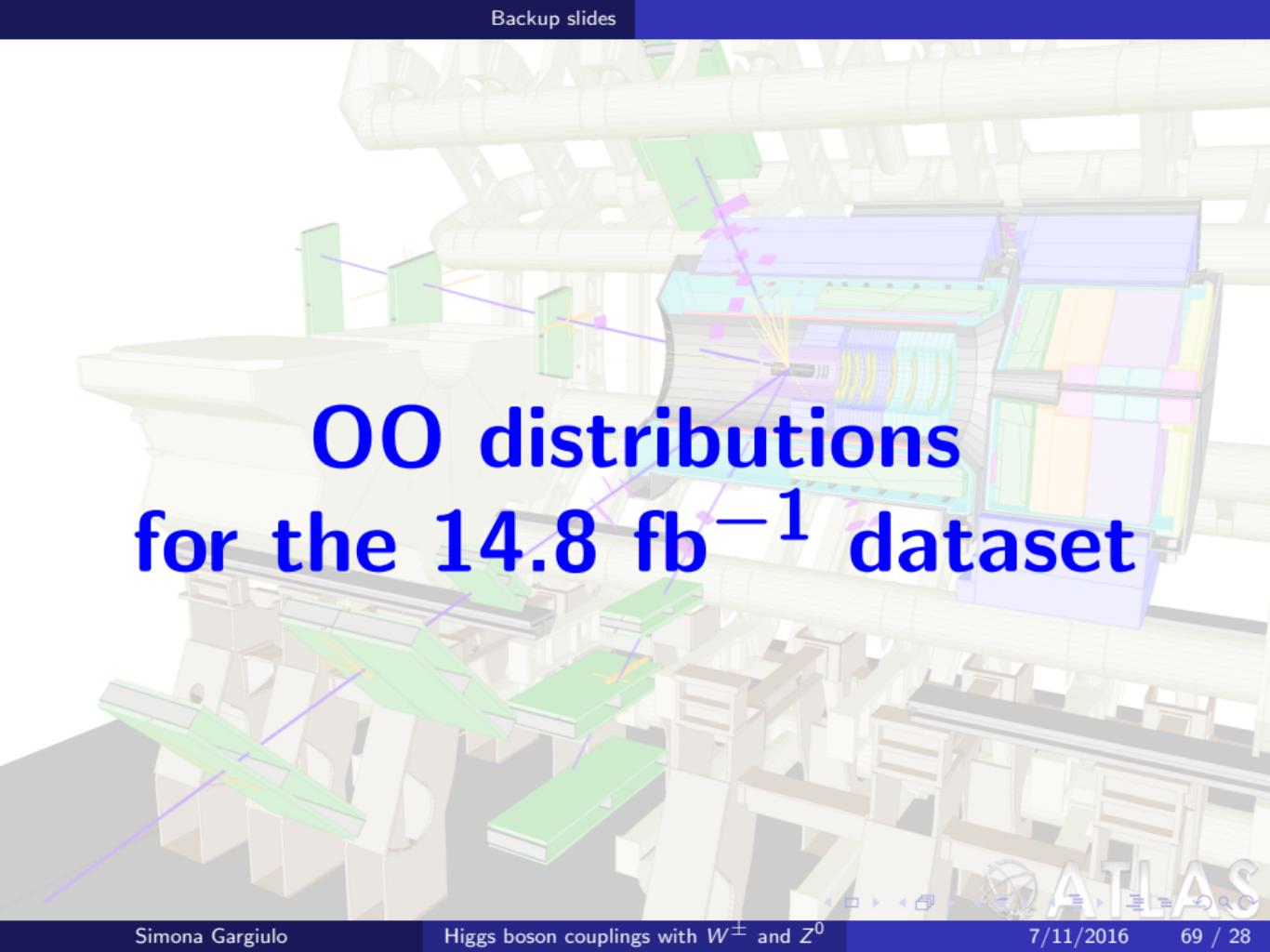
( $L = 14.8 \text{ fb}^{-1}$ )



