

$W^\mp H^\pm$ production and CP asymmetry at the LHC

DAO Thi Nhung

Based on

Wolfgang Hollik, Le Duc Ninh, D.T.N, Phys.Rev.D38:075003



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IMPRS colloquium

13th May 2011

1 Overview

- Theoretical framework
- Charged Higgs searches at colliders

2 $pp \rightarrow H^\pm W^\mp$

- The lowest order
- The effective bottom-Higgs couplings
- Neutral Higgs propagator resummation
- NLO corrections to $b\bar{b} \rightarrow H^\pm W^\mp$
- Numerical results

3 Conclusions

Where charged Higgs bosons come from?

- What is the mechanism to generate particle masses? The Higgs mechanism is confirmed when Higgs bosons are found.
- No theoretical and experimental constraint on the number of Higgs bosons

$$\text{SM: one Higgs doublets } \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} \xrightarrow{EWSB} h^0$$

- Two-Higgs-Doublet-Model (2HDM) is the simplest extension of the SM

$$\begin{pmatrix} H_1^0 \\ H_1^- \end{pmatrix} \text{ and } \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix} \xrightarrow{EWSB} h^0, H^0 \text{ (CP even), } A^0 \text{ (CP odd), } H^\pm$$

- Type I: fermions couple to one doublet \rightarrow No FCNC at tree-level
- Type II: down-type fermions couple to H_1 , up-type fermions to H_2 (required by the MSSM) \rightarrow No FCNC at tree-level
- Type III: fermions couple to both H_1 and H_2

$H^\pm \rightarrow$ clear signal of physics beyond the SM

compare to 2HDM type II:

- Two Higgs doublets with opposite hypercharge are required (analytic superpotential, anomaly free)
- Quartic coupling in Higgs potential is fixed

$$V = m_1^2 H_{ui}^* H_{ui} + m_2^2 H_{di}^* H_{di} + \epsilon^{ij} (m_{12}^2 H_{ui} H_{dj} + \text{H.c.}) \\ + \frac{g_1^2 + g_2^2}{8} (H_{ui}^* H_{ui} - H_{di}^* H_{di})^2 + \frac{g_2^2}{2} |H_{ui}^* H_{di}|^2$$

- Predict a light neutral Higgs boson: $m_{h^0} < 140$ GeV
- Number of Higgs-sector parameters are reduced

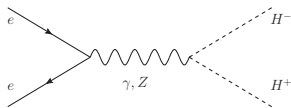
$$M_{H^\pm} (M_{A^0}), \tan \beta = \frac{v_2}{v_1}$$

other good points of the MSSM: solve hierarchy problem, unification, darkmatter candidate, ...

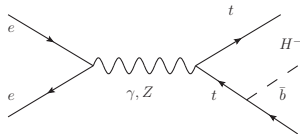
e^-e^+ colliders (LEP, future ILC,...)

- Two main production processes

1) $e^-e^+ \rightarrow H^-H^+$



2) $e^-e^+ \rightarrow H^-t\bar{b}$



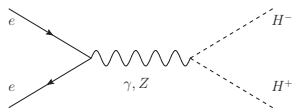
- subsequence decays:

- $M_{H^\pm} < m_t - m_b$: $H^- \rightarrow \tau\bar{\nu}_\tau$, $H^- \rightarrow \bar{c}s$
- $M_{H^\pm} > m_t + m_b$: $H^- \rightarrow \bar{t}b$, $H^- \rightarrow h^0/AW$

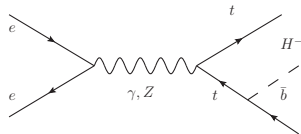
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LEP (192-209 GeV) analysis based on process 1):

- $M_{H^\pm} \geq 78.6$ GeV at 95% C.L for general 2HDM
- within MSSM, $M_{H^\pm}^2 = M_A^2 + M_W^2$, $M_A \geq 93.4$ GeV
 $\rightarrow M_{H^\pm} \geq 120$ GeV

Hadron colliders (Tevatron, LHC)

■ Production processes

- 1 $pp \rightarrow H^- t$ [Plehn, Shou, M. Beccaria, Elber, Dittmaier]
largest production rate
- 2 $pp \rightarrow H^\pm W^\mp$ [Kniehl, O. Brein, Hollik, Gao, Rauch, Yang]
- 3 $pp \rightarrow H^- H^+$ [Eichten, Plehn, Hollik, Kniehl]

