

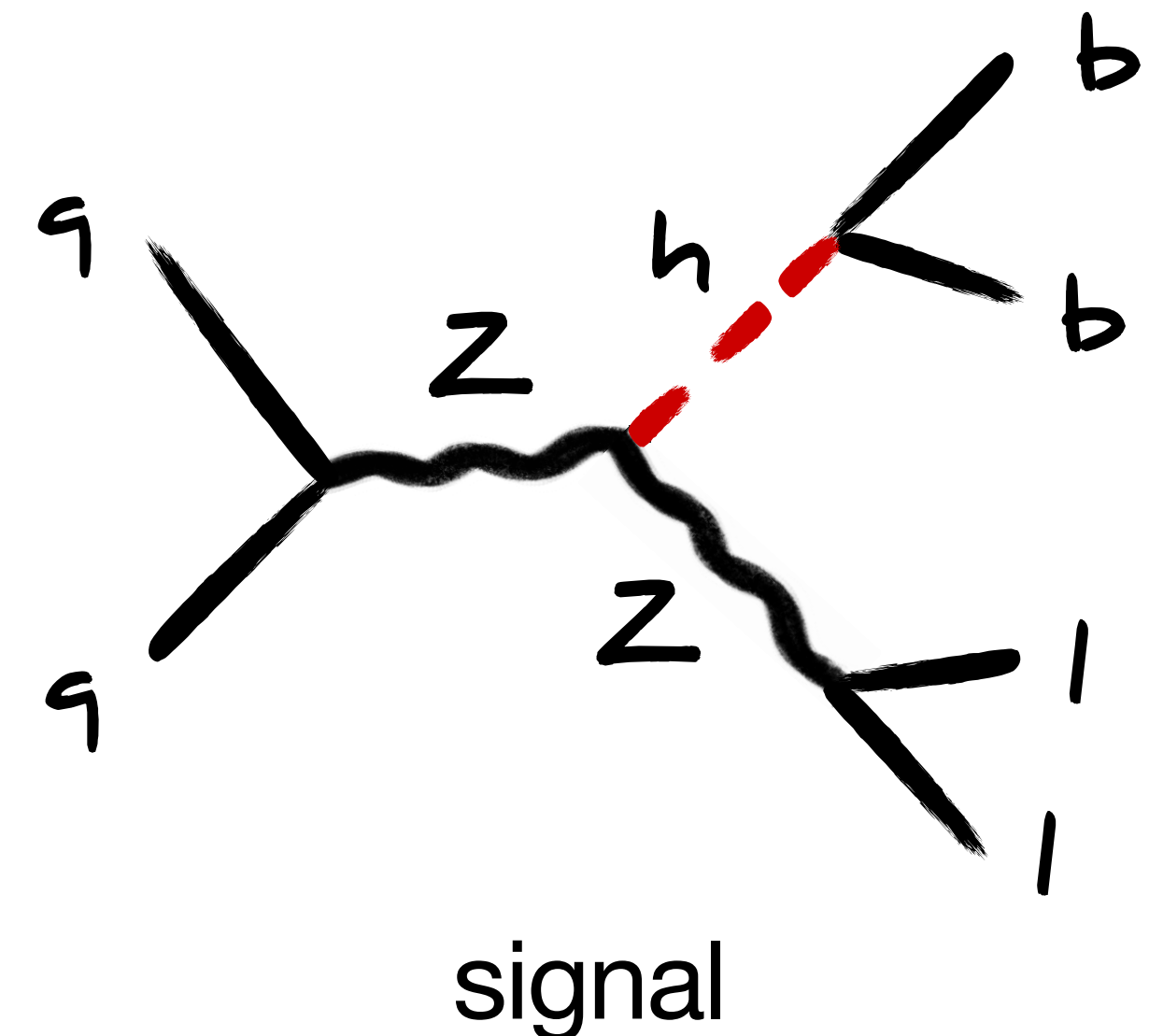
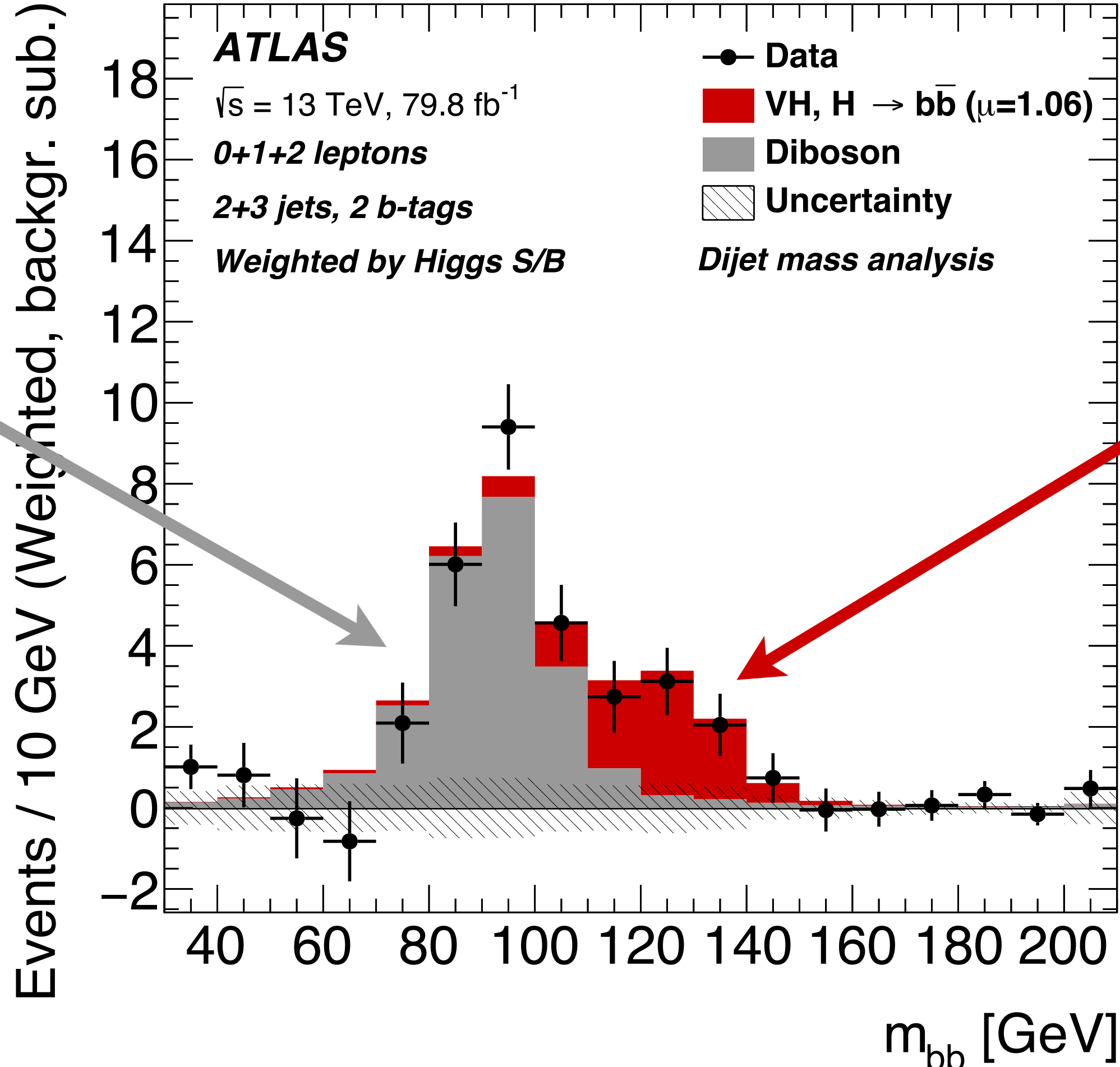
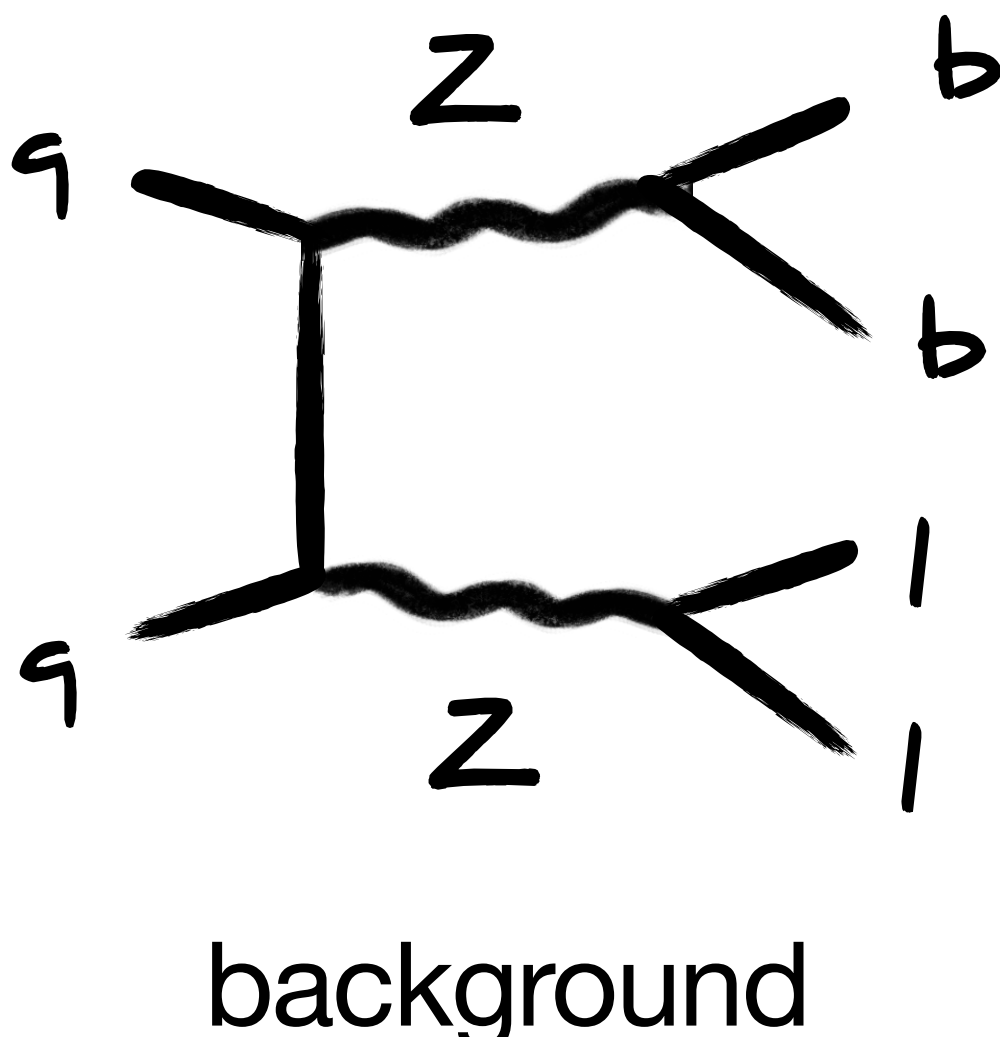
Uli Haisch, MPI Munich
Workshop on Tools for High Precision LHC Simulations, 2.11.22

**NNLO+PS predictions for $Zh \rightarrow l^+l^-b\bar{b}$
production in SMEFT**



Observation of $h \rightarrow b\bar{b}$ @ LHC Run II

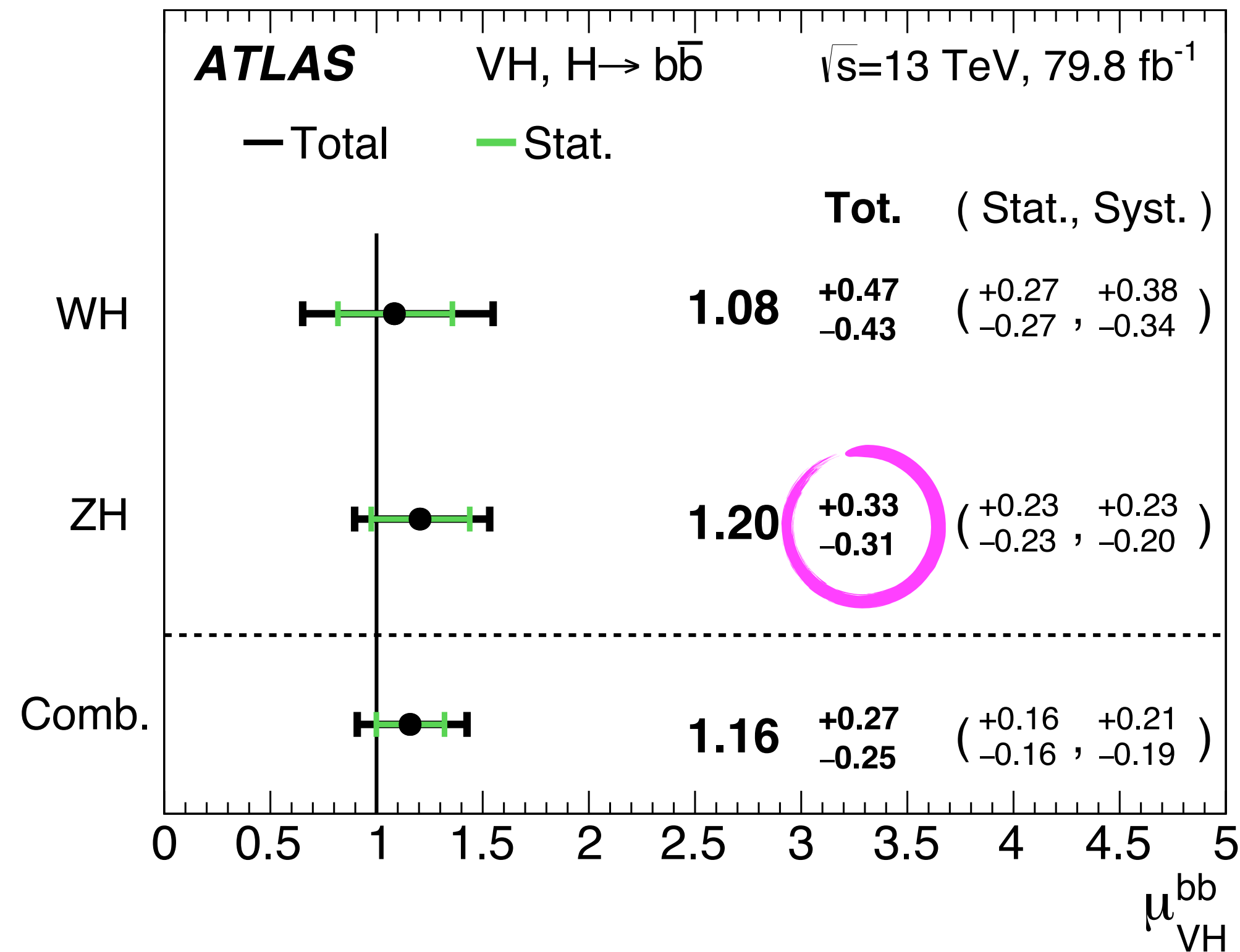
[ATLAS, 1808.08238]



[see also CMS, 1808.08242]

From 5σ to precision measurements

[ATLAS, 1808.08238]

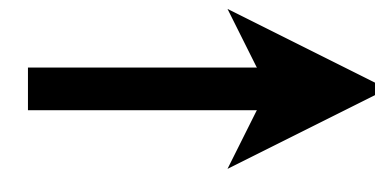
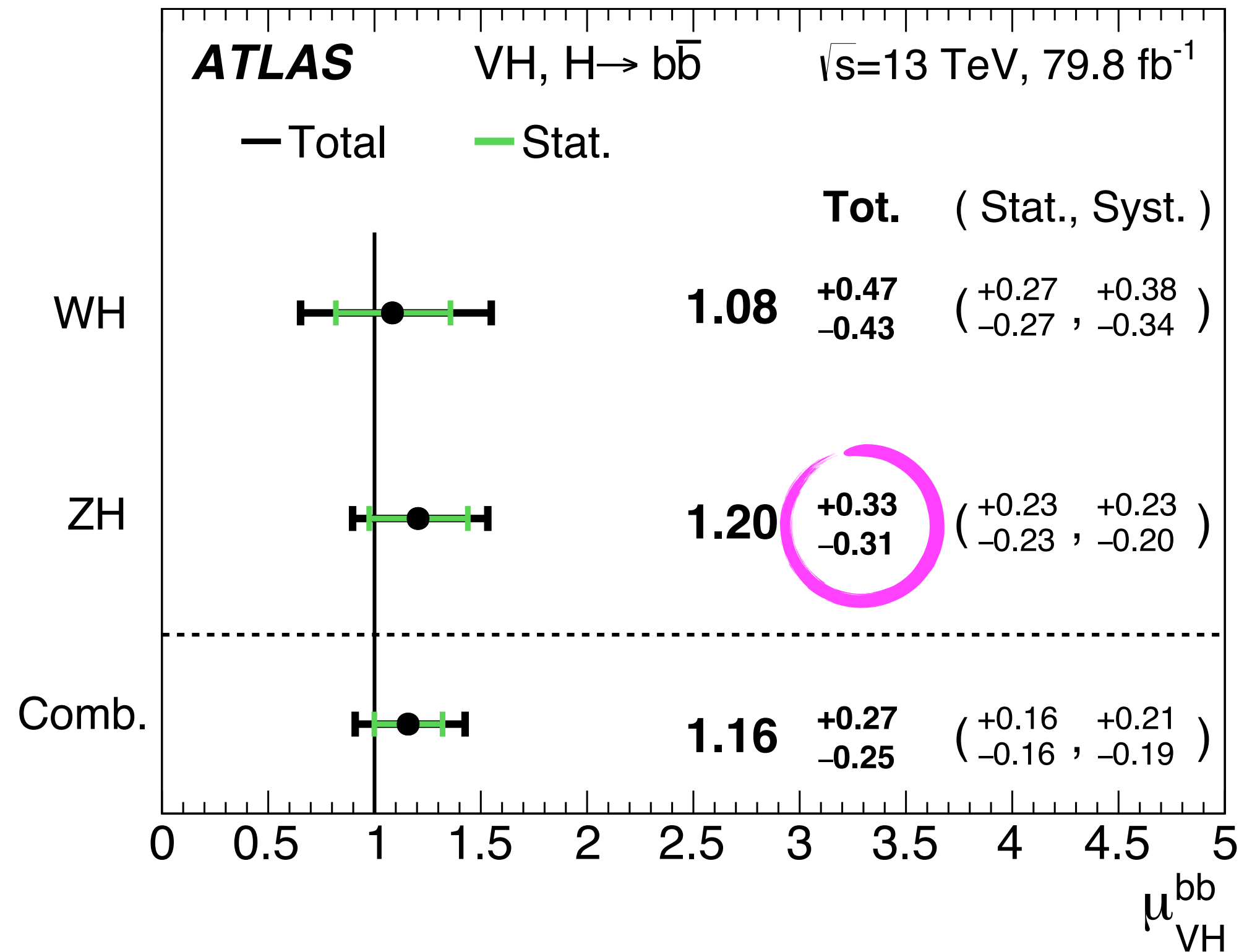


