

# Constrained fits for $t\bar{t}$ event selection and top mass determination in the electron + jets channel

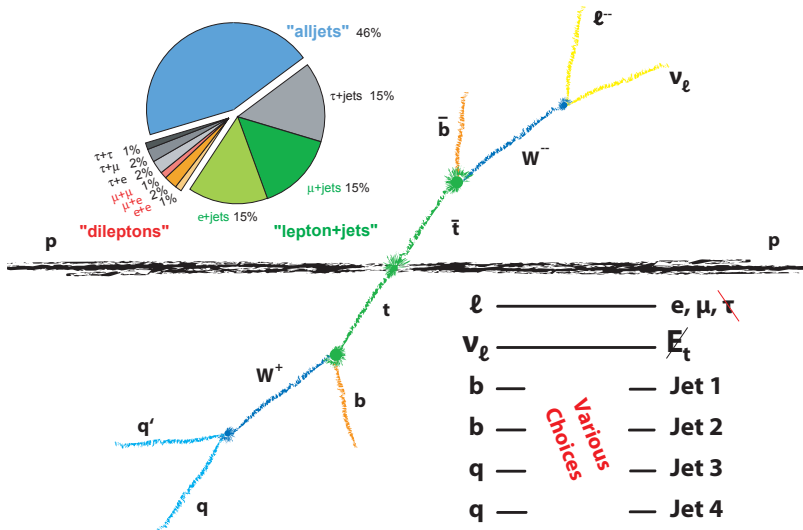
Philipp Weigell

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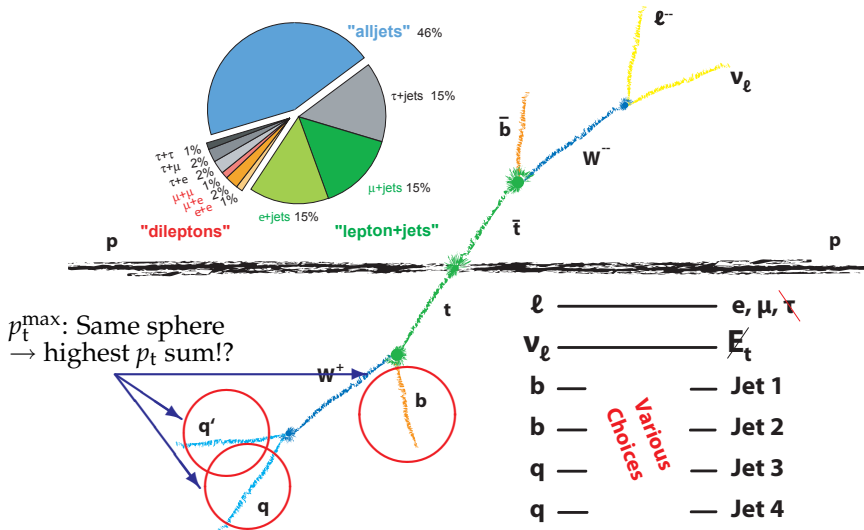
ATLAS-D  
Bonn, 24.09.2009



