

# How to recognize different types of trees from quite a long way away

Daniel Härtl

Max-Planck-Institut für Physik, München

IMPRS Young Scientist Workshop at Ringberg Castle

July 28, 2010



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Max-Planck-Institut für Physik  
(Werner-Heisenberg-Institut)

**No. 1**  
**The Larch**



# The Pink Lecture Series: Strings at the TeV Scale

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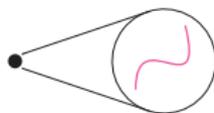
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- 1 Introduction
- 2 String Scattering
- 3 String Effects
- 4 Conclusion

# String Theory in a Nutshell

- Point particles are in fact **strings**.



- They can be **open** or **closed**.



bosons, fermions, ...



graviton, ...

- String masses arise from **oscillations**.



light



heavy

- Strings propagate in **10-dimensional spacetime**.

⇒ Compactification:  $\mathcal{M}_{10} = \mathbb{R}^{(3,1)} \times \mathcal{Y}_6$ .

# Energy Scales in Quantum Gravity

- Four-dimensional gravity becomes strong at the **Planck scale**

$$M_{\text{Pl},4} = \sqrt{\frac{\hbar c}{G}} \sim 10^{19} \text{ GeV}.$$

- TeV scale quantum gravity is possible in theories with  $n$  **large extra-dimensions** of size  $R$  [ADD '98]:

$$(M_{\text{Pl},4})^2 \sim (M_{\text{Pl},4+n})^{2+n} R^n.$$

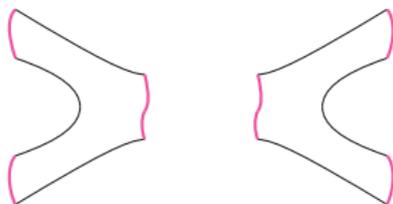
- For string compactifications to  $D = 4$  the **string scale**  $M_S$  satisfies

$$(M_{\text{Pl},4})^2 \sim g_S^{-2} (M_S)^8 V_6.$$

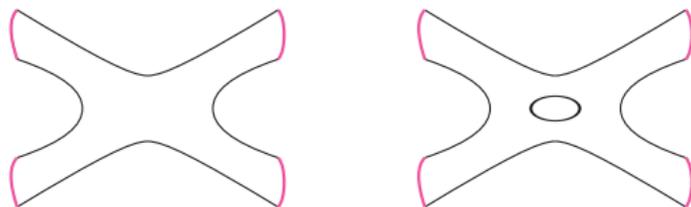
- Strings could be **discovered at LHC** if  $g_S < 1$ ,  $M_S \sim \mathcal{O}(\text{TeV})$ .
- **Gravitational constraints** from phenomenology, astrophysics and cosmology demand  $M_S > 1 \text{ TeV}$  [ADD '98].

# Open String Interactions

Strings can interact in two ways, i.e. by **joining** and **splitting**.



**Open string diagrams** then look like



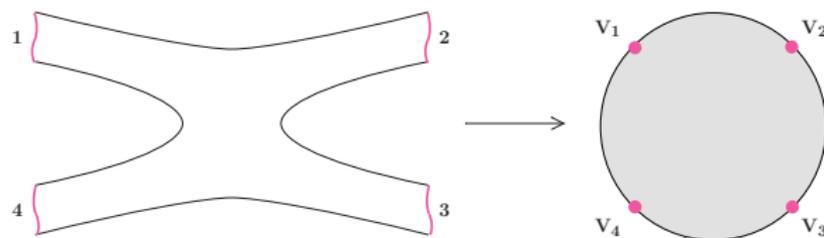
String diagrams are 2d surfaces in 10d space-time.

**No. 12 b**



# Disk Diagrams

Using the [Riemann mapping theorem](#) tree-level diagrams can be mapped onto the unit disk  $\mathbb{D}$ .