In LHC Run II, signal strength in Vh production found to be SM-like within 25%

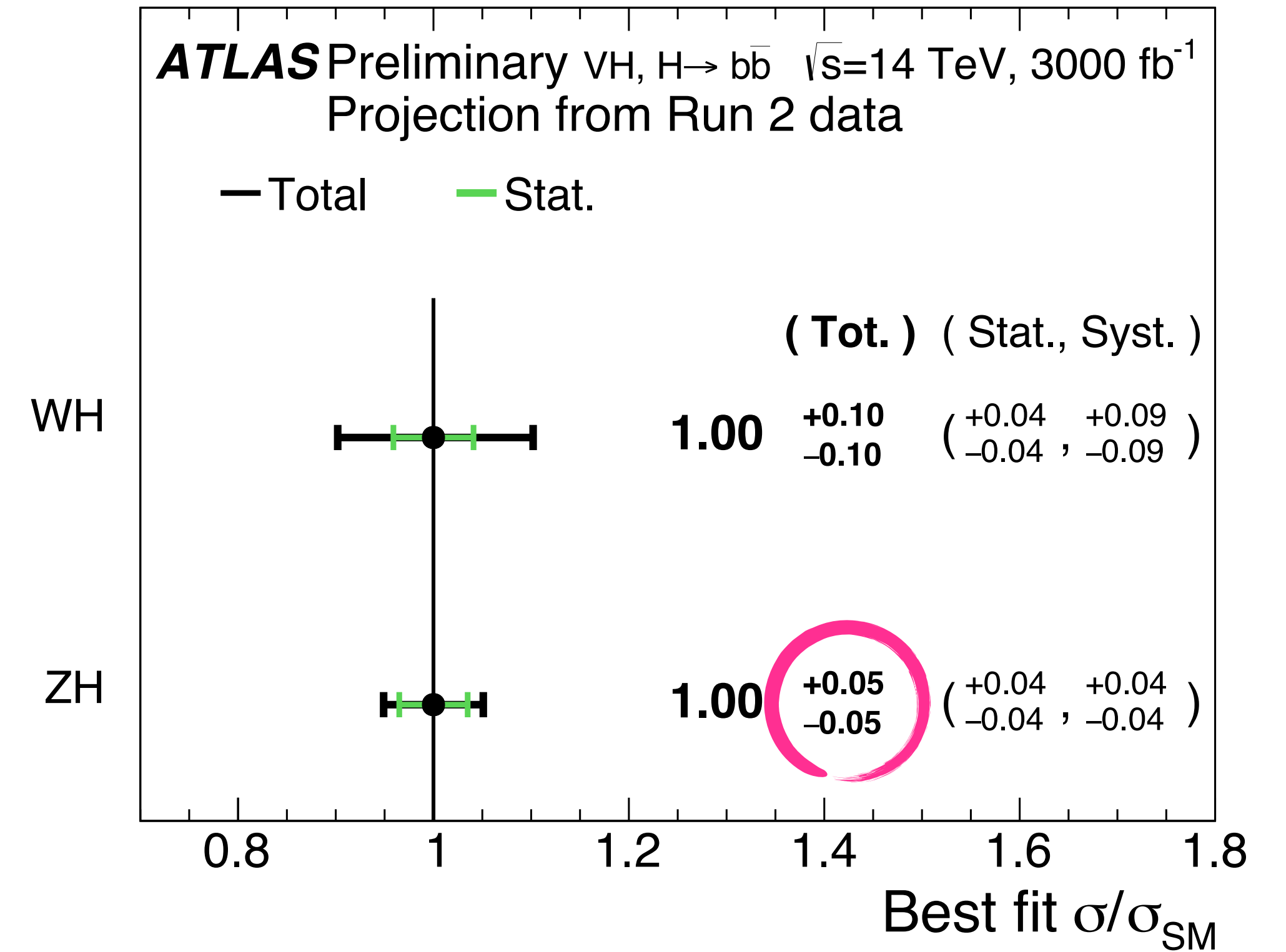
[see also CMS, 1808.08242]

From 5σ to precision measurements

[ATLAS, 1808.08238]



[ATL-PHYS-PUB-2018-054]



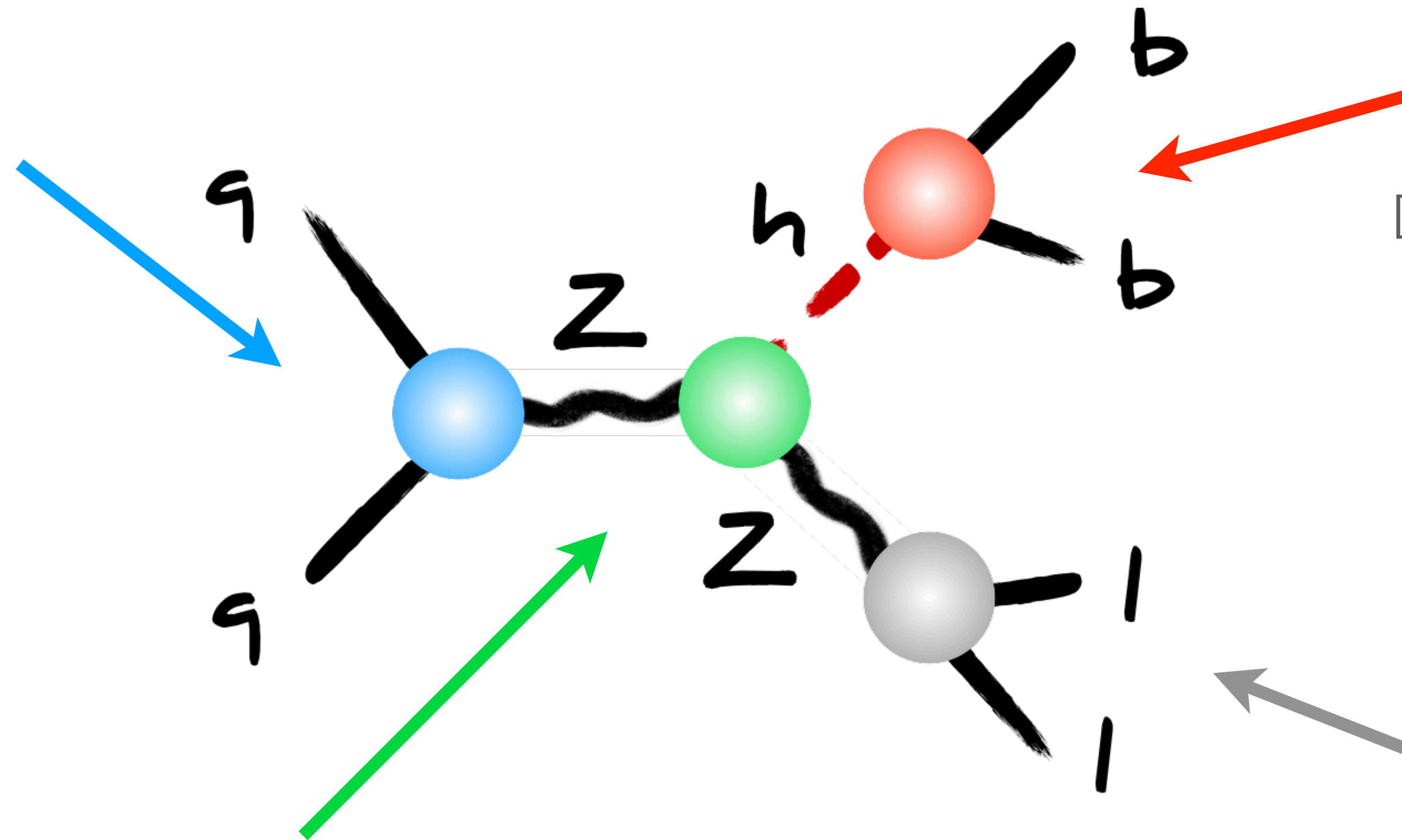
Ultimate accuracy projected to be 10% to 5% in Wh & Zh channel @ HL-LHC

[see also CMS, 1808.08242; CMS-PAS-FTR-18-011]

Anatomy of SMEFT effects

corrections to $q\bar{q}Z$
& $q\bar{q}Zh$ vertices

[Greljo et al., 1710.04143;
Alioli et al., 1804.07407;
Bishara et al., 2208.11134]



corrections to
Higgs decay

[Gauld et al., 1607.0635;
Cullen et al., 1904.06358; 2007.15238]

corrections to hZZ vertex

[Maltoni et al., 1311.1829, Mimasu et al., 1512.02572;
Degrande et al., 1609.04833; Greljo et al., 1710.04143;
Alioli et al., 1804.07407; Bizon et al., 2106.06328]

if EWPO imposed,
effects in Z decay
negligible

Goal of 2204.00663, ...

Within SM, NNLO+PS accuracy has been recently achieved for Zh production with $Z \rightarrow l^+l^-$ & $h \rightarrow b\bar{b}$

Match this accuracy in SMEFT, so that numerical impact of missing higher-order QCD effects related to dimension-six operators are below 1% once experimental constraints on Wilson coefficients are taken into account

Many SMEFT operators, so first consider subset of operators that directly contribute in QCD; do operators contributing to hZZ , $q\bar{q}Z$ & $q\bar{q}Zh$ vertices later

Operators considered in our work

$$Q_{H\Box} = (H^\dagger H) \Box (H^\dagger H)$$

$$Q_{HD} = (H^\dagger D_\mu H)^* (H^\dagger D^\mu H)$$

$$Q_{bH} = y_b (H^\dagger H) \bar{q}_L b_R H$$

$$Q_{bG} = \frac{g_s^3}{(4\pi)^2} y_b \bar{q}_L \sigma_{\mu\nu} T^a b_R H G^{a,\mu\nu}$$

$$Q_{HG} = \frac{g_s^2}{(4\pi)^2} (H^\dagger H) G_{\mu\nu}^a G^{a,\mu\nu}$$

$$Q_{3G} = \frac{g_s^3}{(4\pi)^2} f^{abc} G_\mu^{a,\nu} G_\nu^{b,\sigma} G_\sigma^{c,\mu}$$

Operators normalised such that Wilson coefficients are expected to be of $O(1)$ in UV-complete weakly-coupled BSM models

Factorisable contributions

Since operators $Q_{H\Box}$, Q_{HD} & Q_{bH} do not contain a gluon, associated SMEFT effects factorise to all orders in strong coupling constant. SMEFT results can be obtained from SM matrix elements by following simple replacement:

$$y_b^2 \rightarrow y_b^2 \left\{ 1 + \frac{2v^2}{\Lambda^2} \left[C_{H\Box} - \frac{C_{HD}}{4} - \text{Re}(C_{bH}) \right] \right\}$$

corrections due to
Higgs wave function



correction due to
Yukawa operator



Factorisable contributions

For example in case of partial $h \rightarrow b\bar{b}$ decay rate factorisable corrections are:

$$\Gamma(h \rightarrow b\bar{b})_{\text{SMEFT}}^{\text{fac}} = \frac{3y_b^2 m_h}{16\pi} \left\{ 1 + \frac{2v^2}{\Lambda^2} \left[C_{H\Box} - \frac{C_{HD}}{4} - \text{Re}(C_{bH}) \right] \right\} \\ \times \left[1 + \frac{\alpha_s}{\pi} 5.67 + \left(\frac{\alpha_s}{\pi} \right)^2 29.15 \right]$$

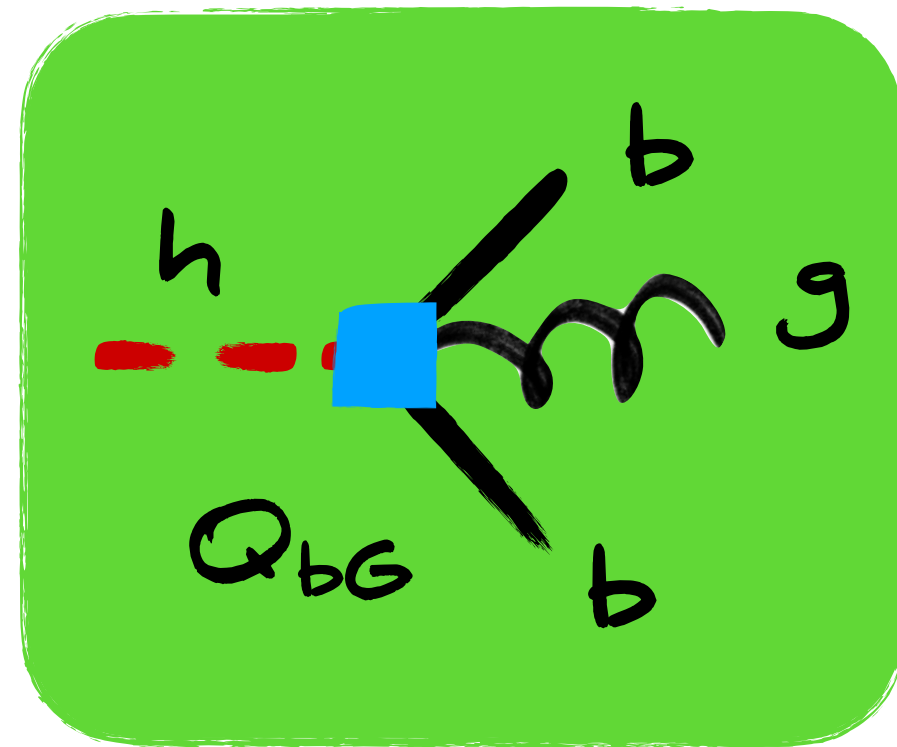


NLO & NNLO QCD
correction in SM

[in principle extension to N⁴LO possible using SM results given in Baikov et al., hep-ph/0511063; Herzog et al., 1707.01044]

Non-factorisable contributions

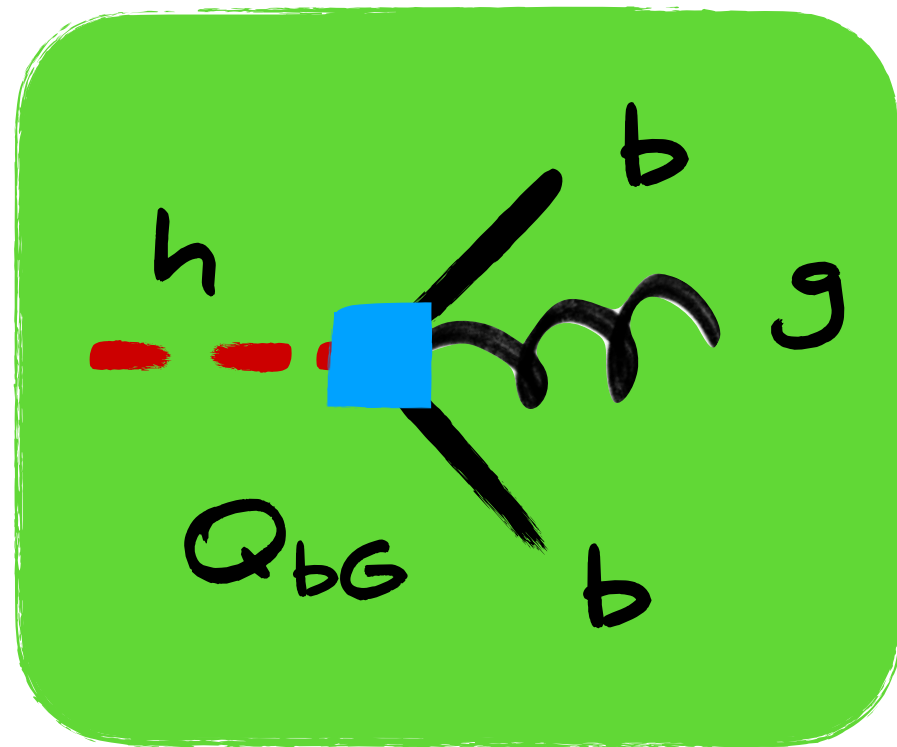
Dominant non-factorisable corrections arise from dipole operator Q_{bG} :



