

Alessandro Ratti

# HIGH PRECISION PREDICTIONS FOR HEAVY QUARK PHYSICS

Max-Planck-Institut  
für Physik



Ringberg

09 May 2022

# SUMMARY

- The top-pair production with MiNNLOps
- The bottom-pair production: general aspects and state of the art
- My current work: MiNNLOps applied to the bottom pair production (preliminary results)



# What do we mean for heavy quarks?

	mass →	charge →	spin →																									
QUARKS	$\approx 2.3 \text{ MeV}/c^2$	$2/3$	$1/2$	<b>u</b>	up	$\approx 1.275 \text{ GeV}/c^2$	$2/3$	$1/2$	<b>c</b>	charm	$\approx 173.07 \text{ GeV}/c^2$	$2/3$	$1/2$	<b>t</b>	top	0	0	1	<b>g</b>	gluon	$\approx 126 \text{ GeV}/c^2$	0	0	0	<b>H</b>	Higgs boson		
	$\approx 4.8 \text{ MeV}/c^2$	$-1/3$	$1/2$	<b>d</b>	down	$\approx 95 \text{ MeV}/c^2$	$-1/3$	$1/2$	<b>s</b>	strange	$\approx 4.18 \text{ GeV}/c^2$	$-1/3$	$1/2$	<b>b</b>	bottom	0	0	1	<b>γ</b>	photon								
	$0.511 \text{ MeV}/c^2$	-1	$1/2$	<b>e</b>	electron	$105.7 \text{ MeV}/c^2$	-1	$1/2$	<b>μ</b>	muon	$1.777 \text{ GeV}/c^2$	-1	$1/2$	<b>τ</b>	tau	0	-1	1	<b>Z</b>	Z boson								
	$< 2.2 \text{ eV}/c^2$	0	$1/2$	<b>ν<sub>e</sub></b>	electron neutrino	$< 0.17 \text{ MeV}/c^2$	0	$1/2$	<b>ν<sub>μ</sub></b>	muon neutrino	$< 15.5 \text{ MeV}/c^2$	0	$1/2$	<b>ν<sub>τ</sub></b>	tau neutrino	$80.4 \text{ GeV}/c^2$	$\pm 1$	1		<b>W</b>	W boson							

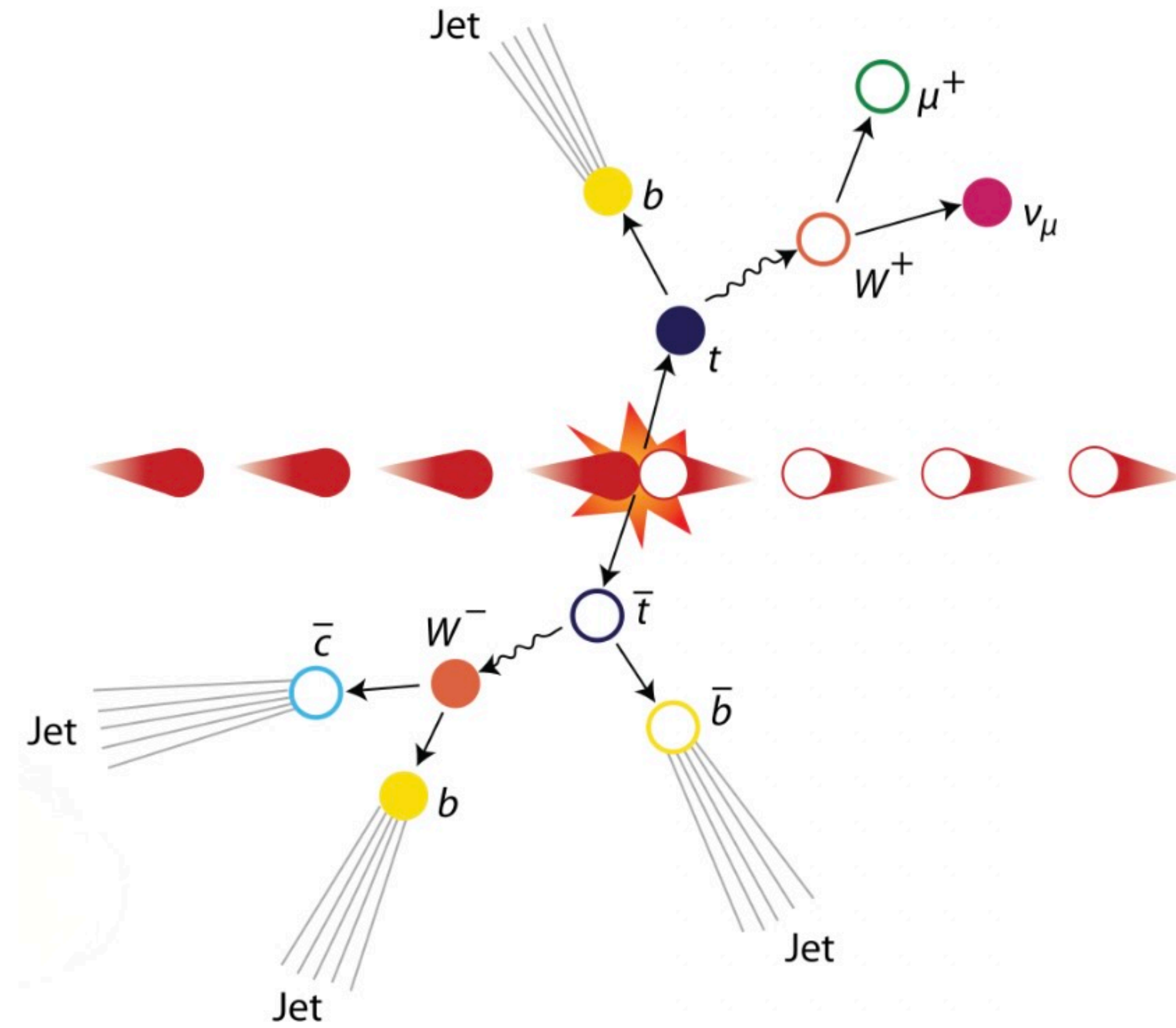
Typically c, b, t

... But in our analysis, just top and bottom will be considered massive



# Top-pair production at the LHC

## Theoretical aspects





# Top-pair production at the LHC

**Top mass is big**

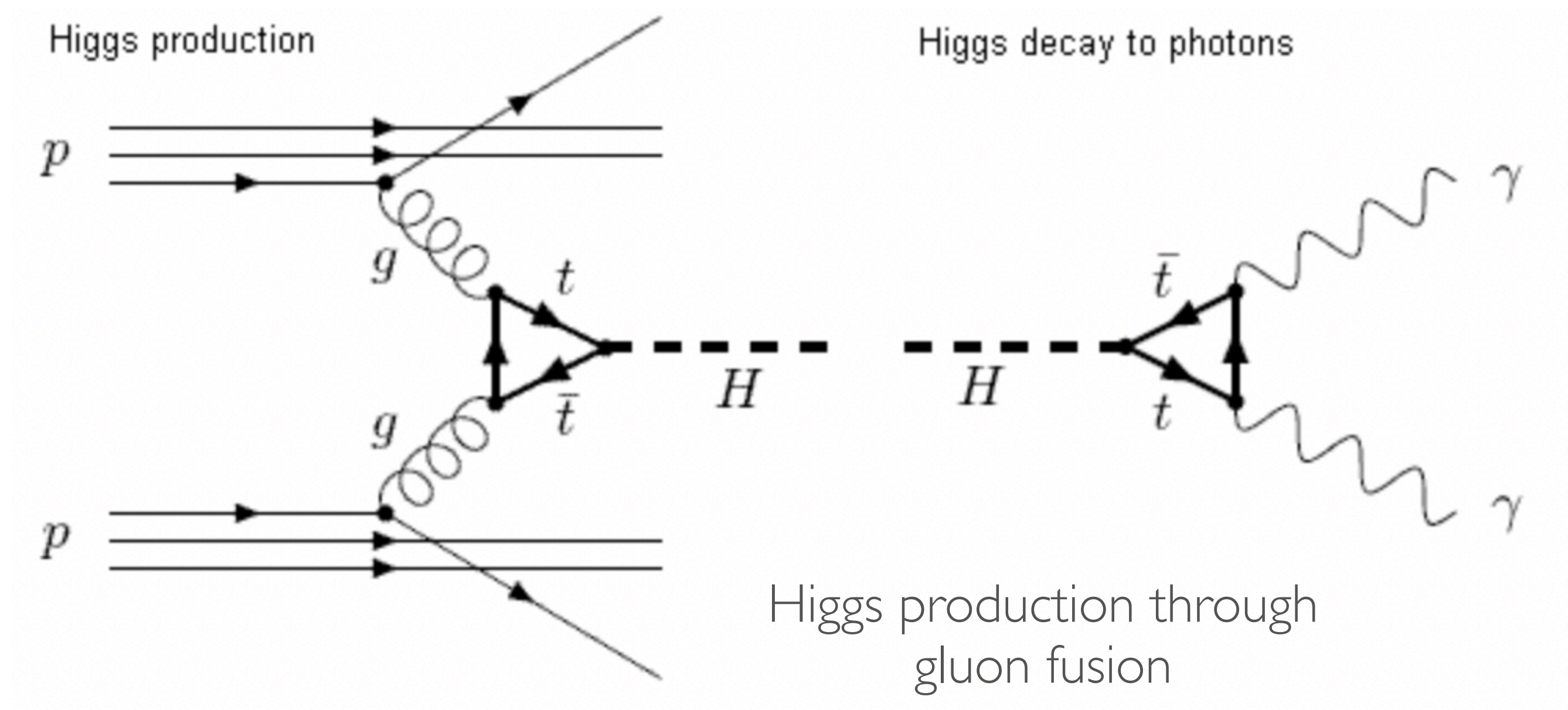
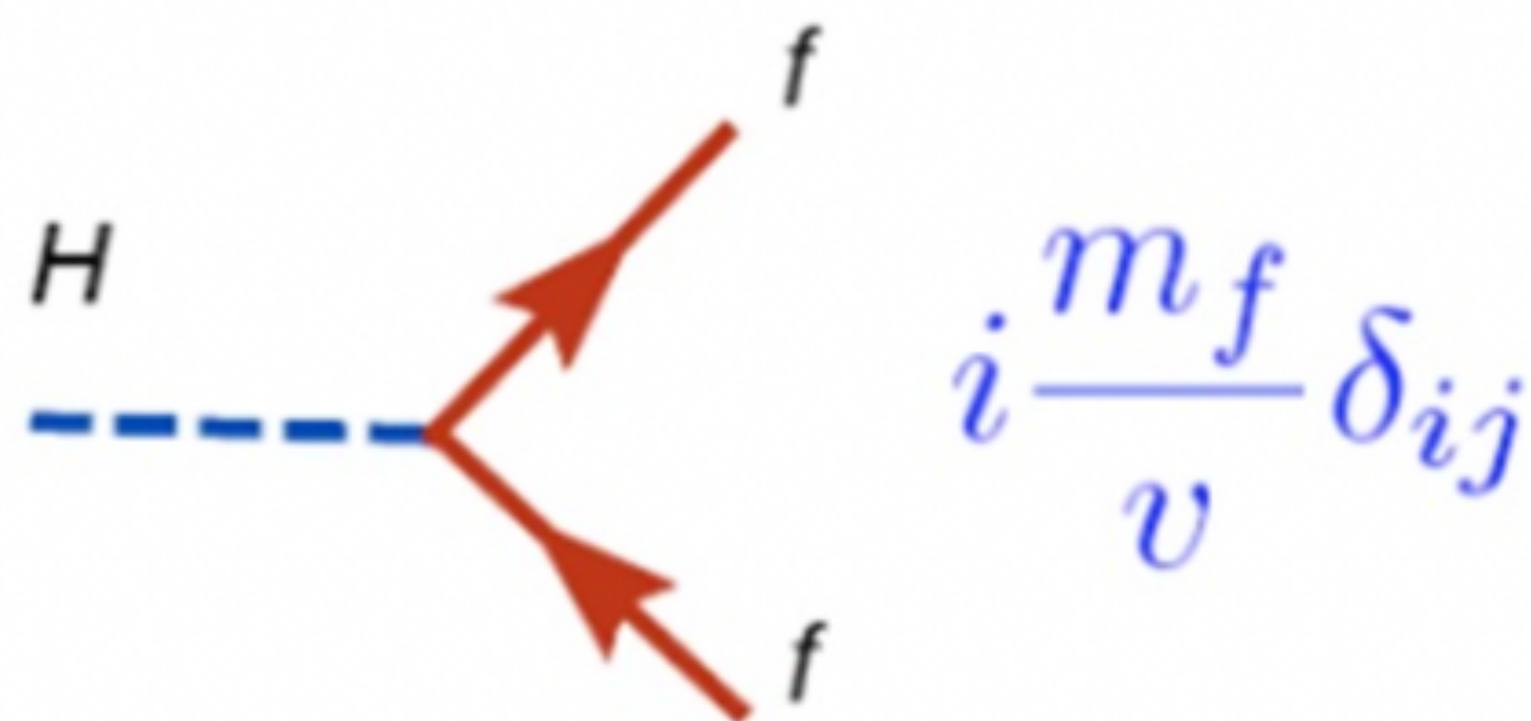