# Fit to $k_{Avv} = 5$ using $OO_2^A$

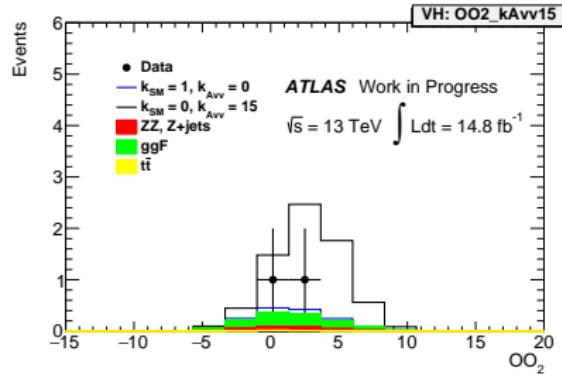
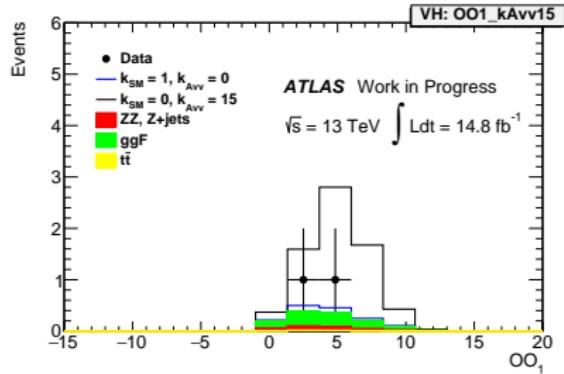
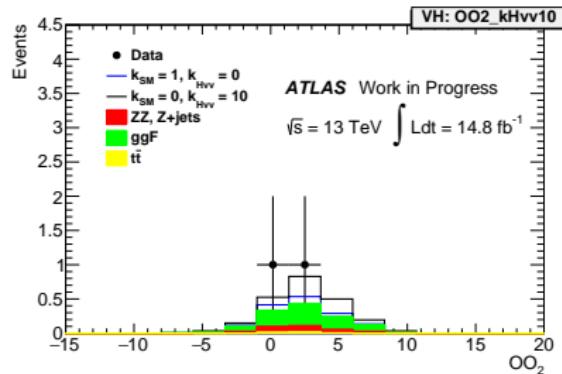
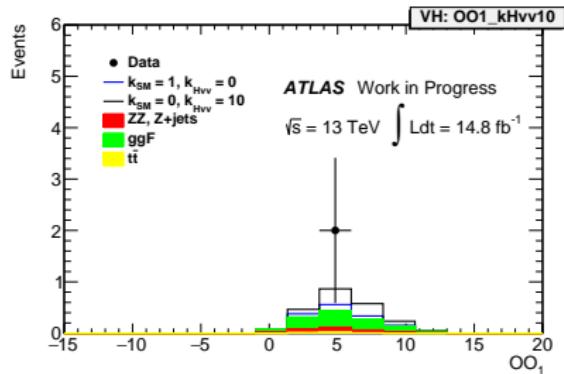
( $L = 14.8 \text{ fb}^{-1}$ )