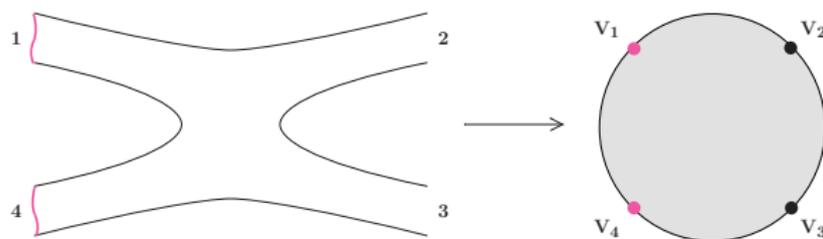
The  $V_i$ 's are [vertex operators](#) creating and annihilating string states.

## Riemann Mapping Theorem

If  $U \subset \mathbb{C}$  is open and simply connected, there exists a unique biholomorphic mapping  $f$  from  $U$  onto the open unit disk  $\mathbb{D}$ .

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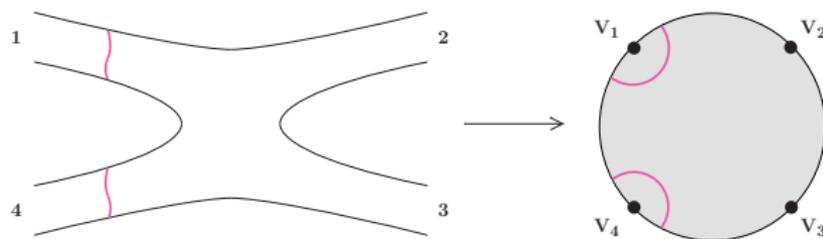
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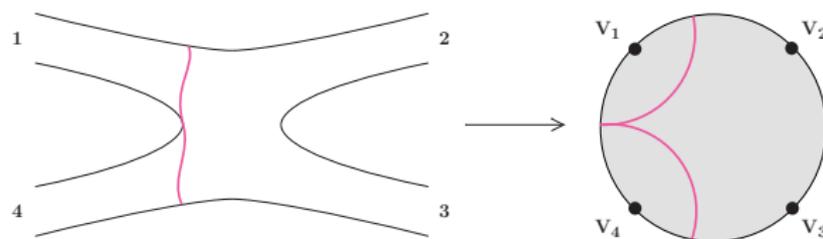
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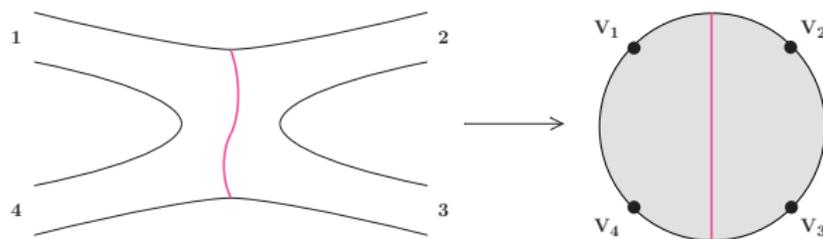
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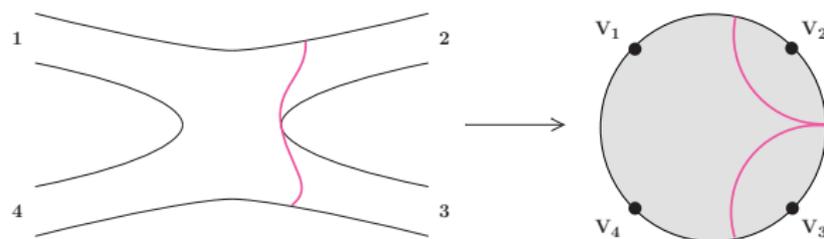
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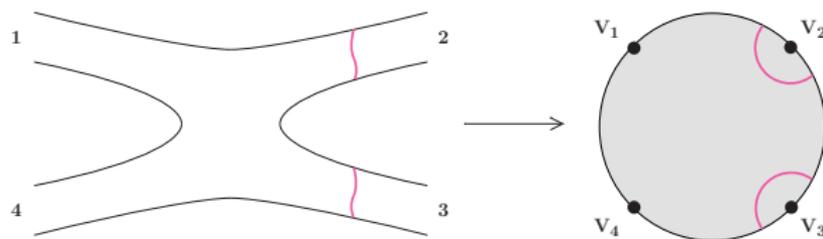
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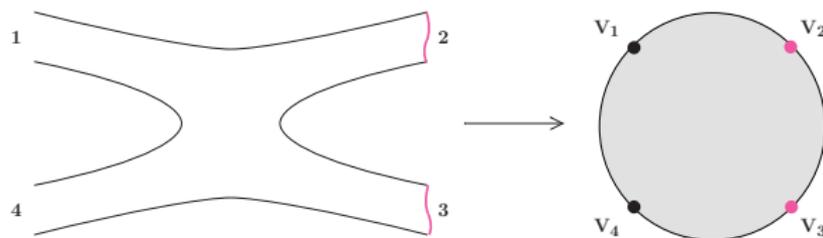
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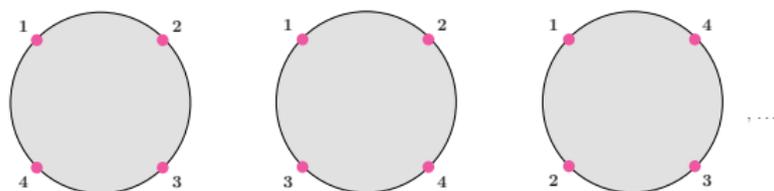
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# The Full Amplitude