Big **Yukawa coupling**  
with Higgs



Top physics strongly  
related to **Higgs  
physics** (Higgs  
production, running...)

$$M_t \sim 173 \text{ GeV}/c^2$$





# Top-pair production at the LHC

Total cross section for tt production is really high



Top-pair production is a background for most LHC processes

$\sigma_{\text{NNLO}}$ [pb]	$q_T$ subtraction	TOP++
8 TeV	$238.5(2)^{+3.9\%}_{-6.3\%}$	$238.6^{+4.0\%}_{-6.3\%}$
13 TeV	$793.4(6)^{+3.5\%}_{-5.7\%}$	$794.0^{+3.5\%}_{-5.7\%}$

	<i>ZZ</i>	<i>WW</i>	<i>WZ</i>
baseline cuts	$pp \rightarrow \ell^- \ell^+ \nu_{\ell'} \bar{\nu}_{\ell'}$	$pp \rightarrow \ell^- \ell'^+ \nu_{\ell'} \bar{\nu}_{\ell}$	$pp \rightarrow \ell^- \ell^+ \ell' \nu_{\ell'}$
$\sigma_{\text{LO}}$ [fb]	$18.9417(4)^{+4.2\%}_{-5.2\%}$	$240.221(5)^{+5.1\%}_{-6.2\%}$	$21.8960(3)^{+4.2\%}_{-5.3\%}$
$\sigma_{\text{NLO EW}}$ [fb]	$17.7713(4)^{+4.3\%}_{-5.4\%}$	$235.118(5)^{+5.1\%}_{-6.1\%}$	$21.1849(4)^{+4.3\%}_{-5.4\%}$
$\sigma_{\text{NLO QCD}}$ [fb]	$25.690(1)^{+2.9\%}_{-2.4\%}$	$370.35(1)^{+4.2\%}_{-3.3\%}$	$38.138(1)^{+4.7\%}_{-3.8\%}$
$\sigma_{\text{NNLO QCD}}$ [fb]	$29.63(2)^{+3.0\%}_{-2.6\%}$	$424.6(3)^{+3.0\%}_{-2.7\%}$	$42.28(2)^{+2.3\%}_{-2.1\%}$
$\sigma_{\text{NNLO QCD+EW}}$ [fb]	$28.46(2)^{+3.3\%}_{-2.7\%}$	$419.5(3)^{+3.0\%}_{-2.8\%}$	$41.57(2)^{+2.4\%}_{-2.2\%}$
$\sigma_{\text{NNLO QCD} \times \text{EW}}$ [fb]	$27.92(2)^{+3.1\%}_{-2.6\%}$	$416.0(3)^{+3.0\%}_{-2.7\%}$	$40.90(2)^{+2.2\%}_{-2.1\%}$
$\sigma_{\text{NNLO QCD} \times \text{EW}_{\text{qq}}}$ [fb]	$27.92(2)^{+3.1\%}_{-2.6\%}$	$413.5(3)^{+3.0\%}_{-2.7\%}$	$40.53(2)^{+2.1\%}_{-2.1\%}$



