

Unified Matter Inflation

Stefan Antusch

*Max Planck Research Group:
"Beyond the Standard Model"*

Project Review 2010

Max-Planck-Institut für Physik
(Werner-Heisenberg-Institut)



Max Planck Research Group: Beyond the Standard Model

Members:

- ▶ Group leader: **Stefan Antusch**

- ▶ Postdocs:
 - **Lorenzo Calibbi**
 - **Yu Min Kim** (arrived 10/10)
 - **Toshihiko Ota**
 - **Enrique Fernandez-Martinez**
(since 10/10 → CERN)
 - **Koushik Dutta**
(since 10/10 → DESY)

▶ Phd students:

- **Jochen Baumann**
- **Sebastian Halter**
- **Philipp Kostka**
(defended his thesis 12/10)
- **David de Sousa Seixas**
- **Martin Spinrath**
(since 10/10 → SISSA)

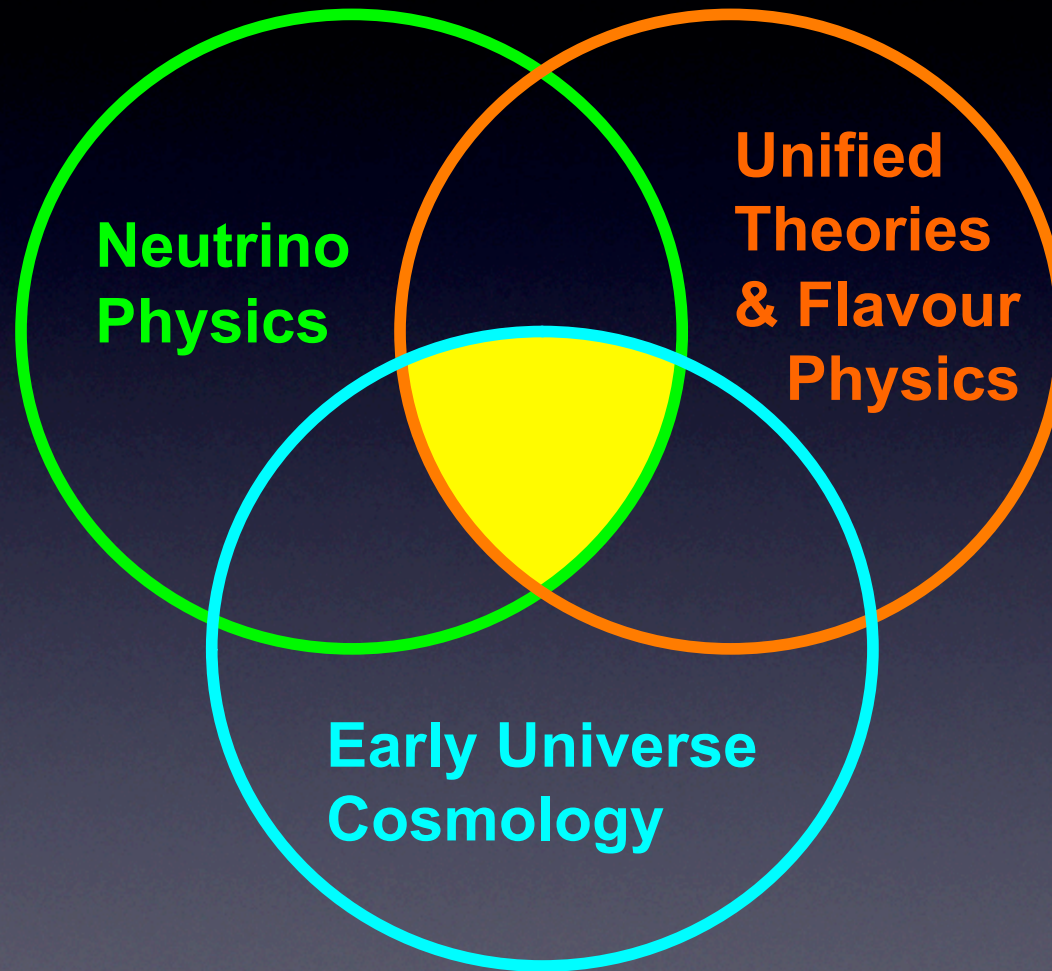
▶ Diploma students:

- **Valerie Domcke**
(thesis handed in 11/10)
- **Vinzenz Maurer**



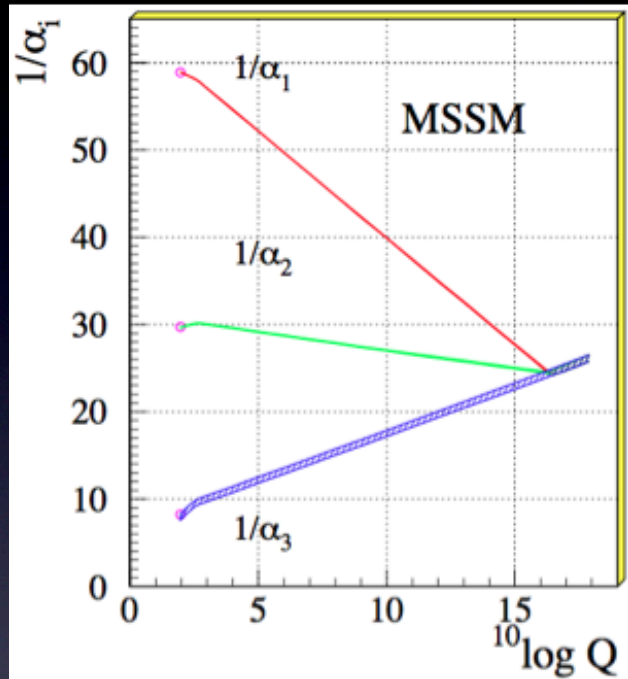
Max Planck Research Group: Beyond the Standard Model

Research:



Grand Unified Theories: 'Unification of forces and Matter'

@ energies $\sim 10^{16}$ GeV



(assuming supersymmetry)

Quarks:	u	c	t
	d	s	b
Leptons:	e	μ	τ
	ν_e	ν_μ	ν_τ
	↓	↓	↓
SO(10) GUTs:	16 ₁	16 ₂	16 ₃

