



# **Jet and Event Shape Observables at LHC**

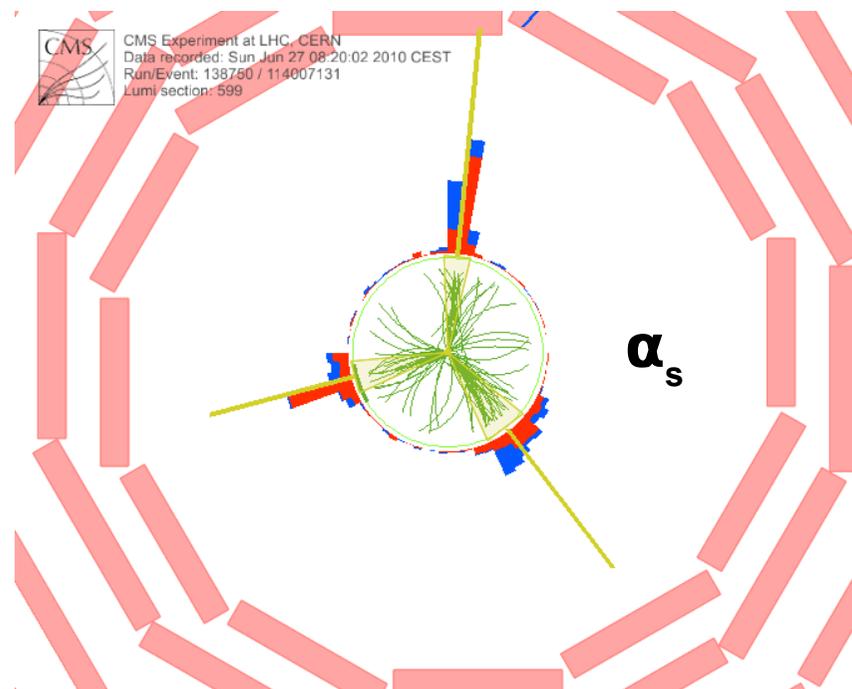
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Institut für Experimentelle Kernphysik**



Karlsruhe Institute of Technology

# The Menu

- Experimental Uncertainties
- Absolute Measurements
- Shape Measurements
- Ratio Measurements
- Discussion



**QCD** at work ...

Experiment Pages for public Results:

**ATLAS public results:** <https://twiki.cern.ch/twiki/bin/view/AtlasPublic>

**CMS public results:** <https://twiki.cern.ch/twiki/bin/view/CMSPublic/PhysicsResults>

**ALICE publications:** <http://aliweb.cern.ch/Documents/generalpublications>

**LHCb publications:** <https://lhcb-doc.web.cern.ch/lhcb-doc/Published Papers/default.htm>

**No extractions of  $\alpha_s$  from LHC yet, good time for this workshop ...**



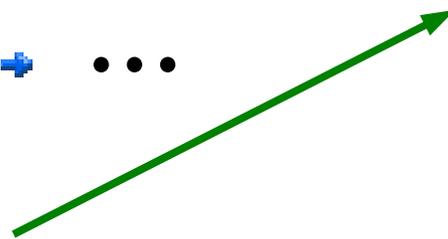
# Jet Analysis Uncertainties

- **Experimental Uncertainties**  
(~ in order of importance):

- ➔ **Jet Energy Scale (JES)**
  - ➔ Noise Treatment
  - ➔ Pile-Up Treatment
- ➔ **Luminosity**
- ➔ Jet Energy Resolution (JER)
- ➔ Trigger Efficiencies
- ➔ Resolution in Rapidity
- ➔ Resolution in Azimuth
- ➔ Non-Collision Background
- ➔ ...

- **Theoretical Uncertainties:**

- ➔ PDF Uncertainty
- ➔ pQCD (Scale) Dependence
- ➔ Non-perturbative Corrections
- ➔ PDF Parameterization
- ➔ NLO-NLL matching schemes
- ➔ Electroweak Corrections
- ➔ **Knowledge of  $\alpha_s(M_Z)$**
- ➔ ...



This is what we want to improve on here

# Luminosity

Common to all cross section measurements:

Initial Uncertainty: **11%**

ATLAS arXiv:1101.2185v1, CMS-PAS-EWK-10-004

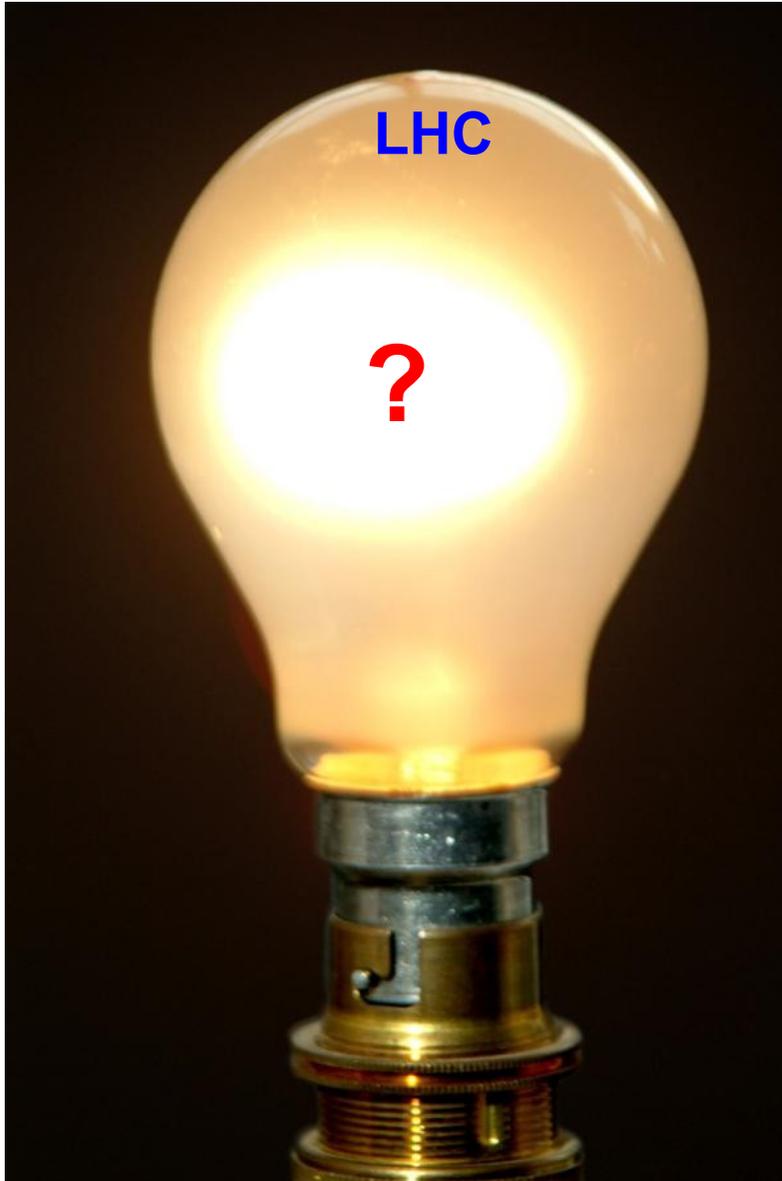
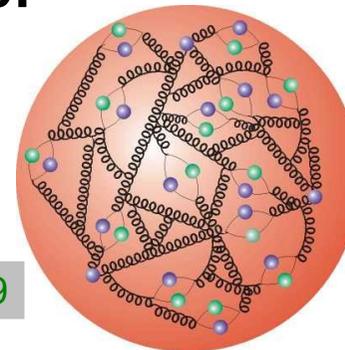
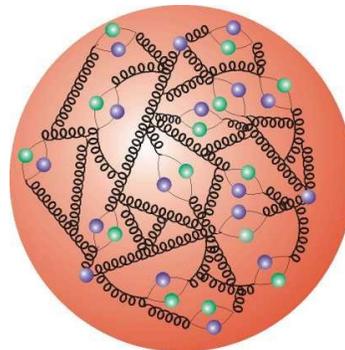
From van-der-Meer Scans:  
Uncertainty dominated (10%) by  
beam intensity measurement

Ultimately achievable:

↘ **5% ?**

**?**

S.White: CERN-THESIS-2010-139



HERA-Proton, DESY

# Jet Energy Scale

Pre-Data Assumptions:  $\sim 10\%$   $\rightarrow$  up to 60% uncertainty on cross sections

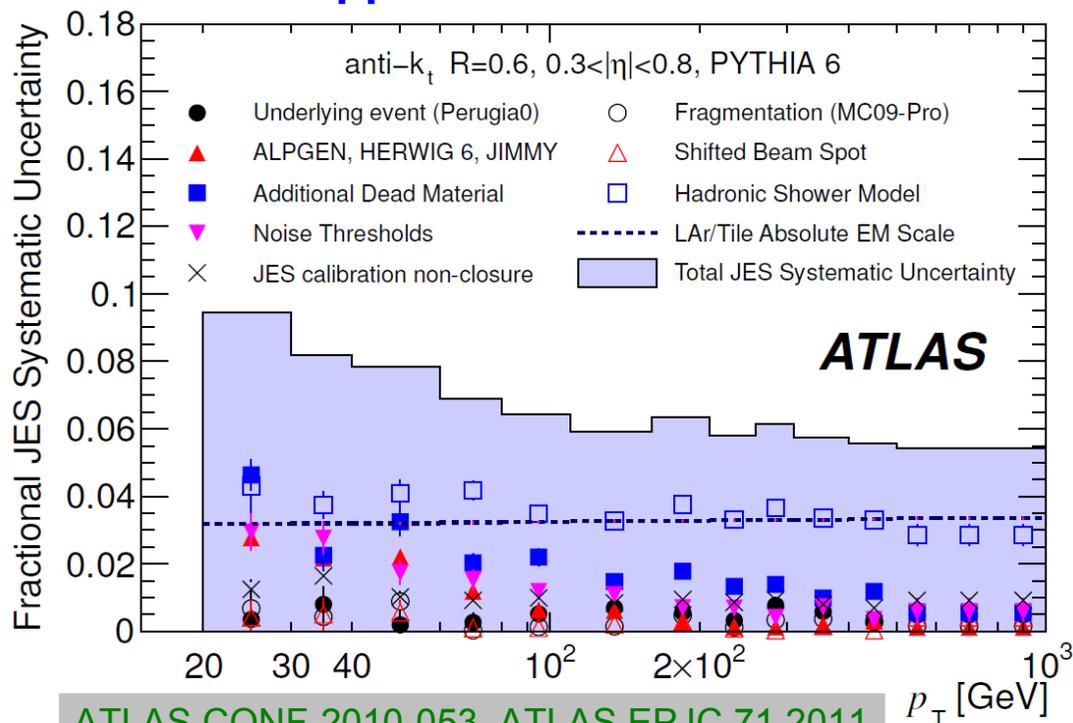
This year at ICHEP and later: 5 - 10%

Very good detector performances observed, MC modelling works better than anticipated.

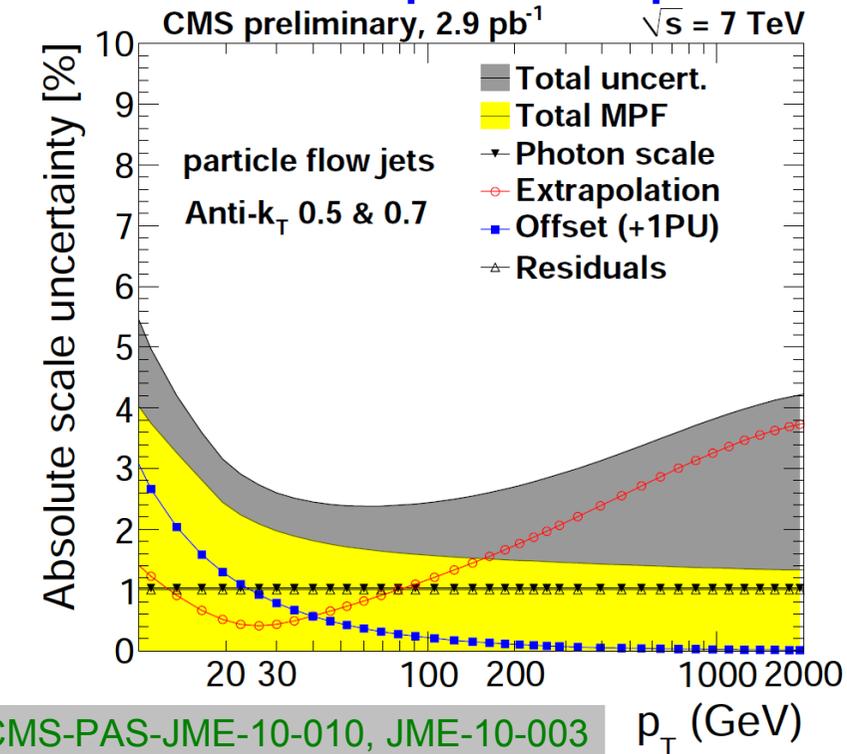
Can expect further improved results from both experiments ...

Enormous progress, took years at Tevatron.

## Applied in ICHEP results

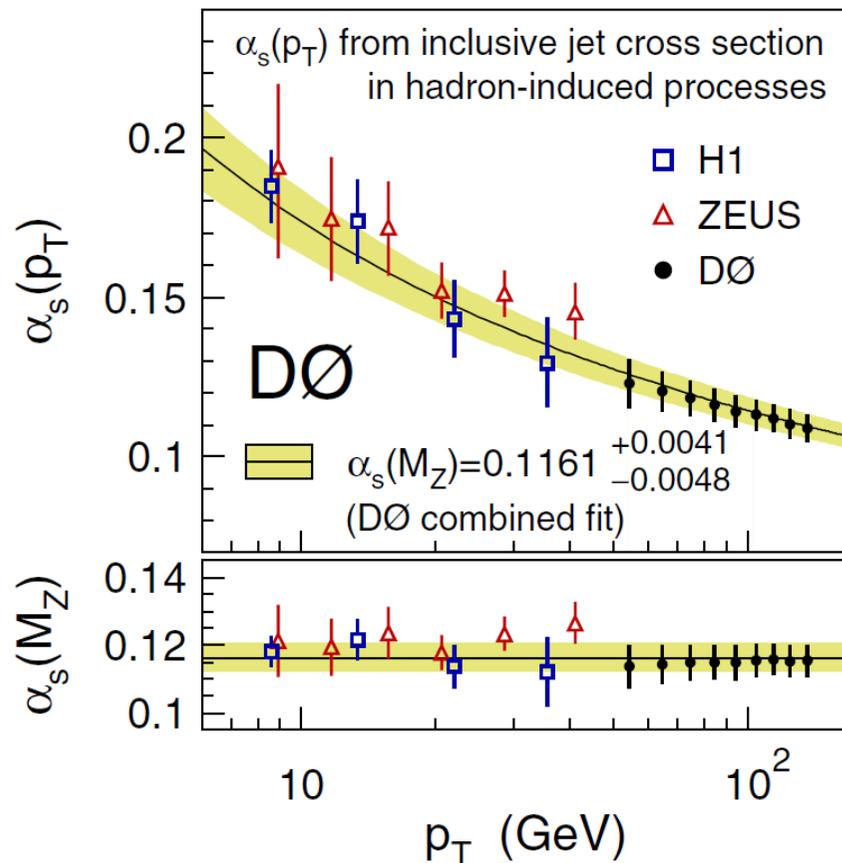


## Derived from 2.9/pb until Sep. 2010



# Absolute Measurements

Affected directly by large systematic uncertainties: **JES, Luminosity, JER**  
 Need to be careful to avoid circular reasoning when also used in PDFs  
**Not an easy way to go ...**



Prospect of still improving a lot on  
 systematic experimental uncertainties at LHC

← Allows to measure  $\alpha_s(p_T)$

CDF 2002:  $\alpha_s = 0.1178 + 0.0081 - 0.0095$   
 DØ 2009:  $\alpha_s = 0.1161 + 0.0041 - 0.0048$

CDF PRL88 2002, DØ PRD80 2009

# Available Results

Range in transverse momentum (ICHEP):  $\sim 0.7$  TeV (Tevatron limit)

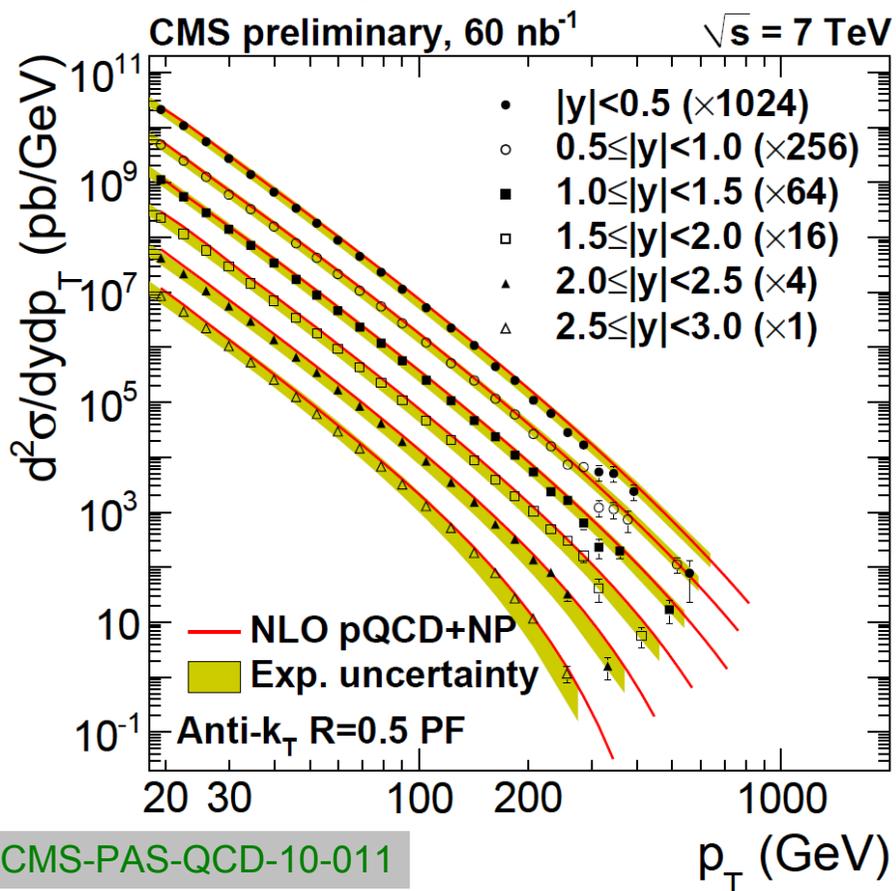
Range in dijet mass (ICHEP):  $\sim 1.5$  TeV

Rapidities up to: 2.8 (ATLAS), 3.0 (CMS)

1000 times more luminosity about to be evaluated!

