



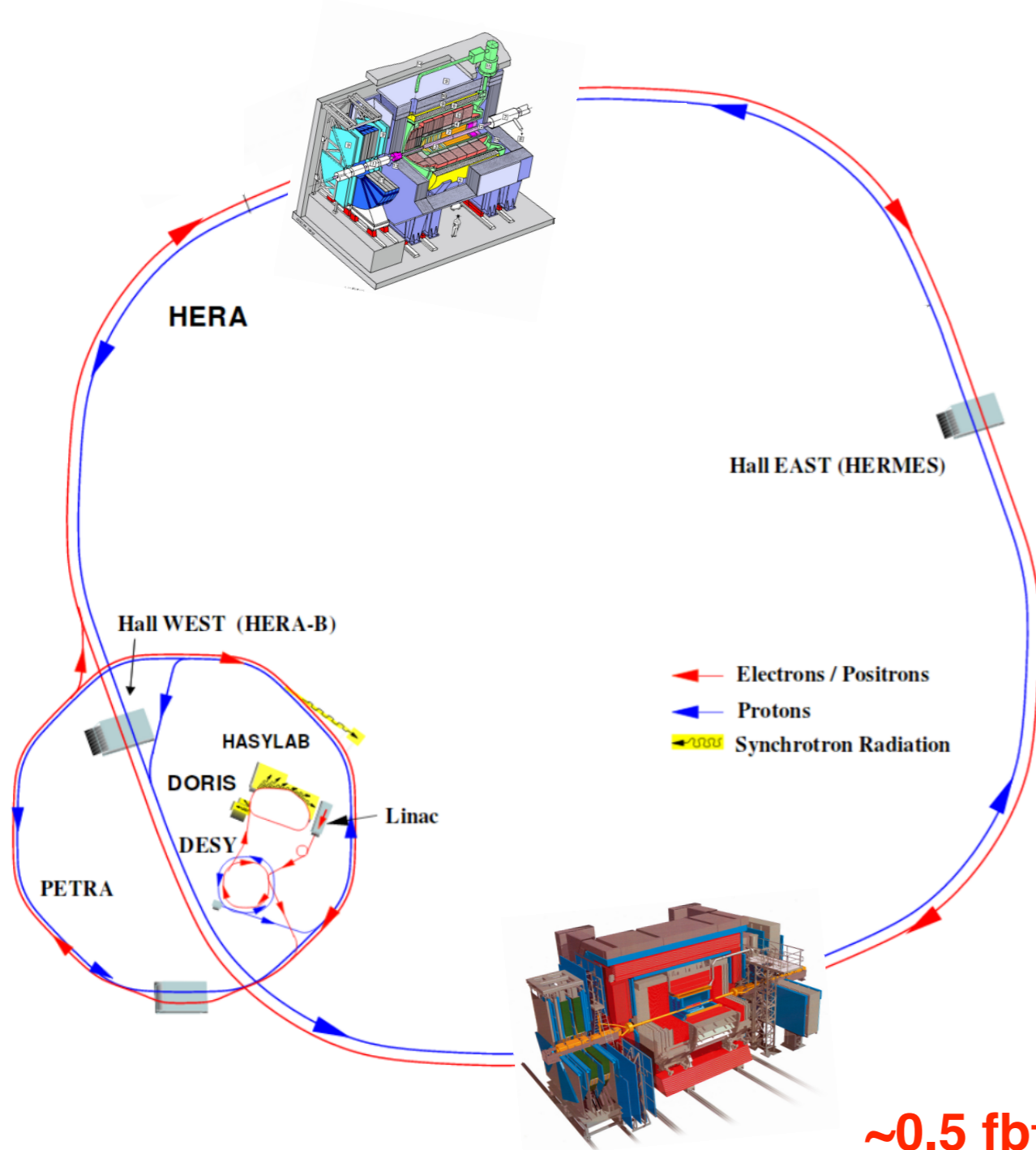
What the HERA data tell us about low- x physics



I. Abt, A. Cooper-Sarkar, B. Foster,
[V. Myronenko](#),
K. Wichmann, M. Wing

Prospects for a VHE eP and eA collider
Max-Planck-Institut für Physik
Munich, Germany 2017

The HERA collider and the experiments



Location: Hamburg, Germany

Research operation: 1992 - 2007

Length: 6336 m

Proton and electron (positron) beams

4 experimental halls

2 experiments on colliding beams

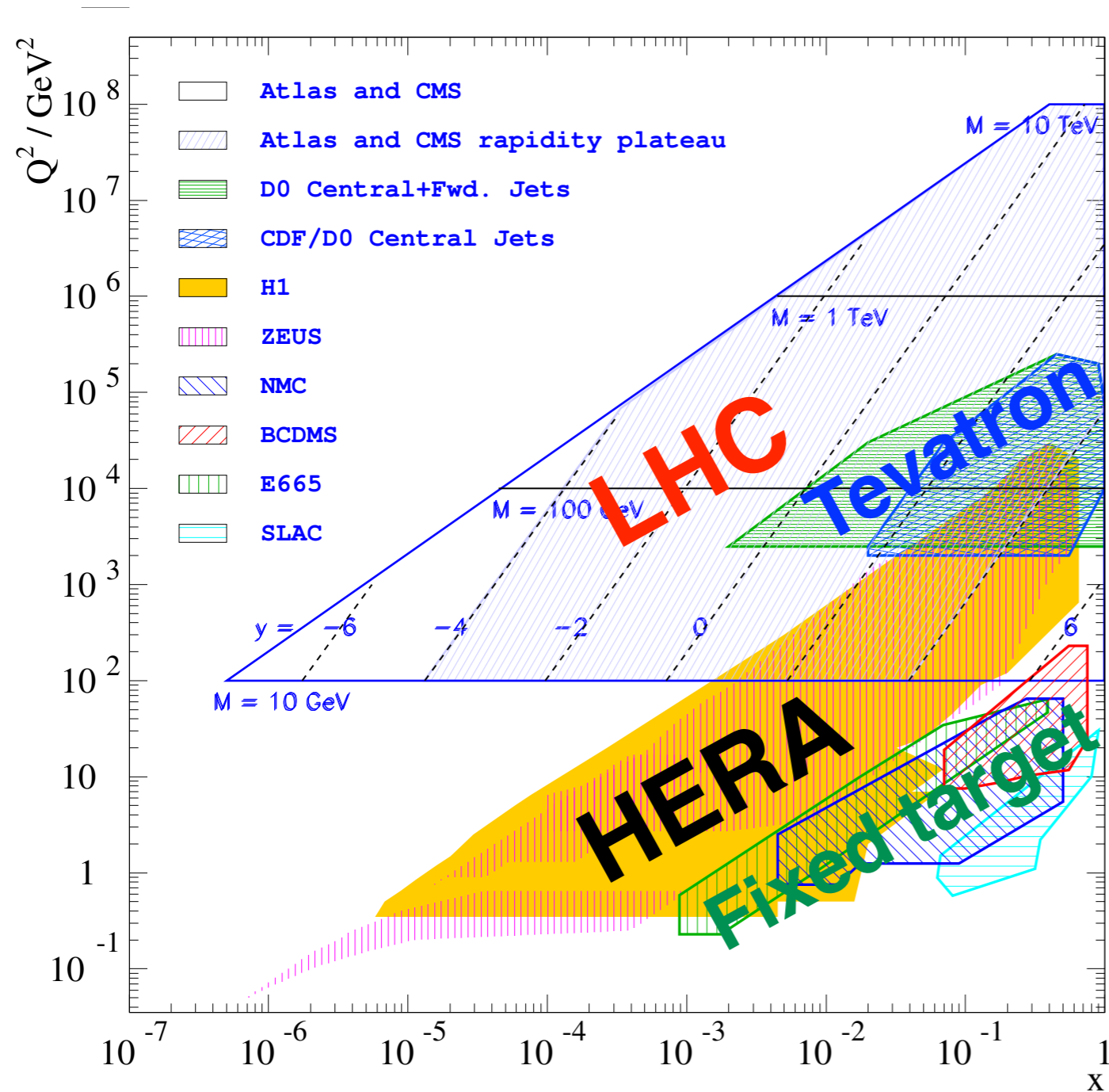
$$E_P = 920(820, 575, 460) GeV$$

$$E_e = 27.5 GeV$$

$$\sqrt{s} = 318(300, 252, 225) GeV$$

~0.5 fb⁻¹ of DIS data collected by each experiment

HERA data



Collected data spans:

6 orders of magnitude in x_{Bj}

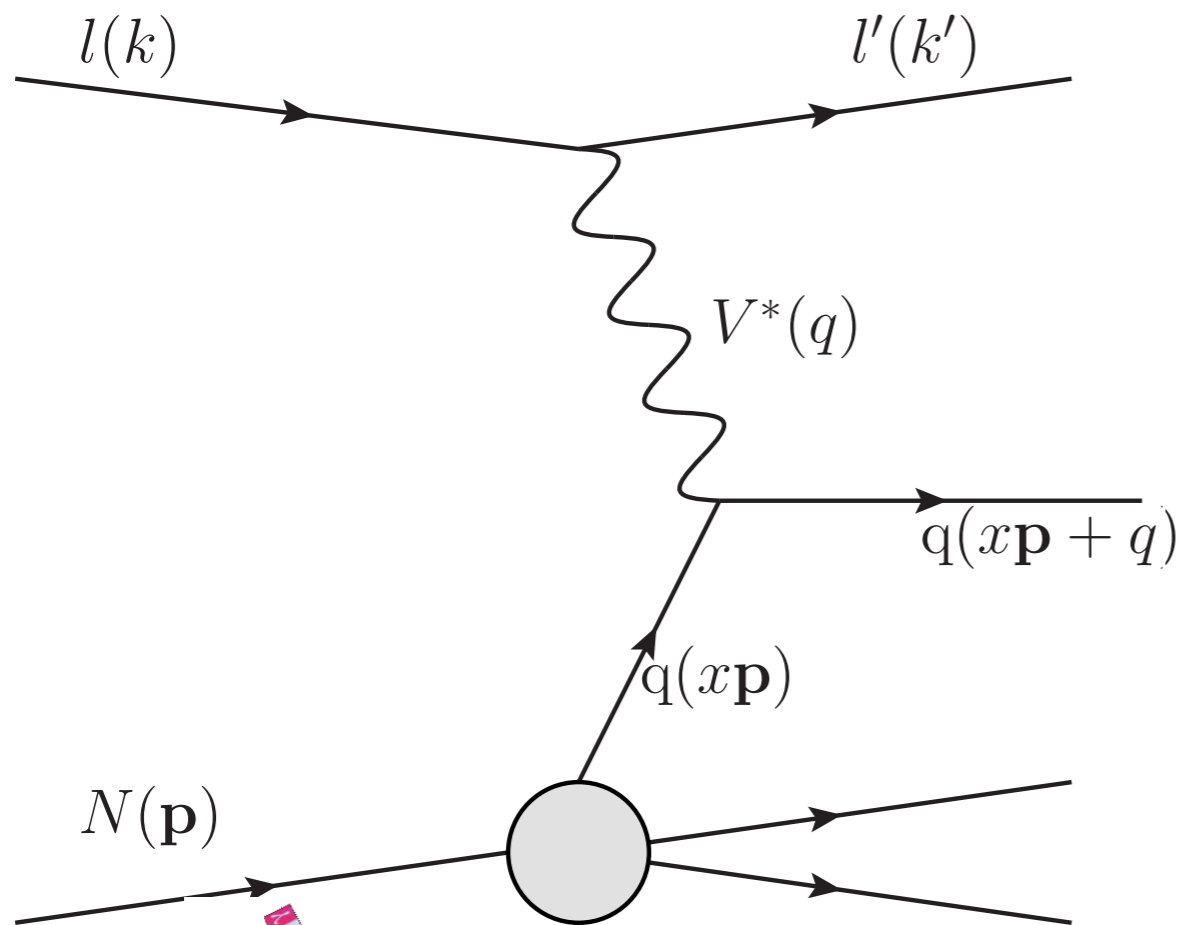
6 orders of magnitude in Q^2

Core of any PDF extraction

Basis for probing
QCD and EW physics

Unique data for testing low- x
phenomenological models

Deep-Inelastic scattering at HERA



$$Q^2 = -q^2 = -(k - k')^2$$

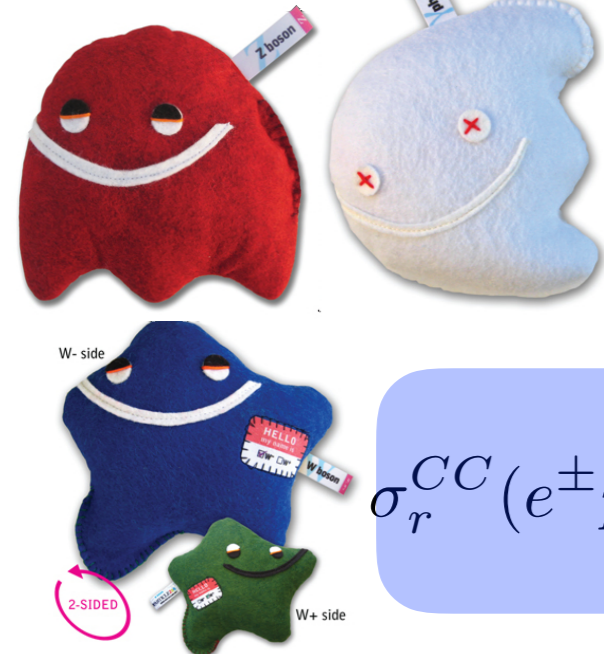
$$x_{Bj} = \frac{Q^2}{2pq} \quad y = \frac{pq}{pk}$$

$$s = (p + k)^2 \quad Q^2 = xys$$

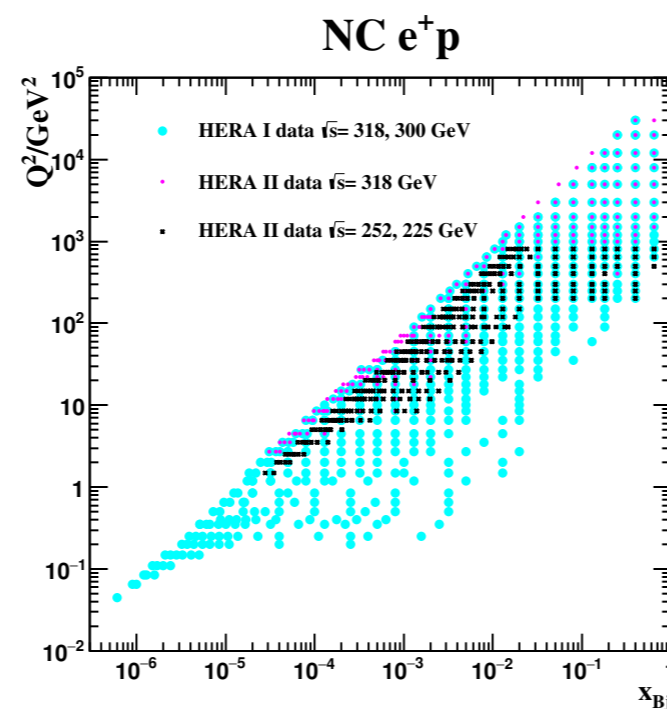
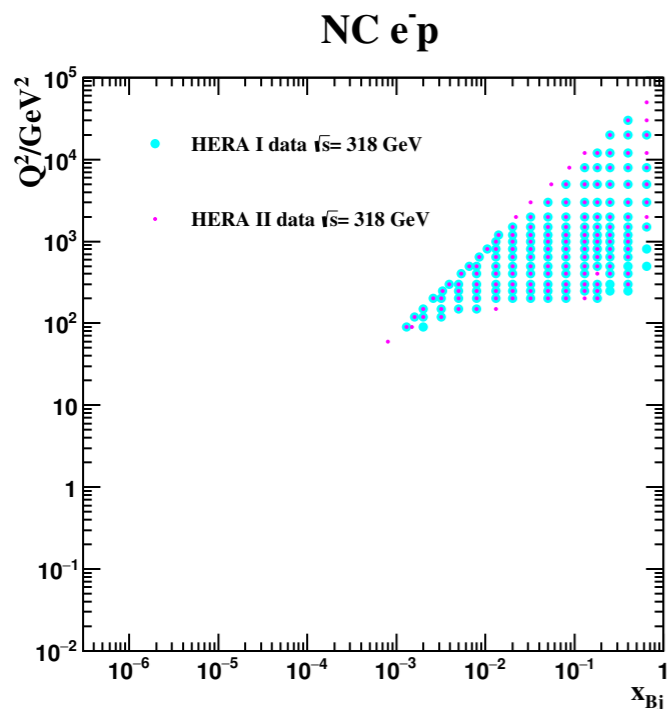
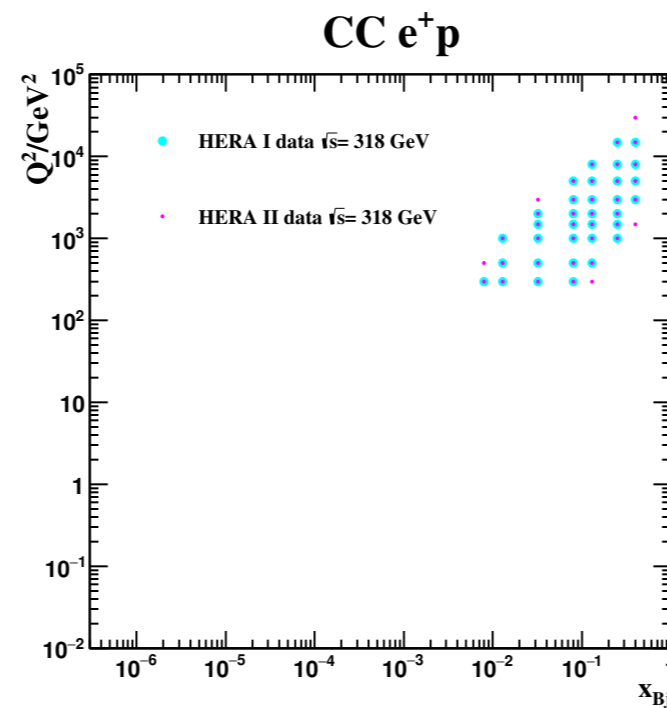
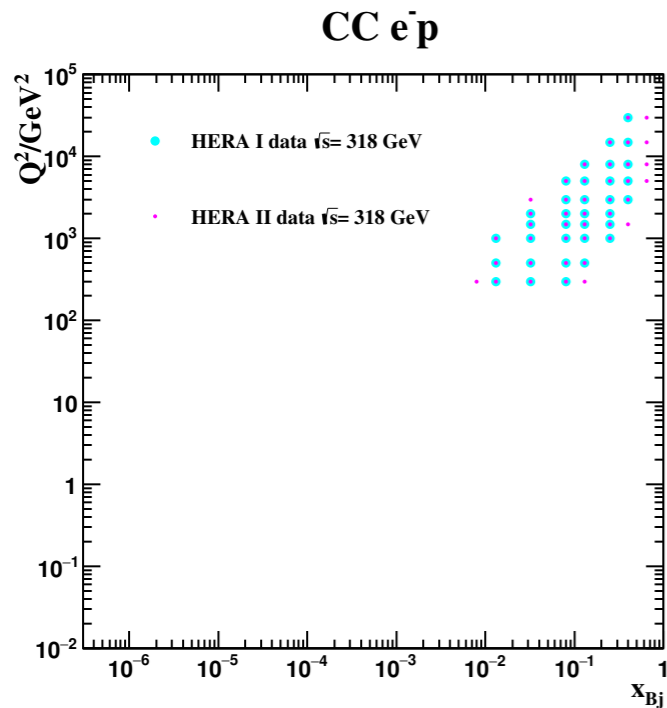
Neutral Current (**NC**) and Charged current (**CC**) reactions are possible

$$\sigma_r^{NC}(e^\pm p) = \frac{d^2\sigma^{NC}(e^\pm p)}{dx dQ^2} \cdot \frac{xQ^4}{2\pi\alpha^2 Y_+} = \widetilde{F}_2^{NC} \mp \frac{Y_-}{Y_+} x \widetilde{F}_3^{NC} - \frac{y^2}{Y_+} \widetilde{F}_L^{NC}$$

$$\sigma_r^{CC}(e^\pm p) = \frac{d^2\sigma^{CC}(e^\pm p)}{dx dQ^2} \cdot \frac{2\pi x (Q^2 + M_W^2)^2}{G_F^2 M_W^4} = \frac{Y_+}{2} \widetilde{F}_2^{CC} \mp \frac{Y_-}{2} x \widetilde{F}_3^{CC} - \frac{y^2}{2} \widetilde{F}_L^{CC}$$



DIS in various reactions



CC $e^\pm p$:

Sensitive to quark-flavour decomposition.

