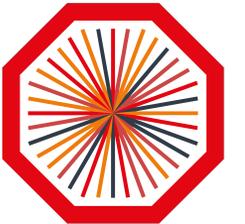
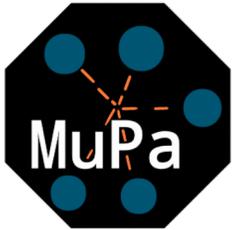


Symmetry Plane Correlations in Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV with ALICE at the LHC

Marcel Lesch

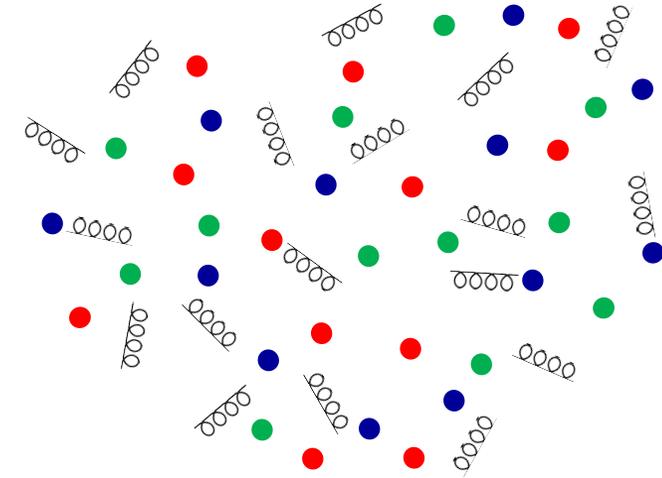
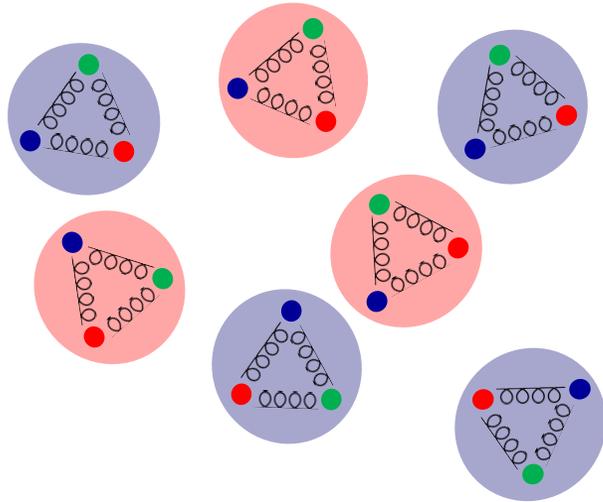
Technical University of Munich

15th of November 2021, IMPRS Recruiting Workshop



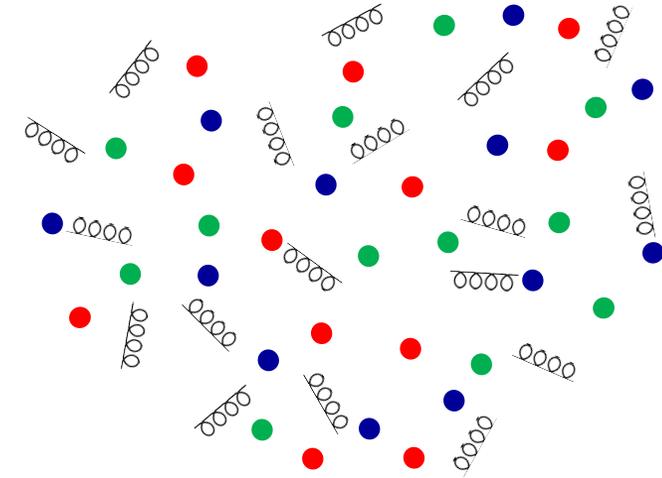
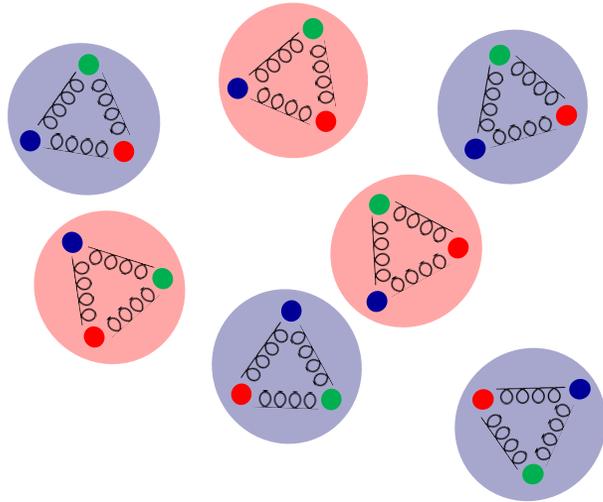
ALICE

Study of an extreme state of matter

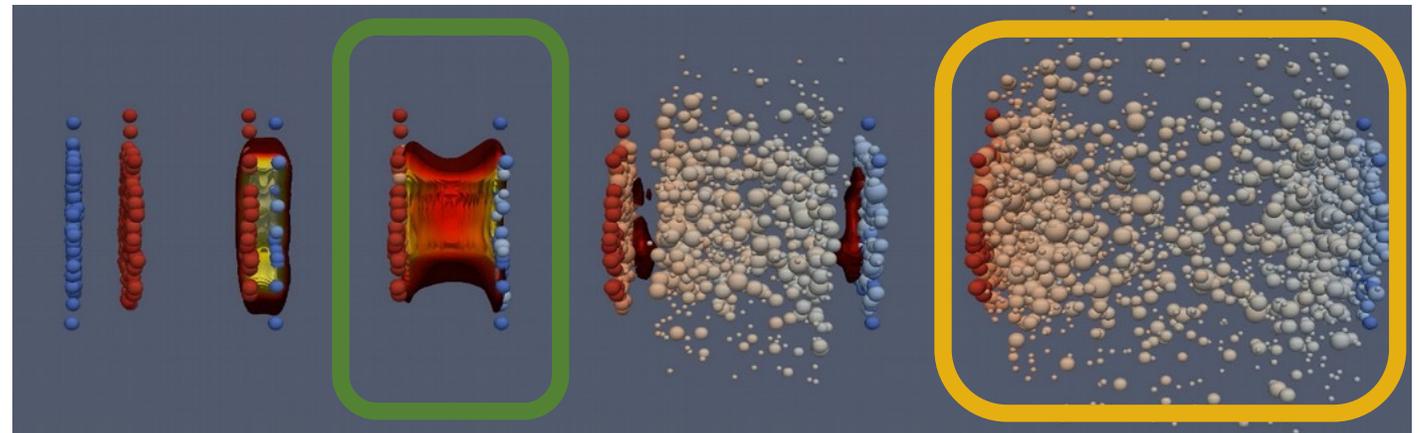


- Existence of Quark-Gluon Plasma (QGP) at extreme temperatures
- Important for
 - the evolution of the Early Universe
 - the general understanding of the strong interaction

