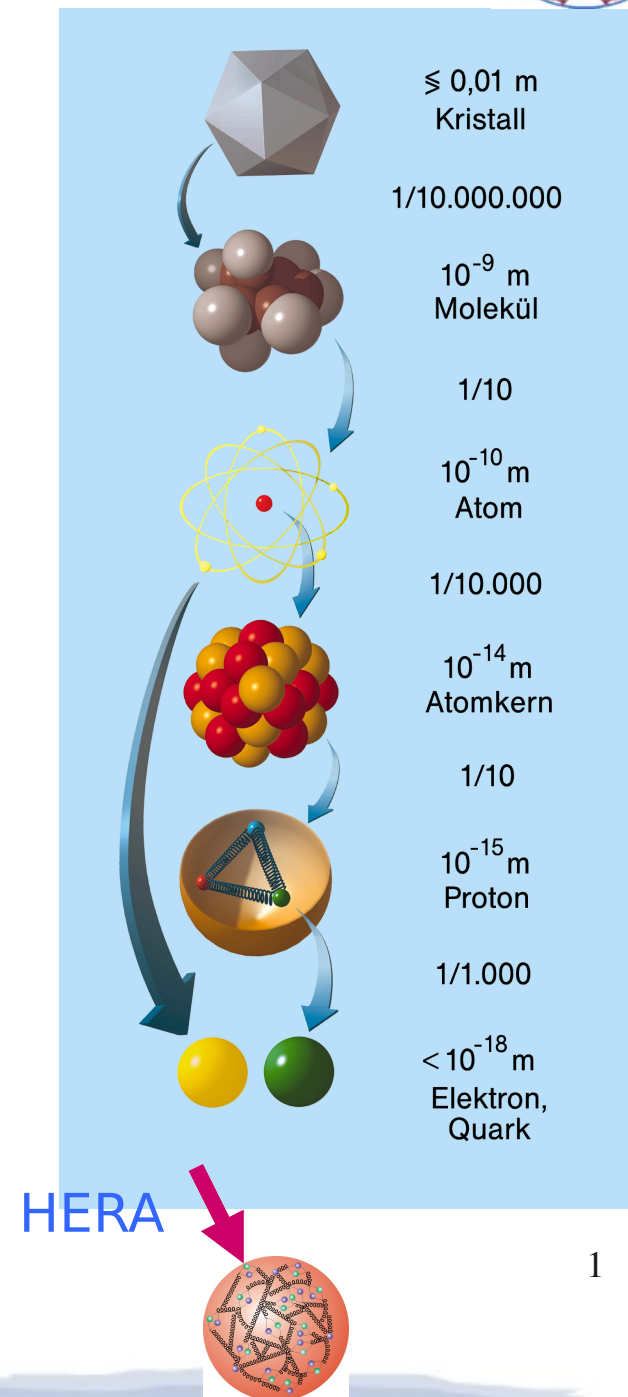


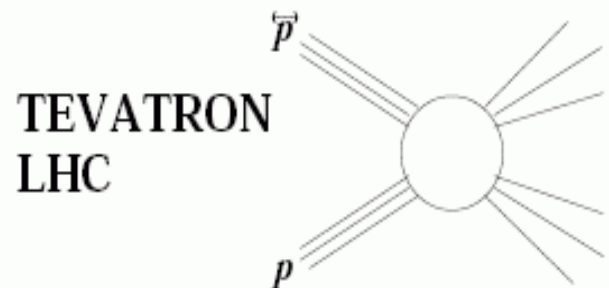
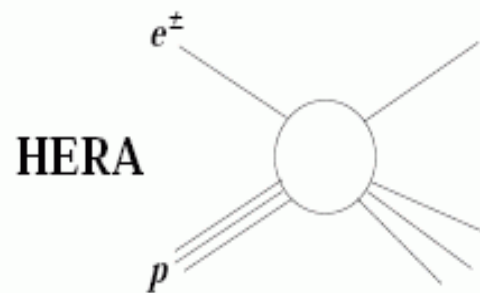
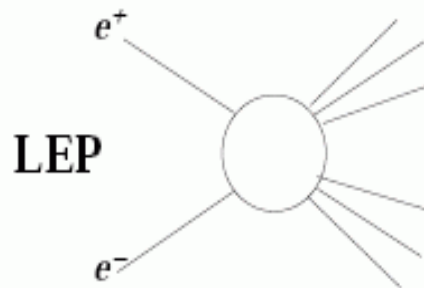
Study of NC cross sections using Zeus detector at HERA

Ritu Aggarwal
Punjab Uni. India / MPI, Munich

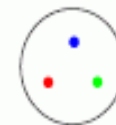
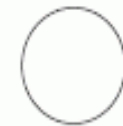


Motivation : What's inside proton?

Proton Models



proton



partons

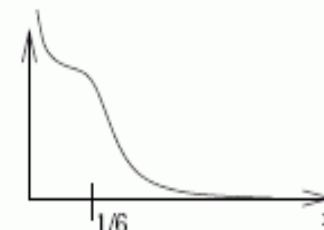
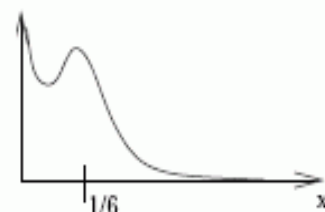
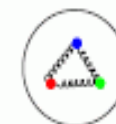
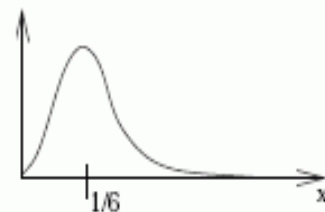
quark

anti quark

gluon



x = momentum fraction
of proton constituents



increasing resolution

Deep Inelastic Scattering

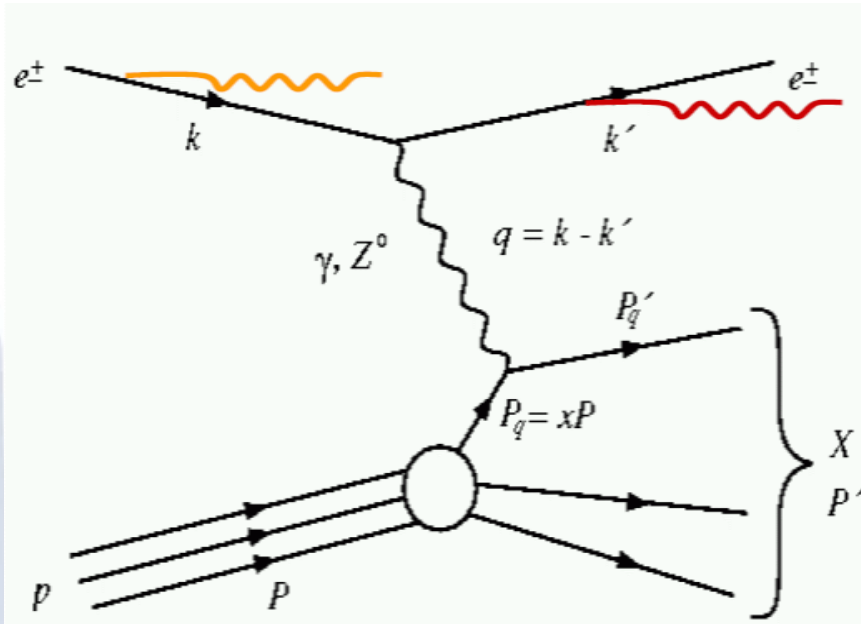
DIS cross-section can be described by :-

Q^2 : Four momentum transfer
(probing power)

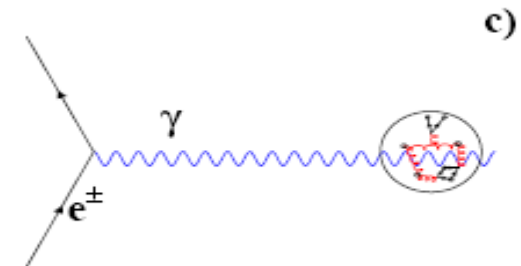
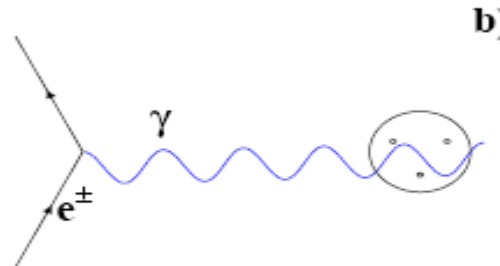
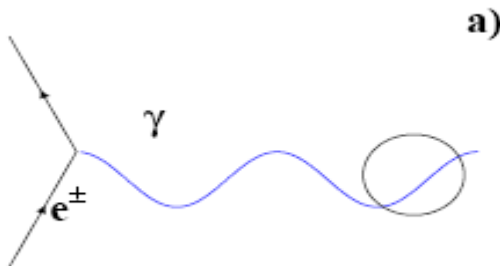
x : Bjorken Scaling variable
(momentum fraction of struck quark)

y : inelasticity

$\sqrt{s}$ = center of mass energy



$$\Delta p \cdot \Delta x \approx \hbar \Leftrightarrow \sqrt{Q^2} \approx \frac{\hbar}{\lambda}$$



DIS Cross-sections and Structure functions

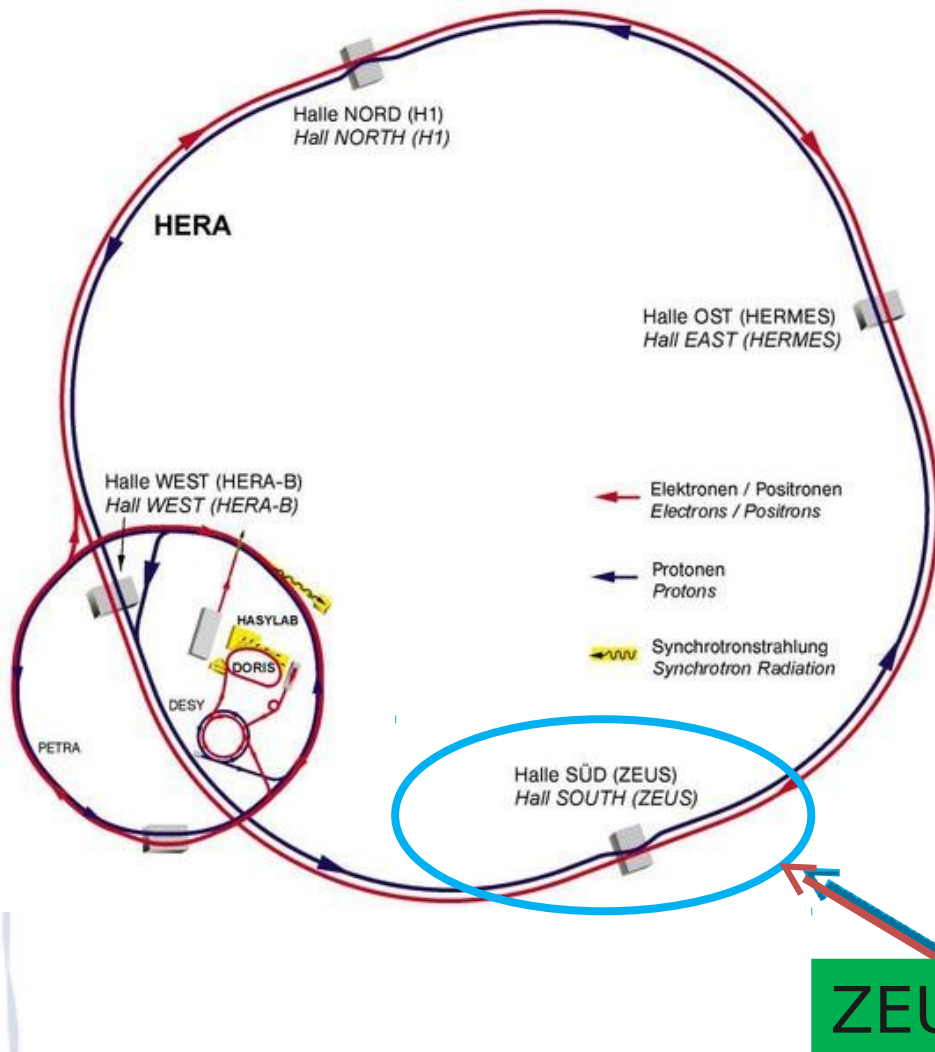
$$\frac{d^2\sigma(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left[Y_+ F_2(x, Q^2) \mp Y_- xF_3(x, Q^2) - y^2 F_L(x, Q^2) \right]$$