Z.Nagy,  
NLOJet++  
PRD68 2003  
PRL88 2002

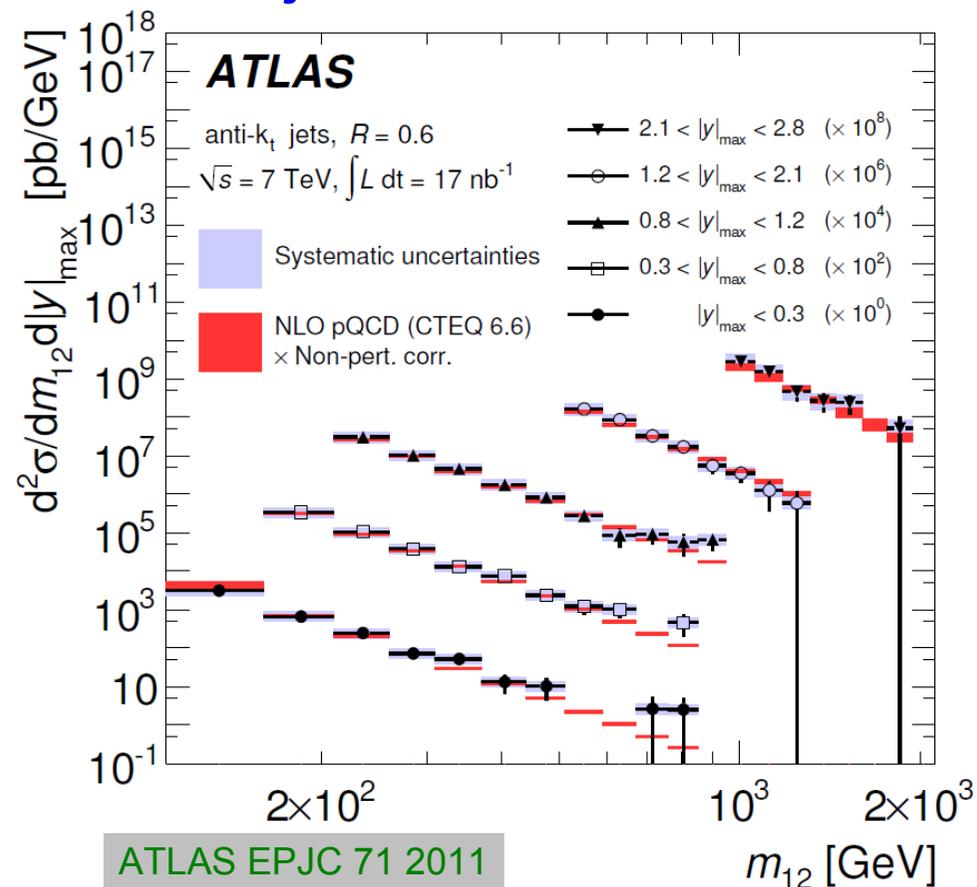
## Inclusive jet $p_T$ cross section



CMS-PAS-QCD-10-011

Klaus Rabbertz

## Dijet mass cross section



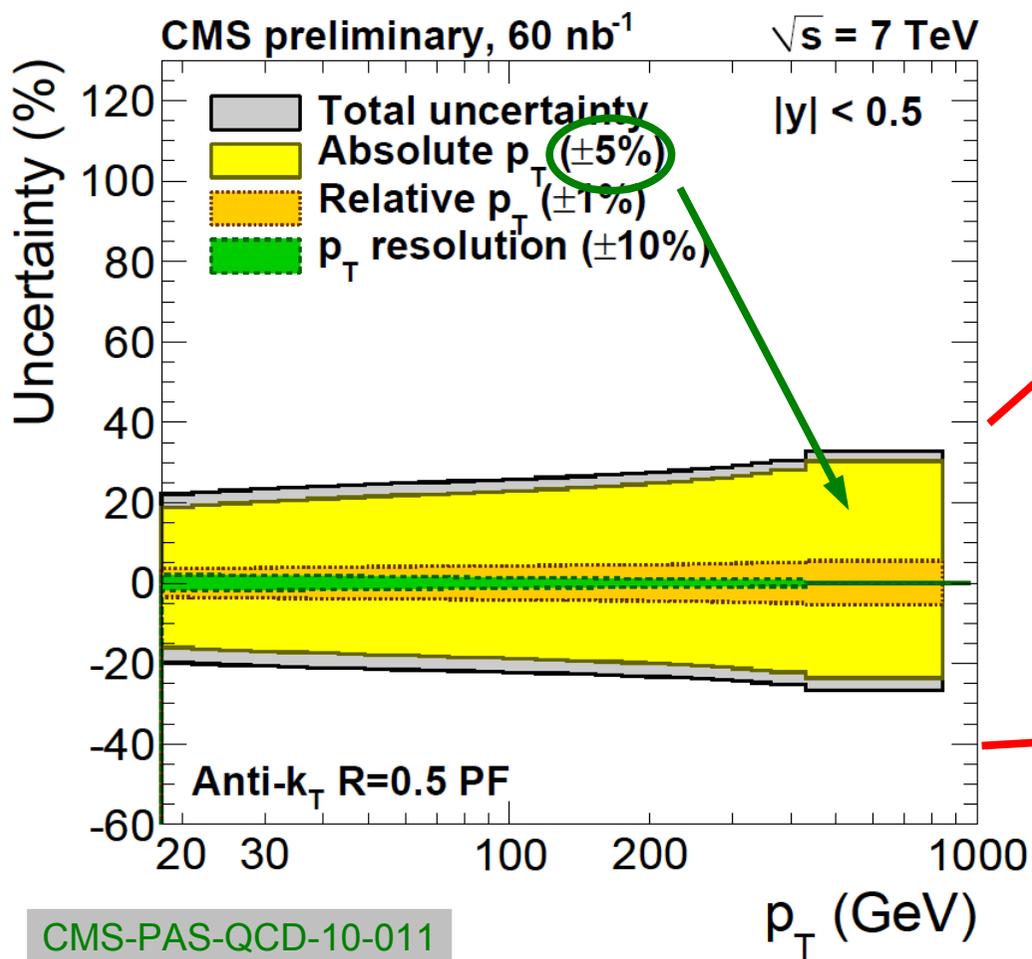
ATLAS EPJC 71 2011

$\alpha_s$ -Workshop 2011

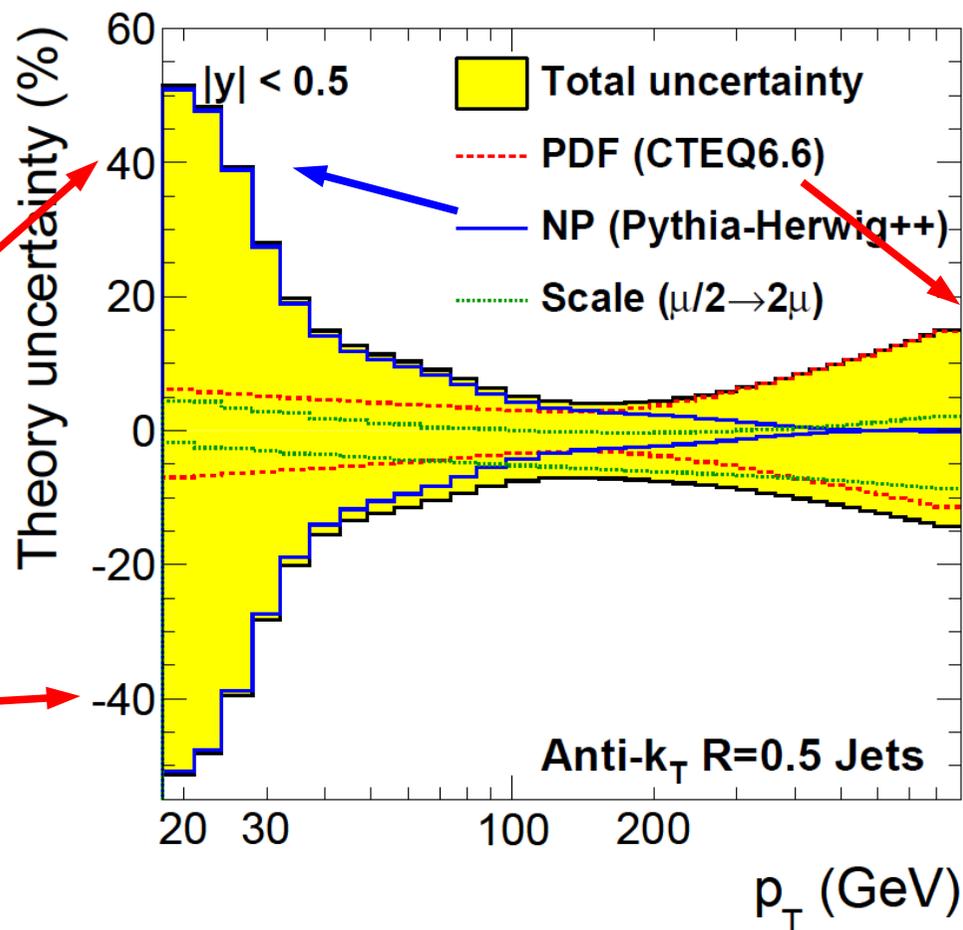
# Contrasting Uncertainties

Dominant: **JES**  
 Luminosity: **11%, not shown**

Dominant at low  $p_T$ : **NP Corrections**  
 at high  $p_T$ : **PDF**



40%

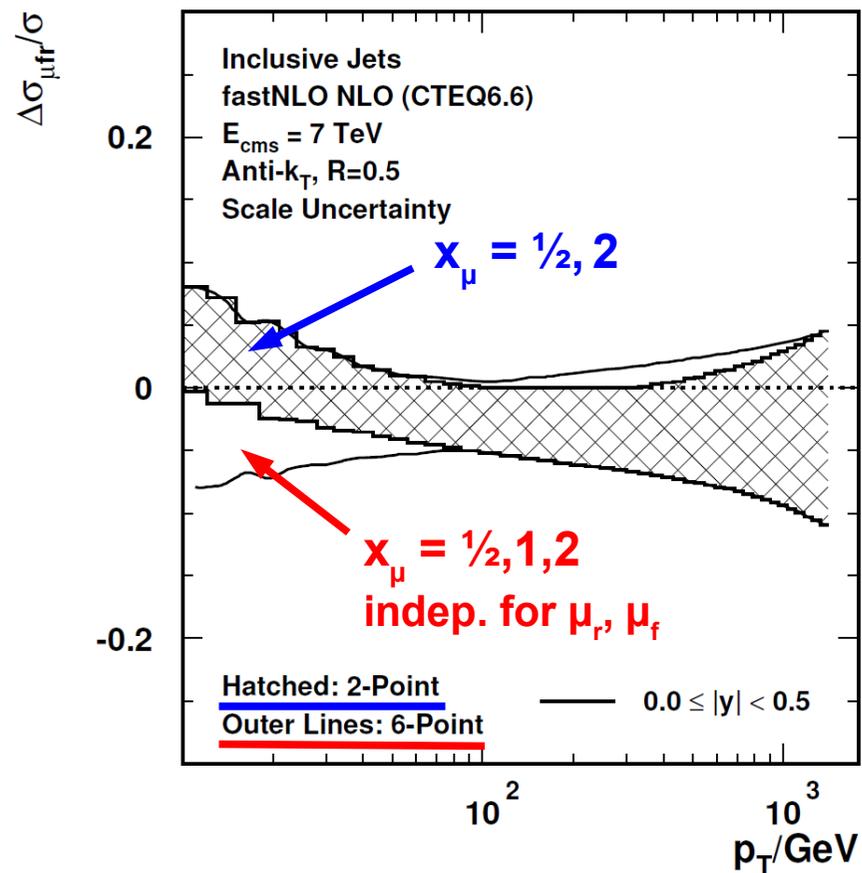


# Scale and PDF revisited

## Asymmetric scale variations:

Independent variation of  $\mu_r$  and  $\mu_f$

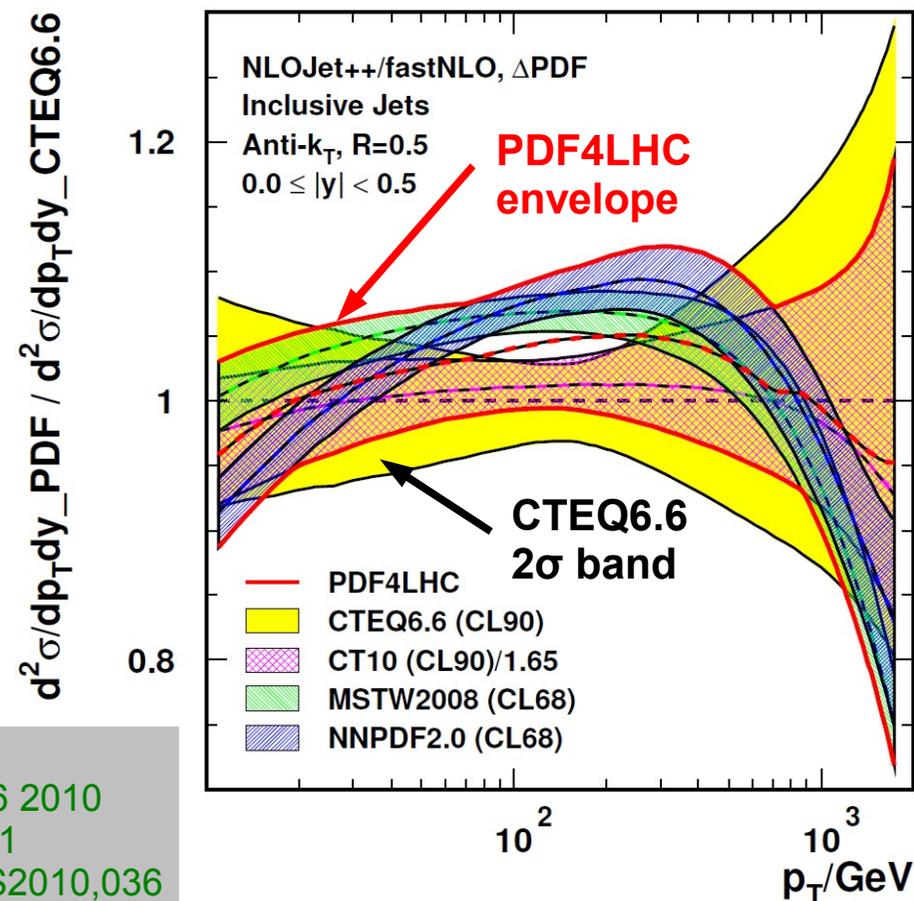
by factors of  $\frac{1}{2}$  and 2 avoiding rel. factors of 4  
 (6-point:  $(\frac{1}{2}, \frac{1}{2}), (\frac{1}{2}, 1), (1, \frac{1}{2}), (1, 2), (2, 1), (2, 2)$ )  
 Compared to symmetric variation (2-point)



See e.g.:  
 A.Banfi et al., JHEP06 2010  
 ATLAS EPJC 71 2011  
 J. Huston, POSCI, DIS2010,036

## A la PDF4LHC:

Envelope of predictions of CTEQ, MSTW and NNPDF at CL68  
 Compared to CTEQ6.6 (CL90)



# NP revisited and $\alpha_s$

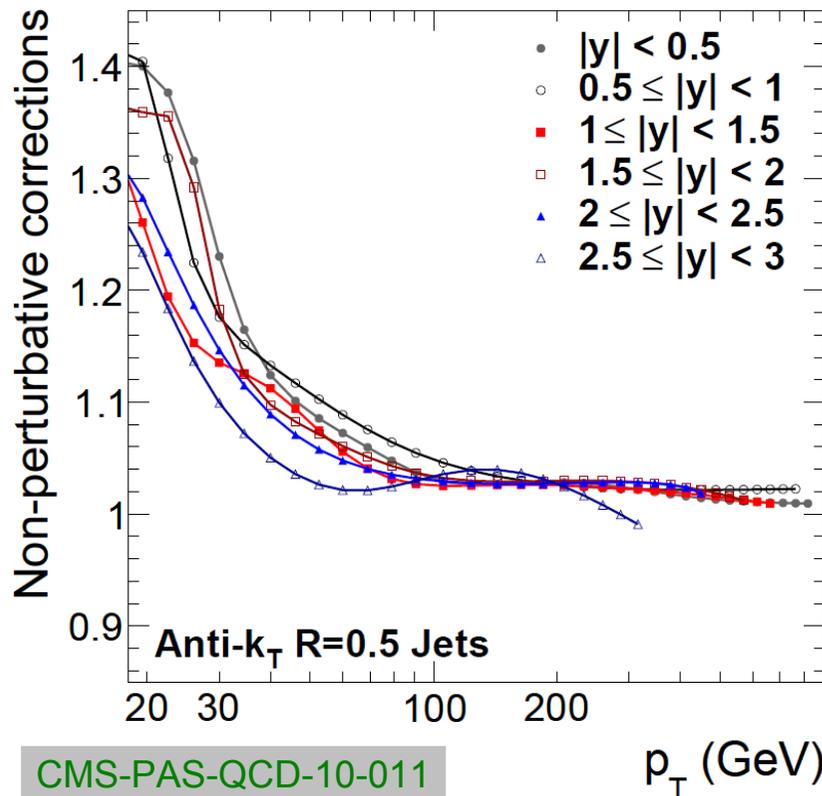
To compare with data correct NLO for:

- Multiple Parton Interactions (MPI)
- Hadronization & Decays (Lund, Cluster)

**POWHEG Box for dijet production to be evaluated!**

S. Alioli et al., arXiv:1012.3380

## NP Correction Factors



CMS-PAS-QCD-10-011

Klaus Rabbertz

Effect of changing  $\alpha_s(M_Z)$  by  $\pm 0.003$ :

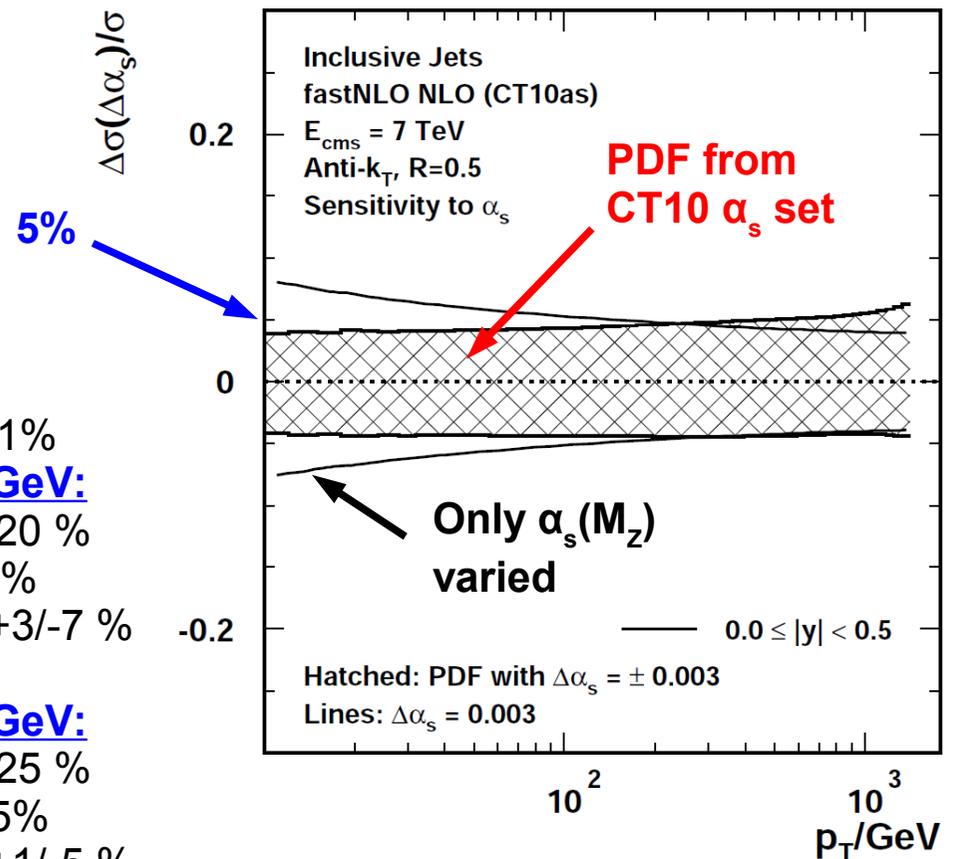
- Either by choosing PDF member (hatched)
- or by changing value separately (lines)

### Recall:

Lumi: 11%  
**at 100 GeV:**  
 JES: ~ 20 %  
 PDF: 5 %  
 Scale: +3/-7 %

### at 500 GeV:

JES: ~ 25 %  
 PDF: 15%  
 Scale: +1/-5 %



Munich, Germany, 10.02.2011

$\alpha_s$ -Workshop 2011

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# Shape Measurements

- **Reduction strategy 1: Normalized distributions**

- ➔ **No luminosity uncertainty**
- ➔ **Reduced sensitivity to jet energy scale (JES) or resolution (JER)**

- **Jet angular measurements**

- ➔ **Dijet chi distribution: Nice for new physics, not for  $\alpha_s$  ...**
- ➔ **Dijet azimuthal decorrelation: Sensitive to QCD radiation,  $\rightarrow \alpha_s$  ?**

NLO available, resummation in progress: [A. Banfi, arXiv:0906.4958](#)

- **Event shapes**

- ➔ **Long tradition of QCD measurements e.g.  $\alpha_s$ , in particular in  $e^+e^-$**

- ➔ **Good description of data requires NLO + resummation**

from NNLO+NLLA:  
[G. Dissertori et al., JHEP08 2009](#)

- ➔ **Transverse thrust, transverse thrust minor,  $y_{23}$  ...**

- ➔ **NLO like above, resummation requires the “global” versions, see**

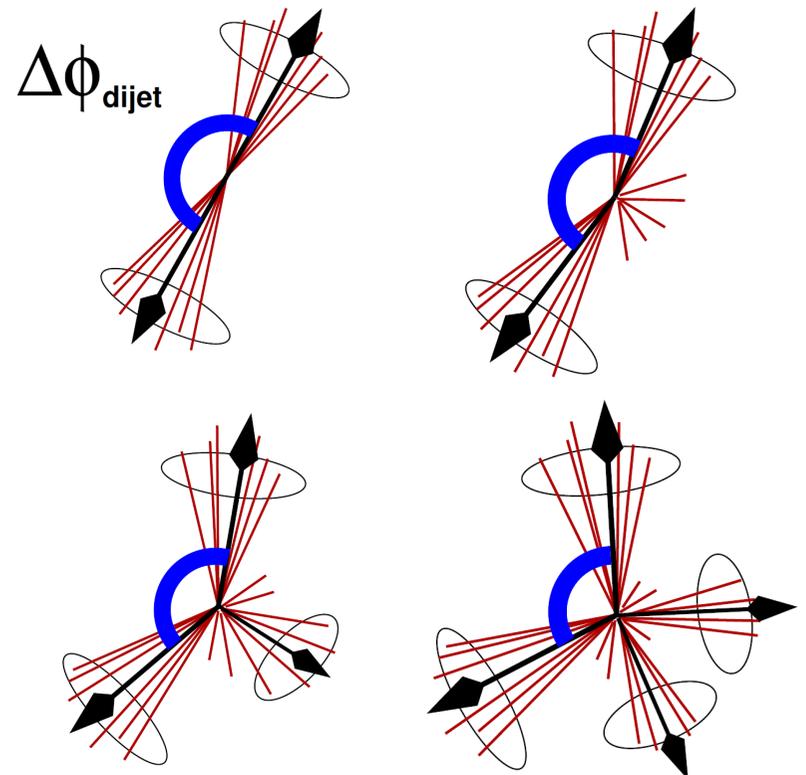
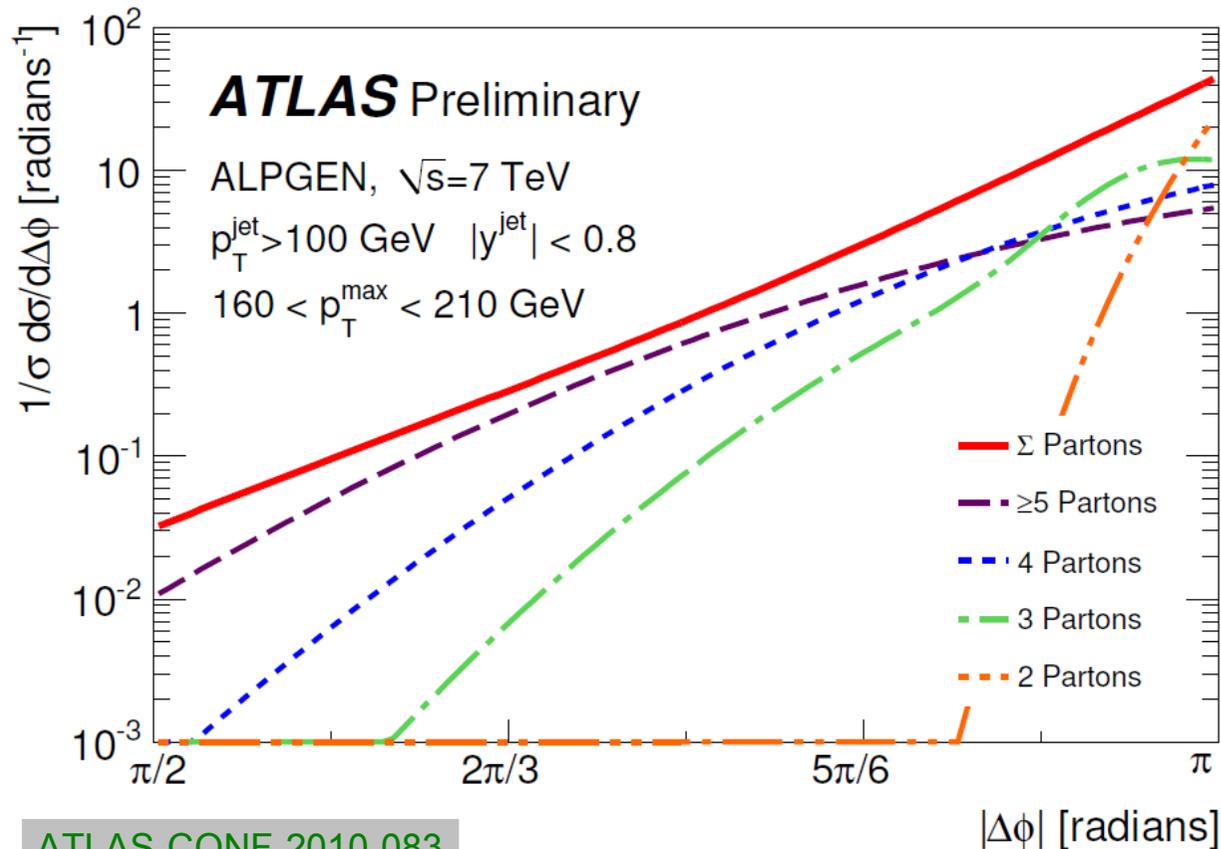
[A. Banfi et al., JHEP06 2010](#)

# Azimuthal Decorrelation

Born limit has dijets with  $|\Delta\Phi| = \pi$

With increasing number of partons smaller separation angles become possible

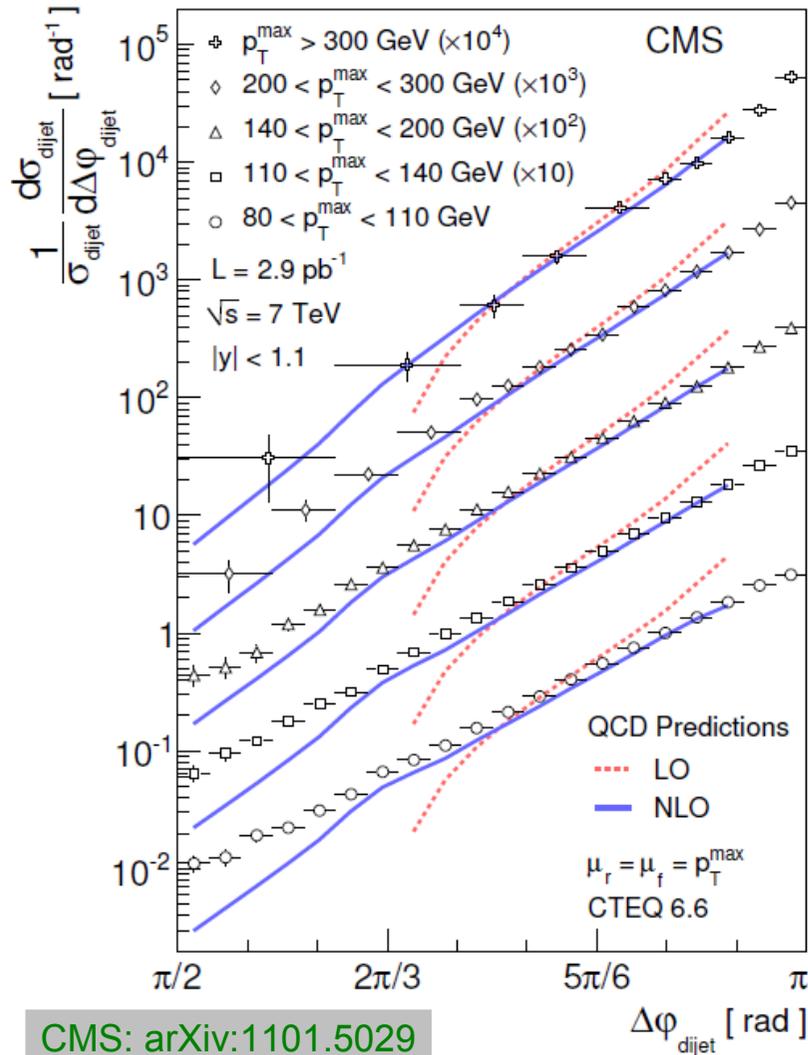
Depends on  $\alpha_s$  ...