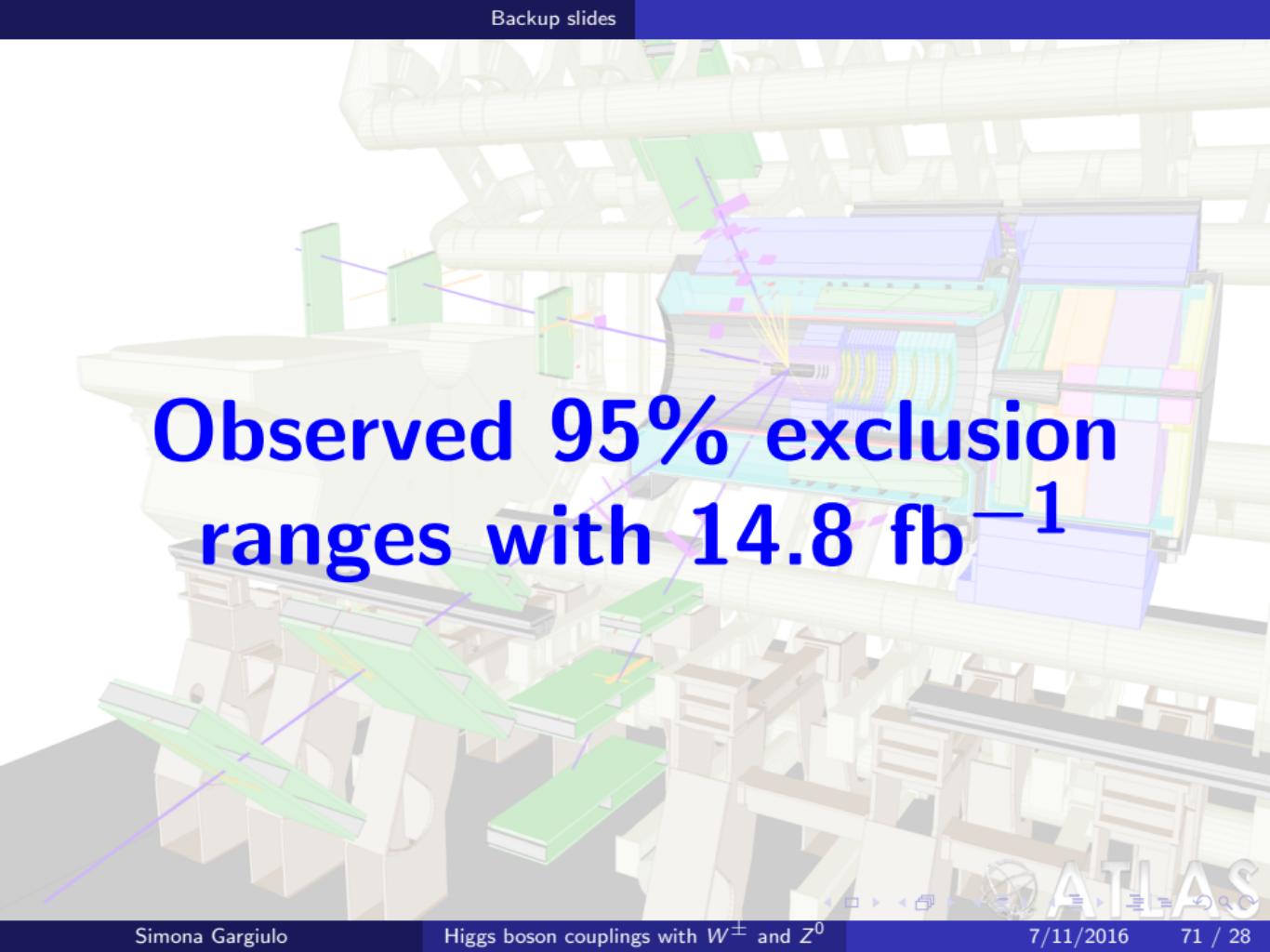




# OO distributions for the $14.8 \text{ fb}^{-1}$ dataset

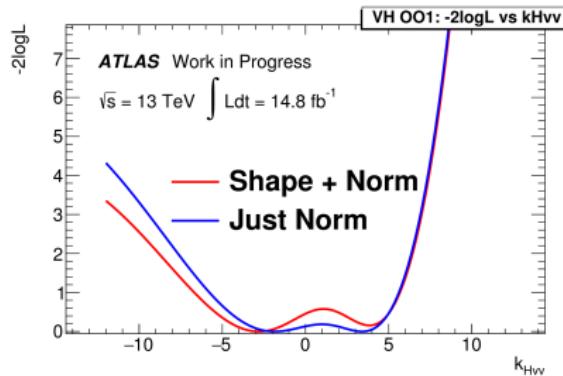
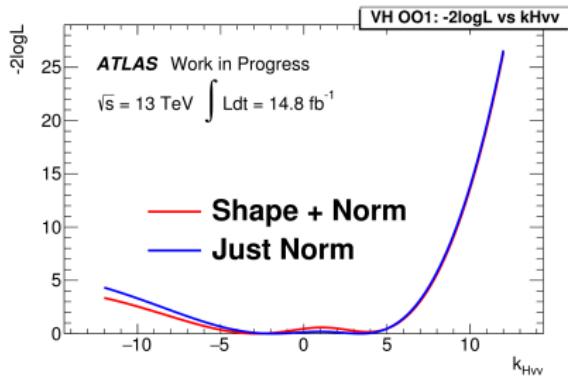
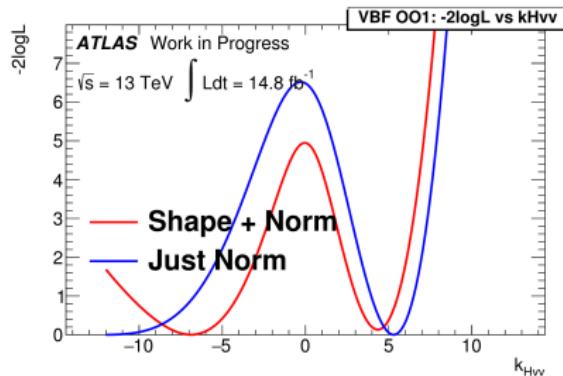
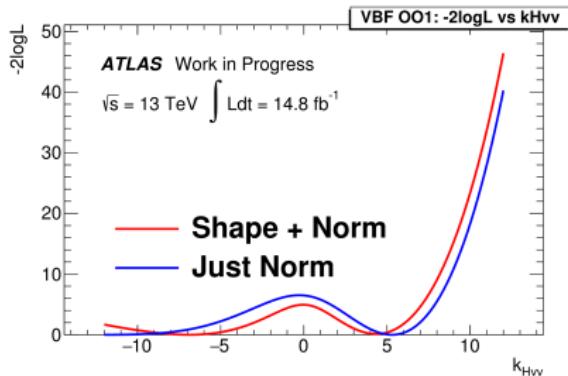
# OO distributions for the VH-category



A semi-transparent background image of the ATLAS particle detector at the Large Hadron Collider (LHC) at CERN. The detector is a complex cylindrical structure with various components like the central interaction region, muon chambers, and calorimeters.

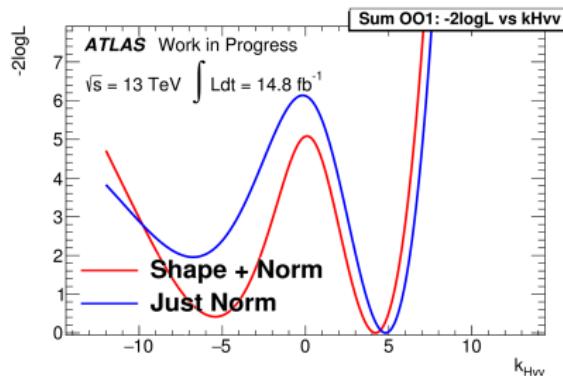
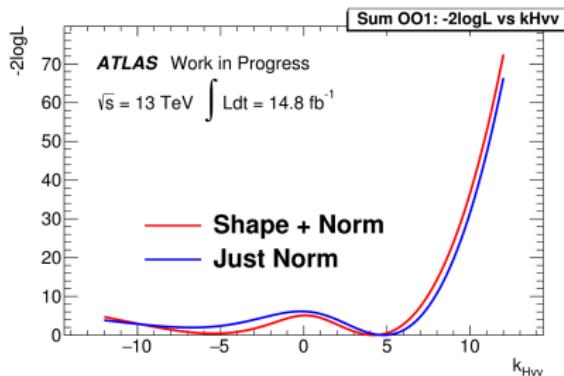
Observed 95% exclusion  
ranges with  $14.8 \text{ fb}^{-1}$