$$2xF_1^{NC}(x, Q^2) - F_2^{NC}(x, Q^2) = F_L^{NC}(x, Q^2)$$

$$\text{Where } Y_\pm = 1 \pm (1-y)^2$$

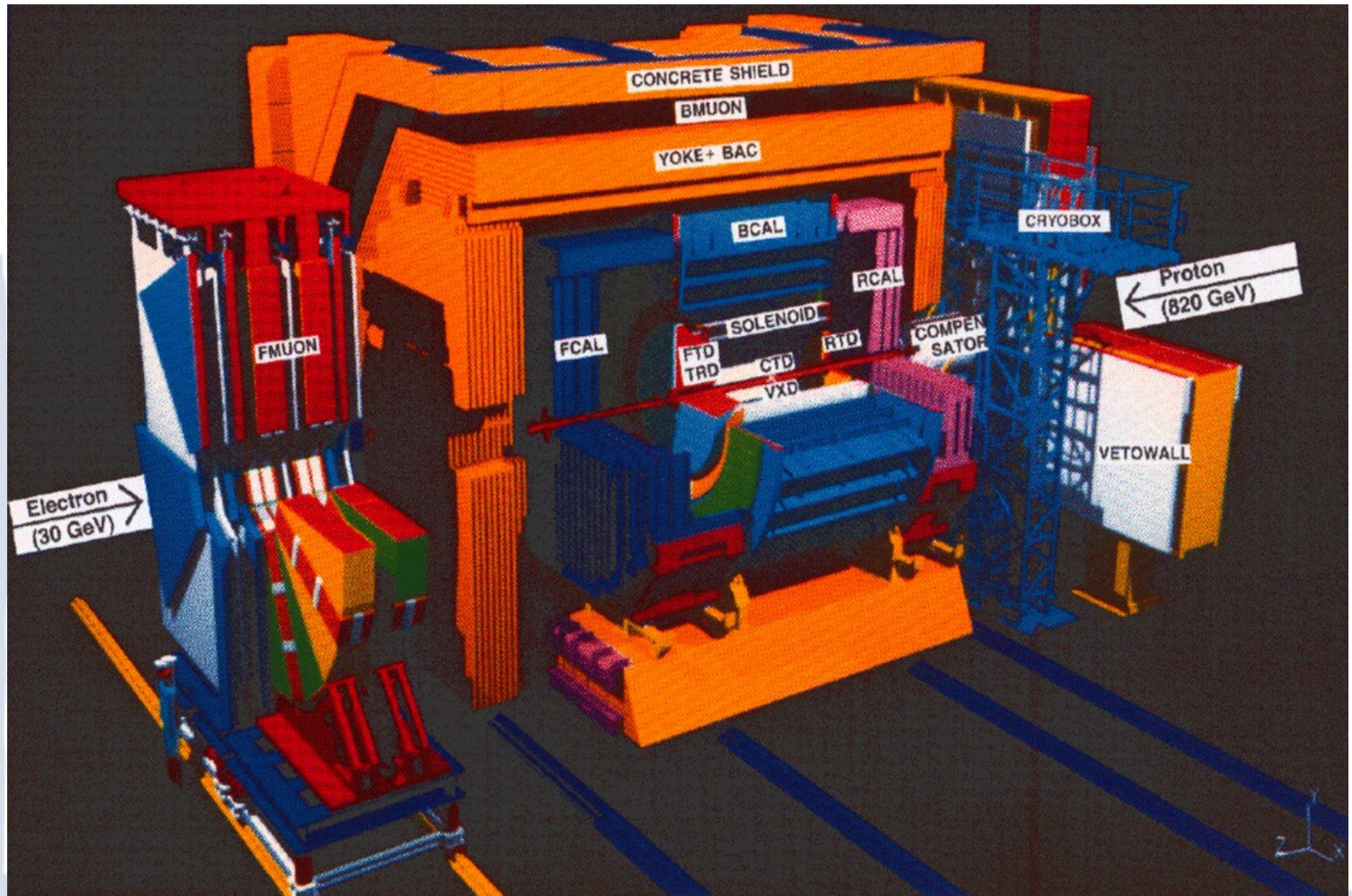
- $2xF_1^{NC}(x, Q^2)^2$ proportional to the transverse component of cross-section in which **transverse boson is exchanged**.
- $F_2^{NC}(x, Q^2)$ includes cross-section of **both longitudinal and transversely polarized boson**.
- $xF_3^{NC}(x, Q^2)$ contains **parity violating part of cross-section** which is negligible at low Q^2 .

HERA (Hadron Electron Ring Accelerator)

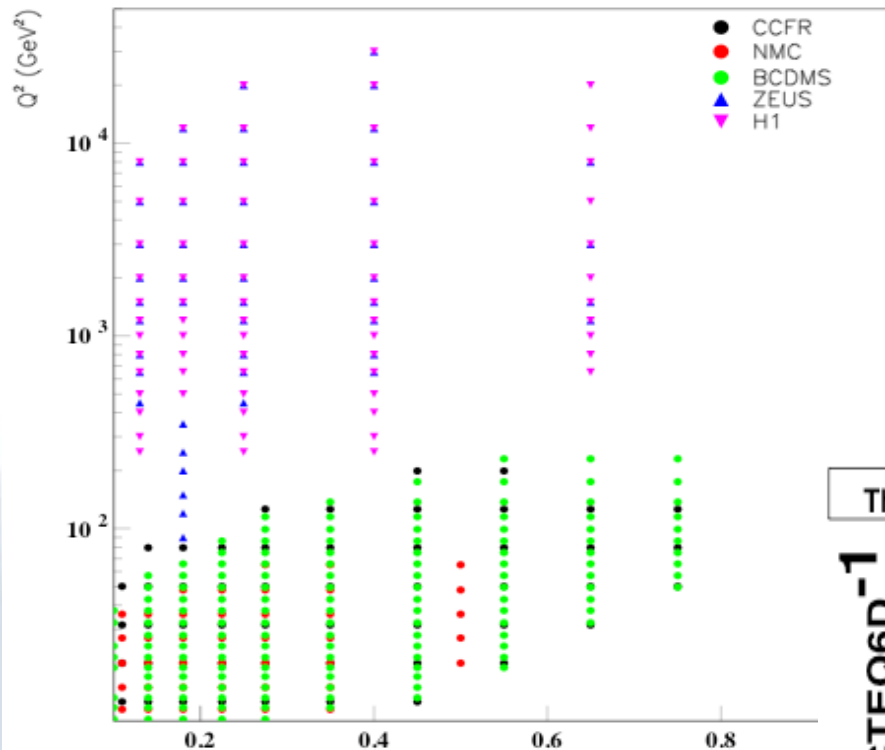


- Circumference 6.3 Km
- Electron Beam Energy **27.5 GeV**
- Different Proton Beam Energy for different time periods of running (**920, 460, 575**) **GeV** as (HER, LER, MER)
- Instantaneous luminosity $10^{32} \text{ cm}^{-2}\text{sec}^{-1}$
- Storage capacity of **210 bunches**
- Bunch spacing of **96 ns**

ZEUS Detector



Motivation for high-x cross sections

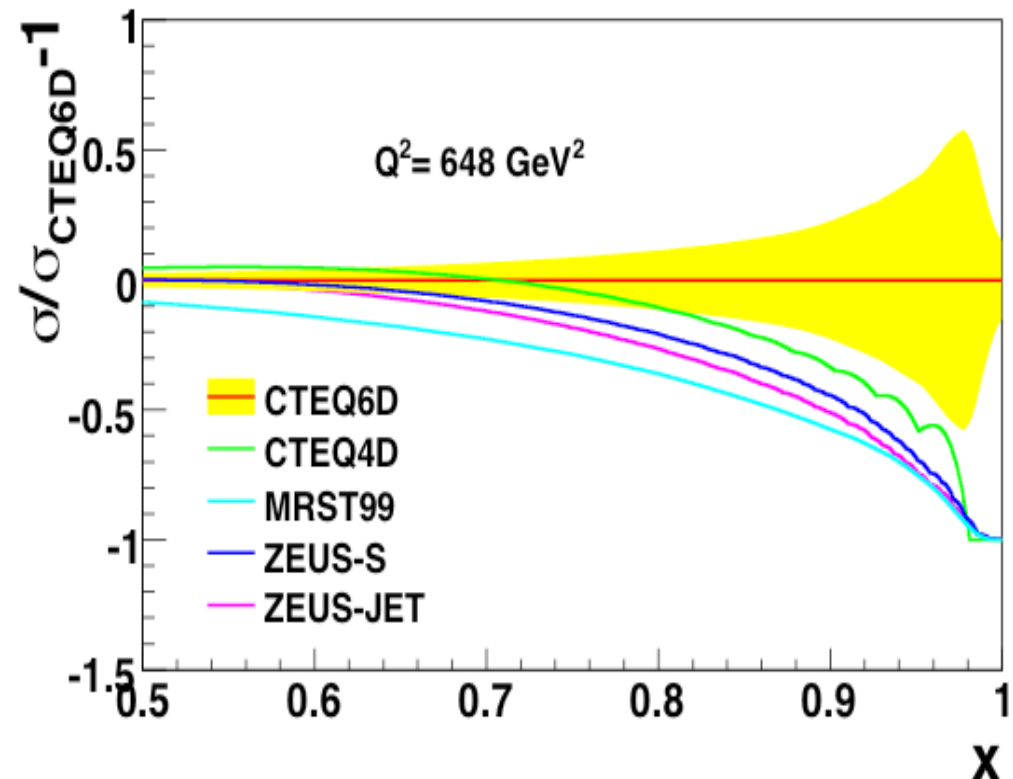


- The PDF's are poorly determined at high- x .
- parametrization $xq \propto (1-x)^\eta$.