ATLAS-CONF-2010-083

# $\Delta\Phi$ : Available Data

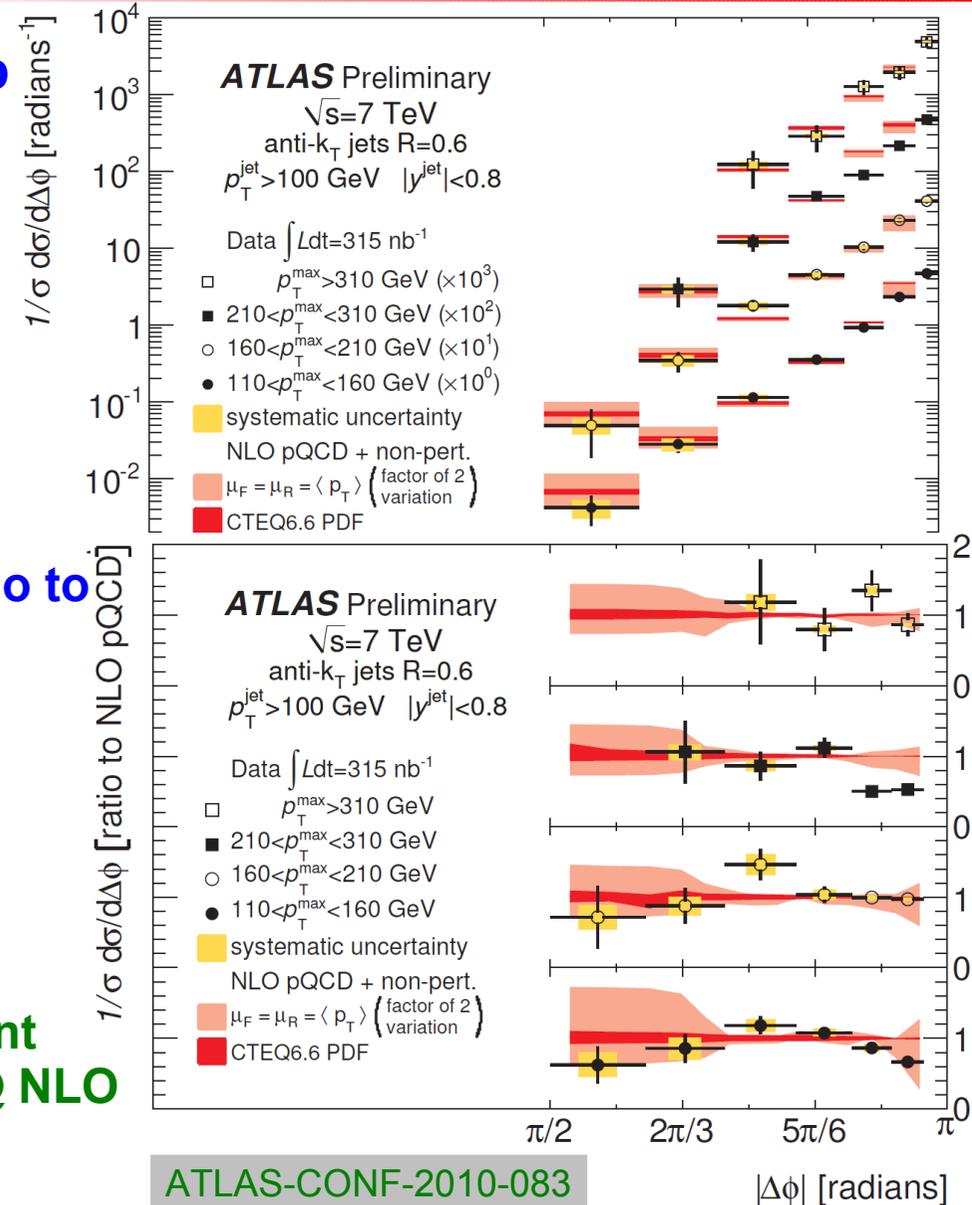
CMS, 2.9 / pb, Exp. Unc.11 - 3% ATLAS, 0.3 / pb



CMS: arXiv:1101.5029

ATLAS, Ratio to pQCD \* NP

Good agreement where pQCD @ NLO



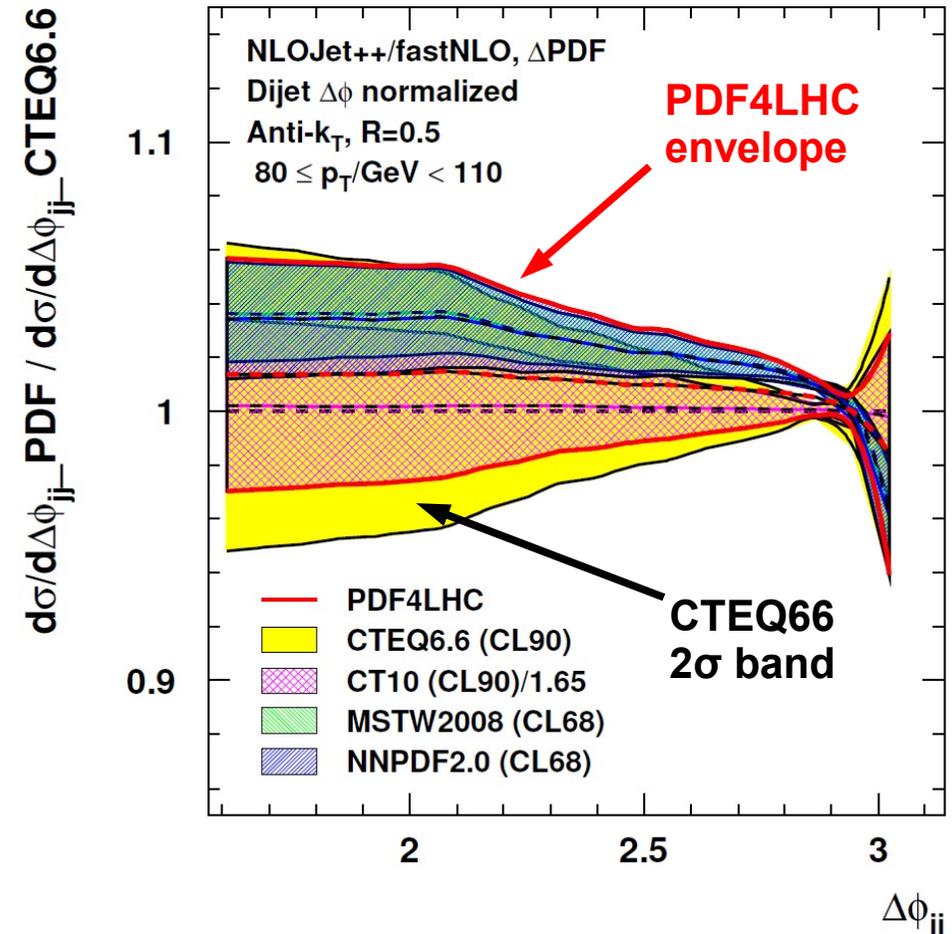
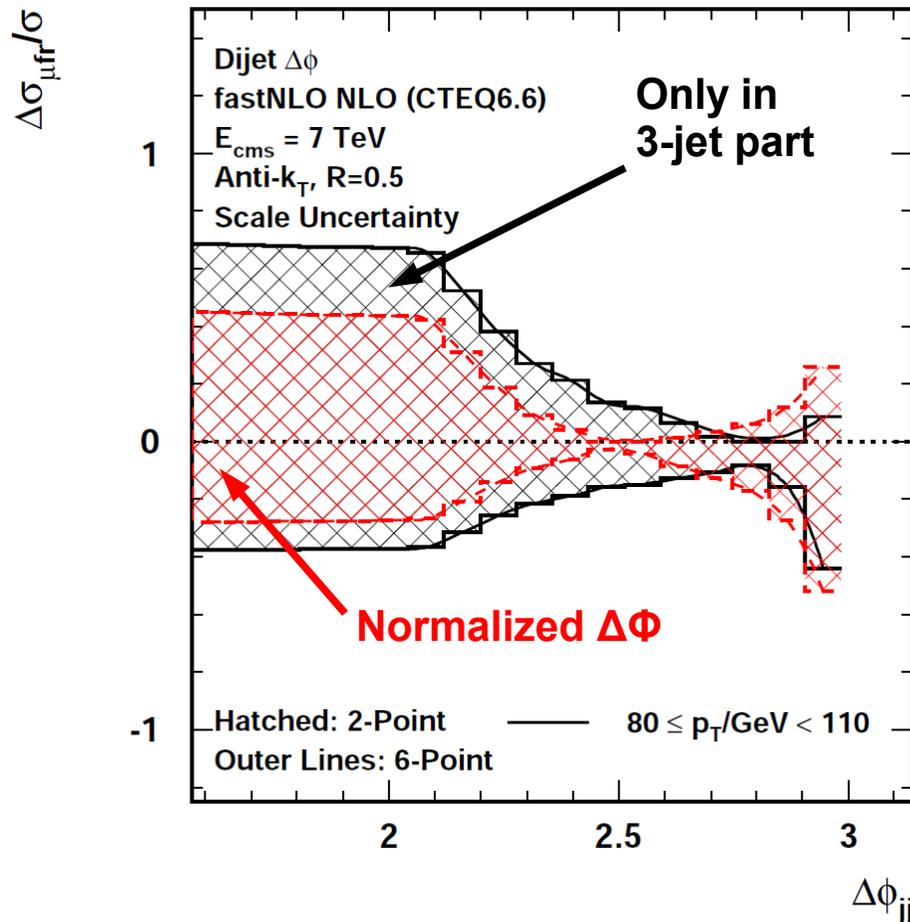
ATLAS-CONF-2010-083

# $\Delta\Phi$ : Scale and PDF

Sensitivity to  $\Delta\alpha_s = \pm 0.003$ :  $\sim 3\%$  (Plot in backup slides)

Look into average  $\Delta\Phi$  (event shape mean) ?

Low  $p_T$  bin:  $80 < p_T / \text{GeV} < 110$



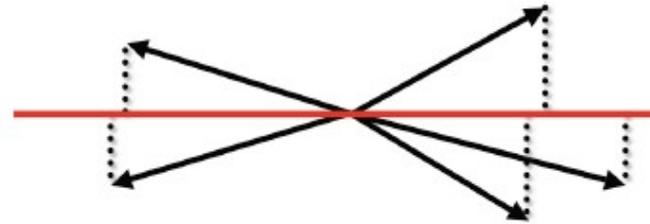
# Event Shapes

## Definition:

Transverse global Thrust

## Similar as Event Shapes in $e^+e^-$ and ep

- In praxis, need to restrict rapidity range:  $|\eta| < 1.3 \rightarrow$  Transverse central thrust
- Less sensitive to JES & JER uncertainty
- No luminosity uncertainty
- Useful for MC tuning

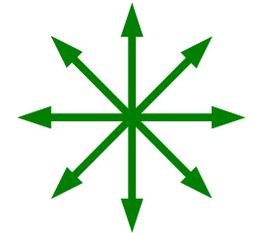


$$T_{\perp,g} \equiv \max_{\vec{n}_T} \frac{\sum_i |\vec{p}_{\perp,i} \cdot \vec{n}_T|}{\sum_i p_{\perp,i}}$$



linear ~ dijet

$$T \longrightarrow 0$$



spherical ~ multijet

$$T \longrightarrow 2/\pi$$

Redefine to get  $\tau_{\perp,g} \equiv 1 - T_{\perp,g} \longrightarrow 0$  in LO dijet case

# Central Thrust: Available Data

Good description by standard MC like Pythia or Herwig++ (NLO not yet checked)

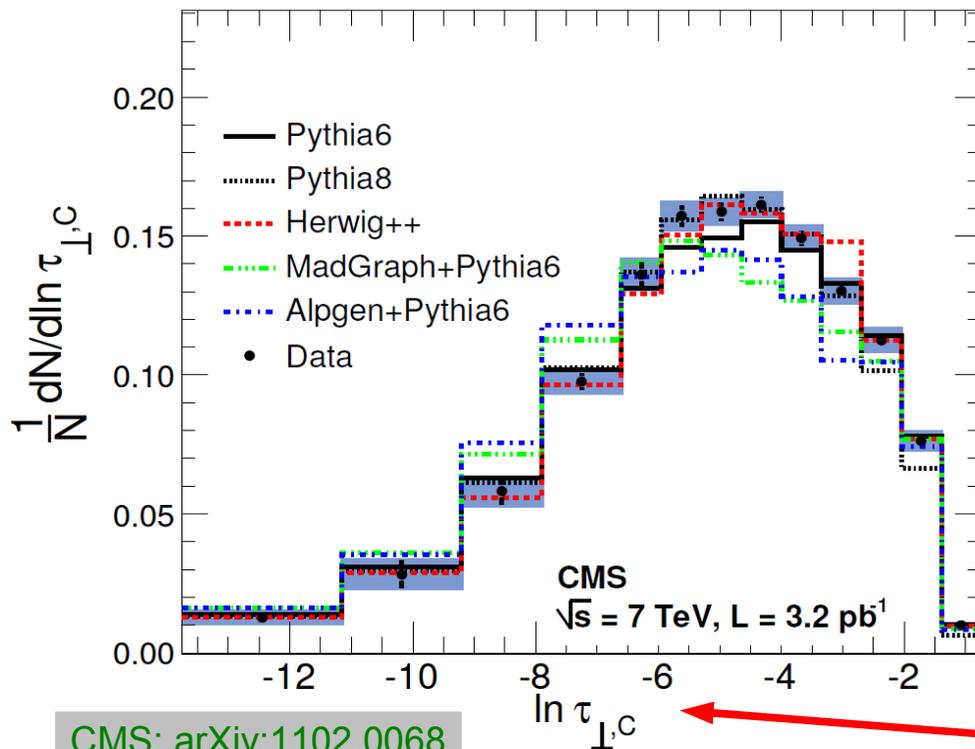
Less so by multi-jet improved MadGraph or Alpgen ...

but improves when looking into multi-jet events (not shown)

Thrust Minor also available

Experimental Uncertainties of order  $\sim 5\%$

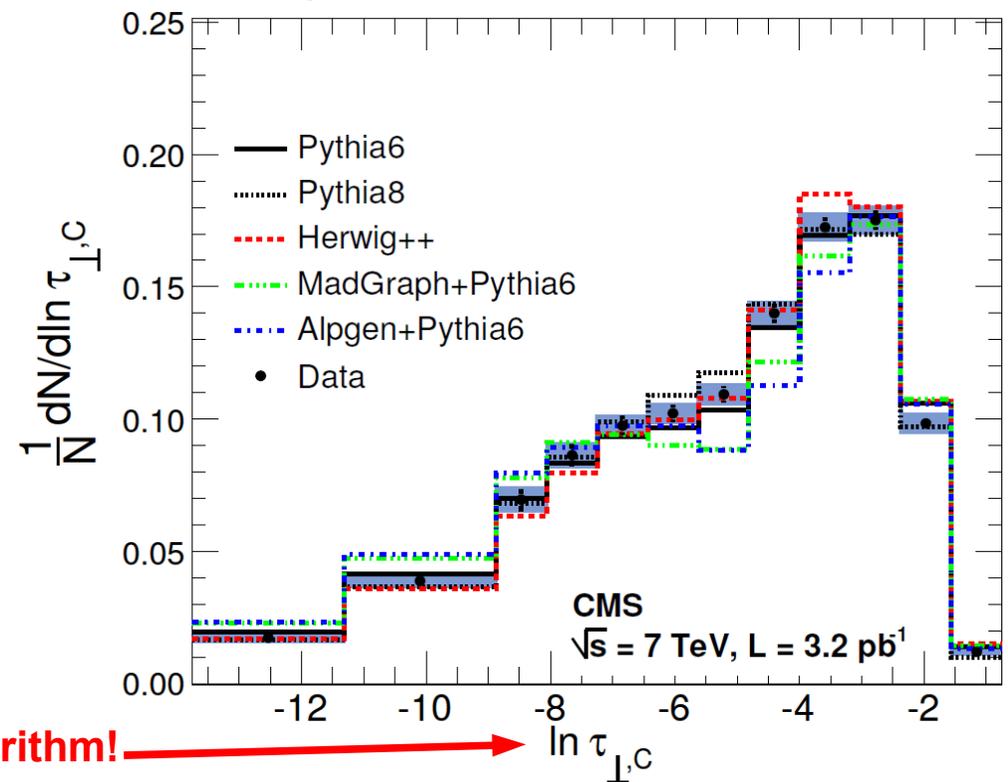
Low  $p_T$  bin:  $90 < p_T / \text{GeV} < 125$



CMS: arXiv:1102.0068

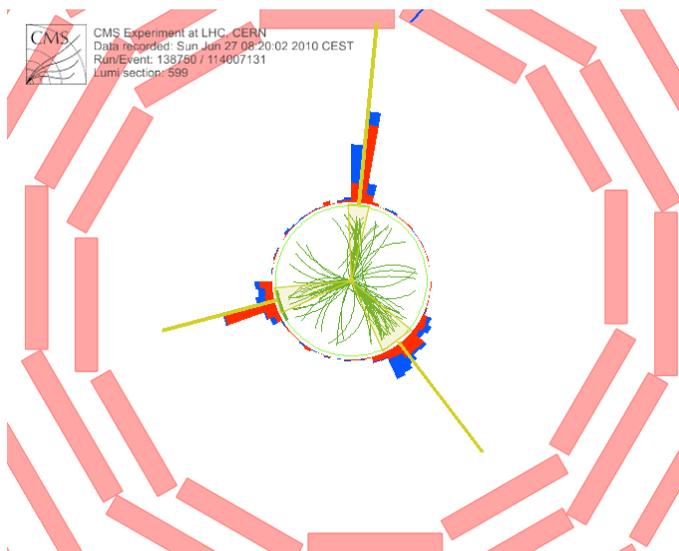
← **logarithm!** →

High  $p_T$  bin:  $200 < p_T / \text{GeV}$



# Ratio Measurements

- **Reduction strategy 2: Jet cross section ratios**
  - ➔ **Dijet centrality ratio: Nice for new physics, not sensitive to  $\alpha_s$ .**
  - ➔ **Jet cross-section ratio  $R=0.7$  /  $R=0.5$  or kT / SISCone: Interesting, but for  $\alpha_s$  ?**
  - ➔ **3+-jet to 2+-jet cross-section ratio: Directly sensitive to  $\alpha_s$  !**
  - ➔ **Will not discuss ratios within jets (jet shapes, subjet multiplicity)**
- **Many uncertainties cancelled (luminosity) or reduced (JES, ...)**

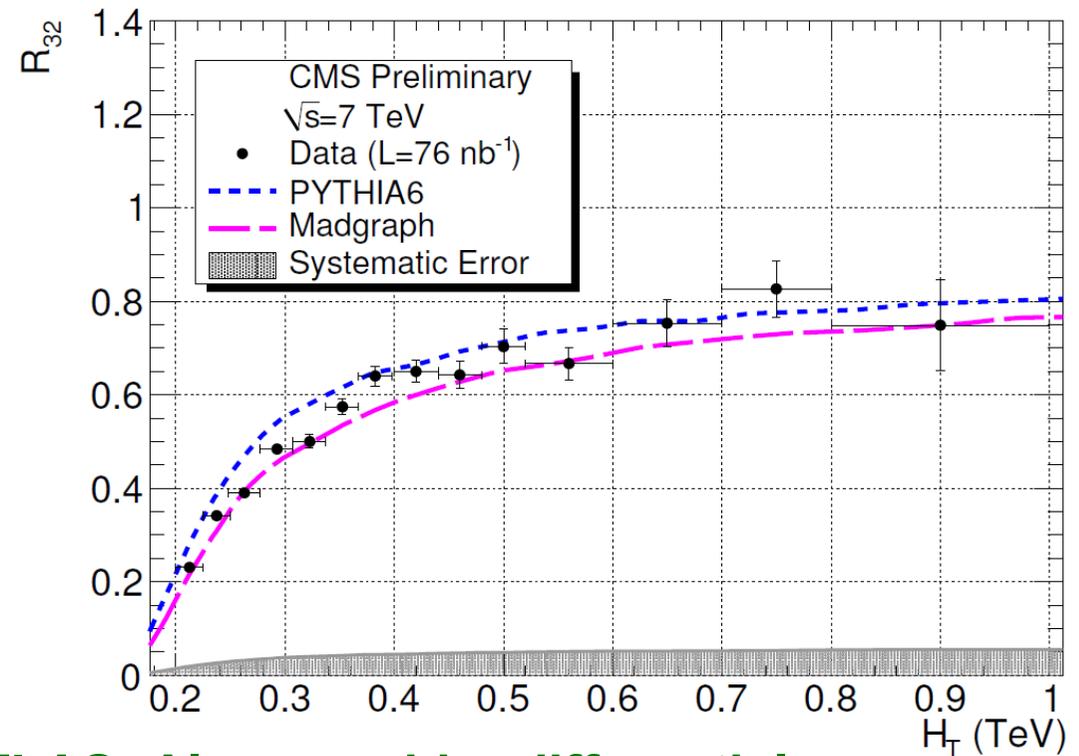
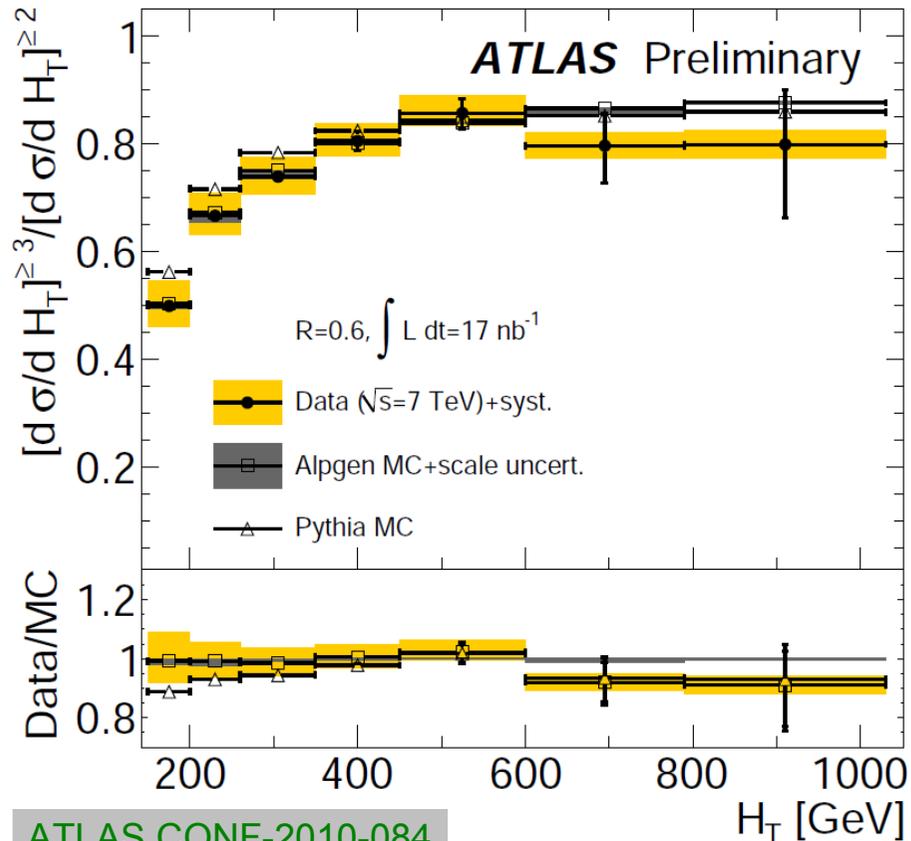


→ **strong coupling  $\alpha_s$**

# Inclusive 3+/2+ Jet Ratio

**ATLAS:** anti-kT R=0.6,  $|y| < 2.8$   
 $p_{T_i} > 30$  GeV,  $p_{T_1} > 60$  GeV  
 $H_T = \sum |p_{T_i}|$   
 exp. Uncertainty  $< \sim 10\%$

**CMS:** anti-kT R=0.5,  $|y| < 2.5$   
 $p_{T_i} > 50$  GeV,  $p_{T_1} > 60$  GeV  
 $H_T = \sum |p_{T_i}|$   
 exp. Uncertainty  $< \sim 10\%$