Forces unified:

$SU(3)_C \times SU(2)_L \times U(1)_Y \subset G_{GUT}$.
Examples: $G_{GUT} = SU(5)$, $G_{GUT} = SO(10)$

Matter particles unified:

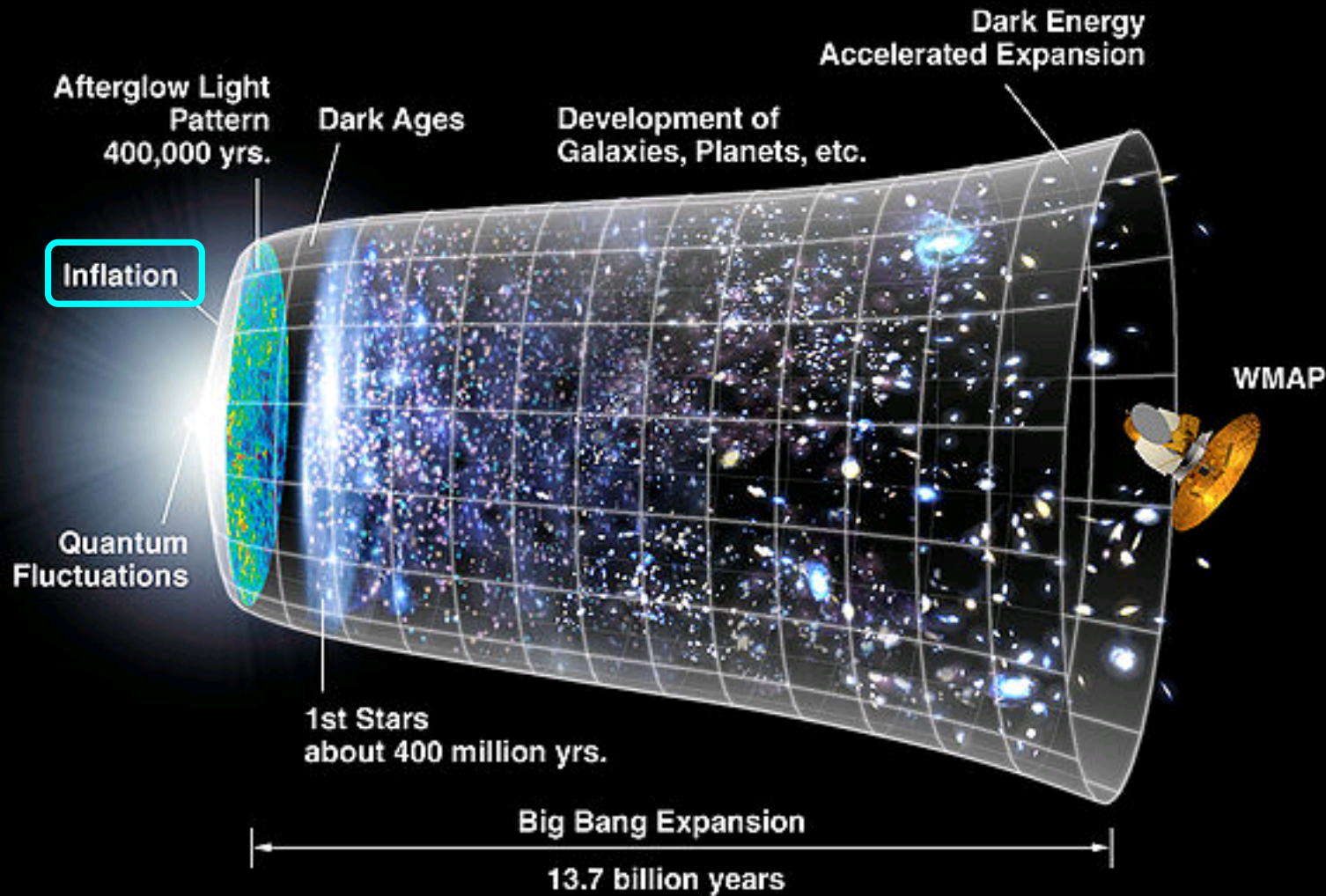
All known matter particles of one family plus one RH neutrino are in

$$16_i = (q_L \quad u_R^c \quad e_R^c \quad d_R^c \quad \ell_L \quad \nu_R^c)_i$$



Inflation = Era of accelerated expansion in the very early universe

picture from WMAP website



vacuum energy for inflation: typically $\sim 10^{16}$ GeV (\rightarrow Grand Unified Theories)



Outline

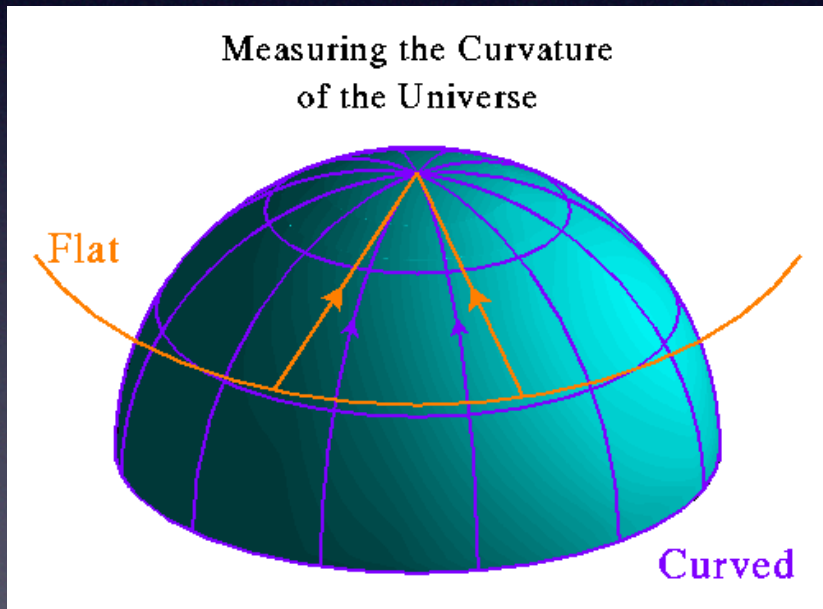
- ➔ Cosmic inflation: A successful paradigm for the early universe
- ➔ How can inflation be realised in particle physics?
 - Framework: Local supersymmetry (= supergravity)
 - Challenge: The η -problem; Possible solution: Symmetries
 - New class of models: 'Tribrid inflation' + Symmetries
 - Promising inflaton candidate: The 'Unified Matter Superparticle'