Hadron colliders (Tevatron, LHC)

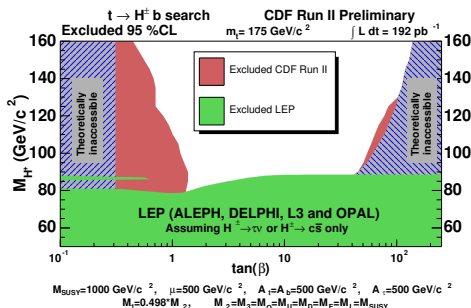
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CDF analysis based on:

- $gg \rightarrow t\bar{t} \rightarrow (H^+ \bar{b}) \bar{t}$
- $M_{H^\pm} < m_t - m_b$
- important coupling Htb

Phys.Rev.Lett.96:042003



Many studies are done in the **real MSSM**

- $gg \rightarrow H^\pm W^\mp$: loop induced

[Barrientos Bendezu and Kniehl; Brein, Hollik and Kanemura]

- $b\bar{b} \rightarrow H^\pm W^\mp$: calculated at NLO

- SM-QCD corrections [Hollik and Zhu; Gao, C.S. Li and Z. Li]
- SUSY-QCD corrections [Zhao, C.S. Li and Z. Li; Rauch]
- Yukawa corrections [Yang, C.S. Li, Jin and Zhu]
- **Full EW corrections: missing**

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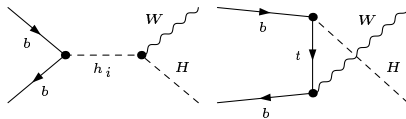
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Our work:

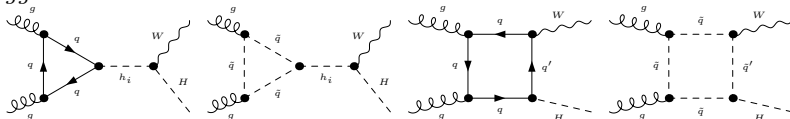
- compute in general **complex MSSM**
- **full EW corrections** to $b\bar{b} \rightarrow H^\pm W^\mp$, consistently combine with QCD corrections,
- CP violating effects
- use **the effective bottom-Higgs couplings**
- use **the neutral Higgs propagator resummation**

The lowest order: $b\bar{b} \rightarrow H^\pm W^\mp, gg \rightarrow H^\pm W^\mp$

■ $b\bar{b} \rightarrow H^\pm W^\mp$



■ $gg \rightarrow H^\pm W^\mp$



Importances

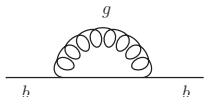
■ bottom-Higgs couplings:

$$\lambda_{b\bar{b}h/H/A} \propto \frac{m_b}{\cos\beta}, \quad \lambda_{b\bar{t}H^\pm} \propto \left(\frac{m_t}{\tan\beta} P_L + m_b \tan\beta P_R \right)$$

■ neutral Higgs propagator: $\frac{i}{p^2 - m_{h^2}}, m_h^2?$

The effective bottom-Higgs couplings

- Leading contribution $\alpha_s^n \ln^n(m_b/\mu_R)$ from SM-QCD are resummed into running $m_b^{\overline{\text{DR}}}(\mu_R)$

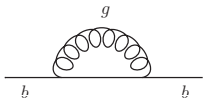


$$m_b^{\overline{\text{DR}}}(\mu_R) = m_b \left[1 - \frac{\alpha_s}{3\pi} (5 - 6 \ln \frac{m_b}{\mu_R}) \right]$$

- SM-QCD corrections do not depend on $\ln m_b$
- ensure convergent property of perturbative expansion

The effective bottom-Higgs couplings

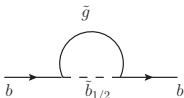
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- Leading contribution $\Delta m_b \propto \tan \beta$ from SUSY corrections are resummed into bottom-Higgs couplings $\lambda_{bbh} \propto \frac{m_b}{1 + \Delta m_b}$

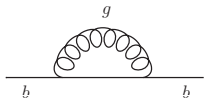


$$\Delta m_b^{SQCD} = \frac{2\alpha_s}{3\pi} M_3^* \mu^* \tan \beta I(M_{\tilde{b}_1}^2, M_{\tilde{b}_2}^2, M_{\tilde{g}}^2)$$

$$I(a, b, c) = -\frac{ab \ln \frac{a}{b} + bc \ln \frac{b}{c} + ca \ln \frac{c}{a}}{(a-b)(b-c)(c-a)}$$