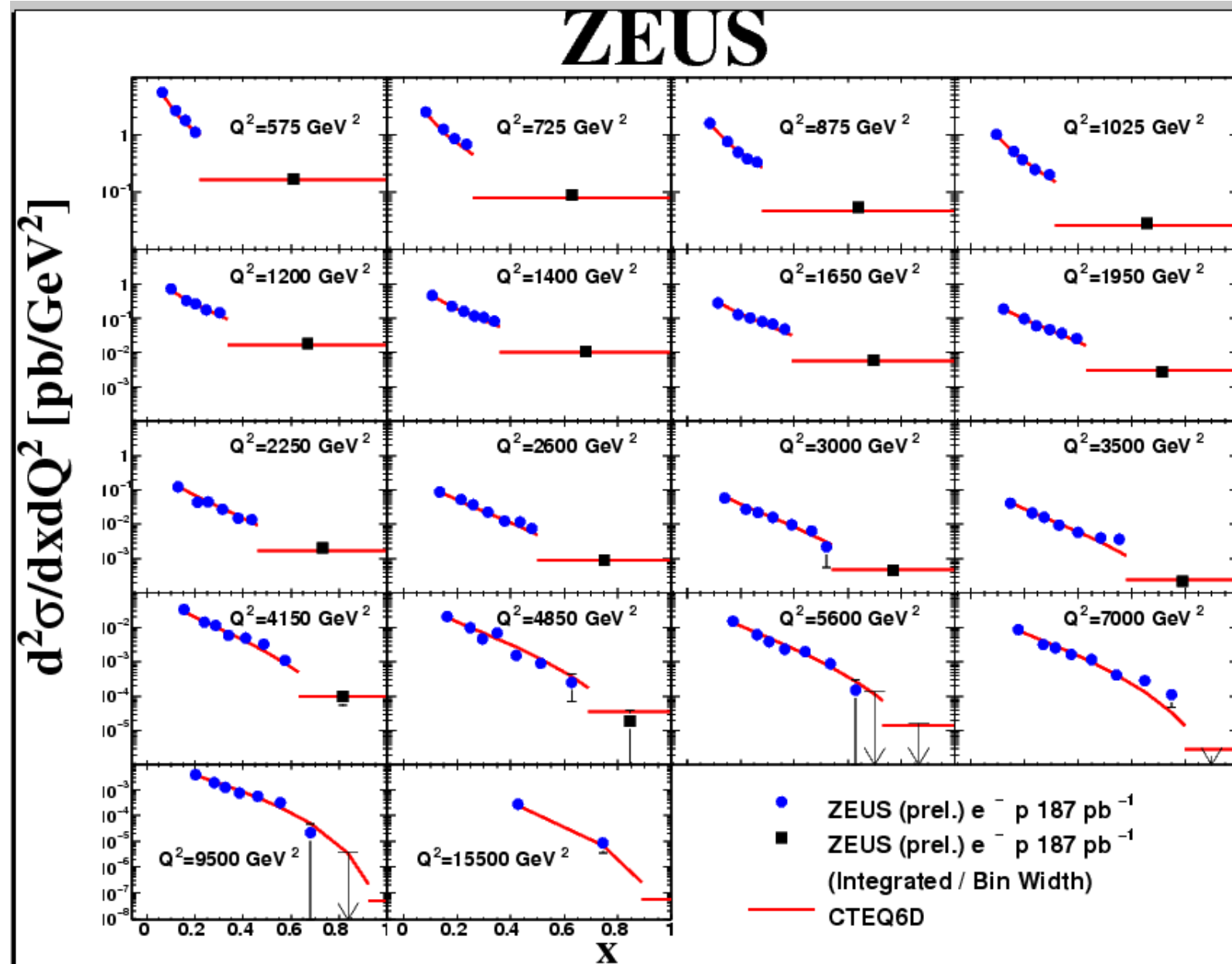
BCDMS has measured F_2
up to $x=0.75$

H1, ZEUS have measured
 F_2 up to $x=0.65$

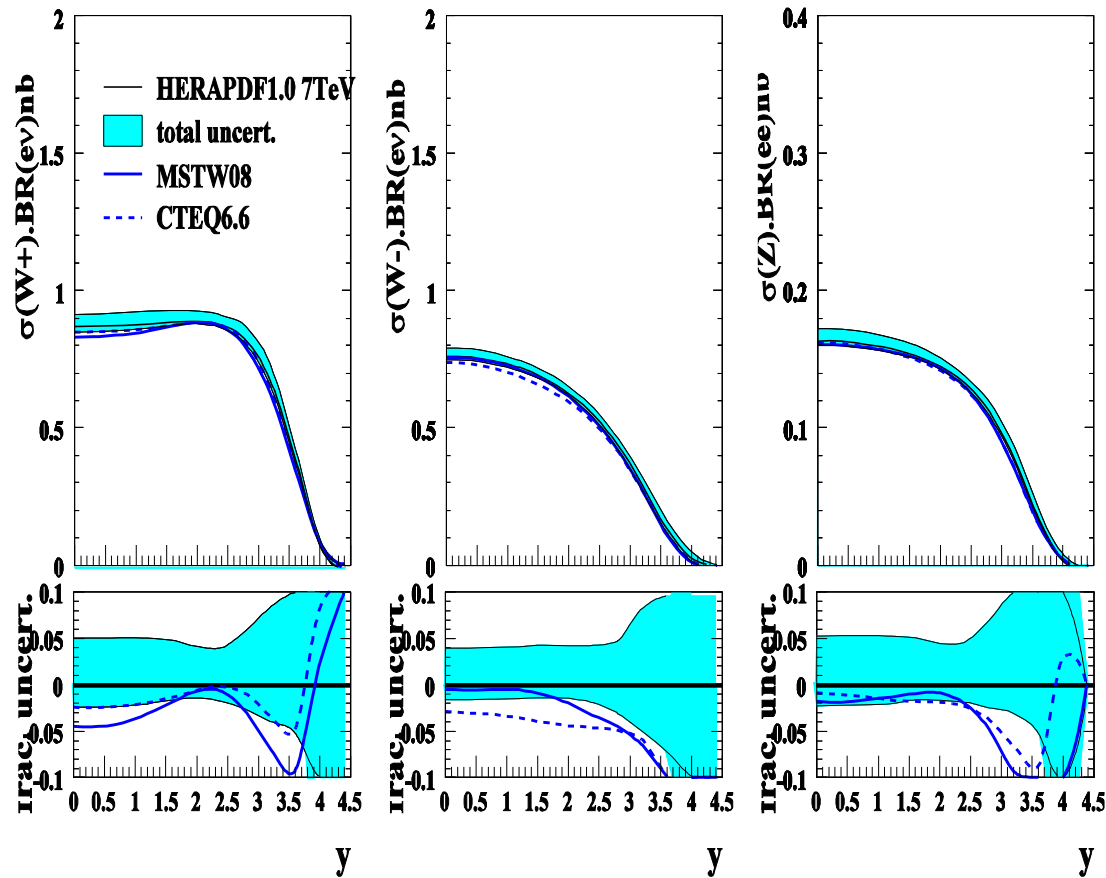
The fraction difference of $d^2\sigma/dxdQ^2$ to the CTEQ6D



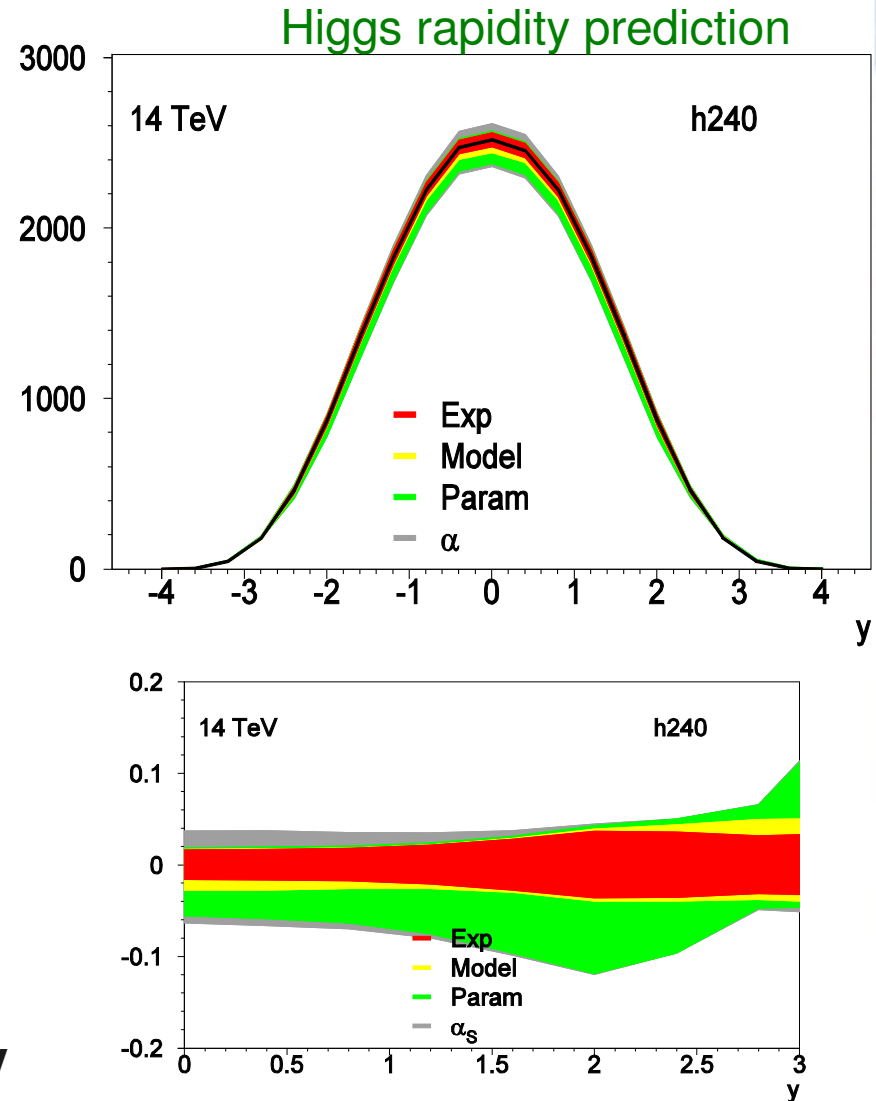
High-x NC e-p cross-section on the way to be fed to HERApdf's fit



Why talk about HERA physics in LHC scenario..?



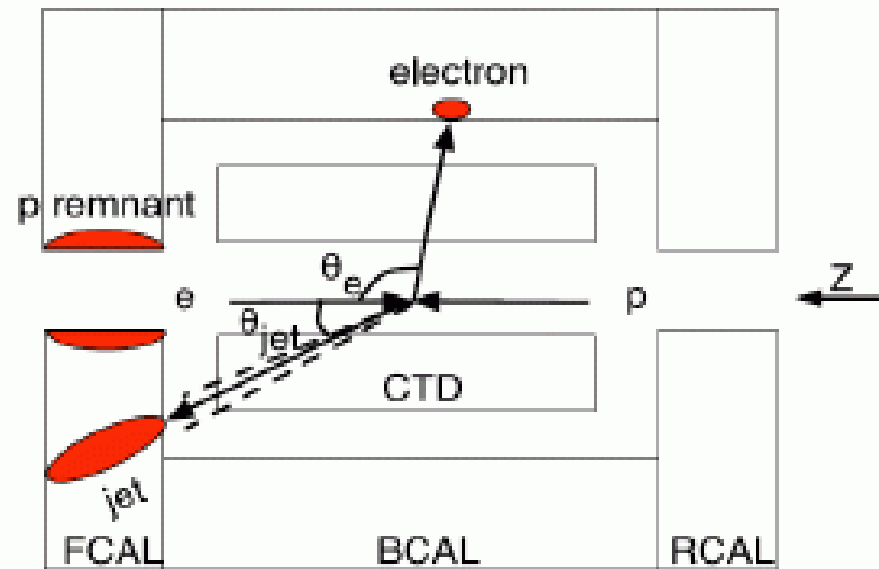
HERAPDF : W^+, W^-, Z^0 predictions at 7TeV



For more information :

https://www.desy.de/h1zeus/combined_results/benchmark/herapdf1.0.html

My focus : High-x cross section with Kinematic fit

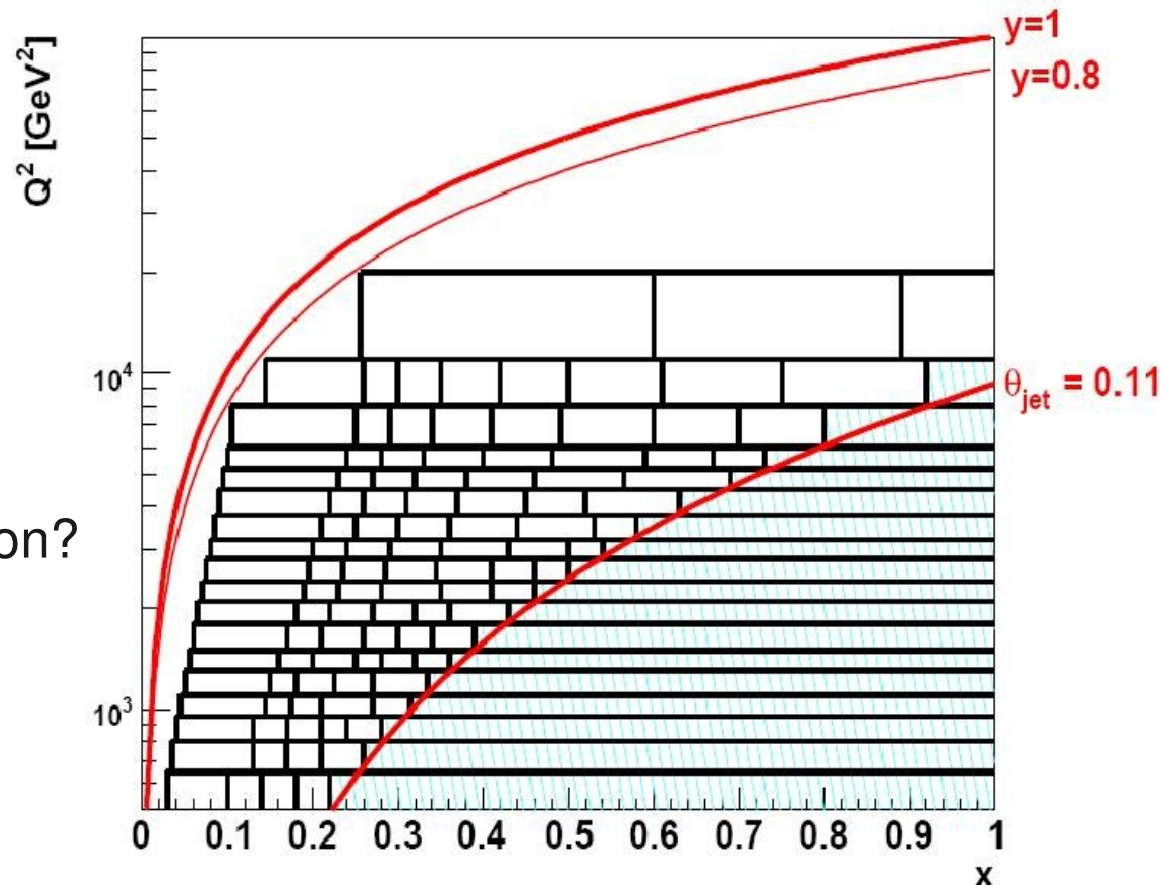


- › Motivation
- › Formulation & Parametrisation
- › Obtaining KF using BAT
- › Comparison to other methods
- › Summary

x, Q² binning of the events

$$\frac{d\sigma(X_i)}{dX} = \frac{N_{i,data}}{N_{rec,i}^{MC}} \frac{d\sigma^{SM,Born}}{dX}(X_i)$$

How to reconstruct
Kinematic variables
of an event
from the available information?