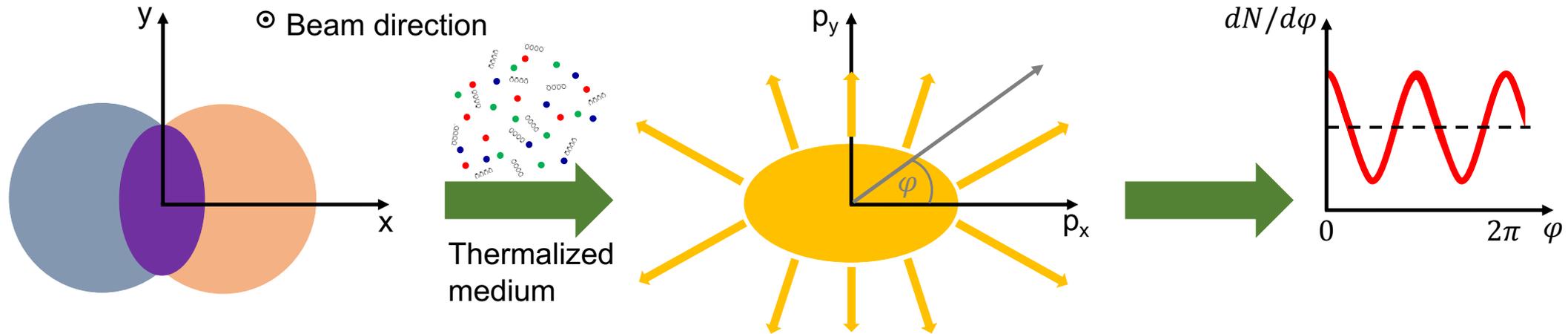
Study of an extreme state of matter



- Study of the **QGP** in heavy-ion collisions, e.g. Pb-Pb at the LHC
- Collectivity of **produced particles** introduced by QGP

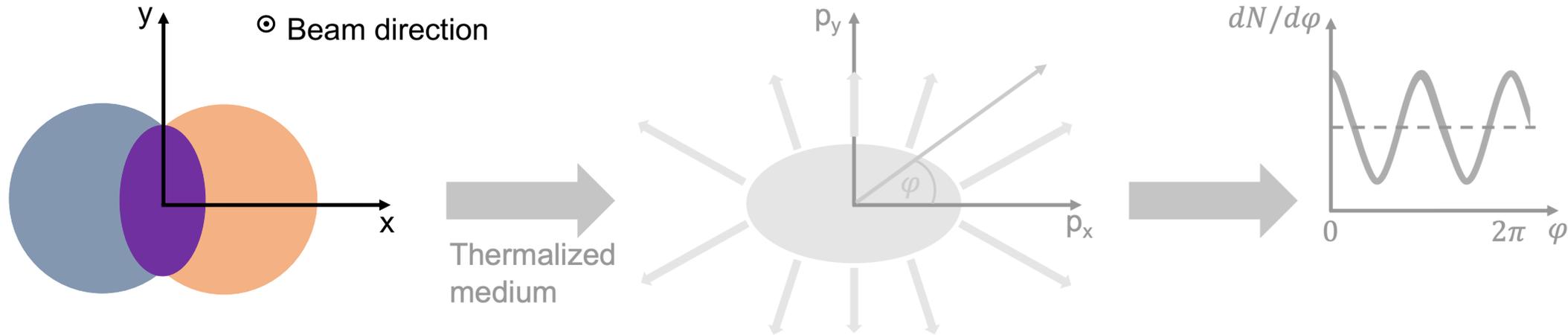


Anisotropic Flow

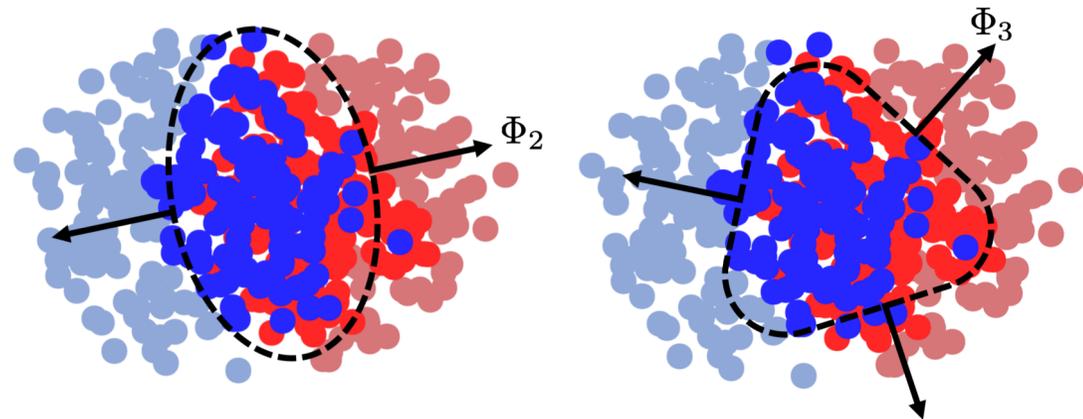


Anisotropic Flow: Transition from anisotropy in coordinate space to anisotropy in momentum space via thermalized medium

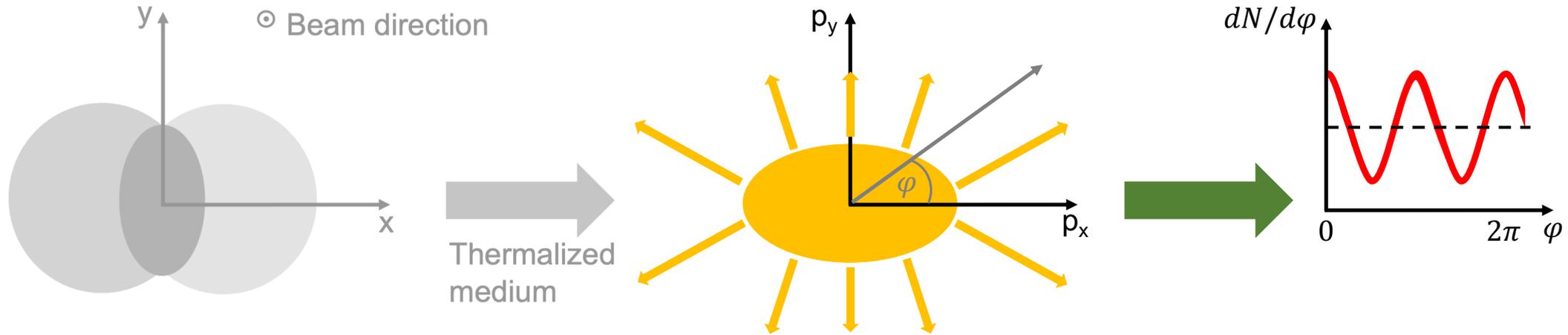
From initial state



- **Initial state** (coordinate space) characterised by $C_n = c_n e^{in\Phi_n}$

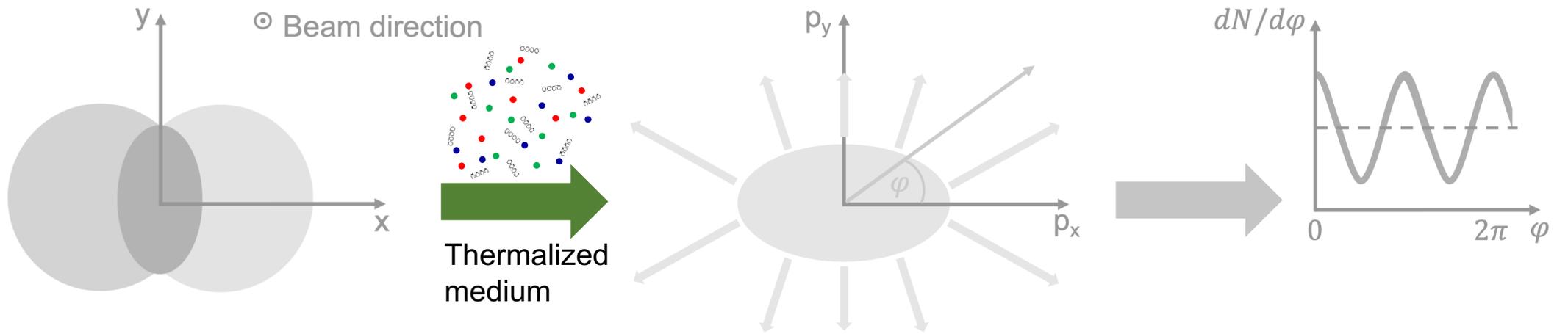


From initial state to final state



- **Initial state** (coordinate space) characterised by $C_n = c_n e^{in\Phi_n}$
- **Final state** (momentum space) characterised by $V_n = v_n e^{in\Psi_n}$

