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Max-Planck-Institut für Physik  
(Werner-Heisenberg-Institut)

# Neutrino flavor evolution in supernova: theory and experiment

**FRANCESCO CAPOZZI**  
**(Theoretical Astroparticle Group)**

SFB 1258

Neutrinos  
Dark Matter  
Messengers



**elusives**  
neutrinos, dark matter & dark energy physics

# MPP contribution

~100 papers from our astroparticle group: ~10% of total

HEP

108 record trovati

- 25 ►► salta al record: 1

La ricerca ha impiegato 0.17 secondi.

## 1. Normal-mode Analysis for Collective Neutrino Oscillations

Sagar Airen (Indian Inst. Tech., Mumbai & Munich, Max Planck Inst.), Francesco Capozzi (Munich, Max Planck Inst.), Sovan Chakraborty (Munich, Max Planck Inst. & Indian Inst. Tech., Guwahati), Basudeb Dasgupta (Tata Inst.), Georg Raffelt, Tobias Stirner (Munich, Max Planck Inst.). Sep 24, 2018. 26 pp.

MPP-2018-224, TIFR-TH-18-25

e-Print: [arXiv:1809.09137 \[hep-ph\]](#) | [PDF](#)

[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [Harvmac](#) | [EndNote](#)  
[ADS Abstract Service](#)

[Record dettagliato](#) - [Citato da 2 record](#)

## 2. Collisional triggering of fast flavor conversions of supernova neutrinos

Francesco Capozzi (Munich, Max Planck Inst.), Basudeb Dasgupta (Tata Inst.), Alessandro Mirizzi (Bari U. & INFN, Bari), Manibrata Sen (Tata Inst.), Günter Sigl (Hamburg U., Inst. Theor. Phys. II). Aug 20, 2018. 6 pp.

MPP-2018-206, TIFR/TH/18-27

e-Print: [arXiv:1808.06618 \[hep-ph\]](#) | [PDF](#)

[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [Harvmac](#) | [EndNote](#)  
[ADS Abstract Service](#)

[Record dettagliato](#) - [Citato da 1 record](#)

## 3. Model-independent diagnostic of self-induced spectral equalization versus ordinary matter effects in supernova neutrinos

Francesco Capozzi (Munich, Max Planck Inst.), Basudeb Dasgupta (Tata Inst.), Alessandro Mirizzi (Bari U. & INFN, Bari). Jul 2, 2018. 16 pp.

Published in [Phys.Rev. D98 \(2018\) no.6, 063013](#)

TIFR/TH/18-15, MPP-2018-147, TIFR-TH-18-15

DOI: [10.1103/PhysRevD.98.063013](#)

e-Print: [arXiv:1807.00840 \[hep-ph\]](#) | [PDF](#)

[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [Harvmac](#) | [EndNote](#)  
[ADS Abstract Service](#); [Link to Article from SCOAP3](#)

[Record dettagliato](#) - [Citato da 1 record](#)

## 4. Flavor-dependent neutrino angular distribution in core-collapse supernovae

Irene Tamborra (Bohr Inst.), Lorenz Huedepohl (Garching, Max Planck Inst.), Georg Raffelt (Munich, Max Planck Inst.), Hans-Thomas Janka (TUM-IAS, Munich). Jan 31, 2017. 10 pp.

Published in [Astrophys.J. 839 \(2017\) 132](#)

DOI: [10.3847/1538-4357/aa6a18](#)

e-Print: [arXiv:1702.00060 \[astro-ph.HE\]](#) | [PDF](#)

[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [Harvmac](#) | [EndNote](#)  
[ADS Abstract Service](#)

[Record dettagliato](#) - [Citato da 17 record](#)

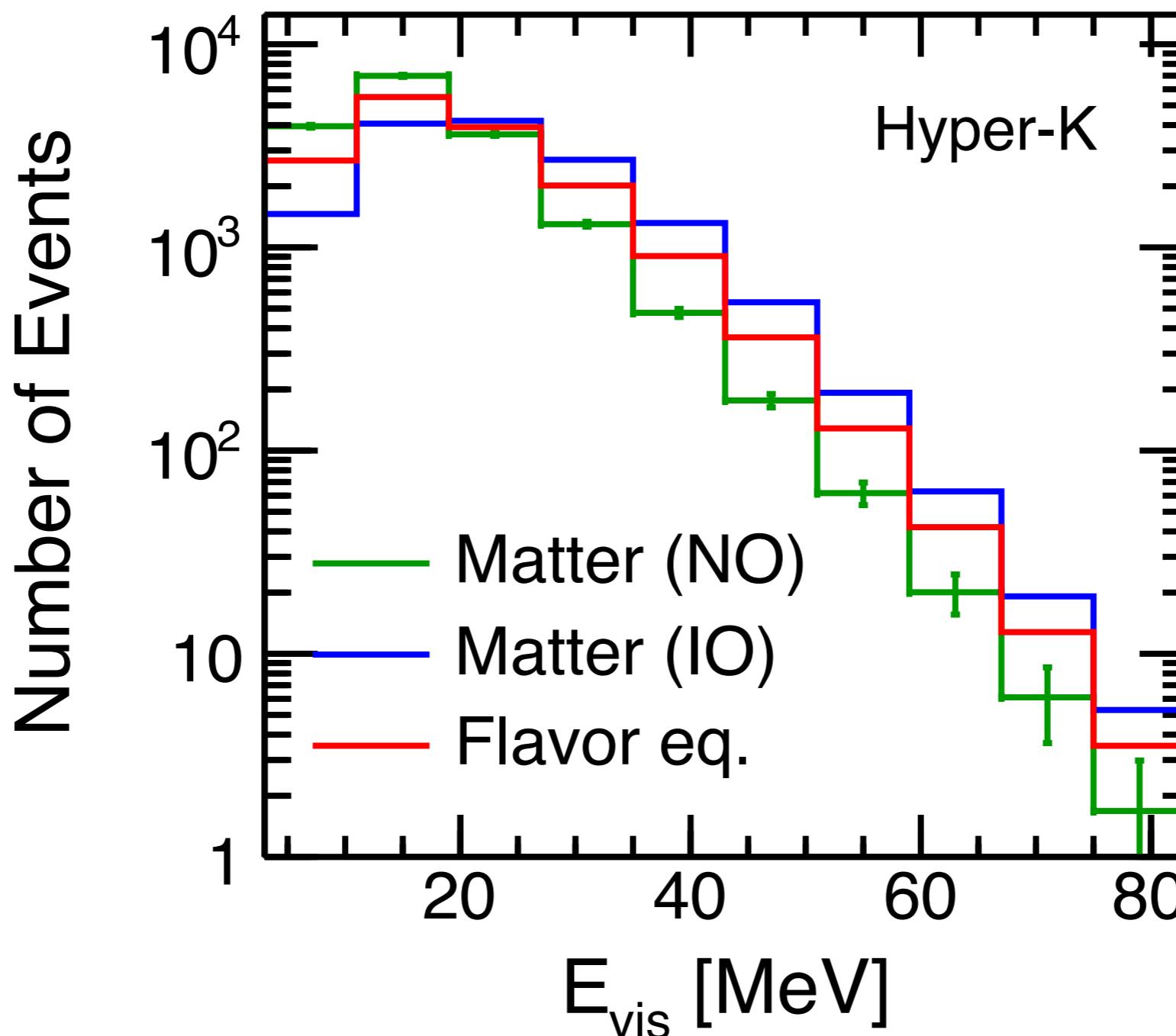
## 5. Fast Pairwise Conversion of Supernova Neutrinos: A Dispersion-Relation Approach

Ignacio Izquierre, Georg Raffelt (Munich, Max Planck Inst.), Irene Tamborra (Bohr Inst.). Oct 5, 2016. 6 pp.

Published in [Phys.Rev.Lett. 118 \(2017\) no.2, 021101](#)

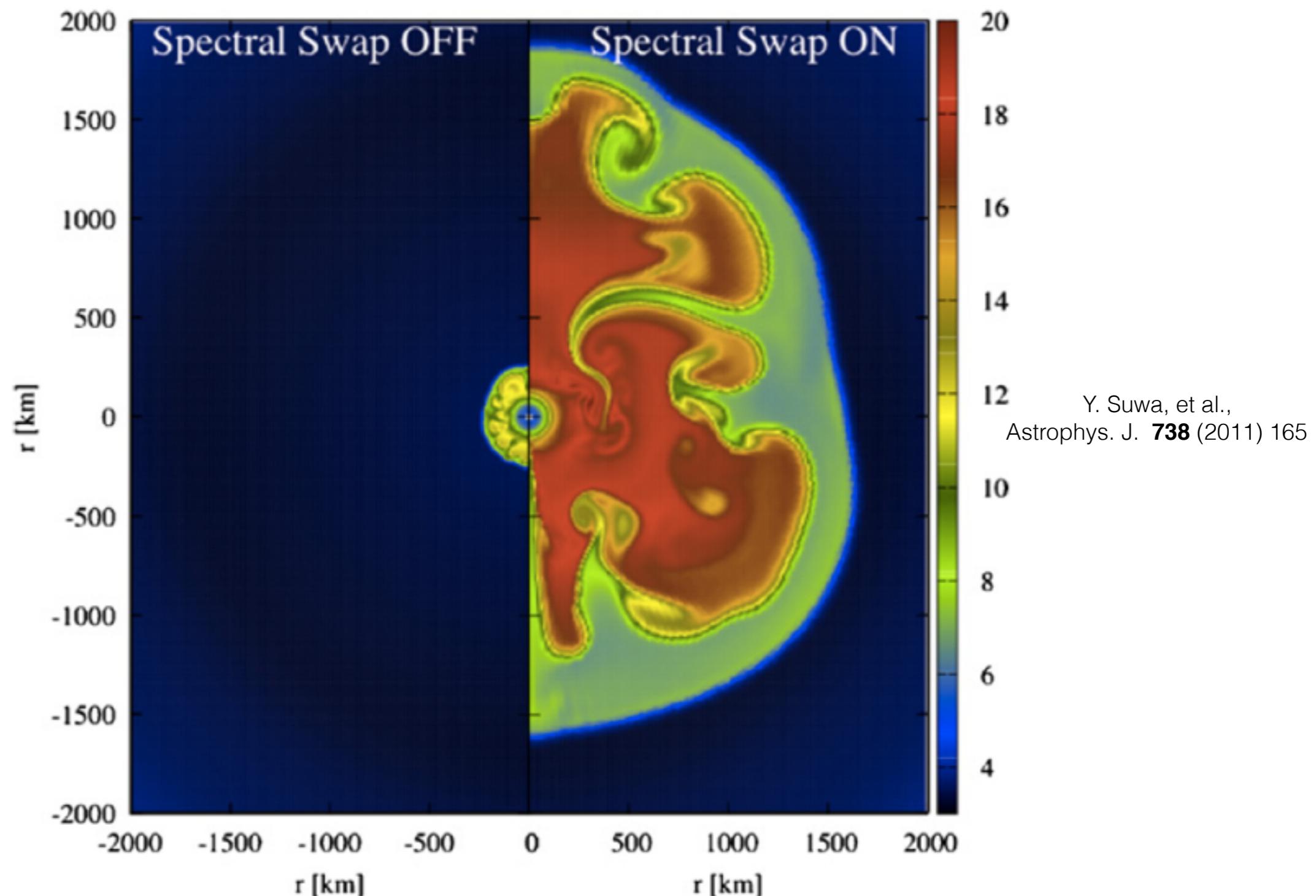
# Why do we care?

Understanding conversions  $\Leftrightarrow$  correct interpretation of SNv signal



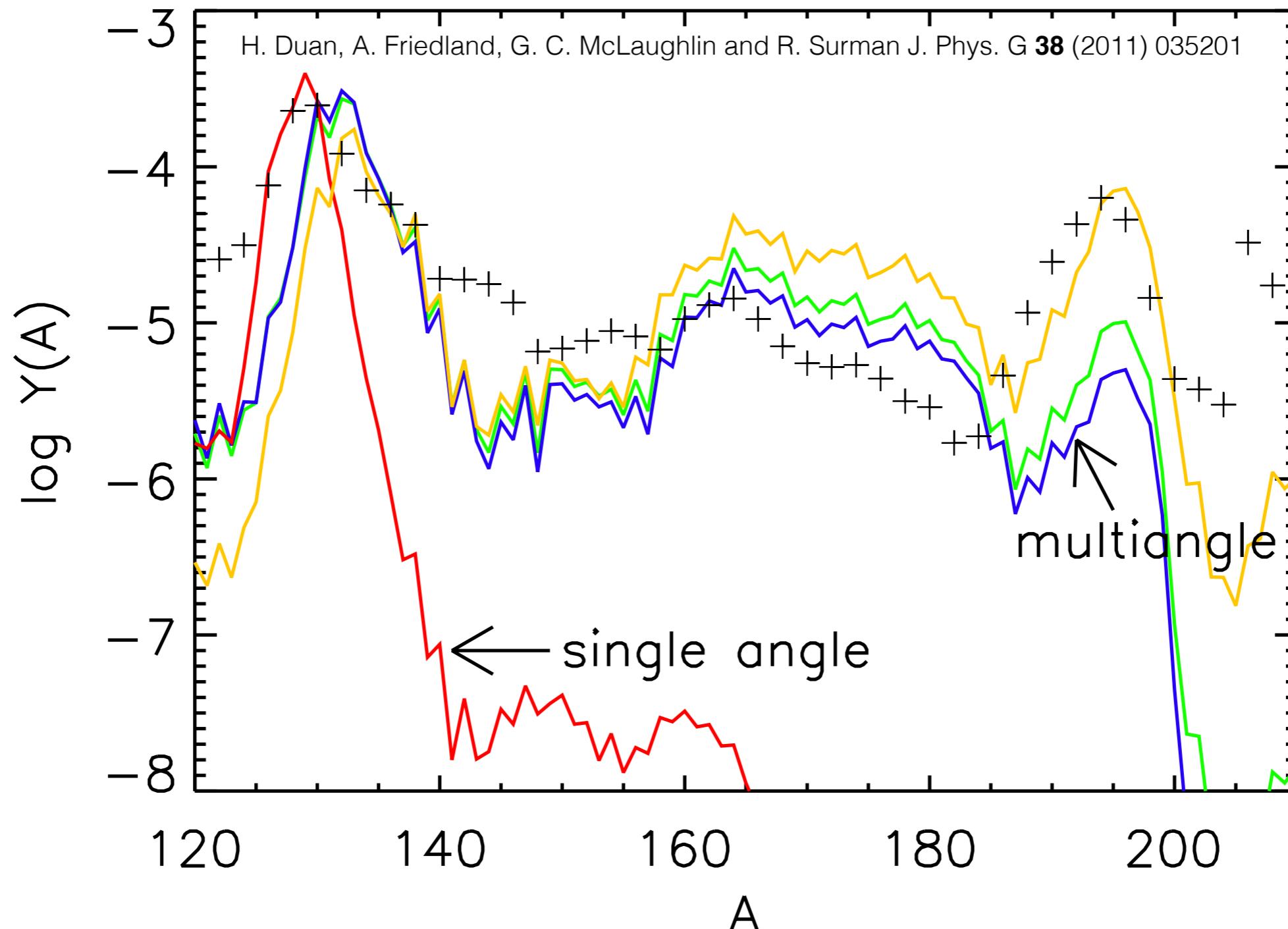
# Why do we care?

Flavour conversions alter the neutrino heating of the shock



# Why do we care?

Flavour conversions alter the nucleosynthesis processes



Outer  
layer

## Accretion phase

( $t < 0.5$  s)