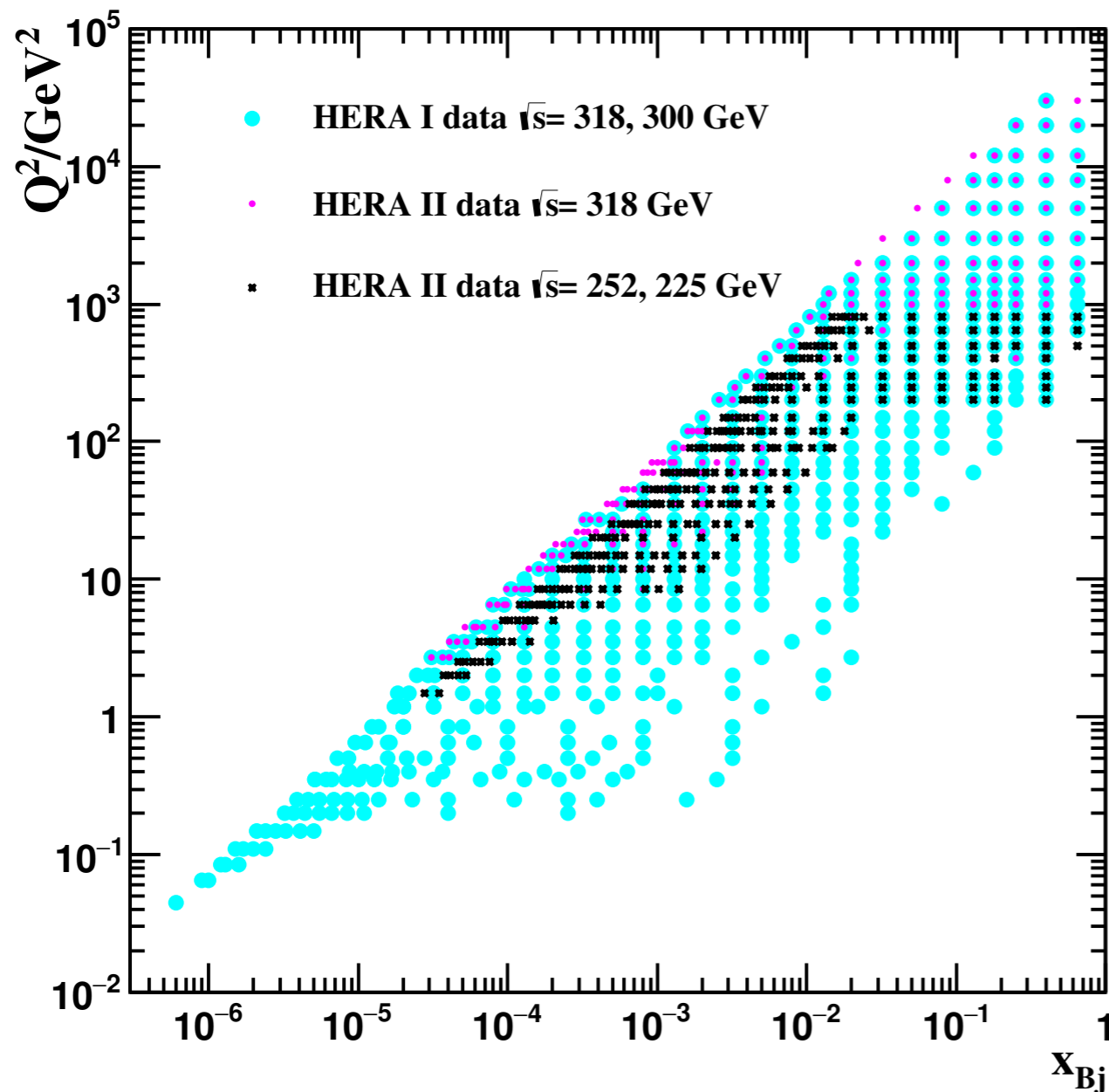
NC $e^\pm p$:

Probe valence-quark distribution (F_2 , xF_3)

Gluon content of the proton (scaling violation)

NC e^+p DIS data

NC e^+p



Covers widest cinematic range

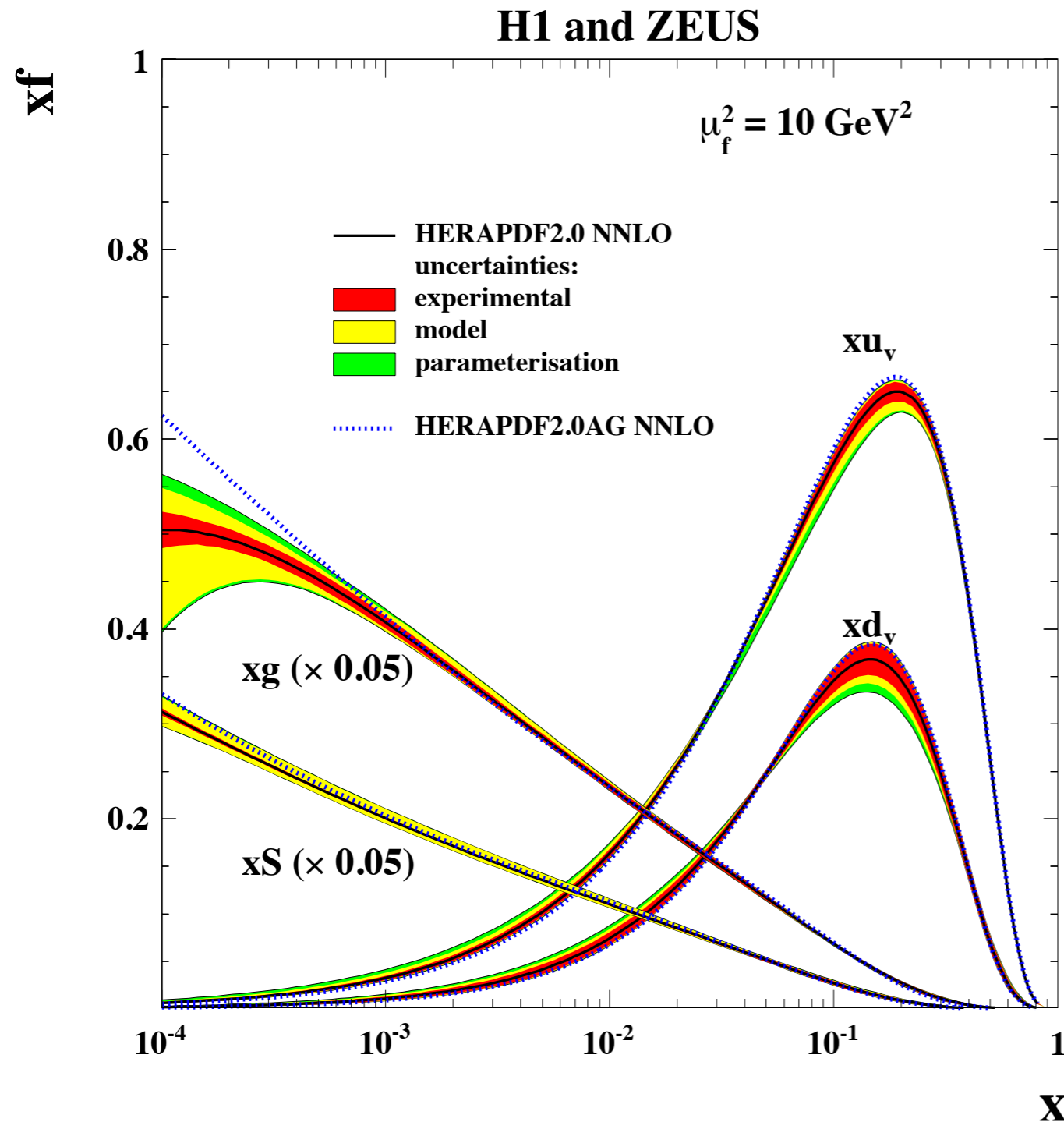
Available in several \sqrt{s}

NC e^+p @($\sqrt{s} = 318$ GeV):

Probes the **lowest** x_{Bj} and Q^2

Lowest- x_{Bj} data is **~16 years old!**

DIS data for PDF extraction



Eur.Phys.J. C75 (2015) no.12, 580, [\[arXiv:1506.06042\]](https://arxiv.org/abs/1506.06042)

Basic idea:
fit QCD predictions to exp. data

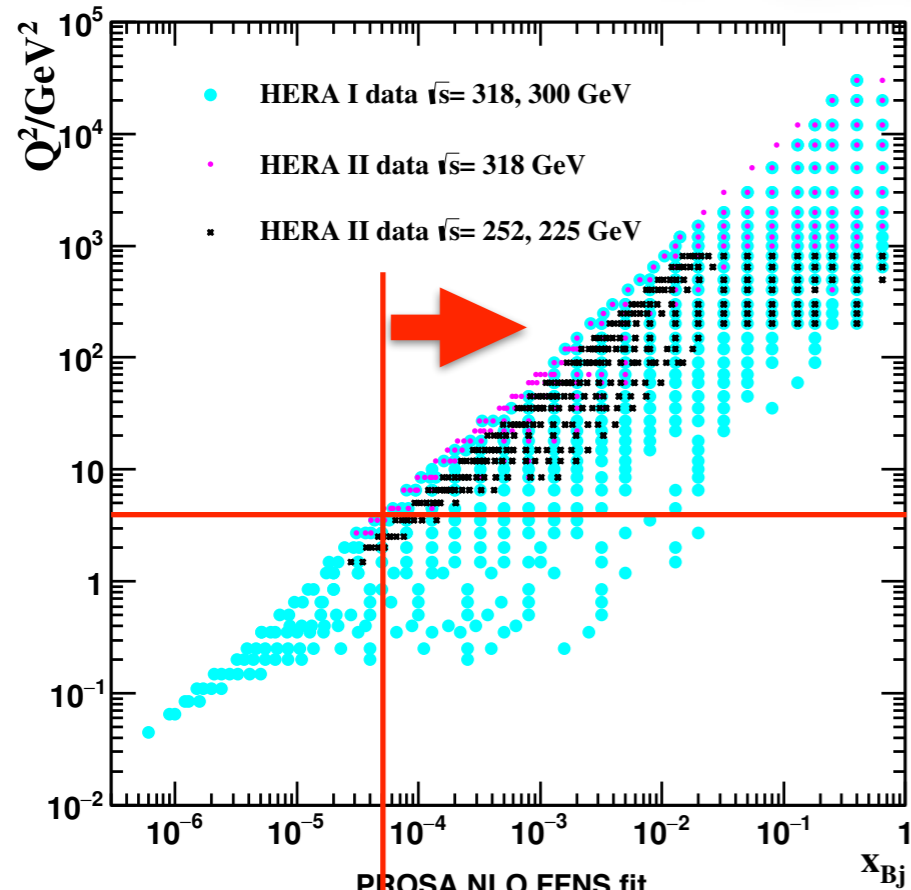
$$\sigma_{A \rightarrow C}(q, p) = \sum_a \int_x^1 d\xi f^a(\xi, \mu) \sigma_{a \rightarrow C}(q, \xi, p, \mu, \alpha_s)$$

DIS data constrains the PDFs:

HERAPDF - based on HERA only
Other PDFs - use HERA as a basis

PDFs at low x

NC e^+p

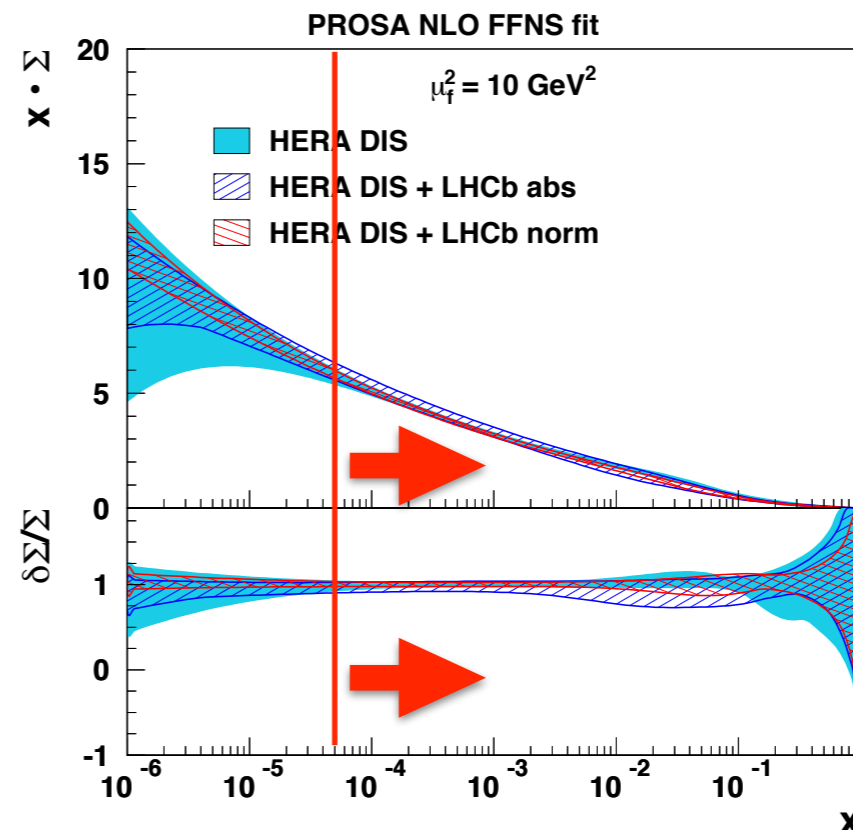
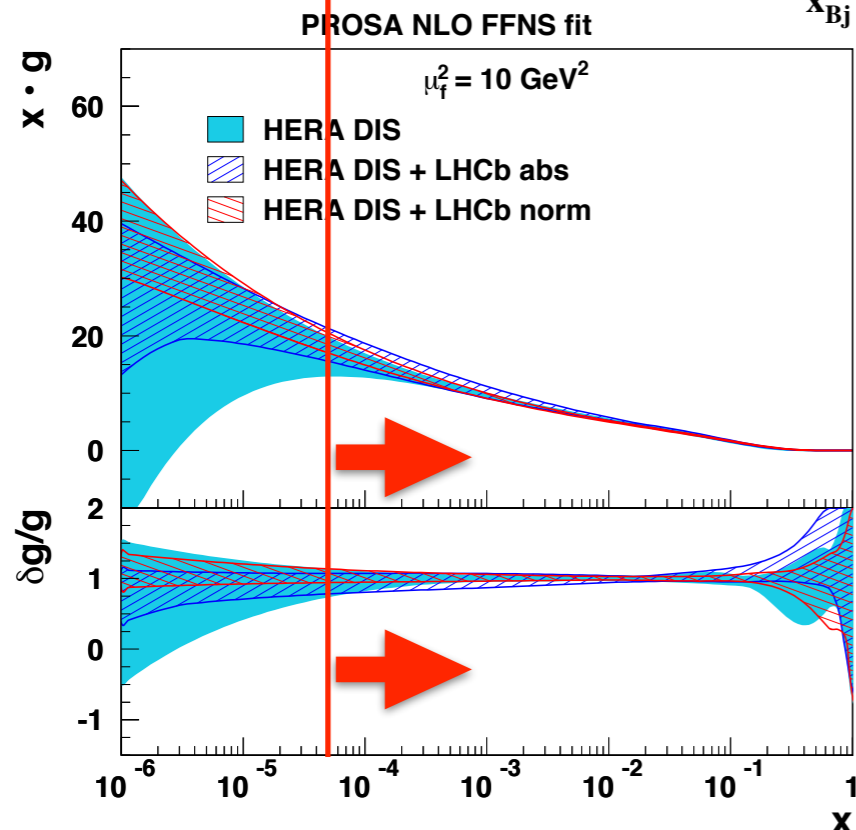


Perturbative region can not be extended to very low Q^2

Low $Q^2 \leftrightarrow$ low x_{Bj}

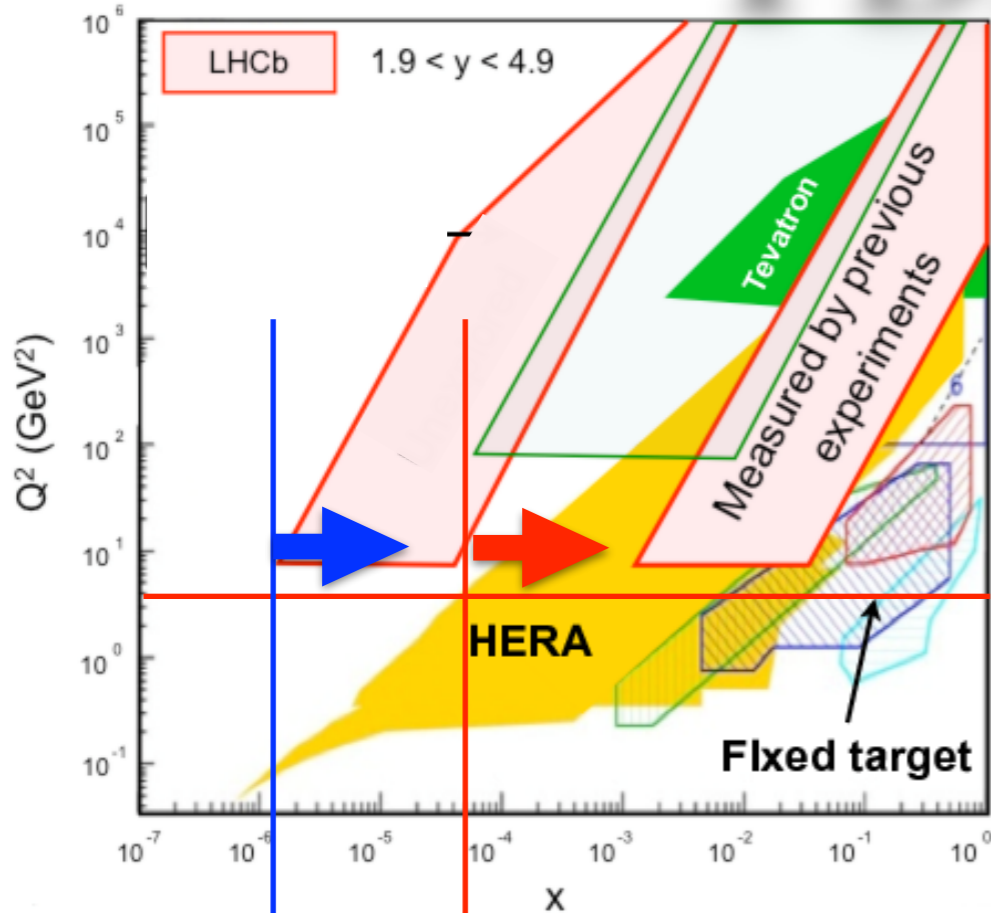
HERA data provides PDF info only down to $x_{Bj} \approx 10^{-5}$