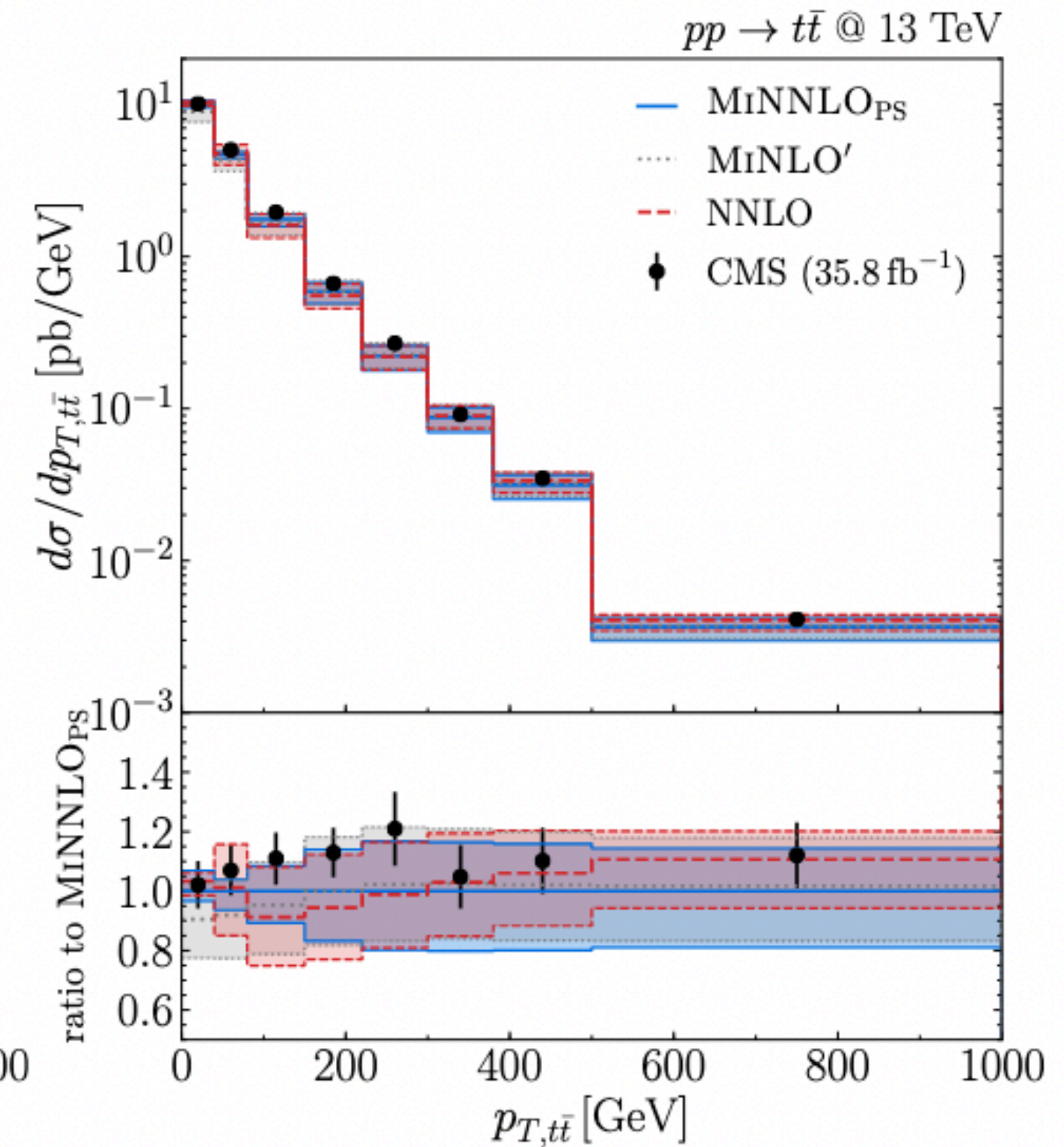
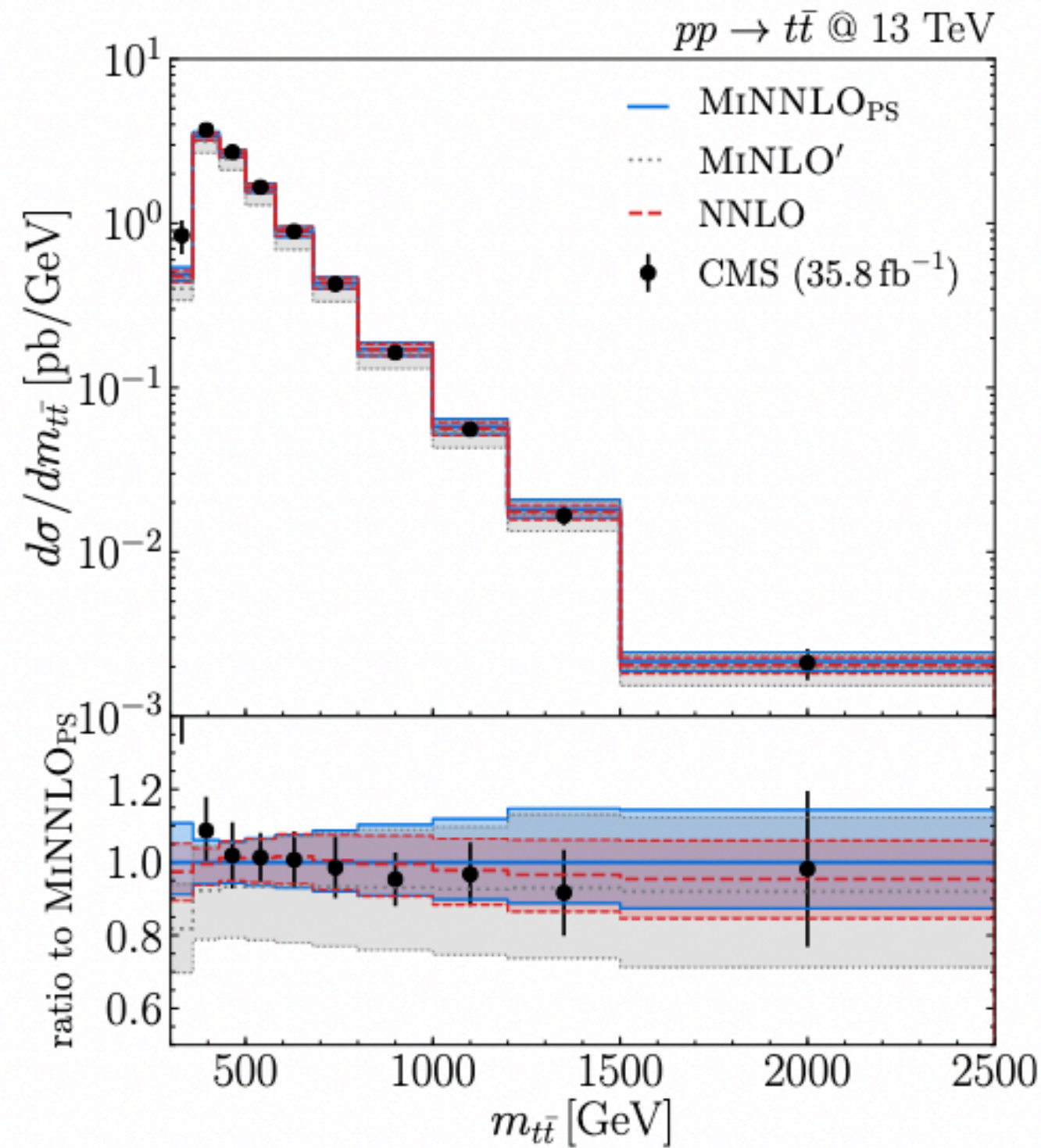
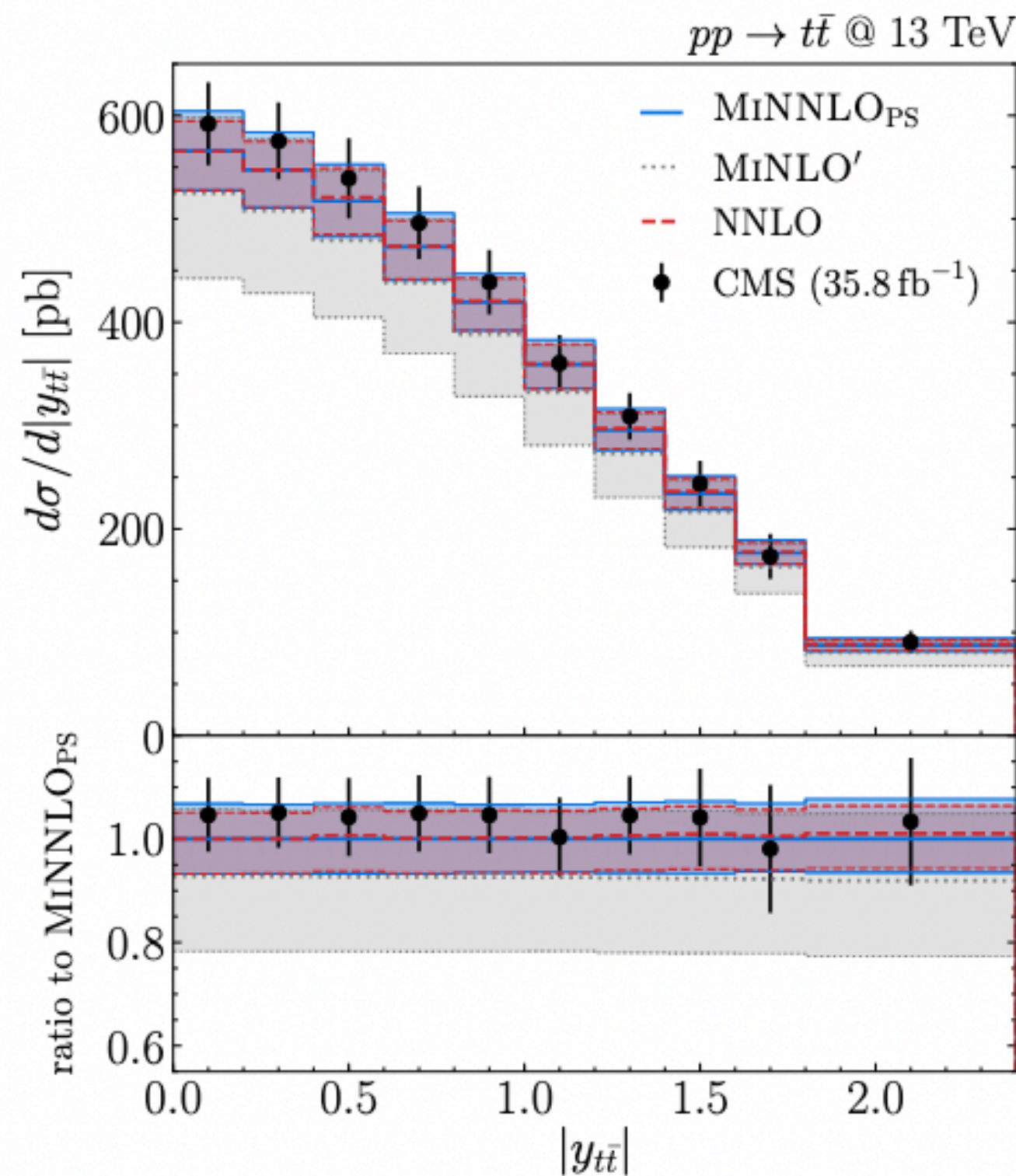
# Top-pair production with MiNNLOps

MiNNLOps adapted to processes involving final state cartons

$\sigma_{\text{NNLO}}$ [pb]	$q_T$ subtraction	TOP++
8 TeV	$238.5(2)^{+3.9\%}_{-6.3\%}$	$238.6^{+4.0\%}_{-6.3\%}$
13 TeV	$793.4(6)^{+3.5\%}_{-5.7\%}$	$794.0^{+3.5\%}_{-5.7\%}$

MiNLO'	MiNNLO <sub>PS</sub>
$695.6(3)^{+22\%}_{-17\%}$ pb	$775.5(2)^{+9.8\%}_{-7.2\%}$ pb

(13 TeV)

