

Status of the MPI Time-Dependent Analysis

Vladimir Chekelian, MPI group meeting 10.01.2019

methodological goal: development of the dt resolution function to make use of PXD
physics topics: time-dependent CP asymmetry, lifetimes, mixing & oscillations
method: unbinned maximum likelihood fits of $\Delta t = t(B_{sig}) - t(B_{tag})$ distr.
maximum $L = \prod_i P(\Delta t_i, \text{physics \& event reco parameters})$
framework: RooFit package in Root

The event probability density function (PDF) is a convolution of a true physics PDF and a resolution function $R_{sig, bkg}(\Delta t - \Delta t')$:

$$P_{sig, bkg}(\Delta t) = \int_{-\infty}^{+\infty} d(\Delta t') \wp_{sig, bkg}(\Delta t') R_{sig, bkg}(\Delta t - \Delta t')$$

Status:

- 1. First (unrealistic) shots for $R_{sig}(\Delta t - \Delta t')$ with $\Delta t(\text{true})$ used as a parameter.*
- 2. First experience with fits of the time-dependent CP asymmetry for B_0 & $B_0\text{bar}$*
 - fit activates only the first free parameter, the others keep initial values*
 - extreme time consumption to make model distribution for comparison with data (>50 hours for one histo with 72 bins)*

Model for the Δt Resolution Function

Resolution Function $R_{\text{sig, bkg}}(\Delta t - \Delta t')$:

- defined within the RooFit package in Root
- based on event properties, e.g. $\delta_i(\Delta t)$ – uncertainty of Δt_{rec} in event “i”.
- obtained by fitting of the Δt -pull distributions $\rightarrow (\Delta t_{i,\text{rec}} - \Delta t_{i,\text{true}}) / \delta_i(\Delta t)$
- Δt resolution function is a transformation of the Δt -pull shape description:

Δt -pull model $\rightarrow \Delta t$ resolution function

Gauss: $\Delta t_{\text{Pull}} \rightarrow \Delta t * \delta_{\text{ev}}(\Delta t)$, $\mu_{\text{Pull}} \rightarrow \mu_{\text{Pull}} * \delta_{\text{ev}}(\Delta t)$, $\sigma_{\text{Pull}} \rightarrow \sigma_{\text{Pull}} * \delta_{\text{ev}}(\Delta t)$

- Δt -pulls are fitted by three gaussian functions:

$$f_1 * G_1(\Delta t_{\text{Pull}}, \mu_1, \sigma_1) + f_2 * G_2(\Delta t_{\text{Pull}}, \mu_2, \sigma_2) + (1 - f_1 - f_2) * G_3(\Delta t_{\text{Pull}}, \mu_3, \sigma_3)$$

8 [10] free parameters:

$$G_1: \quad \mu_1 = c0 + c1 * \delta_{\text{ev}}(\Delta t) [+ c2 * \Delta t(\text{true})], \quad c0, c1, [c2]$$

$$\quad \sigma_1 = s0 + s1 * \delta_{\text{ev}}(\Delta t) [+ s2 * \Delta t(\text{true})], \quad s0, s1, [s2]$$

$$G_2: \quad \mu_2, \sigma_2$$

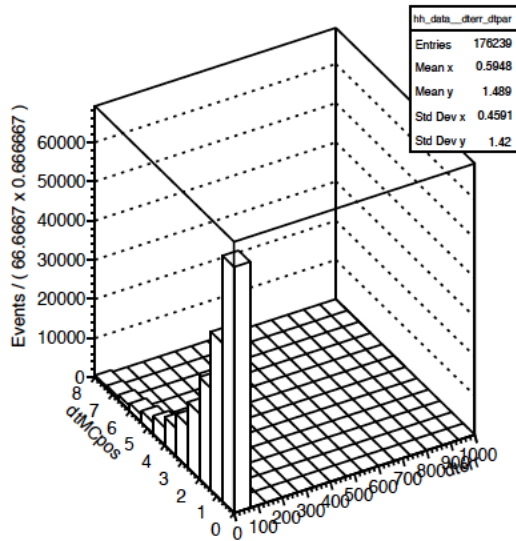
$$G_3: \quad \mu_3 = 0., \sigma_3 = 8. \text{ are fixed}$$

$$\text{Fractions:} \quad f_1, f_2$$

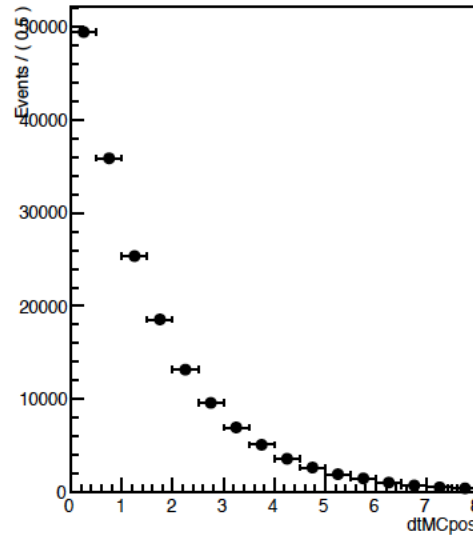
\rightarrow Fitted separately in positive and negative $\Delta t(\text{true})$ domains; $c2, s2$ are added only for $\Delta t(\text{true}) < 0$.

