



# Effective Field Theory interpretation of the $pp \rightarrow H \rightarrow 4\ell$ Higgs boson decay measurements with the ATLAS detector

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# Standard Model Effective Field Theory



- Effective Field Theories assume that new physics occurs at an energy scale,  $\Lambda$ , much greater than the interaction energy  $E \ll \Lambda$
- SMEFT extends the Standard Model (SM) Lagrangian by introducing higher-dimensional operators:

$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM} + \mathcal{L}^{(5)} + \mathcal{L}^{(6)} + \mathcal{L}^{(7)} + \dots$$

where  $\mathcal{L}^{(D)} = \sum_i \frac{C_i^{(D)}}{\Lambda^{D-4}} O_i^{(D)}$

- The leading contributions to new physics are from the dimension-6 operators:

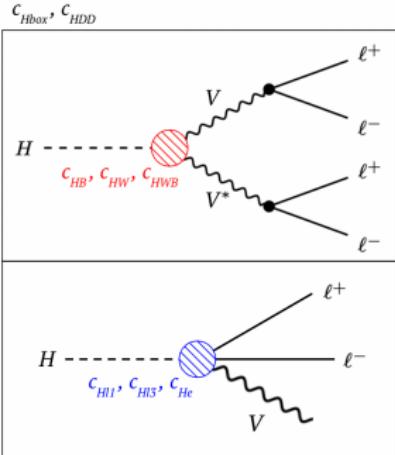
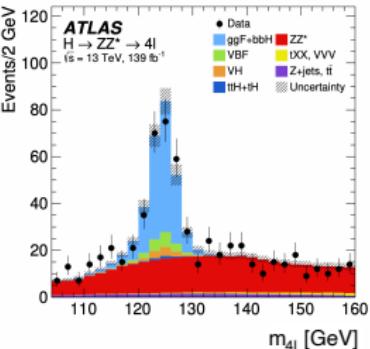
$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM} + \sum_i \frac{C_i}{\Lambda^2} O_i = \mathcal{L}_{SM} + \sum_i c_i O_i$$

# $H \rightarrow 4\ell$ Decay Channel



[arxiv.org/pdf/2004.03447.pdf](https://arxiv.org/pdf/2004.03447.pdf)

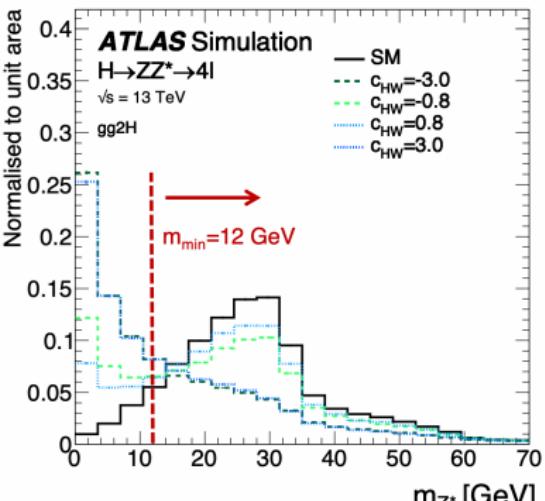
- The  $H \rightarrow 4\ell$  decay channel has a clear Higgs boson signature and a high signal-to-background ratio
- Generate events with a Higgs boson decaying into two pairs of oppositely charged leptons
- Wilson Coefficients,  $c_i$ , associated with the couplings between the Higgs boson and its decay products
- 8 Wilson Coefficients are considered:
  - $c_{Hbox}, c_{HDD}$
  - $c_{HB}, c_{HW}, c_{HWB}$
  - $c_{HI1}, c_{HI3}, c_{He}$



# $H \rightarrow 4\ell$ Decay Channel



- There are several observables which are strongly dependent on some of the Wilson Coefficients,  $c_i$
- The strongest BSM dependence is in the invariant mass of the off-shell Z-boson ( $m_{Z^*}$ )
- An event selection cut of  $m_{Z^*} > 12\text{ GeV}$  is introduced to suppress the background



[arxiv.org/pdf/2004.03447.pdf](https://arxiv.org/pdf/2004.03447.pdf)

