

# SUPERSYMMETRY AT THE LHC

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- Minimal set of MSSM conventions
- SUSY at the Tevatron
- SUSY searches at the LHC
- SUSY measurements at the LHC

# TeV SCALE SUPERSYMMETRY: 1

SUSY idea: solve hierarchy problem by just doubling particle number?!

- stops (scalar) cancel top loop [couplings protected]
  - gauginos (neutral or charged) cancel  $W, Z$  loop
  - higgsinos cancel Higgs loop [mix with neutralinos]
  - since we are at it, let's postulate gluino for 2-loop, plus sleptons and squarks
- ⇒ (1) hierarchy problem solved
- ⇒ (2) rich collider and non-collider phenomenology guaranteed
- ⇒ (3) Lorentz algebra properly extended

Serious change in Higgs sector

- adjoint Higgs field not allowed in  $\mathcal{L}$ 
    - how to give mass to  $t$  and  $b$ ?
    - two Higgs doublets
- ⇒ SUSY Higgs sector interesting in itself
- ⇒ no MSSM know-how needed

|               |                            | spin | d.o.f. |               |
|---------------|----------------------------|------|--------|---------------|
| fermion       | $f_L, f_R$                 | 1/2  | 1+1    |               |
| → sfermion    | $\tilde{f}_L, \tilde{f}_R$ | 0    | 1+1    |               |
| gluon         | $G_\mu$                    | 1    | n-2    |               |
| → gluino      | $\tilde{g}$                | 1/2  | 2      | Majorana      |
| gauge bosons  | $\gamma, Z$                | 1    | 2+3    |               |
| Higgs bosons  | $h^o, H^o, A^o$            | 0    | 3      |               |
| → neutralinos | $\tilde{\chi}_i^o$         | 1/2  | 4 · 2  | Majorana      |
| gauge bosons  | $W^\pm$                    | 1    | 2 · 3  |               |
| Higgs bosons  | $H^\pm$                    | 0    | 2      |               |
| → charginos   | $\tilde{\chi}_i^\pm$       | 1/2  | 2 · 4  | Dirac         |
| graviton      | $G$                        | 2    | 5      |               |
| → gravitino   | $\tilde{G}$                | 3/2  | 5      | hard to catch |

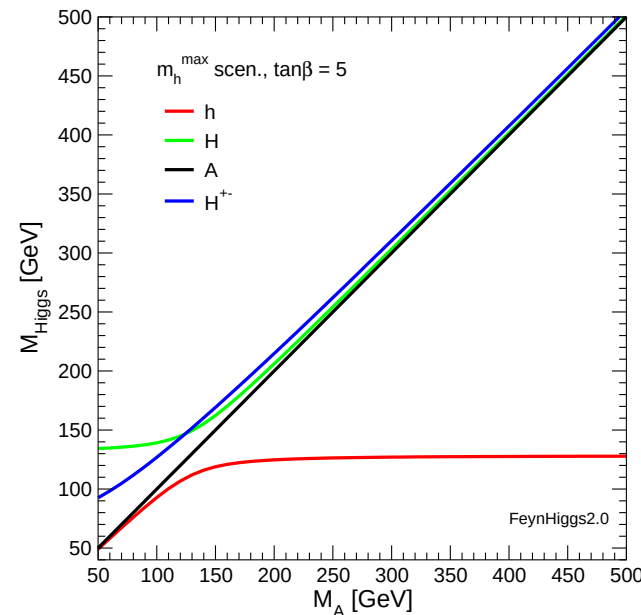
# SUPERSYMMETRIC HIGGS SECTOR: 1

## Required by supersymmetry: two Higgs doublet model

- one (complex) Higgs doublet: 4 degrees of freedom  
→ three for longitudinal  $W, Z$ , one for scalar Higgs
- two Higgs doublets: 8 degrees of freedom  
→ three for longitudinal  $W, Z$ , five for Higgs particles  
→ scalars  $h^0, H^0$ , pseudoscalar  $A^0$ , charged  $H^\pm$
- free parameters
  - (1) still only one free mass scale:  $m_A$
  - (2) two vacuum expectation values:  $\tan \beta = v_t/v_b$

## All you need to know: plateau structure [FeynHiggs]

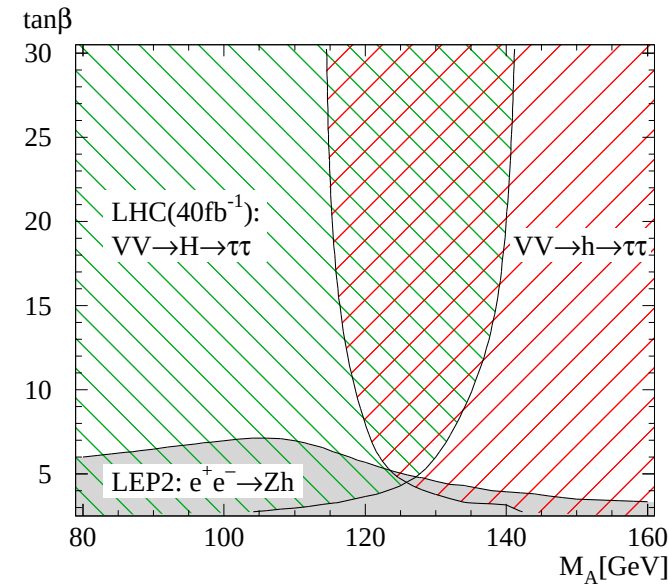
- ‘plateau Higgses’ coupling to  $W, Z$
- heavy  $H^0, A^0$  with  $\tan \beta$ -enhanced coupling to  $b, \tau$
- light  $h^0$  mass limited from above  $m_h \lesssim 135$  GeV



## SUPERSYMMETRIC HIGGS SECTOR: 2

### Challenge: find one Higgs at the LHC

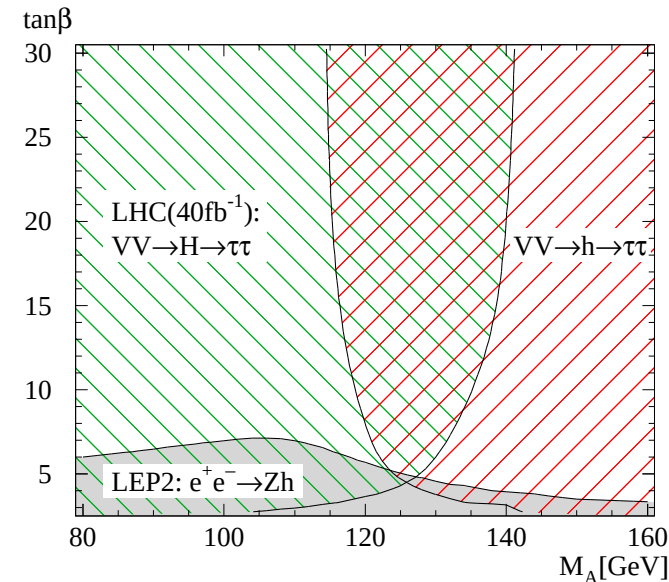
- decoupling regime  $m_A \gtrsim 160$  GeV  
→  $h^0$  looks like SM Higgs [of corresponding mass]  
→  $qq \rightarrow qqh^0 \rightarrow qq\tau\tau$
  - other end  $m_A \lesssim 120$  GeV  
→  $qq \rightarrow qqH^0 \rightarrow qq\tau\tau$
  - in between: maybe even two bumbs
- ⇒ **No-lose theorem:**  $qq \rightarrow qq\{h^0, H^0\} \rightarrow qq\tau\tau$