One has to sum over all **cyclic non-equivalent configurations**



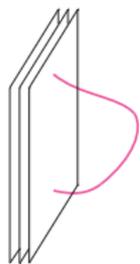
and **integrate** over the vertex operator positions  $z_i$

$$\mathcal{A}(1, \dots, N) \propto \int \prod_{i=1}^N dz_i \sum_{\sigma \in S_{N-1}} \langle V_1(z_1) V_{\sigma(2)}(z_{\sigma(2)}) \dots V_{\sigma(N)}(z_{\sigma(N)}) \rangle.$$

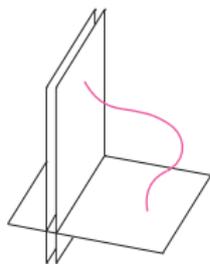
Challenges:

- Integration,
- Interacting CFT of  $\psi$  &  $S$  fields in  $\langle V_1 \dots V_n \rangle \rightarrow$  [DH, Schlotterer, Stieberger '09].

# Strings & Branes & Gauge Theories

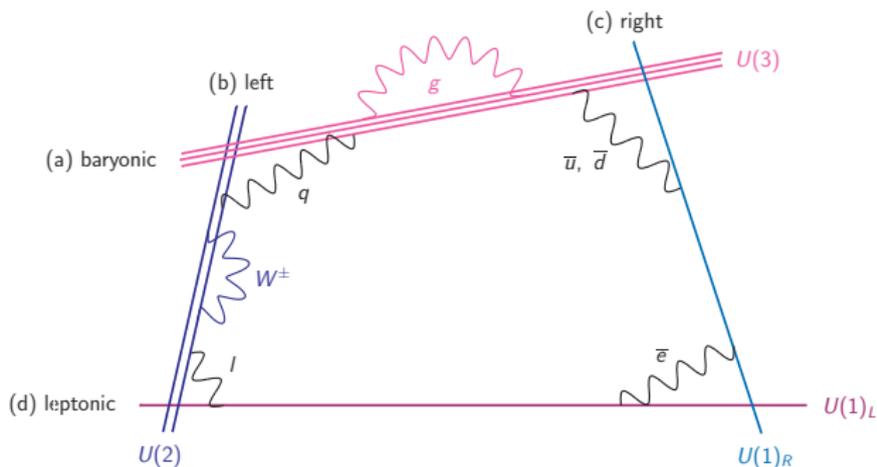


$U(N)$  gauge bosons,



chiral fermions.