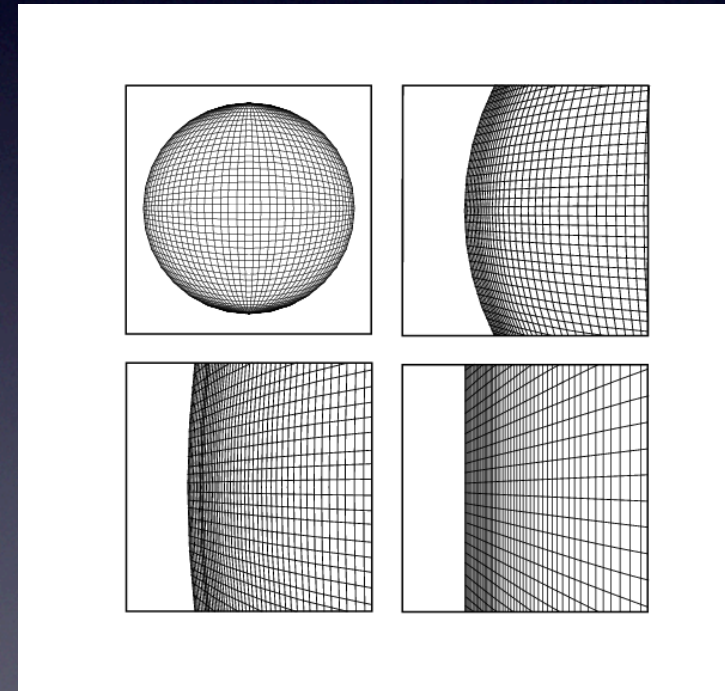
Why inflation?

- ▶ The “Flatness Problem”: Why is the universe so flat?

Exponential expansion:
”flattens“ the universe



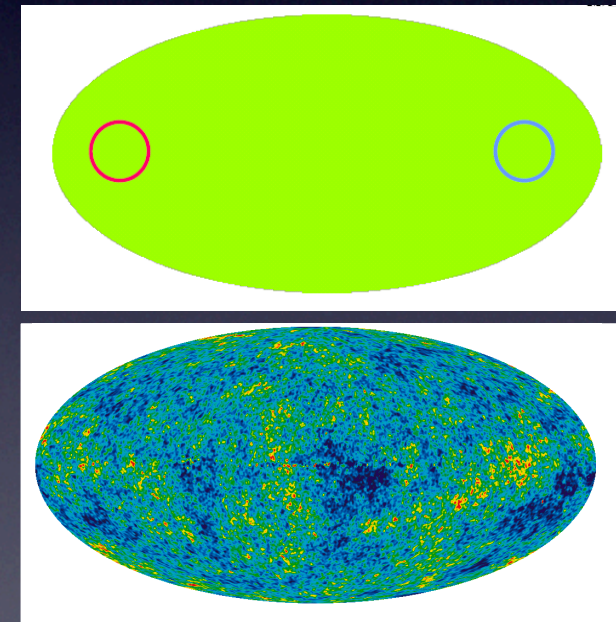
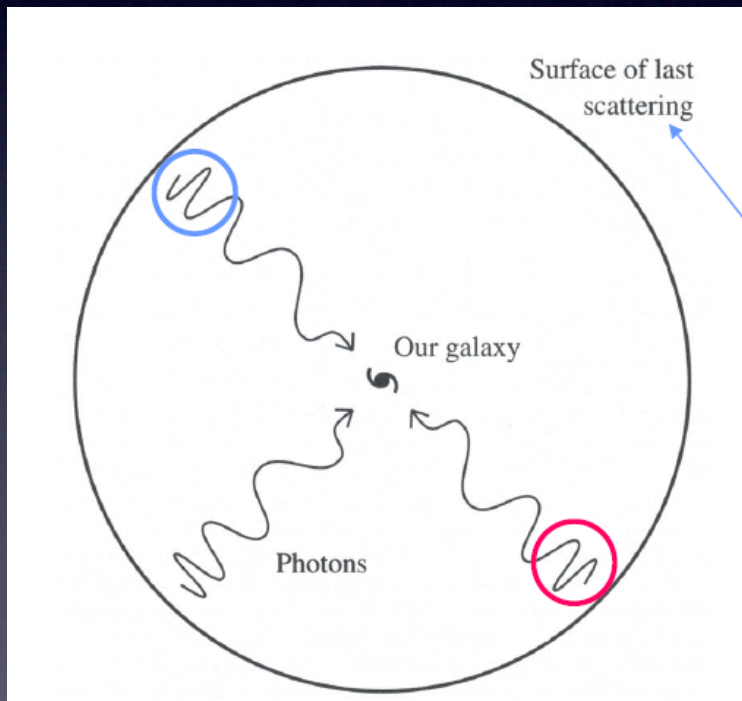
Today: $\Omega_k < 0.01$; Planck times: $\Omega_k < 10^{-60}$



Why inflation?