# SUPERSYMMETRIC HIGGS SECTOR: 2

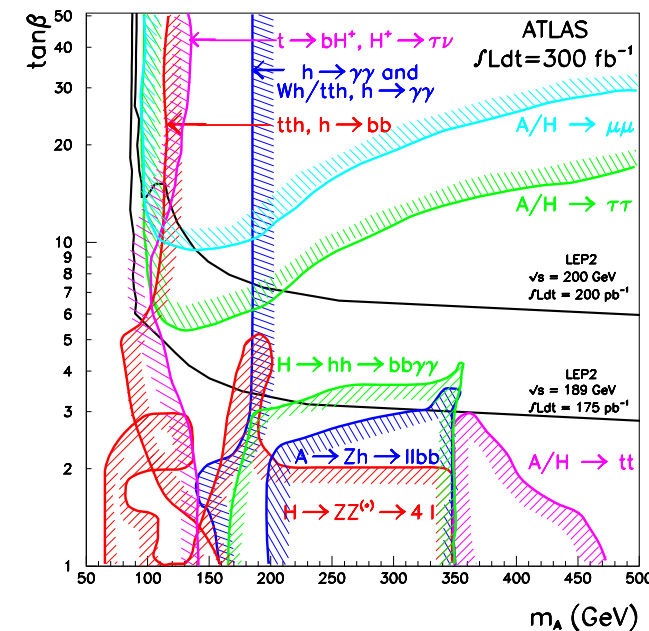
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## Nightmare: confirm SUSY Higgs sector

- decoupling regime  $m_A \gtrsim 160$  GeV  
 $\rightarrow$  Yukawa coupling for  $H^0, A^0, H^\pm$ :  $m_b \tan \beta$   
 $\rightarrow$  enhanced production e.g.  $b\bar{b} \rightarrow H^0$  or  $gb \rightarrow tH^-$   
 $\rightarrow$  decays  $H^0 \rightarrow \tau\tau, \mu\mu$  or  $H^- \rightarrow \tau\bar{\nu}$
- intermediate  $m_A \sim 120$  GeV:  
 $\rightarrow$  many (light-ish) Higgses  $h^0, H^0, A^0$  observable  
 $\rightarrow$  top quark decays  $t \rightarrow bH^+$ ? [Tevatron?]



## Structures in the SUSY spectrum

- gauginos–higgsinos mixing:  $m_{\tilde{\chi}_2^0} \sim m_{\tilde{\chi}_1^+}$  or  $m_{\tilde{\chi}_1^0} \sim m_{\tilde{\chi}_1^+}$  in **MSSM**

$$\begin{pmatrix} m_{\tilde{B}} & 0 & -m_Z s_w c_\beta & m_Z s_w s_\beta \\ 0 & m_{\tilde{W}} & m_Z c_w c_\beta & -m_Z c_w s_\beta \\ -m_Z s_w c_\beta & m_Z c_w c_\beta & 0 & -\mu \\ m_Z s_w s_\beta & -m_Z c_w s_\beta & -\mu & 0 \end{pmatrix} \begin{pmatrix} m_{\tilde{W}} & \sqrt{2} m_W s_\beta \\ \sqrt{2} m_W c_\beta & -\mu \end{pmatrix}$$

- stop and sbottom mixing in **MSSM**

$$\begin{pmatrix} m_Q^2 + m_t^2 + \left(\frac{1}{2} - \frac{2}{3} s_w^2\right) m_Z^2 c_{2\beta} & -m_t (A_t + \mu \cot \beta) \\ -m_t (A_t + \mu \cot \beta) & m_U^2 + m_t^2 + \frac{2}{3} s_w^2 m_Z^2 c_{2\beta} \end{pmatrix}$$

- heavy gluinos, squarks through **unification**:  $m_{\tilde{B}, \tilde{W}, \tilde{g}}/m_{1/2} \sim 0.4, 0.8, 2.6$   
 $m_{\tilde{\ell}, \tilde{q}}/m_{1/2} \sim 0.7, 2.5$  [ $m_0 \ll m_{1/2}$ ]

[mass and coupling unification independent]

- lightest SUSY partner  $\tilde{\chi}_1^0, \tilde{\nu} \Rightarrow$  after dark matter data  $\tilde{\chi}_1^0 \sim \tilde{B}, \tilde{W}$  [gravitinos?]

## Supersymmetric parameter conventions

- comparison of specialized codes crucial [remember: e.g. Comphep–Pythia–Isajet]
- ⇒ fix SUSY conventions once for all
- soft breaking parameters [e.g.  $\pm A_t$ ]
- scale dependence of couplings, masses [e.g.  $m(q = \text{TeV}, v, m_t)$ ]
- definitions of mass matrixes, mixing angles [e.g.  $\tilde{t}_{L,R}$  up or down?]

## SUSY Les Houches Accord [Allanach, Skands et al.]

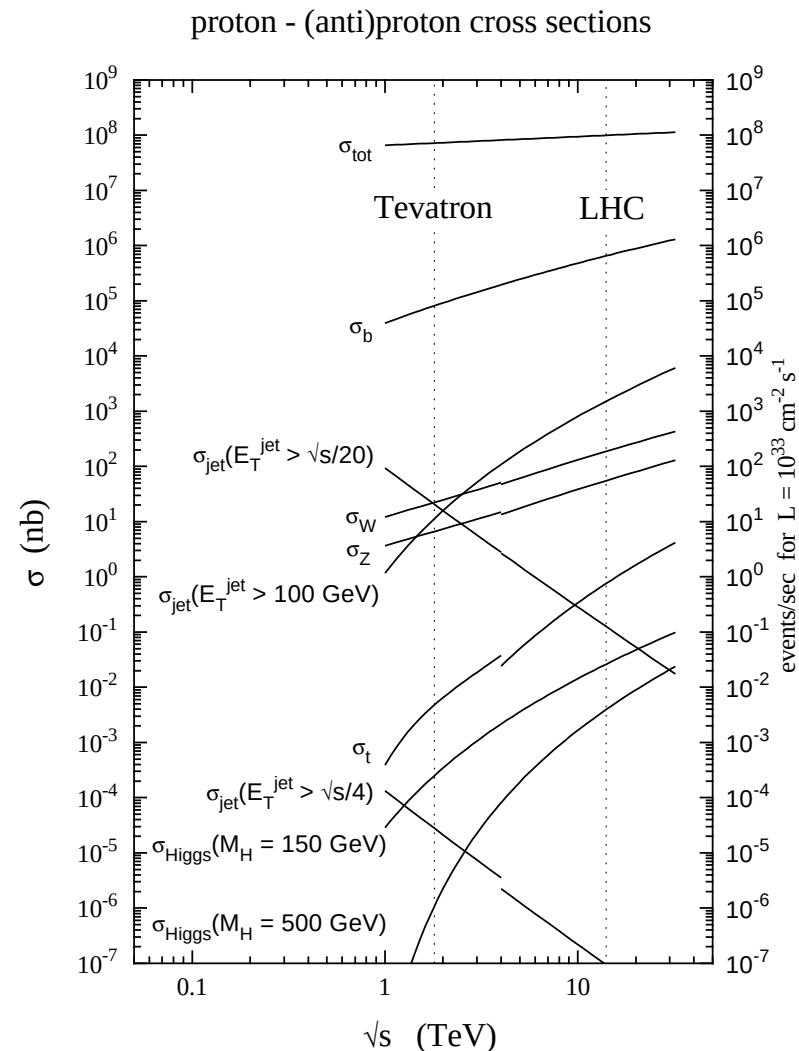
- spectrum generators: SoftSusy, SPheno, FeynHiggs,...
- multi-purpose Monte Carlos: Pythia, Herwig, Sherpa
- matrix element generators: Whizard, Smadgraph
- NLO cross sections: Prospino2
- NLO decay rates: Sdecay
- SUSY parameter extraction: Fittino, Sfitter
- dark matter: Micromegas
- ⇒ **fixed parameter convention and read-write format** [list still growing]