- Signal Acceptance:

$$A^{BSM} = \frac{N_{fiducial}^{BSM}}{N_{total}^{BSM}} \Rightarrow \frac{A^{BSM}}{A^{SM}} \propto \frac{\sigma_{fid}^{BSM}(c_i)/\sigma_{fid}^{SM}}{\sigma_{tot}^{BSM}(c_i)/\sigma_{tot}^{SM}}$$

- The cross section can be parametrised in terms of the Wilson Coefficients,  $c_i$ :

$$\frac{\sigma^{BSM}(c_{ij})}{\sigma^{SM}} = 1 + \sum_i \alpha_i c_i + \sum_{i,j} \beta_{ij} c_i c_j$$

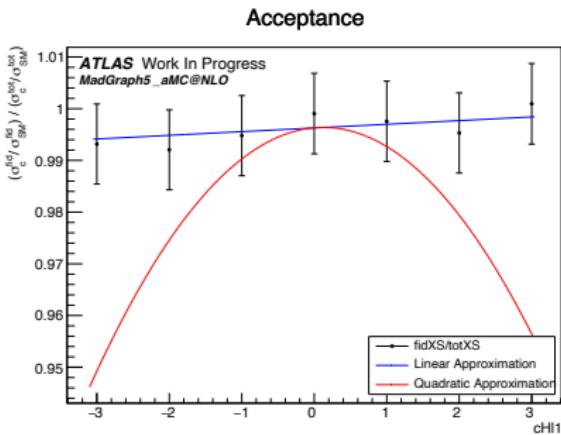
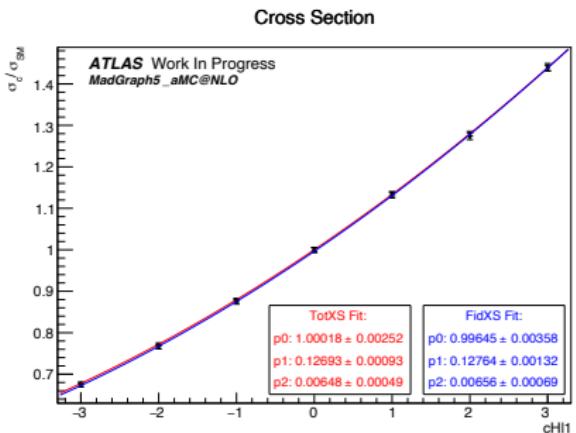
- For one coupling, the acceptance can be approximated using a Taylor expansion:

$$\frac{A^{BSM}}{A^{SM}} = \frac{1 + a_{fid} c_i + b_{fid} c_i^2}{1 + a_{tot} c_i + b_{tot} c_i^2}$$

$$\approx 1 + (a_{fid} - a_{tot}) c_i + (b_{fid} - b_{tot} - a_{fid} a_{tot}) c_i^2 + \dots$$

# Acceptance Example - $c_{Hl1}$

- Signal samples with 200,000 events were generated using MadGraph5 at NLO, for different  $c_i$  values for each of the 8 the Wilson coefficients considered
- An example for  $c_{Hl1}$  :



$$\Rightarrow \frac{A^{BSM}}{A^{SM}} \approx 0.9966 + 0.0012c_{Hl1} - 0.0161c_{Hl1}^2$$

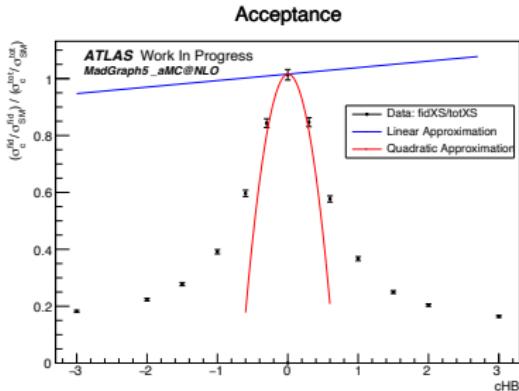
# Acceptance Parametrisation



- The acceptance was calculated for the 8 couplings, in the quadratic approximation, when all other Wilson coefficients are set to zero:

**ATLAS Work in Progress**

|            | Quadratic Approximation  |                      |
|------------|--------------------------|----------------------|
| $c_{Hbox}$ | $0.997 + 0.002 c_{Hbox}$ | $-0.015(c_{Hbox})^2$ |
| $c_{HDD}$  | $0.998 + 0.003 c_{HDD}$  | $-0.001(c_{HDD})^2$  |
| $c_{Hl1}$  | $0.996 + 0.002 c_{Hl1}$  | $-0.016(c_{Hl1})^2$  |
| $c_{Hl3}$  | $0.998 - 0.001 c_{Hl3}$  | $-0.055(c_{Hl3})^2$  |
| $c_{He}$   | $0.998 + 0.001 c_{He}$   | $-0.010(c_{He})^2$   |
| $c_{HWB}$  | $1.018 - 0.164 c_{HWB}$  | $-0.707(c_{HWB})^2$  |
| $c_{HW}$   | $1.014 + 0.167 c_{HW}$   | $-0.649(c_{HW})^2$   |
| $c_{HB}$   | $1.014 + 0.025 c_{HB}$   | $-2.339(c_{HB})^2$   |



- The largest quadratic terms are observed for the Wilson Coefficients defining the coupling between the Higgs and vector bosons,  $c_{HWB}$ ,  $c_{HW}$  and  $c_{HB}$

# Quadratic Approximation - Mixed Terms



- To include the quadratic terms in the acceptance, the mixing between the couplings must also be considered
- For two couplings:

$$\frac{\sigma^{BSM}(c_1, c_2)}{\sigma^{SM}} = 1 + \alpha_1 c_1 + \beta_1 c_1^2 + \alpha_2 c_2 + \beta_2 c_2^2 + \gamma_{12} c_1 c_2$$

- Two ways to calculate the mixed terms:
  1. Three Point Calculation - The mixed term is calculated from the following approximation:
$$\sigma_{(c_1=1, c_2=1)} = \gamma_{12} c_1 c_2 + \sigma_{(c_1=1, c_2=0)} + \sigma_{(c_1=0, c_2=1)} - 1$$
  2. 2D Fit - Calculate the acceptance for large number of coupling combinations and extract the mixed term using a two dimensional fit

# Mixed Terms Comparison



- From 8 couplings, there are 28 combinations of two couplings
- A selection of the mixed terms are shown below, focusing on the coupling combinations with the largest mixed terms:

**ATLAS** Work in Progress

| Couplings: | Total Cross Section |                  | Fiducial Cross Section |                  |
|------------|---------------------|------------------|------------------------|------------------|
|            | Three Points        | 2D Fit           | Three Points           | 2D Fit           |
| cHI1, cHe  | -0.0031 ± 0.0079    | -0.0010 ± 0.0002 | -0.0017 ± 0.0113       | -0.0011 ± 0.0002 |
| cHI1, cH13 | -0.0094 ± 0.0073    | -0.0099 ± 0.0002 | -0.0082 ± 0.0104       | -0.0102 ± 0.0002 |
| cHW, cHDD  | 0.06783 ± 0.0111    | 0.06715 ± 0.0007 | 0.04187 ± 0.0128       | 0.04696 ± 0.0006 |
| cHB, cHW   | -0.0305 ± 0.0250    | -0.0329 ± 0.0030 | -0.0596 ± 0.018        | -0.0607 ± 0.0015 |
| cHW, cHWB  | -1.3105 ± 0.0124    | -1.3106 ± 0.0015 | -0.1512 ± 0.0132       | -0.1537 ± 0.0009 |
| cHB, cHWB  | -1.4263 ± 0.0228    | -1.4264 ± 0.0030 | -0.2048 ± 0.0173       | -0.1857 ± 0.0015 |

- 2D fit provides an error on the mixed terms which is  $\sim 10x$  smaller than the three point calculation

# 2D Acceptance



- Mixed terms largest for  $(c_{HB}, c_{HWB})$ :