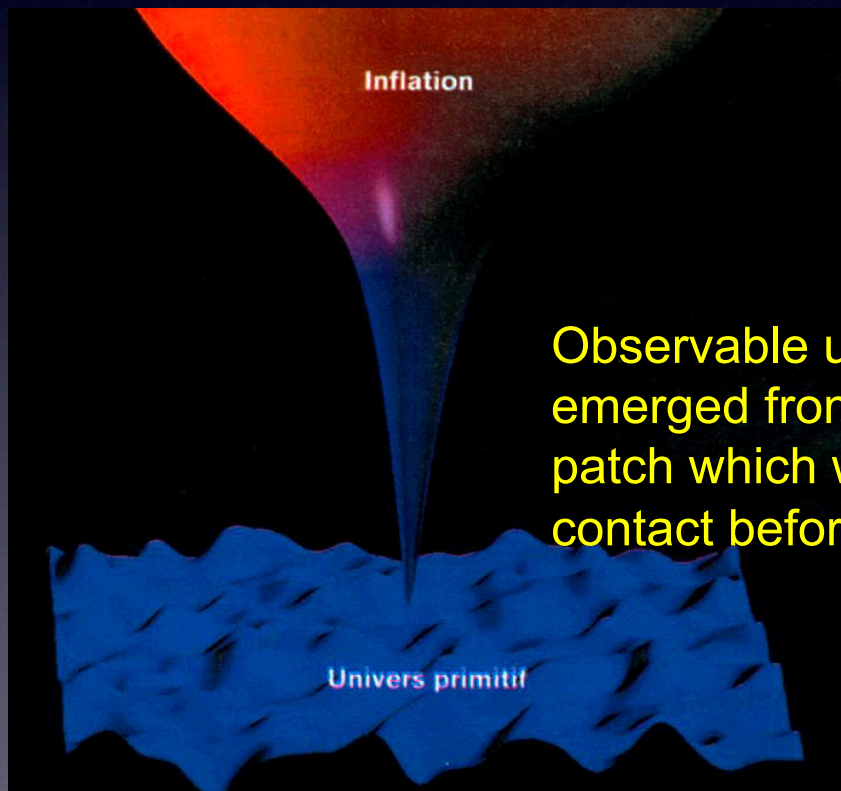
A. Guth ('81), A. D. Linde,
A. Albrecht and P. J. Steinhard,
V.F. Mukhanov, G.V. Chibisov,
A.H. Guth and S.Y. Pi,
A.A. Starobinsky, S.W. Hawking

- ▶ The “Flatness Problem”: Why is the universe so flat? → Solved!
- ▶ The “Horizon Problem”: Why is the universe so homogenous. In particular, why is the CMBR so uniform (isotropic on large scales)?

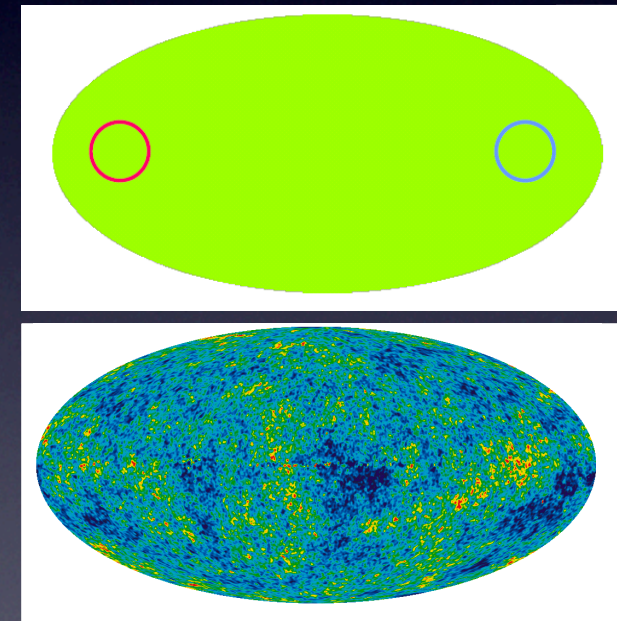


Why inflation?

- ▶ The “Flatness Problem”: Why is the universe so flat? → Solved!
- ▶ The “Horizon Problem”: Why is the universe so homogenous. In particular, why is the CMBR so uniform (isotropic on large scales)? → Solved!



Observable universe emerged from a small patch which was in causal contact before inflation



✓ Plus: Quantum fluctuations of the inflaton field can be seed of structure ...

How can inflation be realised?

- ▶ Basic formula: Einstein's equations of General Relativity

Λ : Cosmological constant

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R + \Lambda g_{\mu\nu} = 8\pi G_N T_{\mu\nu}$$

Metric $g_{\mu\nu}$: Gravity \leftrightarrow
geometry of space-time

Energy momentum tensor:
represents particle theory &
content of the universe



How can inflation be realised?

- ▶ Simple and attractive possibility: **Slowly rolling scalar field ϕ** (minimally coupled to gravity)

$$T_{\mu\nu} = \partial_{\mu}\phi\partial_{\nu}\phi - g_{\mu\nu} \left(\frac{1}{2}\partial_{\rho}\phi\partial_{\rho}\phi + V(\phi) \right)$$

If the vacuum energy $V(\phi)$ dominates:

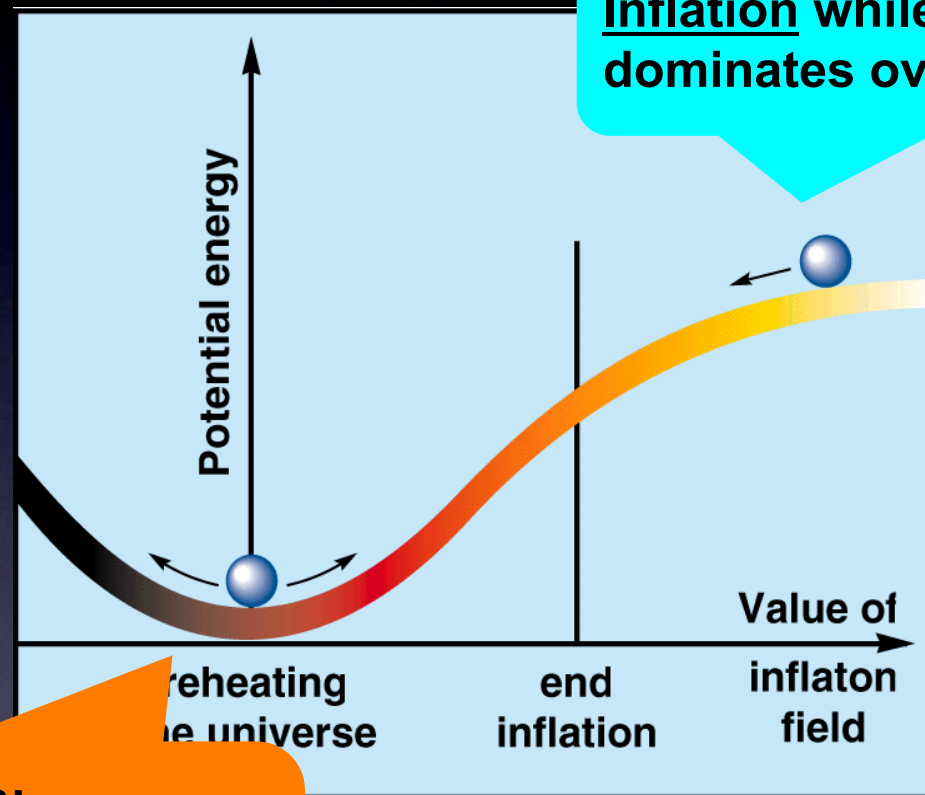
$$\Rightarrow a(t) = \exp \left(\sqrt{\frac{8\pi G_N V(\phi)}{3}} t \right)$$