## Conversion of beam energy into particle mass

- search for new particles easier if particle produced  
→ highest possible energies required
- clean  $e^+e^-$  colliders:  
LEP:  $Z$  pole  
LEP2: 206 GeV for e.g.  $ZH$   
ILC/CLIC: 1...4 TeV in future
- powerful hadron colliders:  
Tevatron:  $p\bar{p}$  with 2 TeV [valence quarks]  
LHC:  $pp$  with 14 TeV [gluons]
- **LHC mass reach  $\sim 3$  TeV** [win by luminosity]

## New physics at hadron colliders

- what is a jet and what is inside? [ $b, \tau$  tag]
- trigger: 'no leptons — no data'
- backgrounds  $pp \rightarrow jj$  or  $pp \rightarrow WZ + \text{jets}$
- **statistics:  $S/\sqrt{B} > 5$  we call discovery**

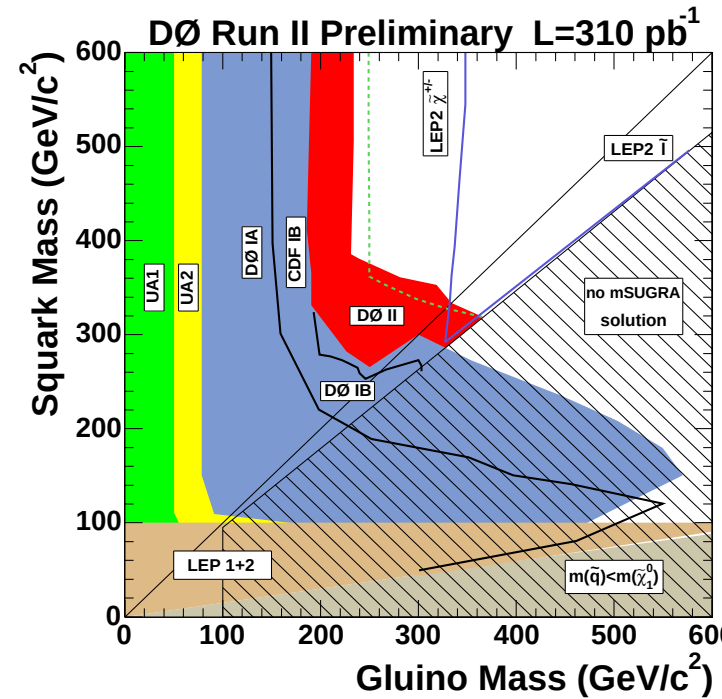




# SUPERSYMMETRY AT THE TEVATRON: 1

## Inclusive: squarks and gluinos at Tevatron

- squarks, gluinos strongly interacting,  $\sigma \sim \text{pb}$   
 $p\bar{p} \rightarrow \tilde{q}\tilde{q}^*, \tilde{q}\tilde{g}, \tilde{g}\tilde{g}$  [best if  $m(\tilde{q}) \sim m(\tilde{g})$ ]
  - decays to jets and LSP and  
 $\tilde{g} \rightarrow \tilde{q}\bar{q}, \tilde{q}_L \rightarrow q\tilde{\chi}_2^0, \tilde{q}_R \rightarrow q\tilde{\chi}_1^0$   
additional jets and leptons possible
- ⇒ **very promising search for jets plus LSP**



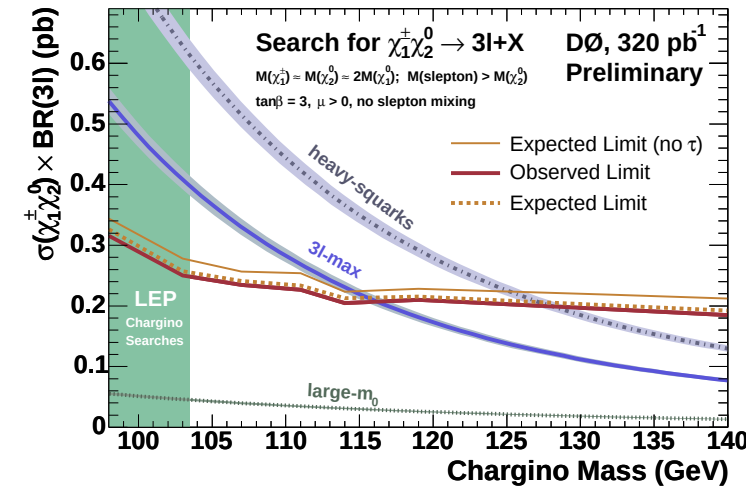
## Necessary model assumptions

- assume 100% branching into inclusive jets+LSP
  - for detector efficiencies  $m(\tilde{\chi}_2^0), \dots$
  - gluino decay into squark or vice versa?
- ⇒ mSUGRA assumed, but effect moderate

# SUPERSYMMETRY AT THE TEVATRON: 2

## More specialized: trilepton channels

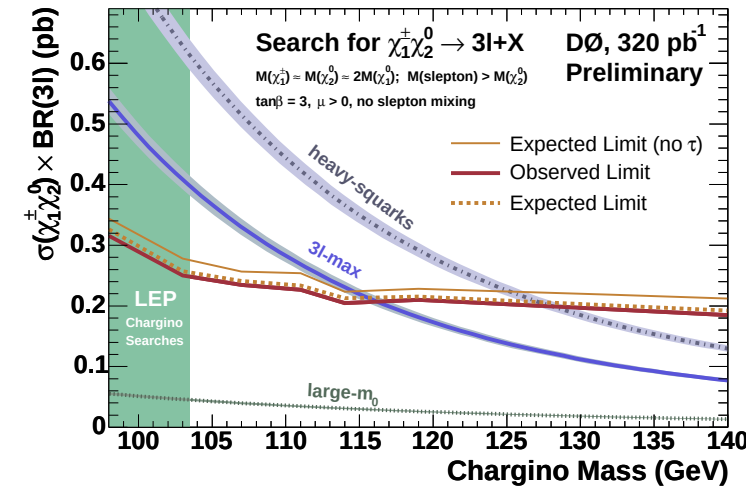
- generally assumed that charginos are light
- largest cross section  $p\bar{p} \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_2^0$   
decays  $\tilde{\chi}_1^+ \rightarrow \ell^+ \nu \tilde{\chi}_1^0$  and  $\tilde{\chi}_2^0 \rightarrow \ell^+ \ell^- \tilde{\chi}_1^0$
- gaugino rate determined by  $t$  channel squark
- signature plagued by  $W, Z$  background
- $\Rightarrow$  about to pass LEP2 chargino limits



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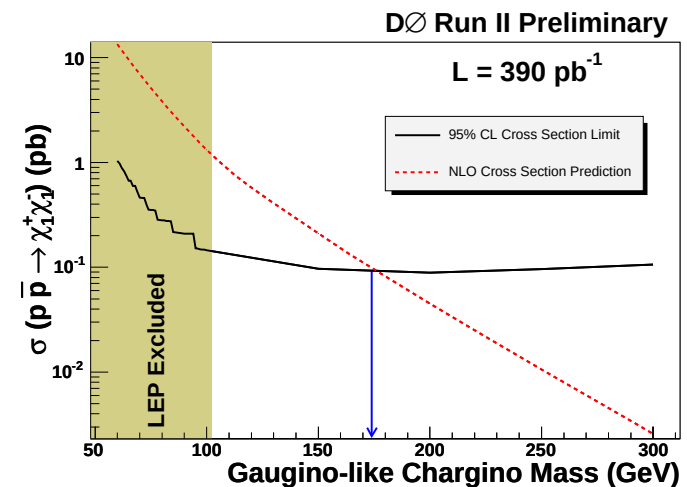
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## Even more specialized: long-lived gauginos

- stable on the detector time scale of  $ns$
- like massive muons in tracker–muon chamber
- gauginos motivated by GMSB or AMSB

⇒ SUSY at the LHC does not come out of nowhere!