### Shock wave

v - sphere

$R \sim 10$  km

$\bar{v}_\alpha$

$v_\alpha$

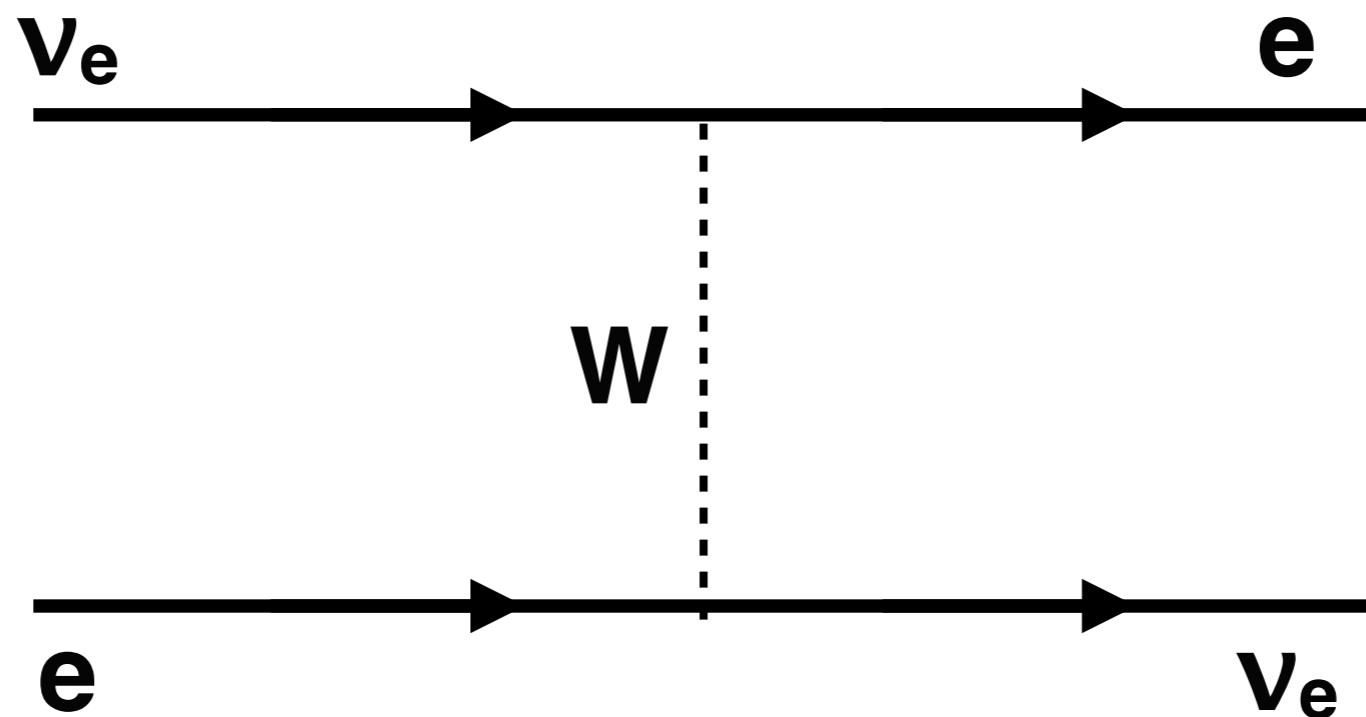
$v_\beta$

$\bar{v}_\beta$

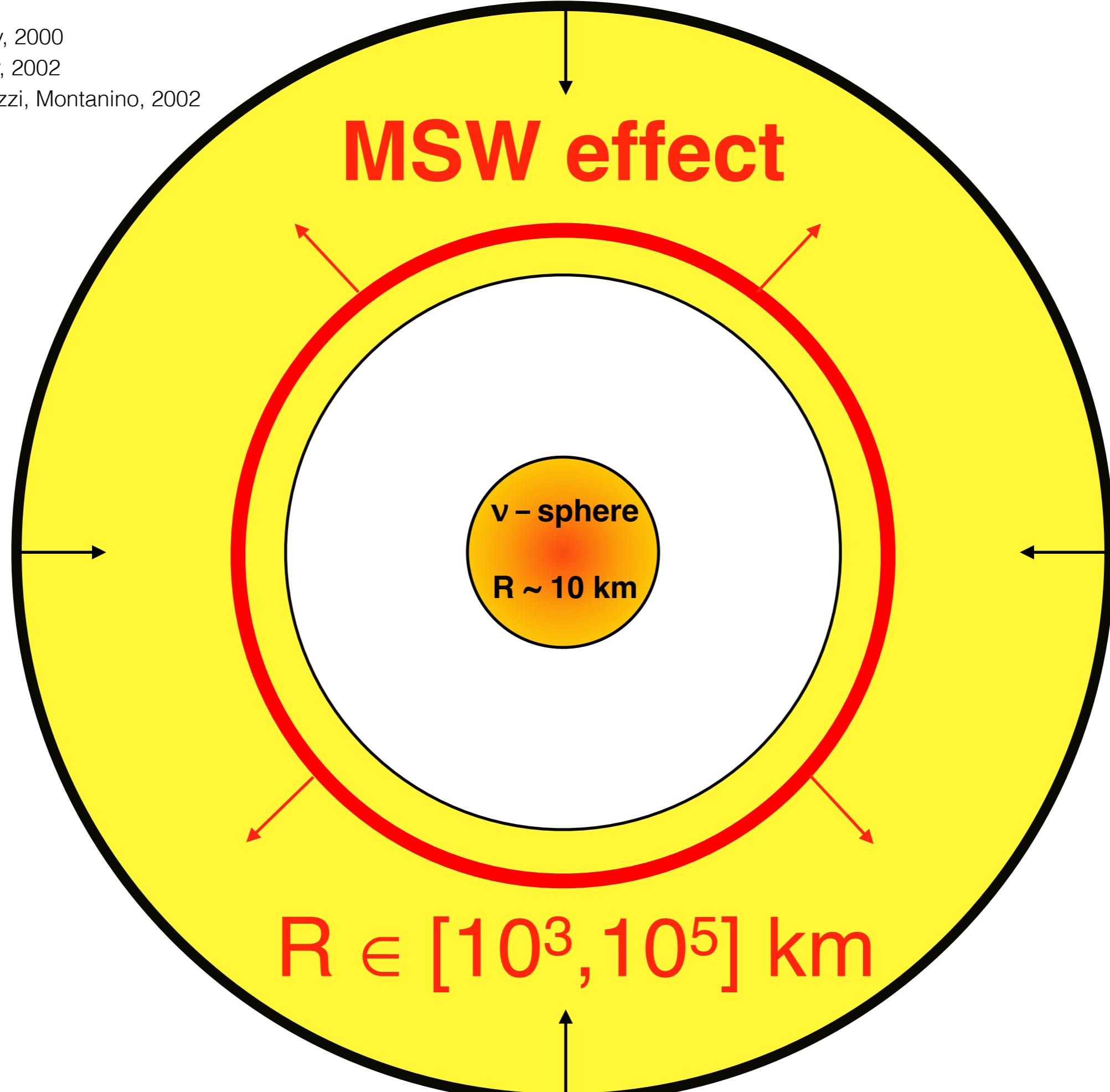
$\alpha, \beta = e, x$

# MSW effect

$$\lambda = \sqrt{2} G_F n_e$$



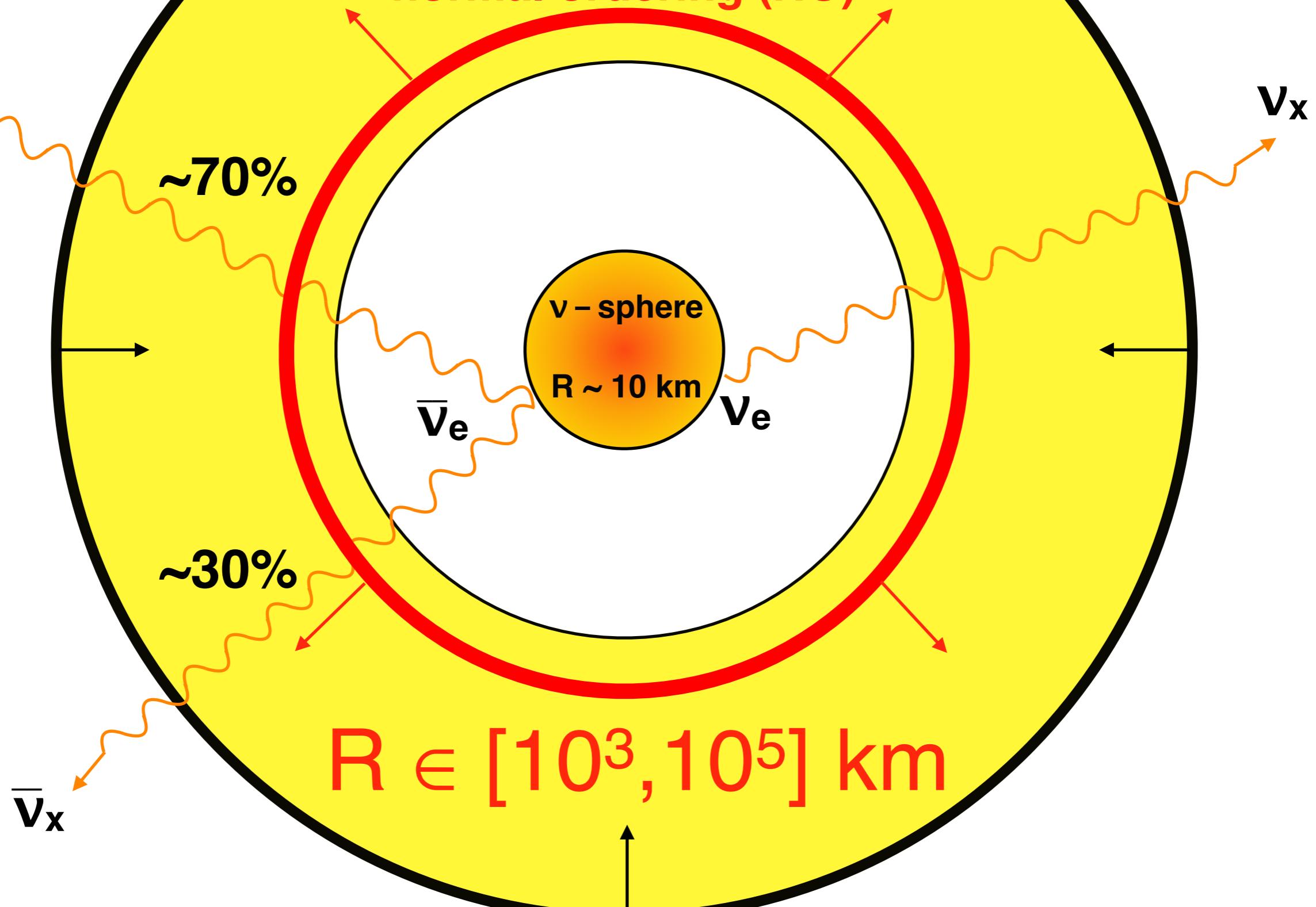
- [1] Dighe, Smirnov, 2000
- [2] Schirato, Fuller, 2002
- [3] Fogli, Lisi, Mirizzi, Montanino, 2002



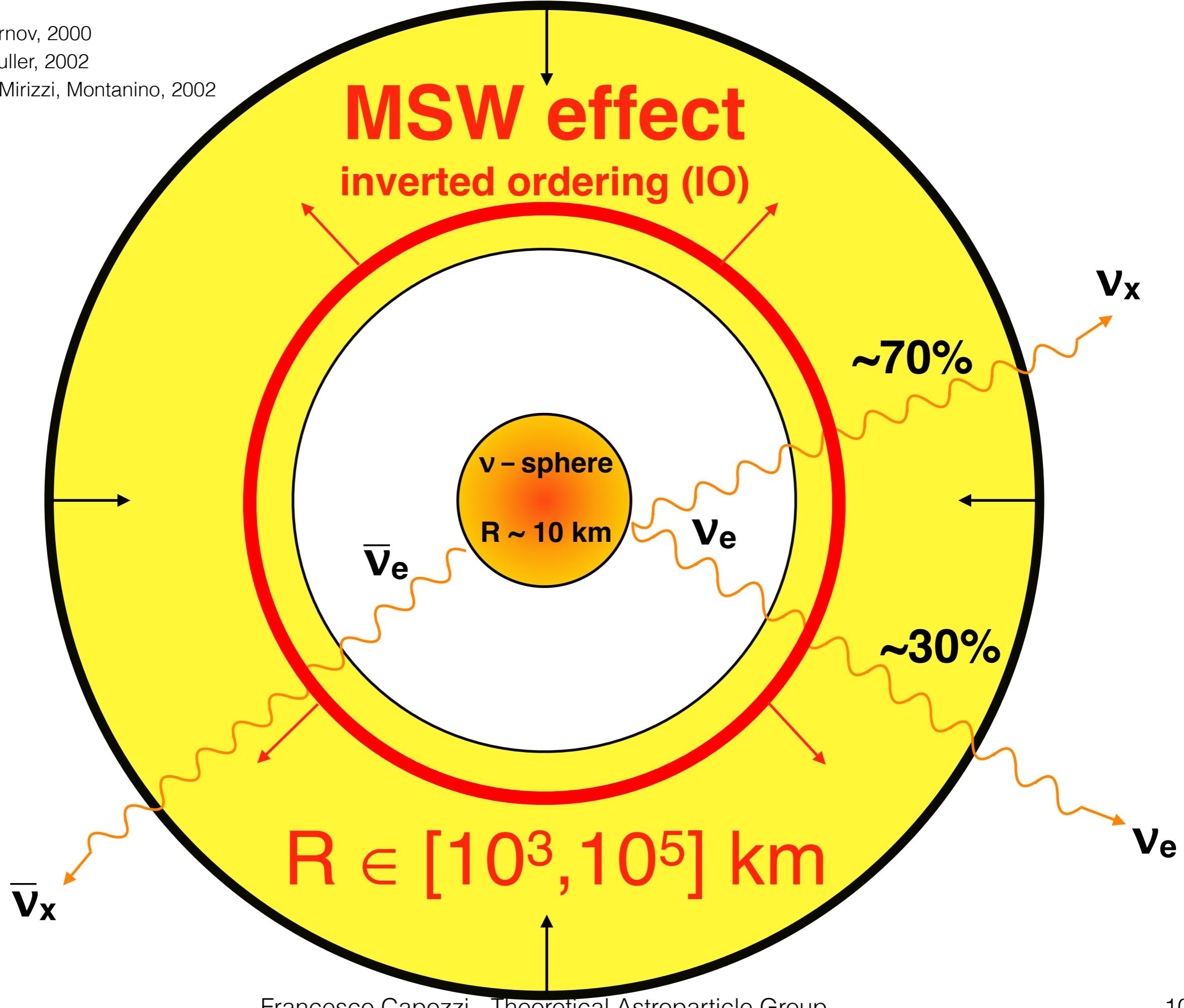
- [1] Dighe, Smirnov, 2000
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# MSW effect

normal ordering (NO)



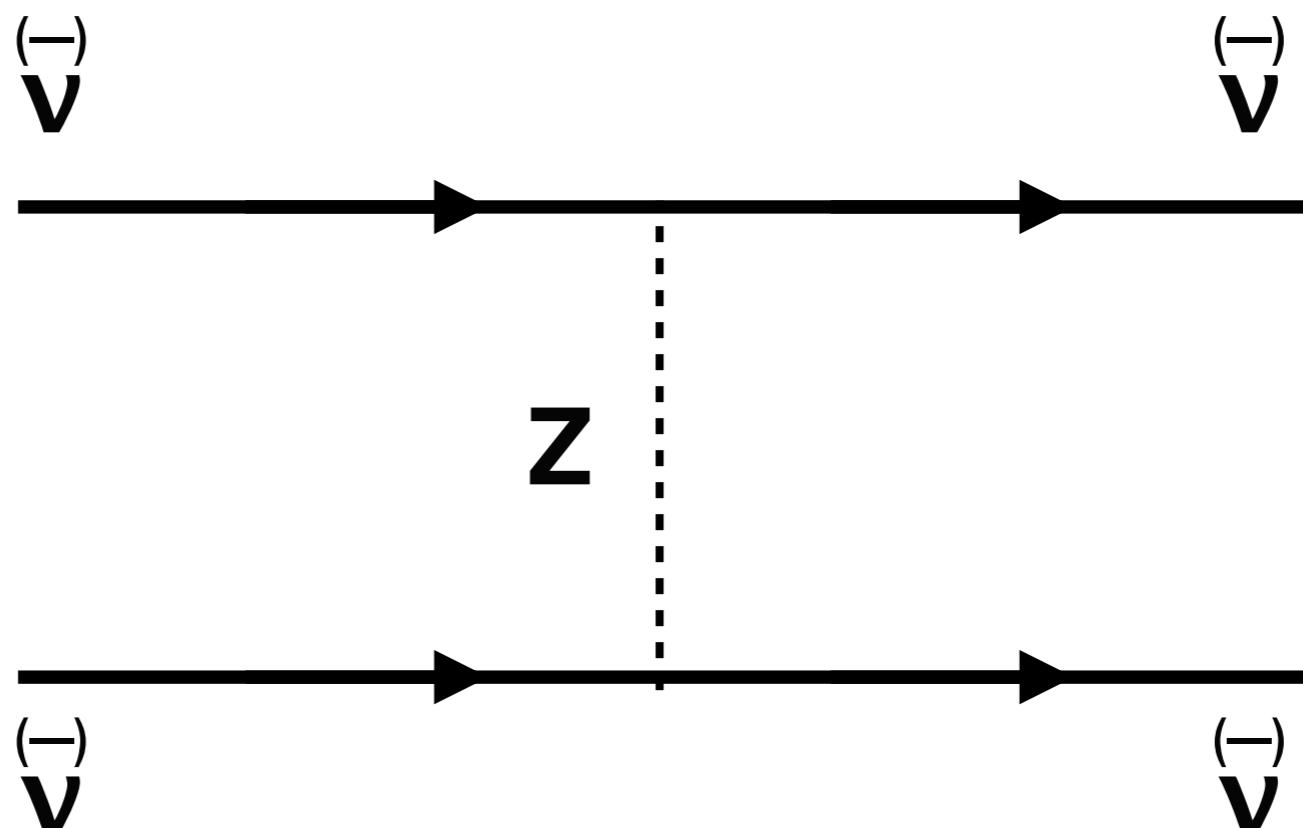
- [1] Dighe, Smirnov, 2000
- [2] Schirato, Fuller, 2002
- [3] Fogli, Lisi, Mirizzi, Montanino, 2002



# Self induced slow conversions

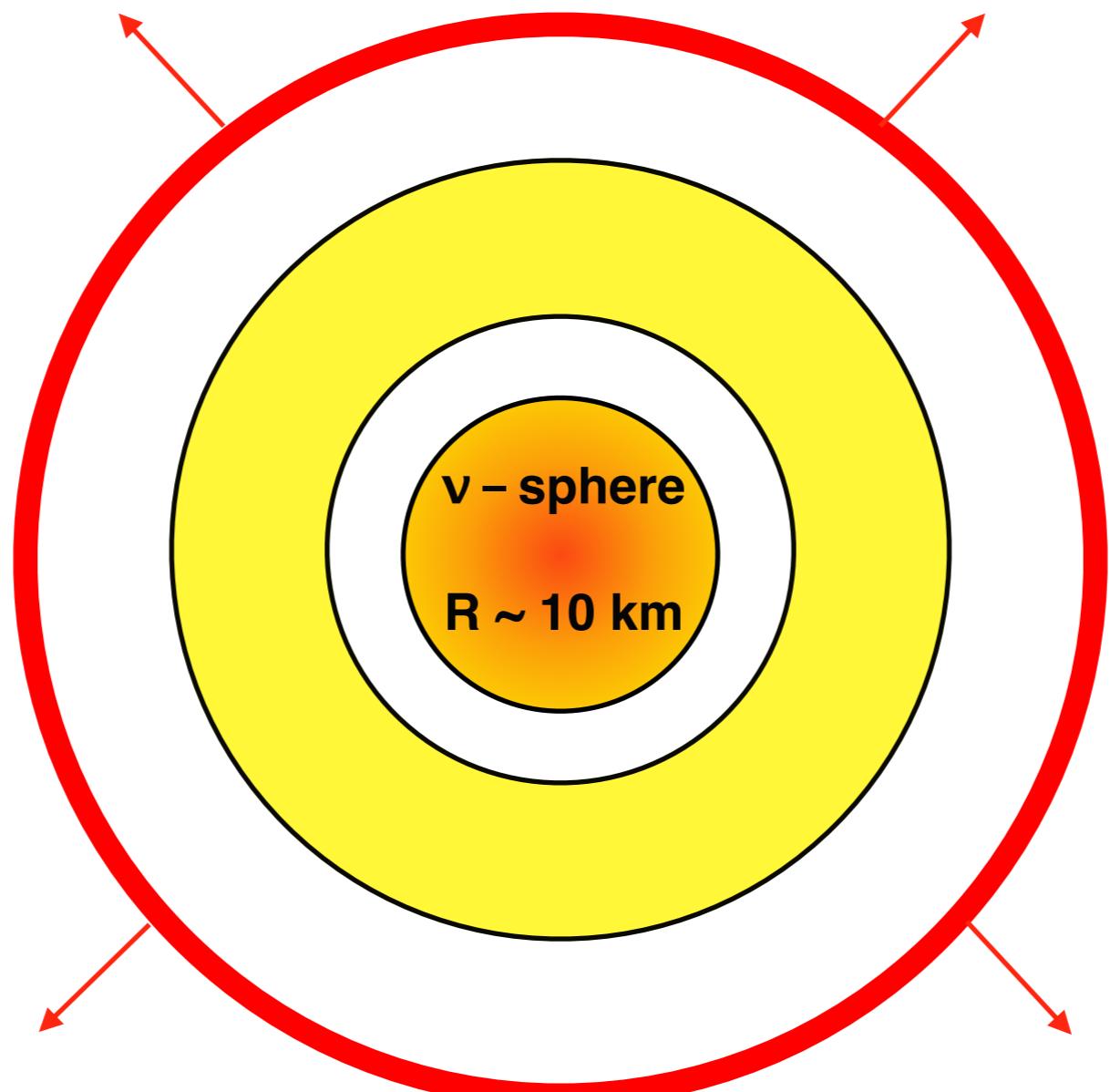
$$\mu = \sqrt{2} G_F n_\nu$$

$$\text{time} \propto \sqrt{\mu \omega_{\text{vac}}}$$



- [1] Pantaleone, 1992
- [2] Hannestad, Raffelt, Sigl, Wong, 2006
- [3] Duan, Fuller, Carlson, Qian, 2006
- [4] Fogli, Lisi, Marrone, Mirizzi, 2007