and the universe “inflates”!

Important: **The field ϕ is dynamical \Rightarrow inflation can end!**



Dynamics during and after inflation



Inflation while vacuum energy dominates over kinetic energy

Decays of the inflaton:

→ matter & antimatter, and possibly their asymmetry get produced!

Requirements for realising inflation

- ▶ “Slow roll” inflation: Vacuum energy has to dominate over kinetic energy!

- “Slow roll parameters” small: $\epsilon, |\eta|, \xi \ll 1$, $V \sim V_0$ dominates

$$\epsilon = \frac{M_P^2}{2} \left(\frac{V'}{V} \right)^2, \quad \eta = M_P^2 \left(\frac{V''}{V} \right), \quad \xi = M_P^4 \left(\frac{V' V'''}{V^2} \right)$$

“slope of V”

“inflaton mass”



The η -problem

- ▶ Challenge for realising inflation: Flat enough potential,

$$m_\phi \ll \mathcal{H}$$

- Generic (effective field theory)

$$\mathcal{H} = \frac{\sqrt{V}}{\sqrt{3}M_P}$$

$$V \subset V_0 \frac{\phi^\dagger \phi}{M_P^2} \Rightarrow m_\phi \sim \mathcal{H} \leftrightarrow \eta \sim 1$$

- In supergravity (with $K = \phi^* \phi$ and V_0 from F-term)

$$V_F = e^{K/M_P^2} \left(K^{i\bar{j}} D_i W D_{\bar{j}} W^* - \frac{3|W|^2}{M_P^2} \right)$$
$$V_F \sim \left(1 + \frac{\phi^\dagger \phi}{M_P^2} + \dots \right) V_0 \quad \text{with } D_i W := W_i + K_i W$$

E.J Copeland, A.R. Liddle, D.H. Lyth, E.D. Stewart, D. Wands ('94)



Approaches to solve the η -problem: 3 strategies in supergravity

- Expansion of K in fields/ M_P :

*requires tuning of parameters!
(at 1%-level)*

$$K = |\phi|^2 + \frac{\lambda_\phi}{M_P^2} |\phi|^4 + \frac{\lambda_{\phi i}}{M_P^2} |\phi|^2 |X_i|^2 + \dots$$

- 'Shift' symmetry:

$$\phi \rightarrow \phi + i\alpha$$

*protects $\text{Im}[\phi]$ from obtaining
a SUGRA mass by symmetry!*

$$K = f(\phi + \phi^*)$$

(used in many works ...)

- Heisenberg symmetry:

*solves the η -problem for $|\phi|$ by
symmetry!*

$$T \rightarrow T + i\beta, \quad T \rightarrow T + \alpha^* \phi + |\alpha|^2/2, \quad \phi \rightarrow \phi + \alpha$$

$$K = f(\rho), \quad \text{with} \quad \rho = T + T^* - |\phi|^2$$

T: 'modulus field' \rightarrow has to be stabilised

Binetruy, Gaillard ('87),
Gaillard, Murayama, Olive ('95),
S.A., Bastero-Gil, Dutta, King, Kostka ('08,'09)



Approaches to solve the η -problem: 3 strategies in supergravity

▶ Expansion of K in fields/ M_P :

▶ 'Shift' symmetry:

Remark:

Symmetries have to be broken
to allow for slope of $V(\phi)$!
→ approximate symmetries

▶ Heisenberg symmetry:



Can the inflaton field be a Gauge Non-Singlet in SUGRA inflation?

Note: ... incomplete table!

*) problems pointed out by Brax et al ('06), Davis, Postma ('08)

	K expansion + tuning	Shift symmetry	Heisenberg symmetry	Non-singlet Inflaton
Singlet inflaton in 'Hybrid Inflation'	(yes) Copeland et al; Dvali, Shafi, Schaefer ('94)	X*	X	X
H is the inflaton in 'New Inflation'	(yes) Shafi, Senoguz ('04)	X (?)	X (?)	yes
Matter field inflaton in 'Tribrid Inflation'	(yes) S.A., Bastero-Gil, King, Shafi ('04)	yes S.A., Dutta, Kostka ('09) Postma, Mooij ('10)	yes S.A., Bastero-Gil, Dutta, King, Kostka ('08)	yes S.A., Bastero-Gil, Baumann Dutta, King, Kostka ('10)
Singlet large field 'Chaotic Inflation'	X	yes Kawasaki et al ('00)	yes S.A., Bastero-Gil, Dutta, King, Kostka ('09)	X



Unified Matter Inflation in SUSY GUTs

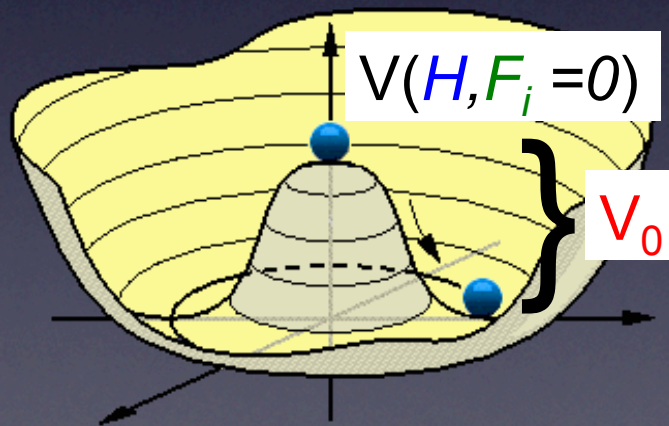
- ▶ New class of models: 'Tribrid Inflation'

$$W = S(\bar{H}H - M^2) + \frac{1}{\Lambda} (\bar{F}F_i)(\bar{H}H)$$

Driving field
(its F-term provides
the vacuum energy)