Model for Δt -pull at positive $\Delta t(\text{true})$

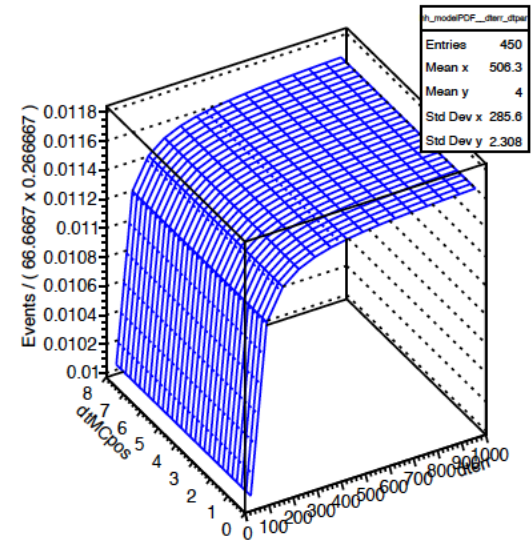
Histogram of hh_data_dterr_dtpar



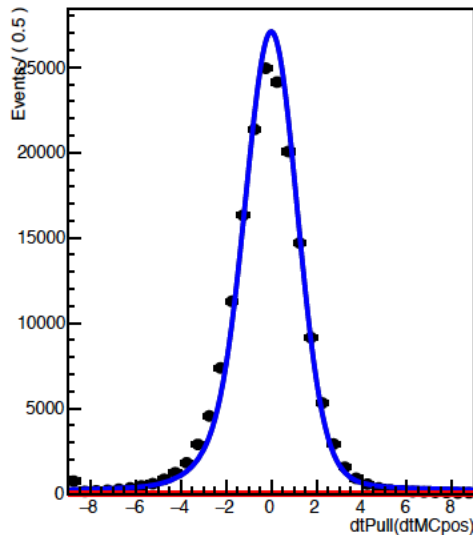
Projection of (dtPull|dtpar) on dtpar



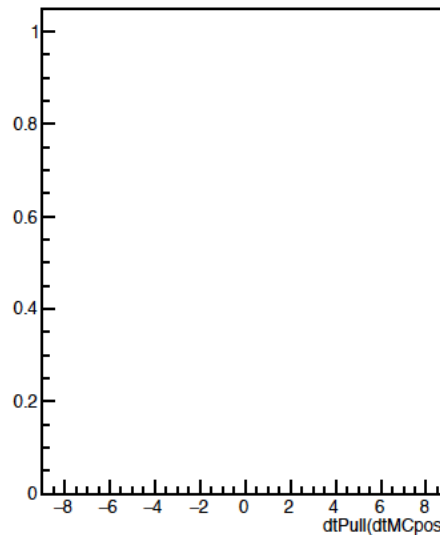
Histogram of hh_modelPDF_dterr_dtpar



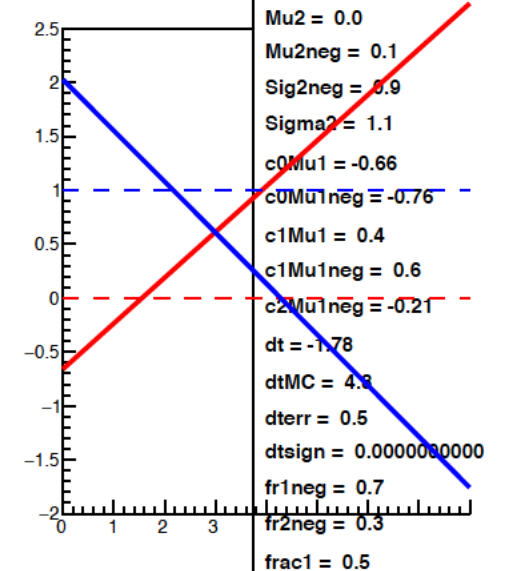
Projection of (dtPull|dtpar) on dtPull



modelPDF: dtpar=min,middle,max

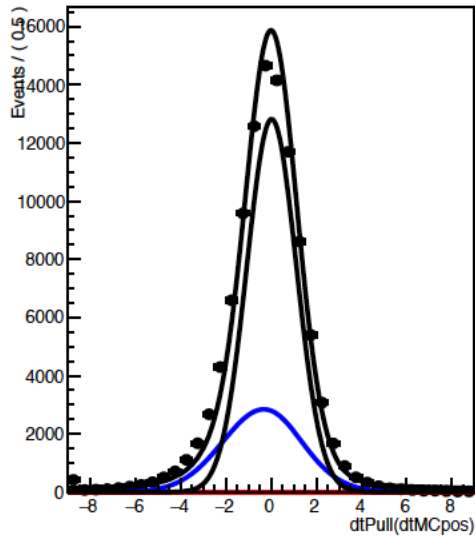