Motivation

Default Method (s)

Calculate x, y, Q^2 from

any of the two measured quantities $D = (E_e, \theta_e, E_j, \theta_{had})$

eg. Double Angle : (θ_e, θ_{had})

Electron Method : (E_e, θ_e)

Hadron Method : (E_j, θ_{had}) etc.

Results are expected to improve if we
use all the 4 quantities at a single time..

...Kinematic fitting

Principle : Use the best available information to find kinematic variables

Formulation

Aim : $\lambda = (x, y, E_\gamma)$ from measured quantities $D = (E_e, \theta_e, E_j, \theta_{had})$

Choose a set of values for λ .



From λ , calculate E, θ, F, γ .



Compare these Quantities to D and calculate a probability.

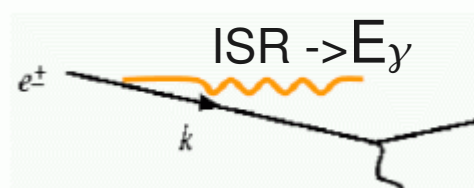
$$P(\lambda|D) \propto P(D|\lambda)P_o(\lambda)$$

Where $P(D|\lambda) = P(E_e|E)P(E_j|F)P(\theta_e|\theta)P(\theta_j|\gamma)$

and $P_o(\lambda) = (1-x)^5 f(E_\gamma/E_e) y^2/x^2$



Find **λ with highest probability**

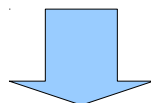


Where $f(a) = [1+(1-a)^2]/a$

Formulation...

The core of the method is to find $P(E_e|E)$, $P(E_j|F)$, $P(\theta_e|\theta)$, $P(\theta_{had}|\gamma)$

Simplest case : Expected for all of these is a **gaussian** of the measured quantities centered at the predicted quantities with some widths.



Next step

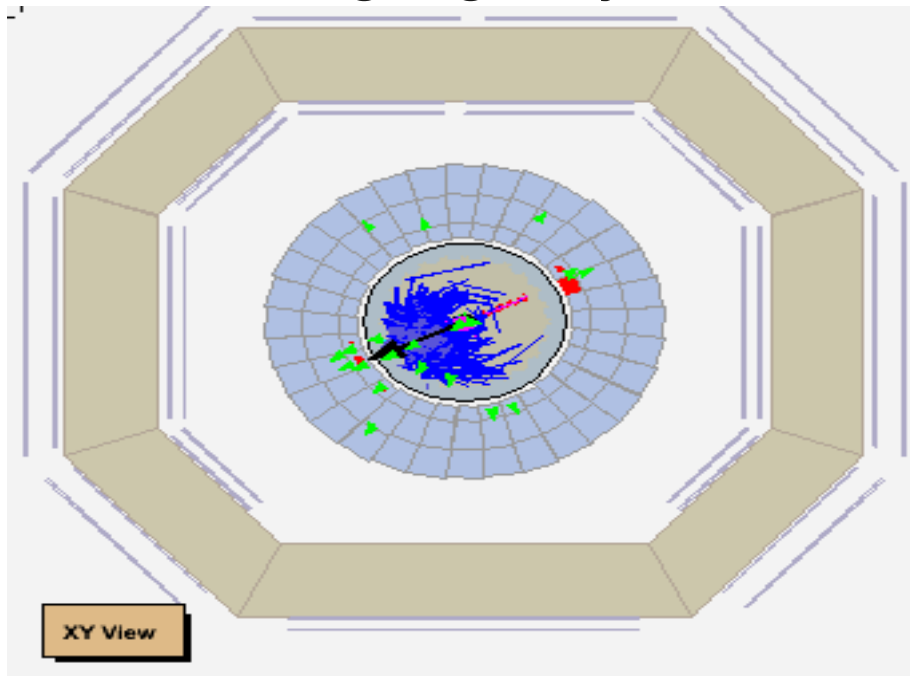
Find functional form of these probability distribution functions and **parametrize the parameters of the PDF** in terms of the predicted quantities.

Study is done on **MC** comparing the measured quantities to the true quantities..

Parametrization

two category of events

Single good jets

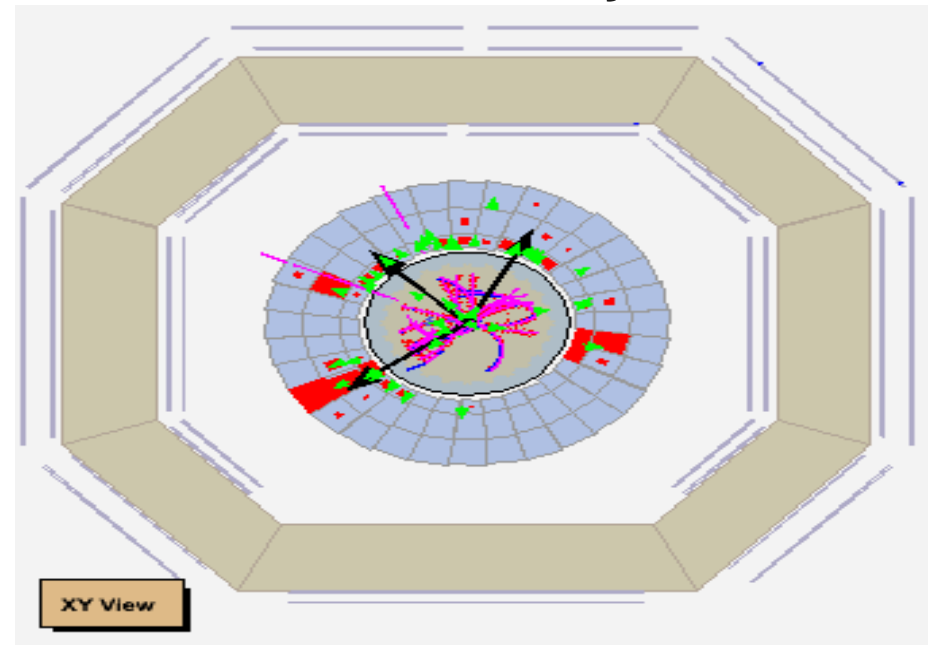


1 jet + Missing $E_{mpz} < 5 \text{ GeV}$

$P(E_e|E), P(E_j|F), P(\theta_e|\theta) \Rightarrow \text{Gaussian}$

$$P(\theta_{\text{had}}|\gamma) \frac{b^2}{f(\gamma)} = A/2 e^{\frac{b^2}{4c^2}} e^{b(\gamma-m)} \text{Erfc}(c(\gamma-m))$$

Hadron system



1 jet + Missing $E_{mpz} \geq 5 \text{ GeV}$
& multijet events

$P(E_e|E), P(E_j|F), P(\theta_e|\theta)$

$P(\theta_{\text{had}}|\gamma) \Rightarrow \text{Gaussian}$

Using BAT to get best λ

Choose a set of values for λ .



From λ , calculate E, F, θ, γ .



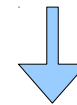
Compare these Quantities to D and calculate a probability.

$$P(\lambda|D) \propto P(D|\lambda)Po(\lambda)$$



Find λ with highest probability

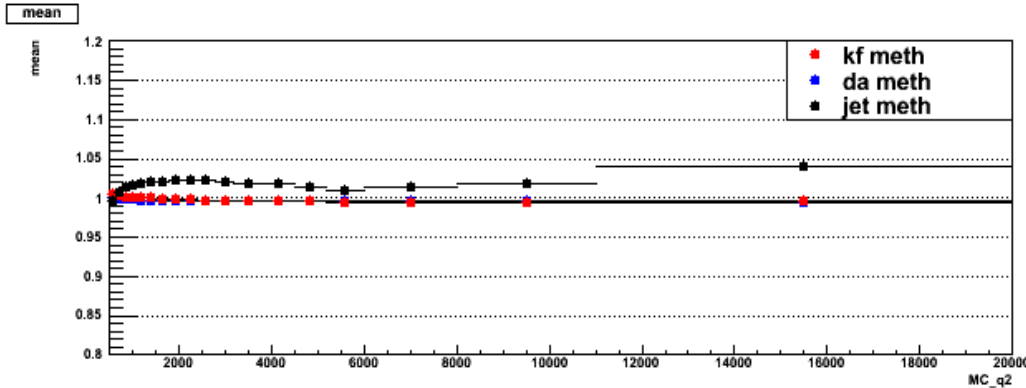
Provide $P(D|\lambda)Po(\lambda)$



**BAT does the job
for you**

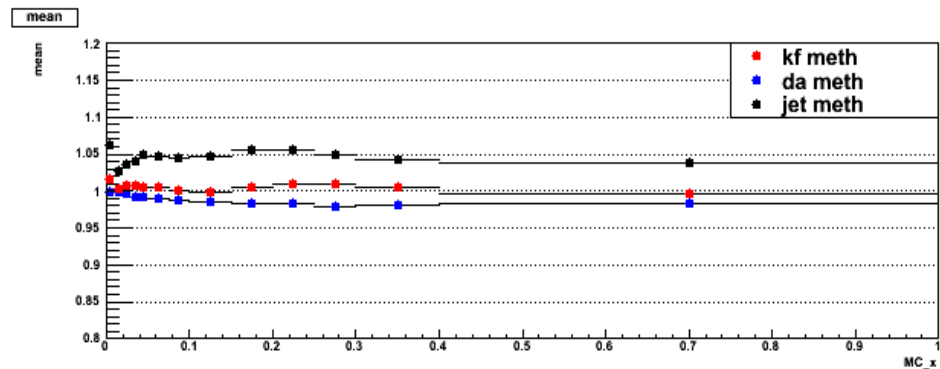
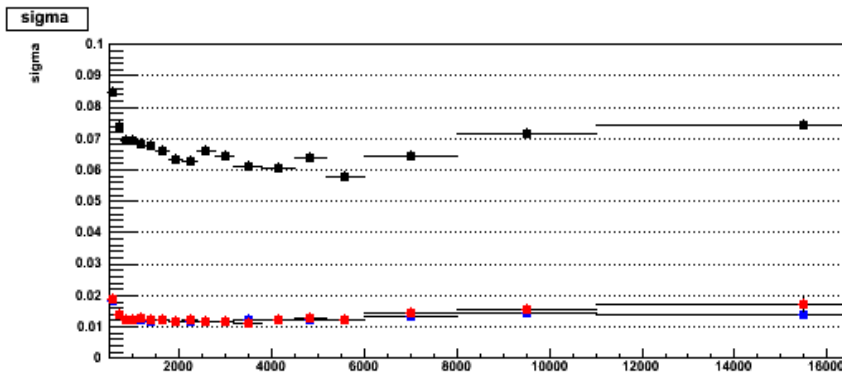
BAT- More information:
<http://www.mppmu.mpg.de/bat/>