Waterfall fields
(= Higgs fields that give
mass to the matter fields)

Inflaton field(s)
(are here gauge non-singlets)



S.A., M. Bastero-Gil, J. Baumann, K. Dutta, S. F. King, P. M. Kostka ('10)



Unified Matter Inflation in SUSY GUTs

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Driving field

(its F-term provides the vacuum energy)

Waterfall fields

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Inflaton field(s)

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The Unified Matter Superparticle:

$$16_i = (q_L \quad u_R^c \quad e_R^c \quad d_R^c \quad \ell_L \quad \nu_R^c)_i$$

Right-handed neutrinos: Get their large masses after inflation and induce small masses of light ν 's

Example: SO(10) GUTs

F_i in representation 16 of SO(10)

\bar{F} in representation $\bar{16}$ of SO(10)

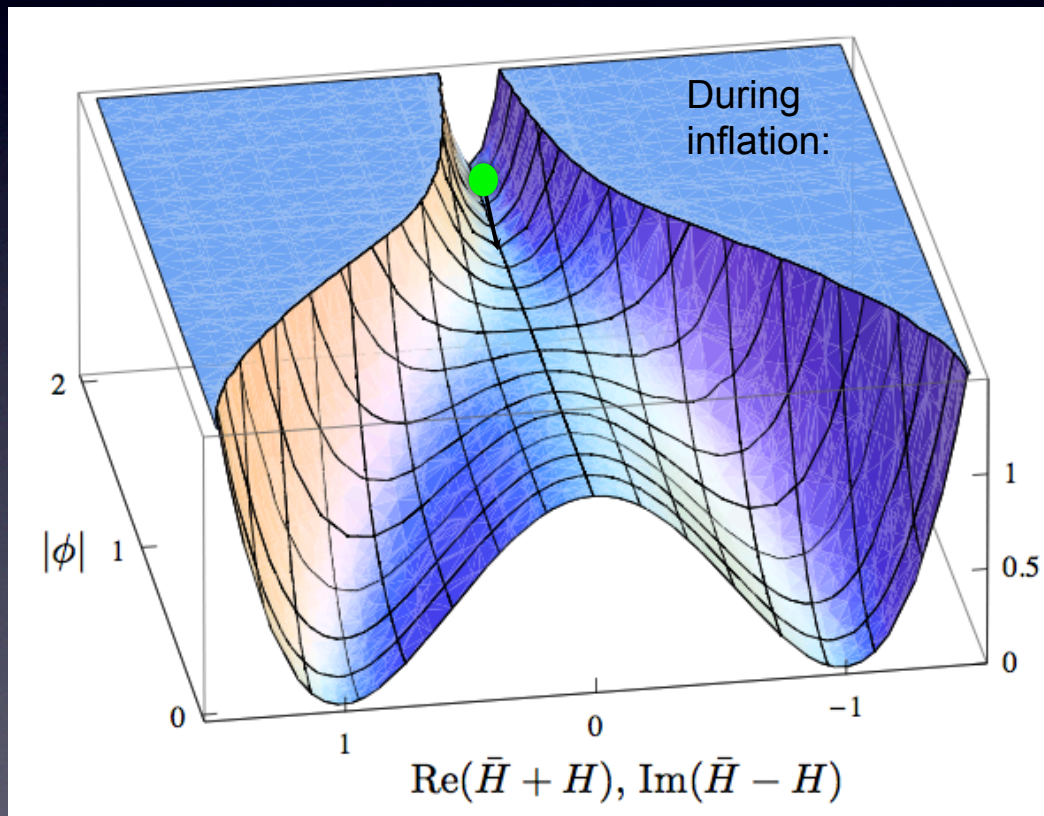
$i = (1, \dots, 4)$

S.A., M. Bastero-Gil, J. Baumann, K. Dutta, S. F. King, P. M. Kostka ('10)