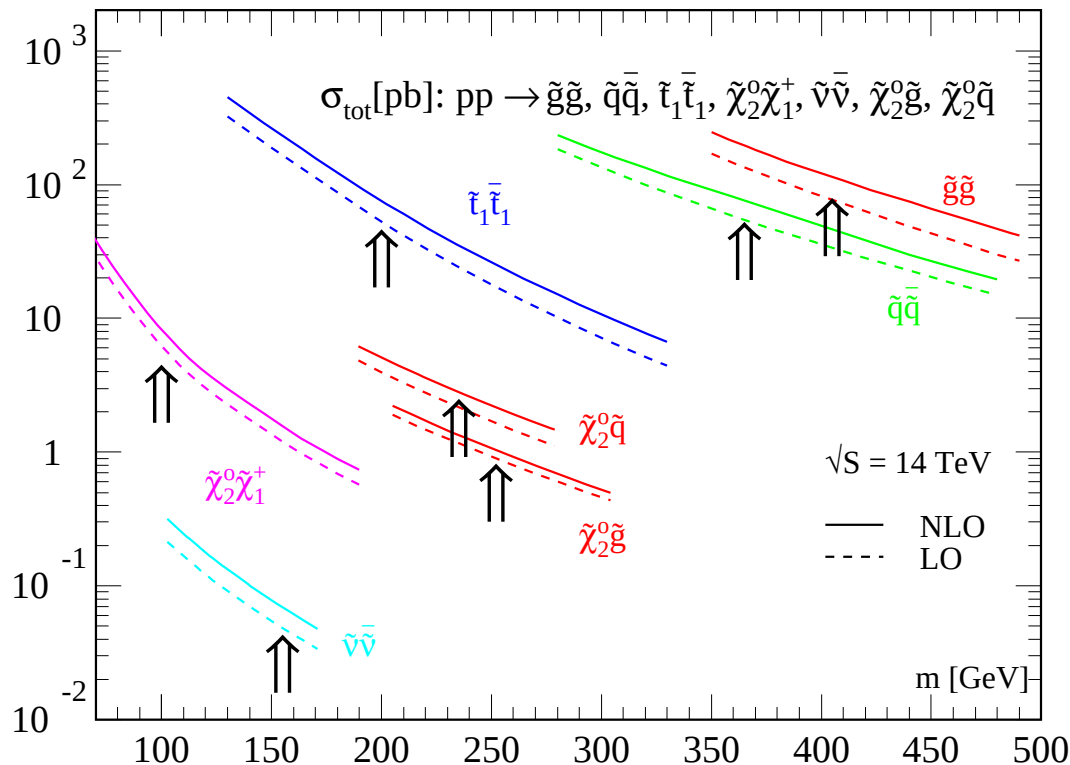


## Supersymmetry at the LHC

- (1) **possible discovery** — signals for new physics, exclusion of parameter space
- (2) **measurements** — masses, cross sections, decays
- (3) **parameter studies** — MSSM Lagrangean, SUSY breaking

## SUSY signals included

- QCD coupling  $g\tilde{q}\tilde{q}, q\tilde{g}\tilde{q}, g\tilde{g}\tilde{g}$
- jets and  $\cancel{E}_T$ :  $pp \rightarrow \tilde{q}\tilde{q}^*, \tilde{g}\tilde{g}, \tilde{q}\tilde{g}$
- funny tops:  $pp \rightarrow \tilde{t}_1\tilde{t}_1^*$
- like sign dileptons:  $pp \rightarrow \tilde{g}\tilde{g}$   
 $[\tilde{g} \rightarrow \tilde{u}\tilde{u} \rightarrow \tilde{\chi}_1^+ d\bar{u} \text{ or } \tilde{g} \rightarrow \tilde{u}^* u \rightarrow \tilde{\chi}_1^- \bar{d}u]$
- tri-leptons:  $pp \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^-$   
 $[\tilde{\chi}_2^0 \rightarrow \tilde{\ell}\bar{\ell} \rightarrow \tilde{\chi}_1^0 \ell\bar{\ell}; \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \ell\bar{\nu}]$

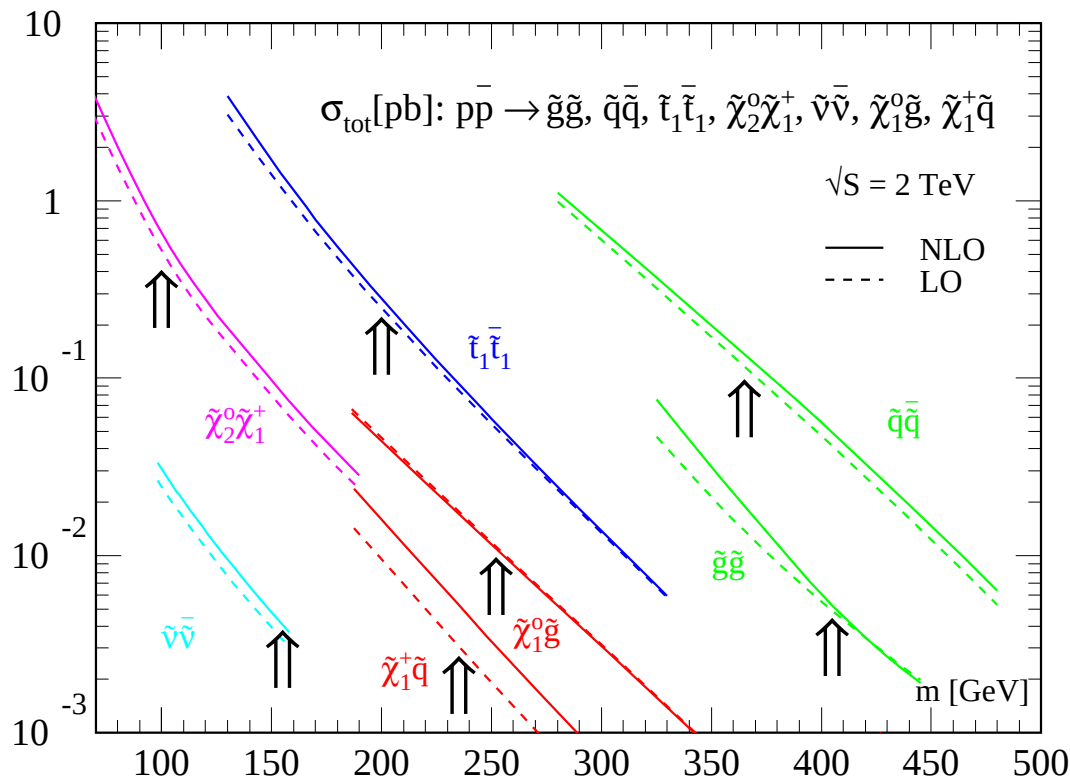


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# SUPERSYMMETRY AT LHC: 2

## Tevatron-type LHC searches

- inclusive jet + missing energy [squark-gluino dominant]
- stops to bottom-chargino [top-like]
- like-sign dileptons [gluino Majorana if fermion]
- trileptons [signal down, background up]
- all R-parity conserving...