# Fit to $k_{Hvv} = 0$ using $OO_1^H$ ( $L = 14.8 \text{ fb}^{-1}$ )



# Fit to $k_{HVV} = 0$ using $OO_1^H$

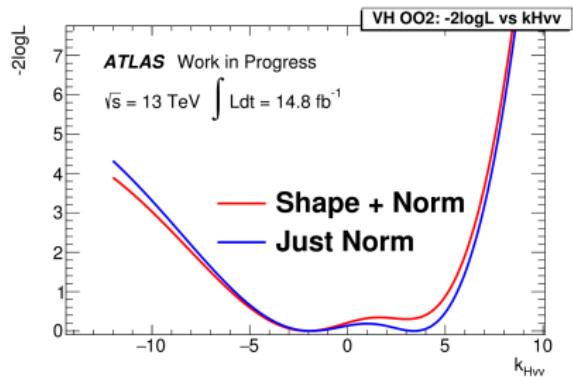
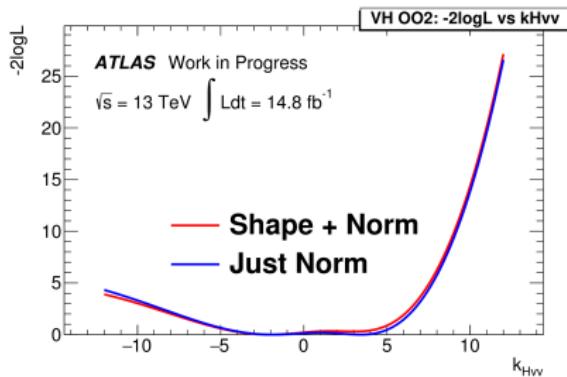
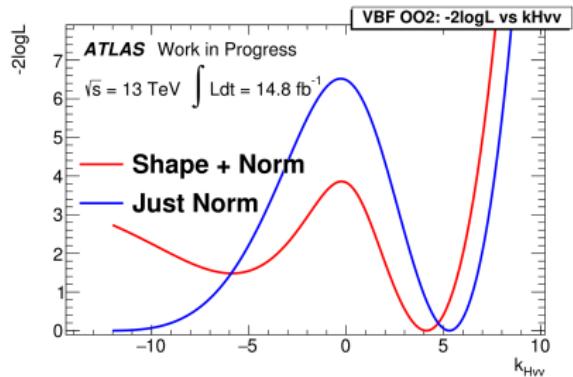
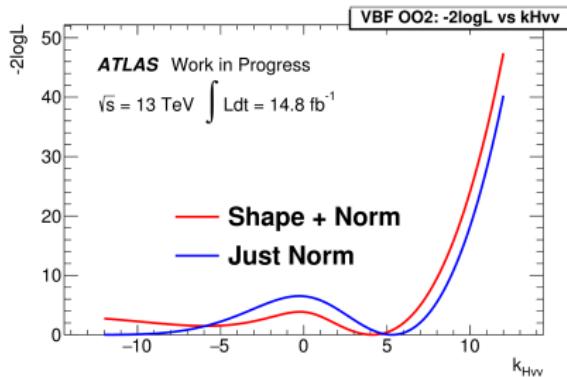
( $L = 14.8 \text{ fb}^{-1}$ )



Optimal observables		Cross section alone	
Observable	$k_{HVV}$	Observable	$k_{HVV}$
$OO_1^H$	[-11, -1.3], [1.4, 6.3]	$OO_1^H$ (single bin)	[-12, -3.1], [2.0, 6.8]

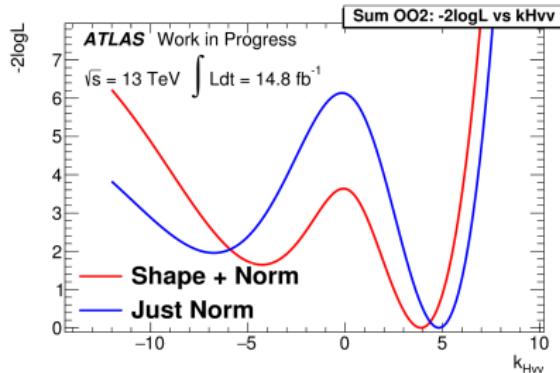
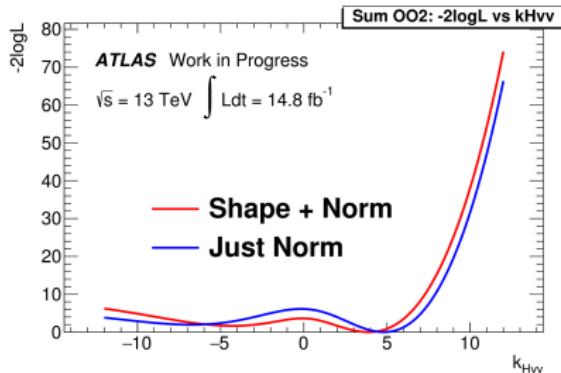
**Table:** Observed 95% confidence intervals on  $k_{HVV}$  for  $OO_1^H$  and for the sum between the VBF and VH loglikelihoods.