Everything below - pure extrapolation



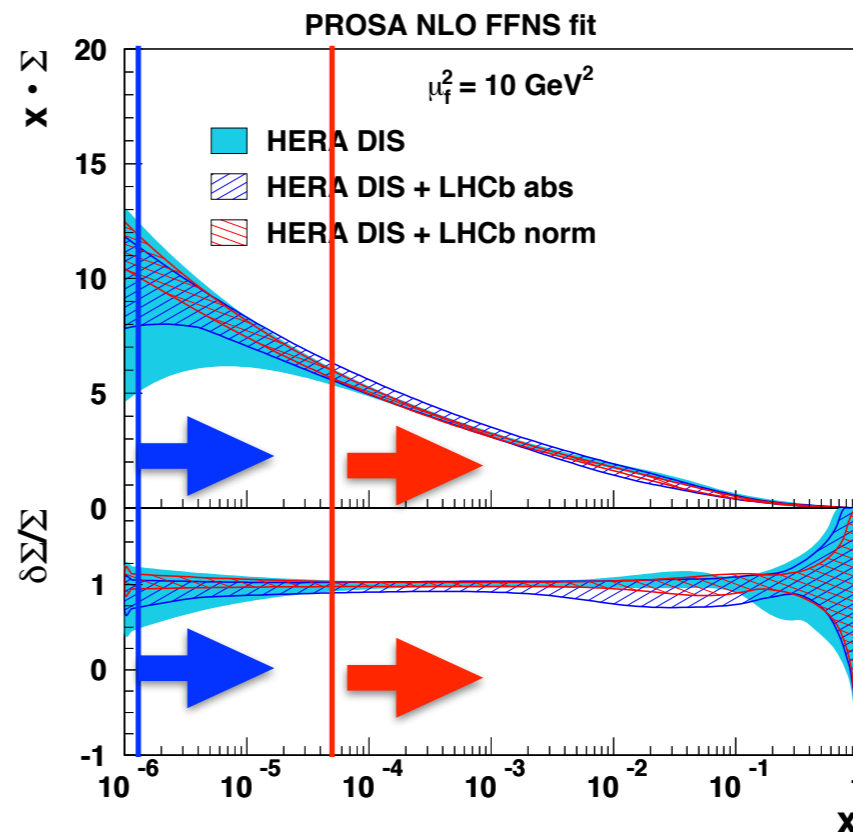
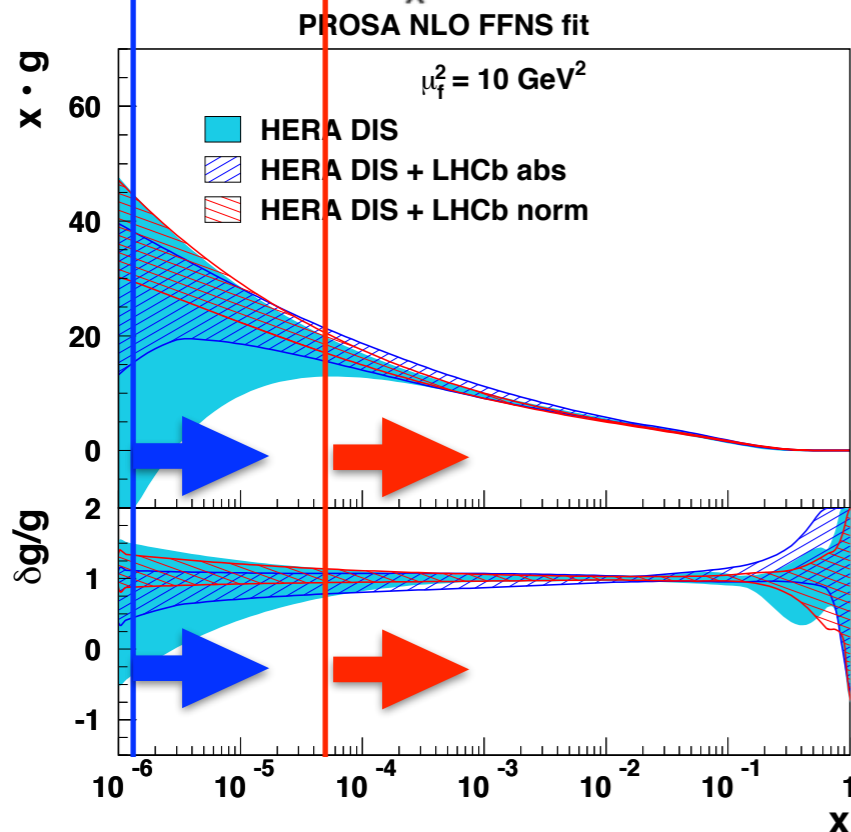
Eur.Phys.J. C75 (2015) no.8, 396, [arXiv:1503.04581]

PDFs at low x



Additional low-x data helps understanding proton structure!

Any potential input from VHEeP?

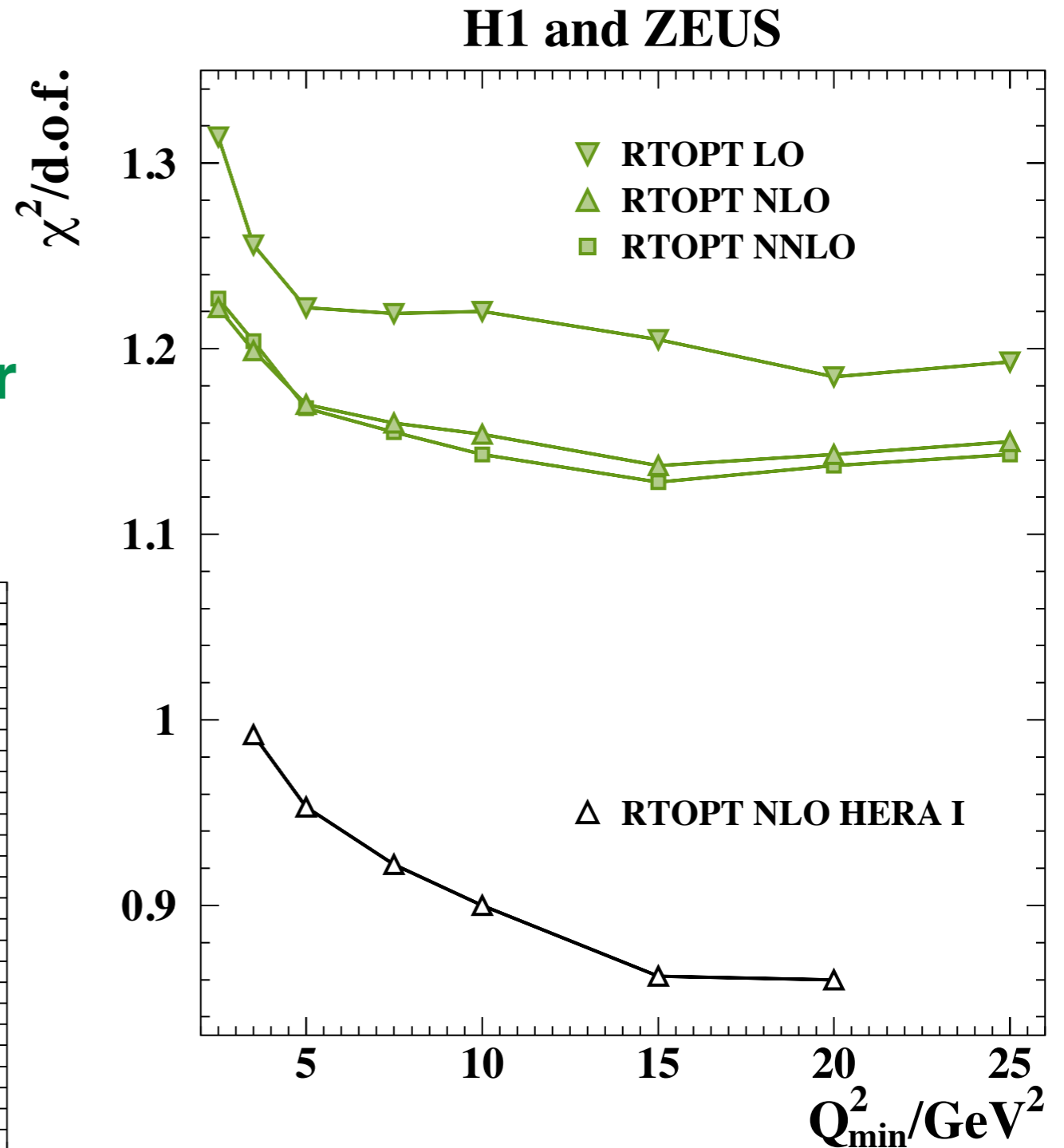
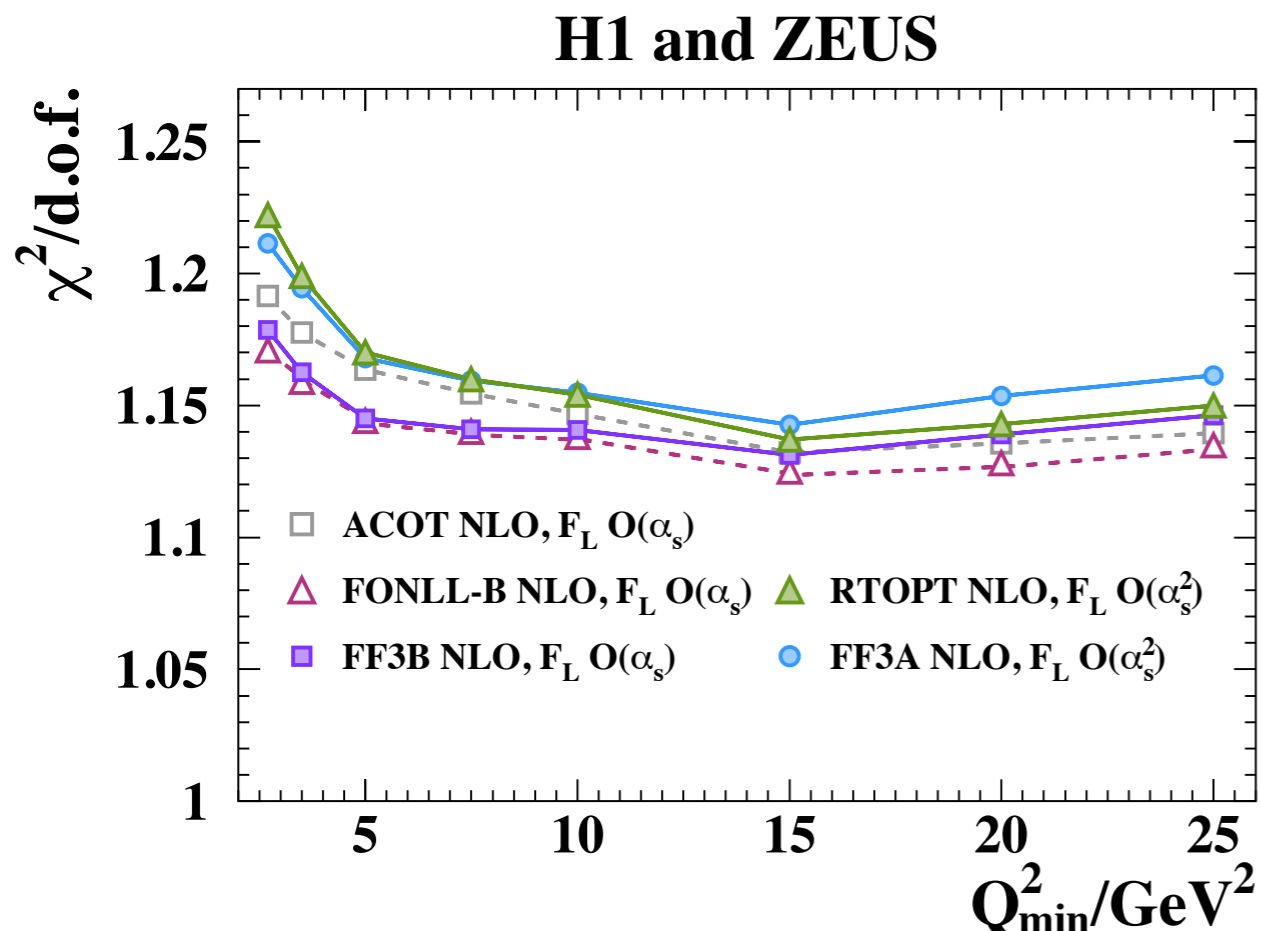


Eur.Phys.J. C75 (2015) no.8, 396, [arXiv:1503.04581]

Low- Q^2 data and pQCD

DGLAP data description
worsens at low Q^2

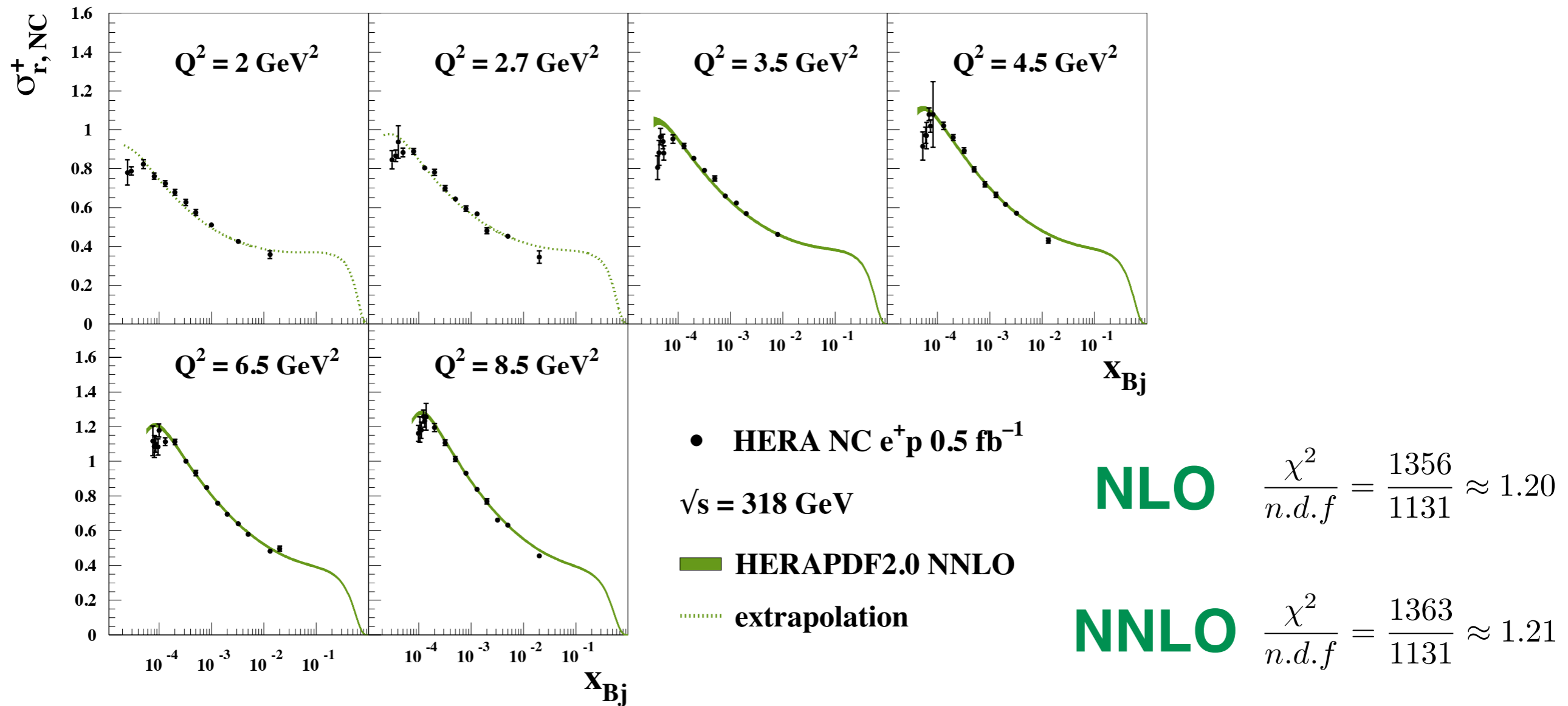
Effect independent of
HF scheme or **calculation order**



Eur.Phys.J. C75 (2015) no.12, 580, [[arXiv:1506.06042](https://arxiv.org/abs/1506.06042)]

Low x_{Bj} data and pQCD

Data at $Q^2 = [3.5, 15] \text{ GeV}^2$ cause $\sim 1/3$ of the excess in $\chi^2 / \text{n.d.f}$
 Rest - fluctuations overall full HERA kinematic region



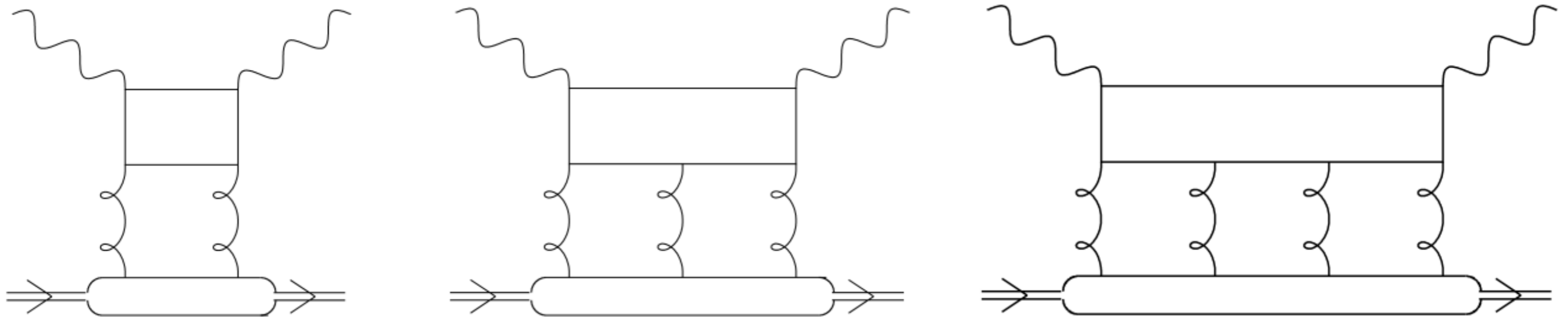
A possible solution, **a higher-twist correction**, was studied...