# Lepton + jets Channel

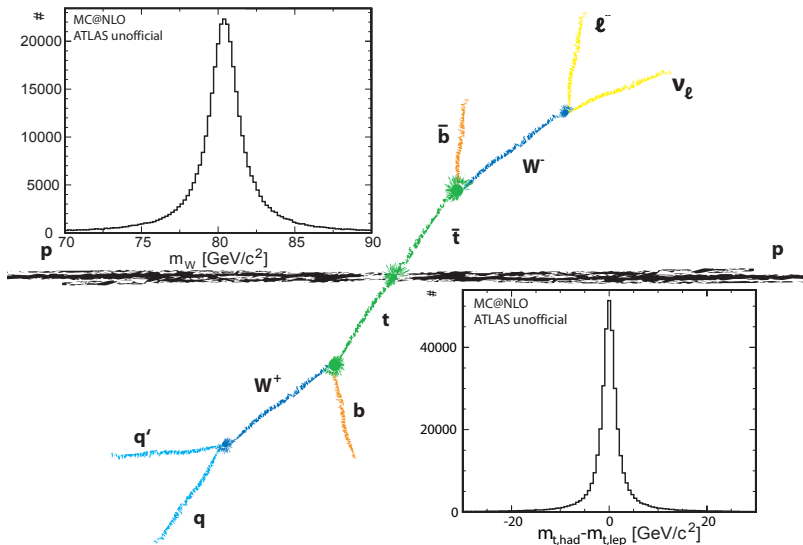


# Lepton + jets Channel



# Lepton + jets Channel

World average  $W$  mass:  $80.398 \text{ GeV}/c^2$



# Fit Variables and Constraints

## Invariant Masses

- $m_{W,\ell} = \sqrt{(p_\ell + p_\nu)^2} = \sqrt{(E_\ell + E_\nu)^2 - (\vec{p}_\ell + \vec{p}_\nu)^2}$
- $m_{W,h} = \sqrt{(p_{q_1} + p_{q_2})^2} = \sqrt{(E_{q_1} + E_{q_2})^2 - (\vec{p}_{q_1} + \vec{p}_{q_2})^2}$
- $m_{t,\ell} = \sqrt{(p_\ell + p_\nu + p_{b,\ell})^2} = \sqrt{(E_\ell + E_\nu + E_{b,\ell})^2 - (\vec{p}_\ell + \vec{p}_\nu(p_{v,x}, p_{v,y}, p_{v,z})^T + \vec{p}_{b,\ell})^2}$
- $m_{t,h} = \sqrt{(p_{q_1} + p_{q_2} + p_{b,h})^2} = \sqrt{(E_{q_1} + E_{q_2} + E_{b,h})^2 - (\vec{p}_{q_1} + \vec{p}_{q_2} + \vec{p}_{b,h})^2}$

## Constraints (loose)

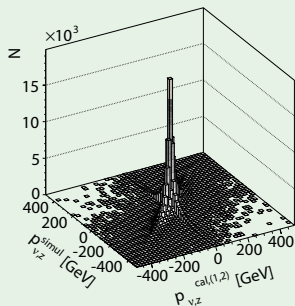
		Initial value	Uncertainty
$m_{W,\ell} - X_1 = 0$	$X_1$	80.4 GeV/c <sup>2</sup>	6 GeV/c <sup>2</sup>
$m_{W,h} - X_2 = 0$	$X_2$	80.4 GeV/c <sup>2</sup>	6 GeV/c <sup>2</sup>
$m_{t,\ell} - m_{t,h} - X_3 = 0$	$X_3$	0 GeV/c <sup>2</sup>	5 GeV/c <sup>2</sup>

# Neutrino Treatment

$\nu$  not measured  $\rightarrow$  need to recover

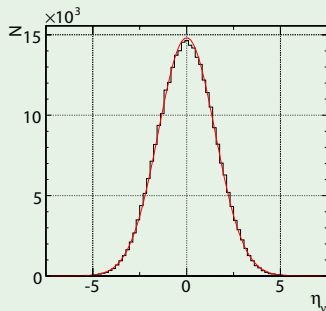
Standard:  $p_{\nu,z}$

Idea Calculate  $p_{\nu,z}$  from  
W constraint



Novel:  $\eta_\nu$

Idea Use Pseudorapidity



# From Dataset to Selection

## Datasets

**Statistics** 11.5k e + jets events

**Generator** MC@NLO + Herwig/Jimmy  
+ Geant

**Phase Space** Restrictions

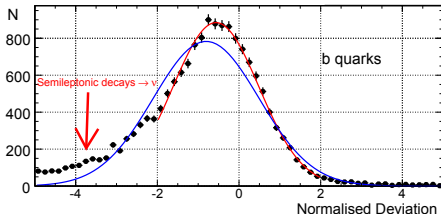
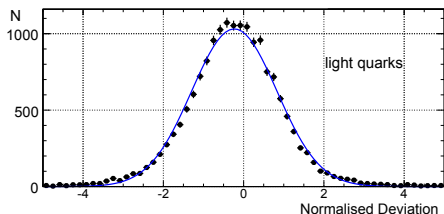
- $N_{\text{jet}} = 4$  &  $N_e = 1$
- $p_t > 20 \text{ GeV}/c$  &  $\|\eta\| < 2.5$

**Matched** 3.5k within  $\Delta R < 0.2$

# Determination of the Resolution

We assume the following detector resolution:

$$\frac{\sigma(E)}{E} = \frac{\alpha_i}{\sqrt{E}} \quad [E] = \text{GeV}$$



	b quarks	light quarks	leptons
$\alpha_i$	148 %	114 %	21 %

(Distributions not centered at 0 due to jet energy scale)



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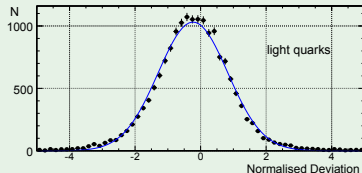
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## Resolution



## Selection Recipe

1. Take an event
2. Assign each jet to all possible roles  $\Rightarrow$  e.g. 12 Permutations for 4 jets
3. Do the fit
4. Select the permutation with the smallest  $\chi^2$