# Fit to $k_{Hvv} = 0$ using $OO_2^H$ ( $L = 14.8 \text{ fb}^{-1}$ )



# Fit to $k_{HVV} = 0$ using $OO_2^H$

$(L = 14.8 \text{ fb}^{-1})$

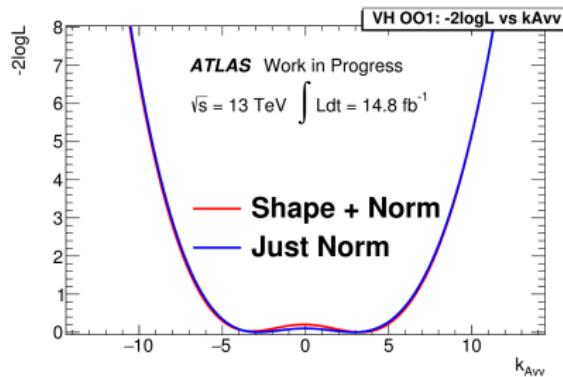
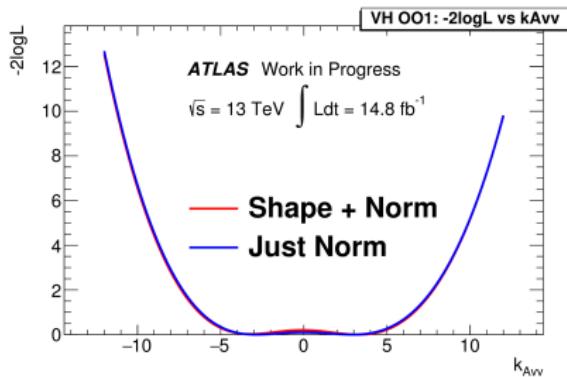
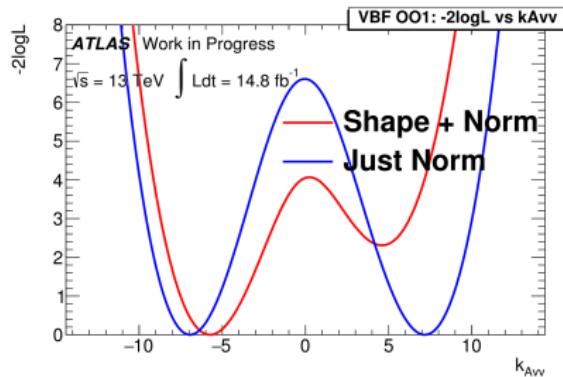
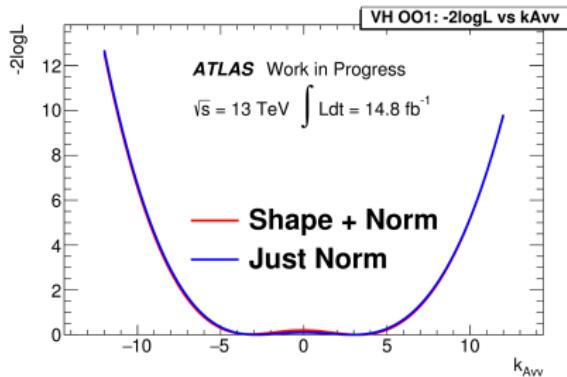


Optimal observables		Cross section alone	
Observable	$k_{HVV}$	Observable	$k_{HVV}$
$OO_2^H$	[-8.8, 6.1]	$OO_2^H$ (single bin)	[-12, -3.1], [2.0, 6.8]

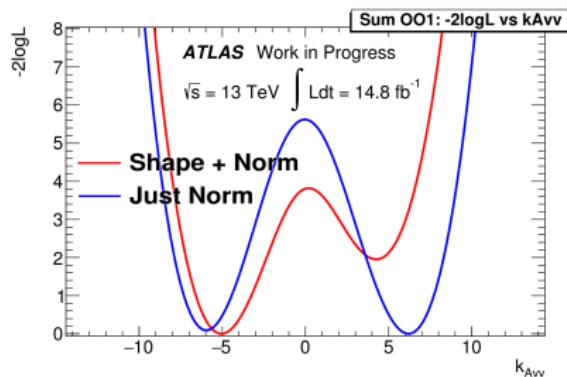
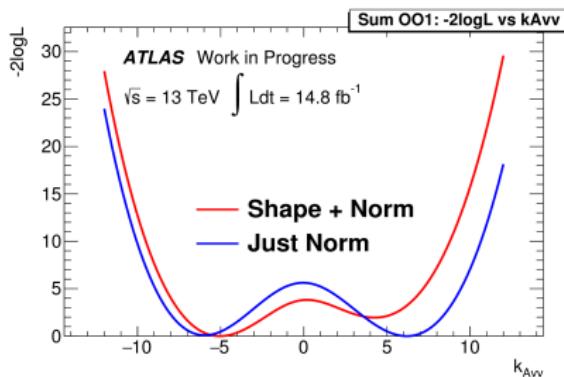
**Table:** Observed 95% confidence intervals on  $k_{HVV}$  for  $OO_2^H$  and for the sum between the VBF and VH loglikelihoods.