Higher-twist correction

The problem might be in absence of **higher-twist corrections** in the evolution equations

May be visualised as gluon leaders with recombining gluons

Eur.Phys.J. C17 (2000) 121-128, [\[hep-ph/0003042\]](https://arxiv.org/abs/hep-ph/0003042)



$$\sigma_{r,NC}^{\pm} = F_2 - \frac{y^2}{Y_+} F_L \quad \text{Cross section - a linear combination of structure functions}$$

Introduce simple twist-4 correction factor to each of st. functions

Higher-twist terms are expected to contribute to F_L ...

$$F_L \frac{4\pi^2\alpha}{Q^2(1-x)} = \sigma_L$$

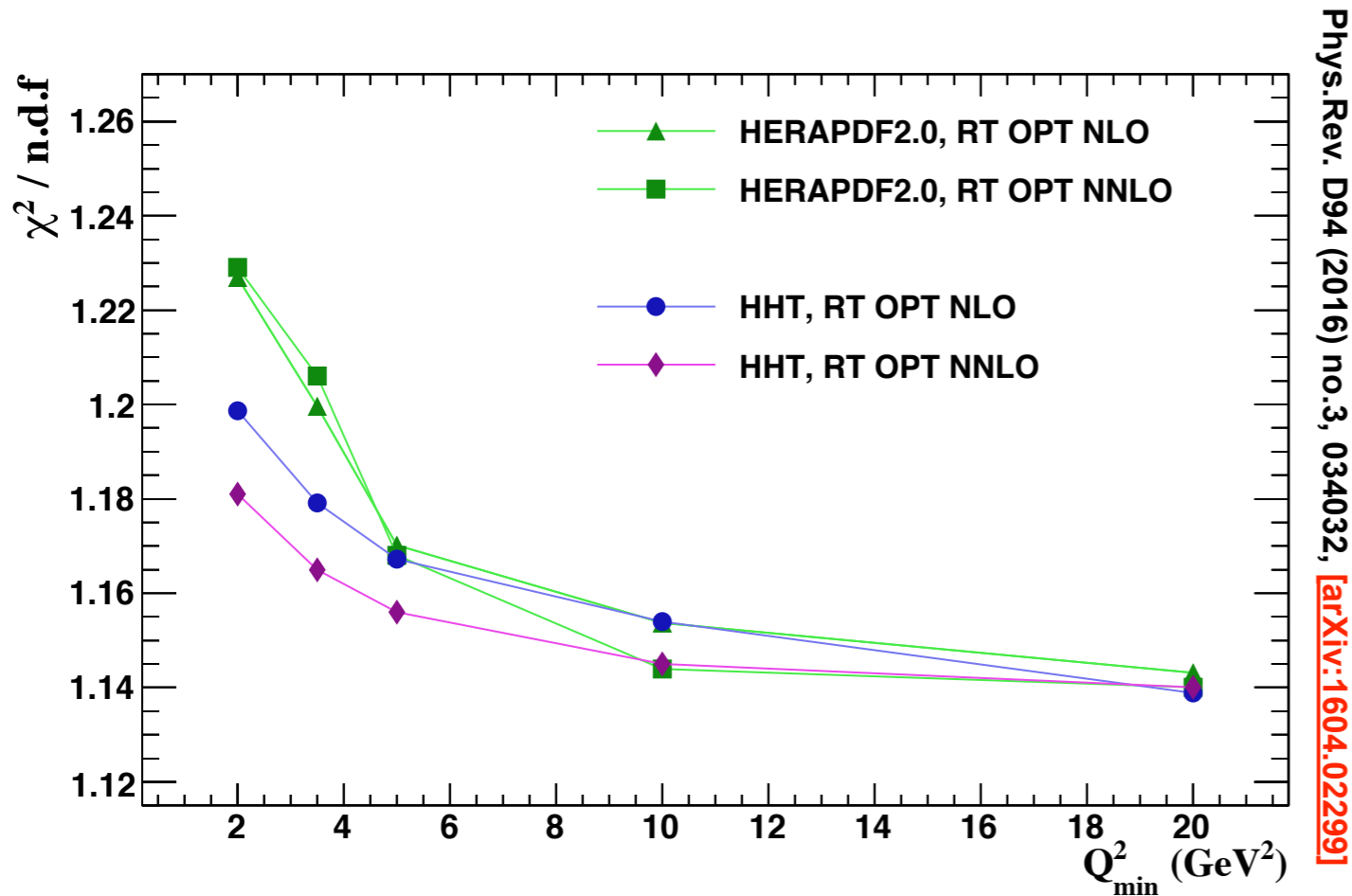
...and cancel for F_2

$$F_2 \frac{4\pi^2\alpha}{Q^2(1-x)} = \sigma_T + \sigma_L$$

$$F_2^{HT} = F_2^{DGLAP} \left(1 + \frac{A_2^{HT}}{Q^2}\right)$$

$$F_L^{HT} = F_L^{DGLAP} \left(1 + \frac{A_L^{HT}}{Q^2}\right)$$

Higher-twist-correction effect



Phys.Rev. D94 (2016) no.3, 034032, [arXiv:1604.02299]

Q_{\min}^2 -dependence curve
flattens substantially

HHT@ F_L : **NLO**
NNLO

$$\frac{\chi^2}{n.d.f.} \approx 1.18$$

$$\Delta\chi^2 = 27$$

$$A_L^{HT} = 4.2 \pm 0.7 \text{ GeV}^2$$

$$\frac{\chi^2}{n.d.f.} \approx 1.16$$

$$\Delta\chi^2 = 47$$

$$A_L^{HT} = 5.5 \pm 0.6 \text{ GeV}^2$$

HHT@ F_2 : **NLO**
no significant improvement **NNLO**

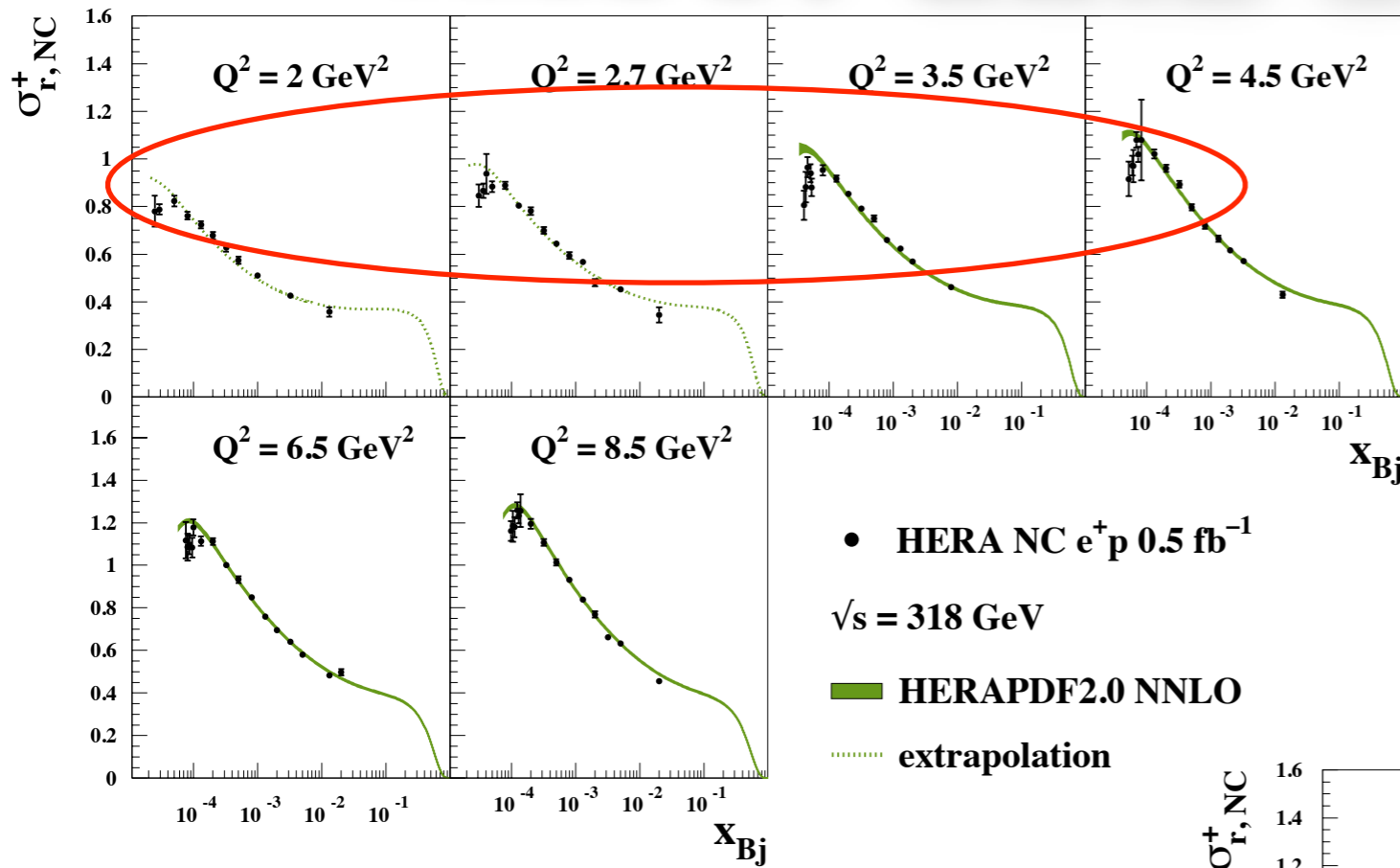
$$\frac{\chi^2}{n.d.f.} \approx 1.20$$

corr. factors

$$\frac{\chi^2}{n.d.f.} \approx 1.20$$

consistent with 0

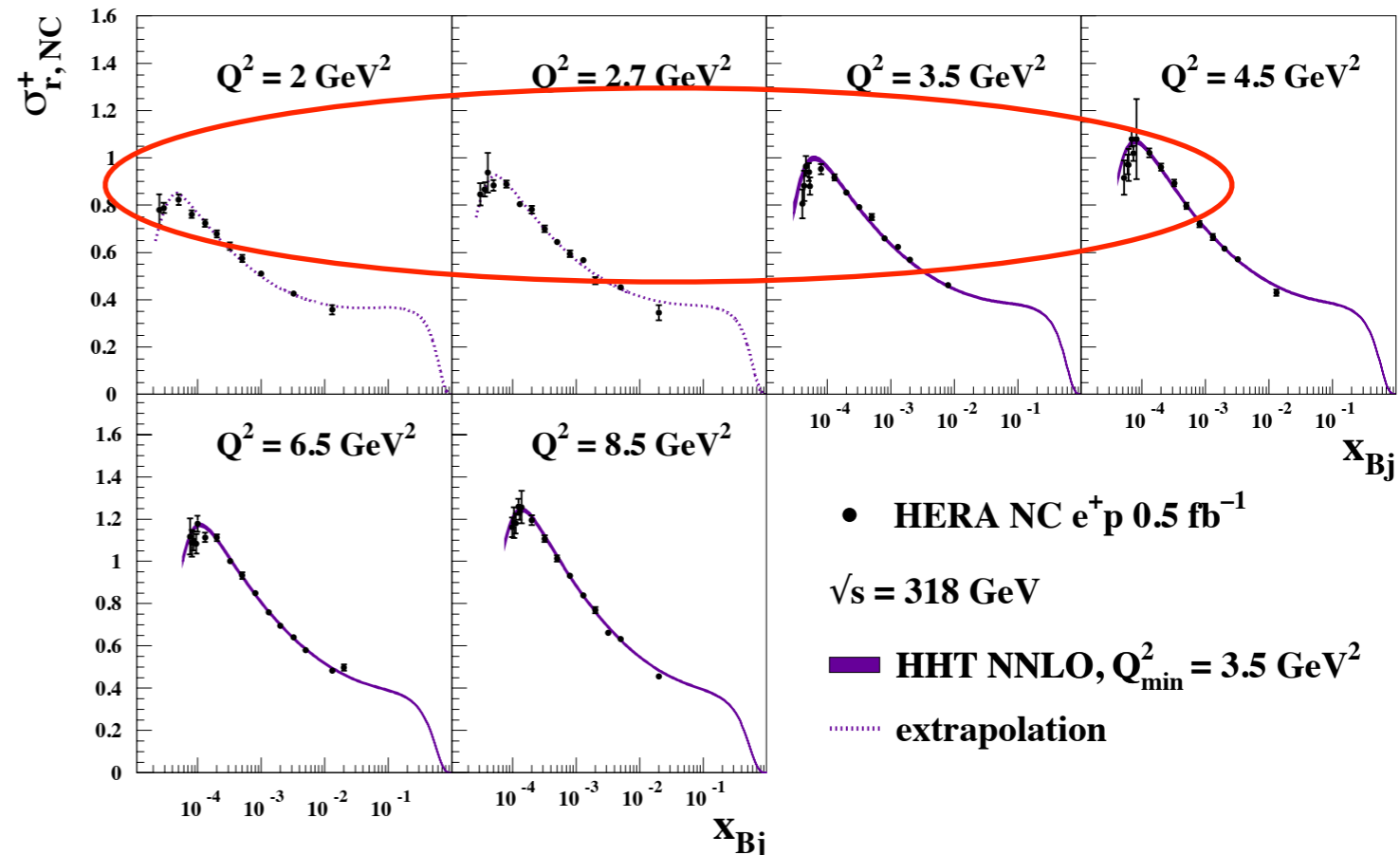
HHT: data description



HERAPDF systematically undershoots low-x data

HHT improves low-x-data description significantly!

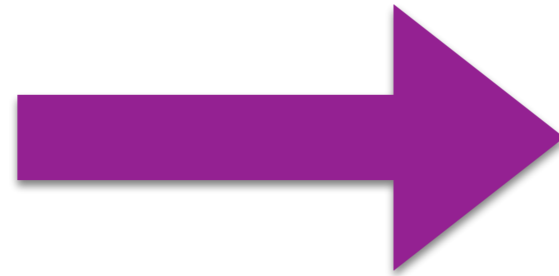
Predictions describe data even below 3.5 GeV^2 !



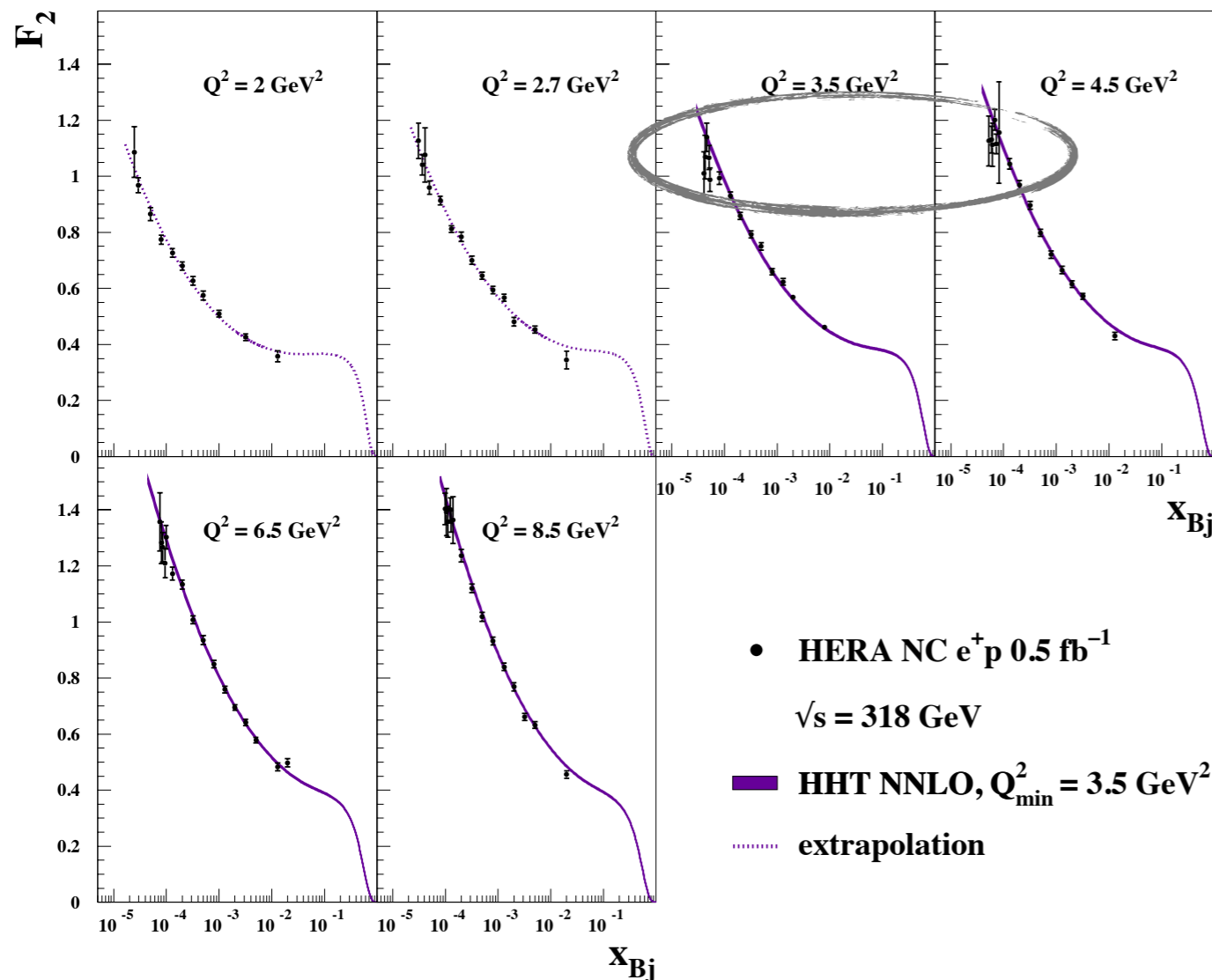
HHT-prediction components

HHT predictions seem to be doing a very good job! some details?

$$\sigma_{r,NC}^{\pm} = F_2 - \frac{y^2}{Y_+} F_L$$



$$\sigma_{r,NC}^{\pm} = F_2 - \frac{y^2}{Y_+} F_L \left(1 + \frac{A_L^{HT}}{Q^2} \right)$$



F_2 is extracted from σ_r :

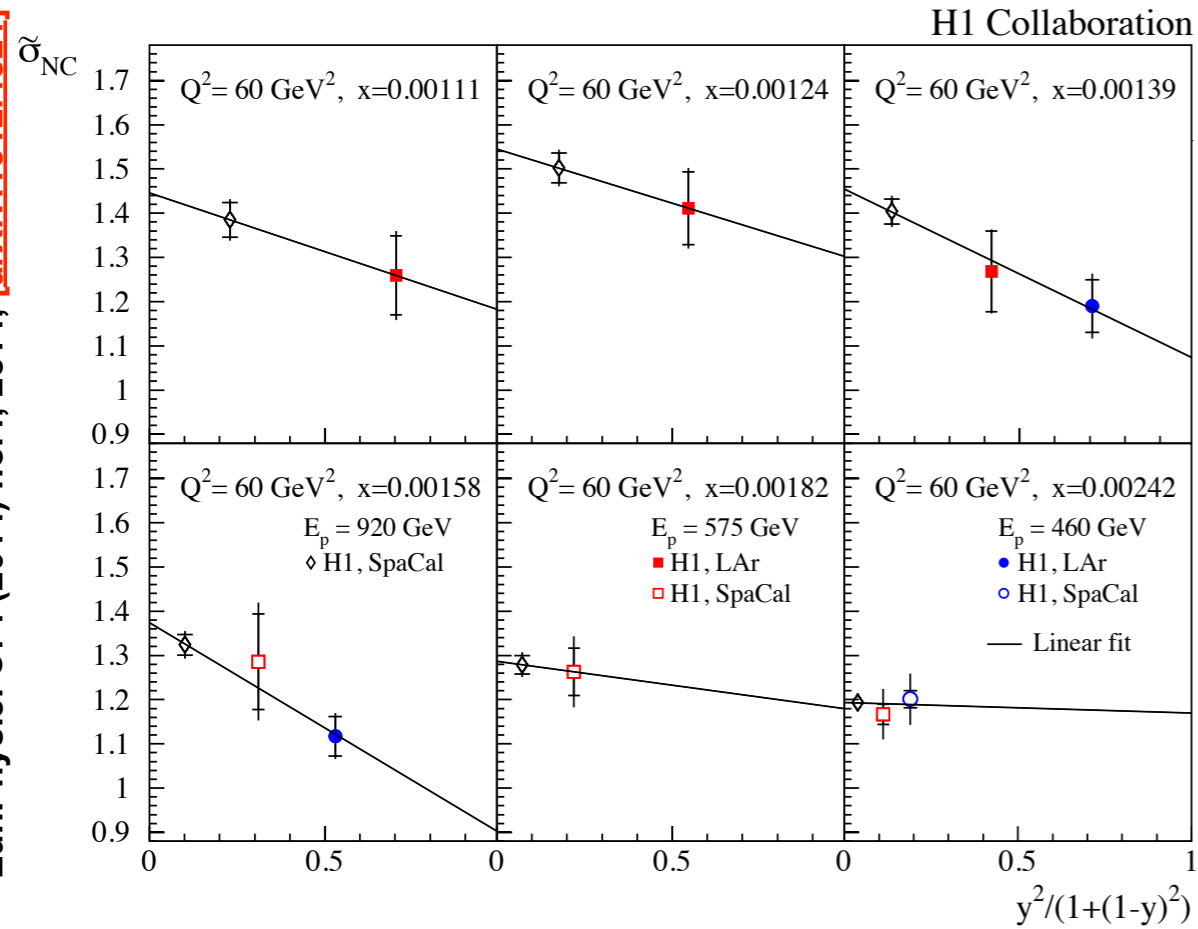
$$F_2^{extr} = F_2^{pred} \frac{\sigma_r^{meas}}{\sigma_r^{pred}}$$

The description is reasonably good...