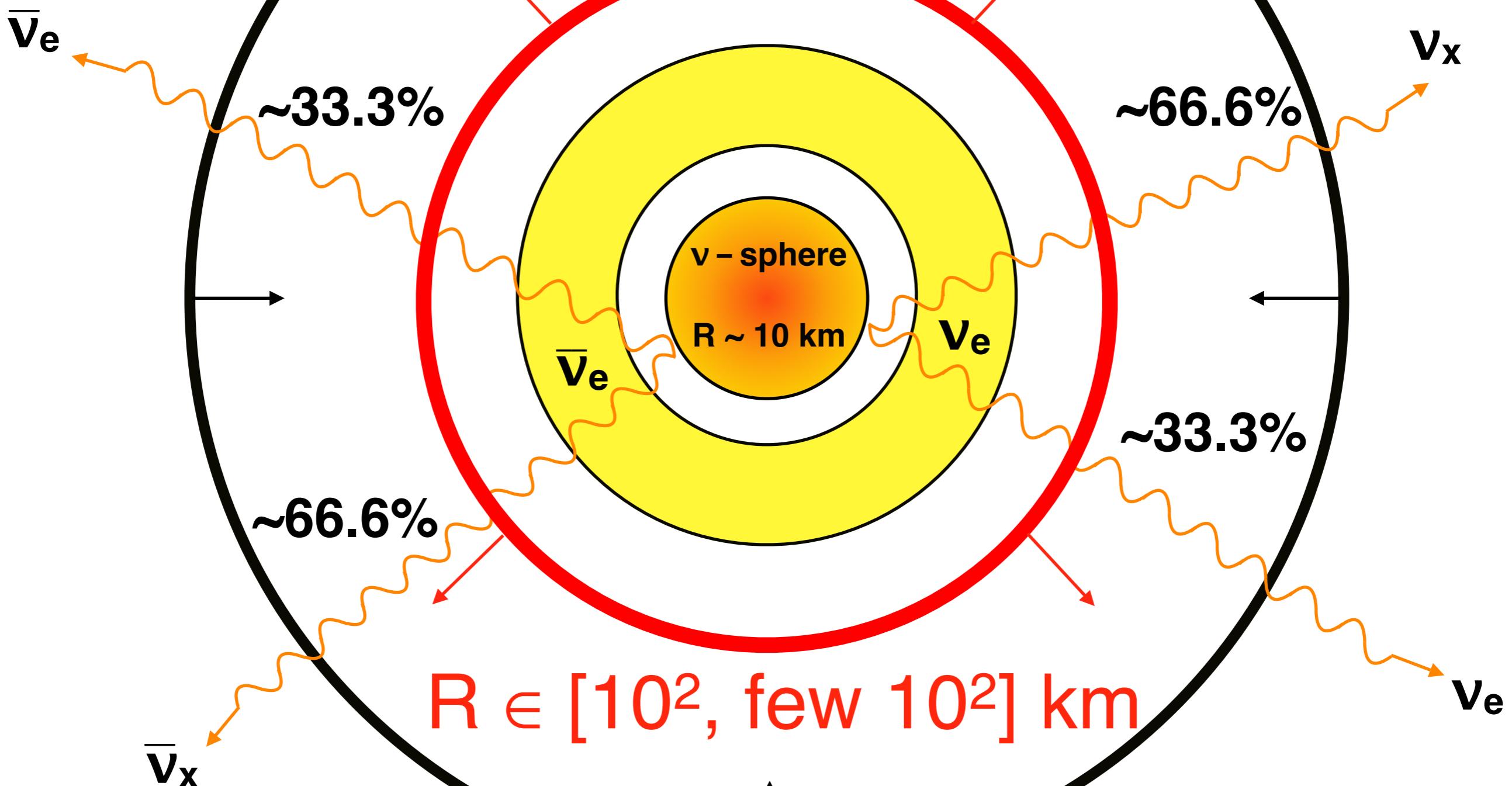
## Self-induced slow conversions



$R \in [10^2, \text{few } 10^2] \text{ km}$

- [1] Pantaleone, 1992
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**Self-induced  
slow conversions**

**WORK IN PROGRESS**

$R \in [10^2, \text{ few } 10^2] \text{ km}$

$\bar{v}_e$

$\sim 33.3\%$



$v_x$

$\sim 66.6\%$



$\sim 66.6\%$



$v_e$

$\sim 33.3\%$

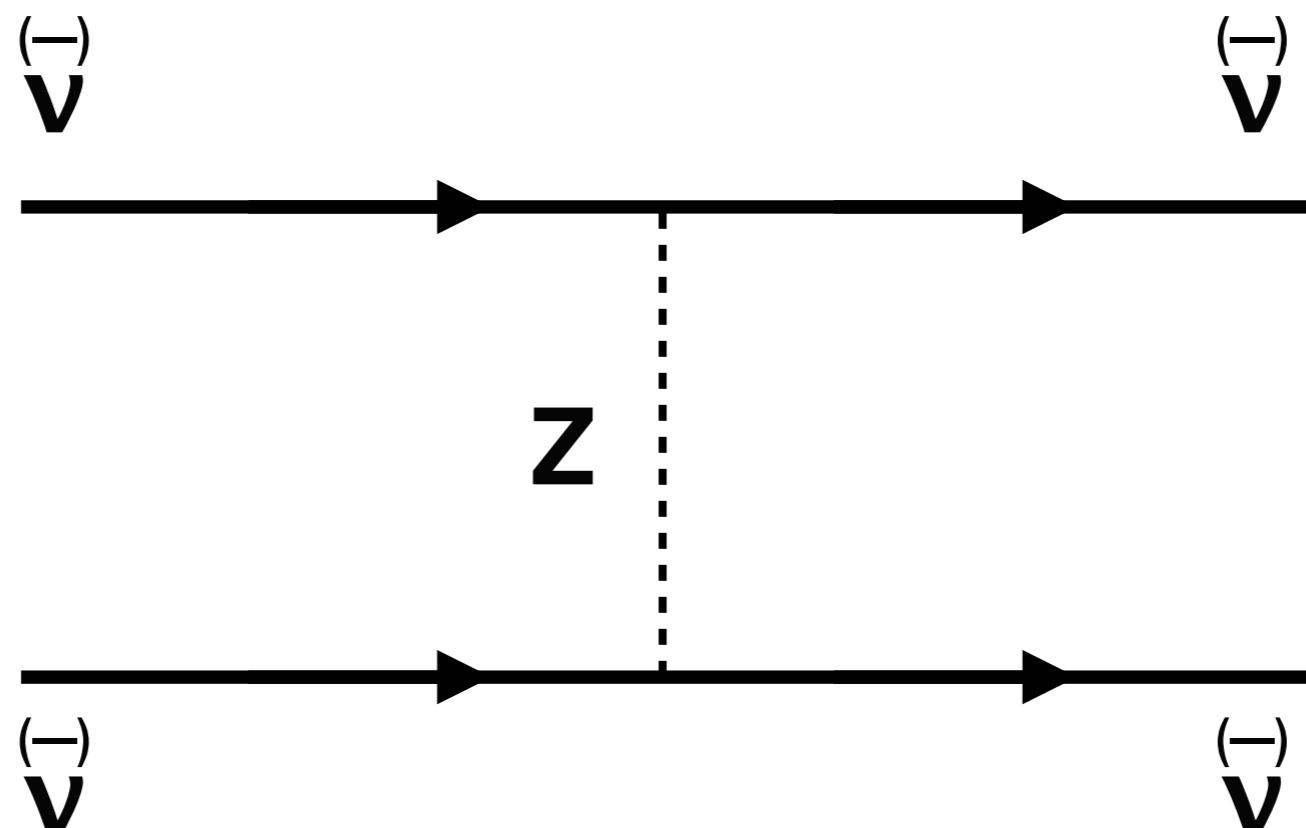


$\bar{v}_x$

# Self induced fast conversions

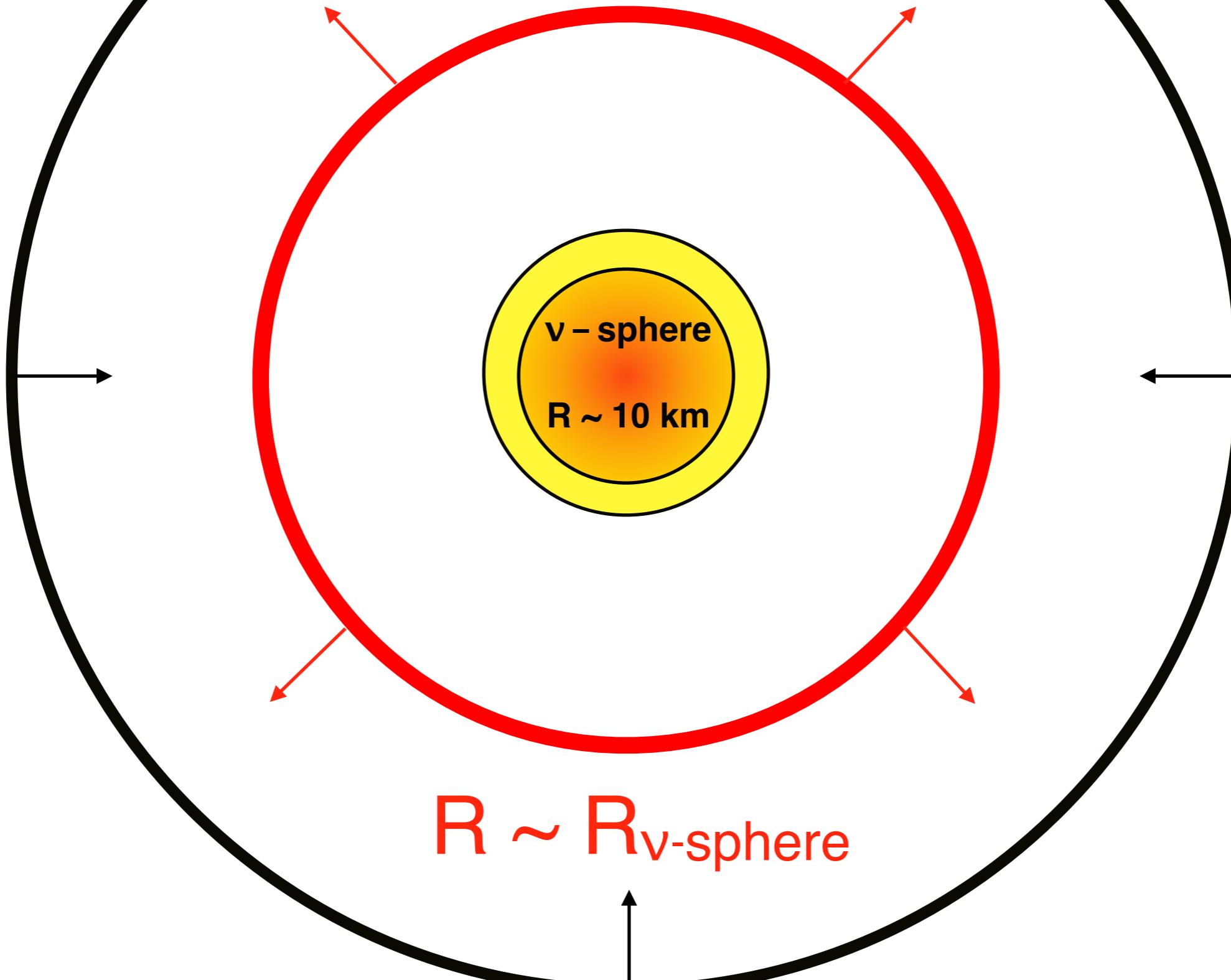
$$\mu = \sqrt{2} G_F n_\nu$$

time  $\propto \mu$



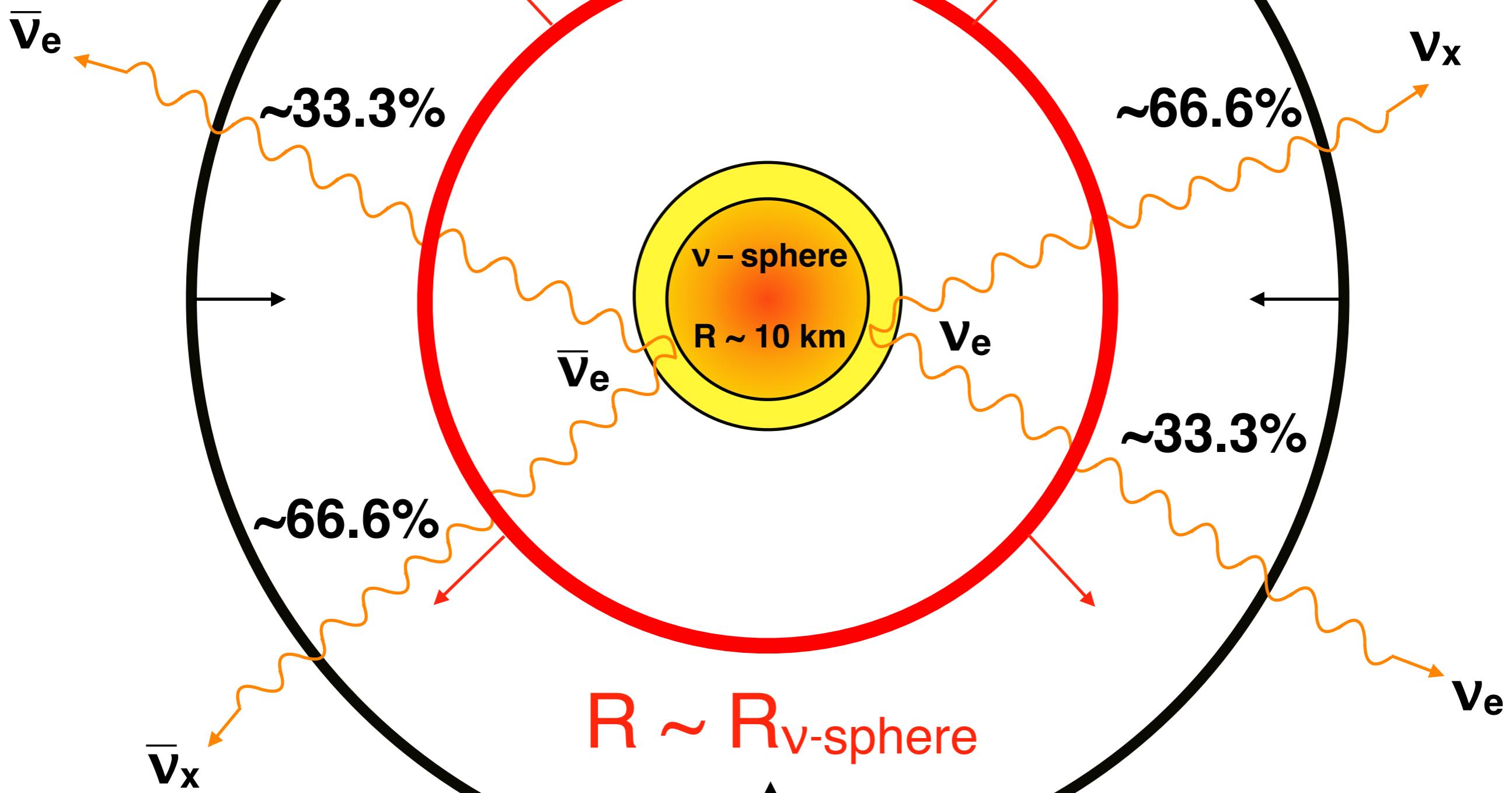
- [1] Sawyer, 2005-2009-2016
- [2] Chakraborty, Hansen, Izaguirre, Raffelt, 2016
- [3] Dasgupta, Mirizzi, Sen 2016
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## Self-induced fast conversions



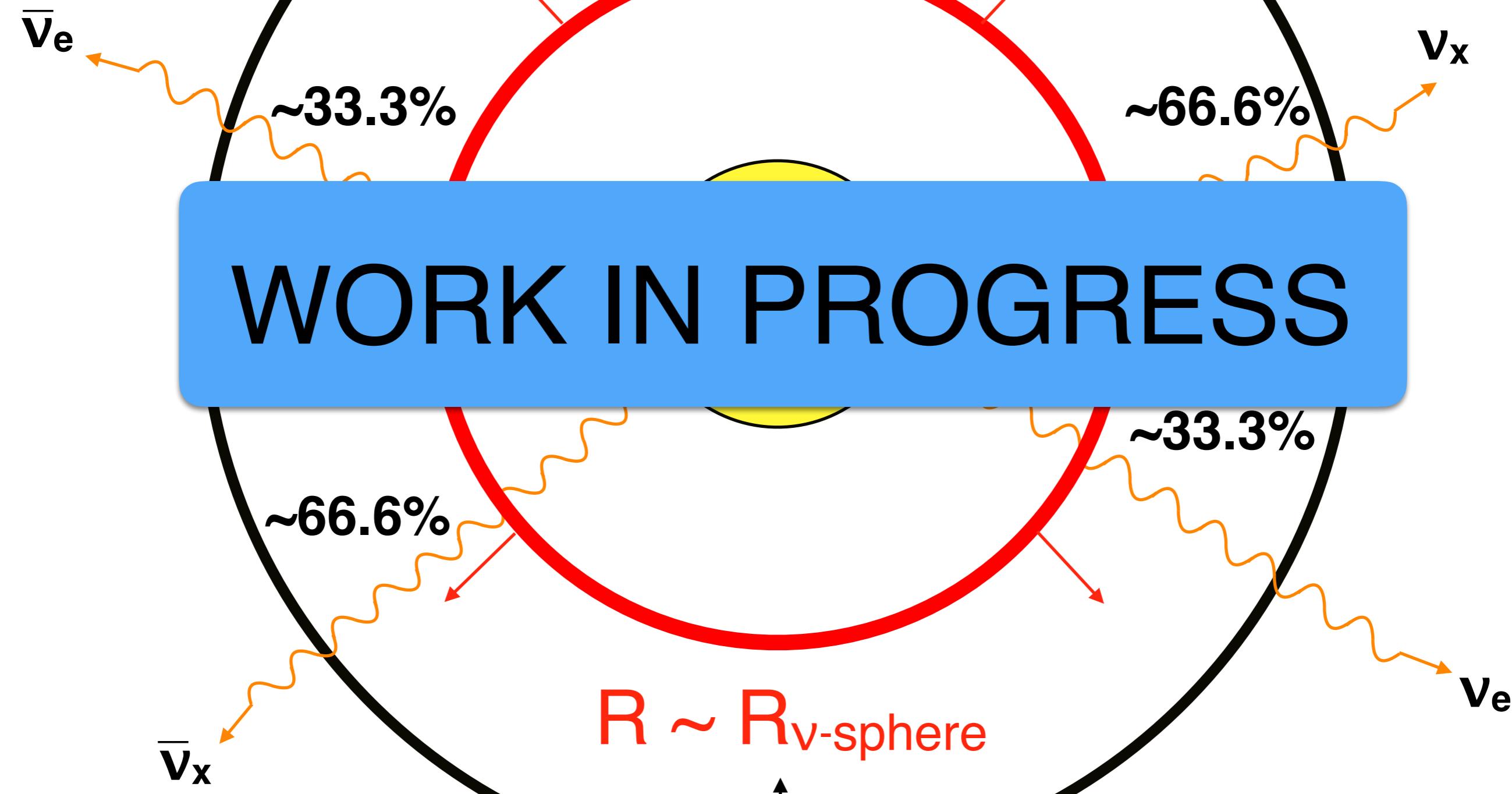
- [1] Sawyer, 2005-2009-2016
- [2] Chakraborty, Hansen, Izaguirre, Raffelt, 2016
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**Self-induced  
fast conversions**



# How to study self-induced conversions

- Numerical Simulations

- Normal mode analysis

- Experimentally?