From initial state to final state – The QGP response

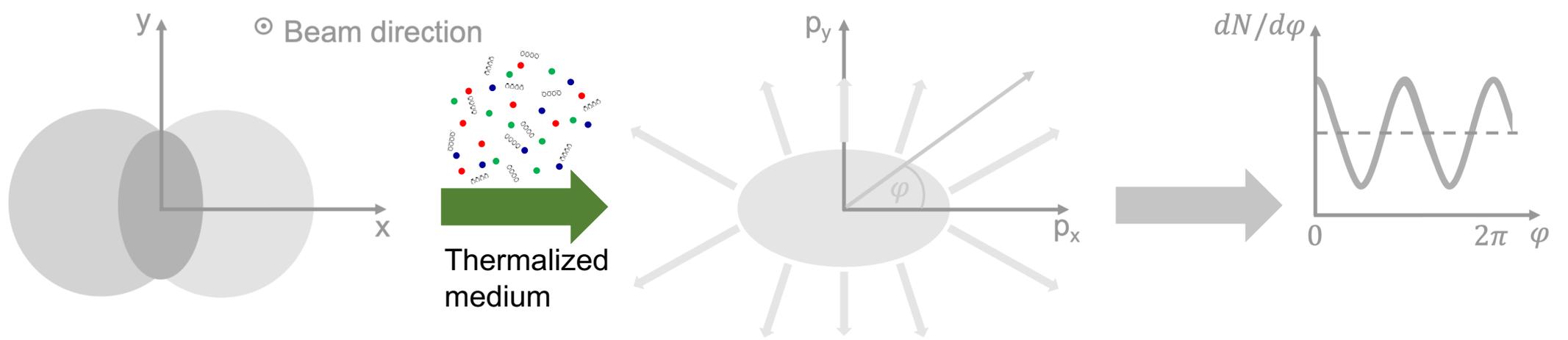


- **Initial state** (coordinate space) characterised by $C_n = c_n e^{in\Phi_n}$
- **Final state** (momentum space) characterised by $V_n = v_n e^{in\Psi_n}$
- **Linear and non-linear response, e.g.:**

$$v_4 e^{i4\Psi_4} = \overbrace{\omega_4 c_4 e^{i4\phi_4}} + \overbrace{\omega_{422} c_2^2 e^{i4\phi_2}} + \dots$$

Li Yan, Chinese Physics C, 42(4), 042001, 2018.

From initial state to final state – The QGP response



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$$v_4 e^{i4\Psi_4} = \underbrace{\omega_4 c_4}_{\text{blue}} e^{i4\phi_4} + \underbrace{\omega_{422} c_2^2}_{\text{red}} e^{i4\phi_2} + \dots$$

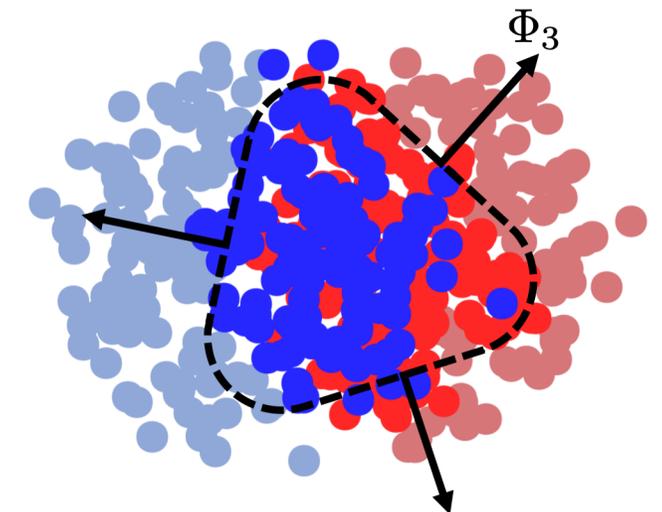
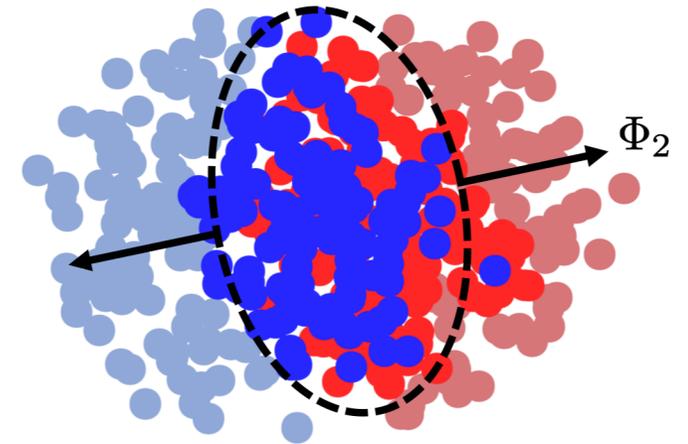
Li Yan, Chinese Physics C, 42(4), 042001, 2018.

Symmetry Plane Correlations (SPC)

- **Final state:** Measurement of single symmetry planes not possible
 → Use Symmetry Plane Correlations, e.g. $\langle \cos[4(\Psi_4 - \Psi_2)] \rangle$
- Comparison of SPC in the initial and final state is sensitive to **linear** and **non-linear** response, e.g.

$\omega_{422} = 0$	$\langle \cos[4(\Psi_4 - \Psi_2)] \rangle = \langle \cos[4(\Phi_4 - \Phi_2)] \rangle$
$\omega_{422} \neq 0$	$\langle \cos[4(\Psi_4 - \Psi_2)] \rangle \neq \langle \cos[4(\Phi_4 - \Phi_2)] \rangle$

→ Imprint of the hydrodynamic evolution of the system



New experimental technique for SPC

- Previous work: **Scalar Product (SP)-Method**

STAR Collaboration. PRC 66, 034904, 2002

R. S. Bhalerao, J.-Y. Ollitrault, S. Pal. PRC 88, 024909, 2013

- Example:

$$\langle \cos[4(\Psi_4 - \Psi_2)] \rangle_{SP} = \frac{\langle v_2^2 v_4 \cos[4(\Psi_4 - \Psi_2)] \rangle}{\sqrt{\langle v_2^4 \rangle \langle v_4^2 \rangle}}$$

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- Problem:

$$\langle v_2^4 v_4^2 \rangle \neq \langle v_2^4 \rangle \langle v_4^2 \rangle$$

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- **New technique for SPC must be developed!**

- New: **Gaussian Estimator (GE)**

- Modelling of multi-harmonic flow fluctuations with 2D Gaussian

- Example:

$$\langle \cos[4(\Psi_4 - \Psi_2)] \rangle_{\text{GE}} = \sqrt{\frac{\pi}{4}} \frac{\langle v_2^2 v_4 \cos[4(\Psi_4 - \Psi_2)] \rangle}{\sqrt{\langle v_2^4 v_4^2 \rangle}}$$

- Details see:

A. Bilandzic, **ML**, S. F. Taghavi:

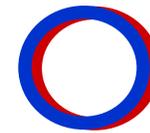
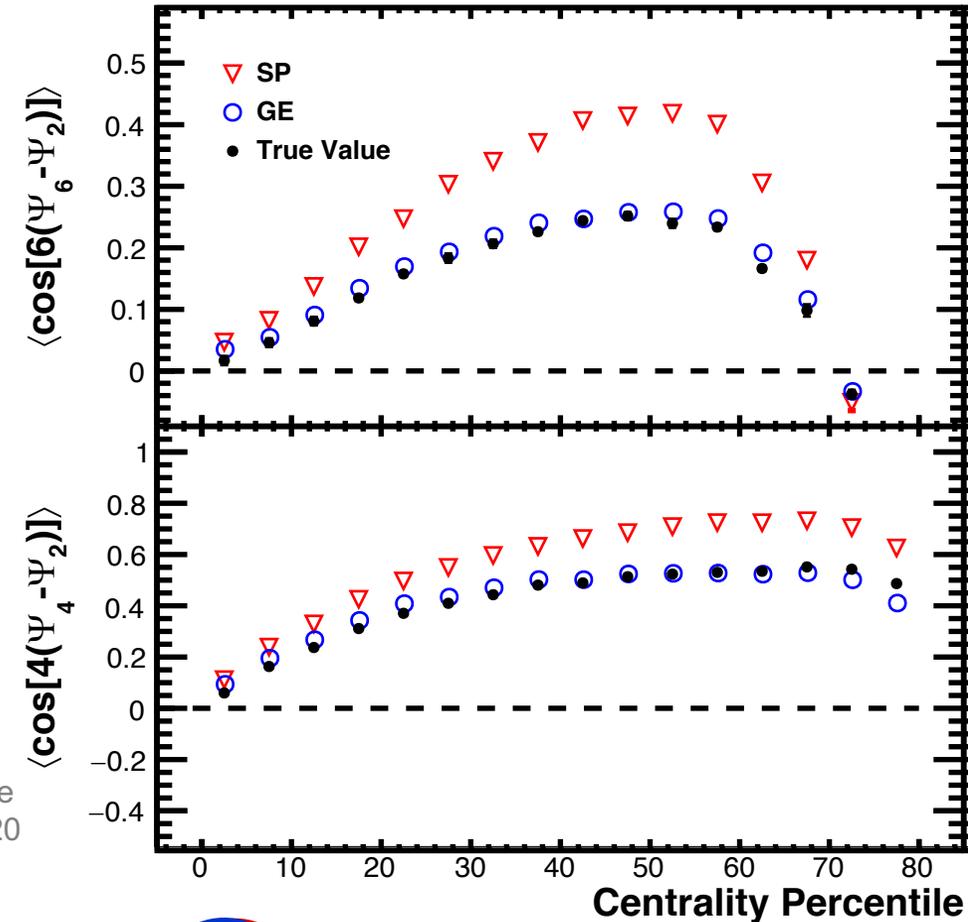
“New estimator for symmetry plane correlations in anisotropic flow analyses”

PRC **102**, 024910 – 2020

Gaussian Estimator for SPC

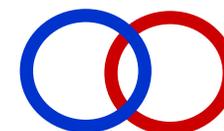
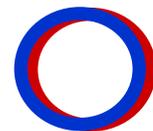
- Comparison of GE to SP and "true" value in iEBE-VISHNU (Pb-Pb $\sqrt{s_{NN}} = 2.76$ TeV)
- Clear improvement over existing SP-method
- GE reproduces the "true" value of SPC extremely well in central to mid-central collisions!

A. Bilandzic, ML, S. F. Taghavi: "New estimator for symmetry plane correlations in anisotropic flow analyses", PRC 102, 024910 – 2020



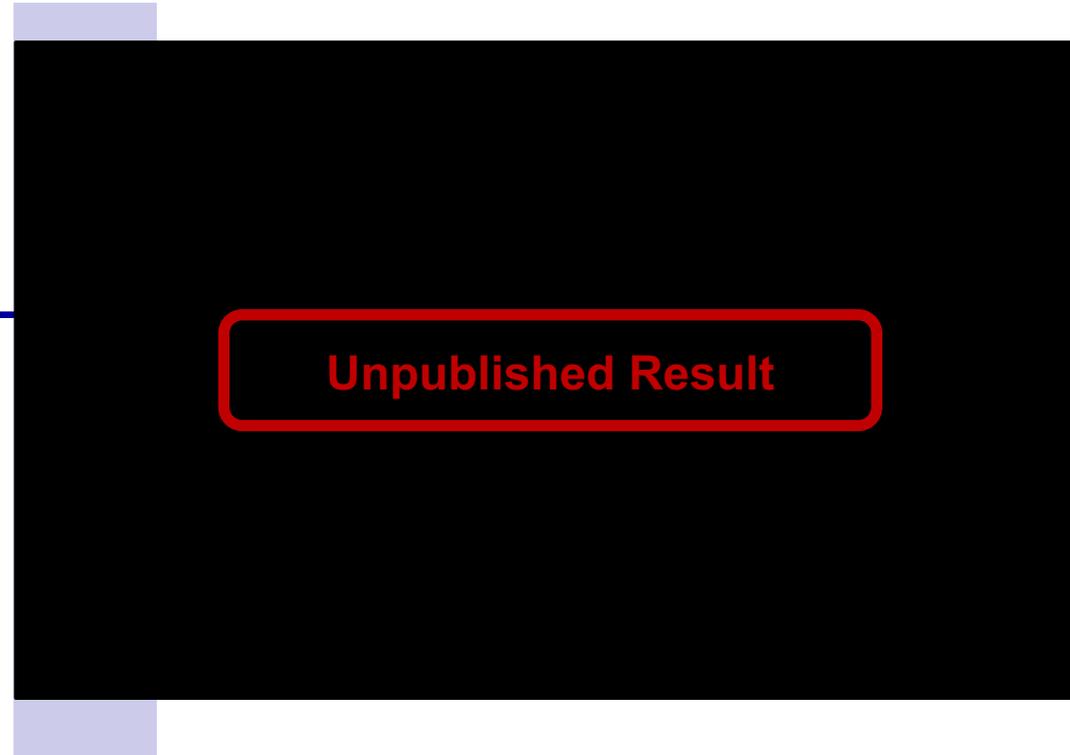
First experimental results with GE

ATLAS results from: ATLAS
Collaboration, Phys. Rev. C 90,
024905, 2014.



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Unpublished Result

**No initial anisotropy
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→ Symmetry planes
only due to random
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**Correlated symmetry
planes**

- Correlation from initial state?
- Impact of non-linear response?

Correlations between ψ_2 and ψ_4

- Comparison of state-of-the-art model

T_RENTo + iEBE-VISHNU

J. E. Bernhard, J. S. Moreland, and S. A. Bass, "Bayesian estimation of the specific shear and bulk viscosity of quark-gluon plasma," Nature Phys. 15 no. 11, (2019) 1113–1117.

$$\omega_{422} = 0 \quad \langle \cos[4(\Psi_4 - \Psi_2)] \rangle = \langle \cos[4(\Phi_4 - \Phi_2)] \rangle$$

$$\omega_{422} \neq 0 \quad \langle \cos[4(\Psi_4 - \Psi_2)] \rangle \neq \langle \cos[4(\Phi_4 - \Phi_2)] \rangle$$