Mu1 (red), Sigma1=a+b*x

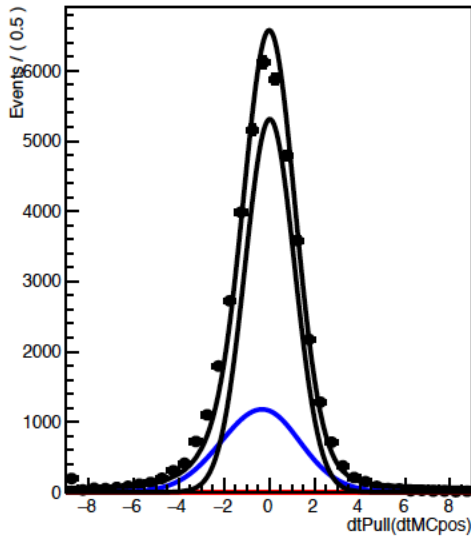


Model for Δt -pull at positive $\Delta t(\text{true})$

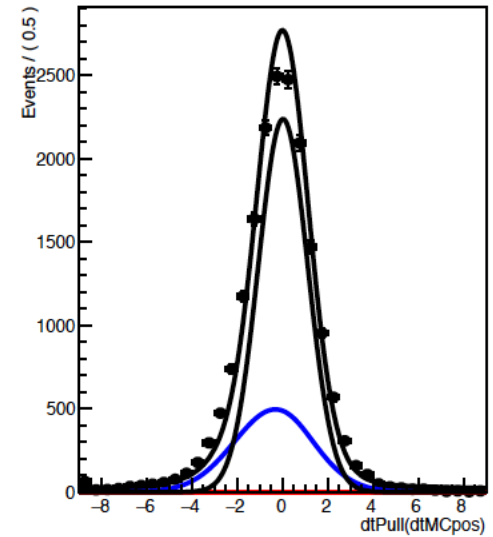
dtPull: 1st slice (of 6) in dtpar



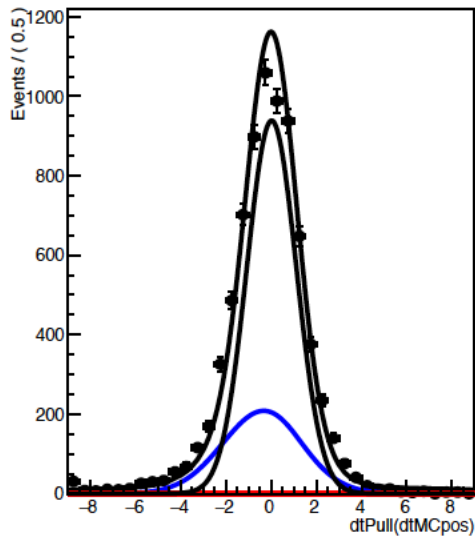
dtPull: 2nd slice (of 6) in dtpar



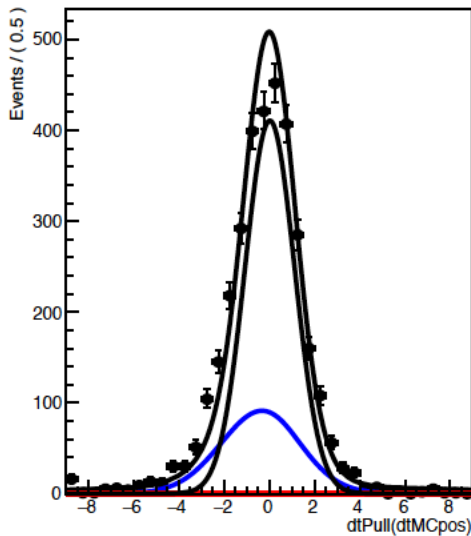
dtPull: 3rd slice (of 6) in dtpar



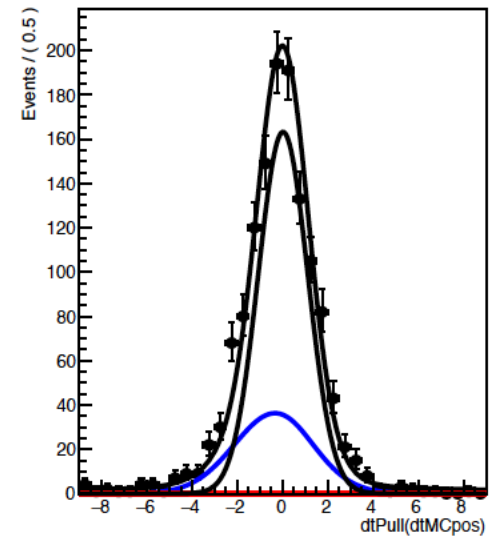
dtPull: 4th slice (of 6) in dtpar



dtPull: 5th slice (of 6) in dtpar