# Fit to $k_{Avv} = 0$ using $OO_1^A$

( $L = 14.8 \text{ fb}^{-1}$ )



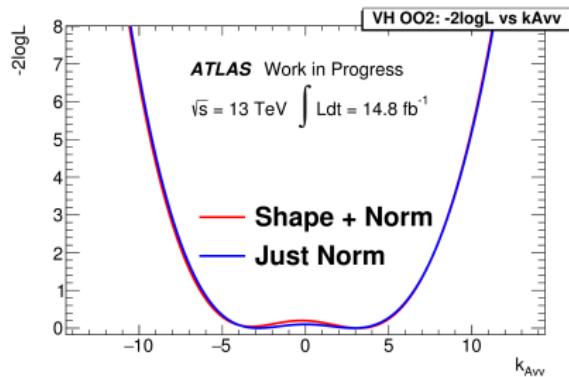
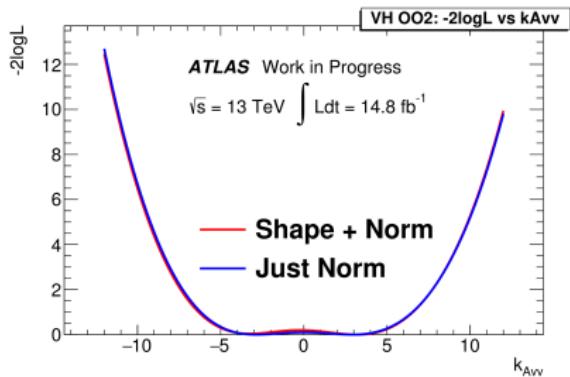
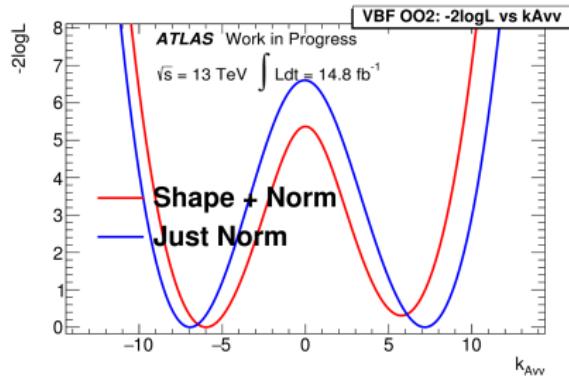
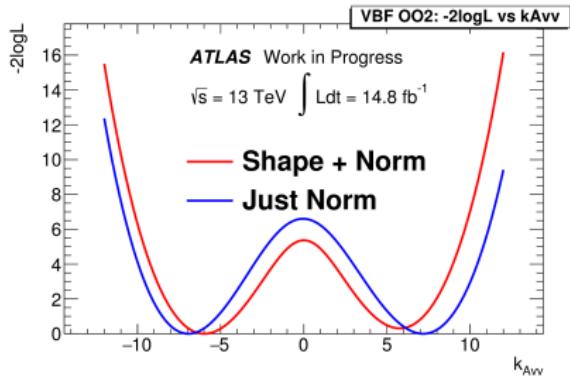
# Fit to $k_{AVV} = 0$ using $OO_1^A$ ( $L = 14.8 \text{ fb}^{-1}$ )



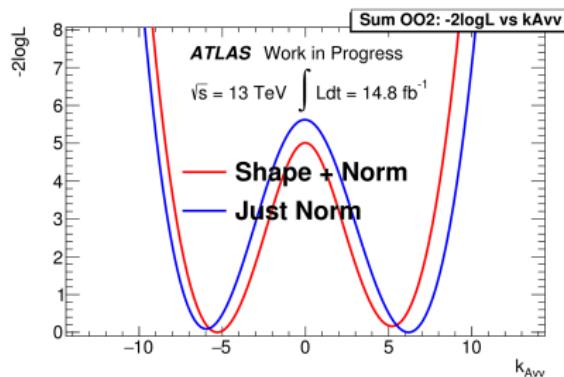
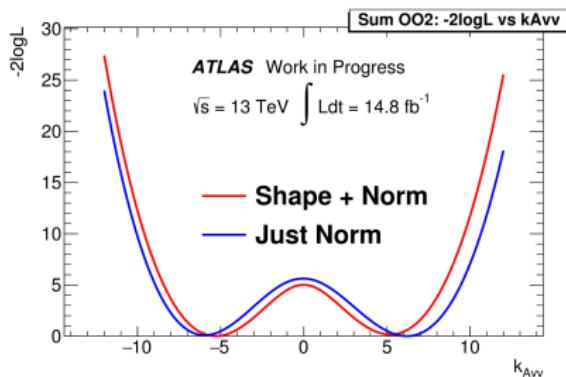
<b>Optimal observables</b>		<b>Cross section alone</b>	
Observable	$k_{AVV}$	Observable	$k_{AVV}$
$OO_1^A$	[-8.0 ,6.6]	$OO_1^A$ (single bin)	[-8.6, -2.3], [2.2, 9.1]

**Table:** Observed 95% confidence intervals on  $k_{AVV}$  for  $OO_1^A$  and for the sum between the VBF and VH loglikelihoods.