Unpublished Result

Correlations between ψ_2 , ψ_3 and ψ_5

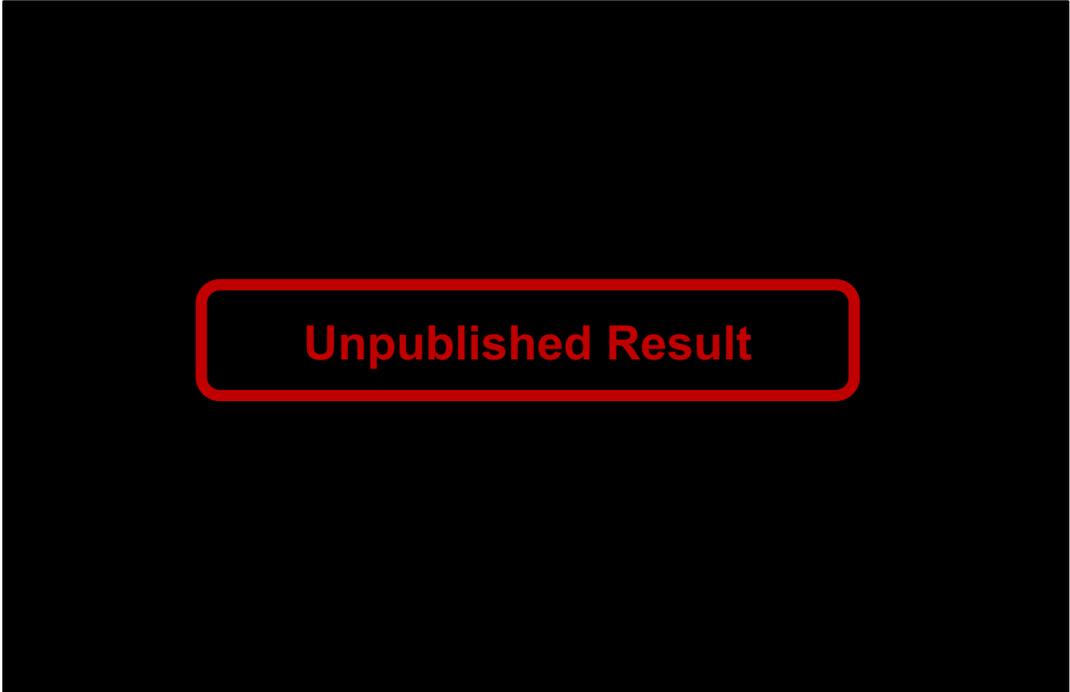
- Probing of linear and non-linear response of ψ_5 to ψ_2 and ψ_3
- Linear response dominates in the model
- Model describes the data extremely well



Unpublished Result

Correlations between four symmetry planes

- First experimental extraction of SPC between 4 planes
- Proof of feasibility for higher order SPC
- Large difference between data and models for higher order flow
 - Data presents great opportunity for model tuning



Unpublished Result

Summary

- GE estimates SPC more accurately than other existing methods
- First experimental results from ALICE using the GE (in total 9 different combinations)
→ Currently under preparation for paper proposal

Further Work:

- First cumulant to probe the correlations between SPC, see

A. Bilandzic, **ML**, C. Mordasini, S. F. Taghavi:
“Multivariate cumulants in flow analyses: The Next Generation”, arXiv 2101.05619



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Unpublished Result

THANK YOU!

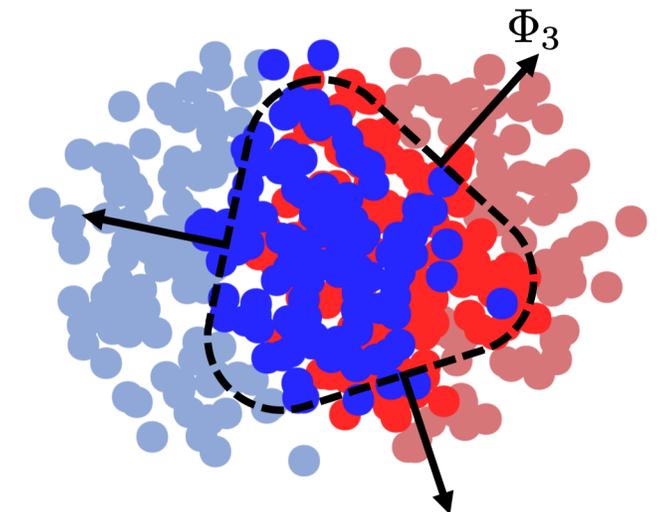
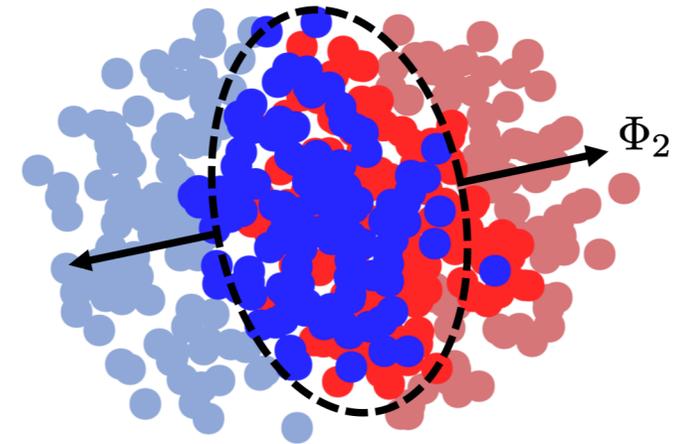
Backup

Symmetry Plane Correlations (SPC)

- **Initial state:** Higher order participant planes from fluctuations
- **Final state:** Measurement of single symmetry planes not possible
 → Use Symmetry Plane Correlations, e.g. $\langle \cos[4(\Psi_4 - \Psi_2)] \rangle$
- Comparison of SPC in the initial and final state is sensitive to linear and non-linear response, e.g.

$$v_2^2 v_4 e^{i4(\Psi_4 - \Psi_2)} = \boxed{\omega_2^2 \omega_4 c_2^2 c_4 e^{i4(\phi_4 - \phi_2)}} + \boxed{\omega_{422} \omega_2^2 c_2^2} + \dots$$

→ Imprint of the hydrodynamic evolution of the system



Scalar Product Method

- Previous work: **Scalar Product (SP)-Method**

$$\langle \cos(c_1 \Psi_1 + 2c_2 \Psi_2 + \dots + lc_l \Psi_l) \rangle$$

$$= \frac{\langle v_1^{c_1} v_2^{c_2} \dots v_l^{c_l} \cos(c_1 \Psi_1 + 2c_2 \Psi_2 + \dots + lc_l \Psi_l) \rangle}{\sqrt{\langle v_1^{2c_1} \rangle \langle v_2^{2c_2} \rangle \dots \langle v_l^{2c_l} \rangle}}$$

STAR Collaboration.
PRC 66, 034904, 2002

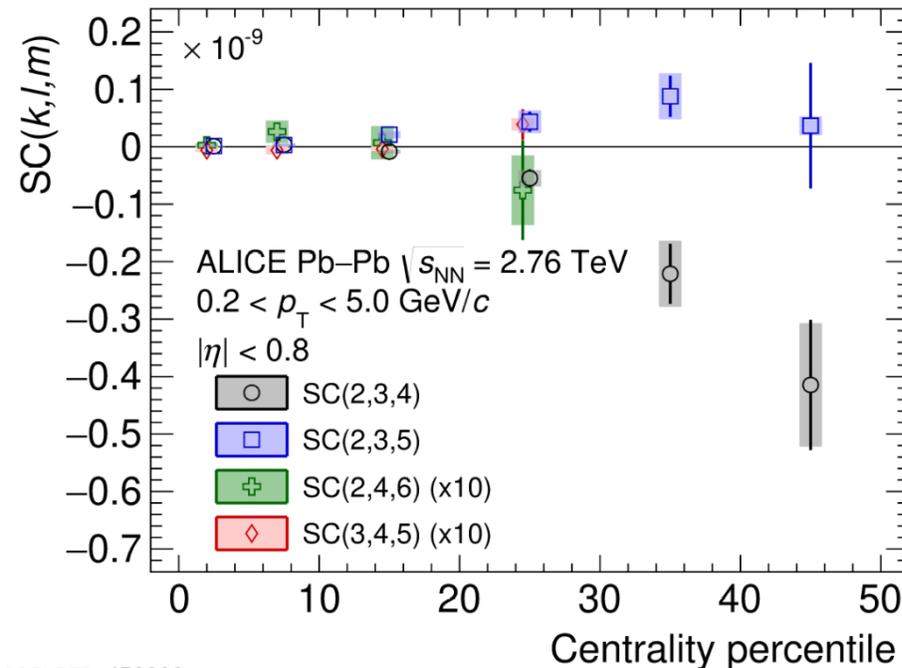
R. S. Bhalerao, J.-Y. Ollitrault, S. Pal.
PRC 88, 024909, 2013

- Problem:

$$\langle v_n^2 v_m^2 \rangle \neq \langle v_n^2 \rangle \langle v_m^2 \rangle$$

$$\langle v_k^2 v_l^2 v_m^2 \rangle \neq \langle v_k^2 \rangle \langle v_l^2 \rangle \langle v_m^2 \rangle$$