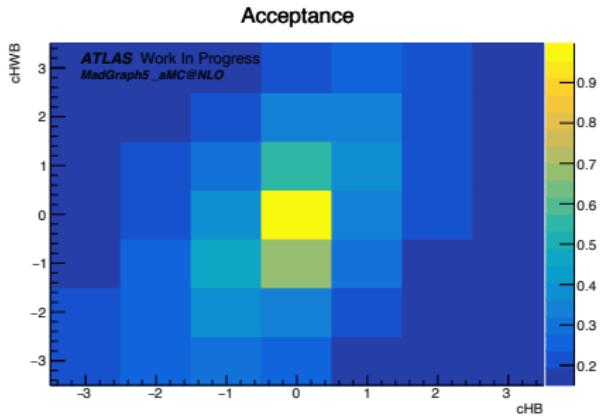
Fiducial Cross Section (2D fit):

$$0.998 - 0.084c_{HB} + 0.020c_{HWB} + 0.364c_{HB}^2 + 0.100c_{HWB}^2 - 0.186c_{HB}c_{HWB}$$

Total Cross Section (2D fit):

$$0.999 - 0.112c_{HB} + 0.180c_{HWB} + 2.658c_{HB}^2 + 0.791c_{HWB}^2 - 1.426c_{HB}c_{HWB}$$

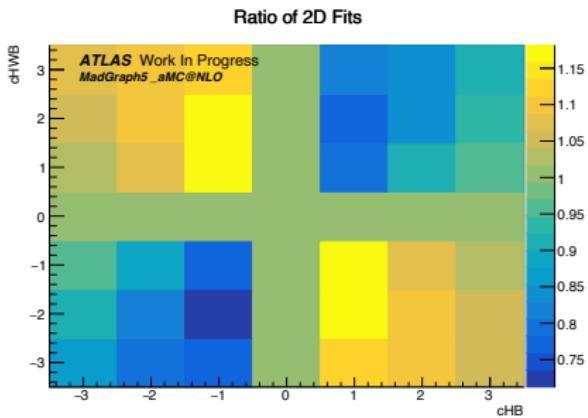
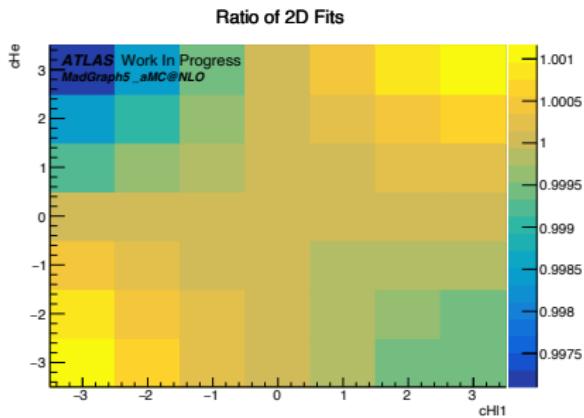
- Acceptance for two couplings is approximated by the ratio of the 2D fitting functions of the fiducial and total cross section:



# Impact of Mixed Terms



- Taking the ratio of the acceptance approximations with and without the mixed terms shows the mixed terms can contribute up to  $\sim 15\%$  to the overall acceptance:



# Conclusions



- Effect of the Standard Model Effective Field Theory on the  $H \rightarrow 4\ell$  decay channel was investigated, with a focus on calculating the acceptance corrections
- For some Wilson coefficients, the contribution of the quadratic terms to the acceptance is large
- To include the quadratic terms when determining the acceptance, one also must include the mixed terms
- The mixed terms are largest for the Wilson Coefficients associated with the coupling of the Higgs boson to the vector bosons and these terms can contribute up to  $\sim 15\%$  of the overall acceptance