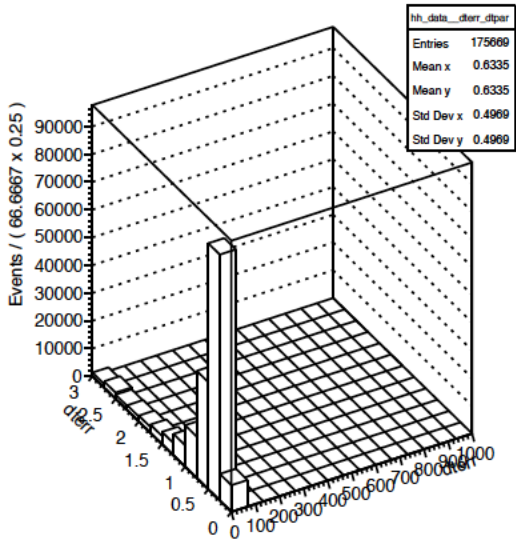


dtPull: 6th slice (of 6) in dtpar

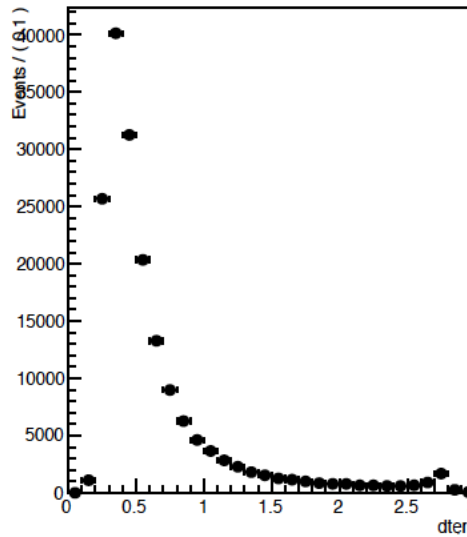


Model for Δt -pull at negative $\Delta t(\text{true})$

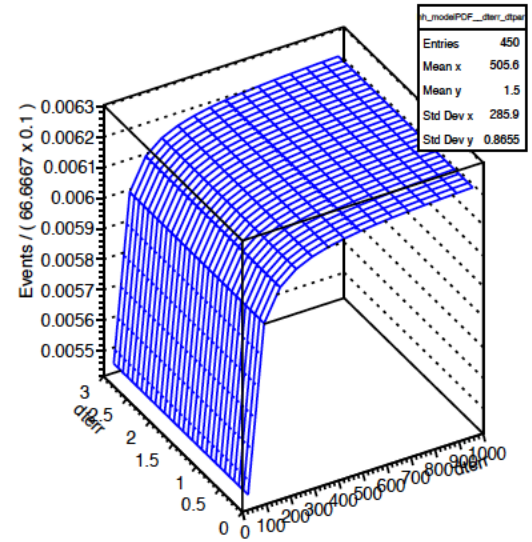
Histogram of hh_data_dtterr_dtpar



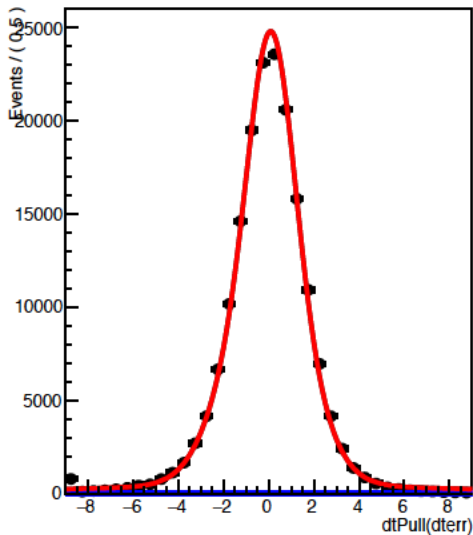
Projection of (dtPull|dtpar) on dtpar



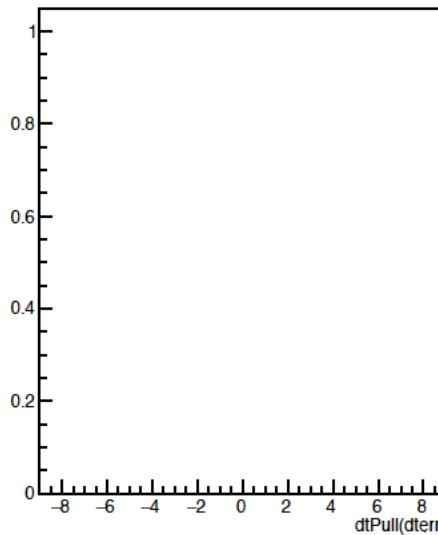
Histogram of hh_modelPDF_dtterr_dtpar



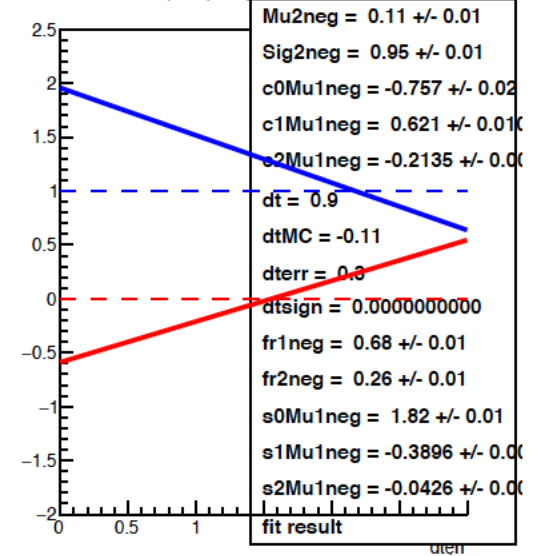