**New technique for SPC
must be developed!**



ALICE Collaboration, Phys. Rev. Lett. 127 092302 (2021)

Everything is Gaussian if you are brave enough

- **Starting point:** Modelling of multi-harmonic flow fluctuations

$\mathcal{R}_x = v_{n_1}^{a_1} \cdots v_{n_k}^{a_k} \cos(a_1 n_1 \Psi_{n_1} + \cdots + a_k n_k \Psi_{n_k})$ and $\mathcal{R}_y = v_{n_1}^{a_1} \cdots v_{n_k}^{a_k} \sin(a_1 n_1 \Psi_{n_1} + \cdots + a_k n_k \Psi_{n_k})$
with a 2D Gaussian

- Use this 2D Gaussian to calculate $\langle \cos(a_1 n_1 \Psi_{n_1} + \cdots + a_k n_k \Psi_{n_k}) \rangle$

→ **Gaussian Estimator (GE):**

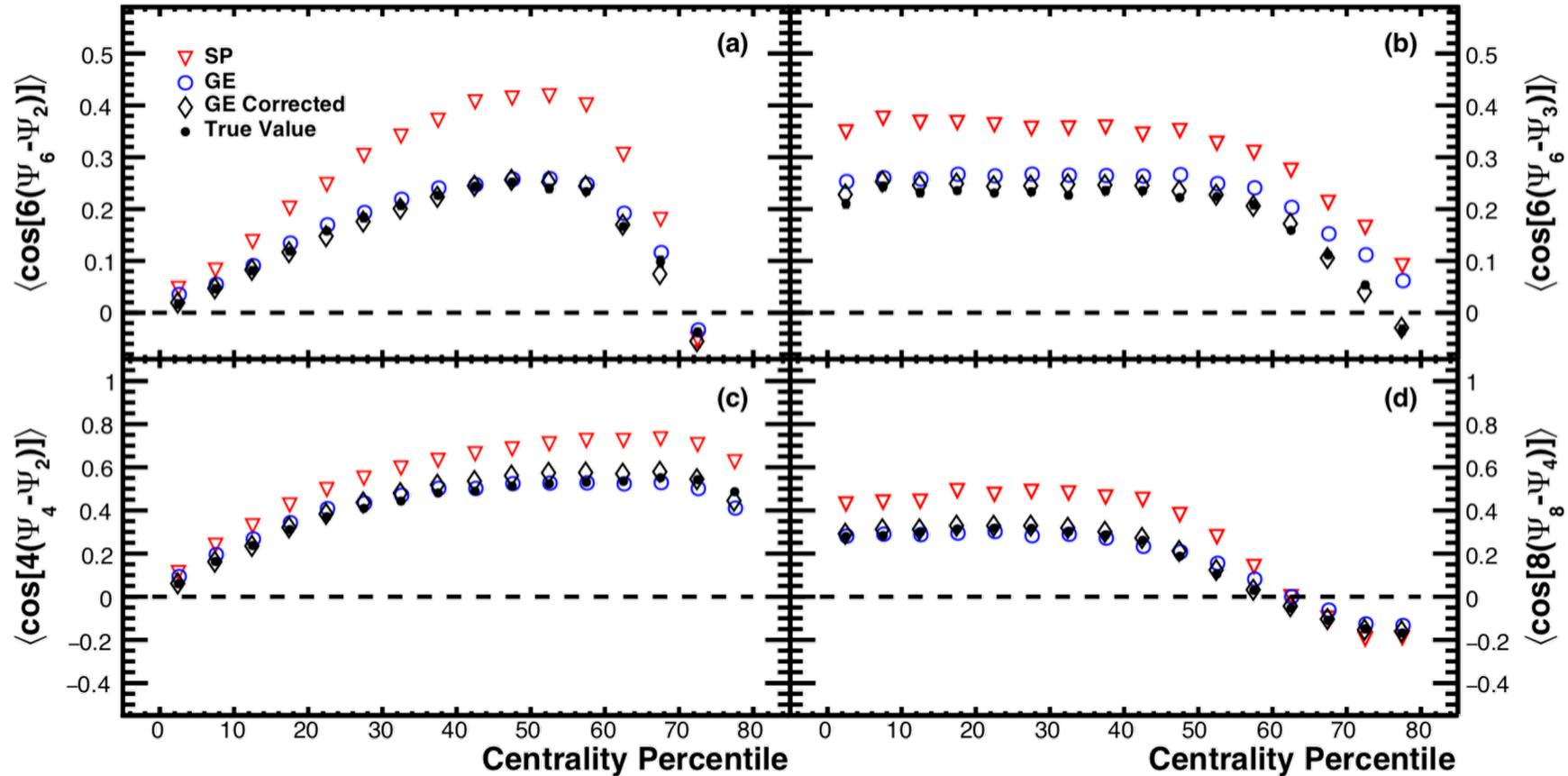
$$\langle \cos(a_1 n_1 \Psi_{n_1} + \cdots + a_k n_k \Psi_{n_k}) \rangle_{\text{GE}} = \sqrt{\frac{\pi}{4}} \frac{\langle v_{n_1}^{a_1} \cdots v_{n_k}^{a_k} \cos(a_1 n_1 \Psi_{n_1} + \cdots + a_k n_k \Psi_{n_k}) \rangle}{\sqrt{\langle v_{n_1}^{2a_1} \cdots v_{n_k}^{2a_k} \rangle}}$$

- Details see:

A. Bilandzic, **ML**, S. F. Taghavi: “*New estimator for symmetry plane correlations in anisotropic flow analyses*”, PRC **102**, 024910 – 2020