**ATLAS: Also consider differential 2-jet Rate ( $\sim$  event shape ...)**

ATLAS CONF-2010-084

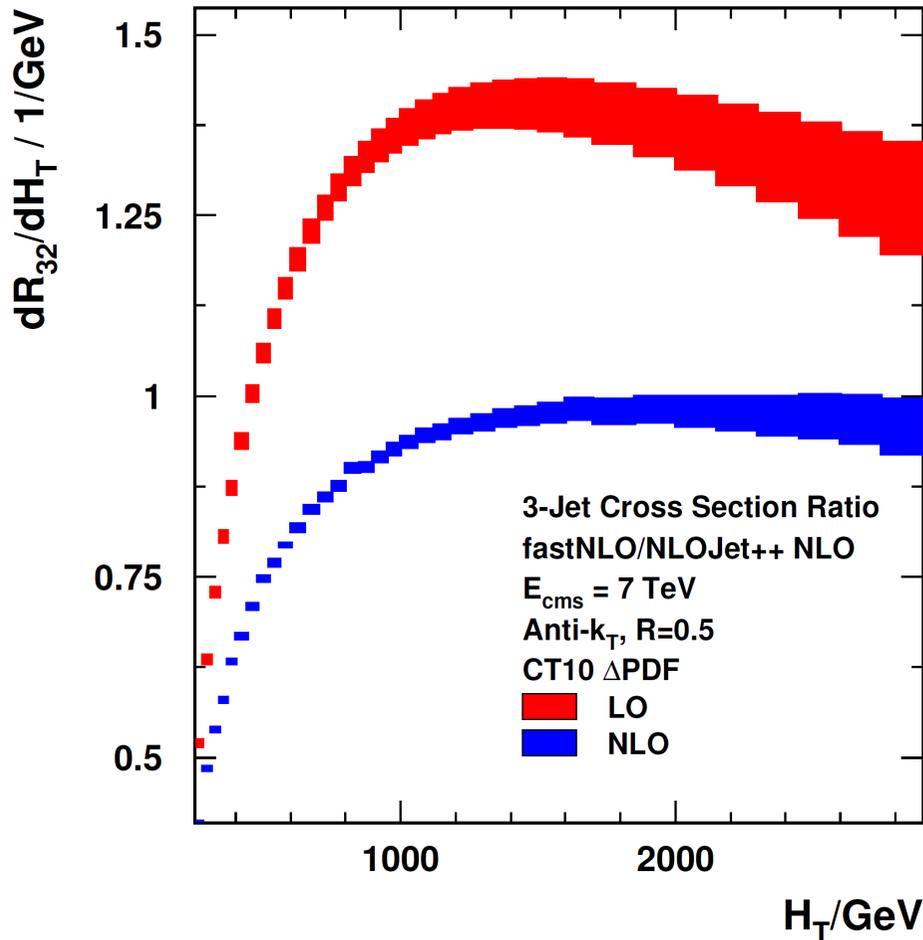
CMS-QCD-10-012

# 3+/2+: NLO Prediction & $\Delta$ PDF

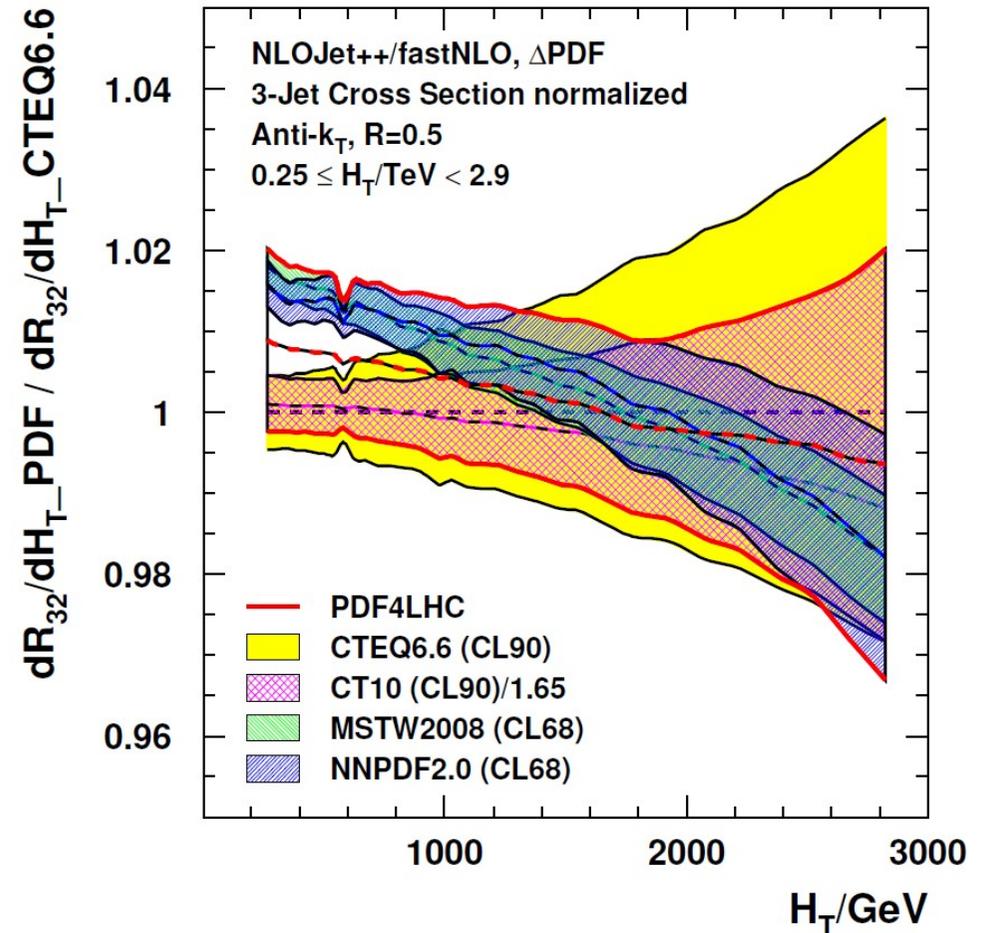
CMS like selection  
(ATLAS not very different)

LO > 1 ?!

K factors ~ 0.67



PDF uncertainty reduced  
by a factor ~ 10 in ratio



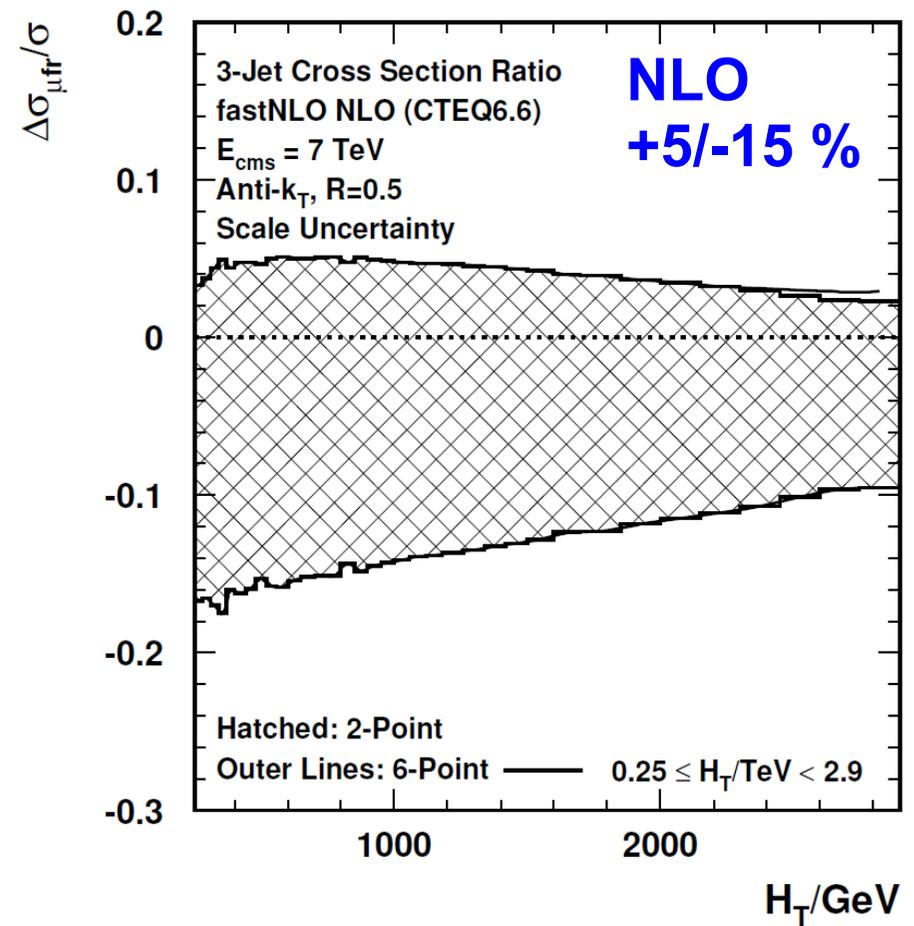
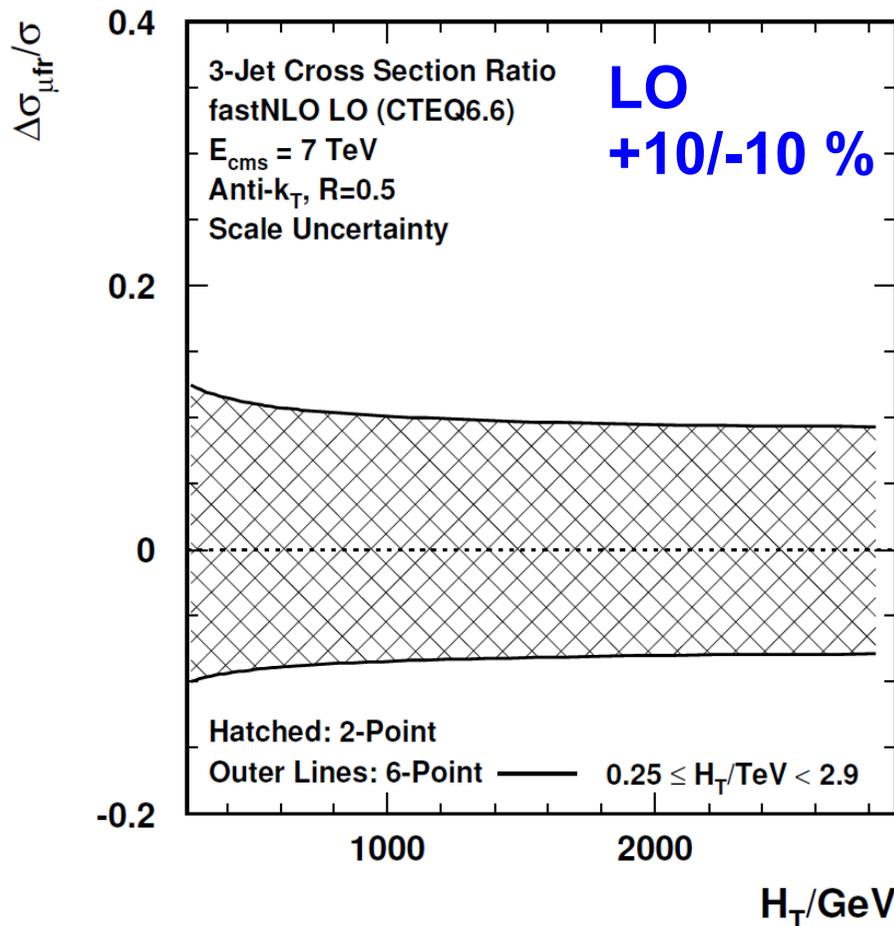
# 3+/<sub>2+</sub>: Scale Dependence

Simultaneous variation in numerator and denominator

No large difference between symmetric and add. asymm. scale variations

No real improvement when going to NLO ...

ATLAS quotes 5 % from Alpgen

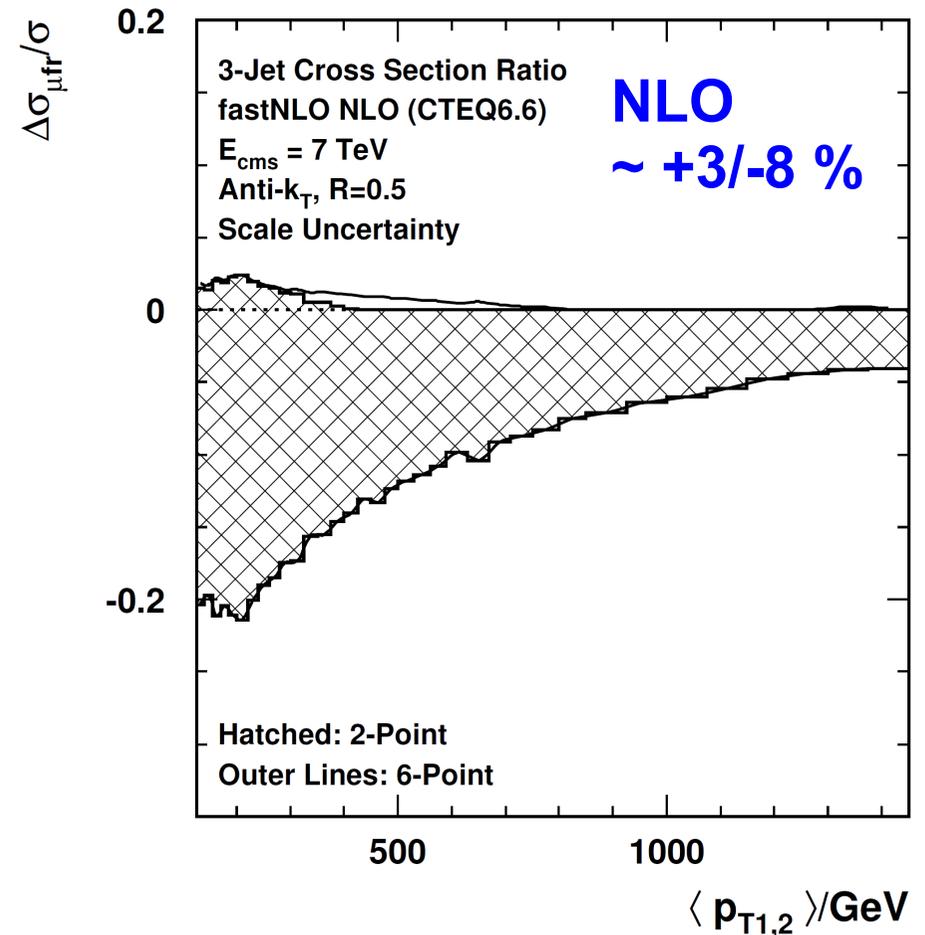
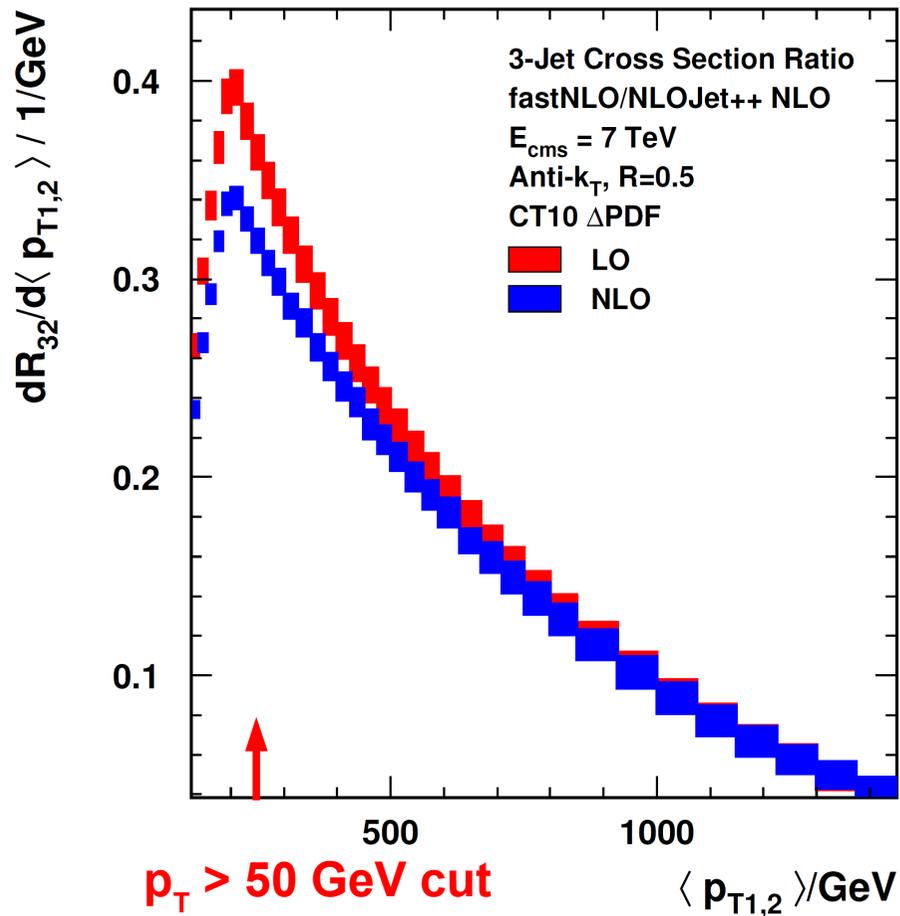


# 3+/2+ Revisited

Made some adaptations after chat with Gavin Salam:

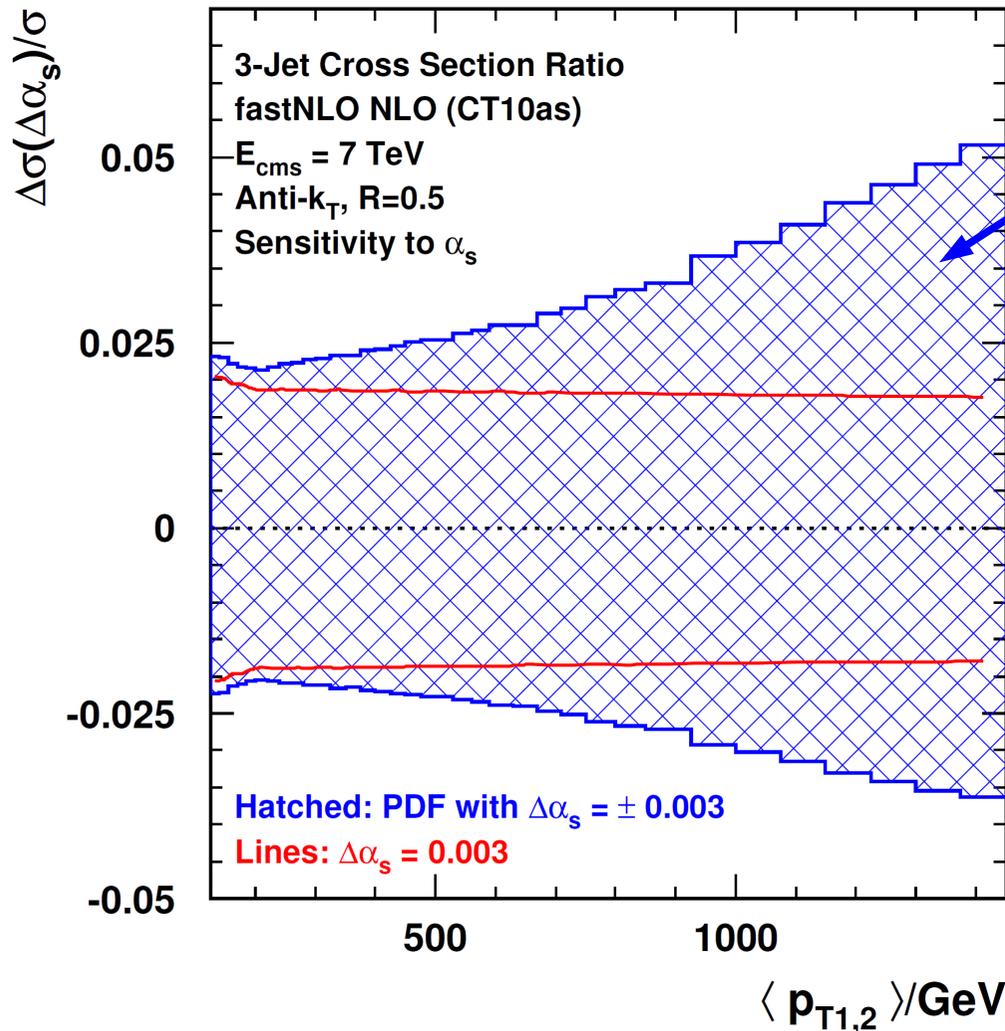
- changed scale from  $H_T$  to average dijet  $p_T$ :  $\langle p_{T1,2} \rangle$
- require hard third jet:  $p_{T3} > 0.25$  times  $\langle p_{T1,2} \rangle$

Not optimal yet,  
but clearly better



# 3+/2+: Sensitivity to $\alpha_s$

## $\alpha_s$ Sensitivity



CT10as members with  
 $\alpha_s = 0.118 \pm 0.003$

$\alpha_s(M_Z)$  only changed  
 $\alpha_s = 0.118 \pm 0.003$

To be further investigated ...



# Summary/Discussion

- **Detector performances and MC modelling better than anticipated**
- **Improving rapidly on experimental systematics**
- **Can do much better jet measurements than originally hoped for**
- **Are there other (jet) observables to measure  $\alpha_s$  at LHC?**
- **Comments/suggestions are welcome**

Thank you for your attention

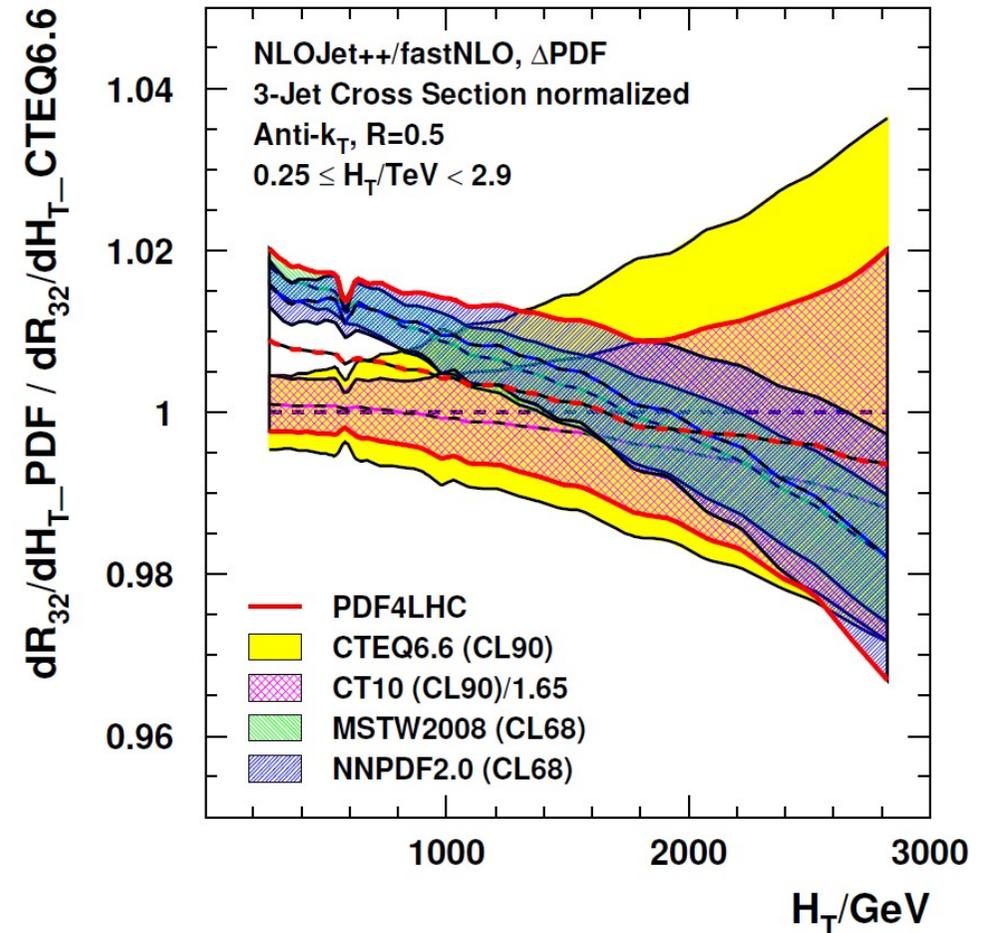
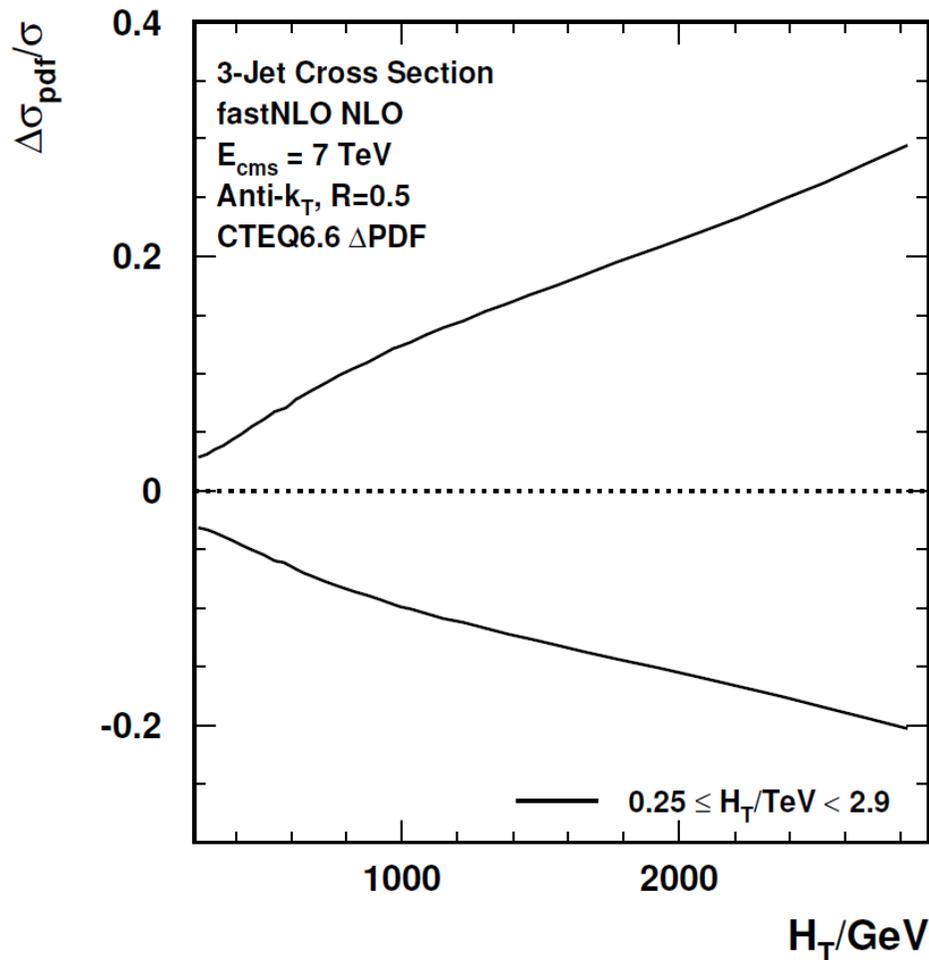