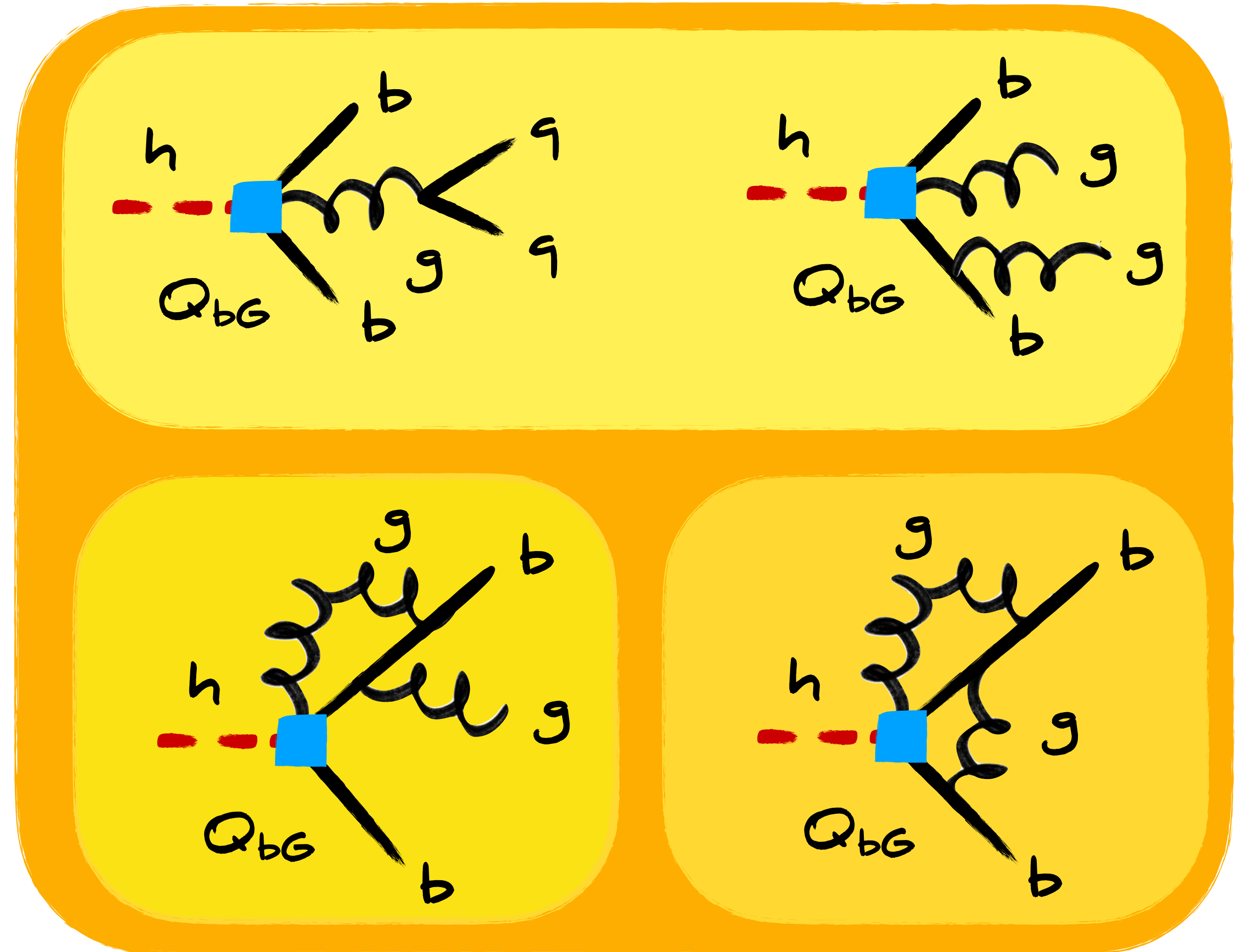
leading contribution from
interference of $h \rightarrow b\bar{b}g$
amplitude in SMEFT & SM

Non-factorisable contributions

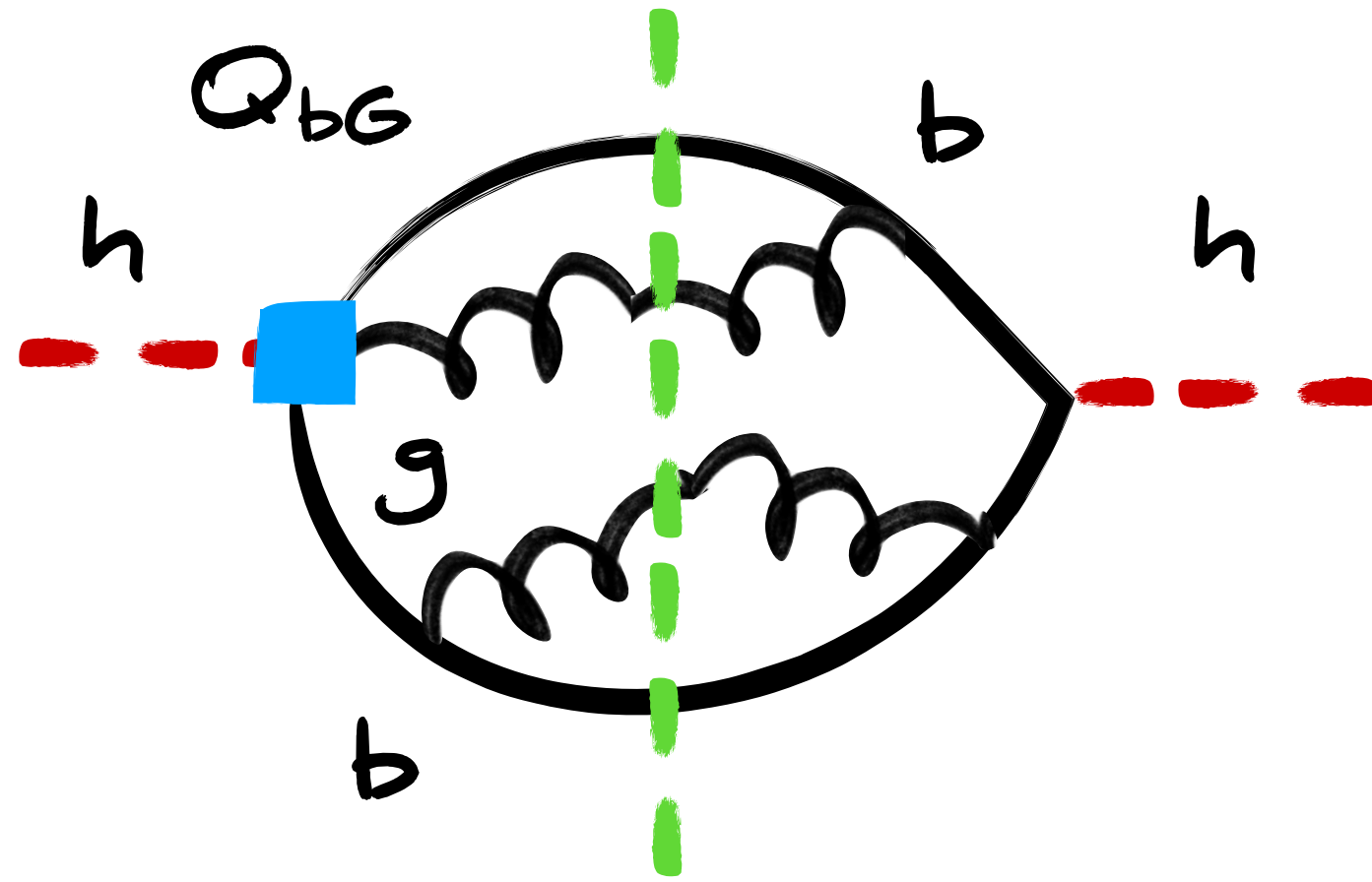
Dominant non-factorisable corrections arise from dipole operator Q_{bG} :



beyond leading order, double real, 1-loop single real & 2-loop virtual contributions



Non-factorisable contributions



$$\begin{aligned}
 f_{bb\bar{b}gg}(p_1, p_2, p_3, p_4) = & \frac{4y_{24}^2}{y_{23}y_{34}y_{234}} + \frac{y_{13}^2 y_{24}^2}{2y_{14}y_{23}y_{34}y_{134}y_{234}} + \frac{(10}{ \\
 & + \frac{(4y_{24} + 19y_{34} - 4)y_{24}}{y_{23}y_{134}y_{234}} + \frac{(4y_{14}(y_{23} + 2) + y_{13}(12y_{24} + 7))}{2y_{34}y_{134}y_{234}} \\
 & - \frac{2y_{34}^2}{y_{13}y_{14}y_{134}} + \frac{y_{34}^2(y_{23} + y_{24} + y_{34} - 1)}{y_{13}y_{14}y_{23}y_{134}} + \frac{y_{34}^2(y_{23} + 3y_{24} +}{y_{13}y_{14}y_{134}y_{23}} \\
 & + \frac{18y_{34} + 2y_{24}(4y_{13} + 2y_{23} + 2y_{24} + 2y_{34} + 19) - 3}{2y_{134}y_{234}} + \frac{12y_{14}}{ \\
 & + \frac{2y_{14}y_{24}(2y_{24} + 3y_{34} - 1) + y_{34}(3y_{34}^2 + (9y_{24} - 2)y_{34} + 4)}{y_{13}y_{23}y_{134}y_{234}}
 \end{aligned}$$

Non-factorisable contributions

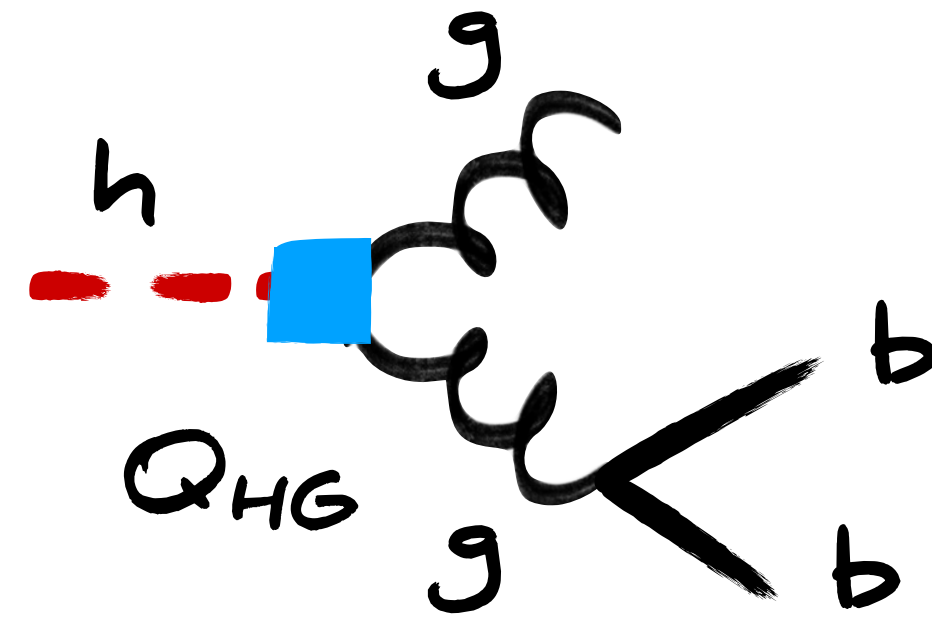
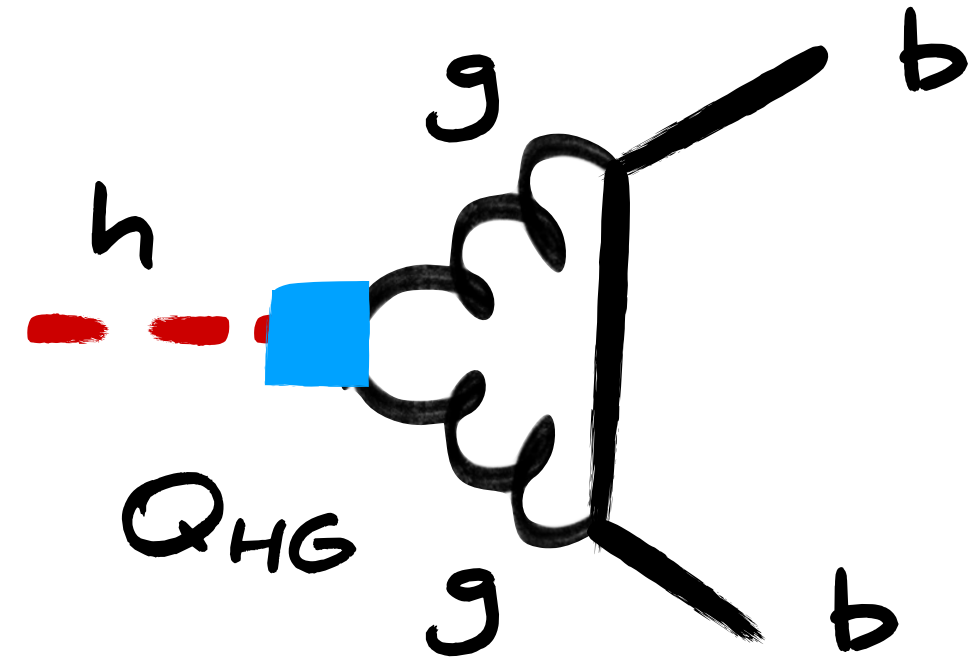
Q_{bG} corrections implemented into POWHEG-BOX. Possible to obtain realistic exclusive description of $pp \rightarrow Zh \rightarrow l^+l^-b\bar{b}$ production with NNLO accuracy using MiNLO' & MiNNLO_{PS} methods. Applying code to Higgs decay leads to:

$$\Gamma(h \rightarrow b\bar{b})_{\text{SMEFT}}^{\text{non}} = \frac{3y_b^2 m_h}{16\pi} \left(\frac{\alpha_s}{\pi}\right)^2 \frac{m_h^2}{3v^2} \left[1 + \frac{\alpha_s}{\pi} 17.32\right] \frac{v^2}{\Lambda^2} \text{Re}(C_{bG})$$



new term represents
a 60% correction

Contributions from Q_{HG}

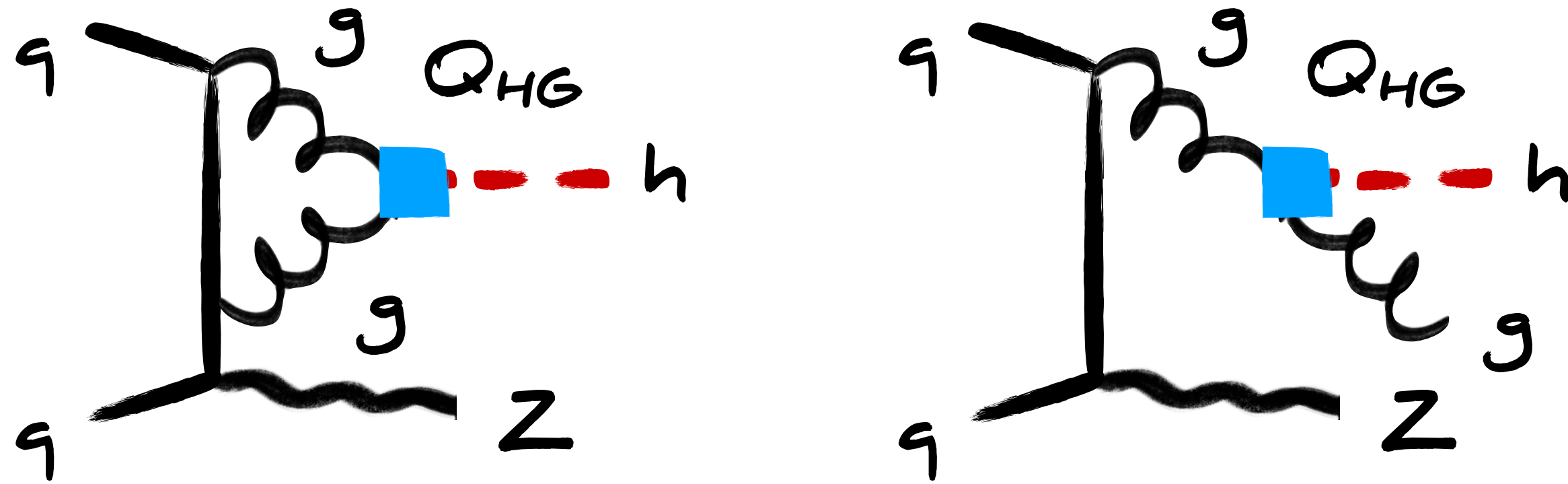


$$c_{HG} = \frac{v^2}{\Lambda^2} C_{HG} \in [-0.09, 0.06]$$

[Ellis et al., 2012.02779]

$$\frac{\Gamma(h \rightarrow b\bar{b})_{\text{SMEFT}}^{HG}}{\Gamma(h \rightarrow b\bar{b})_{\text{SM}}^{\text{LO}}} = \left(\frac{\alpha_s}{\pi}\right)^2 \left[\frac{19}{3} - 2\zeta_2 + \frac{1}{3} \ln^2 \left(\frac{m_b^2}{m_h^2} \right) \right] c_{HG} \in [-2.7, 1.7] \cdot 10^{-3}$$