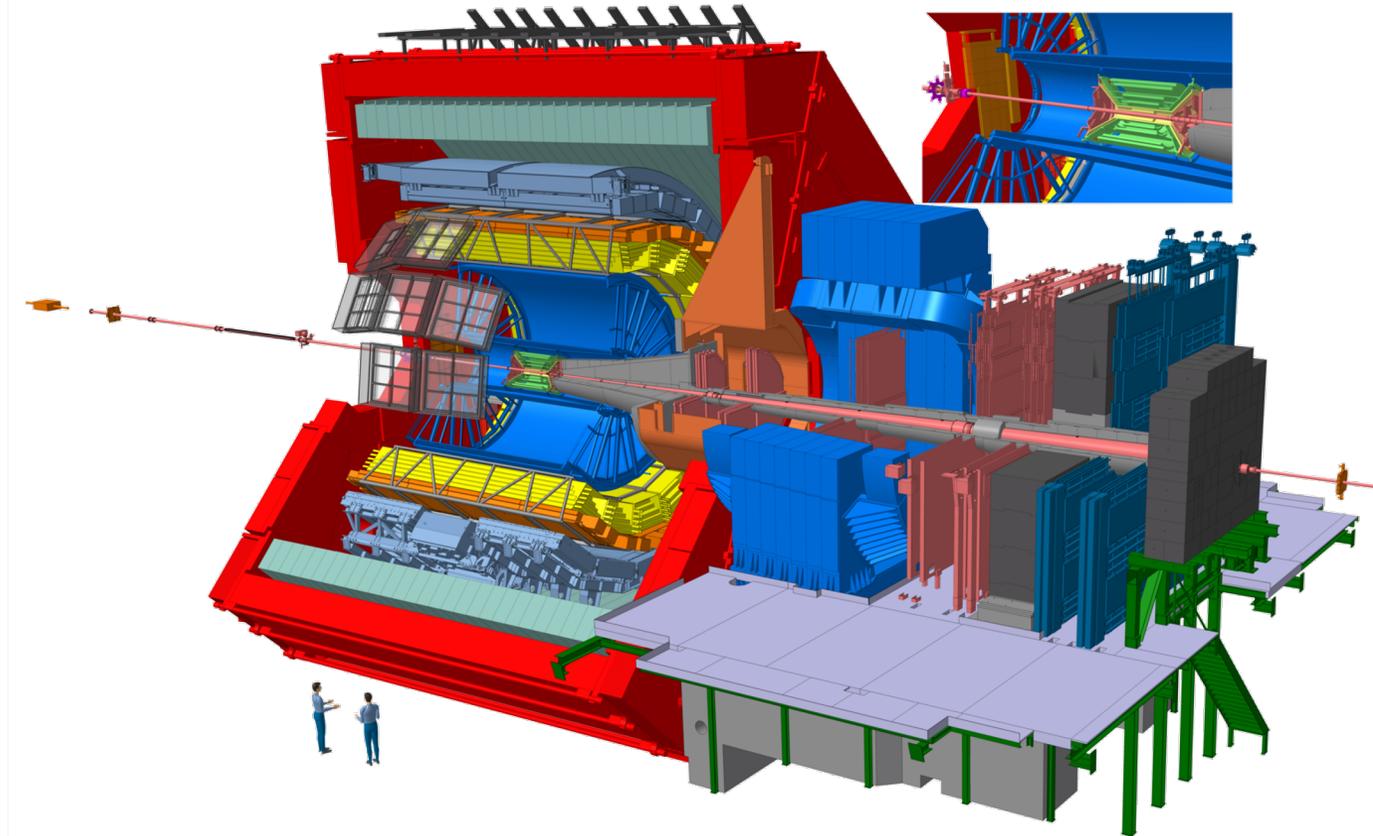
Gaussian Estimator for SPC

A. Bilandzic, ML, S. F. Taghavi: "New estimator for symmetry plane correlations in anisotropic flow analyses", PRC 102, 024910 – 2020



ALICE - A Large Ion Collider Experiment

- Dedicated heavy ion experiment at the LHC
- **Inner Tracking System**
 - Used for PV determination
 - SPD clusters for centrality determination
- **Time Projection Chamber**
 - Used as the main detector for track reconstruction (φ, p_T, \dots)



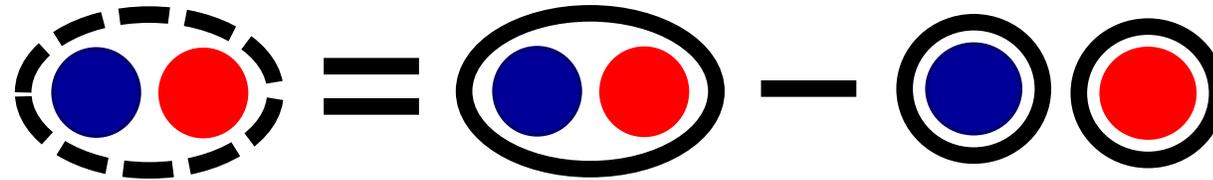
A. Tauro, "ALICE Schematics" (2017), [CERN CDS](#)

Is this all we can do with Symmetry Planes?

Answer: No, there is more

Cumulants

- Cumulants probe the **genuine** correlation between variables
- Example: Lowest order, two-variate cumulant



$$\kappa_{1,1} = \langle X_1 X_2 \rangle - \langle X_1 \rangle \langle X_2 \rangle$$

- Cumulants in flow analyses, e.g. symmetric cumulants:

$$SC(m, n) = \langle \underbrace{v_n^2}_{\text{blue}} \underbrace{v_m^2}_{\text{red}} \rangle - \langle \underbrace{v_n^2}_{\text{blue}} \rangle \langle \underbrace{v_m^2}_{\text{red}} \rangle$$

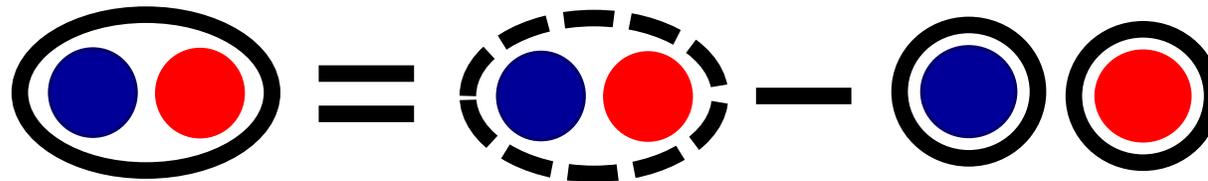
Cumulant of Symmetry Plane Correlation (CSC)

- Approach: Use SPC as the statistical observables in the cumulant expansion

$$X_1 = e^{ib(\Psi_c - \Psi_d)}$$

$$X_2 = e^{ik(\Psi_l - \Psi_m)}$$

- Example:



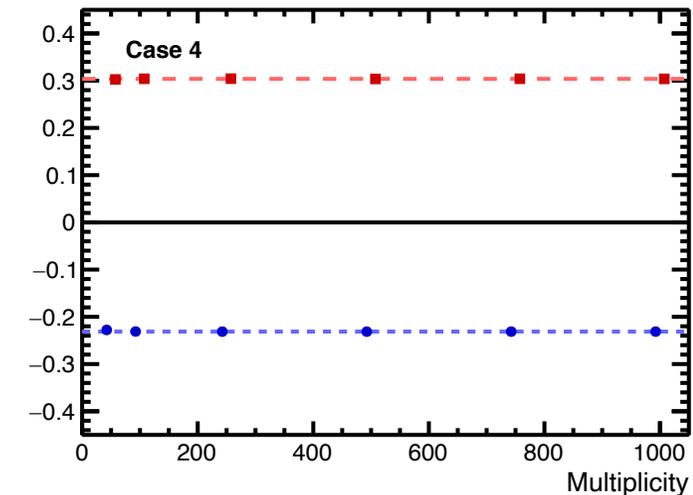
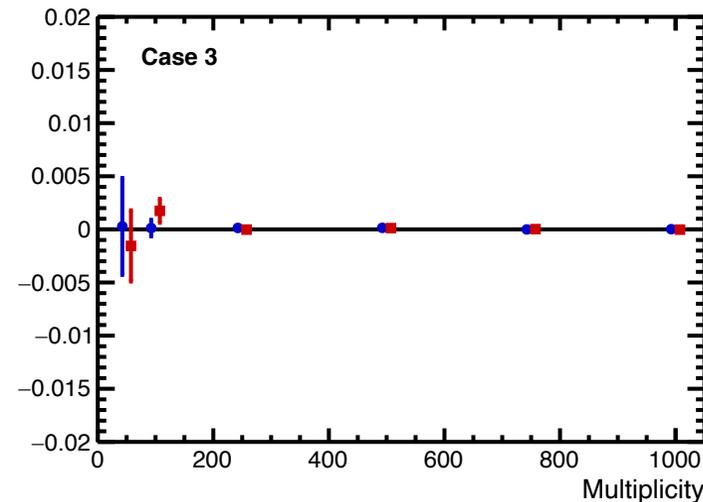
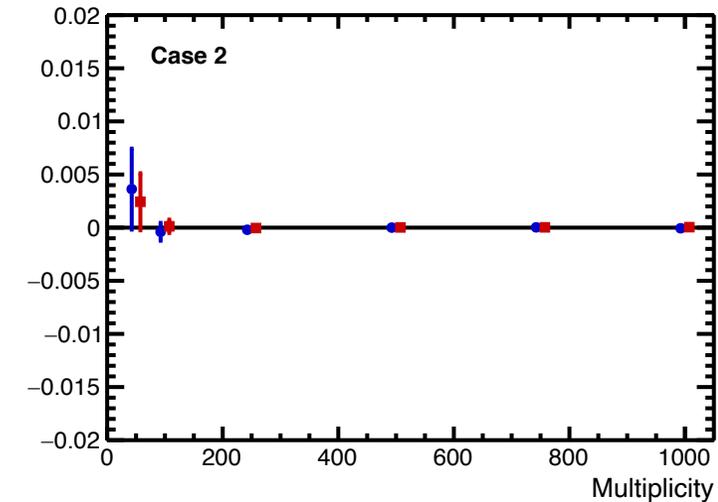
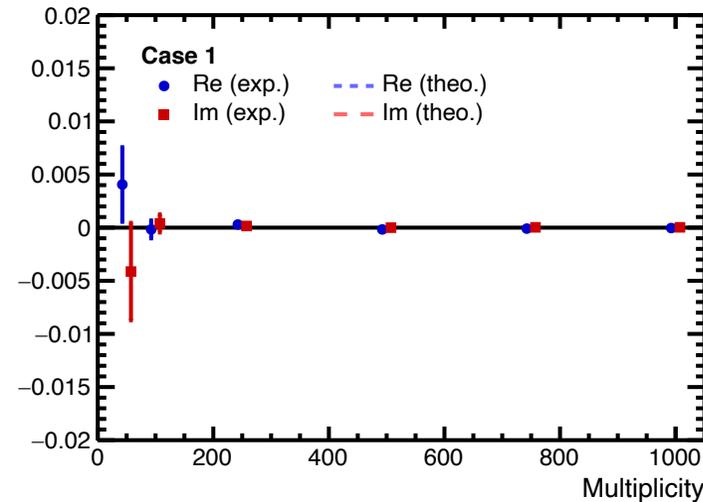
$$\text{CSC}(4\delta_{4,2}, 6\delta_{6,3}) = \left\langle e^{i(4(\Psi_4 - \Psi_2) + 6(\Psi_6 - \Psi_3))} \right\rangle - \left\langle e^{i4(\Psi_4 - \Psi_2)} \right\rangle \left\langle e^{i6(\Psi_6 - \Psi_3)} \right\rangle$$