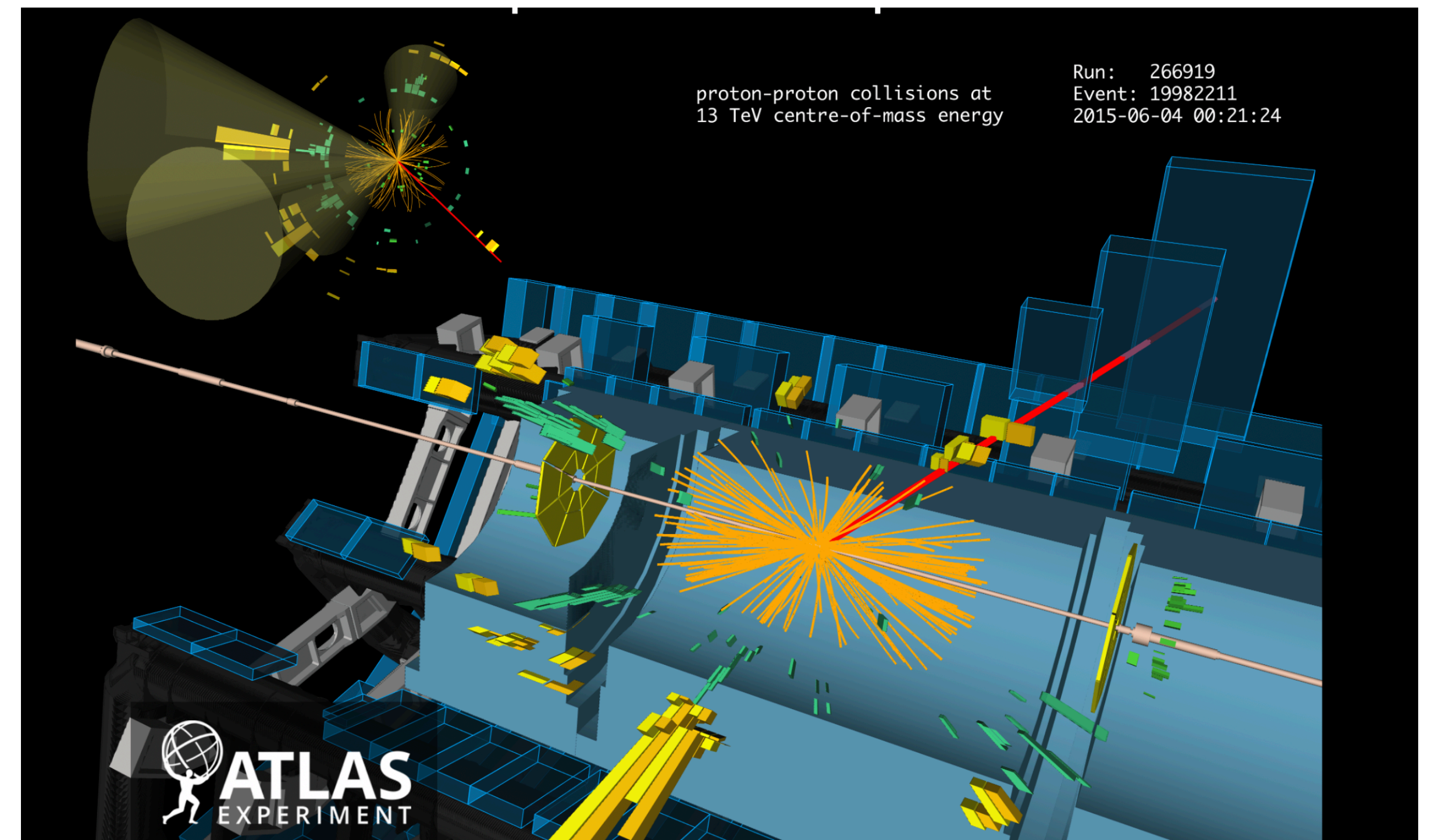




# Bottom-pair production at the LHC

Experimental results from:

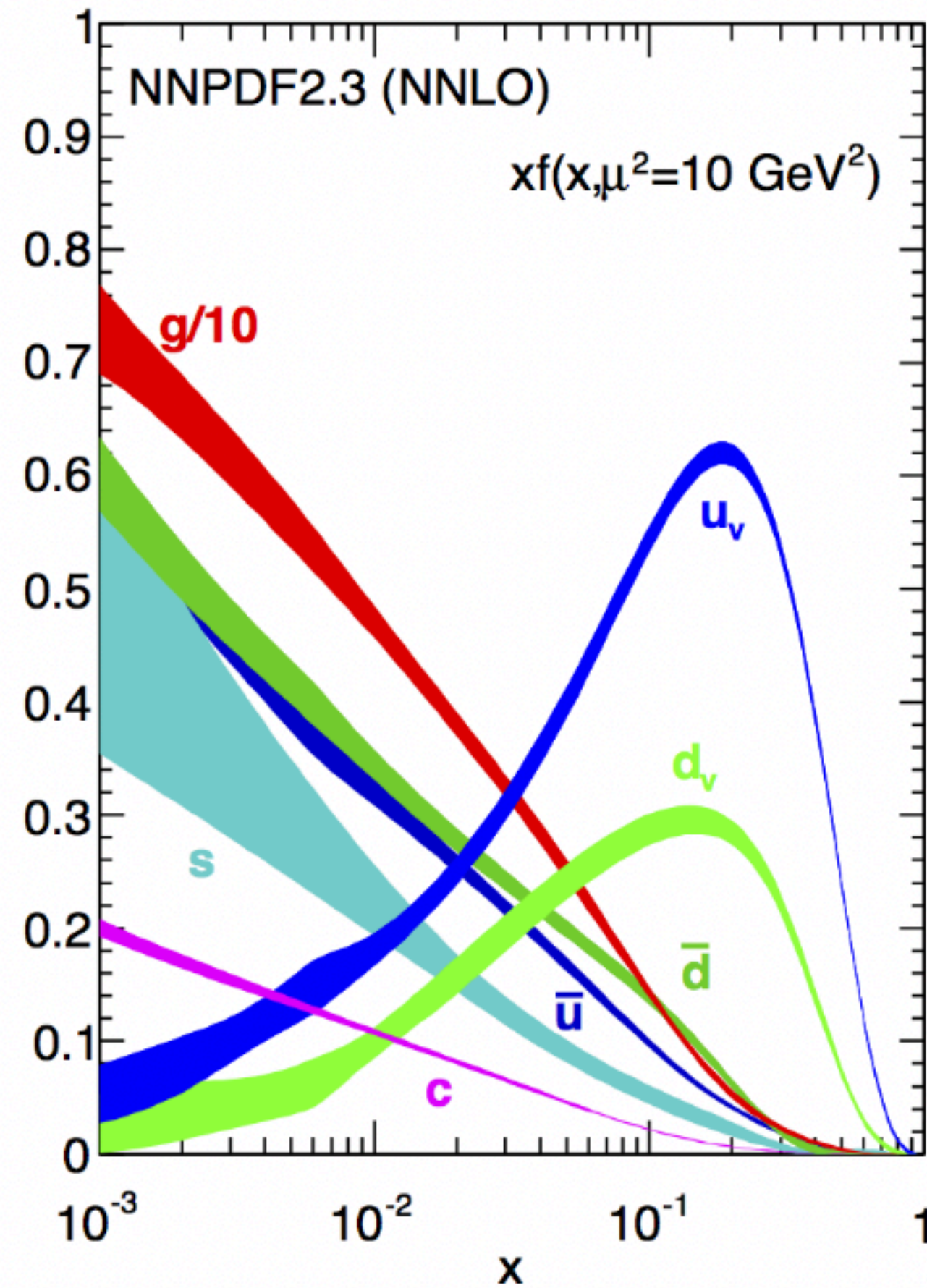
- UAI collaboration at **CERN**
- CDF and D0 collaborations at **Fermilab Tevatron**
- **ALICE, ATLAS, CMS, LHCb**





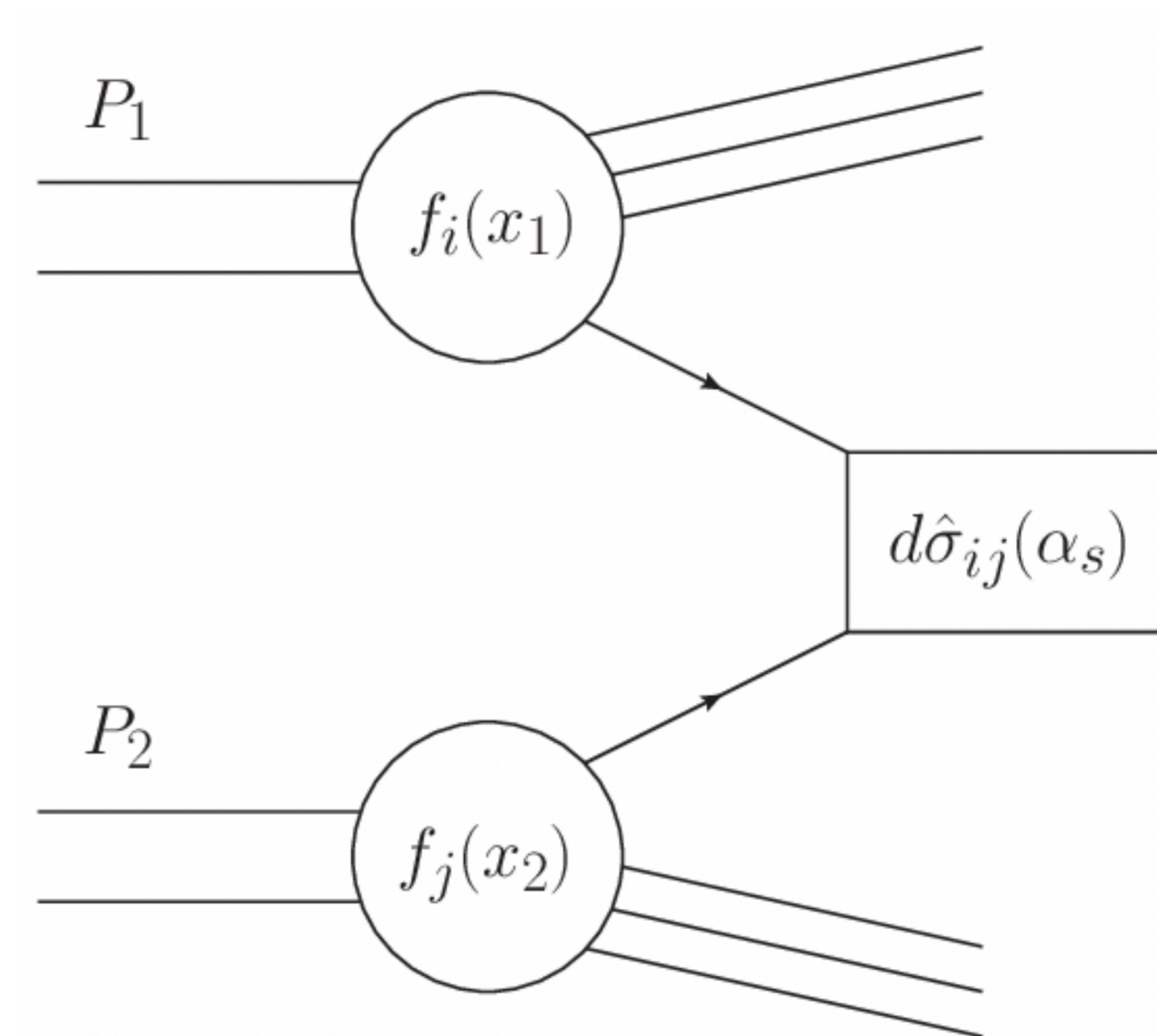
# Bottom-pair production at the LHC

## Theoretical aspects



Plot from PDG2013 update

$$d\sigma(pp \rightarrow b\bar{b} + X) = \sum_{i,j} \int dx_1 dx_2 f_i(x_1) f_j(x_2) d\hat{\sigma}_{ij}(\alpha_s)$$