# Numerical simulations

---

We need to solve a Boltzmann kinetic equation

$$(\partial_t + \hat{\mathbf{p}} \cdot \partial_{\mathbf{x}}) \varrho_{\mathbf{p}} = -i[\mathsf{H}_{\mathbf{p}}, \varrho_{\mathbf{p}}] + \mathcal{C}[\varrho]$$

# Numerical simulations

We need to solve a Boltzmann kinetic equation

**Flavor conversions**

$$(\partial_t + \hat{\mathbf{p}} \cdot \partial_{\mathbf{x}}) \varrho_{\mathbf{p}} = -i[\mathsf{H}_{\mathbf{p}}, \varrho_{\mathbf{p}}] + \mathcal{C}[\varrho]$$

# Numerical simulations

We need to solve a Boltzmann kinetic equation

**Collisions**

$$(\partial_t + \hat{\mathbf{p}} \cdot \partial_{\mathbf{x}}) \varrho_{\mathbf{p}} = -i[\mathsf{H}_{\mathbf{p}}, \varrho_{\mathbf{p}}] + \mathcal{C}[\varrho]$$

# Numerical simulations

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Only solvable with some approximations

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No conversions: study supernova explosion

# Numerical simulations

We need to solve a Boltzmann kinetic equation

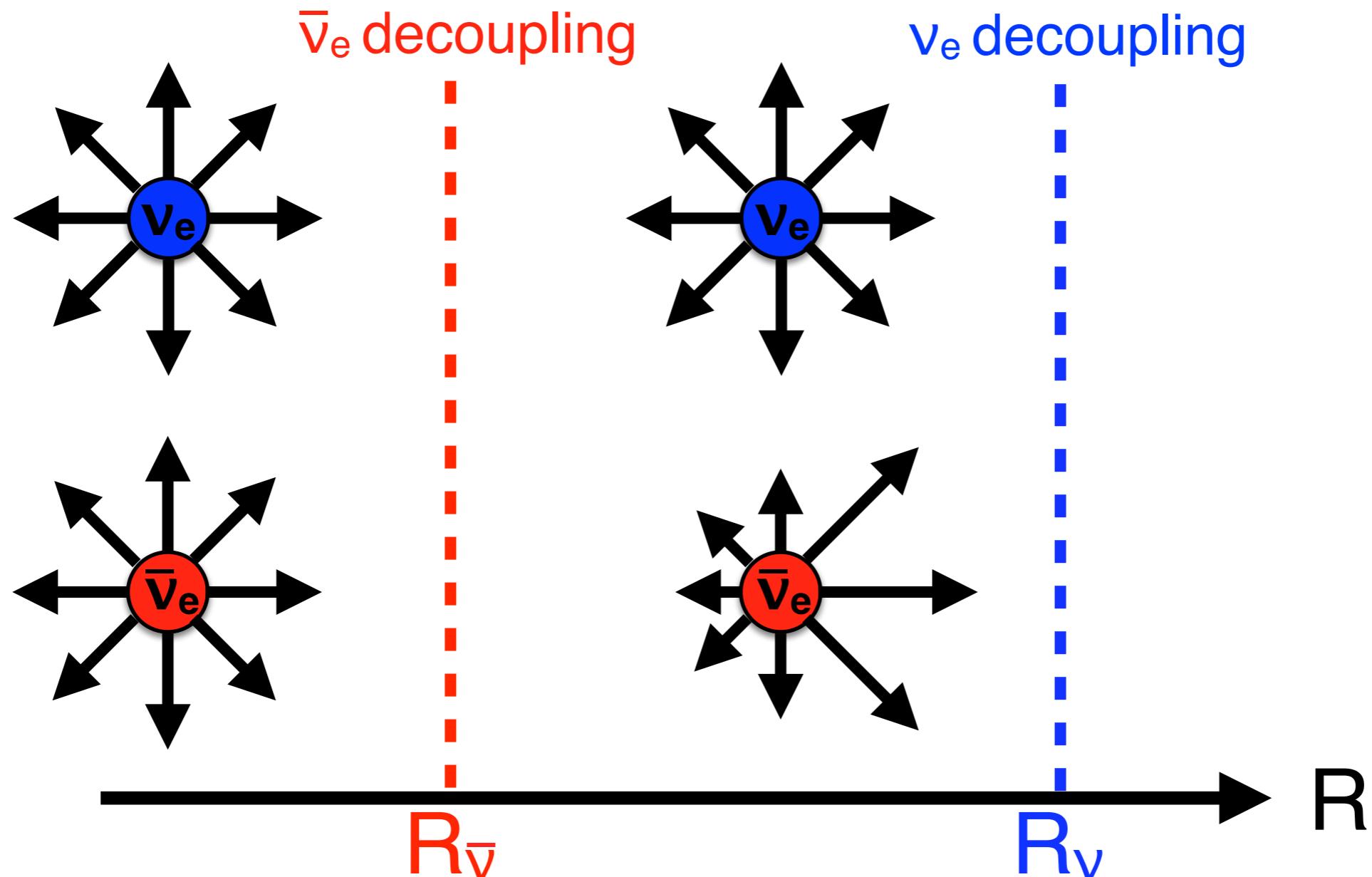
$$(\partial_t + \hat{\mathbf{p}} \cdot \partial_{\mathbf{x}}) \varrho_{\mathbf{p}} = -i[\mathsf{H}_{\mathbf{p}}, \varrho_{\mathbf{p}}] + \cancel{c[\varrho]}$$

Only solvable with some approximations

No collisions: study flavor conversions

# Numerical simulations: fast conversions

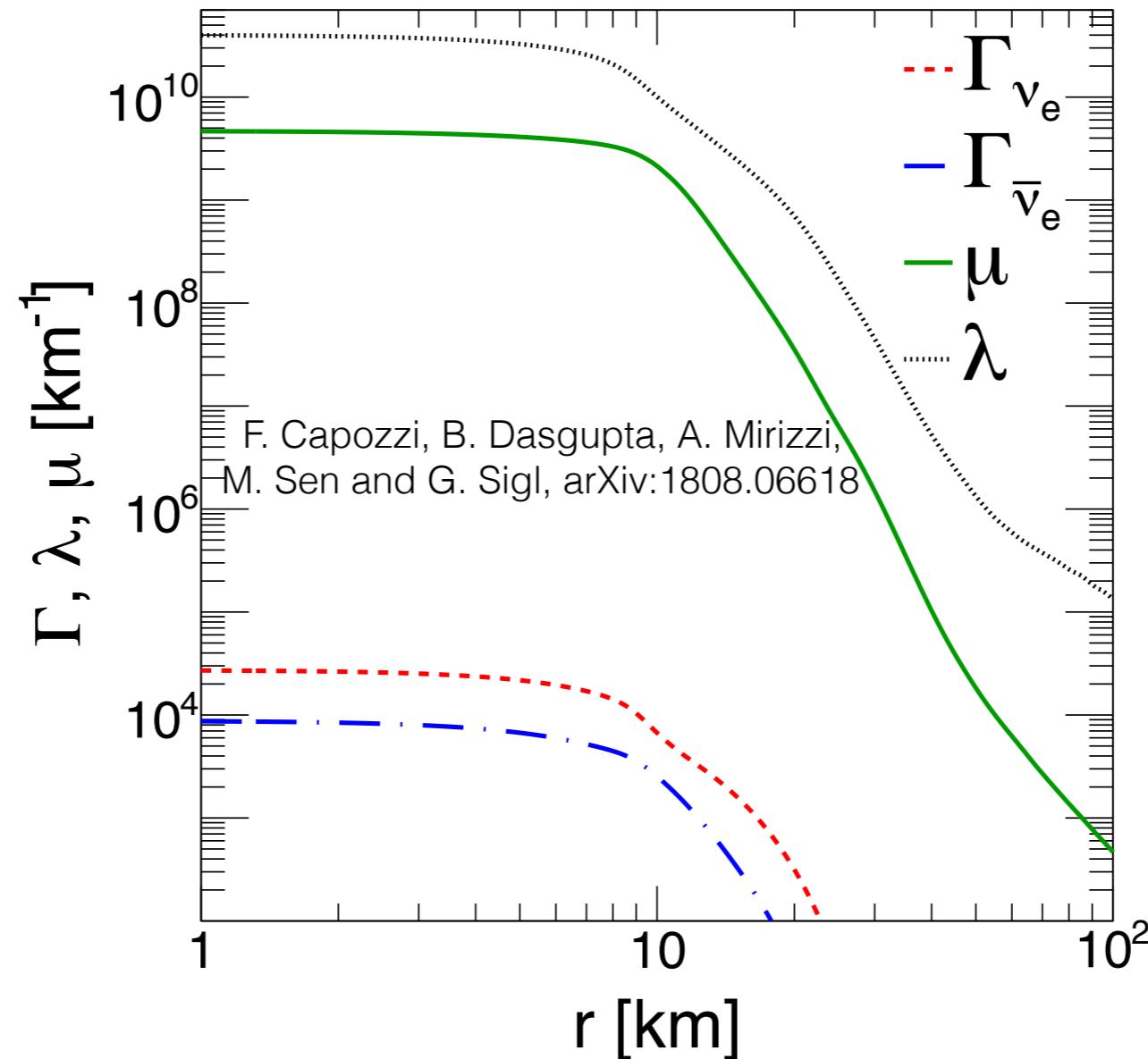
Fast conversions  $\Leftrightarrow$  different angular distributions of  $v_e$  and  $\bar{v}_e$



Favorable conditions are expected before  $v_e$  decoupling

# Numerical simulations: fast conversions

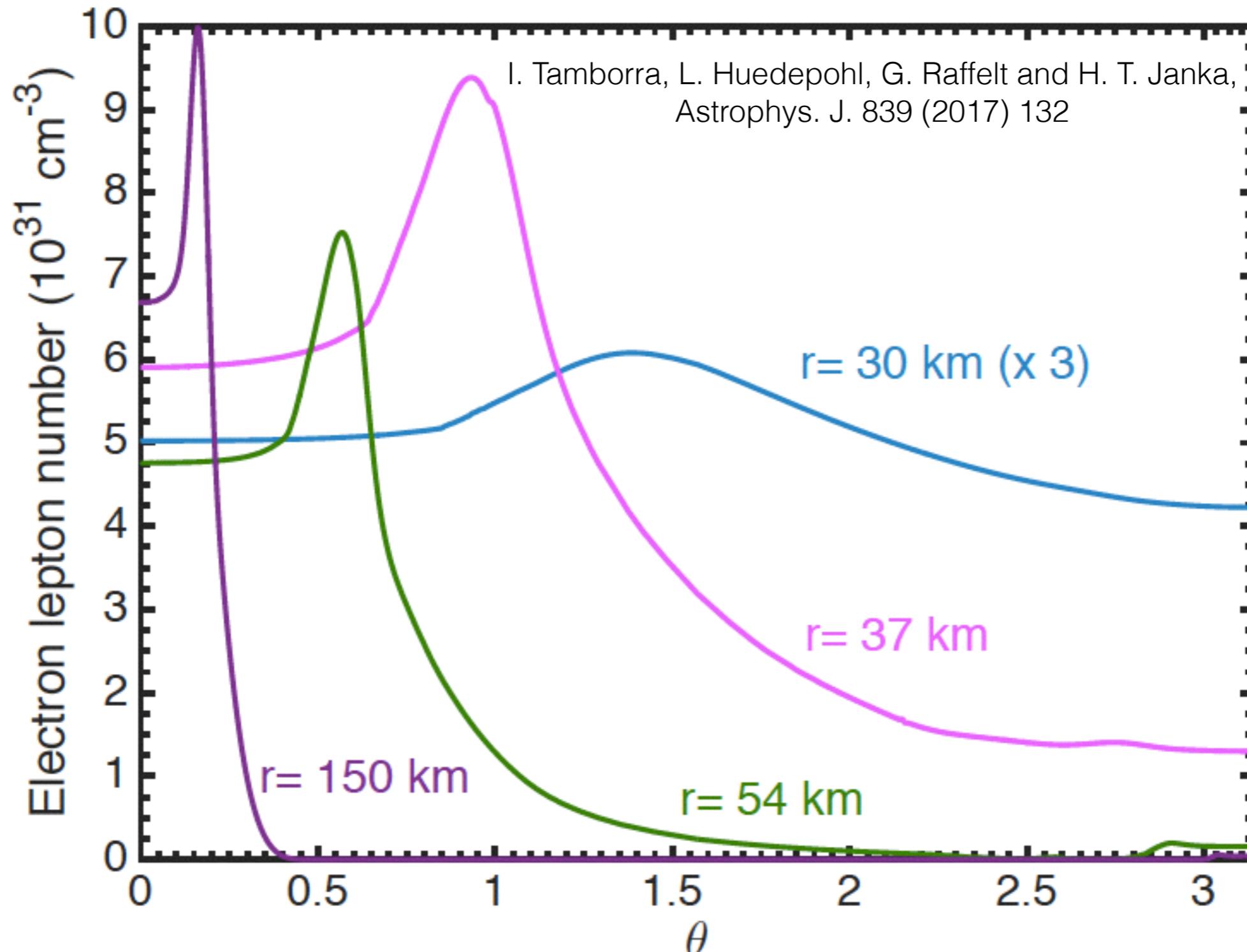
Fast conversions must be simulated with collisions



Collision rate is much smaller than conversion rate ( $\Gamma \ll \mu$ ).  
Collisions generate fast conversion, but do not suppress them

# Numerical simulations: fast conversions

No conditions for fast conversion in 1D simulations



# How to study self-induced conversions

---

- Numerical Simulations

- Normal mode analysis

- Experimentally?

# Normal mode analysis

$$\varrho_{\mathbf{v}} \propto \begin{pmatrix} s_{\mathbf{v}}(t, x) \\ S_{\mathbf{v}}^*(t, x) \end{pmatrix} \begin{pmatrix} S_{\mathbf{v}}(t, x) \\ -s_{\mathbf{v}}(t, x) \end{pmatrix}$$

# Normal mode analysis

$$\varrho_{\mathbf{v}} \propto \left( S_{\mathbf{v}}(t, x) - S_{\mathbf{v}}^*(t, x) \right)$$

**occupation numbers**

**occupation numbers**

$\varrho_{\mathbf{v}}$

occupation numbers

$$S_{\mathbf{v}}(t, x)$$
$$S_{\mathbf{v}}^*(t, x)$$

$$S_{\mathbf{v}}(t, x)$$
$$- S_{\mathbf{v}}(t, x)$$

# Normal mode analysis

$$\varrho_v \propto \left( S_v(t, x) - S_v^*(t, x) \right)$$

occupation numbers      flavour coherence

flavour coherence      occupation numbers

# Normal mode analysis

$$\varrho_{\mathbf{v}} \propto \begin{pmatrix} s_{\mathbf{v}}(t, x) \\ S_{\mathbf{v}}^*(t, x) \end{pmatrix} \begin{pmatrix} S_{\mathbf{v}}(t, x) \\ -s_{\mathbf{v}}(t, x) \end{pmatrix}$$

**Neutrinos are produced in flavour eigenstates**

$$s_{\mathbf{v}}(t, x) \simeq 1$$

**Standard oscillations suppressed by strong matter effects**

$$S_{\mathbf{v}}(t, x) \ll 1$$

# Normal mode analysis

Self induced conversions can introduce a rapid growth of S

$$S_{\mathbf{v}}(t, \mathbf{x}) = Q_{\mathbf{v}} e^{i(\mathbf{k} \cdot \mathbf{x} - \omega t)}$$

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## DISPERSION RELATION

$$D(\omega, k) = 0$$

- I. Izaguirre, G. Raffelt and I. Tamborra, Phys. Rev. Lett. 118 (2017) no.2, 021101  
F. Capozzi, B. Dasgupta, E. Lisi, A. Marrone and A. Mirizzi, Phys. Rev. D 96 (2017) no.4, 043016  
S. Airen, F. Capozzi, S. Chakraborty, B. Dasgupta, G. Raffelt and T. Stirner, arXiv:1809.09137

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S. Airen, F. Capozzi, S. Chakraborty, B. Dasgupta, G. Raffelt and T. Stirner, arXiv:1809.09137

$\omega, k \in \mathbb{C} \Rightarrow$  FLAVOUR INSTABILITY

# Normal mode analysis: future work

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**Extend analysis to more complicated (multi-D) models**

F. Capozzi, G. Raffelt, T. Stirner [MPP astro-particle group]

# Normal mode analysis: future work

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## **Extend analysis to more complicated (multi-D) models**

F. Capozzi, G. Raffelt, T. Stirner [MPP astro-particle group]

## **Apply analysis to real supernova simulation and look for instabilities**

F. Capozzi, B. Dasgupta, H.-T. Janka, R. Glas, A. Mirizzi, M. Sen

# How to study self-induced conversions

---

- Numerical Simulations
- Normal mode analysis
- Experimentally?

# Information from experiments

Experiments can distinguish flavour conversion scenarios?

Scenario	Mass Ordering	$P_{ee}$	$\bar{P}_{ee}$
ME	NO	0	$\cos^2 \theta_{12} \simeq 0.7$
ME	IO	$\sin^2 \theta_{12} \simeq 0.3$	0
FE	either	$1/3 \simeq 0.33$	$1/3 \simeq 0.33$

ME = Matter effects (MSW)

FE = flavour equalisation

# Information from experiments

We use three detection channels



**$\nu$ -proton elastic scattering (pES)**

$$\stackrel{\leftarrow}{\nu}_{e,\mu,\tau} + p \rightarrow \stackrel{\leftarrow}{\nu}_{e,\mu,\tau} + p$$

$$F_{\text{pES}}(E_\nu) = F_{\nu_e}(E_\nu) + F_{\bar{\nu}_e}(E_\nu) + 4F_{\nu_x}(E_\nu)$$

# Information from experiments

We use three detection channels



**inverse  $\beta$  decay (IBD)**



$$F_{\text{IBD}}(E_\nu) = F_{\bar{\nu}_e}(E_\nu)\bar{P}_{ee} + F_{\nu_x}(E_\nu)(1 - \bar{P}_{ee})$$

# Information from experiments

We use three detection channels



$\nu$  charged-current on  $^{40}\text{Ar}$  (ArCC)



$$F_{\text{ArCC}}(E_\nu) = F_{\nu_e}(E_\nu)P_{ee} + F_{\nu_x}(E_\nu)(1 - P_{ee})$$

# Information from experiments: ratios

---

Assume we are in normal mass ordering. We define:

$$R = \frac{F_{\text{pES}}}{F_{\text{ArCC}}} \quad x = \frac{F_{\nu_e}^0}{F_{\nu_x}^0} \leq 1 \quad \bar{x} = \frac{F_{\bar{\nu}_e}^0}{F_{\bar{\nu}_x}^0} \leq 1$$

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$$\bar{x} = \frac{F_{\bar{\nu}_e}^0}{F_{\bar{\nu}_x}^0} \leq 1$$

$$R_{\text{ME}} = \begin{cases} 4 & x, \bar{x} \ll 1 \\ 5 & x \ll 1, \text{ and } \bar{x} \lesssim 1 \\ 6 & x \lesssim \bar{x} \lesssim 1 \end{cases},$$

$$R_{\text{FE}} = \begin{cases} 6 & x, \bar{x} \ll 1 \\ 7.5 & x \ll 1, \text{ and } \bar{x} \lesssim 1 \\ 6 & x \lesssim \bar{x} \lesssim 1 \end{cases}$$

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**R > 6 disfavours “matter effects only” scenario**

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$R > 6$  disfavours “matter effects only” scenario

**$R < 6$  disfavours “flavour equalisation” scenario**

# Information from experiments: ratios

---

Assume we are in normal mass ordering. We define:

$$\bar{R} = \frac{F_{\text{pES}}}{F_{\text{IBD}}}$$

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$$\bar{x} = \frac{F_{\bar{\nu}_e}^0}{F_{\bar{\nu}_x}^0} \leq 1$$

$$\bar{R}_{\text{ME}} = \begin{cases} 13.3 & x, \bar{x} \ll 1 \\ 5 & x \ll 1, \text{ and } \bar{x} \lesssim 1 \\ 6 & x \lesssim \bar{x} \lesssim 1 \end{cases},$$

$$\bar{R}_{\text{FE}} = \begin{cases} 6 & x, \bar{x} \ll 1 \\ 5 & x \ll 1, \text{ and } \bar{x} \lesssim 1 \\ 6 & x \lesssim \bar{x} \lesssim 1 \end{cases}$$

# Information from experiments: ratios

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**$\bar{R} > 6$  disfavours “flavour equalization” scenario**

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$\bar{R} \sim 5 - 6$  leads to degeneracy between scenarios

# Conclusions

Three complimentary ways of studying flavour conversions:

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**1) we can use “brute force” numerical simulations**

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- 2) we can use normal mode analysis

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- 3) **real data can in principle exclude some scenario**