## Approximate Sugra relations

$$m^2(\tilde{e}_R) = m_0^2 + 0.15 m_{1/2}^2 - s_w^2 D$$

$$m^2(\tilde{e}_L) = m_0^2 + 0.52 m_{1/2}^2 - (1/2 - s_w^2) D$$

$$m^2(\tilde{\nu}) = m_0^2 + 0.52 m_{1/2}^2 + 1/2 D$$

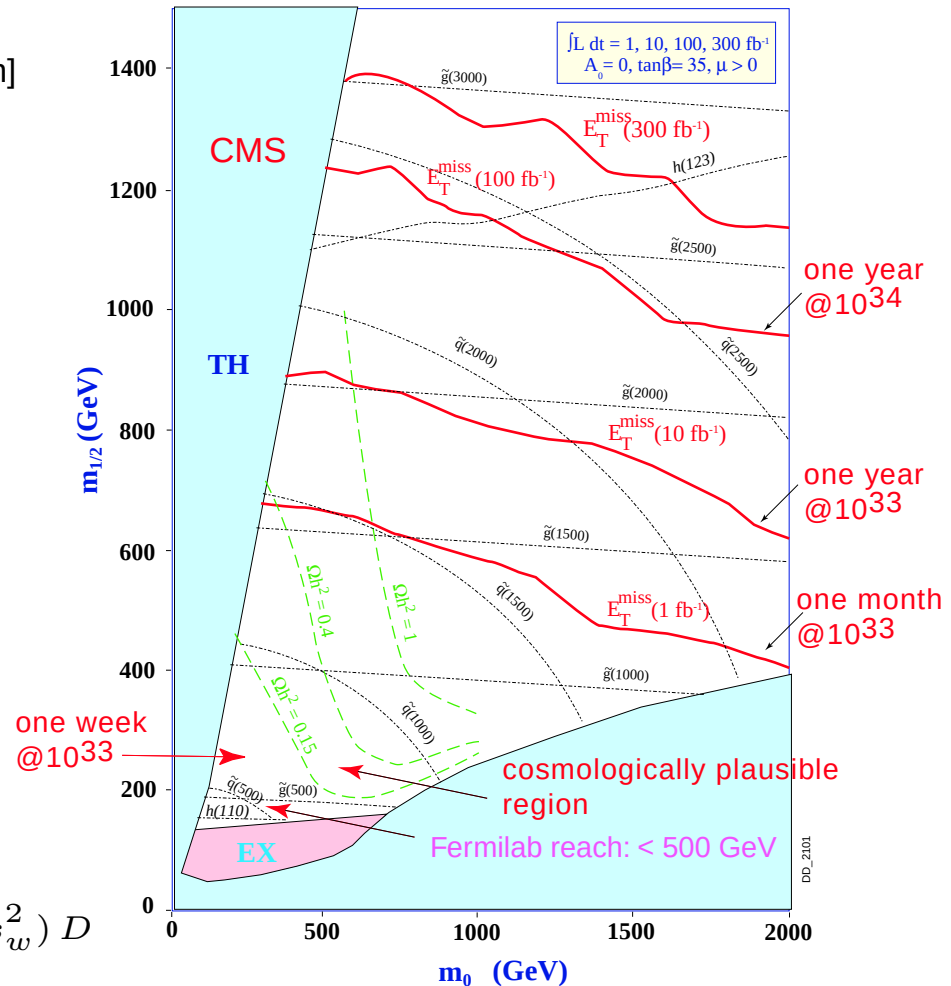
$$m^2(\tilde{u}_R) = m_0^2 + (0.07 + C) m_{1/2}^2 + 2/3 s_w^2 D$$

$$m^2(\tilde{d}_R) = m_0^2 + (0.02 + C) m_{1/2}^2 - 1/3 s_w^2 D$$

$$m^2(\tilde{u}_L) = m_0^2 + (0.47 + C) m_{1/2}^2 + (1/2 - 2/3 s_w^2) D$$

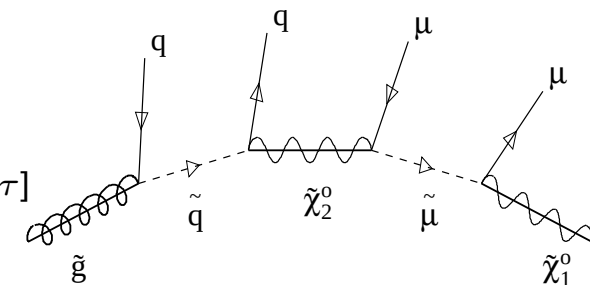
$$m^2(\tilde{d}_L) = m_0^2 + (0.47 + C) m_{1/2}^2 - (1/2 - 1/3 s_w^2) D$$

$$D = m_Z^2 c_{2\beta}$$



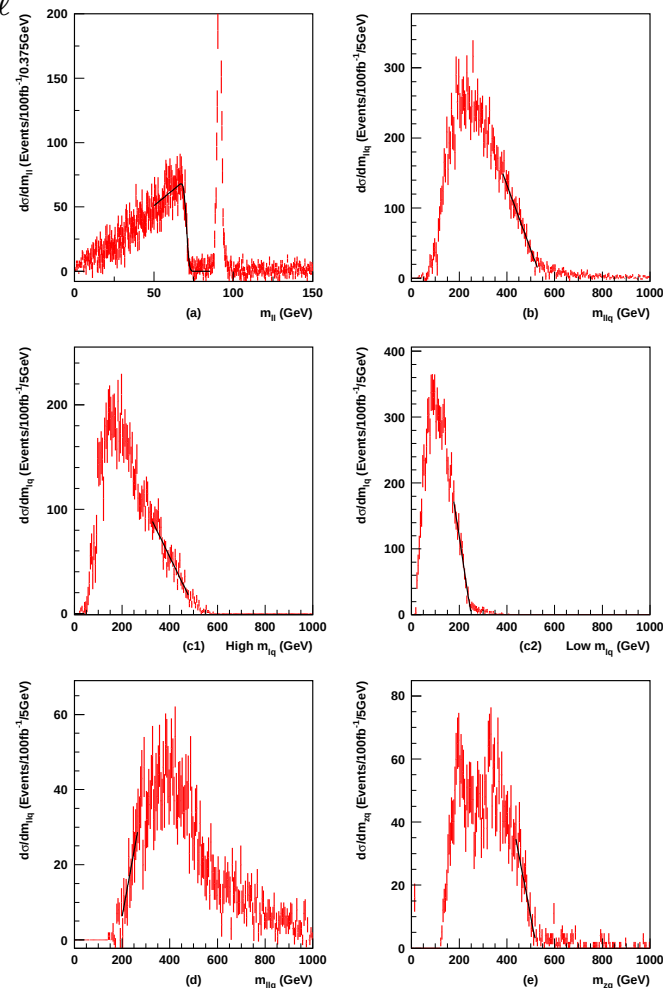
## Spectra from cascade decays

- decay  $\tilde{g} \rightarrow \tilde{q}\bar{q} \rightarrow \tilde{\chi}_2^0 q\bar{q} \rightarrow \mu^+ \mu^- q\bar{q} \tilde{\chi}_1^0$  [better not via  $Z$  or to  $\tau$ ]
- cross sections some 100 pb [more than  $3 \times 10^5$  events]
- thresholds & edges  $m_{\ell\ell}^2 < (m_{\tilde{\chi}_2^0}^2 - m_{\tilde{\ell}}^2)(m_{\tilde{\ell}}^2 - m_{\tilde{\chi}_1^0}^2)/m_{\tilde{\ell}}^2$
- detector resolution, calibration, systematic errors, shape analysis, cross sections as input?