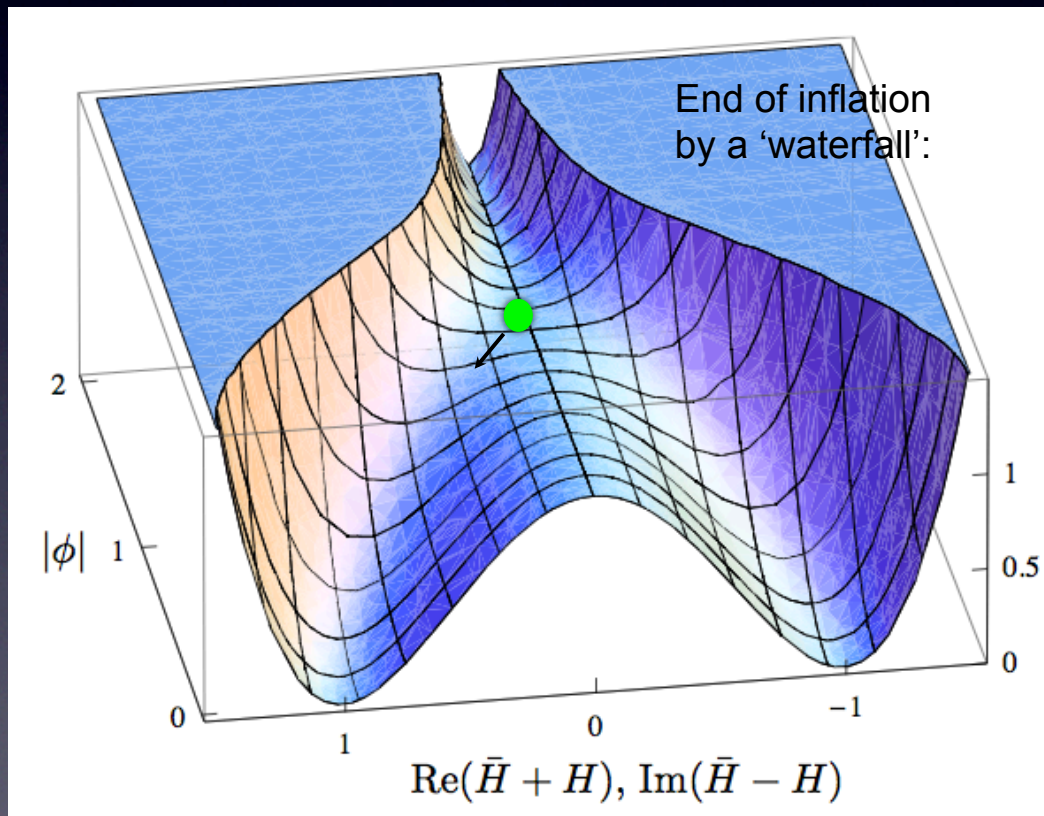
Unified Matter Inflation in SUSY GUTs

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Unified Matter Inflation in SUSY GUTs

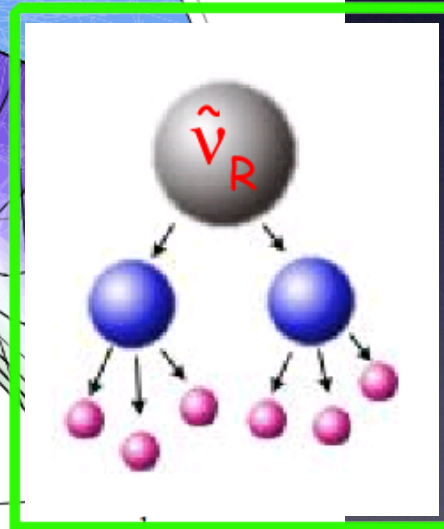
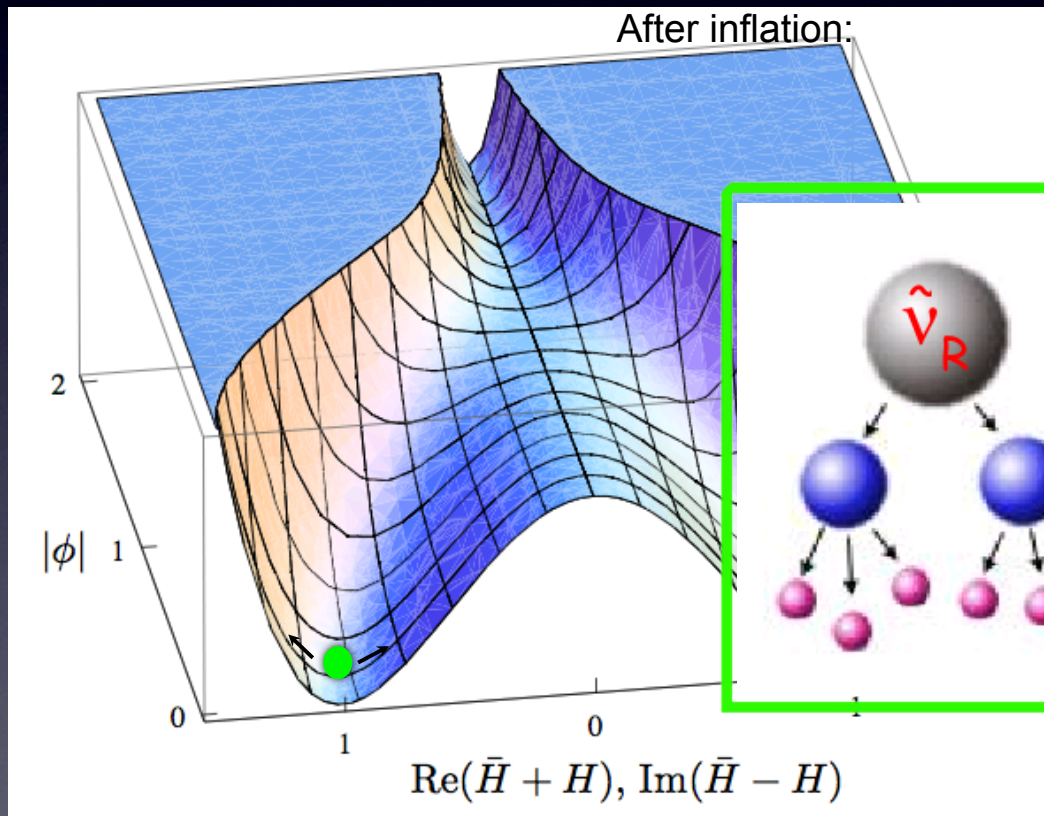
$$W = S(\bar{H}H - M^2) + \frac{1}{\Lambda}(\bar{F}F_i)(\bar{H}H)$$



Non-thermal Leptogenesis after Inflation

When the $\tilde{\nu}_R$ component dominates the universe after inflation ...

$$\mathbf{16}_i = (q_L \quad u_R^c \quad e_R^c \quad d_R^c \quad \ell_L \quad \nu_R^c)_i$$



⇒ The matter-antimatter asymmetry of the universe can be generated very efficiently via the (non-thermal) leptogenesis mechanism!