Comparing the resolution and bias for x & Q2 : 1jet good



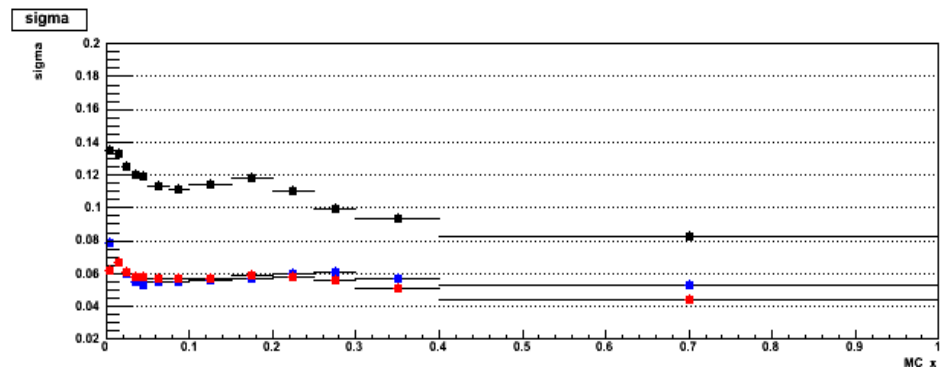
Bias in Q^2_{meth} / Q^2_{MC}

resolution Q^2_{meth} / Q^2_{MC}



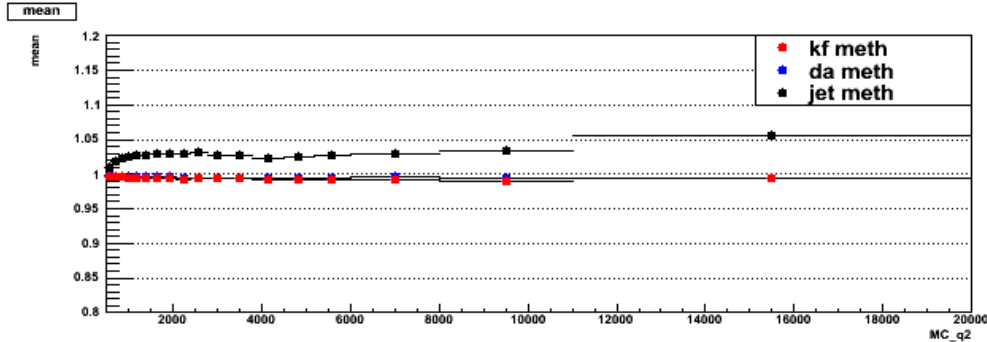
Bias in x_{meth} / x_{MC}

Resolution x_{meth} / x_{MC}

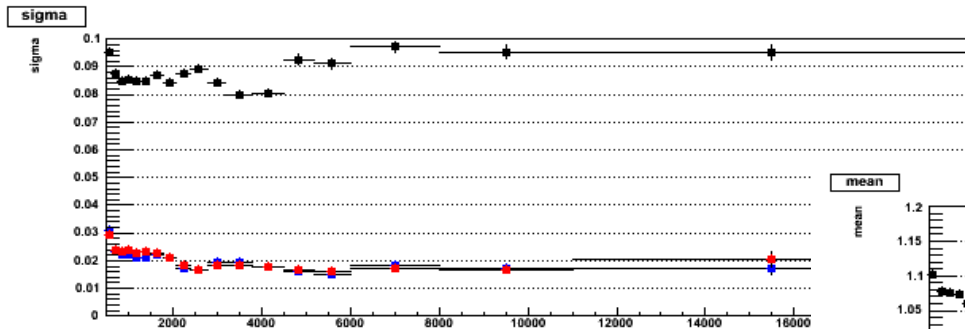


Kpf doing a good job!

Comparing the resolution and bias for x & Q2 : hadsys

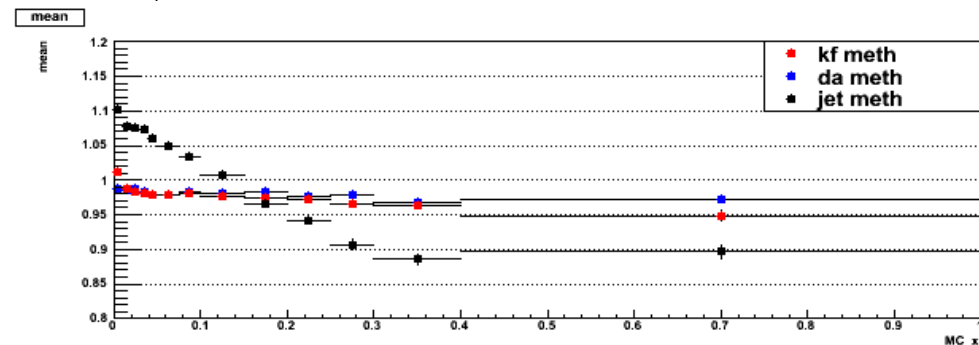


Bias in $Q^2_{\text{meth}} / Q^2_{\text{MC}}$

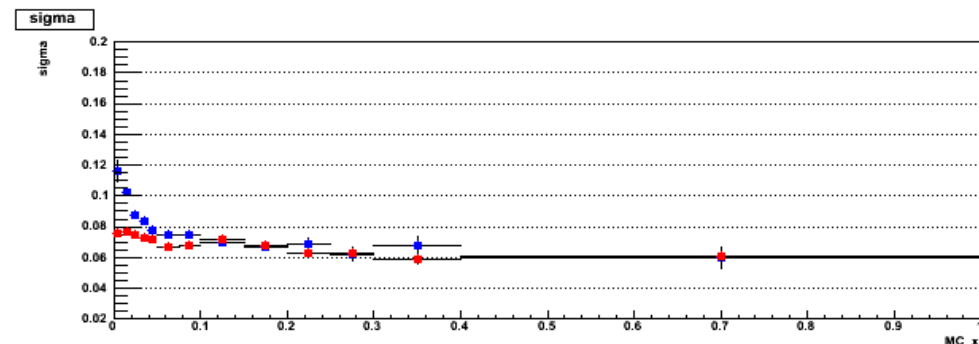


resolution $Q^2_{\text{meth}} / Q^2_{\text{MC}}$

Bias in $x_{\text{meth}} / x_{\text{MC}}$



Resolution $x_{\text{meth}} / x_{\text{MC}}$



Kpf doing a good job!

SUMMARY:

- Deep inelastic scattering and results from HERA.
- Reconstruction of Kinematic variables.
- Introduction of new method - Kinematic fit method.
- use whole information - expect better outcome.
- Usefulness of this method over other methods .

Thanks

Formulation..

$$E = xyP + Ar(1-y) \qquad \cos \theta = \frac{xyP - Ar(1-y)}{xyP + Ar(1-y)}$$

$$F = x(1-y)P + yAr \qquad \cos \gamma = \frac{x(1-y)P - Ary}{x(1-y)P + Ary}$$

Where :

A : Electron beam Energy

P : Proton beam Energy

Ar = Electron energy participating in scattering A - E_y

Electron Method

$$Q_e^2 = 4E_e E'_e \cos^2 \frac{\theta_e}{2},$$

$$y_e = 1 - \frac{E'_e}{2E_e}(1 - \cos \theta_e), \quad x_e = Q_e^2 / y_e s$$

DA Method

$$Q_{DA}^2 = \frac{4E_e^2 \sin \gamma_h (1 + \cos \theta_e)}{\sin \gamma_h + \sin \theta_e - \sin(\theta_e + \gamma_h)},$$

$$y_{DA} = \frac{\sin \theta_e (1 - \cos \gamma_h)}{\sin \gamma_h + \sin \theta_e - \sin(\theta_e + \gamma_h)}, \quad x_{DA} = Q_{DA}^2 / (s y_{DA})$$

Hadron Method

$$y_h = \frac{\sum_i (E_i - p_{z,i})}{2E_e}, \quad Q_h^2 = \frac{P_{T,h}^2}{1 - y_h}, \quad x_h = \frac{Q_h^2}{s y_h}$$

Elpt-jet method

$$x_{pt_e} = \frac{(p_{t_e} / \sin \theta_{jet})(1 + \cos \theta_{jet})}{2E_p \left(1 - \frac{(p_{t_e} / \sin \theta_{jet})(1 - \cos \theta_{jet})}{2E_e}\right)} \quad x = \frac{E_{jet}(1 + \cos \theta_{jet})}{2E_p \left(1 - \frac{E_{jet}(1 - \cos \theta_{jet})}{2E_e}\right)}$$

MC sample:

04/05e- : DJANGO 1.6, Ariadne 4.12, CTEQ-5D with $Q^2 > 400 \text{ GeV}^2$

Selection:

Vertex:

Valid vertex && $|Z_{\text{vtx}}| < 50. \text{ cm}$

Electron:

1 e- candidate ($E_e > 15 \text{ GeV}$)

Fiducial volume cuts:

BCAL+FCAL e-s

no cracks, no RCAL

$|DME| > 1.4 \text{ cm}$ && $|DCE| > 0.5 \text{ cm}$

In CTD Acceptance

$DCA < 10 \text{ cm}$

Superlayers > 4

$\text{TrkP} > 5. \text{ GeV}$

Not in Acc. Of CTD

$\text{Pt elec} > 30. \text{ GeV}$

Kinematics:

$45 < E_{\text{mpz}} < 65$

$\text{Pt}/\sqrt{s} < 5 \text{ GeV}$

$y_{\text{el}} < 0.95$

Jets

“good jets”

1 jet events in FCAL/BCAL

Box cut 40.40 cm^2

Avoid FBCAL crack

Missing $E_{\text{mpz}} < 5 \text{ GeV}$

$E_t > 10 \text{ GeV}$

“hadsys jets”

1,2,3(<4) jet events in FBCAL

Box cut

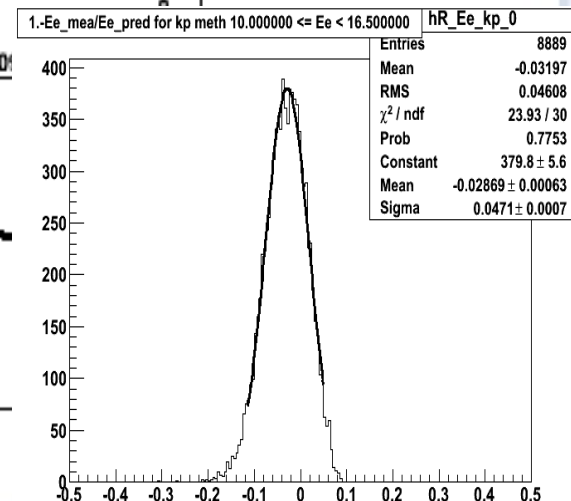
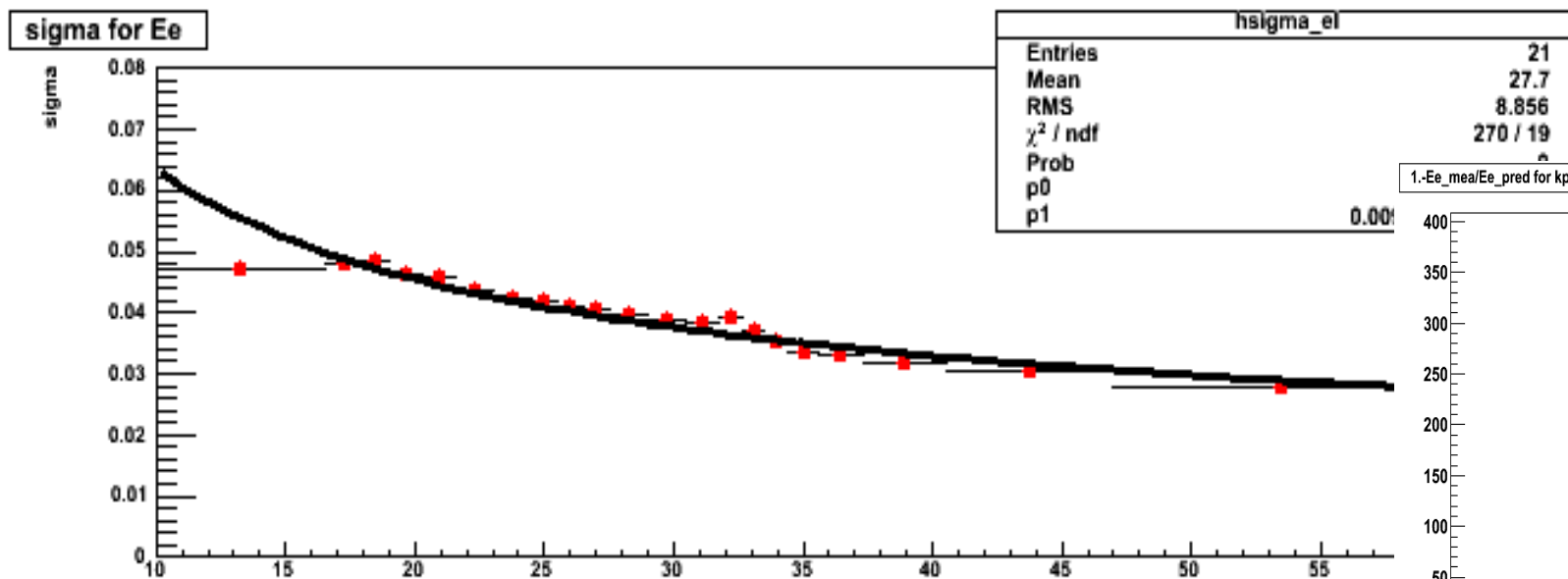
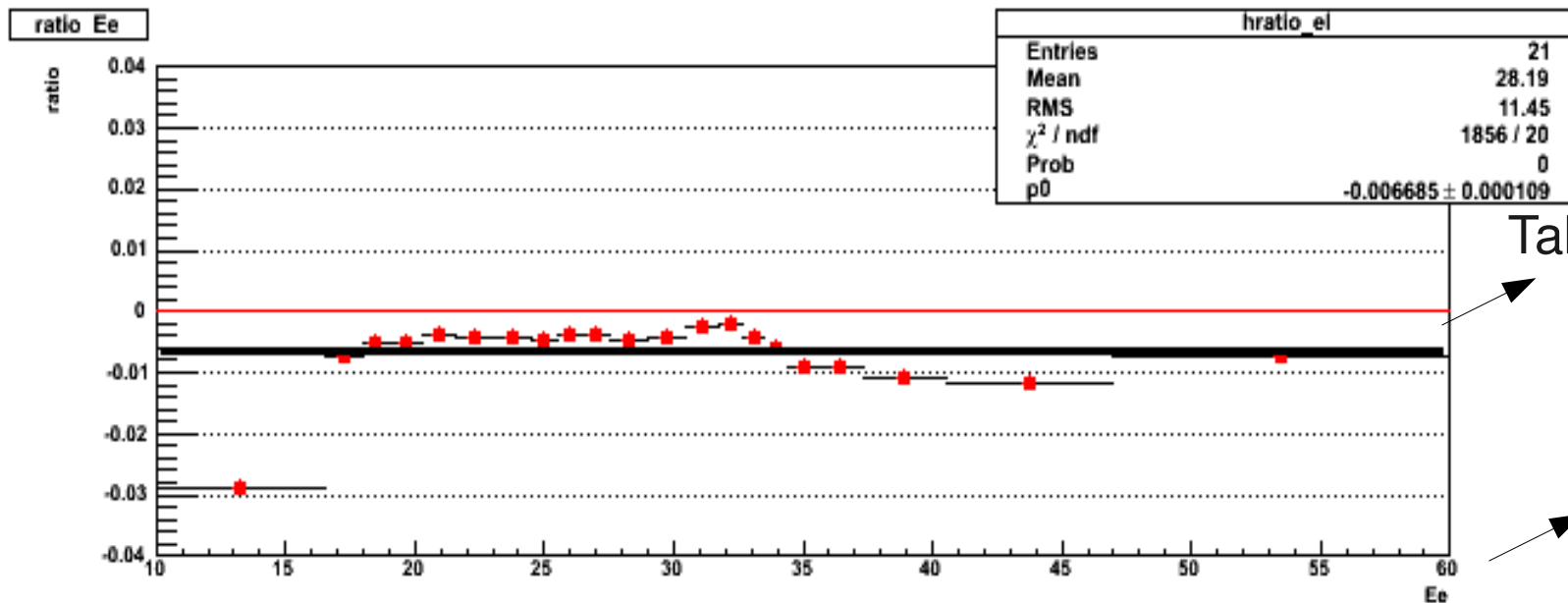
None of the jets in FBCAL crack