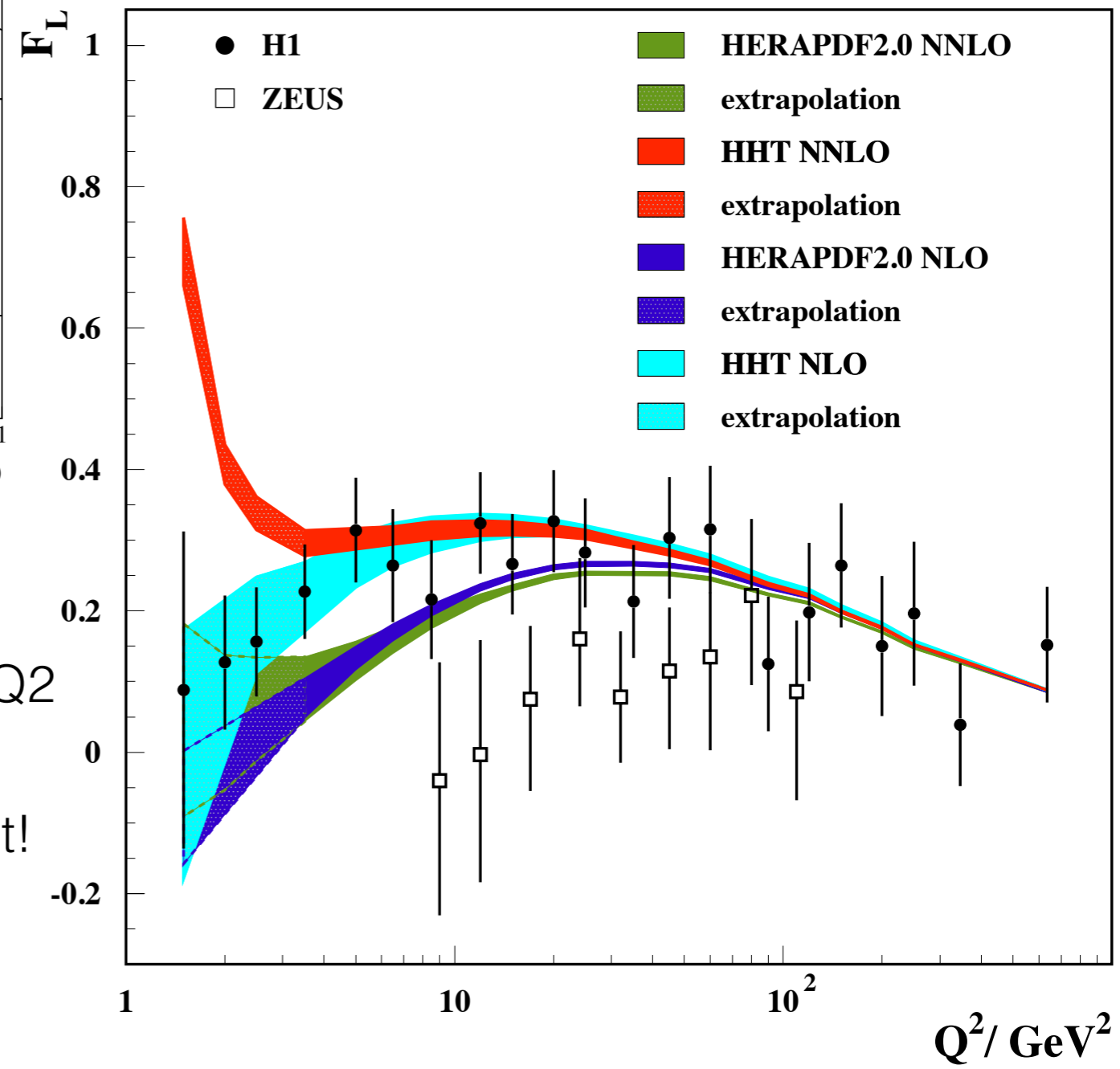
Warning:
a model-dependent extraction!

HHT-prediction components

Eur.Phys.J. C74 (2014) no.4, 2814, [arXiv:1312.4821]



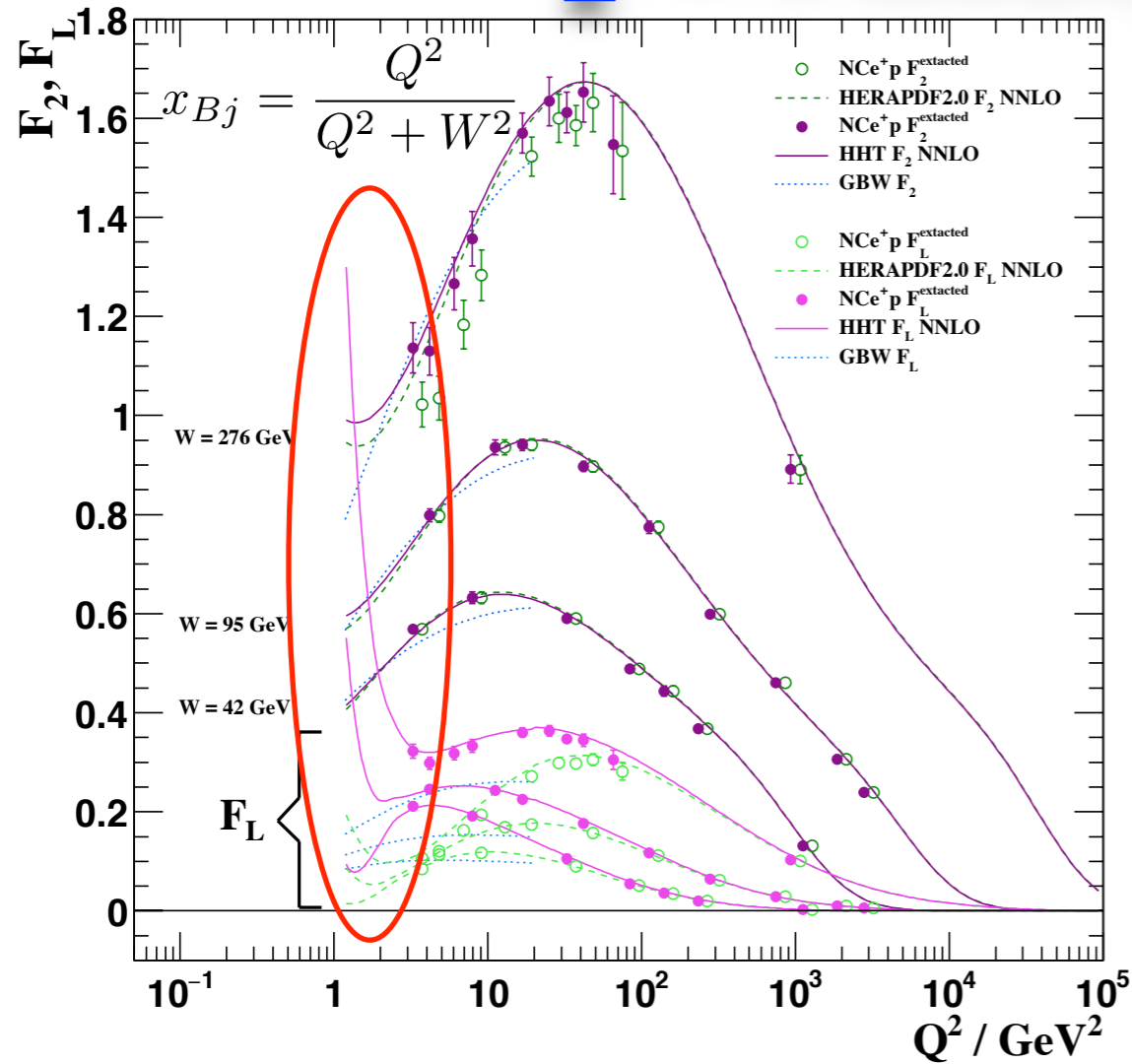
Model-independent F_L measurements exists:
reduced E_p runs!



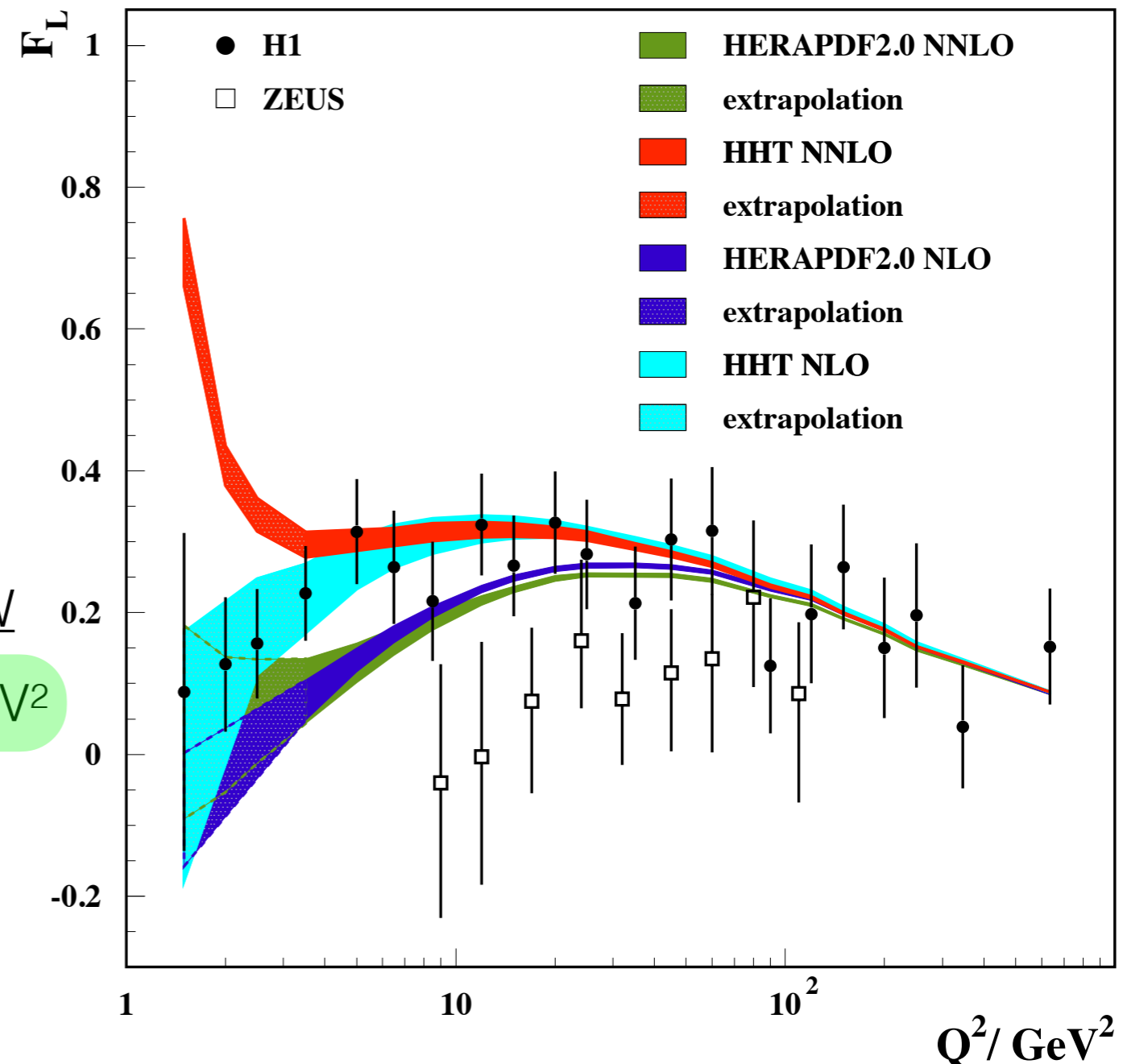
Phys.Rev. D94 (2016) no.3, 034032, [arXiv:1604.02299]

F_L @NNLO shows a huge upturn at small Q^2
Direct F_L measurements **do not confirm** it!

HHT-prediction components



Model-independent F_L measurements exists:
reduced E_p runs!



Phys.Rev. D94 (2016) no.3, 034032, [arXiv:1604.02299]

The upturn is more pronouncing at high W

Still reasonable predictions for $Q^2 > 3.5 \text{ GeV}^2$

More investigations required for reasonable F_L predictions!



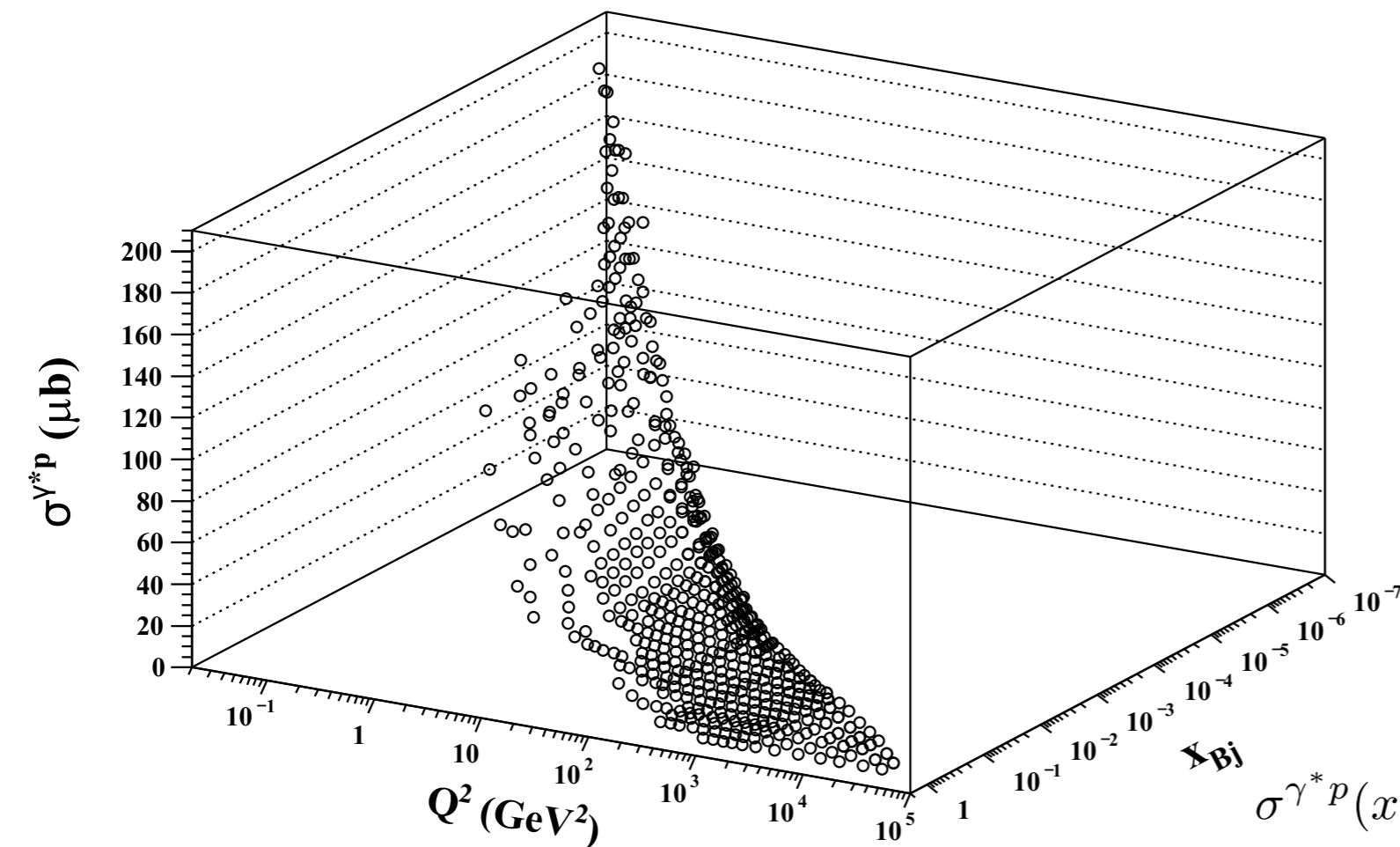
What if I told you

there is physics below 3.5 GeV^2

NC e+p from different angles

$$F_2^{extr} = F_2^{pred} \frac{\sigma_r^{meas}}{\sigma_r^{pred}} \quad \text{will be used further}$$

Predictions for extraction: $Q \geq 3.5 \text{ GeV}^2 \rightarrow \text{HHT}$; $Q^2 < 3.5 \text{ GeV}^2 \rightarrow \text{BKS}$



BKS pheno. model:
 $F_L \propto Q^4$ as $Q^4 \rightarrow 0$,
 Photon-gluon fusion mechanism,
 Soft Pomeron exchange assumed