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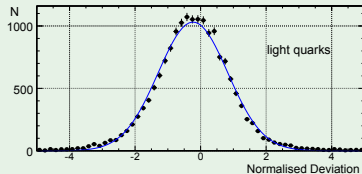
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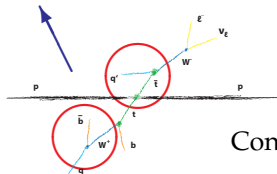
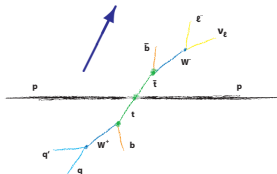
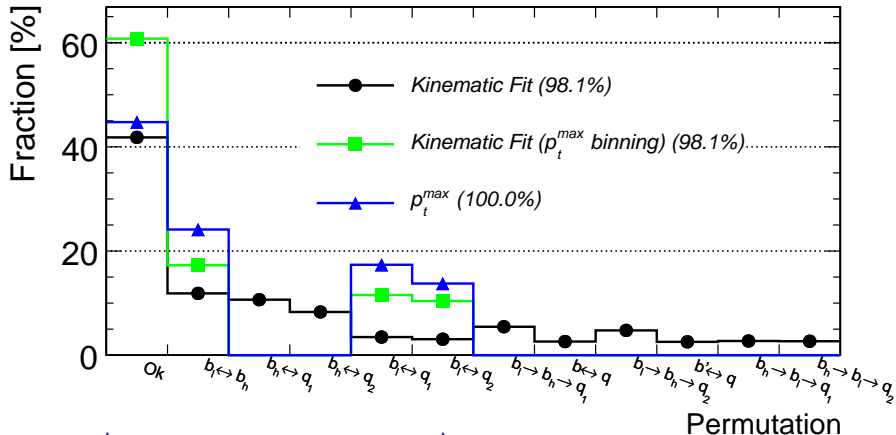
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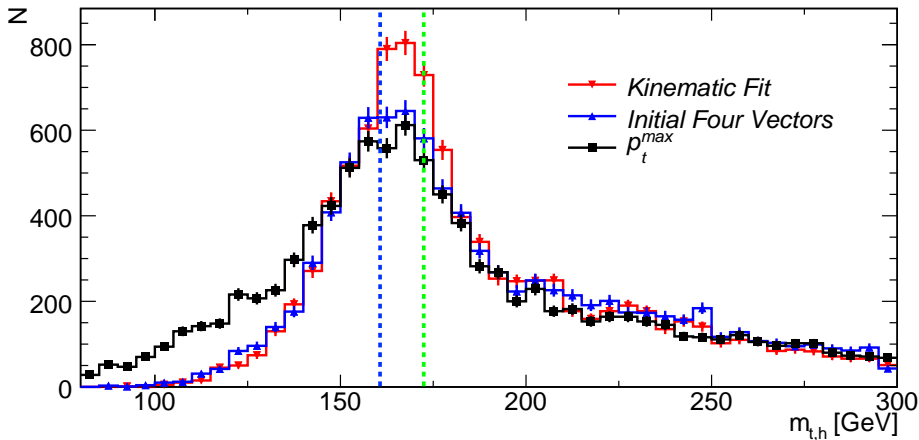
# Distribution of Selected Permutation



Convergence rate: 98.1 %

# Mass Resolution Improvement

Fitting process  $\rightarrow$  Improved four vectors  $\rightarrow$  Resolution



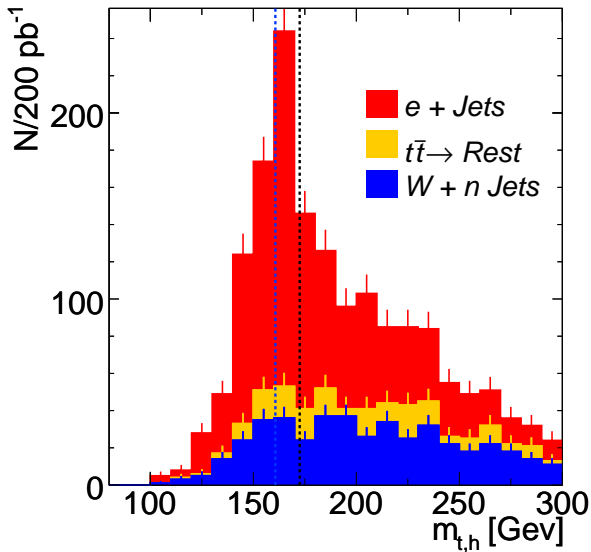
# Convergence Rates

Fit converges more often for signal than background ...

T	$t\bar{t}(e + \text{jets})$	$t\bar{t}(\text{rest})$	W + 4 jets	W + 5 jets
$p_{\nu,z}$	87.2	70.8	76.9	73.7
$\eta_{\nu}$	87.5	70.0	76.0	72.4

... and the novel approach for the  $\nu$  performs better

# Mass Reconstruction



## Conclusions

- Constrained  $\chi^2$ -fit + loosening for widths
- Fit selects correct jets in about  $\approx 65\%$  ( $p_{t,max}$ :  $\approx 40\%$ )
- Neutrino recoverment better with  $\eta_\nu$
- Backgrounds can be suppressed
- Constraints ( $m_W, \dots$ ) improve resolution