Recent study in 'Tribrid (sneutrino) inflation':
S.A., Baumann, Domcke, Kostka ('10)



Unified Matter Inflation in SUSY GUTs

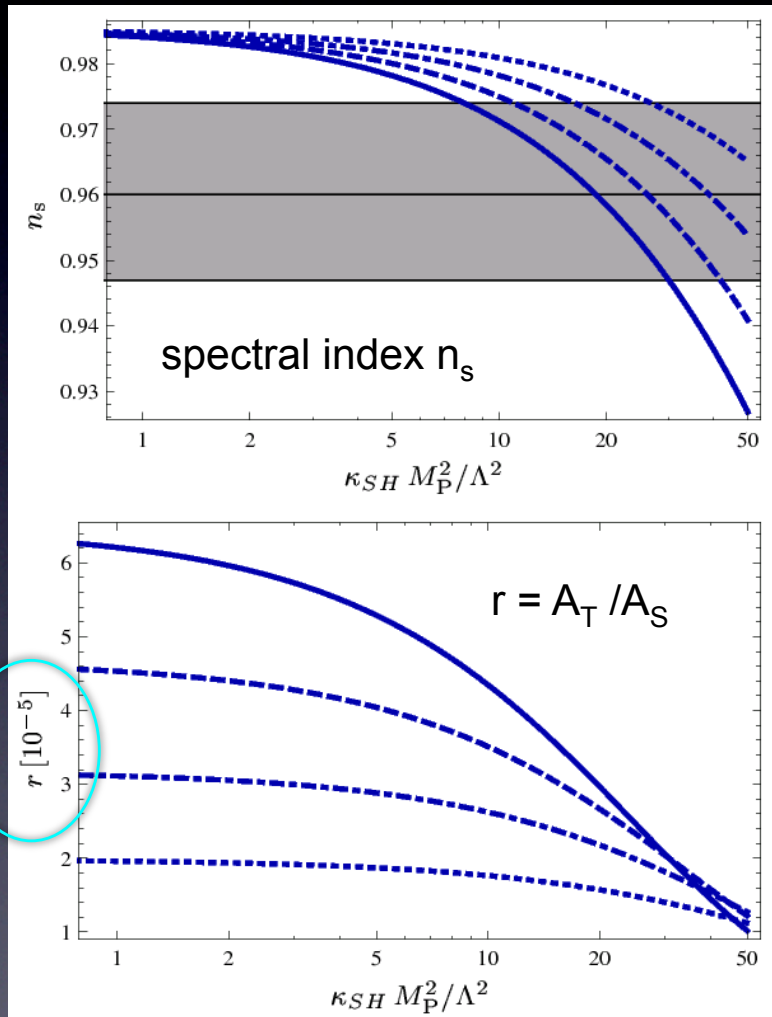
- ▶ Various challenges for such 'Gauge Non-Singlet' (GNS) inflation models ... all resolved:
 - ✓ SUGRA η -problem can be solved by Heisenberg symmetry:
 - ✓ '2-loop gauge η -problem' (Dvali '95) solved
 - ✓ Monopole problem can be solved
 - ✓ Modulus ρ stabilized by large vacuum energy V_0 during inflation

S.A., M. Bastero-Gil, J. Baumann, K. Dutta, S. F. King, P. M. Kostka ('10)

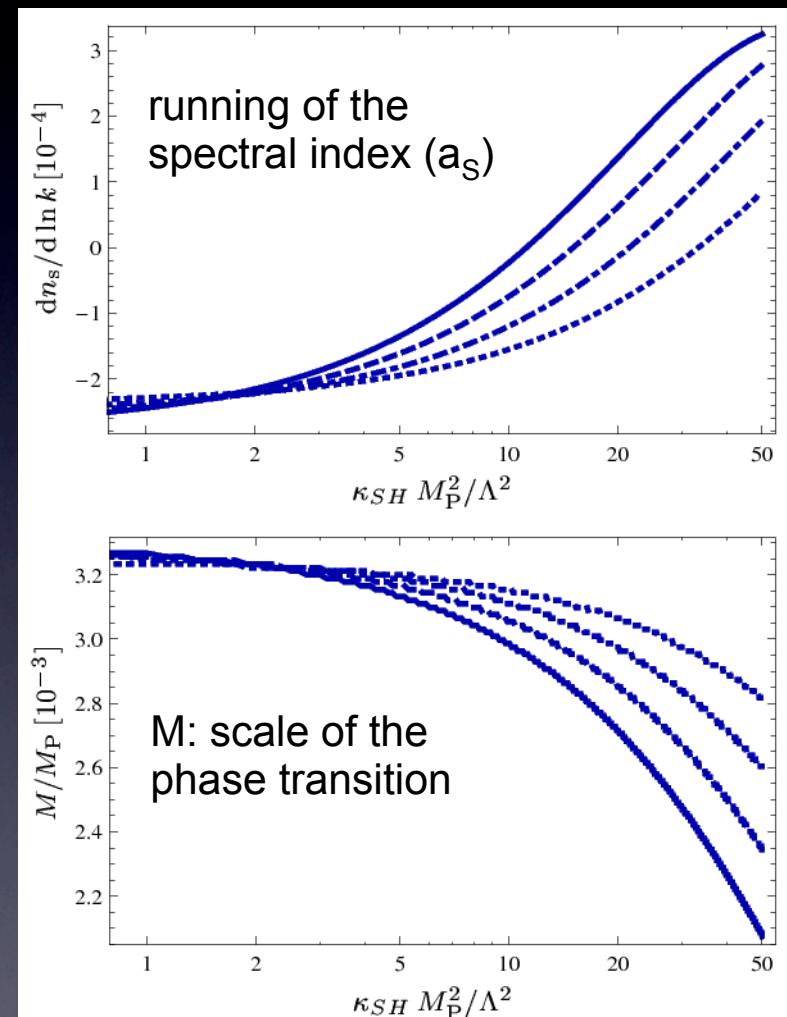


In an explicit model: calculation of the predictions for CMB observables ...

S.A., K. Dutta, P. M. Kostka ('09)



very small
(as typical for Hybrid models)



Example: predictions in toy model of "Tribrid inflation"



Conclusions and Outlook

- Cosmic inflation: A successful paradigm for the early universe
 - Challenge: The η -problem
 - Big open question: How connected to particle physics?
- New class of inflation models in supergravity: ‘Tribrid Inflation’
 - The η -problem can be solved, e.g., by a Heisenberg symmetry
 - The inflaton can reside in the matter sector of the theory
- Attractive inflaton candidate: The ‘Unified Matter Superparticle’
- Outlook: Generalisation of this scenario may also open up new ways to realise inflation in string theory ...

S.A., Dutta, Erdmenger, Halter (in preparation)