Contributions from Q_{HG}



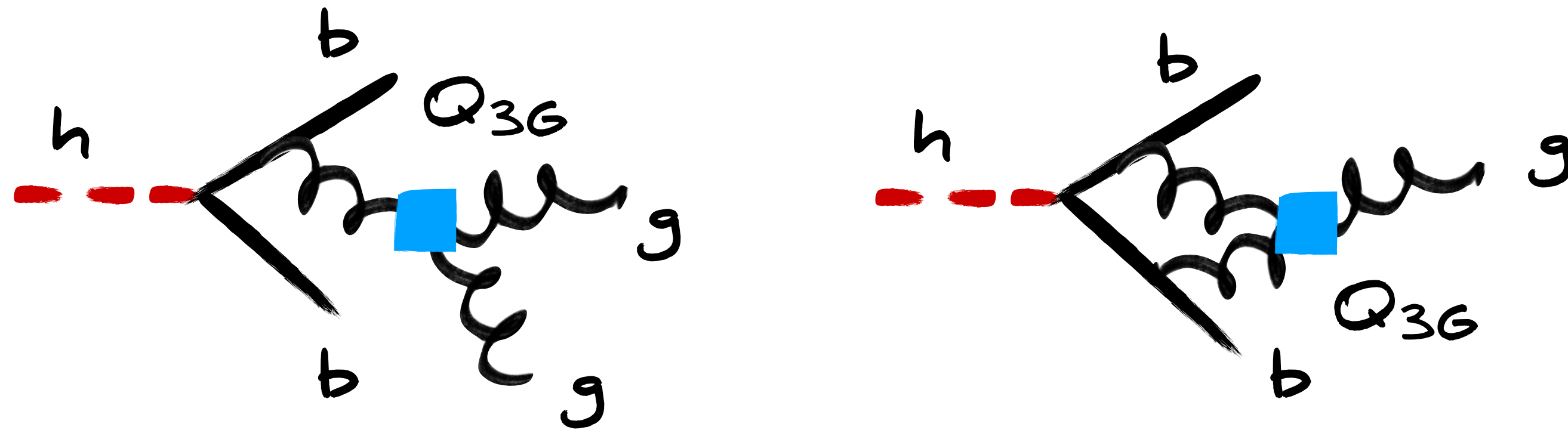
$$c_{HG} = \frac{v^2}{\Lambda^2} C_{HG} \in [-0.09, 0.06]$$

[Ellis et al., 2012.02779]

$$\frac{\sigma(pp \rightarrow hZ)_{\text{SMEFT}}^{HG}}{\sigma(pp \rightarrow hZ)_{\text{SM}}^{\text{LO}}} = 3 \left(\frac{\alpha_s}{\pi} \right)^2 \delta c_{HG} \in [-3.9, 2.4] \cdot 10^{-3}$$

numerically, one has $\delta = 10.7$

Contributions from Q_{3G}



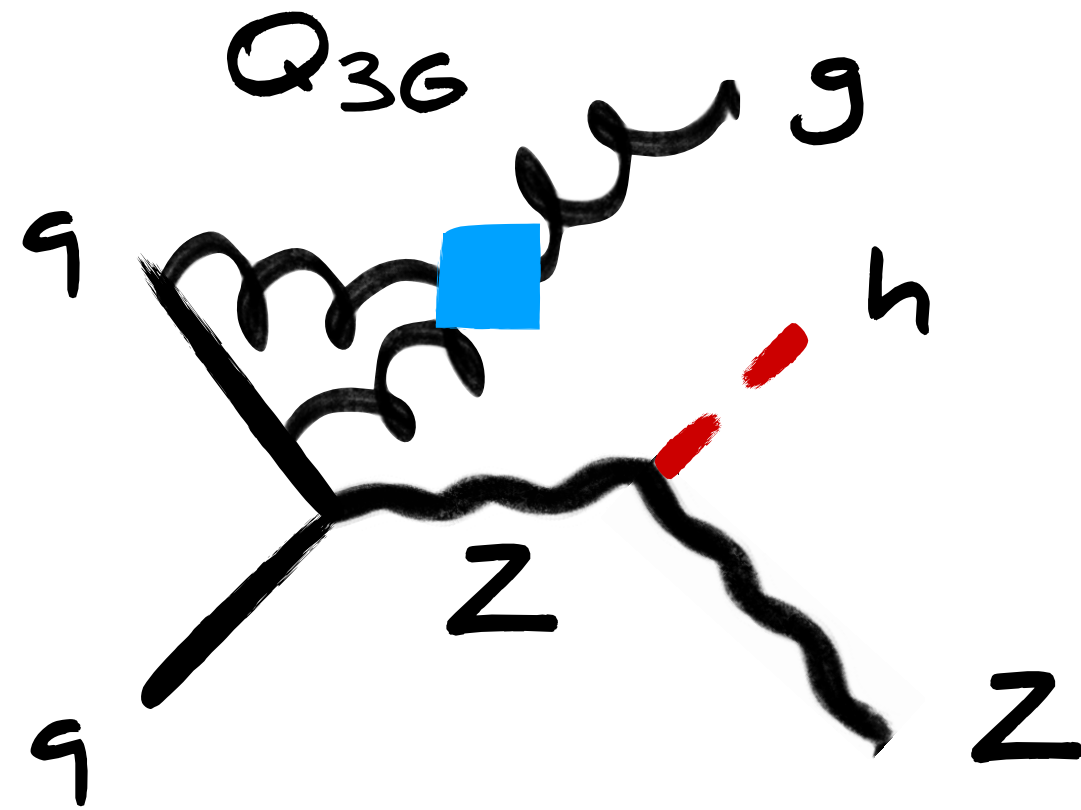
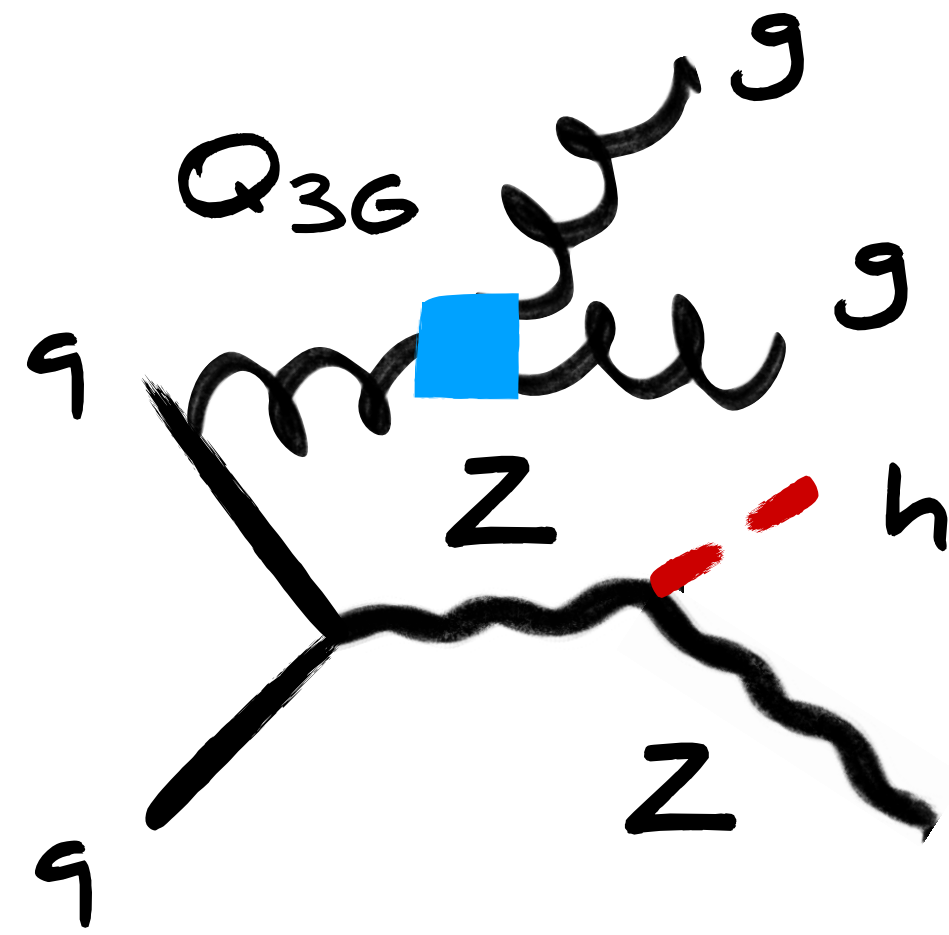
$$c_{3G} = \frac{v^2}{\Lambda^2} C_{3G} \in [-12.5, -4.1]$$

[Ellis et al., 2012.02779]

$$\frac{\Gamma(h \rightarrow b\bar{b})_{\text{SMEFT}}^{3G}}{\Gamma(h \rightarrow b\bar{b})_{\text{SM}}^{\text{LO}}} = N_{3G}^{\text{dec}} \left(\frac{\alpha_s}{\pi}\right)^2 \frac{m_h^2}{v^2} c_{3G} \in [-0.3, -0.1] \cdot 10^{-3}$$

explicit calculation gives $N_{3G}^{\text{dec}} = 2.23$

Contributions from Q_{3G}



$$c_{3G} = \frac{v^2}{\Lambda^2} C_{3G} \in [-12.5, -4.1]$$

[Ellis et al., 2012.02779]

$$\frac{\sigma(pp \rightarrow hZ)_{\text{SMEFT}}^{3G}}{\sigma(pp \rightarrow hZ)_{\text{SM}}^{\text{LO}}} = N_{3G}^{\text{prod}} \left(\frac{\alpha_s}{\pi} \right)^3 c_{3G} \in [-5.8, -1.9] \cdot 10^{-3}$$

quoted number corresponds to $N_{3G}^{\text{prod}} = 10$

Phenomenology analysis

We have seen that QCD corrections associated to operators other than $Q_{H\Box}$, Q_{HD} , Q_{bH} & Q_{bG} do not exceed level of a few permille

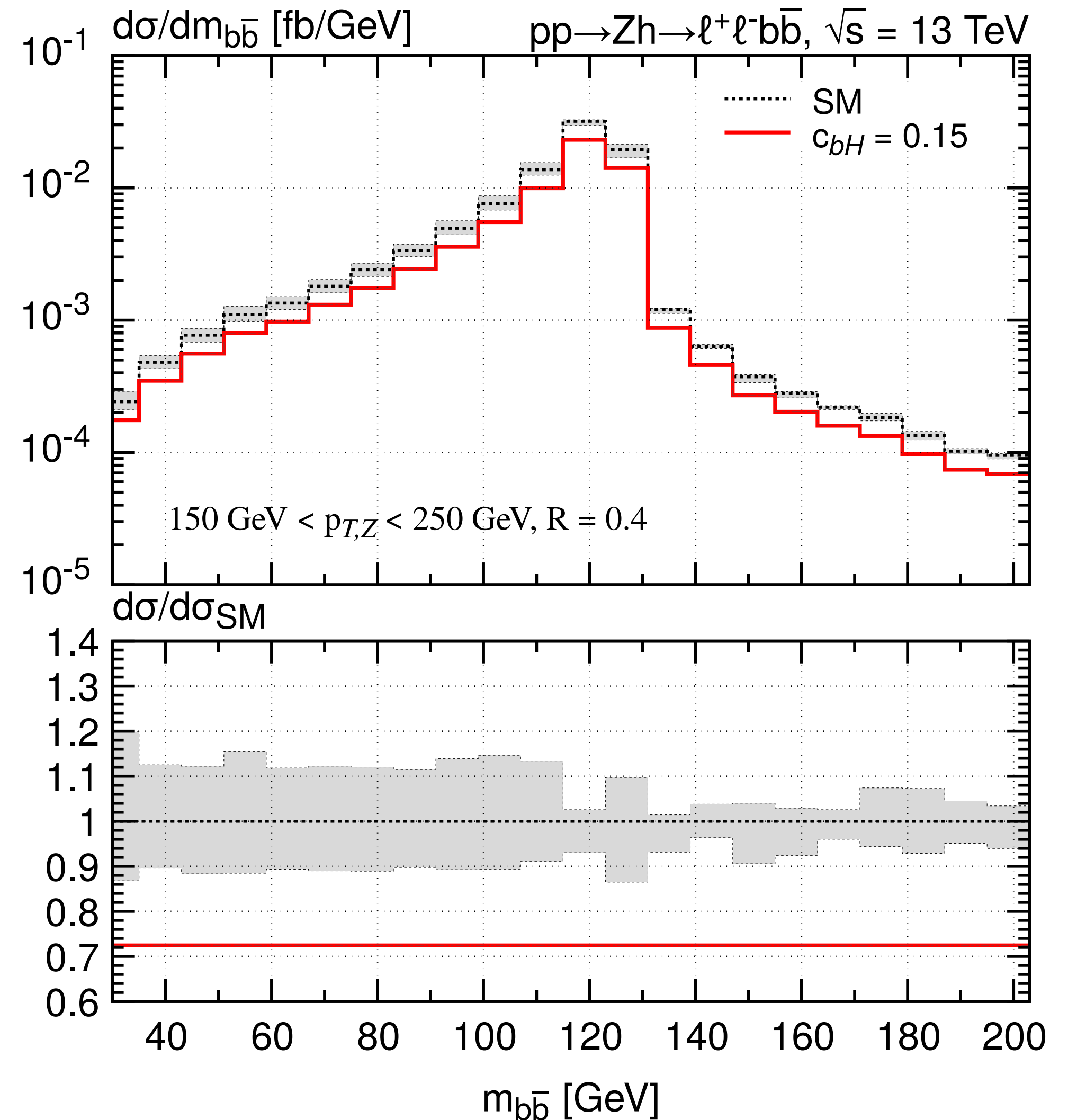
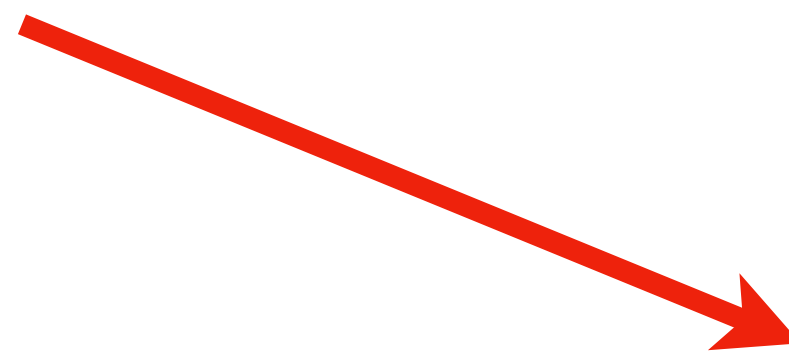
Maximal size of factorisable corrections to partial $h \rightarrow b\bar{b}$ decay rate can be derived from global fits of SMEFT Wilson coefficients:

$$\frac{\Gamma(h \rightarrow b\bar{b})_{\text{SMEFT}}^{\text{N}^3\text{LO}}}{\Gamma(h \rightarrow b\bar{b})_{\text{SM}}^{\text{N}^3\text{LO}}} - 1 \in [-39, 26]\% \quad \text{for} \quad c_{bH} = \frac{v^2}{\Lambda^2} \text{Re}(C_{bH}) \in [-0.13, 0.20]$$

[Ellis et al., 2012.02779]

Phenomenology analysis

factorisable contributions just lead to a constant shift, i.e. a K-factor, in all $pp \rightarrow Zh \rightarrow \ell^+ \ell^- b \bar{b}$ distributions



Interlude: bounds on dipole operator Q_{bG}

Observable	Wilson coefficient	95% CL bound
Dijet angular distributions	$ c_{bG} $	2864
Two b -tagged jets	$ c_{bG} $	152
Z -boson production with two b -jets	$ c_{bG} $	438
Searches for neutron electric dipole moment	$ \text{Im}(c_{bG}) $	0.05

Due to chirality-flipping nature of Q_{bG} no interference between SMEFT & SM amplitudes for $m_b = 0$. Resulting LHC bounds on $|c_{bG}|$ thus very weak. $|\text{Im}(c_{bG})|$ instead severely constrained by neutron electric dipole moment