# Fit to $k_{Avv} = 0$ using $OO_2^A$ ( $L = 14.8 \text{ fb}^{-1}$ )



# Fit to $k_{AVV} = 0$ using $OO_2^A$ ( $L = 14.8 \text{ fb}^{-1}$ )



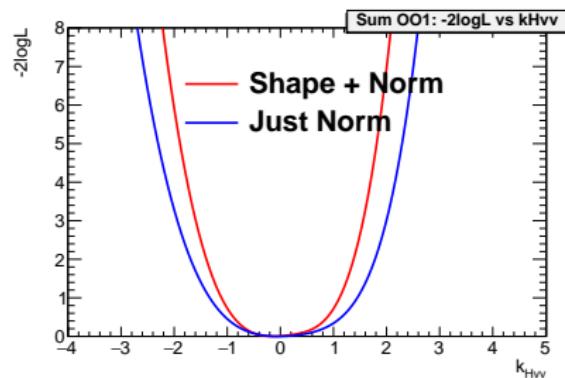
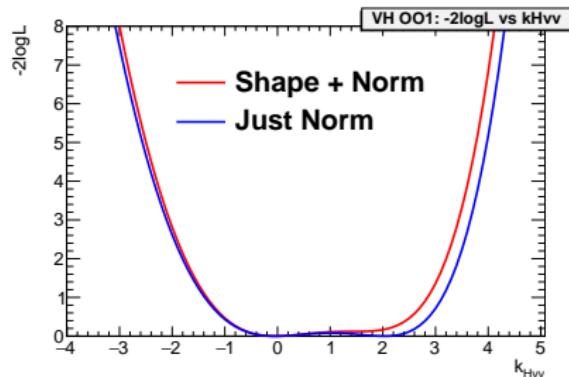
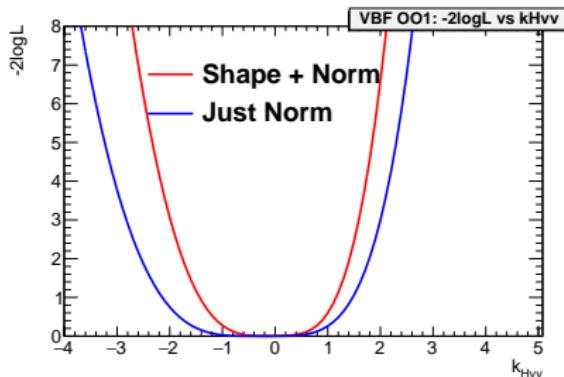
Optimal observables		Cross section alone	
Observable	$k_{AVV}$	Observable	$k_{AVV}$
$OO_2^A$	$[-8.1, -1.5], [1.5, 8.1]$	$OO_2^A$ (single bin)	$[-8.6, -2.3], [2.2, 9.1]$

**Table:** Observed 95% confidence intervals on  $k_{AVV}$  for  $OO_2^A$  and for the sum between the VBF and VH loglikelihoods.

# Prospects with $300 \text{ fb}^{-1}$ of data: a look at HL-LHC

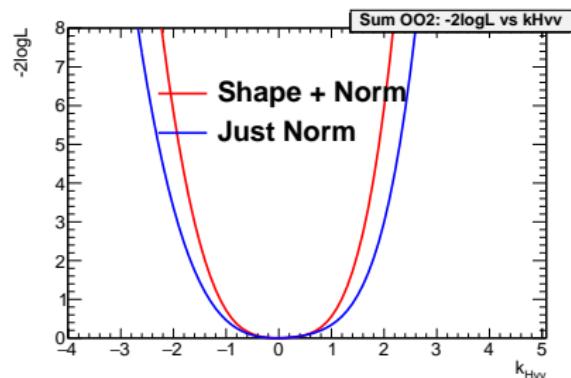
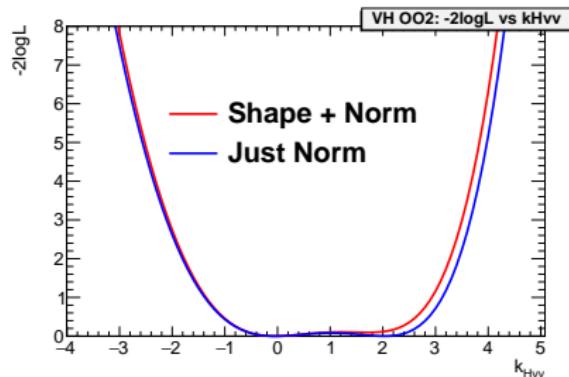
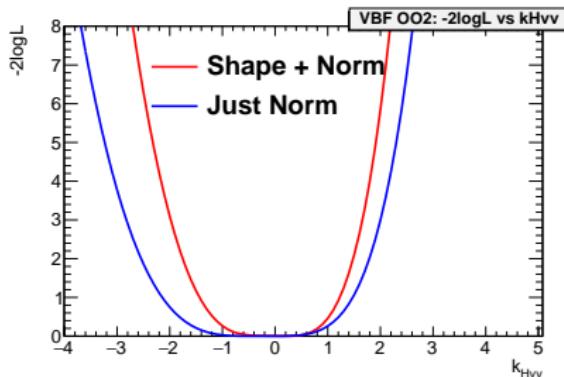
# Fit to $k_{Hvv} = 0$ using $OO_1^H$

( $L = 300 \text{ fb}^{-1}$ )