# BACKUP

# SMEFT Operators - $H \rightarrow 4l$



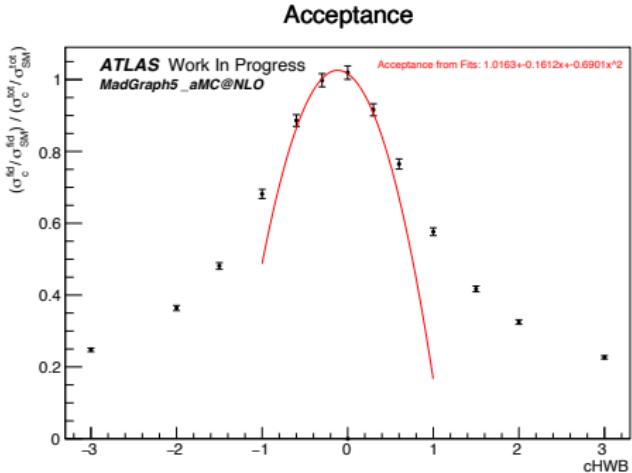
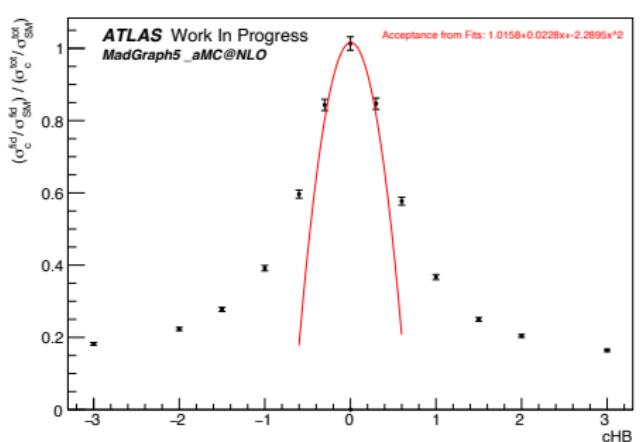
| Wilson Coefficient | Operator  |
|--------------------|---|
| $c_{Hbox}$         | $(H^\dagger H) \square (H^\dagger H)$   |
| $c_{HDD}$          | $(H^\dagger D^\mu H)^* (H^\dagger D_\mu H)$                                     |
| $c_{HB}$           | $H^\dagger H B_{\mu\nu} B^{\mu\nu}$   |
| $c_{HW}$           | $H^\dagger H W_{\mu\nu}^I W^{I\mu\nu}$  |
| $c_{HWB}$          | $H^\dagger \tau^I H W_{\mu\nu}^I B^{\mu\nu}$                                    |
| $c_{Hl1}$          | $(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{l}_p \gamma^\mu l_r)$          |
| $c_{Hl3}$          | $(H^\dagger i \overleftrightarrow{D}_\mu^I H)(\bar{l}_p \tau^I \gamma^\mu l_r)$ |
| $c_{He}$           | $(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{e}_p \gamma^\mu e_r)$          |

# Acceptance - Full Taylor Expansion



$$\frac{A^{BSM}}{A^{SM}} = \frac{a_{fid} + b_{fid}c_i + c_{fid}c_i^2}{a_{tot} + b_{tot}c_i + c_{tot}c_i^2}$$
$$\approx a_{fid}a_{tot} + (a_{tot}b_{fid} - a_{fid}b_{tot})c_i + (a_{tot}c_{fid} - a_{fid}c_{tot} - b_{fid}b_{tot})c_i^2 + \dots$$

# Acceptance Parametrisation



Acceptance Parametrisation (Linear Approximation):