- Interpretation:

- SPC as static pictures
- CSC as dynamic picture for the evolution of SPC relative to each other
- Details see: A. Bilandzic, **ML**, C. Mordasini, S. F. Taghavi: “*Multivariate cumulants in flow analyses: The Next Generation*”, arXiv 2101.05619

Toy Monte Carlo Studies

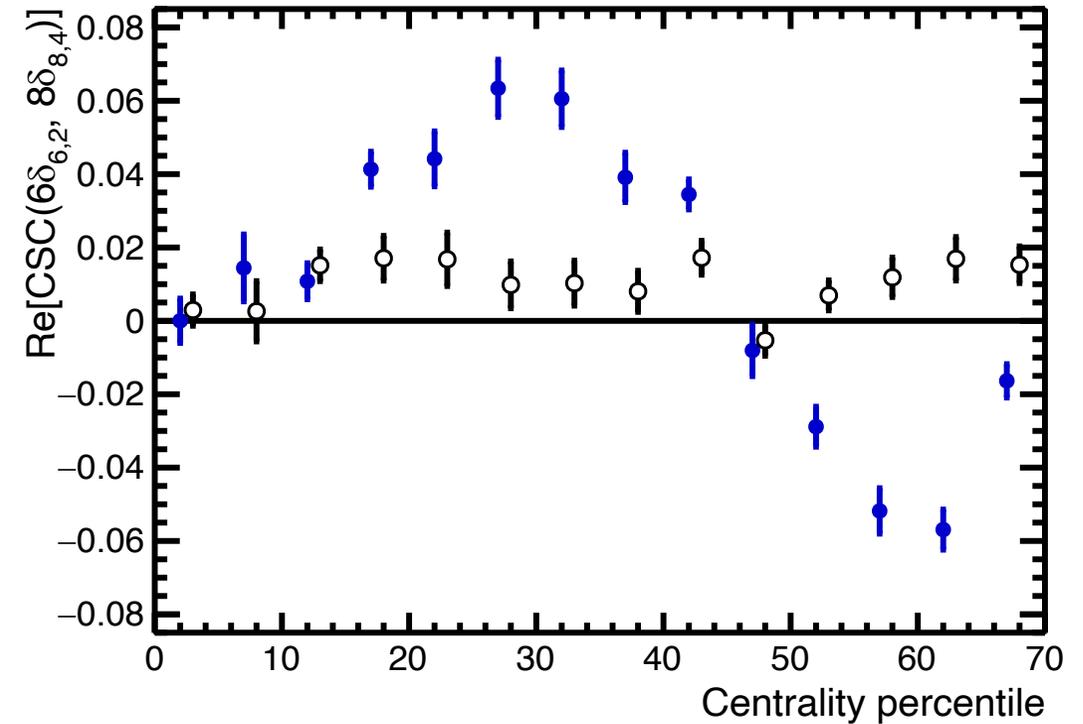
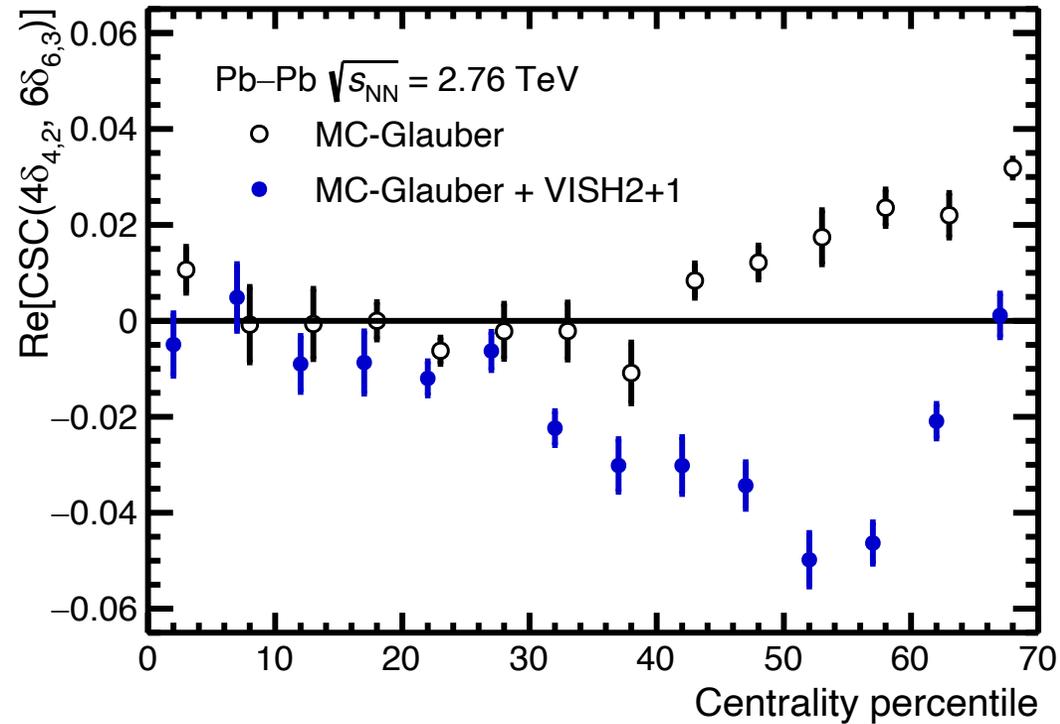
- Study of CSC in a controlled environment with known input
- Cases 1-3: uncorrelated SPC \rightarrow CSC yields zero
- Case 4: genuine correlation between the two SPC \rightarrow non-zero value



A. Bilandzic, ML, C. Mordasini, S. F. Taghavi: "Multivariate cumulants in flow analyses: The Next Generation", arXiv 2101.05619

First model predictions for CSC

A. Bilandzic, ML, C. Mordasini, S. F. Taghavi: "New estimator for symmetry plane correlations in anisotropic flow analyses", arXiv 2101.05619



- Non-trivial signal in the initial and final state
- Indication that symmetry plane correlations are (anti-) correlated to each other