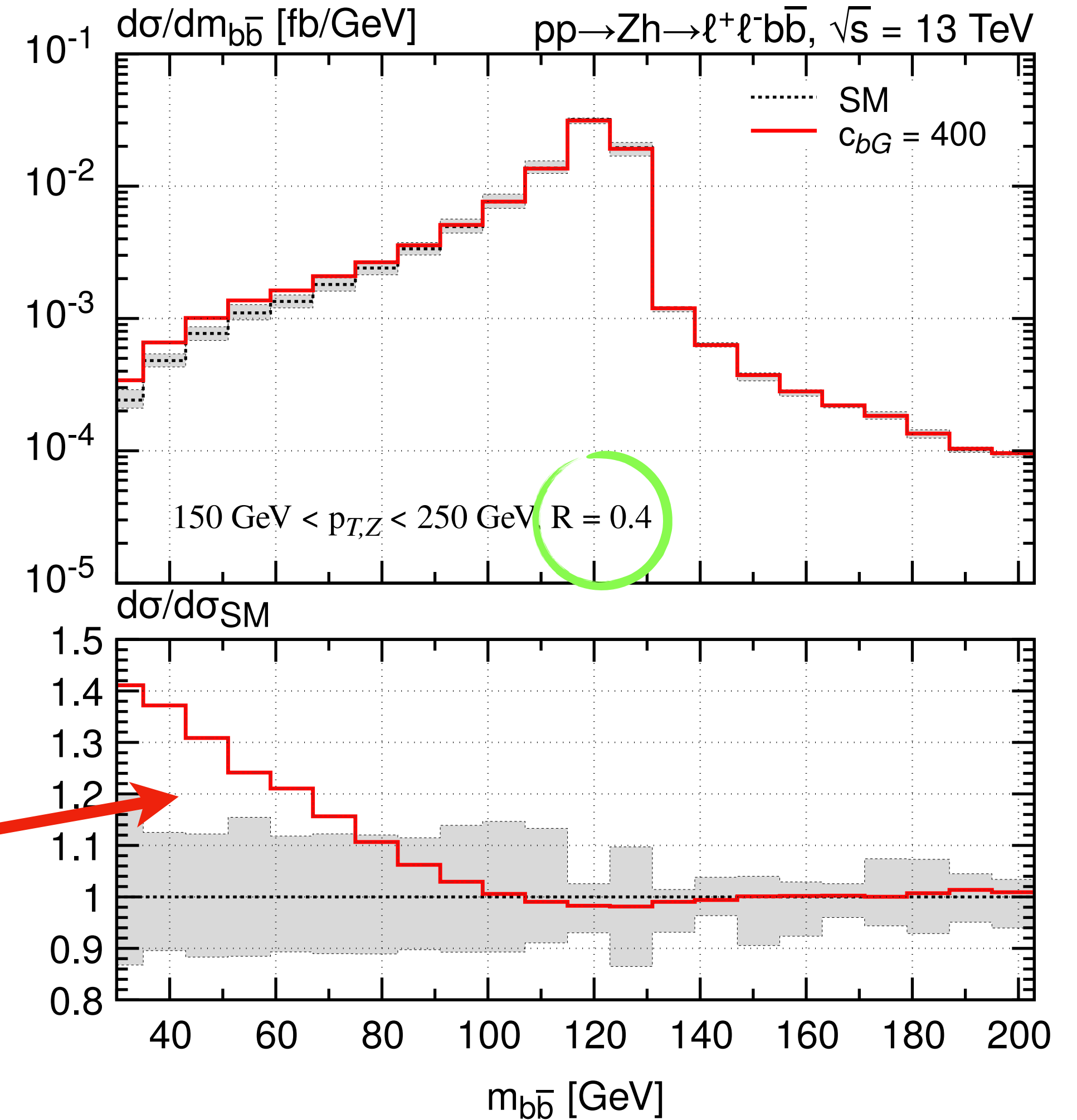
Phenomenology analysis

Despite large Wilson coefficient of Q_{bG} possible size of non-factorisable contributions to partial $h \rightarrow b\bar{b}$ decay rate smaller than that of factorisable ones by a factor of $O(5)$:

$$\frac{\Gamma(h \rightarrow b\bar{b})_{\text{SMEFT}}^{\text{N}^3\text{LO}}}{\Gamma(h \rightarrow b\bar{b})_{\text{SM}}^{\text{N}^3\text{LO}}} - 1 \in [-6.3, 6.3]\% \text{ for } c_{bG} = \frac{v^2}{\Lambda^2} \text{Re}(C_{bG}) \in [-438, 438]$$

But non-factorisable contributions lead to non-trivial modifications of spectra in $pp \rightarrow Zh \rightarrow l^+l^-b\bar{b}$ production

Phenomenology analysis

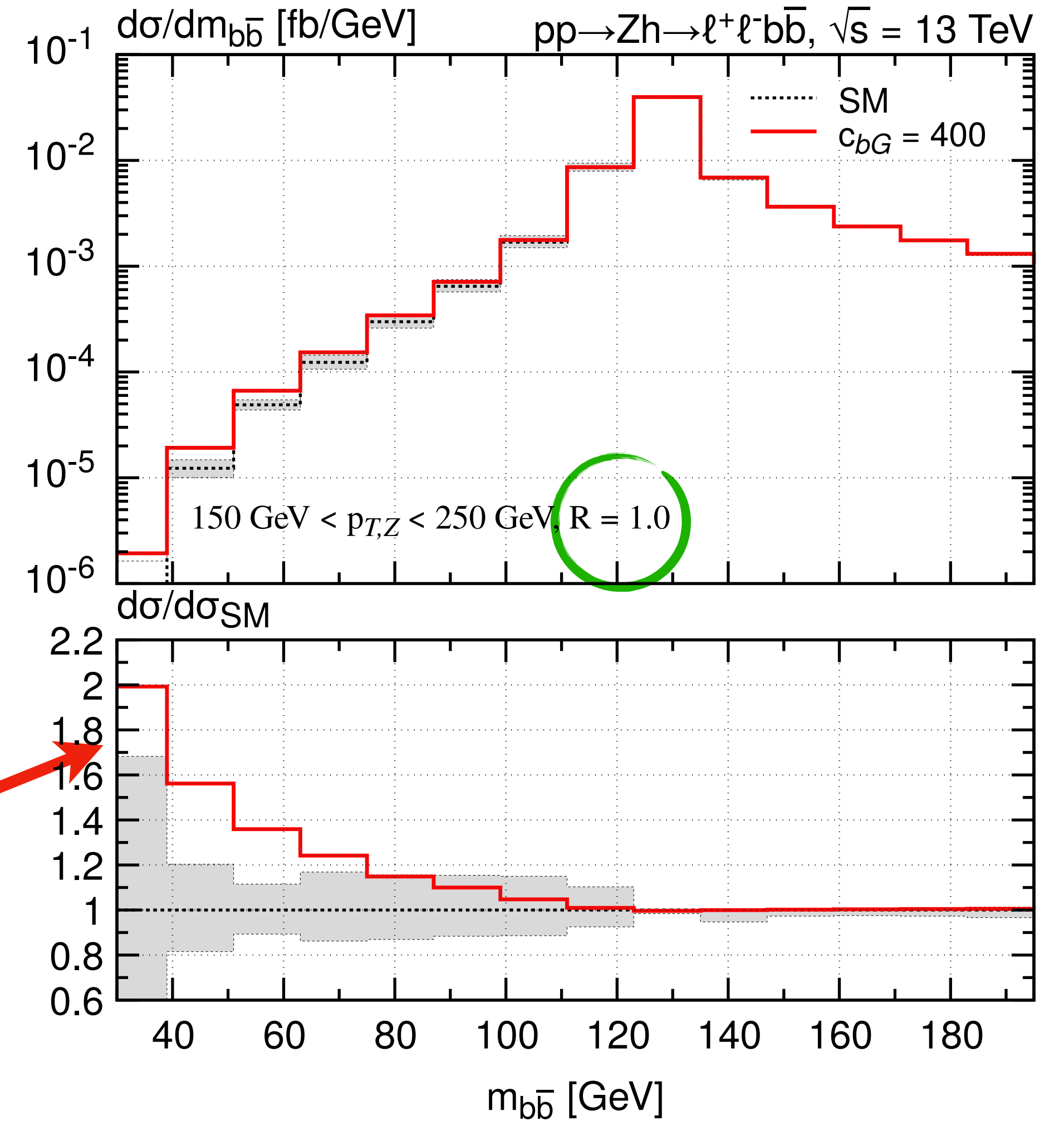


extra gluon emission in leading-order Q_{bG} contribution tends to reduce dibottom invariant mass relative to SM

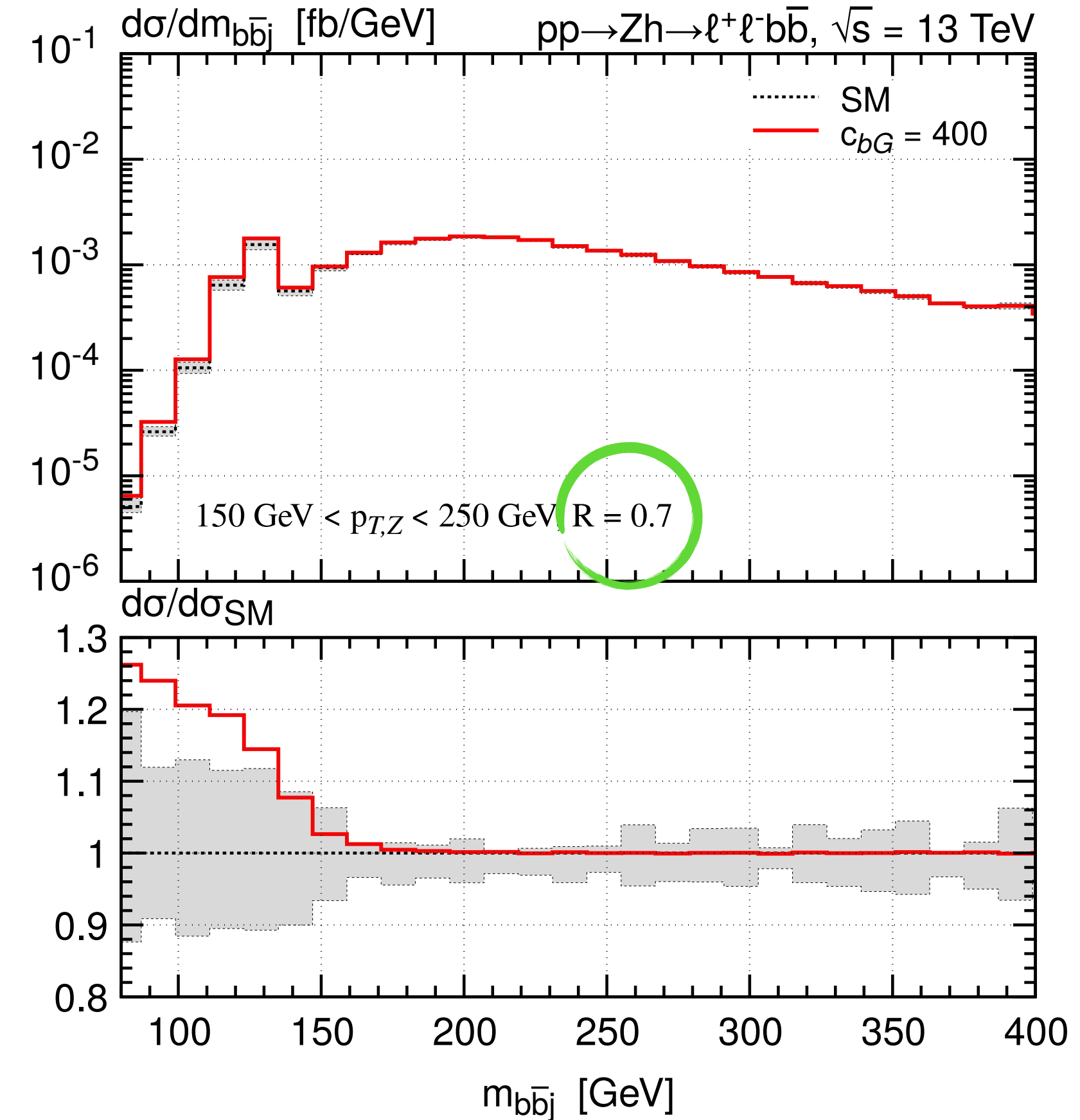
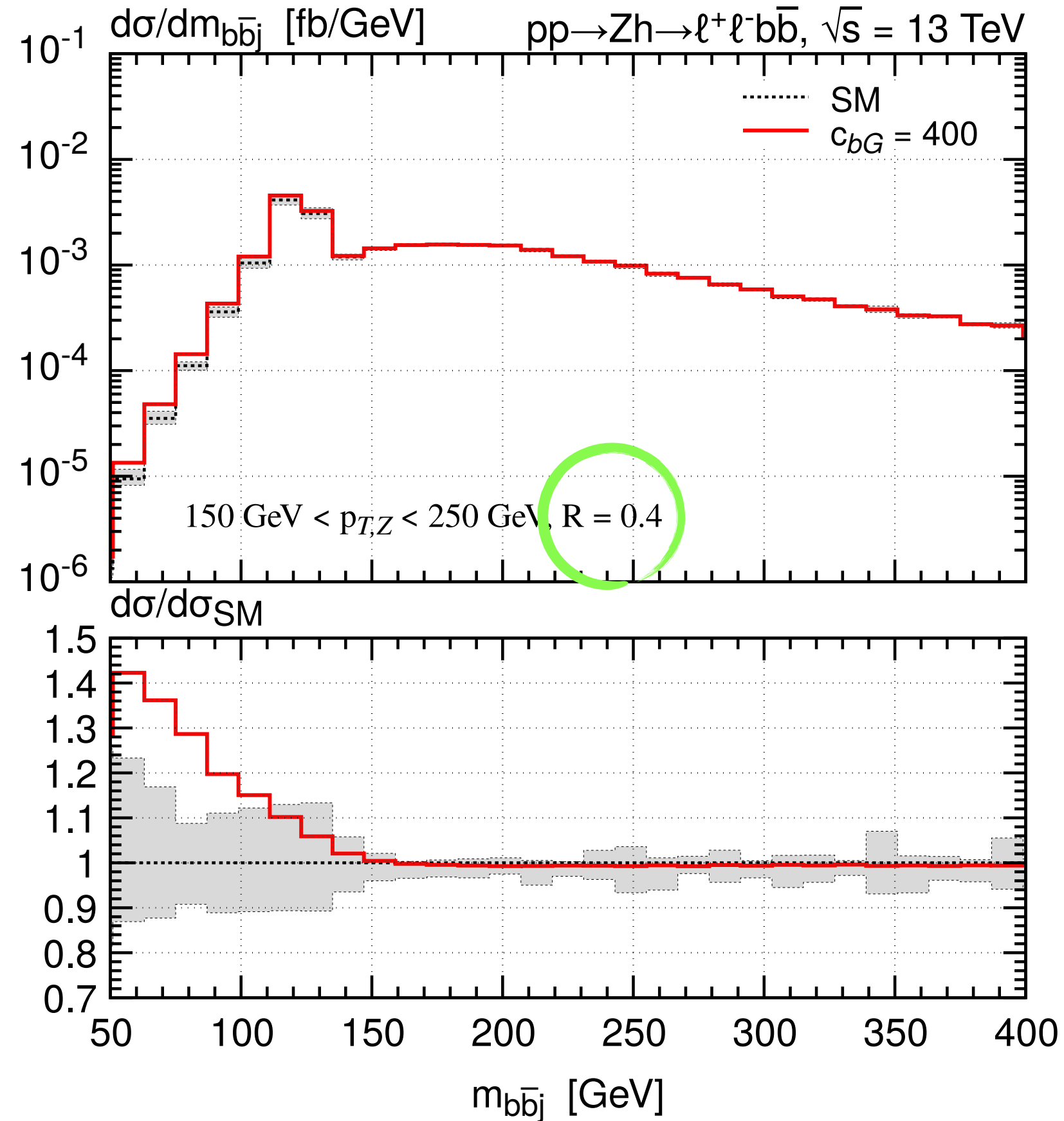
Phenomenology analysis