⇒  $\tilde{q}_L$  cascade reconstruction great

[known even from Atlas TDR]







# SUPERSYMMETRY AT LHC: 4

## Complex final states

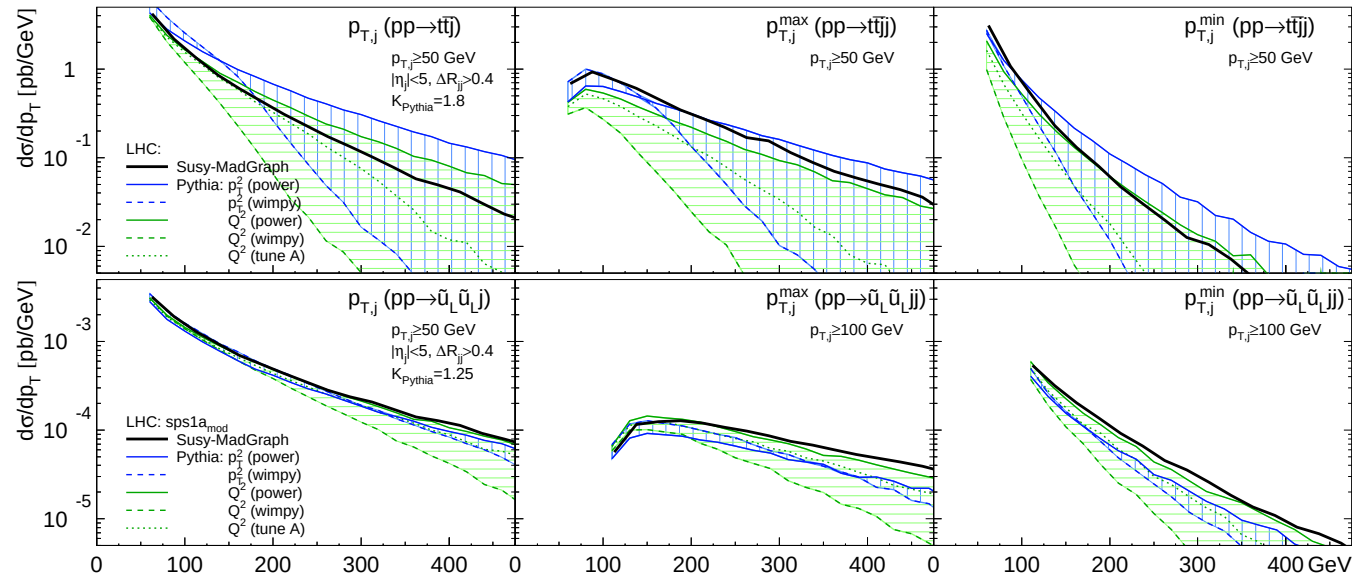
- Majoranas and fermion number violation in tools like Madgraph
- complete set of Feynman rules [400+ processes compared: Madgraph - Whizard - Sherpa]

## Squarks and gluinos always with many jets

- cascade studies sensitive to jets?
- matrix element  $\tilde{g}\tilde{g}+2j$  and  $\tilde{u}_L\tilde{g}+2j$  [ $p_{T,j} > 100$  GeV]
- Pythia shower tuned at Tevatron

| $\sigma$ [pb] | $t\bar{t}_{600}$ | $\tilde{g}\tilde{g}$ | $\tilde{u}_L\tilde{g}$ |
|---------------|------------------|----------------------|------------------------|
| $\sigma_{0j}$ | 1.30             | 4.83                 | 5.65                   |
| $\sigma_{1j}$ | 0.73             | 2.89                 | 2.74                   |
| $\sigma_{2j}$ | 0.26             | 1.09                 | 0.85                   |

⇒ SUSY easier than tops



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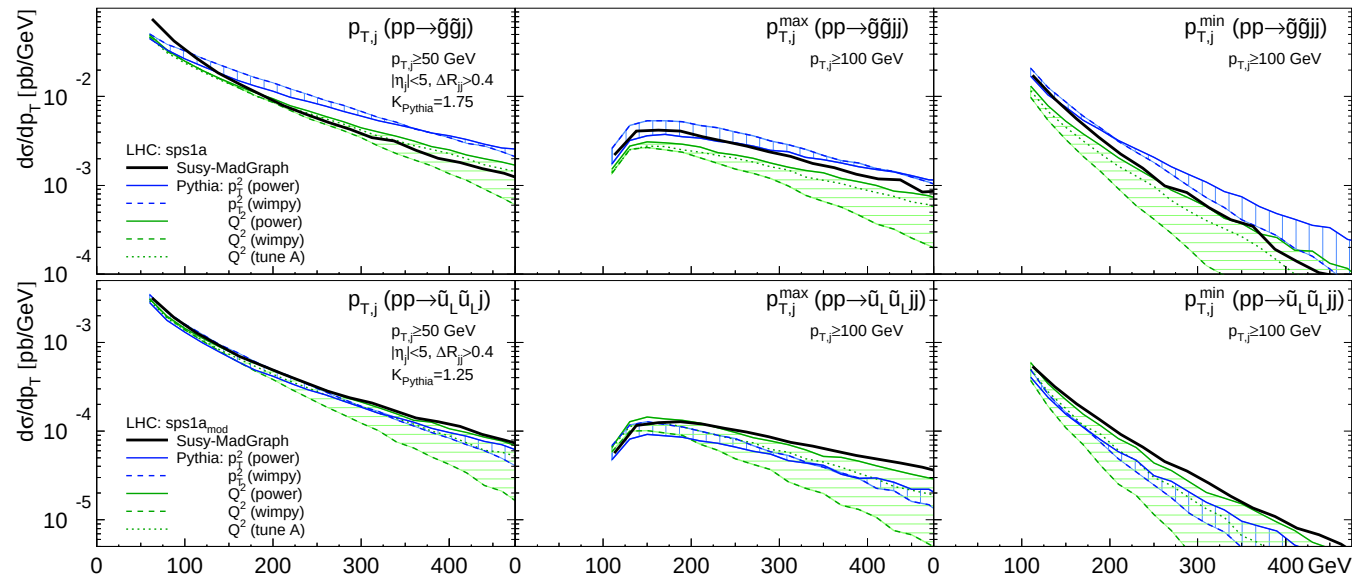
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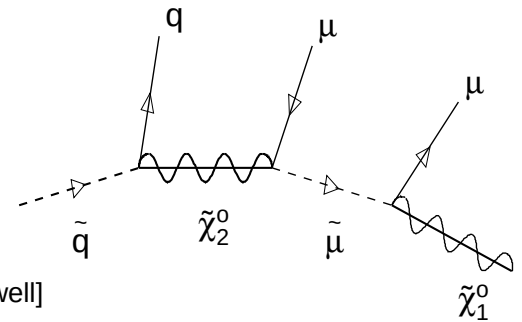
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## How to make sure it is SUSY

- assume neutralino is found in cascades
- compare with a model where gluino is a boson,...
- straw man: universal extra dimensions

[mass spectra degenerate —ignore this information; cross section factor 10 larger —ignore this as well]

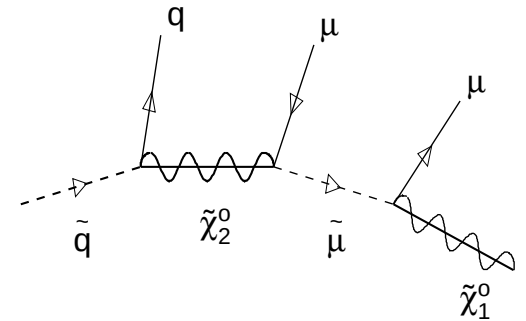


## Squark cascade

- decay chain  $\tilde{q}_L \rightarrow q\tilde{\chi}_2^0 \rightarrow q\ell\bar{\ell} \rightarrow q\ell\bar{\ell}\tilde{\chi}_1^0$   
compared with first excited  $Z$  and  $\ell$  [assume near/far lepton for now]
- polarization: 1:  $(q_L, \ell_L^-, \ell_L^+)$   
or 2:  $(q_L, \ell_L^+, \ell_L^-) = (q_L, \ell_R^-, \ell_R^+) = (\bar{q}_L, \ell_L^-, \ell_L^+)$
- distribution of angle  $\theta$  between  $q$  and  $\ell$ :  $dP_{1,2}^{\text{SUSY}}/d\cos\theta \propto (1 \mp \cos\theta)$
- ⇒ rescaled invariant mass variable instead:  $\hat{m} = m_{q\ell}/m_{q\ell}^{\text{max}} = \sin\theta/2$