The effective bottom-Higgs couplings

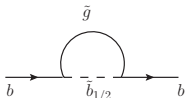
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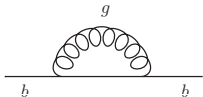
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- if Δm_b close to -1 , λ can be very large

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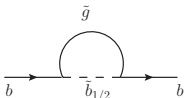
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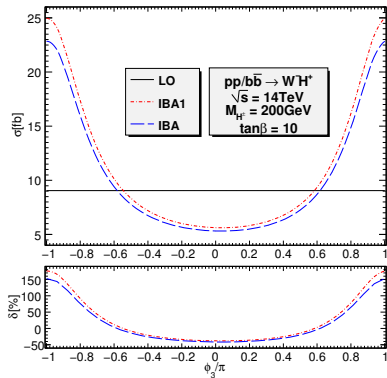
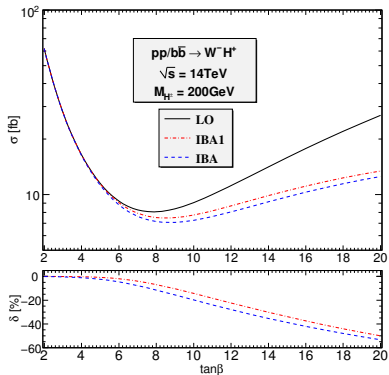
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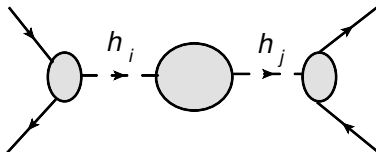
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- Δm_b in general is complex
- if Δm_b close to -1 , λ can be very large
- To avoid double counting, we have to subtract the Δm_b -related corrections in one-loop calculation



- $\delta = (\sigma_{\text{IBA}} - \sigma_{\text{LO}})/\sigma_{\text{LO}}$
- 50% at $\tan\beta = 20$
- even 150% at $\phi_3 = \pm\pi$



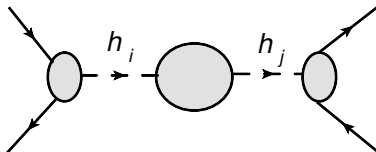
$$\mathcal{A}(p^2) = \sum_{ij} \Gamma_i \Delta_{ij}(p^2) \Gamma_j, \quad i = h, H, A,$$

$\Gamma_{i,j}$ are one-particle irreducible Higgs vertices.

$$\Delta(p^2) = i[p^2 - \mathcal{M}(p^2)]^{-1},$$

$$\mathcal{M}(p^2) = \begin{pmatrix} m_h^2 - \hat{\Sigma}_{hh}(p^2) & -\hat{\Sigma}_{hH}(p^2) & -\hat{\Sigma}_{hA}(p^2) \\ -\hat{\Sigma}_{hH}(p^2) & m_H^2 - \hat{\Sigma}_{HH}(p^2) & -\hat{\Sigma}_{HA}(p^2) \\ -\hat{\Sigma}_{hA}(p^2) & -\hat{\Sigma}_{HA}(p^2) & m_A^2 - \hat{\Sigma}_{AA}(p^2) \end{pmatrix}.$$

- m_i ($i = h, H, A$) are the lowest-order Higgs-boson masses
- $\hat{\Sigma}_{ij}$ the renormalized self-energies, $\hat{\Sigma}_{h/H/A}$ vanish in real MSSM,
- Loop-corrected masses are obtained by diagonalizing $\mathcal{M}(p^2)$



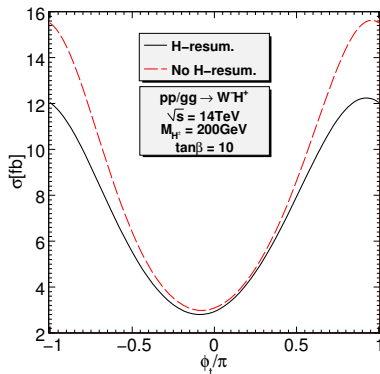
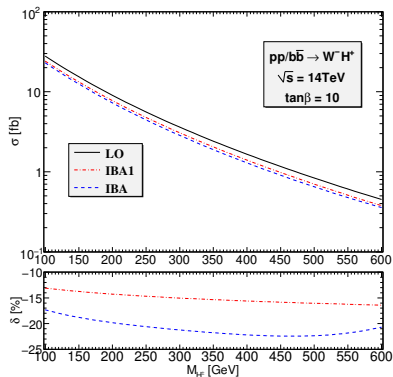
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- To avoid double counting, we have to discard all $h_i h_j$ self-energies diagrams in NLO EW corrections