size of effect depends on radius parameter R used to reconstruct anti- k_t jets



Phenomenology analysis

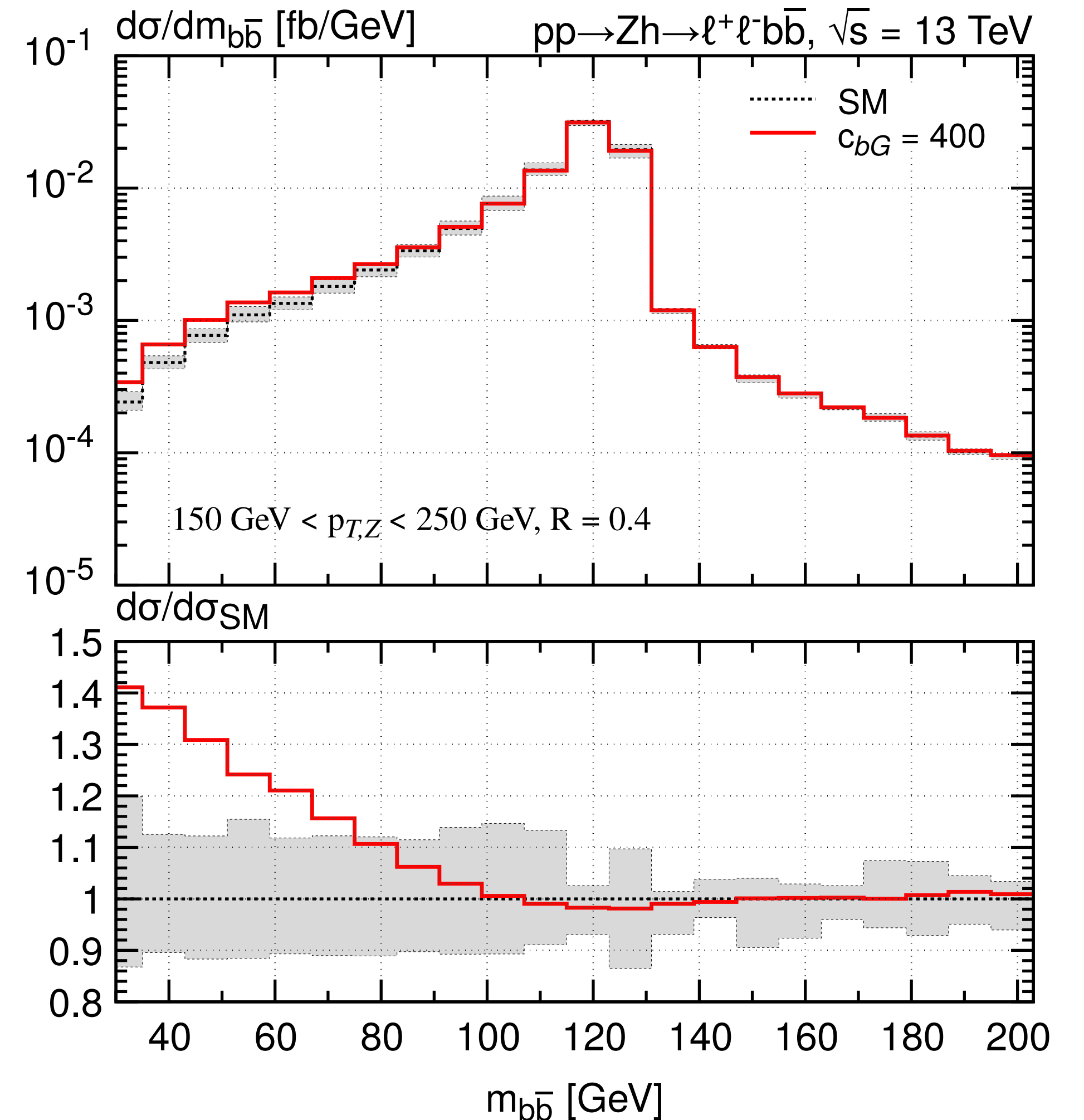


Also 3-jet invariant mass reduced on average. Effects again R-dependent

Outlook

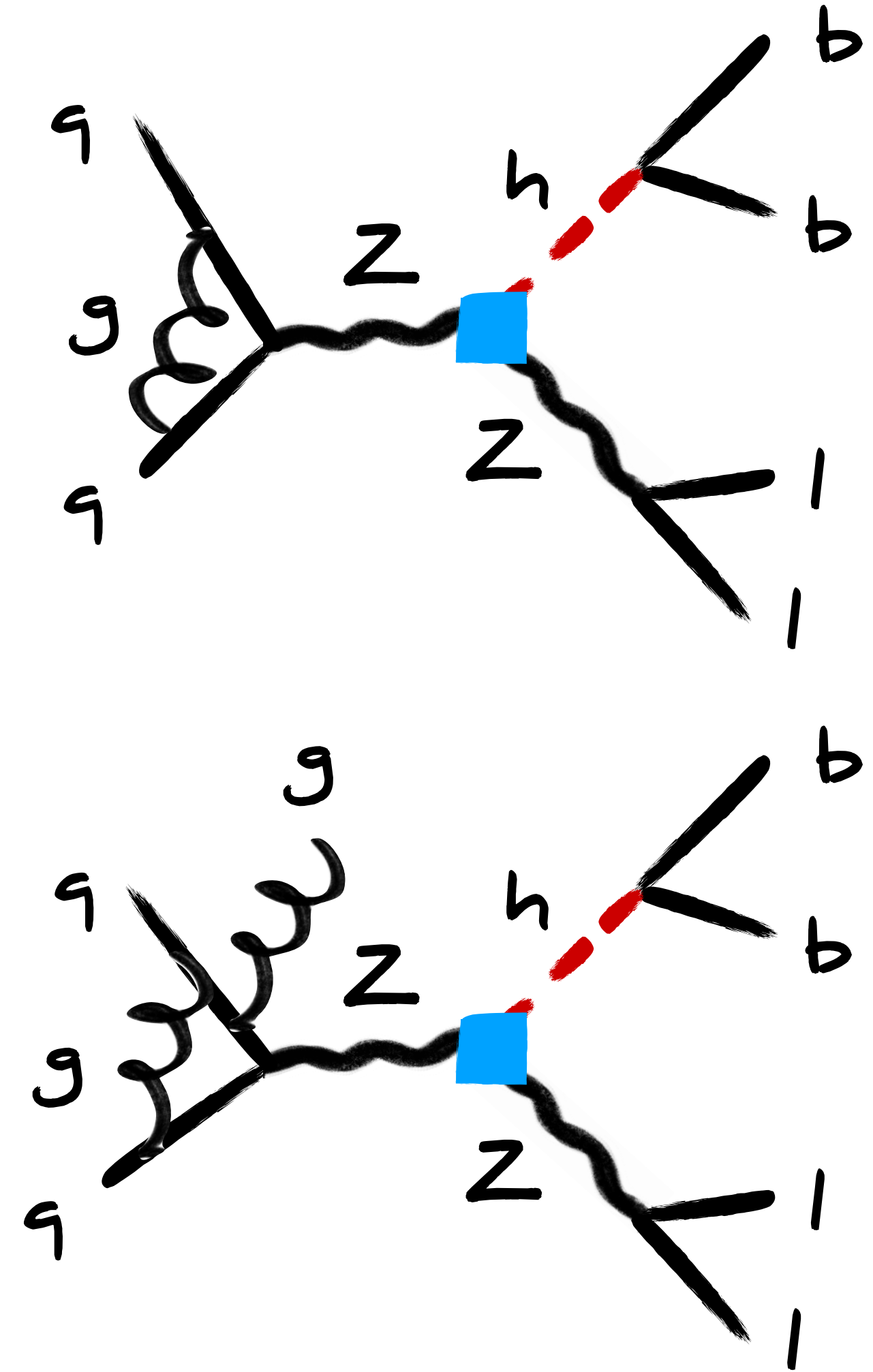
Non-trivial shape changes of distributions in $pp \rightarrow Zh \rightarrow \ell^+\ell^-b\bar{b}$ production in combination with R-dependence may allow to enhance sensitivity to dipole operator Q_{bG} which is presently only very weakly constrained

Further opportunities at a e^+e^- machine using event shapes



Outlook

Inclusion of EW SMEFT operators that modify hZZ vertex straightforward since full information already encoded in SM Drell-Yan amplitudes

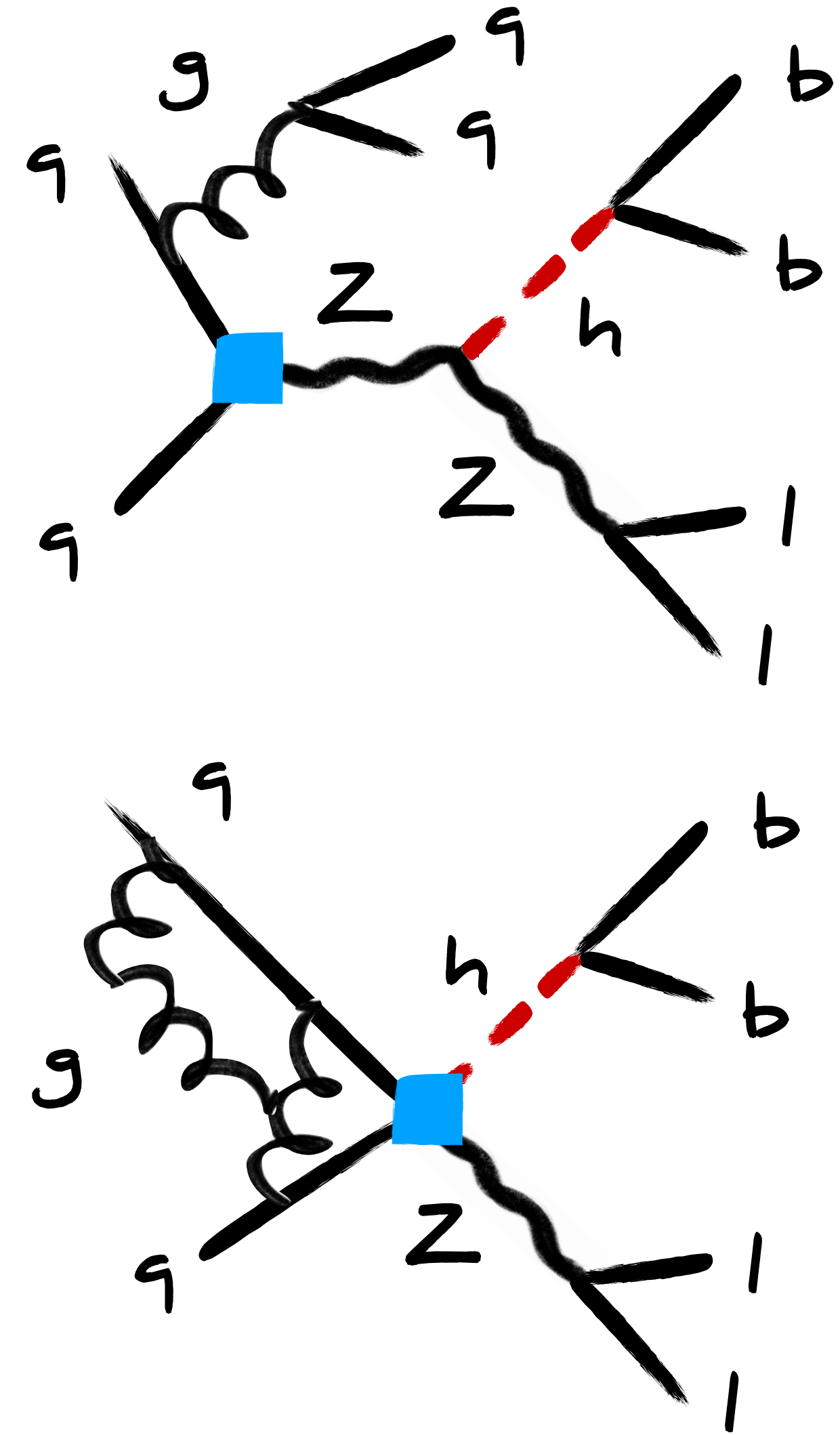


Outlook

Same is true for QCD corrections involving SMEFT operators modifying $q\bar{q}Z$ & $q\bar{q}Zh$ vertices

NNLO+PS implementation of dominant contributions from EW SMEFT operators in POWHEG-BOX framework ongoing.

Stay tuned!



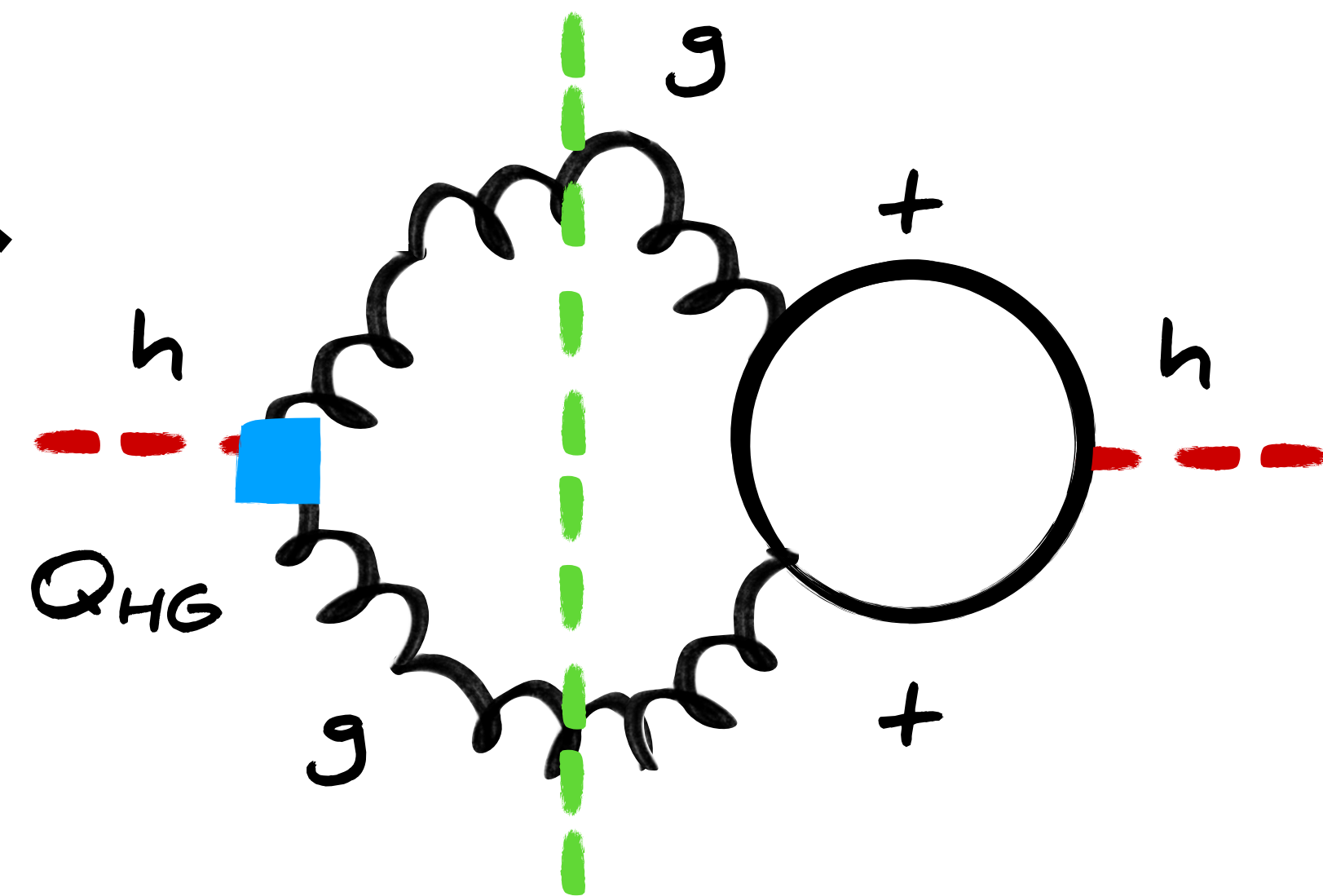
Backup



SMEFT corrections to total Higgs width

$$\Gamma_h^{\text{SMEFT}} = (1 + 2c_{\text{kin}}) \left[\Gamma_h^{\text{SM}} - (2\Delta c_{bH} - K_{bG} \Delta_{\text{non}} c_{bG}) \Gamma(h \rightarrow b\bar{b})_{\text{SM}}^{\text{LO}} + 6K_{HG} c_{HG} \Gamma(h \rightarrow gg)_{\text{SM}}^{\text{LO}} \right]$$