$$1 + 0.163c_{HWB} + 0.023c_{HB} - 0.161c_{HWB}$$

# Cross Sections

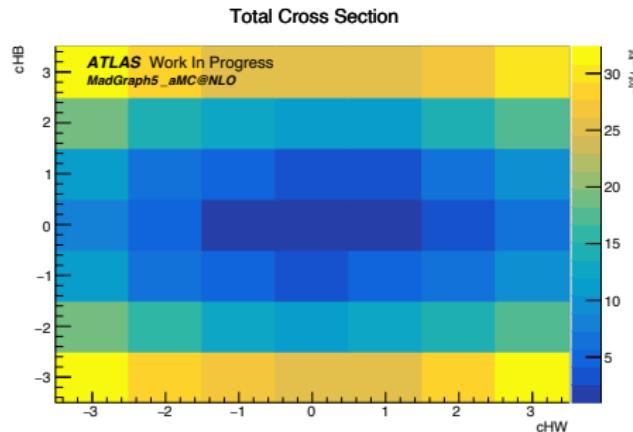


|                         | <b>Fiducial Fit:</b>                        | <b>Total Fit:</b>                           |
|-------------------------|---|---|
| <b>cH<sub>box</sub></b> | $0.997 + 0.122c_{Hbox} + 0.004(c_{Hbox})^2$ | $1.000 + 0.120c_{Hbox} + 0.004(c_{Hbox})^2$ |
| <b>cHe</b>              | $0.998 - 0.101c_{He} + 0.006(c_{He})^2$     | $1.000 - 0.102c_{He} + 0.006(c_{He})^2$     |
| <b>cH<sub>I1</sub></b>  | $0.0996 + 0.128c_{Hl1} + 0.007(c_{Hl1})^2$  | $1.000 + 0.127c_{Hl1} + 0.007(c_{Hl1})^2$   |
| <b>cH<sub>I3</sub></b>  | $0.998 - 0.236c_{Hl3} + 0.016(c_{Hl3})^2$   | $1.000 - 0.235c_{Hl3} + 0.016(c_{Hl3})^2$   |
| <b>cH<sub>DD</sub></b>  | $0.998 + 0.008c_{HDD} + 0.018(c_{HDD})^2$   | $1.000 + 0.005c_{HDD} + 0.019(c_{HDD})^2$   |
| <b>cH<sub>WB</sub></b>  | $1.017 + 0.019c_{HWB} + 0.101(c_{HWB})^2$   | $1.001 + 0.180c_{HWB} + 0.791(c_{HWB})^2$   |
| <b>cH<sub>W</sub></b>   | $1.014 - 0.037c_{HW} + 0.121(c_{HW})^2$     | $1.000 - 0.200c_{HW} + 0.752(c_{HW})^2$     |
| <b>cH<sub>B</sub></b>   | $1.015 - 0.089c_{HB} + 0.368(c_{HB})^2$     | $0.999 - 0.112c_{HB} + 2.657(c_{HB})^2$     |

Linear Approximation of the Acceptance:

$$1.029 + 0.002c_{Hbox} - 0.001c_{He} + 0.001c_{Hl1} - 0.001c_{Hl3} + 0.003c_{HDD} - \\ 0.161c_{HWB} + 0.163c_{HW} + 0.023c_{HB}$$

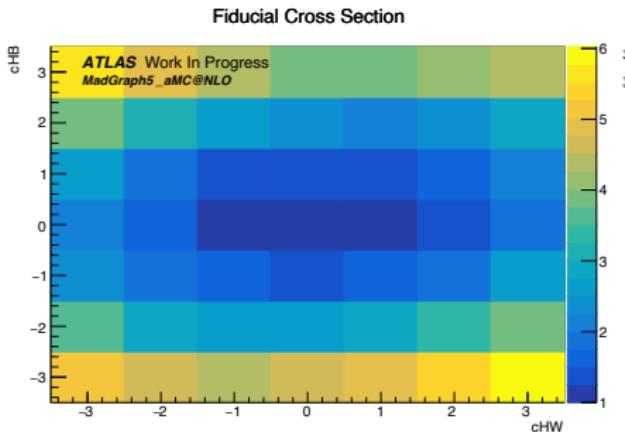
# 2D Cross Section - cHW, cHB



$$\begin{aligned} \text{2D Fit: } & 1.000 - 0.201x - 0.114y \\ & - 0.033xy + 0.752x^2 + 2.66y^2 \end{aligned}$$

Mixed term from 1D fits:

$$-0.031xy$$

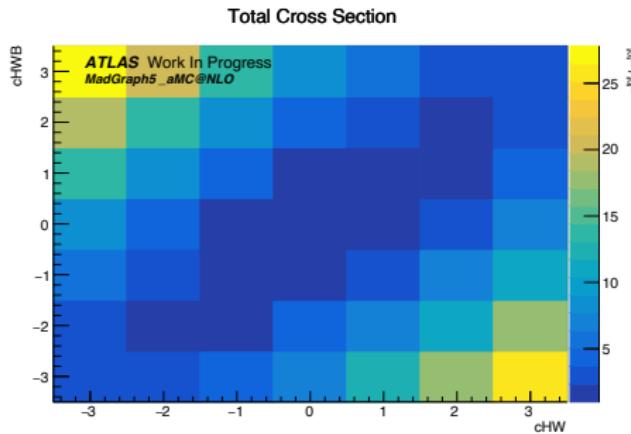


$$\begin{aligned} \text{2D Fit: } & 1.000 - 0.040x - 0.089y \\ & - 0.061xy + 0.118x^2 + 0.363y^2 \end{aligned}$$