Missing $E_{\text{mpz}} \geq 5 \text{ GeV}$ for

1jet events

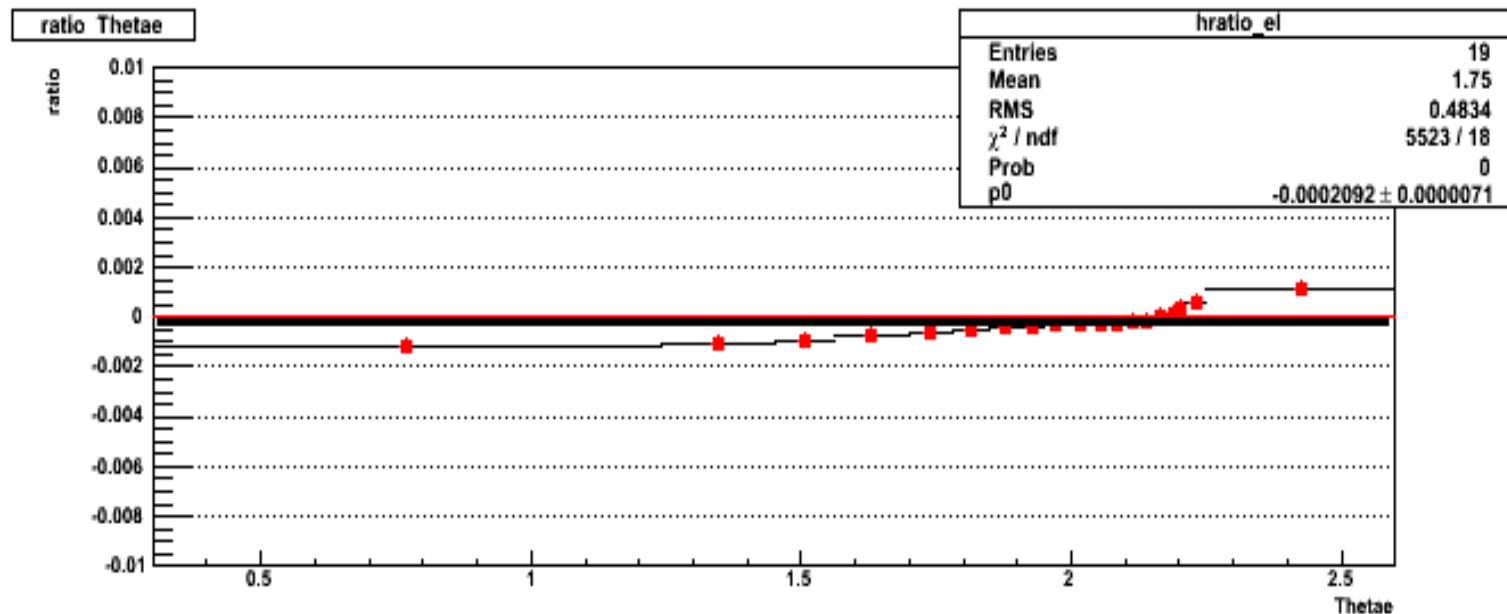
E_t of first jet $> 10 \text{ GeV}$

P(E_e|E): 1-E_e/E in bins of E => a gaussian

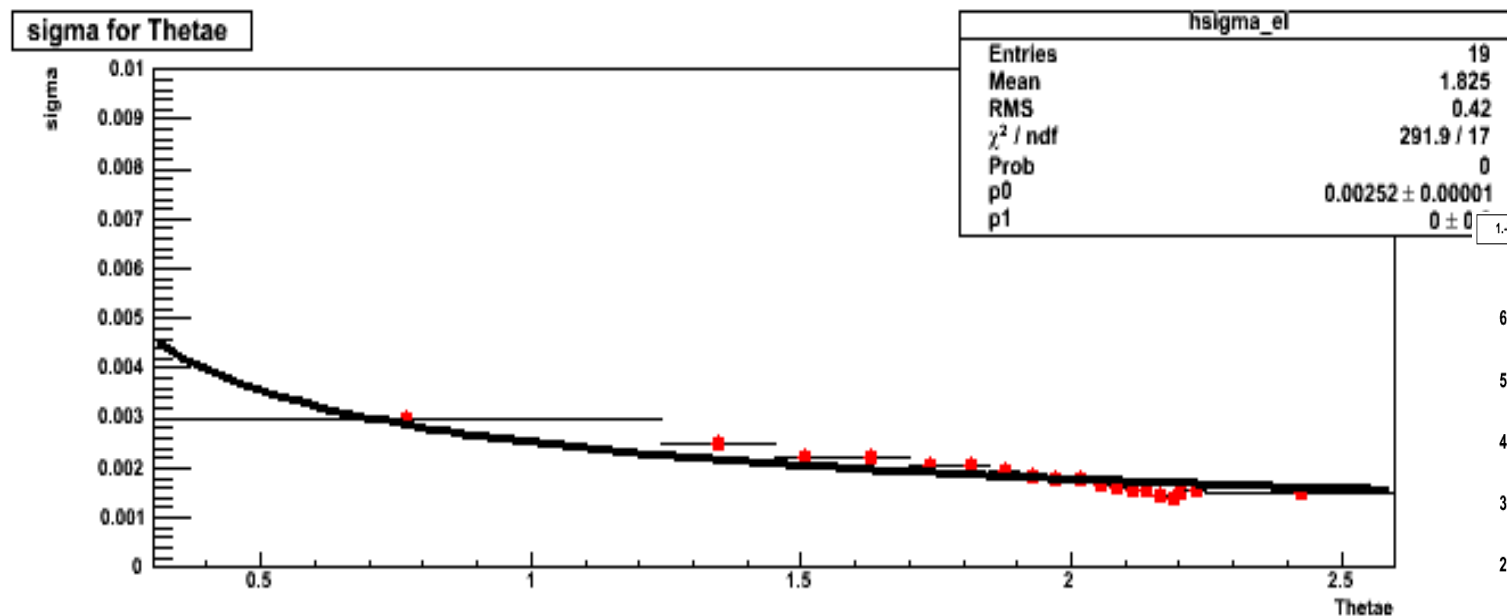


As an example

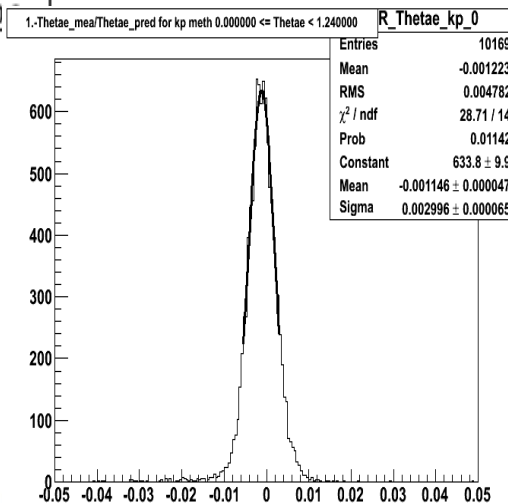
$P(\theta_e|\theta)$: $1-\theta_e/\theta$ in bins of $\theta \Rightarrow$ a gaussian