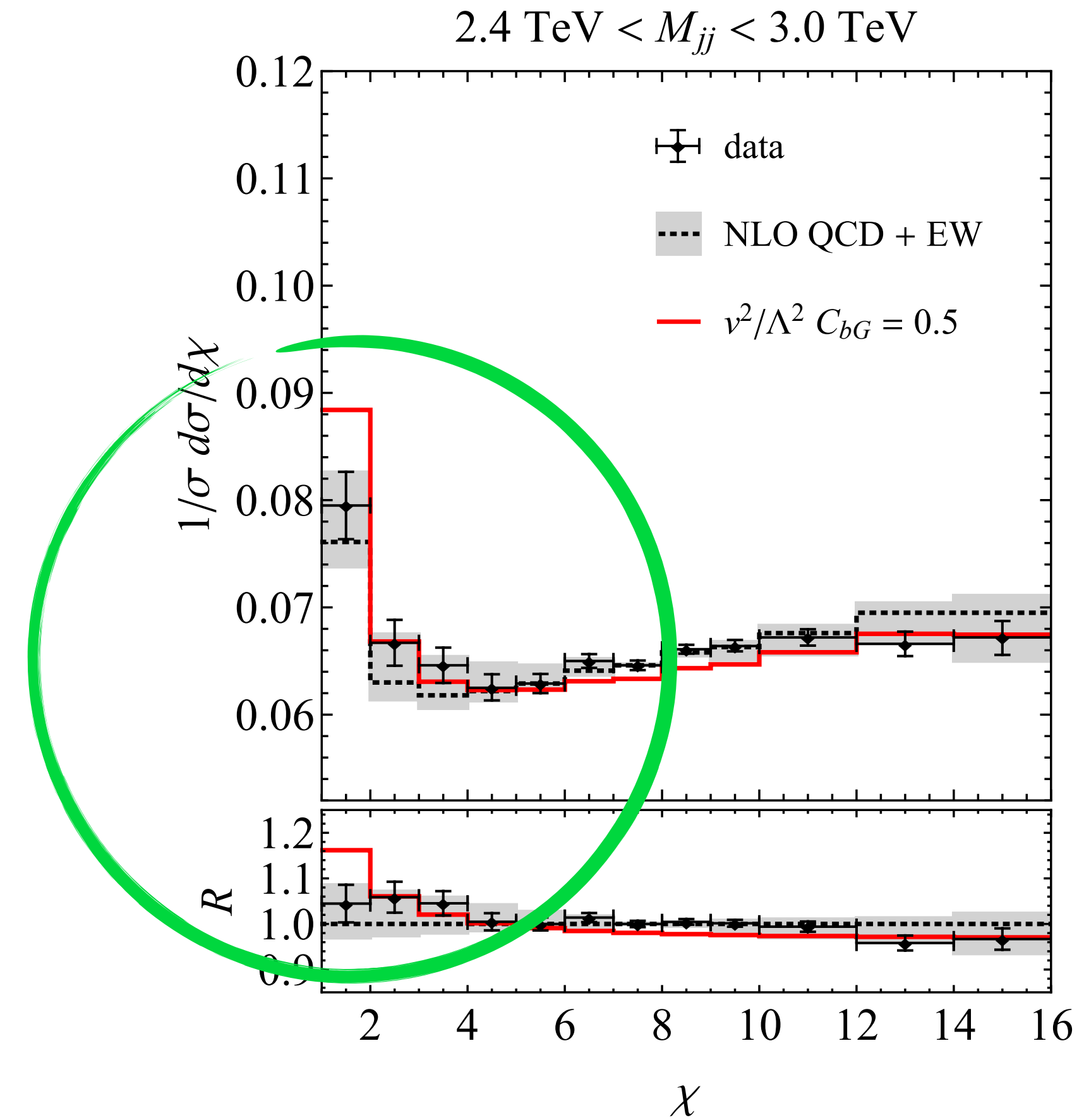
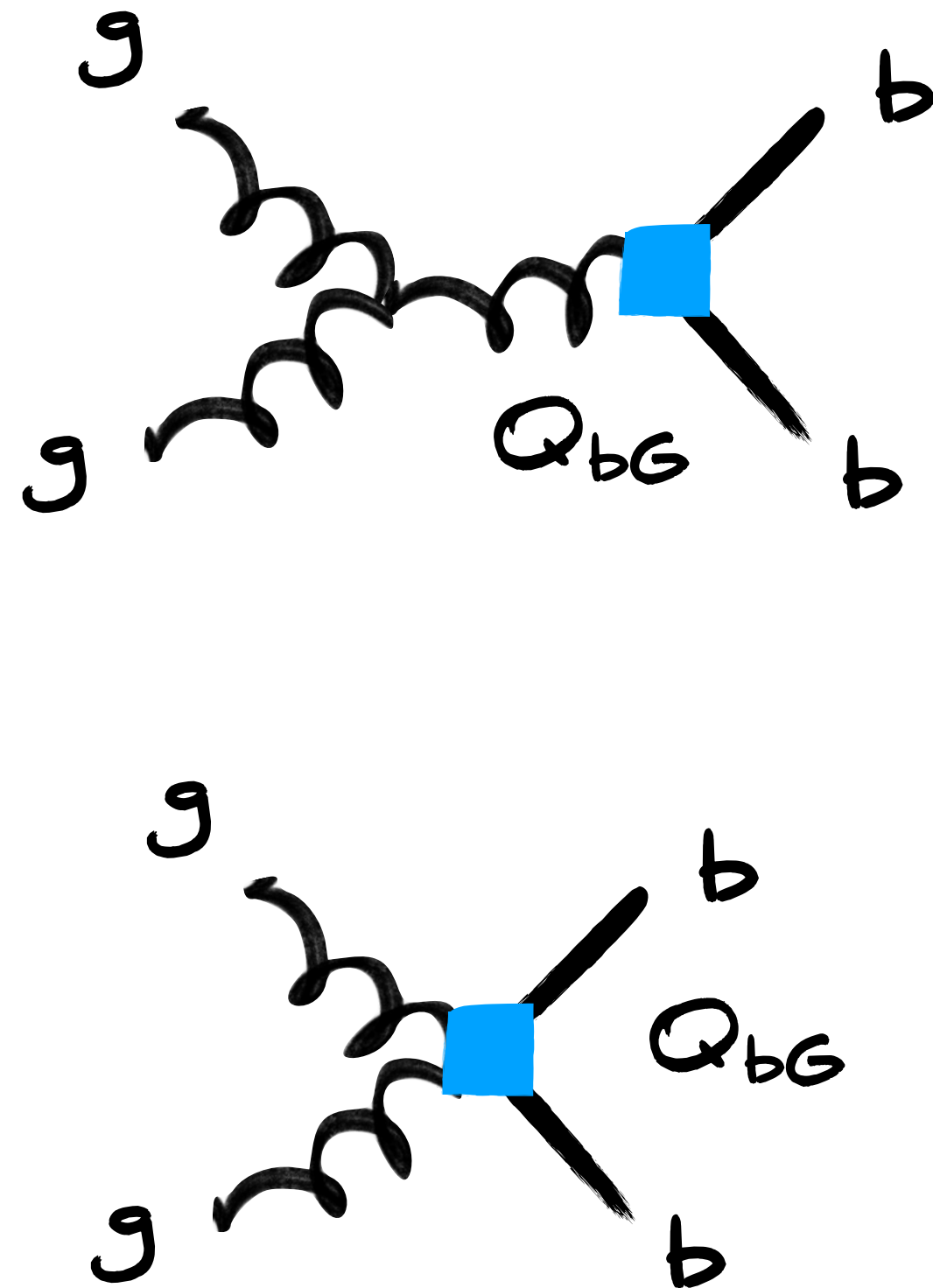
$$K_{HG} = 1.844$$



Event selections

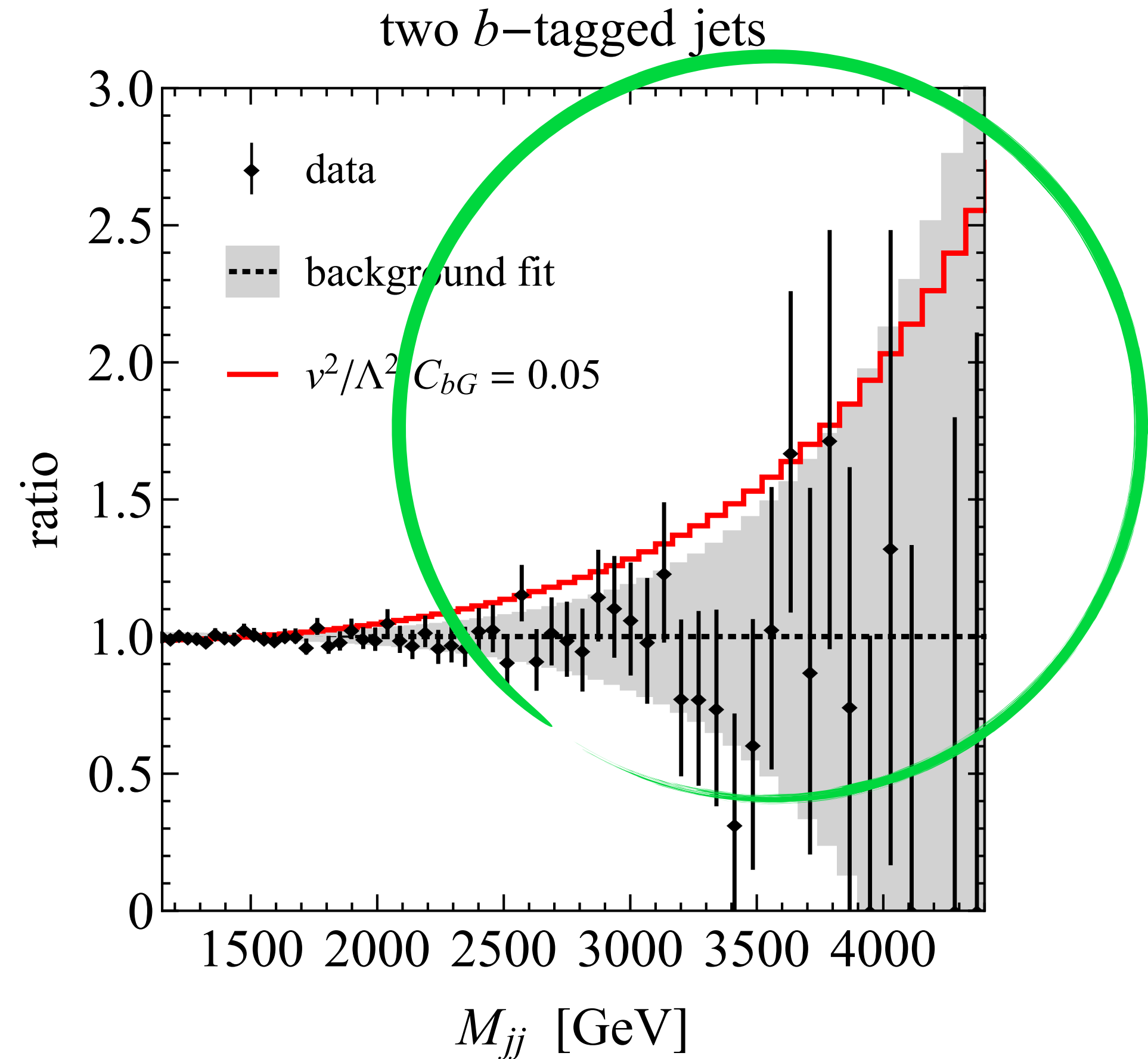
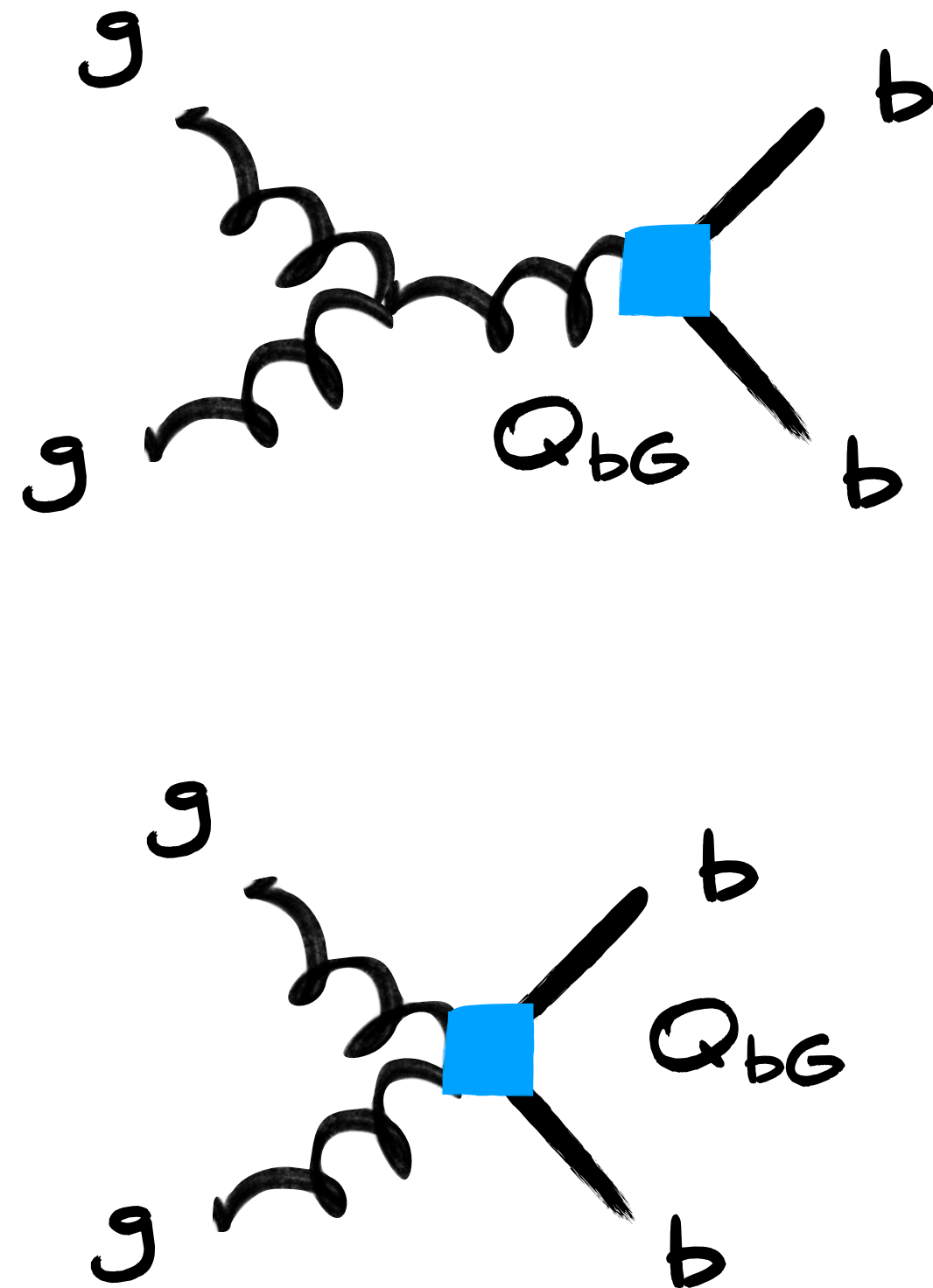
In our differential analysis we select events with two charged leptons (electrons or muons) to explore the $Zh \rightarrow \ell^+ \ell^- b\bar{b}$ signature. The leptons are required to have a transverse momentum of $p_{T,\ell} > 15 \text{ GeV}$ and a pseudorapidity of $|\eta_\ell| < 2.5$. The invariant mass of the dilepton pair is restricted to $m_{\ell^+\ell^-} \in [75, 105] \text{ GeV}$. The events are furthermore required to have at least two b -jets, which are reconstructed using the anti- k_t algorithm [65] as implemented in FastJet [66]. We impose transverse momentum cuts of $p_{T,b} > 25 \text{ GeV}$ and a rapidity threshold of $|\eta_b| < 2.5$ on the b -jets. The definition of potential additional jets use the same thresholds as those of the b -jets. The dominant background processes are $Z + \text{jets}$, $t\bar{t}$, single-top and diboson production. The latter three types of backgrounds can be substantially reduced by requiring large values of $p_{T,Z}$ [67]. Hence, to improve the signal-to-background ratio we impose $p_{T,Z} \in [150, 250] \text{ GeV}$. Notice that this $p_{T,Z}$ requirement corresponds to the second resolved $p_{T,Z}$ bin as recommended in the stage 1.2 simplified template cross sections (STXS) framework [68–70] which is also implemented in the latest ATLAS LHC Run II measurements of the $pp \rightarrow Zh \rightarrow \ell^+ \ell^- b\bar{b}$ process [71, 72]. We will also comment on how our results are modified if the other two resolved regions, i.e. $p_{T,Z} \in [75, 150] \text{ GeV}$ and $p_{T,Z} > 250 \text{ GeV}$, are considered.