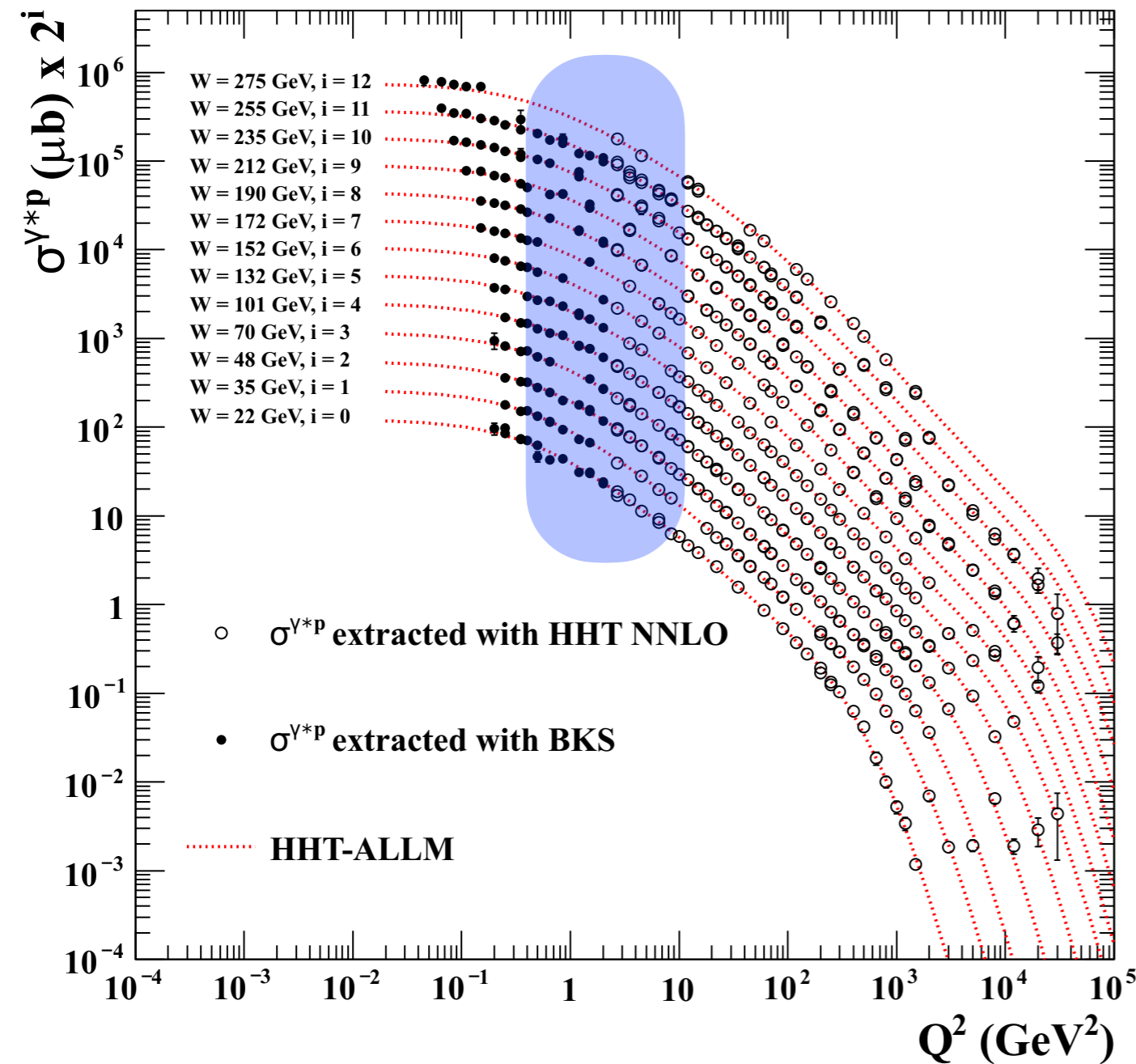
Z.Phys. C74 (1997) 297-306, [[hep-ph/9603230](https://arxiv.org/abs/hep-ph/9603230)]

σ^{γ^*p} - a useful way of F_2 representation

$$\sigma^{\gamma^*p}(x_{Bj}, Q^2) = \frac{4\pi^2\alpha(Q^2 + (2x_{Bj}m_p)^2)}{Q^4(1 - x_{Bj})} F_2(x_{Bj}, Q^2)$$

pQCD breaks at low Q^2 but nature does not!

ALLM: full data description



ALLM model:

23-parameter *ansatz*

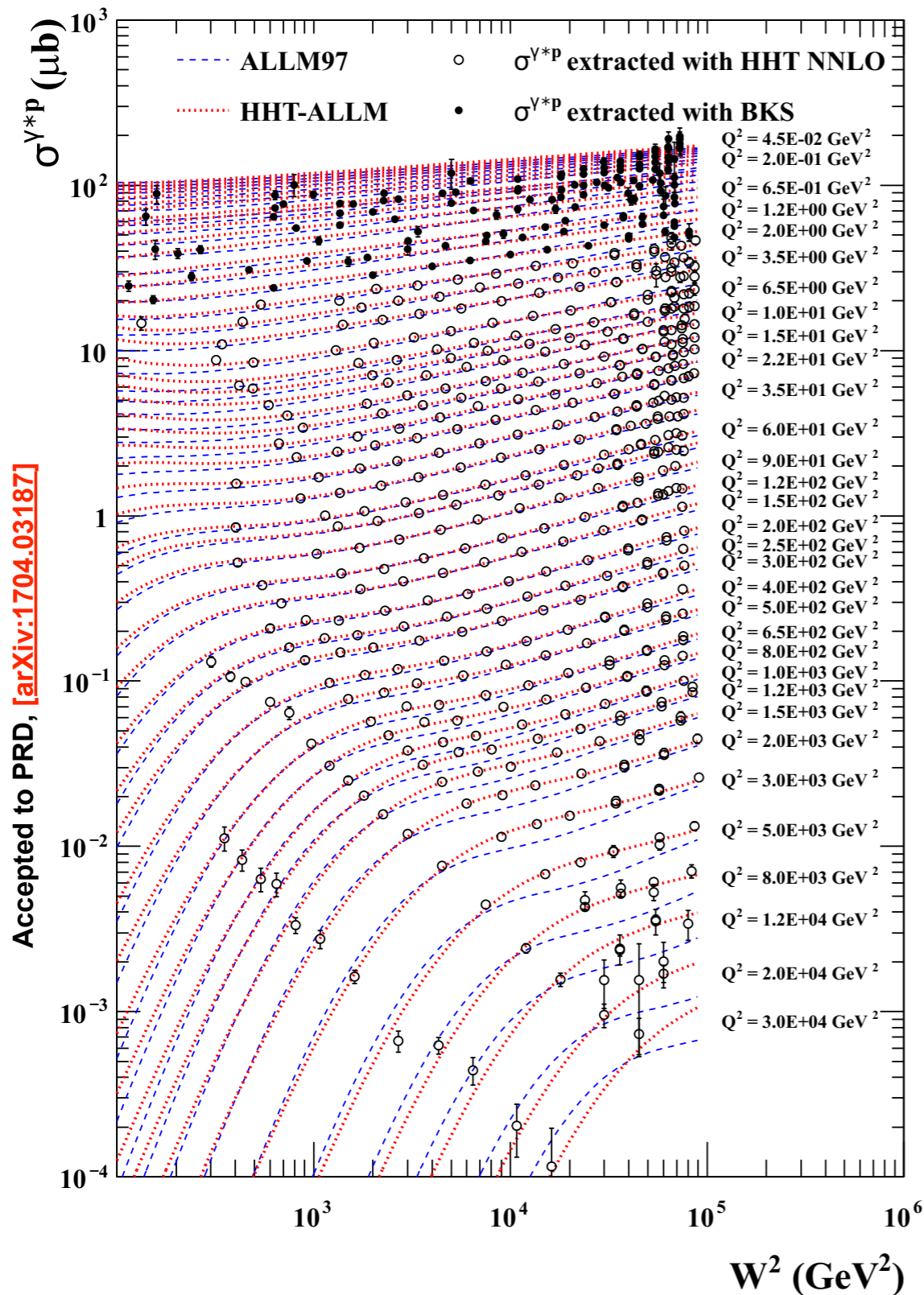
contains Pomeron and Reggeon exchange contributions

$$F_2 = \frac{Q^2}{Q^2 + m_0^2} (F_2^{IP} + F_2^{IR})$$

$$\frac{\chi^2}{n.d.f} \approx 1.06$$

Accepted to PRD, [\[arXiv:1704.03187\]](https://arxiv.org/abs/1704.03187)

ALLM: full data description



ALLM97 used only early HERA data

HHT-ALLM recent update with full HERA data

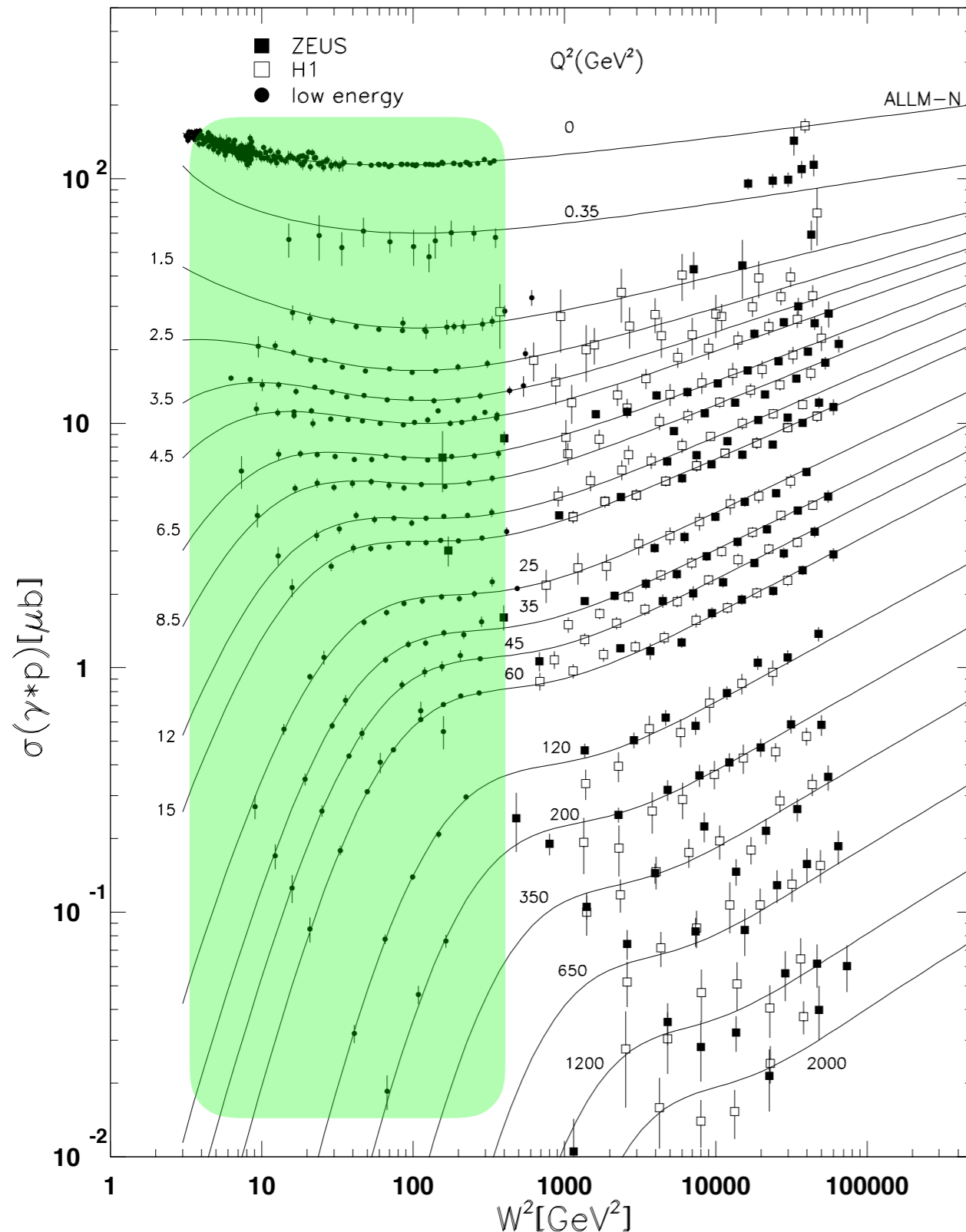
HHT-ALLM describes data remarkably well!

$$\frac{\chi^2}{n.d.f} \approx 1.06$$

Note the **smooth trend** established by the data!

ALLM: full data description

DESY-97-251, [\[hep-ph/9712415\]](https://arxiv.org/abs/hep-ph/9712415)