Mixed term from 1D fits:

$$-0.058xy$$

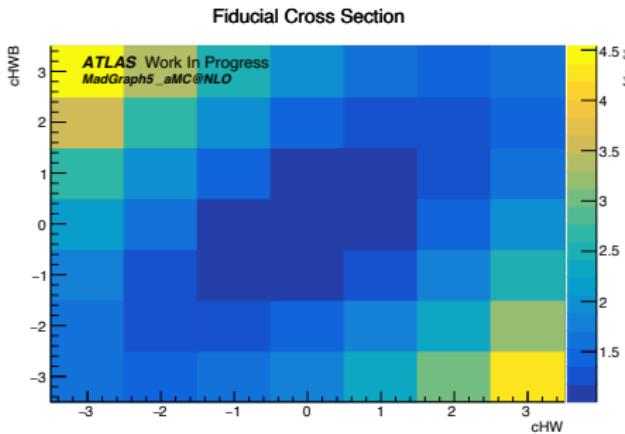
# 2D Cross Section - cHW, cHWB



$$\begin{aligned} \text{2D Fit: } & 1.000 - 0.199x + 0.180y \\ & -1.311xy + 0.751x^2 + 0.791y^2 \end{aligned}$$

Mixed term from 1D fits:

$$-1.309xy$$

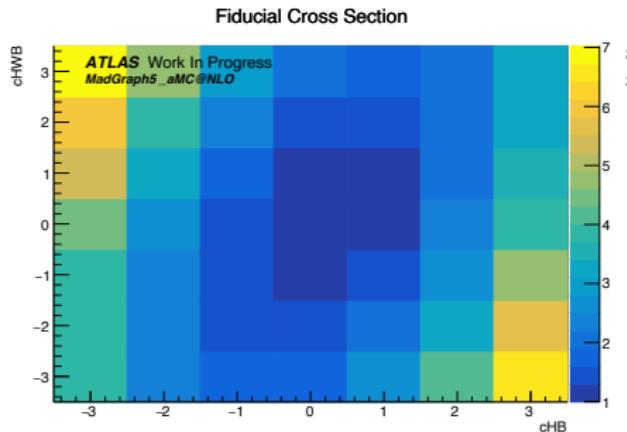
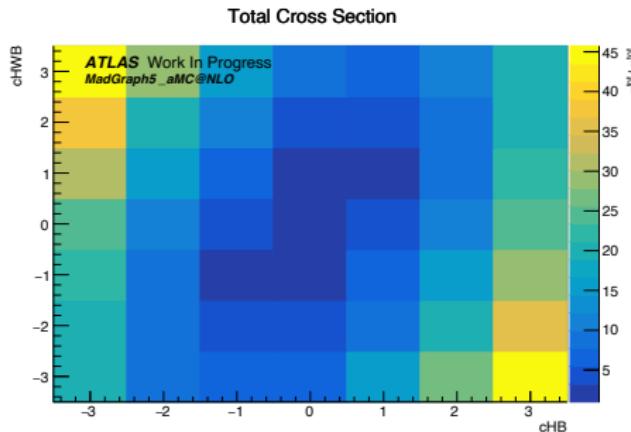


$$\begin{aligned} \text{2D Fit: } & 1.000 - 0.039x + 0.020y \\ & -0.154xy + 0.118x^2 + 0.101y^2 \end{aligned}$$

Mixed term from 1D fits:

$$-0.156xy$$

# 2D Cross Section - cHB, cHWB



$$\begin{aligned} \text{2D Fit: } & 0.999 - 0.112x + 0.180y \\ & -1.426xy + 2.658x^2 + 0.791y^2 \end{aligned}$$

Mixed term from 1D fits:

$$-1.427xy$$

$$\begin{aligned} \text{2D Fit: } & 0.998 - 0.084x + 0.020y \\ & -0.186xy + 0.364x^2 + 0.100y^2 \end{aligned}$$

Mixed term from 1D fits:

$$-0.200xy$$

# 2D Acceptance