Bounds on dipole-type operator Q_{bG}



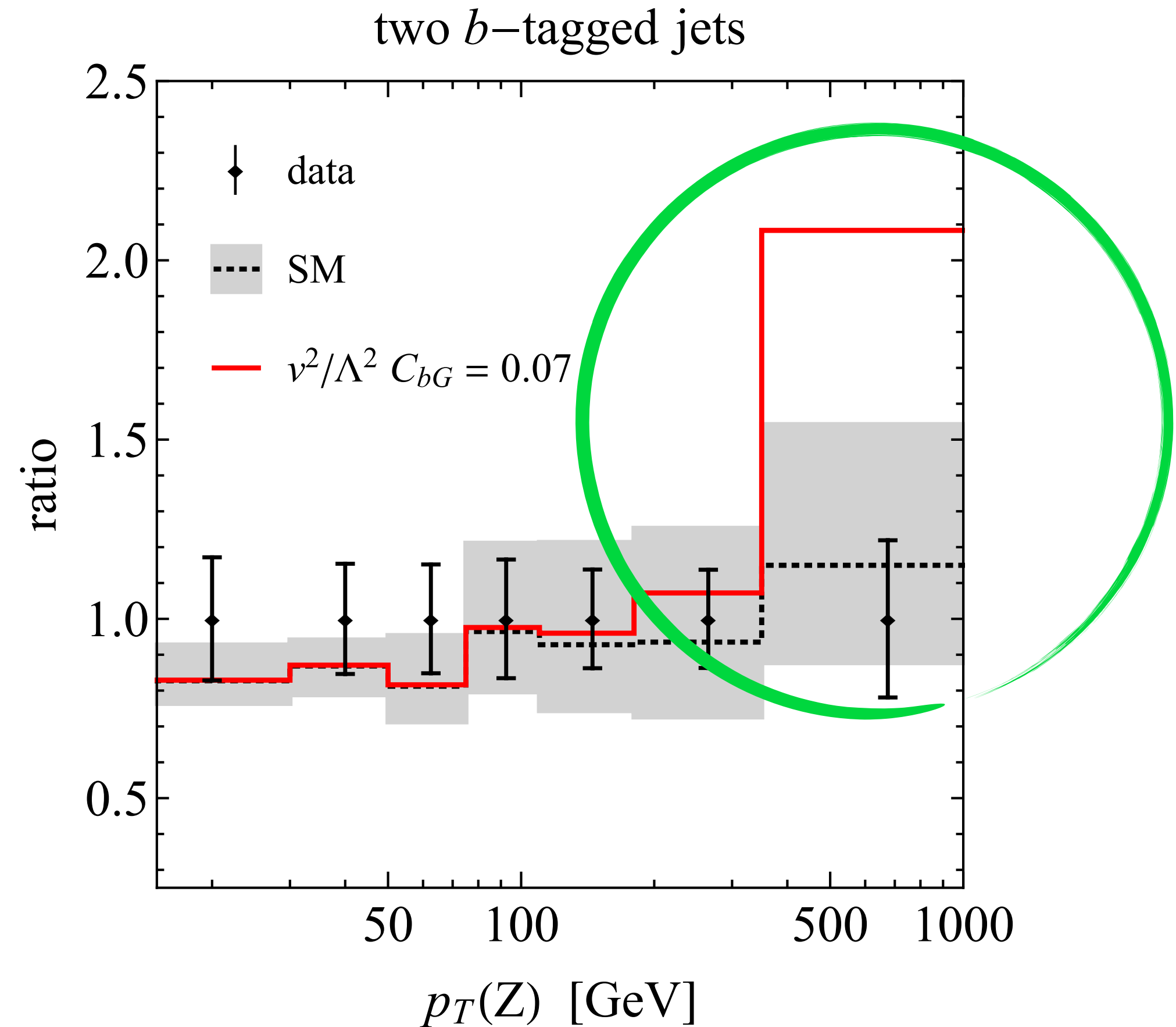
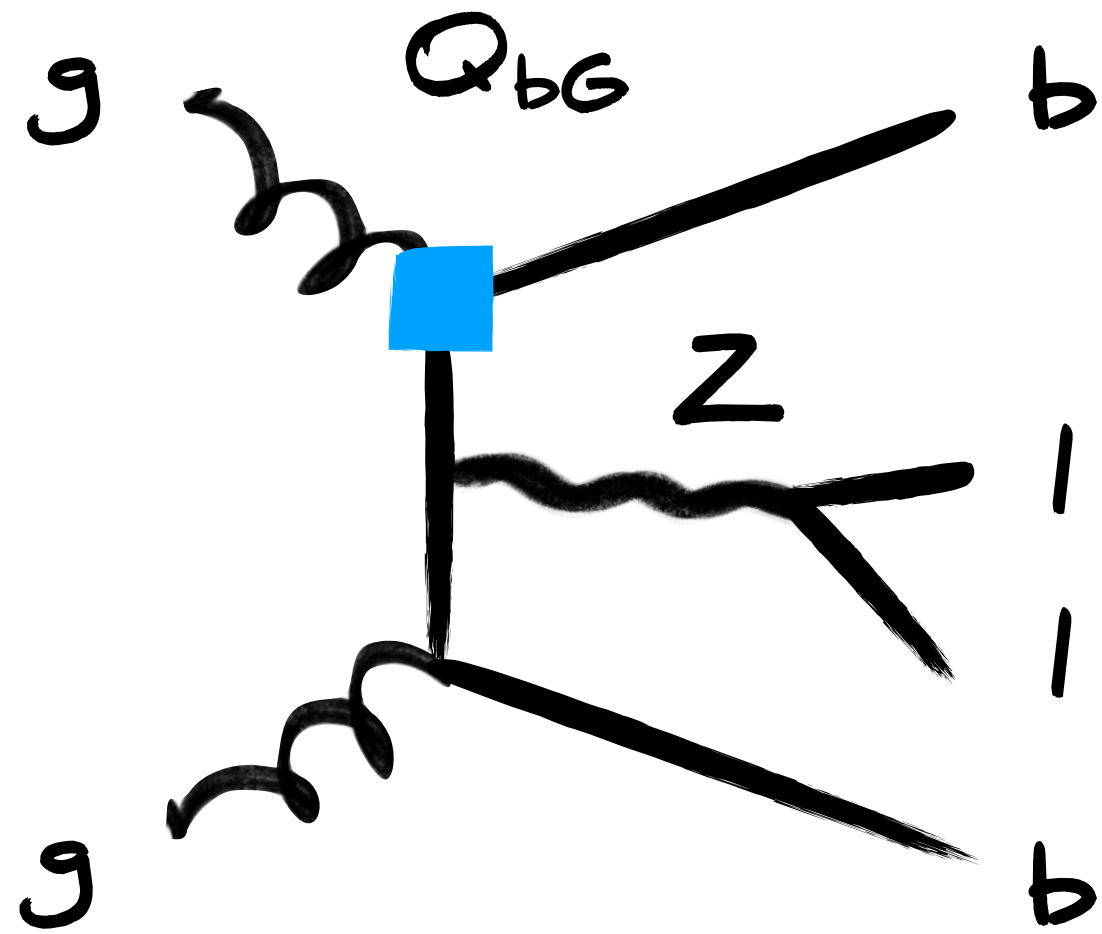
Q_{bG} contributions lead to an enhanced activity of high-energy jets in central region

Bounds on dipole-type operator Q_{bG}



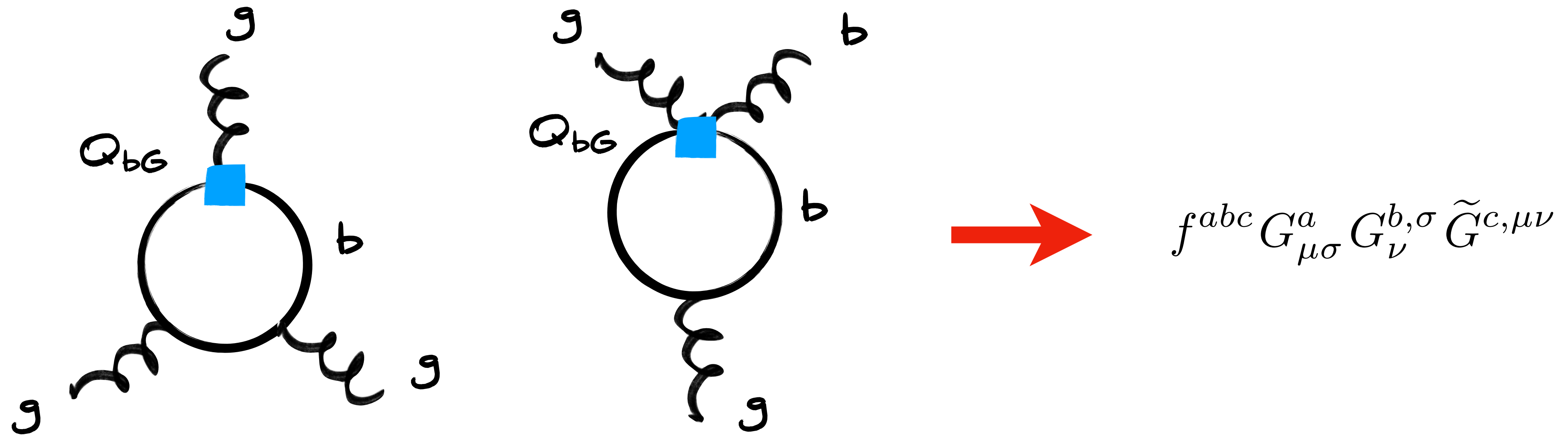
Q_{bG} contributions lead to an enhancement of rate for high dijet invariant masses

Bounds on dipole-type operator Q_{bG}



Q_{bG} effects grow with transverse momentum & lead to more events at high $p_T(Z)$

Bounds on dipole-type operator Q_{bG}



1-loop threshold corrections involving Q_{bG} generate CP-violating Weinberg operator. This operator leads to a non-zero neutron electric dipole moment at hadronic scale

ZZh operators

[Bizon et al., 2106.06328]

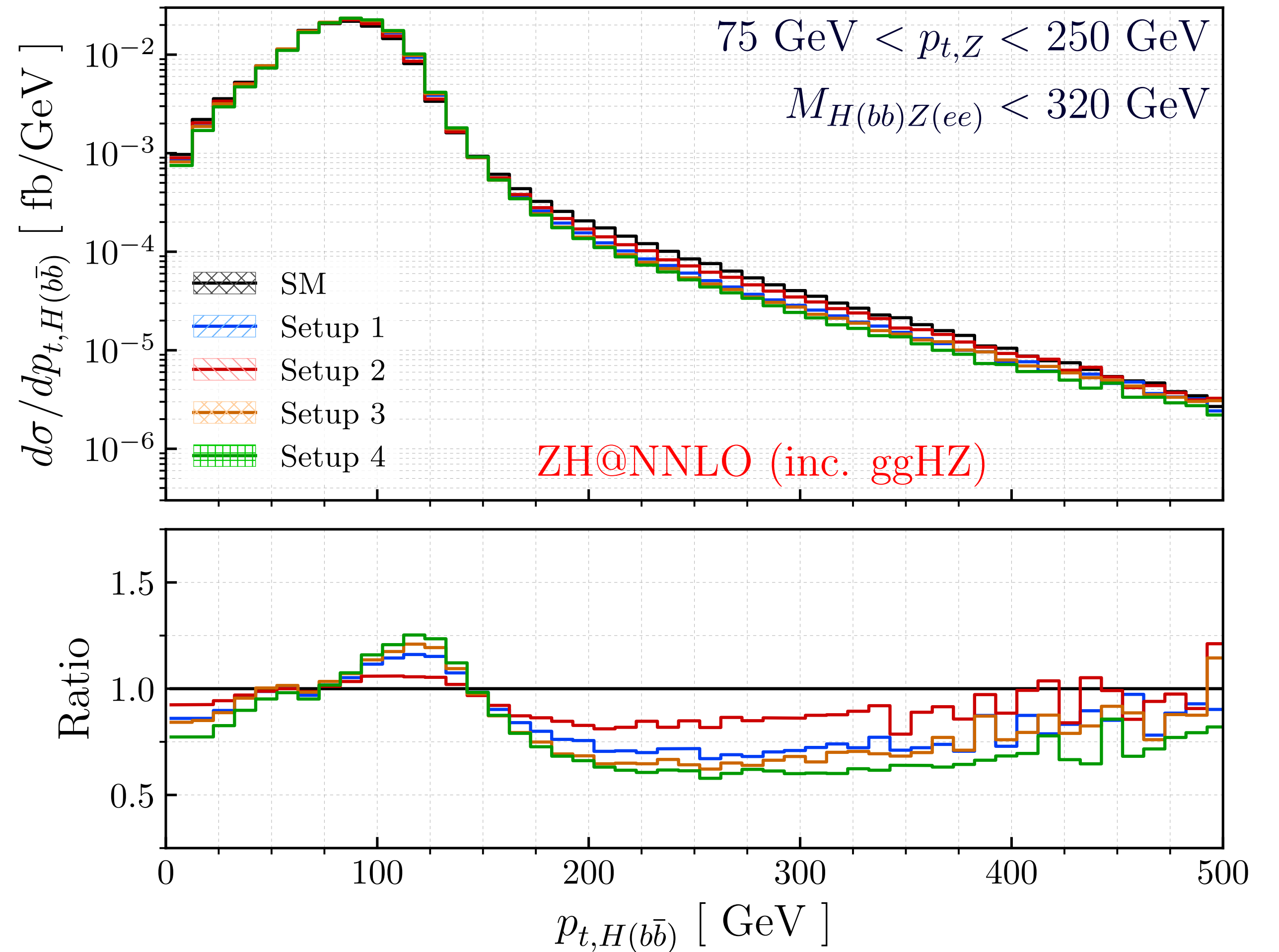
$$\mathcal{L} = -\frac{1}{4\Lambda} g_{hZZ}^{(1)} Z_{\mu\nu} Z^{\mu\nu} h$$

$$-\frac{1}{\Lambda} g_{hZZ}^{(2)} Z_\nu \partial_\mu Z^{\mu\nu} h$$

$$-\frac{1}{4\Lambda} \tilde{g}_{hZZ} Z_{\mu\nu} \tilde{Z}^{\mu\nu} h$$

Setup 1: $g_{hZZ}^{(1)} = 2.8, g_{hZZ}^{(2)} = -0.6$

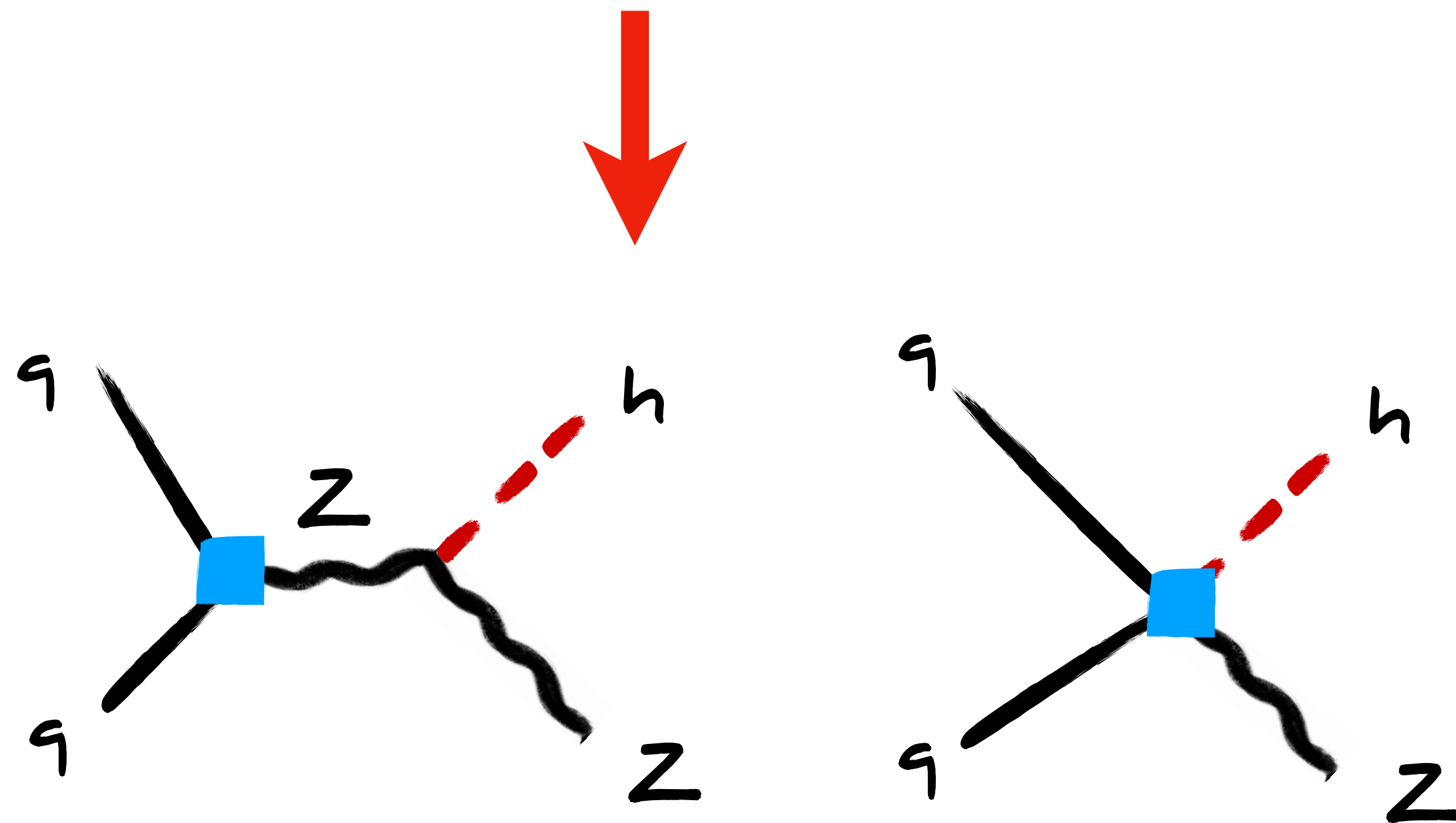
Setup 2: $g_{hZZ}^{(1)} = 1.05, \tilde{g}_{hZZ} = -2.9$



ZZh operators lead to shape changes in kinematic spectra of $pp \rightarrow Zh \rightarrow l+l-b\bar{b}$

$q\bar{q}Z$ & $q\bar{q}Zh$ operators

$$Q_{Hq}^{(1)} = \bar{q}_L \gamma^\mu q_L \left(iH^\dagger \overleftrightarrow{D}_\mu H \right), \dots$$



modifications grow with energy,
making Zh searches @ LHC in
boosted regime competitive with
LEP bounds on Z couplings

$$\propto \frac{(p_Z + p_h)^2}{M_Z^2}$$