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Three complimentary ways of studying flavour conversions:

- 1) we can use “brute force” numerical simulations
- 2) we can use normal mode analysis
- 3) real data can in principle exclude some scenario

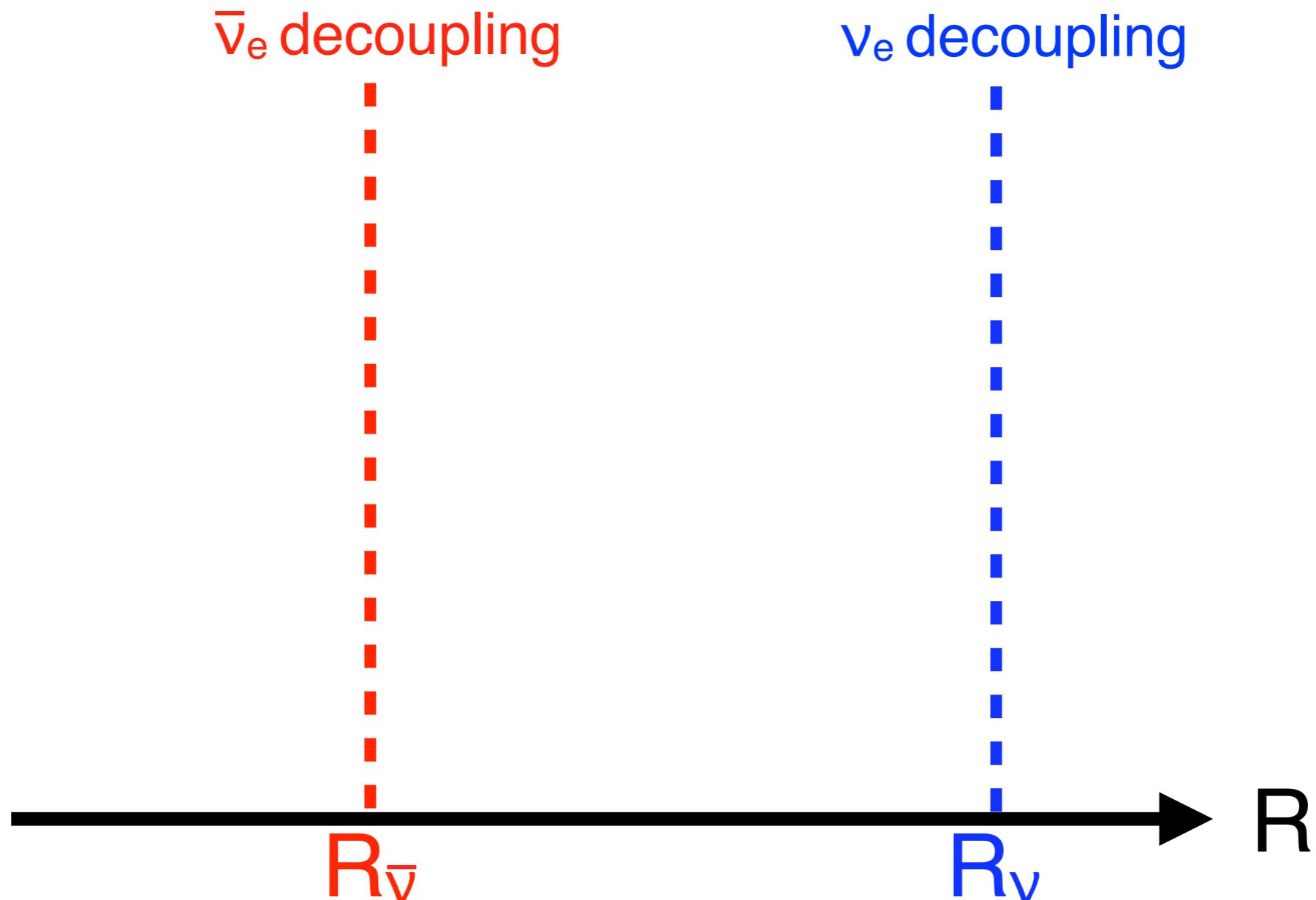
**Synergy with SN explosion simulators is required**

# Thank you

# Backup

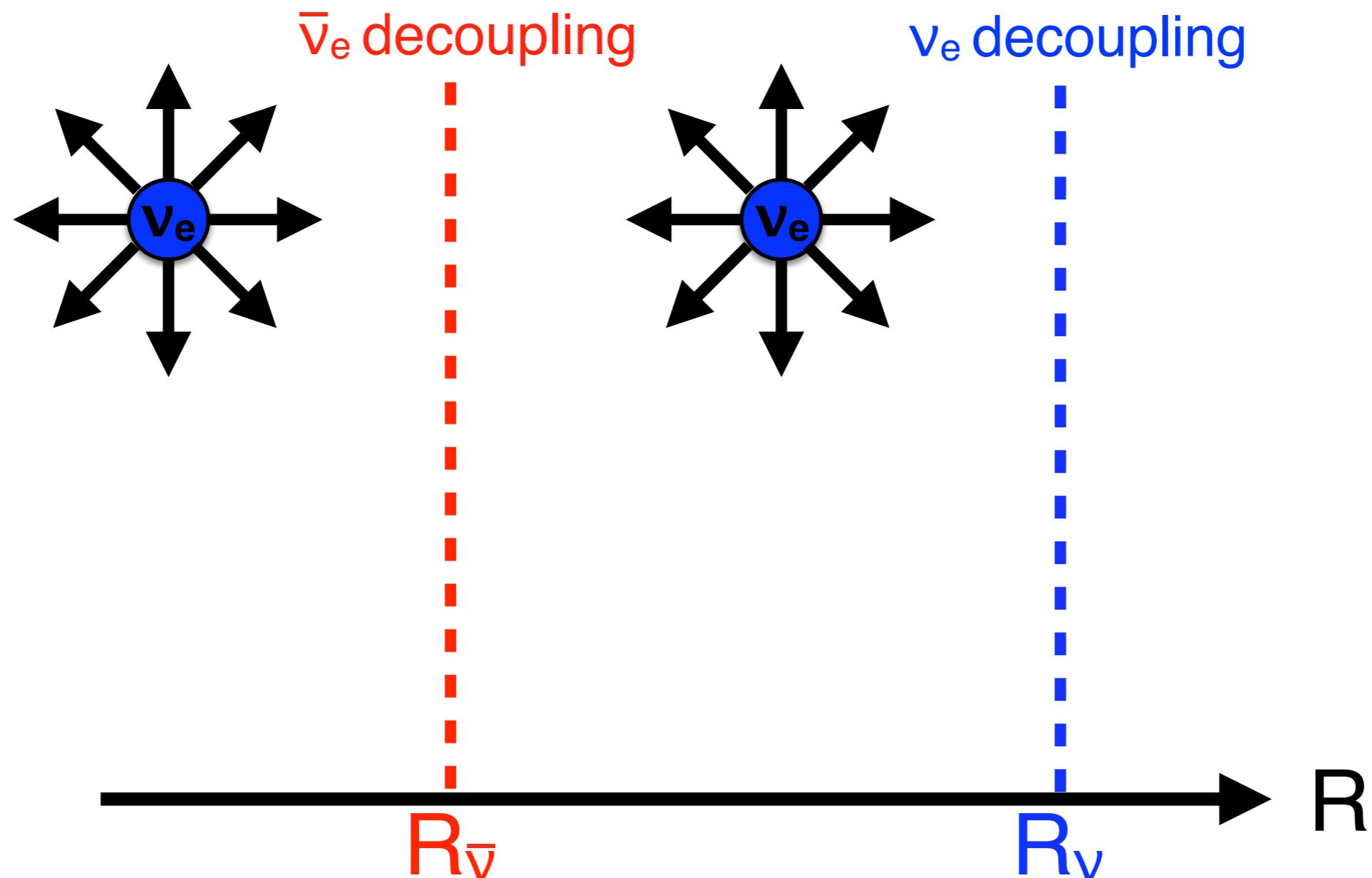
# Numerical simulations: fast conversions

Fast conversions  $\Leftrightarrow$  different angular distributions of  $v_e$  and  $\bar{v}_e$



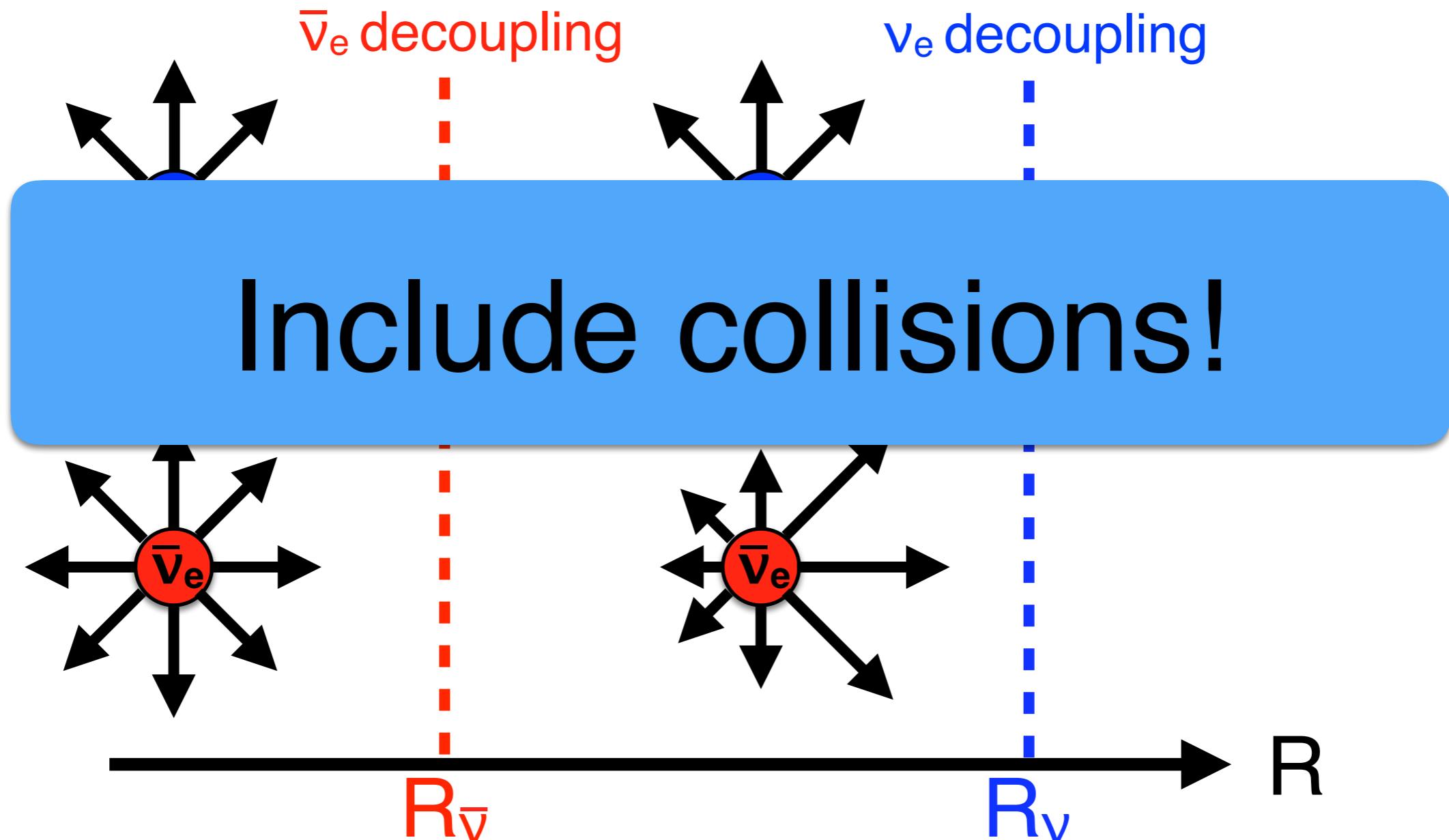
# Numerical simulations: fast conversions

Fast conversions  $\Leftrightarrow$  different angular distributions of  $v_e$  and  $\bar{v}_e$



# Numerical simulations: fast conversions

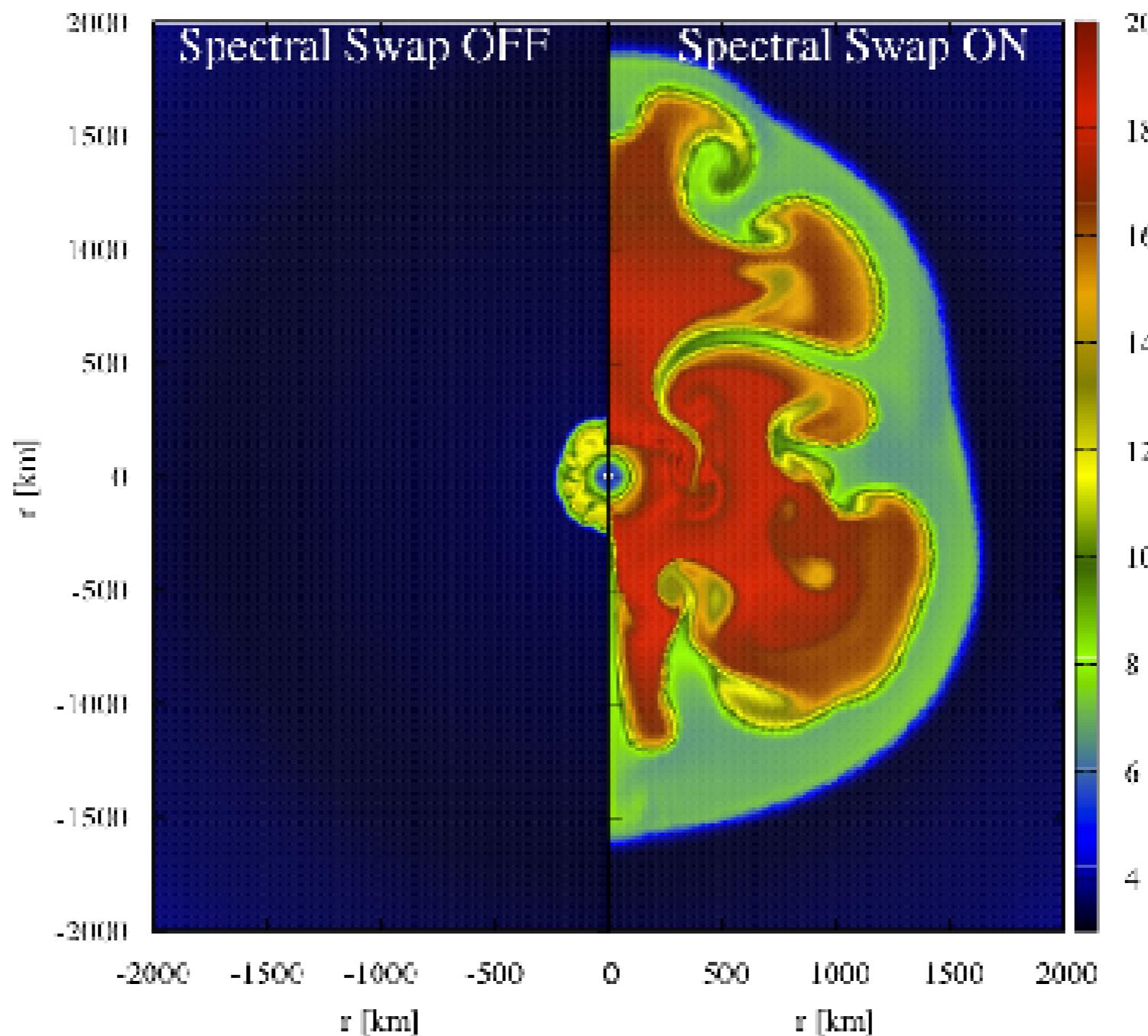
Fast conversions  $\Leftrightarrow$  different angular distributions of  $v_e$  and  $\bar{v}_e$



Favorable conditions are expected before  $v_e$  decoupling

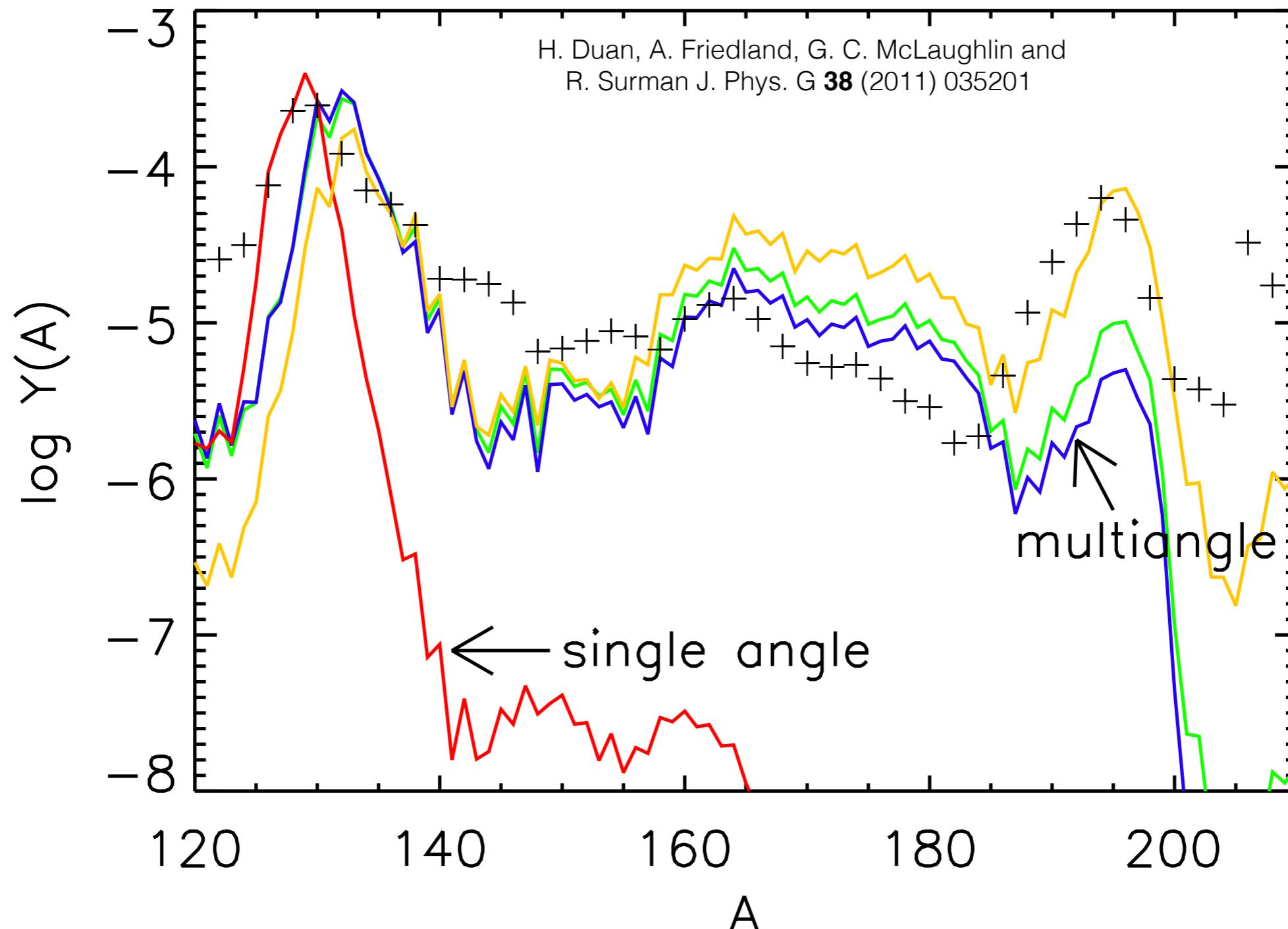
# Flavour conversions: why study them?