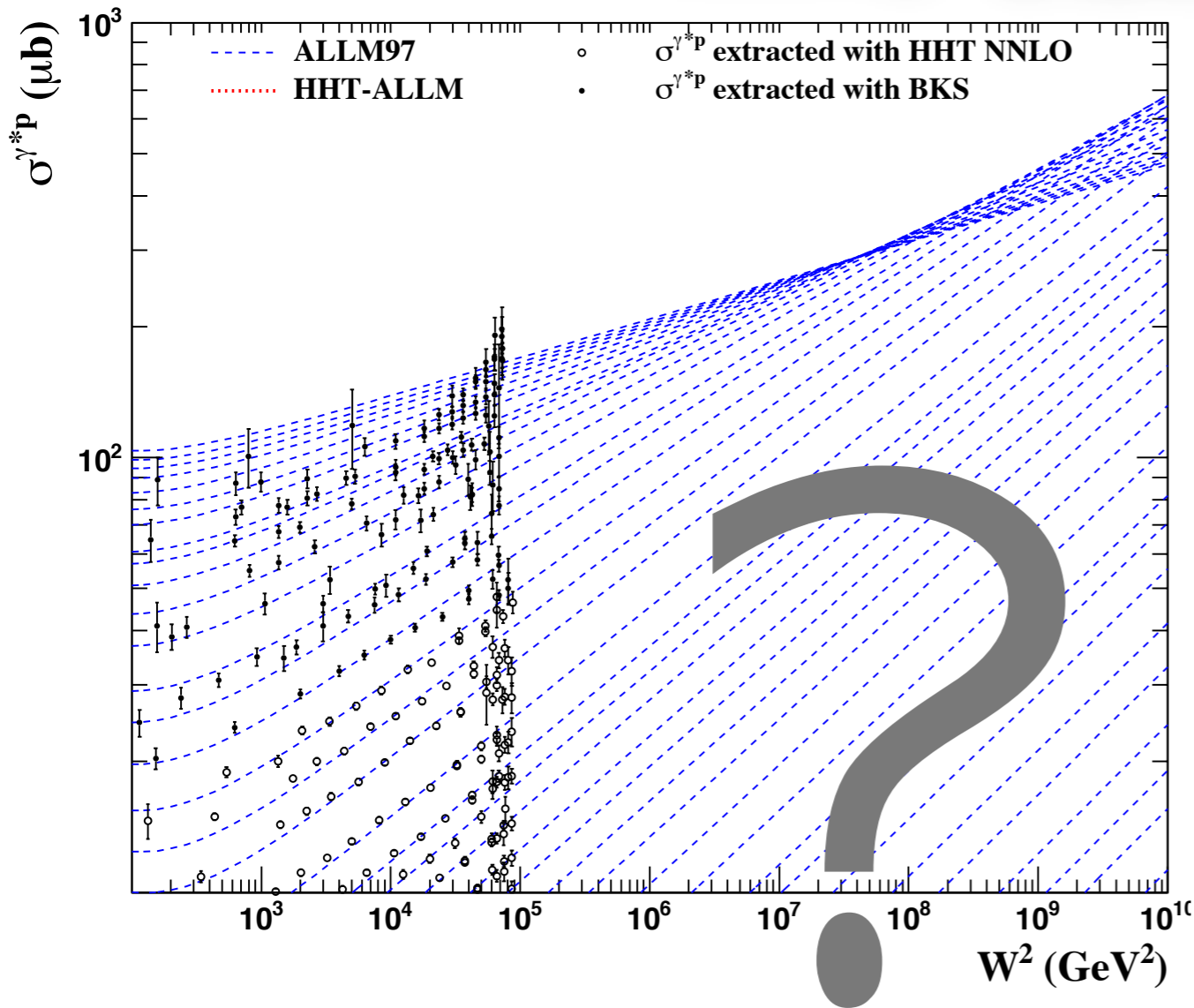


Non-trivial structures observed
at **Fixed Target** at high x

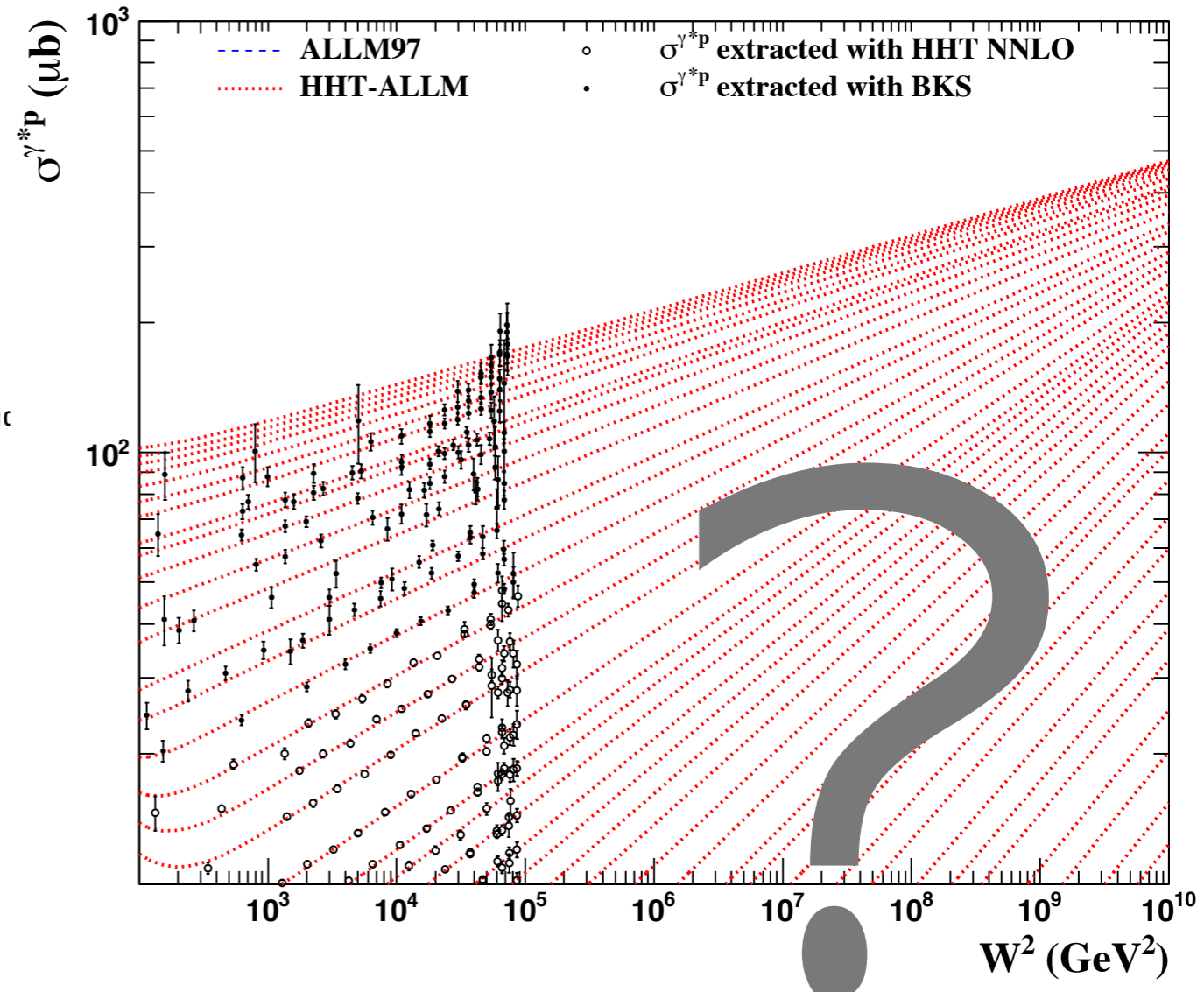
Successfully described by
ALLM97

$$W^2 = Q^2 \left(\frac{1}{x_{Bj}} - 1 \right) + m_P^2$$

ALLM extrapolation



Terra incognita at low x
to be revealed
by future experiments

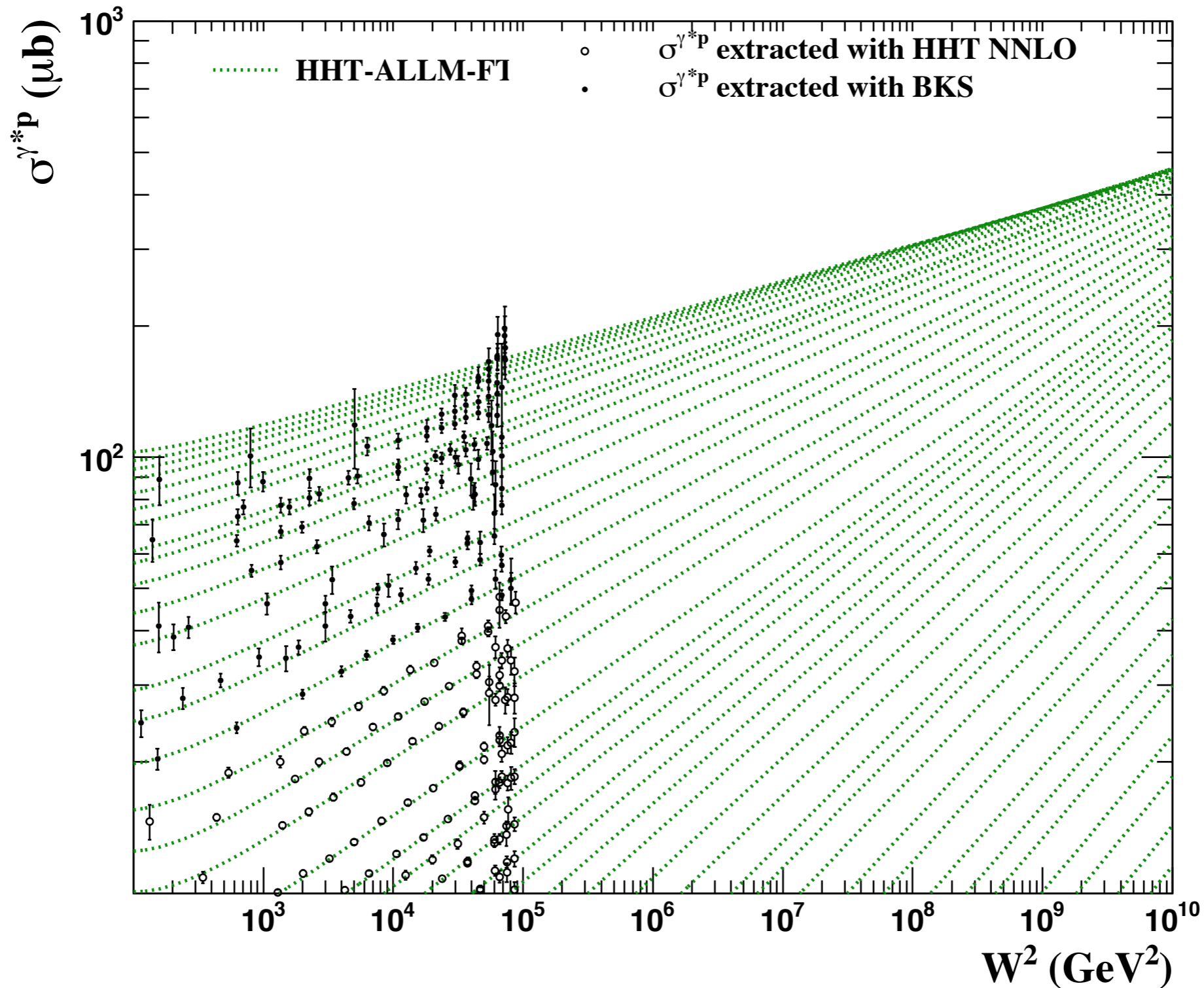


Any new

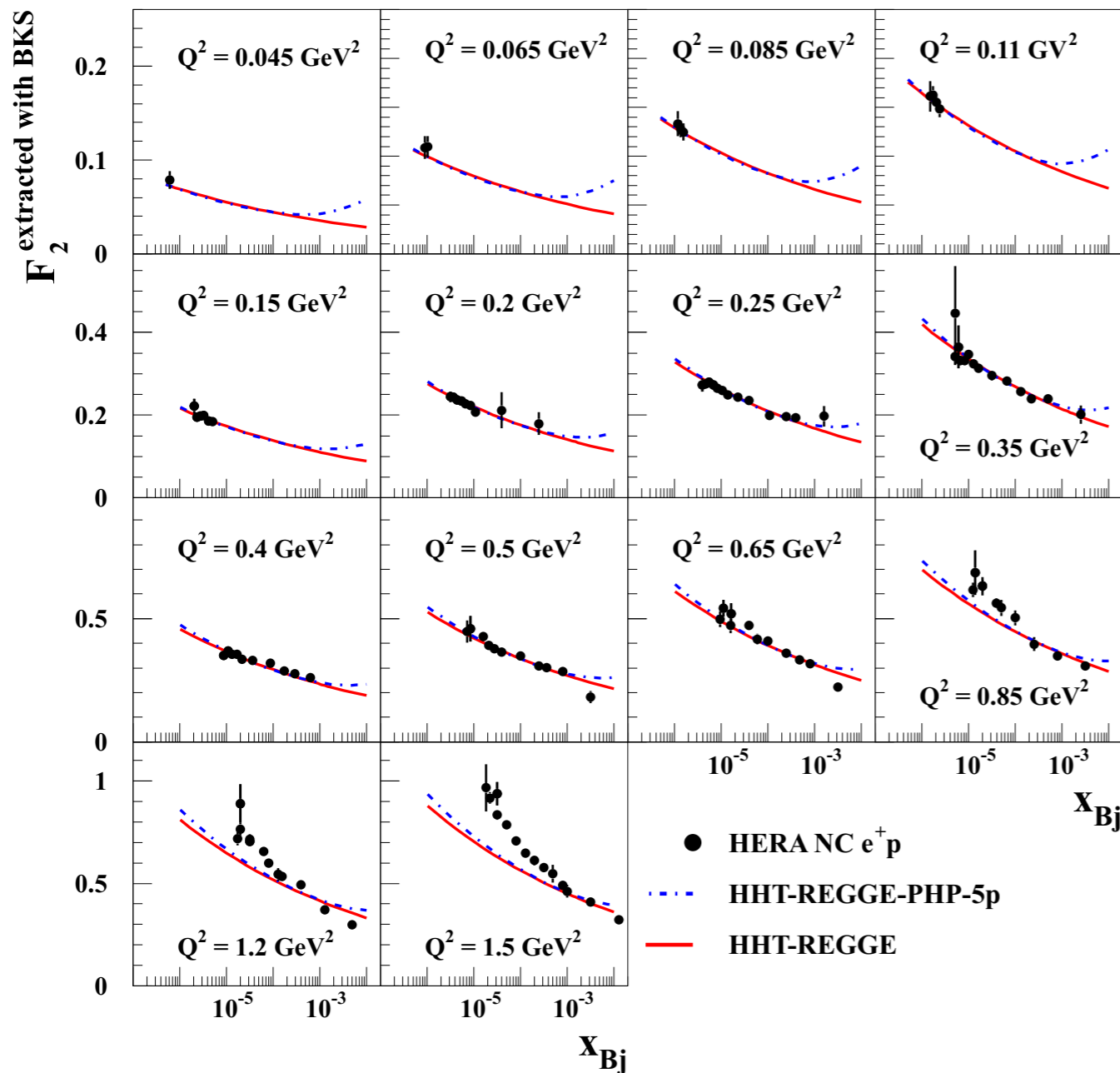
particular structures?

$$W^2 = Q^2 \left(\frac{1}{x_{Bj}} - 1 \right) + m_P^2$$

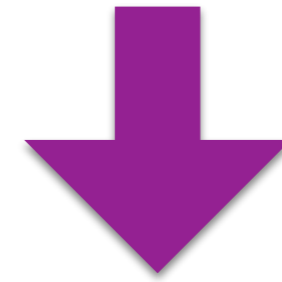
ALLM extrapolation



REGGE fit



Low-x data was cross-calibrated in the latest combination



HHT-REGGE - new Regge fit was performed (only *IP*)!

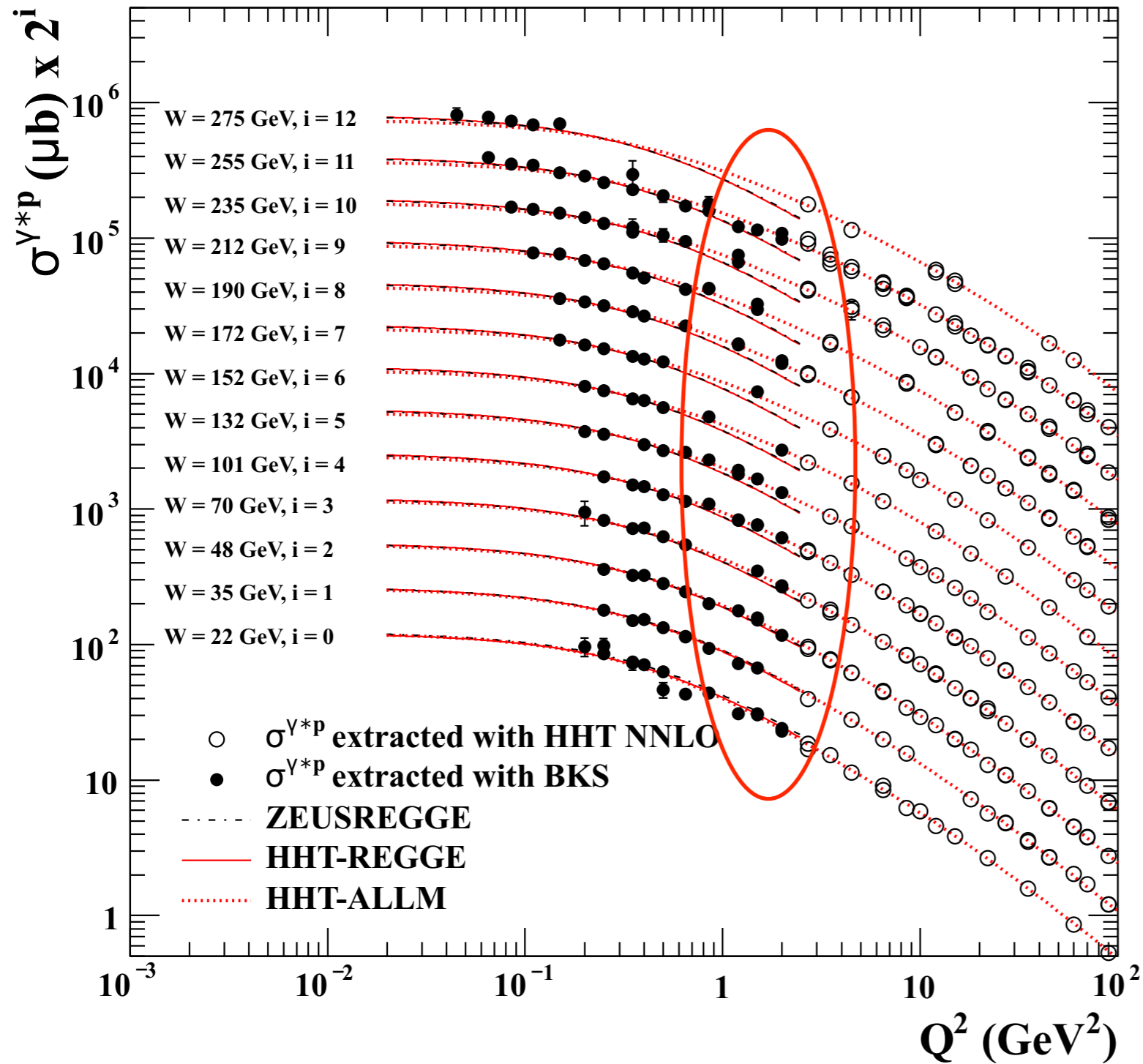
$$Q^2 \leq 0.65 \text{ GeV}^2$$

HHT-REGGE-PHP-5 - done adding PhP data (+IR term)!

FT doesn't seem to help...

$$F_2(x_{Bj}, Q^2) = \frac{Q^2}{4\pi^2\alpha} \cdot \frac{M_0^2}{M_0^2 + Q^2} \cdot \left(A_{IP} \left(\frac{Q^2}{x_{Bj}} \right)^{\alpha_{IP}(0)-1} + \cancel{A_{IR} \left(\frac{Q^2}{x_{Bj}} \right)^{\alpha_{IR}(0)-1}} \right)$$

REGGE fit

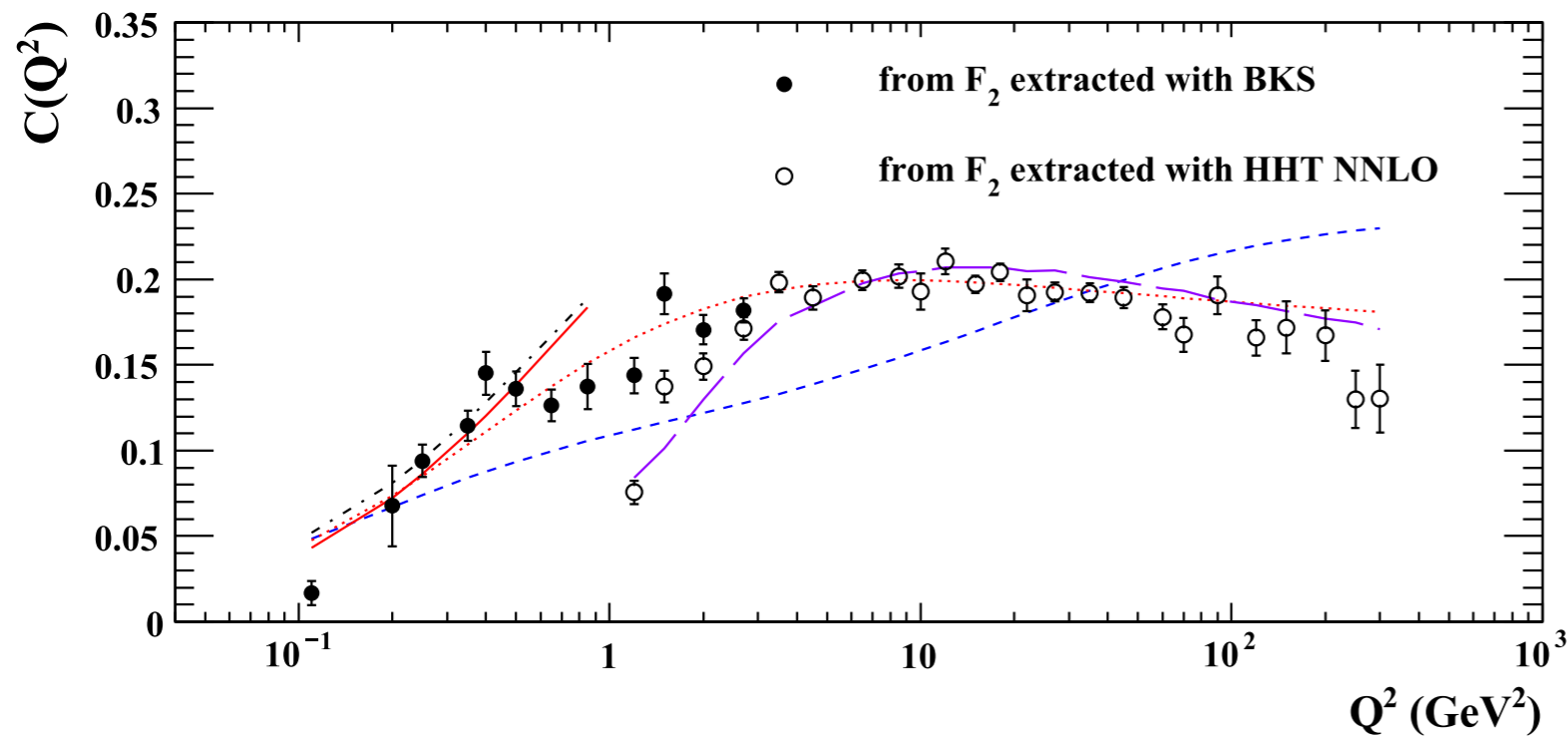
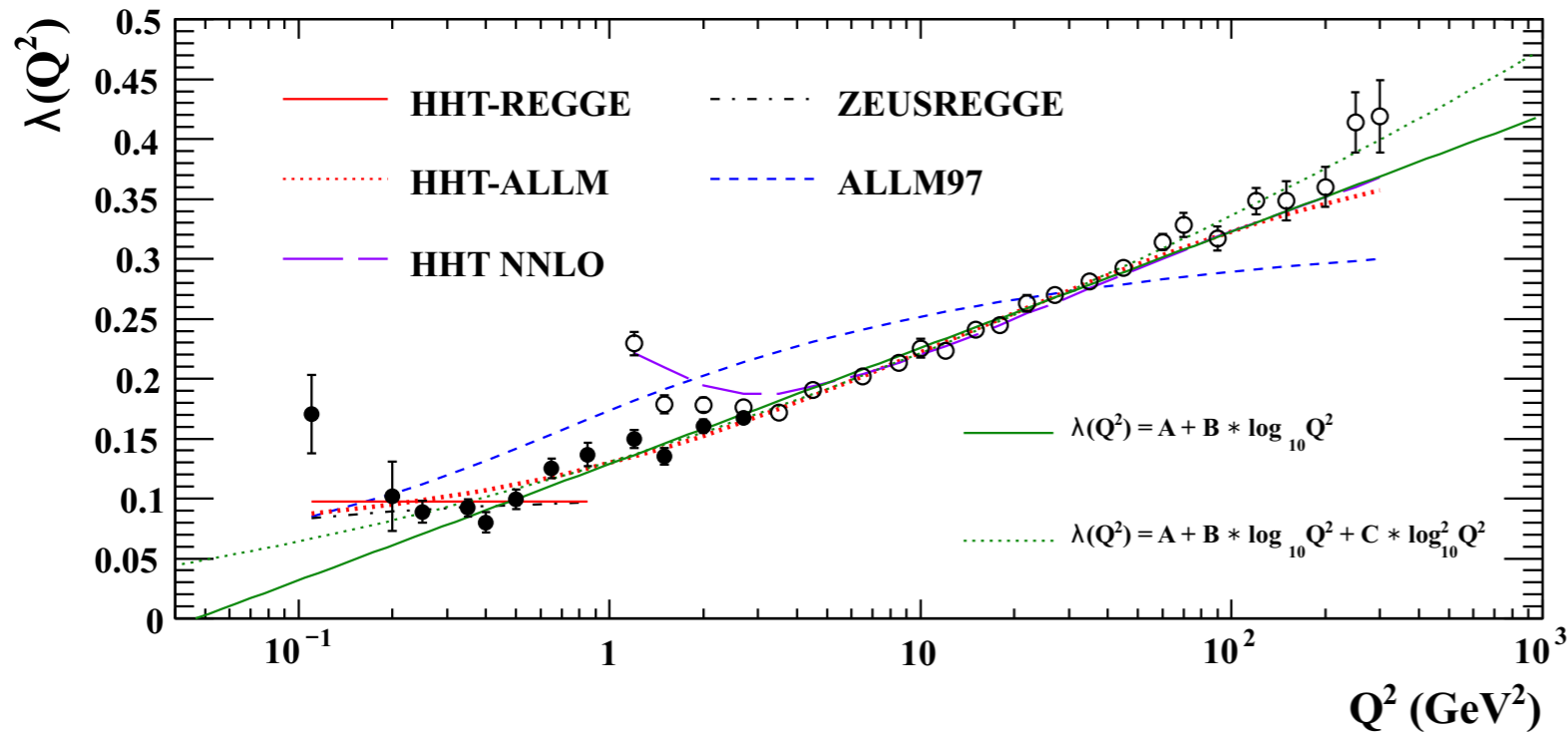