Projection of (dtPull|dtpar) on dtPull



modelPDF: dtpar=min,middle,max

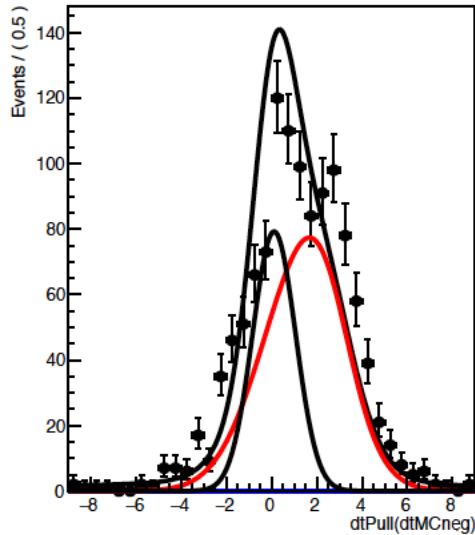


Mu1 (red), Sigma1 = a+b*x

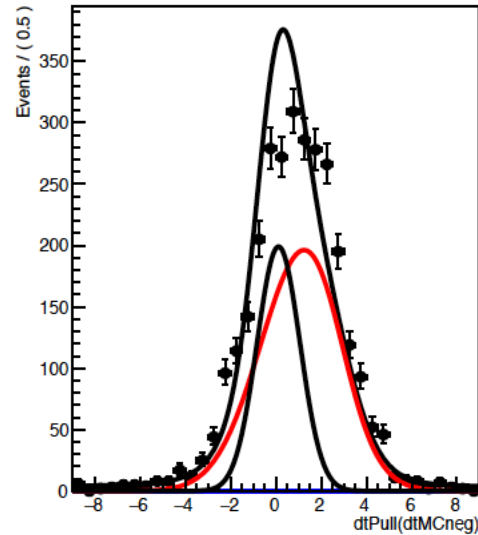


Model for Δt -pull at negative $\Delta t(\text{true})$

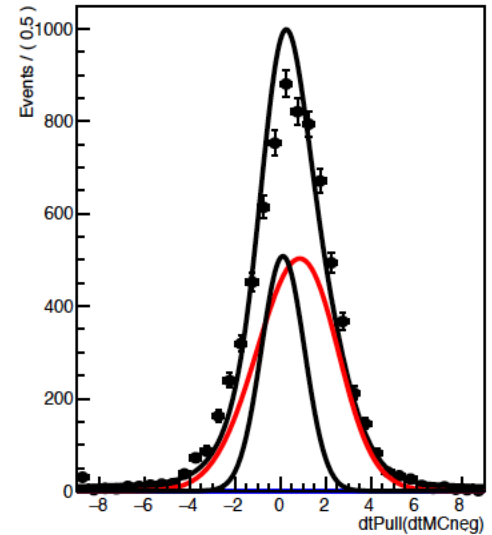
dtPull: 1st slice (of 6) in dtpar



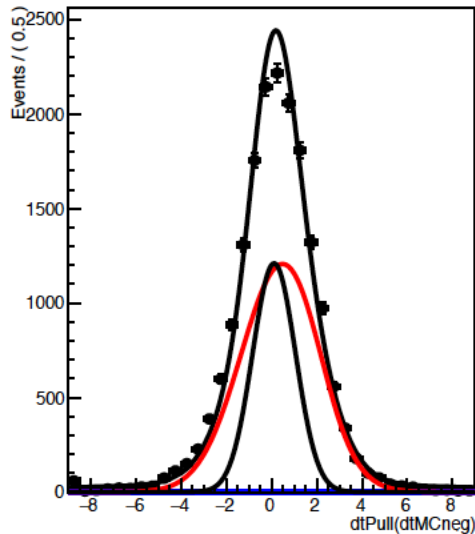
dtPull: 2nd slice (of 6) in dtpar



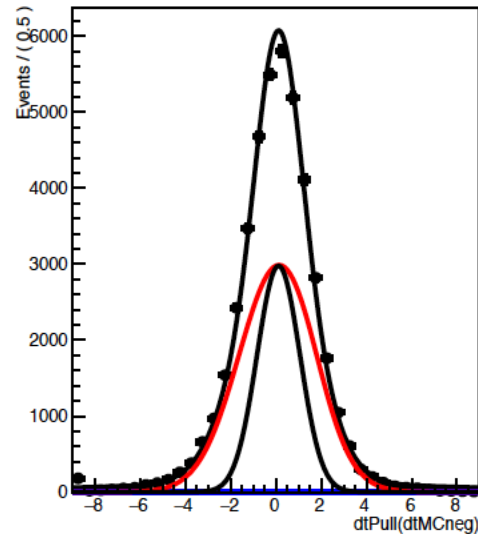