Impact on neutrino heating of the shock



# Flavour conversions: why study them?

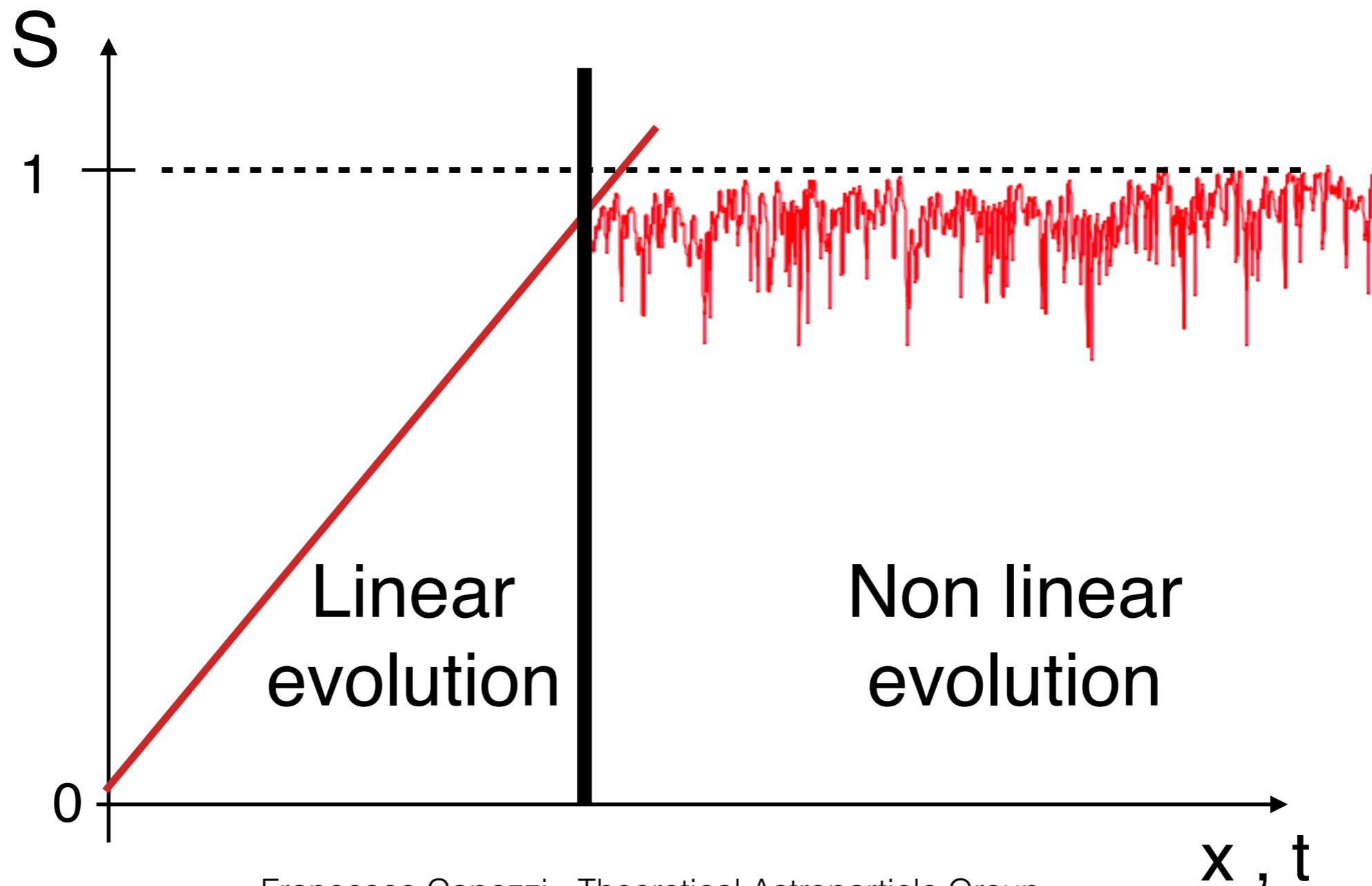
Impact on nucleosynthesis (r-process)



# Normal mode analysis

Self induced conversions can introduce a rapid growth of S

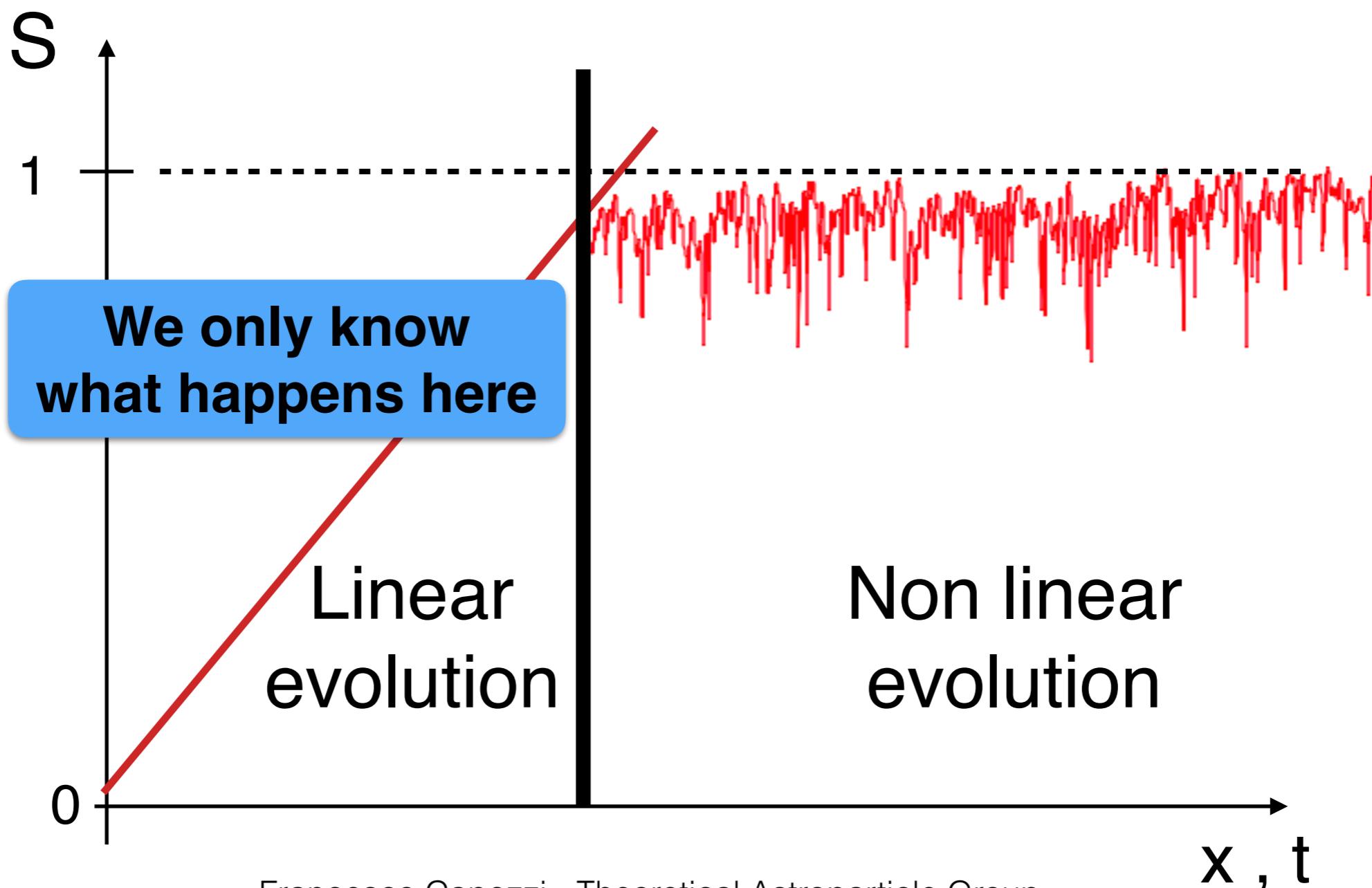
$$S_{\mathbf{v}}(t, \mathbf{x}) = Q_{\mathbf{v}} e^{i(\mathbf{k} \cdot \mathbf{x} - \omega t)}$$



# Normal mode analysis

Self induced conversions can introduce a rapid growth of S

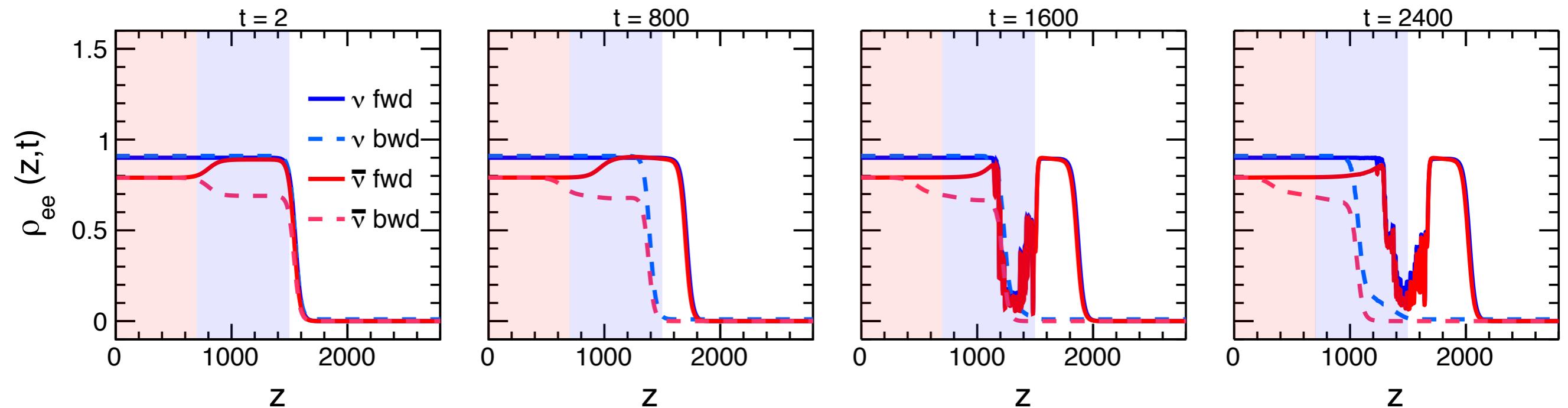
$$S_{\mathbf{v}}(t, \mathbf{x}) = Q_{\mathbf{v}} e^{i(\mathbf{k} \cdot \mathbf{x} - \omega t)}$$



# Numerical simulations: fast conversions

Simulation with toy model in 1 spatial + 1 temporal dimensions

F. Capozzi, B. Dasgupta, A. Mirizzi, M. Sen and G. Sigl, arXiv:1808.06618



After generating fast conversions, collisions are unimportant

# SN fluxes: parametrization

We adopt the following parametrisation:

$$F_\nu^0(E) = \Phi_\nu^0 f_\nu^0(E)$$

$$f_\nu^0(E) = \frac{1}{\langle E_\nu \rangle} \frac{(1 + \alpha_\nu)^{1 + \alpha_\nu}}{\Gamma(1 + \alpha_\nu)} \left( \frac{E}{\langle E_\nu \rangle} \right)^{\alpha_\nu} \exp \left[ -(1 + \alpha_\nu) \frac{E}{\langle E_\nu \rangle} \right]$$

$$\alpha_\nu = \frac{2\langle E_\nu \rangle^2 - \langle E_\nu^2 \rangle}{\langle E_\nu^2 \rangle - \langle E_\nu \rangle^2}$$

[1] M. Keil, G. G. Raffelt, and H.-T. Janka, *Astrophys. J.* **590**, 971–991 (2003)

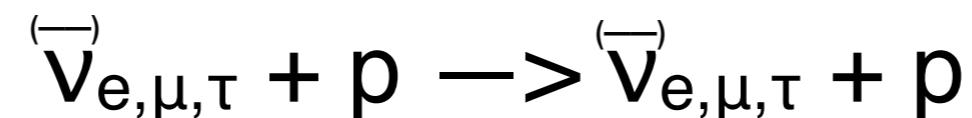
# SN fluxes: parametrization

## List of fit parameters for W and G models

Model	$\langle E_{\nu_e} \rangle$ (MeV)	$\langle E_{\nu_x} \rangle$ (MeV)	$\Phi_{\nu_e} (\times 10^{56})$	$\Phi_{\nu_x} (\times 10^{56})$	$\alpha_{\nu_e}$	$\alpha_{\nu_x}$
W	9.5	15.6	8.53	3.13	3.4	2.0
G	10.9	14.0	5.68	2.67	3.1	2.5

Model	$\langle E_{\bar{\nu}_e} \rangle$ (MeV)	$\langle E_{\bar{\nu}_x} \rangle$ (MeV)	$\Phi_{\bar{\nu}_e} (\times 10^{56})$	$\Phi_{\bar{\nu}_x} (\times 10^{56})$	$\alpha_{\bar{\nu}_e}$	$\alpha_{\bar{\nu}_x}$
W	11.6	15.6	7.51	3.13	4.0	2.0
G	13.2	14.0	4.11	2.67	3.3	2.5

# JUNO: $\nu$ -proton elastic scattering (pES)



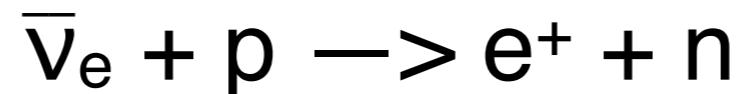
$$\frac{dN_{\text{pES}}}{dE_{\text{vis}}} = N_p \int_0^{+\infty} dT'_p \frac{dT_p}{dT'_p} W(T'_p, E_{\text{vis}}) \int_{E_\nu^0}^{\infty} dE_\nu F_{\text{pES}}(E_\nu) \frac{d\sigma_{\text{pES}}(E_\nu, T_p)}{dT_p}$$

$$F_{\text{pES}} \equiv 4F_{\nu_x}^0 + F_{\bar{\nu}_e}^0 + F_{\nu_e}^0$$

$$W(T'_p, E_{\text{vis}}) = \frac{\exp\left(-\frac{(T'_p - E_{\text{vis}})^2}{2\sigma_E^2}\right)}{\sqrt{2\pi}\sigma_E}$$

$$\frac{\sigma_E}{E_{\text{vis}}} = 0.03 \sqrt{E_{\text{vis}}/\text{MeV}}$$

# Hyper-Kamiokande: inverse $\beta$ decay

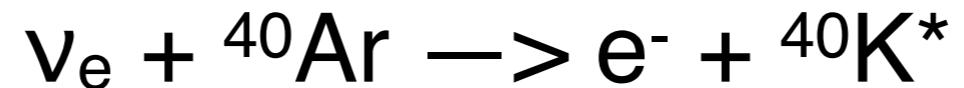


$$\frac{dN_{\text{IBD}}}{dE_{\text{vis}}} = N_p \int_{E_T}^{\infty} dE_{\nu} F_{\text{IBD}}(E_{\nu}) \sigma_{\text{IBD}}(E_{\nu}) W(E_{\nu} - 0.782 \text{ MeV}, E_{\text{vis}})$$

$$F_{\text{IBD}} \equiv \begin{cases} 0.7F_{\bar{\nu}_e}^0 + 0.3F_{\nu_x}^0 & \text{matter effects only, with NO} \\ F_{\nu_x}^0 & \text{matter effects only, with IO} \\ 0.33F_{\bar{\nu}_e}^0 + 0.66F_{\nu_x}^0 & \text{flavor eq.} \end{cases}$$

$$\frac{\sigma_E}{E_{\text{vis}}} = 0.6 \sqrt{E_{\text{vis}}/\text{MeV}}$$

# DUNE: $\nu$ -CC scattering on $^{40}\text{Ar}$ (ArCC)



$$\frac{dN_{\text{ArCC}}}{dE_{\text{vis}}} = N_{\text{Ar}} \sum_{i=1}^{N_{\text{ex}}} \int_0^\infty dE_\nu F_{\text{ArCC}}(E_\nu) \sigma_{\text{ArCC}}^i(E_\nu) W(E_{\text{vis}}, T_e)$$

$$F_{\text{ArCC}} \equiv \begin{cases} F_{\nu_x}^0 & \text{matter effects only, with NO} \\ 0.3F_{\nu_e}^0 + 0.7F_{\nu_x}^0 & \text{matter effects only, with IO} \\ 0.33F_{\nu_e}^0 + 0.66F_{\nu_x}^0 & \text{flavor equalization} \end{cases}$$

$$\sigma_E = 0.11 \sqrt{E_{\text{vis}}/\text{MeV}} + 0.02 E_{\text{vis}}/\text{MeV}$$

# Reconstructing $\nu$ flux from pES

We define the extrema and midpoint for the neutrino energy bins as  $[E_\nu^i, E_\nu^{i+1}]$  and  $\bar{E}_\nu^i$ , respectively, where  $E_\nu^i = \sqrt{T_p^i m_p}/2$

$$\left. \frac{d\tilde{F}_{\text{pES}}}{dE_\nu} \right|_{\bar{E}_\nu^N} = \frac{N_{\text{pES}}^N}{K_{NN}}$$

$$\left. \frac{d\tilde{F}_{\text{pES}}}{dE_\nu} \right|_{\bar{E}_\nu^i} = \left( N_{\text{pES}}^i + \sum_{j>i} \left. \frac{d\tilde{F}_{\text{pES}}}{dE_\nu} \right|_{\bar{E}_\nu^j} K_{ij} \right) / K_{i,i},$$

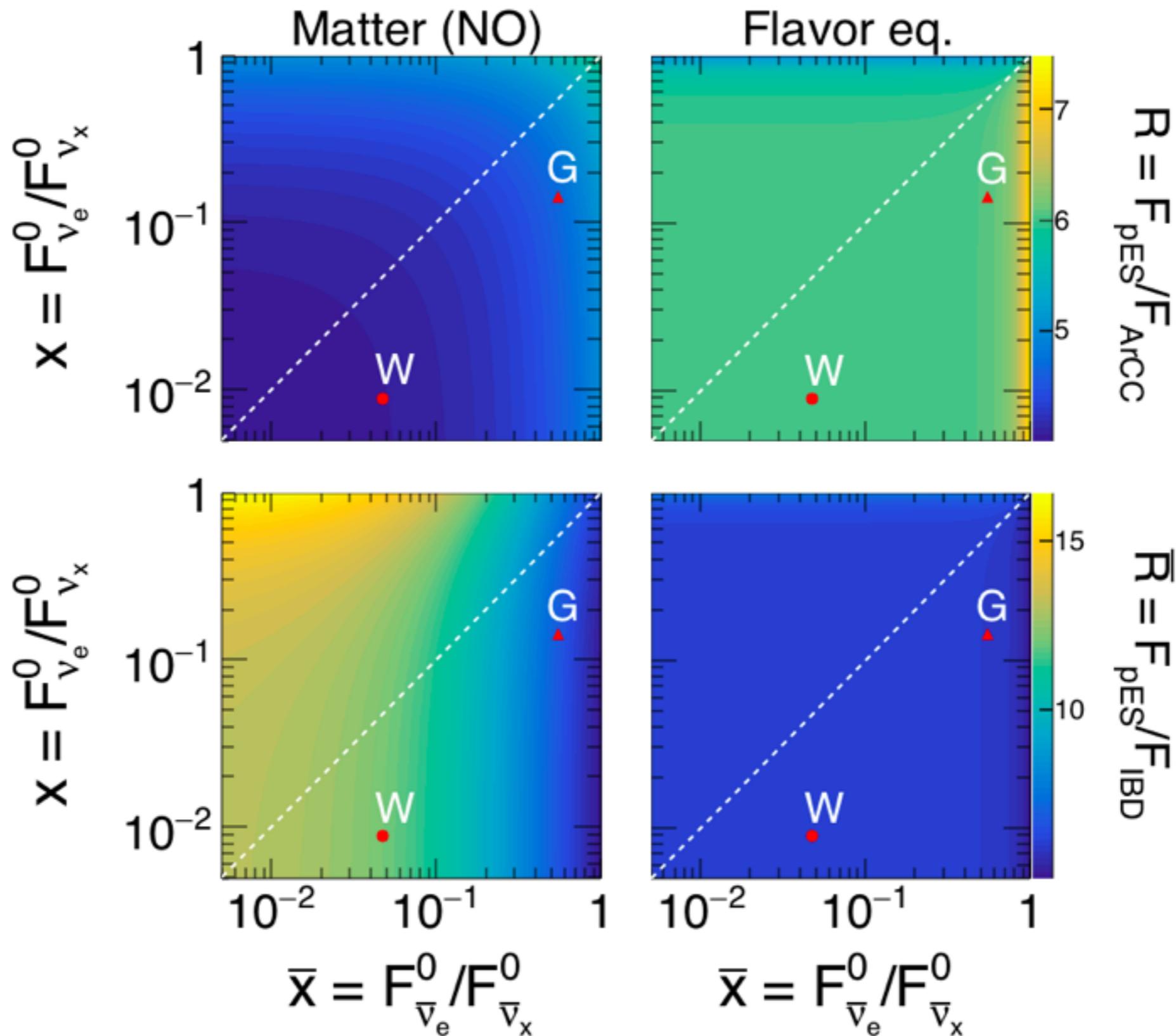
$$K_{i,j} = N_p \Delta T'_p \left. \frac{dT_p}{dT'_p} \right|_{\bar{T}'_p^i} \left. \frac{d\sigma_{\text{pES}}(E_\nu, T_p)}{dT_p} \right|_{(\bar{T}'_p^i, \bar{E}_\nu^j)}$$