The SM from intersecting D6-branes:



# Stringy QCD results

All tree-level amplitudes  $pp \rightarrow pp$  are of the form [Lüst, Stieberger, Taylor '08]

$$\mathcal{A}(k_1, k_2, k_3, k_4, M_S) \sim \frac{s u}{t M_S^2} B(-s/M_S^2, -u/M_S^2),$$

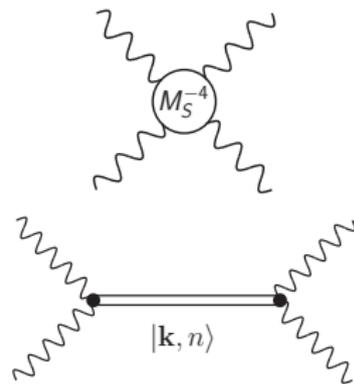
where  $s, u, t$  are the Mandelstam variables and  $B(x, y)$  is the Euler beta function.

- $M_S$ -expansion:

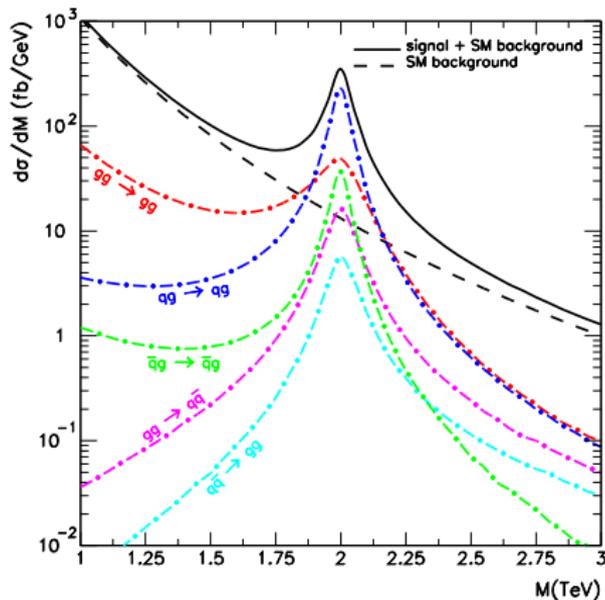
$$\mathcal{A} \sim \frac{t}{s} - \frac{\pi^2}{6} t u M_S^{-4} + \mathcal{O}(M_S^{-6}).$$

- pole-expansion:

$$B = - \sum_{n=0}^{\infty} \frac{M_S^{2-2n}}{n!} \frac{1}{s - nM_S^2} \left[ \prod_{J=1}^n (u + M_S^2 J) \right]$$



- Production of Regge-excitations [Lüst, Stieberger, Taylor et al. '08]



- model-dependent corrections from  $qq \rightarrow qq$  [Lüst, Stieberger, Taylor et al. 09],
- photons at tree-level [Anchordoqui, Taylor et al. '08]:  $gg \rightarrow g\gamma$ ,  $gg \rightarrow \gamma\gamma$ .

- You should now be able to recognize [the larch](#) from a long way away.
- You should watch [Monty Python's Flying Circus](#).

- TeV scale quantum gravity can be realized in theories with large extra dimensions.
- String theory is the natural playground for such theories.
- LHC might discover stringy effects.

Thanks for your attention.

# Vertex Operators

The **vertex operators** for gluons and fermions are

$$V_{A^a}(z, \xi, k) = g_A \lambda^a e^{-\phi(z)} \xi^\mu \psi_\mu(z) e^{i k_\nu X^\nu(z)},$$
$$V_{\psi_\beta^\alpha}(z, u, k) = g_\psi \lambda_\beta^\alpha e^{-\phi(z)/2} u^\lambda S_\lambda(z) e^{i k_\nu X^\nu(z)} \Xi(z),$$

where  $\psi^\mu$  is an **external (4d) vector spin field**,  $e^{ikX^\nu}$  is the **momentum part**, and  $\Xi$  is an **internal (6d) field**.

The correlation function of vertex operators factorizes

$$\langle V_1(z_1) \dots V_N(z_N) \rangle \propto \underbrace{\langle \mathcal{O}_X \rangle \cdot \langle \mathcal{O}_\Xi \rangle}_{\text{well-known}} \cdot \langle \mathcal{O}_{\psi, S} \rangle.$$

A formula for arbitrary  $\psi$ - $S$  correlators at tree-level can be found in [DH, Schlotterer, Stieberger '09].