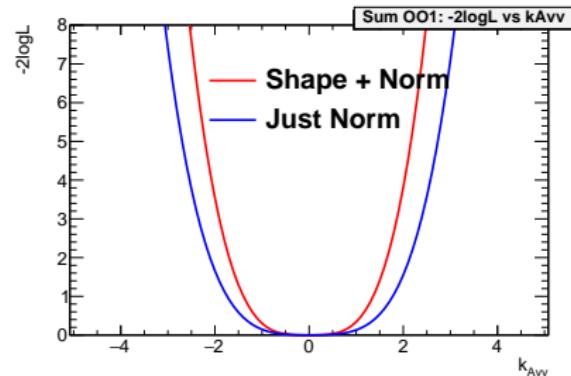
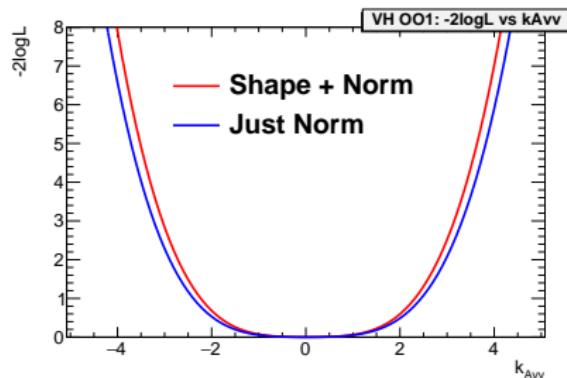
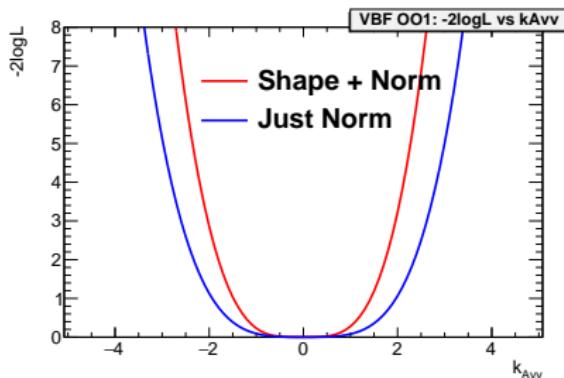
# Fit to $k_{Hvv} = 0$ using $OO_2^H$

( $L = 300 \text{ fb}^{-1}$ )



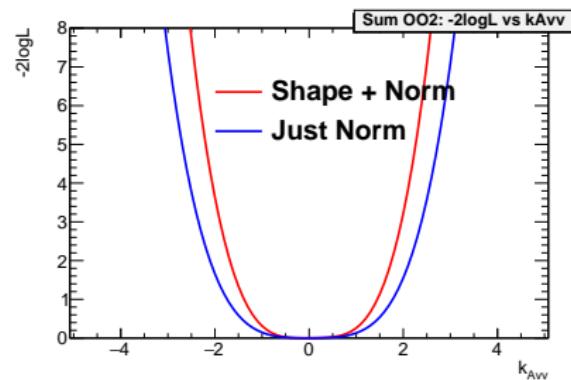
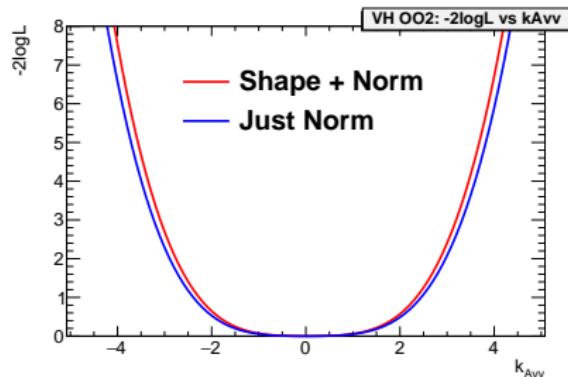
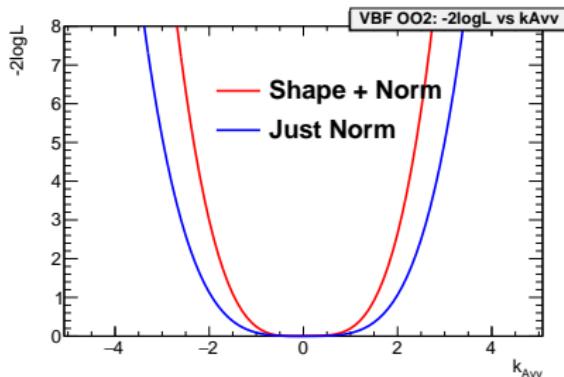
# Fit to $k_{A\bar{V}V} = 0$ using $O\!O_1^A$

( $L = 300 \text{ fb}^{-1}$ )



# Fit to $k_{Avv} = 0$ using $OO_2^A$

( $L = 300 \text{ fb}^{-1}$ )



Results with  $14.8 \text{ fb}^{-1}$ 

**Table:** Expected 95% confidence intervals on  $k_{HVV}$  and  $k_{AVV}$  for the sum between the VBF and VH loglikelihoods. These intervals have been obtained for  $L_{int} = 300 \text{ fb}^{-1}$ .

Optimal observables		
Observable	$k_{HVV}$	$k_{AVV}$
$OO_1^H$	[-1.7, 1.7]	-
$OO_2^H$	[-1.7, 1.8]	-
$OO_1^A$	-	[-2.0, 2.0]
$OO_2^A$	-	[-2.0, 2.1]
Cross section alone		
Observable	$k_{HVV}$	$k_{AVV}$
$OO_1^H$ (single bin)	[-2.1, 2.1]	-
$OO_2^H$ (single bin)	[-2.1, 2.1]	-
$OO_1^A$ (single bin)	-	[-2.5, 2.6]
$OO_2^A$ (single bin)	-	[-2.5, 2.6]