# Reconstructing $\nu$ flux from IBD and ArCC

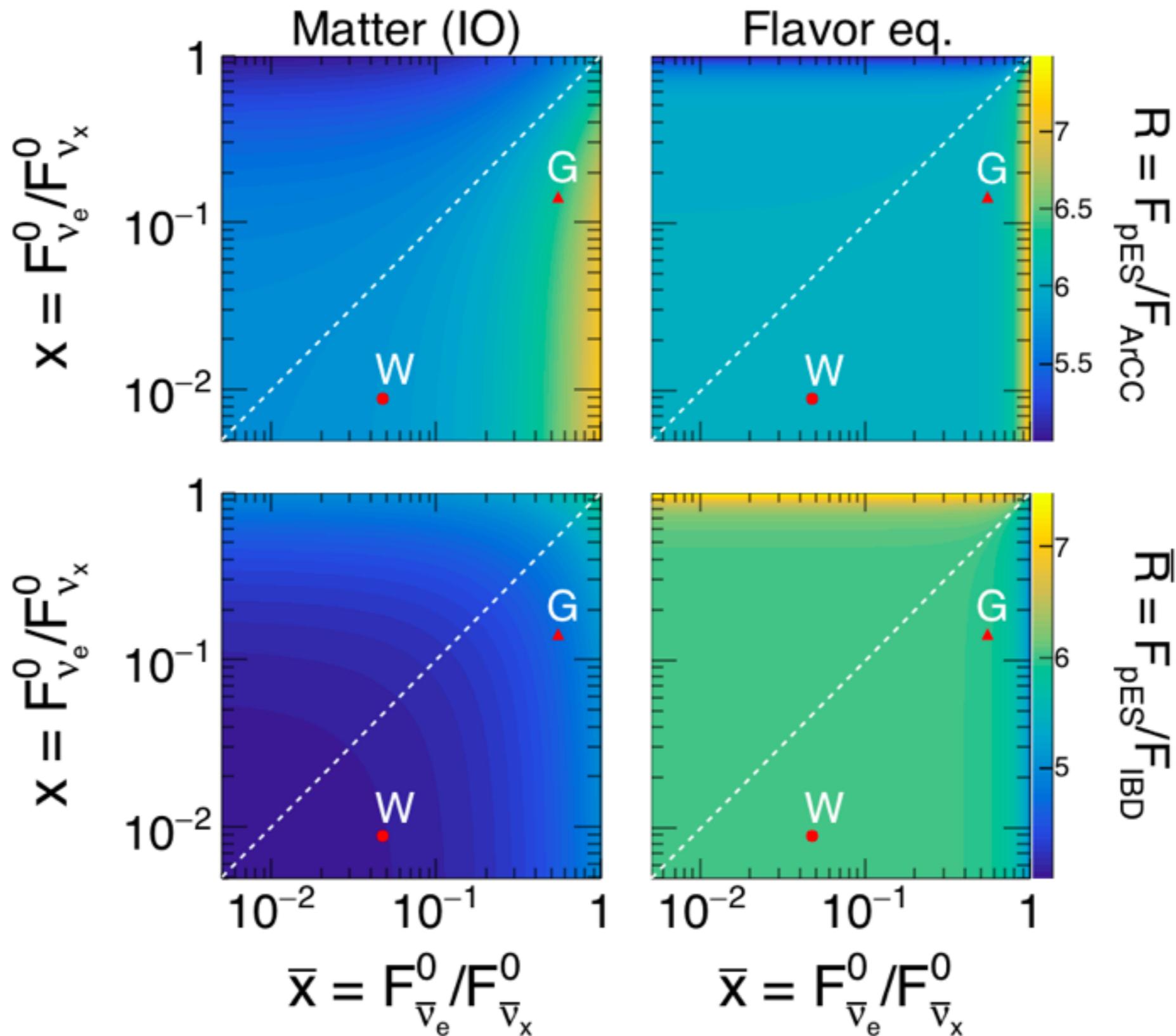
$$\frac{d\tilde{F}_{\text{IBD}}}{dE_\nu} \Big|_{\bar{E}_i} = \frac{1}{N_p \sigma_{\text{IBD}}^{\text{tot}}(\bar{E}_i)} \frac{N_{\text{IBD}}^i}{\Delta E_{\text{vis}}^i}$$

$$\frac{d\tilde{F}_{\text{ArCC}}}{dE_\nu} \Big|_{\bar{E}_i} = \frac{1}{N_{\text{Ar}} \sigma_{\text{ArCC}}^{\text{tot}}(\bar{E}_i)} \frac{N_{\text{ArCC}}^i}{E_{\text{vis}}^i}$$

# Flux ratios: R and $\bar{R}$ , normal ordering

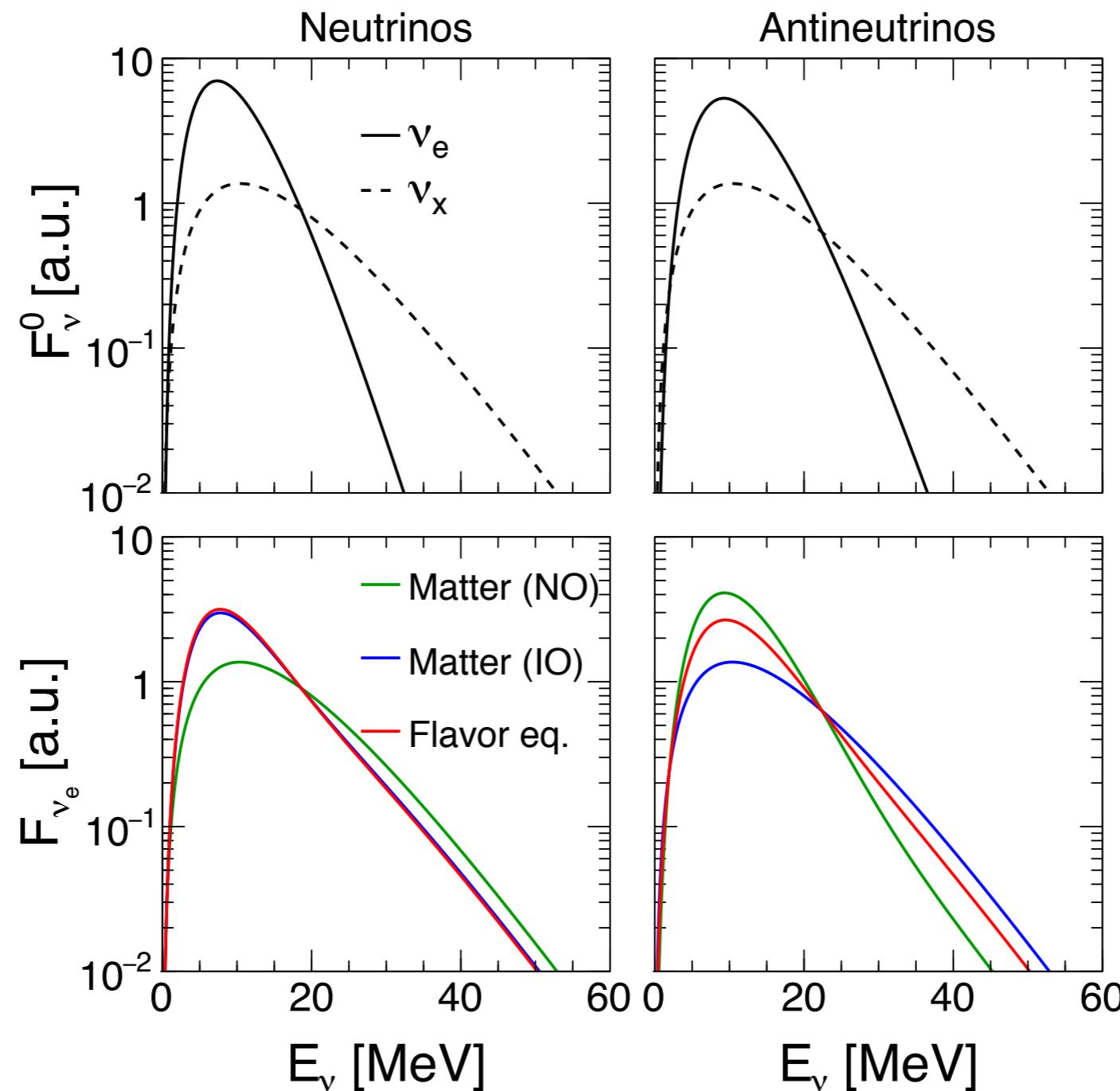


# Flux ratios: R and $\bar{R}$ , inverted ordering



# SN fluxes: Wroclaw/Basel 1D model (W)

## (Un)Oscillated (Anti)Neutrino energy fluxes

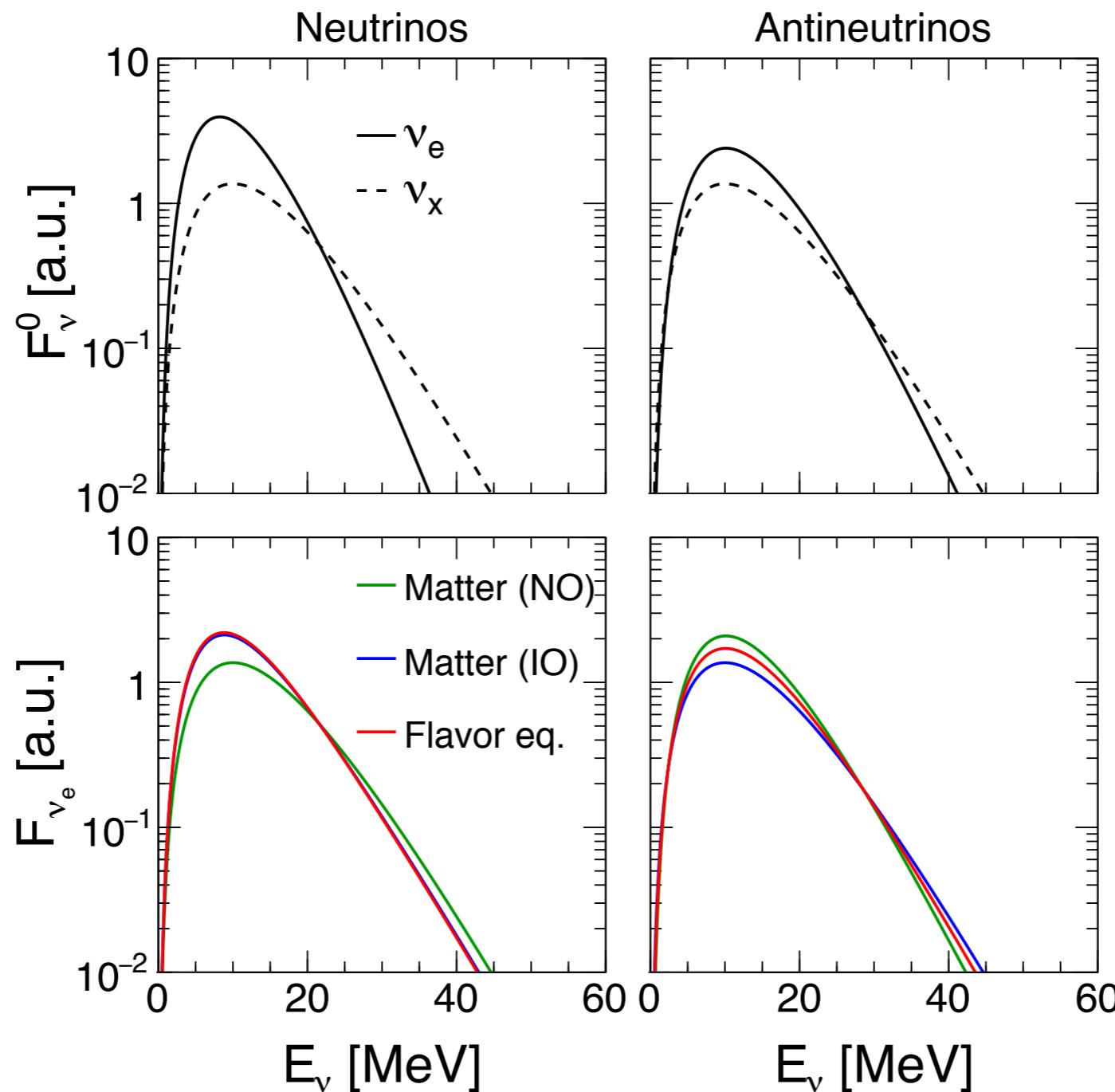


Fit parameters from:  
Fischer, et al.,  
Astron. Astrophys. **517**, A80 (2010)

In NO differences in  $P_{ee}$  for both  $\nu$  and  $\bar{\nu}$

# SN fluxes: Garching 1D model (G)

(Un)Oscillated (Anti)Neutrino energy fluxes

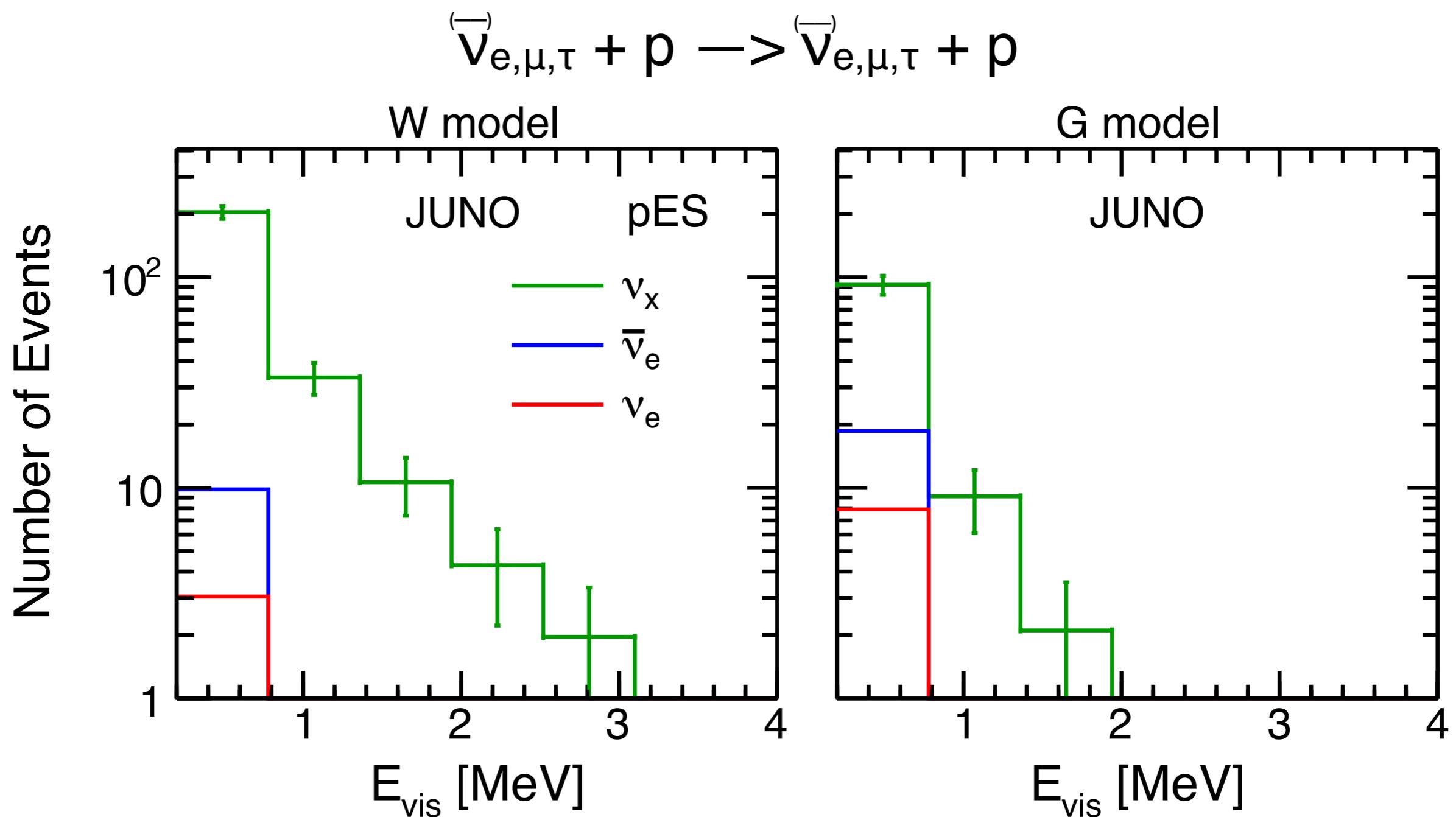


Fit parameters from:  
Serpico, *et al.*,  
Phys. Rev. D**85**, 085031 (2012)