# *Backup Slides*

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# 3+/2+: PDF Uncertainty

Only 3-jet part (numerator)



# Central Thrust and Multi-Jets

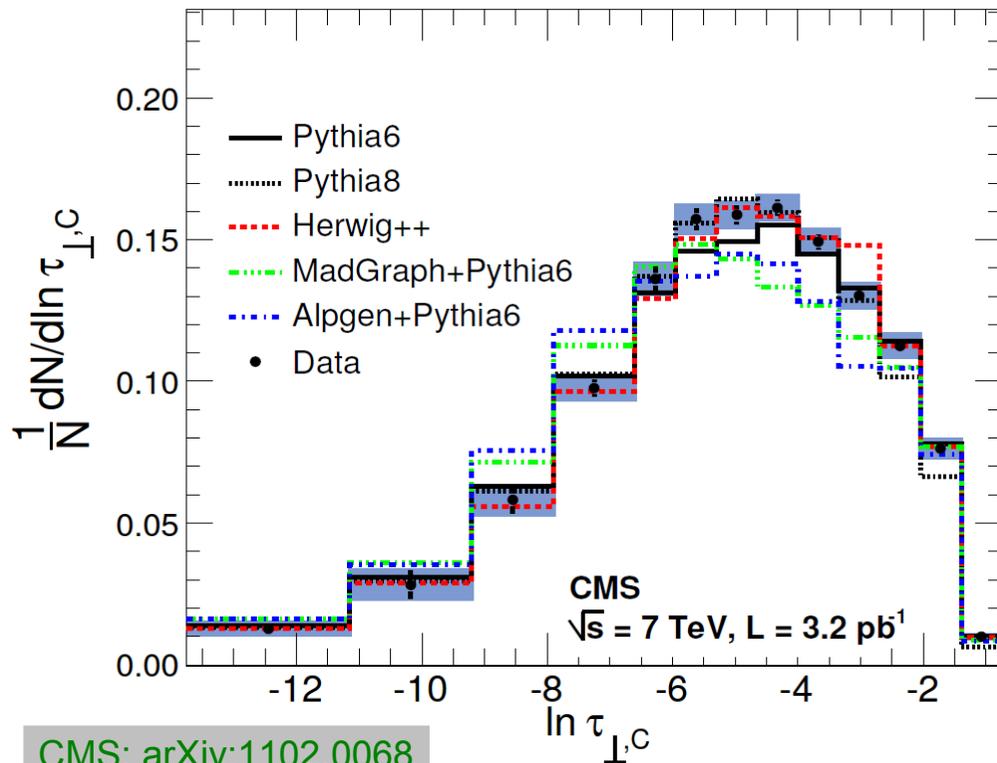
## Dijet case:

- ➔ Good description by Pythia, Herwig++
- ➔ Alpgen & MadGraph off

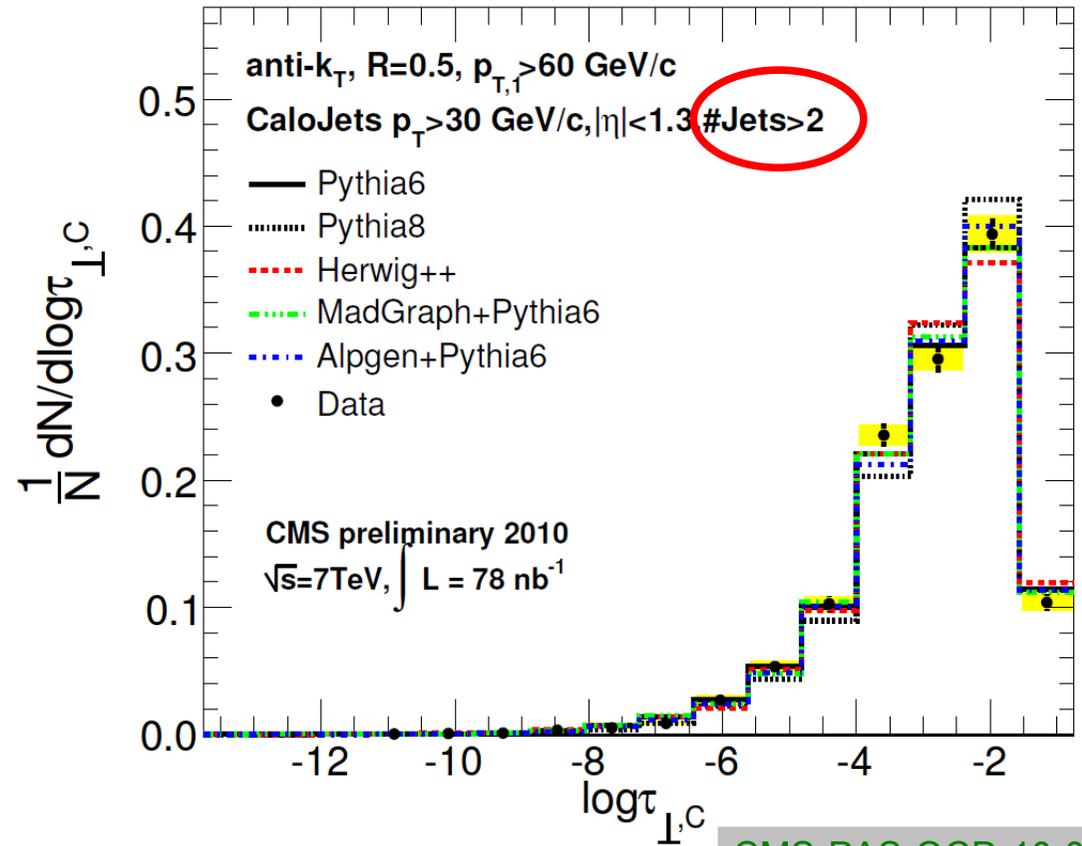
## Multijet case:

- ➔ Pythia, Herwig++ ok
- ➔ Alpgen & MadGraph better

Low  $p_T$  bin:  $90 < p_T / \text{GeV} < 125$



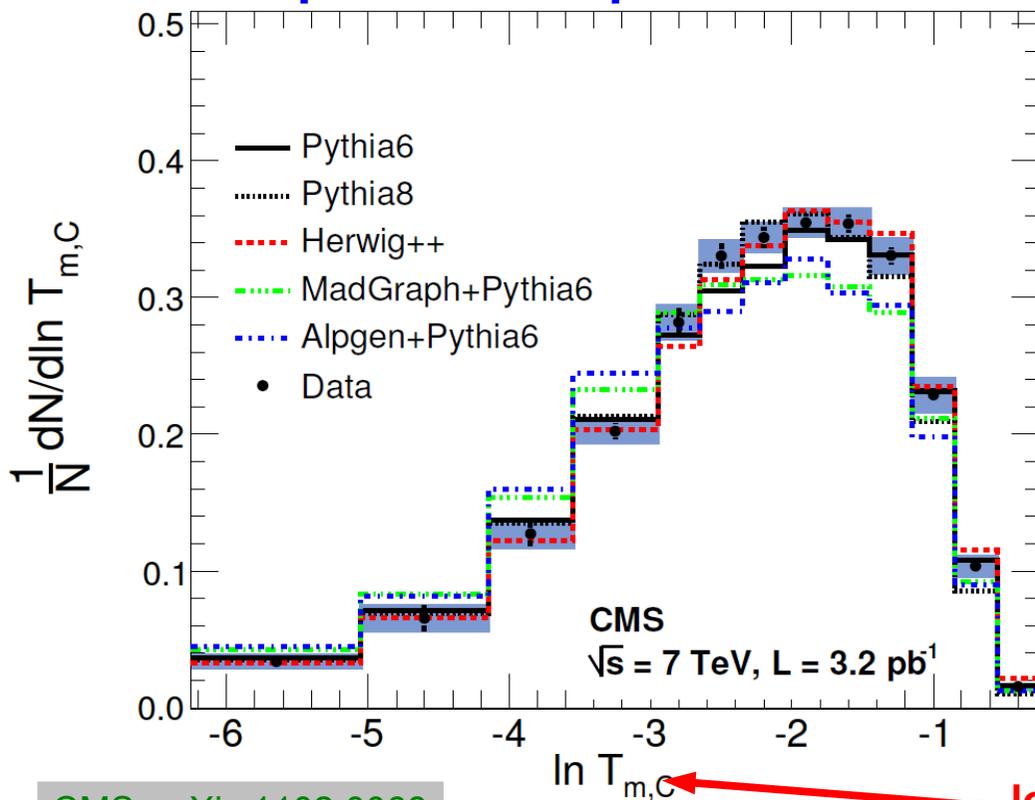
CMS: arXiv:1102.0068



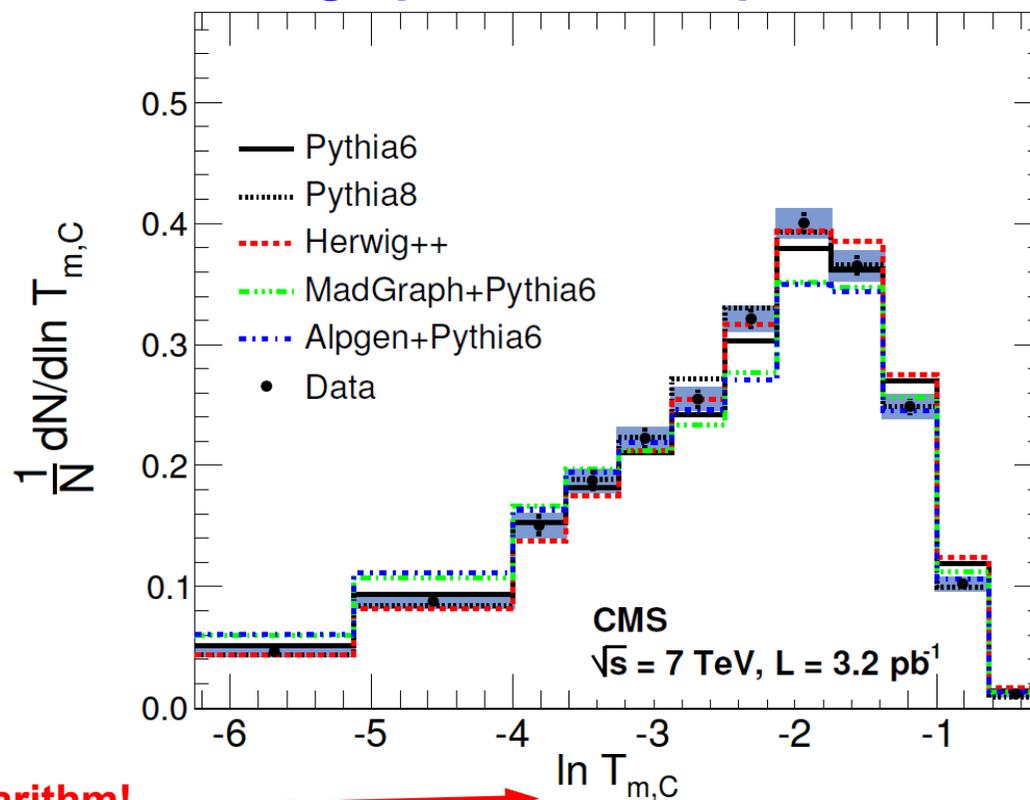
CMS-PAS-QCD-10-013

# Thrust Minor: Available Data

Low  $p_T$  bin:  $90 < p_T / \text{GeV} < 125$



High  $p_T$  bin:  $200 < p_T / \text{GeV}$



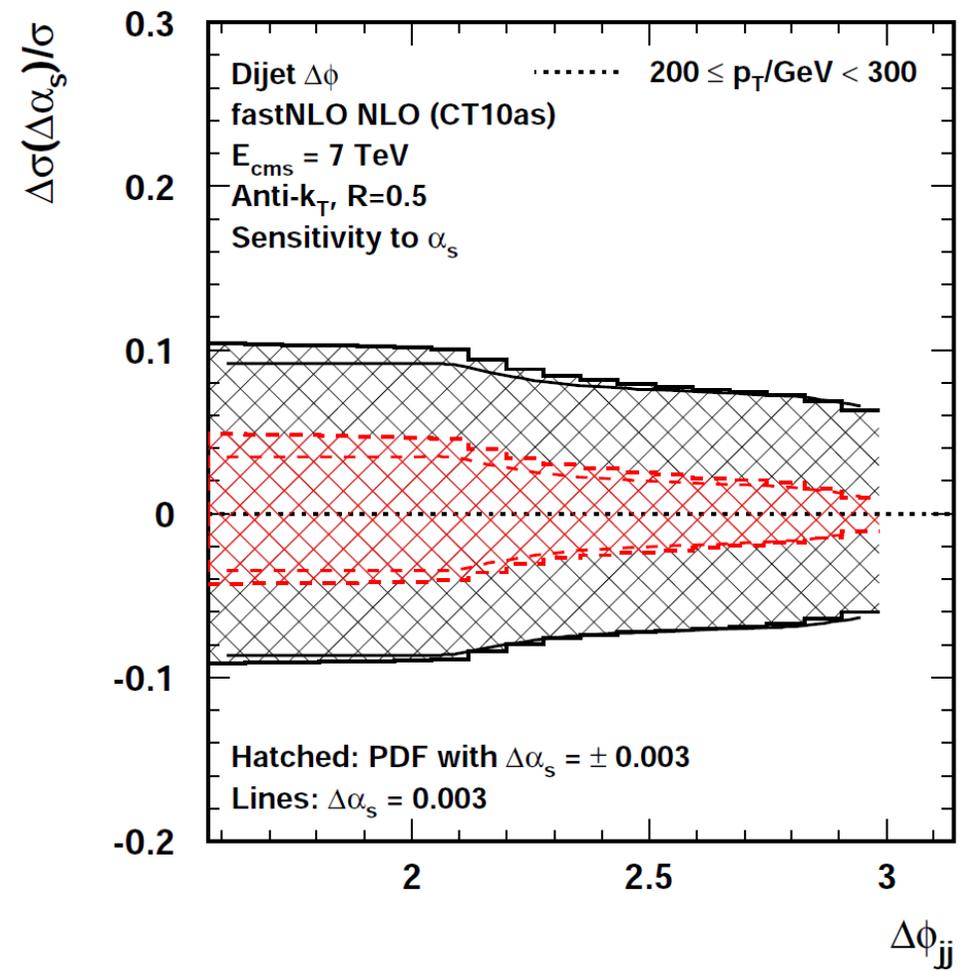
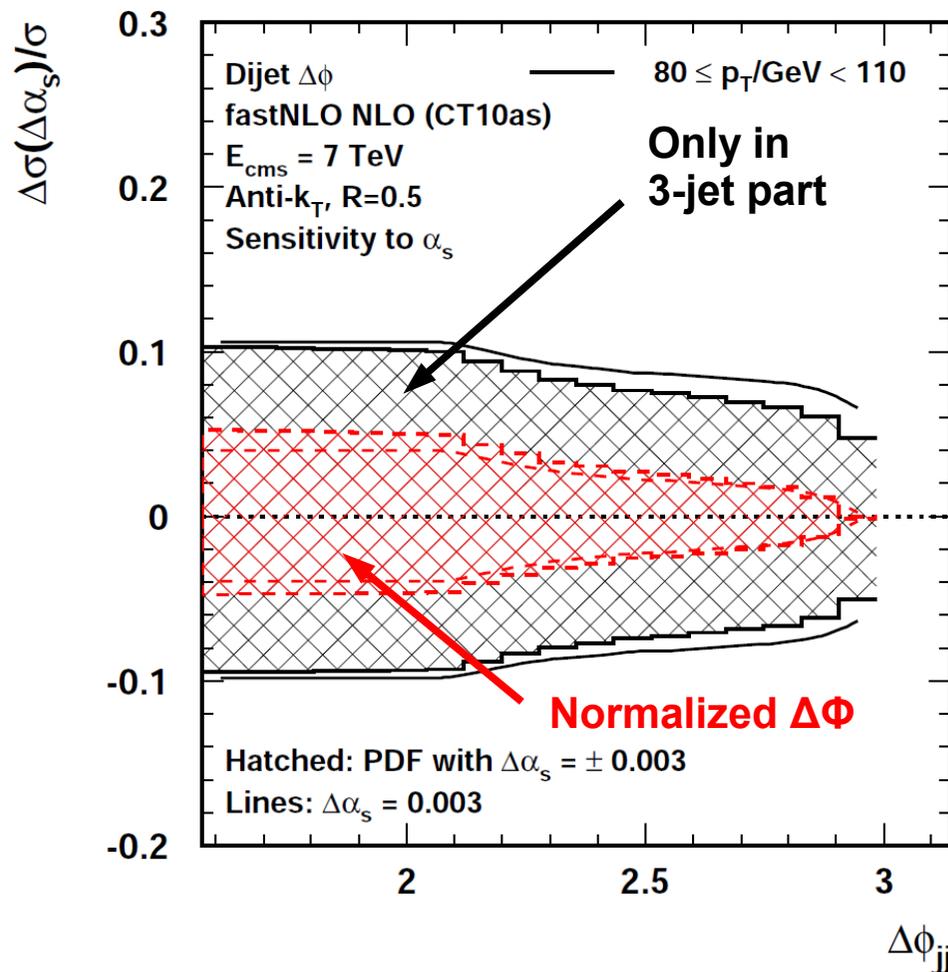
CMS: arXiv:1102.0068

logarithm!

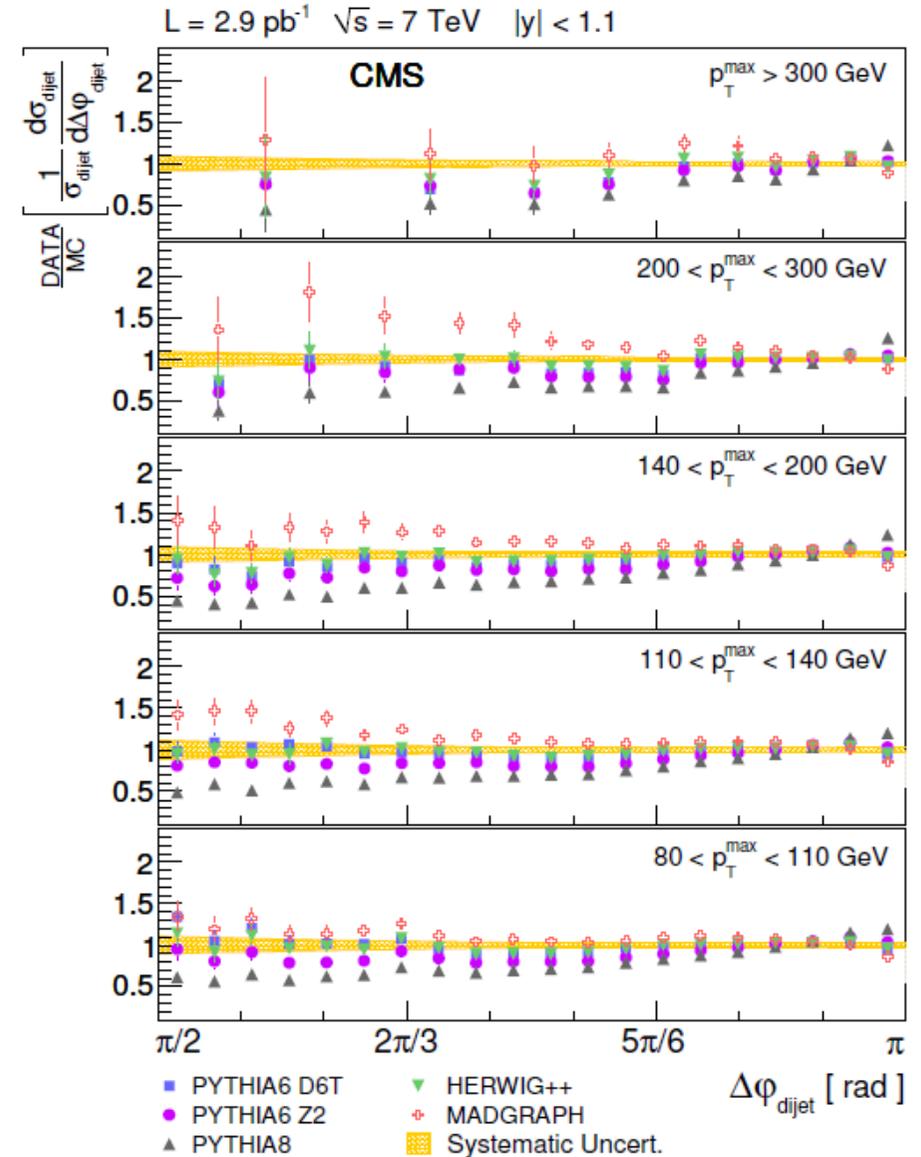
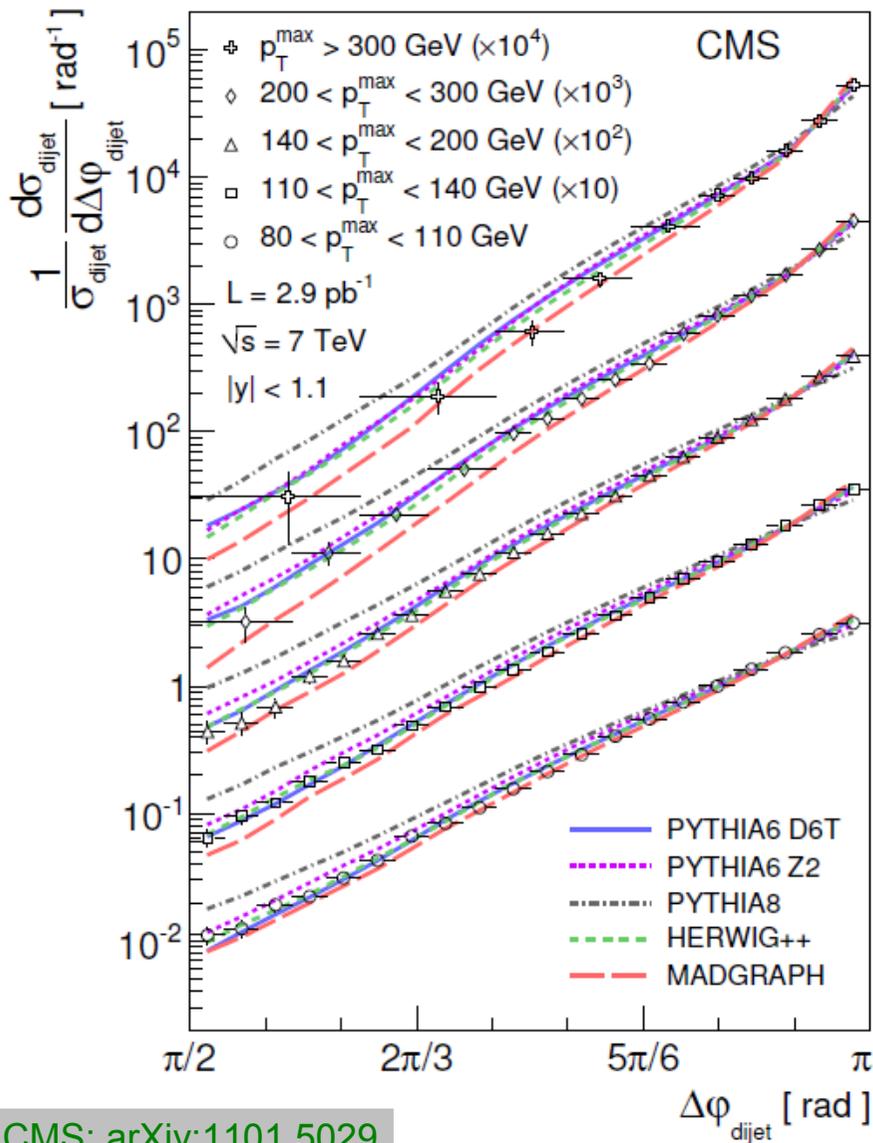
# $\Delta\phi$ : Sensitivity to $\alpha_s$