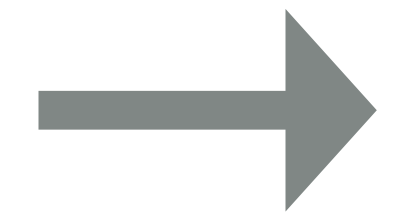
# Bottom-pair production at the LHC

## Theoretical aspects

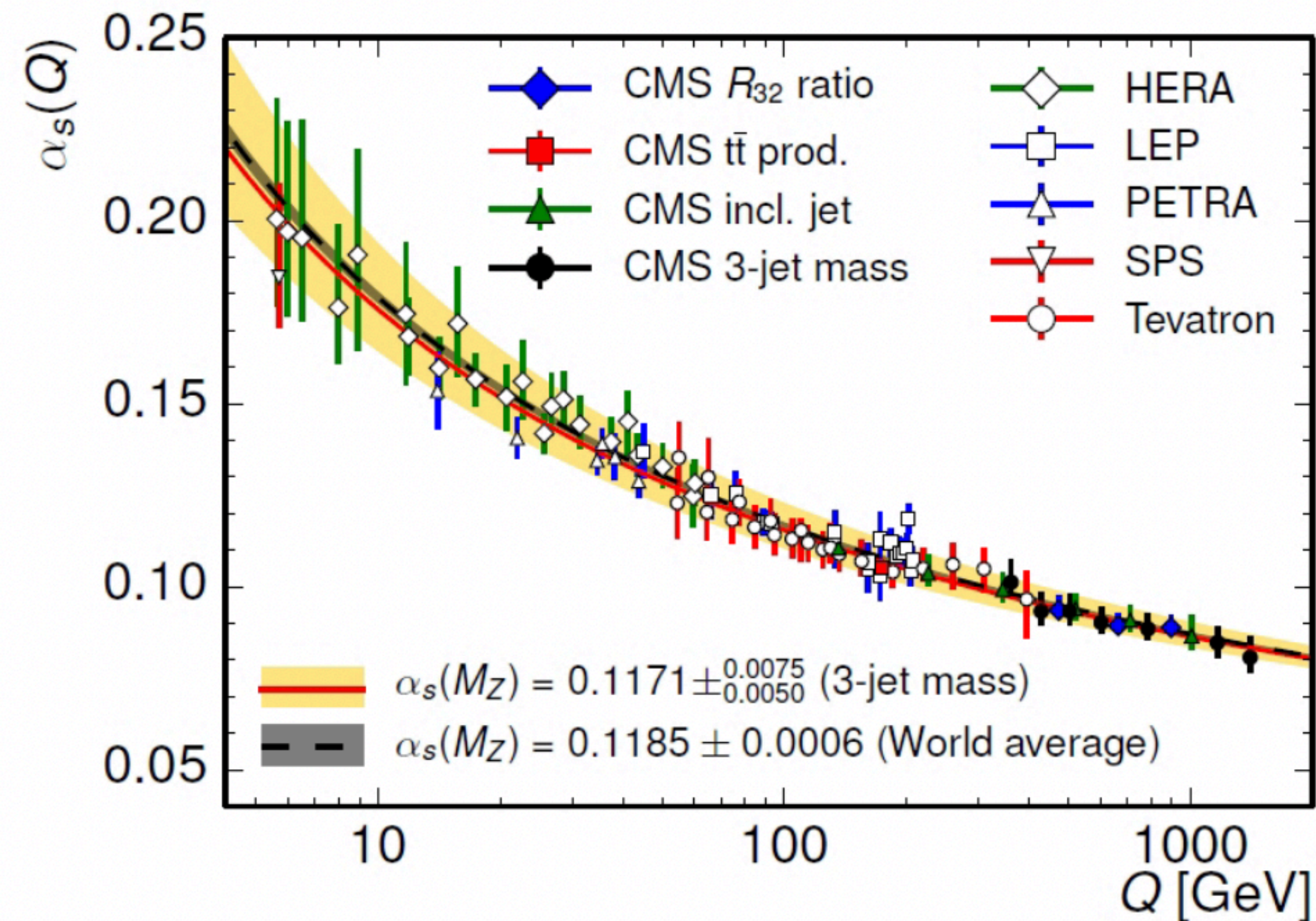
Slow convergence of  
perturbative series

$$\sigma = \sigma^{(0)} \alpha_s(\mu) + \sigma^{(1)} \alpha_s^2(\mu) + \sigma^{(2)} \alpha_s^3(\mu) + \dots$$