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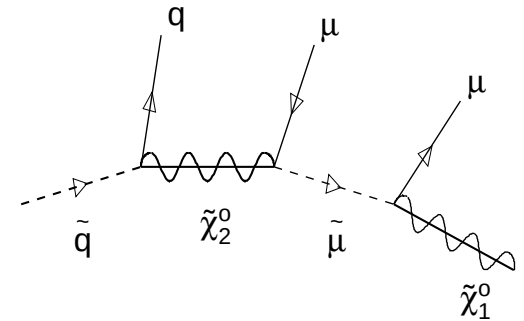


## UED and SUSY distributions [ $Z_L^*$ for $m_{q^*} \gg m_{Z^*}$ , $Z_T^*$ for $m_{q^*} \ll m_{Z^*}$ ]

$$\begin{aligned} \frac{dP_1^{\text{SUSY}}}{d\hat{m}} &= 4\hat{m}^3 & \frac{dP_2^{\text{SUSY}}}{d\hat{m}} &= 4\hat{m} (1 - \hat{m}^2) \\ \frac{dP_1^{\text{UED,T}}}{d\hat{m}} &= \frac{12\hat{m}}{2+y} \left( y\hat{m}^2 + (1-y)\hat{m}^4 \right) & \frac{dP_2^{\text{UED,T}}}{d\hat{m}} &= \frac{12\hat{m}}{2+y} \left( 1 + (y-2)\hat{m}^2 + (1-y)\hat{m}^4 \right) \\ \frac{dP_{1,2}^{\text{UED,L}}}{d\hat{m}} &= \frac{6\hat{m}}{2+y} \left( y + 4(1-y)(\hat{m}^2 - \hat{m}^4) \right) & y &= m_{\ell^*}^2 / m_{Z^*}^2 \end{aligned}$$

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compared with first excited  $Z$  and  $\ell$
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## UED and SUSY distributions [SPS1a spectrum]

$$\frac{dP_1^{\text{SUSY}}}{d\hat{m}} = 4\hat{m}^3$$

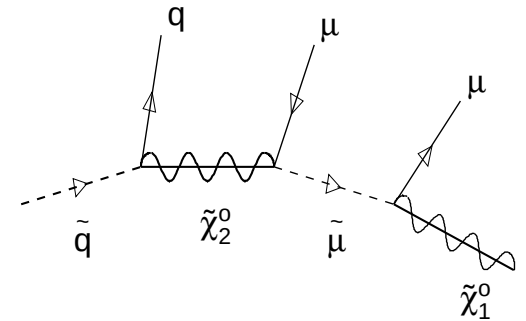
$$\frac{dP_2^{\text{SUSY}}}{d\hat{m}} = 4\hat{m} (1 - \hat{m}^2)$$

$$\frac{dP_1^{\text{UED}}}{d\hat{m}} = 1.213 \hat{m} + 3.108 \hat{m}^3 - 2.310 \hat{m}^5$$

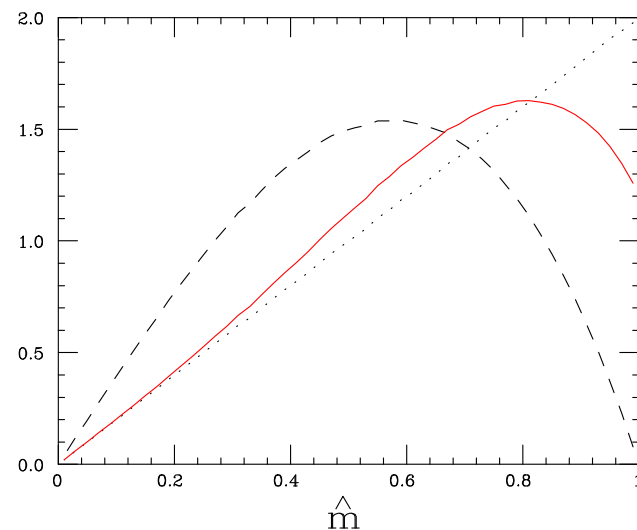
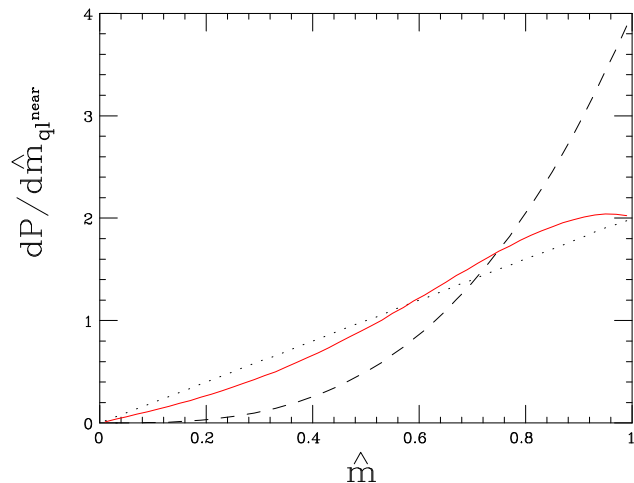
$$\frac{dP_2^{\text{UED}}}{d\hat{m}} = 2.020 \hat{m} + 1.493 \hat{m}^3 - 2.310 \hat{m}^5$$

## Squark cascade

- decay chain  $\tilde{q}_L \rightarrow q\tilde{\chi}_2^0 \rightarrow q\ell\tilde{\ell} \rightarrow q\ell\bar{\ell}\tilde{\chi}_1^0$   
compared with first excited  $Z$  and  $\ell$
  - polarization: 1:  $(q_L, \ell_L^-, \ell_L^+)$   
or 2:  $(q_L, \ell_L^+, \ell_L^-) = (q_L, \ell_R^-, \ell_R^+) = (\bar{q}_L, \ell_L^-, \ell_L^+)$
  - distribution of angle  $\theta$  between  $q$  and  $\ell$ :  $dP_{1,2}^{\text{SUSY}}/d\cos\theta \propto 1 \mp \cos\theta$
- $\Rightarrow$  rescaled invariant mass variable instead:  $\hat{m} = m_{ql}/m_{ql}^{\text{max}} = \sin\theta/2$