Low  $p_T$  bin:  $80 < p_T / \text{GeV} < 110$

High  $p_T$  bin:  $200 < p_T / \text{GeV} < 300$



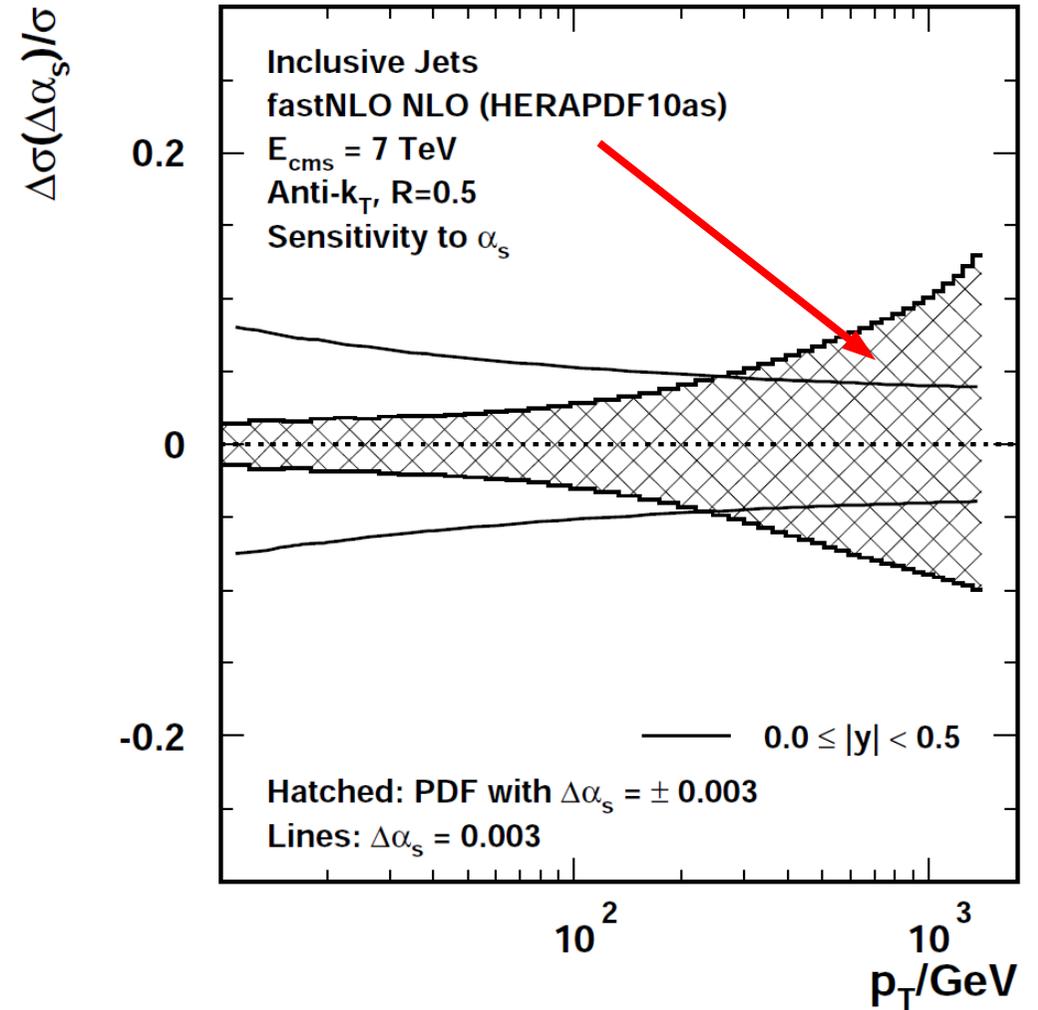
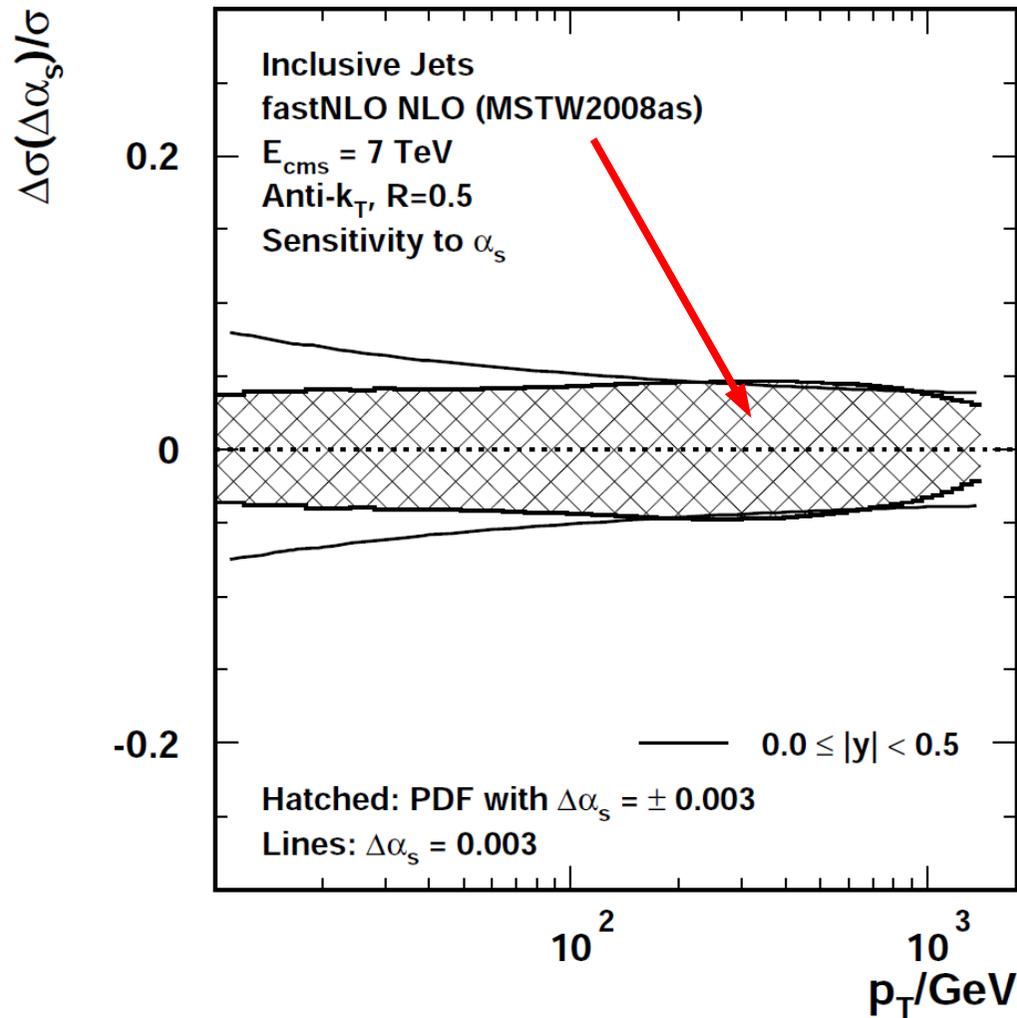
# $\Delta\Phi$ : Comparison to MC



CMS: arXiv:1101.5029

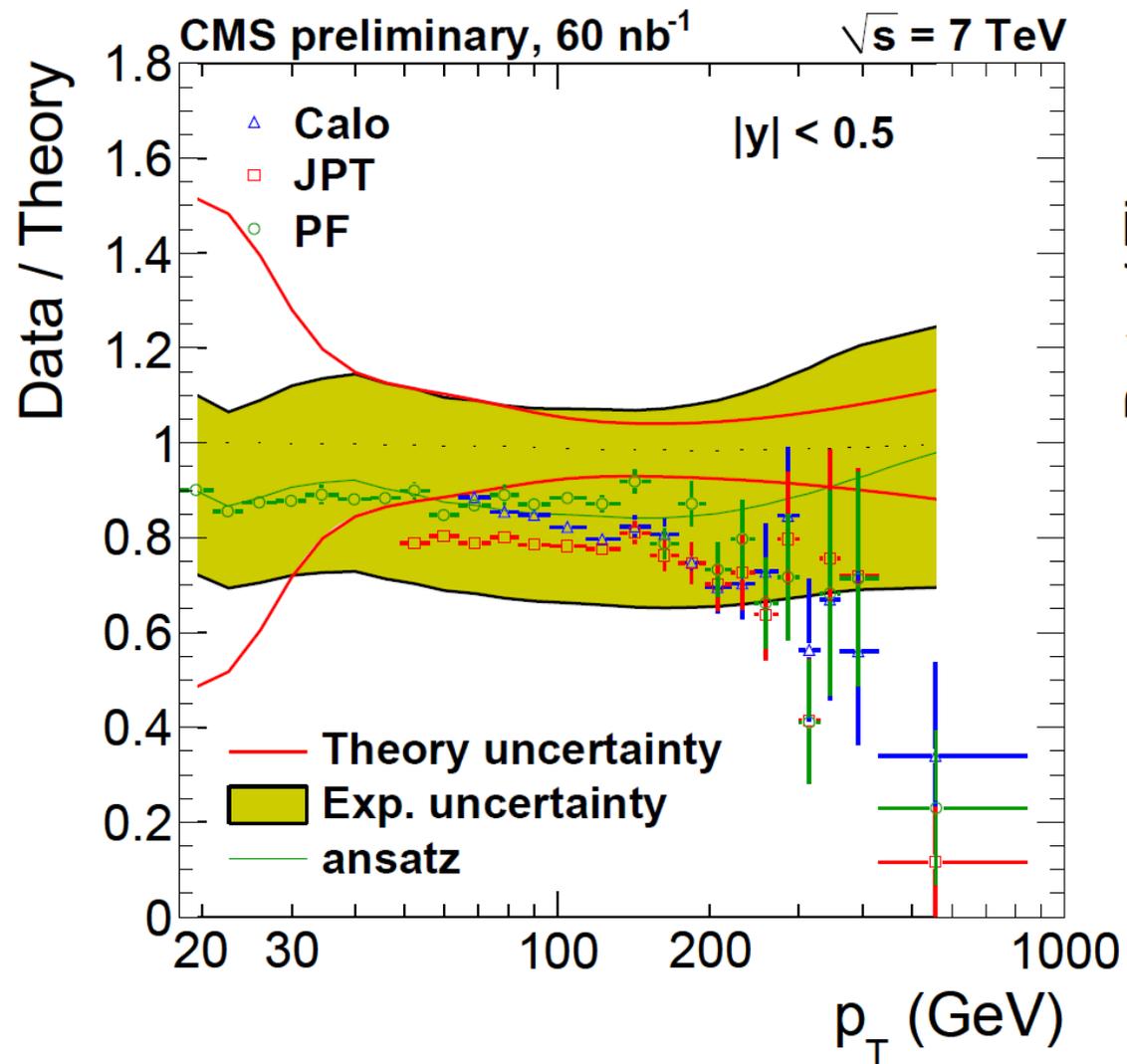
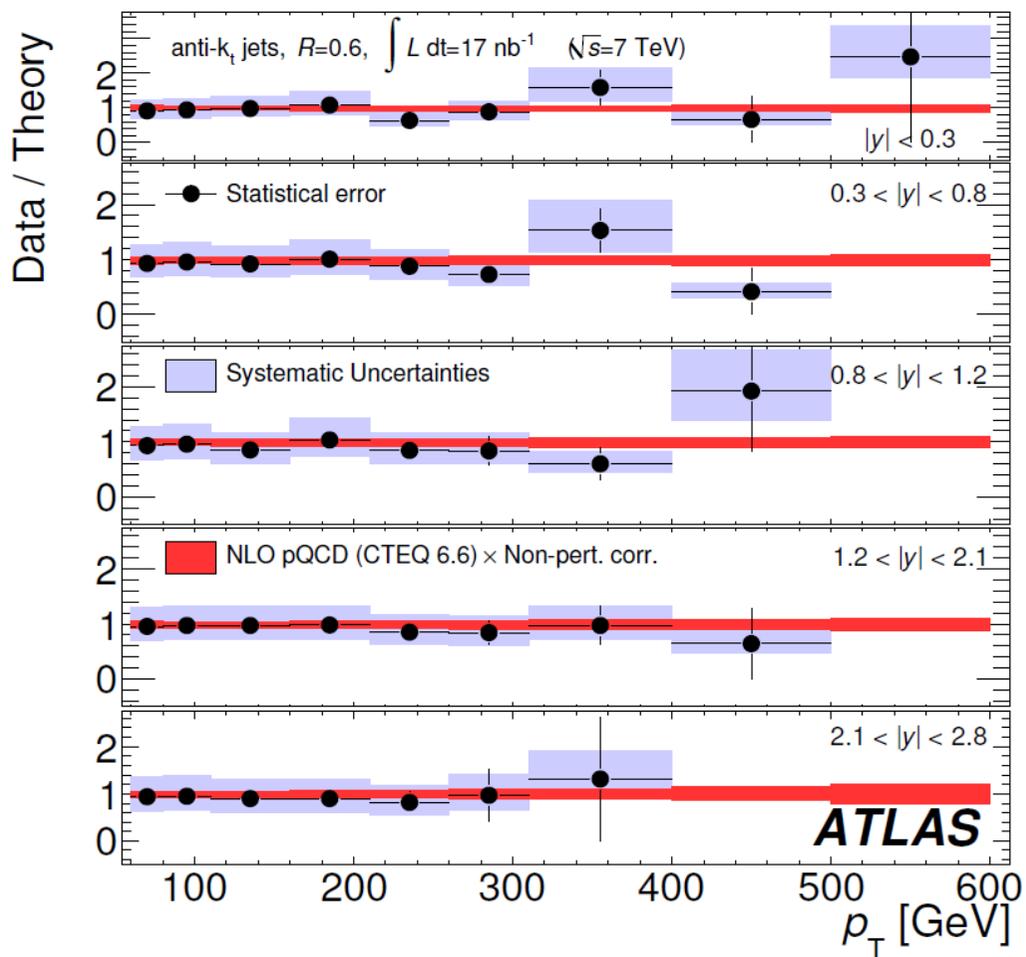
# Sensitivity to $\alpha_s$

## Inclusive Jet $p_T$



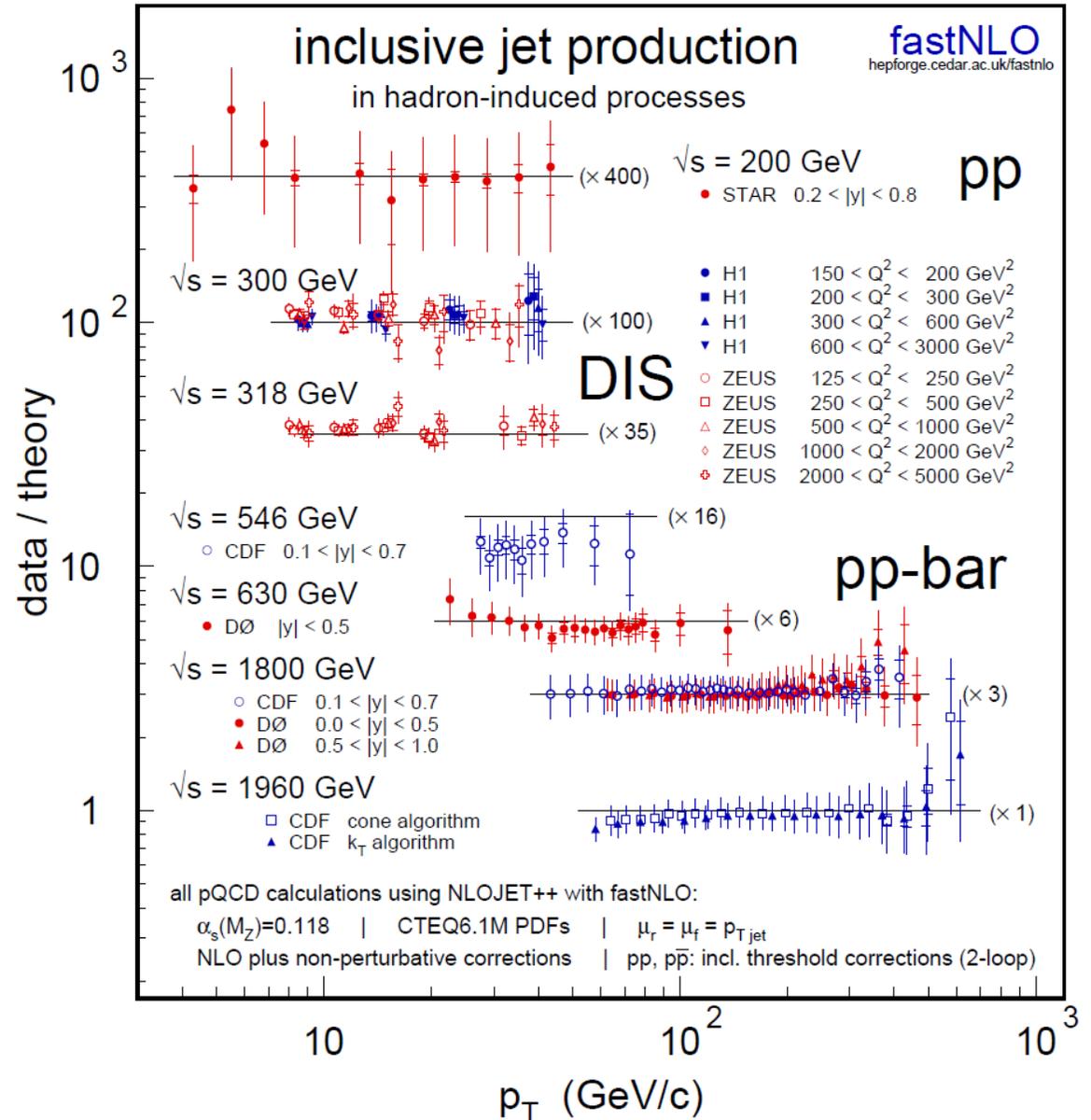
# Incl. Jet $p_T$ : Data / Theory

Compatible within uncertainties!



# Previous Jets Data / Theory

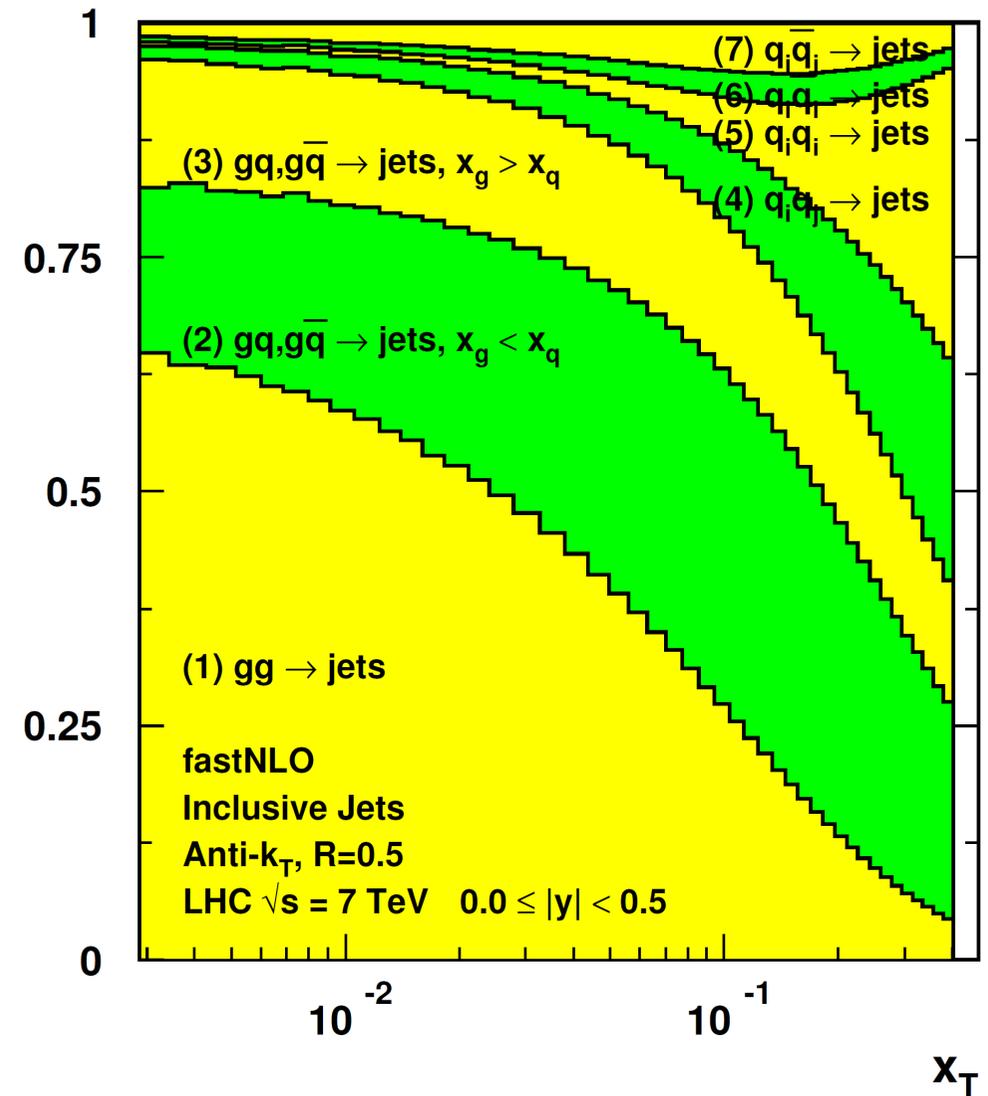
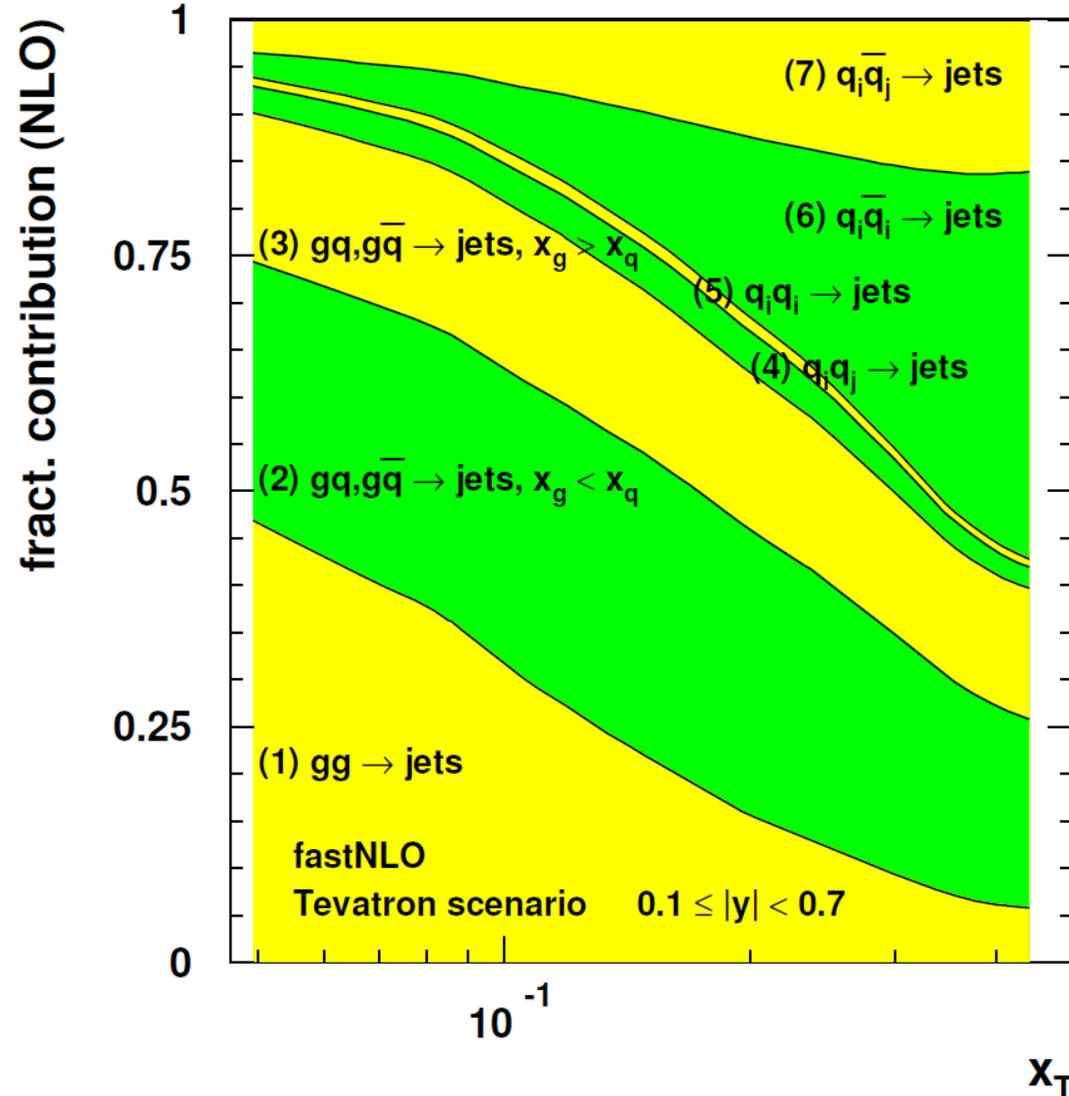
- Comparison of jet data from
  - ➔ STAR at RHIC
  - ➔ H1 and ZEUS at HERA
  - ➔ CDF and D0 at Tevatron
- Compatible with NLO pQCD