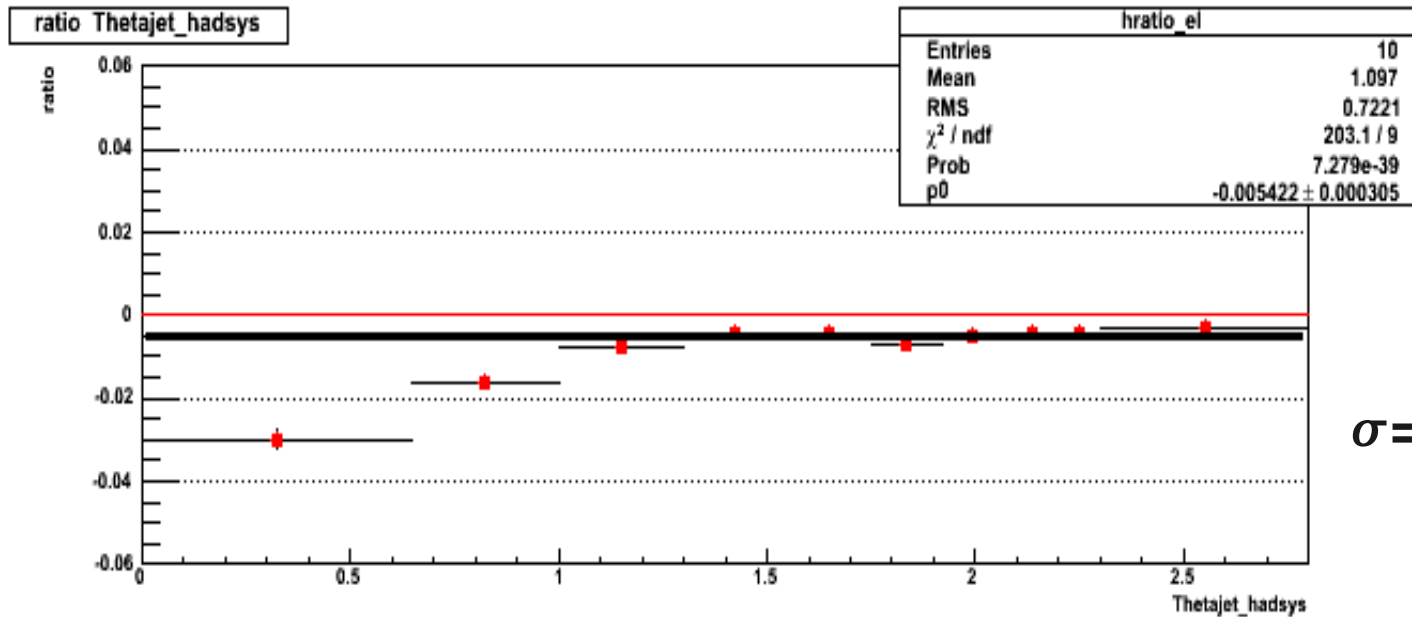
Taking Offset = 0



$\sigma = a/\sqrt{\theta} \oplus b$

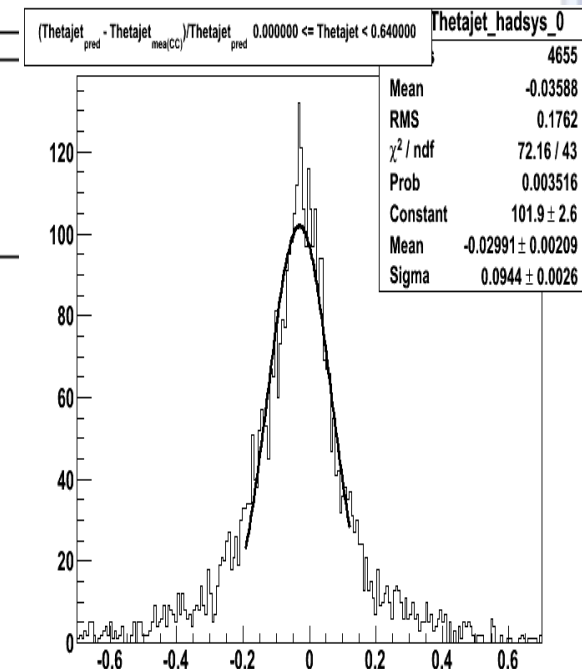
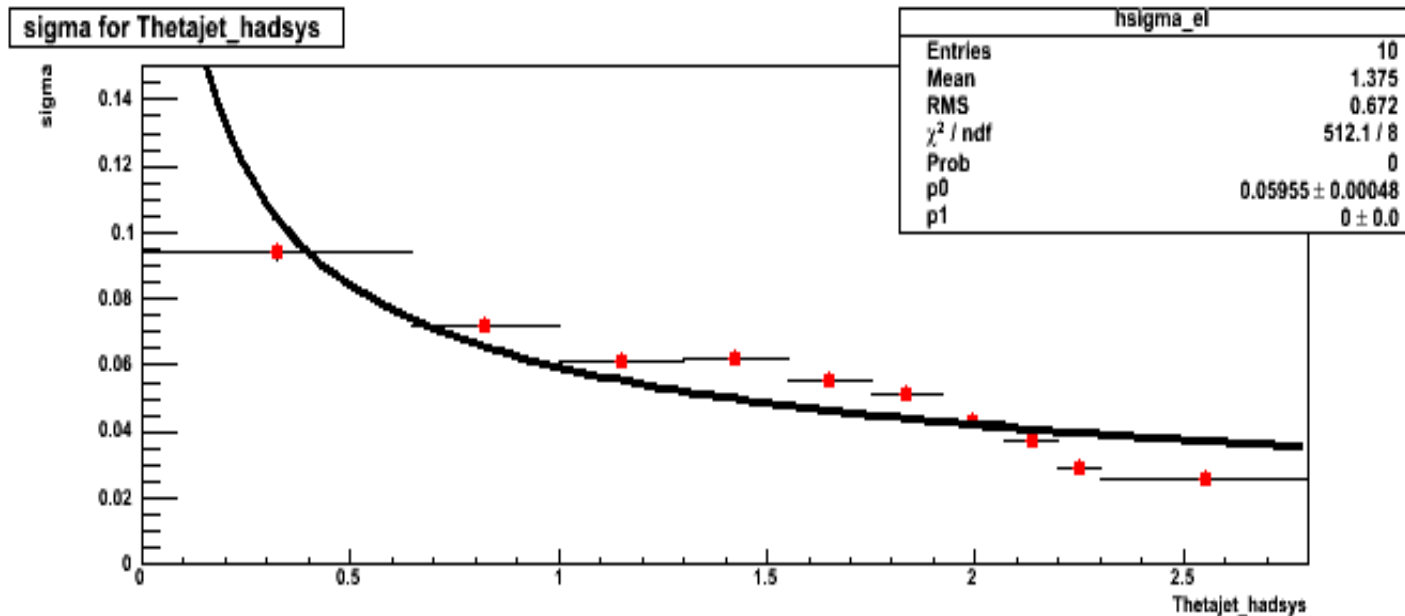


$P(\theta_{j_had}|\gamma_{had})$: $1-\theta_{j_had}/\gamma_{had}$ in bins of γ_{had} => a gaussian

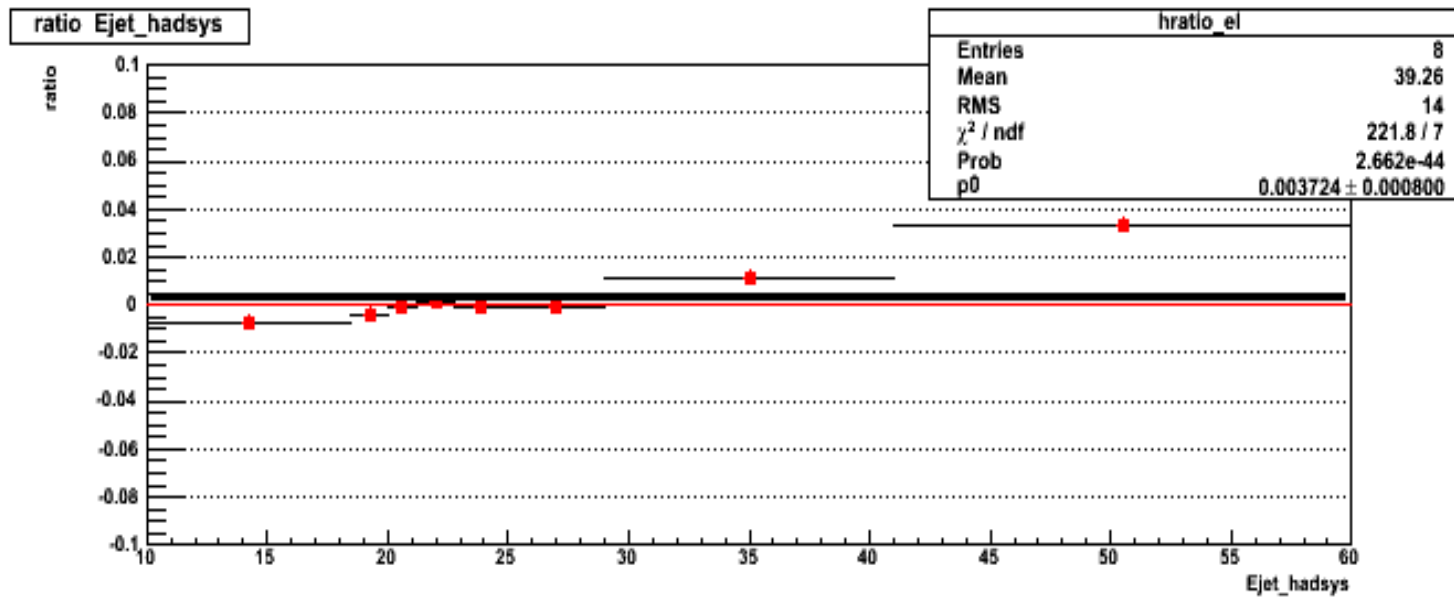


Taking Offset = 0

$$\sigma = a/\sqrt{\gamma_{had}} \oplus b$$

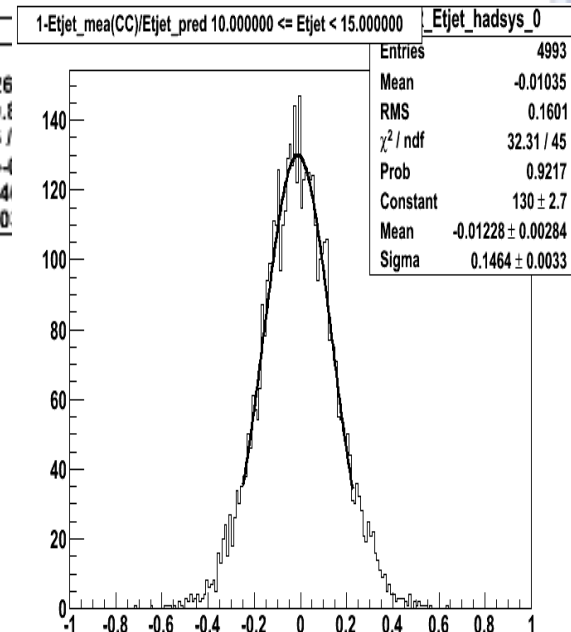
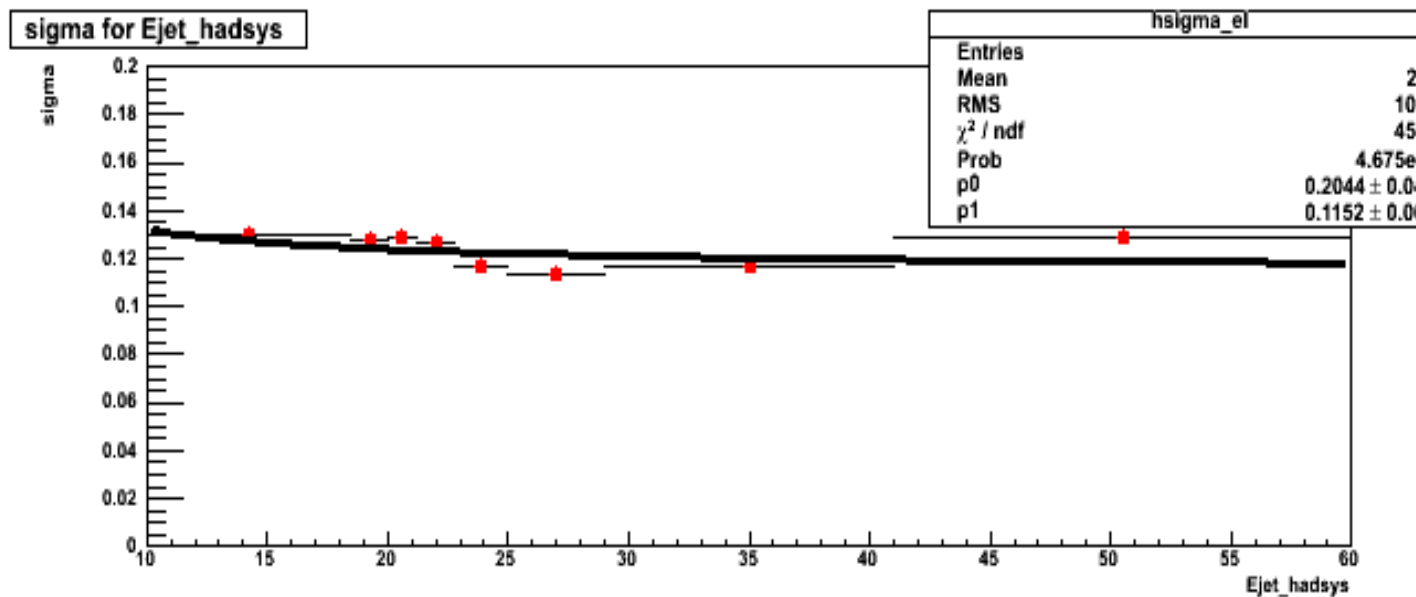


$P(E_{j_had}|F_{had})$: $1-E_{j_had}/F_{had}$ in bins of $F_{had} \Rightarrow$ a gaussian