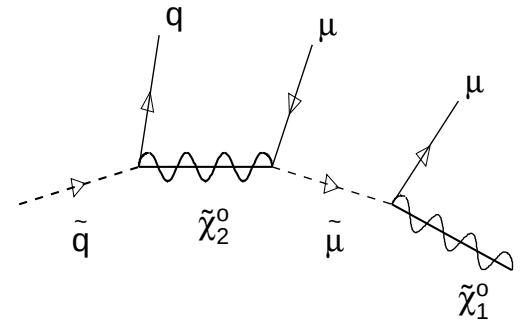


## UED and SUSY distributions [SPS1a spectrum]

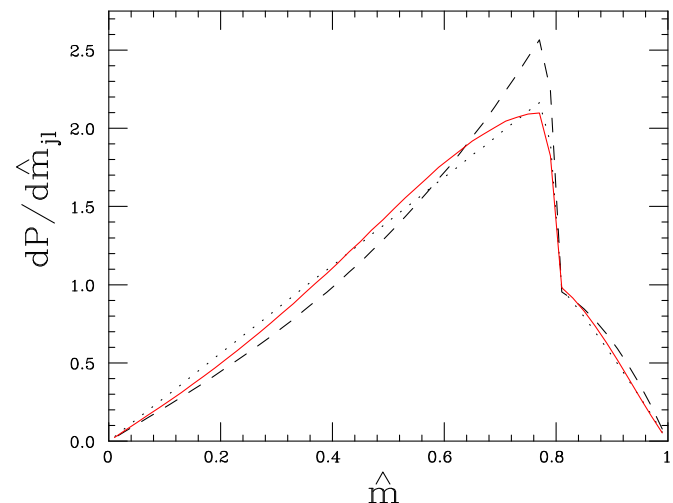
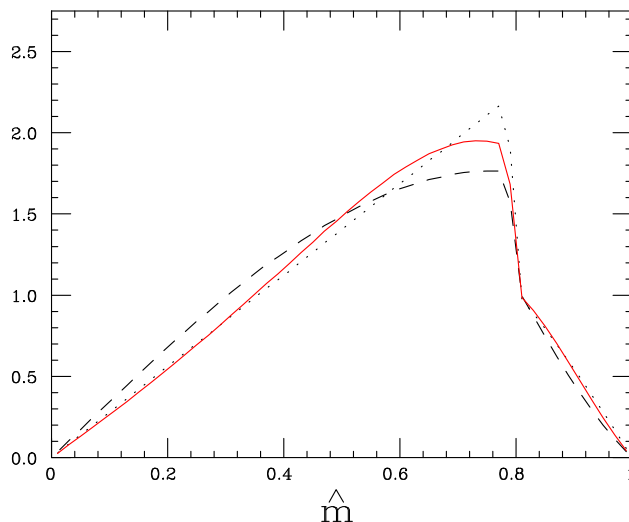


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or 2:  $(q_L, \ell_L^+, \ell_L^-) = (q_L, \ell_R^-, \ell_R^+) = (\bar{q}_L, \ell_L^-, \ell_L^+)$
  - initial-state asymmetry  $pp \rightarrow \tilde{q} \tilde{q} \quad [\bar{q}/\tilde{q} \sim 2]$
- $\Rightarrow$  even better:  $\mathcal{A} = [\sigma(j\ell^+) - \sigma(j\ell^-)] / [\sigma(j\ell^+) + \sigma(j\ell^-)]$



## UED and SUSY distributions [SPS1a spectrum, now $\ell^-$ vs $\ell^+$ ]



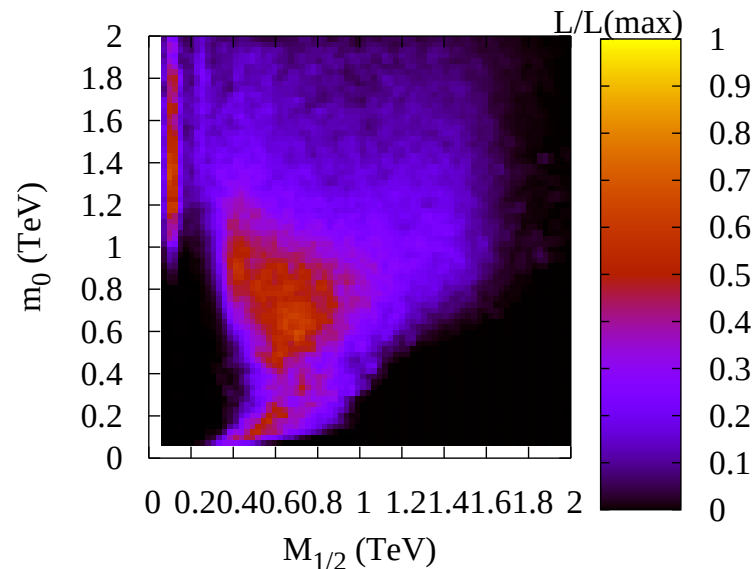
# SUPERSYMMETRIC PARAMETERS

## SUSY parameters from observables

- parameters: weak-scale MSSM Lagrangean
- measurements: masses or edges  
branching fractions  
cross sections
- errors: general correlation, statistics & systematics & theory
- problem in grid: huge phase space, local minimum?  
problem in fit: domain walls, starting values, global minimum?

## First go at problem

- ask a friend who knows how SUSY is broken
- ⇒ mSUGRA
- fit  $m_0, m_{1/2}, A_0, \tan \beta, \text{sign}(mu)$
  - no problem, include indirect constraints
- ⇒ who the hell believes in mSUGRA?
- **mSUGRA just testing ground for methods**





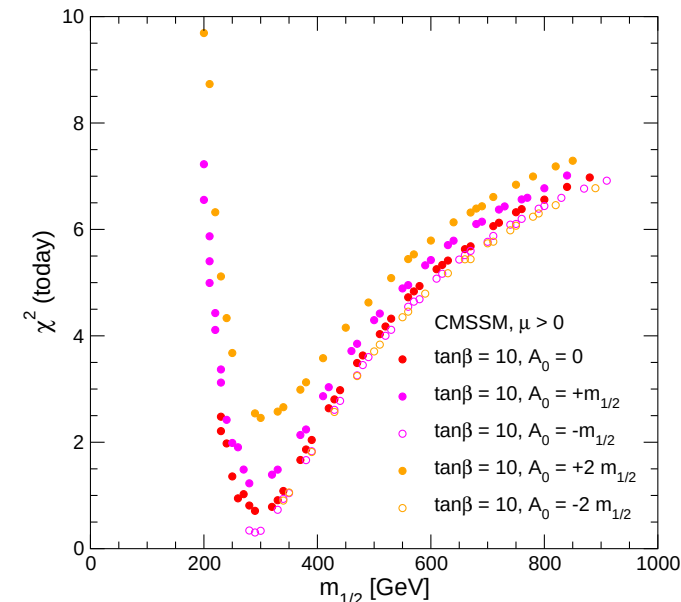
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## Combination of methods [Sfitter, Fittino]

- (1) grid for closed subset  
(2) fit of remaining parameters  
(3) complete fit
  - more modern alternatives:  
simulated annealing  
Markov Chains
- ⇒ **LHC+ILC with no assumptions**

|                      | LHC                | ILC               | LHC+ILC           | SPS1a  |
|----------------------|--------------------|-------------------|-------------------|--------|
| $\tan\beta$          | $10.22 \pm 9.1$    | $10.26 \pm 0.3$   | $10.06 \pm 0.2$   | 10     |
| $M_1$                | $102.45 \pm 5.3$   | $102.32 \pm 0.1$  | $102.23 \pm 0.1$  | 102.2  |
| $M_3$                | $578.67 \pm 15$    | fi x 500          | $588.05 \pm 11$   | 589.4  |
| $M_{\tilde{\tau}_L}$ | fi x 500           | $197.68 \pm 1.2$  | $199.25 \pm 1.1$  | 197.8  |
| $M_{\tilde{\tau}_R}$ | $129.03 \pm 6.9$   | $135.66 \pm 0.3$  | $133.35 \pm 0.6$  | 135.5  |
| $M_{\tilde{\mu}_L}$  | $198.7 \pm 5.1$    | $198.7 \pm 0.5$   | $198.7 \pm 0.5$   | 198.7  |
| $M_{\tilde{q}^3_L}$  | $498.3 \pm 110$    | $497.6 \pm 4.4$   | $521.9 \pm 39$    | 501.3  |
| $M_{\tilde{t}_R}$    | fi x 500           | $420 \pm 2.1$     | $411.73 \pm 12$   | 420.2  |
| $M_{\tilde{b}_R}$    | $522.26 \pm 113$   | fi x 500          | $504.35 \pm 61$   | 525.6  |
| $A_\tau$             | fi x 0             | $-202.4 \pm 89.5$ | $352.1 \pm 171$   | -253.5 |
| $A_t$                | $-507.8 \pm 91$    | $-501.95 \pm 2.7$ | $-505.24 \pm 3.3$ | -504.9 |
| $A_b$                | $-784.7 \pm 35603$ | fi x 0            | $-977 \pm 12467$  | -799.4 |

### LHC phenomenology beyond the Standard Model

- Tevatron optimal training ground for SUSY at LHC
  - many new tools/ideas on the market
  - lots of more work to be done
- ⇒ LHC will be the coolest experiment ever!