Cosmological Sector of the Barrett-Crane GFT Model

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arXiv: 2112.00091

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November 15, 2021

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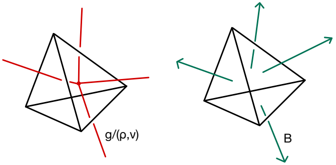

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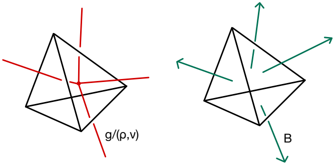

Figure: Geometric interpretation of GFT quanta

$$A = \sqrt{\rho^2 + 1 - \nu^2} = \sqrt{B \cdot B}$$

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- Other GFT models viable ⇒ 'universal' behavior?

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Domain of condensate wavefunction is diffeomorphic to minisuperspace of homogeneous 3-geometries

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Conjecture: Mircoscopic details, such as simplicity constraints, do not affect the coarse grained relational evolution

[Dittrich 2021]

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References

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