$\mu = \text{renorm. scale}$



$m_b$



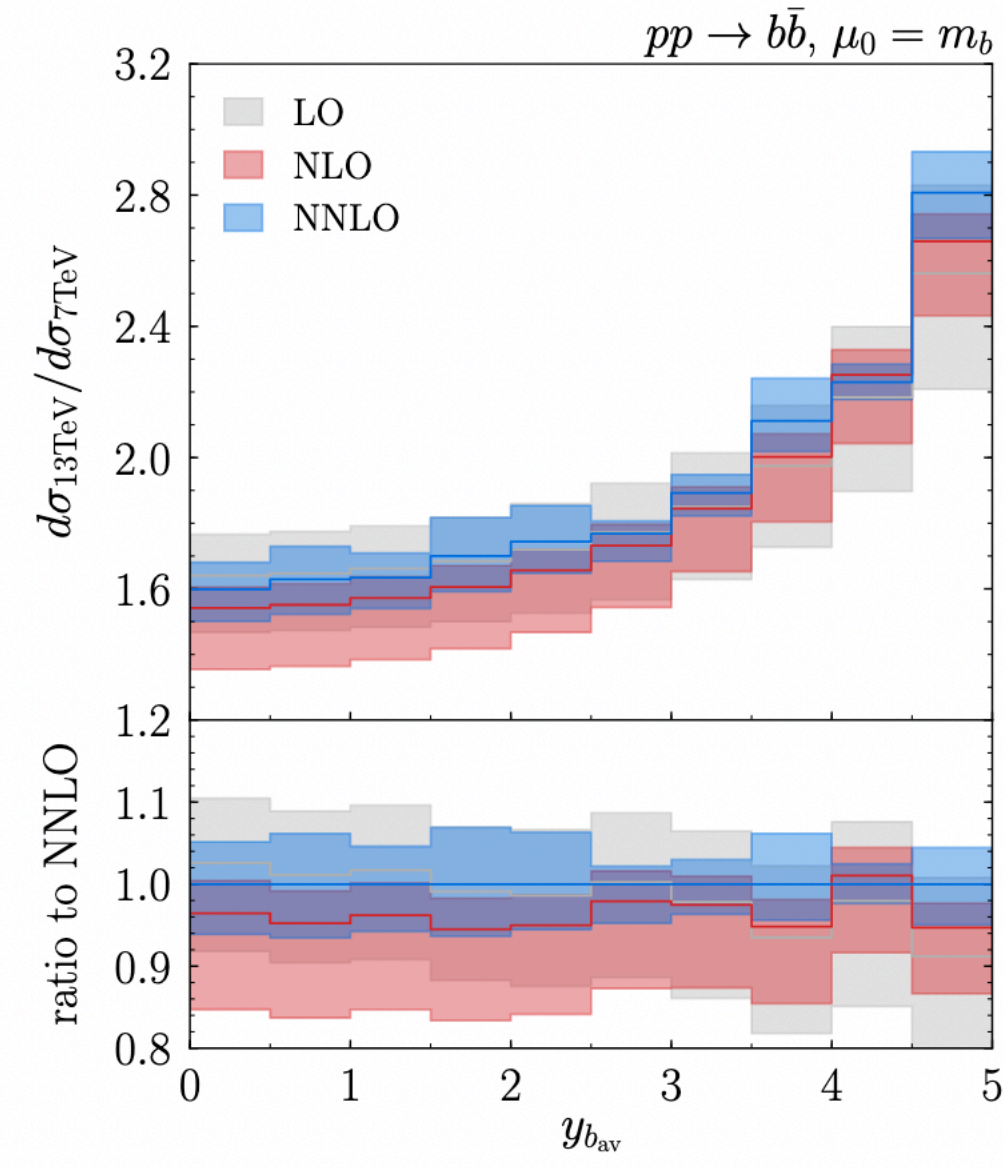
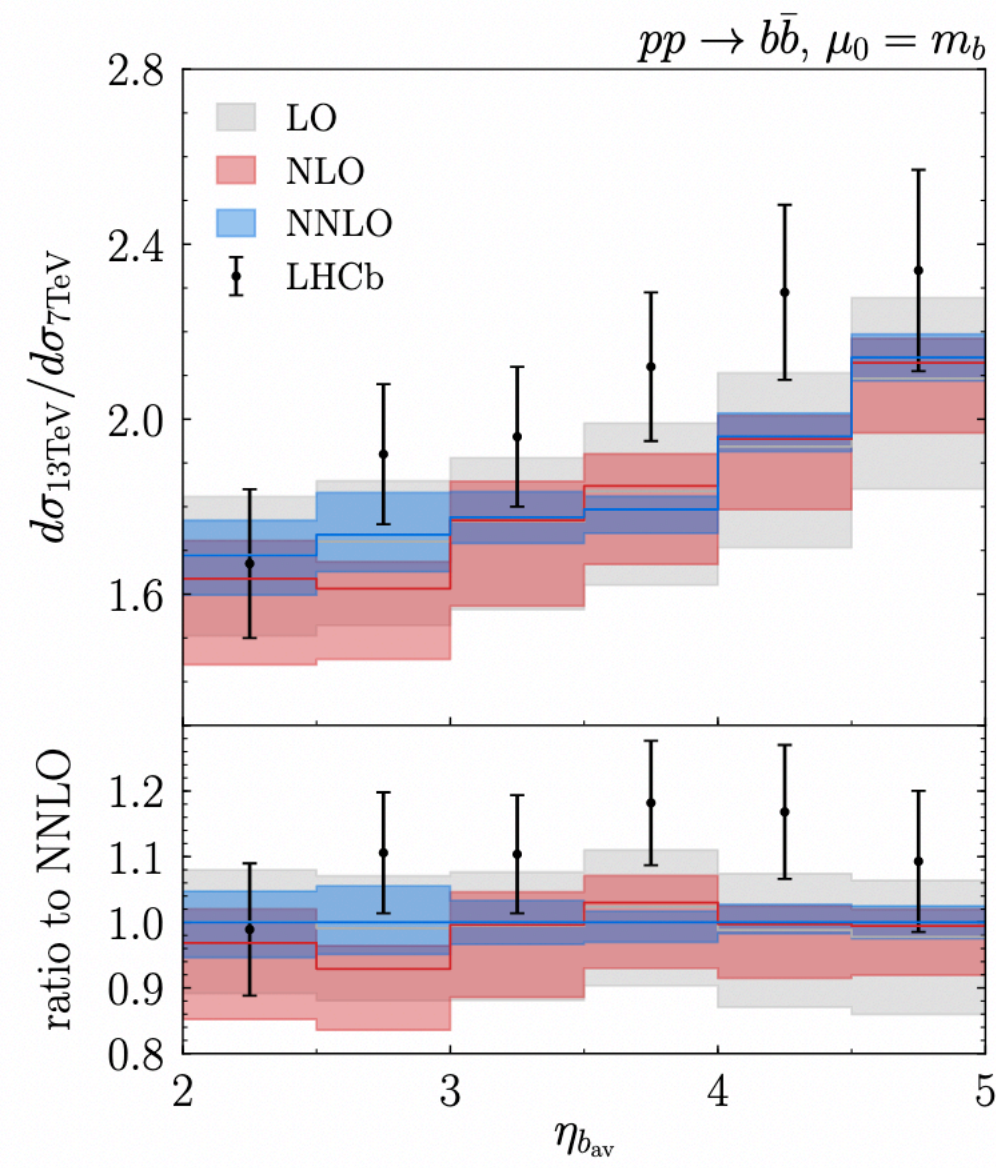
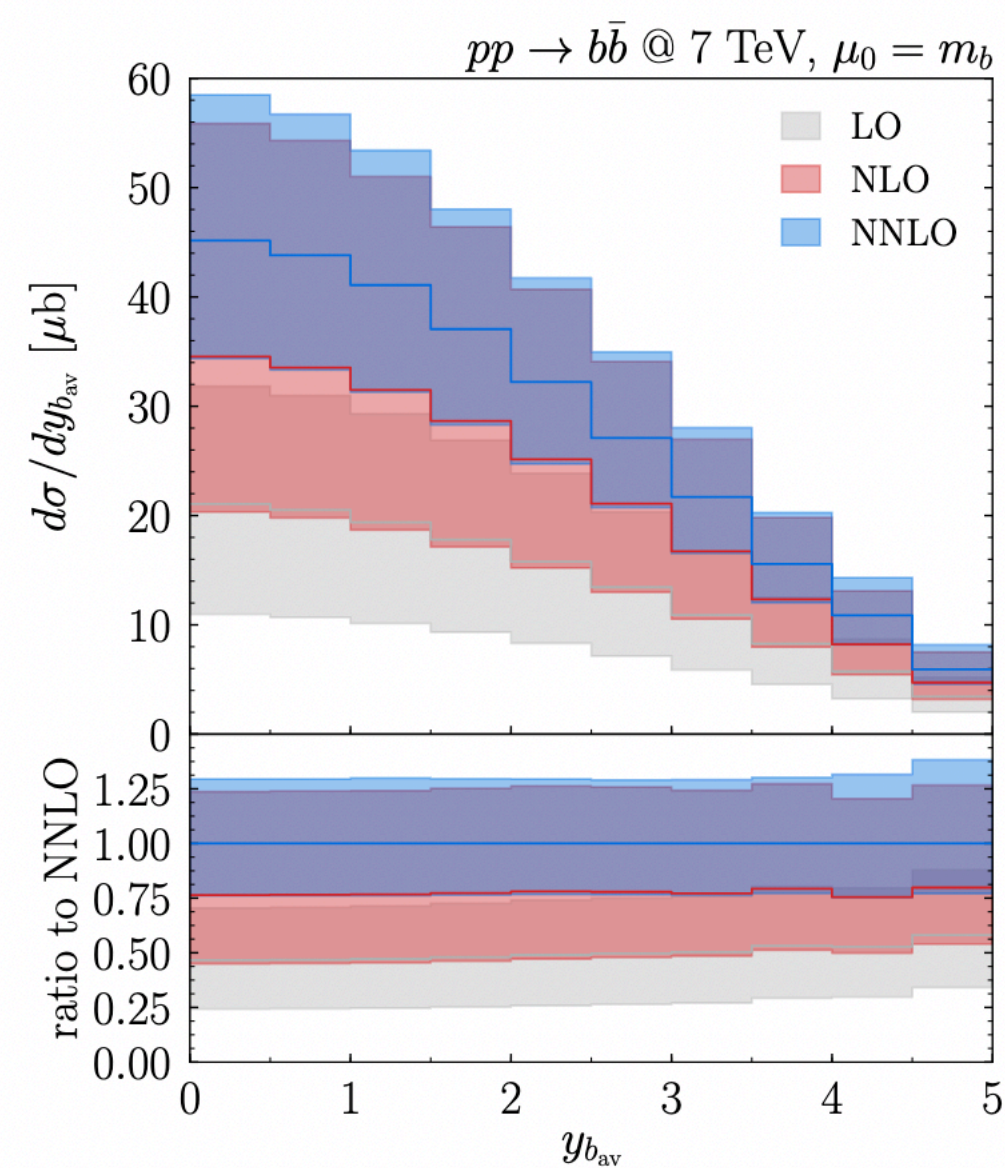
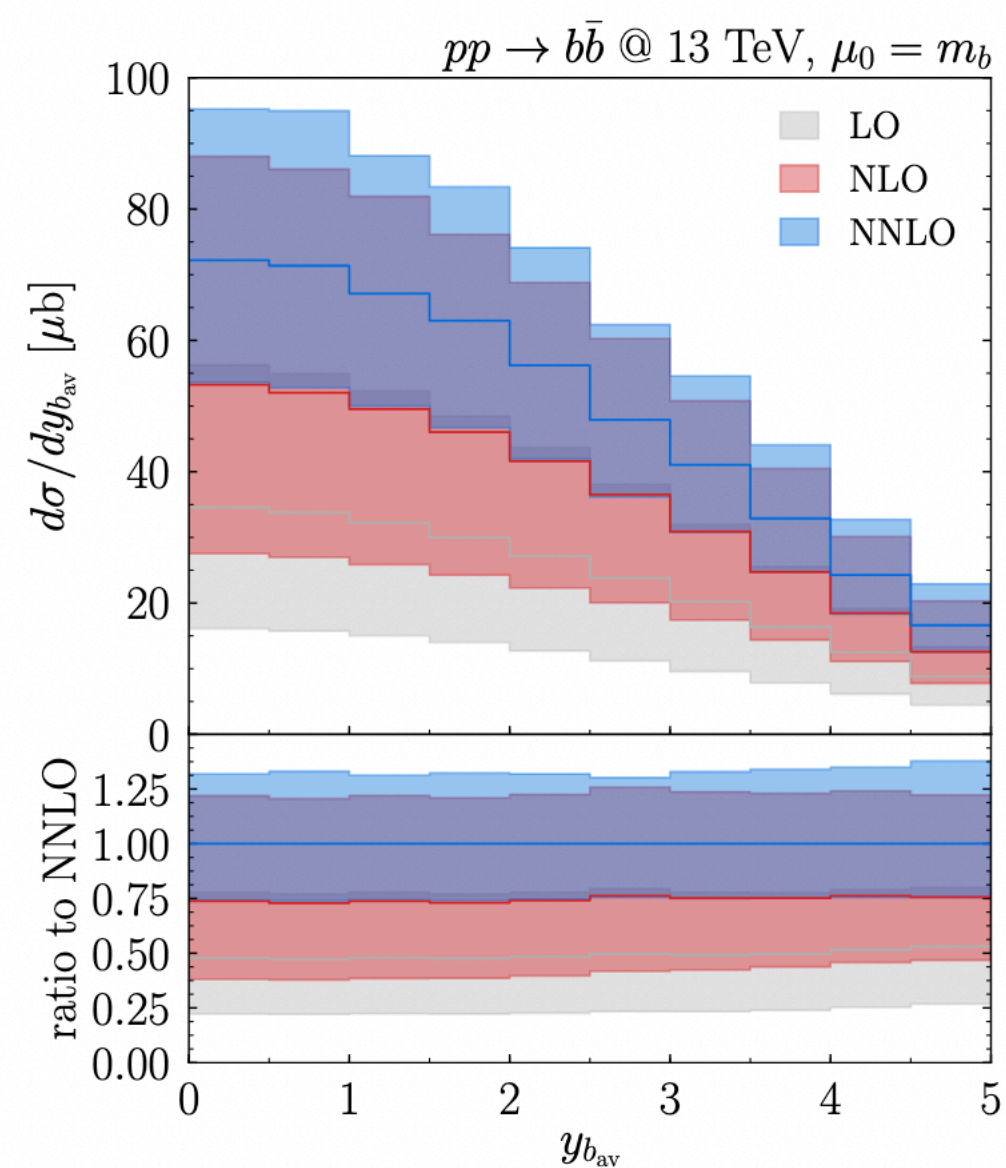


# Bottom-pair production at the LHC

## Theoretical aspects

Slow convergence of perturbative series

$\sigma$ [ $\mu\text{b}$ ]	$p\bar{p}$ @ 1.96 TeV	$pp$ @ 7 TeV	$pp$ @ 13 TeV
	$\mu_0 = m_b$		
LO	34.66 $+51\%$ $-32\%$	138.7 $+51\%$ $-46\%$	249.0 $+59\%$ $-51\%$
NLO	60.23 $+54\%$ $-28\%$	219.8 $+61\%$ $-39\%$	378.6 $+65\%$ $-45\%$
NNLO	75.4(3) $+22\%$ $-21\%$	288(2) $+30\%$ $-24\%$	508(3) $+32\%$ $-25\%$