Regge diverges from data as $x_{Bj} \rightarrow 0$

Lacking data at high W (low x_{Bj})!

$$W^2 = Q^2 \left(\frac{1}{x_{Bj}} - 1 \right) + m_P^2$$

Characteristics of F_2



At fixed Q^2 the F_2 can be described by LO pQCD approx.: $F_2 = C(Q^2)x_{Bj}^{-\lambda(Q^2)}$

Low Q^2 : soft Pomeron

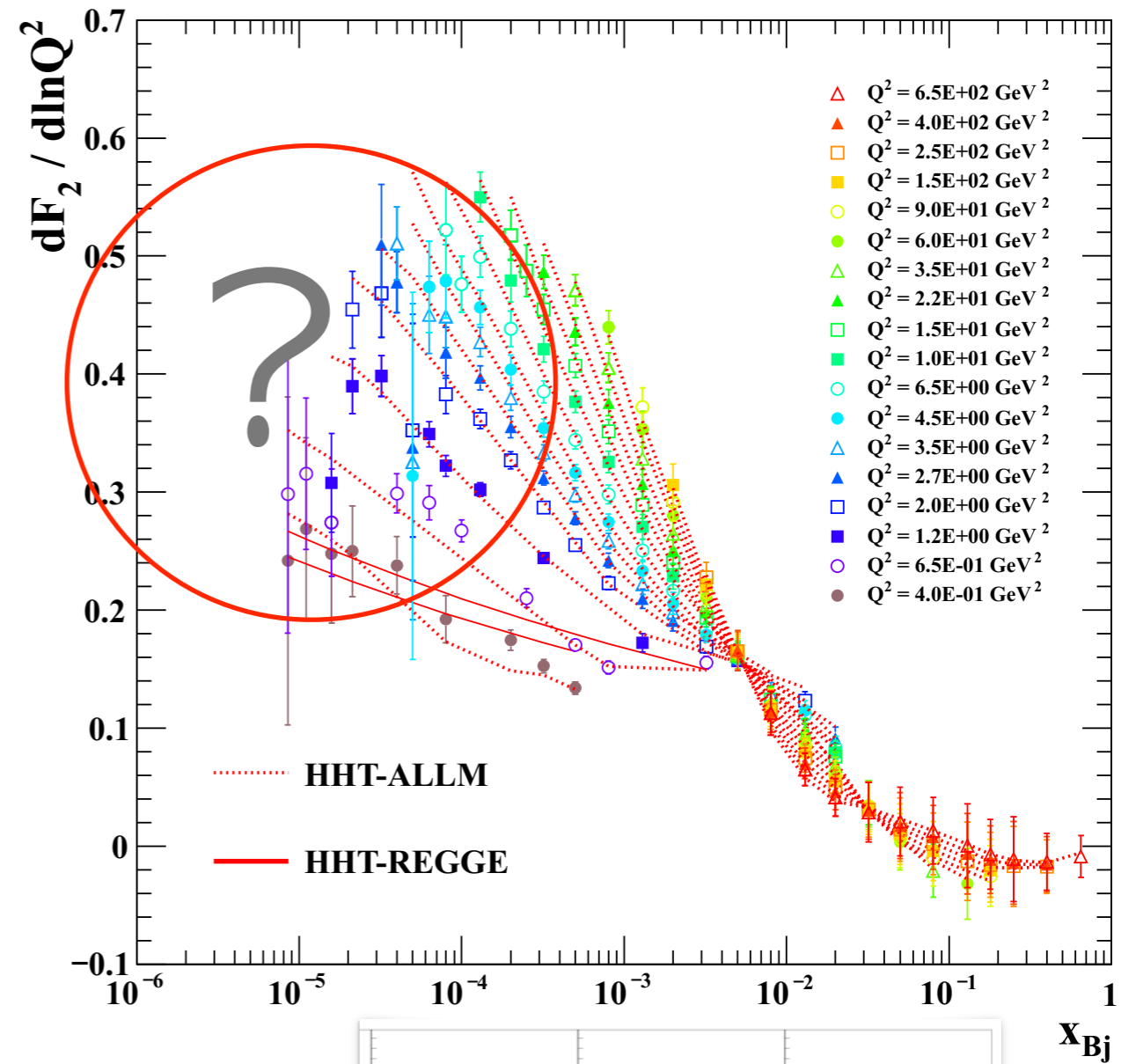
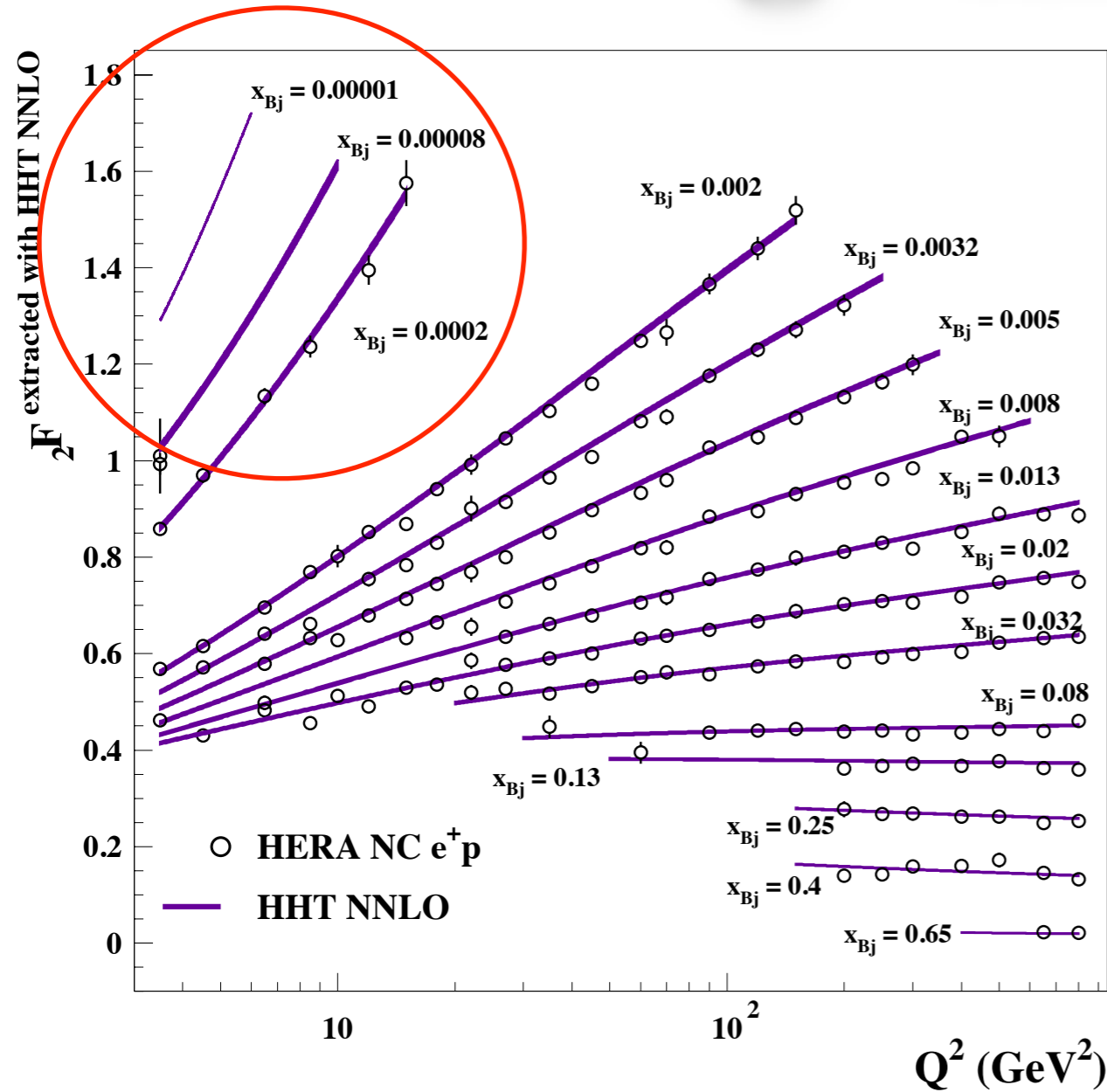


$$\lambda \approx const$$

High Q^2 : "effective" Pomeron

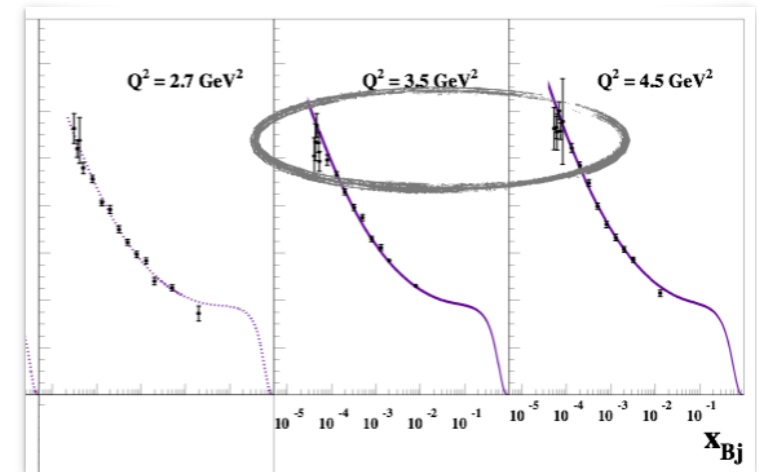
Note: description by simple polynomials!

Scaling violation in DIS

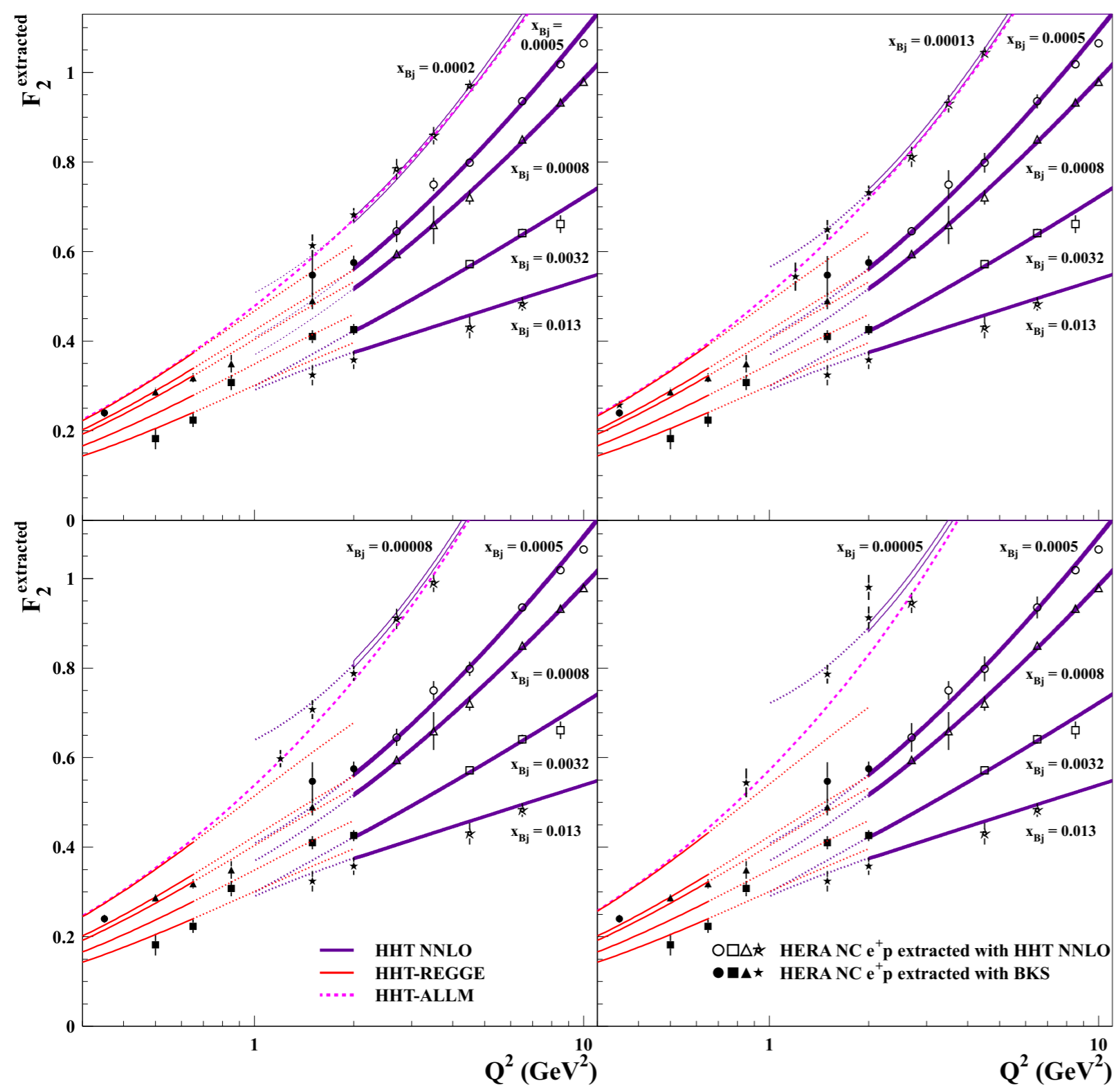


Statistical limitations at low x_{Bj}

Fluctuations? Something more significant?..



When pQCD meets Regge



Gap between pQCD and Regge grows as $x_{Bj} \rightarrow 0$

Does nature have any preferences?..

...and, whose side are you on?



**Side?! I am on nobody's side,
because nobody is on my side!**

Summary

HERA provided reach possibilities of studying nature

Proton structure

pQCD tests

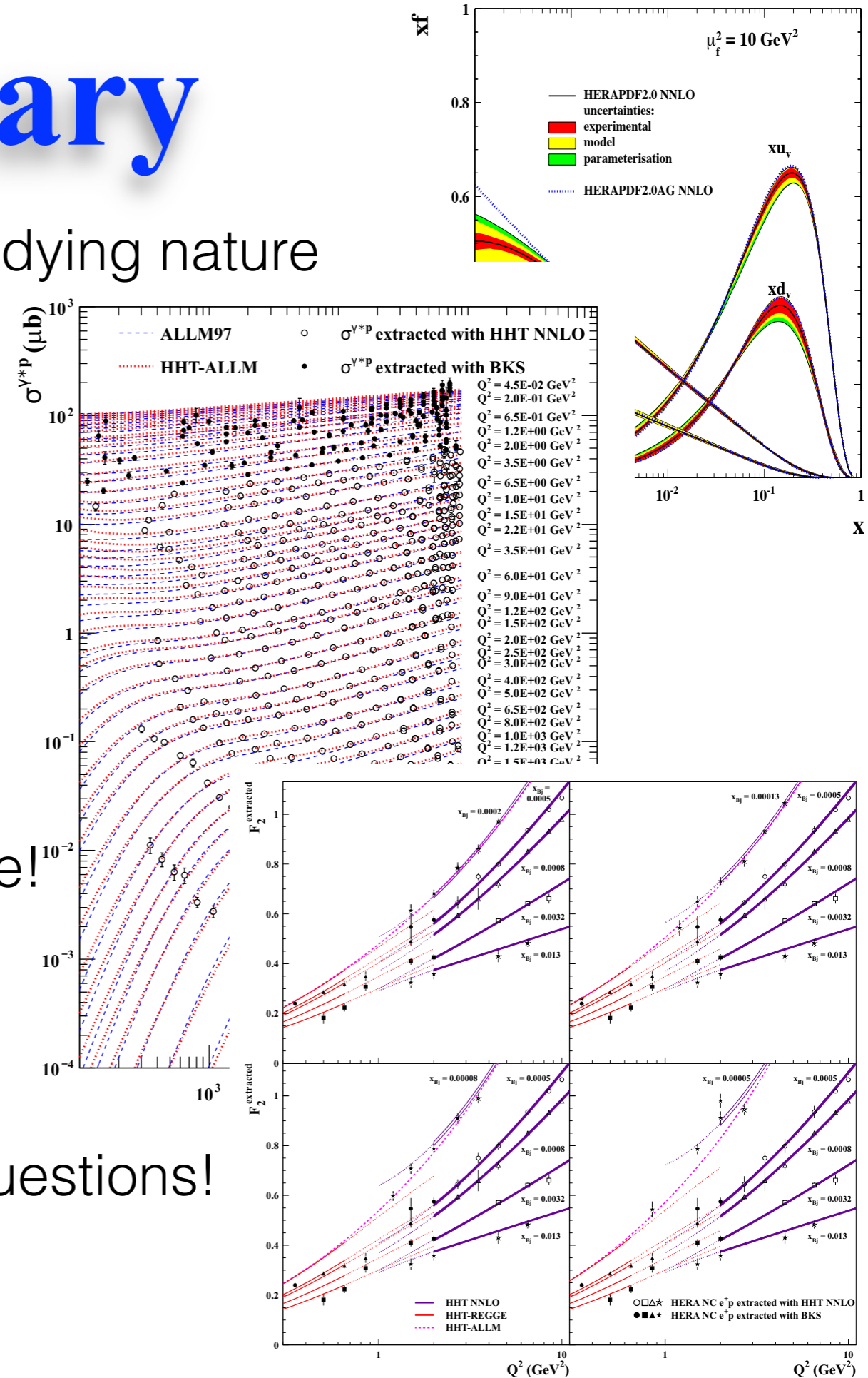
Phenomenological models,

Gluon saturation..?

Studies trigger more questions each time!

Time to improve our knowledge!

Time to ask more questions!



Backup
...not necessarily useful