# Jet Cross Section Decomposition

Tevatron, 1.96 TeV

LHC, 7 TeV



# Jet Algorithms at LHC

## Primary algorithm at LHC:

### → Anti- $k_T$ :

ATLAS  $R = 0.4, 0.6$

CMS  $R = 0.5, 0.7$

### → $k_T$ : $R = 0.4, 0.6$

(ATLAS & CMS)

### → SIScone: $R = 0.5, 0.7$

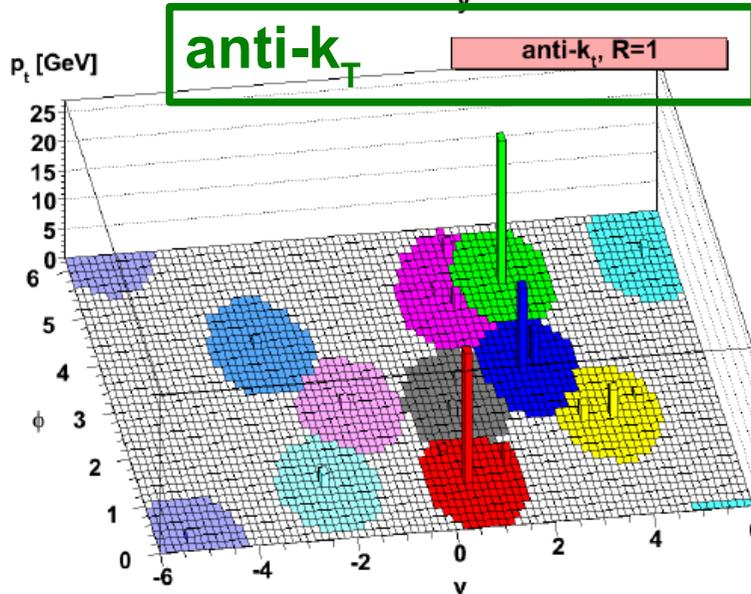
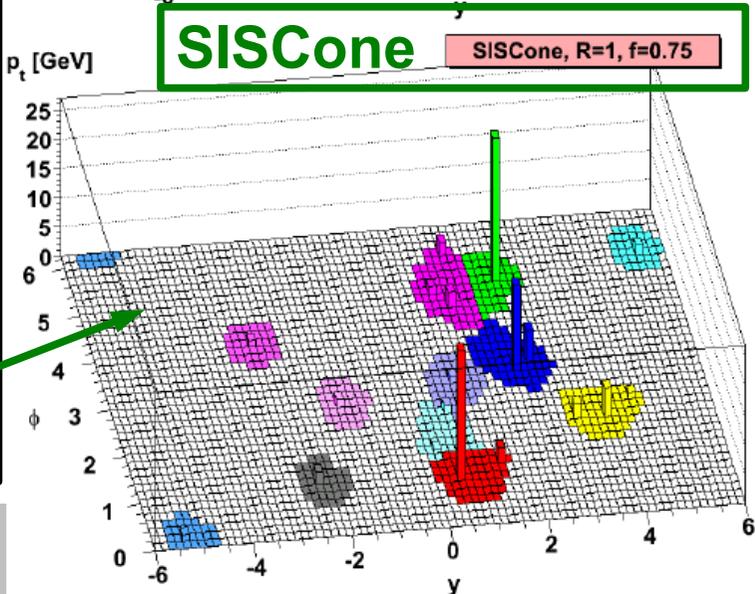
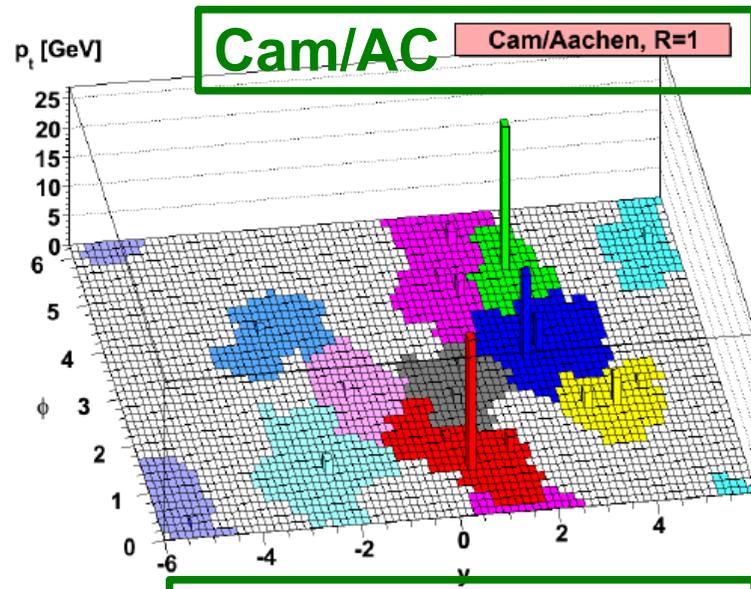
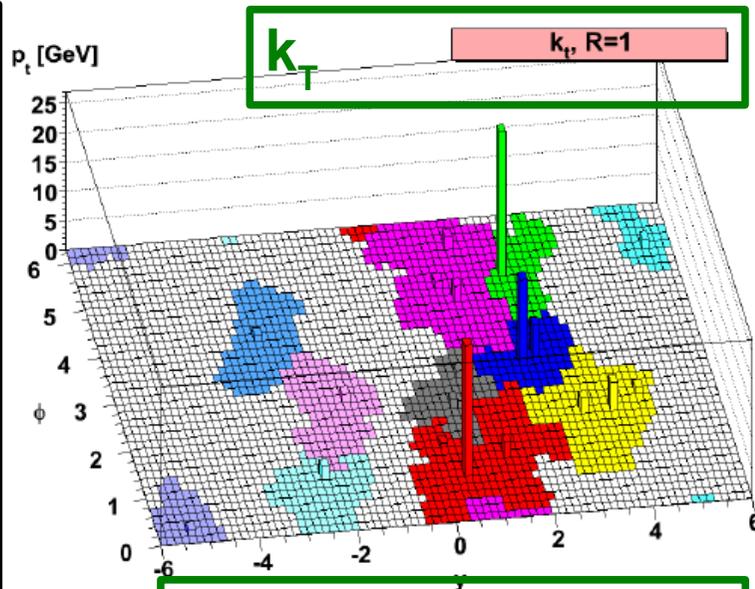
(CMS)

### → Cambridge/Aachen

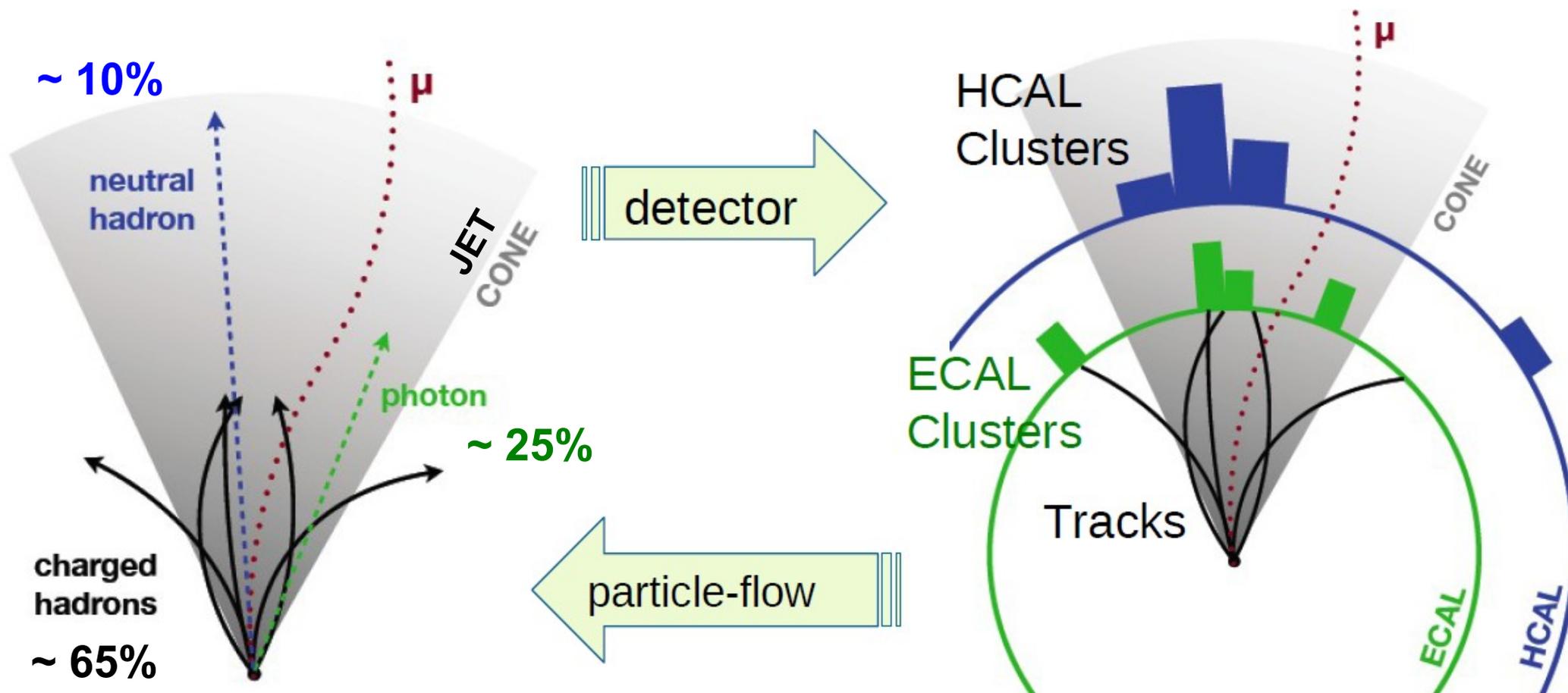
used in jet substructure, for example in boosted top

General interest to work with all four

Fast  $k_T$ , Cacciari/Salam, PLB641, 2006  
 SIScone, Salam/Soyez, JHEP05, 2007  
 anti- $k_T$ , Cacciari et al., JHEP04, 2008



# Particle Flow Concept



**Associate particle types to all measurements,  
apply type-dependent corrections**

# Jet Calibration and Uncertainty

## Jet calibration:

Simple  $P_{T,jet}$  and  $y$  dependent correction applied to measured jets at the electro-magnetic scale.

Using particle level (truth) from Monte Carlo simulation as reference.

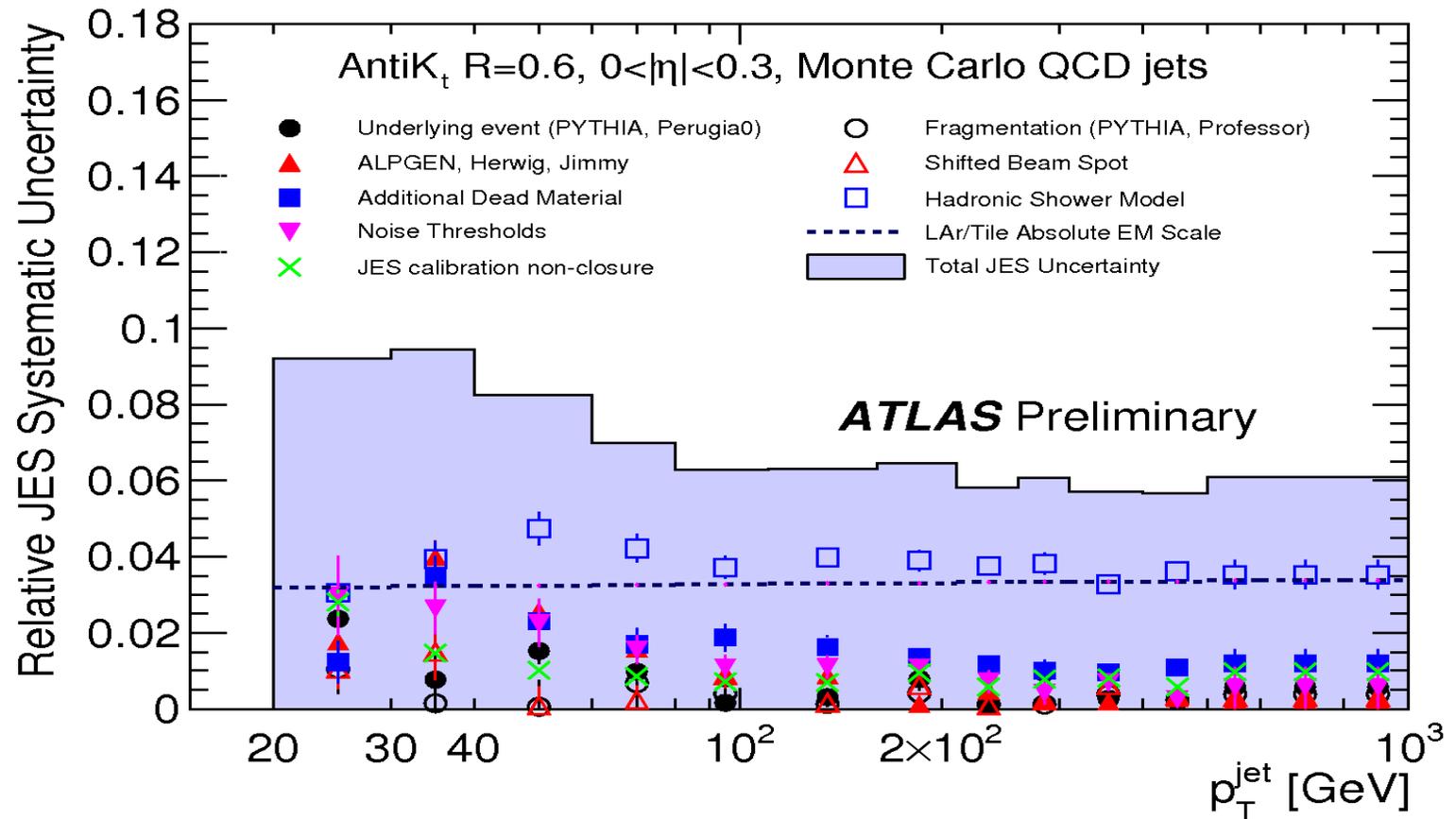
## Jet energy scale uncertainty:

Evaluated using MC using various detector configurations, hadronic shower and physics models  
Based on large test-beam experience.

In-situ measurements:

- 1) Using Di-jet balance to transport uncertainty central  $\rightarrow$  forward
  - 2) Additional uncertainty for pile-up from average tower energy per vertex
  - 3) Cross-checked with single isolated hadron response measurement ( $E_{calo} / p_{track}$ )
- Uncertainty via:  
deconvolution of jets in individual particles

Example:

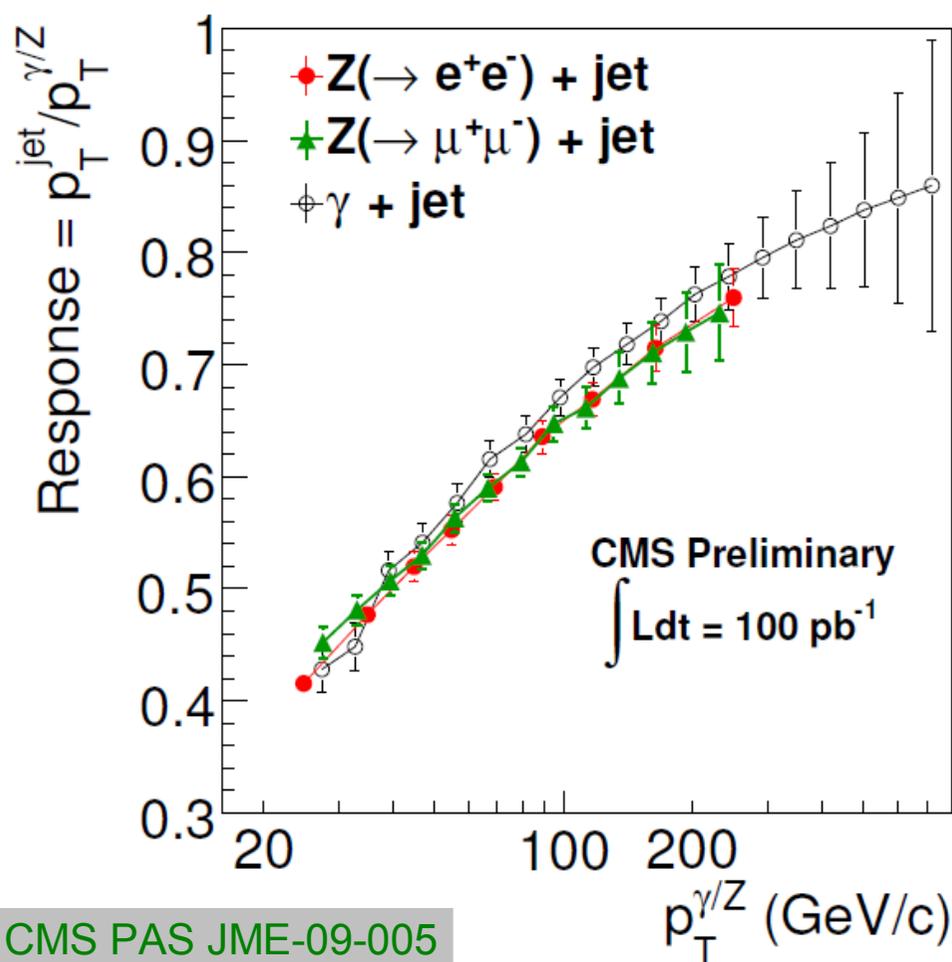


Jet energy scale uncertainty smaller than 7% for  $p_{T,jet} > 100$  GeV

# Absolute Correction (Simulation Result)

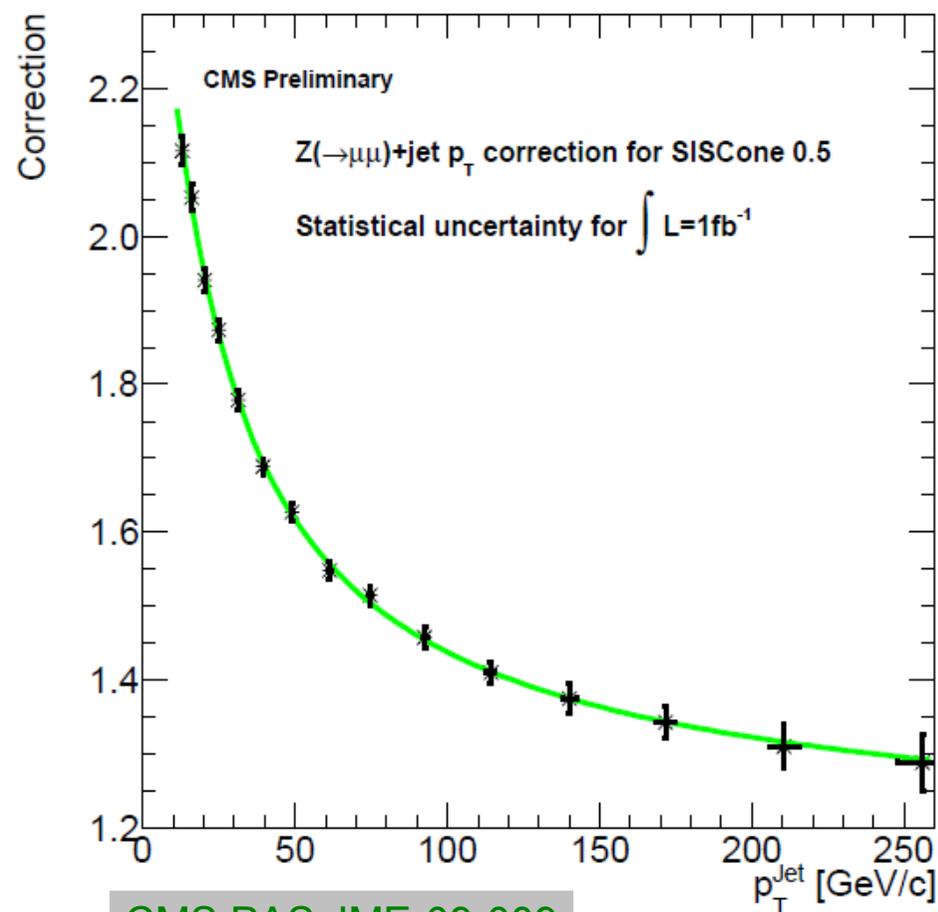
CMS detector simulation, calorimeter towers,  $E_{\text{CMS}} = 10 \text{ TeV}$

Comparison of jet responses



CMS PAS JME-09-005

Derived correction at the example  
of  $Z(\rightarrow \mu\mu) + 1\text{jet}$

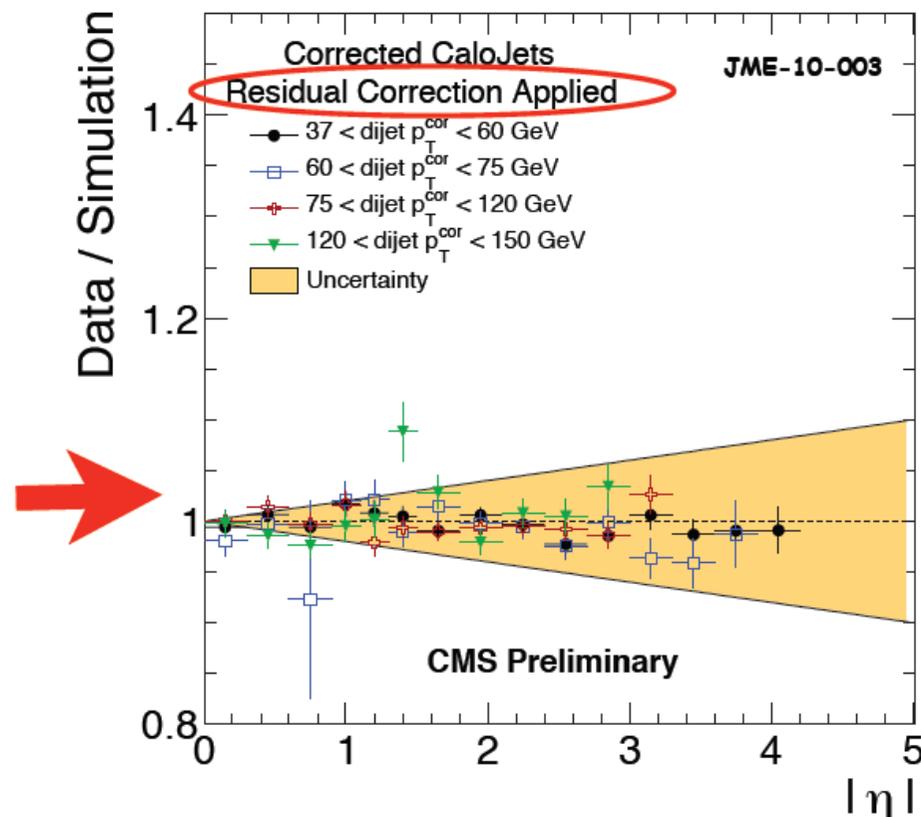
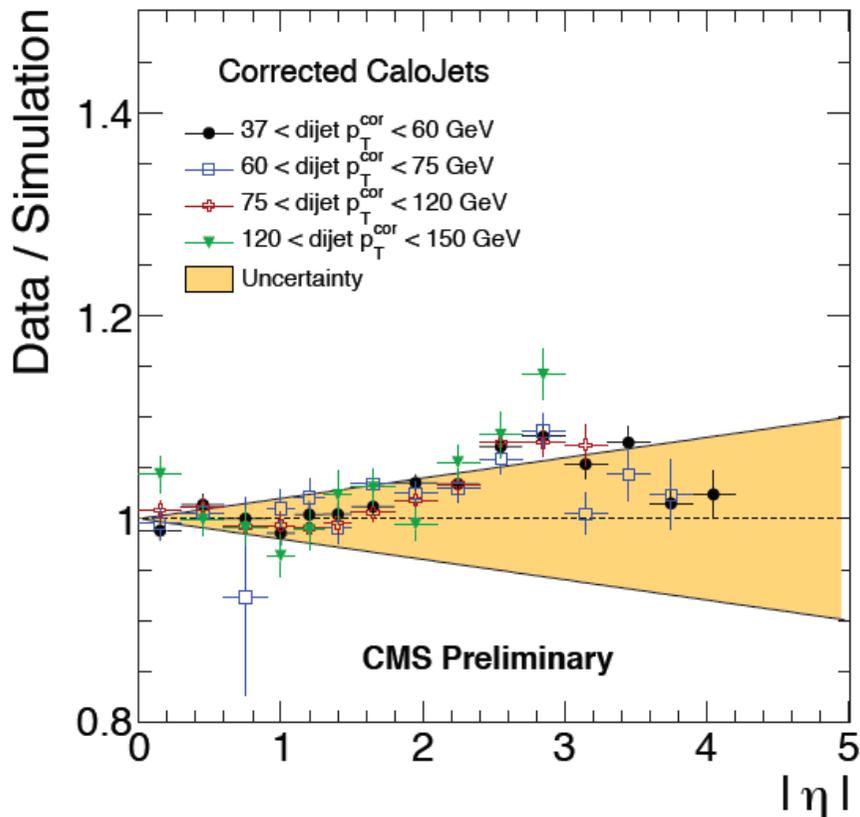