# Bottom-pair production at the LHC

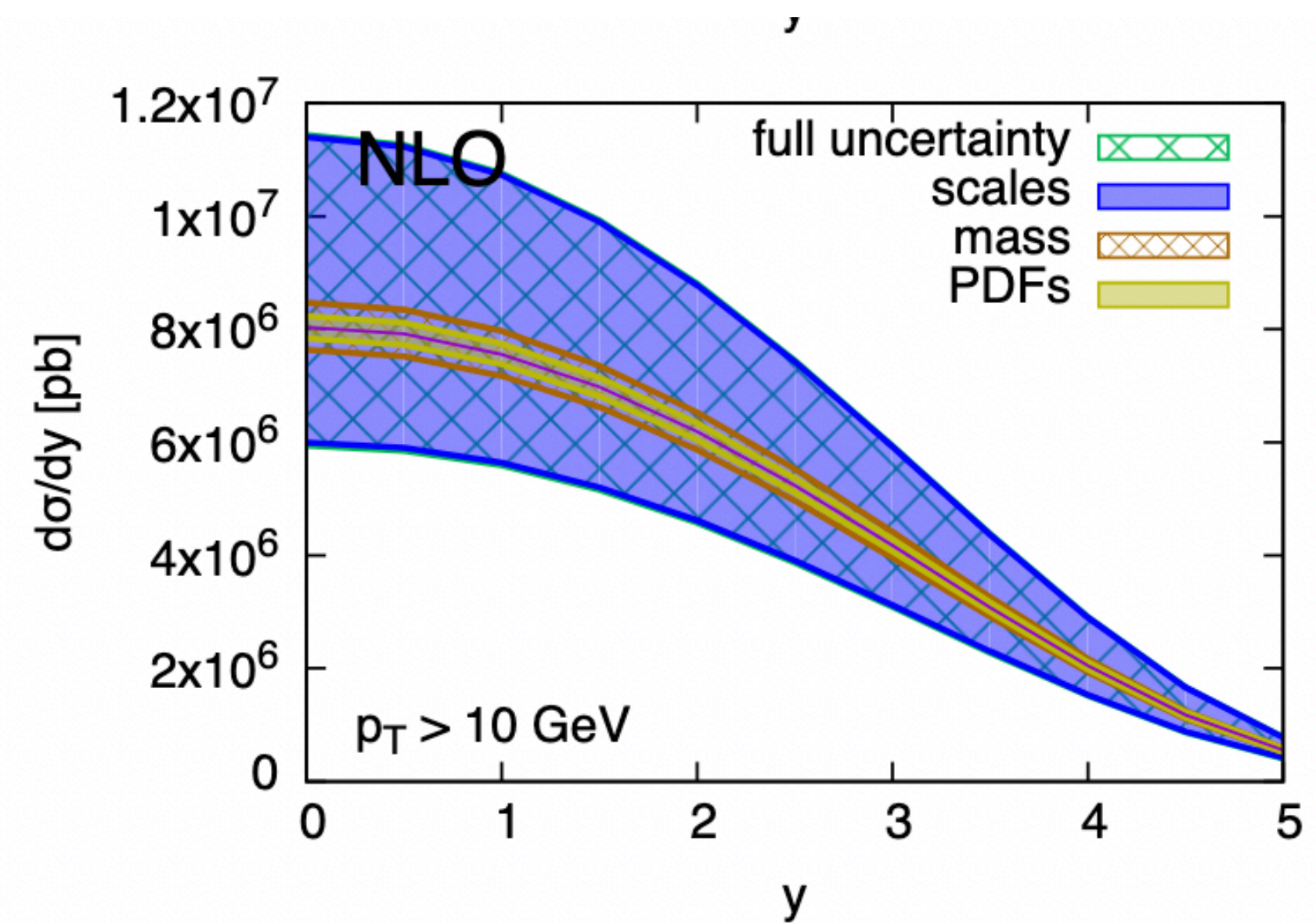
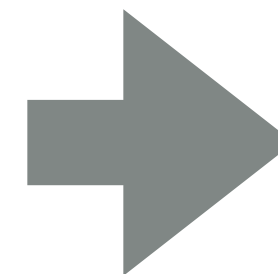
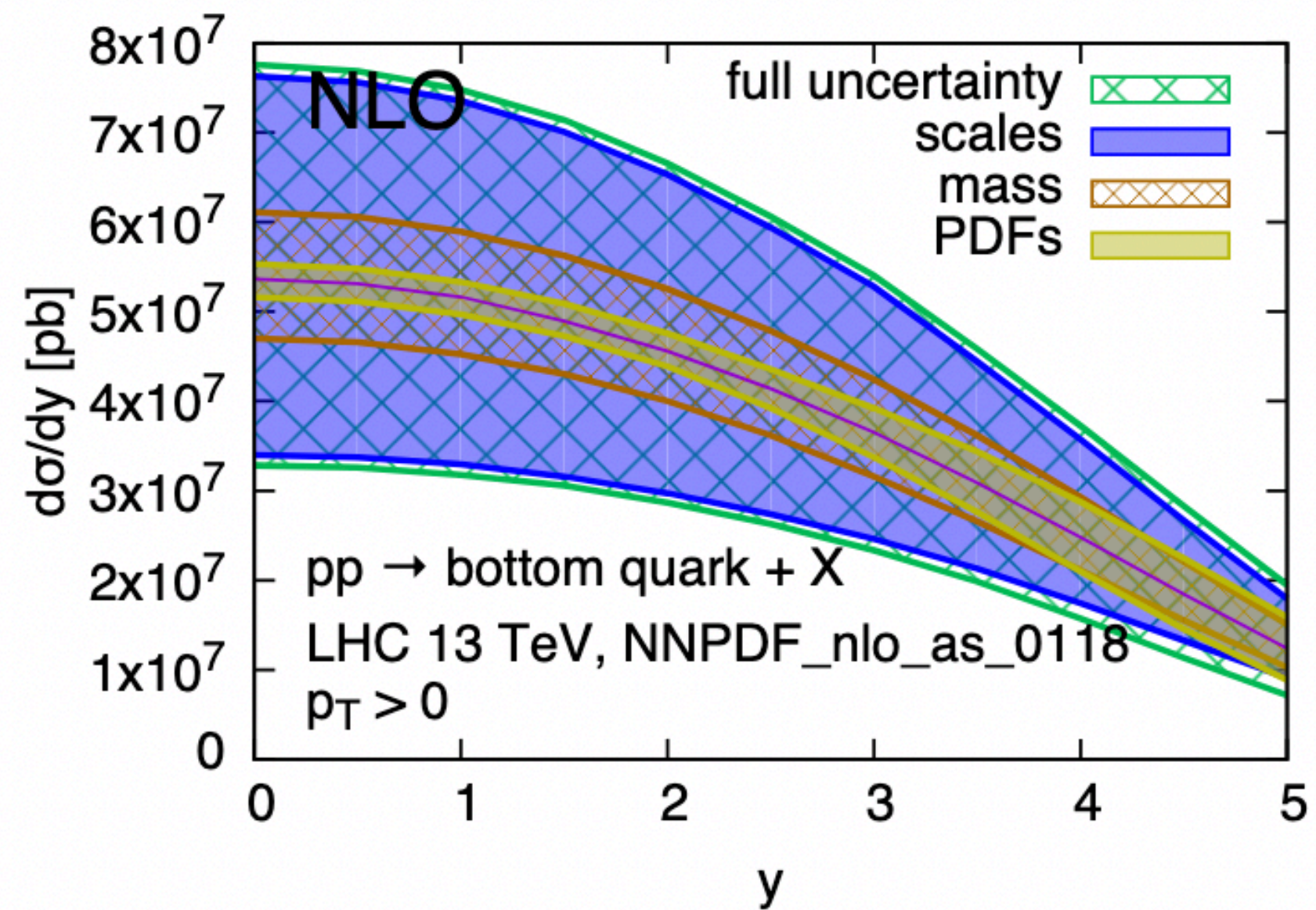
## Theoretical aspects

Resummation of large logarithms can be performed at high  $p_T$

$$\sigma = \sigma^{(0)} \alpha_s(\mu) + \sigma^{(1)} \alpha_s^2(\mu) + \sigma^{(2)} \alpha_s^3(\mu) + \dots$$

$$L = \ln(p_T/m_b)$$

(Can be performed through fragmentation functions...)