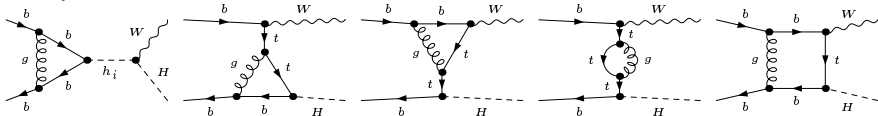


- less than 10% in subprocesses $b\bar{b} \rightarrow W^{\mp} H^{\pm}$
- large effects (30% at $\phi_t = \pm\pi$) in subprocesses $gg \rightarrow W^{\mp} H^{\pm}$

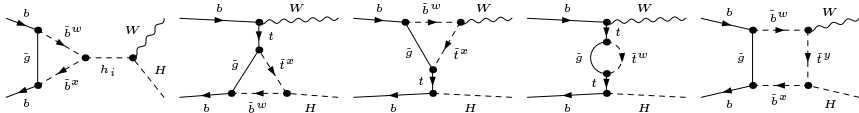
NLO corrections to $b\bar{b} \rightarrow H^\pm W^\mp$

Virtual contributions:

SM-QCD



SUSY-QCD



EW part consists of 352 self-energies + 440 triangles + 153 boxes

Real contributions:



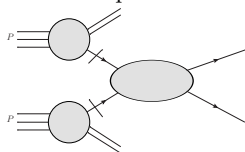
Gluon induce, photon induce:



Divergencies:

- **UV divergencies** are cured by renormalization,
 - OS-scheme for W-boson, M_{H^\pm} , m_t
 - DR-scheme for $\tan\beta$, m_b , H^\pm wave function
- **IR divergencies** are cancelled between the virtual part and the gluon and photon radiations
- **Mass singularities** of the type $\alpha_s \ln(m_b)$ and $\alpha \ln(m_b)$ are absorbed into (anti-) bottom PDF
- In the gluon- and photon-induced processes, **the top quark can be on-shell** then $t \rightarrow Wb$ ($t \rightarrow Hb$). This contribution belongs to tH (tW) production so it needs to be subtracted in a gauge-invariant way.

Drell-Yan process



$$\sigma^{pp} = \sum_{i,j} \int dx_1 dx_2 [F_i^p(x_1, \mu_F) F_j^p(x_2, \mu_F) \hat{\sigma}^{ij}(\mu_R) + i \leftrightarrow j],$$

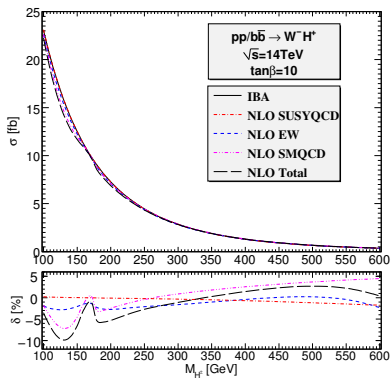
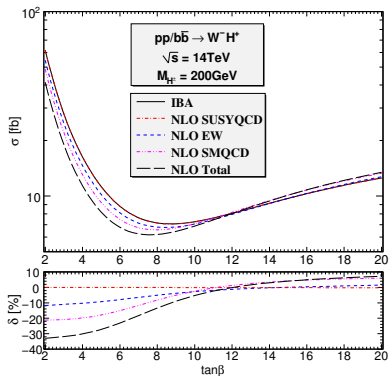
PDF: [MRST2004qed](#)