dtPull: 3rd slice (of 6) in dtpar



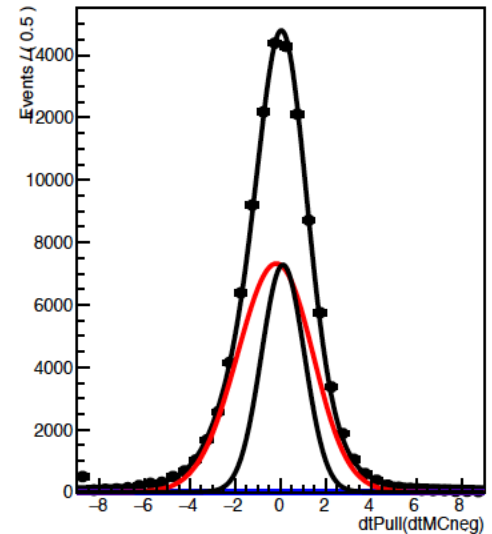
dtPull: 4th slice (of 6) in dtpar



dtPull: 5th slice (of 6) in dtpar

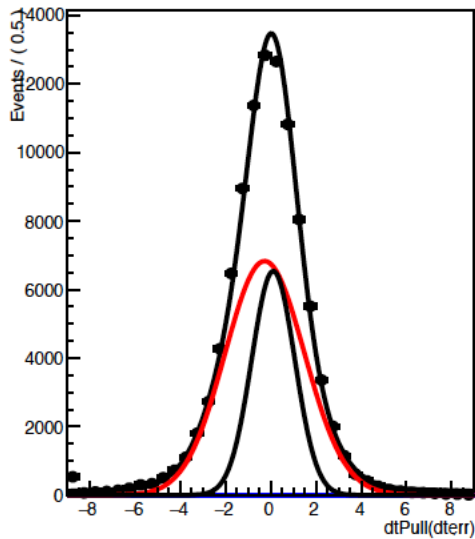


dtPull: 6th slice (of 6) in dtpar

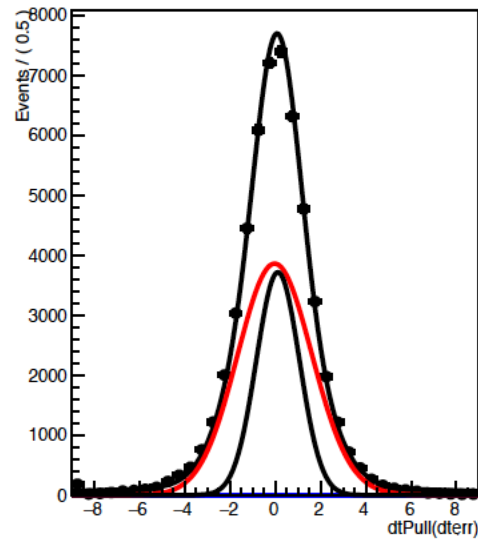


Model for Δt -pull at negative $\Delta t(\text{true})$

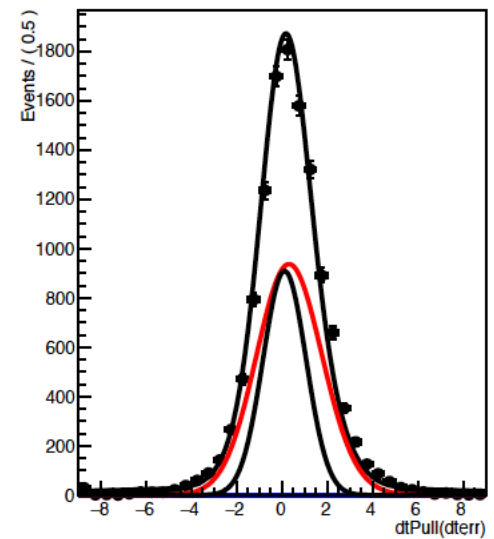
dtPull: 1st slice (of 6) in dtpar



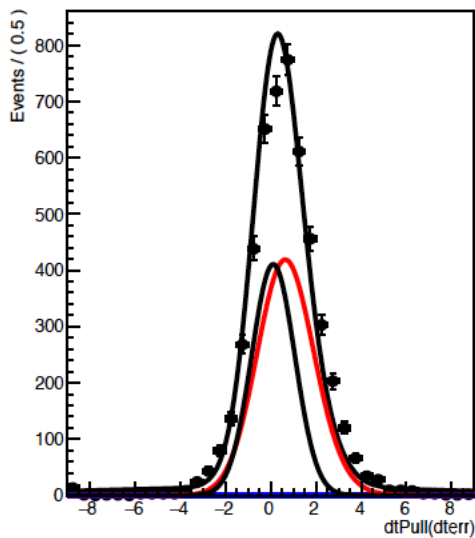