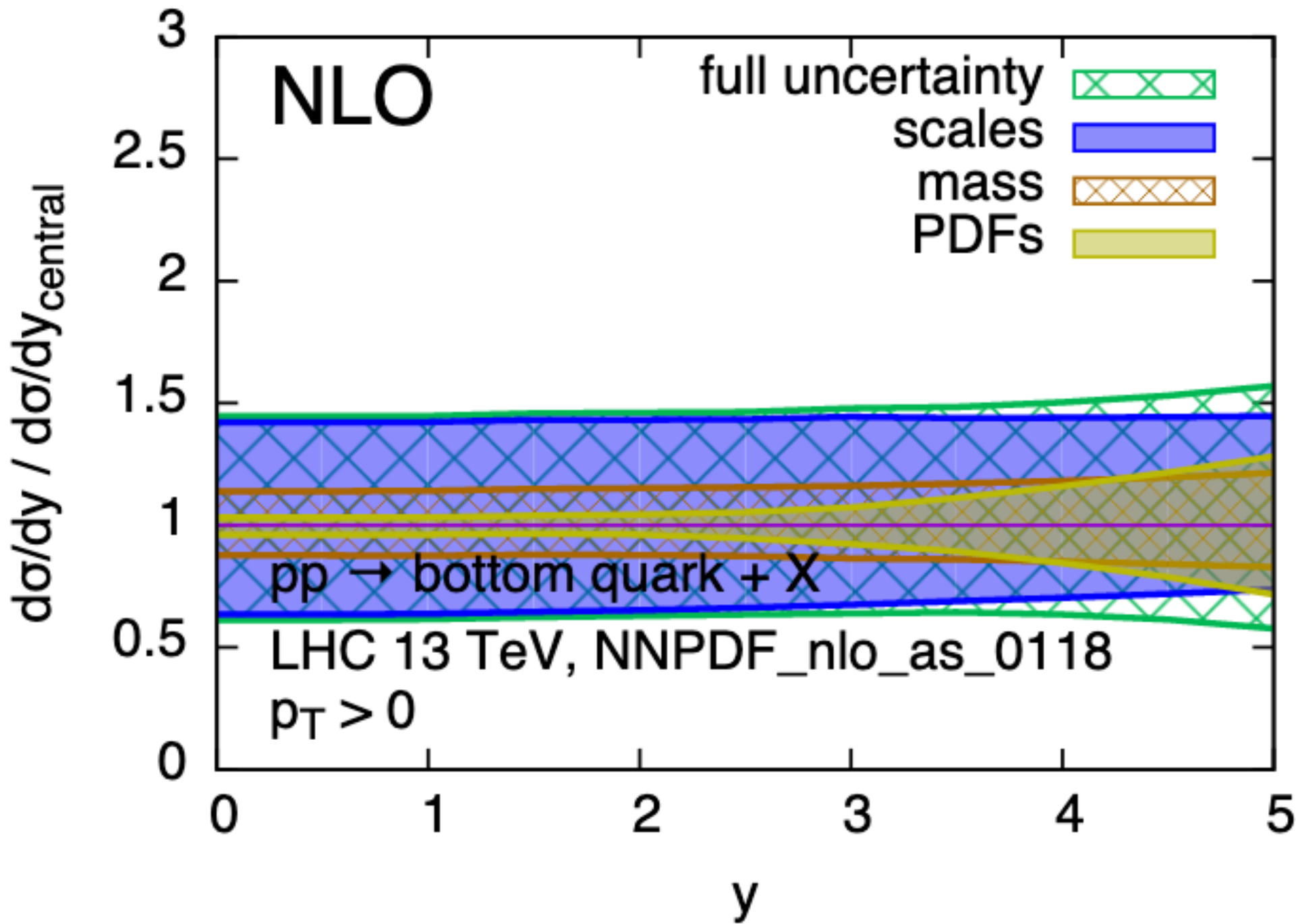




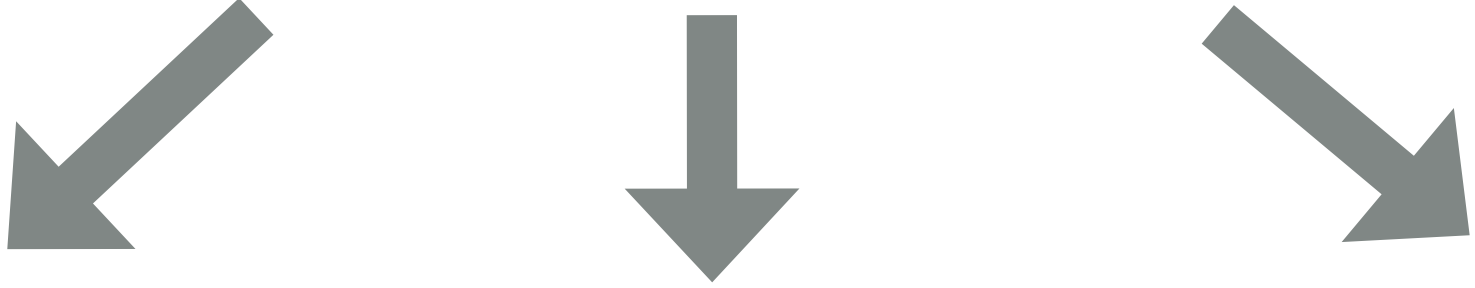
# Bottom-pair production at the LHC

## Theoretical aspects

Bottom-pair production can be exploited to constrain uncertainties of PDFs



Sistematics are given by:



Scale choice

PDFs

Bottom mass

How scale variation is determined (7 points envelope)



# Bottom-pair production at the LHC

## Theoretical aspects

Bottom-pair production can be exploited to constrain uncertainties of PDFs

Systematics are given by:



	$\sigma_{\text{NNLO}}(\mu\text{b})$	$\Delta\sigma_{\text{scale}}$	$\Delta\sigma_{\text{mass}}$	$\Delta\sigma_{\text{PDFs}}$	$\Delta\sigma_{\alpha_S}$
$p\bar{p}$ @ 1.96 TeV	75.4(3)	+22% -21%	+9.8% -8.7%	$\pm 1.3\%$	+0.9% -3.0%
$pp$ @ 7 TeV	288(2)	+30% -24%	+7.9% -7.2%	$\pm 2.8\%$	+0.3% -2.9%
$pp$ @ 13 TeV	508(3)	+32% -25%	+7.4% -6.8%	$\pm 4.6\%$	+0.0% -3.0%

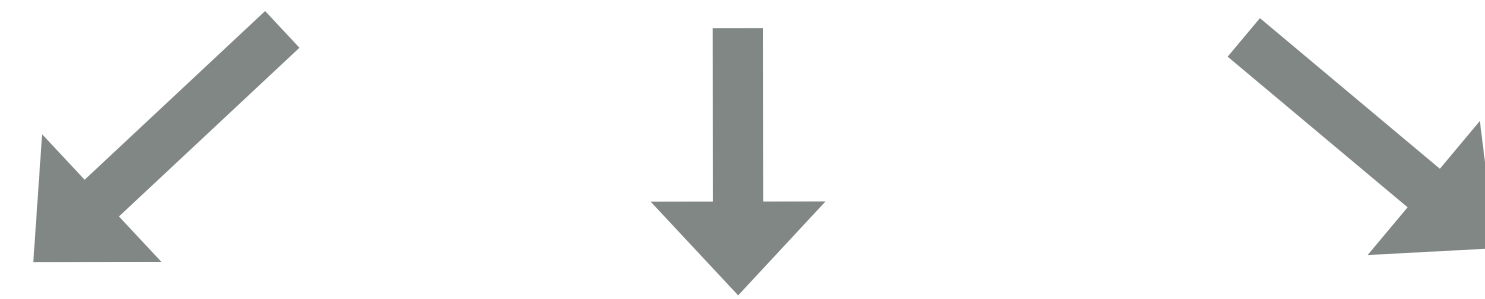


# Bottom-pair production at the LHC

## Theoretical aspects

Bottom-pair production can be exploited to constrain uncertainties of PDFs

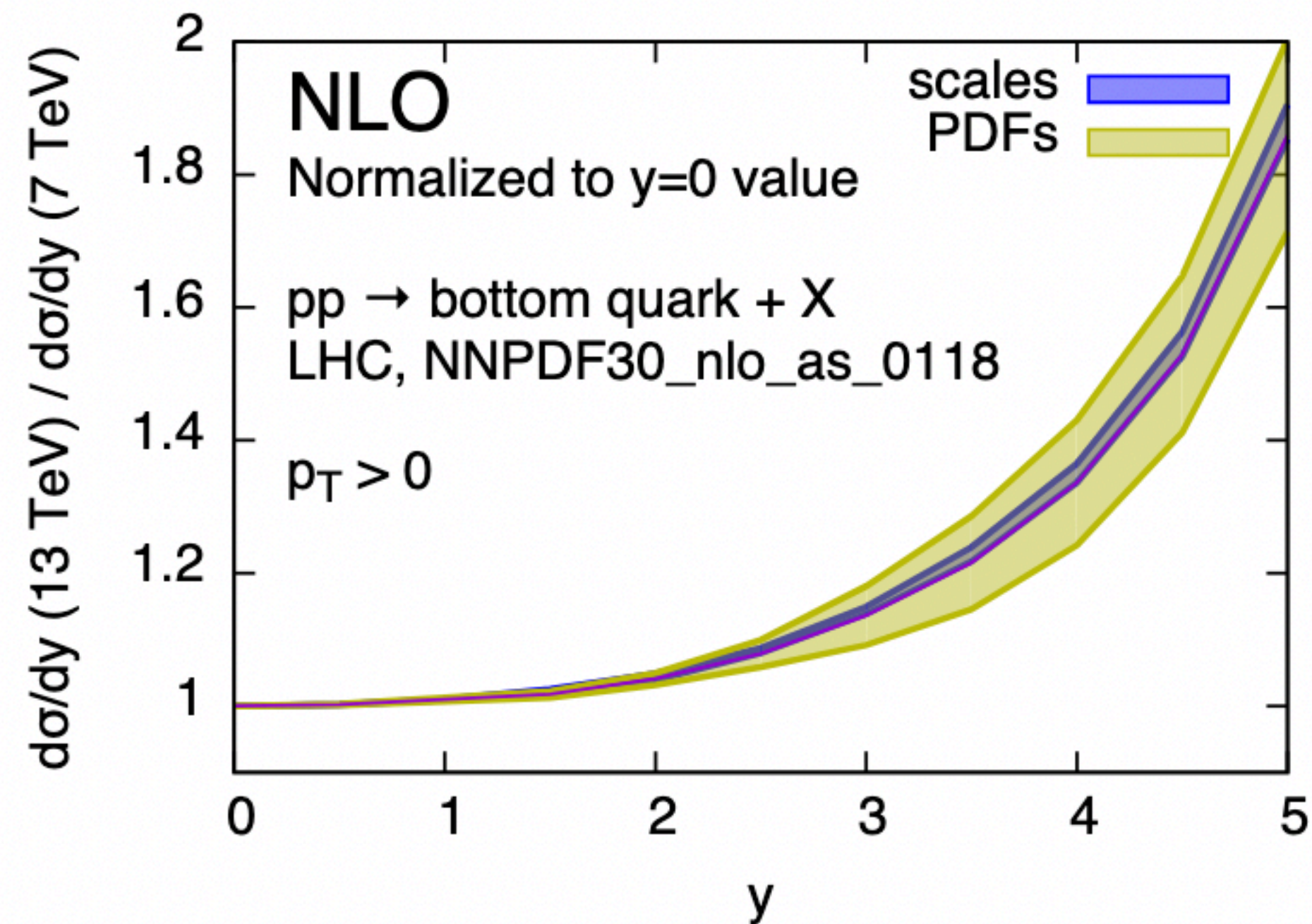
Systematics are given by:



Scale choice

PDFs

Bottom mass



BUT IF WE CONSIDER THE RATIO

$$R(y) = \frac{\left(\frac{d\sigma}{dy}\right)(13\text{ TeV})}{\left(\frac{d\sigma}{dy}\right)(7\text{ TeV})}$$



# Bottom-pair production at the LHC

## Event generator

At the moment:

- Code for bottom-pair production (+ 1 jet) has been implemented in the POWHEG-BOX framework and validated against numerical results from MATRIX
- MiNLO' and MiNNLOps methods implemented, but results are still preliminary

Total cross section  
at NLO for

$$pp \rightarrow b\bar{b} + jet$$

(Cutoff on jet transverse momentum and rapidity)

POWHEG	MATRIX
$37.99 \pm 0.58 \mu b$	$37.48 \pm 0.26 \mu b$



# Bottom-pair production at the LHC

Event generator

**Fixed order results**



# Bottom-pair production at the LHC

Event generator

**MiNLO and MiNNLOps preliminary results**