CMS PAS JME-09-009

# Relative Jet Corrections

- Response rapidity dependence is extracted from dijet asymmetry M. Voutilainen, ICHEP2010
- Residual correction is applied for inclusive jets, other studies are covered by the systematic uncertainty band of 2% times unit of rapidity

$$\text{Jet correction} = \text{Absolute}(p_T) [\text{MC}] \times \text{Relative}(\eta) [\text{MC+data}]$$



# Jet Energy Resolution

## Jet energy resolution (JER):

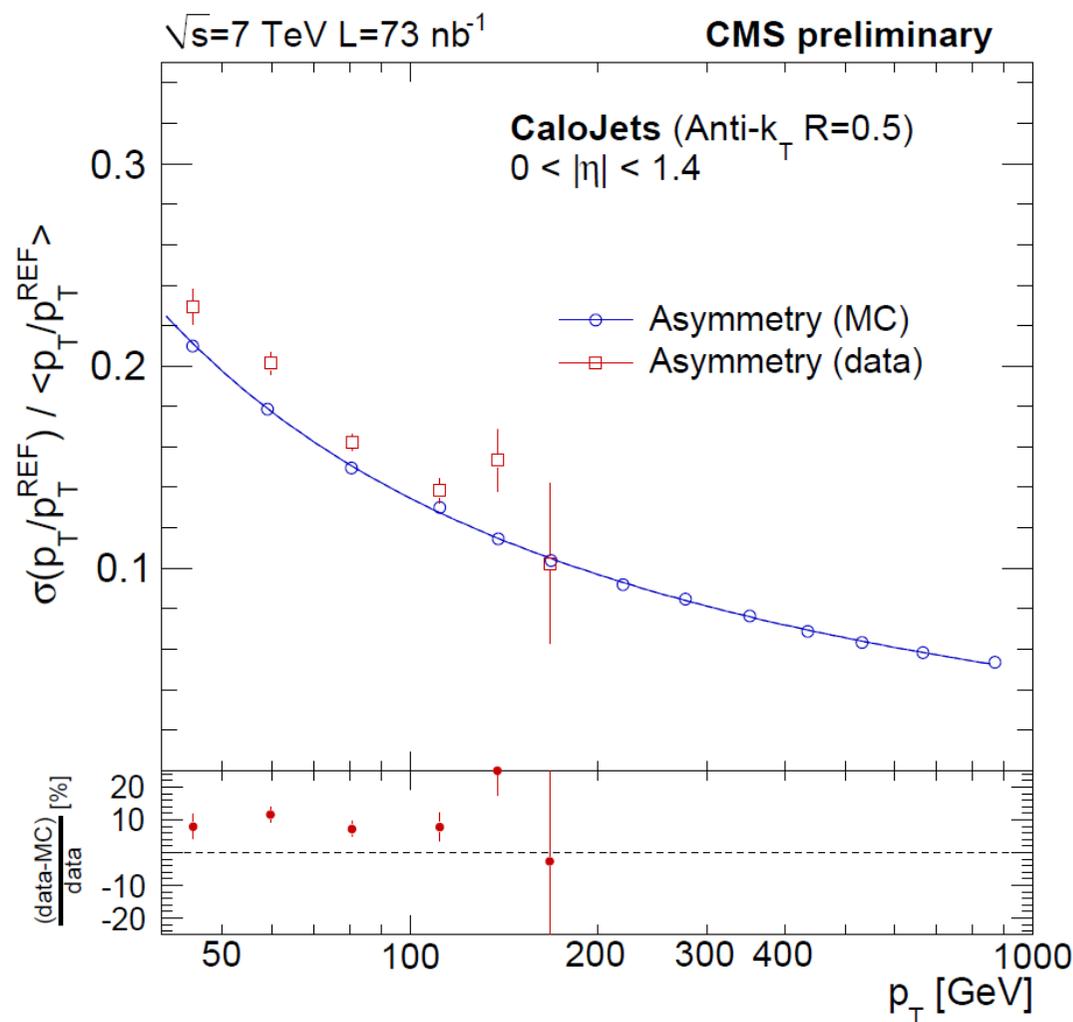
- Can be measured from data using Asymmetry Method used:

For dijet events:

$$A = \frac{(p_T^{\text{jet1}} - p_T^{\text{jet2}})}{(p_T^{\text{jet1}} + p_T^{\text{jet2}})} \Rightarrow \left( \frac{\sigma_{p_T}}{p_T} \right) = \sqrt{2} \sigma_A$$

Used at Tevatron.

- Comparison using MC information (matched jets) gives consistent results



# The ATLAS Detector

## Inner Detector (ID) tracker:

- Si pixel and strip + transition rad. tracker
- $\sigma(d_0) = 15\mu\text{m}@20\text{GeV}$
- $\sigma/p_T \approx 0.05\%p_T \oplus 1\%$

## Calorimeter

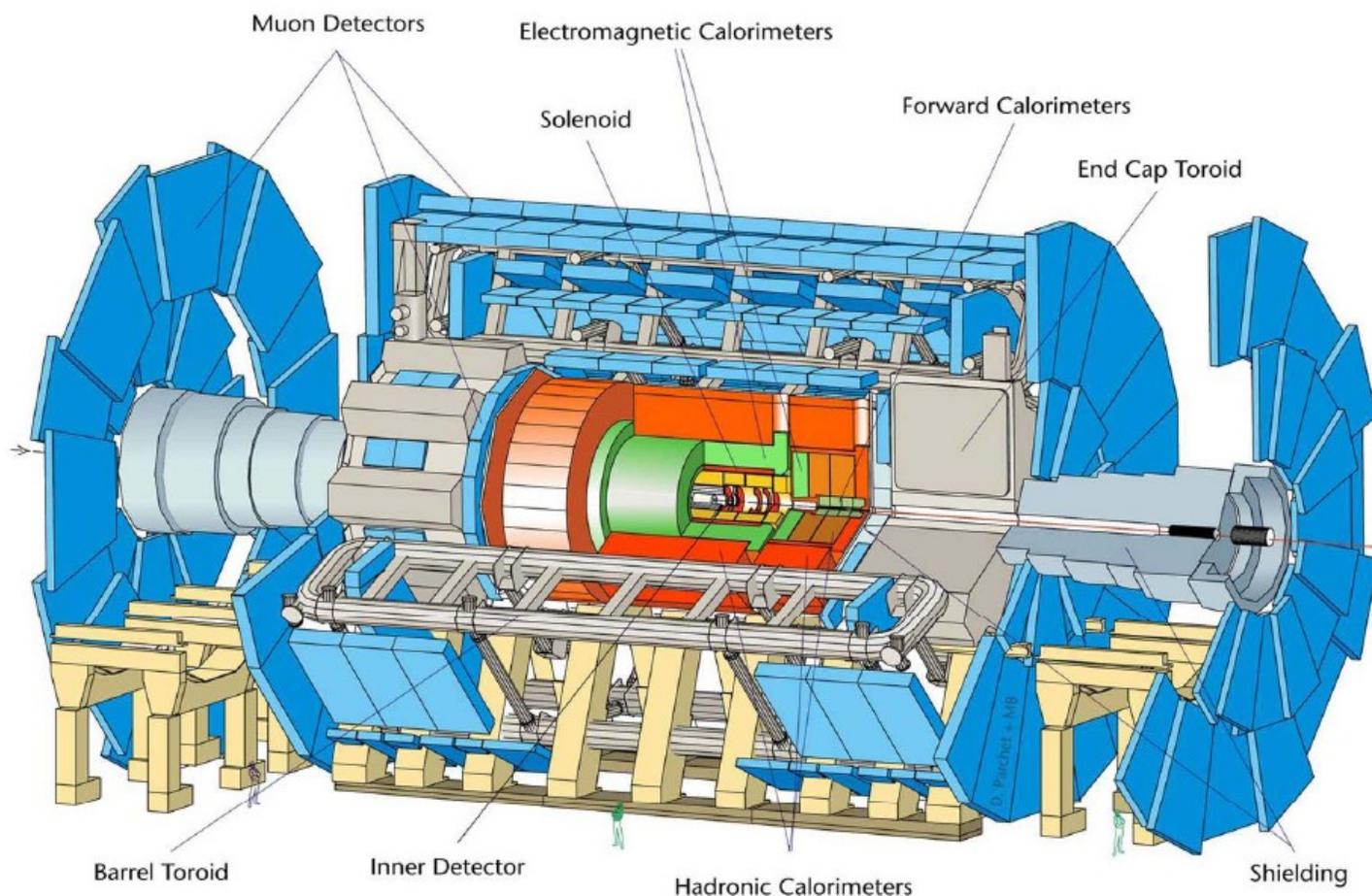
- Liquid Ar EM Cal, Tile Had. Cal
- EM:  $\sigma_E/E = 10\%/\sqrt{E} \oplus 0.7\%$
- Had:  $\sigma_E/E = 50\%/\sqrt{E} \oplus 3\%$

## Muon spectrometer

- Drift tubes, cathode strips: precision tracking +
- RPC, TGC: triggering
- $\sigma/p_T \approx 2\text{-}7\%$

## Magnets

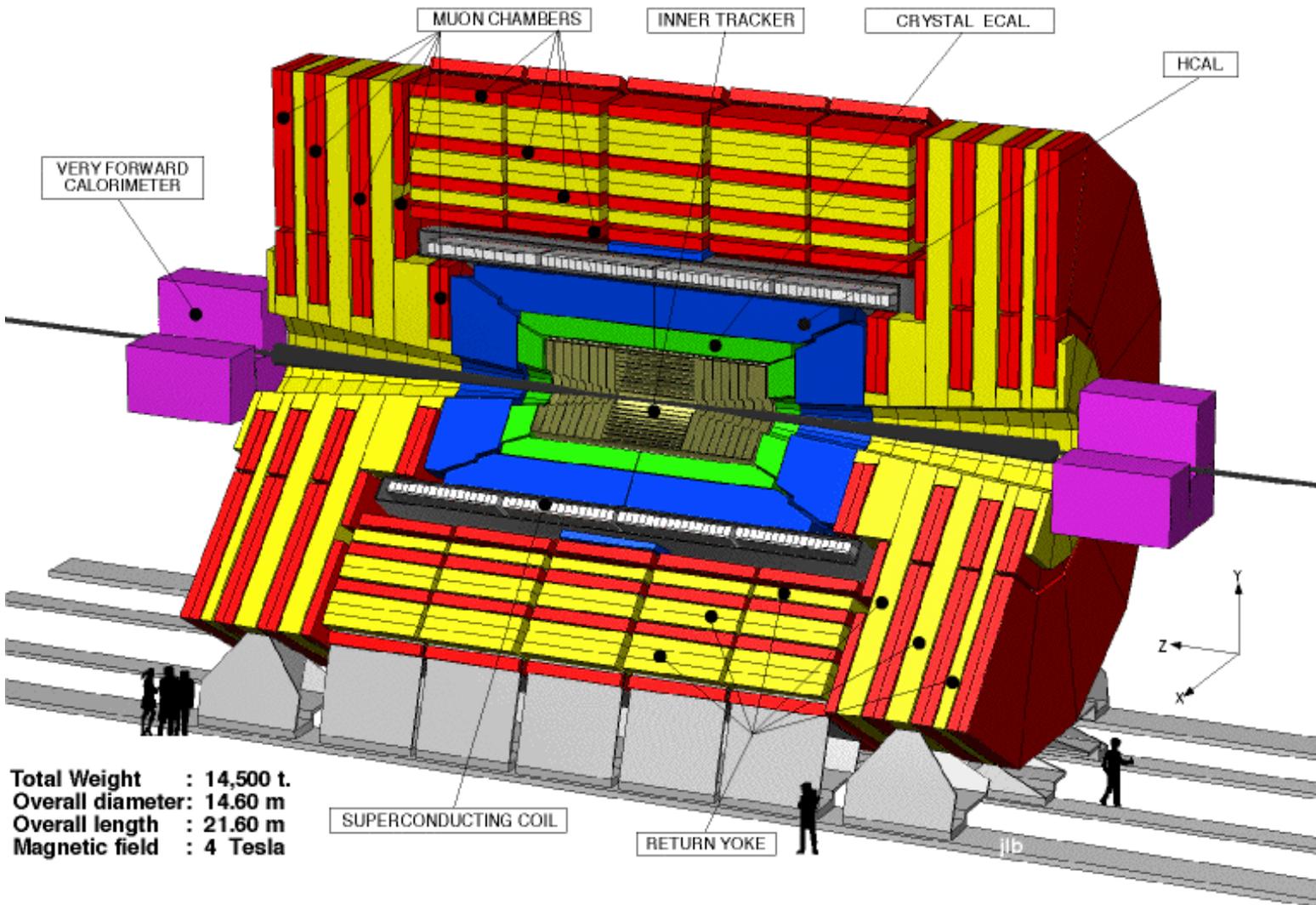
- Solenoid (ID)  $\rightarrow 2\text{T}$
- Air toroids (muon)  $\rightarrow$  up to 4T



Full coverage for  $|\eta| < 2.5$ , calorimeter up to  $|\eta| < 5$

See also JINST 3 2008 S08003

# The CMS Detector



Total Weight : 14,500 t.  
Overall diameter: 14.60 m  
Overall length : 21.60 m  
Magnetic field : 4 Tesla

Inner detector (tracker):

- Si pixel & strip tracker
- $\sigma/p_T \approx 1\text{-}2\%$  ( $\mu$  at 100 GeV)

Calorimeter:

- PbWO<sub>4</sub> crystal ECAL, brass/scintillator HCAL
- ELM:  $\sigma_E/E = 2.8\% \sqrt{E} + 0.3\%$
- HAD:  $\sigma_E/E = 100\% \sqrt{E} + 5\%$

Muon system:

- Drift tubes, cathode strips, resistive plate chambers
- $\sigma/p \approx 10 - 50\%$  (muon alone)
- $\approx 0.7 - 20\%$  (with tracker)

Magnet:

- Solenoid  $\rightarrow$  3.8T

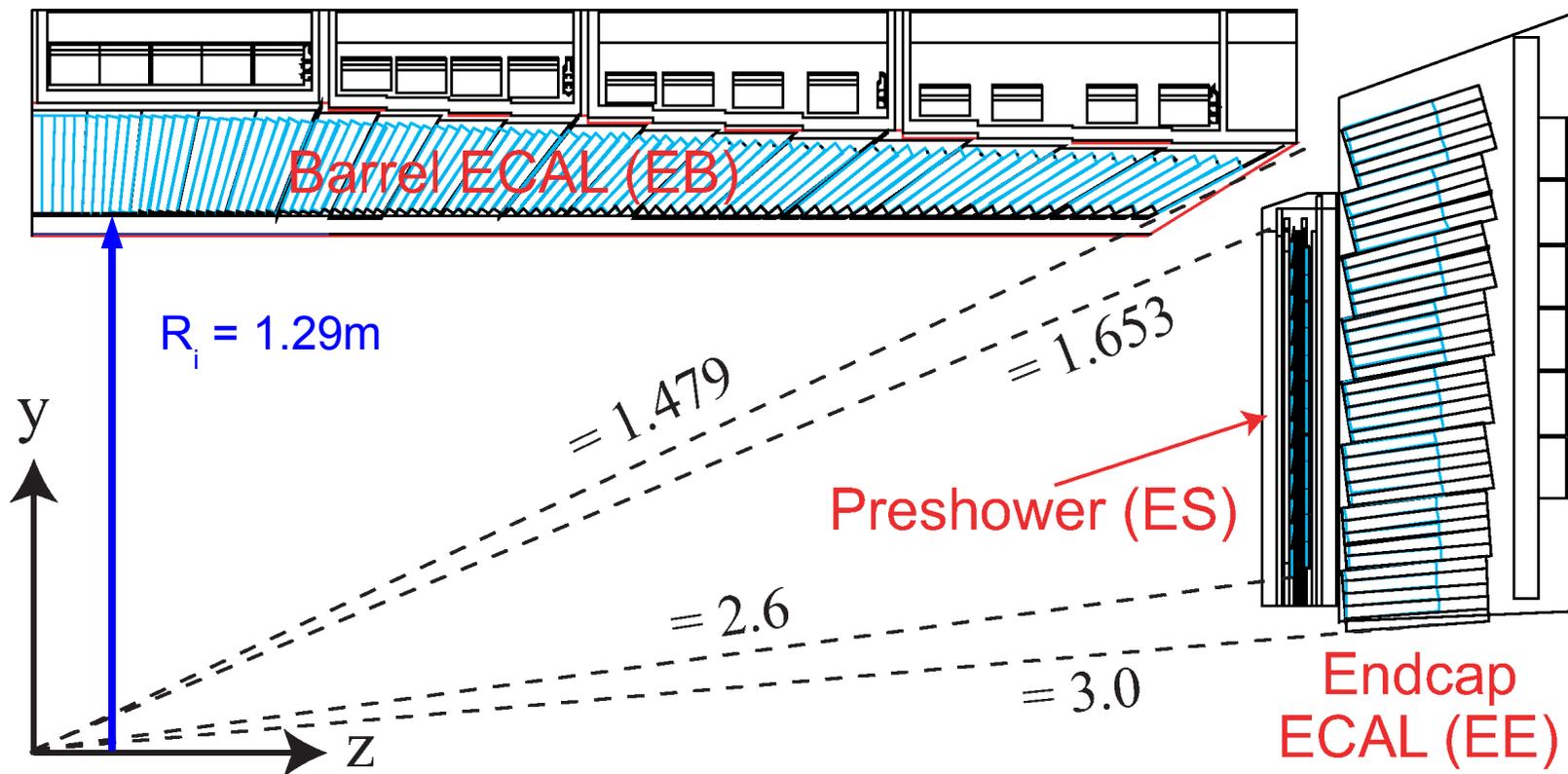
See also:  
PTDR | LHCC-2006-001,  
JINST 3 2008 S08003

# Electromagnetic Calorimeter

## Barrel (EB):

- $\eta$  segments: 2x85
- $\phi$  segments: 360
- 61200 crystals (PbWO<sub>4</sub>, 26 X<sub>0</sub>)
- $\Delta\eta \times \Delta\phi \approx 0.0174 \times 0.0174$

## Segmentation



## Energy resolution from test beam:

$S = 2.8\%$ ,  $N = 120 \text{ MeV}$ ,  $C = 0.30\%$

$$\left(\frac{\sigma}{E}\right)^2 = \left(\frac{S}{\sqrt{E}}\right)^2 + \left(\frac{N}{E}\right)^2 + C^2$$

## Segmentation

## Endcaps (EE):

- (x,y) grid on two halves
- front face 28 x 28 mm<sup>2</sup>
- 2 x 2 x 3662 crystals = 14648 (PbWO<sub>4</sub>, 25 X<sub>0</sub>)

# Hadronic Calorimeter

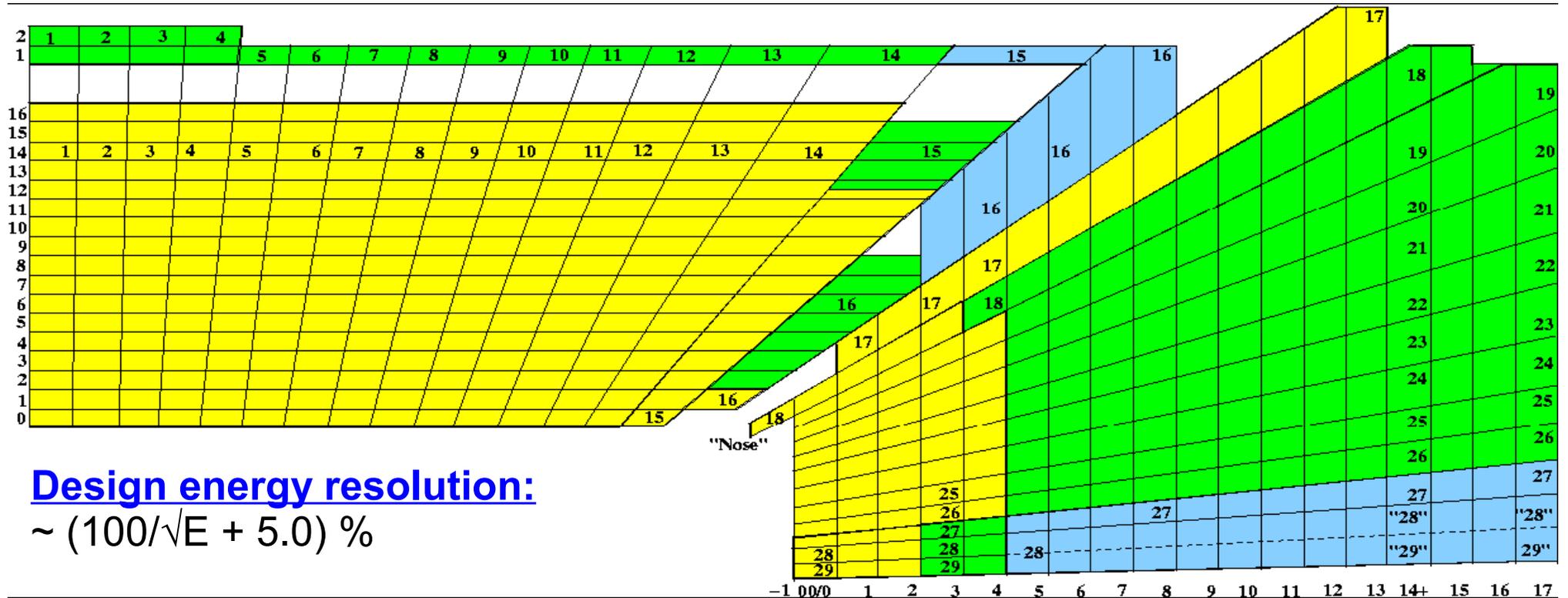
## HCAL (tower structure):

- Barrel (HB):  $|\eta| < 1.4$ , 2592 towers
- Endcaps (HE):  $1.3 < |\eta| < 3.0$ , 2592 "
- Outside coil (HO):  $|\eta| < 1.26$ , 2160 "
- Depth (Brass abs. & plast. scint.,  $\approx 6 - 10 \lambda_N$ )
- $\Delta\eta \times \Delta\phi \approx 0.087 \times 0.087 \rightarrow 0.350 \times 0.175$

- Forward (HF):  $2.9 < |\eta| < 5.0$  (not shown)
- 2 x 864 towers (Brass, quartz fibers,  $\approx 10 \lambda_N$ )
- $\Delta\eta \times \Delta\phi \approx 0.111 \times 0.175 \rightarrow 0.302 \times 0.350$

## CASTOR calorimeter (not shown):

- $5.1 < |\eta| < 6.5$ ,  $\approx 22 X_0$ ,  $\approx 10 \lambda_N$



## Design energy resolution:

$$\sim (100/\sqrt{E} + 5.0) \%$$