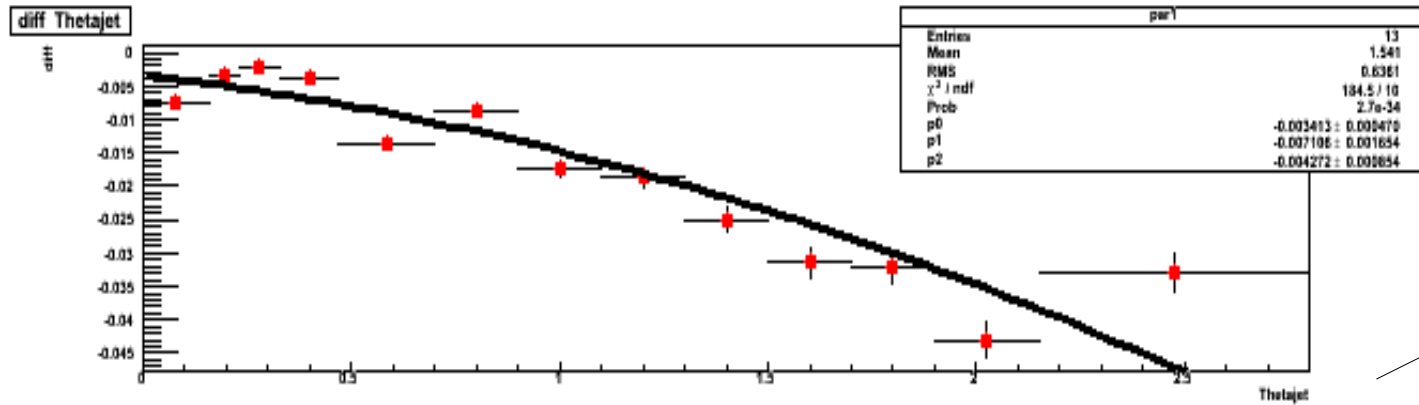


Taking Offset = 0

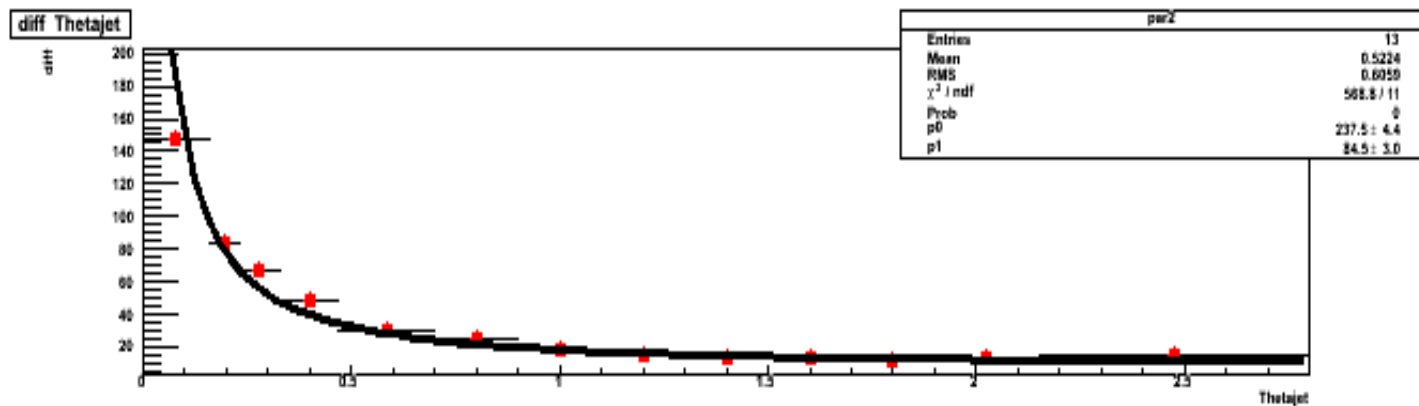
$$\sigma = a/\sqrt{F_{had}} \oplus b$$



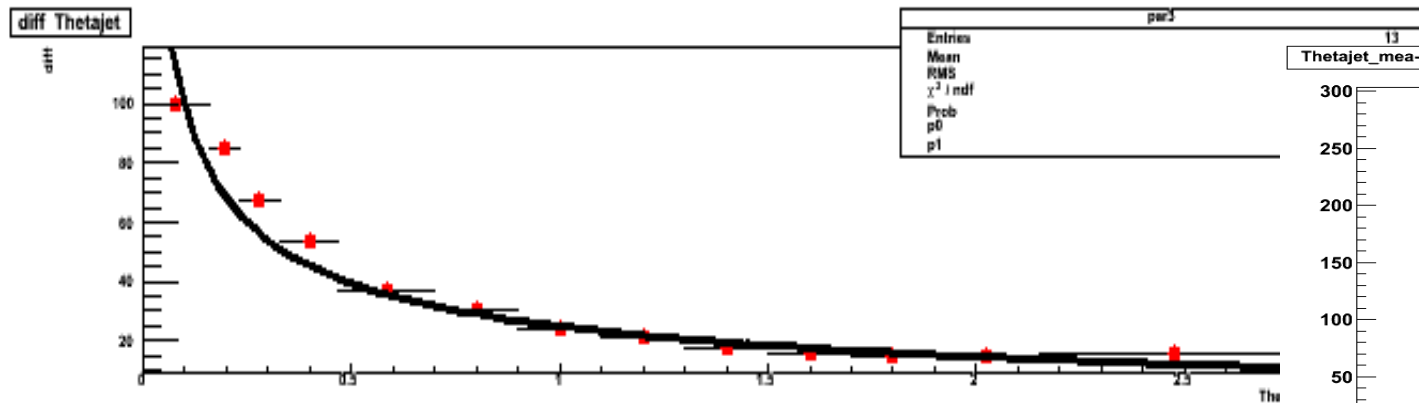
$P(\theta_j|\gamma): 1-\theta_j/\gamma$ in bins of $\gamma \Rightarrow f(\gamma) = A/2 e^{\frac{b^2}{4c^2}} e^{b(\gamma-m)} \text{Erfc}(c(\gamma-m))$



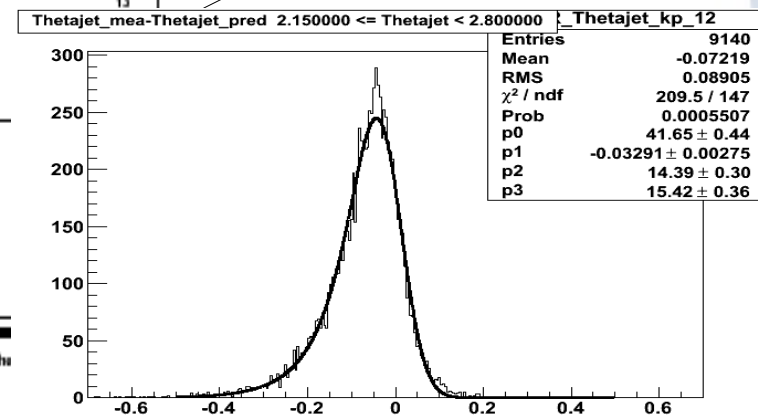
m : II order pol in γ



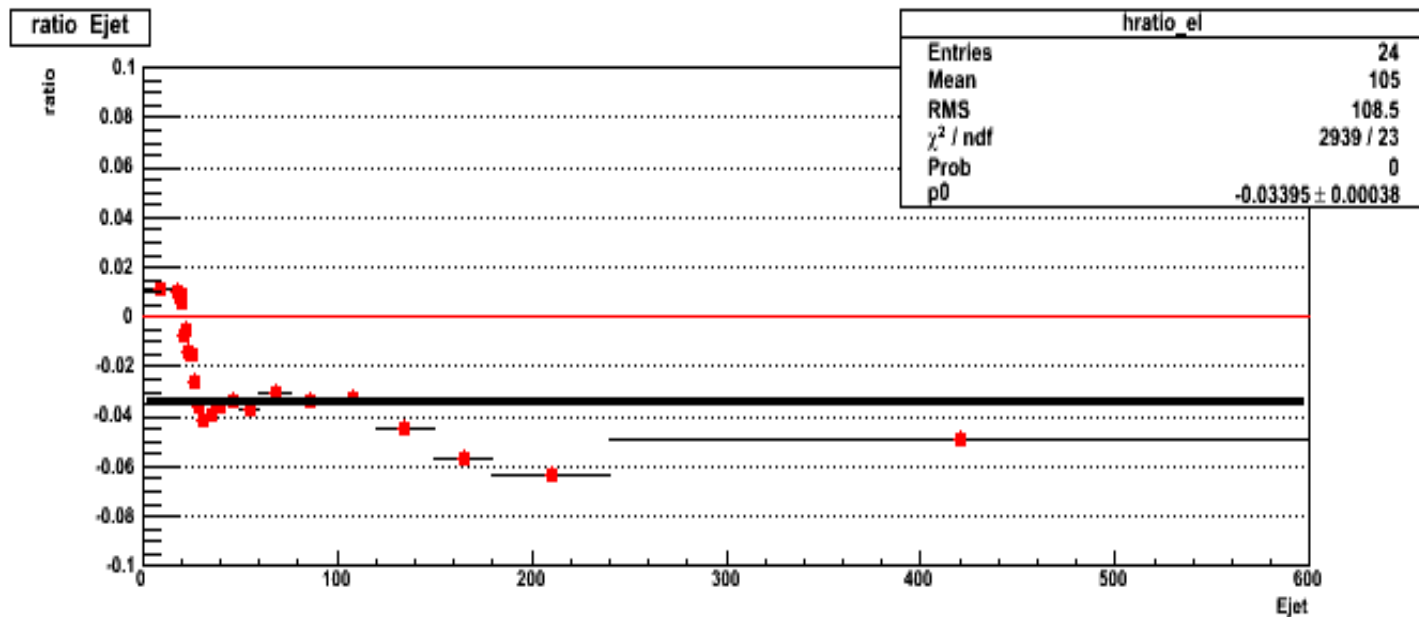
$b = \sqrt{a/\gamma + b}$



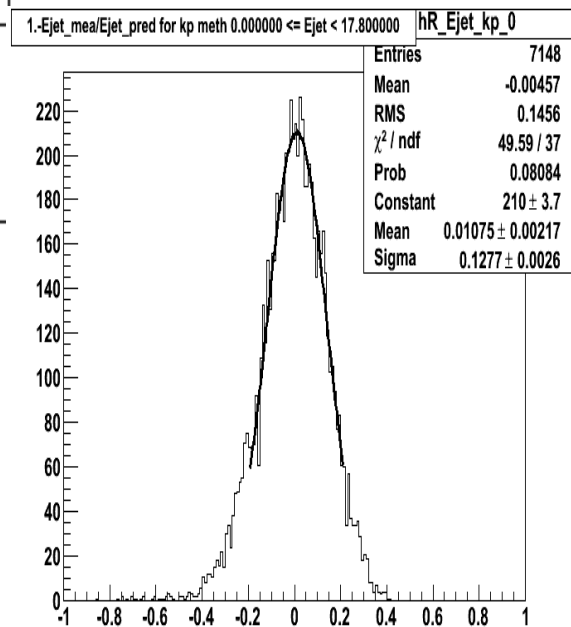
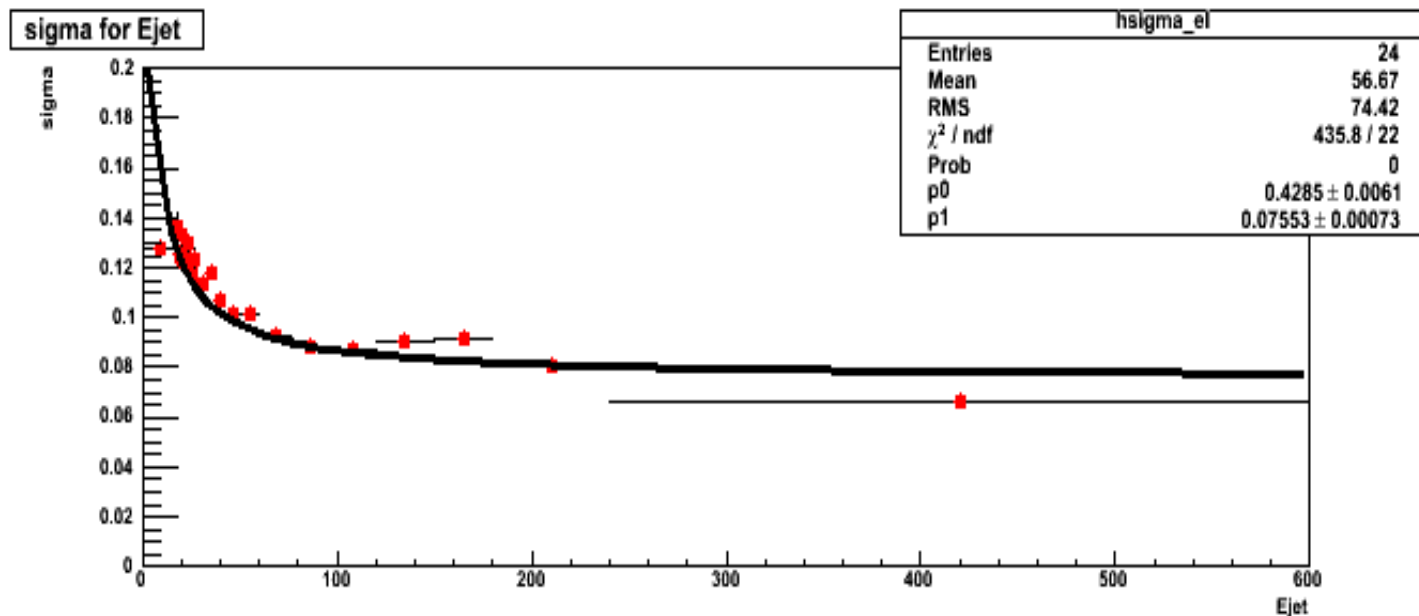
$C = a/\sqrt{\gamma + b}$



$P(E_j|F)$: $1-E_j/F$ in bins of $F \Rightarrow$ a gaussian



Taking Offset = -0.034



$$\sigma = a/\sqrt{F} \oplus b$$