dtPull: 2nd slice (of 6) in dtpar



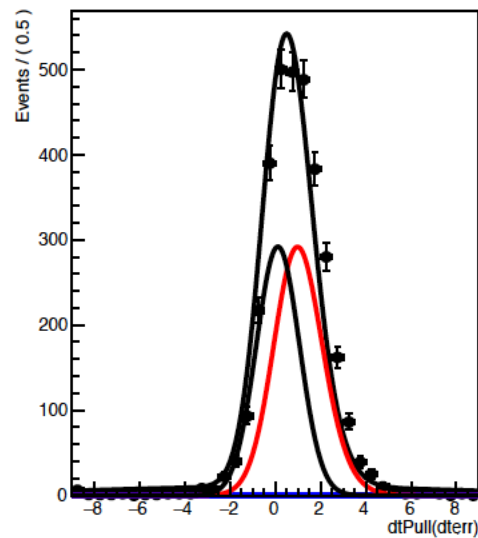
dtPull: 3rd slice (of 6) in dtpar



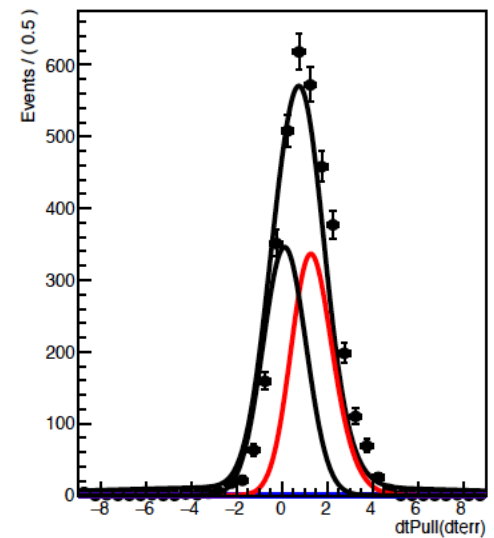
dtPull: 4th slice (of 6) in dtpar



dtPull: 5th slice (of 6) in dtpar



dtPull: 6th slice (of 6) in dtpar



Fit of the Δt Distributions for B^0 & B^0 bar

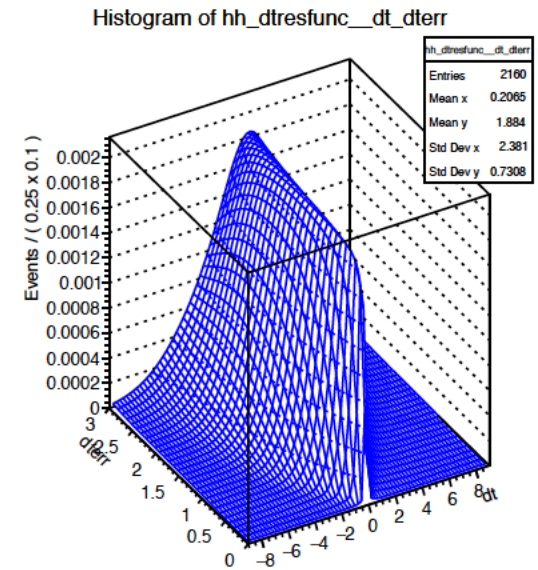
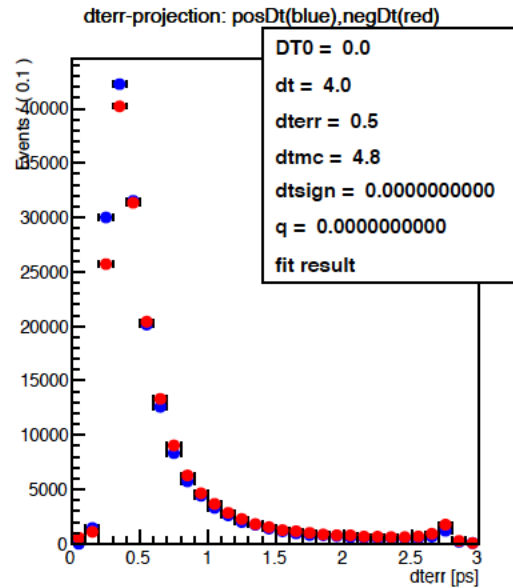
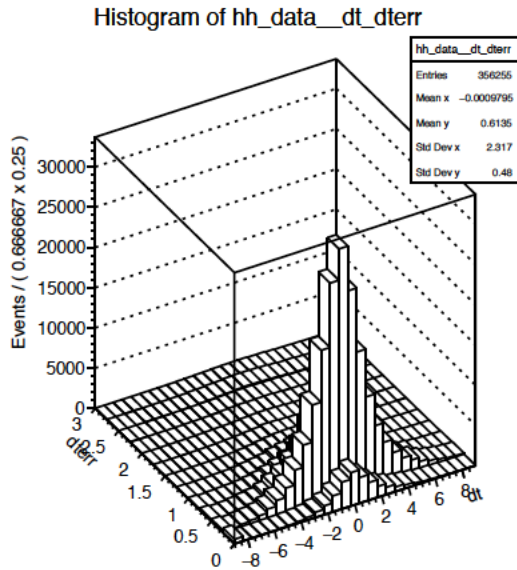
→ Time dependent analyses:

unbinned maximum likelihood fit to $\Delta t = t_{B^{sig}} - t_{B^{tag}}$

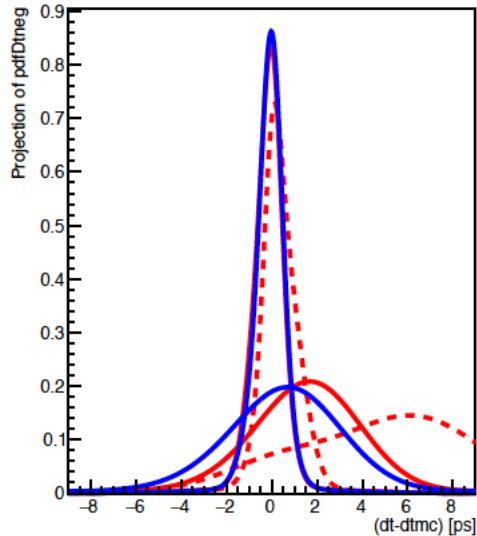
maximum $L = \prod_i P(\Delta t_i, \text{physics \& event reco parameters})$, where

$$P_{sig, bkg}(\Delta t) = \int_{-\infty}^{+\infty} d(\Delta t') \phi_{sig, bkg}(\Delta t') R_{sig, bkg}(\Delta t - \Delta t')$$

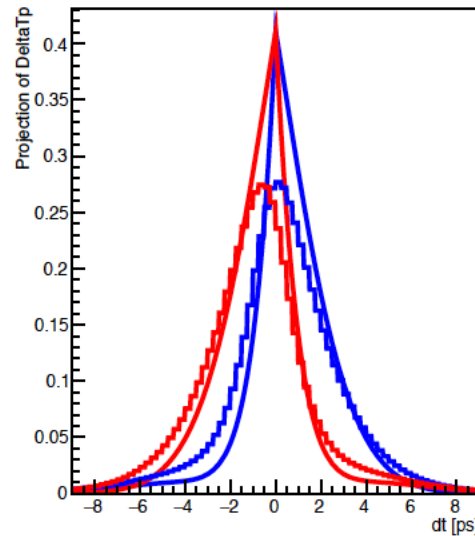
Fit of the Δt Distributions for B0&B0bar



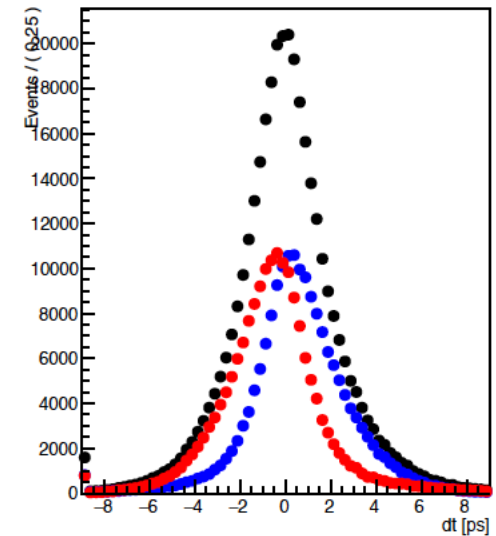
dt resolution function



DeltaTp(blue) & DeltaTm(red)

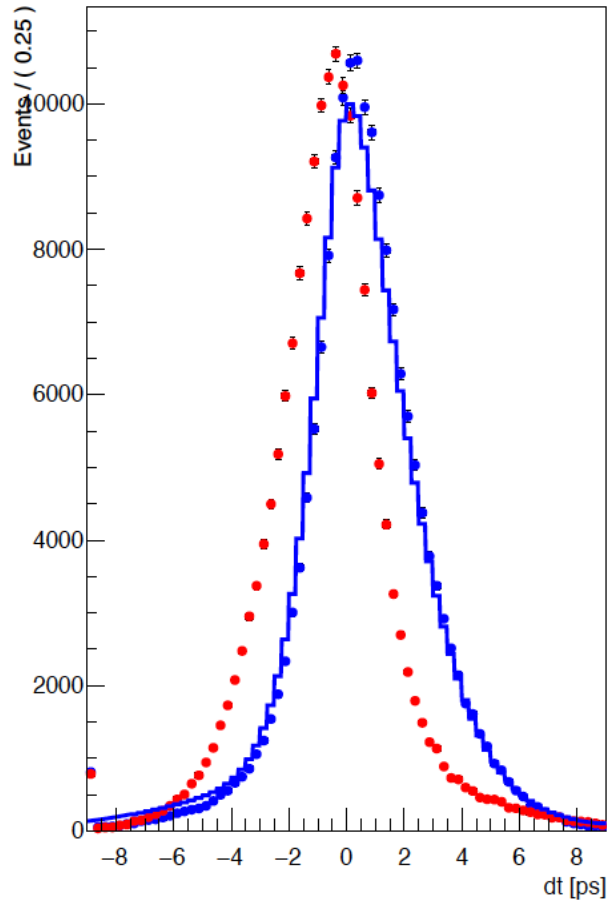


B0tag(blue) + B0tagBar(red)



Fit of the Δt Distributions for B^0 & $B^0\text{bar}$

$B^0\text{tag}(q=1,\text{blue}), B^0\text{tagBar}(-1,\text{red})$



$B^0\text{tag}(q=1,\text{blue}), B^0\text{tagBar}(-1,\text{red})$