CP asymmetry

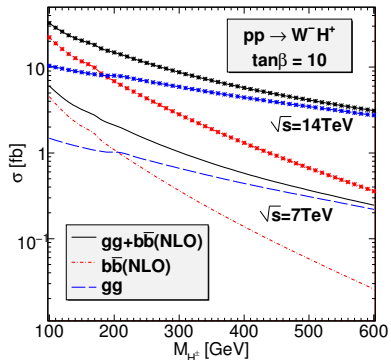
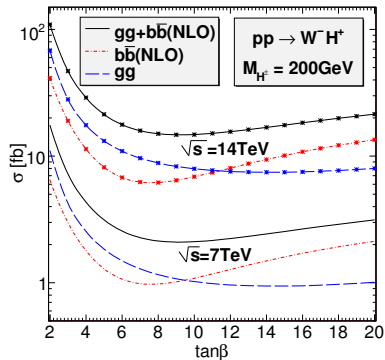
$$\delta_{pp}^{\text{CP violation}} = \frac{\sigma(pp \rightarrow W^- H^+) - \sigma(pp \rightarrow W^+ H^-)}{\sigma(pp \rightarrow W^- H^+) + \sigma(pp \rightarrow W^+ H^-)}.$$

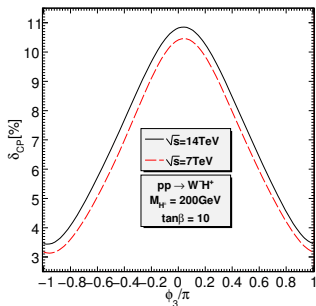
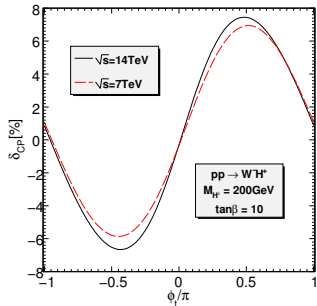
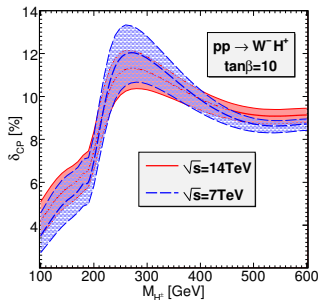
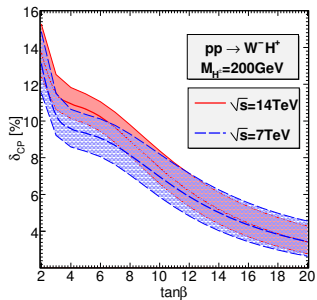
Use [CPX scenario](#) for numerical studies

NLO corrections to $b\bar{b} \rightarrow H^\pm W^\mp$



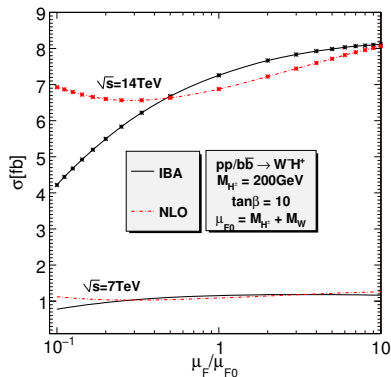
Total hadronic cross section





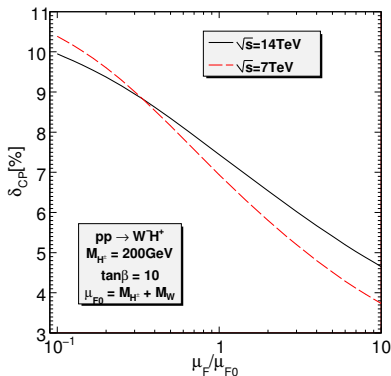
$$\delta = [|\sigma(\mu_{F0}/2) - \sigma(\mu_{F0})| + |\sigma(2\mu_{F0}) - \sigma(\mu_{F0})|]/\sigma(\mu_{F0})$$

$$\mu_R = \mu_F, \mu_{F0} = M_W + M_{H^\pm}$$



$$\text{■ NLO: } \delta = 9\%(9\%)$$

$$\text{■ IBA: } \delta = 14\%(7\%)$$



$$\text{■ 14 TeV } \delta = 24\%$$

$$\text{■ 7 TeV: } \delta = 34\%$$

- $pp \rightarrow W^\mp H^\pm$ have been studied in general **complex MSSM**
- NLO EW, QCD corrections to $b\bar{b} \rightarrow W^\mp H^\pm$ are important for precision searches
- NLO corrections significantly reduce scale dependence
- **Large CP asymmetry** is mainly induced from gg fusion
- **The effective bottom-Higgs couplings** have significant effects on $b\bar{b}$ annihilation
- **The Higgs mixing resummation** gives large effects on gg fusion, and CP asymmetry
- Production rates and CP asymmetry strongly depend on **$\tan \beta, M_{H^\pm}, \phi_t, \phi_3$**

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THANK YOU FOR YOUR ATTENTION