Smaller differences compared to W model

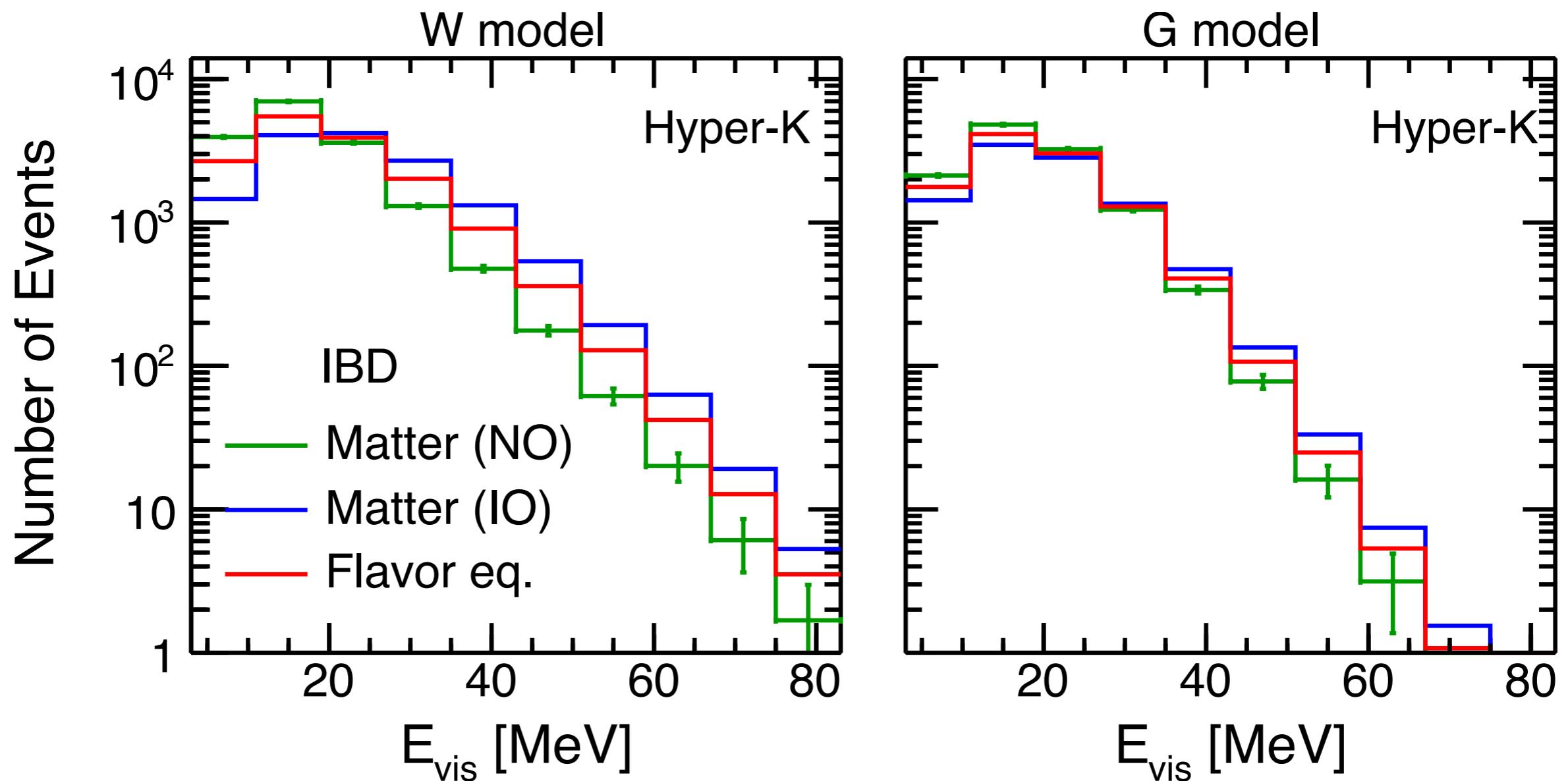
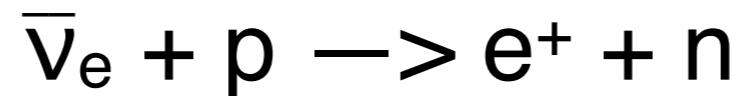
# 1) Three SNv detection channels

# JUNO: $\nu$ -proton elastic scattering (pES)



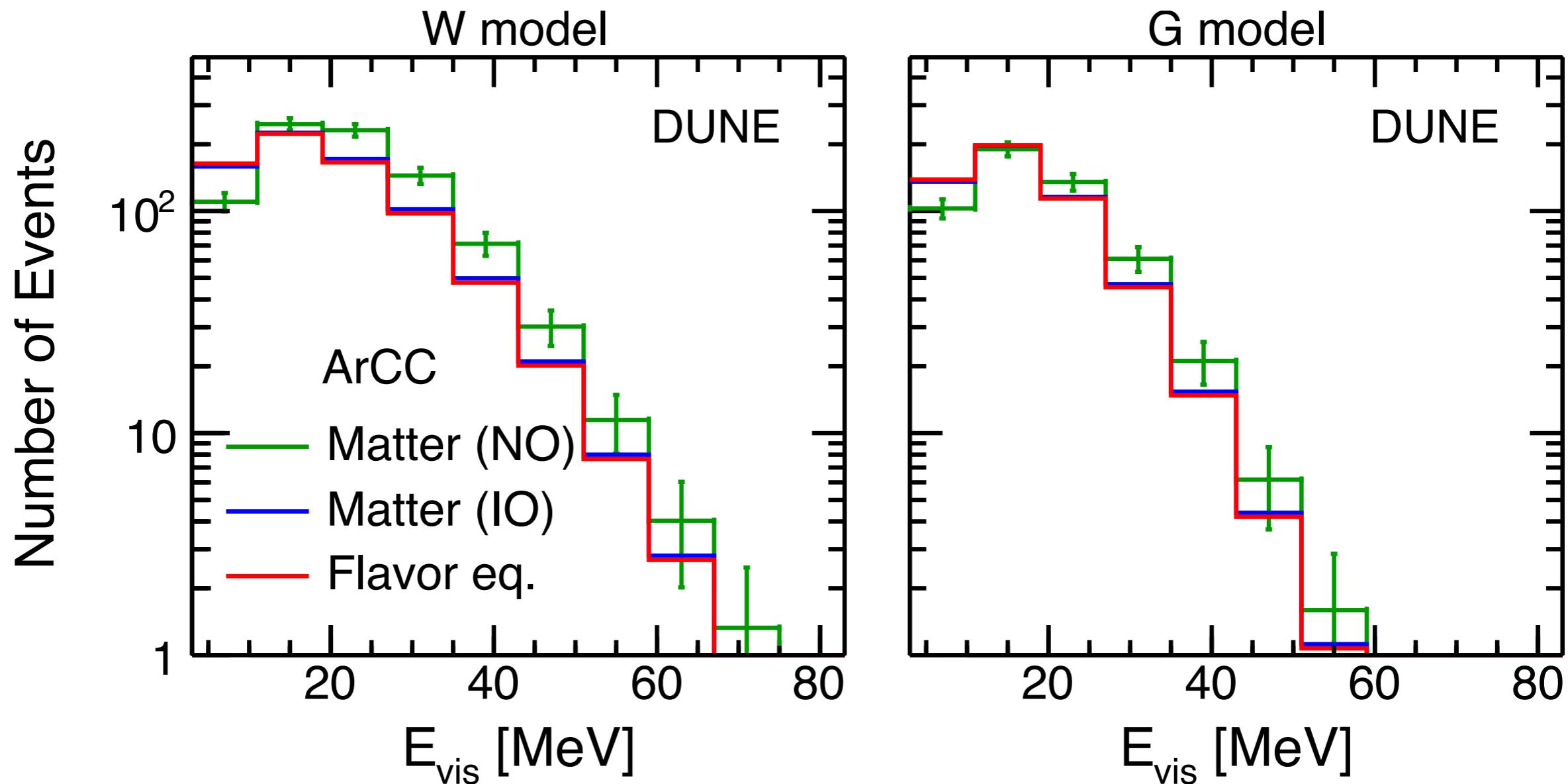
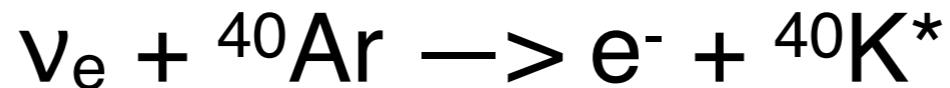
JUNO is sensitive mainly to  $\nu_x$  and to  $E_\nu > 25$  MeV.  
No dependence on flavour conversions

# Hyper-Kamiokande: inverse $\beta$ decay



Hyper-K is sensitive to  $\bar{\nu}_e$

# DUNE: $\nu$ -CC scattering on $^{40}\text{Ar}$ (ArCC)



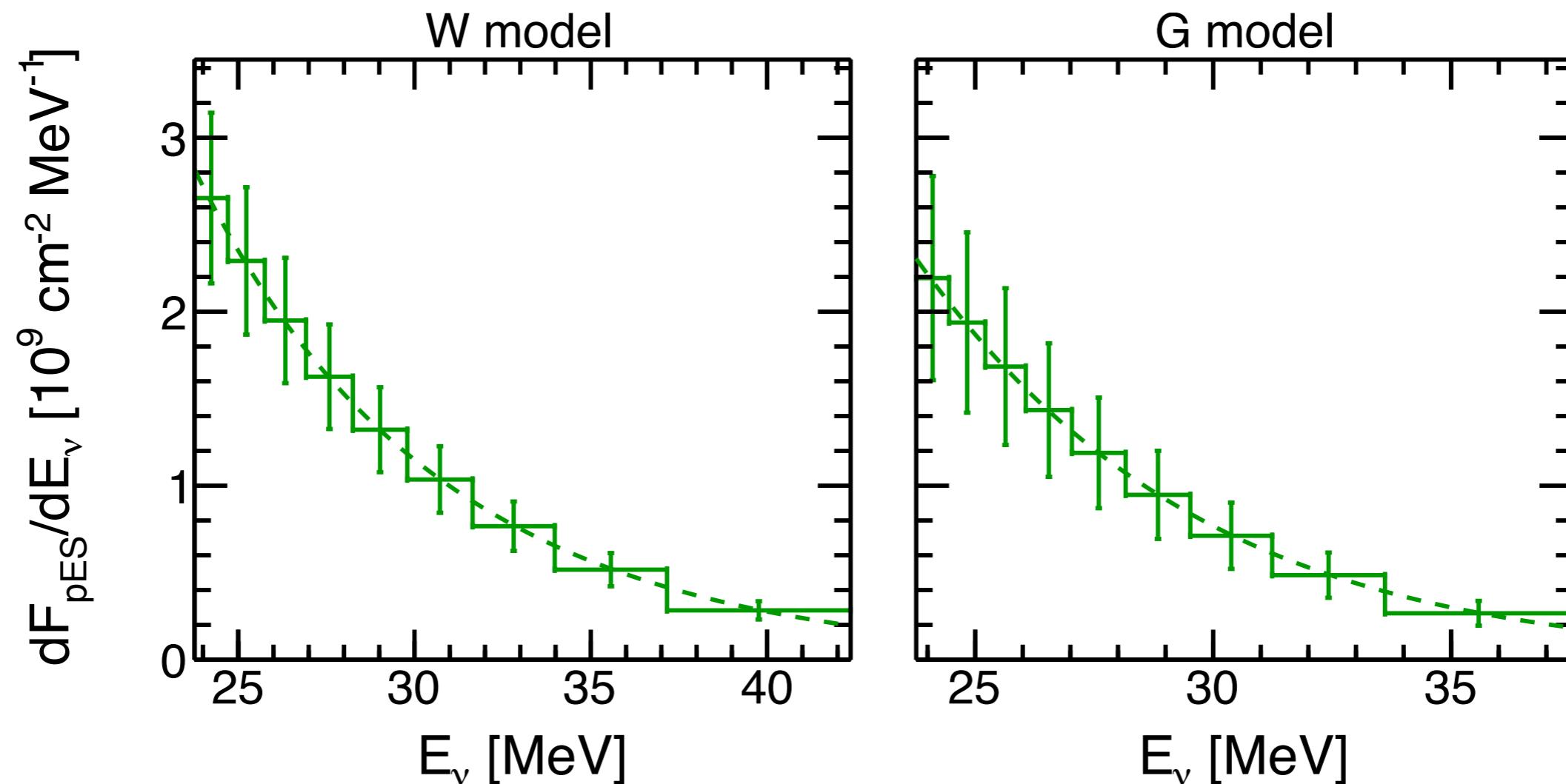
DUNE is sensitive to  $\nu_e$

# 2) Reconstructing oscillated $\nu$ -fluxes

# Reconstructing $\nu$ flux from pES

$$\frac{N_i}{\Delta E_{\text{vis}}^i} \rightarrow \frac{dF_{\text{pES}}}{dE_\nu} \underset{\sim}{\simeq} \frac{dF_{\nu_x}}{dE_\nu}$$

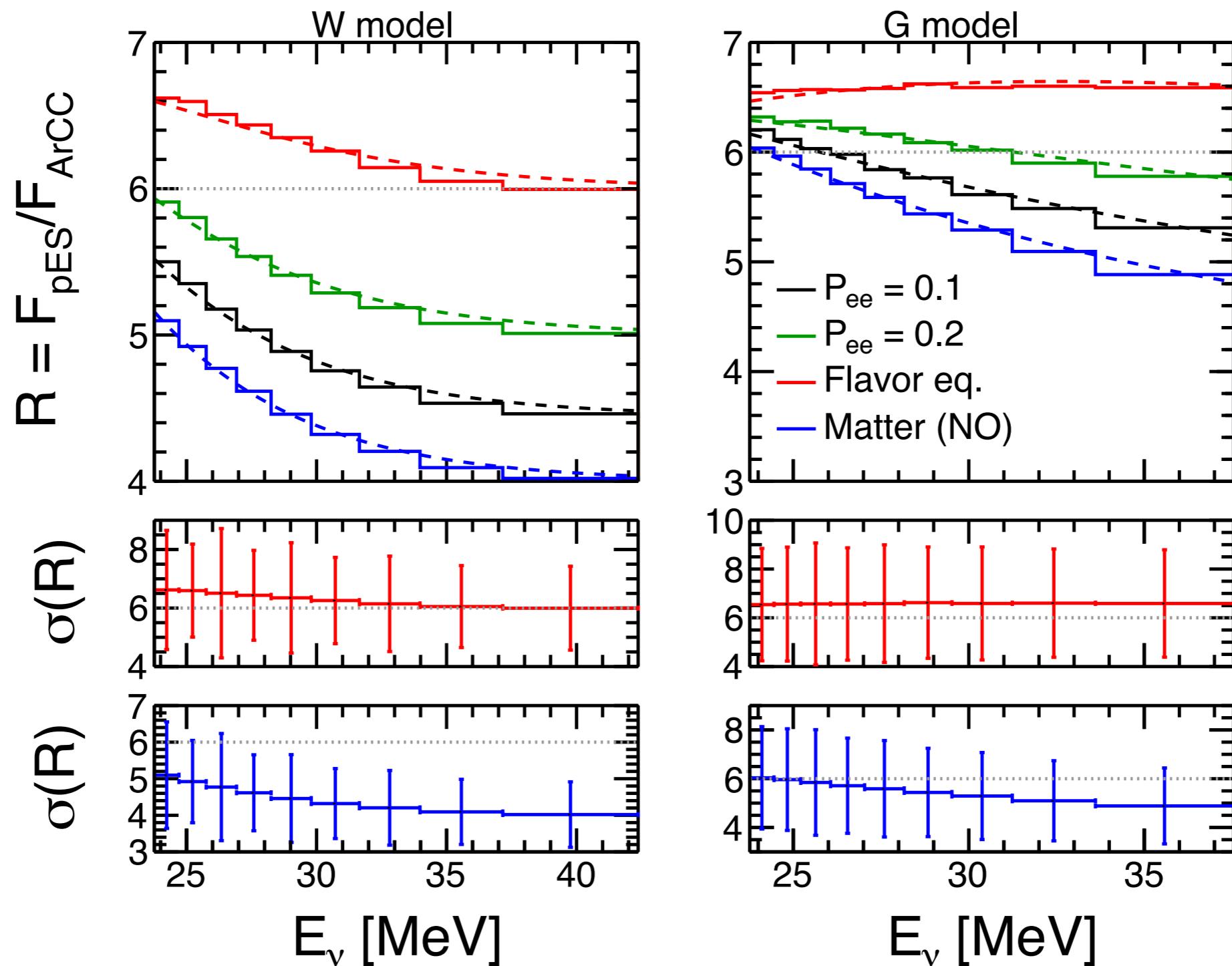
- [1] H. L. Li, Y. F. Li, M. Wang, L. J. Wen and S. Zhou, Phys. Rev. D **97** (2018) no.6, 063014
- [2] B. Dasgupta and J. F. Beacom, Phys. Rev. D **83** (2011) 113006



Similar reconstruction method applies to IBD and ArCC

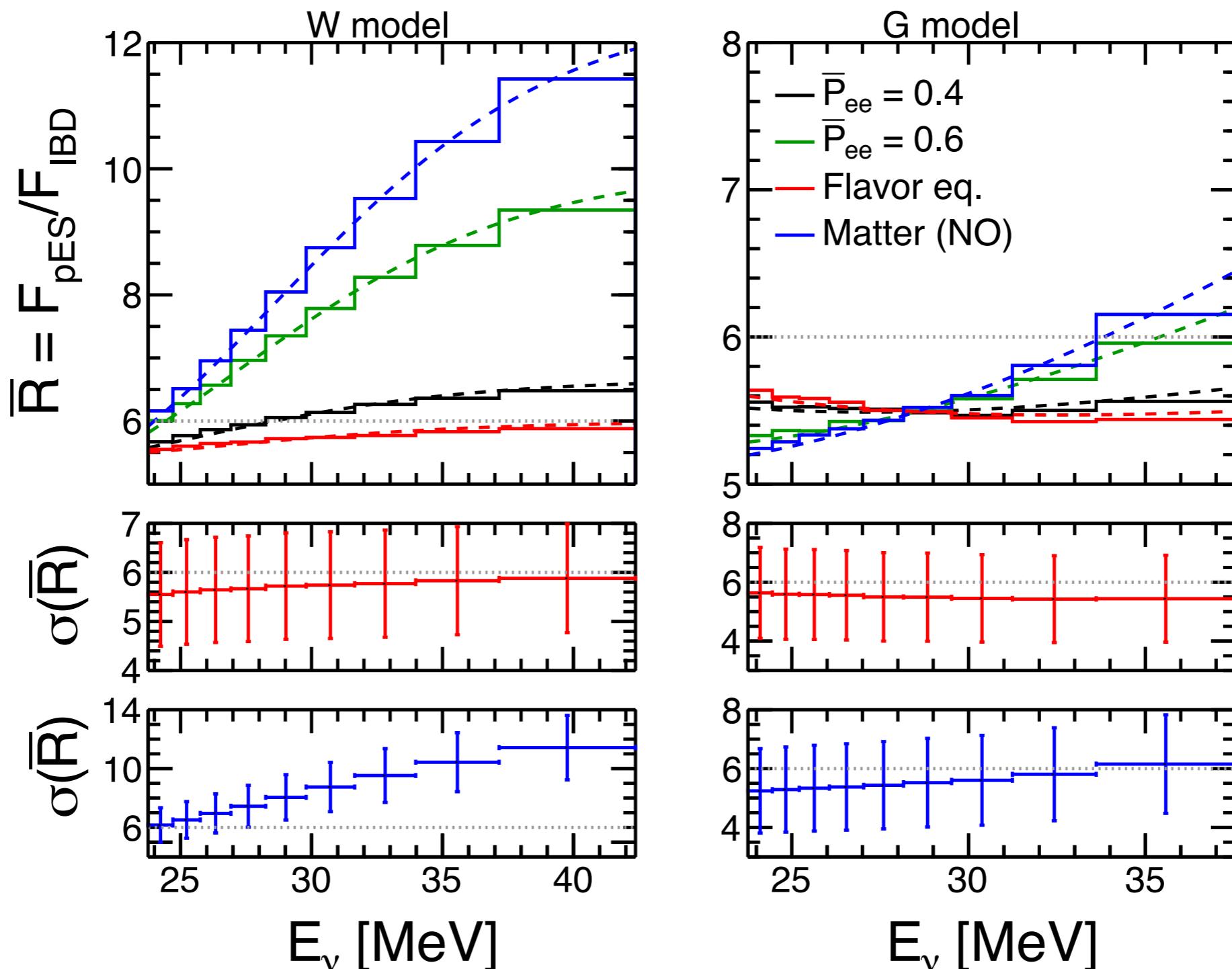
# 3) Flux ratios:

# Statistical significance: R at 10 kpc



In the case of pure “matter effects” we can disfavour flavour equalisation at  $\sim 2\sigma$  (only for W model)

# Statistical significance: $\bar{R}$ at 10 kpc



In the case of pure “matter effects” we can disfavour flavour equalization at  $>\sim 2\sigma$  (only for W model)